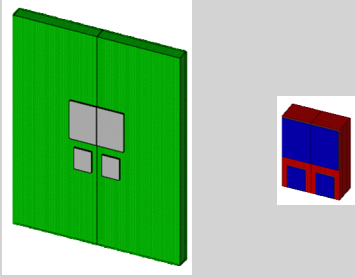


# Predicting Thermal Mechanical Fatigue of 63Sn37Pb Solder



$$N \approx \left( \frac{a}{\Delta \gamma_{EQPS}} \right)^b$$

$$\Delta w = \frac{1}{N} = \left( \frac{\Delta \gamma_{EQPS}}{a} \right)^b$$

Mike Neilsen and Paul Vianco

Sandia National Laboratories  
New Mexico, USA

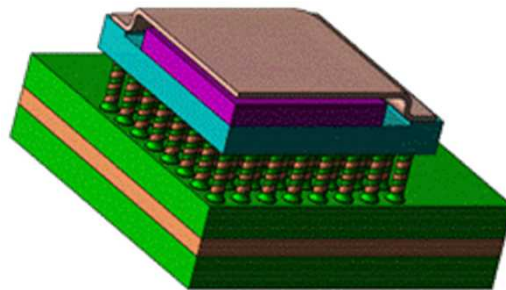
JOWOG28, AWE, Aldermaston, UK  
Aug. 29-Sept. 01, 2017



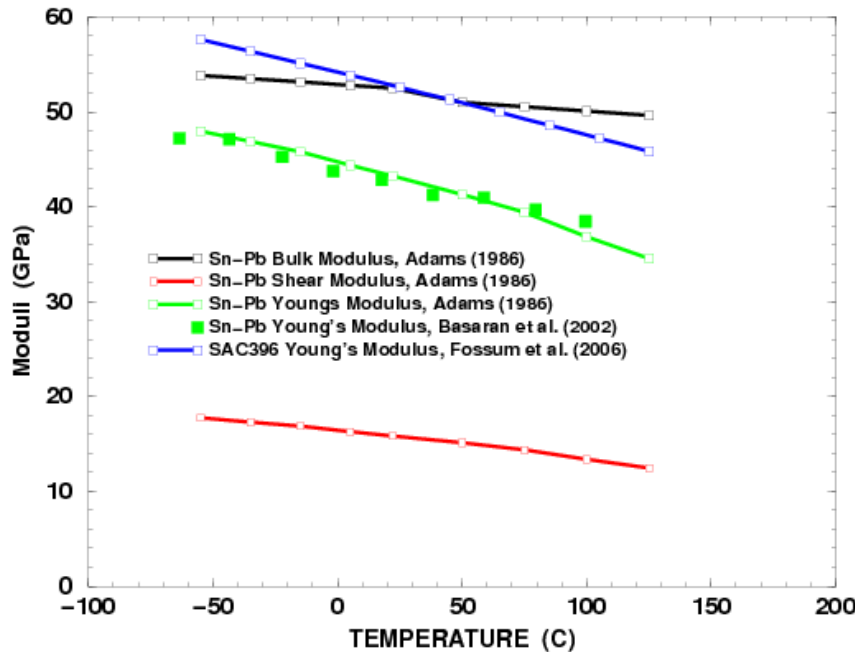
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# Outline

- ❑ Mechanical Behavior of Eutectic 63Sn37Pb and SAC Solder
- ❑ Low Cycle Fatigue Failure Criteria
- ❑ Unified Creep Plasticity Damage (UCPD) Model for Solder
- ❑ Simulating Crack Initiation and Growth
- ❑ Applications



# Elasticity – 63Sn37Pb and SAC396



$$E \text{ (GPa)} = 54.21 - 0.06358\theta - 2.685 \times 10^{-5}\theta^2$$

$\theta$  = temperature (C)

95.5Sn-3.9Ag-0.6Cu solder

$$G \text{ (GPa)} = 24.28 - 0.0290\theta$$

$$K \text{ (GPa)} = 61.06 - 0.0274\theta$$

$\theta$  = temperature (K)

60Sn-40Pb solder

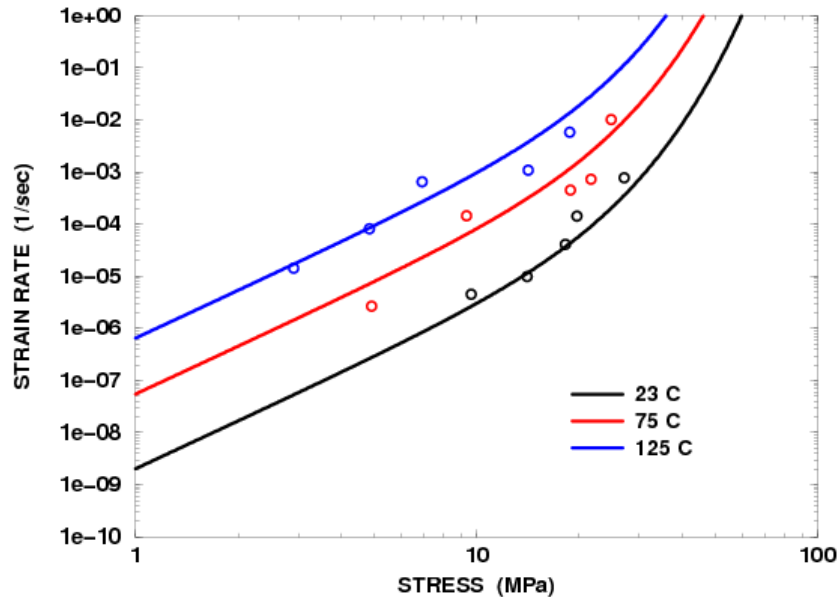
## References:

P. Adams, 'Thermal Fatigue of Solder Joints in Micro-electronic Devices,' M.S. Thesis, ME, MIT, Aug.1986.

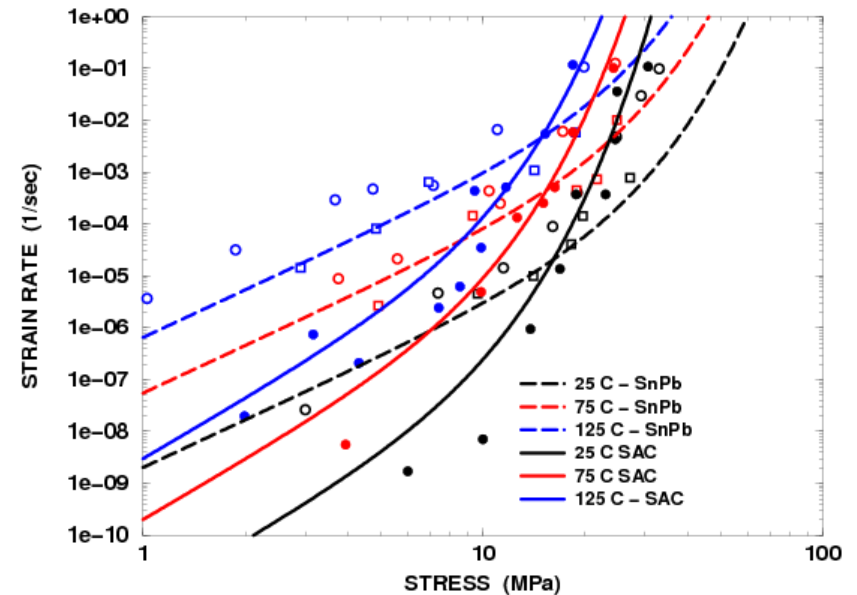
C. Basaran et al., 'Measuring intrinsic elastic modulus of Pb/Sn solder alloys,' *Mech. of Materials*, **34** (2002).

M.K. Neilsen and P.T. Vianco, 'UCPD Model for Pb-Free Solder,' *J. Electronic Packaging*, **136** (2014).

# Creep – 63Sn37Pb and SAC396



63Sn37Pb



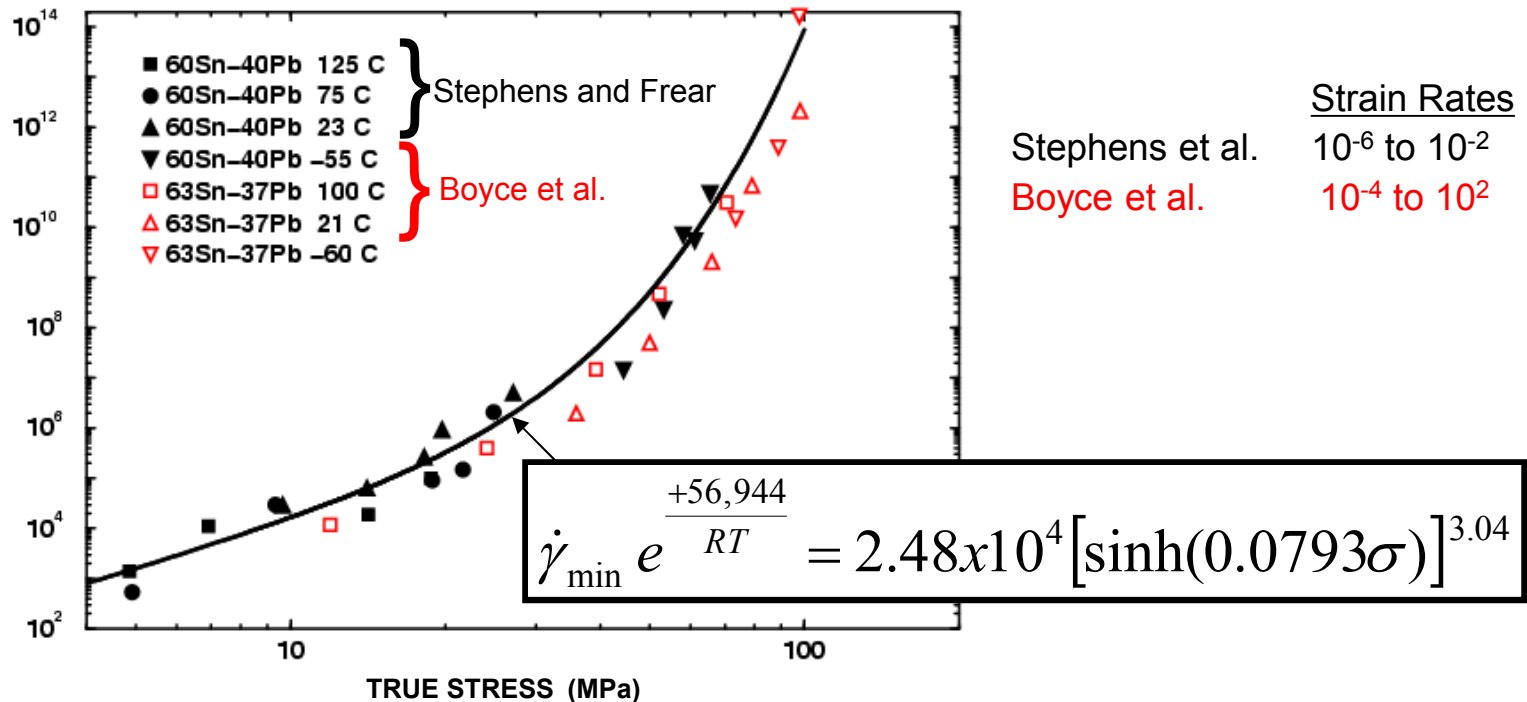
SAC396 vs. SnPb

## References:

Stephens, J.J., and Frear, D.R., 'Time-Dependent Deformation Behavior of Near-Eutectic 60Sn-40Pb Solder,' *Metallurgical and Materials Transactions A*, **30A**, (1999).

S. Ganesan, M. Pecht, **Lead-free Electronics**, Wiley, (2004).

# Zener-Holloman Plot – 63Sn37Pb



## References:

Stephens, J.J., and Frear, D.R., 'Time-Dependent Deformation Behavior of Near-Eutectic 60Sn-40Pb Solder,' *Metallurgical and Materials Transactions A*, **30A**, (1999).

Boyce, B., Brewer, L., Perricone, M., and Neilsen, M., 'On the Strain Rate and Temperature-Dependent Tensile Behavior of Eutectic SnPb Solder,' *Journal of Electronic Packaging*, **133**, (2011).

# UCP Model for Solder

$$\dot{\boldsymbol{\sigma}} = \mathbf{E} : \dot{\boldsymbol{\epsilon}}^e = \mathbf{E} : (\dot{\boldsymbol{\epsilon}} - \dot{\boldsymbol{\epsilon}}^{in})$$

$$\dot{D} = \frac{A_1 \dot{\gamma}}{(D - D_0)^{A_3}} - A_2 (D - D_0)^2$$

$$\dot{\boldsymbol{\epsilon}}^{in} = \frac{3}{2} \dot{\gamma} \mathbf{n} = \frac{3}{2} f \sinh^p \left( \frac{\tau}{D} \right) \mathbf{n}$$

$$\dot{\mathbf{B}} = \frac{A_4 \dot{\boldsymbol{\epsilon}}^{in}}{\beta^{A_6}} - A_5 \beta \mathbf{B}$$

$$\mathbf{n} = \frac{\mathbf{s} - \frac{2}{3} \mathbf{B}}{\tau}$$

$$\beta = \sqrt{\frac{2}{3} \mathbf{B} : \mathbf{B}}$$

$$\tau = \sqrt{\frac{3}{2} \left( \mathbf{s} - \frac{2}{3} \mathbf{B} \right) : \left( \mathbf{s} - \frac{2}{3} \mathbf{B} \right)}$$

## Reference:

Boyce, B., Brewer, L., Perricone, M., and Neilsen, M., 'On the Strain Rate and Temperature-Dependent Tensile Behavior of Eutectic Sn-Pb Solder,' *J. Electronic Packaging*, **133**, (2011).

# Low Cycle Fatigue Experimental Data

Sn-Pb Coffin-Manson (Solomon, 1986)

$$N_f = \left( \frac{1.14}{\Delta\gamma_p} \right)^{\frac{1}{0.51}} \approx \left( \frac{1.31636}{\Delta\gamma_{EQPS}} \right)^{1.96078}$$

SAC305 Coffin-Manson (Zhou, 2009)

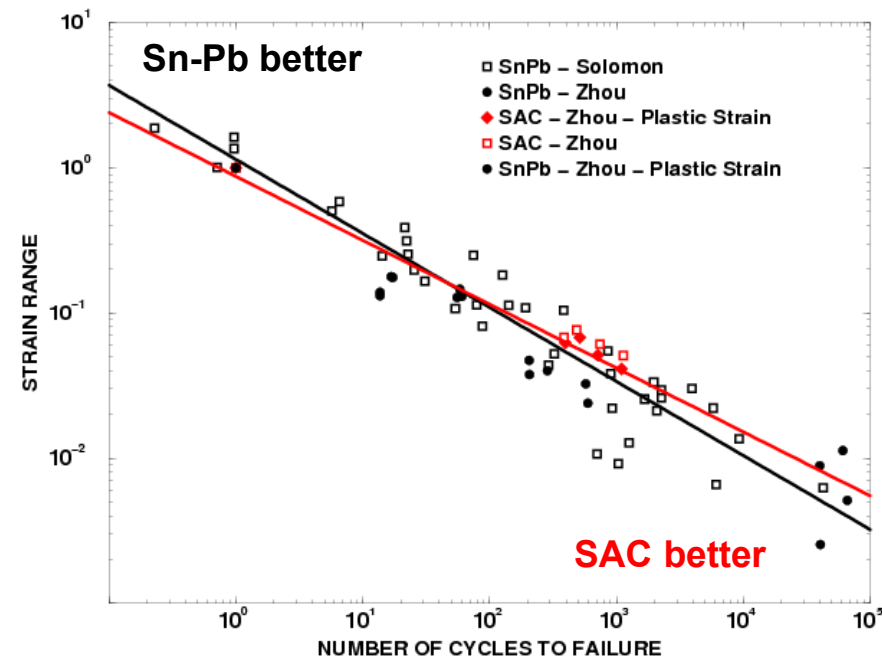
$$N_f = \frac{1}{2} \left( \frac{1.18}{\Delta\gamma_{EQPS}} \right)^{\frac{1}{0.44}} \approx \left( \frac{0.86985}{\Delta\gamma_{EQPS}} \right)^{2.273}$$

$\Delta\gamma_p$  = plastic shear strain range

$\Delta\gamma_{EQPS}$  = equivalent plastic strain increment  
from complete load/unload cycle

References: H.D. Solomon, *IEEE Trans., CHMT-9, Dec. 1986*

Y. Zhou et al., *J. Electronic Packaging, Vol. 131, Mar. 2009*



# UCPD Model for Solder

$$\dot{\boldsymbol{\sigma}} = \mathbf{E} : \dot{\boldsymbol{\epsilon}}^e = \mathbf{E} : (\dot{\boldsymbol{\epsilon}} - \dot{\boldsymbol{\epsilon}}^{in})$$

$$\dot{\boldsymbol{\epsilon}}^{in} = \frac{3}{2} \dot{\gamma} \mathbf{n} = \frac{3}{2} f \sinh^p \left( \frac{\tau}{D(1-cw)} \right) \mathbf{n}$$

$$\dot{D} = \frac{A_1 \dot{\gamma}}{(D - D_0)^{A_3}} - A_2 (D - D_0)^2$$

$$\dot{\mathbf{B}} = \frac{A_4 \dot{\boldsymbol{\epsilon}}^{in}}{\beta^{A_6}} - A_5 \beta \mathbf{B}$$

$$\mathbf{n} = \frac{\mathbf{s} - \frac{2}{3} \mathbf{B}}{\tau} \quad \beta = \sqrt{\frac{2}{3} \mathbf{B} : \mathbf{B}}$$

$$\tau = \sqrt{\frac{3}{2} \left( \mathbf{s} - \frac{2}{3} \mathbf{B} \right) : \left( \mathbf{s} - \frac{2}{3} \mathbf{B} \right)}$$

$$N = \left( \frac{a}{\Delta \gamma_{EQPS}} \right)^b$$

$$\Delta w \approx \frac{1}{N} = \left( \frac{\Delta \gamma_{EQPS}}{a} \right)^b$$

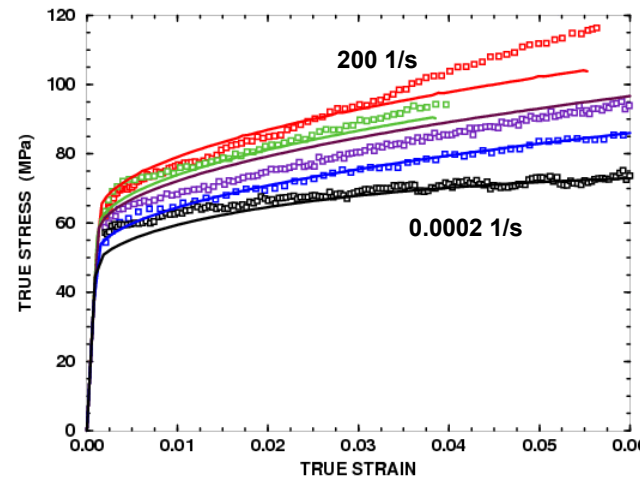
$$w = \sum_{i=1}^m \Delta w^i = \sum_{i=1}^m \left( \frac{\Delta \gamma_{EQPS}^i}{a} \right)^b$$

Reference:

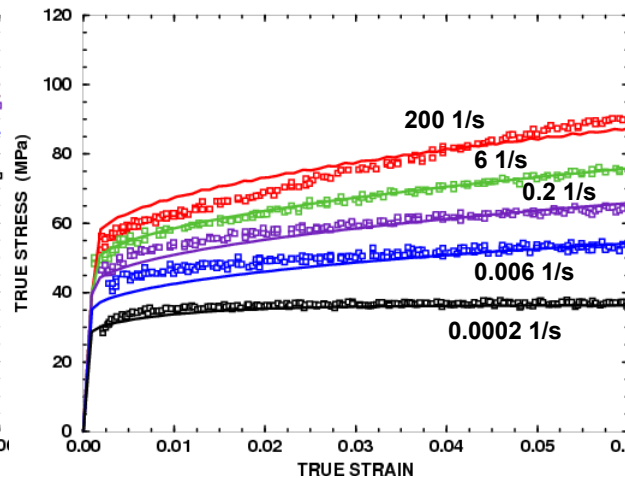
M.K. Neilsen and P.T. Vianco, 'UCPD Model for Pb-Free Solder,' *J. Electronic Packaging*, **136** (2014).



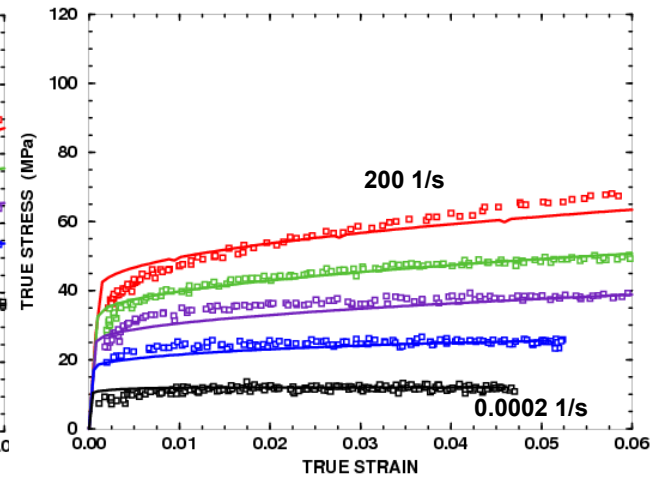
# 63Sn-37Pb Solder



-60 °C isothermal tests



21 °C isothermal tests



100 °C isothermal tests

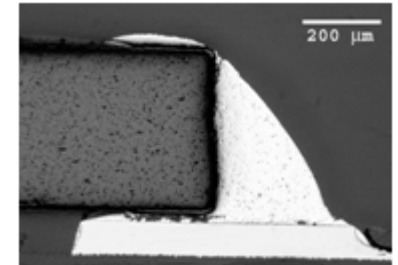
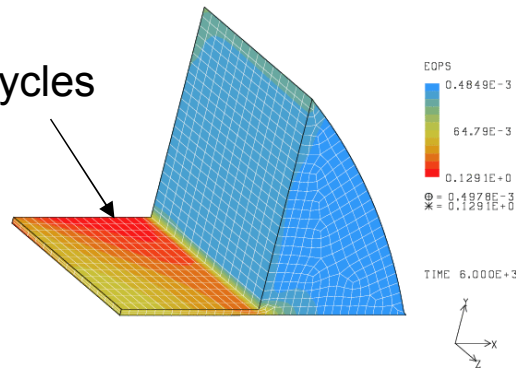
Comparison of UCPD model predictions (solid lines) with experimental data (symbols) for **wide range of strain rates** from 0.0002 per second to 200.0 per second.

Ref: Boyce, B., Brewer, L., Perricone, M., and Neilsen, M., 'On the Strain Rate and Temperature-Dependent Tensile Behavior of Eutectic Sn-Pb Solder,' J. Electronic Packaging, **133**, Sept. 2011.

# Solder Life Prediction

1. Simulate 1 or a few thermal cycles.
2. Compute increment in equivalent plastic strain or damage in worst element
3. Generate Lifetime Prediction using Coffin-Manson relationship

Crack Starts Here at 100 cycles



500 cycles

*Cycles to Generate Electrical Open = ???*  
*Need to Model Crack Initiation and Growth*

# Challenges for Modeling Crack Growth

**Problem:** Capture Effects of 100's or 1000's of Thermal Cycles with Simulation that Runs in a Reasonable Amount of Time

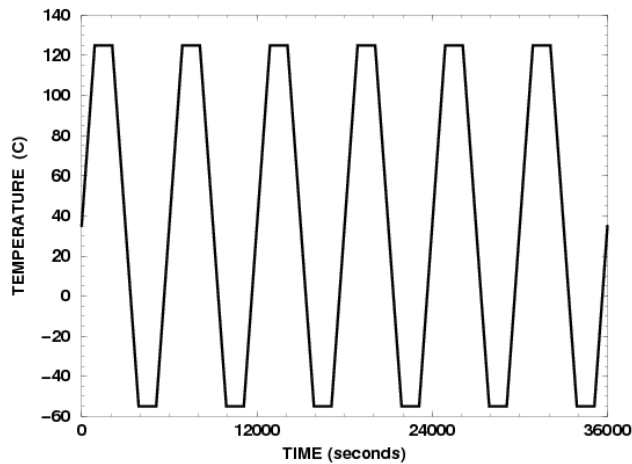
**Solution:** Accelerated Simulation – Acceleration Factor Applied to Damage.

**Problem:** Capture Geometry Changes Due to Introduction and Growth of Crack

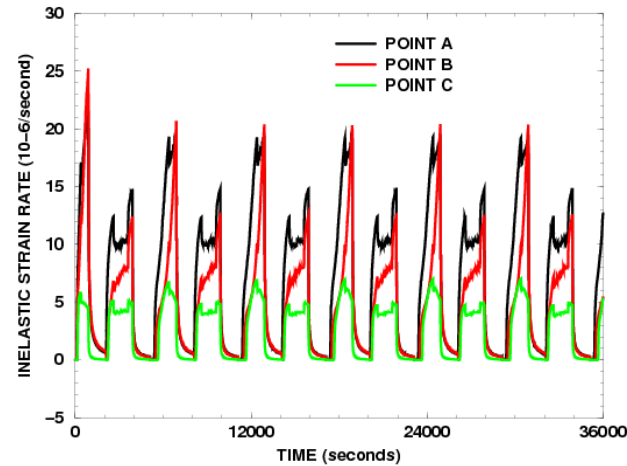
**Solution:** Smeared Cracking Approach – Replace Cracked Elements with Very Flexible Elastic Material.

What to do about local model giving mesh dependent solutions ?

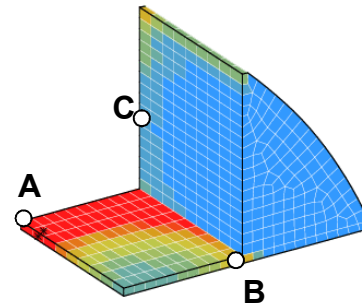
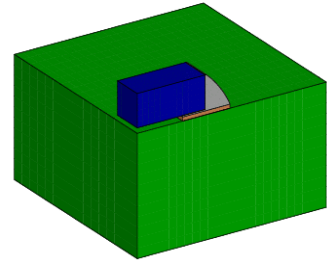
# Acceleration of Simulations - UCPD



Temperature History



Strain Rate History



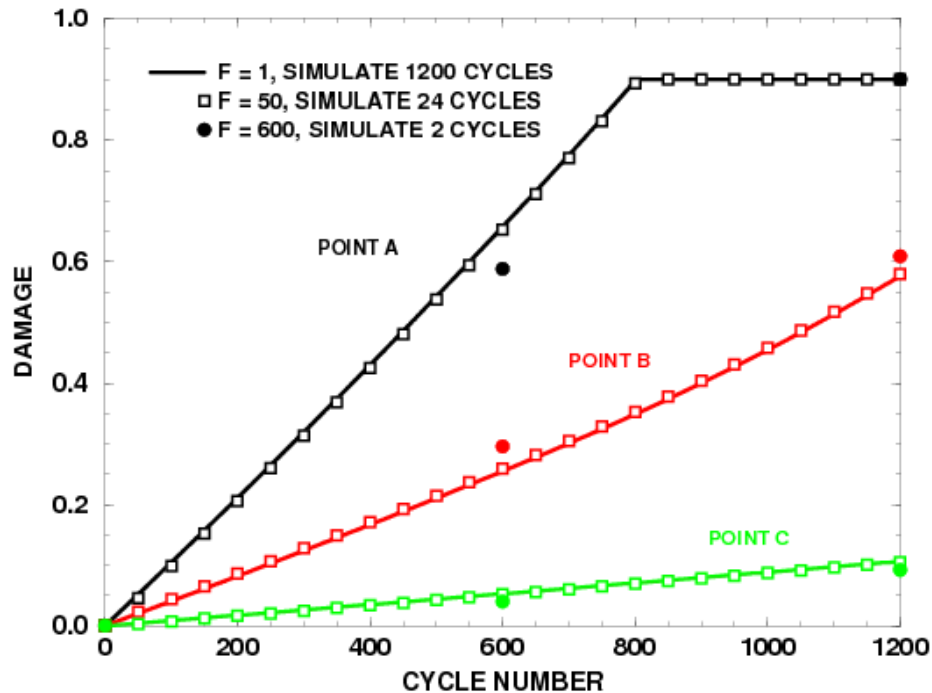
If inelastic rate histories vary little with cycle number then:

apply acceleration factor,  $F$ , to damage rate equation

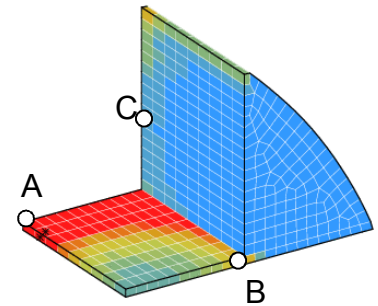
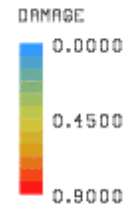
to capture effects of  $F$  cycles with each simulation cycle

$$w = \sum_{i=1}^m F \Delta w^i = \sum_{i=1}^m F \left( \frac{\Delta \gamma_{EQPS}^i}{a} \right)^b$$

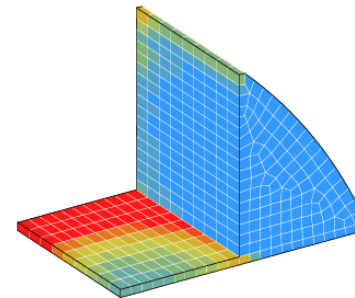
# Acceleration of Simulations - UCPD



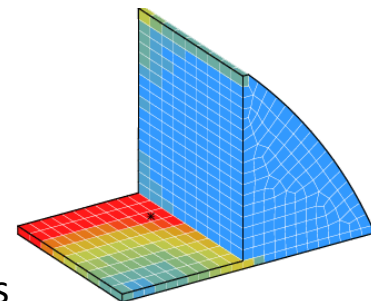
So does this really work ? Yes.



F = 1, simulated 1200 cycles



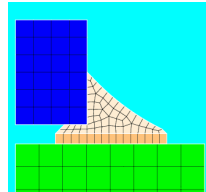
F = 50, simulated 24 cycles



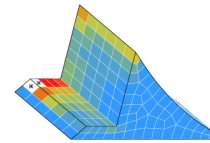
F = 600, simulated 2 cycles

# Eliminating Mesh Dependence

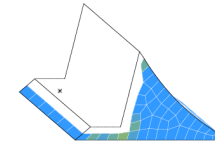
$$w = \sum_{i=1}^m F \left( \frac{\Delta \gamma_{EQPS}^i}{a} \right)^b$$



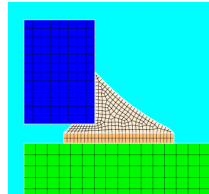
318 solder elements



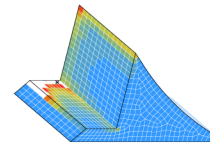
4,000 cycles



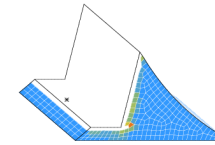
61,500 cycles



2,782 solder elements

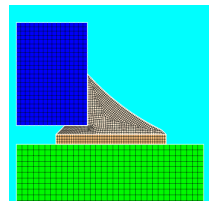
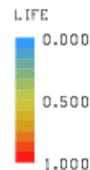


2,000 cycles

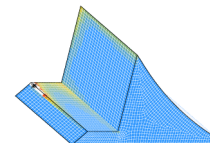


39,500 cycles

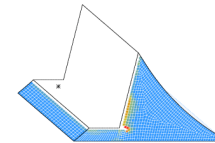
$$Life = \frac{w}{w_{fail}} = \frac{w}{0.9}$$



22,152 solder elements



600 cycles



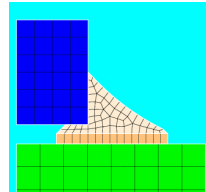
24,000 cycles

# Eliminating Mesh Dependence

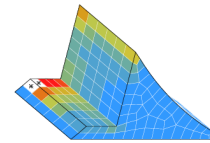
$$w = \sum_{i=1}^m \left( \frac{V^{1/3}}{\lambda} \right)^d F \left( \frac{\Delta \gamma_{EQPS}^i}{a} \right)^b$$

$$\lambda = 0.0254 \text{ mm}, d = 0.675$$

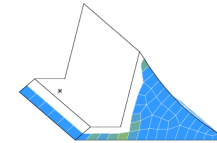
$$V = \text{element volume}$$



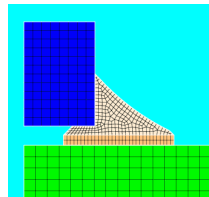
318 solder elements



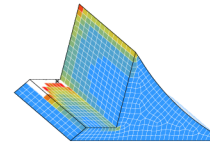
2,000 cycles



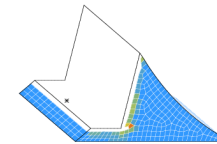
24,750 cycles



2,782 solder elements

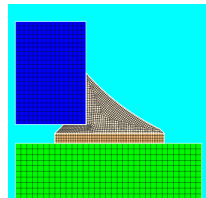
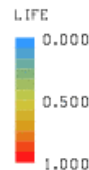


1,000 cycles

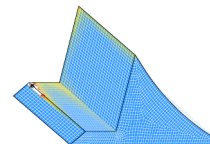


25,750 cycles

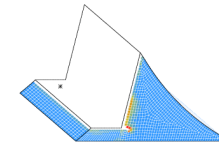
$$Life = \frac{w}{w_{fail}} = \frac{w}{0.9}$$



22,152 solder elements

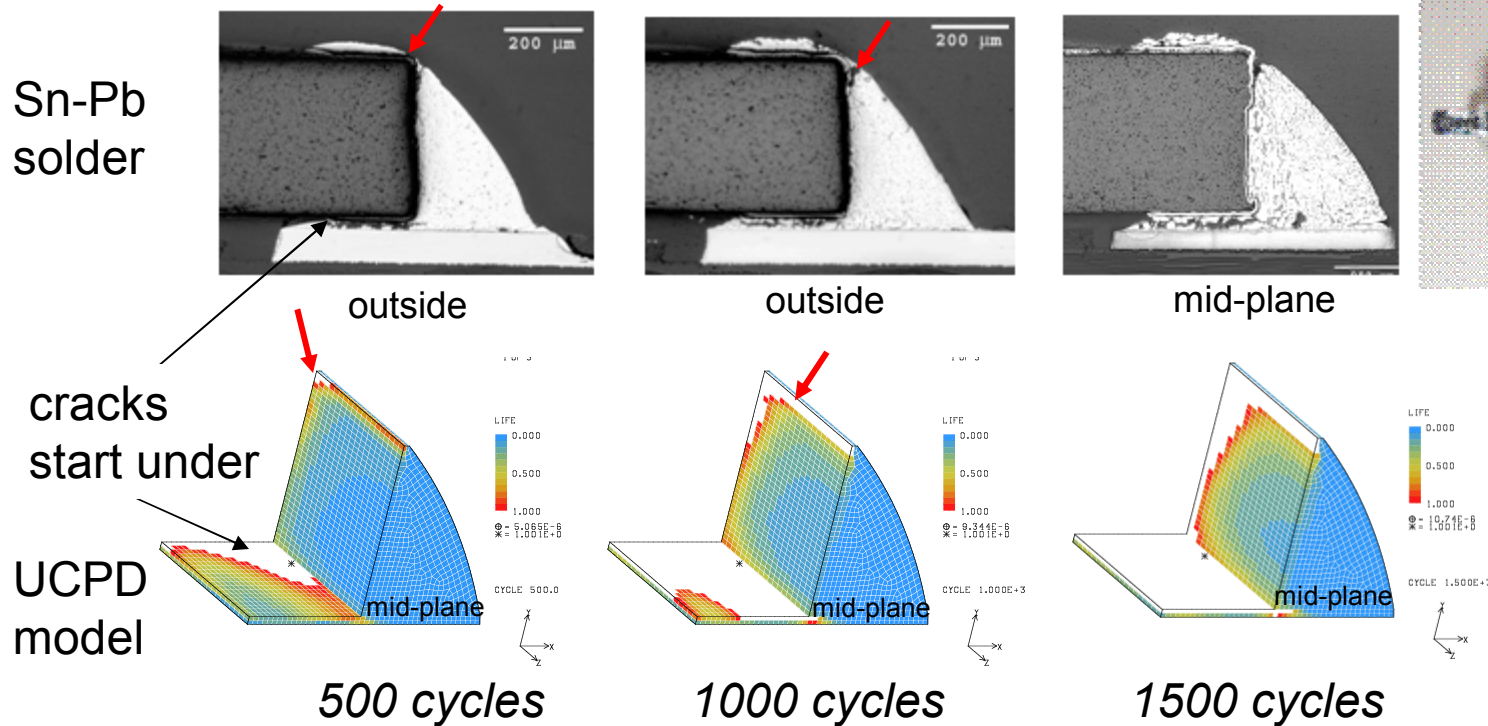


750 cycles



26,000 cycles

# Sandia R23 63Sn37Pb Solder



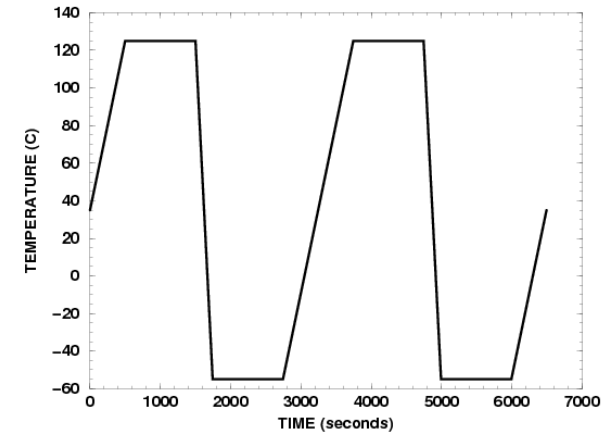
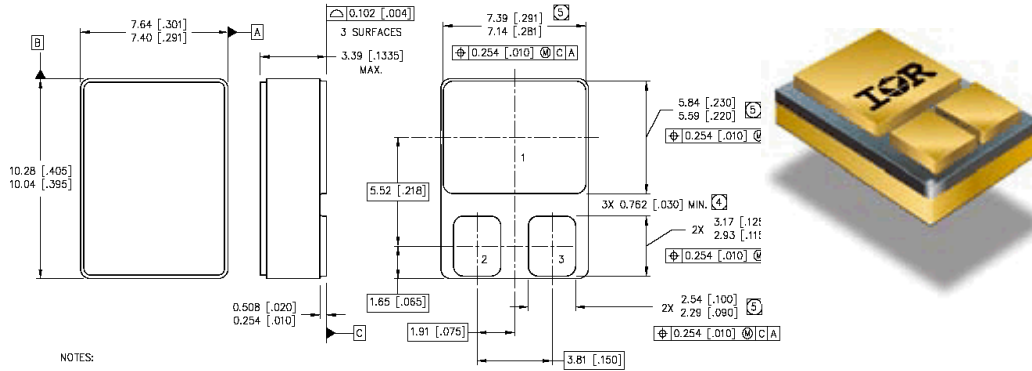
*Accelerated Aging -55 to 125 Thermal Cycles*

*Failure based on damage  $w = 0.90$*

*White elements = cracked elements.*

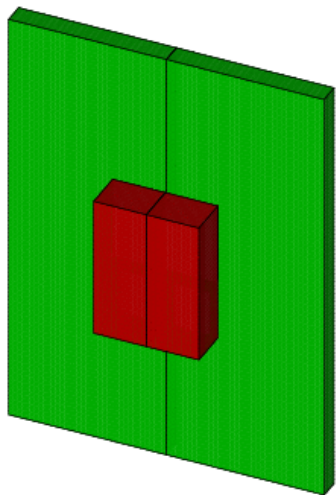


# SMD-0.5 63Sn37Pb Solder

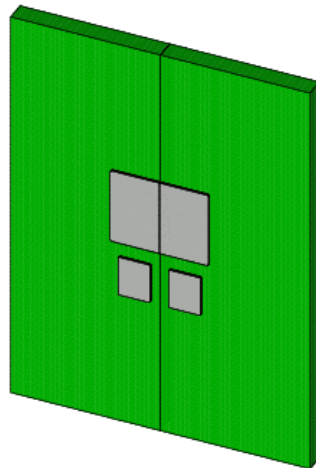


## Case Outline and Dimensions - SMD-0.5 (Ceramic Lid)

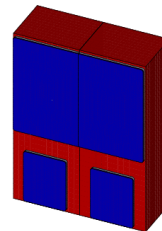
Reference <http://www.irf.com/product-info/hi-rel/gssurface.html>



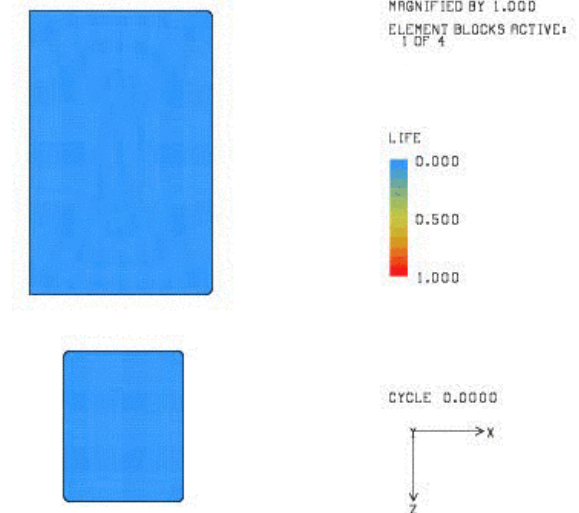
Model – top view



pwb, pads, and solder



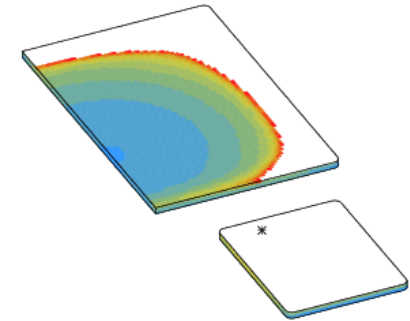
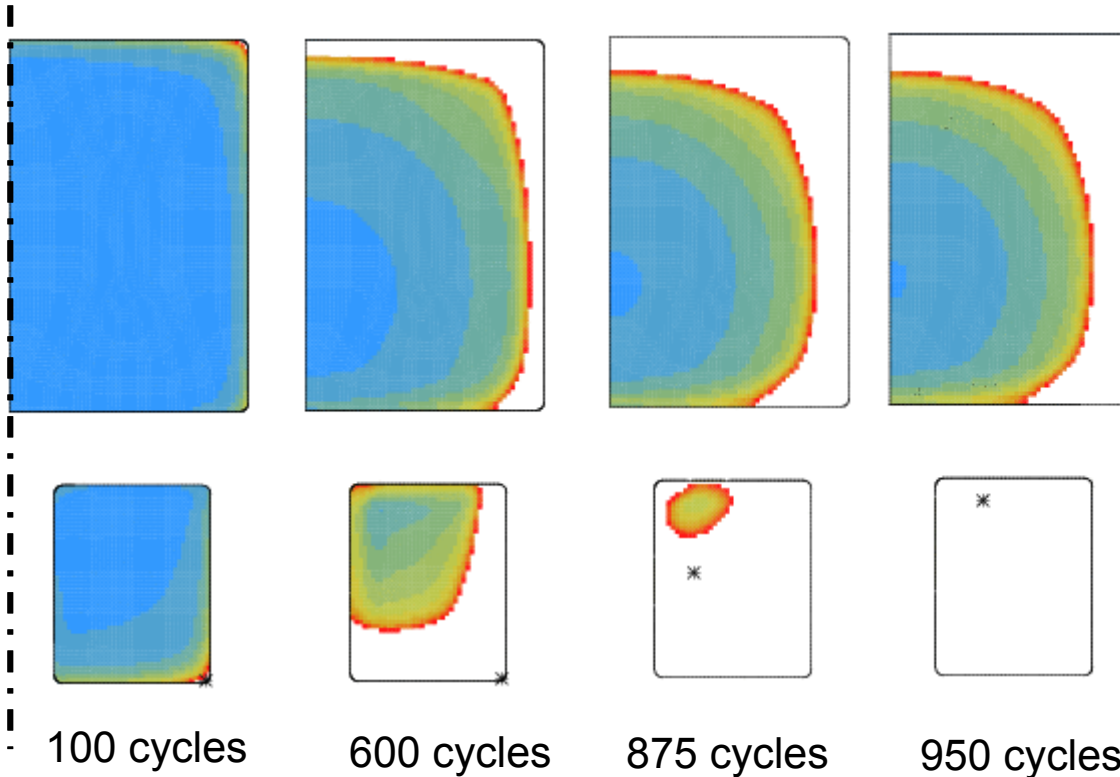
SMD-0.5



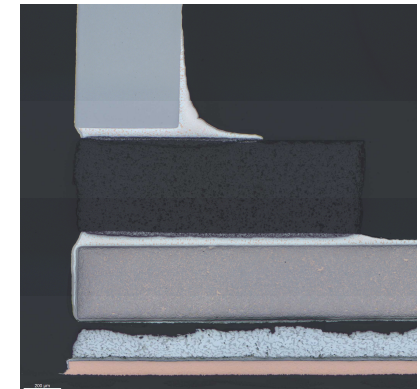
# SMD-0.5 63Sn37Pb Solder

Model: Open at 950 cycles with 5 mil solder

Experiment: Open at 1009 cycles

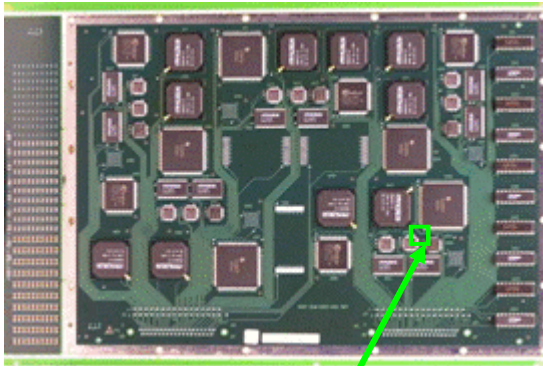


950 cycles  
Model



1009 cycles  
Experiment

# CLCC-20 63Sn37Pb Solder



**Experiment:** 63Sn37Pb solder

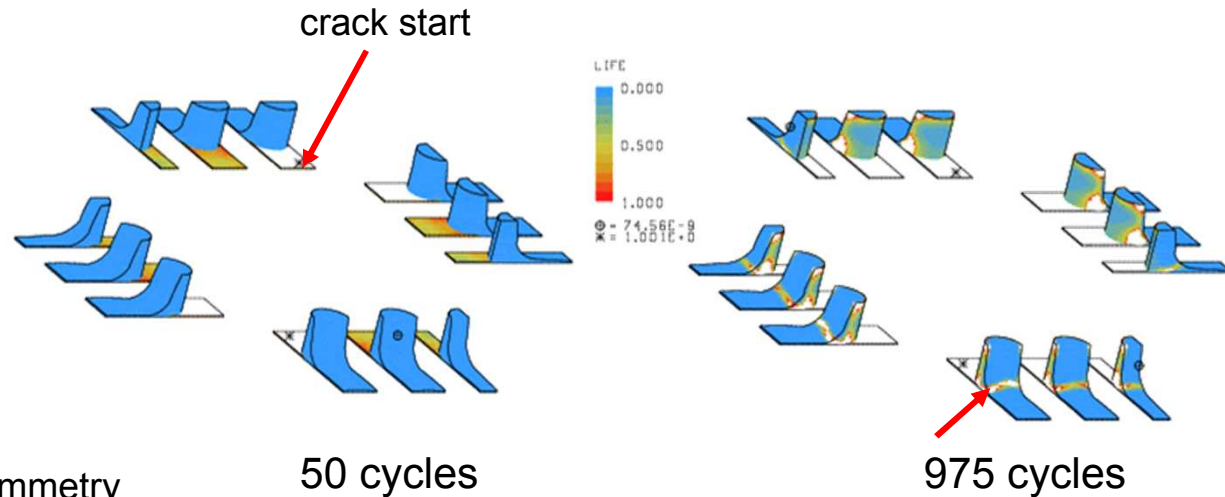
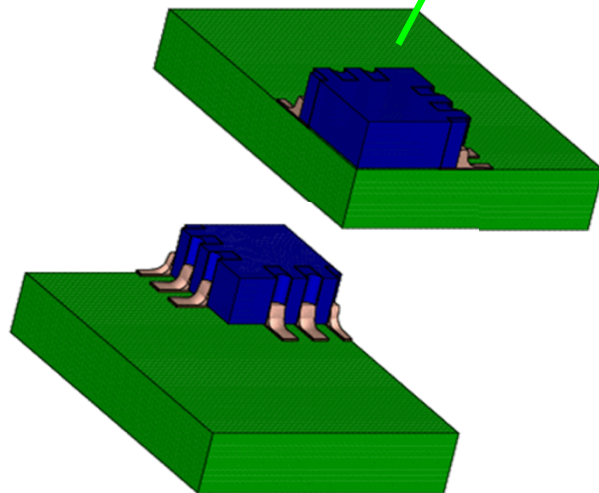
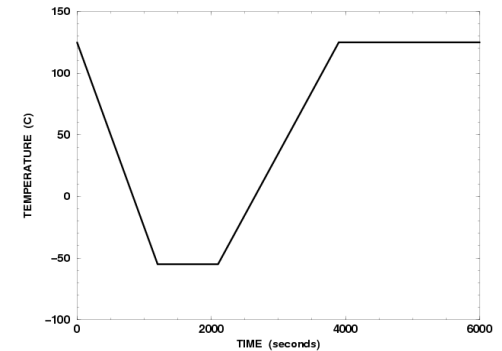
First Failure: 455 cycles

N10: 469 cycles

**N63: 727 cycles**

**Model:** 63Sn37Pb solder

**Electrical open: 975 cycles**



CLCC-20 - Finite Element Model –  $\frac{1}{4}$  symmetry

Reference: D. Hillman et al., 'JCAA/JG-PP No-Lead Solder Project: -55°C to 125°C Thermal Cycle Testing Final Report, Rockwell Collins, May 2006.

# Summary

- ❑ Solder exhibits a variety of complex behavior (Creep, Plasticity, Damage)
- ❑ A new UCPD Model was developed for solder with damage based on an empirical Coffin-Manson low-cycle fatigue failure criterion
- ❑ Model does not require remeshing with crack growth and instead uses diffuse cracking approach and replaces cracked solder with very flexible elastic material
- ❑ Model was validated by comparing model predictions with experimental data for a variety of component types