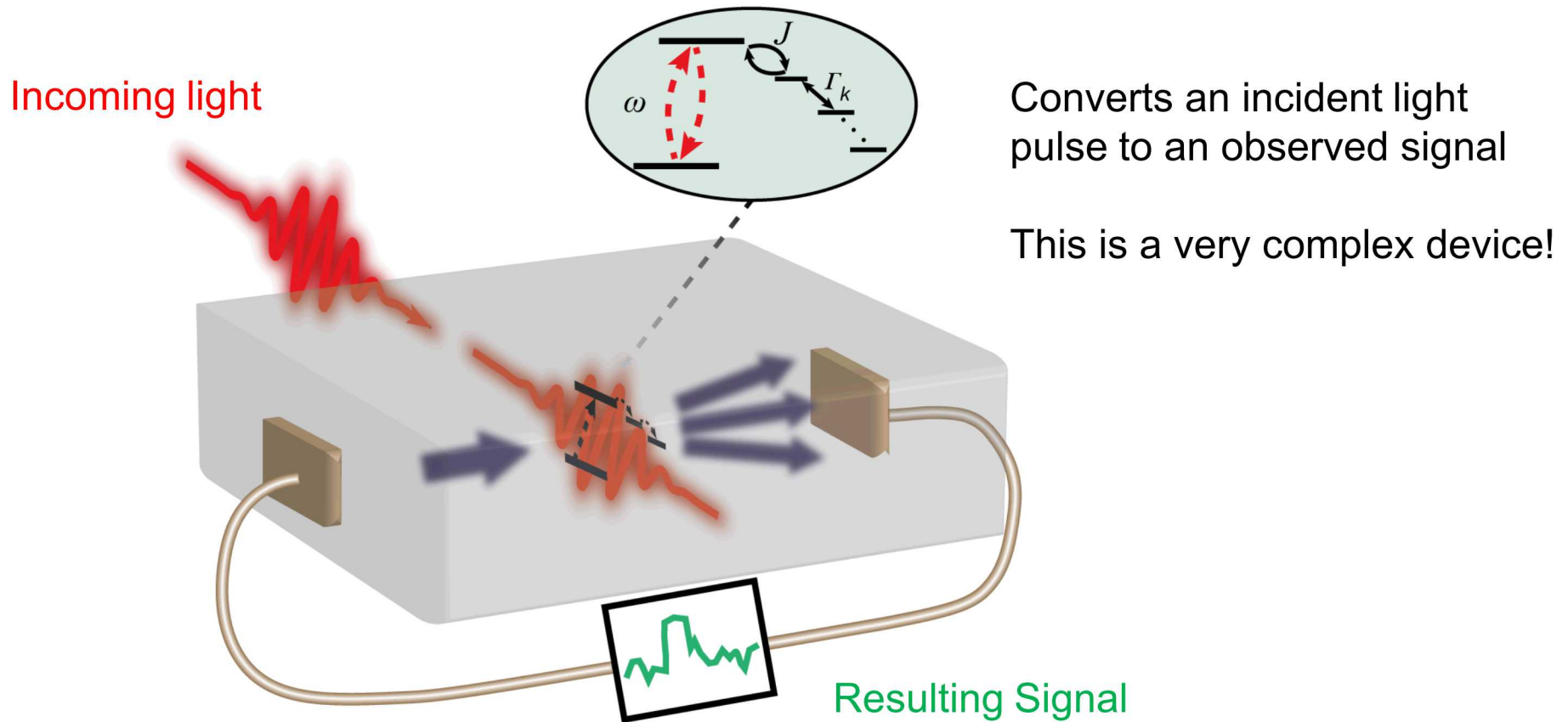


Fundamental Limits to Single-Photon Detection Determined by Quantum Coherence and Backaction

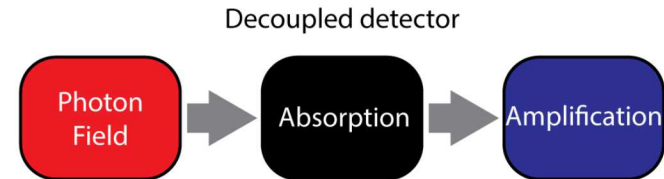
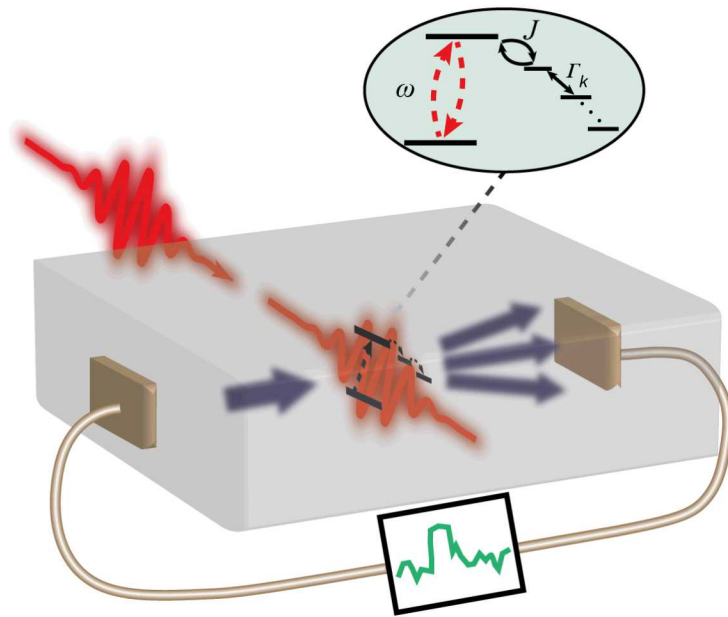
Steve Young
Mohan Sarovar
François Léonard

A General Photodetector



We will treat the simplest representative cases to understand the core tradeoffs

A General Photodetector

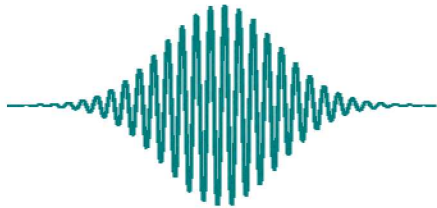


Conventional treatments assume timescale separation of detection stages

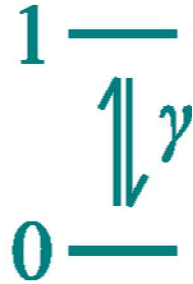
We want to treat as much as possible quantum mechanically, including the impact of amplification; ie, backaction from the measurement process

We will use an open quantum systems formalism that includes a quantized EM field

Isolated System



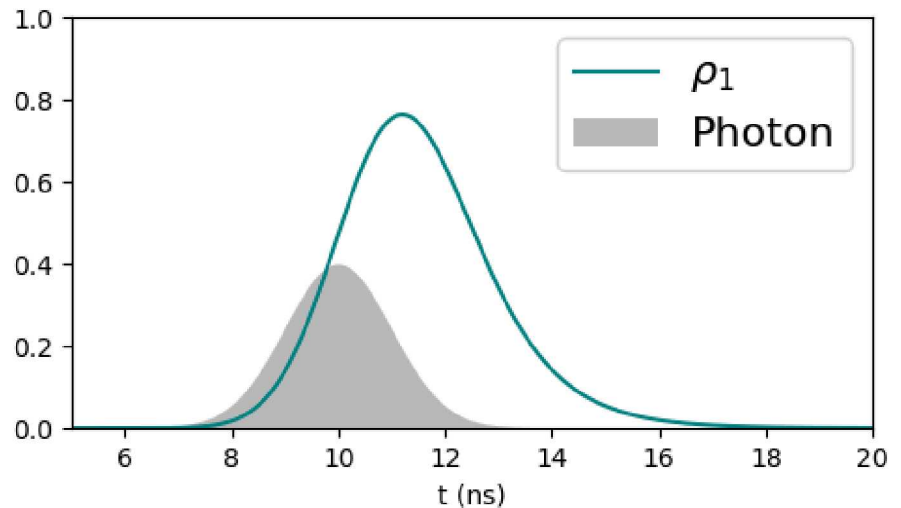
1 Photon



- Single photon, 1ns width Gaussian wavepacket
- Two optically coupled states

How does *measuring* this excitation affect performance?

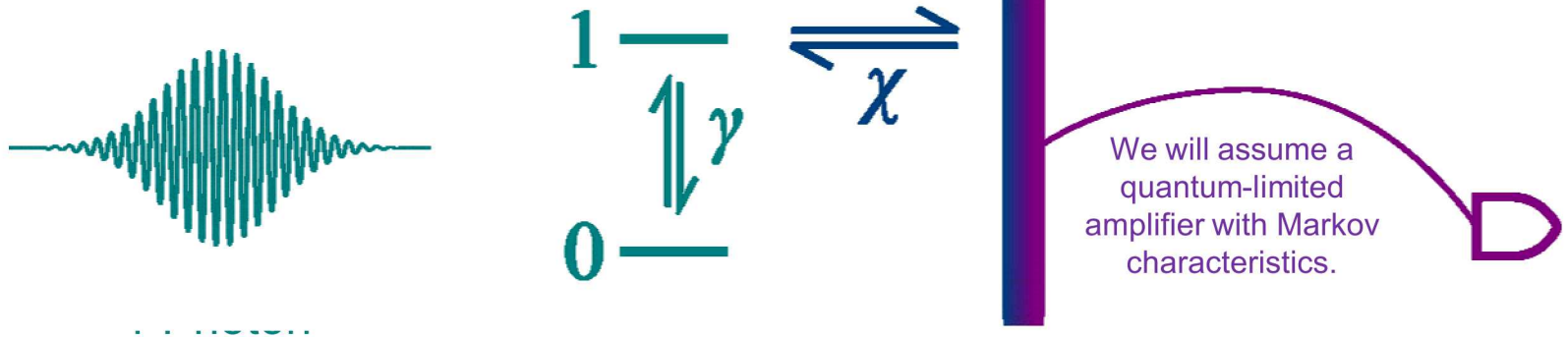
~80% excitation probability



Directly Measured System

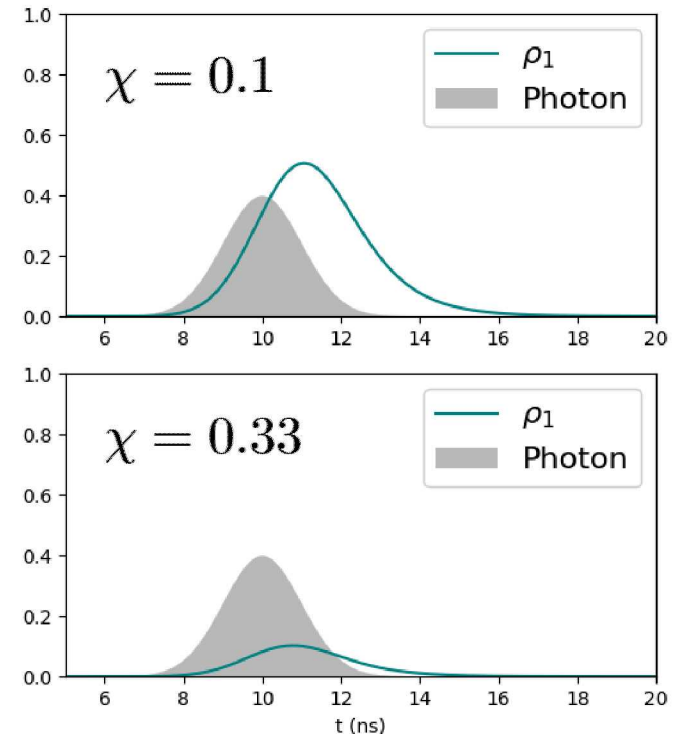
Quantum

Classical

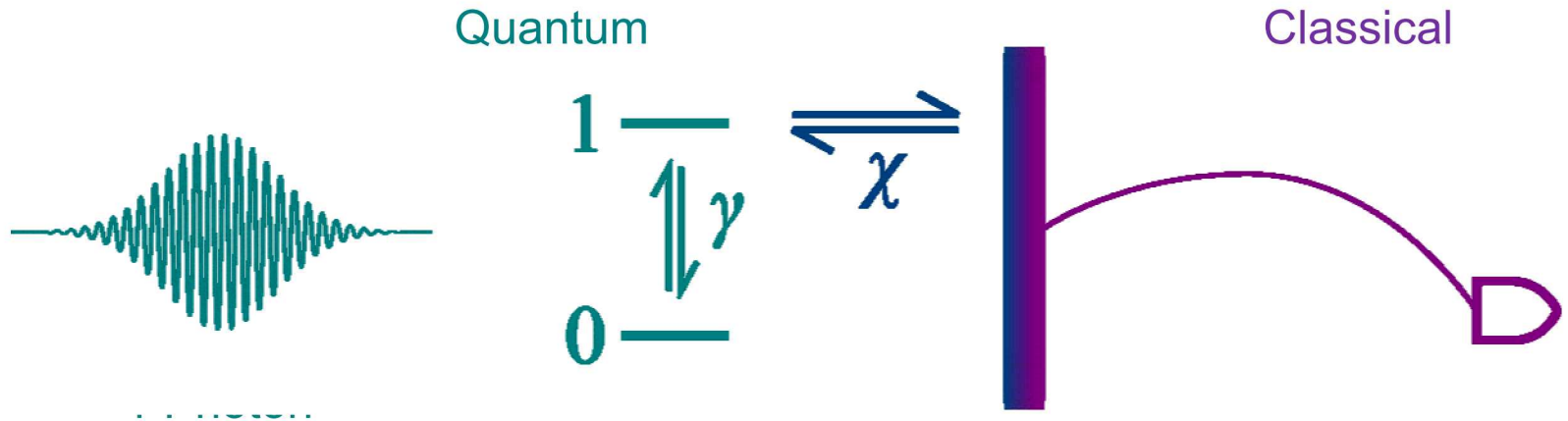


- Excited state coupled to bath whose classical state is monitored
- Excitation changes output reading
- Introduces **decoherence**
- Average excitation probability is reduced according to strength of coupling and signal amplification

**Amplification (measurement)
backaction limits performance**



Directly Amplified System



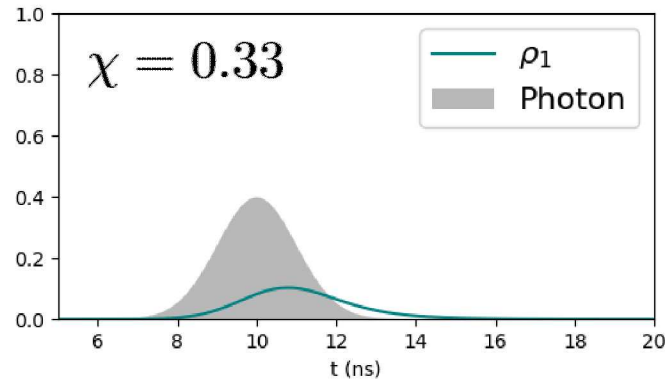
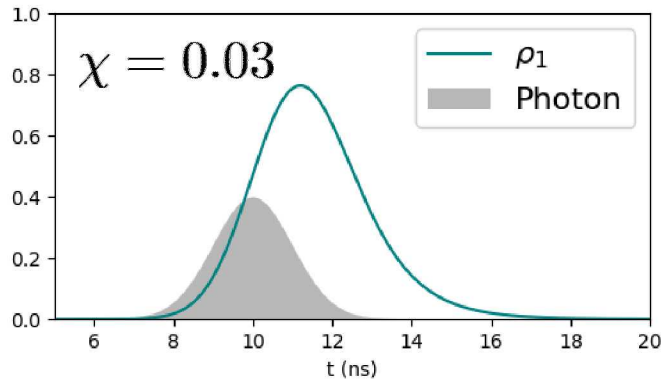
What about modeling *actual measurements*, not just averages?

- Simulate individual events
- Dynamics are conditioned on the measured current
- Obtain measured current as well as excitation population
- Amplification introduces intrinsic noise

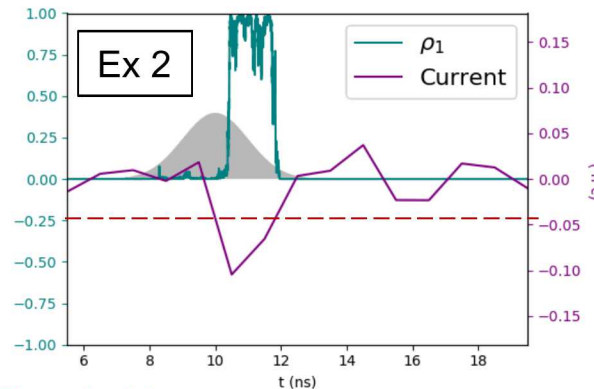
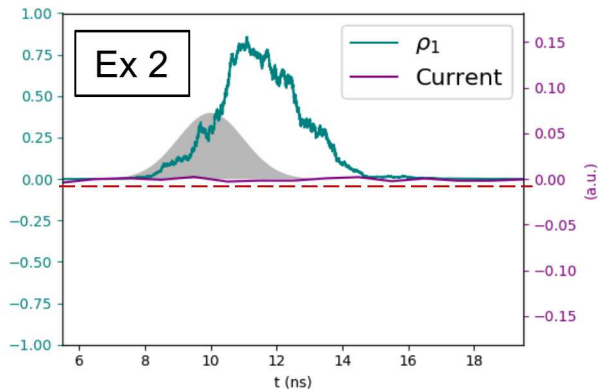
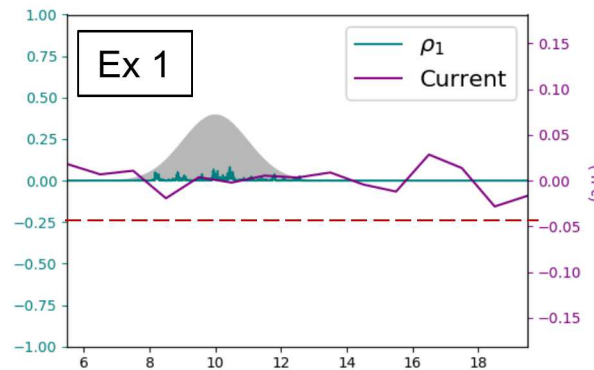
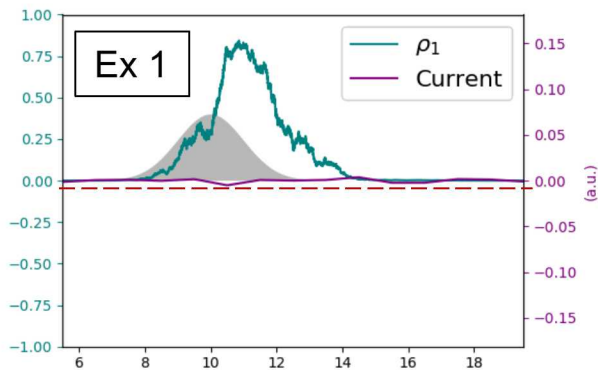
$$I_t = \int_t^{t+t_m} \chi^2 \rho_1(t') dt' + \frac{\chi}{2} dW_t$$

A purple arrow points from the 'intrinsic noise' text in the list above to the stochastic term $\frac{\chi}{2} dW_t$ in the equation.

Directly Amplified System



Weaker amplification gives better average signal, but with a lot of noise



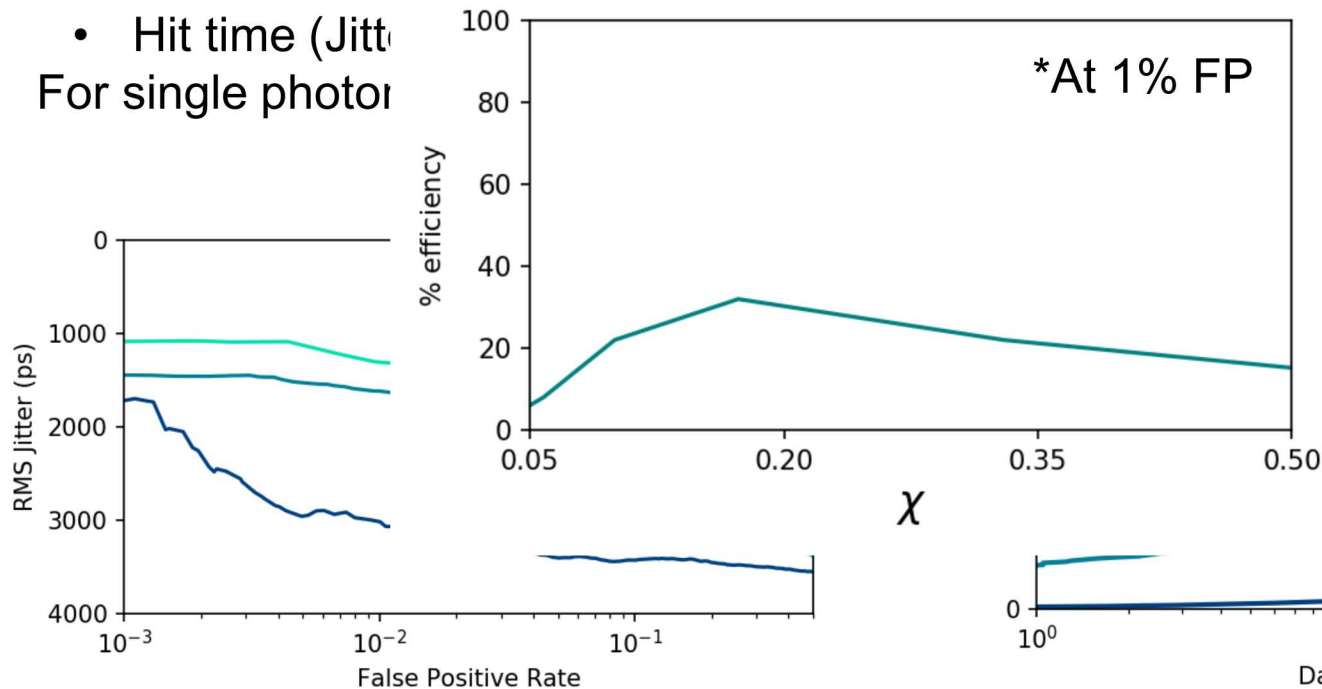
Stronger amplification yields a few recognizable hits

----- Hit Threshold

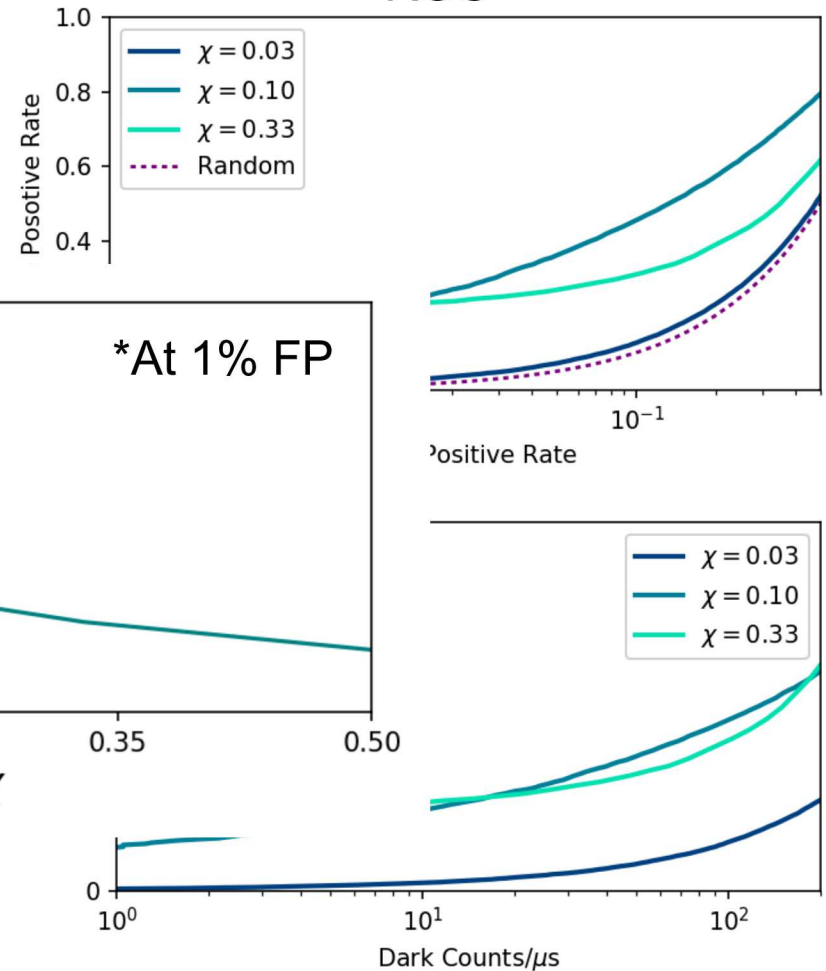
Directly Amplified System

Metrics

- Perform many runs
- Vary threshold for counting a hit
 - True Positive Rate (Efficiency)
 - False Positive Rate (Dark counts)
 - Hit time (Jitter)
- For single photon

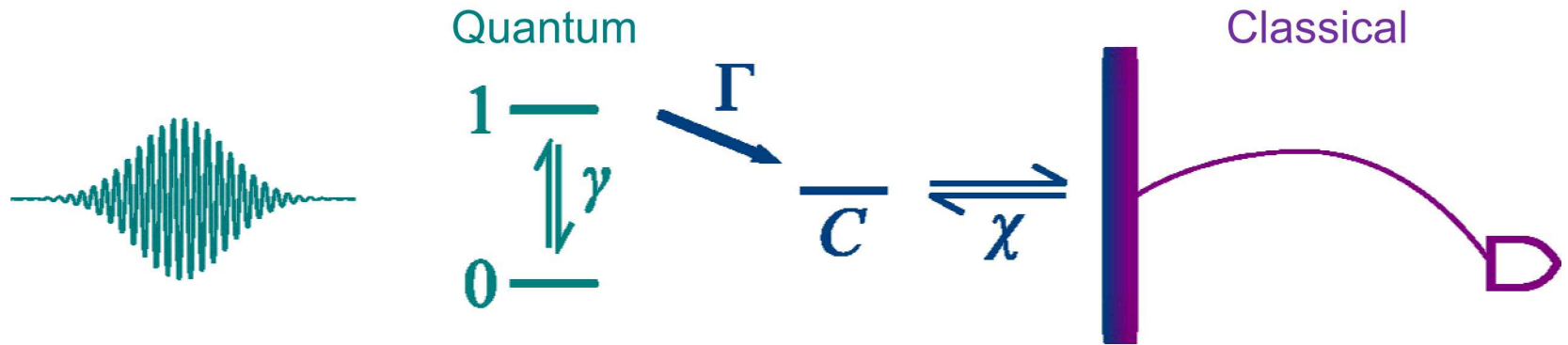


ROC



Direct amplification dramatically reduces performance

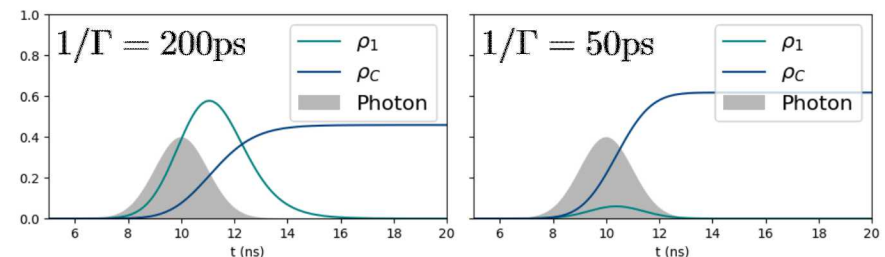
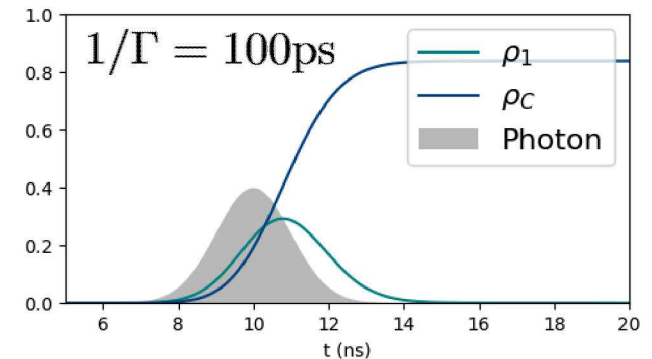
3-State System



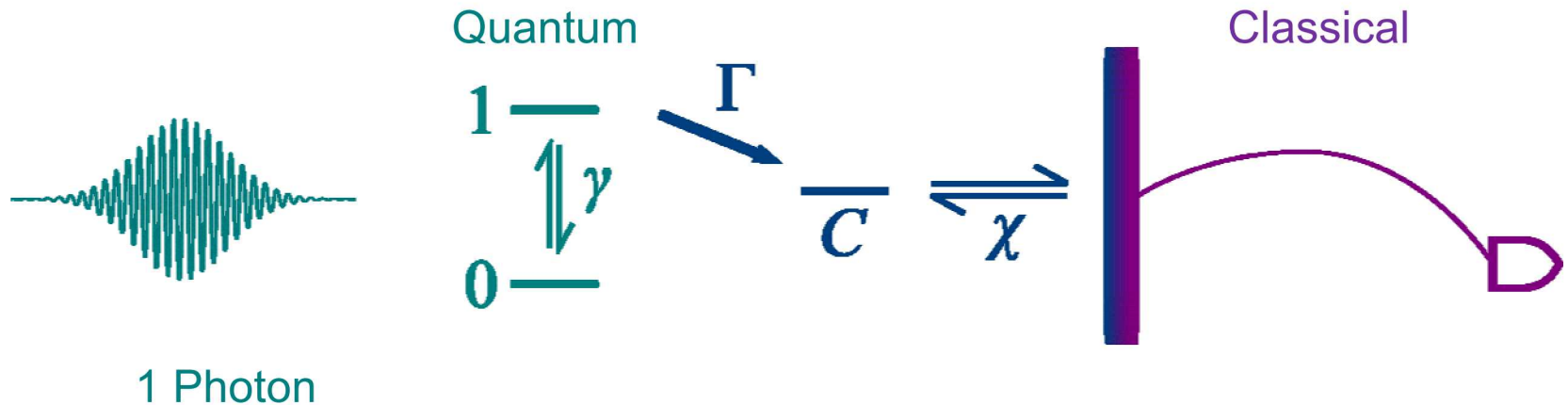
1 Photon

- Excited state relaxes to dark state coupled to bath whose classical state is monitored
- Average excitation is insensitive to amplification!
- Relaxation “protects” excitation but introduces **decoherence**
- Average excitation probability is reduced according to relaxation rate

Relaxation rate must be optimized for performance



3-State System

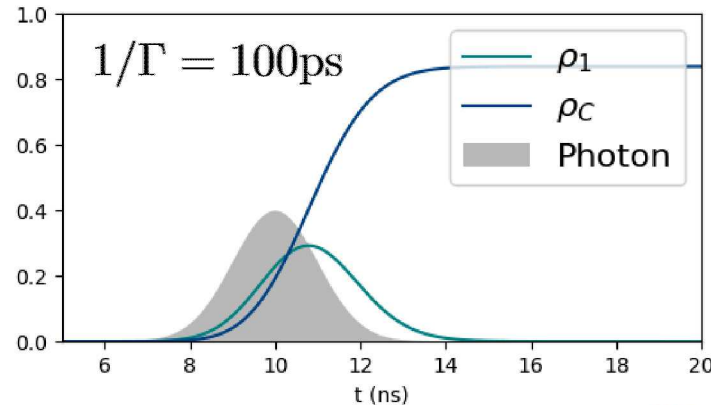


Modeling actual measurements

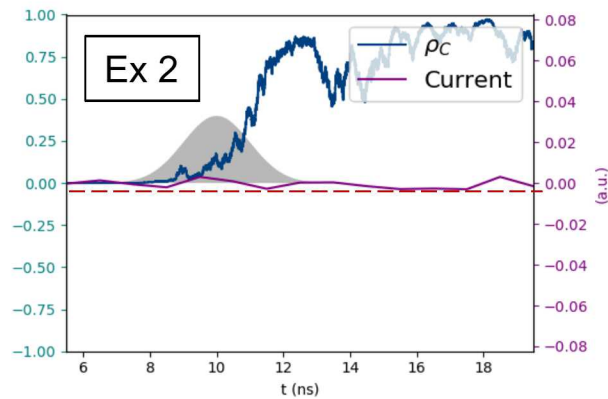
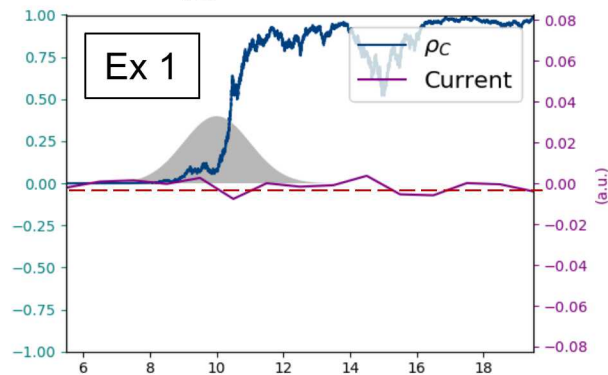
- Individual event dynamics *do* depend on amplification
- Must also still contend with noise

$$I_t = \int_t^{t+t_m} \chi^2 \rho_C(t') dt' + \frac{\chi}{2} dW_t$$

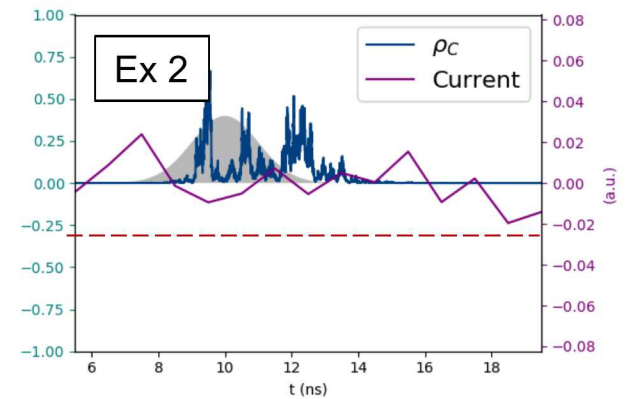
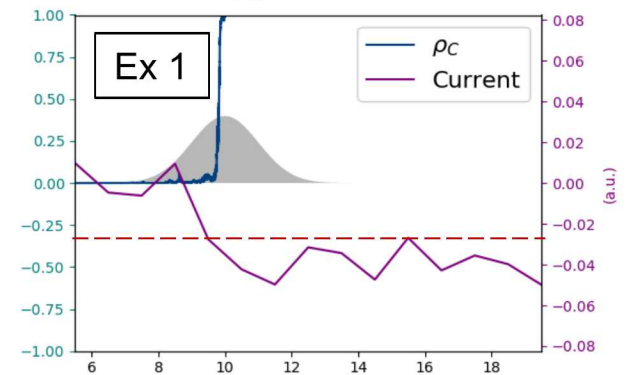
3-State System



$\chi = 0.05$



$\chi = 0.2$



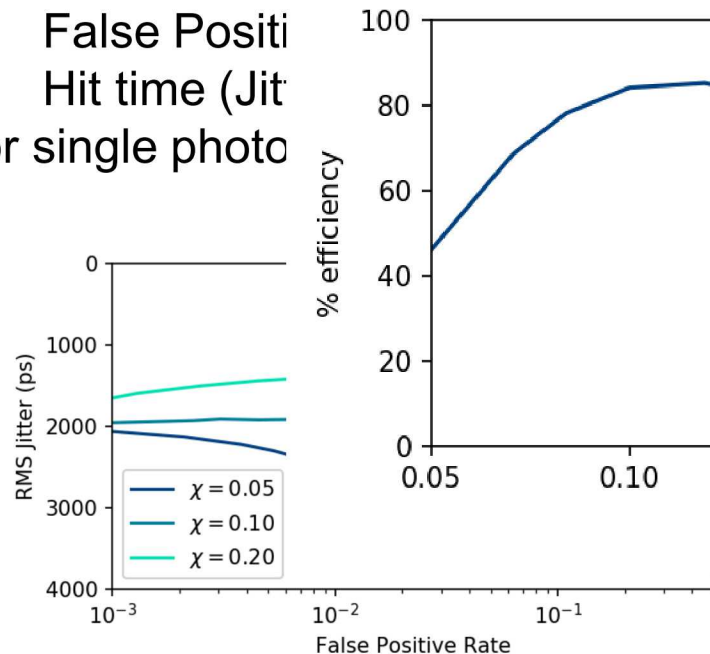
Long lifetime in C state yields more distinct signal

----- Hit Threshold

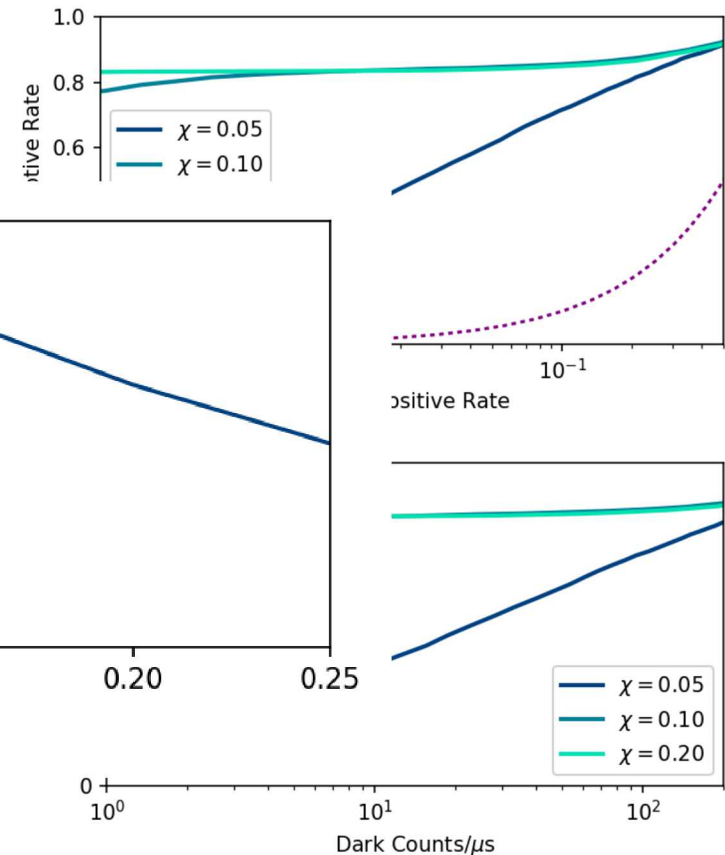
3-State System

Metrics

- Perform many runs
- Vary threshold for counting a hit
 - True Positive Rate (Efficiency)
 - False Positive Rate
 - Hit time (Jitter)
- For single photo



ROC



Intermediate state sidesteps negative impact of amplification on performance

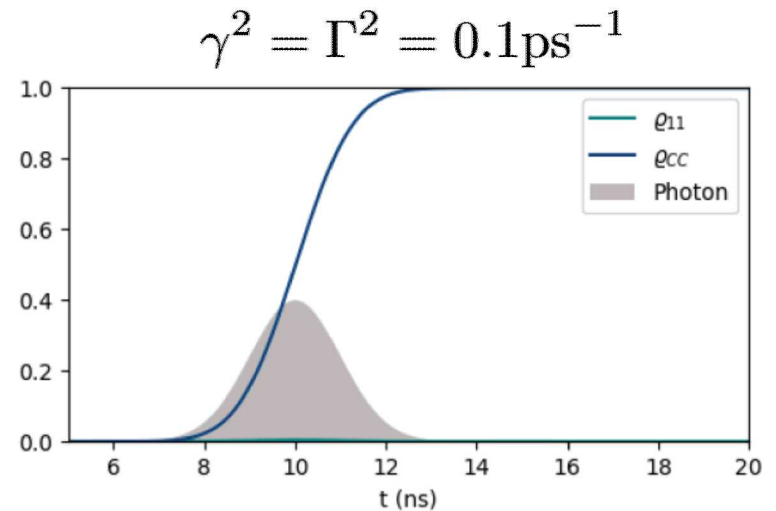
Ideal Detection

Simple two state system shows pulse shape and duration dependent performance
What about the monitored case?

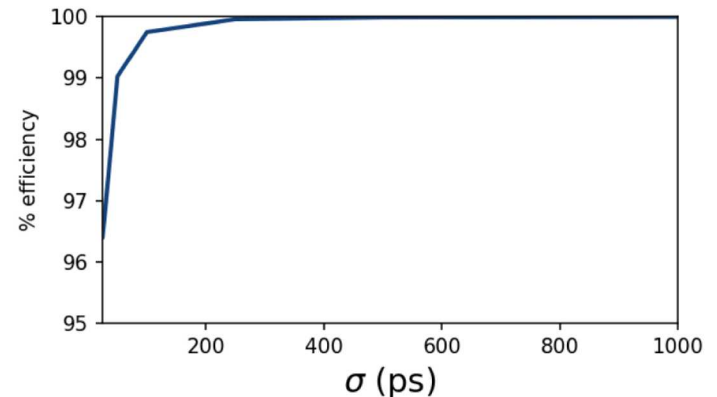
Suppose $\gamma^2 = \Gamma^2 \gg \frac{1}{\sigma_{\text{Pulse}}}$

When pulse is long compared to
excitation and relaxation rates,
detection efficiency approaches
unity!

Even much shorter pulses can be
detected efficiently



Average dynamics



Conclusions

- Can simulate fully quantum detection
- Generate detector metrics and quantify tradeoffs and limits
- We learn that:
 - Details of amplification matter
 - Detector can be tuned to minimize negative impact of amplification
- Ongoing work: Extend to more complicated systems, *e.g.*:
 - Multiple photons in pulse
 - Excitations into band

Acknowledgements

Sandia National Laboratories is a multimission laboratory managed and operated by National Technology and Engineering Solutions of Sandia, LLC., a wholly owned subsidiary of Honeywell International, Inc., for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-NA-0003525.

Work supported by the DARPA DETECT program