

# Molecular dynamics study of shock compression in porous silica glass

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# Overview

- Motivation
- Methodology
- Results
- Conclusions

# Motivation for studying porous silica

- Low density silica aerogels with a range of initial densities are commonly used in extreme conditions:
  - Space missions [1, 2]
  - High P research [3, 4, 5]
- Gaining a more detailed understanding of the processes occurring under these conditions is important.
- Validate model by comparison with experiment.



## Experimental data

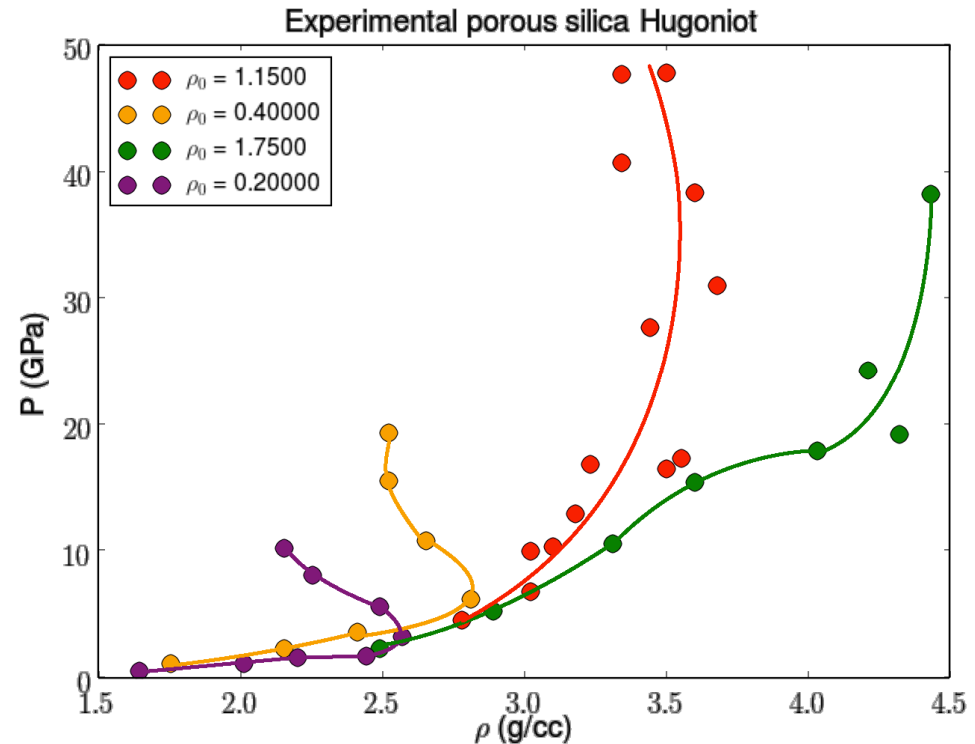
1. M. Burchell et al., *Annu. Rev. Earth Planet. Sci.* **34**, 385 (2006).
2. D. Brownlee et al., *Science* **314**, 1711 (2006).
3. M. D. Knudson, J. R. Asay, and C. Deeney, *J. Appl. Phys.* **97**, 073514 (2005).
4. N. Holmes, *High-Pressure Science and Technology—1993* (AIP, New York, 1994), p. 153.
5. M. D. Knudson and R. W. Lemke, *J. Appl. Phys.* **114**, 053510 (2013).

# Motivation for studying porous silica

An anomalous density inversion in the Hugoniot is observed experimentally at high shock pressures for highly porous silica [6]. This is due to shock energy being converted into kinetic energy as particles are vaporized into the void space. Thermal expansion occurs with respect to the same system shocked to a lower pressure. Local heating during void collapse has been studied with molecular dynamics (MD) [7].

Can we model this density inversion with molecular dynamics?

Can we model this density inversion without using the expensive, propagating, non-equilibrium molecular dynamics (NEMD) model for dynamical shock simulation?

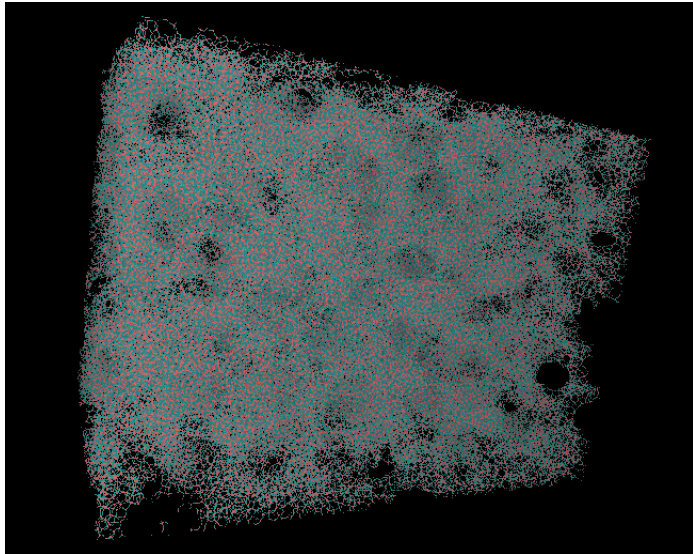


Density inversion in highly porous silica Hugoniot is not well studied with MD.

6. R. F. Trunin, *Experimental data on shock compression and adiabatic expansion of condensed matter* (2001).

7. J. Matthew D. Lane et al., *Comp. Mat. Sci.* **79**, 873-876 (2013).

# Methodology - General



A range of silica systems with various porosities (initial densities) have been created in LAMMPS [8], molecular dynamics package.

Molecular dynamics at the fully atomistic level is employed. Each atom is treated as a partially charged point particle moving under the influence of a user specified potential energy surface:

Short/medium range interactions are calculated using the  $\text{SiO}_2$  BKS potential [9], a simple, tabulated interatomic potential for silica.

Long range interactions are calculated using an Ewald summation.

Each porous silica system is shocked to a range of pressures from the reference state in order to build the Hugoniot.

8. S. Plimpton, *J. Comp. Phys.* **117**, 1-19 (1995).
9. B. W. H. van Beest et al., *Phys. Rev. Lett.* **64**(16), 1955 (1990).

$\rho_0$ (g/cc)	% Porosity
2.212	0
2.09	~5
1.08	~50
0.56	~75
0.23	~90
0.14	~95

# Methodology – Initial System

- Expand spherical voids at 2500 K until desired porosity is reached
- Cool to 300 K.
- Equilibrate
- Remove voids and re-equilibrate.

~50 % porous system

Periodic boundary conditions

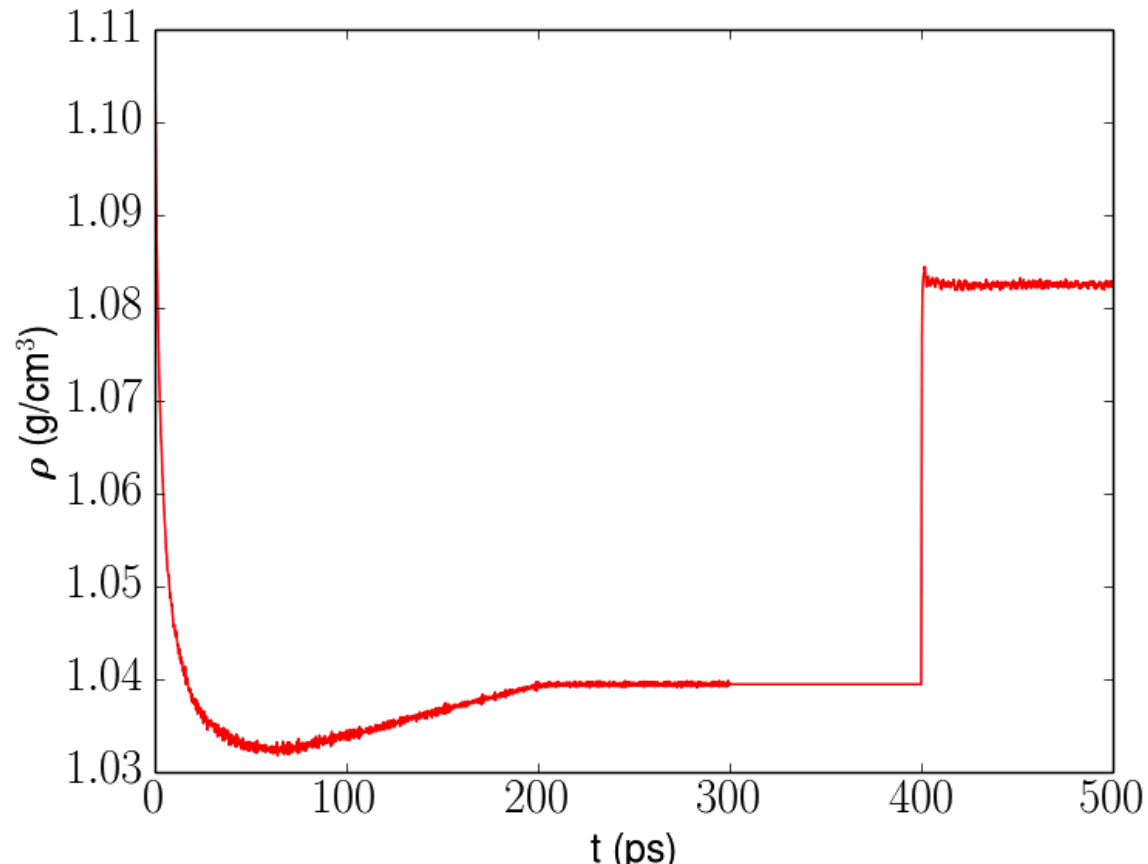
Timestep: 1 fs

Average density: 1.08 g/cc

Average pore diameter: 20.0 Å

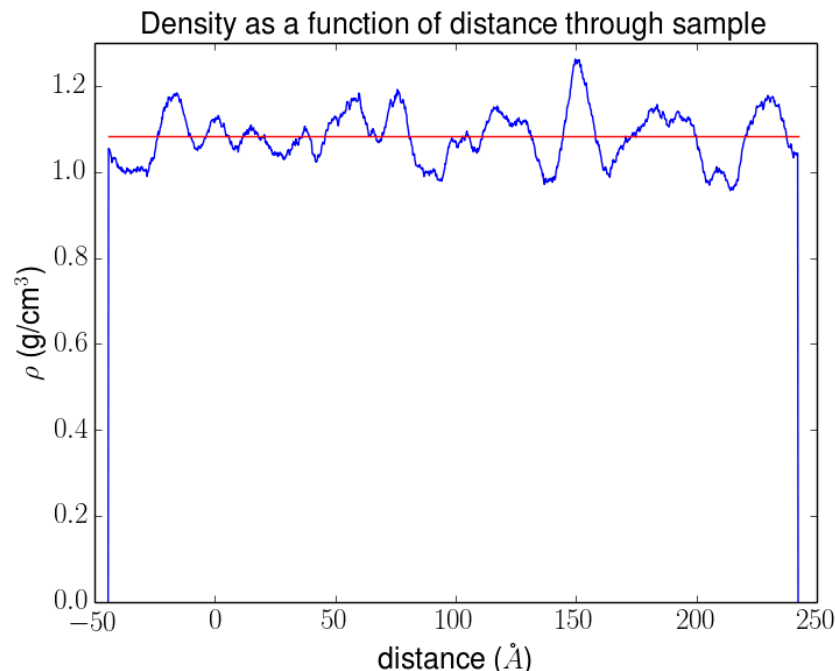
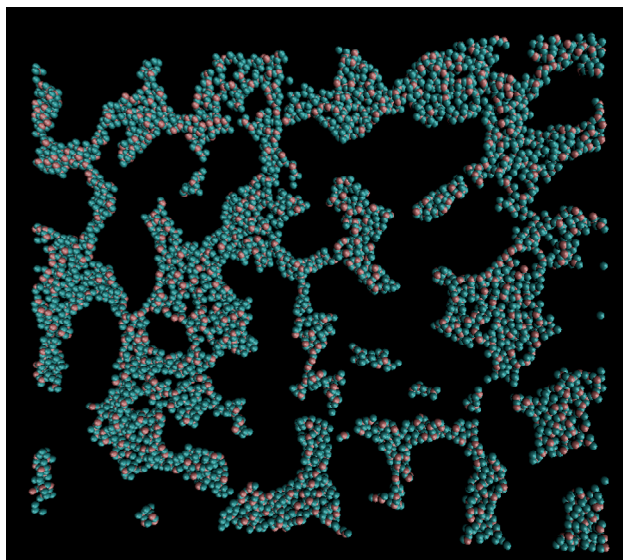
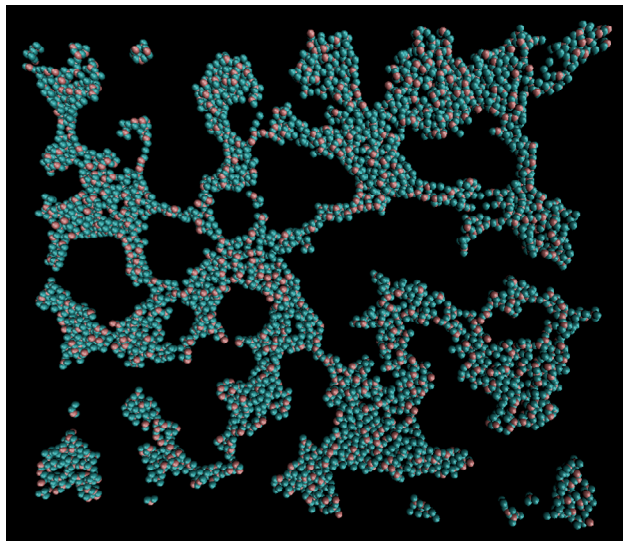
Number of atoms: 373248

Box dimensions: 182 x 217 x 290 Å<sup>3</sup>





# Methodology – Initial System



Each data point - 4 Å slice throughout 50 % porous sample

Average density: 1.08 g/cc

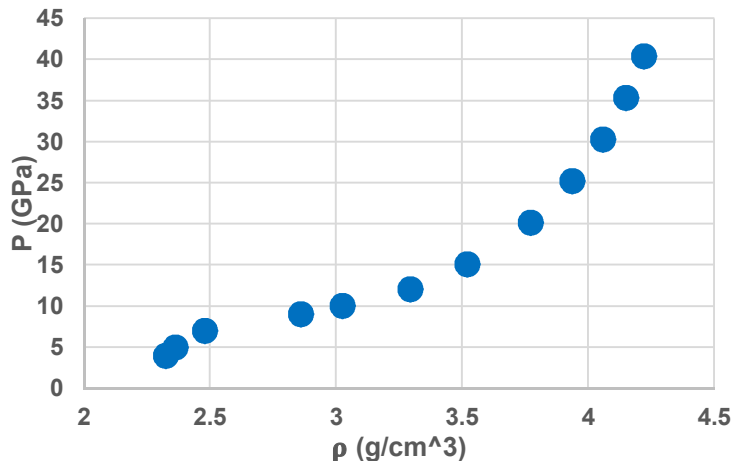
Average pore diameter: 20.0 Å

Number of atoms: 373248

Box dimensions: 182 x 217 x 290 Å<sup>3</sup>

# Methodology – Reproducing the Hugoniot in MD

Hugoniot: the locus of points representing a series of final states originating from a single reference state, when the final and reference states are separated by a discontinuity (a shock), satisfying the jump conditions (energy, mass, and momentum conservations) which relate the initial state to the final state.



## Reproducing the final state in MD

1. Non-equilibrium molecular dynamics. Propagate a shock through the material via a momentum mirror [7, 10], calculate state variables to verify jump conditions.
  - Expensive and requires large system sizes.
  - Effectively reproduces experimental Hugoniot data for porous systems [7].
2. Non-propagating, constant stress Hugoniotstat method [11]. Uniaxially compress system until final pressure is reached and jump conditions are met.
  - Less expensive.
  - Well tested in traditional Hugoniot space.
  - Not guaranteed to evolve along Rayleigh line or any other path through  $\rho$ ,  $P$  space.
  - Path and efficiency of path depend on damping coefficients.
  - Previously untested on porous systems.

10. B. L. Holian and P. S. Lomdahl, *Science* **280**, 2085 (1998).

11. R. Ravelo et al., *Phys. Rev. B* **70**, 014103 (2004).



# Methodology – Reproducing the Hugoniot in MD.

Constant stress Hugoniot method in action.

50 % porous (1.08 g/cc) silica.

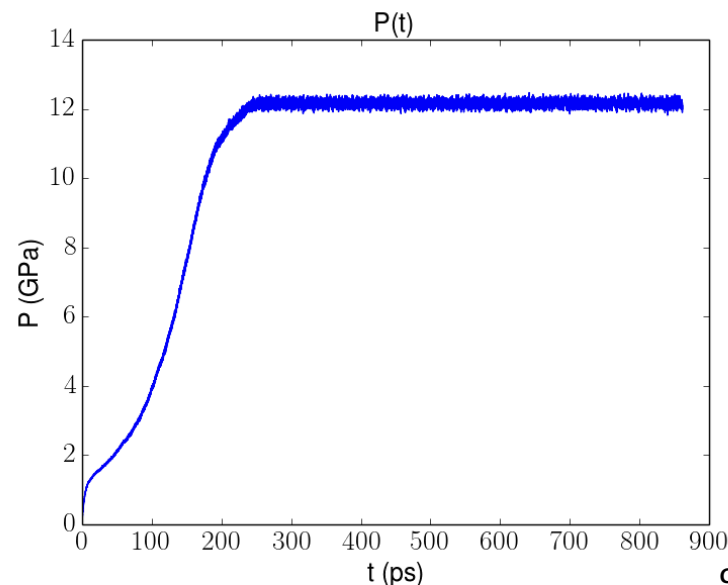
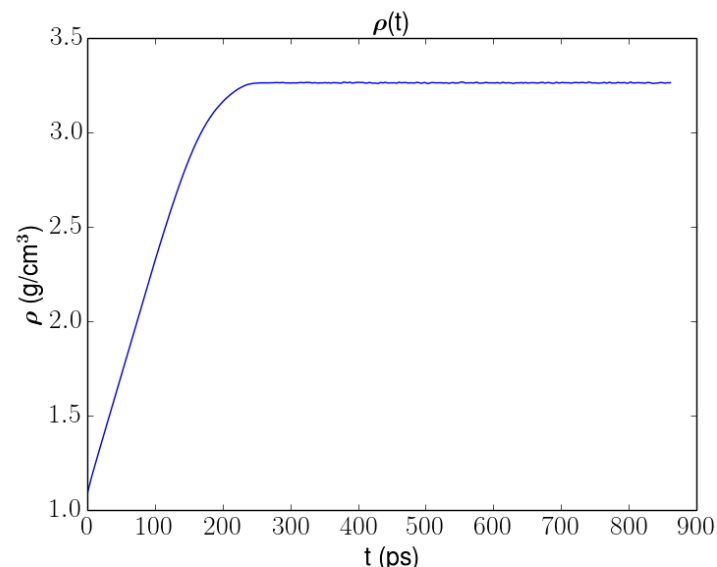
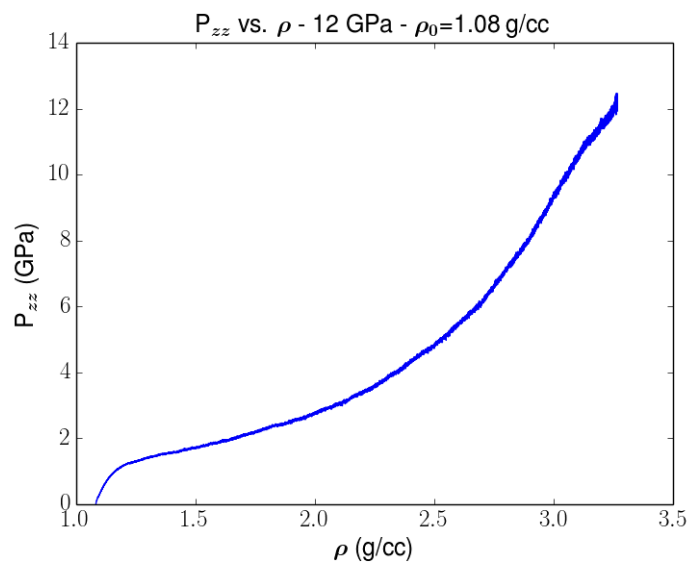
Final pressure: 12 GPa.

Time step: 0.2 fs.

Temperature damping coeff: 20 ps

Pressure damping coeff: 20 ps

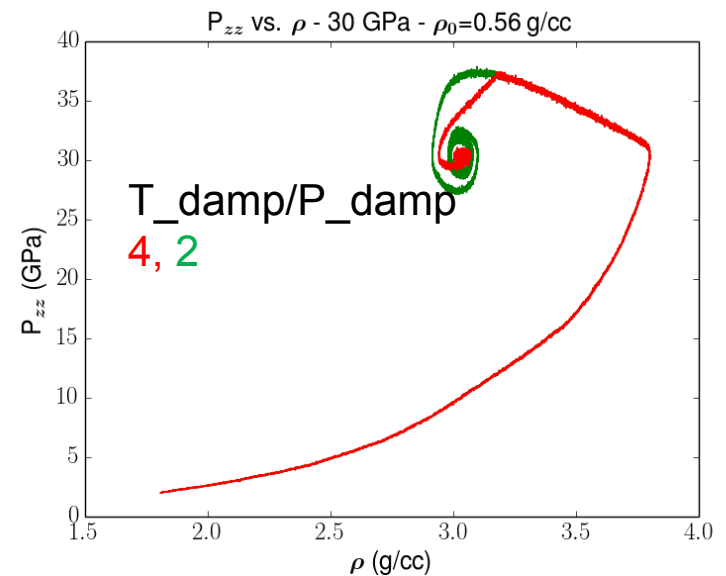
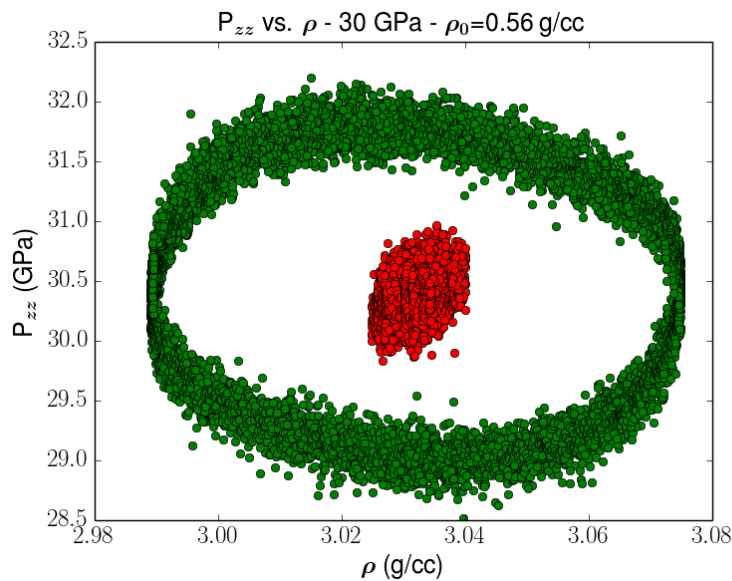
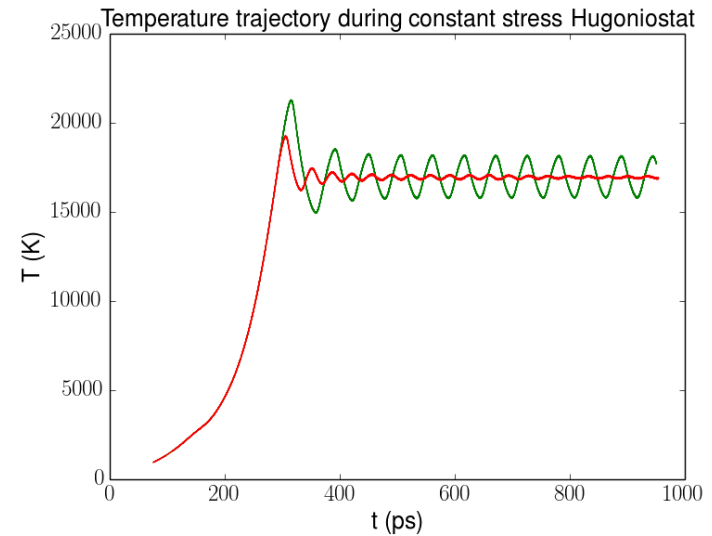
Trajectory:



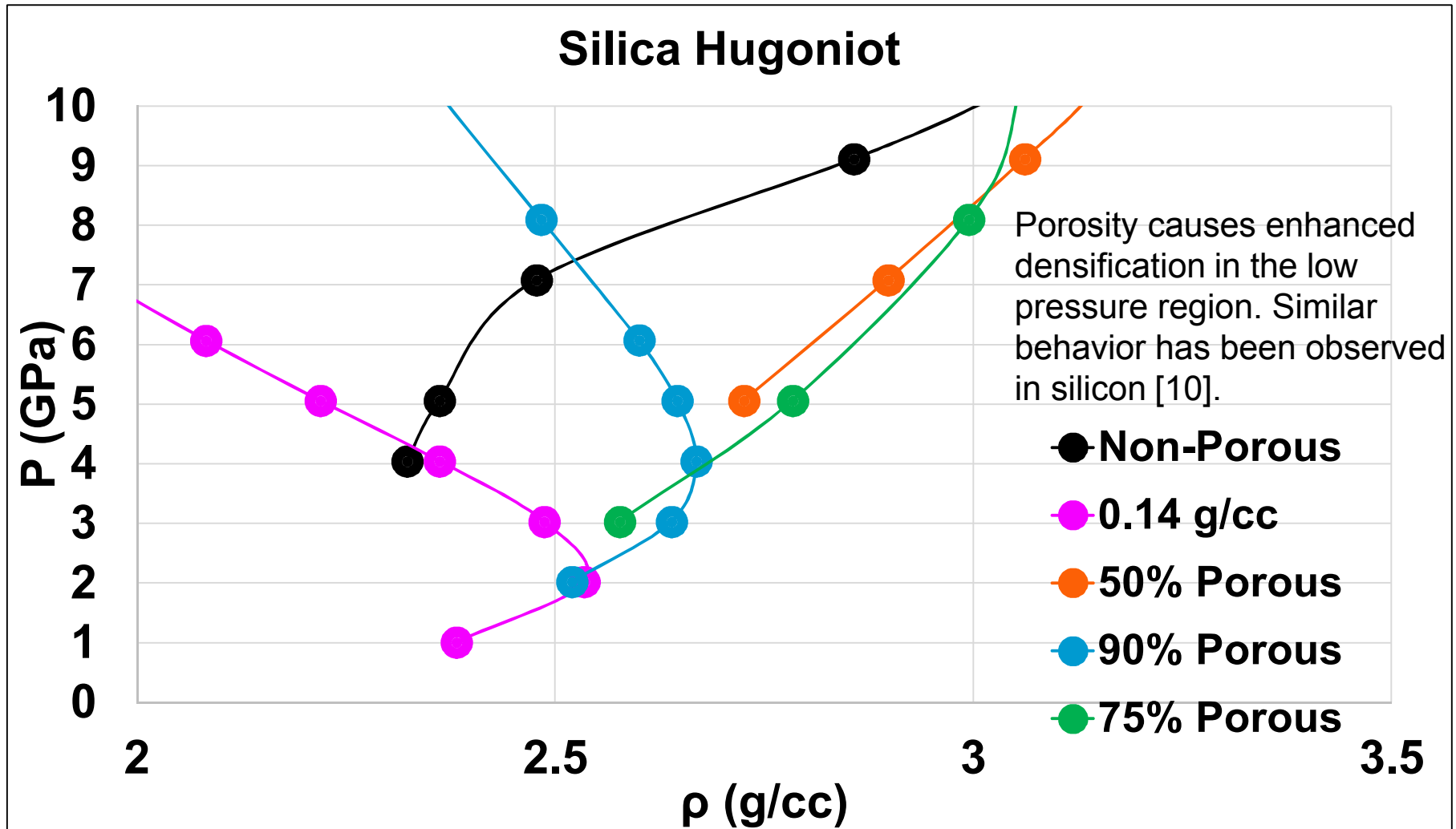
# Methodology – Reproducing the Hugoniot in MD.

75 % porous (0.56 g/cc) silica.  
Final pressure: 30 GPa.  
Time step: 0.2 fs.

System gets very hot (~15000 K)  
compared to an analogous final  
pressure for fully dense silica (~2000 K).  
Final state is not very sensitive to  
damping coefficient ratios.



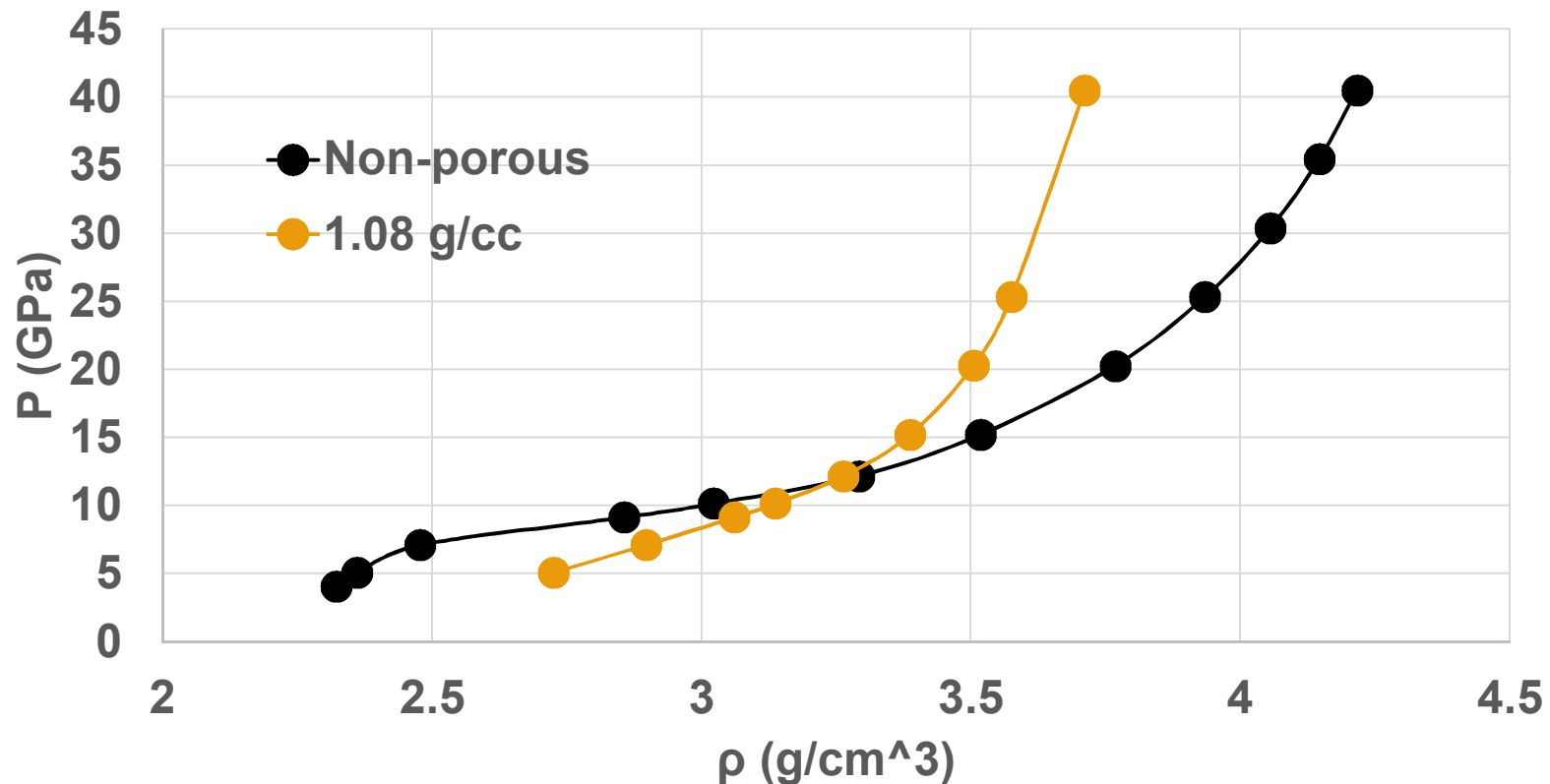
# Results – Enhanced densification



10. J. Matthew D. Lane et al., *Phys. Rev. B* **90**, 134311 (2014)

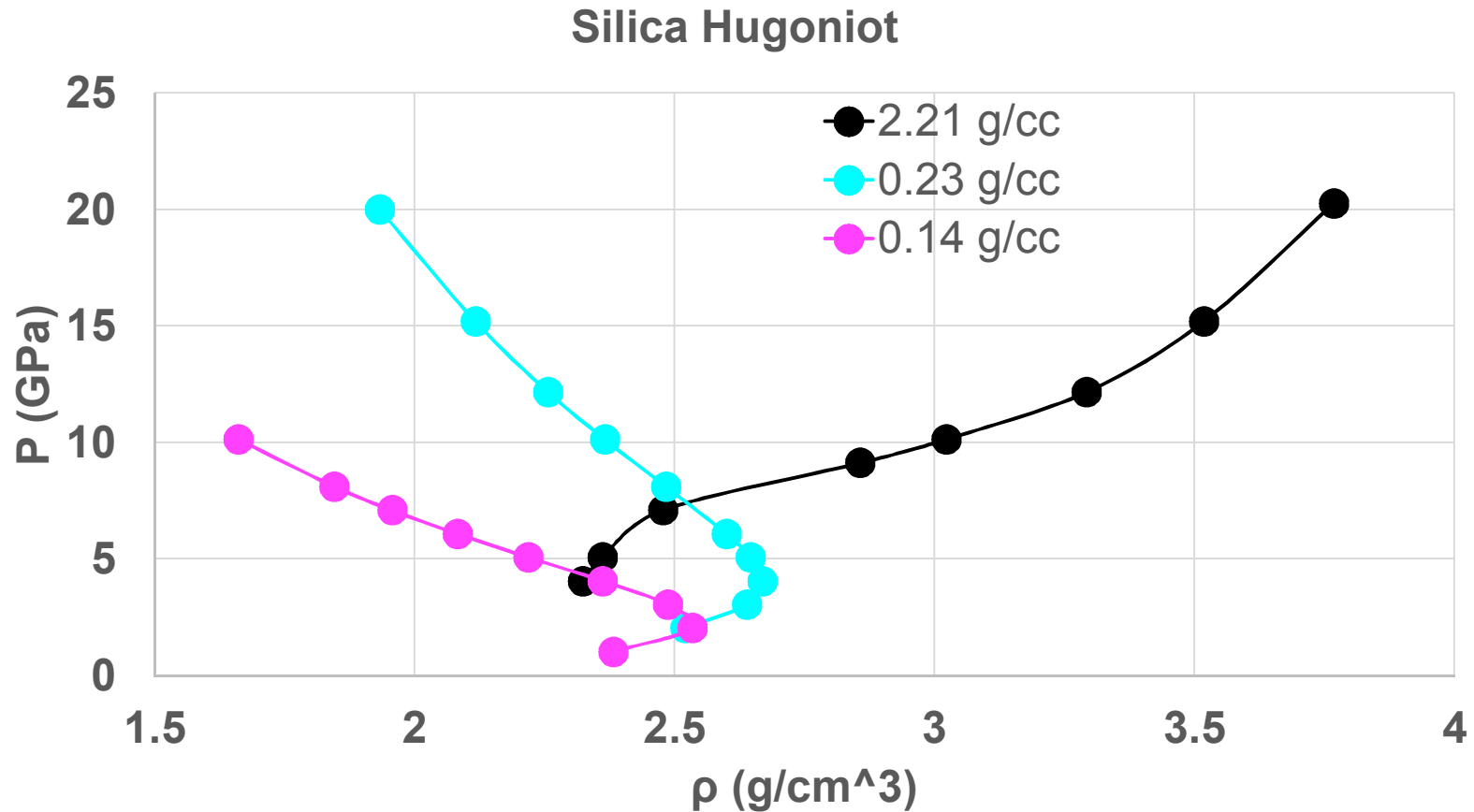
# Results – Enhanced densification

## Silica Hugoniot



Enhanced densification is observed at lower pressures.  
Normal behavior of shocked porous material relative to shocked non-porous material returns above 10 GPa.

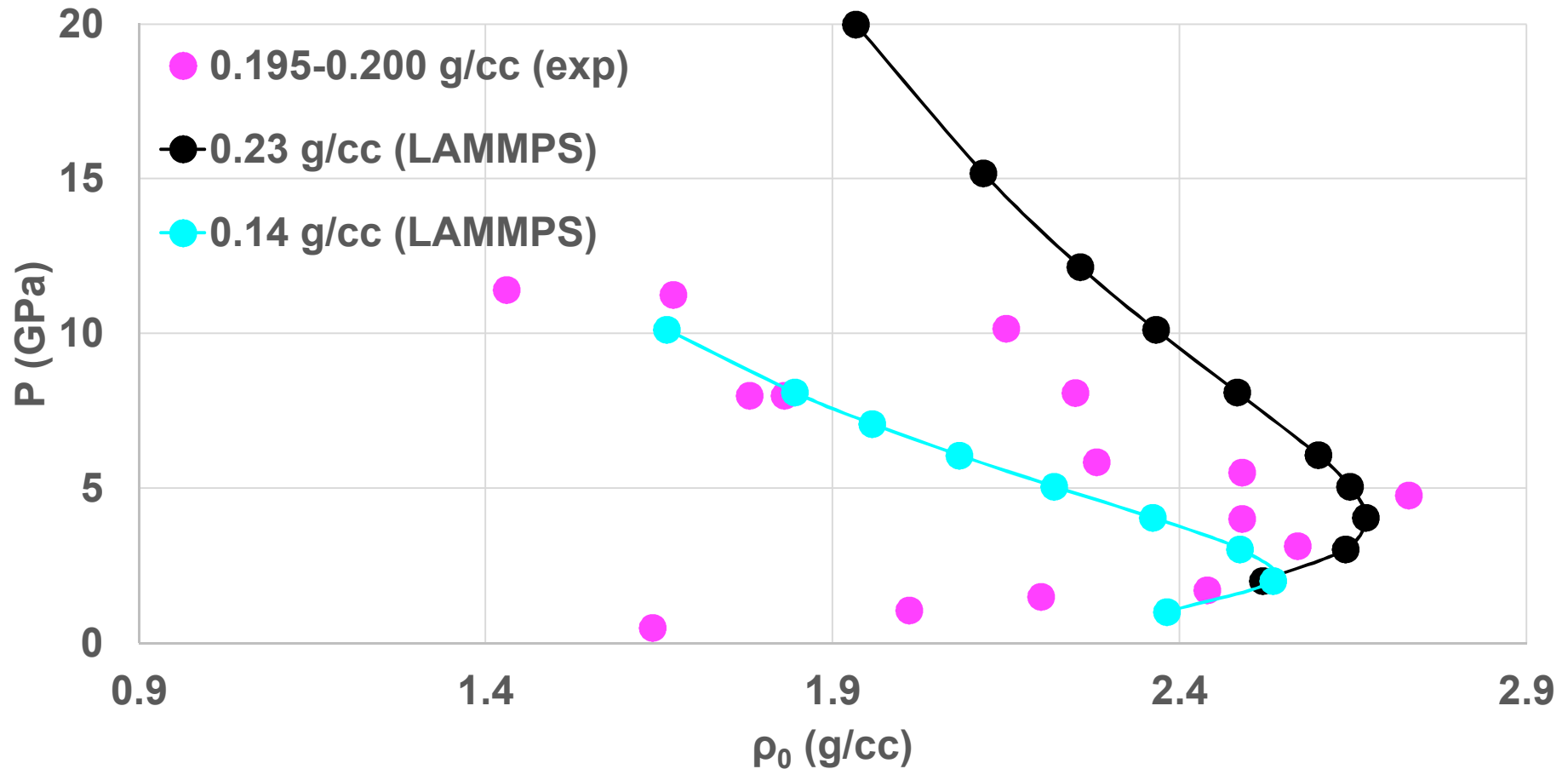
# Results – Density inversion



Demonstrated density inversion is in qualitative agreement with experiments

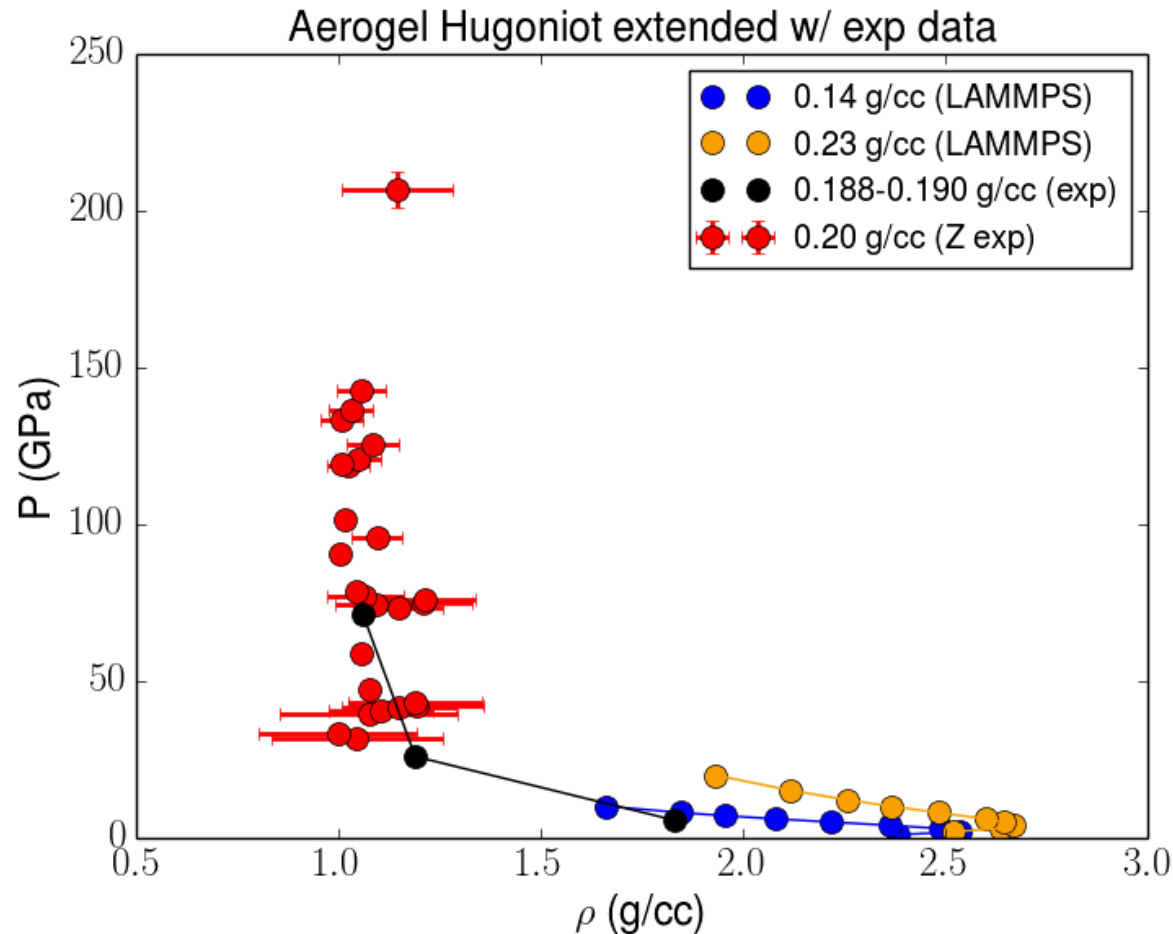
# Results – Density inversion

Aerogel comparison with experiment





# Results – Density inversion



Very high pressure experimental data for highly porous silica, collected using the Z-machine [5], plotted against LAMMPS and other experimental data shows a cusp in the Hugoniot.

Z machine data is not reproducible with molecular dynamics. Simulation at the level of density functional theory is needed.

5. M. D. Knudson and R. W. Lemke, *J. Appl. Phys.* **114**, 053510 (2013).
6. R. F. Trunin, *Experimental data on shock compression and adiabatic expansion of condensed matter* (2001).

# Conclusions

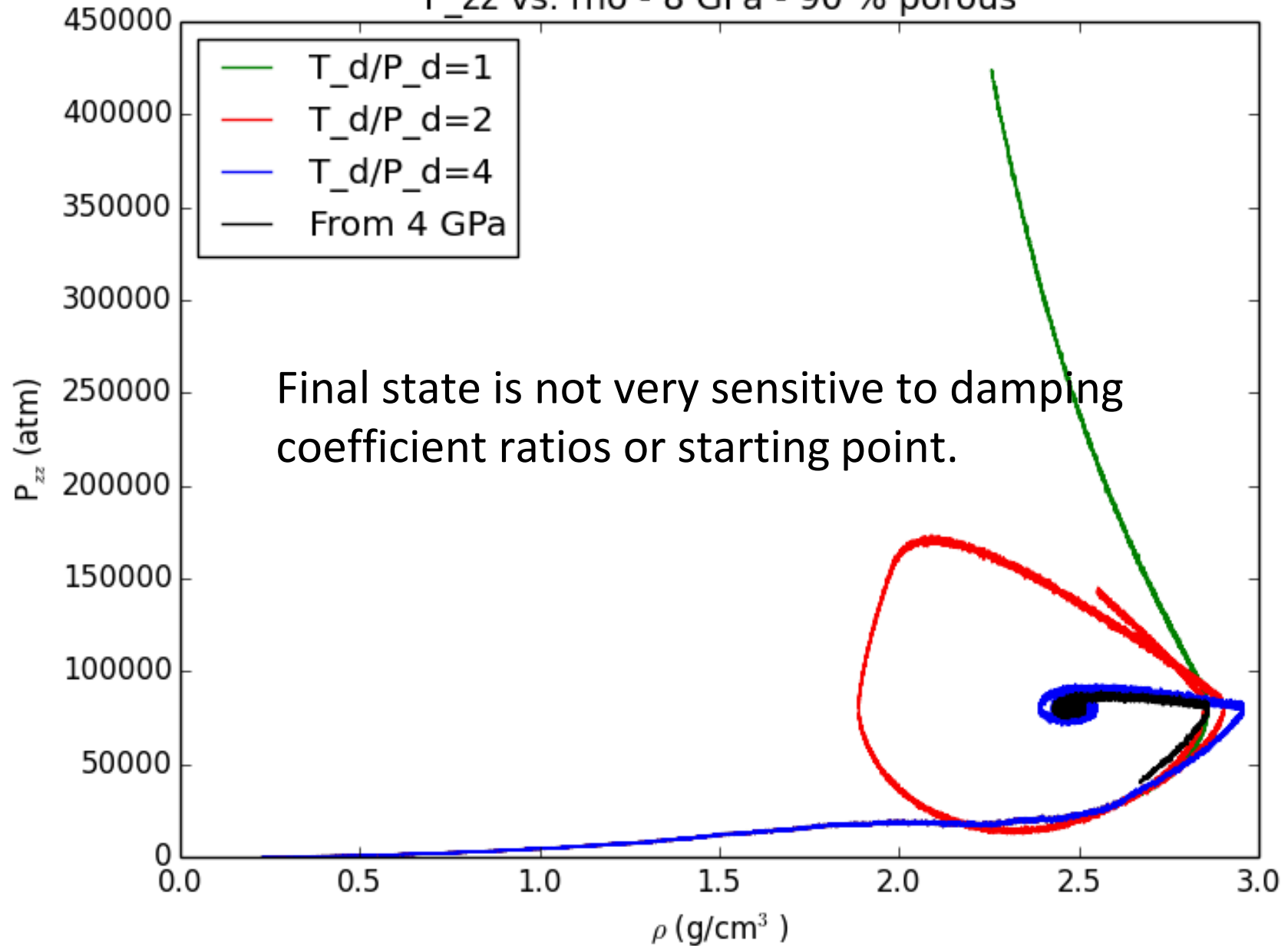
- BKS, a very simple  $\text{SiO}_2$  potential, coupled with the constraint stress Hugoniotat reliably reproduces the Hugoniot for porous  $\text{SiO}_2$ .
- Enhanced densification is observed at lower pressures.
- Negative  $dP/dp$  in the Hugoniot for highly porous  $\text{SiO}_2$  is qualitatively captured in this very simple model.

# Acknowledgements

- Sandia National Labs
  - High Performance Computers
- Kyle Cochran
- Thomas Mattsson



$P_{zz}$  vs.  $\rho$  - 8 GPa - 90 % porous



50 % void radii  
distribution  
In angstroms

Average radius		9.96225607
Range	N voids	
4 to 5	23	
5 to 6	333	
6 to 7	290	
7 to 8	292	
8 to 9	320	
9 to 10	277	
10 to 11	281	
11 to 12	291	
12 to 13	311	
13 to 14	288	
14 to 15	285	
15 to 16	38	