

**Sandia
National
Laboratories**

Deep Learning for Turbulence Modeling

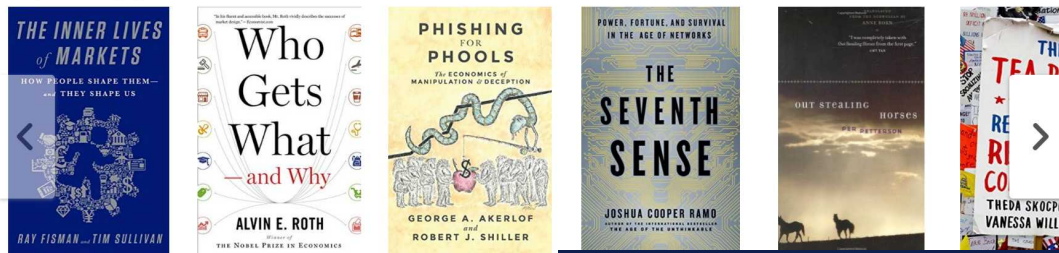
Julia Ling, Andrew Kurzawski, Jeremy Templeton

February 2017

What is Machine Learning?

- Data-driven algorithms to discern patterns and make predictions on big, high-dimensional data
- Linear regression, support vector machines, neural networks

Inspired by your Wish List [See more](#)



MOST EMAILED

MOST VIEWED

1. Julian Assange Repeat to U.S.
2. WNBA Players in Turmoil Rise in Terror
3. Alec Baldwin to host 'Saturday Night Live' on Feb. 11
4. Mark Zuckerberg, in Suit, Testifies in Oculus Intellectual Property Trial



amazonPrime
Original audio series



PANDORA

Classical

+ Create Station

0:12

-4:03

Now Playing

Music Feed

My Profile

Shuffle

Thumbprint Radio

K-Pop Radio

Naturally 7 Radio

Moby Radio

Israel 'IZ' Kamakawi...

Robert Johnson Radio

I Heard It Through Th...

Bliss N Eso Radio

Francis Cabrel Radio

Hip hop

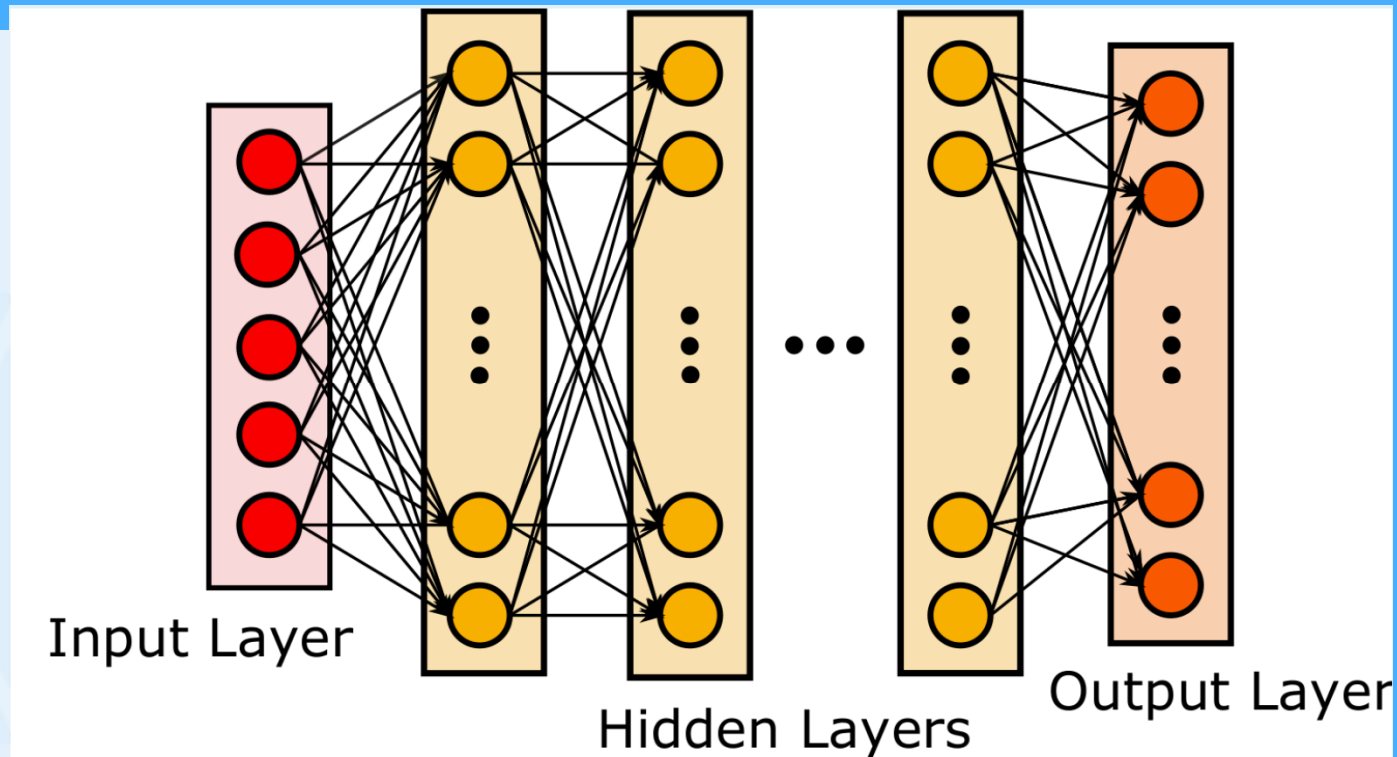
Electropop

Classical



Malena
by Yo-Yo Ma
on We All Love Ennio Morricone

Neural Networks and Deep Learning



$$y = f(w^T x)$$

Turbulence Simulations

- Many physical processes are inherently multi-scale and require constitutive models
- Growing interest in applying machine learning to constitutive modeling
- Leverage the massive data sets from high fidelity simulations and high-res experiments
- We present a method for using deep neural networks to learn a turbulence model



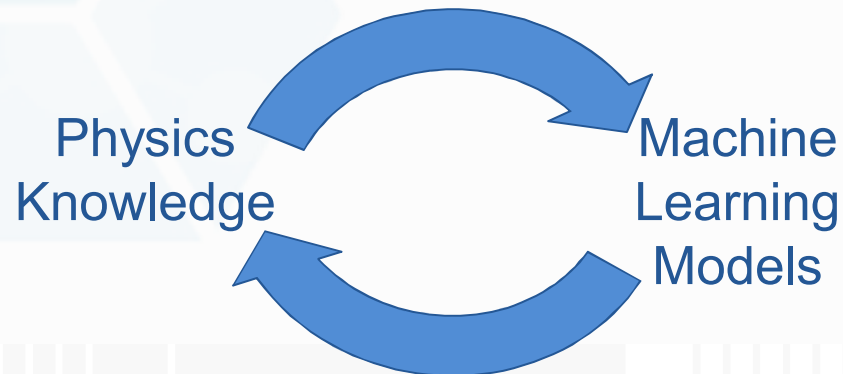
Hokusai (c 1830)



<http://www.windturbinesyndrome.com/2011/wind-turbine-turbulence-what-are-the-micro-climate-effects/>



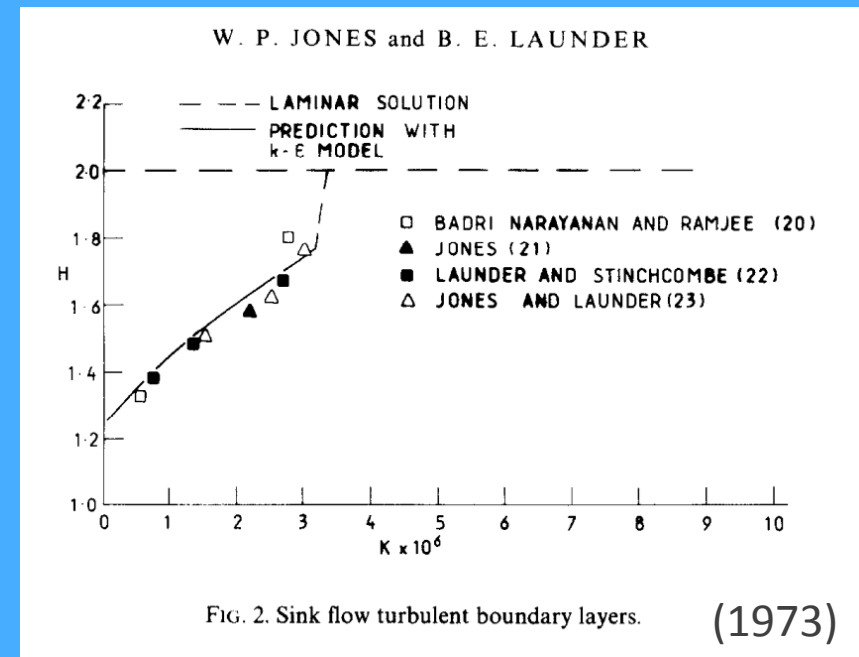
<https://brilliant.org/wiki/rocket-physics/>



Deep Learning for Turbulence Modeling



- In Reynolds Averaged Navier Stokes (RANS), use simplifying assumptions to get computational efficiency
 - Need model for unknown term: the Reynolds stress anisotropy tensor **A**
- Default model: Linear Eddy Viscosity Model
 - Based on theory + sparse experimental data
- Our approach: Deep neural network
- Inputs: Mean strain rate tensor **S**, mean rotation rate tensor **R**
- Outputs: Reynolds stress anisotropy **A**



Deep Learning for Turbulence Modeling



- Inputs: Tensors **S**, **R**
- Output: Tensor **A**
- Would like to enforce Galilean invariance
 - Invariance to inertial coordinate frame transformations

$$\mathbf{A}(\mathbf{Q}\mathbf{S}\mathbf{Q}^T, \mathbf{Q}\mathbf{R}\mathbf{Q}^T) = \mathbf{Q}\mathbf{A}(\mathbf{S}, \mathbf{R})\mathbf{Q}^T$$

- Borrow some ideas from group theory, representation theory
- All Galilean invariant tensors that are a function of **S** and **R** lie on a tensor basis: the *integrity basis* of **S** and **R** for the orthogonal group

$$\mathbf{A} = \sum_{n=1}^{10} f^{(n)} \mathbf{B}^{(n)}$$

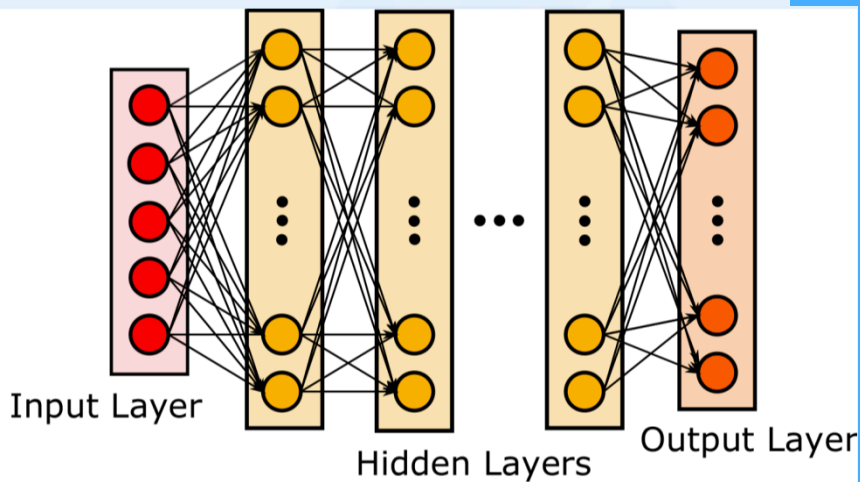
Unknown
coefficients

Known Tensor Basis

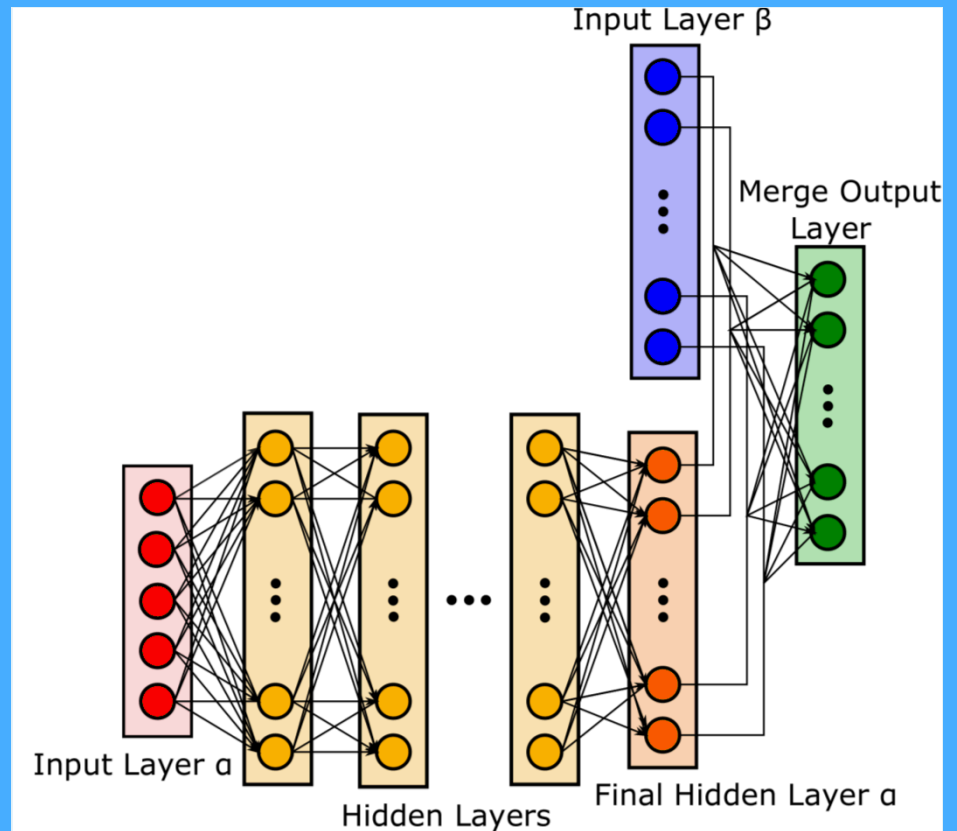
Embedding Galilean Invariance



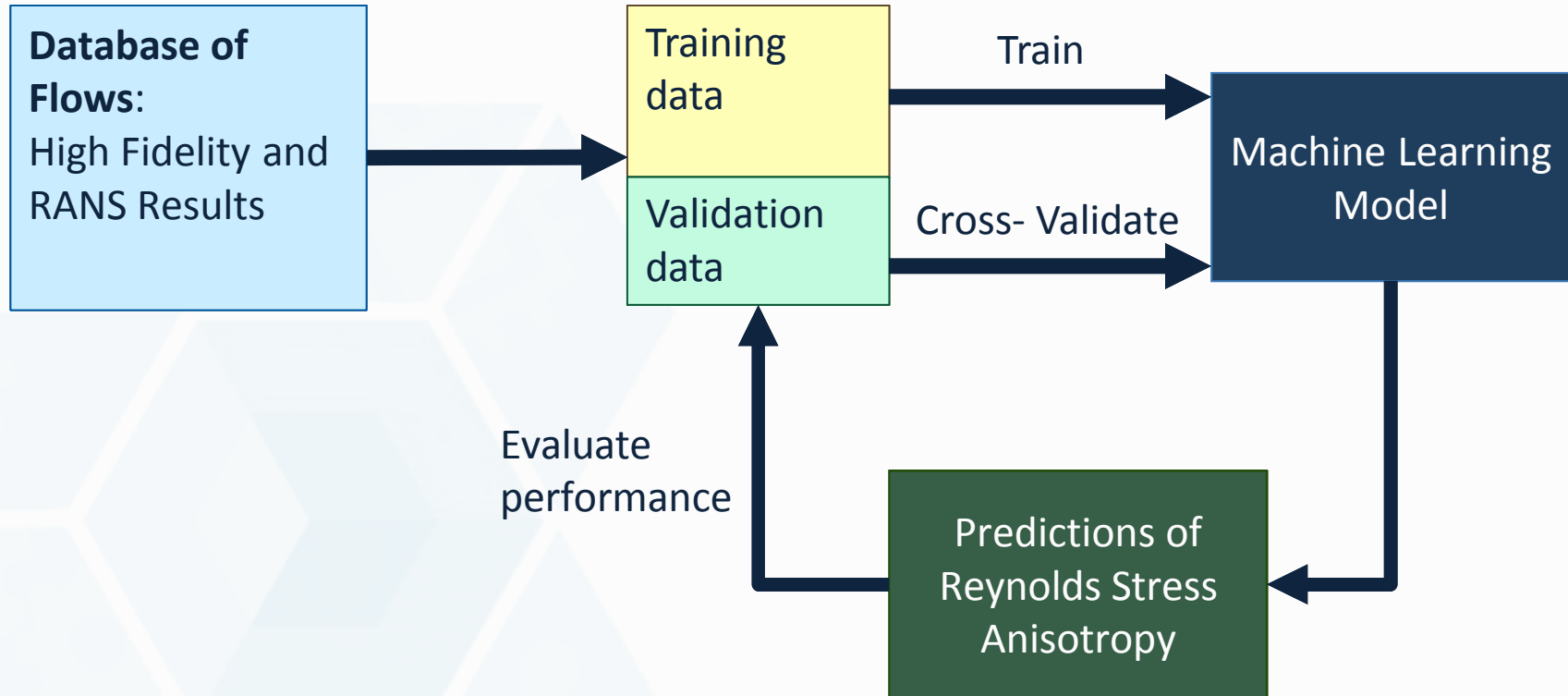
Multi-Layer Perceptron (MLP)



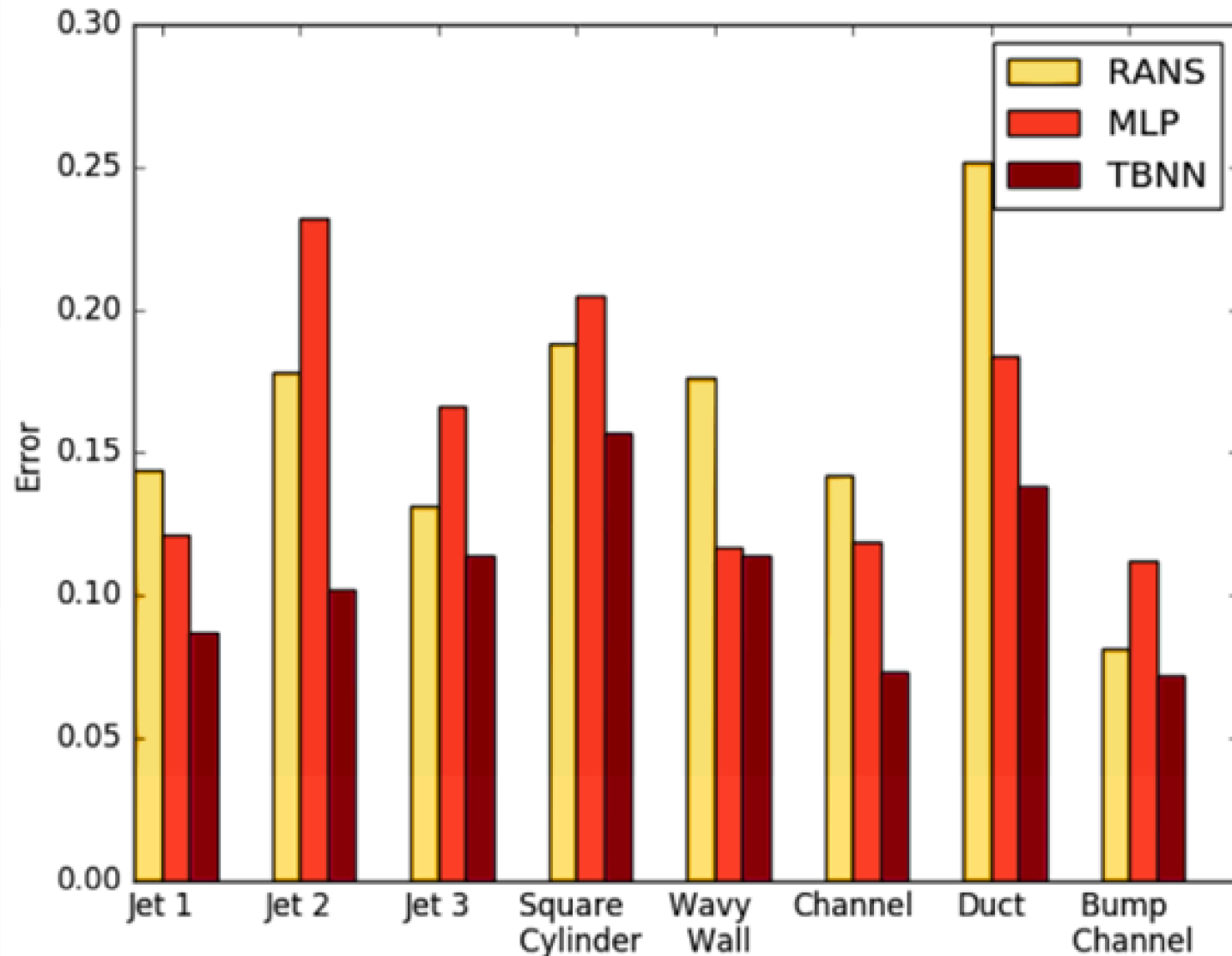
Tensor Basis Neural Network (TBNN)



Model Development



Deep Learning for Turbulence Modeling

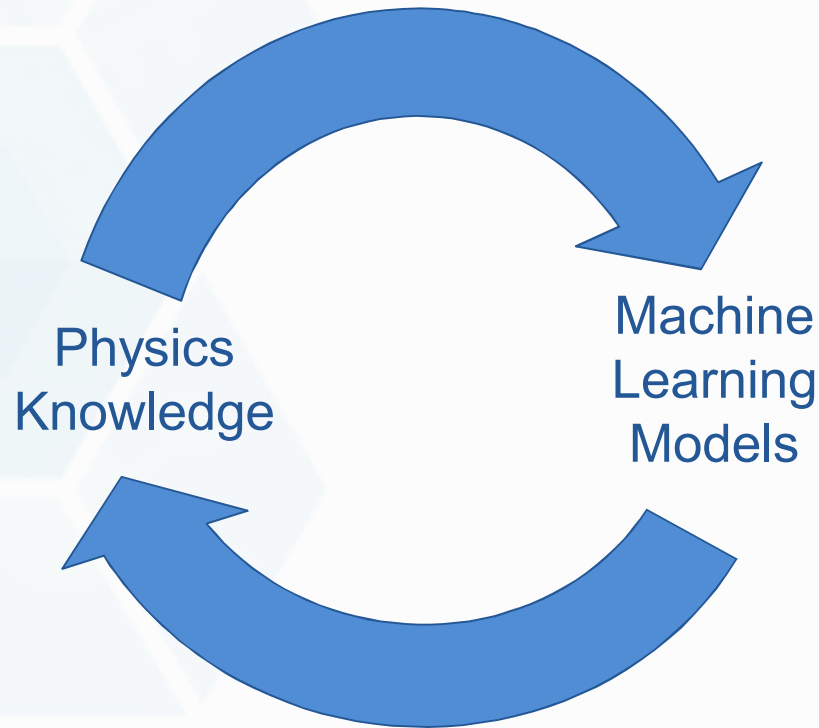


Conclusions

- Developed network architecture to embed known tensor invariance property
- Demonstrated significant improvement over conventional eddy viscosity models, at orders of magnitude lower computational cost than DNS
- First application of deep learning to RANS turbulence modeling

Machine Learning on Physics Systems

Directly embedding scientific domain knowledge into machine learning models can give improved performance, especially in data-limited scenarios



References

- J. Ling, A. Kurzawski, and J. Templeton, “Reynolds Averaged Turbulence Modeling using Deep Neural Networks with Embedded Invariance,” *Journal of Fluid Mechanics*, (2016).
- J. Ling and J. Templeton, “Evaluation of machine learning algorithms for prediction of regions of high Reynolds averaged Navier Stokes uncertainty,” *Physics of Fluids*, (2015).
- J. Ling, A. Ruiz, G. Lacaze, and J. Oefelein, “Uncertainty analysis and data-driven model advances for a Jet-in-Crossflow,” *Journal of Turbomachinery*, (2016).
- J. Ling, R. Jones, and J. Templeton, “Machine Learning Strategies for Systems with Invariance Properties,” *J. Comp. Phys.*, (2016).

Questions?

