

6 DOF Shock and Vibration: Testing and Analysis

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Analytical Structural Dynamics

*Shock and Vibration Exchange
Orlando, FL*

October 7, 2015



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Motivation

- 6 Degree of Freedom (DOF)
 - Inputs applied to a test article/model with 6 DOFs
 - 3 translational DOF, 3 rotational DOF
- Experimental
 - 6 DOF shakers have potential to provide a more representative test of an actual environment than a single-axis test specification
 - Off-axis inputs arise from single-axis testing on single-axis shaker
 - 6 DOF shakers allow off-axis inputs to be controlled/minimized during a single-axis test specification
- Analytical
 - Apply 6 DOF input to models in shock and vibration analysis
 - More accurate post-test analysis and calibration
 - Cross-axis inputs can be significant
 - Investigate unmeasured quantities from testing (i.e. stress)
 - Tool for understanding and developing better 6 DOF testing

Outline

- 6 DOF Analysis Procedure
 - Derivation of 6 DOF inputs
 - Considerations
- Model Configuration
- Vibration
 - 1 DOF vs. 6 DOF Testing
 - Impact on stresses
- Shock
 - Single-axis test spec vs. 6 DOF environment
 - Impact on stresses

Derivation of 6 DOF Inputs

- 6 DOF input is the effective rigid body motion of the structure about seismic mass.
 - Should be relatively non-compliant to avoid capturing deformable effects in the calculation of rigid body motion.
 - Typically use accelerometers on a fixture.
- Consider a measurement by tri-axial accel “i”: $\vec{a}^{(i)}(t)$
- Let the coordinate of this measurement be: $\vec{x}^{(i)}$
- Let the reference/ input location coordinate be: $\vec{x}^{(0)}$
- The accel has a position vector: $\vec{r}^{(i)} = \vec{x}^{(i)} - \vec{x}^{(0)}$

Derivation of 6 DOF Inputs (2)

- Let the effective rigid body acceleration of the structure be:
 - $\vec{A}(t)$ for translational acceleration
 - $\vec{\alpha}(t)$ for angular acceleration
- The accelerometer acceleration can be expressed as:
 - $\vec{a}^{(i)}(t) = [I_{3x3}]\vec{A}(t) + \vec{\alpha}(t) \times \vec{r}^{(i)}$
 - $\vec{a}^{(i)}(t) = [I_{3x3}]\vec{A}(t) + [\vec{\tilde{r}}^{(i)}]^T \vec{\alpha}(t)$
- We can develop a system of equations for multiple measurement points:

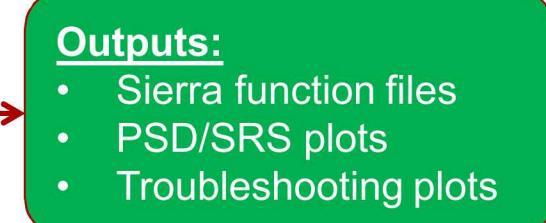
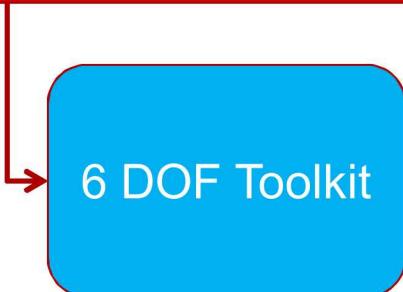
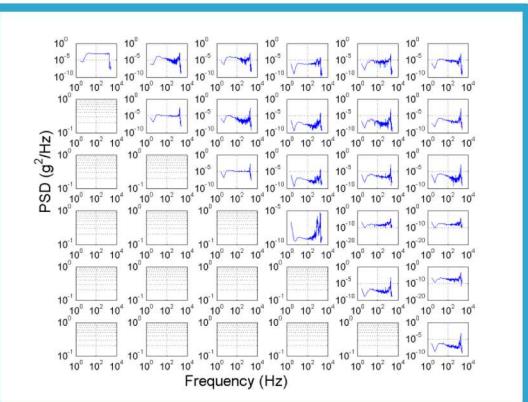
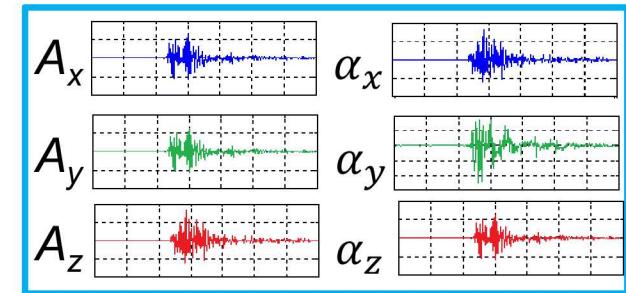
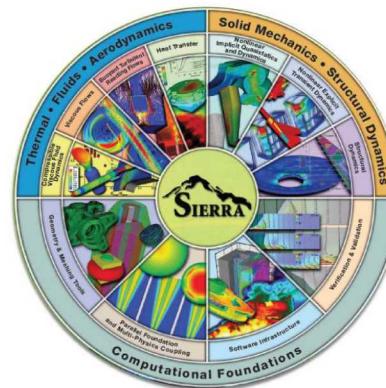
$$[\vec{\tilde{r}}] = \begin{bmatrix} 0 & -r_3 & r_2 \\ r_3 & 0 & -r_1 \\ -r_2 & r_1 & 0 \end{bmatrix}$$

$$\begin{bmatrix} \vec{a}^{(1)}(t) \\ \vec{a}^{(2)}(t) \\ \vdots \\ \vec{a}^{(n)}(t) \end{bmatrix} = \begin{bmatrix} [I_{3x3}] & [\vec{\tilde{r}}^{(1)}]^T \\ [I_{3x3}] & [\vec{\tilde{r}}^{(2)}]^T \\ \vdots & \vdots \\ [I_{3x3}] & [\vec{\tilde{r}}^{(3)}]^T \end{bmatrix} \begin{bmatrix} \vec{A}(t) \\ \vec{\alpha}(t) \end{bmatrix}$$

Solve for RB Accelerations

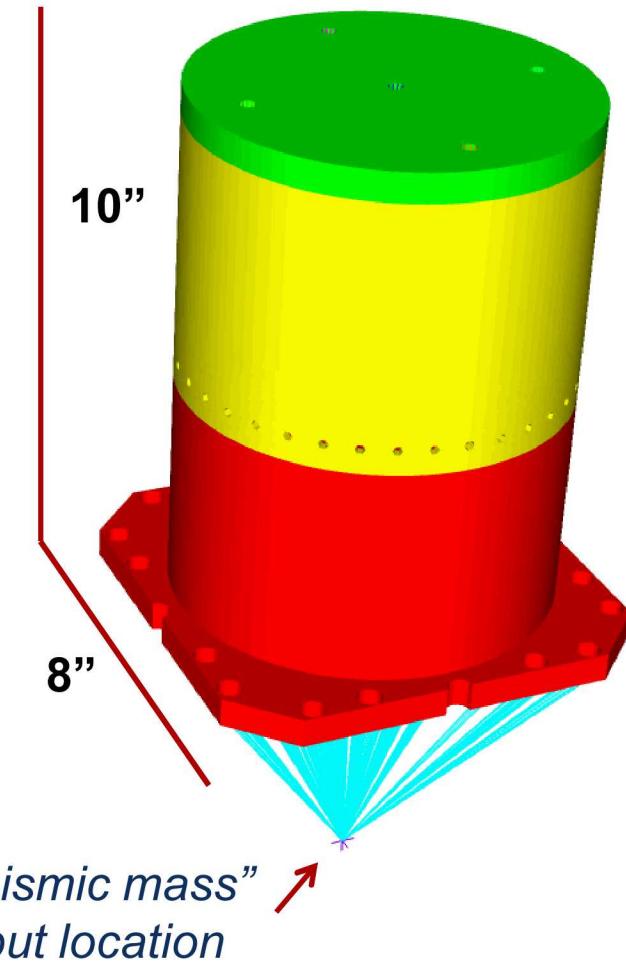
Considerations

- Methodology to derive 6 DOF inputs relies heavily on:
 - Accelerometers mounted to non-compliant points
 - Sufficient measurements to characterize 6 DOF motion
 - Accurate measurement of accelerometer:
 - Position
 - Orientation
 - Polarity (signs do matter)
- Requires measurement of time histories from vibration testing
- Thorough documentation of test setup/instrumentation & accurate channel tables are very helpful
- We've developed some tools to troubleshoot some of these issues

 Written for interface to Sandia's Sierra-SD FEA Software

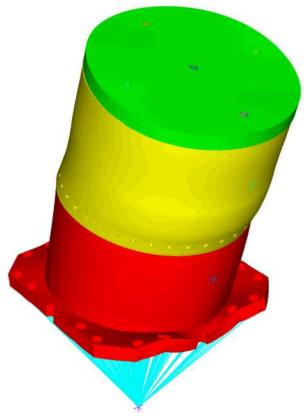
Model Configuration

- 3 piece bolted “can” structure
 - *Bottom can/flange*
 - *Upper can*
 - *Top plate/mass*
 - *Aluminum*
- Test-bed with reasonable complexity
- Rigid elements & concentrated mass model test stand/connection
- Employed in physical 1 DOF and 6 DOF testing
- 6 DOF input will be derived from accelerometers on corners of flange



Analytical Modes

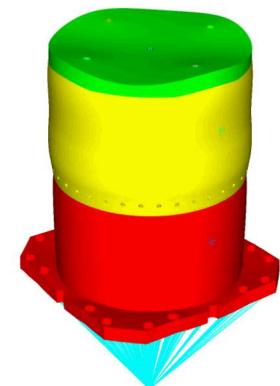
Frequency = 709 Hz



Frequency = 709 Hz



Frequency = 1816 Hz



Frequency = 2761 Hz



Frequency = 2764 Hz

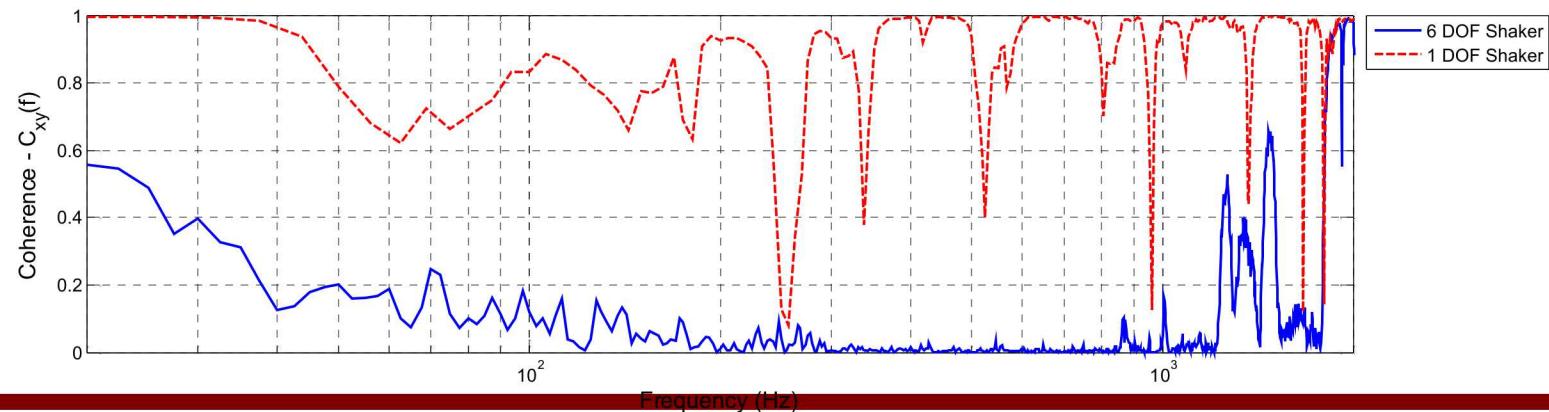
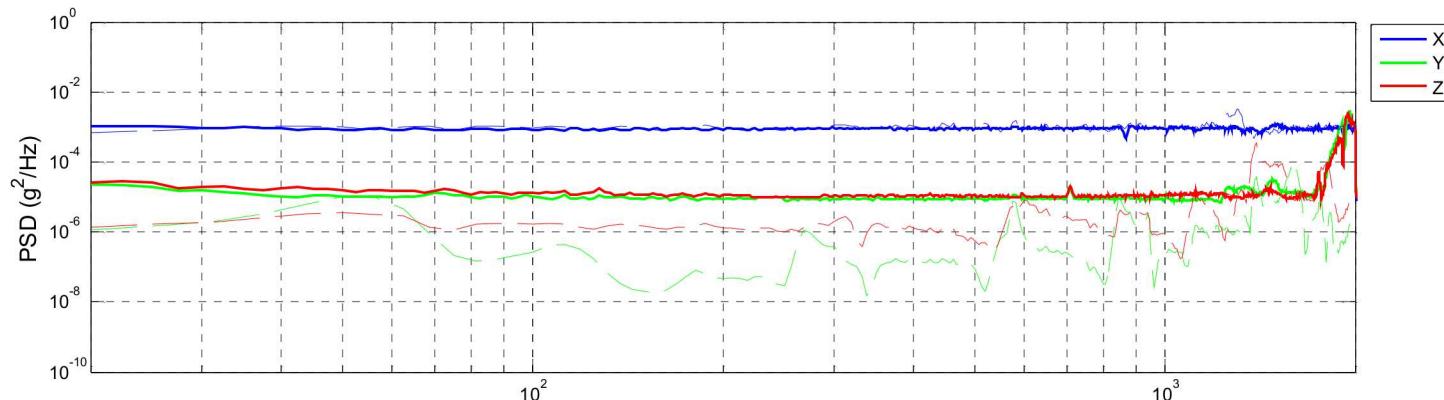


Frequency = 2765 Hz



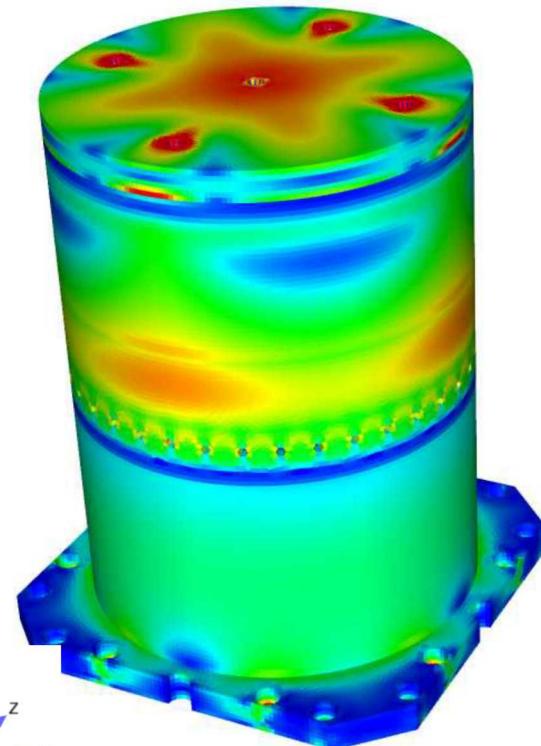
1 DOF vs. 6 DOF Testing

- Single-axis (axial) low level random vibration input on 1 and 6 DOF shakers
 - Off-axis inputs controlled 2 orders of magnitude lower than in-axis
 - Coherence is minimized on 6 DOF shaker

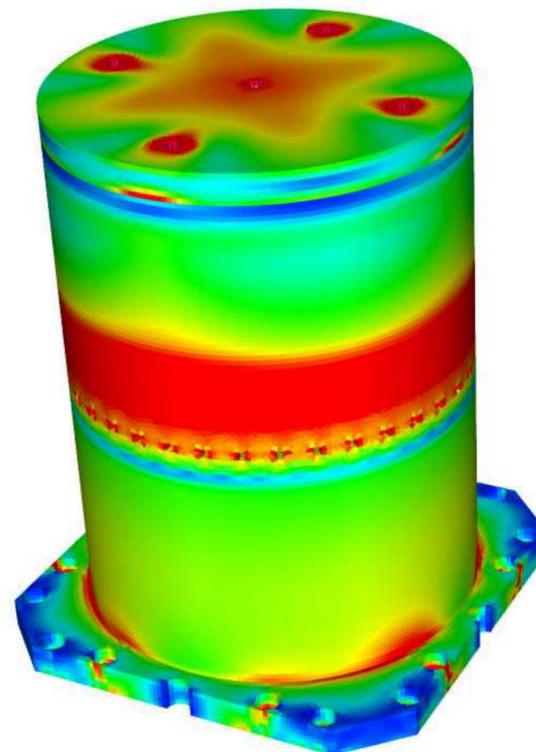


Vibration: Stress Contours

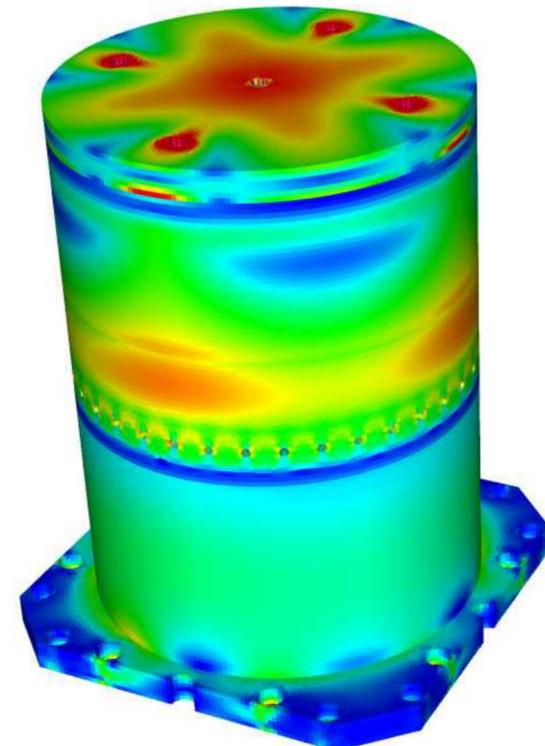
Ideal Single-Axis:



6 DOF Shaker:



1 DOF Shaker:

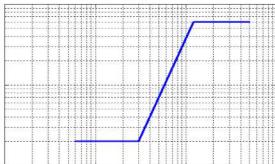


6 DOF Shock Input

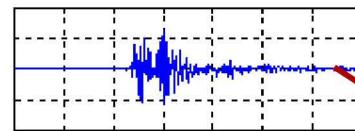
- Comparison of single-axis test spec and 6 DOF input recovered from environment
- Traditionally environmental data is broken out into single-axis test specs
- 6 DOF testing affords new opportunities

Single-Axis Test Spec:

SRS Spec



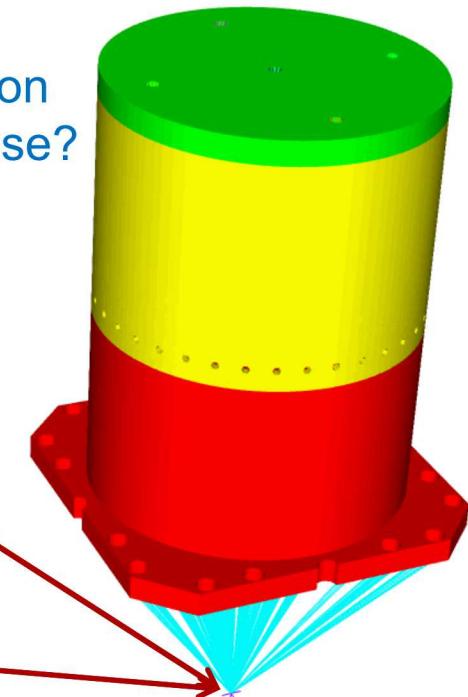
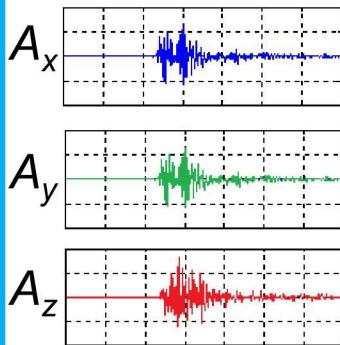
Decayed Sine Series



What's the impact on
component response?
Stresses?

VS.

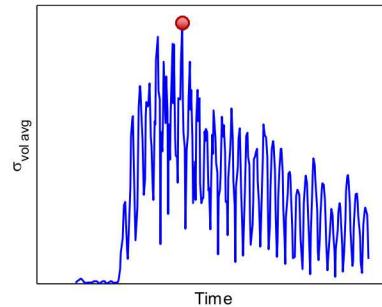
Recovered 6 DOF Input:



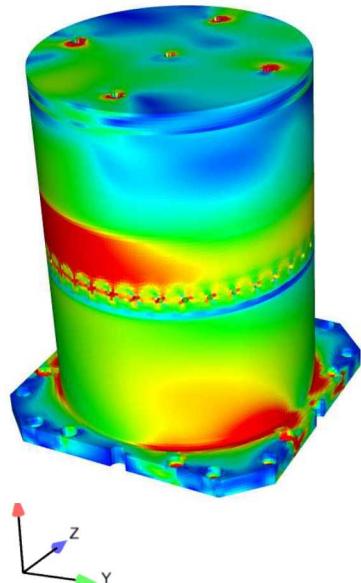
1 & 6 DOF Shock: Stresses

- Compared Von Mises stress distributions at instance of maximum volume averaged stress
- Noticeably different levels and distributions between 6 DOF and 1 DOF inputs

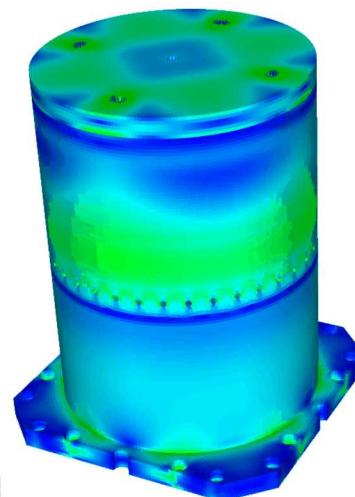
$$\sigma(t)_{vol\ avg} = \frac{\sum_{i=1}^{Nel} \sigma_i(t) v_i}{\sum_{i=1}^{Nel} v_i}$$



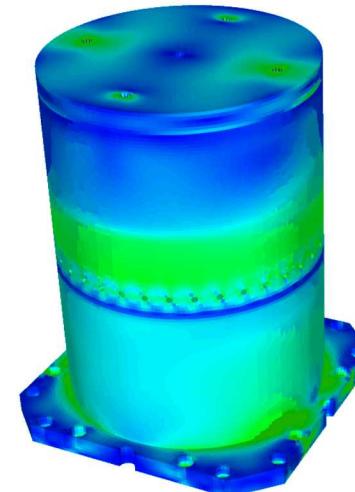
6 DOF:



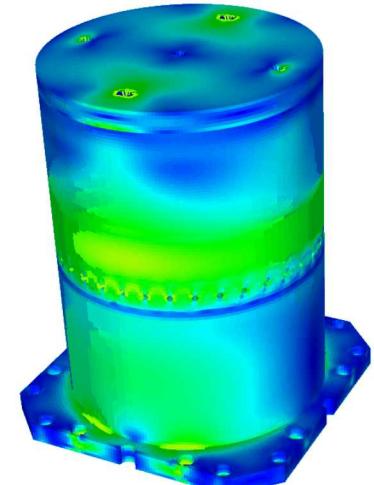
1 DOF X:



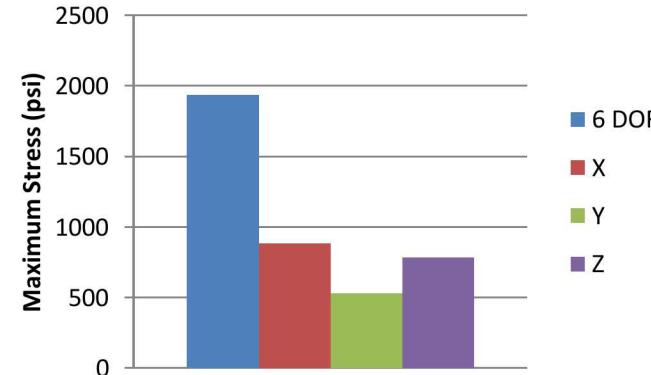
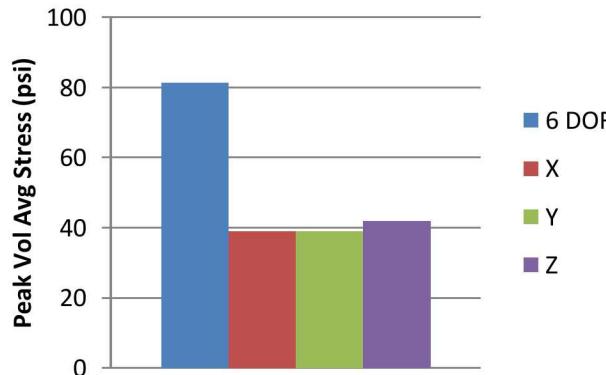
1 DOF Y:



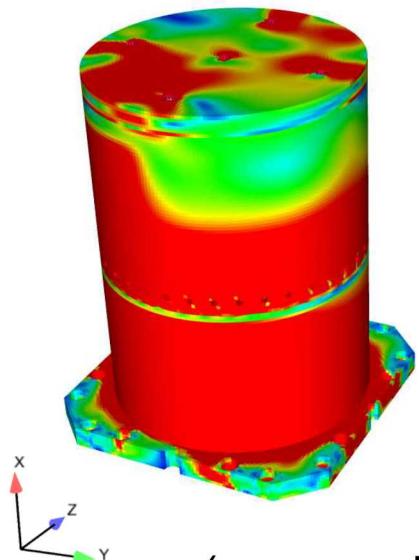
1 DOF Z:



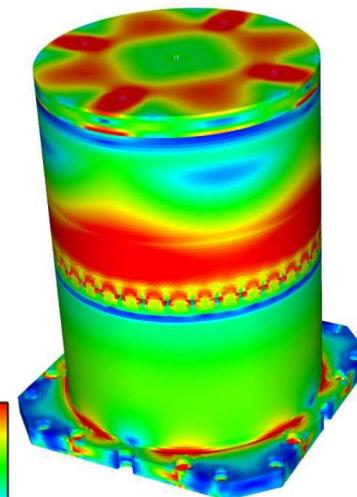
1 & 6 DOF Shock: Stresses (2)



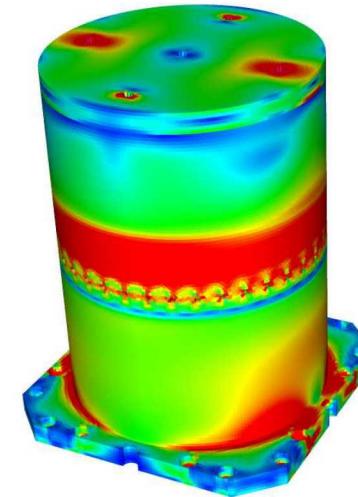
6 DOF:



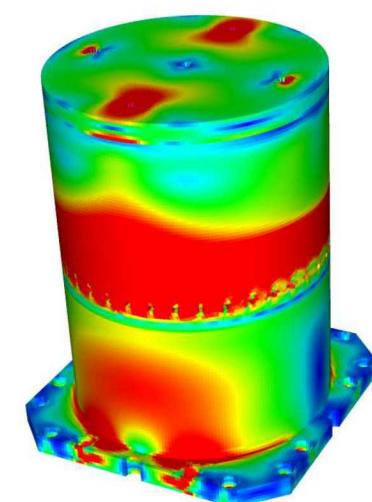
1 DOF X:



1 DOF Y:



1 DOF Z:

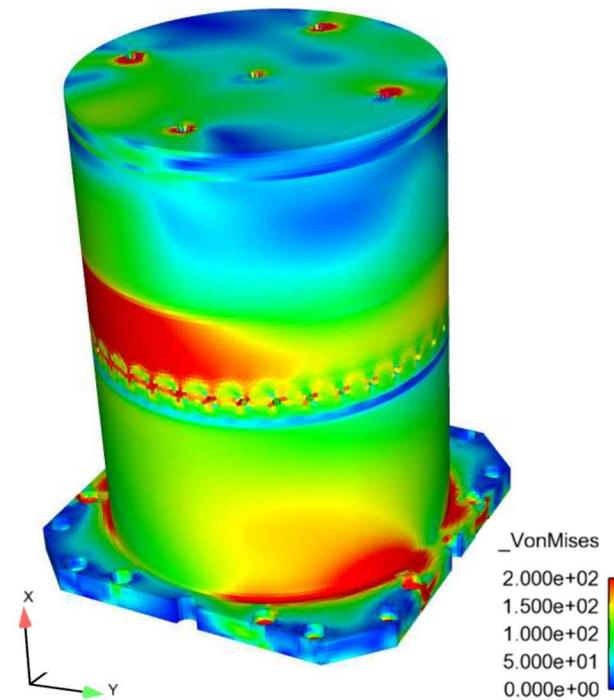


(same as last slide, contours rescaled to lower stress value)

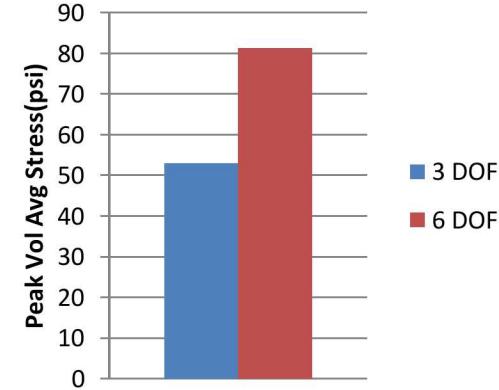
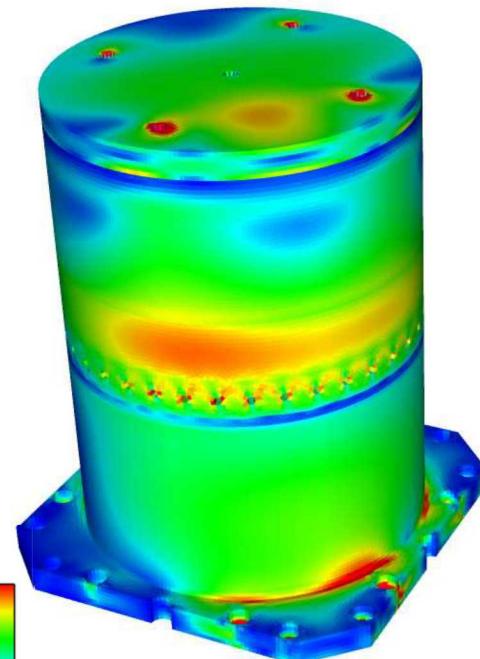
3 & 6 DOF Shock: Stresses

- Can we capture the fundamental input & response with 3 DOF inputs?
- How important are rotations? ... They can be very important

6 DOF:



3 DOF:
(translational)



$$\begin{bmatrix} N^i \\ V_2^i \\ V_3^i \\ T^i \\ M_2^i \\ M_3^i \end{bmatrix} = \begin{bmatrix} \frac{EA}{L} & 0 & 0 \\ 0 & \frac{12EI_3}{L^3} & 0 \\ 0 & 0 & \frac{12EI_2}{L^3} \end{bmatrix} \begin{bmatrix} u_1^i \\ u_2^i \\ u_3^i \\ \theta_1^i \\ \theta_2^i \\ \theta_3^i \end{bmatrix}$$

Conclusions

- 6 DOF testing affords new opportunities for testing
 - More representative, multi-axis test environments
 - More control over single-axis test inputs and associated cross-axis inputs
- 6 DOF analysis allows for greater insight to be obtained
 - Designing better 6 DOF tests, understanding relationships of input and stress
 - Better model validation through accurate characterization of inputs
 - Development of tools to integrate 6 DOF into analysis workflow
- Vibration
 - Compared cross-axis input levels and coherence of tests on 1 & 6 DOF shakers
 - Ongoing work to understand impact of off-axis control levels and coherence
- Shock
 - Compared a 6 DOF test spec to single-axis test specs
 - Examined impact of testing on stresses in a component
 - Rotational input can be very important