

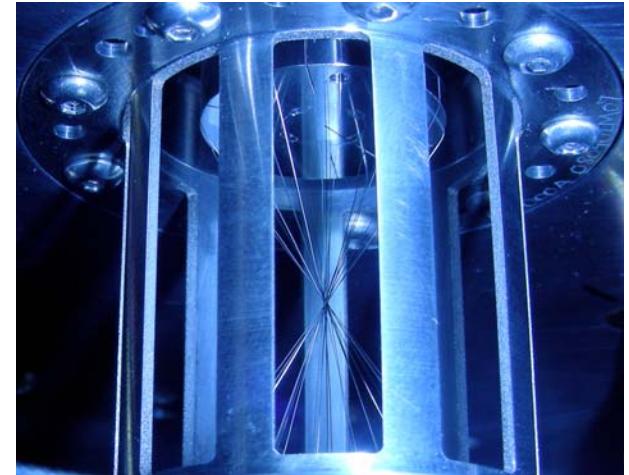


Wire Array Workshop April 6-9, 2009

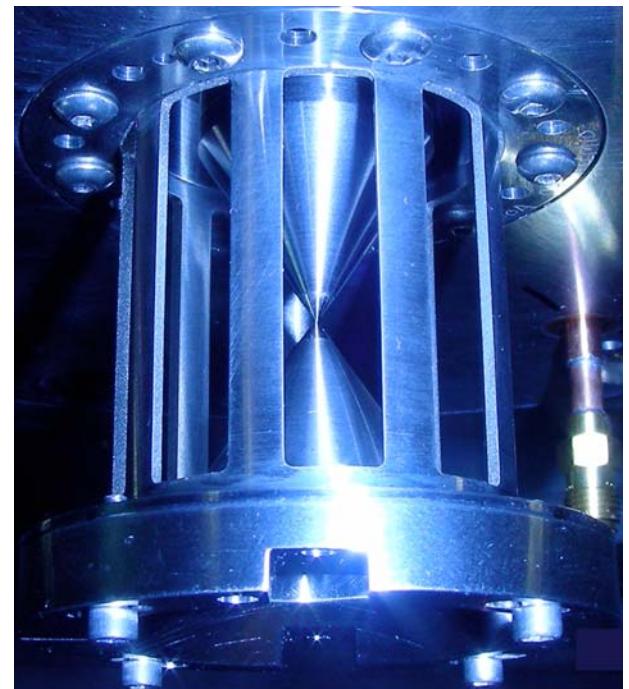
6 MA X-pinch Scaling Experiments

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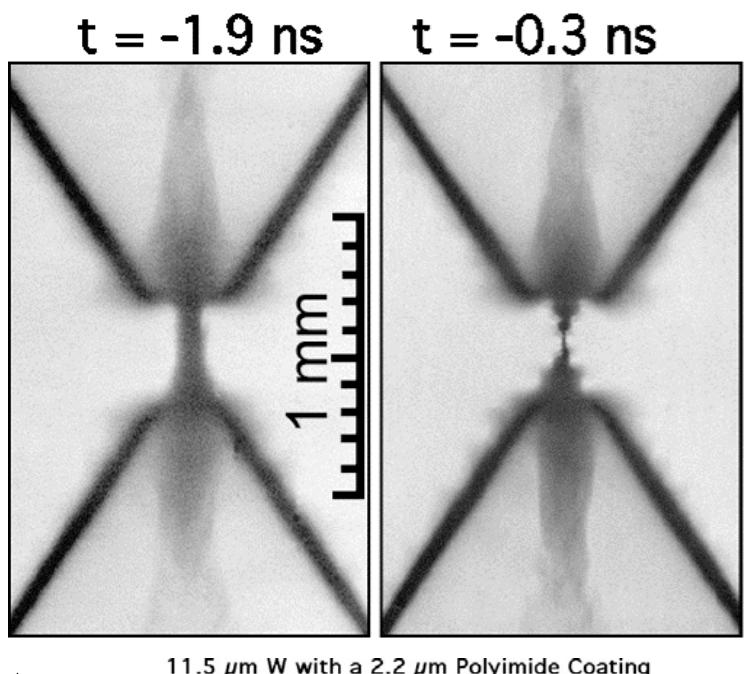




Why study X pinches?

Plasmas at 0.2 MA have extreme properties

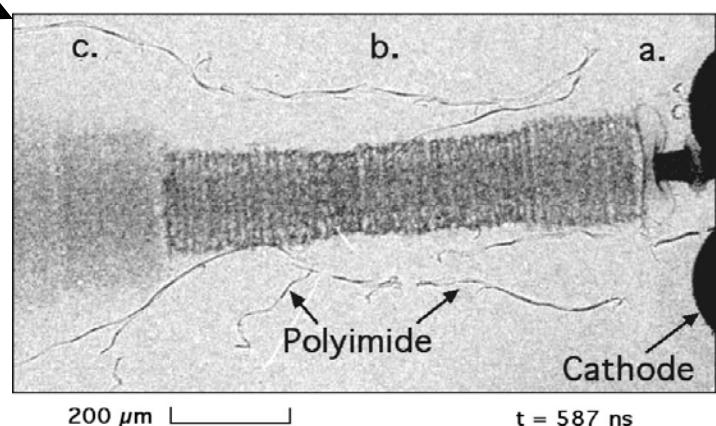
- Diameter: $1.2 \pm 0.5 \mu\text{m}$ ^a
- Duration: 10-100 ps^b
- T_e : ~1 keV (Ti^b, Mo^c)
- n_i : $\geq 0.1 * \text{Solid density}^{b,c}$
- Material pressure at ~1 g/cm³ & 1 keV is ~1 Gbar
- Magnetic pressure of 0.2 MA at 1 μm radius is ~1 Gbar
- Spot size, duration ideal for point-projection backlighting



^a B.M. Song *et al.*, Appl. Optics 44, 2349 (2005).
T.A. Shelkovenko *et al.*, RSI 72, 667 (2001).

^b S.A. Pikuz *et al.*, PRL 89, 035003 (2002).
D.B. Sinars *et al.*, JQSRT 78, 61 (2003).

^c S.B. Hansen *et al.*, PRE 70, 026402 (2004).

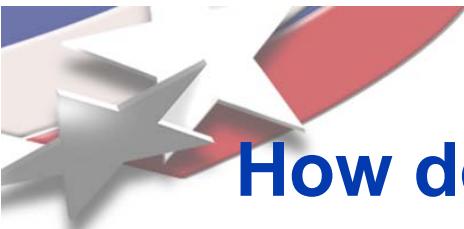




Why study >1 MA X pinches? Possibility of more extreme conditions

- 0.2 MA Mo X-pinch modeling reproduces observations[†]
 - Typical parameters: ~1 μm , ~2 keV, ~5 GW, ~2 ps
 - Model based on approximate Bennett equilibrium conditions and a balance between blackbody radiation and thermal heating
 - Axial mass flow leads to a collapse that is halted when the electron drift velocity exceeds the ion sound speed (critical line density)
- At 1 MA the model breaks down
 - Critical line density criterion: ~30 nm, 1290x solid density plasma
- Assume 100% of current collapses to a radius of 1 μm (Mo X pinch)
 - 1 MA: 80 GW (10x solid density)
 - 10 MA: 3.4 TW (250x solid density)

[†] Chittenden *et al.*, Phys. Rev. Lett. 98, 025003 (2007).



How do X-pinch parameters scale with I ? On-axis mass creates “different” scaling

- To scale a liner implosion self-similarly to different drive conditions, Π should be fixed*

$$\Pi = \frac{\mu_0 I^2 \tau^2}{4\pi m_l r^2} \quad \longrightarrow \quad m_l = \rho \pi r^2$$

$$\frac{I_1^2 \tau_1^2}{\rho_1 r_1^4} = \frac{I_2^2 \tau_2^2}{\rho_2 r_2^4}$$

- Unlike a wire array, we cannot effectively increase the density by increasing the number of wires in the array
- For a fixed density but increasing current, we must increase the diameter of the X-pinch neck
- Increase in radius decreases $J \times B$ pressure, so that mass/length increases ~linearly, not as I^2 as with arrays

* Ryutov, Derzon, & Matzen, Rev. Mod. Phys. 72, 167 (2000).



There are some practical issues with high-current X pinches

- **Mass/length is heavy!**

- 0.4 MA: 0.38 mg/cm
- 1.0 MA: 1.5 - 3.0 mg/cm*
- 6.0 MA: 9-18 mg/cm (I scaling)
108 mg/cm (I^2 scaling)
- 18 MA 20-mm wire array: 6 mg/cm



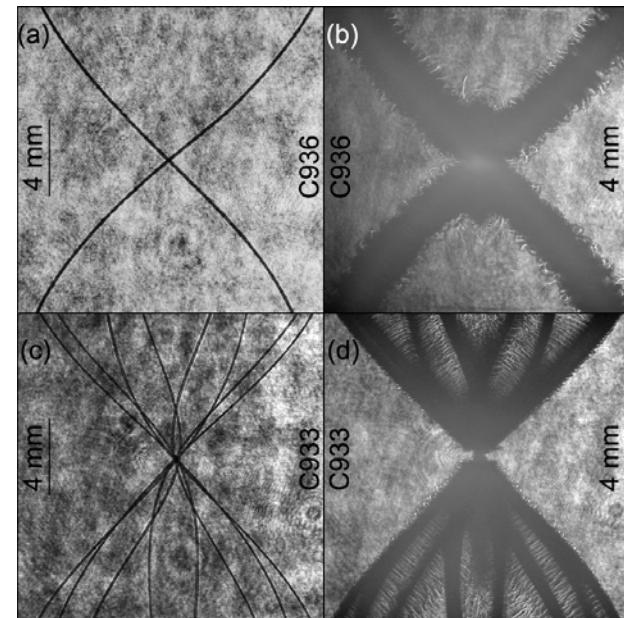
- **X-pinch configurations are complex**
(18 mg/cm; Tungsten)

- 256 x 22 μ m; 4 x 172 μ m; 1 x 345 μ m
- Large wire numbers “knotty”
- Large wire sizes bad?*



- **All materials are not equal**

- Mo, W, NiCr work well at 0.2 MA**
- Al, S.S. work poorly at 0.2 MA**



* D.B. Sinars *et al.*, Phys. Plasmas 15, 092703 (2008).

** S.A. Pikuz, private communication (2007).



We have tested X pinches in three different shot series on the 6 MA SATURN facility

- **Series 1 (April '08)**
 - Single-array X-pinch mass scan
 - Showed ~linear mass scaling with current from 1 MA
- **Series 2 (Sept. '08)**
 - Nested X-pinch scan
 - Solid X-pinch tests (W)
 - Best results from solid XPs (~17 μm sizes?)
- **Series 3 (March '09)**
 - “Better” solid X-pinch tests (W/Cu; Cu/Ni; Ni/Cr)
 - Focus of rest of this talk

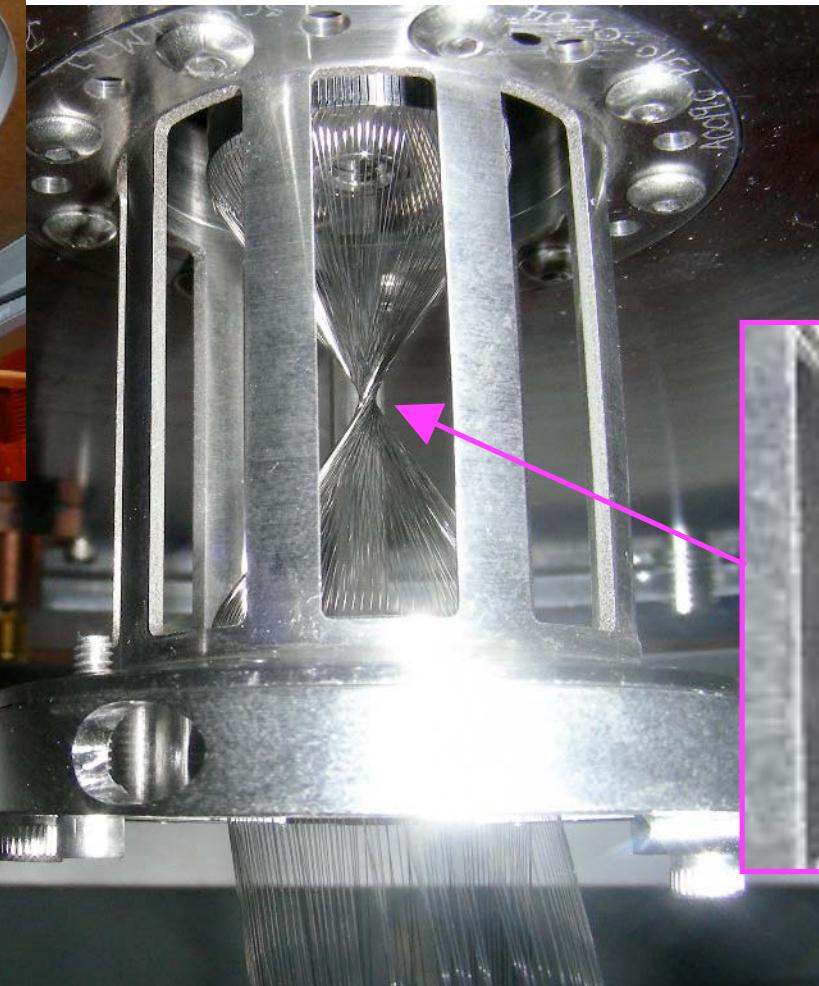
Primary goal of 1st three series: Identify a promising load geometry
Primary goal of next three series: Identify plasma parameters



High Wire-Number Single X Pinch (S3734)



128 x 75 μm W array

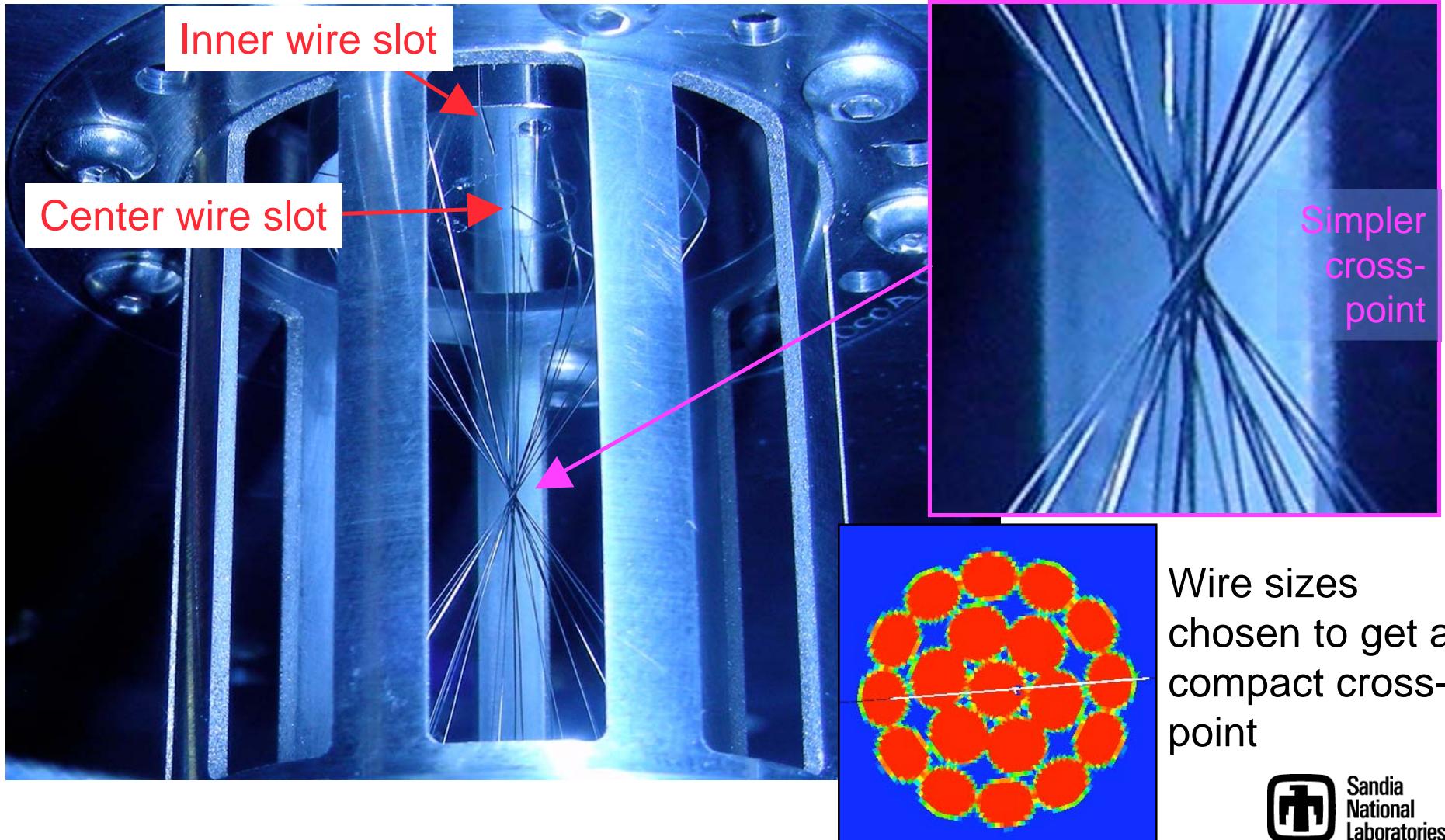


Large diameter W wires required extremely large weights to apply tension!

Extremely complex cross-point

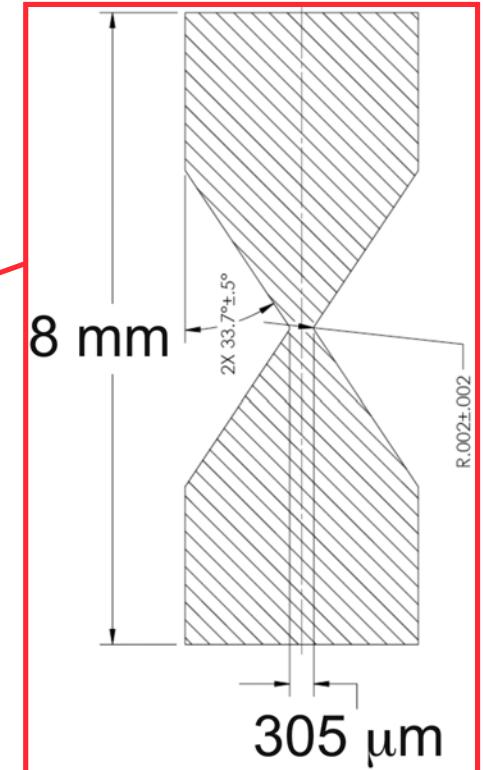
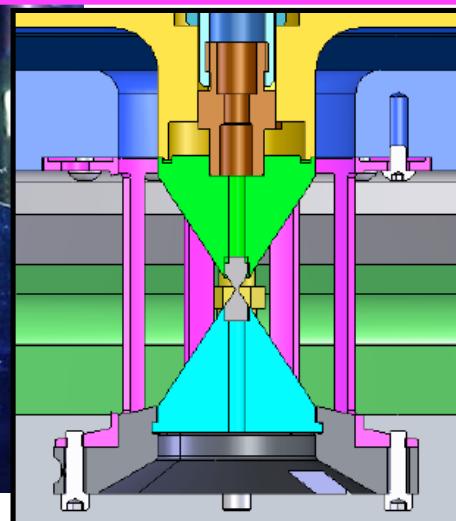
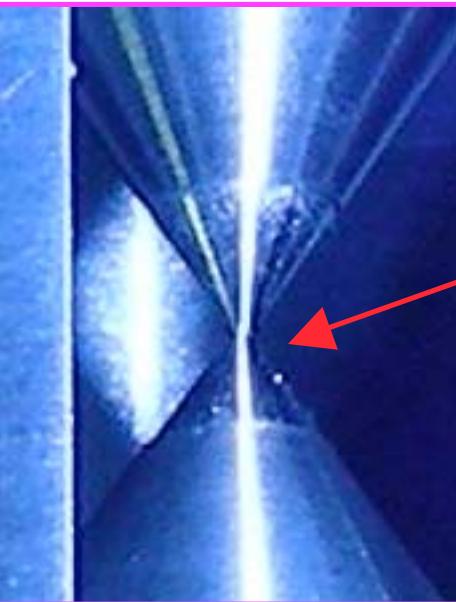
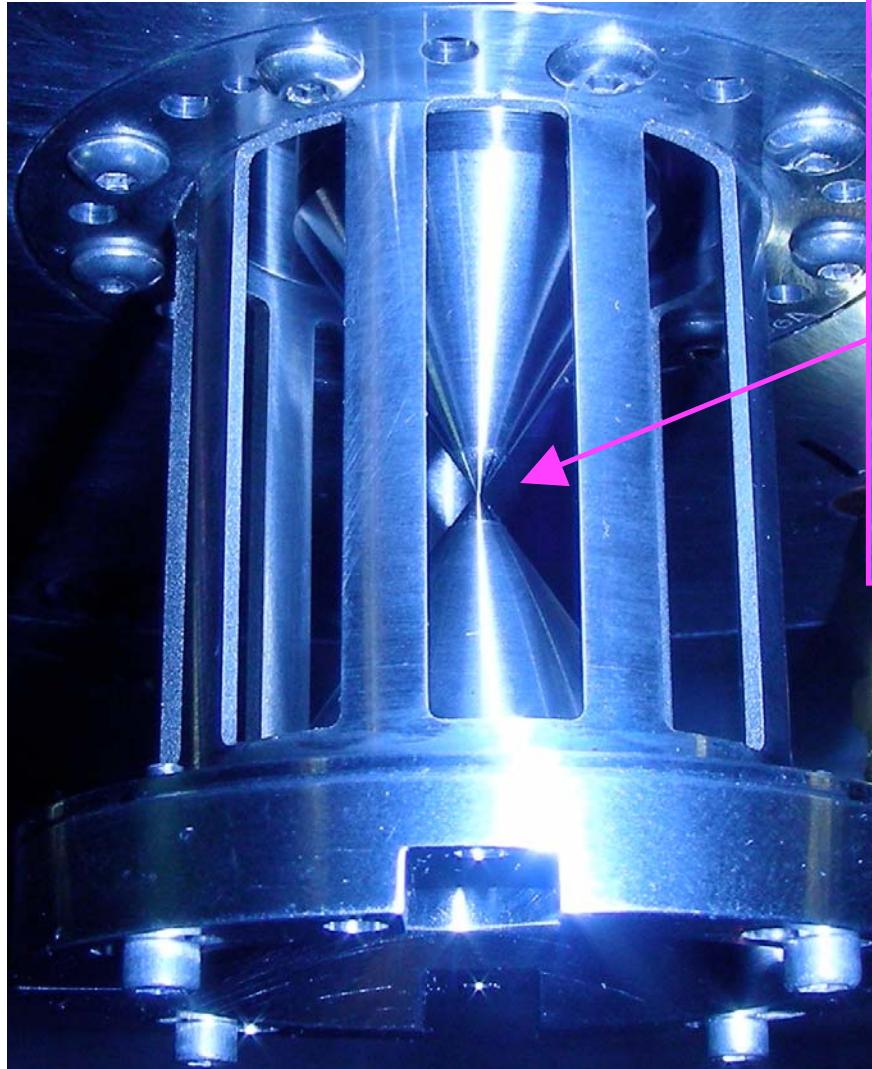


Nested Array X Pinch (S3767)





Solid X Pinch (S3769)

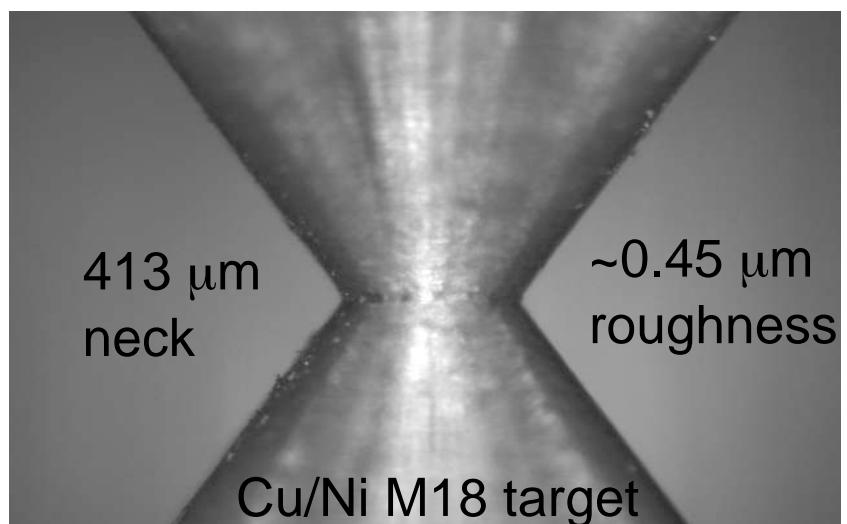
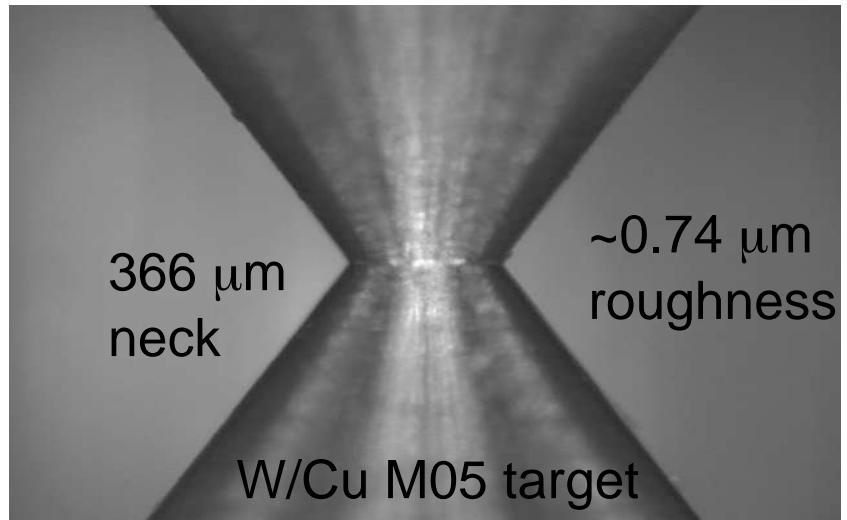
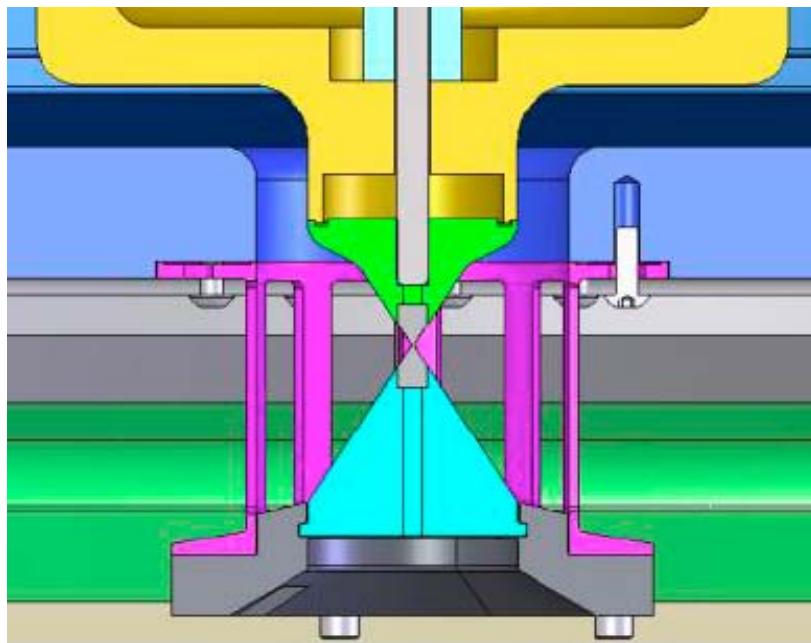


Load comprised of
3 W pieces;
Limiting case of
perfect cross-point



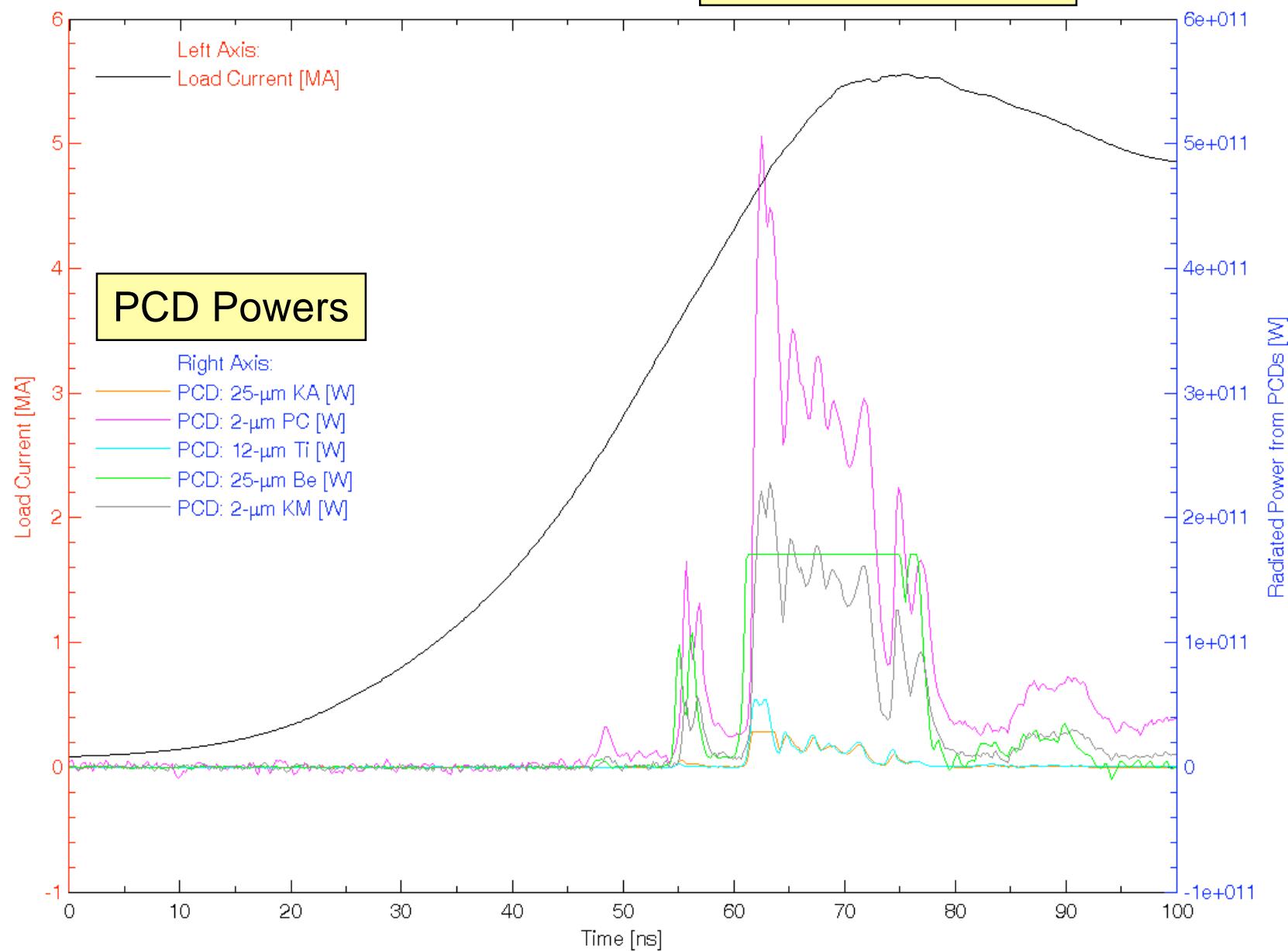
March 2009 solid X-pinch loads have showed the most promise so far....

- Highest radiation powers
- Characterized by multiple narrow x-ray bursts
- Smallest apparent hard x-ray source sizes



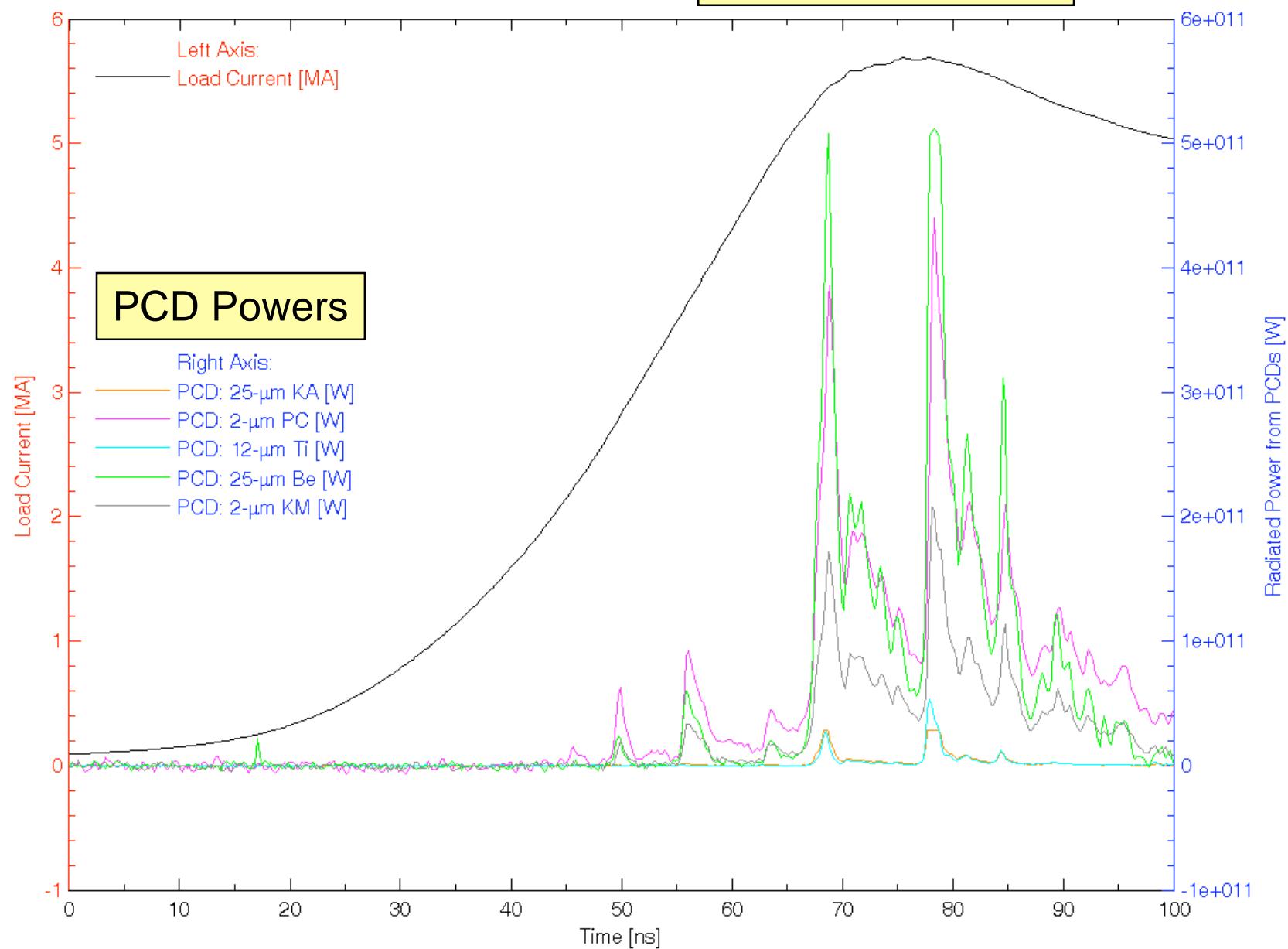
Saturn 3810

W72/Cu28 X pinch

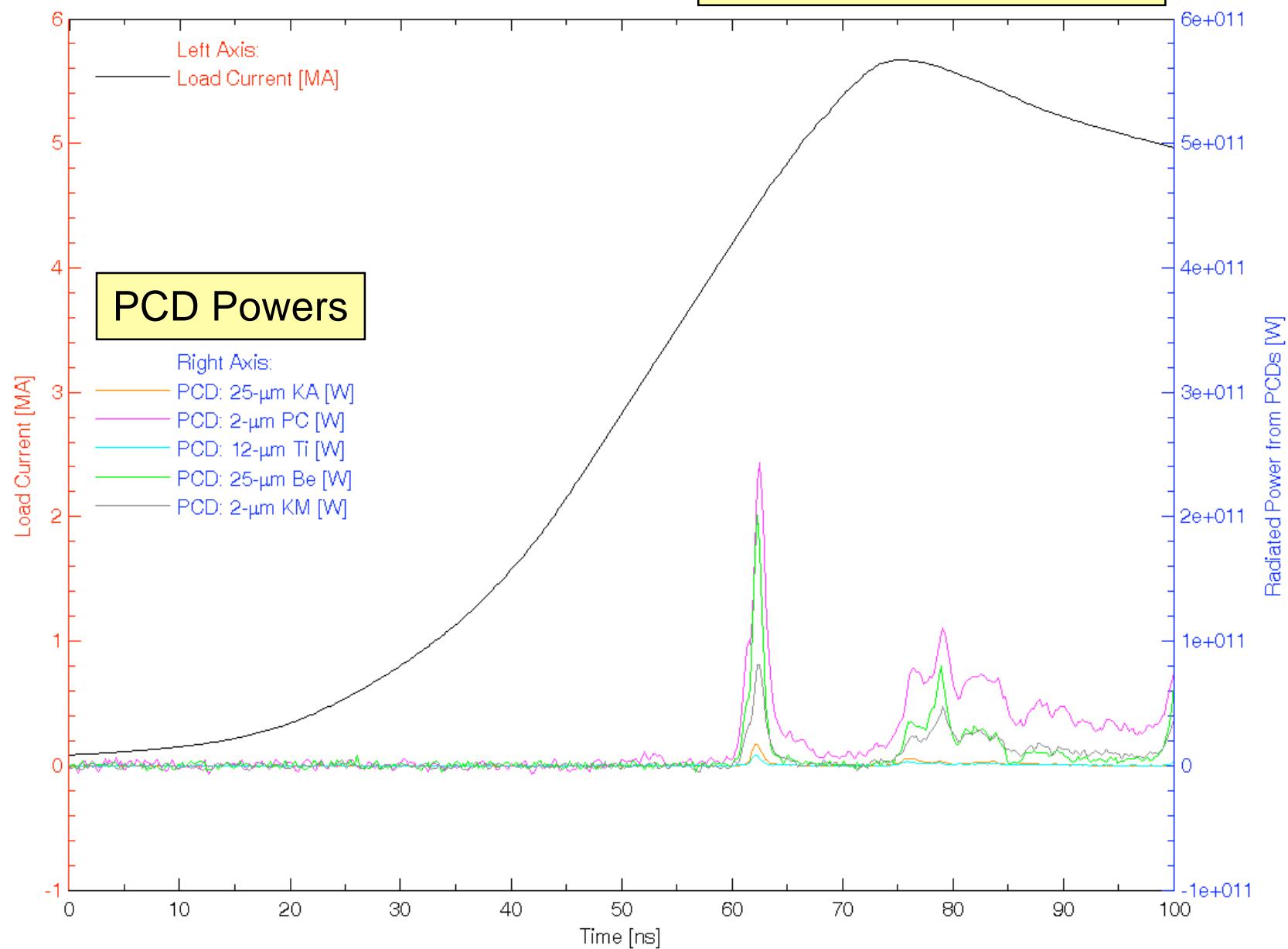


Saturn 3811

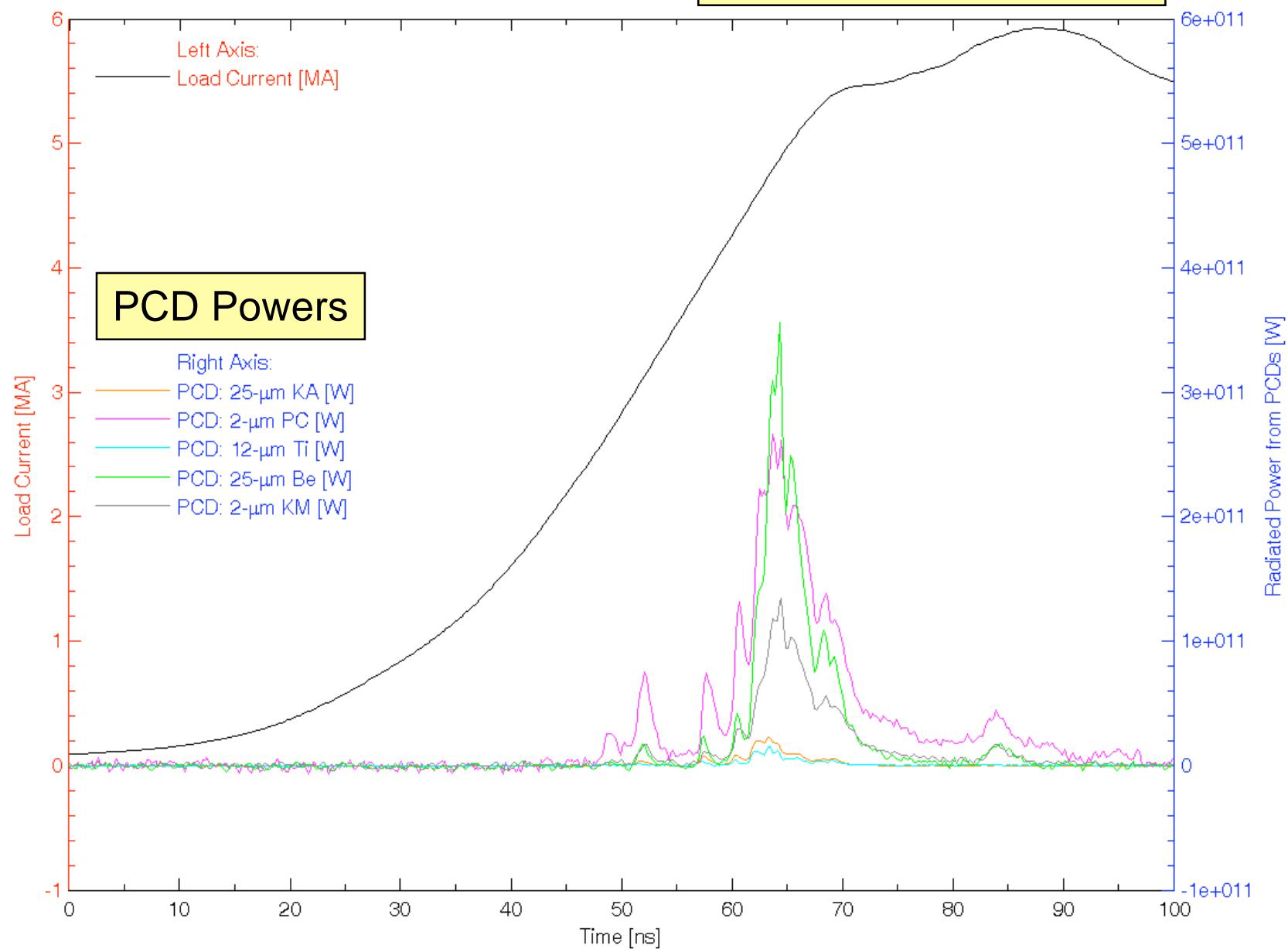
W72/Cu28 X pinch



Saturn 3812

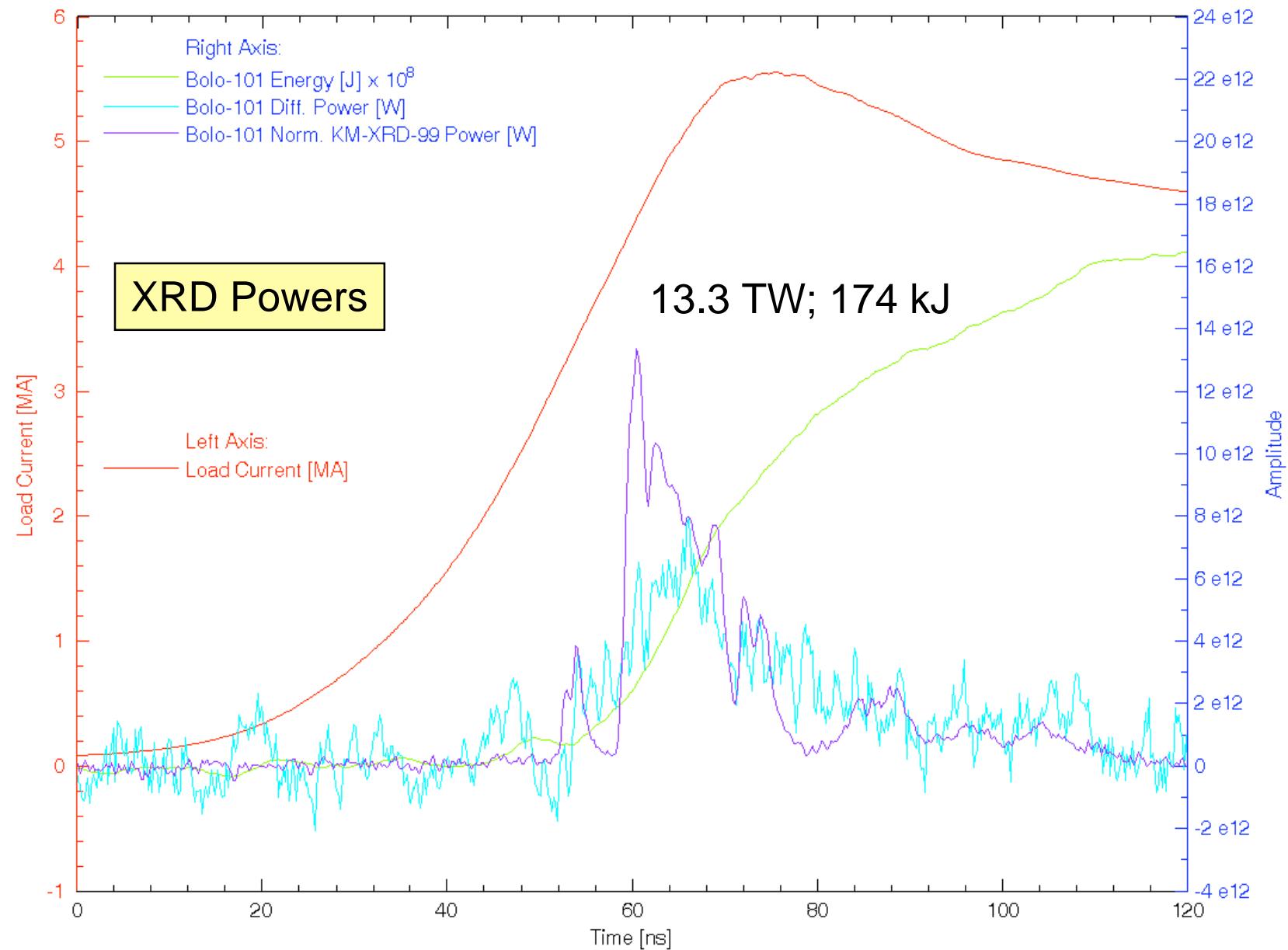
Cu55/Ni44/Mn1 X pinch

Saturn 3814

Cu55/Ni44/Mn1 X pinch

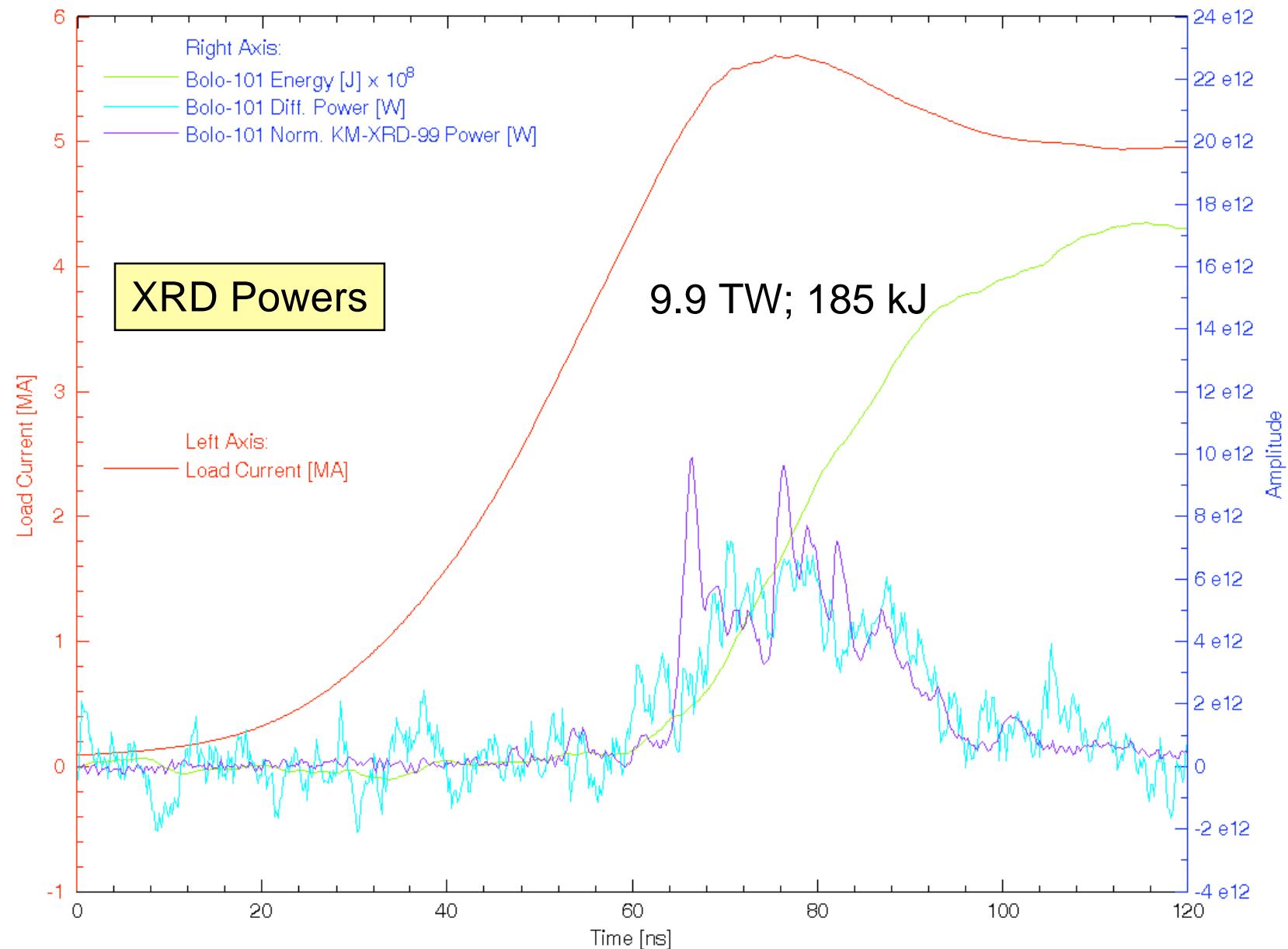
Saturn 3810

W72/Cu28 X pinch



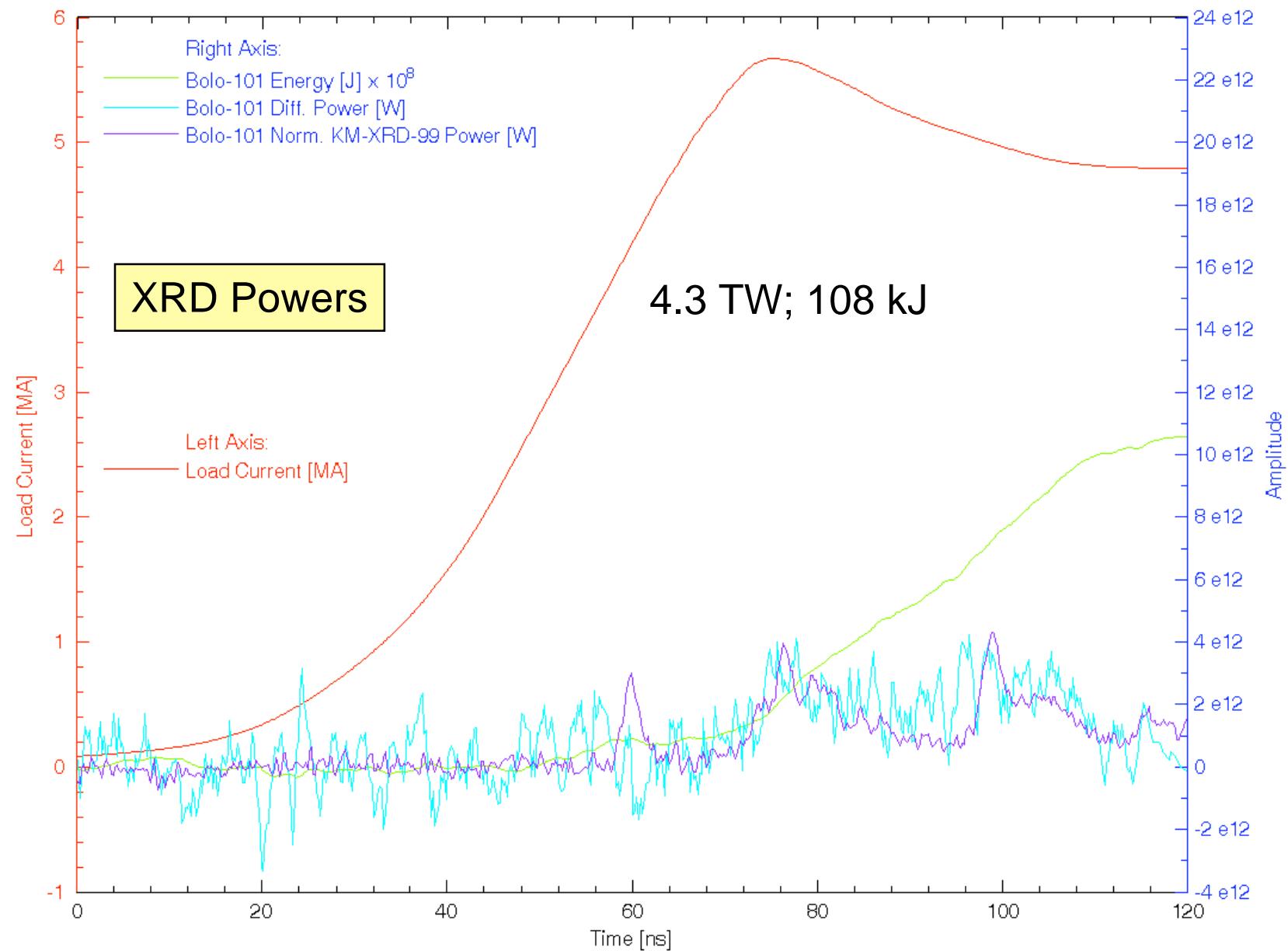
Saturn 3811

W72/Cu28 X pinch



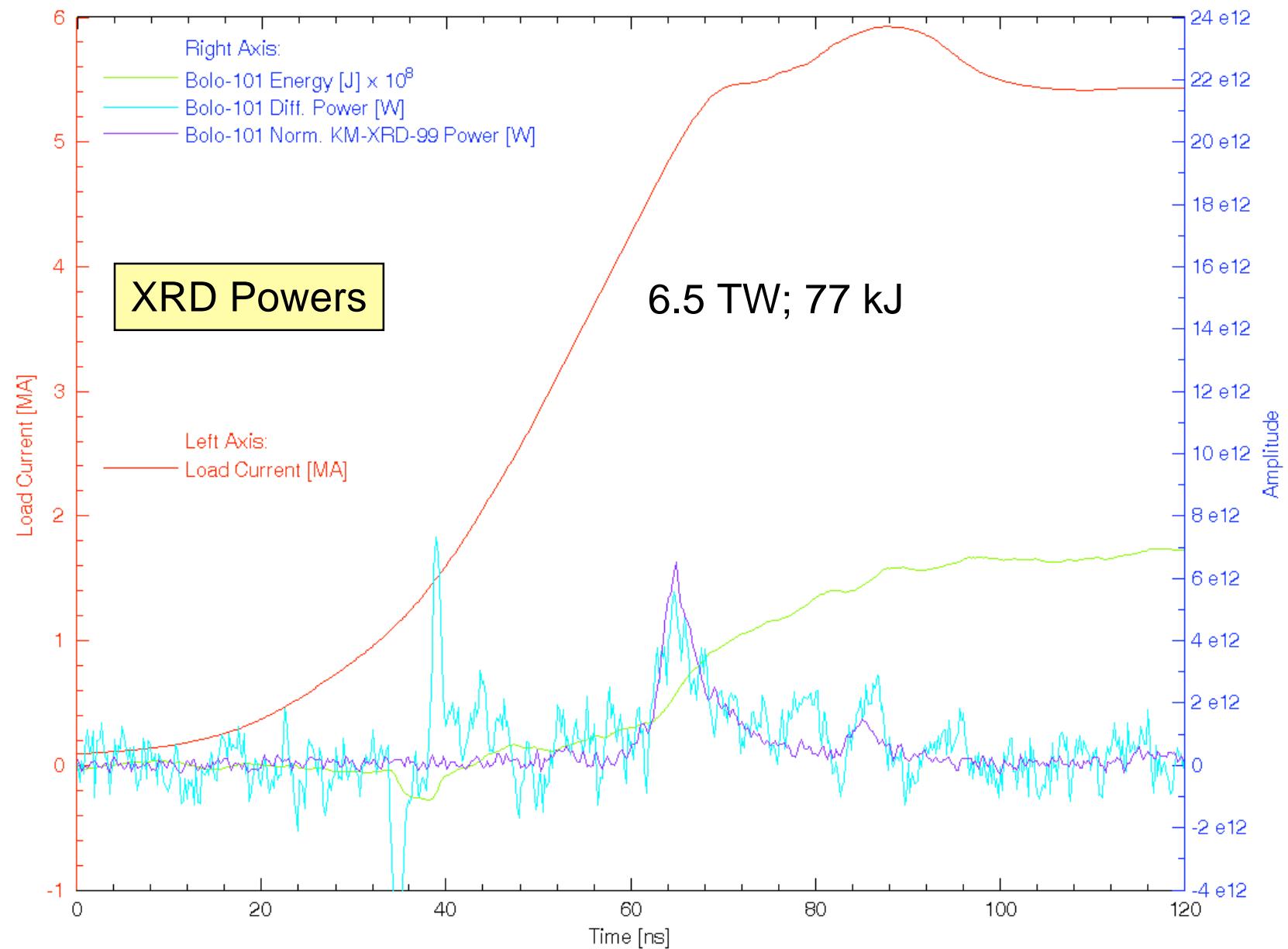
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Cu55/Ni44/Mn1 X pinch

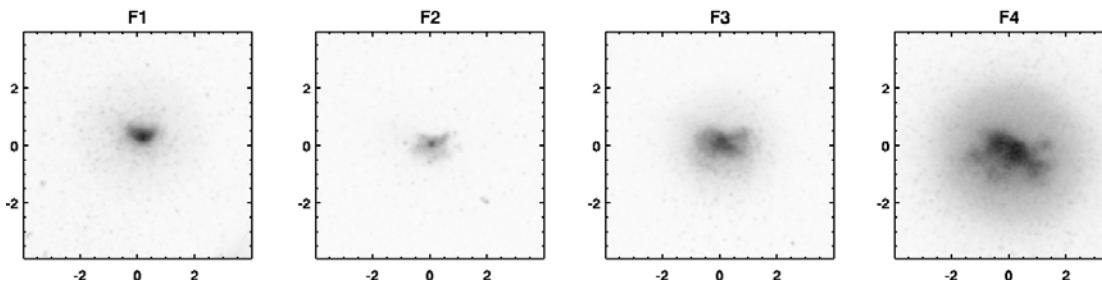
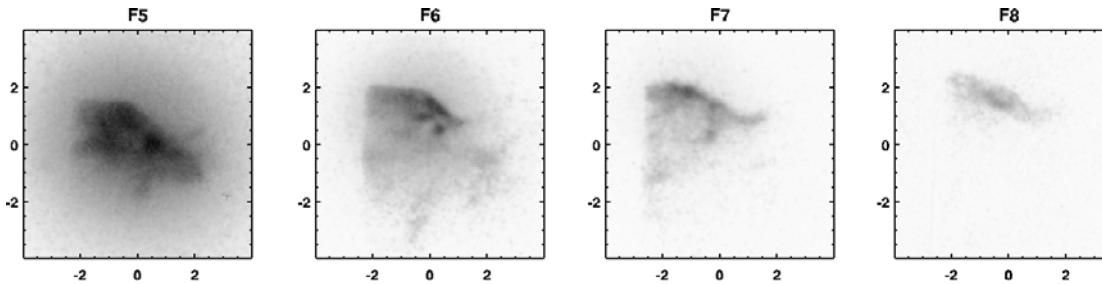
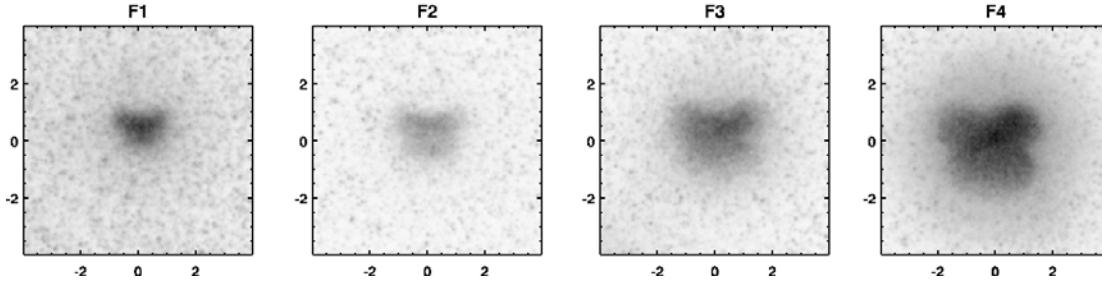
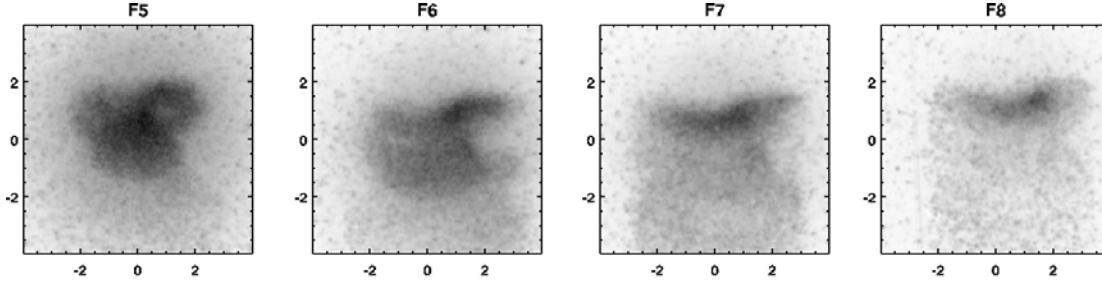


Saturn 3814

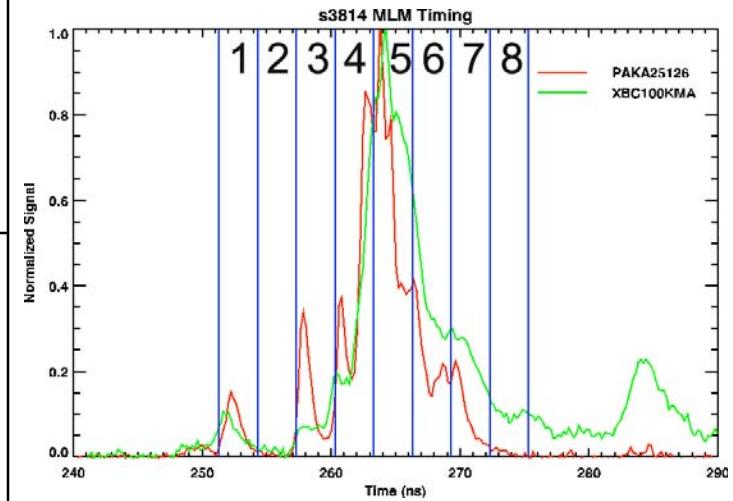
Cu55/Ni44/Mn1 X pinch



Cu/Ni X-pinch gated pinhole camera images show ~3 mm source size for soft x rays



S3814
MLM1
277 eV images
3ns IFT; 3ns gate
~540 μ m resolution



S3814
MLM2
>1 keV images
3ns IFT; 3ns gate
~200 μ m resolution (2 keV)



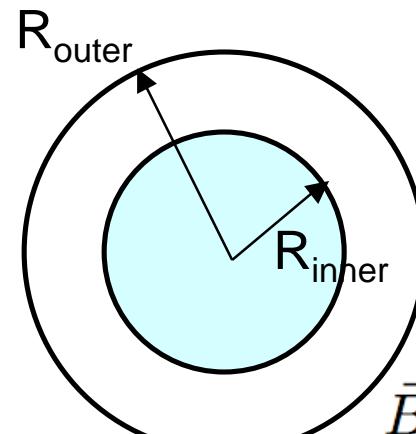
The work done by the JxB force can be quickly estimated for coaxial geometries

Magnetostatic potential energy:

$$U = \frac{1}{2\mu_0} \int_{all\ space} B^2 dV = \frac{1}{2} LI^2$$

For a coaxial system:

$$W' = \frac{\mu_0}{4\pi} \int_0^{t_{final}} I^2(t) \ln \frac{R_{out}}{R_{pinch}(t)} dt$$



$$\vec{B} = \frac{\mu_0 I}{2\pi r} \hat{\phi},$$

for $R_{outer} > r > R_{inner}$

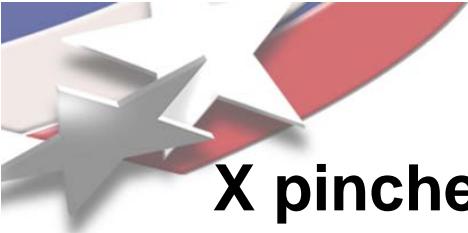
For a constant current:

$$W'_{static} = \frac{\mu_0 I_0^2}{4\pi} \int_0^{t_{final}} \ln \frac{R_{out}}{R_{pinch}(t)} dt =$$

$\frac{\mu_0 I_0^2}{4\pi} \ln \frac{R_0}{R_{final}}$

JxB Work varies with:

- Current
- Convergence Ratio



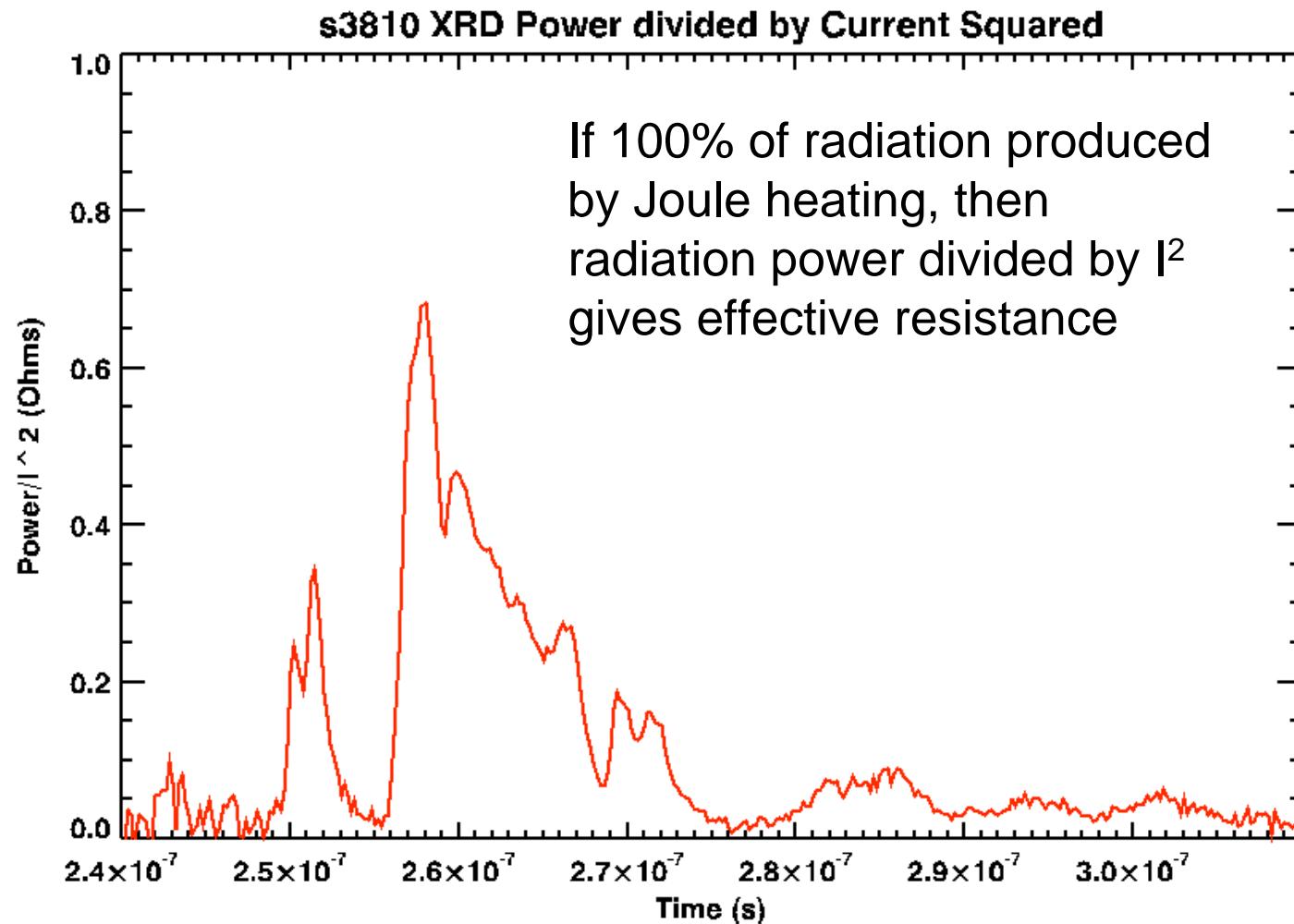
X pinches have “zero” kinetic energy and even at large convergence ratios JxB work is too small

- All mass starts on axis--main work done is compressional JxB (PdV) work
- W/Cu X pinch initial neck diameter = 366 μm
- Example JxB work estimates
 - 10 μm final collapse radius: CR=36.6, $\ln(36.6)=3.6$
 - 1 μm final collapse radius: CR=366, $\ln(366)=5.9$
 - Work $\sim 3\text{e}6 * \ln(\text{CR}) * \text{Pinch height (in m)}$
 - Extreme case of 3 mm tall, 1 μm diameter pinch:
Work $\sim 3\text{e}6 * 5.9 * 0.003 = 53.1 \text{ kJ}$
- Measured Yields: 175 kJ, 184 kJ
- Must be dominated by Ohmic heating? *

* Consistent with assumptions in Chittenden *et al.*, Phys. Rev. Lett. (2007).



Power/I² (“Resistance”) for W/Cu X-pinch test s3810





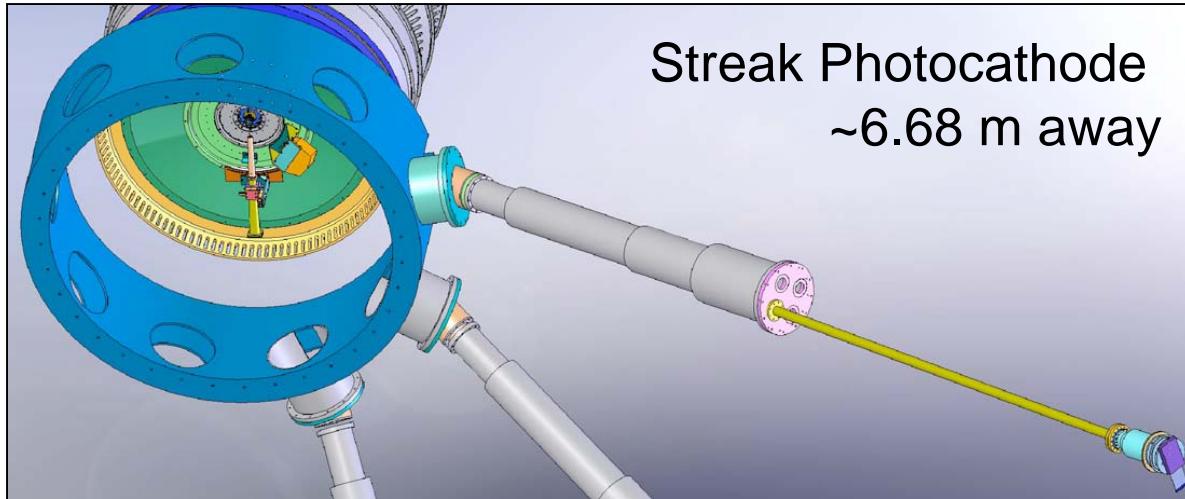
SATURN X pinches have relatively high average energy/power line densities

Shot #	Material	Radiated Energy Yield [kJ]:	Peak Radiated Power (Bolo-Normalized) [TW]:
3808	Ni80/Cr20	164	6.6
3809	Cu55/Ni44/Mn1	96	6.1
3810	W72/Cu28	174	13.3
3811	W72/Cu28	185	9.9
3812	Cu55/Ni44/Mn1	108	4.3
3814	Cu55/Ni44/Mn1	77	6.5

- **SATURN W/Cu X pinches:**
 - ~11.5 TW, ~180 kJ, from a ~3 mm tall region
 - ~4 TW/mm; ~60 kJ/mm
- **SATURN planar arrays:**
 - ~15 TW, ~300 kJ, from a 20 mm tall region
 - <0.1 TW/mm; ~15 kJ/mm
- **Z tungsten Z pinch (Deeney PRE):**
 - ~240 TW, ~1800 kJ, from a 20 mm tall region
 - ~12 TW/mm; ~90 kJ/mm

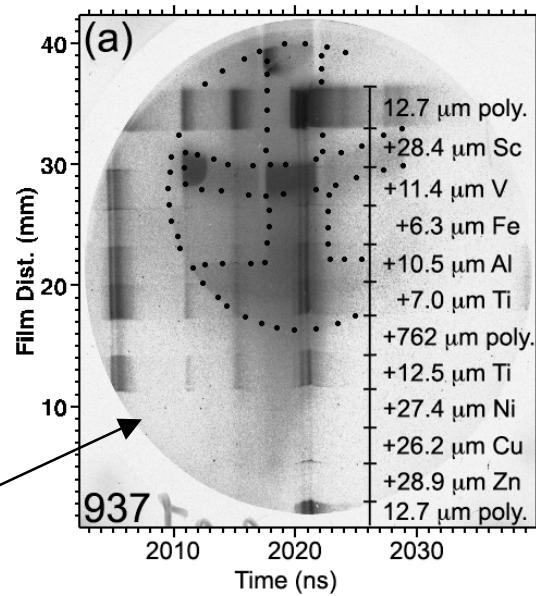


Could the actual powers be higher? Streak camera data measuring x-ray emission duration from Cu/Ni X-pinch

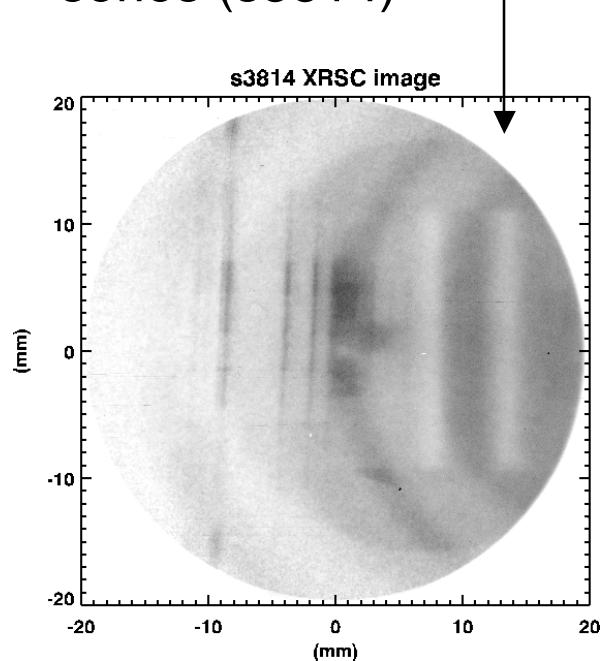


Photocathode covered
with array of filters as
on 1 MA X-pinch
experiments*

* D.B. Sinars *et al.*, Phys.
Plasmas (2008).

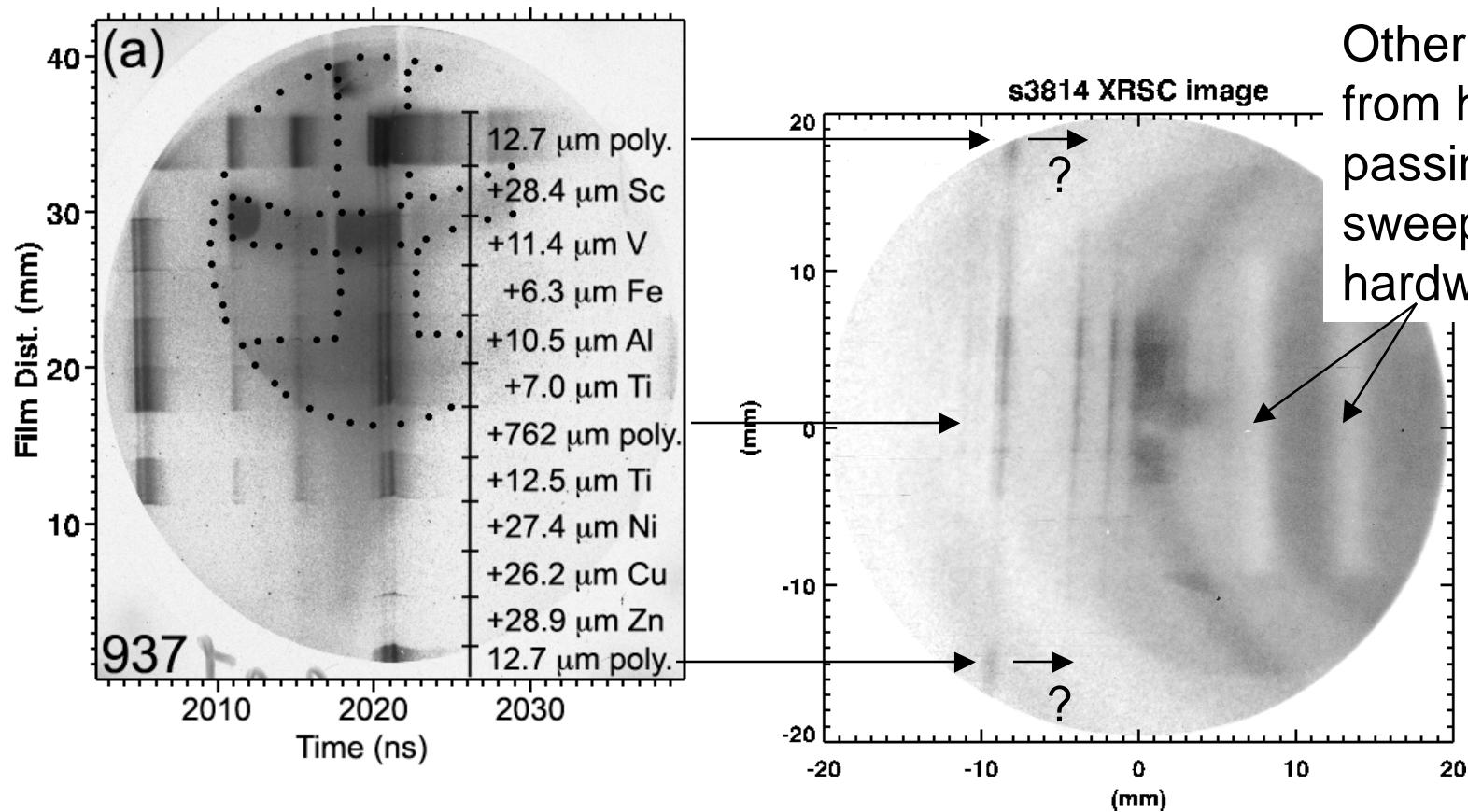


Struggled with too much
signal and a damaged
power supply. After
adding 250 μm polyimide,
got data on final shot of
series (s3814)



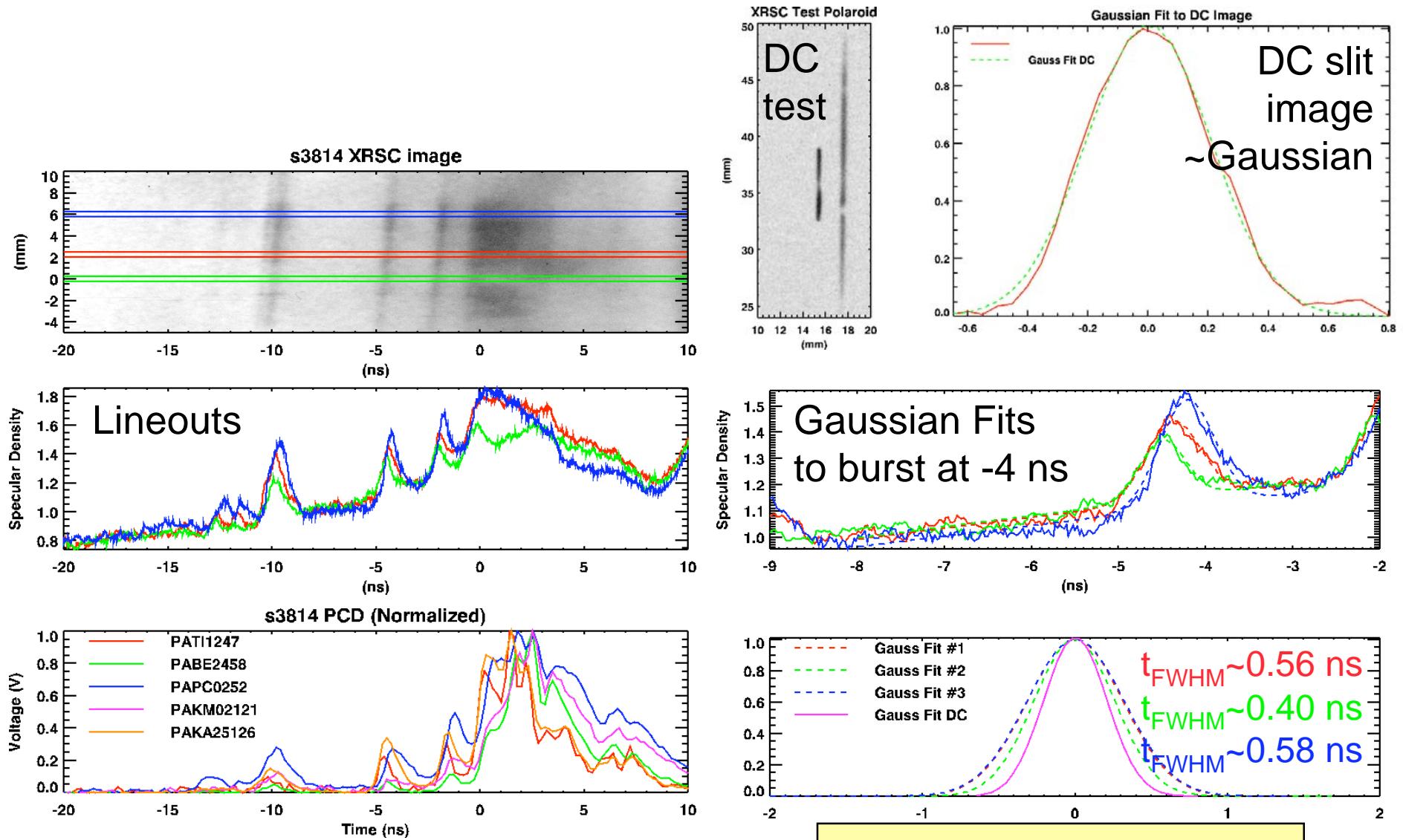


X-ray streak data doesn't quite make sense-- thinnest-filter streaks on end disappear



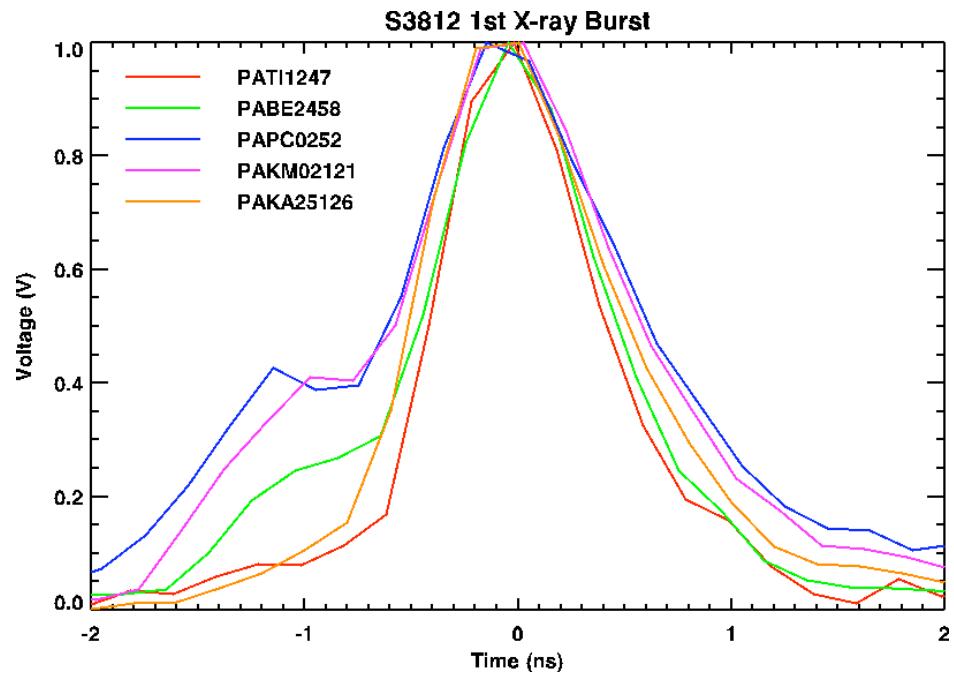
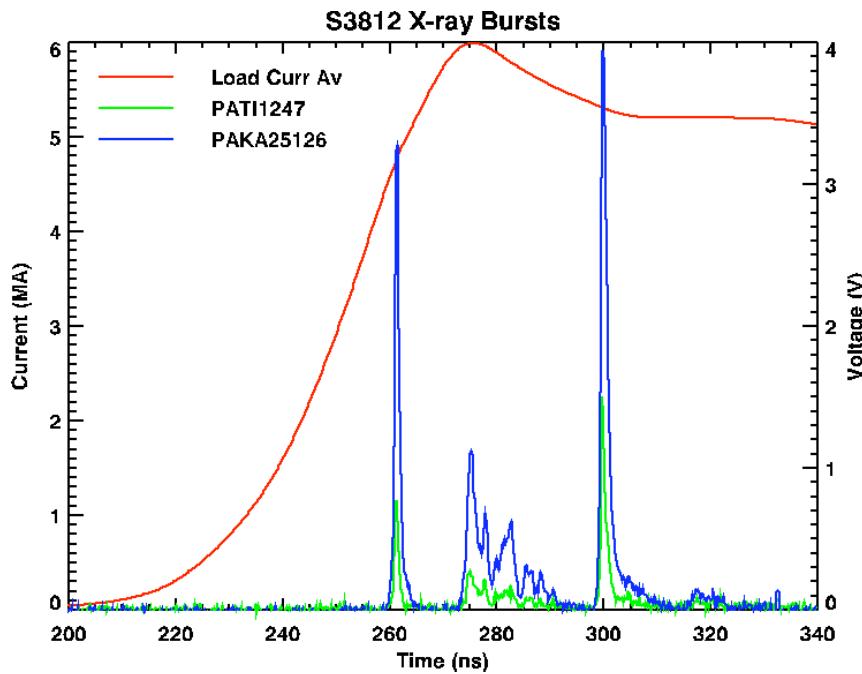
Had some problems with power supply--could not get perfect focusing on ends post-shot. The problem could be with the focusing.

Analysis of Cu/Ni X-pinch X-ray Streak Camera Data (s3814) shows sub-ns bursts





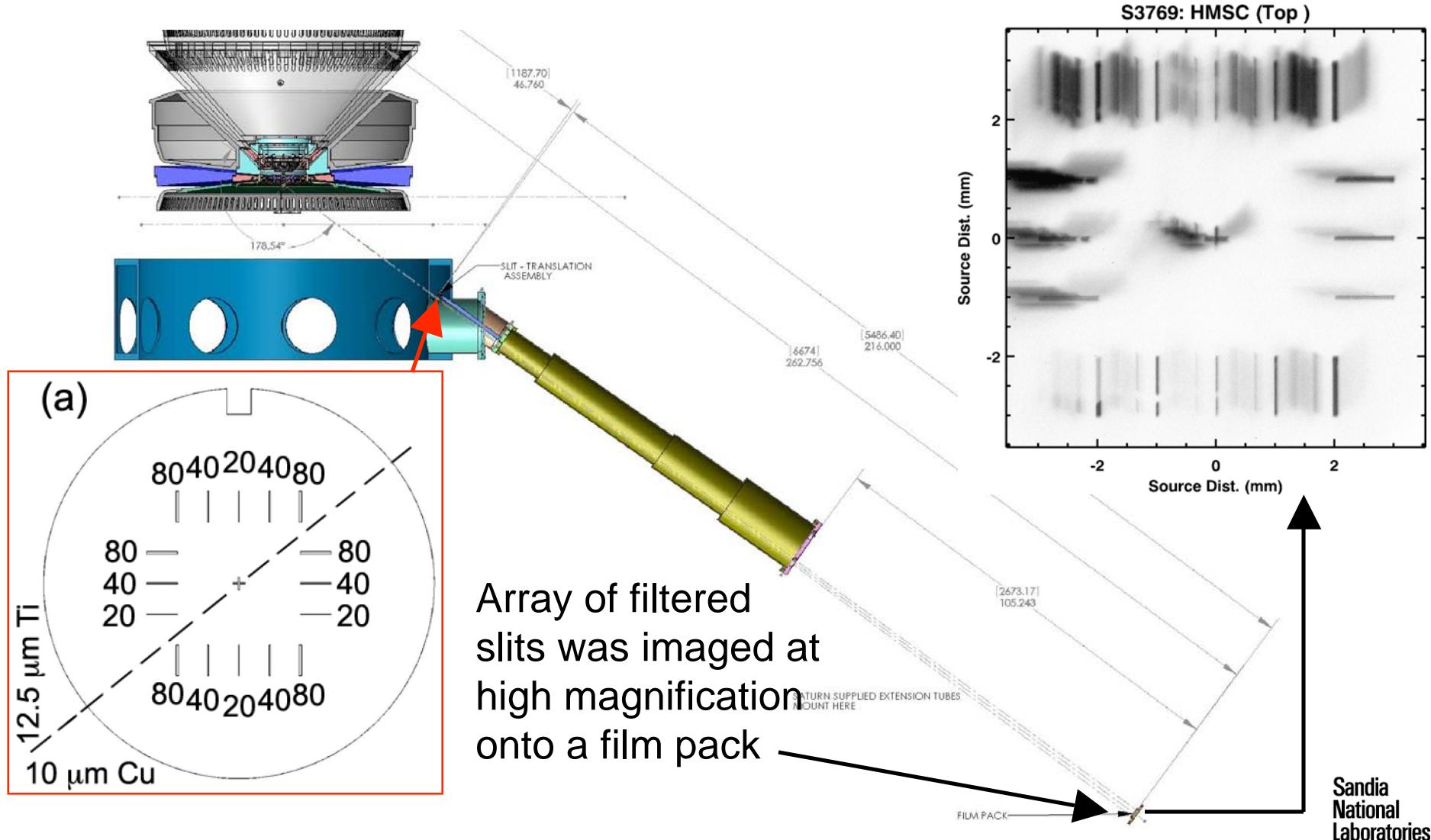
Another Cu/Ni X pinch had a lone burst with a 0.8-1.1 ns FWHM on hard-filtered PCDs



Bottom line: If true x-ray bursts are <0.5 ns duration (as on 0.2 MA experiments), how accurate will traditional bolometer/XRD/PCD measurements be?



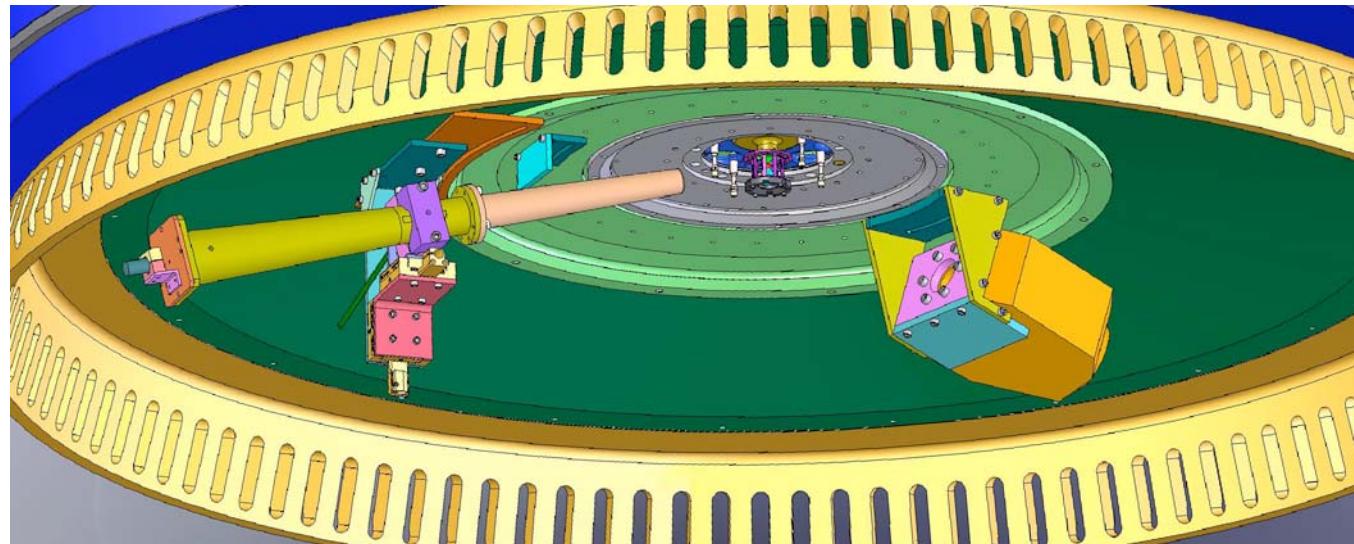
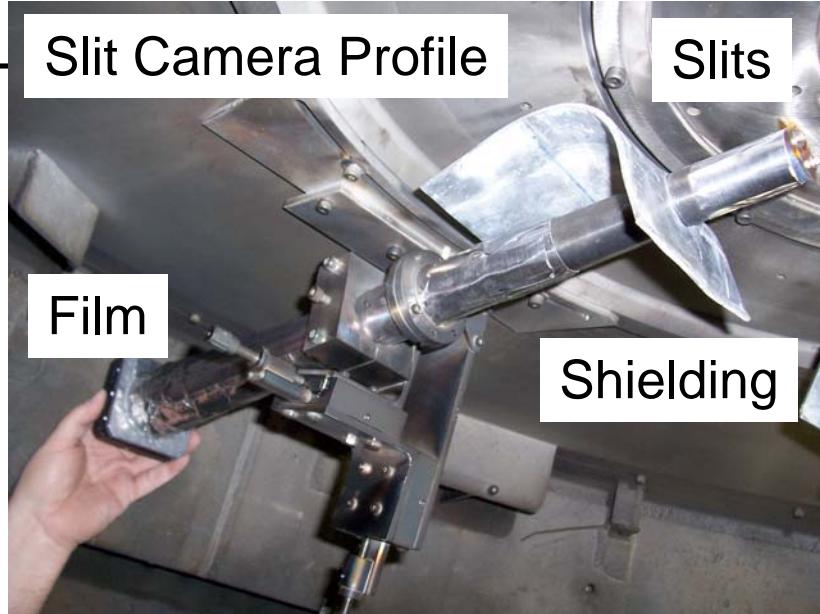
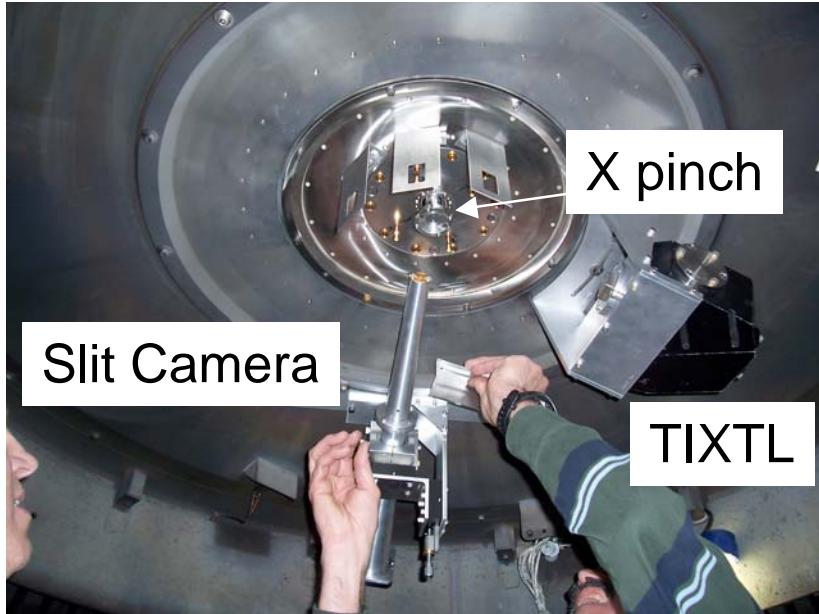
A high-magnification slit camera was used on first 2 series to measure the x-ray source size



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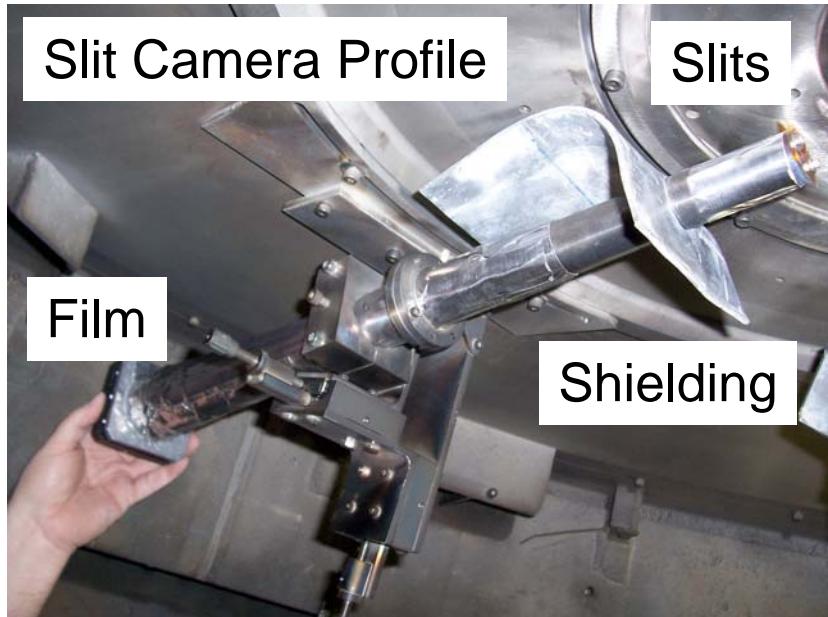
Recent series used an in-chamber slit camera & time-integrated convex spectrometer



- Slits ~0.1 m from X-pinch
- Magnification ~6.6x
- Reduced diffraction blurring (slits ~1.2 m before)



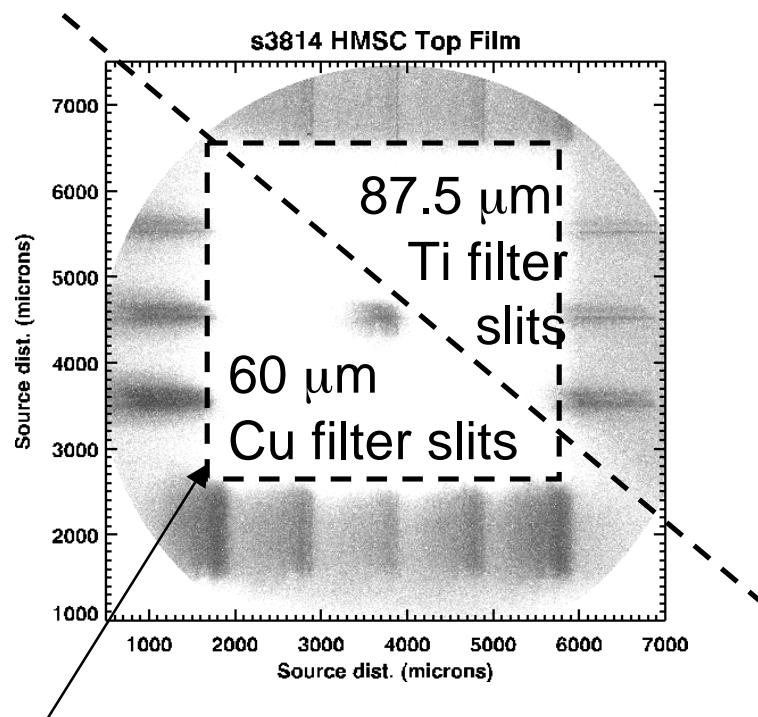
Hard x rays penetrating the Ta slit substrate created significant background on the film



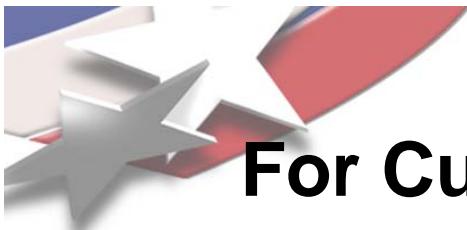
Initially tried to shield film pack with external shielding.

Tests quickly showed that background was coming straight through the slit assembly itself

25 μm Ta slit substrate
+50 μm polyimide filter

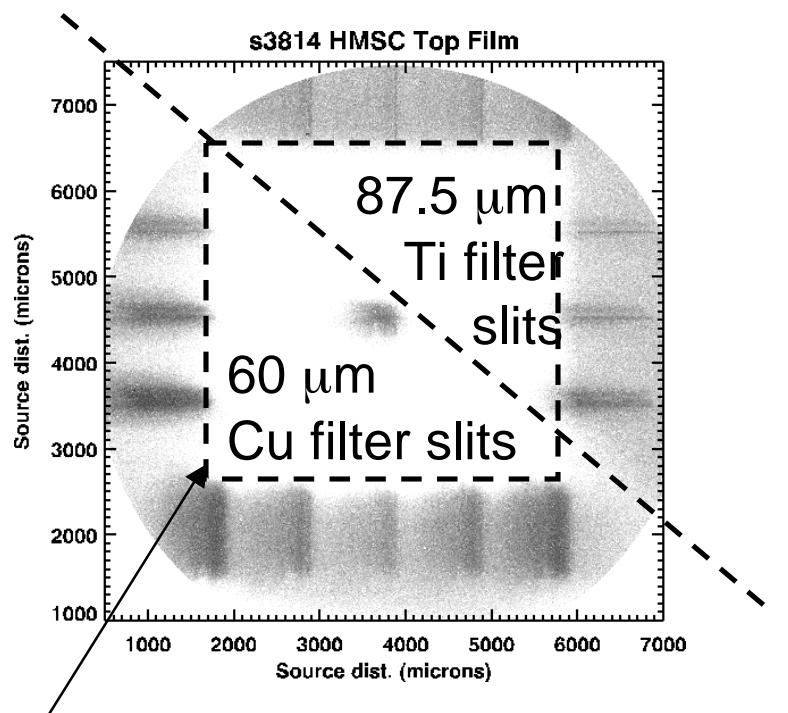


Best result obtained when a ~4 mm thick Pb cube placed behind Ta slit piece

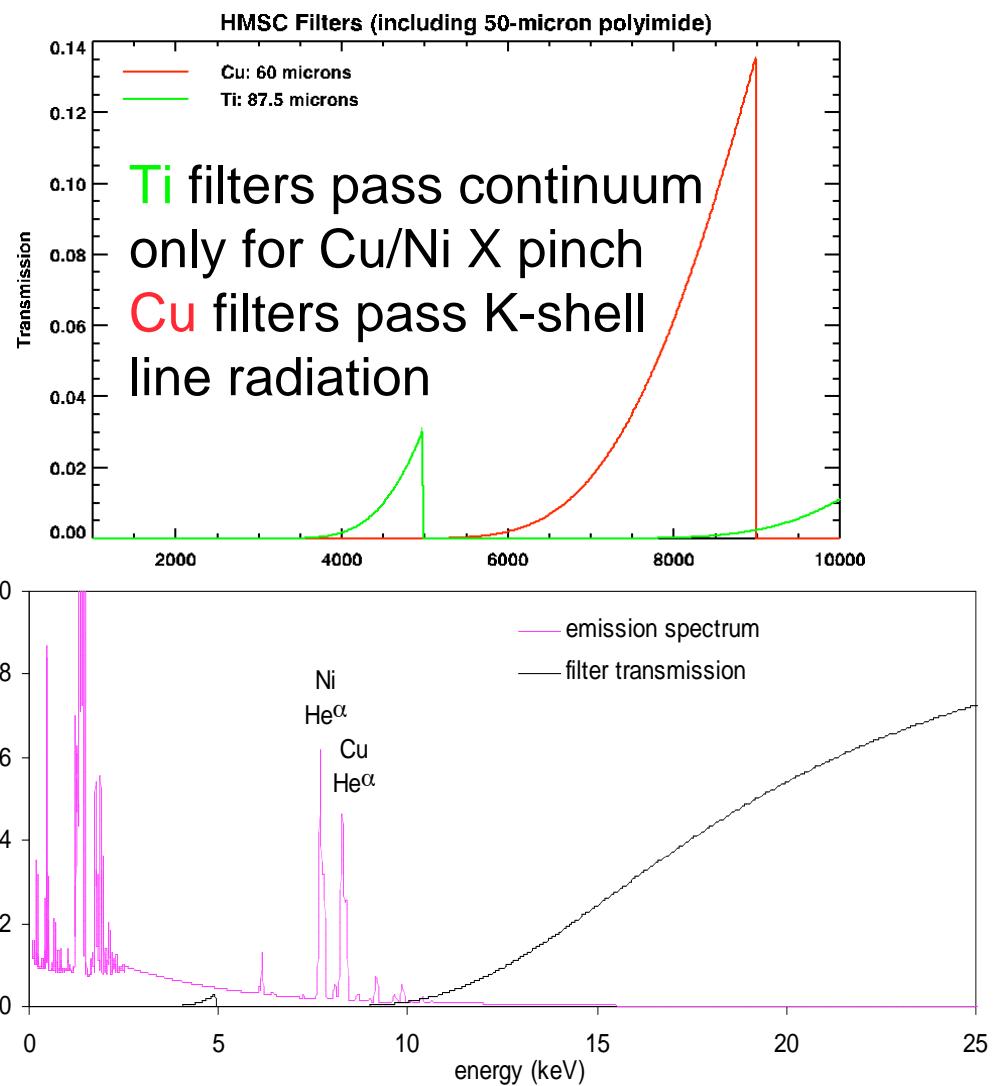


For Cu/Ni X pinches, filtered slits passed either continuum or K-shell line radiation

25 μm Ta slit substrate
+50 μm polyimide filter

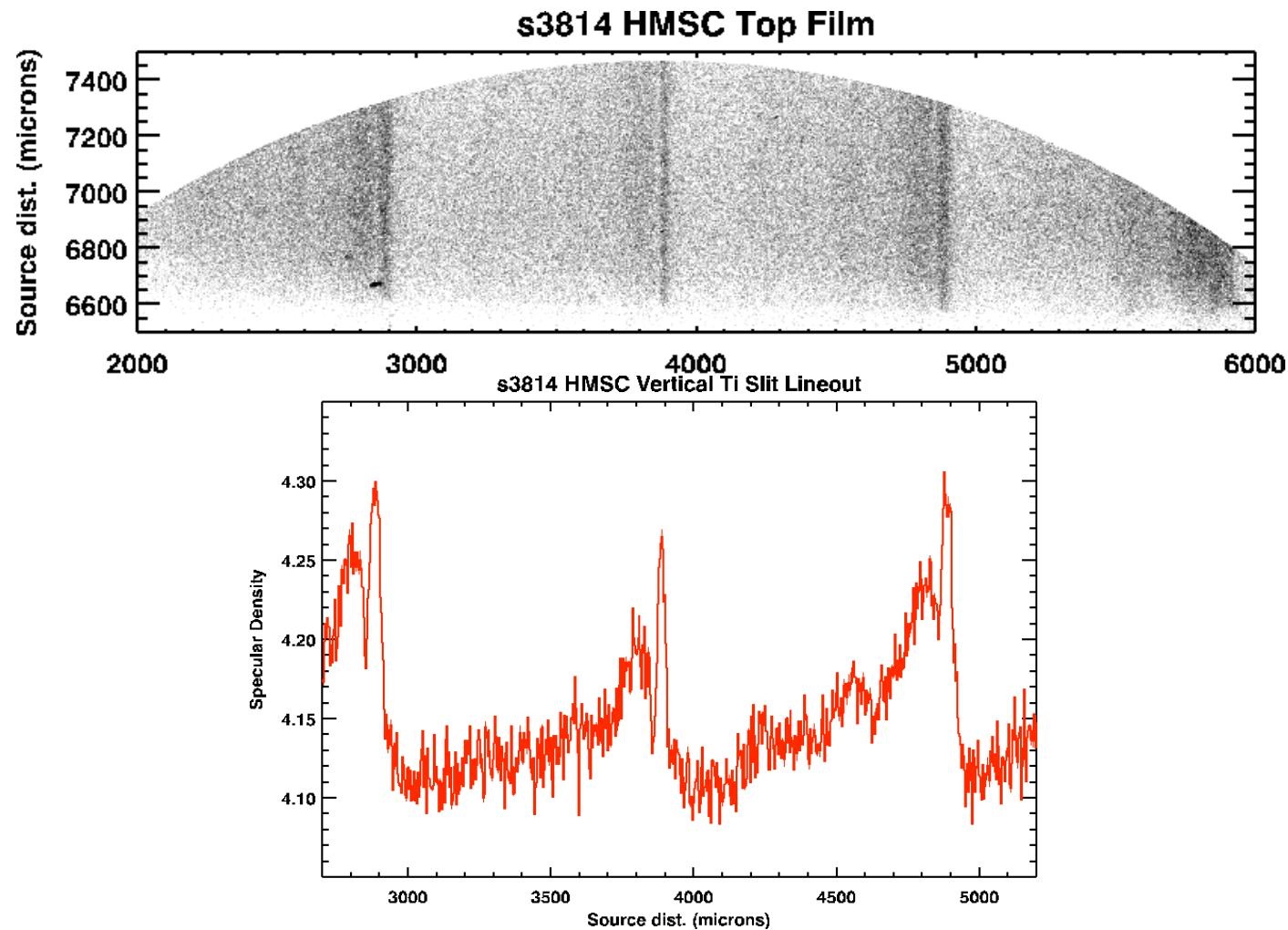


Best result obtained when a
~4 mm thick Pb cube placed
behind Ta slit piece



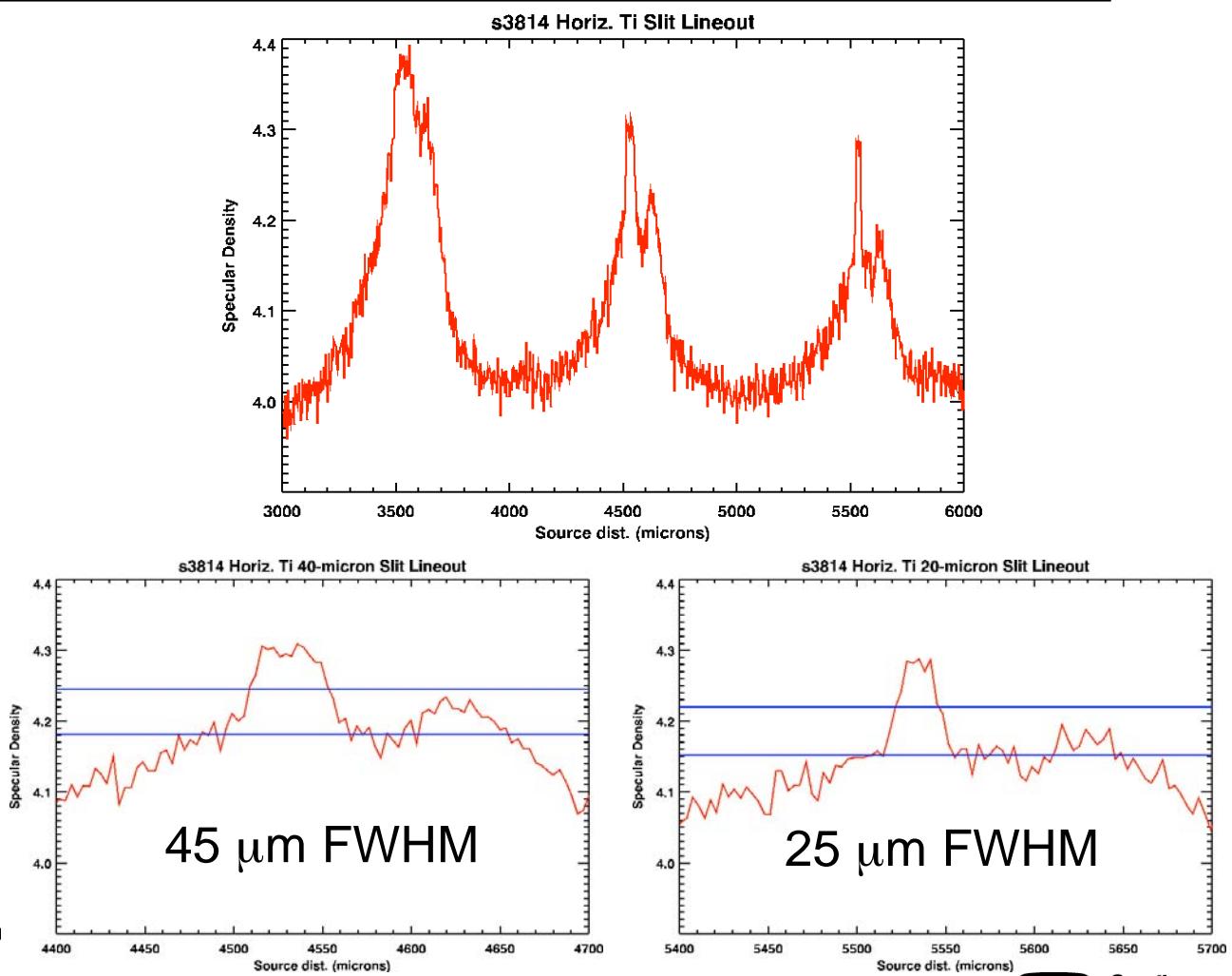
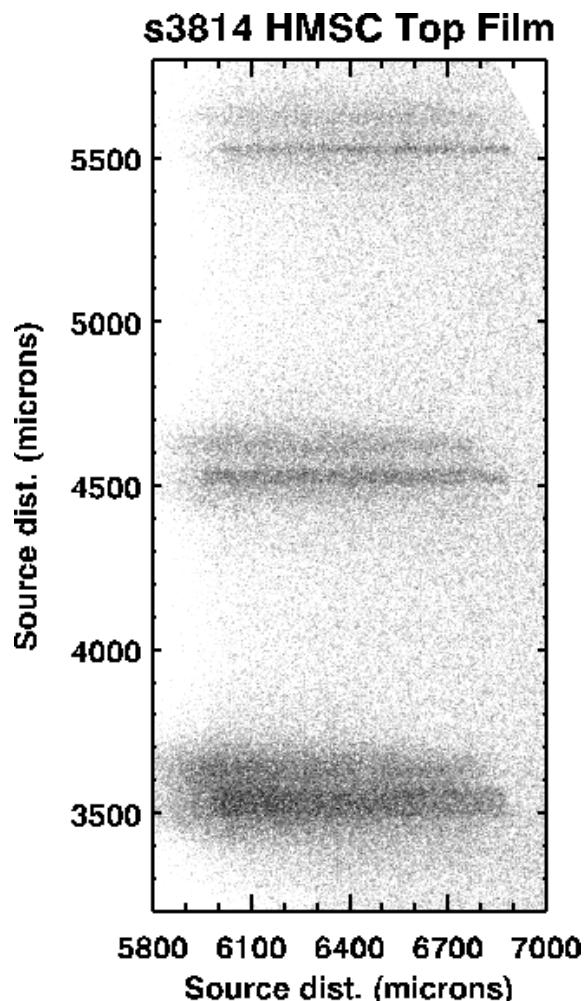


Vertical Ti slit images show at least one narrow x-ray spot for Cu/Ni X pinch (s3814)





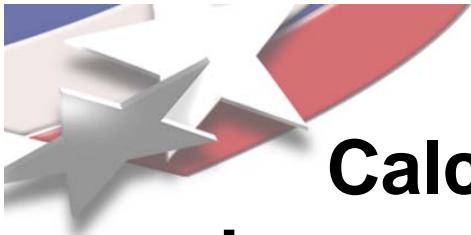
Horizontal Ti slit images also show a small x-ray source from Cu/Ni X pinch



Both consistent with a ~5-10 μ m source?

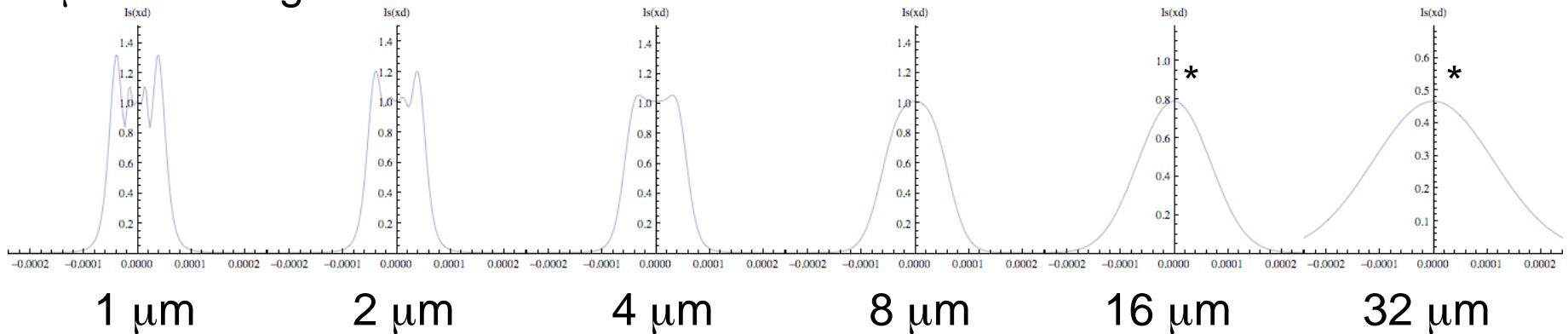


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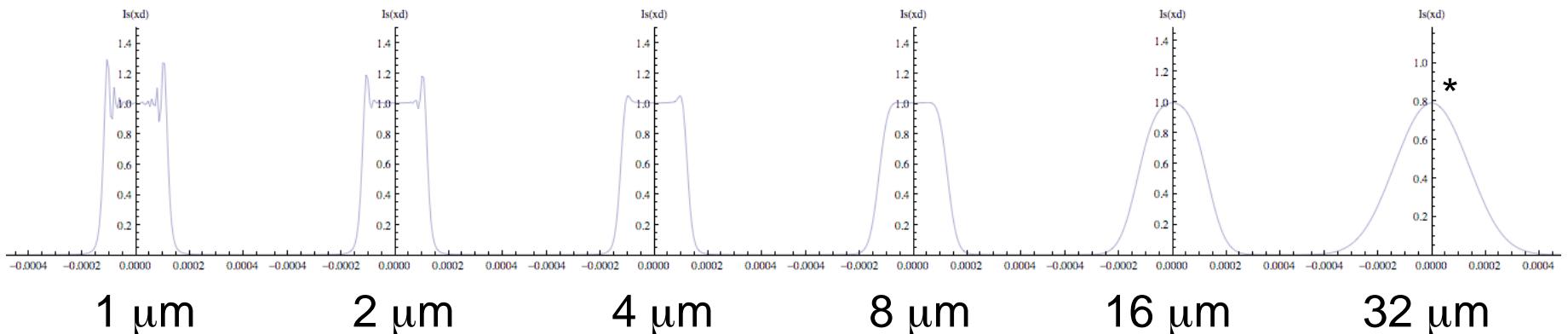


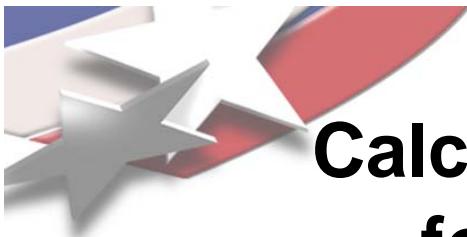
Calculated slit images show effect of changes in source size on slit measurements

20 μm slit images

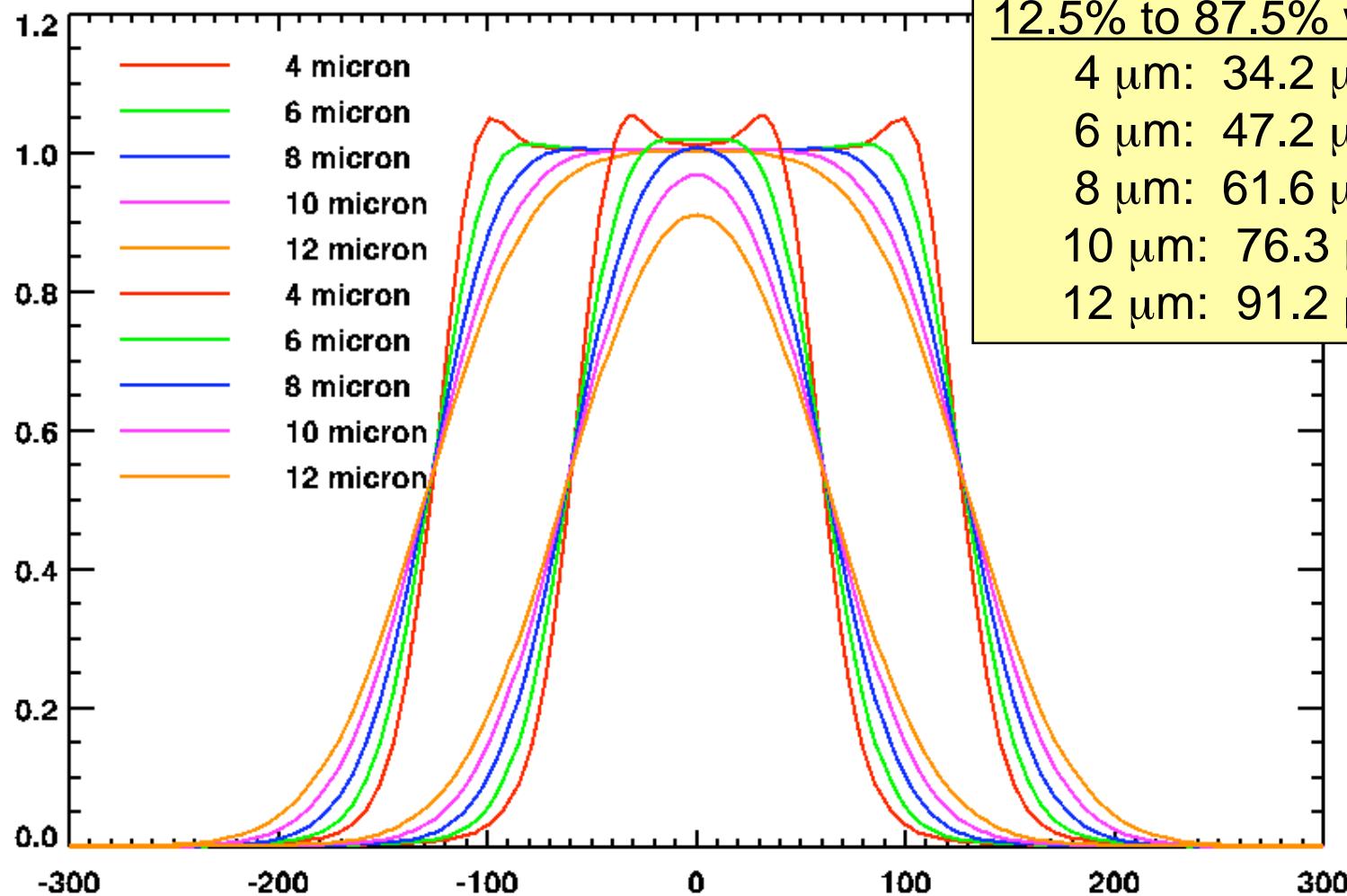


40 μm slit images



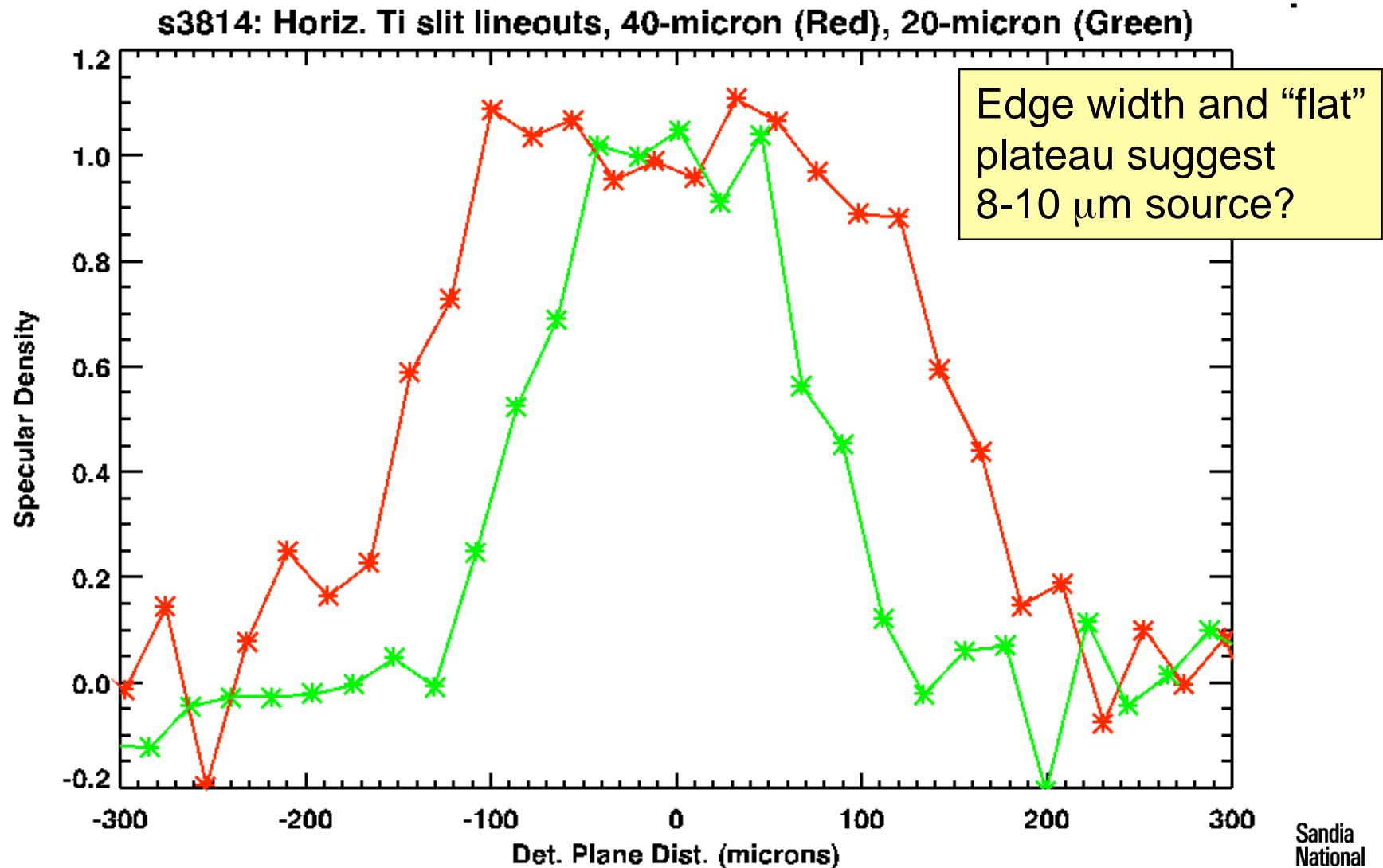


Calculated 40- and 20- μm slit images for selected x-ray source sizes



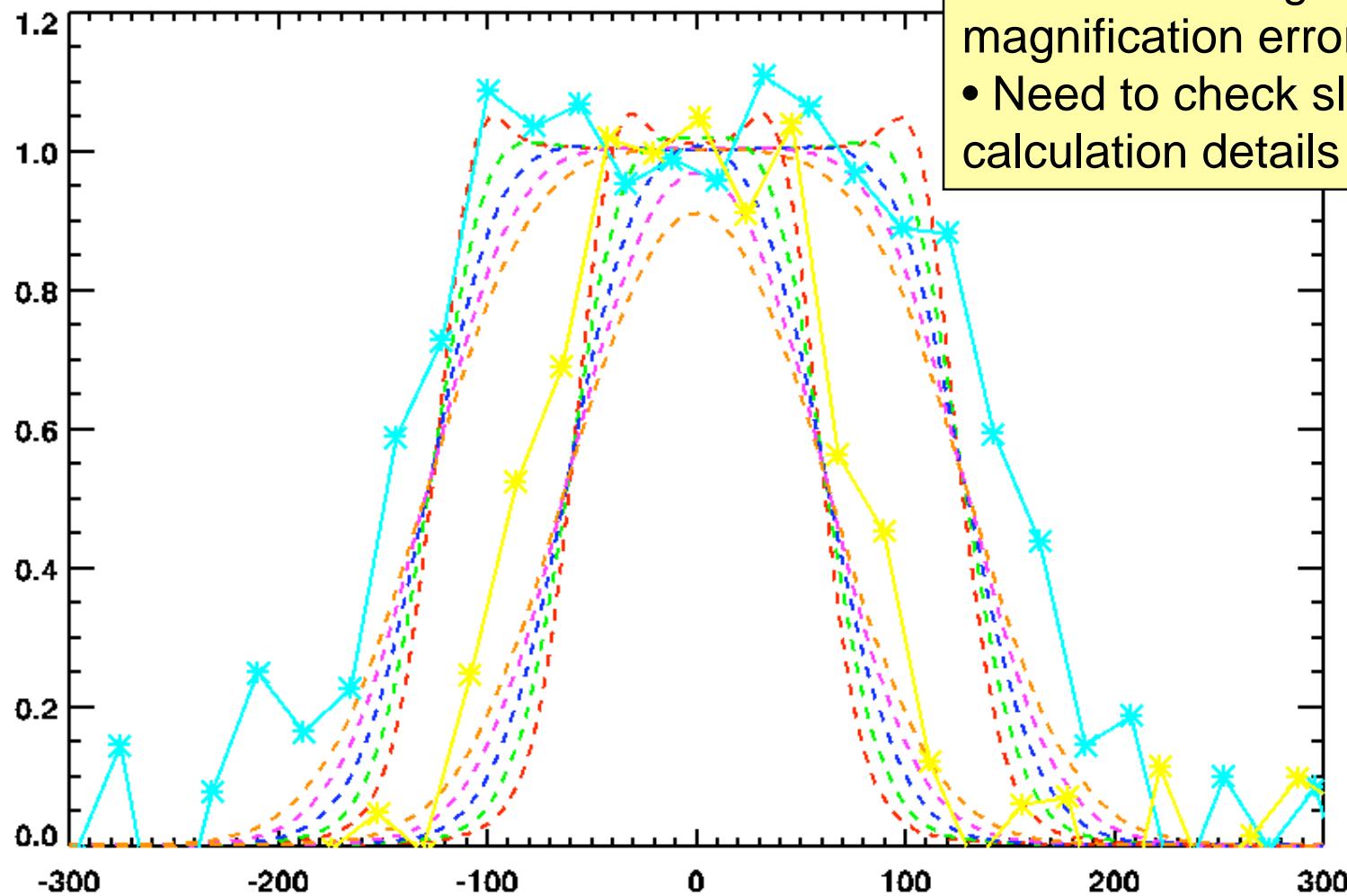


Lineouts appear to show relatively flat tops to the slit images and ~67 μm edge spreads



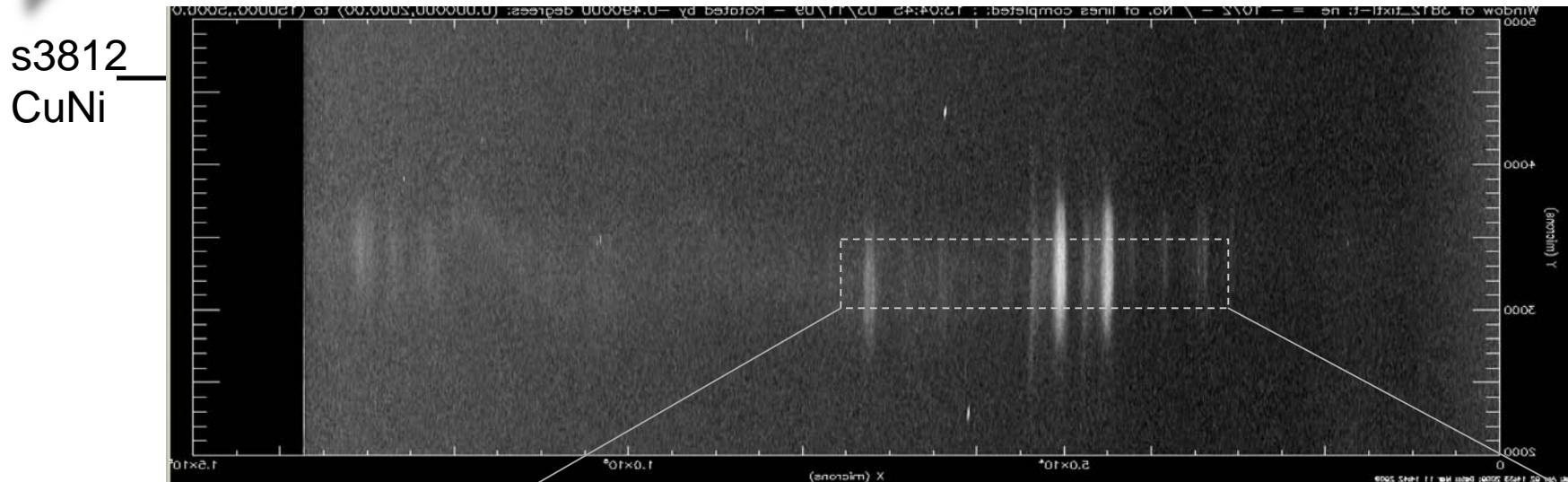


Disclaimer: Calculations think overall width should be ~1.2x narrower





Quick analysis of time-integrated K-shell spectra from Cu/Ni X pinch shows hot plasma



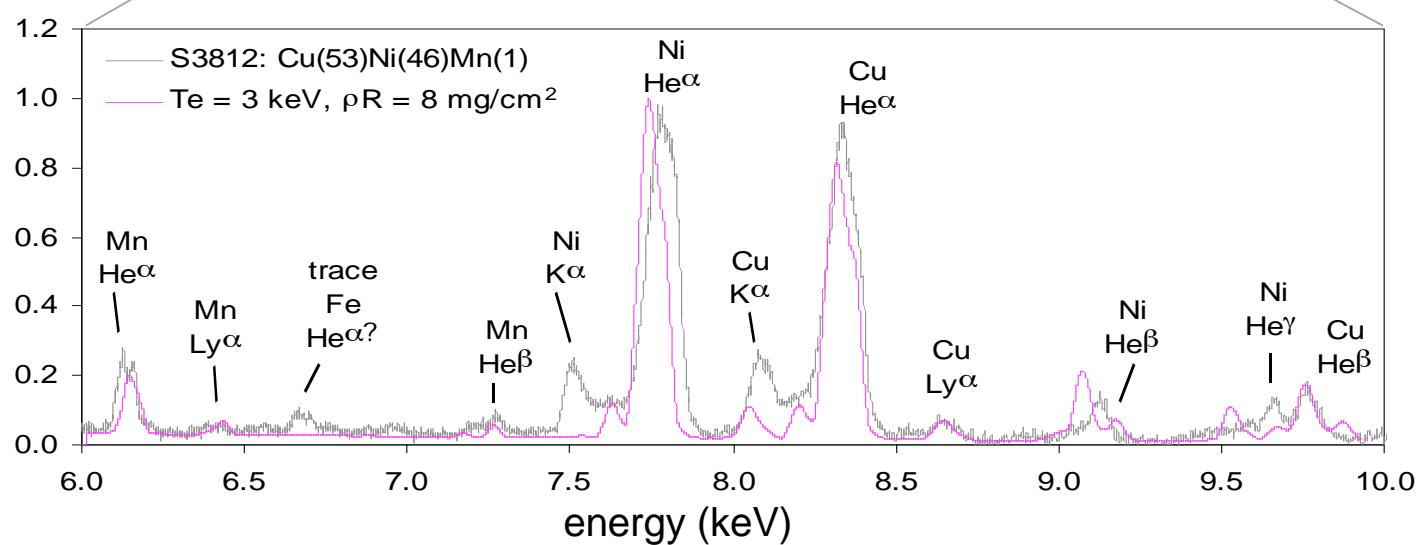
First cut diagnostics:

Estimate ρR by fitting
Mn/Ni He α ratio

Estimate T_e by fitting Ly α /He α ratios

Poor fit above 9 keV

Temperature gradients
evidenced by cold K α
features

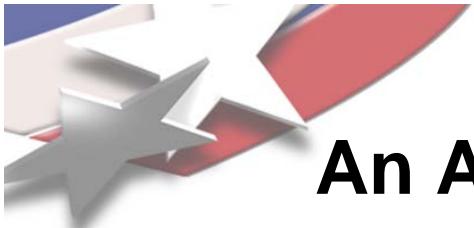


K-shell size $>10 \mu\text{m}$ ($\sim 50 \mu\text{m}$?), so density $\sim 1.6 \text{ g/cc}$? More work needed

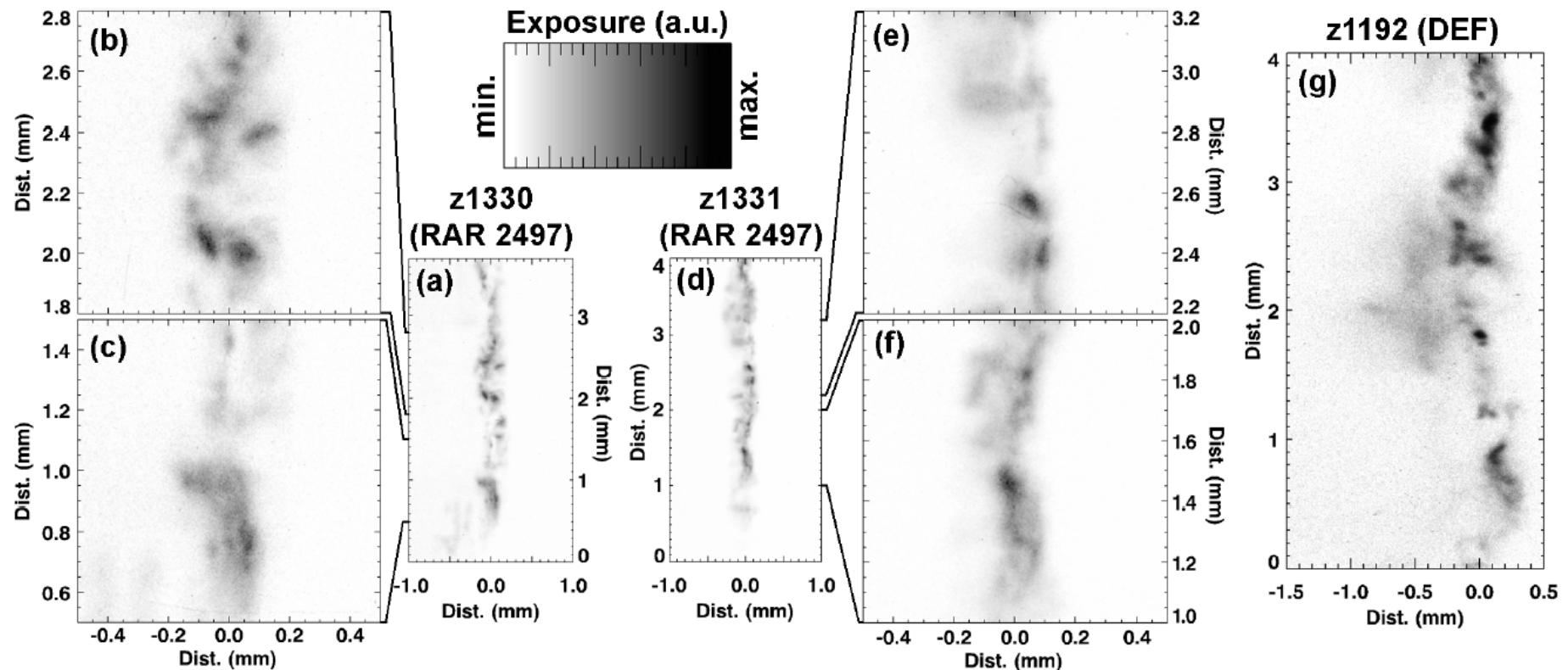


High-current X pinches are a work in progress

- We are halfway through a 3-year research project
 - Have identified a promising geometry
 - May want to slightly increase implosion time again
 - Have made progress in making precision measurements of plasmas created
 - Try to improve streak time resolution
 - Try to reduce background on slit camera
 - Try to understand spectroscopic information--what can we learn about density, B-field?
- Are we producing small plasma spots with extreme plasma parameters?
 - Seem to be getting close....
- Are X pinches a waste of the taxpayer's money?
 - I hope not!



An Aside: Small-scale structures are also seen at very high photon energies

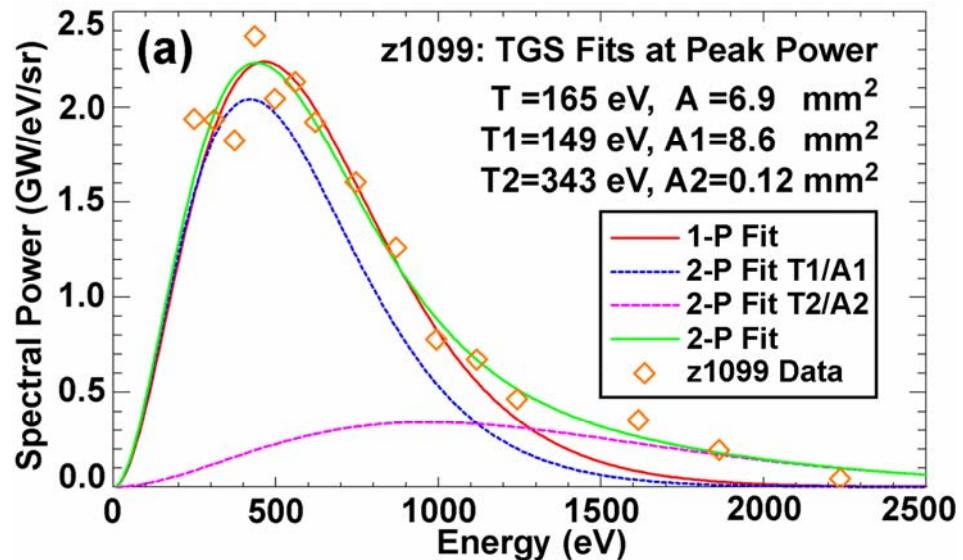


Time-integrated self-emission at 6151 eV (~10-20 μ m resolution)
Emission generally contained within a 400 μ m diameter (CR \sim 50?)
Structure as small as 50-100 μ m visible in images!



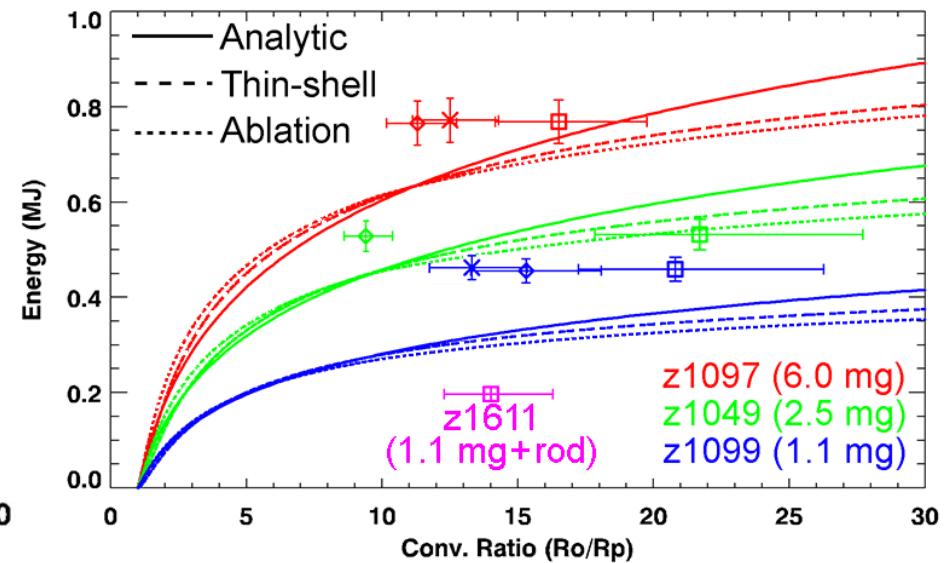
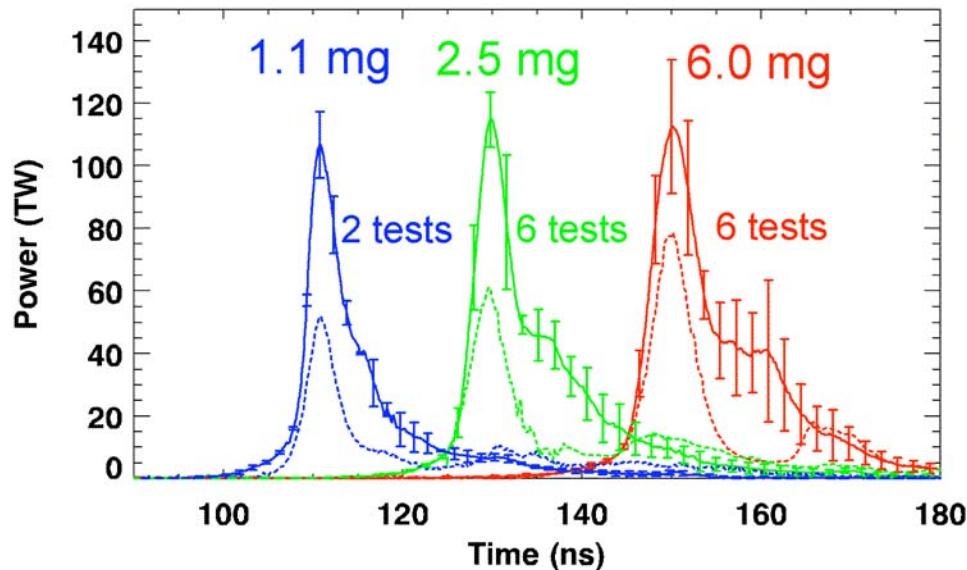
Do “micro-pinches” play a significant role in the total radiation?

- Single-blackbody fits do not match the high-energy tail of emission spectrum
- Can match spectrum using a two-blackbody fit
 - Second blackbody a high-temperature, small-area radiation source
 - Area under this blackbody curve ~30% of total energy radiated by the pinch!
 - Film exposure at 6151 eV roughly consistent with this x-ray source area & extrapolated x-ray yield
- Can also match spectrum with single-blackbody plus bremsstrahlung spectrum (but why so small a diameter?)



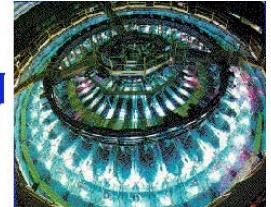


Main radiation pulse in shots with on-axis rods can be explained by observed $J \times B$ work



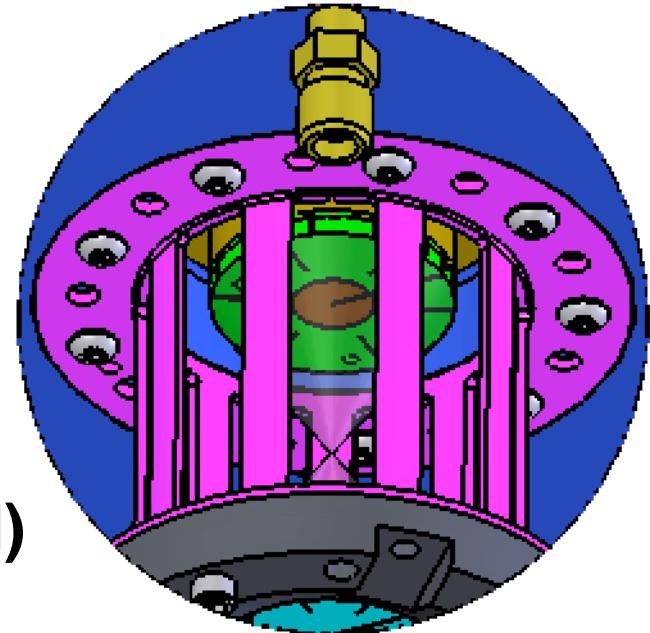
- Main pulse radiation/energy lowered by presence of rod without affecting τ_{imp} , τ_{rise} , τ_{FWHM} .
- In contrast to bare-axis shot, 1.1 mg array-on-rod radiation can be explained by observed $J \times B$ work

Array Mass	E_{main} (kJ)	E_{total} (kJ)	$E_{\text{main}}^{\text{rod}}$ (kJ)	$E_{\text{total}}^{\text{rod}}$ (kJ)
1.1 mg	440 ± 28	832 ± 21	195	488
2.5 mg	532 ± 46	1106 ± 106	306	689
6.0 mg	692 ± 66	1278 ± 239	428	748



Goal of SATURN experiments was to try and create small spots

- Timing: XRDs, PCDs
- X-ray Energy: Bolometers
- Dynamics: X-ray pinhole cameras (gated & time-integrated)
- X-ray Spot Size: High-magnification slit camera
- All diagnostics view load ~35° below horizontal!



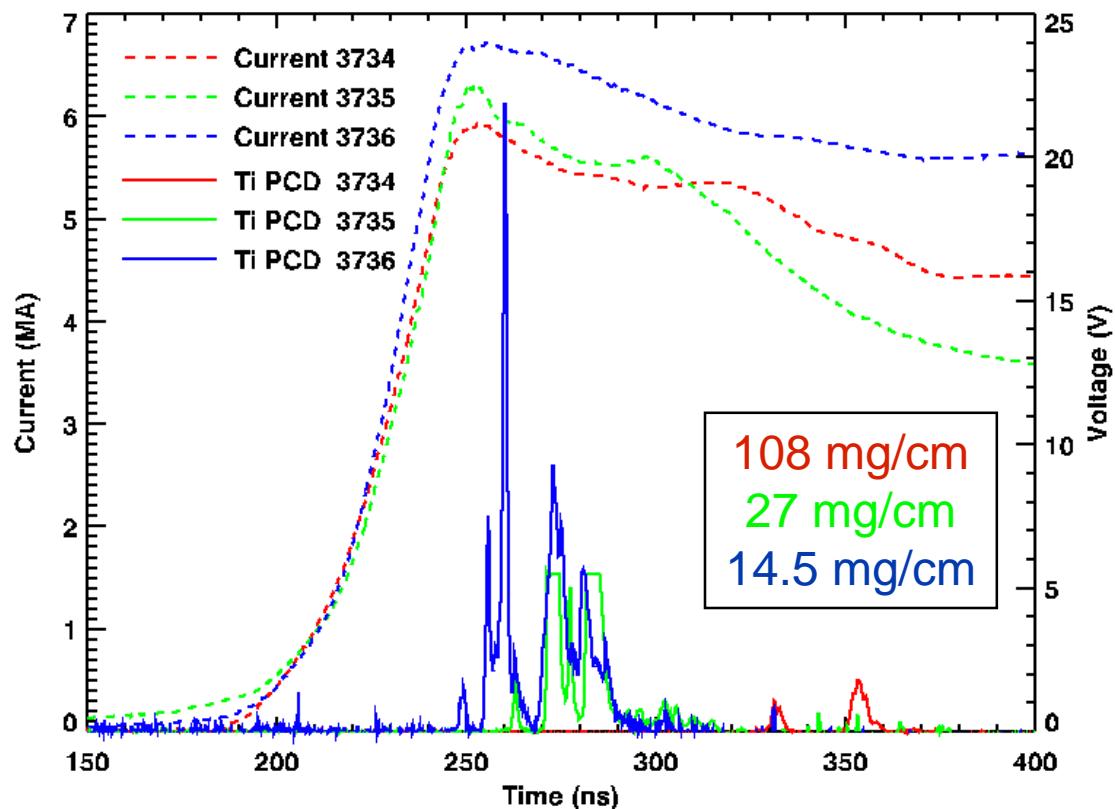


Extra Slides



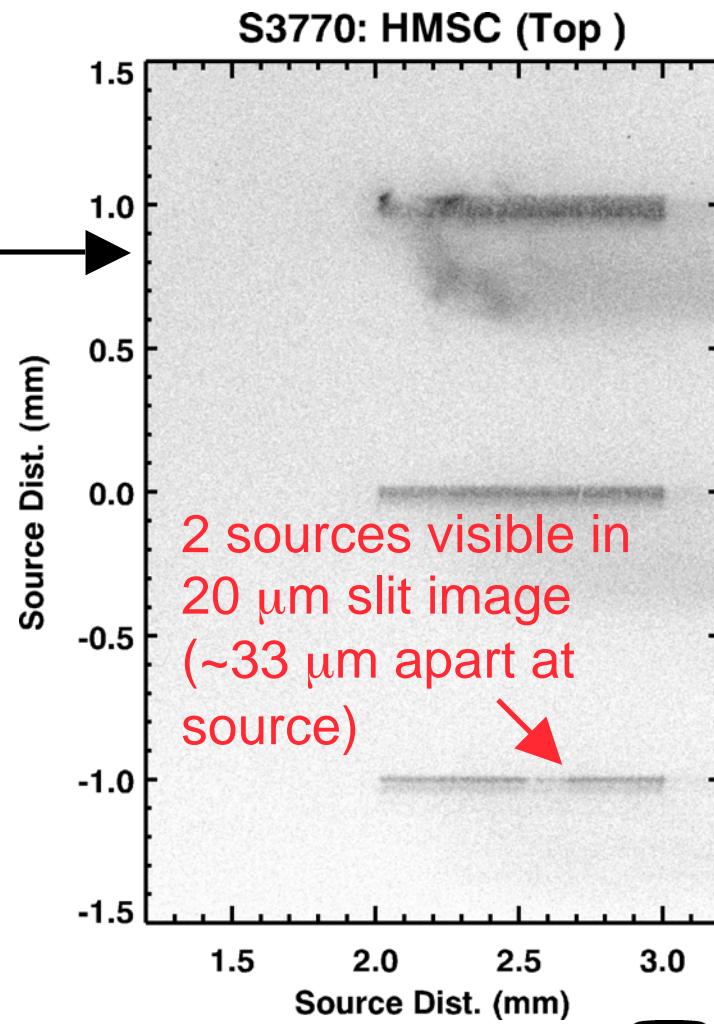
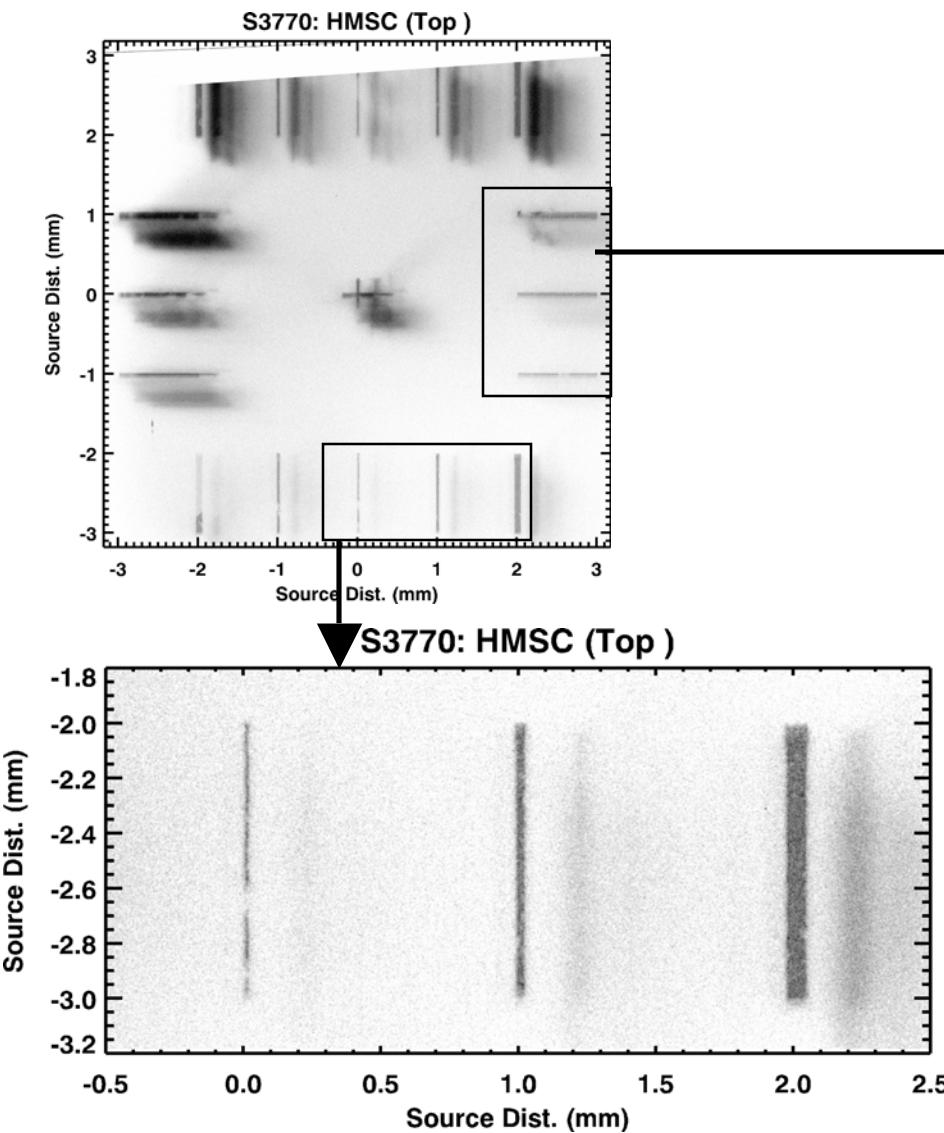
Single-array X-pinch scan consistent with linear scaling of mass/length with current

- XP wire arrays
[30 mm tall, 20 mm diam]
 - S3734: 128 x 75 μm W
(108 mg/cm)
 - S3735: 64 x 53 μm W
(27 mg/cm)
 - S3736: 32 x 53 μm W
(13.6 mg/cm)
- Arrays probably
overtwisted, making the
necks relatively long





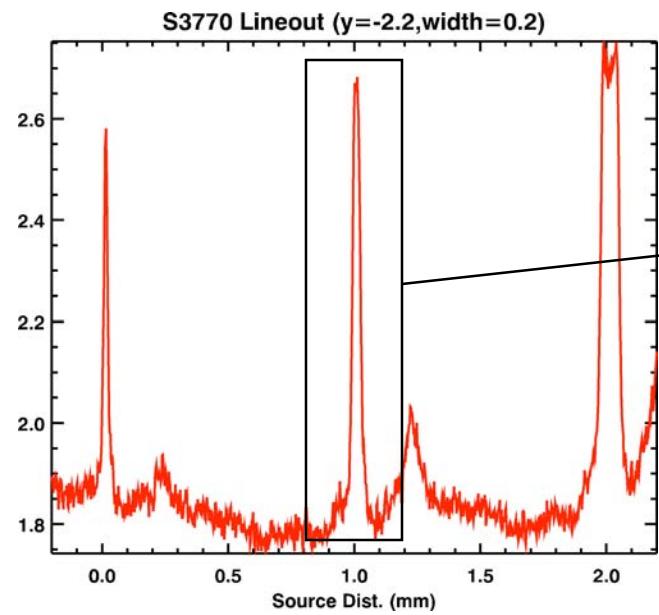
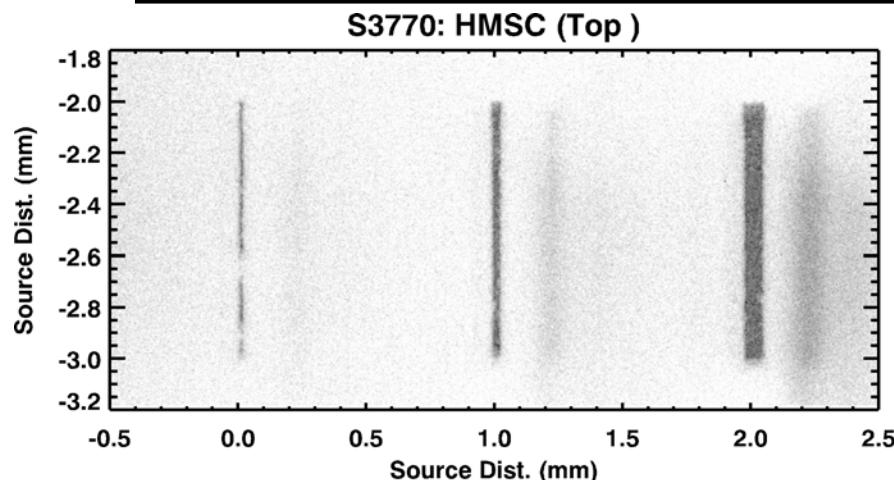
Example slit images from a solid X-pinch test (S3770)



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Laboratories

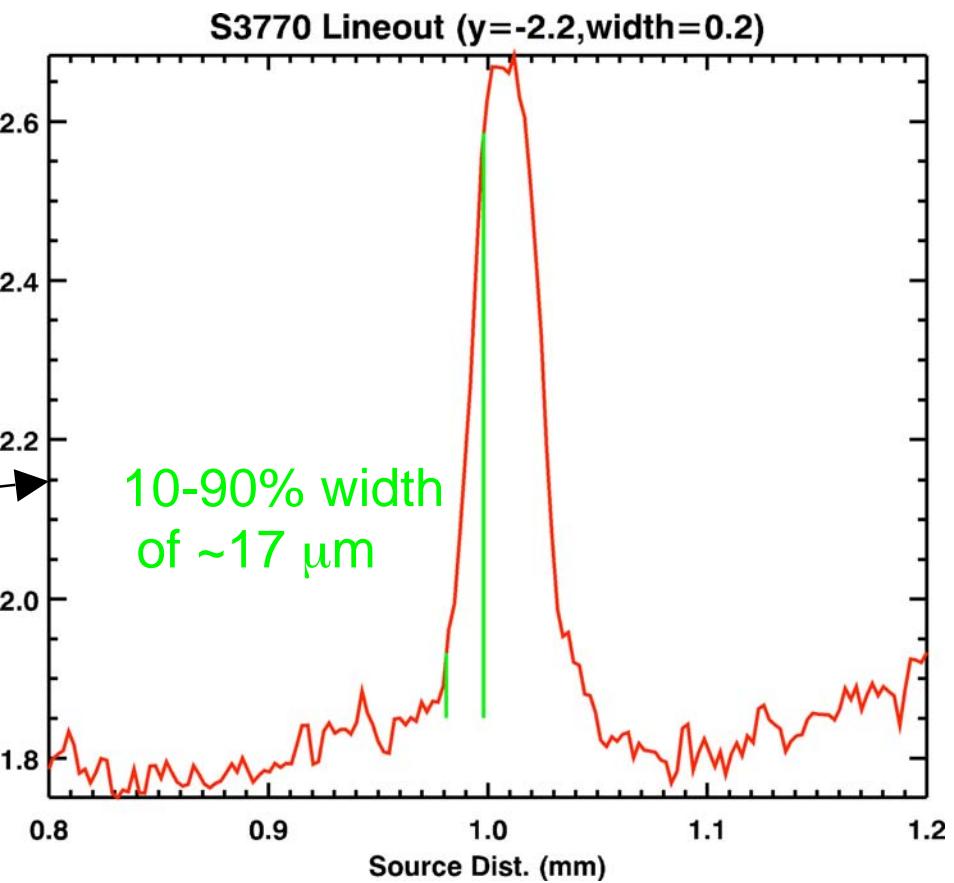


Lineouts consistent with a source size $\leq 17 \mu\text{m}$ diameter (~diffraction limit)



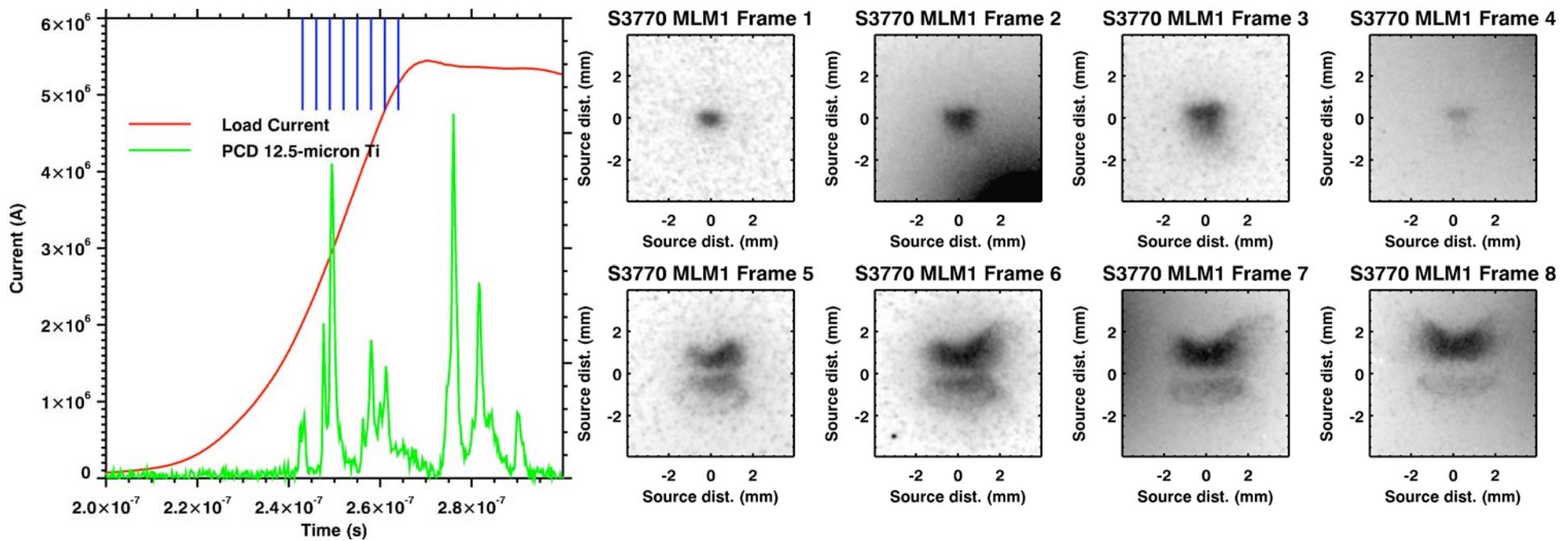
Fresnel diffraction limit:

$$\delta \sim \sqrt{\lambda d} \sim \sqrt{(3.6 \text{\AA})(1.1 \text{m})} \sim 20 \mu\text{m}$$





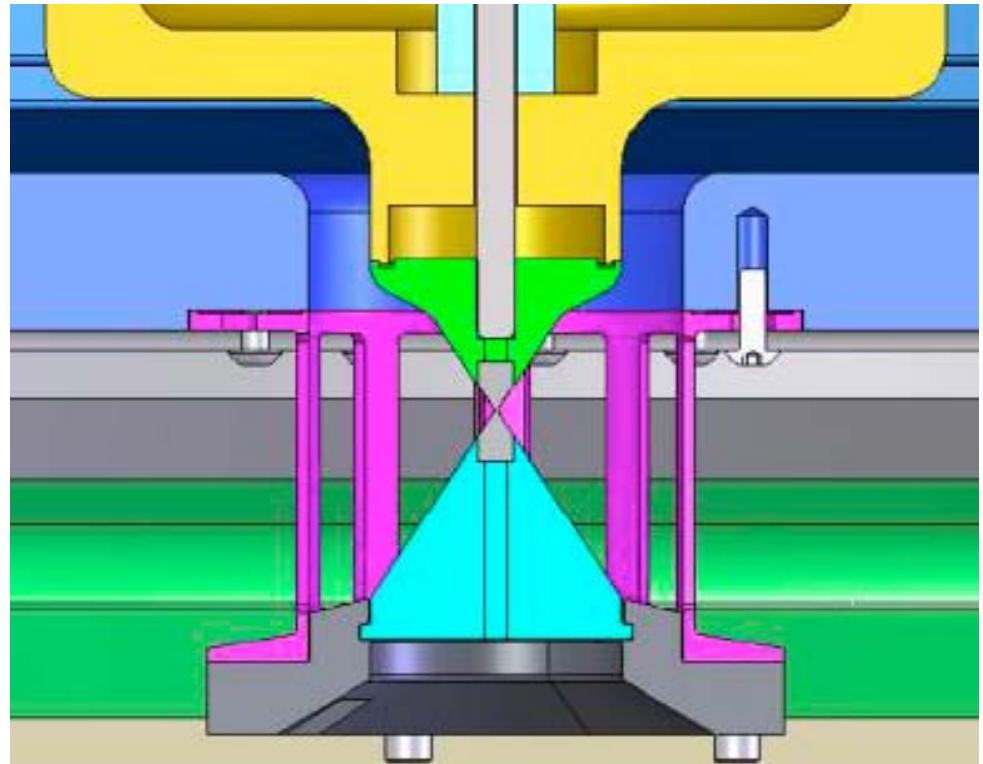
MLM pinhole images may imply small x-ray spots made early in pulse (2-3 MA)



PCD has same filtration as 1/2 of slit camera images
MLM images are in soft 277 eV x rays, but show global dynamics
Mass/length ~ 14 mg/cm, probably needs to increase
Early timing consistent with ongoing simulations (Chittenden, Yu)

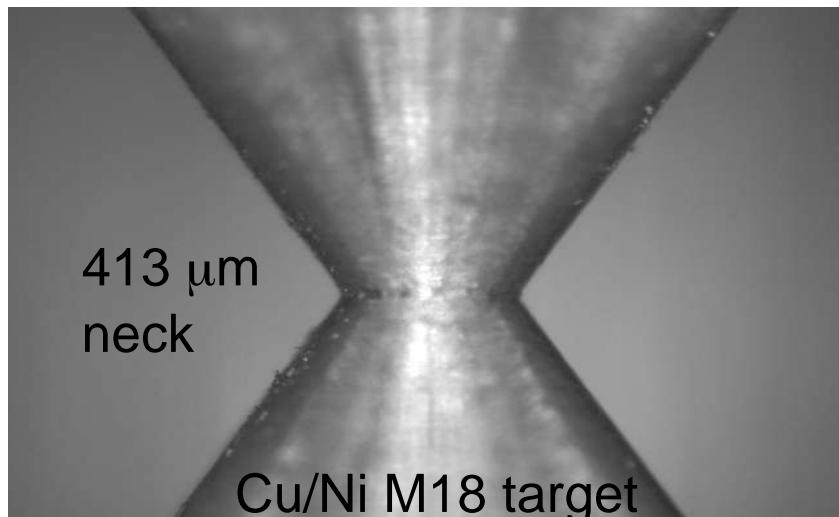
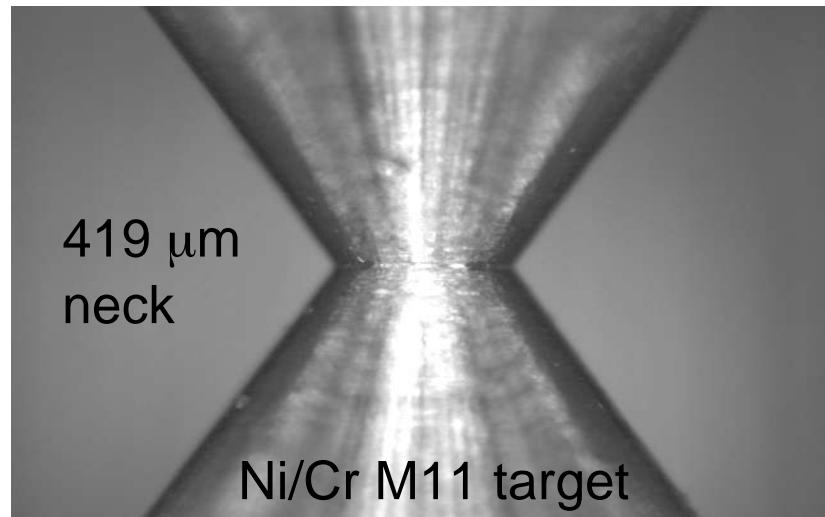
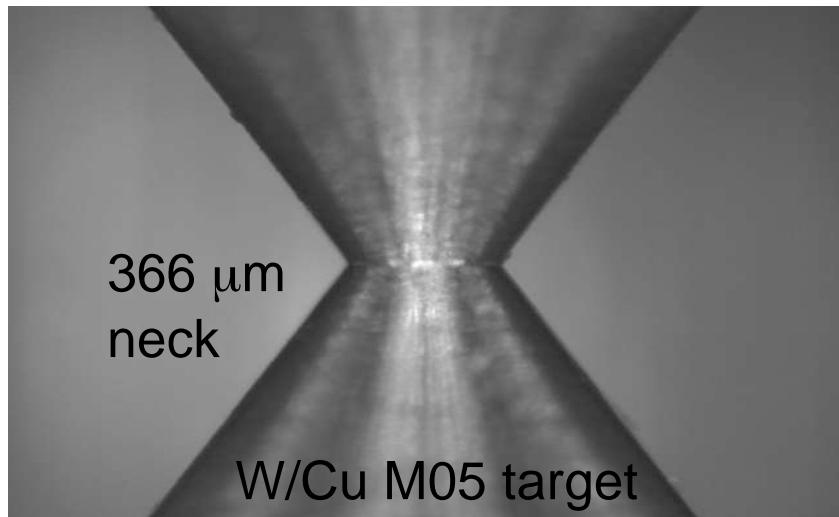


Load Hardware





Photos of cross-point region





Measured roughness of W/Cu X-pinch “Hourglass” (Cylindrical Portion)

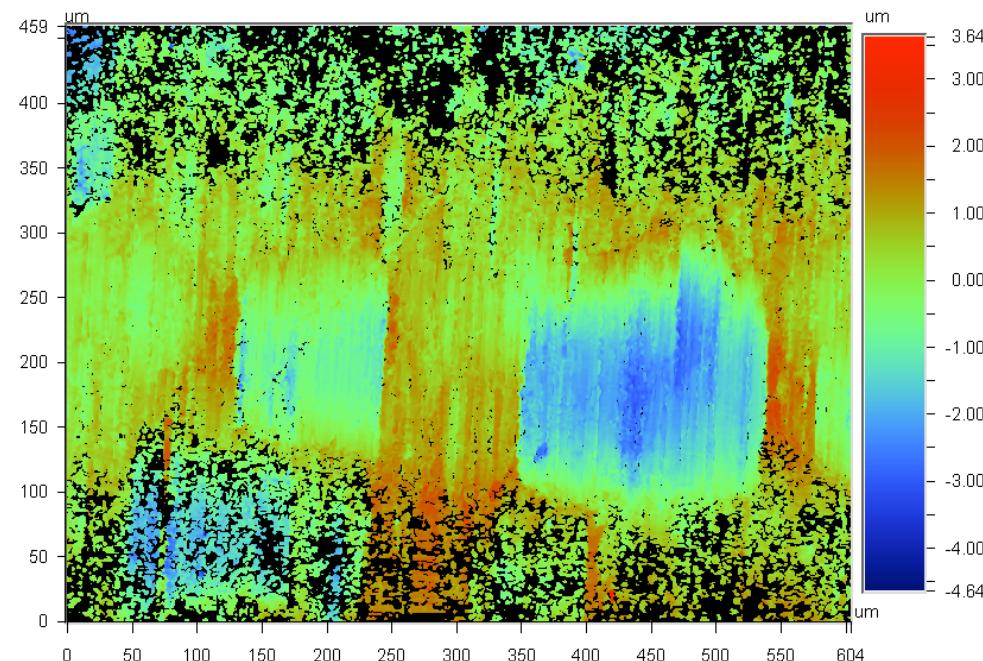


Mag: 10.2 X
Mode: VSI

Surface Data

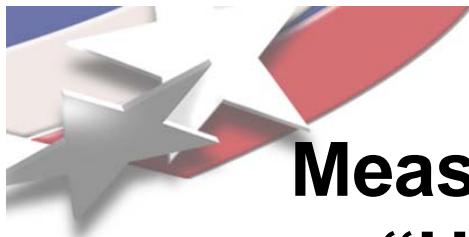
Date: 02/19/200
Time: 12:29:12

Surface Statistics:	
Ra:	741.33 nm
Rq:	936.86 nm
Rz:	5.94 um
Rt:	8.28 um
Set-up Parameters:	
Size:	736 X 480
Sampling:	821.67 nm
Processed Options:	
Terms Removed:	
Cylinder & Tilt	
Filtering:	
None	



Title: P300-0094-000A P05

Note:



Measured roughness of Cu/Ni X-pinch “Hourglass” (Cylindrical Portion)



Mag: 10.2 X
Mode: VSI

Surface Data

Date: 02/18/200
Time: 15:34:21

Surface Statistics:

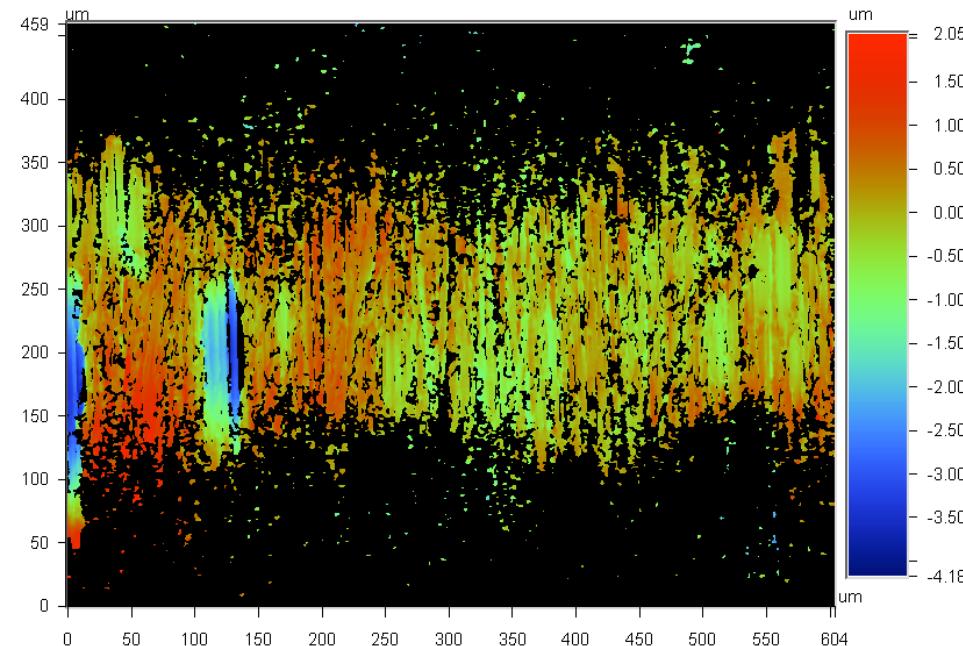
Ra: 449.61 nm
Rq: 662.64 nm
Rz: 5.56 um
Rt: 6.23 um

Set-up Parameters:

Size: 736 X 480
Sampling: 821.67 nm

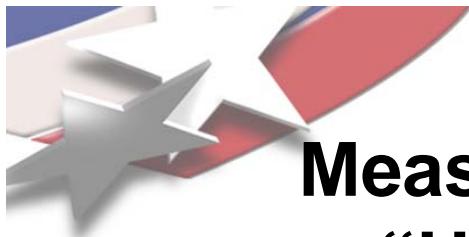
Processed Options:

Terms Removed:
Cylinder & Tilt
Filtering:
None



Title: x-pinch.090120M18

Note: cylinder portion



Measured roughness of Ni/Cr X-pinch “Hourglass” (Cylindrical Portion)



Mag: 10.2 X
Mode: VSI

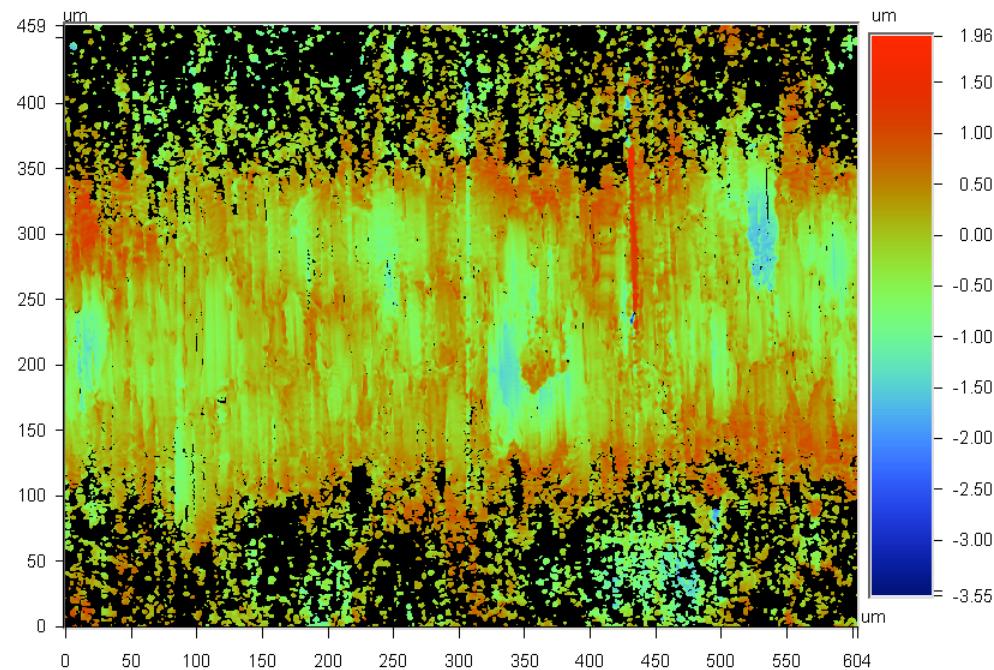
Surface Data

Date: 02/19/200
Time: 12:40:42

Surface Statistics:
Ra: 351.56 nm
Rq: 450.16 nm
Rz: 3.89 μ m
Rt: 5.51 μ m

Set-up Parameters:
Size: 736 X 480
Sampling: 821.67 nm

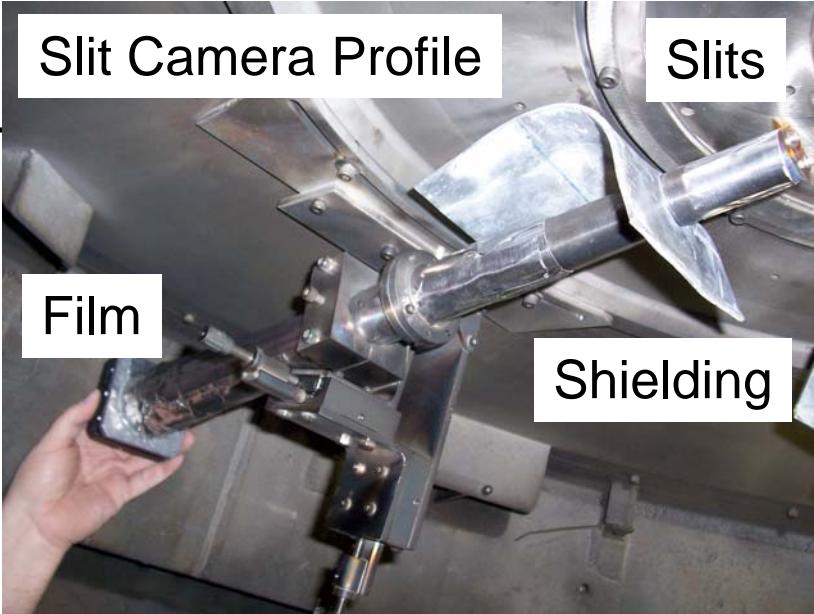
Processed Options:
Terms Removed:
Cylinder & Tilt
Filtering:
None



Title: P300-0095-000A 10
Note:



In-chamber Hardware Photos



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National
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Shielding was damaged each shot from spokes in return can flying outward

