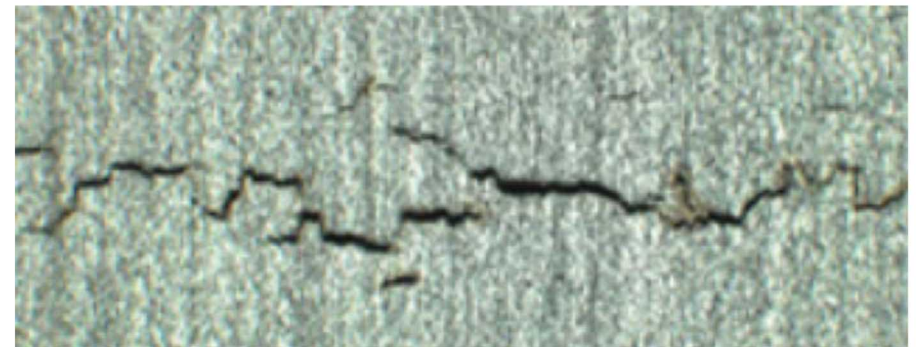
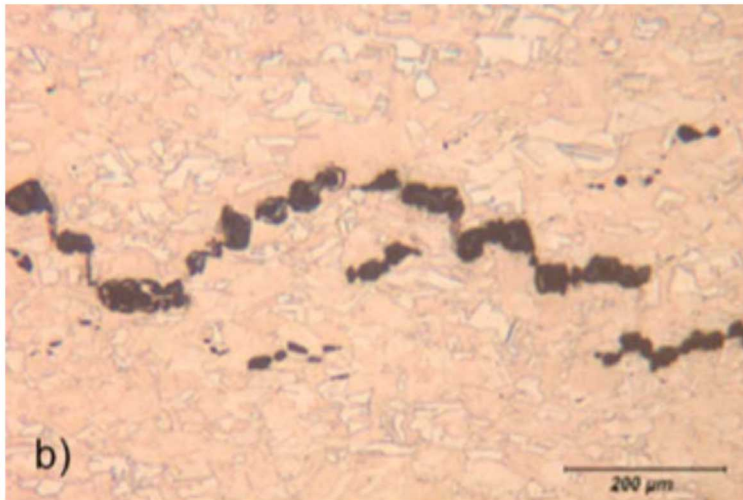
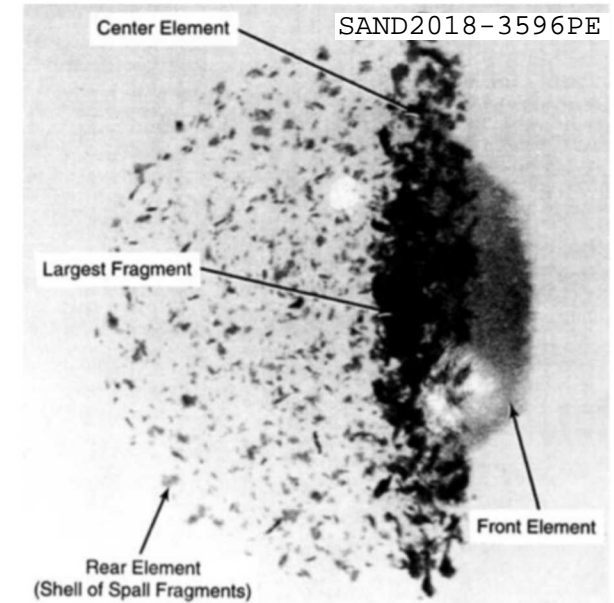


# Spall and Fragmentation

**Tracy Vogler**

**Department 8256, Mechanics of Materials  
Sandia National Laboratories, Livermore CA**

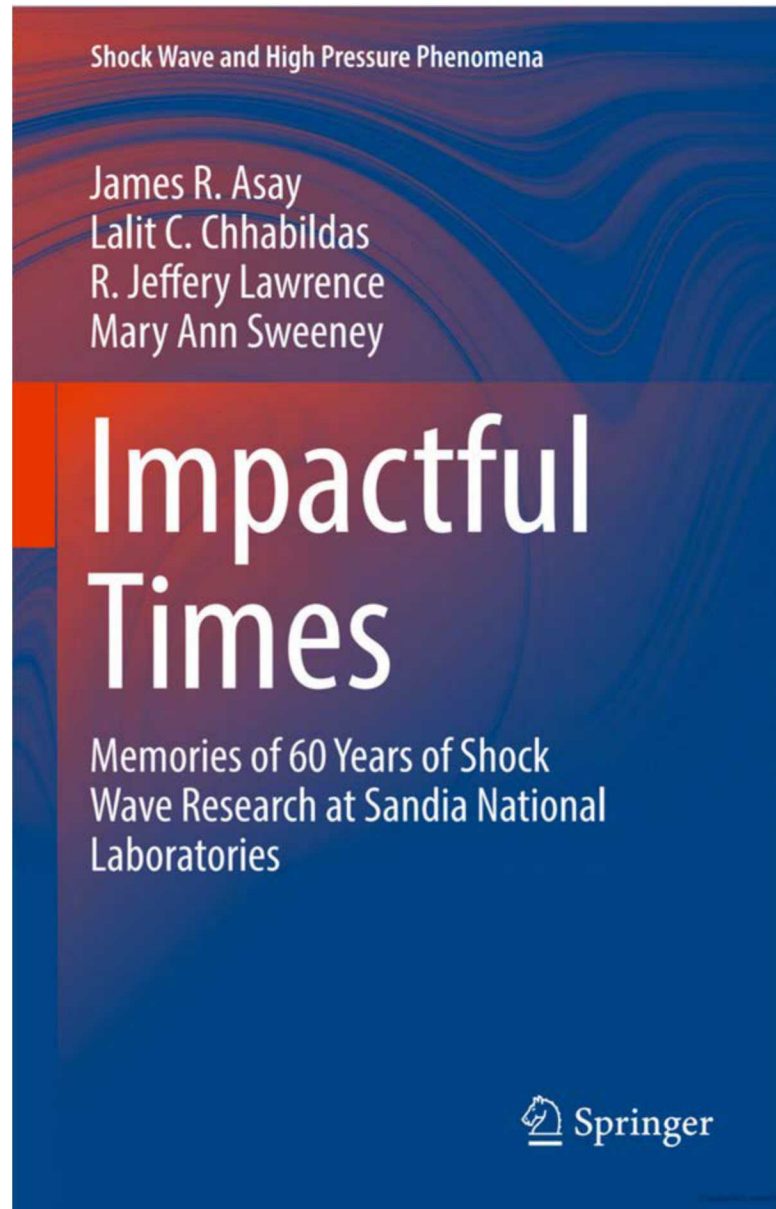




- **Brief Introduction to Shock Physics**
- **Spall**
- **Fragmentation**
- **Closure and Acknowledgements**



# Shock Physics at Sandia



Shock Wave and High Pressure Phenomena

James R. Asay  
Lalit C. Chhabildas  
R. Jeffery Lawrence  
Mary Ann Sweeney

## Impactful Times

Memories of 60 Years of Shock  
Wave Research at Sandia National  
Laboratories

 Springer

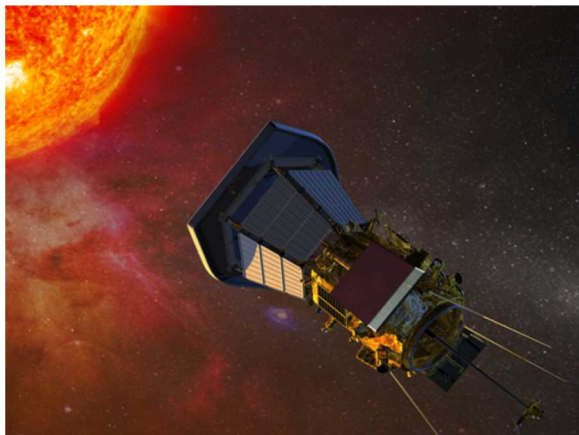
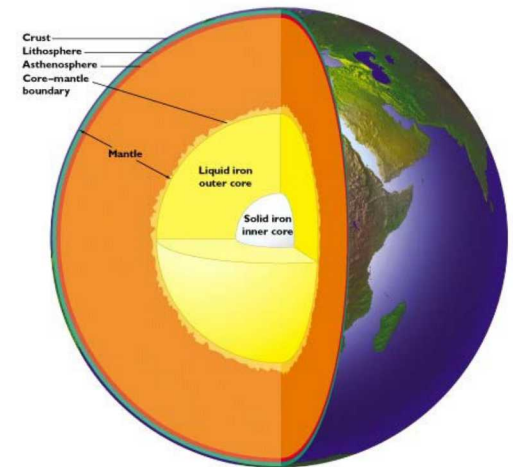
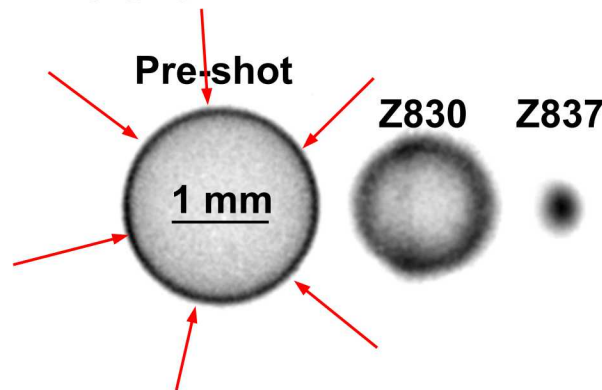
# Why Do We Need To Know the Behavior of Materials Under Extreme Conditions?



- weapons applications (warheads, armor, etc.)
- explosives behavior and applications



- inertial confinement fusion

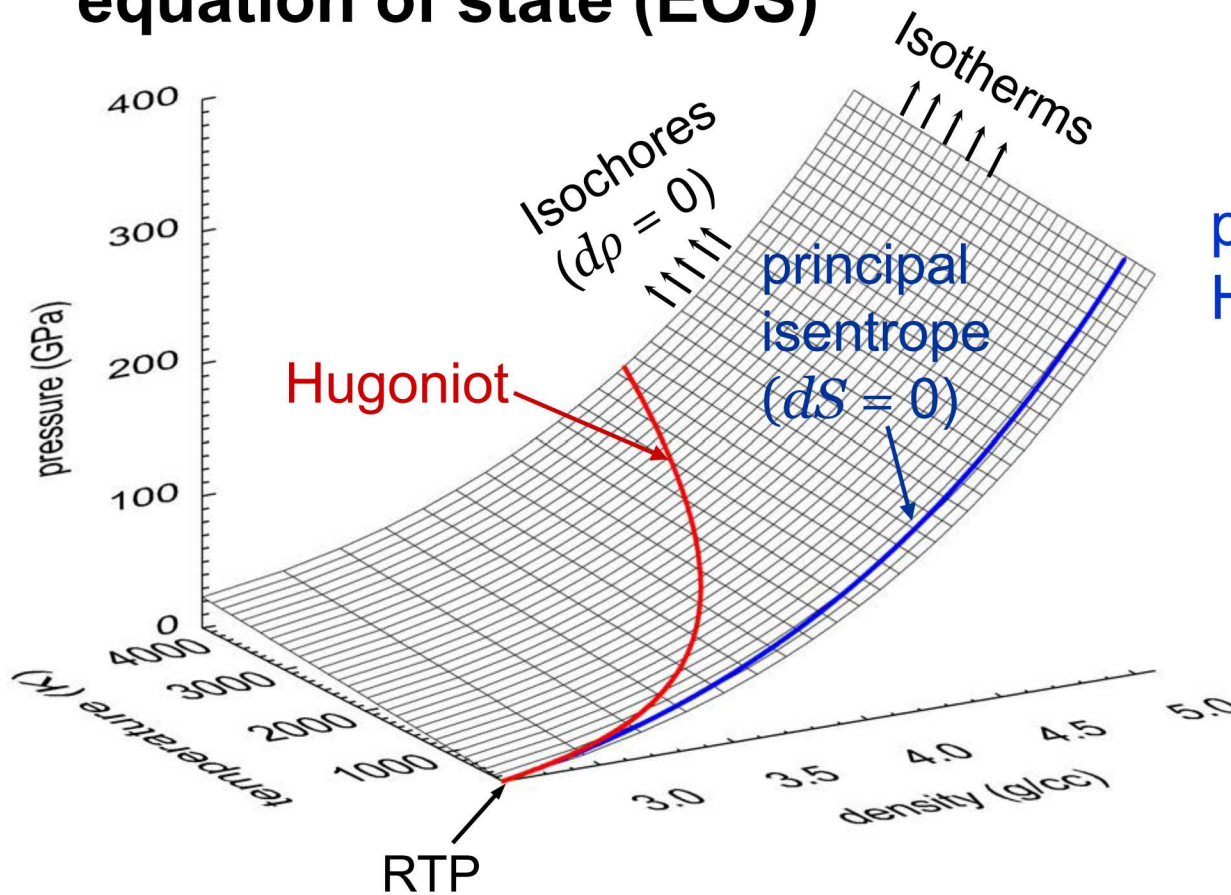


- solar probe
  - 100  $\mu\text{m}$  particles
  - up to 300 km/s velocities
  - $P_{\text{max}} \sim 100 \text{ TPa}$ ,  $T_{\text{max}} \sim 10^6 \text{ K}$

- planetary science ( $P \sim 360 \text{ GPa}$ ,  $T \sim 7000 \text{ K}$ )

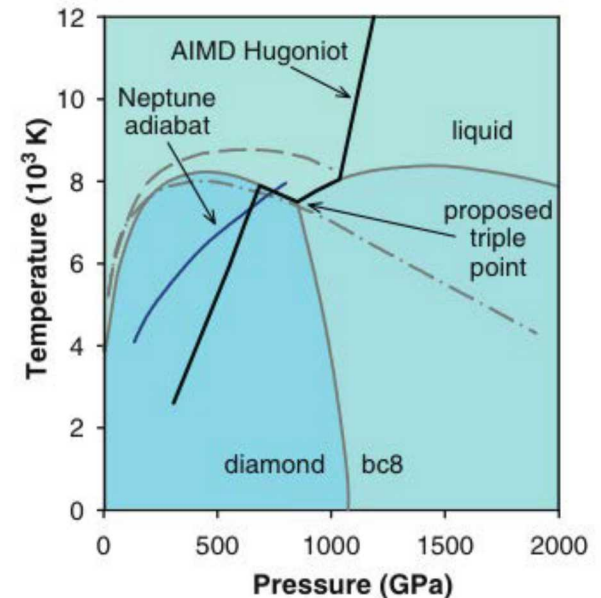
# Material Behavior: EOS & Constitutive Aspects

## equation of state (EOS)



one thermodynamic state variable as a function of two others:

pressure  $P = P(\rho, T)$   
Helmholtz energy  $f = f(v, T)$



**Also: strength, damage, spall, compaction**

Knudson, M. D., M. P. Desjarlais and D. H. Dolan (2008). "Shock-wave exploration of the high-pressure phases of carbon." *Science* **322**: 1822-1825.

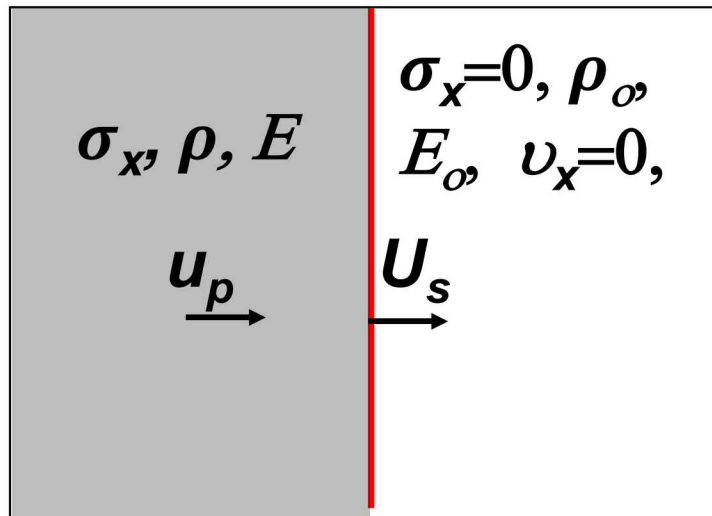


# What is a Shock Wave?

- A “discontinuous” wave that moves at a fixed velocity (if steady)
  - wave front moves at speed  $U_s$  (*shock velocity*)
  - shocked material moves at speed  $u_p$  (*particle or mass velocity*)
  - uniaxial strain condition ( $\epsilon_y = \epsilon_z = \epsilon_{xy} = \epsilon_{yz} = \epsilon_{xz} = 0$ )

**shocked material**

**unshocked material**



$x \longrightarrow$

(fixed wrt unshocked material)

- States ahead and behind shock assumed to be in thermodynamic equilibrium
  - well defined temperature in each state
  - described by equilibrium thermodynamics
- Shock compression is adiabatic
  - often very fast process ( $< 1$  ns)
  - irreversible (i.e. NOT isentropic)
  - temperature *typically* increases



# Conservation Equations and the Shock Hugoniot

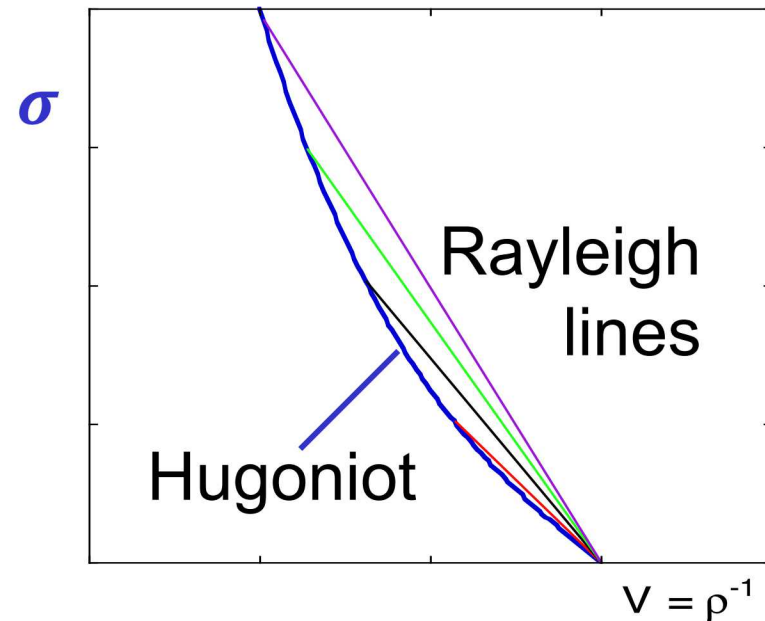
- Five variables:  $\sigma_x$ ,  $u_p$ ,  $U_s$ ,  $\rho$ , and  $E$
- Three conservation relationships (Rankine-Hugoniot jump conditions)
  - By measuring two variables (typically  $\sigma_x$ ,  $u_p$ , or  $U_s$ ), the other three can be determined

## conservation of

mass:  $\rho_0 U_s = \rho (U_s - u_p)$

momentum:  $\sigma_x = \rho_0 U_s u_p$

energy:  $E - E_0 = 0.5\sigma_x (V_0 - V)$

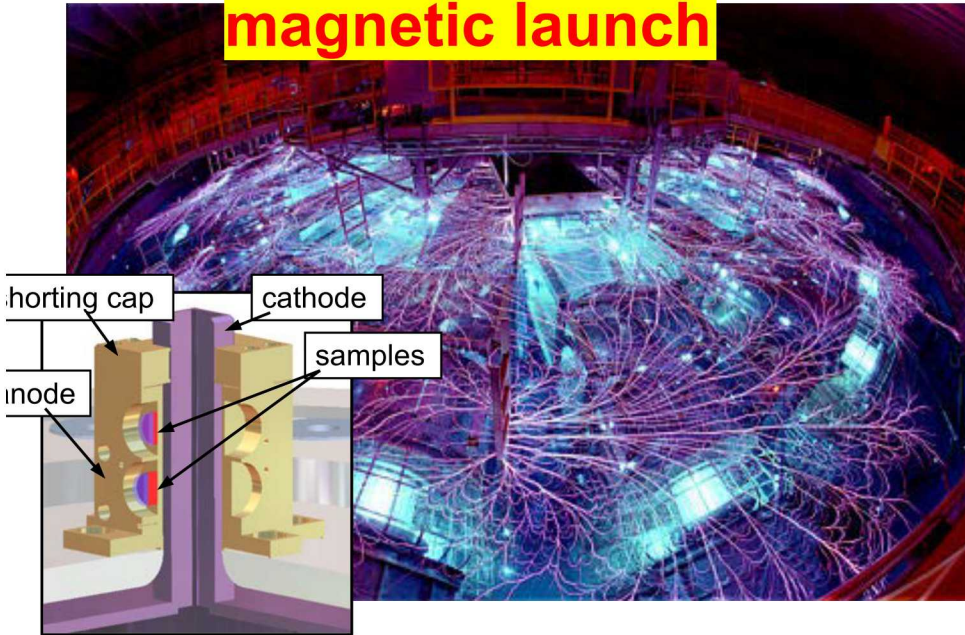


material loads along the Rayleigh line, so the Hugoniot is a collection of end states, not a material response curve  
*the Hugoniot is not a complete equation of state (EOS)!*

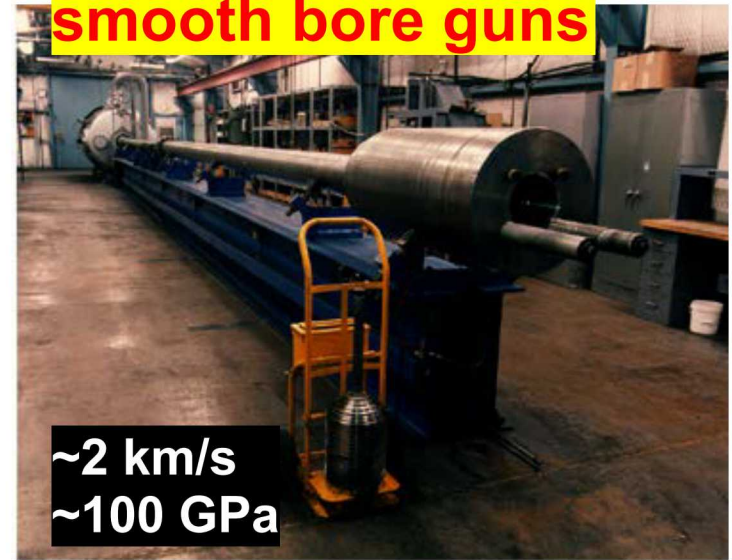


# Techniques for Shock Loading

**magnetic launch**



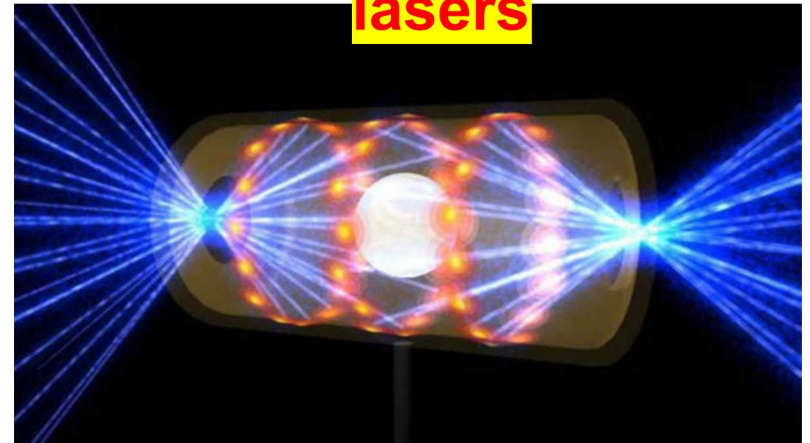
**smooth bore guns**



**explosives**



**lasers**

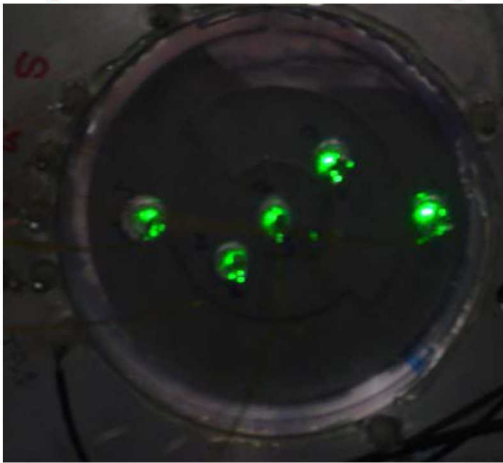




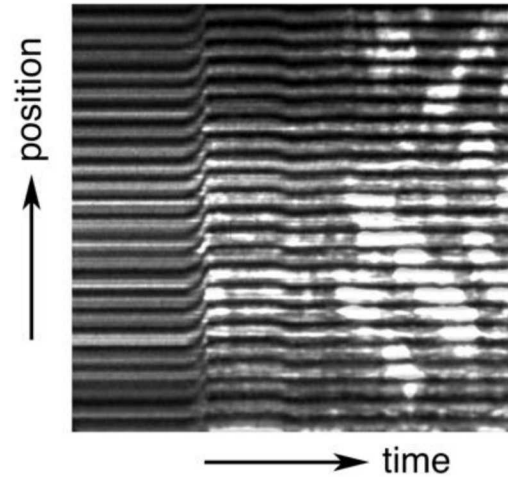
# Shock Physics Diagnostics



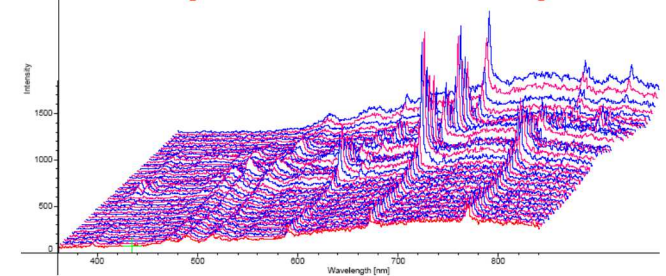
## Velocity Interferometry (VISAR & PDV)



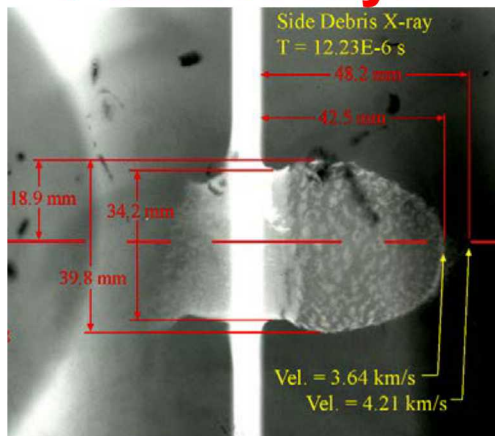
## Line-VISAR



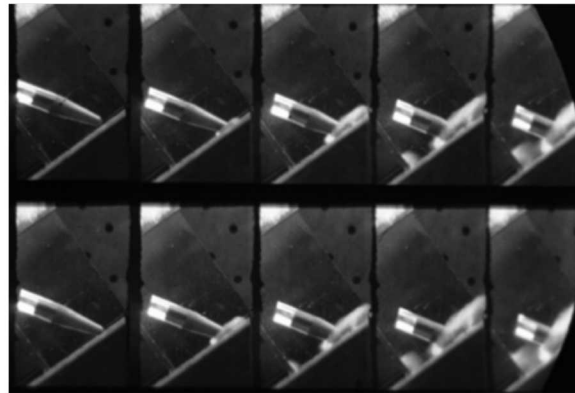
## Time-Resolved Spectroscopy (Visible & IR)



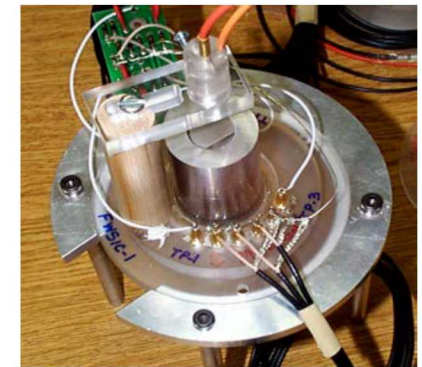
## Flash X-rays



## High-Speed Photography



## Pressure Gauges

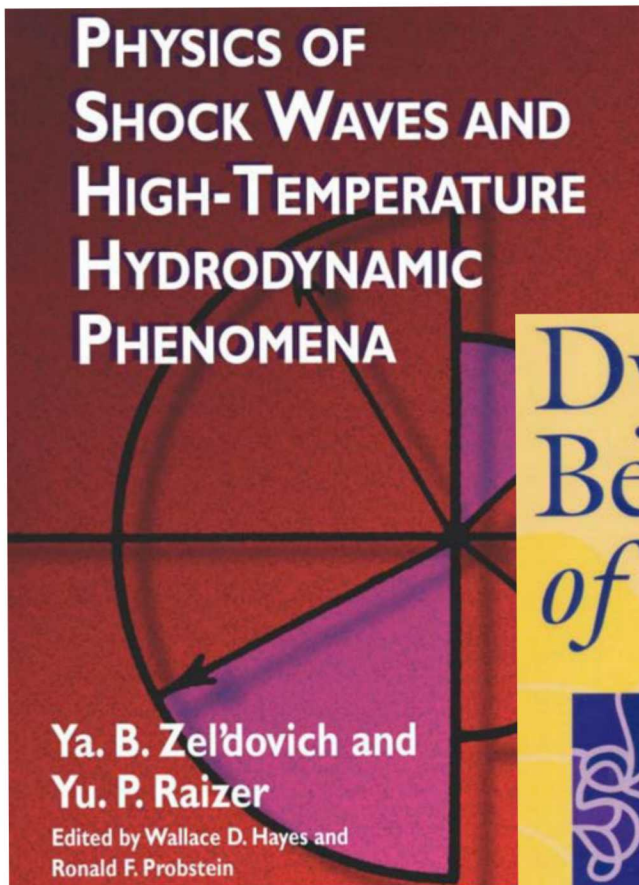


Advanced Diagnostics: pRad, synchrotron (DCS), etc.

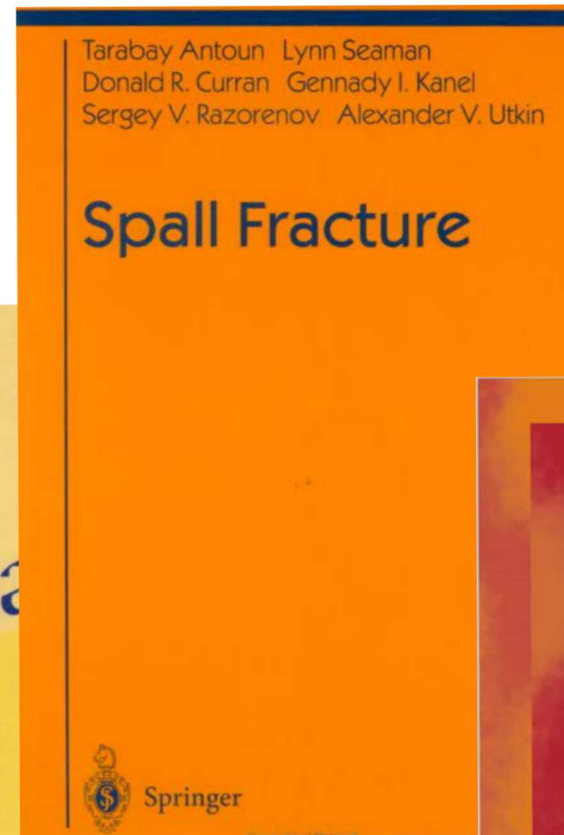


# Some References

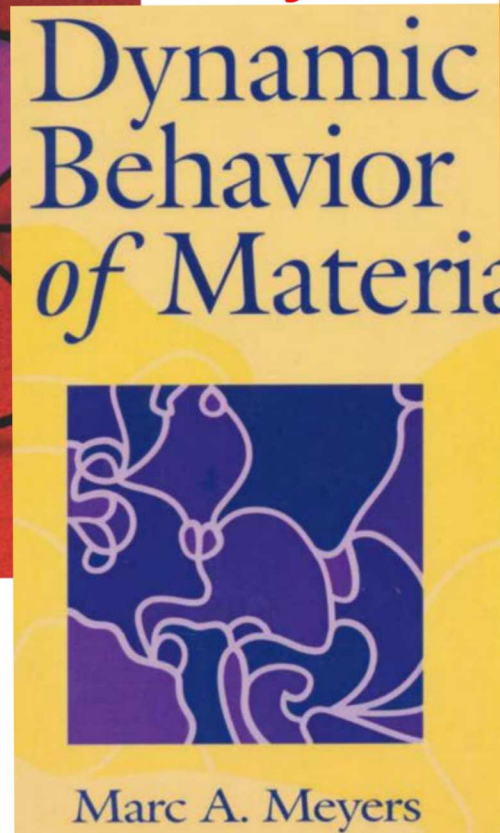
**Zel'dovich & Raizer**



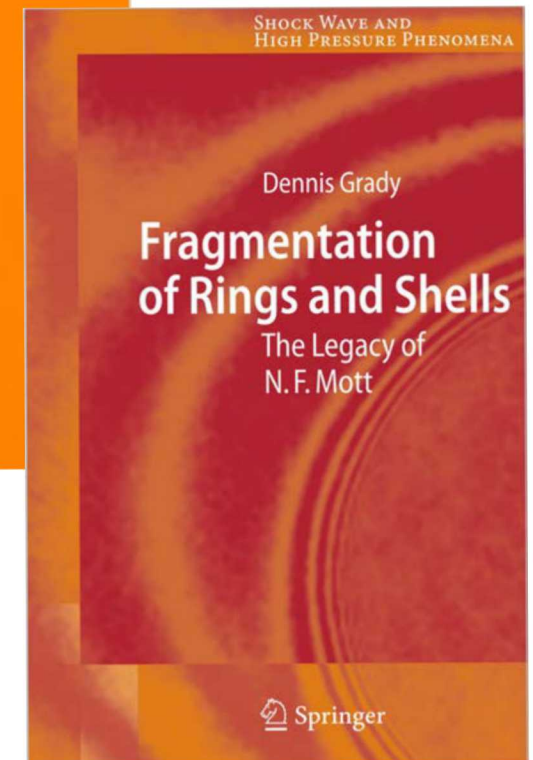
**Antoun et al.**



**Meyers**



**Grady**



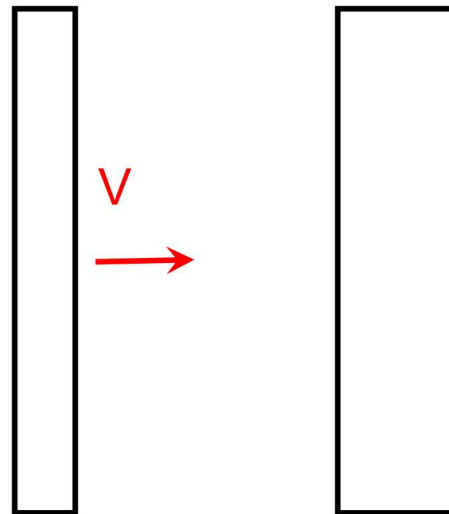


- **Brief Introduction to Shock Physics**
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# What is Spall?

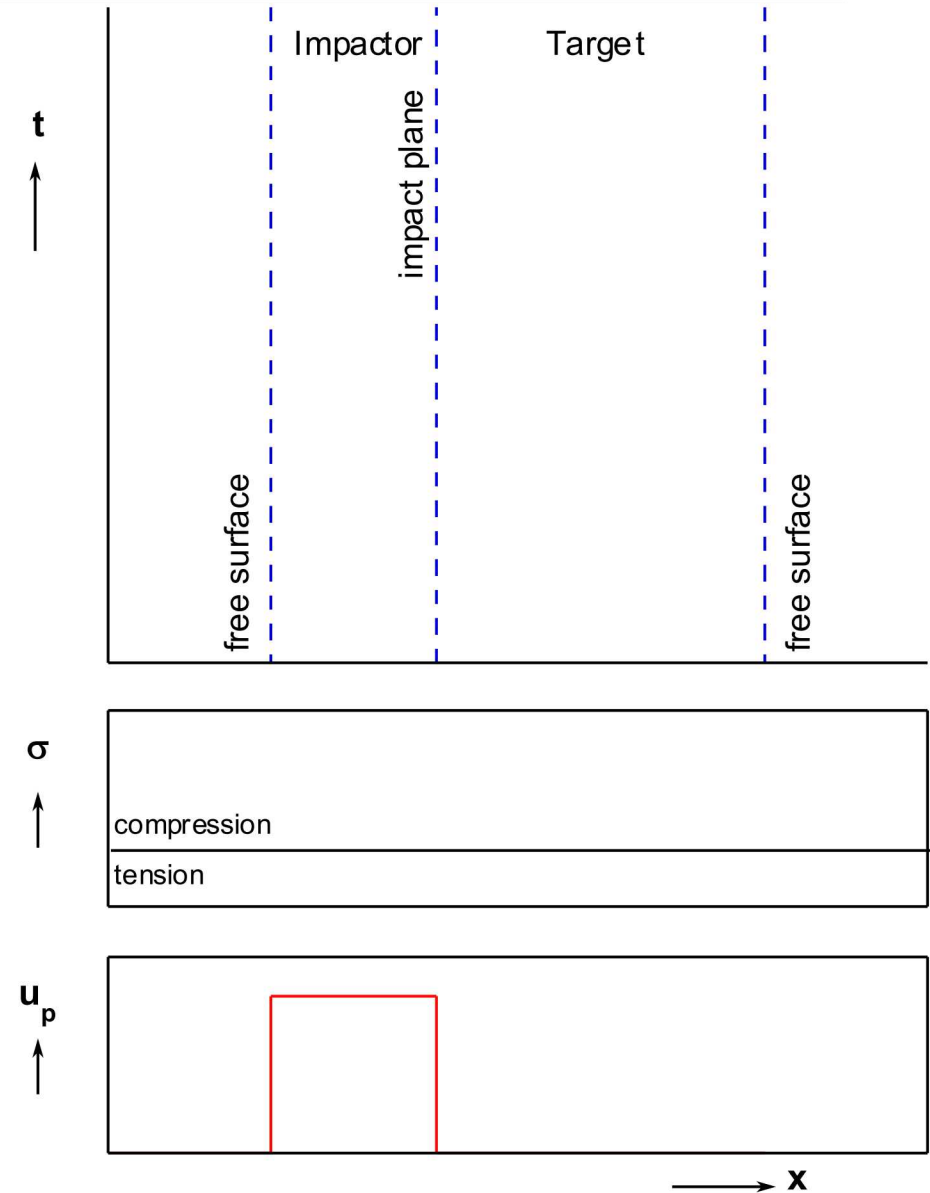
- spall is dynamic tensile failure of a material due to interactions of waves
- failure initiates at internal flaws (triple points, voids, inclusions, etc.) rather than surface flaws
- spall strengths are typically much higher than tensile strengths measured in quasi-static experiments
- spall experiments typically involve plate impact experiments with dimensions of 1:2 for impactor and target





# The Canonical Spall Experiment

- impactor hits stationary target at  $t = 0$

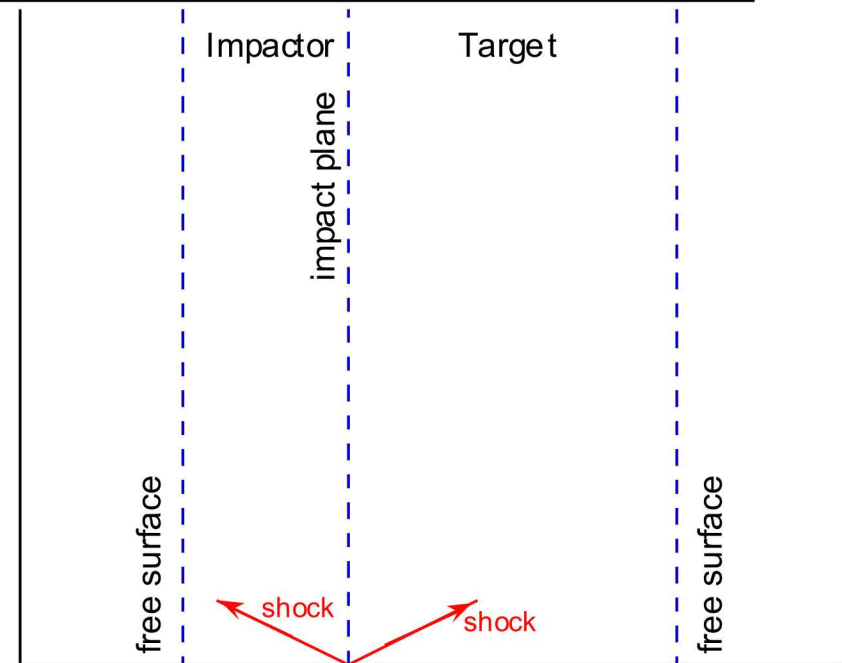




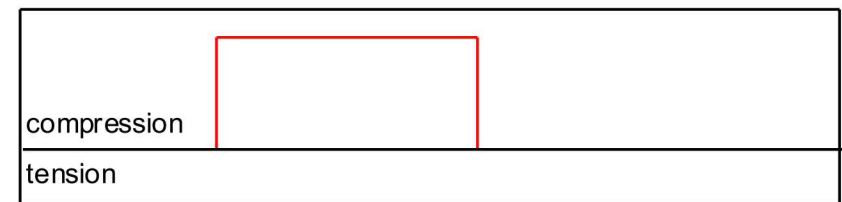
# The Canonical Spall Experiment

- impactor hits stationary target at  $t = 0$
- shocks travel into impactor and target

$t$   
↑



$\sigma$   
↑



$u_p$   
↑



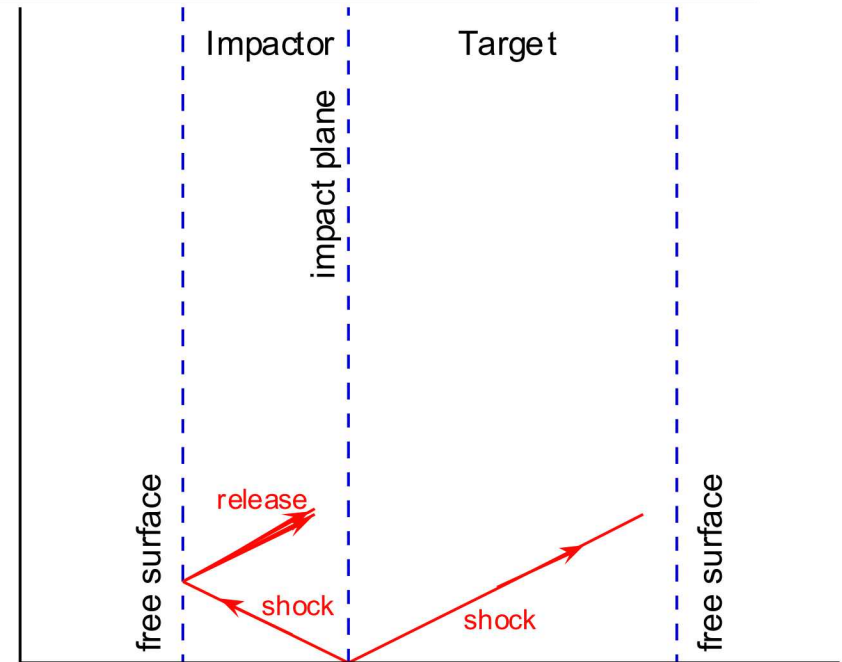
→  $x$



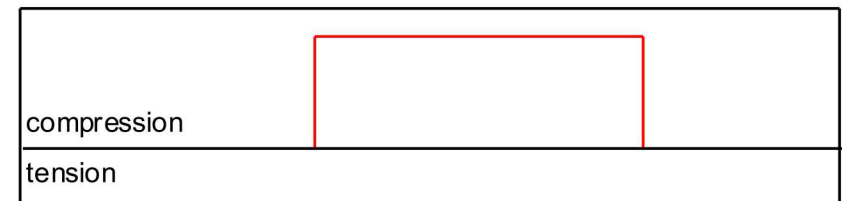
# The Canonical Spall Experiment

- impactor hits stationary target at  $t = 0$
- shocks travel into impactor and target
- shock in impactor reflects from free surface as release (unloading) wave (rarefaction fan)

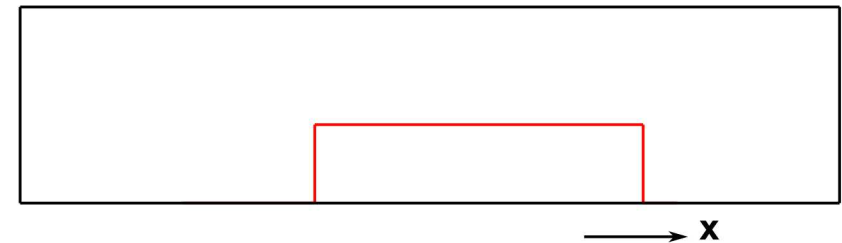
$t$   
↑



$\sigma$   
↑



$u_p$   
↑



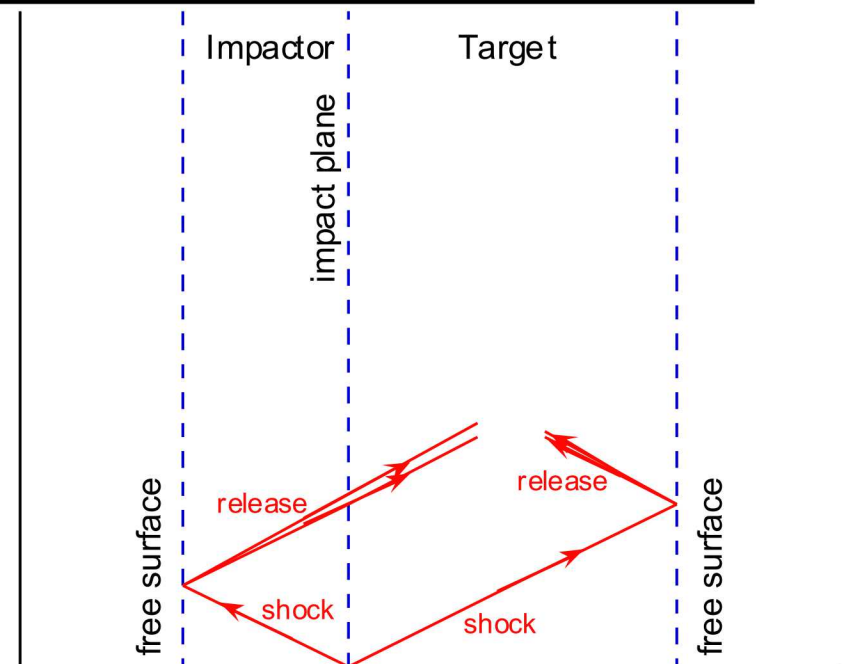
→  $x$



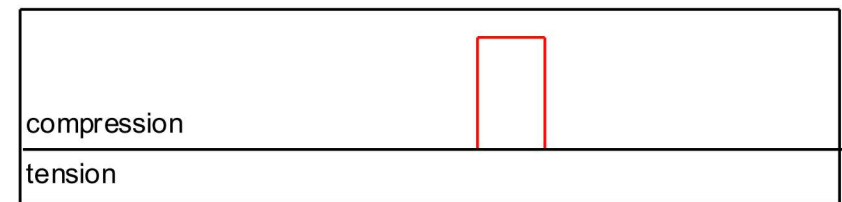
# The Canonical Spall Experiment

- impactor hits stationary target at  $t = 0$
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- shock in impactor reflects from free surface as release (unloading) wave (rarefaction fan)
- same thing happens in target

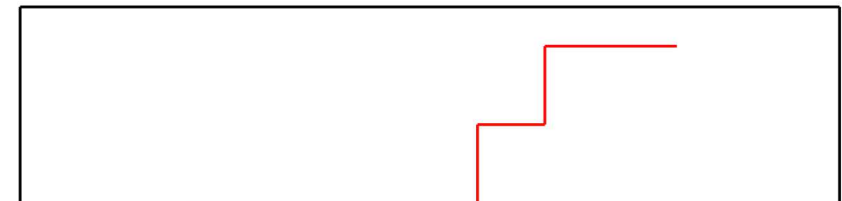
$t$   
↑



$\sigma$   
↑



$u_p$   
↑



→  $x$

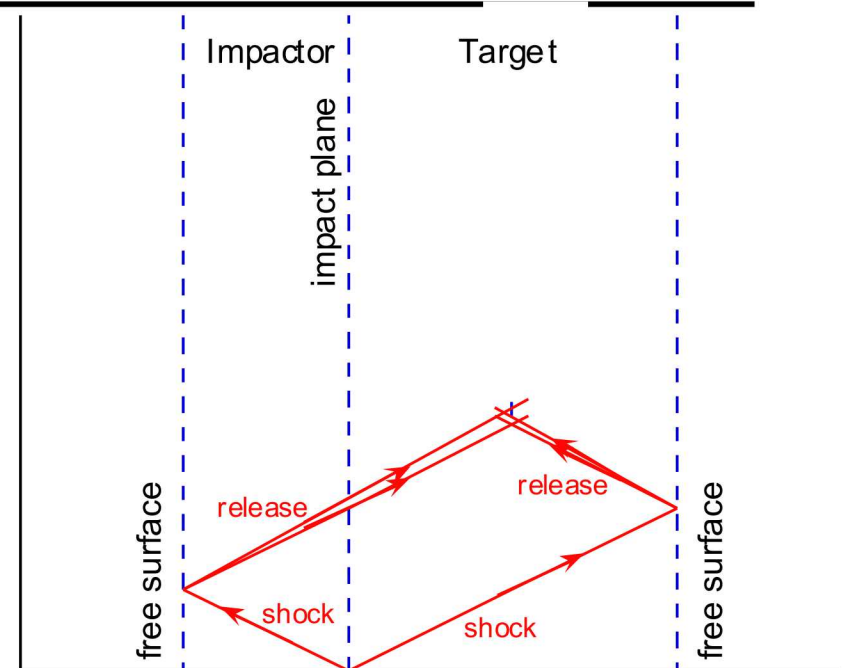


# The Canonical Spall Experiment

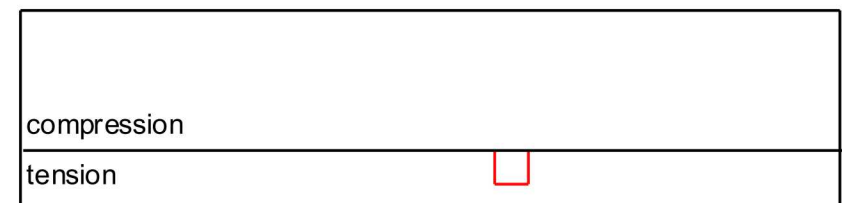


- impactor hits stationary target at  $t = 0$
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- shock in impactor reflects from free surface as release (unloading) wave (rarefaction fan)
- same thing happens in target
- release waves intersect at mid-plane and cause tensile stresses to build

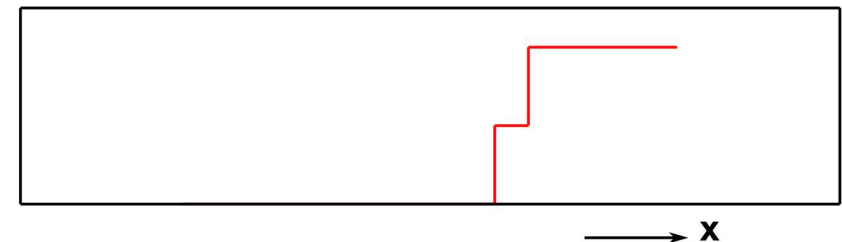
$t$   
↑



$\sigma$   
↑



$u_p$   
↑



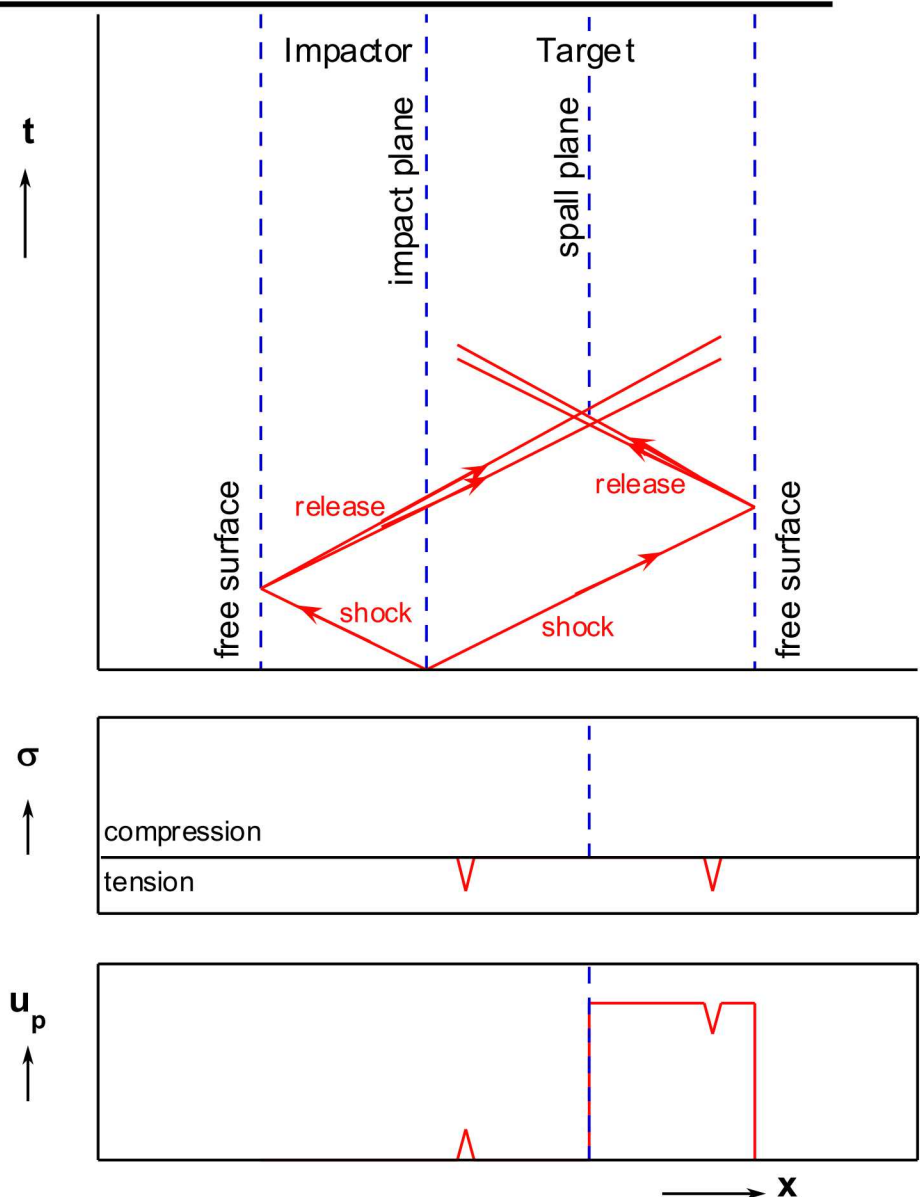
→  $x$



# The Canonical Spall Experiment



- impactor hits stationary target at  $t = 0$
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- shock in impactor reflects from free surface as release (unloading) wave (rarefaction fan)
- same thing happens in target
- release waves intersect at mid-plane and cause tensile stresses to build
- if stresses are large enough, sample fails in tension and spall plane forms

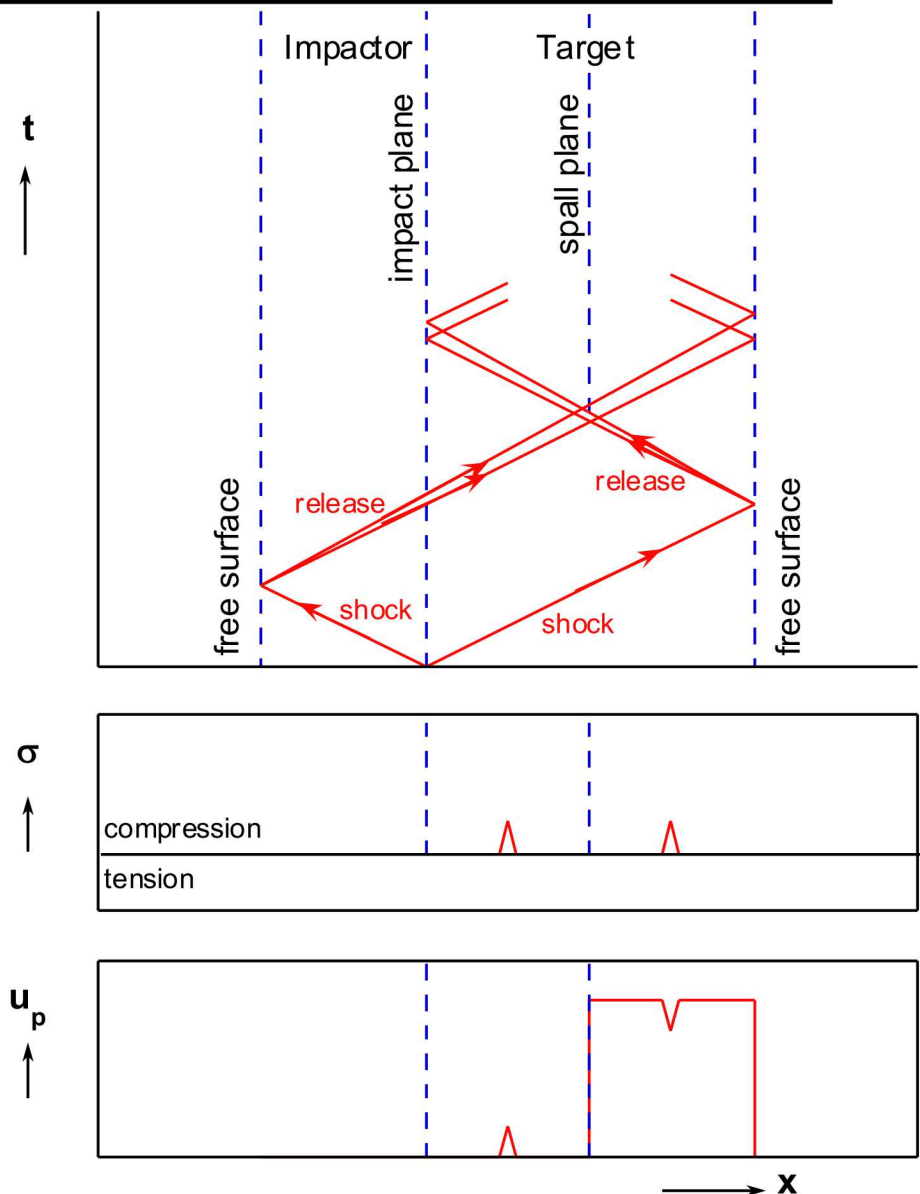




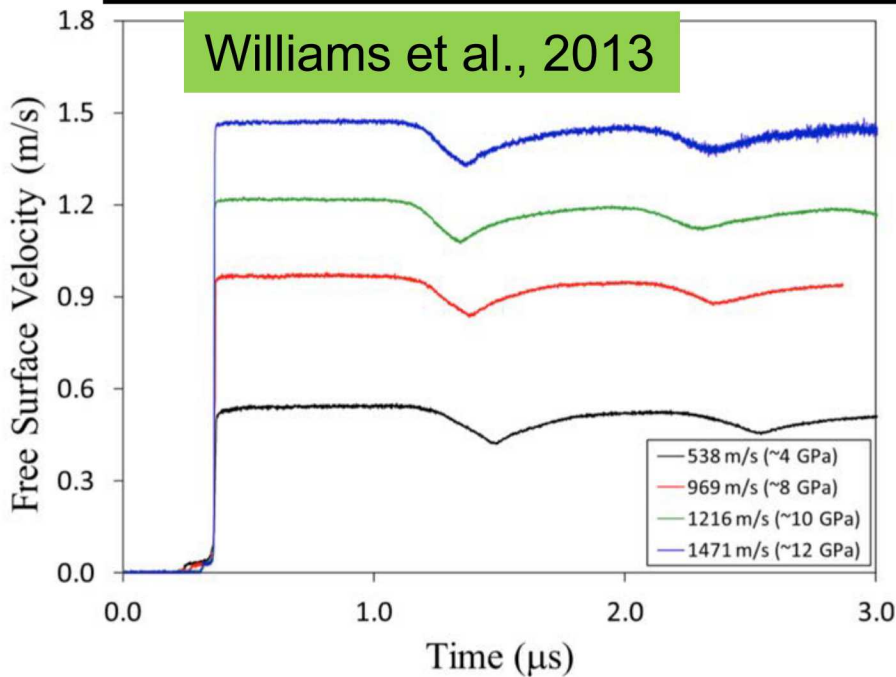
# The Canonical Spall Experiment



- impactor hits stationary target at  $t = 0$
- shocks travel into impactor and target
- shock in impactor reflects from free surface as release (unloading) wave (rarefaction fan)
- same thing happens in target
- release waves intersect at mid-plane and cause tensile stresses to build
- if stresses are large enough, sample fails in tension and spall plane forms
- sample separates at spall plane; waves continue to “ring” in spalled sample



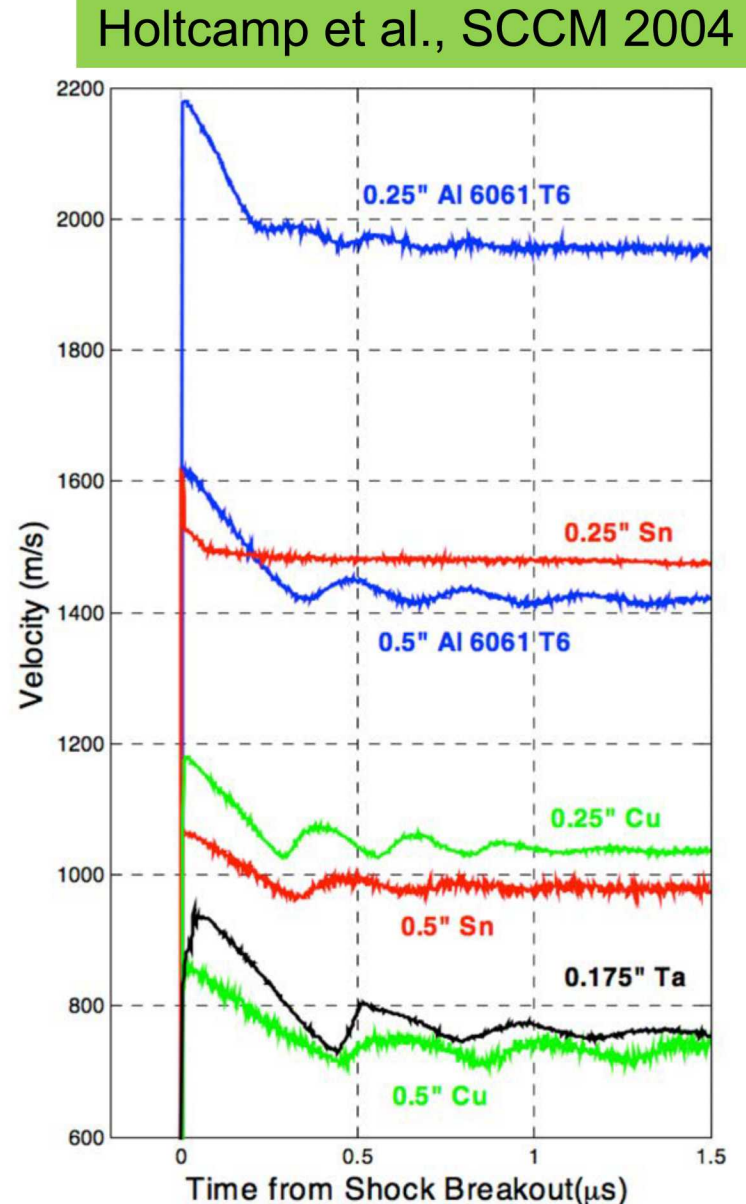
# Typical Velocity Records: Plate Impact and HE Drive



- velocity measured at free surface of target using VISAR or PDV
- acoustic approximation for spall strength:

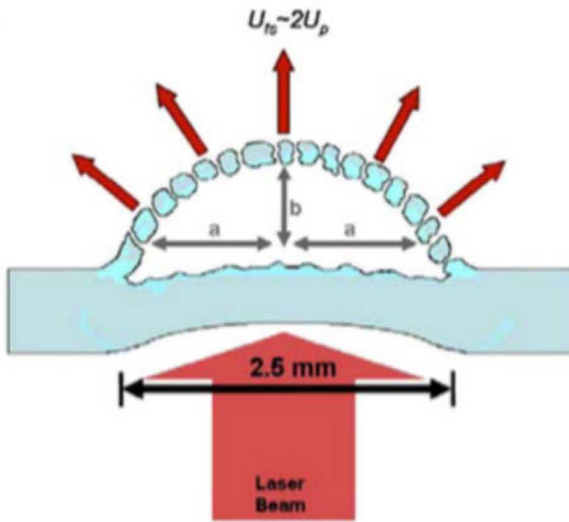
$$\sigma_{sp} = \frac{1}{2} \rho_o c_o \Delta u_{fs}$$

- complications include elastic-plastic behavior and wave interactions





# Other Configurations: HE Drive, Laser Spall, Projectile Impact



Holtcamp et al., SCCM 2004

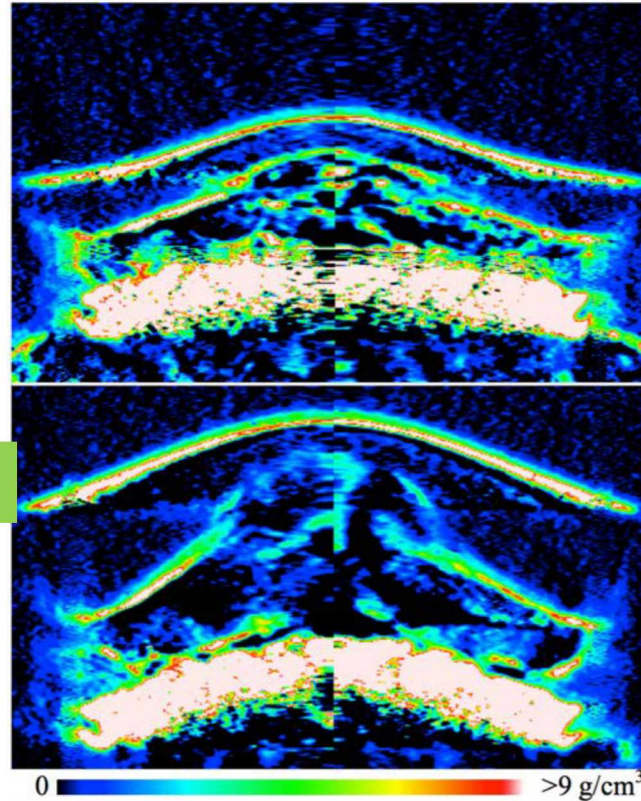
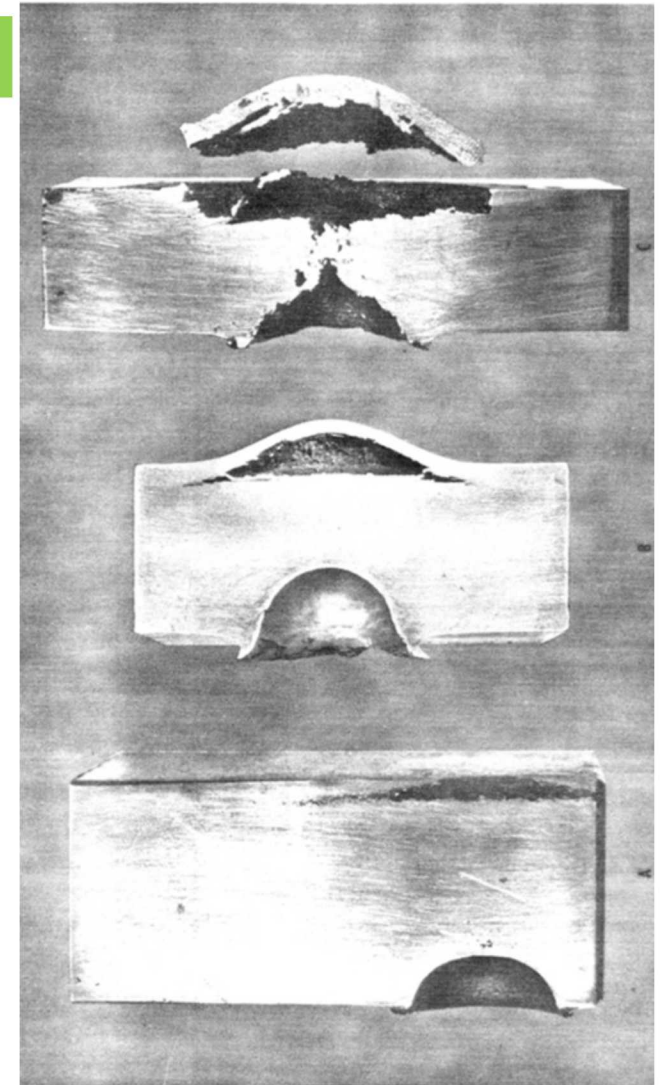


FIGURE 4. Abel inverted volume densities of 1/4" Copper at 32.3  $\mu$ s (top) and 60.9  $\mu$ s (bottom) after detonator initiation. Each image is 50 mm (Horiz) by 30 mm (Vert).

Burtsev et al., CESW 2011

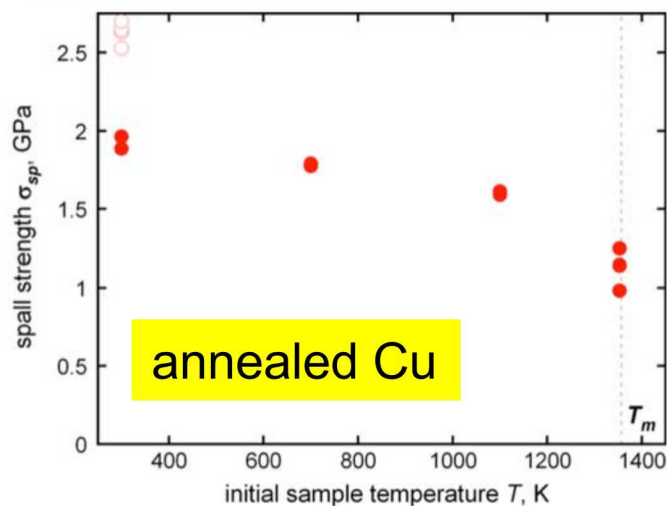




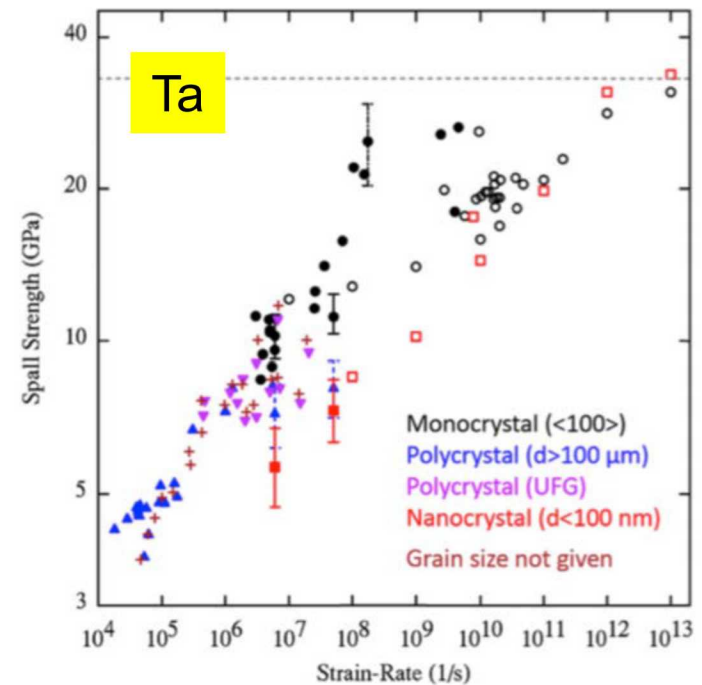
# Trends (1)

- spall strength increases with strain rate ( $\sigma_{sp} \propto \dot{\epsilon}^m$ )
- initial shock amplitude affects spall strength due to defects/damage and increased temperature; “failure front” in brittle materials
- spall strength falls off near melt

Zaretsky & Kanel, JAP 2013



Hahn et al., Acta Mat. 2017

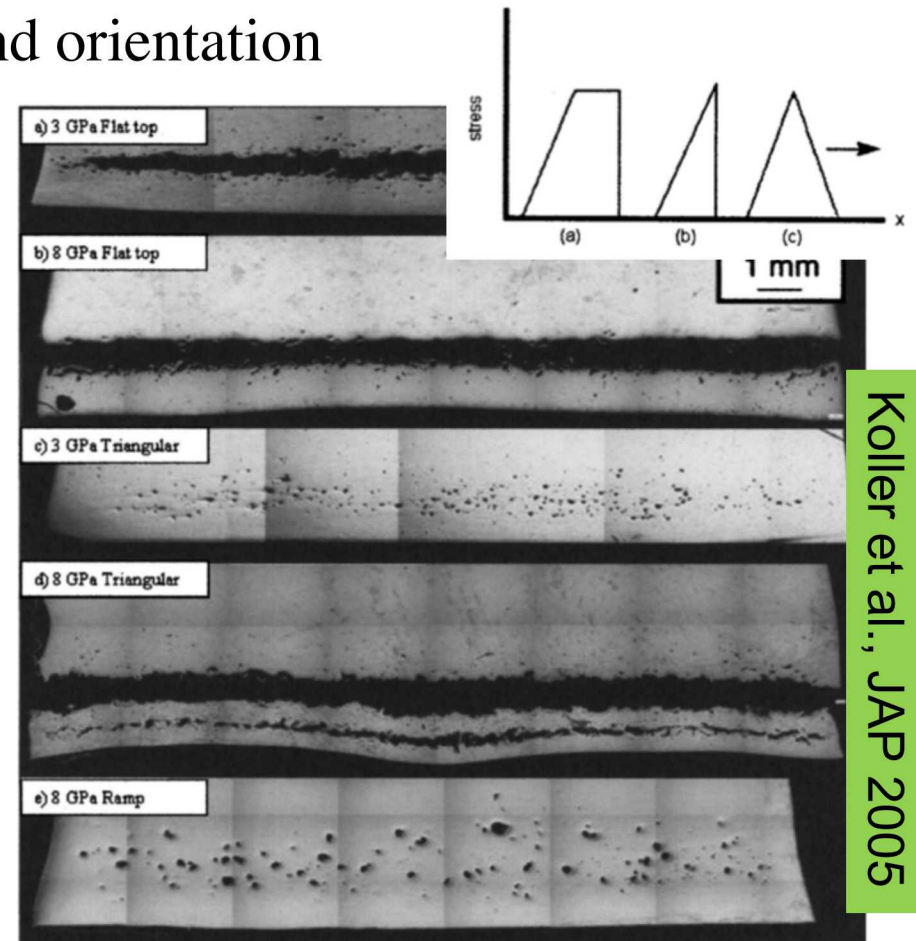
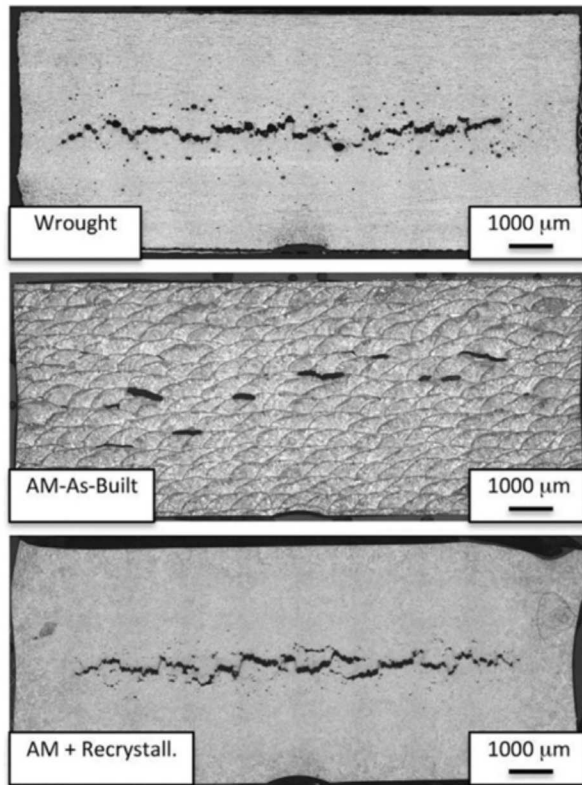




## Trends (2)

- "clean" materials have higher spall strengths; single crystals have highest
- microstructure and flaw distribution can influence spall
- wave shape (i.e. loading history) and orientation (normal vs. sweeping) affect spall

Gray et al., Acta Mat. 2017





# Typical Spall Strengths

## metals

	$\sigma_{sp}$ (GPa)
Al alloy	0.8-1.6
Cu	0.8-1.6
Mg	0.8
Ti-6-4	4.1
U	2.4
Ta	4.6
W	0.4-0.66
Iron	1.4-1.6
304 SS	2.1
4330V steel	4.8

Tarabay et al., page 142

## brittle materials

$\sigma_{sp}$ (GPa)		
BeO	0.08	Yaziv et al. 1986
B4C	0.6-0.8	
SiC	0.5-1.1	Winkler & Stilp, 1992
TiB2	0-0.5	
WC	1.0-2.0	Dandekar 2004
sapphire (elast)	2-2.5	Kanel et al. 2009
diamond	3-16	Abrosimov et al. 2015

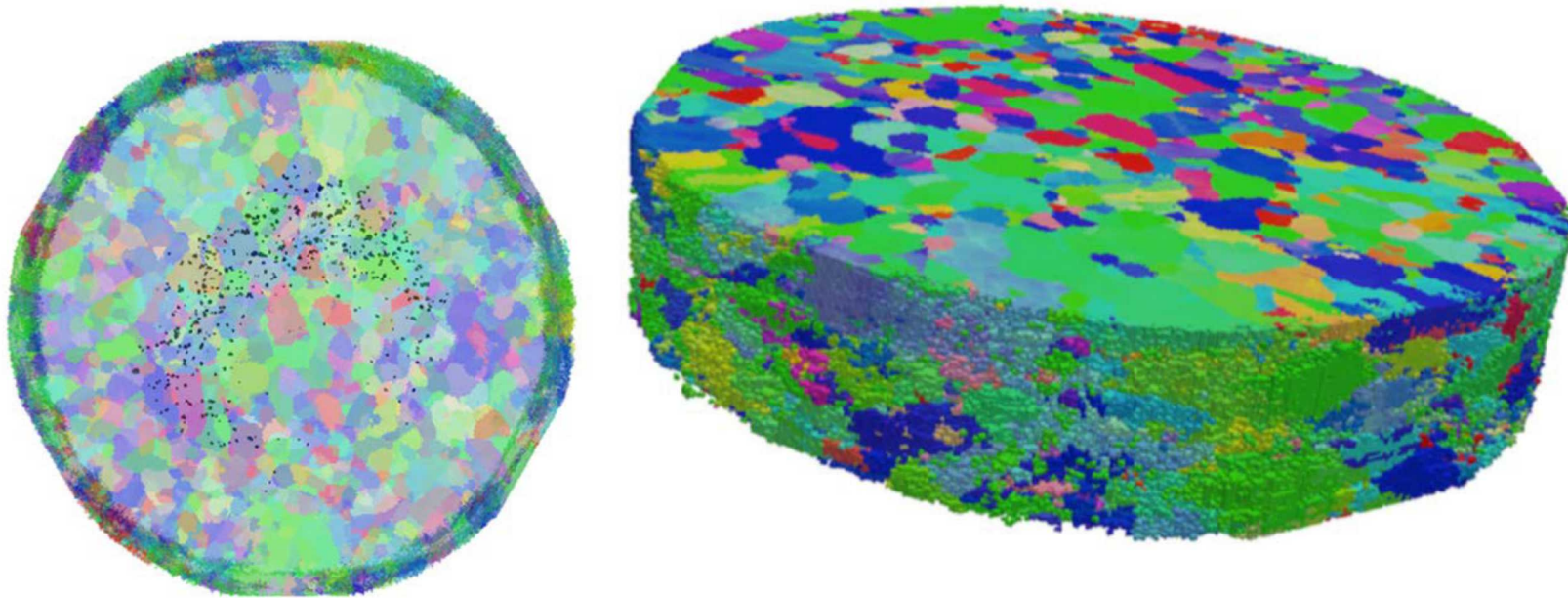
## liquids

$s_{sp}$ (MPa)		
H2O	5-40	Boetler & Suth. 2004
H2O	140-150	Stan et al., 2016
Sn (540 K)	120	Kanel et al. 2015
Pb	<30	Kanel et al. 2015
Zn (693 K)	40-50	Zaretsky 2016

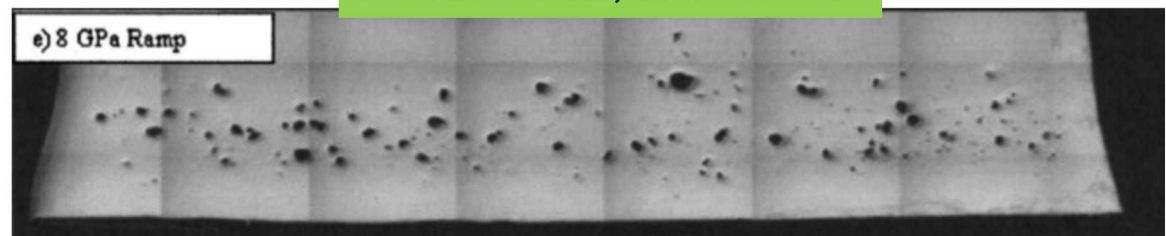


# Recovery Studies

Lieberman et al., AM 2016



Koller et al., JAP 2005

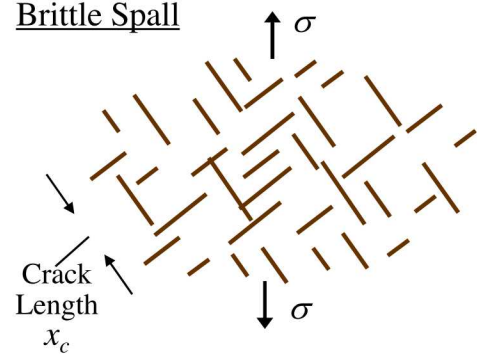


recovery is almost never as soft as you would like!

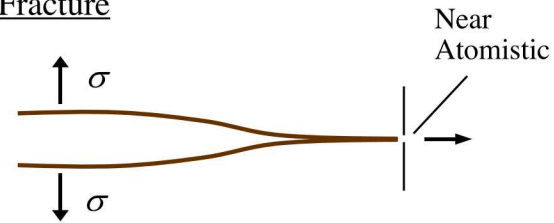


# Micromechanisms of Spall

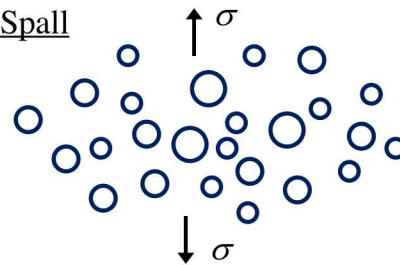
Brittle Spall



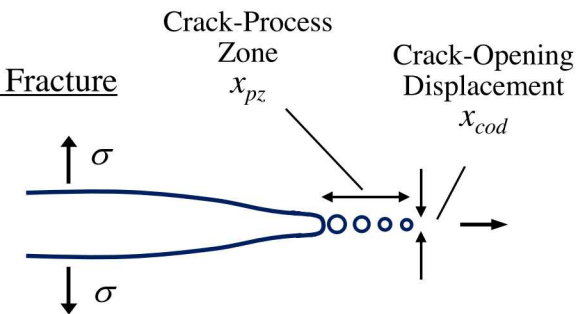
Brittle Fracture



Ductile Spall

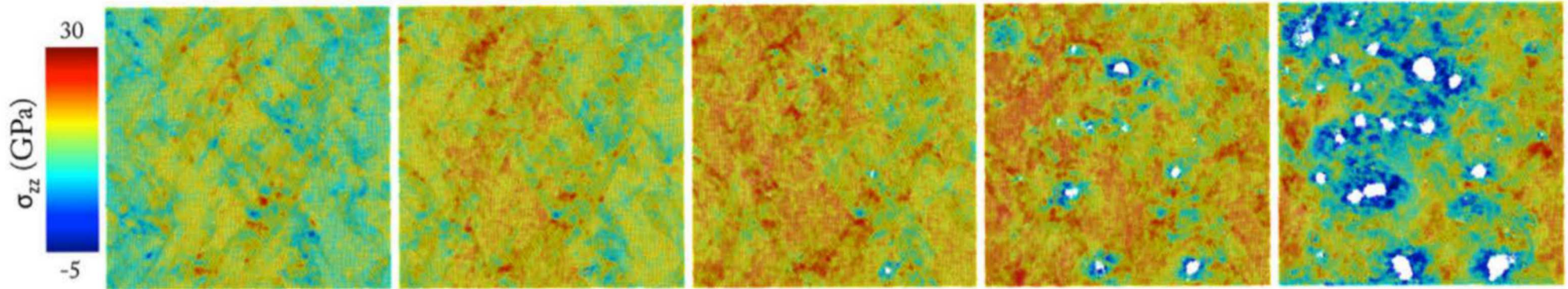


Ductile Fracture

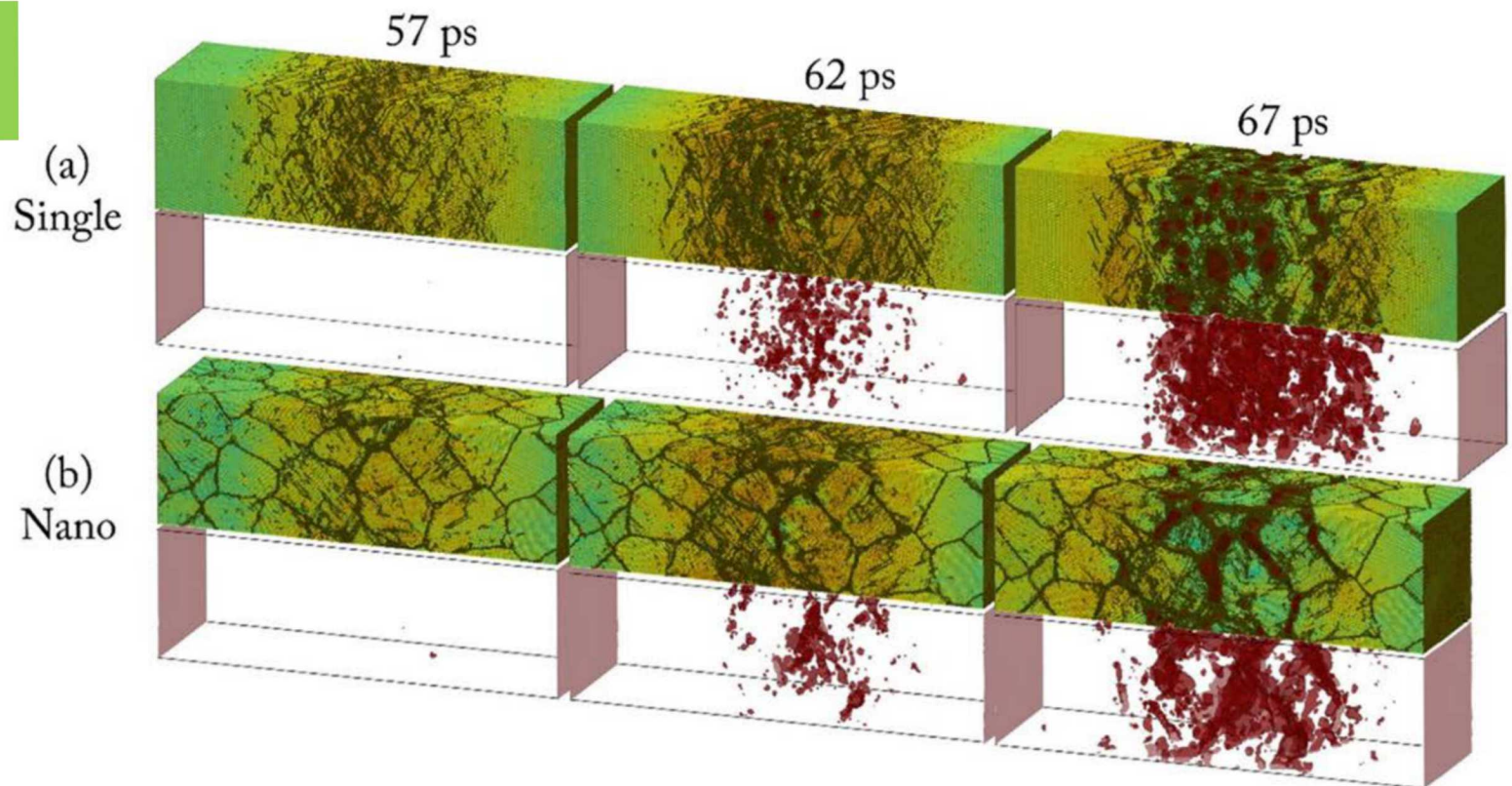




# Spall at the Atomic Level



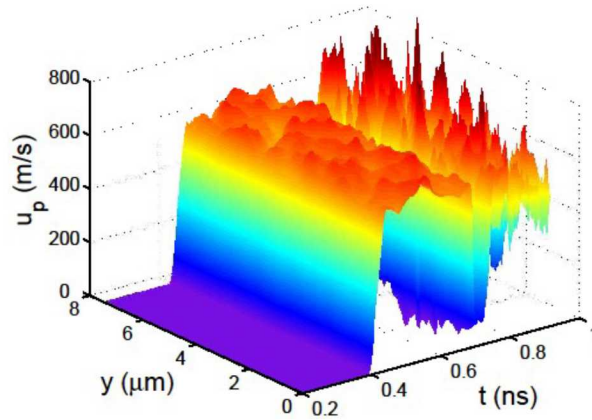
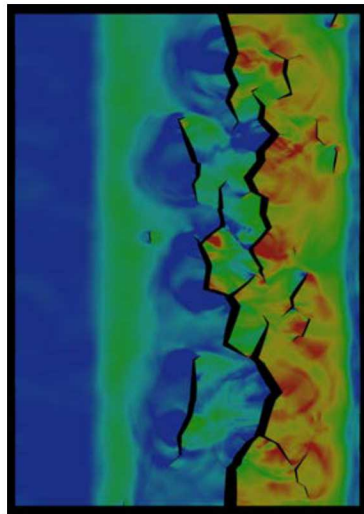
Hahn et al.,  
Acta Mat. 2017



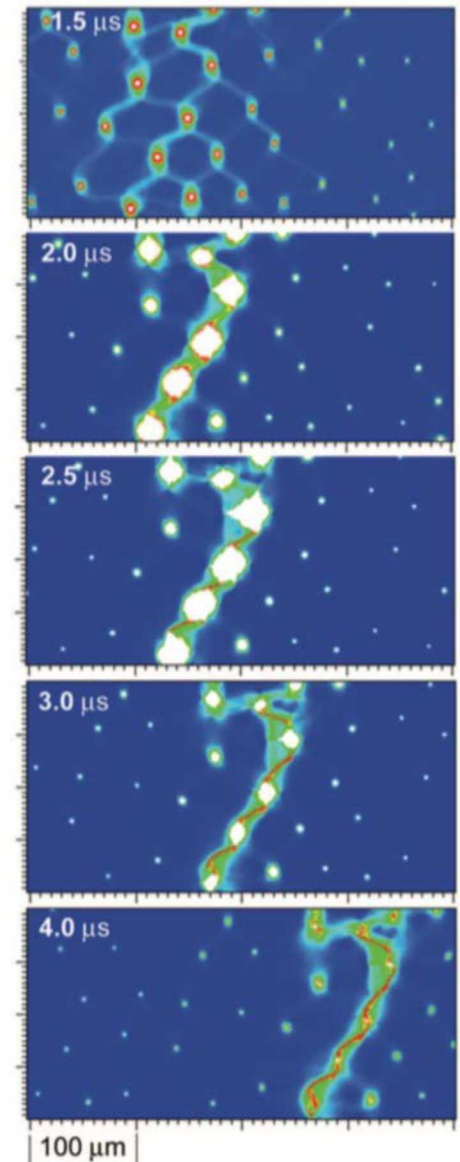


# Modeling Spall at the Grain Scale

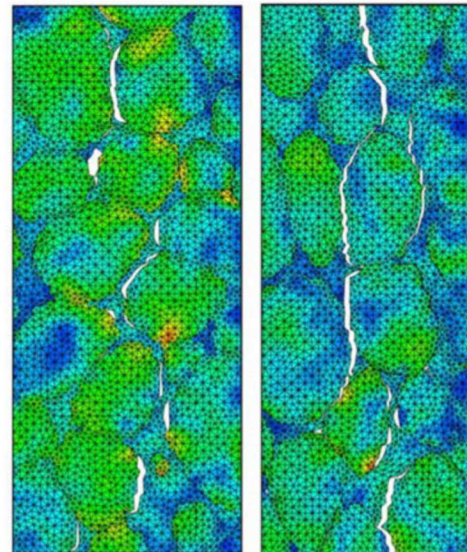
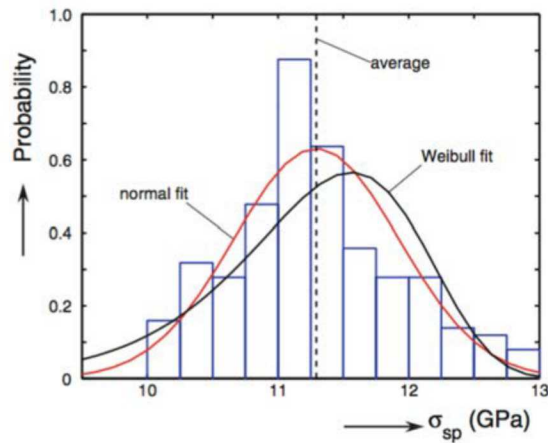
Foulk & Vogler, IJF 2010



Becker et al., JAP 2007



Vogler & Clayton, JMPS 2008





# Modeling Spall at the Continuum Level

Tuler & Butcher, IJFM 1968

$$D(x, t) = \frac{D_o}{t_o} \int_{-\infty}^t \left( \frac{\sigma(x, \tau) - \sigma_o}{\sigma_o} \right)^\lambda d\tau$$

SRI

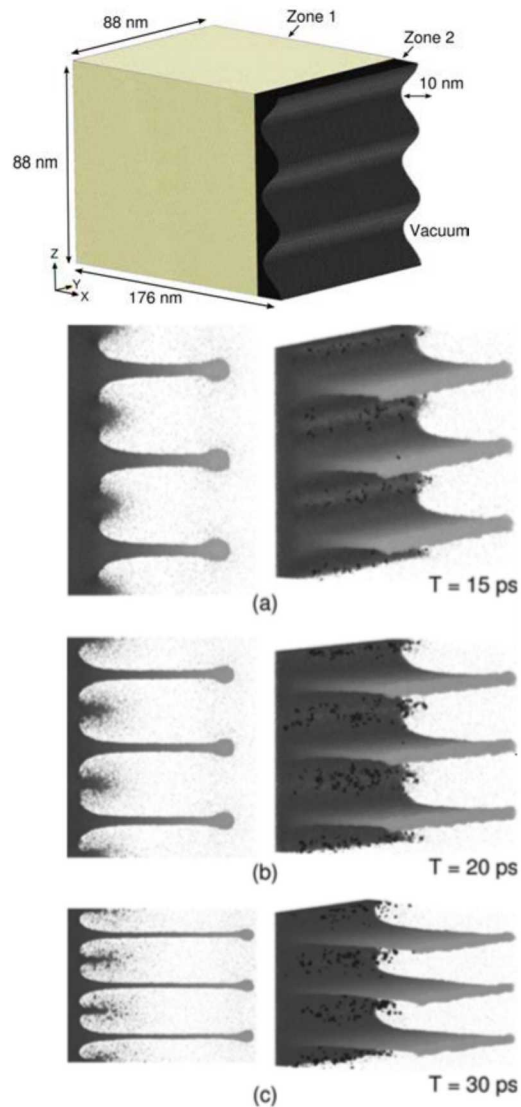
$$\dot{N} = \dot{N}_0 \exp [(\sigma - \sigma_{no})/\sigma_1]$$

$$\dot{R} = \left( \frac{\sigma - \sigma_{go}}{4\eta} \right) R$$

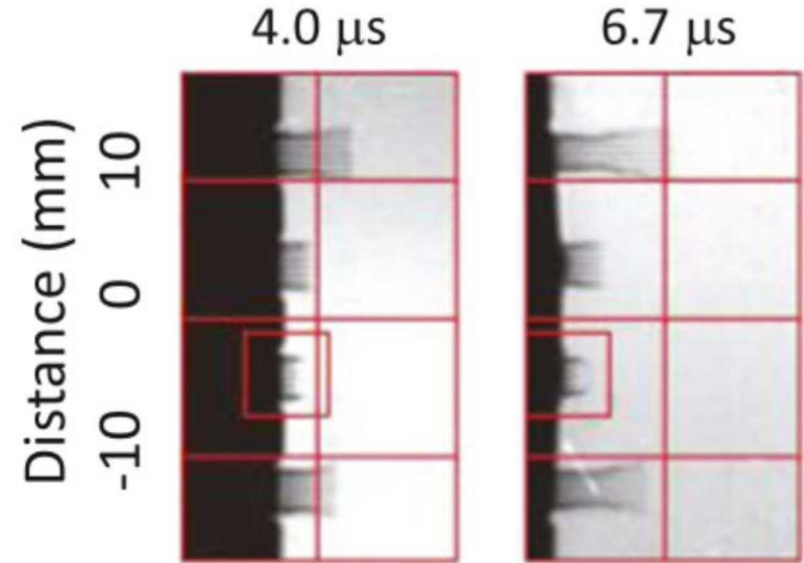


# Ejecta at Surfaces

Durand & Soulard, JAP 2012



Morris et al., EM 2016





- **Brief Introduction to Shock Physics**
- **Spall**
- **Fragmentation**
- **Closure and Acknowledgements**



# Fragmentation

- 
- **breakage of a body into many pieces (J. Bishop - "pervasive fracture") under dynamic loading**
  - **quantities of interest are typically:**
    - **fragment size/mass distribution**
    - **velocity**
  - **relevant from very small (atomic nuclei) to very large (the universe) length scales**
  - **often, modeling of fragmentation involves the search for scaling laws to capture sub-grid physics**
  - **different physics (e.g. brittle fracture, surface-tension dominated breakup) leads to different scaling laws**



# Fragmentation - Motivation



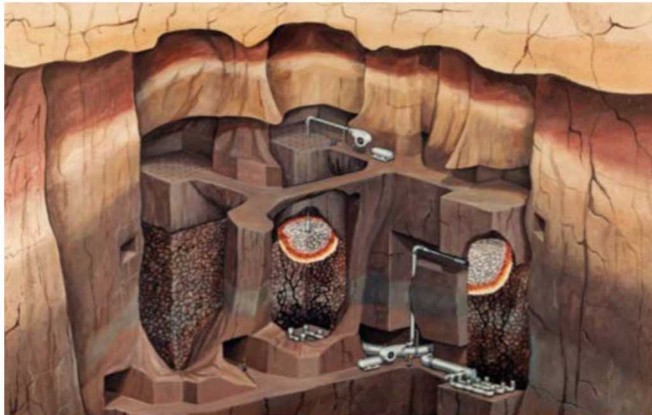
## WEAPONS

- Conventional munitions
- Range safety



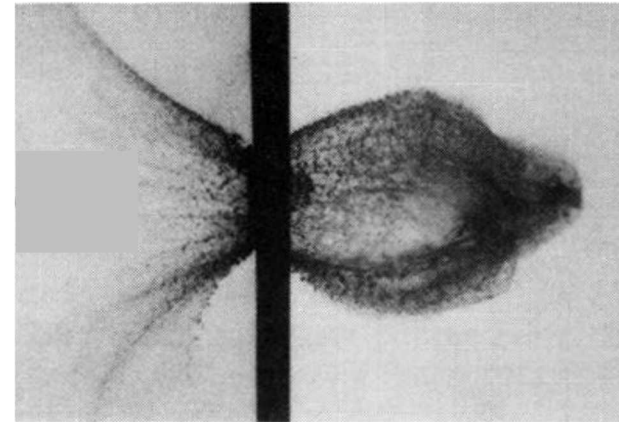
## SAFEGUARDS

- Accidents
- Reactor Safety



## ENERGY

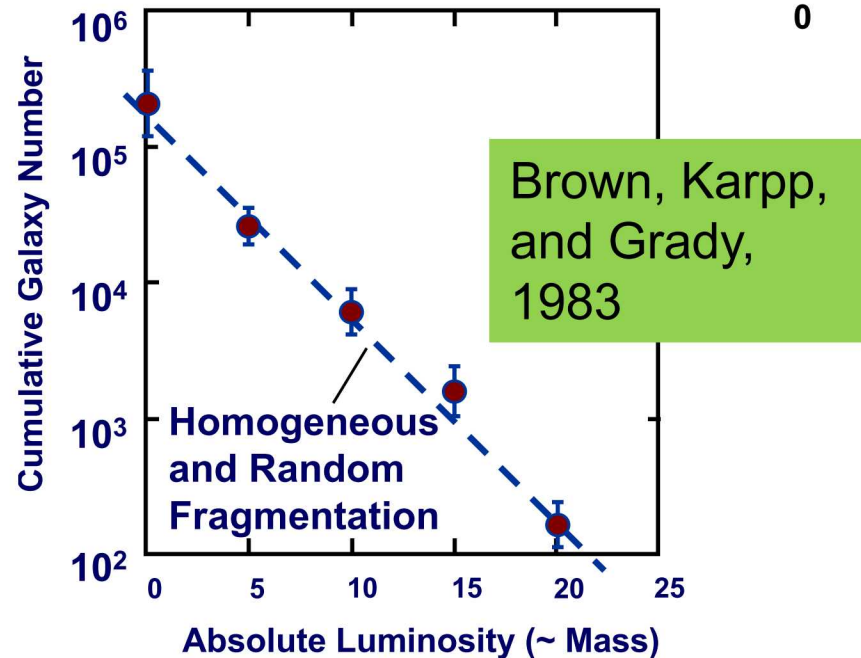
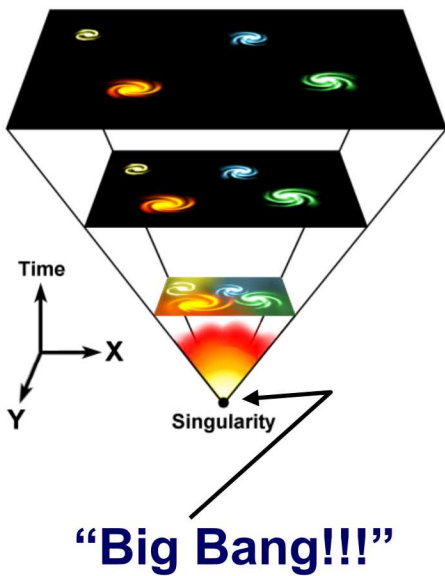
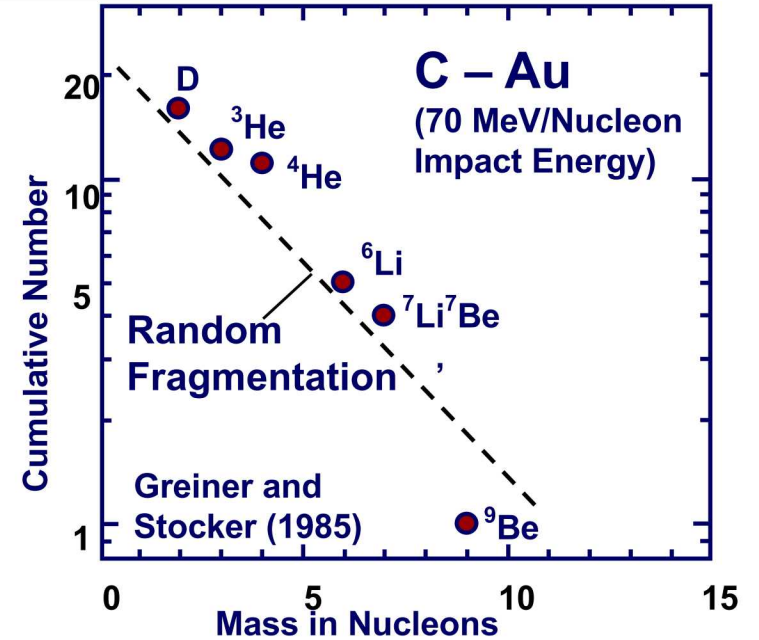
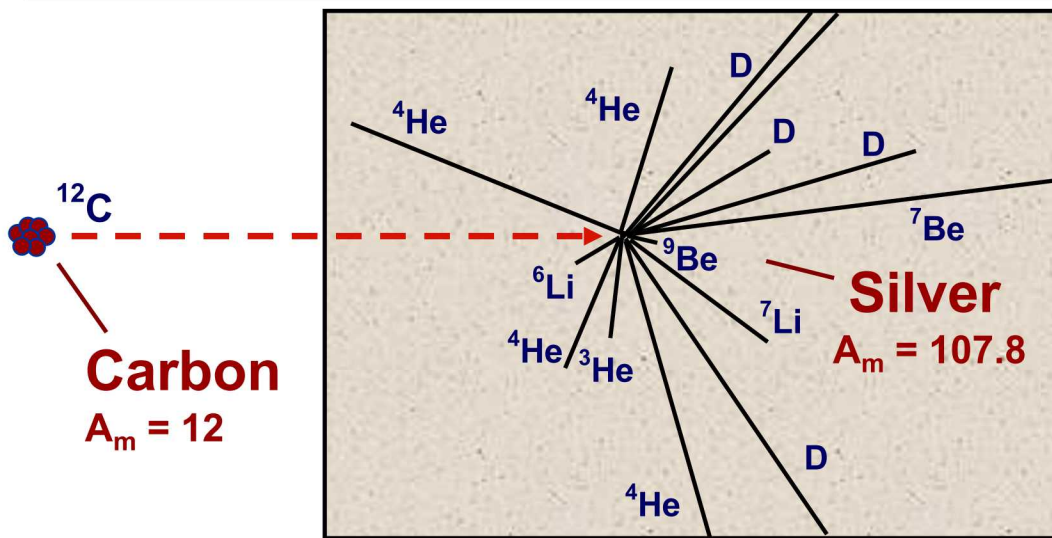
- In Situ Oil Shale Recovery
- Enhance Oil and Gas Extraction



## SHIELDING

- Orbital debris
- Behind armor debris

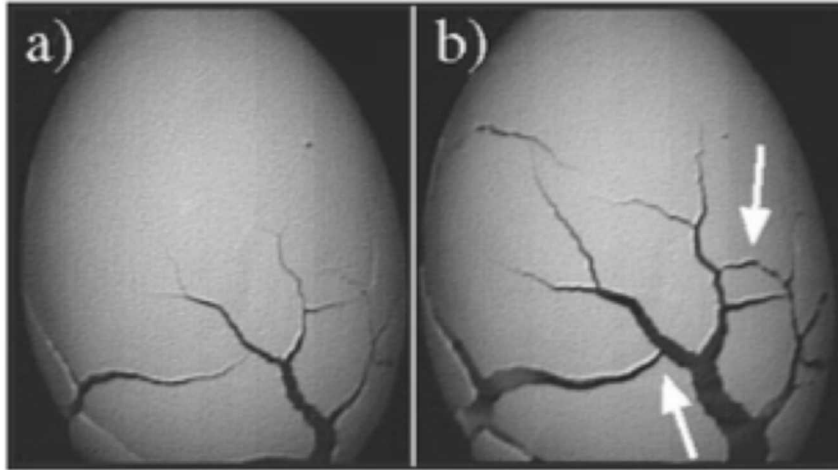
# Fragmentation: Examples



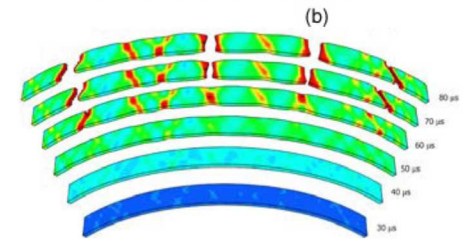
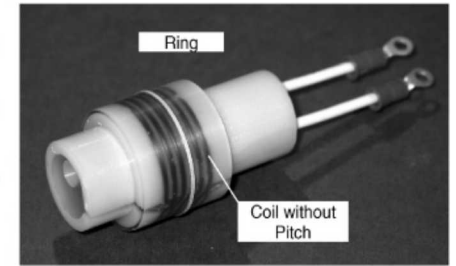
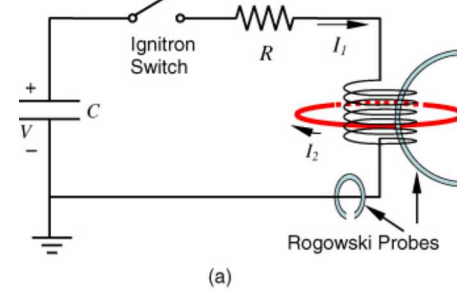


# Fragmentation Experiments

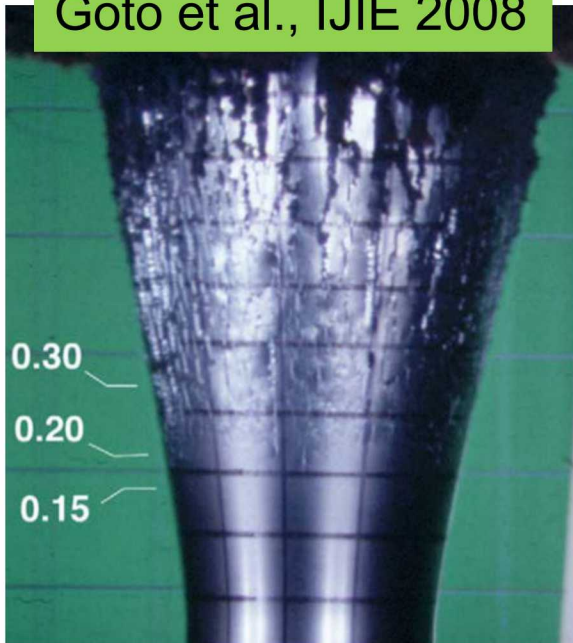
Kun et al., PRL 2004



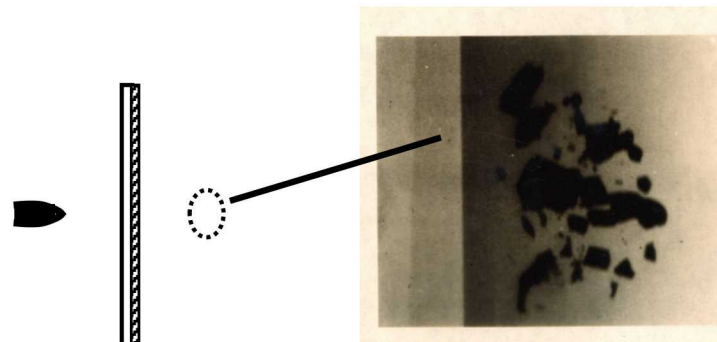
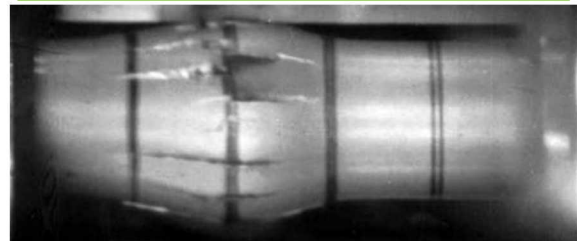
Zhang & Ravi-Chandar, JPD 2009



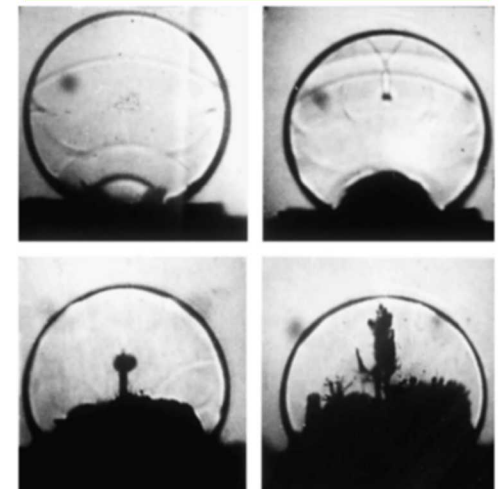
Goto et al., IJIE 2008



Vogler et al., IJIE 2003



Schonert, PT 2004





# Sir Nevill Mott

**Professor of Theoretical Physics at Bristol College(1939)**



**Scientific Advisor to Commanding General  
of Anti-Aircraft Command (40-42)**



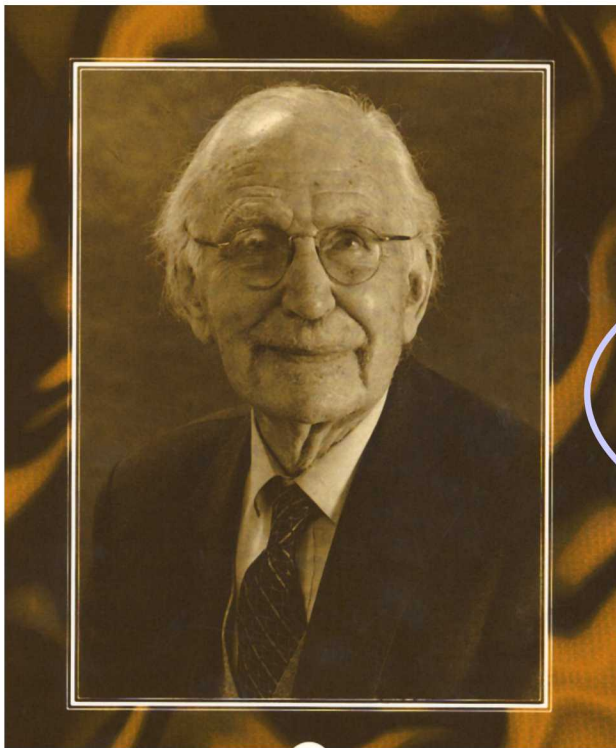
**Head of Mathematical Research on  
Armament at Woolwich Arsenal,  
Fort Halstead (42-45) w/ G. I. Taylor. R. Hill,  
E. H. Lee, H. Bishop, and others ...**



**Nobel Laureate in Physics**



**Knight of the British Realm**





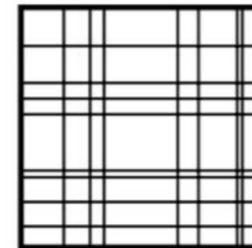
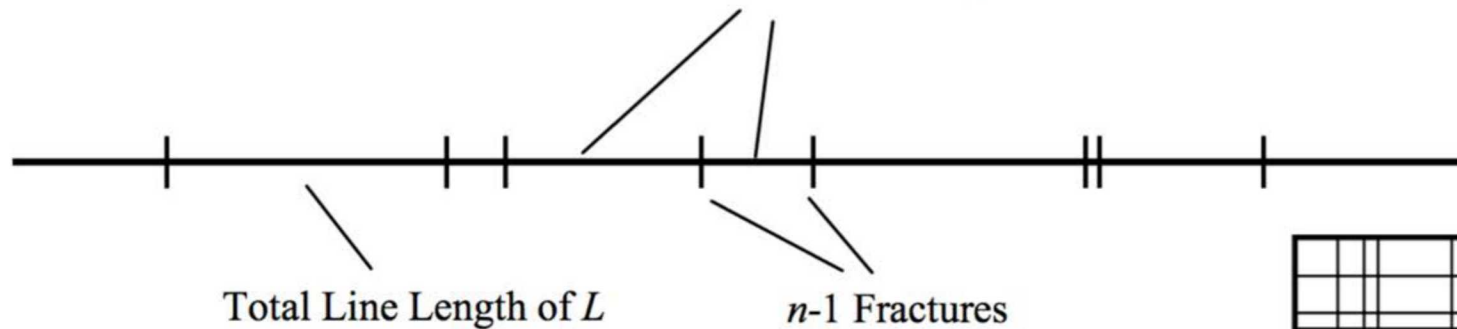
# Geometric Arguments

cumulative distribution:

$$F(l) = 1 - e^{-l/\lambda}$$

$n$  Fragments of Variable length  $l$

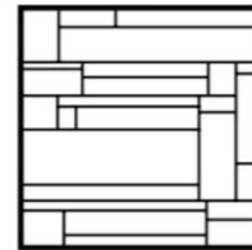
Lienau, 1936



(a)



(b)



(c)



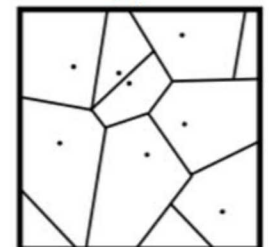
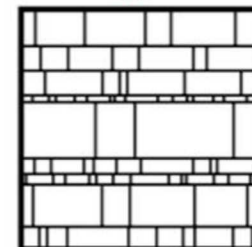
(d)

Mott & Linfoot, 1943

cumulative distribution:

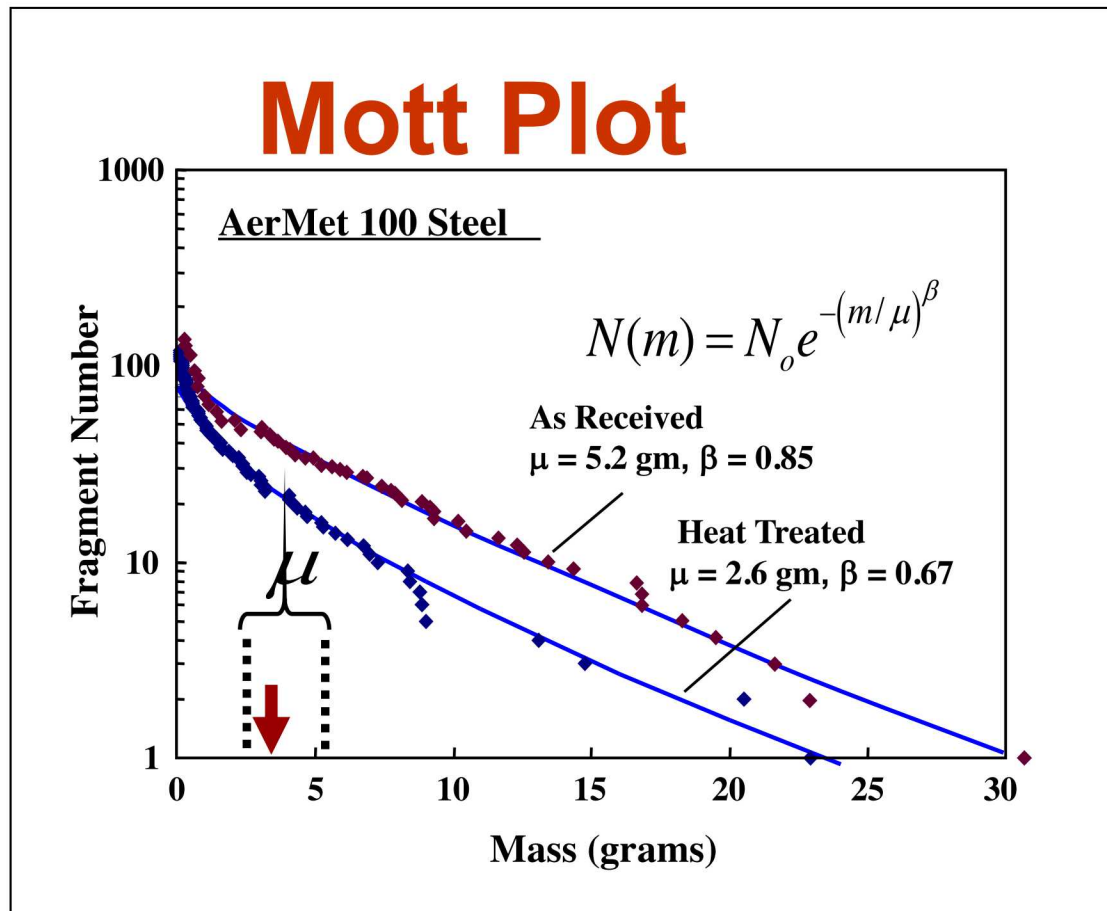
$$F(m) = 1 - e^{-(m/\mu)^{1/2}}$$

generalized results of Lineau motivated by observed mass distributions from fragmenting munitions

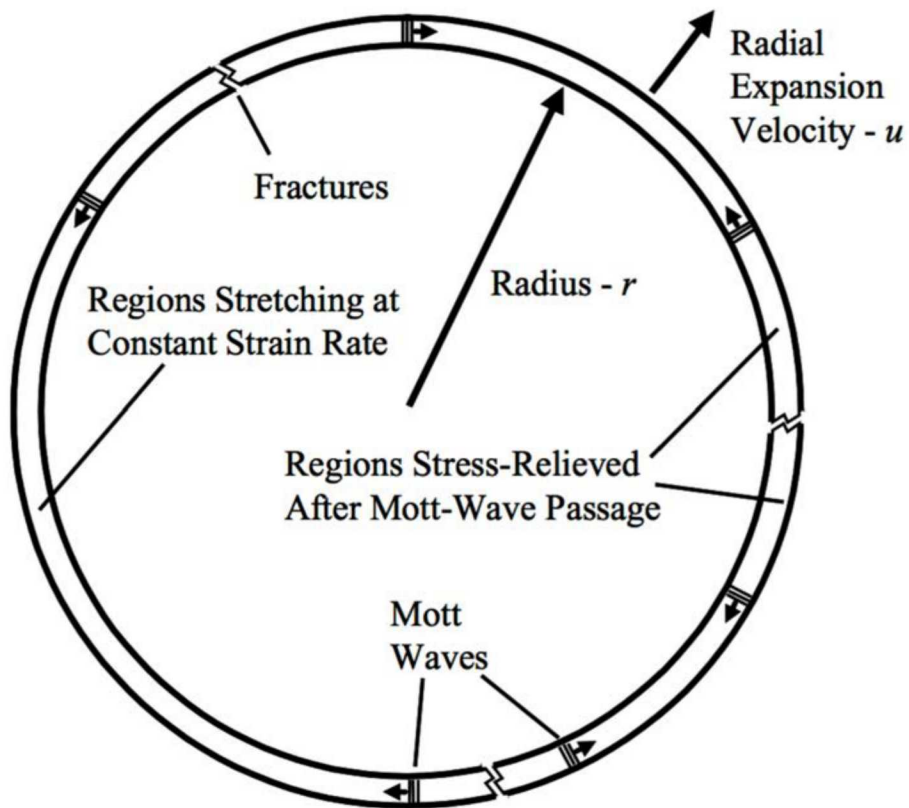




# The Mott-Linfoot Distribution



# Fragmentation of Rings (1)



- consider uniformly expanding ring (or long rod)
- failure initiates at certain locations and occurs instantaneously
- Mott considered rigid-plastic material, but elastic-plastic response is similar
- unloading waves propagate as

$$x = \sqrt{\frac{2Yt}{\rho\dot{\epsilon}}} t$$

- unloading waves unload material so it can no longer fail



## Fragmentation of Rings (2)

- Mott considered the probability of fracture  $\lambda(\varepsilon)$  to be:

$$\lambda(\varepsilon) = \lambda_0$$

$$\lambda(\varepsilon) = \frac{n}{\sigma} \left( \frac{\varepsilon}{\sigma} \right)^{n-1}$$

$$\lambda(\varepsilon) = A e^{\gamma \varepsilon}$$

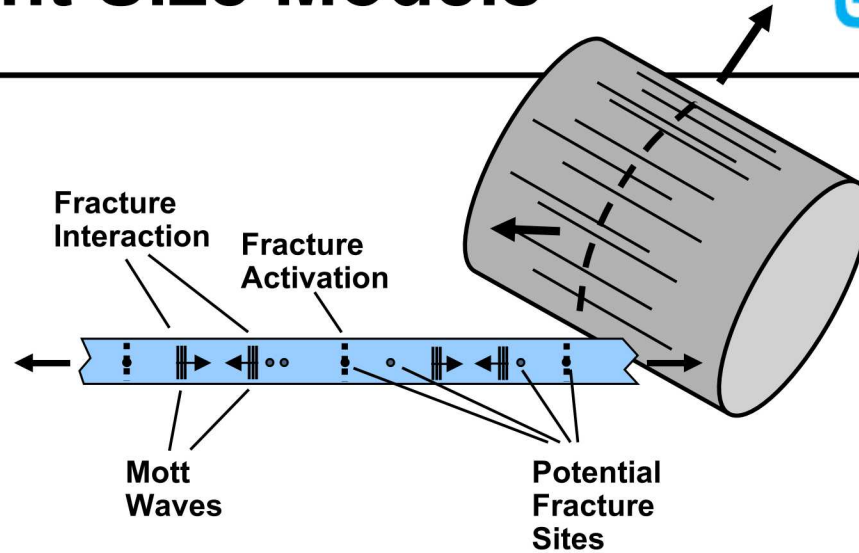
unloading waves unload material  
so it can no longer fail

# Fragment Size Models

## Mott Fragment Size (1943)

- Cylinder Fragmentation
- Fracture Statistics Based

$$\lambda \approx \sqrt{\frac{2Y\sigma}{\rho\dot{\epsilon}}}$$



## Grady Fragment Size (1982)

- More General Fragmentation
- Energy Based

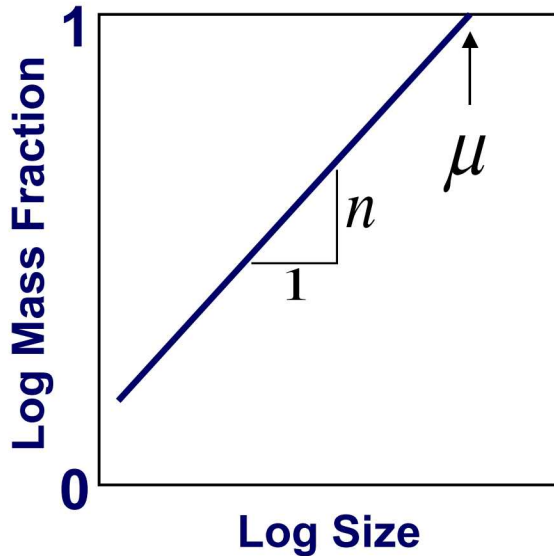
$$\lambda \approx \left( \frac{48\Gamma}{\rho\dot{\epsilon}} \right)^{1/3}$$



# Brittle Fragmentation Distribution

## Schuhmann (1940) Mass-Size Distribution

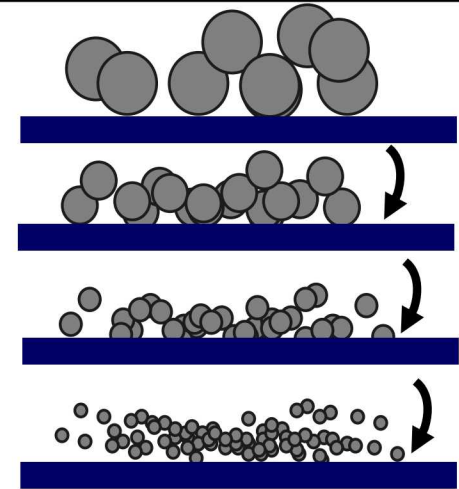
Cumulative Mass Fraction Finer



$$\frac{M(x)}{M_0} = \left( \frac{x}{\mu} \right)^n$$

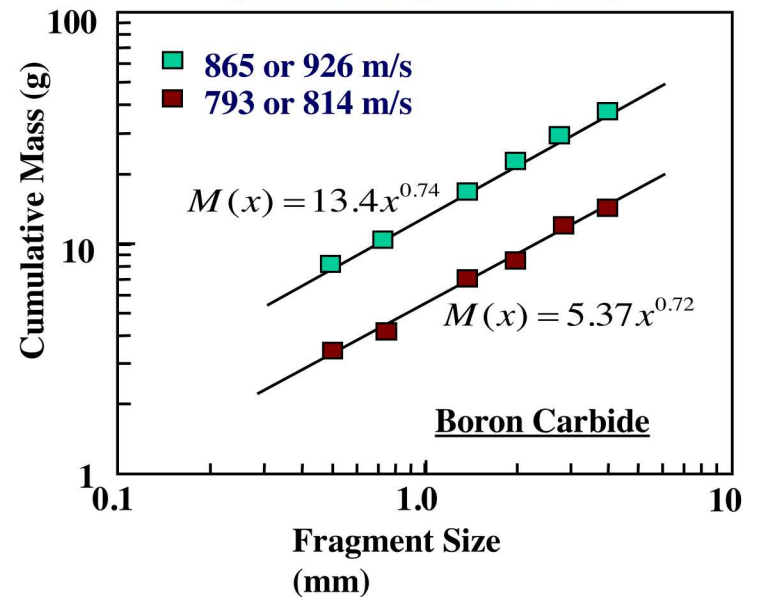
Schuhmann Size Scale

Schuhmann Index



Sieve Analysis

## Schuhmann Plot

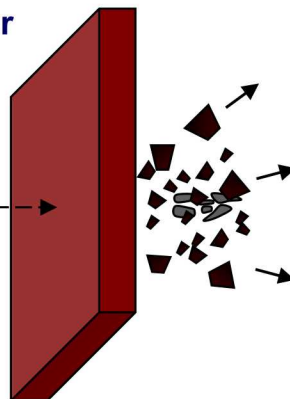


M993 APP  
WC-Co core



(Moynihan et al., 2002)

B4C Armor Package





# Span of Length Scales

- **Horizon Criterion**

$$\lambda \leq 2ct$$

- **Energy Criterion (SE + KE  $\geq$  FE)**

$$\frac{1}{2} \frac{P^2}{\rho c^2} + \frac{1}{120} \rho \varepsilon^2 \lambda^2 \geq \frac{3\Gamma}{ct}$$

- **Dynamic Loading**

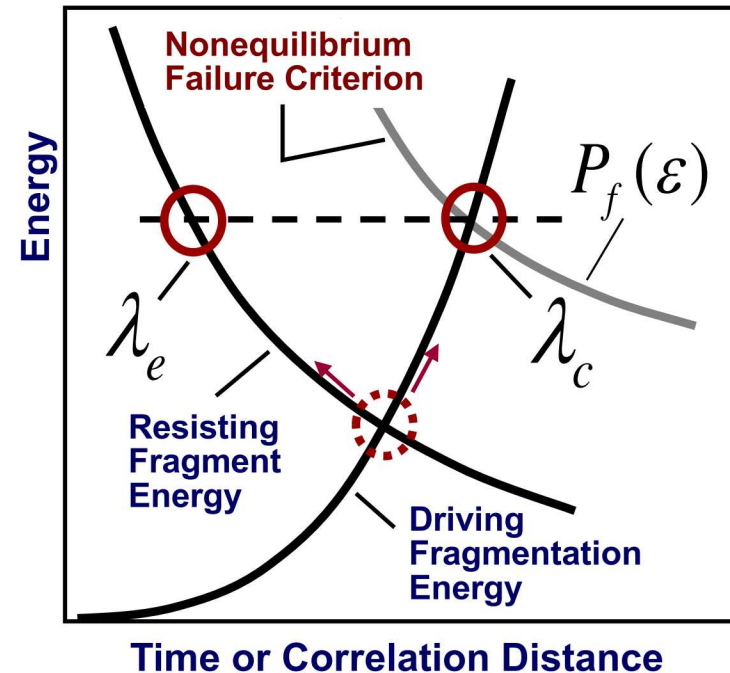
$$P = \rho c^2 \varepsilon t$$

- **Fragmentation Resistance**

$$\Gamma(\varepsilon, T, \lambda)$$

- **Failure Stress (Energy)**

$$P_f(\varepsilon)$$



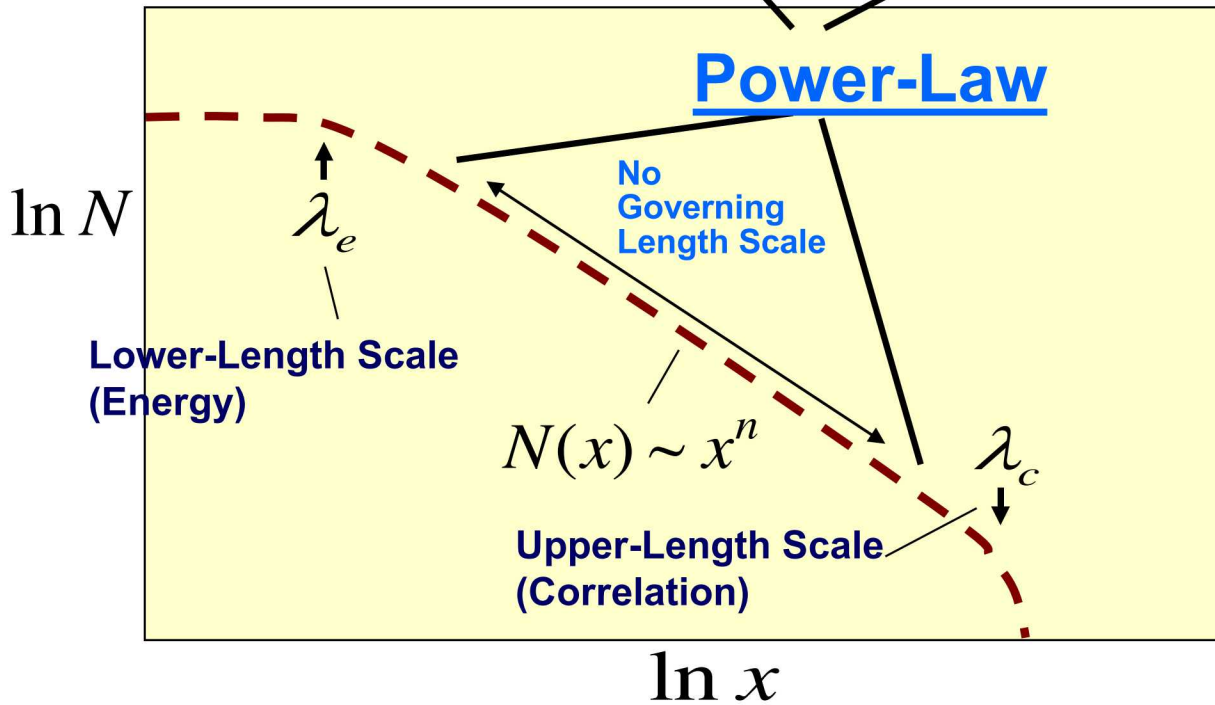
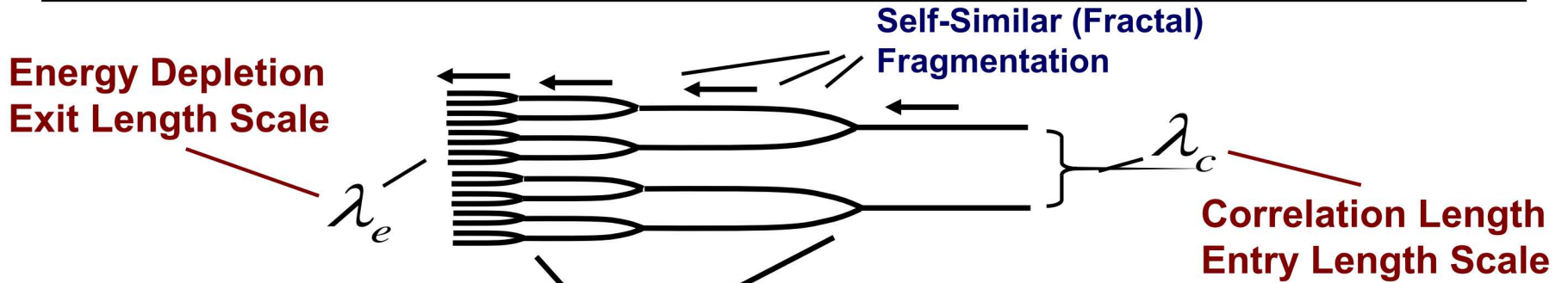
## Entry Fragment Size

$$\lambda_c = 2P_f / \rho c \varepsilon$$

## Exit Fragment Size

$$\lambda_e = 12\rho c^2 \Gamma / P_f^2$$

# Power-Law Physics



Physics of Intermediate Asymptotics



- **Brief Introduction to Shock Physics**
- **Spall Phenomenology and Applications**
- **Fragmentation**
- **Closure and Acknowledgements**



# Conclusions

- 
- **spall is internal fracture caused by the interactions of waves**
    - material (type, flaws/impurities, microstructure, etc.)
    - loading (amplitude, strain rate, shape, direction, etc.)
  - **fragmentation is dynamic breakup into many pieces**
    - rings, cylinders, sphere impact, etc.
    - often approached through scaling laws
    - scaling different for flaw-driven, energy driven, and brittle cases



# Acknowledgements



---

**John Clayton (ARL) - WHA modeling**

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**thanks to Dennis Grady for slides on fragmentation**