

# Multiscale Methods for Uncertainty Propagation for Polycrystalline Aluminum 6061-T6

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# Problem Statement

We seek to:

- Develop an efficient algorithm for multiscale structural reliability prediction for applications where ductile crack nucleation is the mechanism of interest
- Stitch existing multiscale methods and constitutive models in a manner to make multiscale reliability calculations tractable

We will:

- Utilize Stochastic Reduced Order Models (SROMs) to efficiently transfer uncertainty across length scales
- In this presentation primarily focus on the implications of multiscale coupling on the propagation of meso-scale material uncertainty
- Additionally, discuss implications of the construction of the meso-scale finite element model

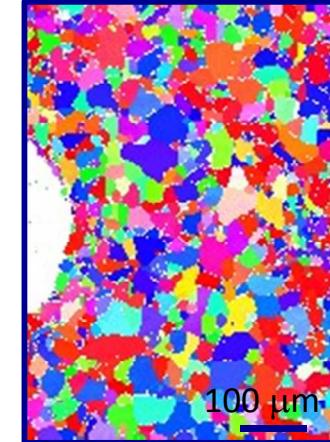
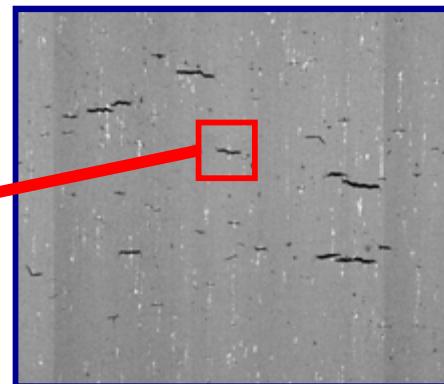
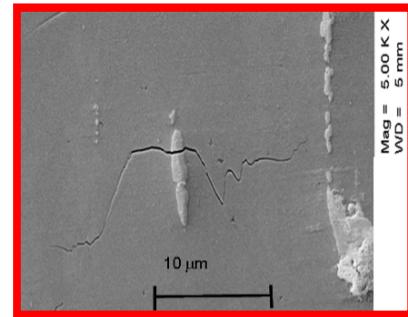
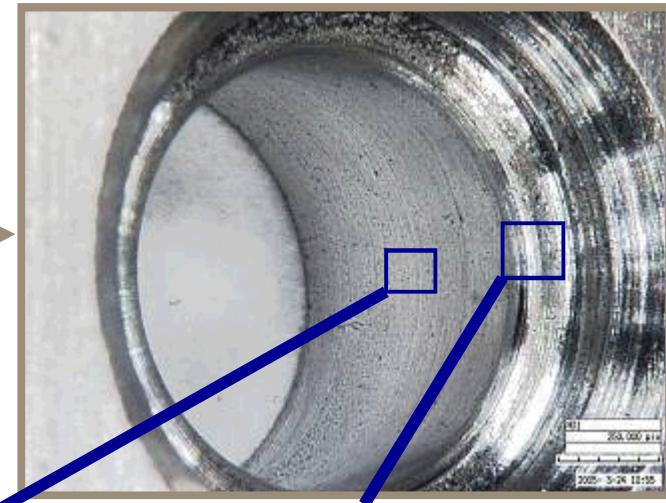
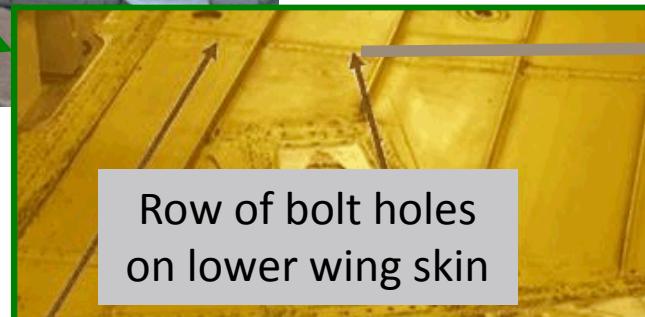
# Outline

- Problem motivation
- Overall fracture prediction approach overview
- High fidelity framework and modeling details
- Modeling considerations studied here:
  - Multiscale coupling impacts
  - Meso-scale meshing (grain aligned element edges)
- Conclusions

Why do multiscale? Because structural reliability is dependent on **random** microstructure (among other sources of randomness)

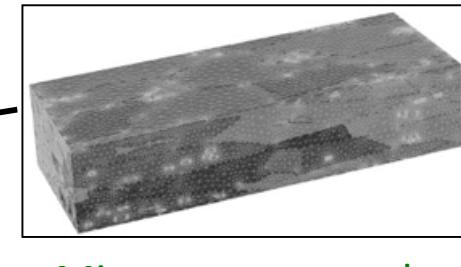
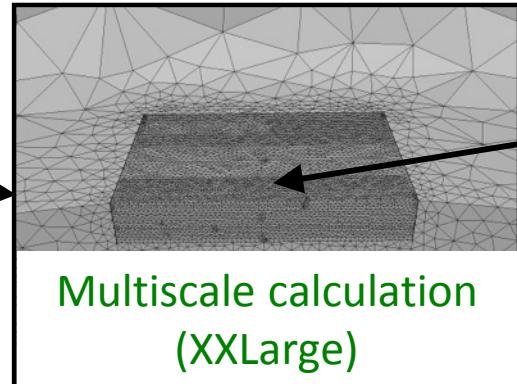
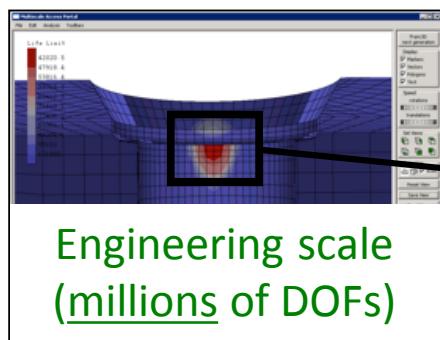


Engineering length scale (meters)



*randomly distributed brittle particles embedded in randomly oriented, anisotropic matrix* 4

# One multiscale calculation is necessary but not sufficient

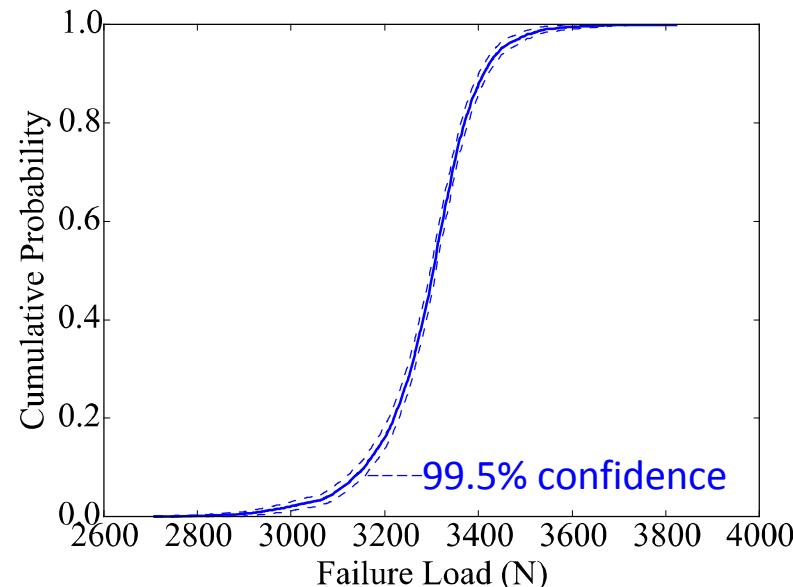


Capturing the tail of the  
cumulative failure

requires many MC samples.

**Our work aims to make this  
computationally tractable.**

**OUR  
CHALLENGE**

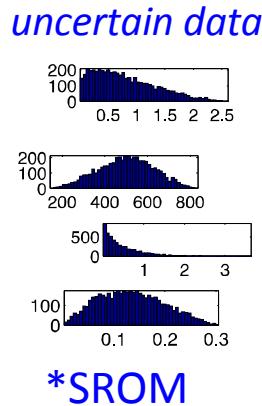


High level goal: tractably propagate fine-scale uncertainty through multiscale calculations

Why does Sandia care? Fracture is local and random, e.g., microstructure, and system/component reliability depends on phenomena occurring at various length scales.

# Schematic of our novel hierarchical approach

## Low fidelity



prior distribution

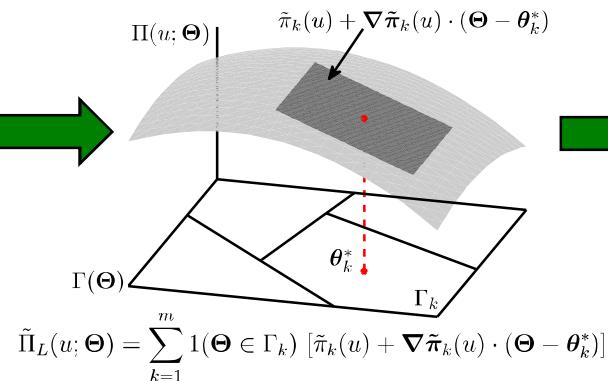
update

## Higher fidelity

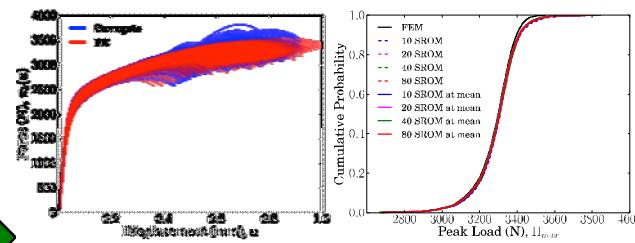
*prior distribution of conditional failure*

$$P'_{\mu}(L | a_i)$$

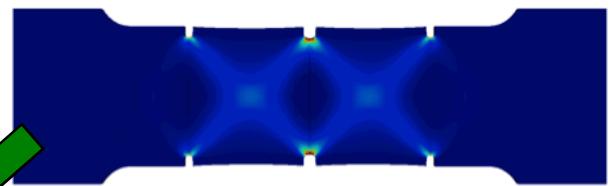
*MCS of engineering-scale response via SROM-surrogate*



*Low-fidelity Probability of Failure*



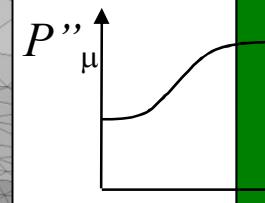
*Hot-spot selection & prioritization*



For hotspot  $i$ , iterate.  
Repeat for all hotspots.

$i++$

$$P_F(L) = \sum_i^{hotspots} P(L | a_i) P(a_i)$$



*posterior distribution of conditional failure*

$$P''_{\mu}(L | a_i)$$

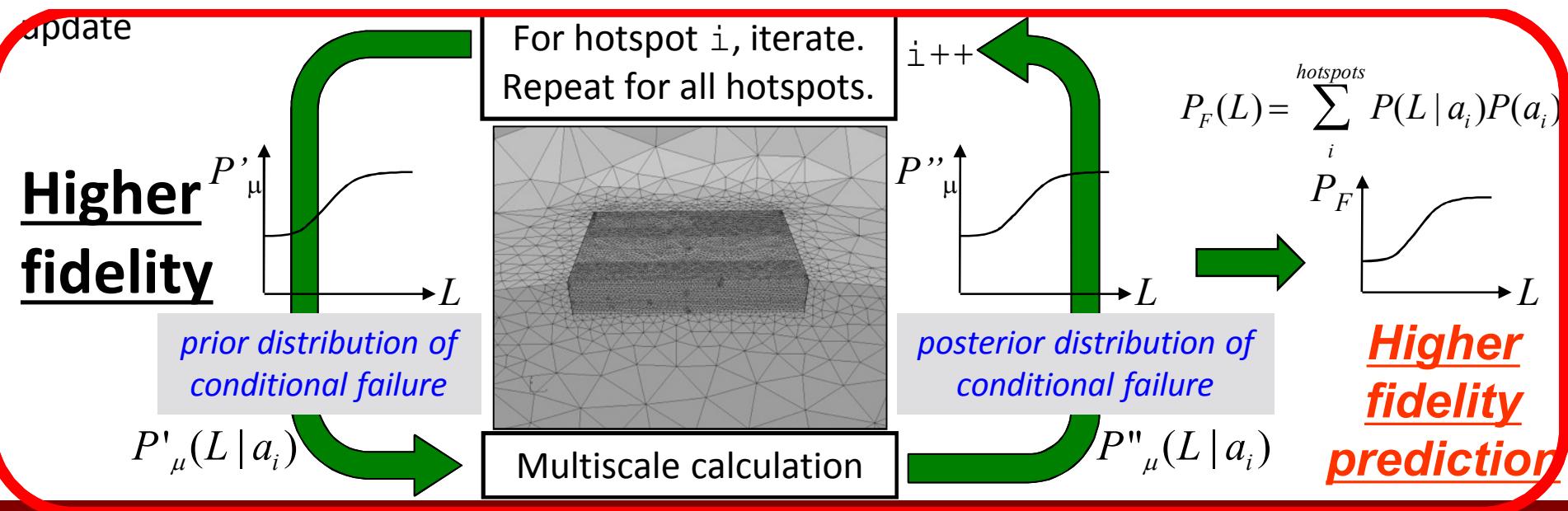
*Higher fidelity prediction*

*Multiscale calculation*

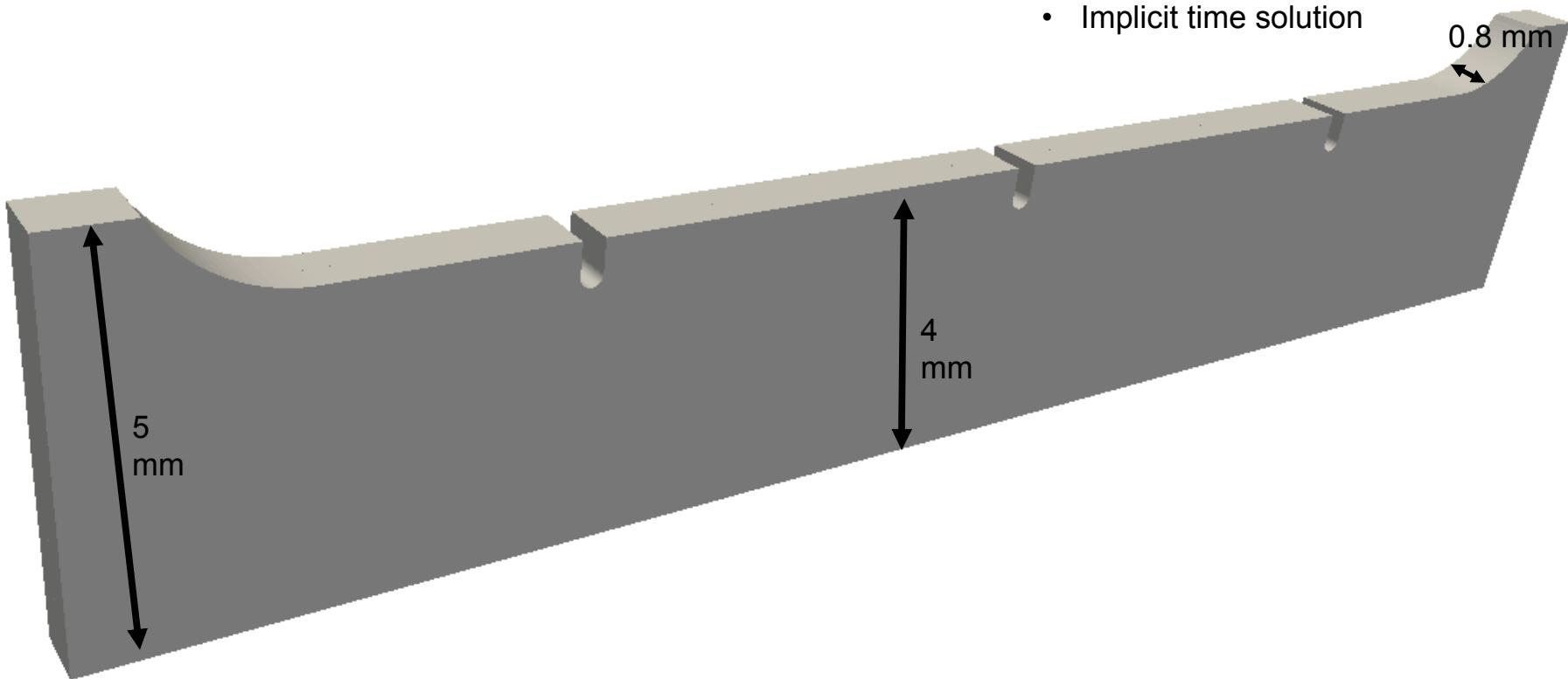
*\*\*we assume hot-spots are independent for now*

# Schematic of our novel hierarchical approach

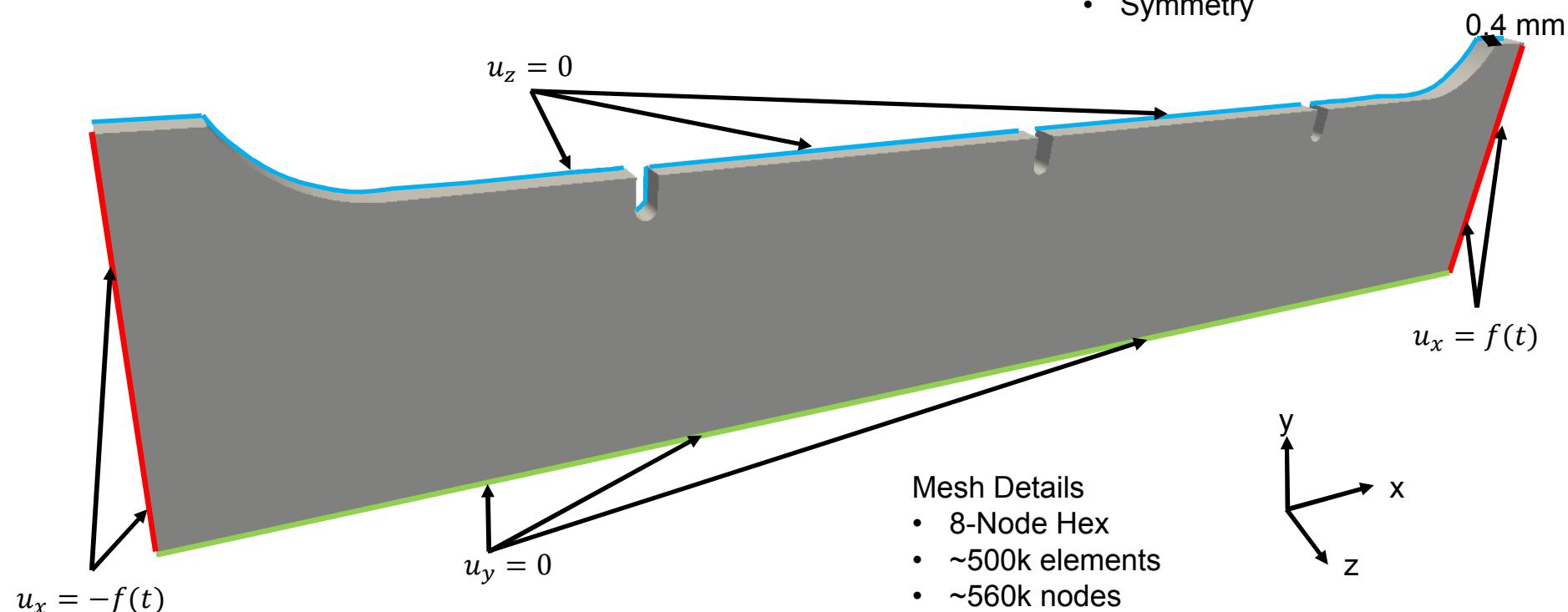
**This presentation's work focuses on this portion of the hierarchical approach**



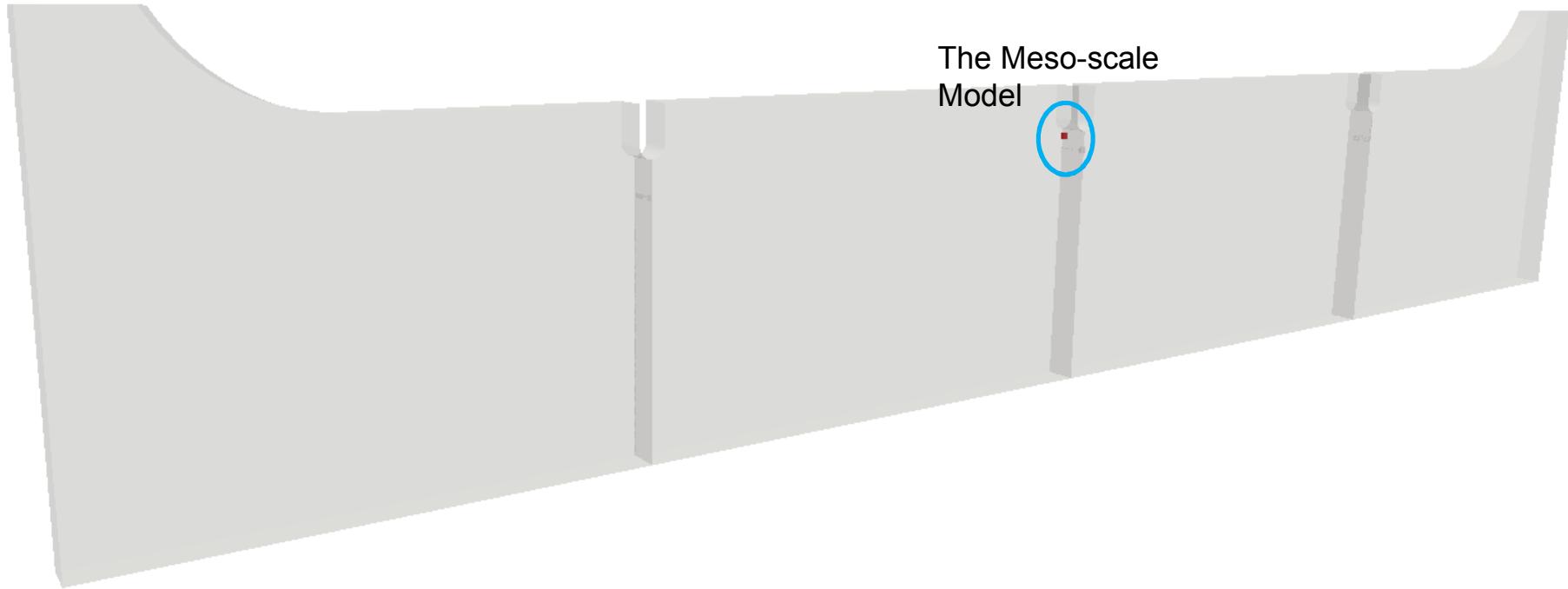
# Engineering Scale Model



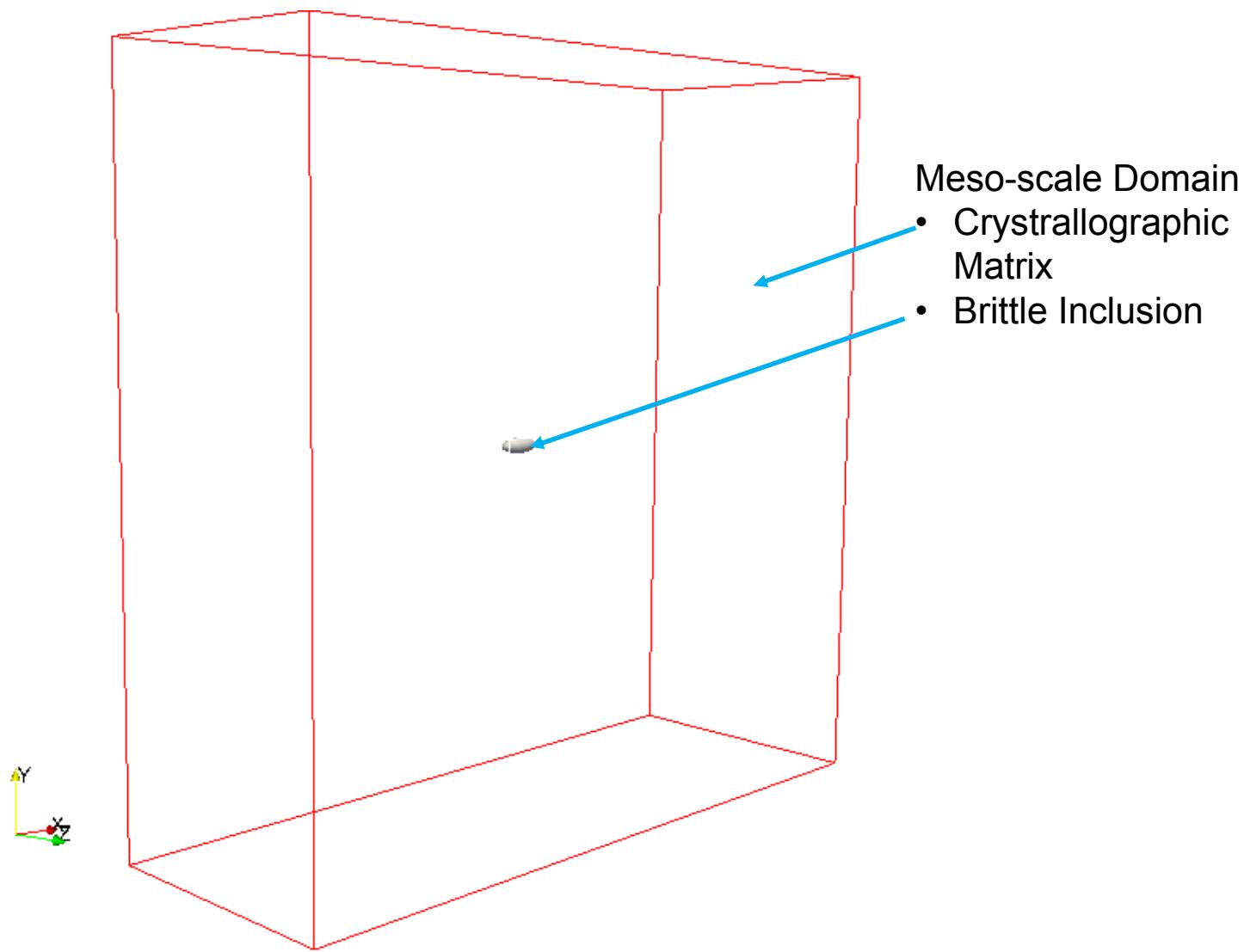
# Engineering Scale Model



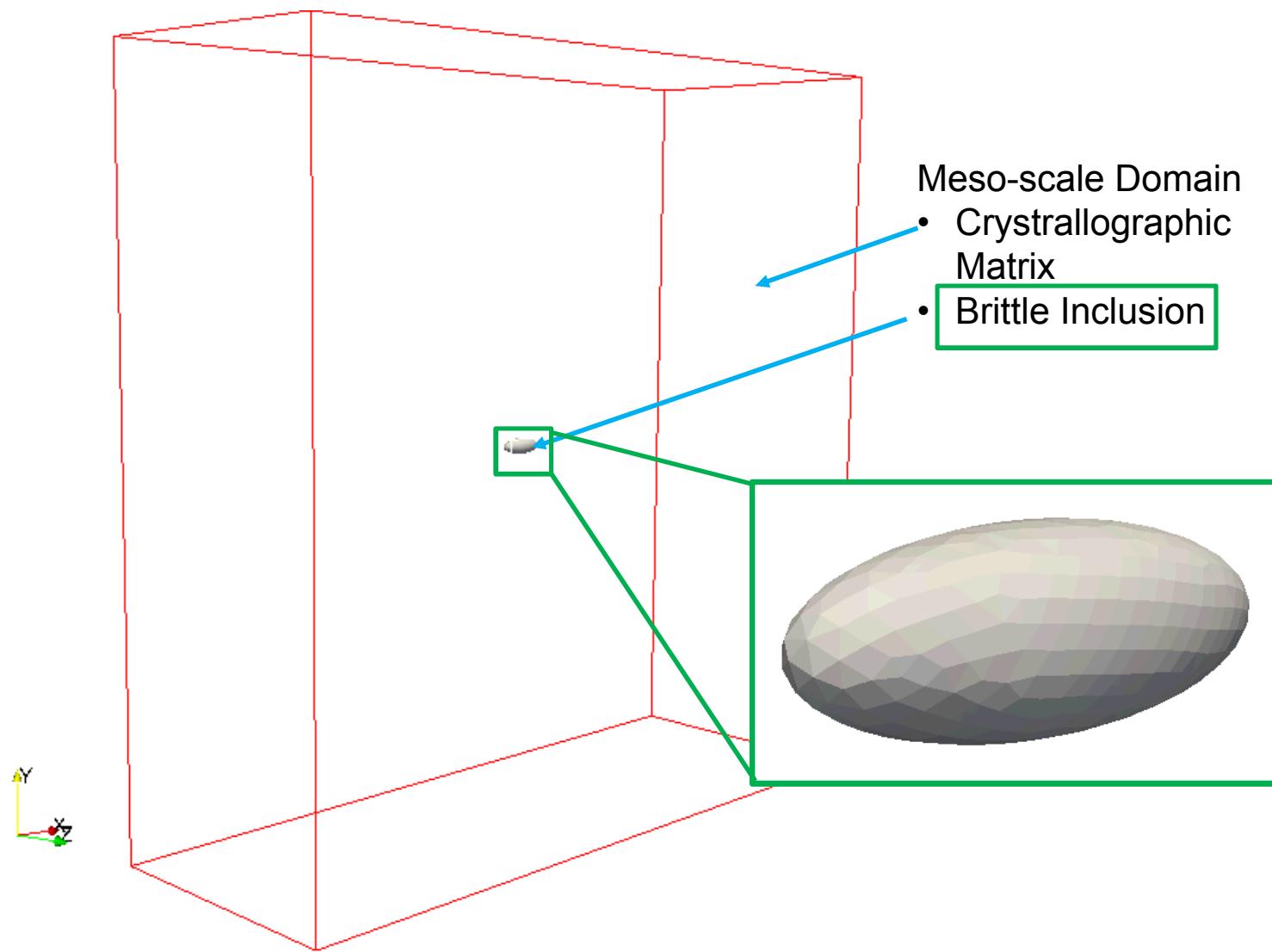
# Switching Scales



# Meso-scale Model

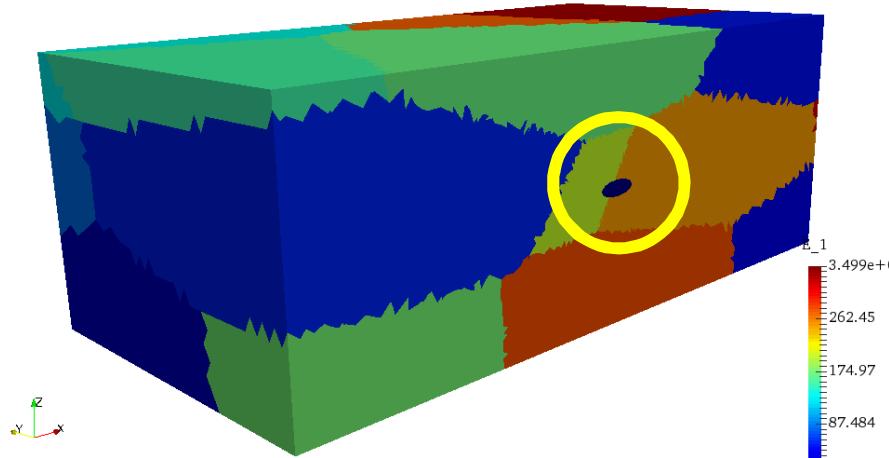


# Meso-scale Model



# Brittle second phase – void nucleation

- Embed an ellipsoidal particle,  $5 \times 1.8 \mu\text{m}$
- Coherent mesh at particle/matrix interface
- 1 morphology (grain geometry) w/  $\sim 27$  grains
- 10 statistical samples of grain orientations
- Grain orientation statistics to match measured experimental data
- Assumed elastic mechanical properties for particle (pure iron)
  - $E = 211 \text{ GPa}$ ,  $\nu = 0.29$
  - Strength 540 MPa
- Assumed perfect and rigid particle/matrix interface bond



*Cross-section through major-axis of ellipsoid*

# Multiscale model considerations

Wish to study the impact of:

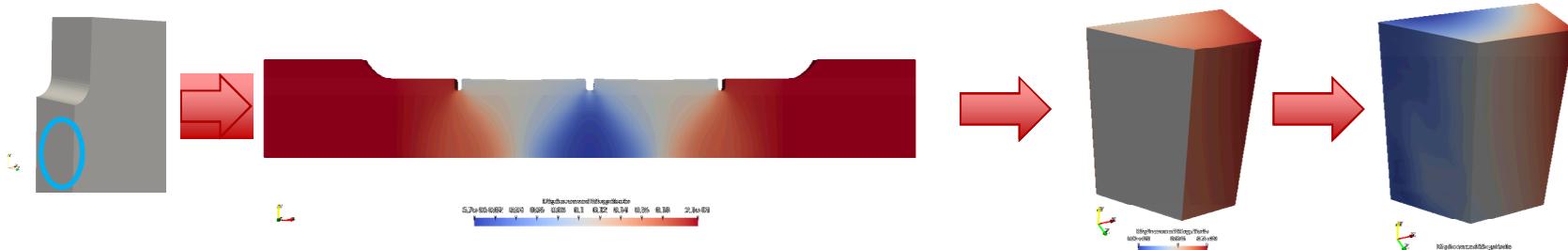
- Multiscale coupling
- Meso-scale model meshing with respect to grains

On the propagation of uncertainty in grain material orientation with respect to:

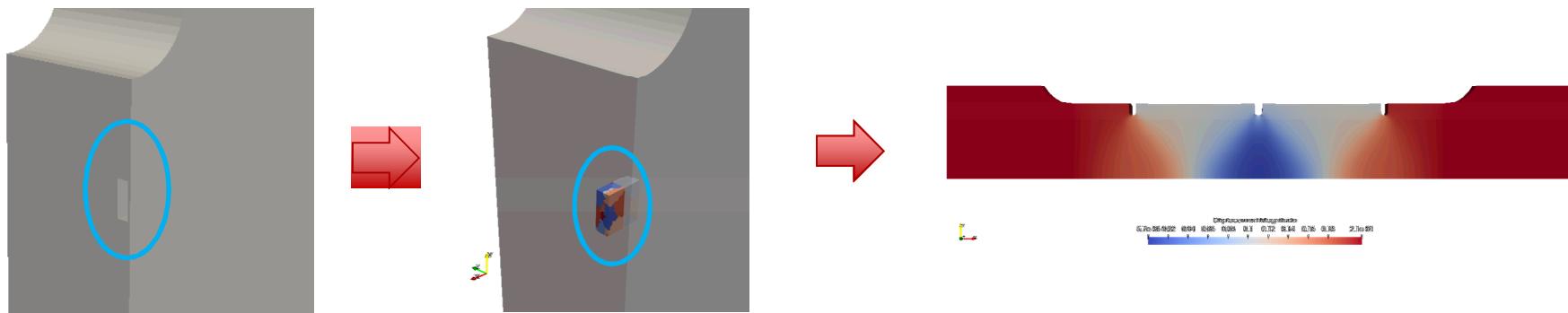
- Brittle inclusion average stress
- Brittle inclusion maximum stress

# Coupling approaches

Submodeling (one-way coupling)



MPC Coupling, Concurrent multiscale modeling (two-way coupling)



# Coupling approaches

## Submodeling (one-way coupling)

- No homogenization
- Map computed displacements from engineering scale model as Dirichlet boundary conditions on the extents of the meso-scale model

## MPC Coupling, Concurrent multiscale modeling (two-way coupling)

- No homogenization
- Directly embed meso-scale model into location of interest

# Coupling approaches

## Submodeling (one-way coupling)

### ***Moderately Expensive:***

Compute once for each unique engineering scale model

### ***Moderately Expensive:***

Compute for each UQ random sample

## MPC Coupling, Concurrent multiscale modeling (two-way coupling)

### ***Very Expensive:***

Compute for each UQ random sample

# Watch mean, first-principal stress in the particle

Assuming elastic and brittle,  
monitor the mean first-principal  
stress in the particle.

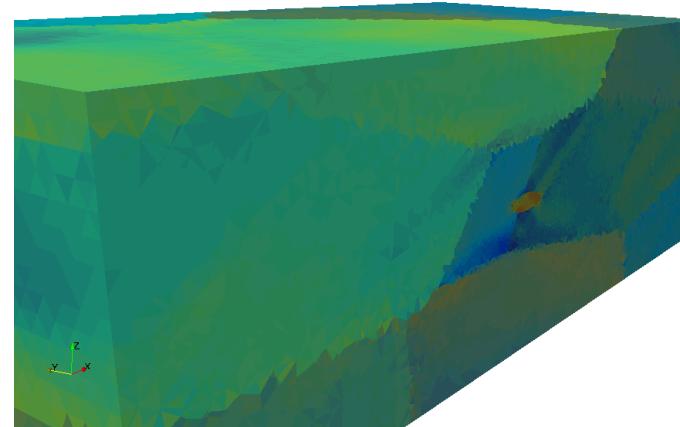
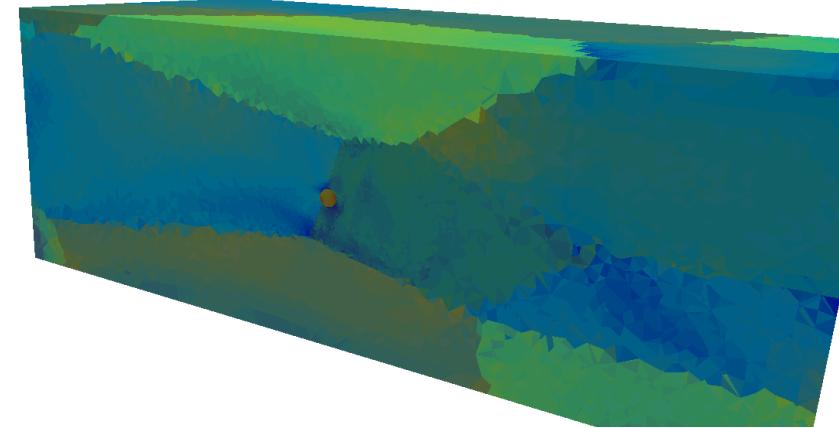
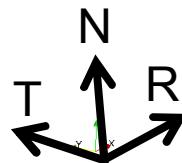
$$Pr(\bar{\epsilon}_{RVE} \in S)$$

$$S = \{\bar{\epsilon}_{RVE} \in \mathbb{R} : g(\bar{\epsilon}_{RVE}) \leq 0\}$$

$$g(\bar{\epsilon}_{RVE}) = \bar{\sigma}_{p,cr} - \bar{\sigma}_p(\bar{\epsilon}_{RVE})$$

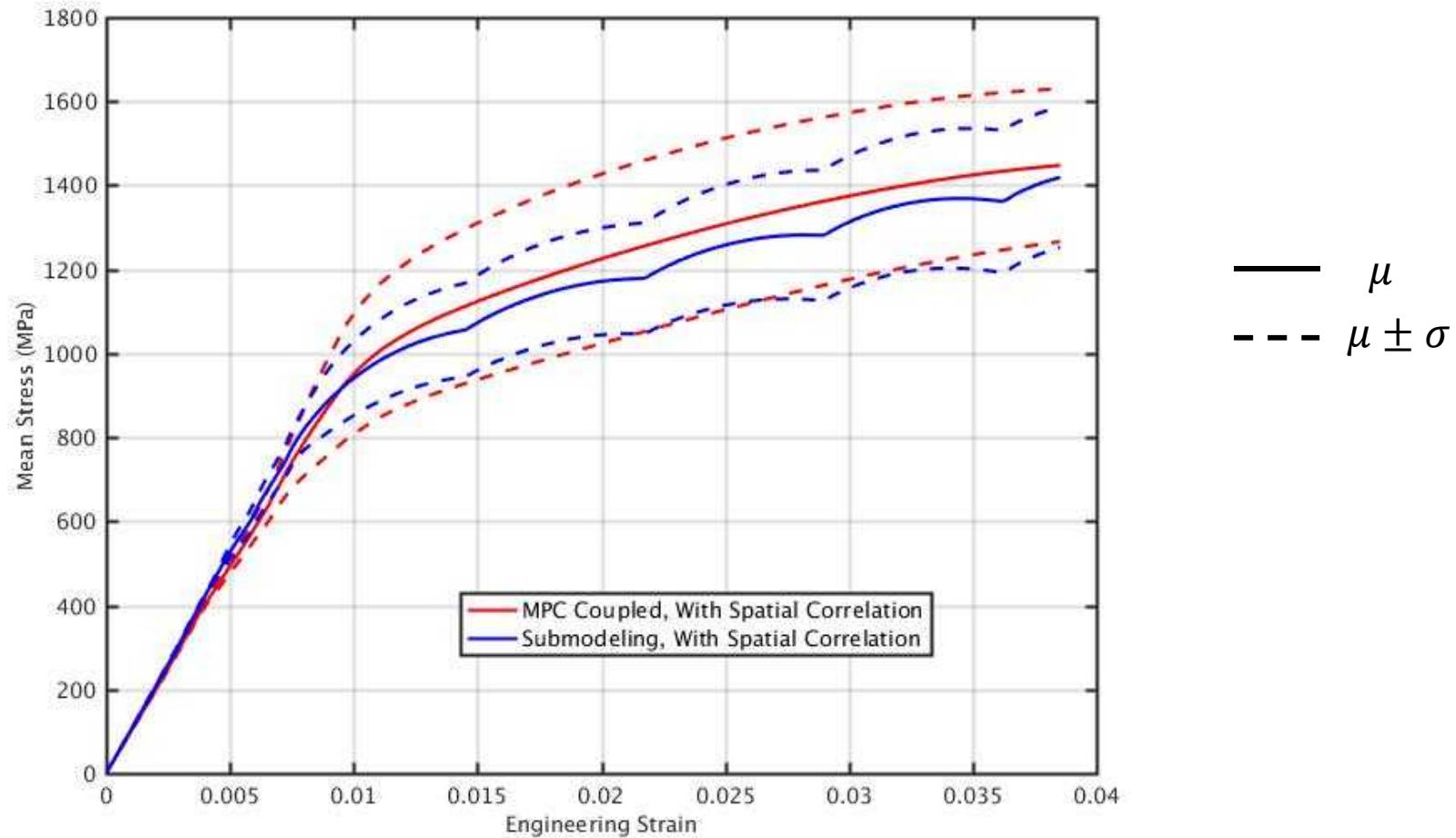
$$\bar{\sigma}_{p,cr} = 540 \text{ MPa}$$

*Maximum principal stress contour plot for s123  
(showing two cross-sections)*

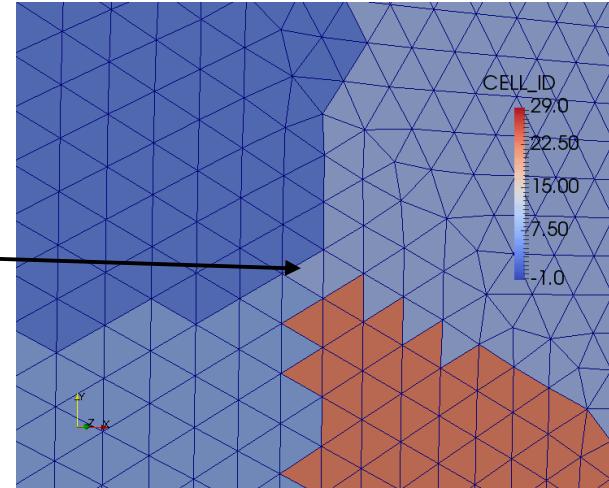
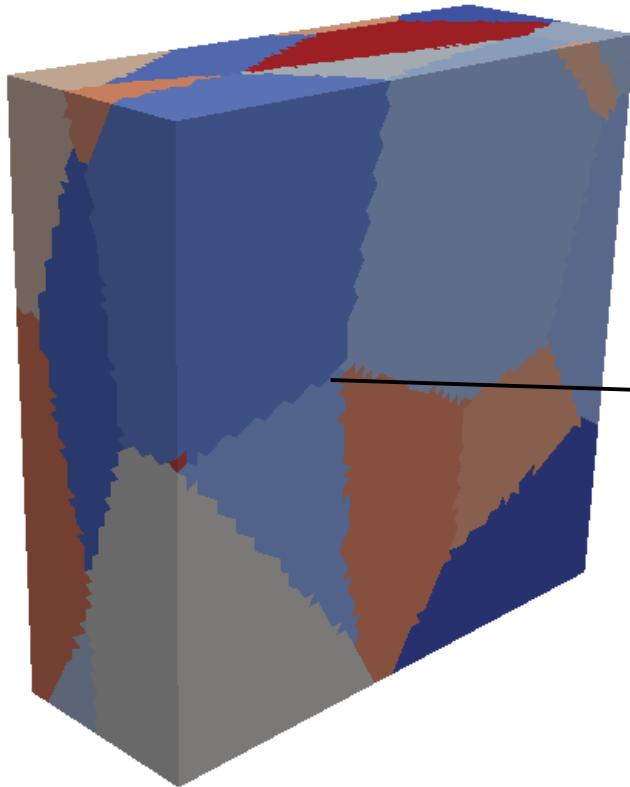


# Coupling Comparison

Grain orientations have spatial correlation



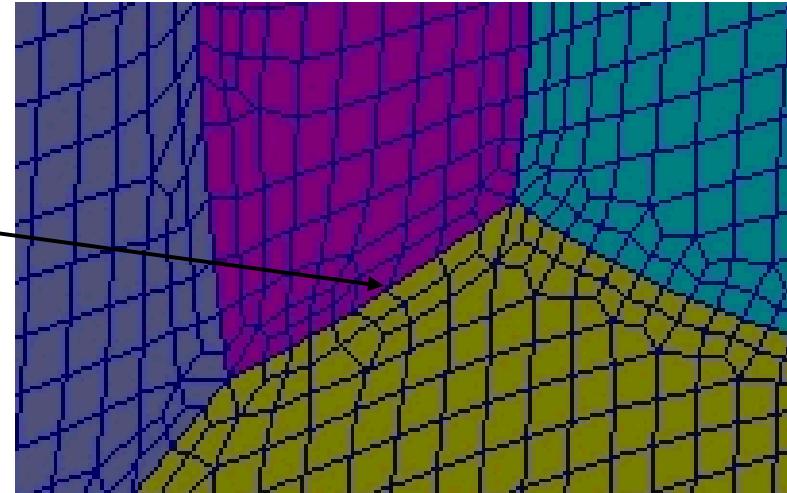
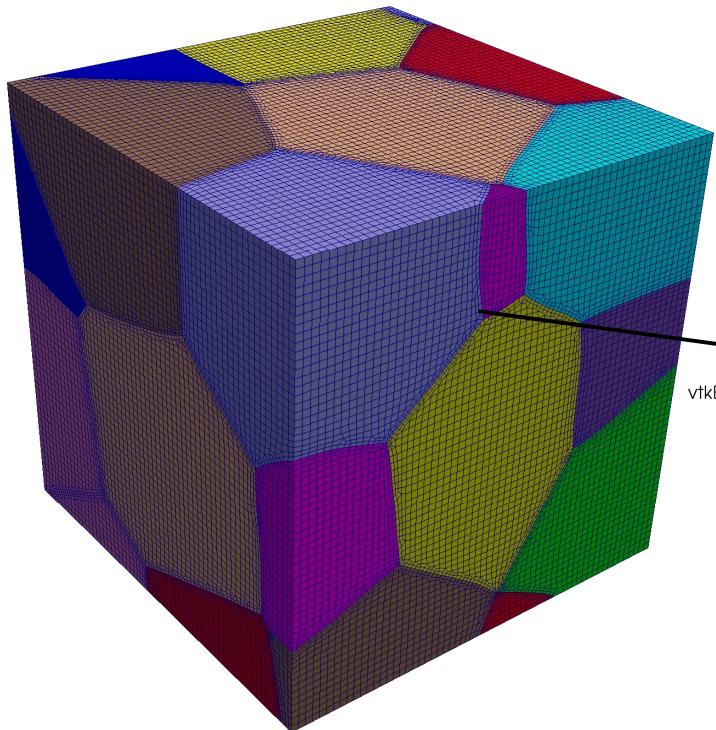
# Meshering approaches



Simpler (Not grain aligned) approach:

- Conformal mesh at volume extents and ellipsoid inclusion
- Element boundaries will not align with grains (jagged grain boundary)

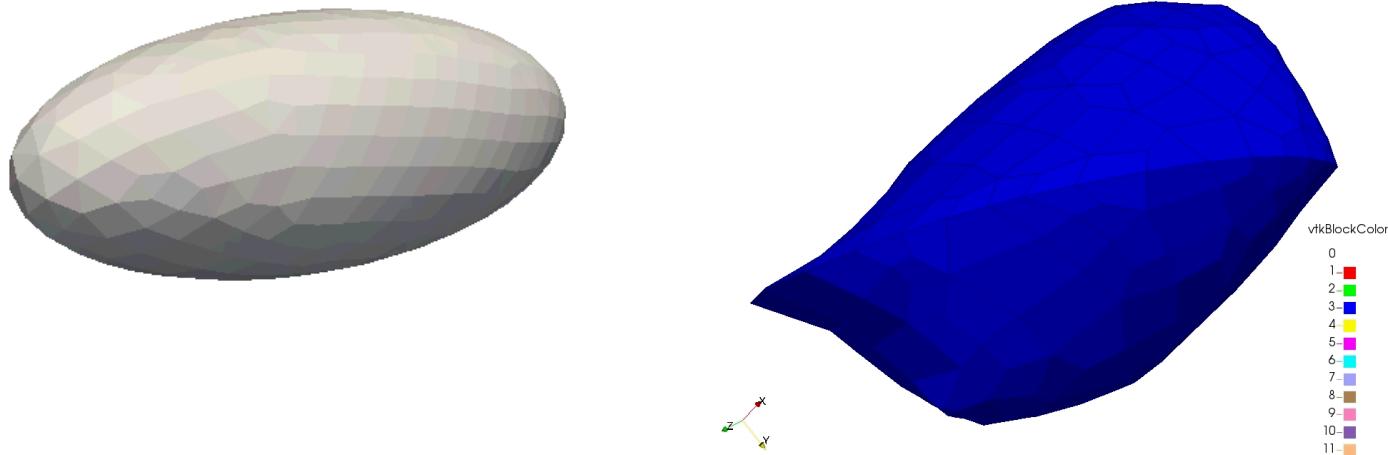
# Meshing approaches



More expensive (Grain aligned) approach:

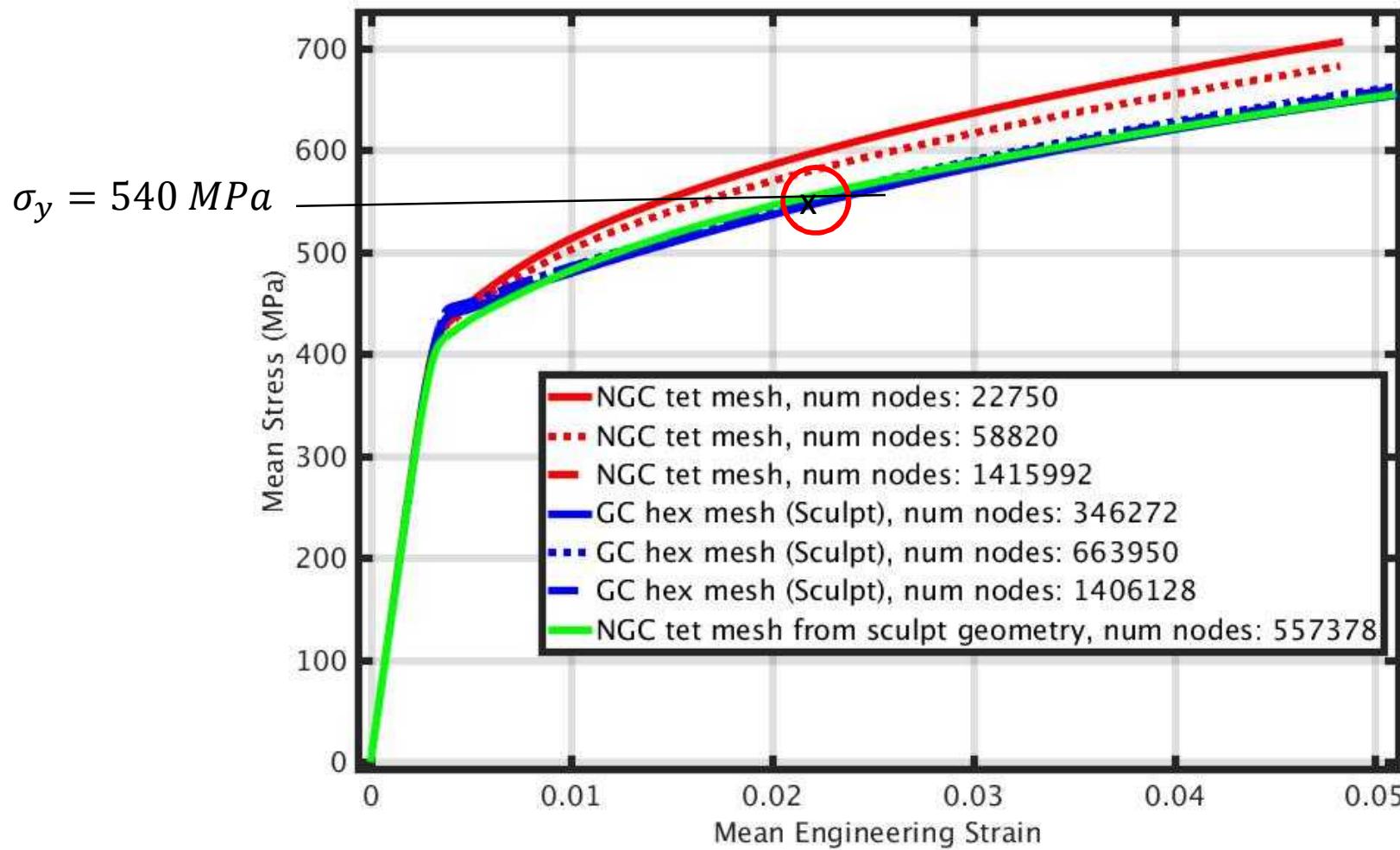
- Use meshing tool (Sculpt) to provide a hexahedral mesh that aligns with ellipsoid and grain boundaries
- Sculpt is an overlay-grid or mesh-first method
- Sculpt does not exactly align nodes with geometries (differences in ellipsoid size and shape are visible)

# Inclusion geometry differences

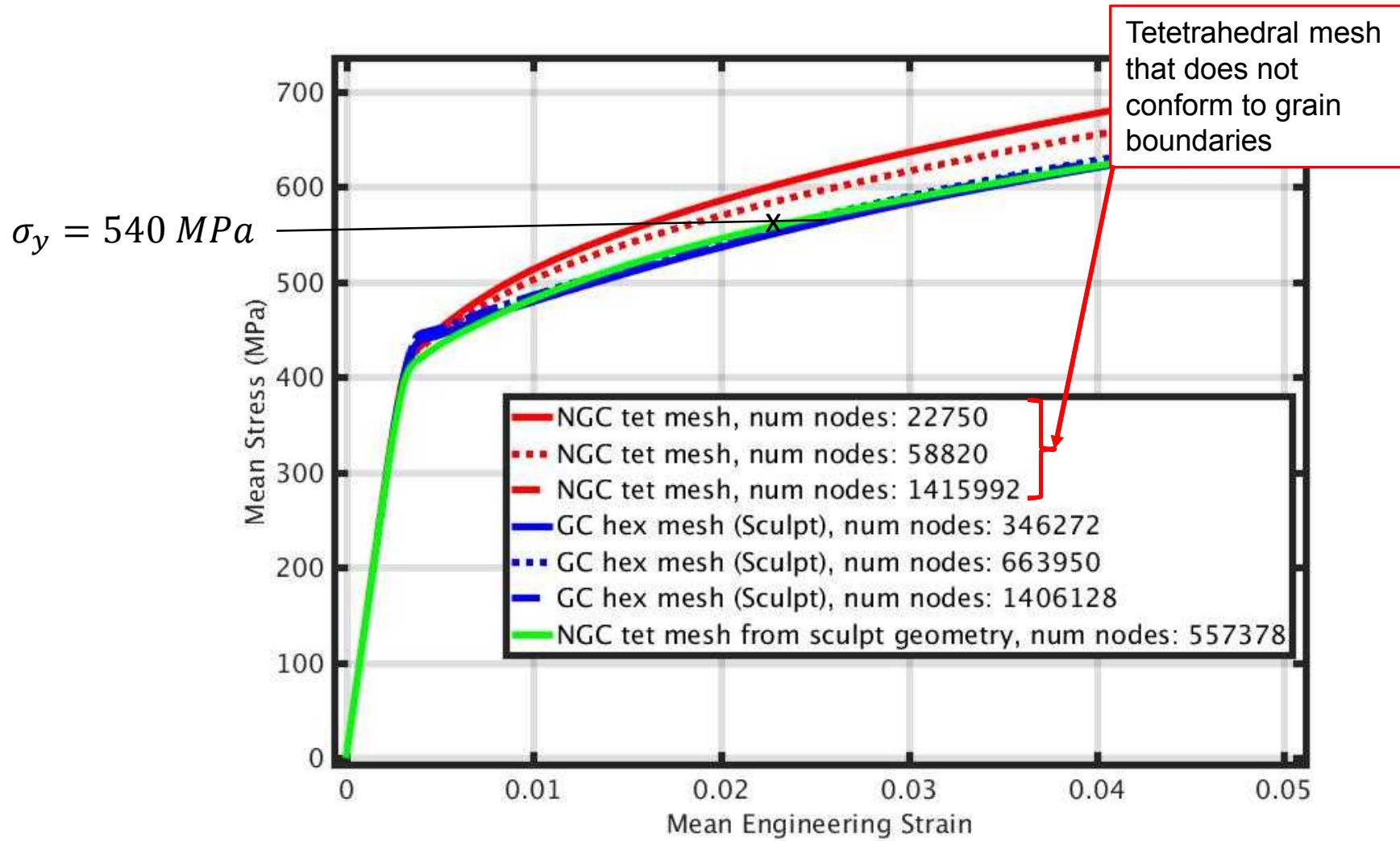


- Sculpt will not precisely adhere to geometry
- Small features (such as inclusion) can be poorly resolved
- Use 5x larger inclusion in following comparison
- Also extract sculpt inclusion geometry and mesh with tetrahedral elements for comparison (jagged grain boundaries)

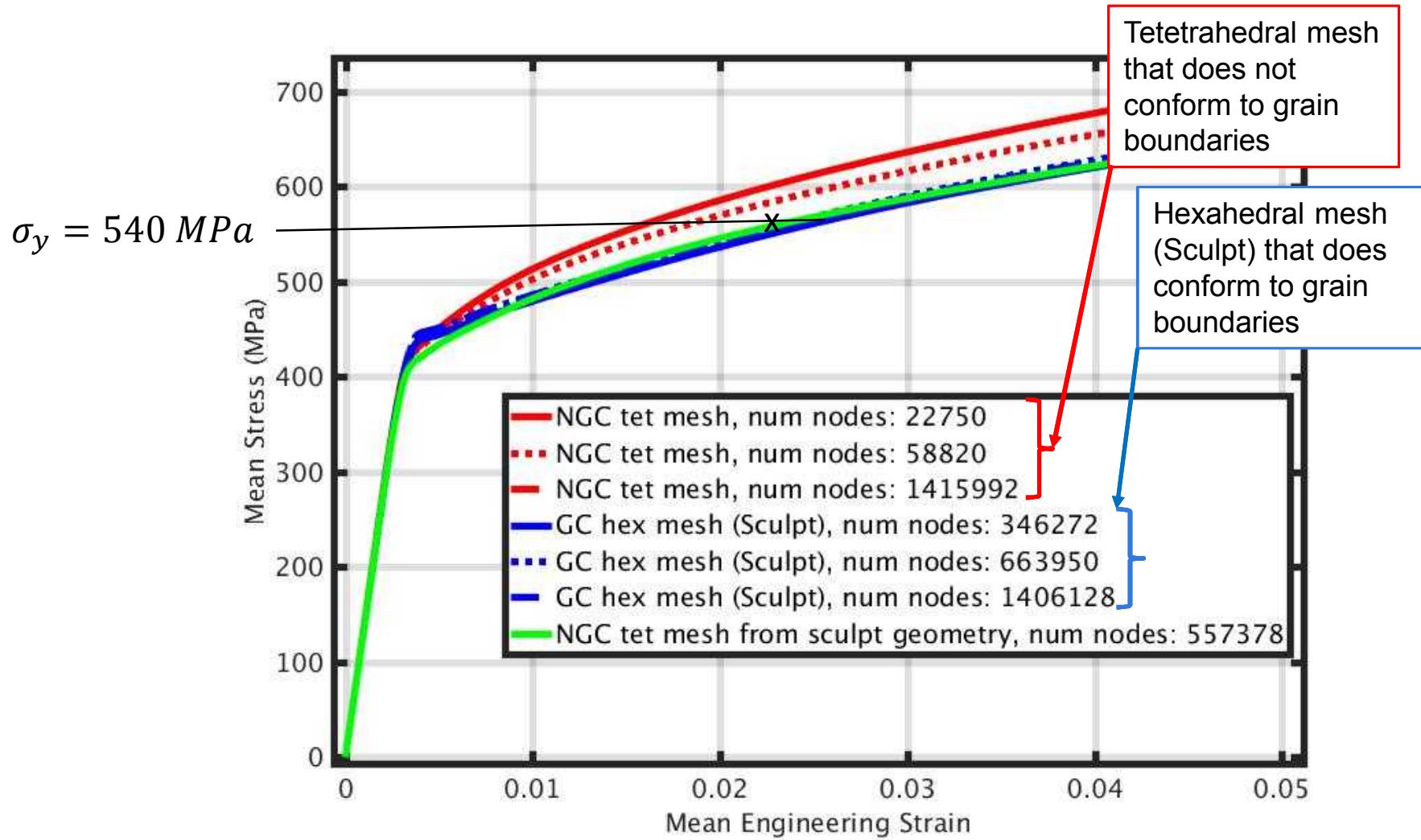
# Meshering consideration results



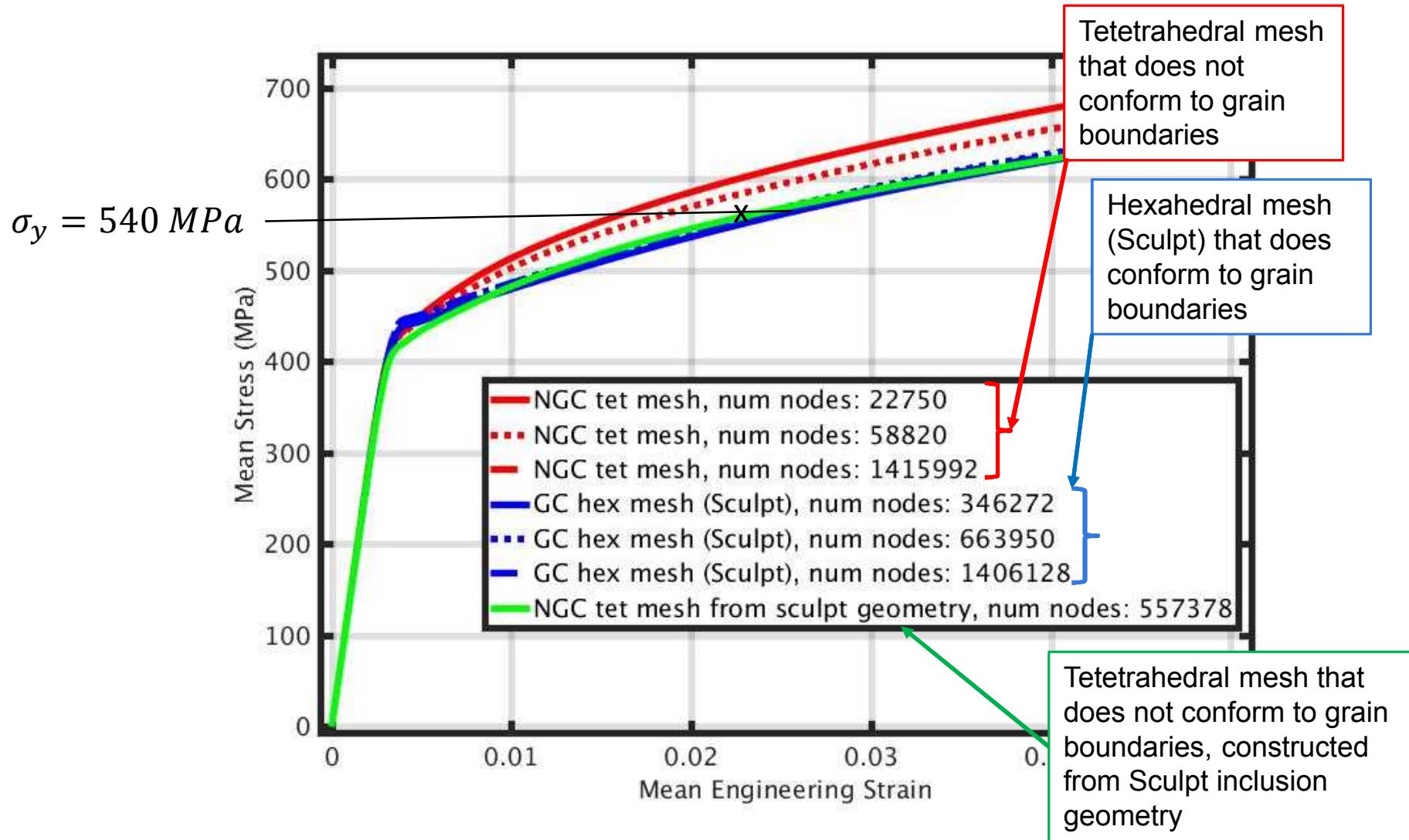
# Meshering consideration results



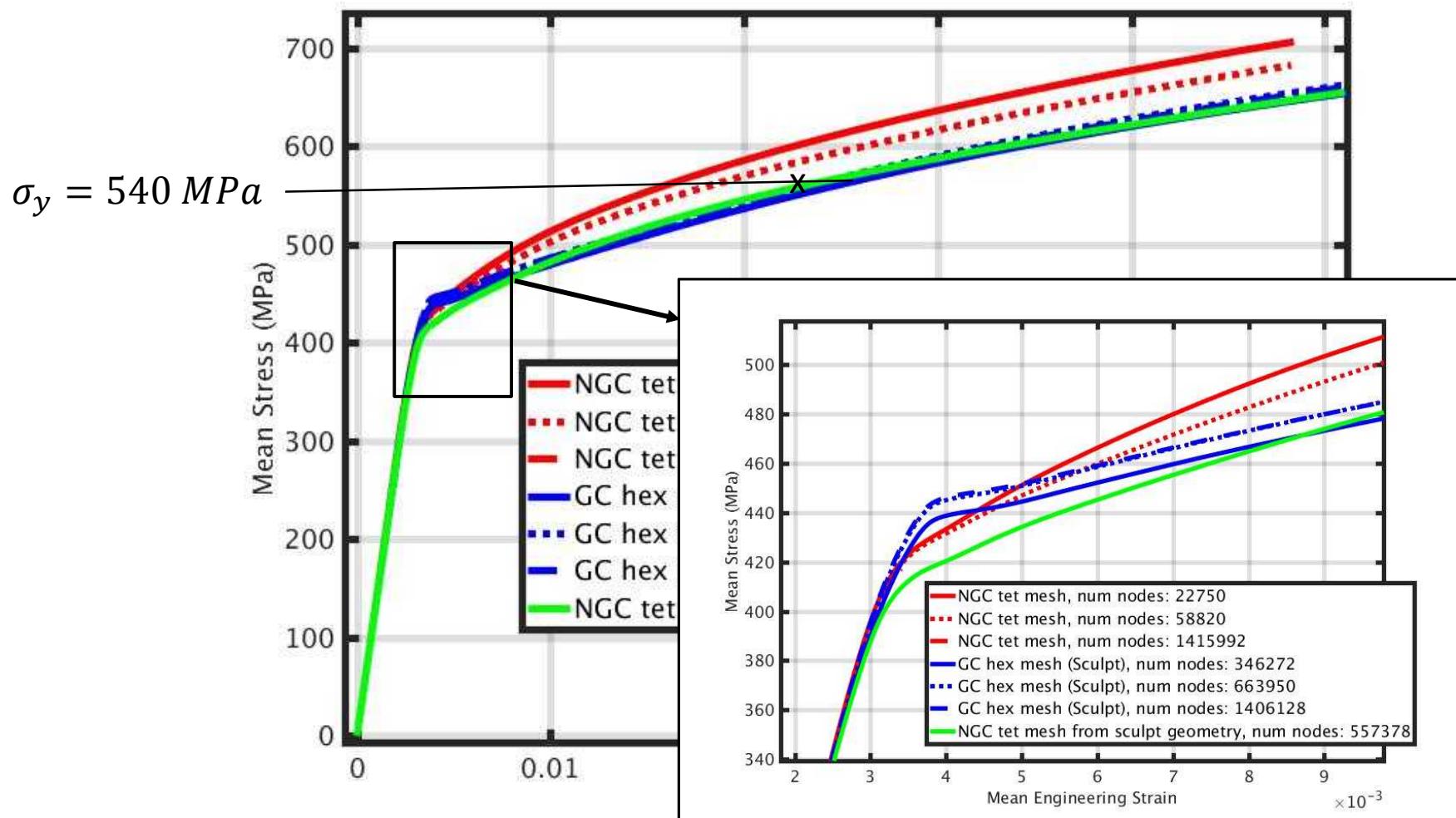
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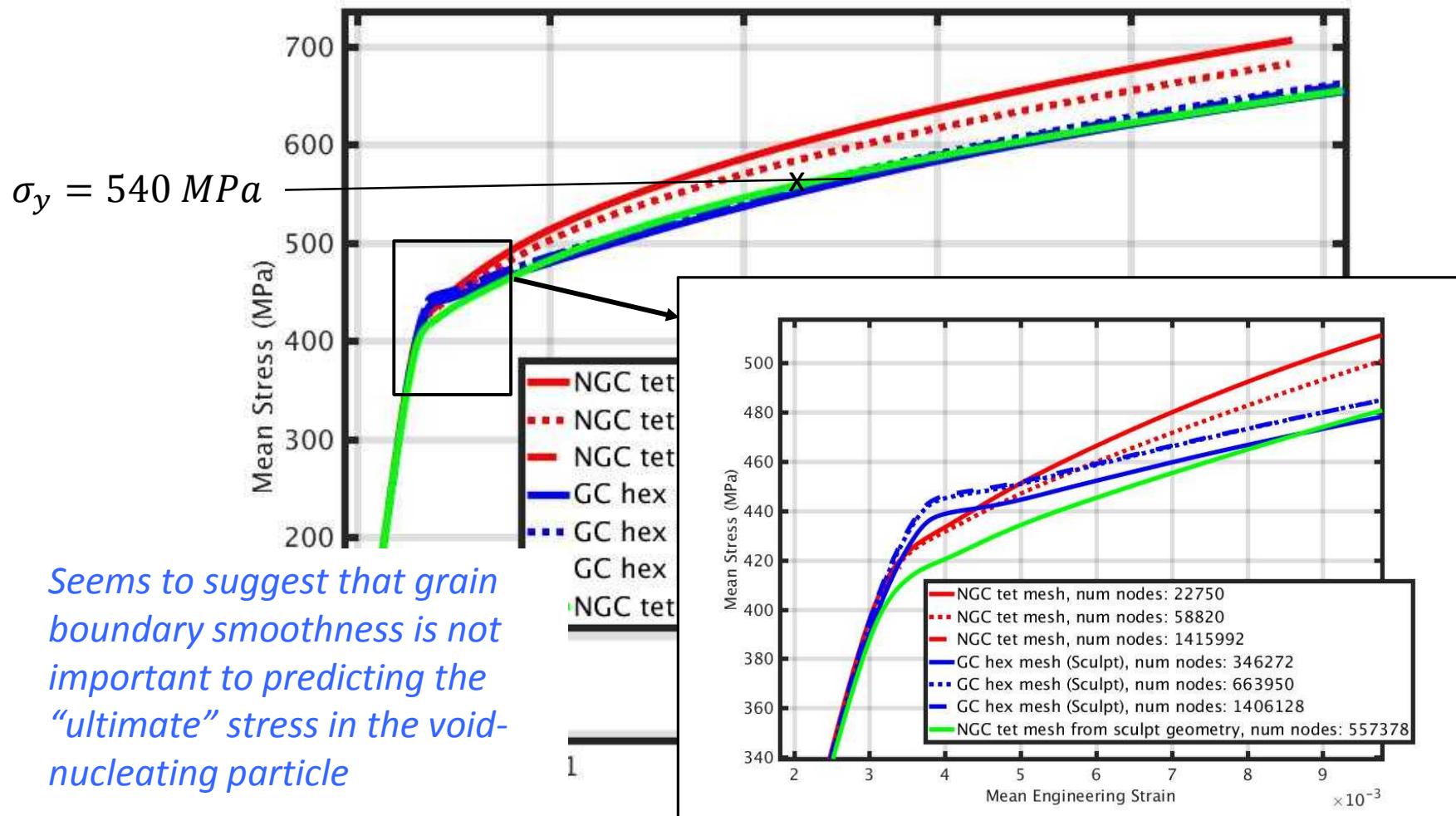
# Meshering consideration results



# Meshing consideration results



# Meshering consideration results



# Conclusions

- At a minimum submodeling appears necessary to estimate mean failure behavior at meso-scale
- With a high fidelity constitutive model at the engineering scale, submodeling holds promise for this work
- Concurrent (two-way) coupling may be necessary to accurately propagate higher moments (standard deviation) of the distribution of mean strains at failure
- Grain boundary smoothness (aligned element edges) is not important to predicting the “ultimate” stress in the void nucleating particle

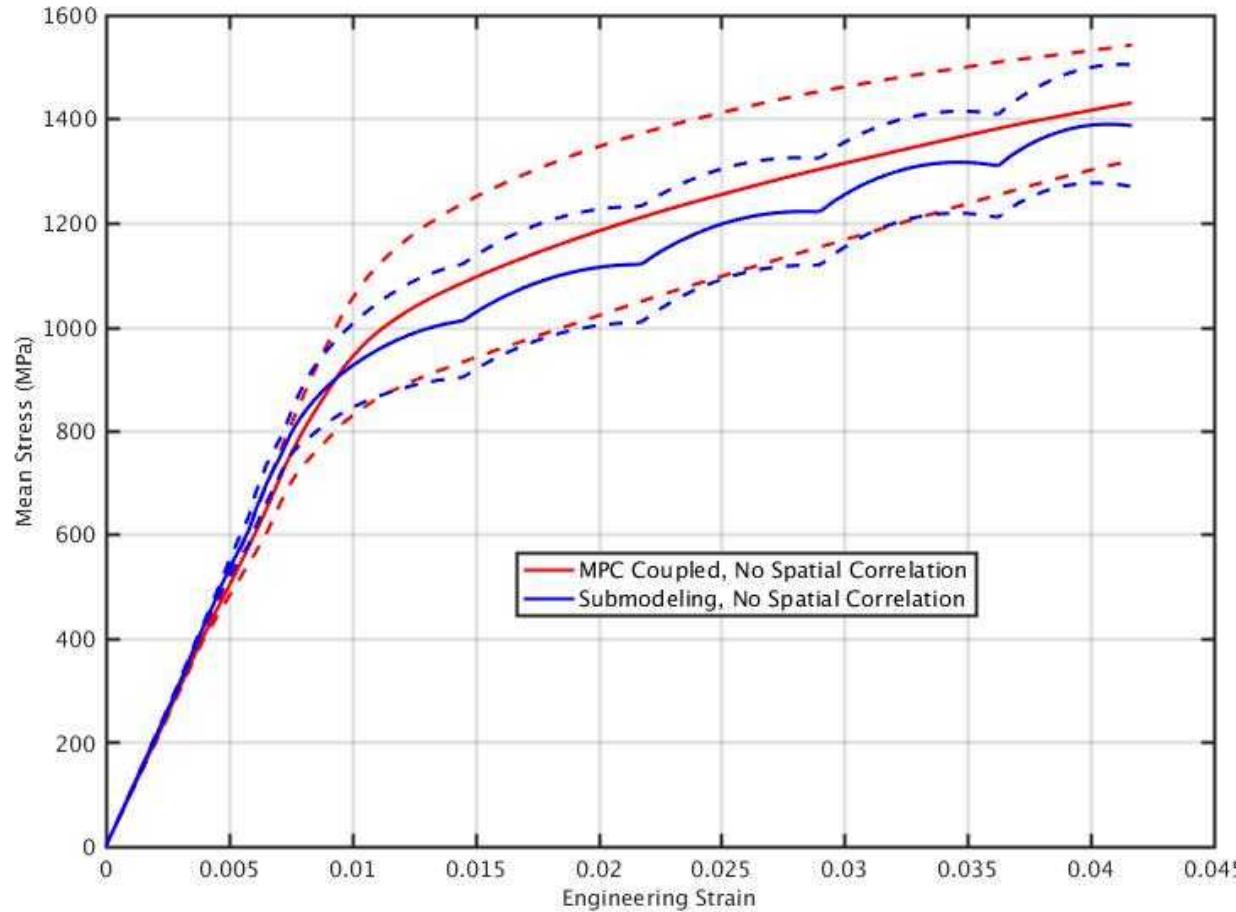
# References

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6. A. Ghahremaniezhad and K. Ravi-Chandar (2012). Ductile failure behavior of polycrystalline Al 6061-T6. *International Journal of Fracture*, 174: pp. 177-202.
7. A. Ghahremaniezhad and K. Ravi-Chandar (2013). Ductile failure behavior of polycrystalline Al 6061-T6 under shear dominant loading. *International Journal of Fracture*, 180: pp. 23- 39

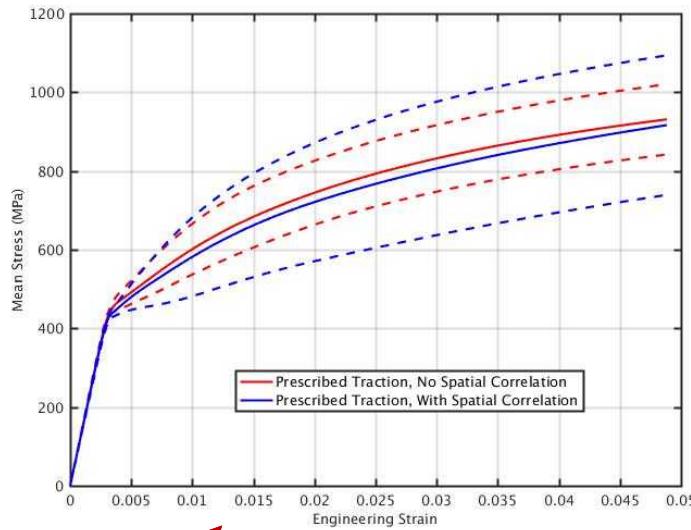
# ADDITIONAL MATERIAL

# Coupling Comparison

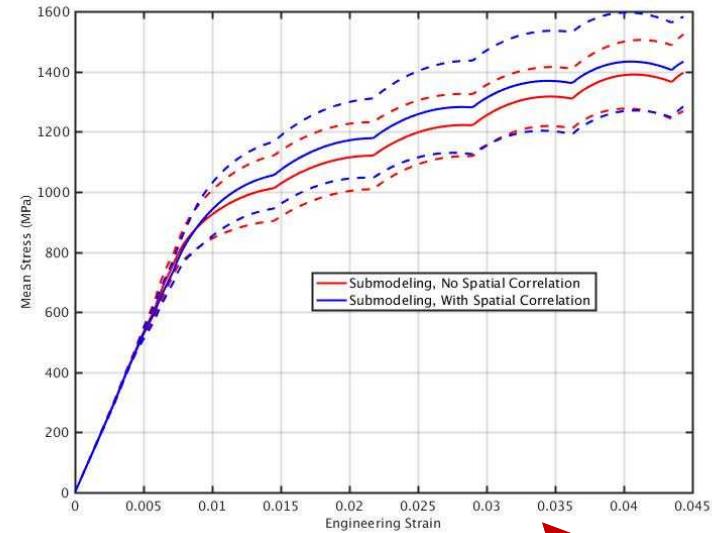
Grain orientations have no spatial correlation



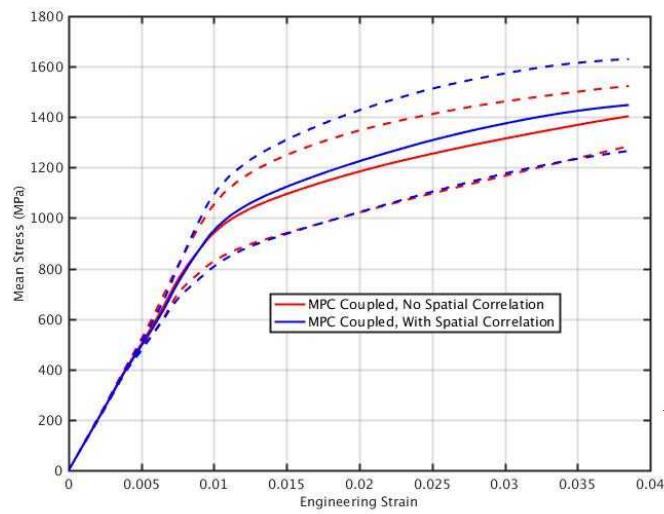
# Grain orientation spatial correlation impact



Prescribed traction

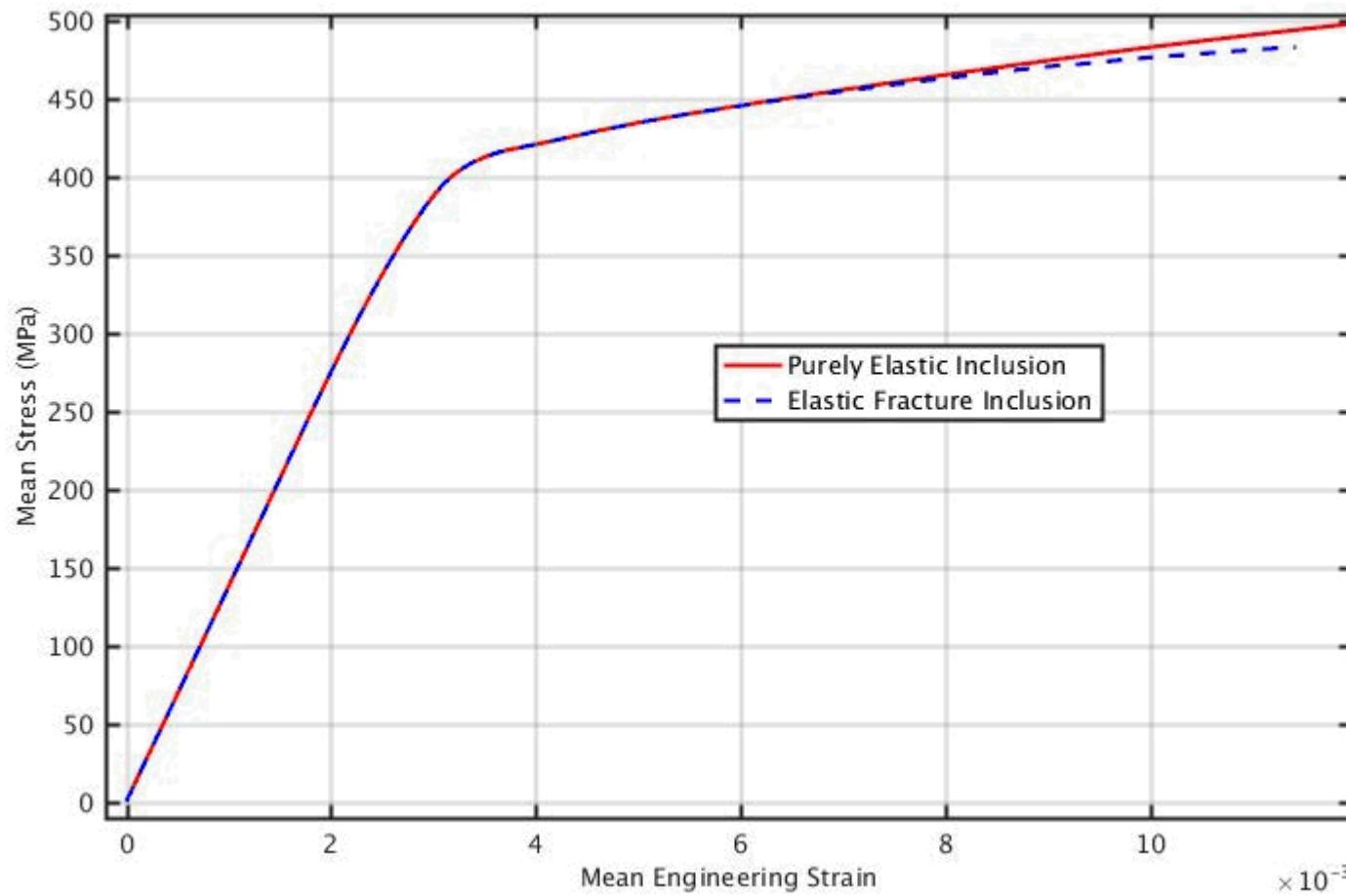


Submodeling



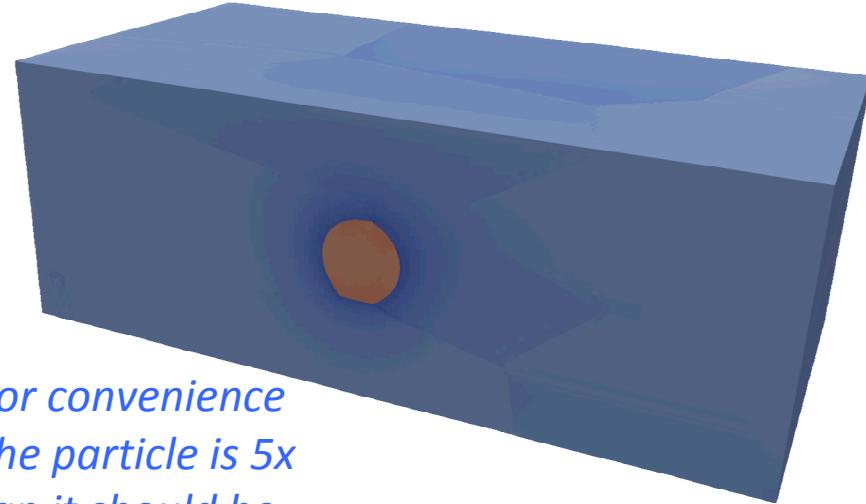
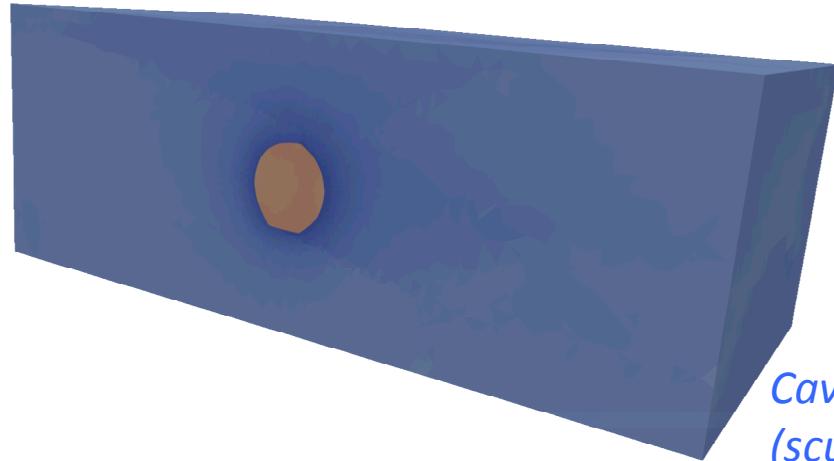
MPC Coupled

# Inclusion Material Model

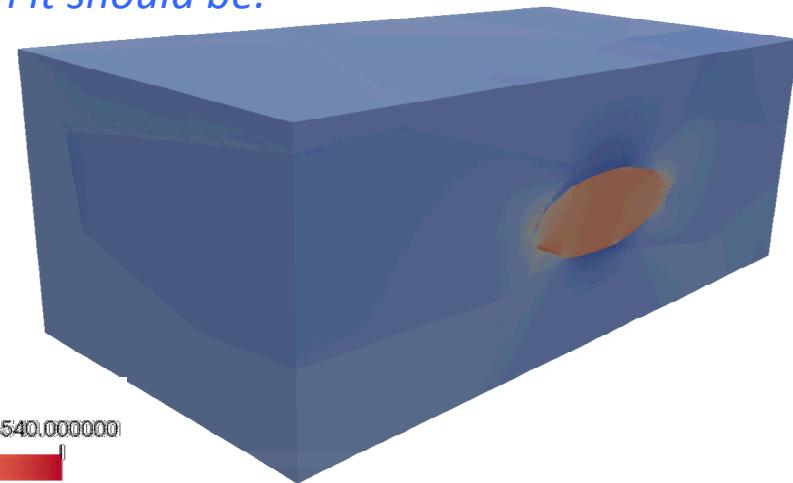
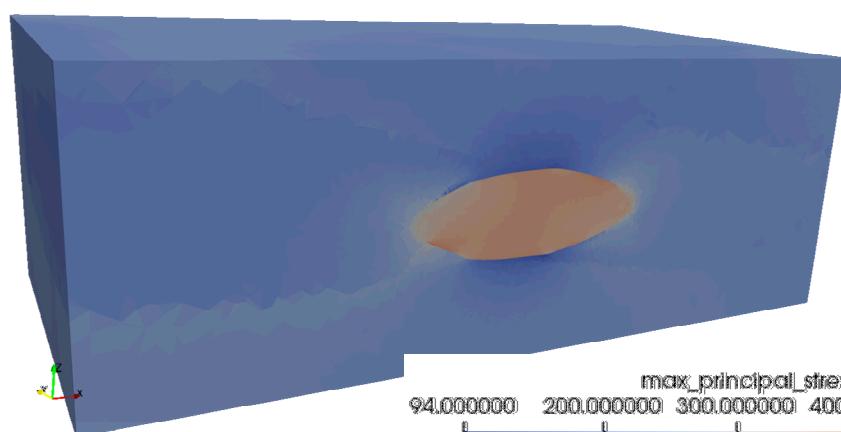


# Computed stress in the particle

We sculpted the mesh and we overlayed tets on a mesh with the sculpted particle

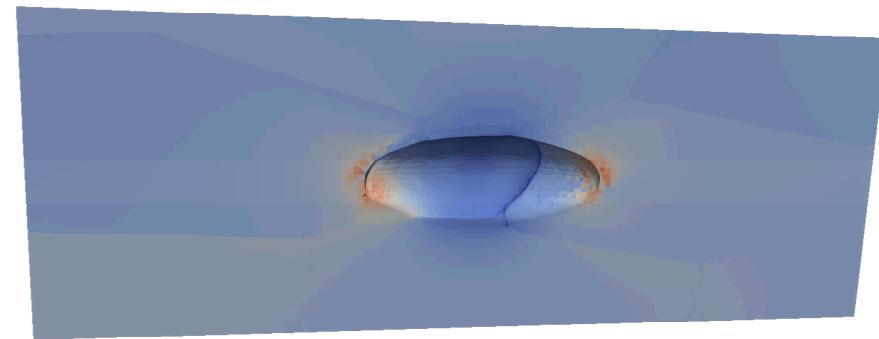
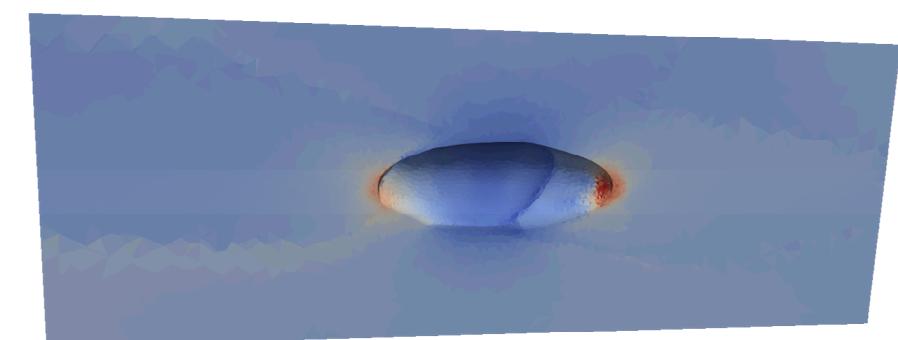
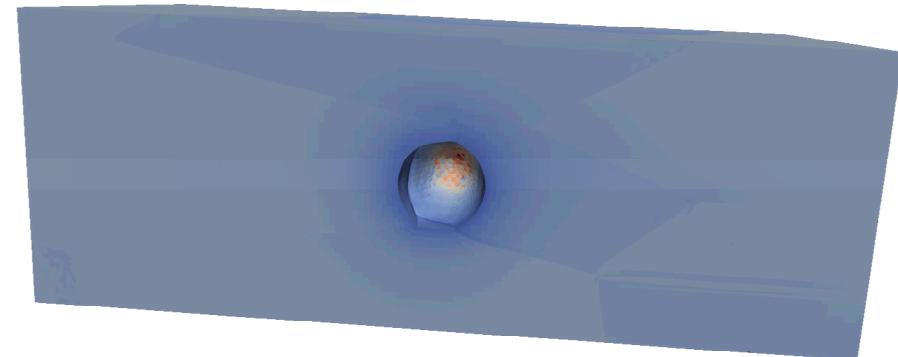
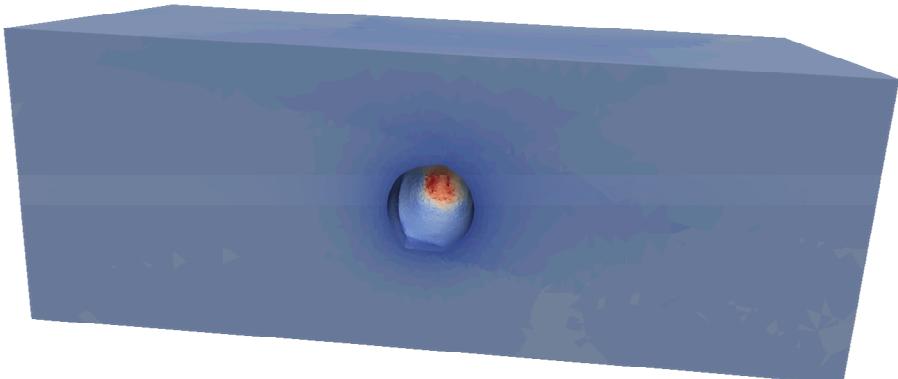


*Caveat: for convenience  
(sculpt) the particle is 5x  
larger than it should be.*



max\_principal\_stress\_1  
94.0000000 200.0000000 300.0000000 400.0000000 540.0000000

# Computed stress nearby the particle



# Computed stress in the particle

