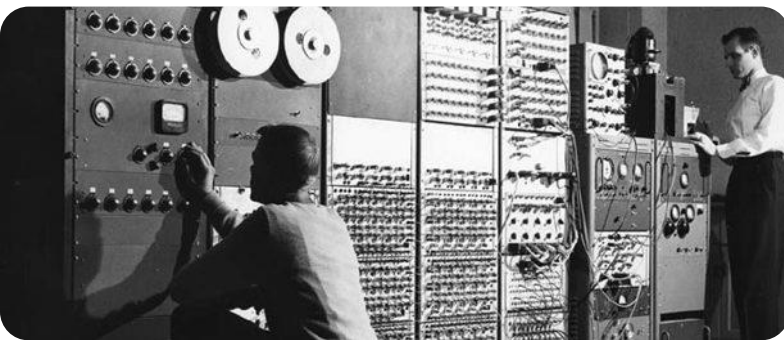


Exceptional service in the national interest



Calibrating Data from the Leo Brady Seismic Network

Brian YOUNG, Robert E. ABBOTT

Instrument Sensitivity

Leo Brady—Data we've got

REVISED 10/17/67

SEISMIC FIELD SHEET...Page 5

TAPE CHANNEL 5 DATA

6819-1

VCO FREQUENCY in CPS	INSTRUMENT	CAL db PTA <u>0</u> PAD	RUN db PTA <u>0</u> PAD	BAND EDGE SENS.*	ELECTR. GAIN	CAL BATT. VOLTS
1120	TSP÷5	48	96	.5v		.45v
1300	TSP×1		↓			
1480	RSP÷25		84			
1660	RSP÷5		↓			
1840	RSP×1		↓			
2030	VSP÷25		84			
2230	VSP÷5		↓			
2450	VSP×1	↓	↓	↓		↓

* Band Edge = 100% of bandwidth

SHORT PERIOD WEIGHT LIFTS

VERTICAL 10.8 DIV. @ 48 db
 RADIAL 14.9 DIV. @ 48 db
 TANGENTIAL 12 DIV. @ 48 db

DAMPING

13:1
11:1
12:1

SHORT PERIOD WEIGHT/MICRONS

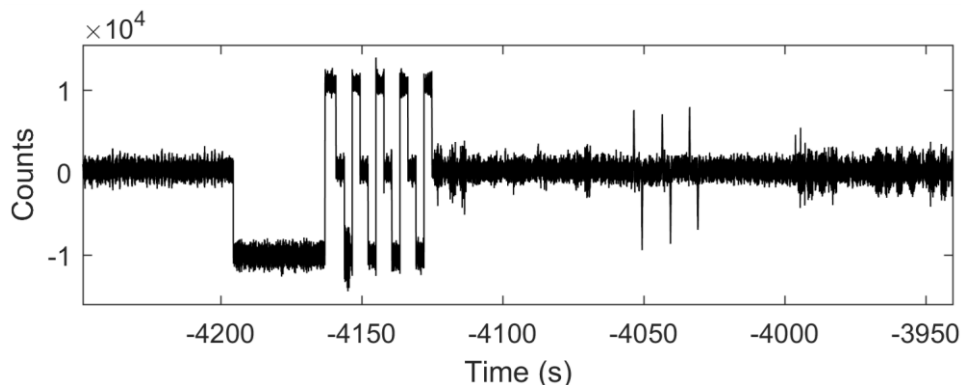
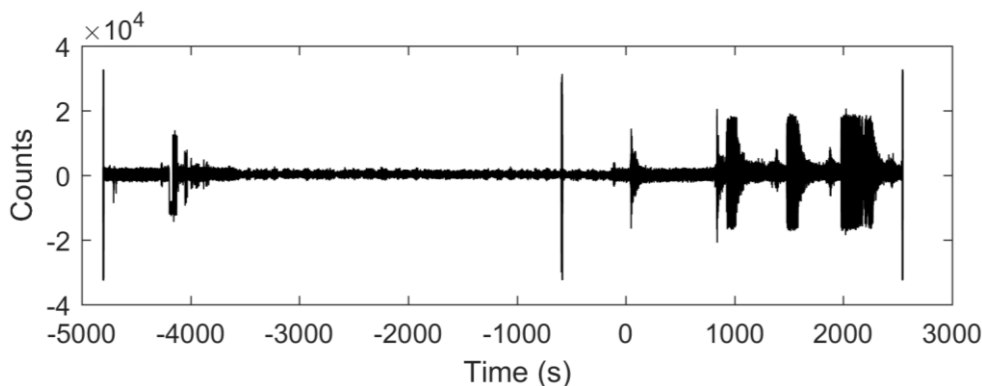
VERTICAL .255 gms. = .319 u
 RADIAL 2.000 gms. = .250 u
 TANGENTIAL 2.000 gms. = .250 u

NOC-23 CALIBRATION

VERTICAL DIV. @ db
 RADIAL/STS DIV. @ db
 RADIAL/NTS DIV. @ db

Seismic Arrival Time*

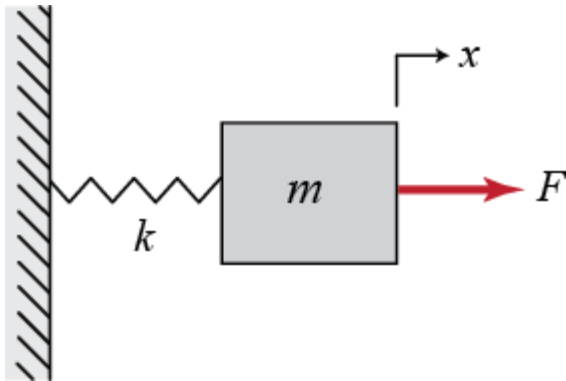
* Ely and Battle Mt. only. Other stations are noted on Field Data Sheet



Boxcar – Leeds – VSP÷5

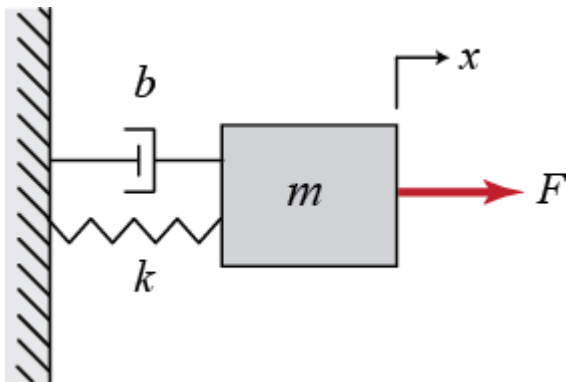
Seismometer theory in 2 slides

$$\sum F = 0 \quad F = ma \quad F = kx$$



$$m\ddot{x} + kx = 0$$

Cartoons: University of Michigan



$$m\ddot{x} + b\dot{x} + kx = 0$$

Seismometer:

$$\ddot{x} + 2\lambda\omega_0\dot{x} + \omega_0^2x = 0$$

Seismometer theory in 2 slides

Seismometer:

$$\ddot{x} + 2\lambda\omega_0\dot{x} + \omega_0^2x = 0$$

Initial conditions for weight lift:

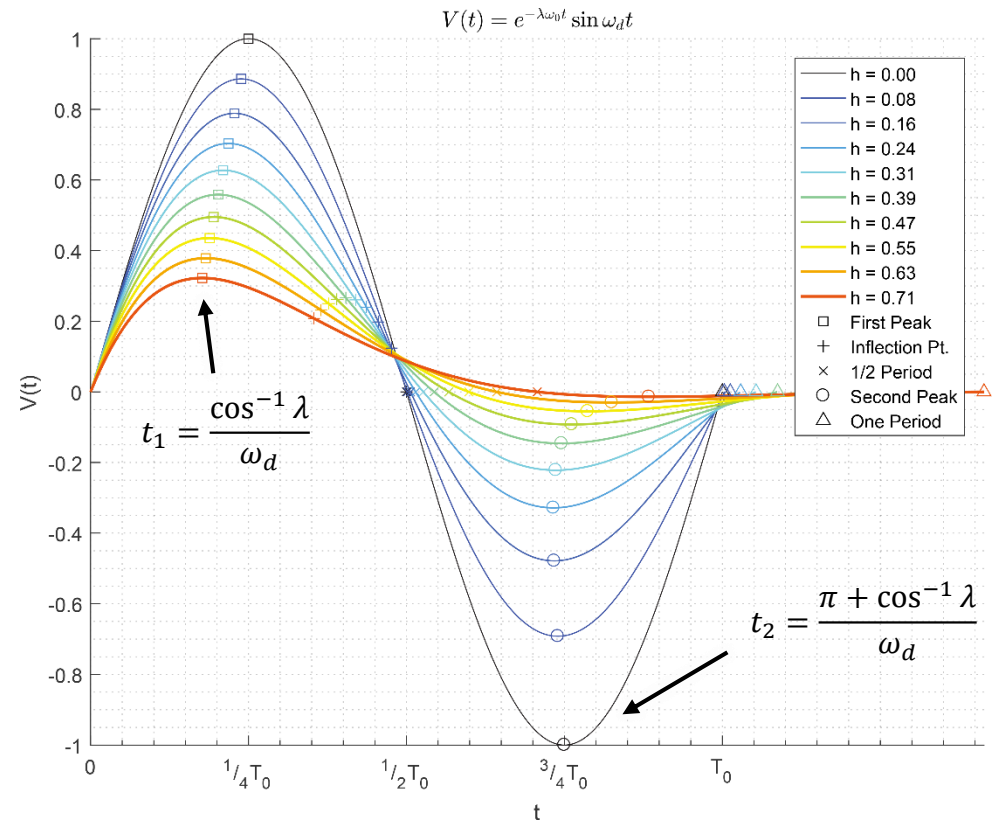
$$x(0) = x_0; \quad \dot{x}(0) = 0$$

Deflection (from Hooke's Law):

$$F = kx \Rightarrow x_0 = \frac{m_w g}{m_s \omega_0^2}$$

Electromagnetic seismometer:

$$V(t) = G\dot{x}(t) = -G \frac{m_w g}{m_s \omega_d} e^{-\lambda\omega_0 t} \sin \omega_d t \quad \omega_d = \omega_0 \sqrt{1 - \lambda^2}$$



Seismometer theory in 2 slides

Seismometer:

$$\ddot{x} + 2\lambda\omega_0\dot{x} + \omega_0^2x = 0$$

Initial conditions for weight lift:

$$x(0) = x_0; \quad \dot{x}(0) = 0$$

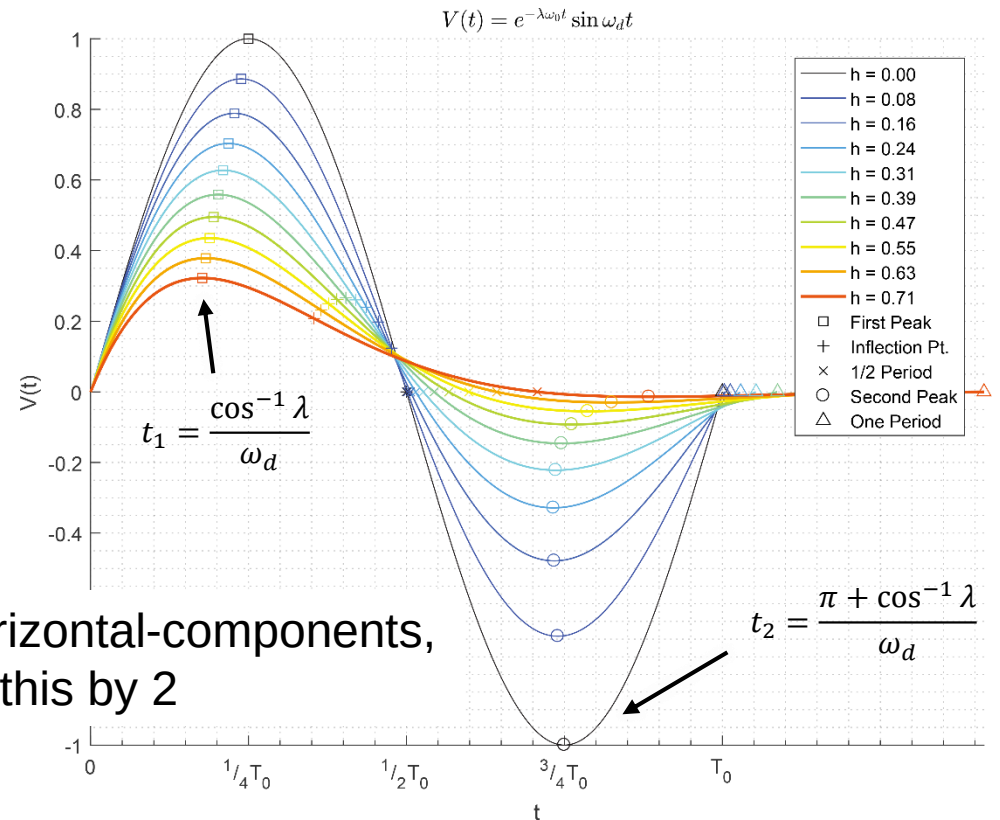
Deflection (from Hooke's Law):

$$F = kx \Rightarrow x_0 = \frac{m_w g}{m_s \omega_0^2}$$

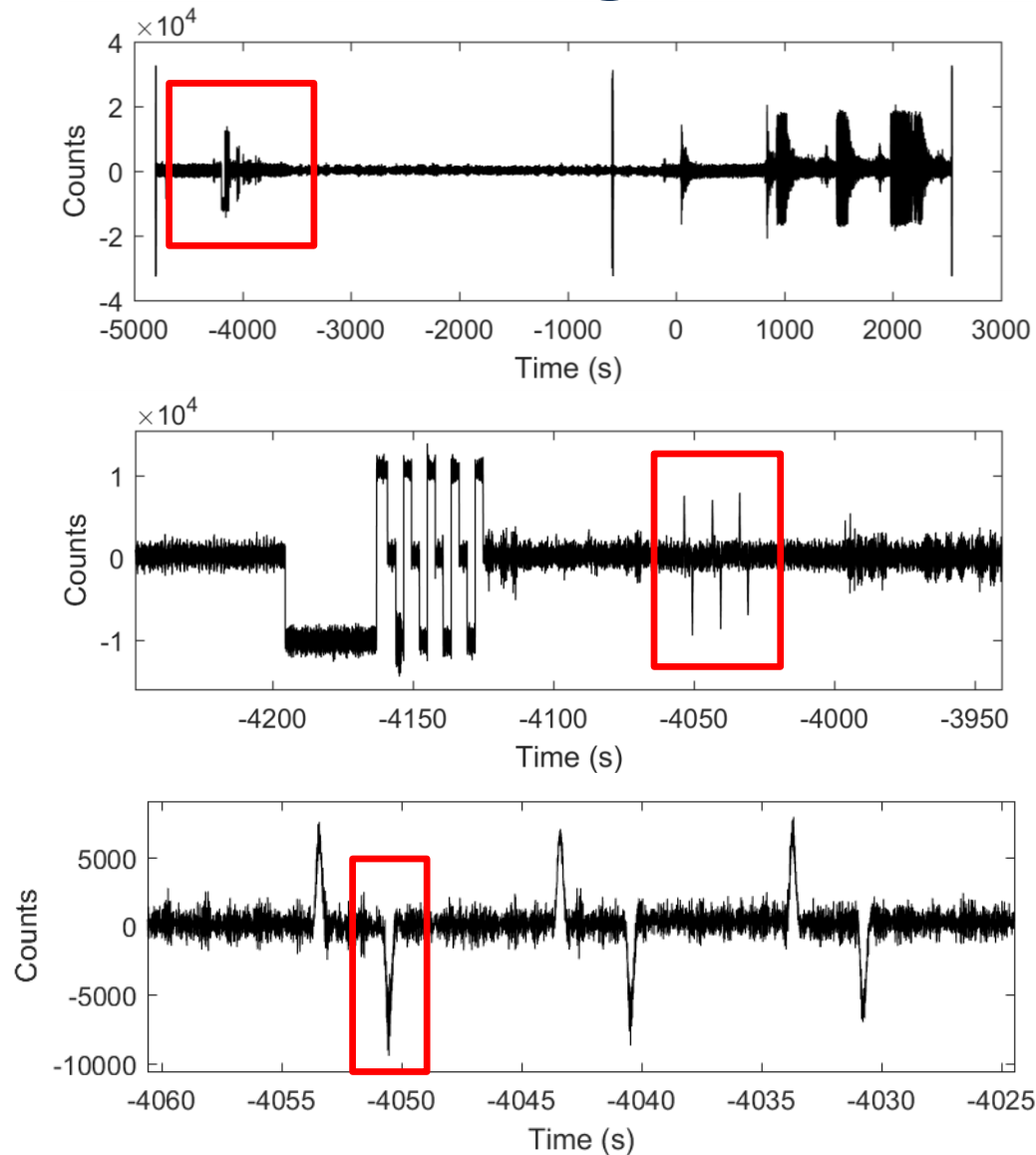
For horizontal-components,
Divide this by 2

Electromagnetic seismometer:

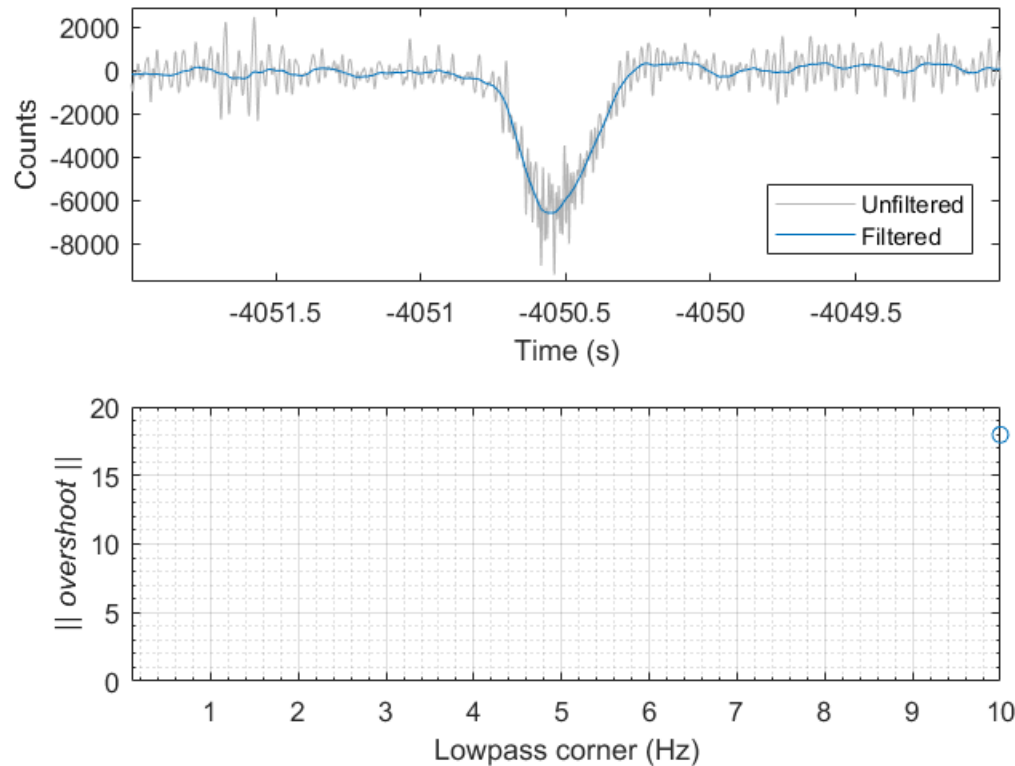
$$V(t) = G\dot{x}(t) = -G \frac{m_w g}{m_s \omega_d} e^{-\lambda\omega_0 t} \sin \omega_d t \quad \omega_d = \omega_0 \sqrt{1 - \lambda^2}$$



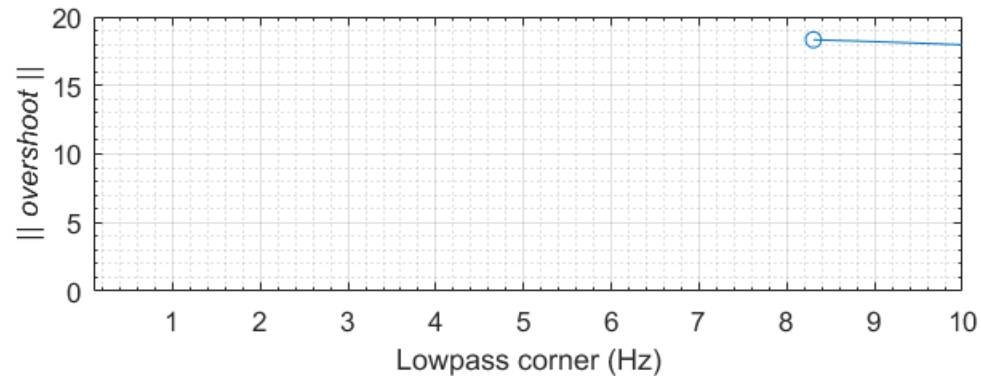
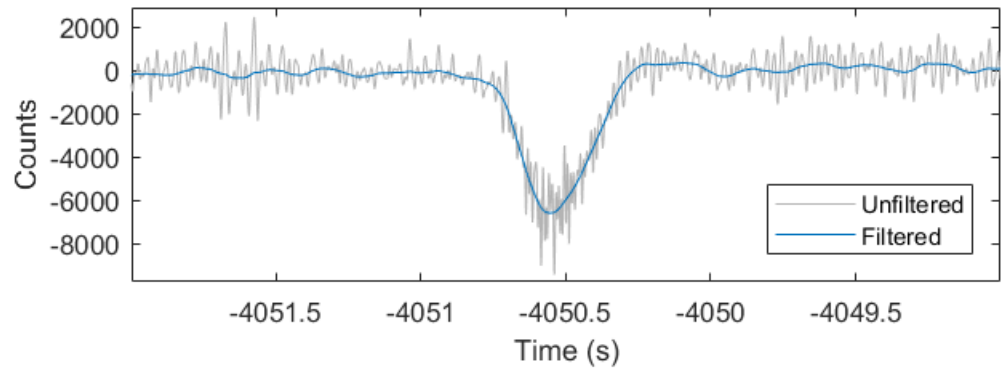
1. Locate the first weight lift



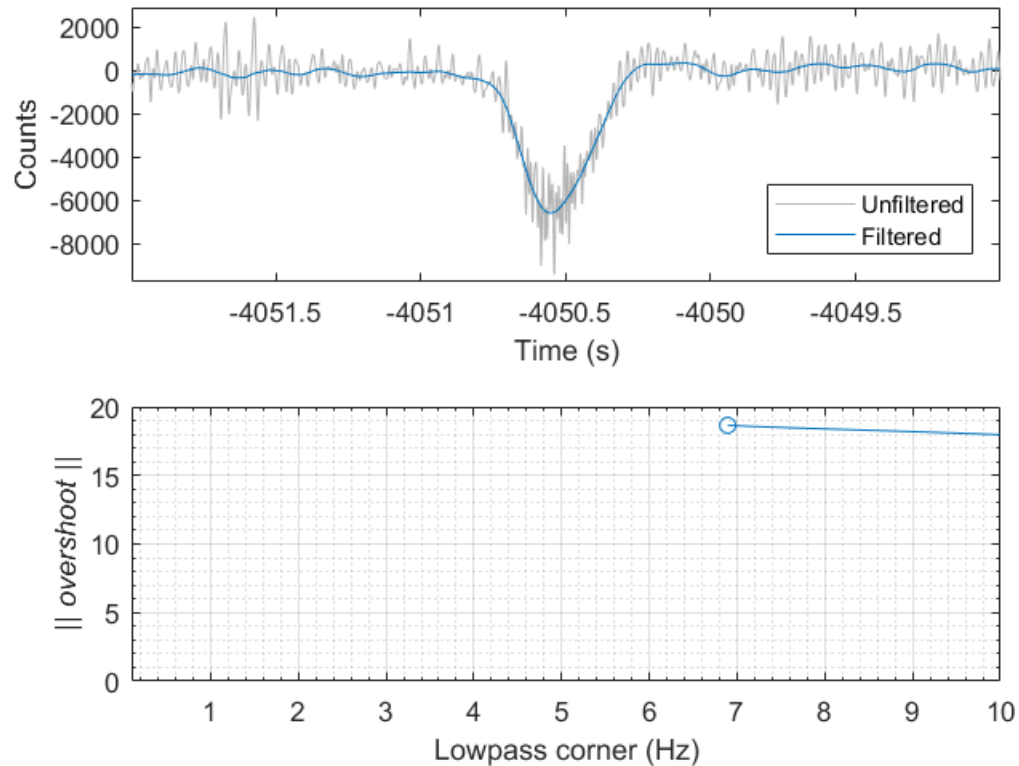
2. Recover the weight lift



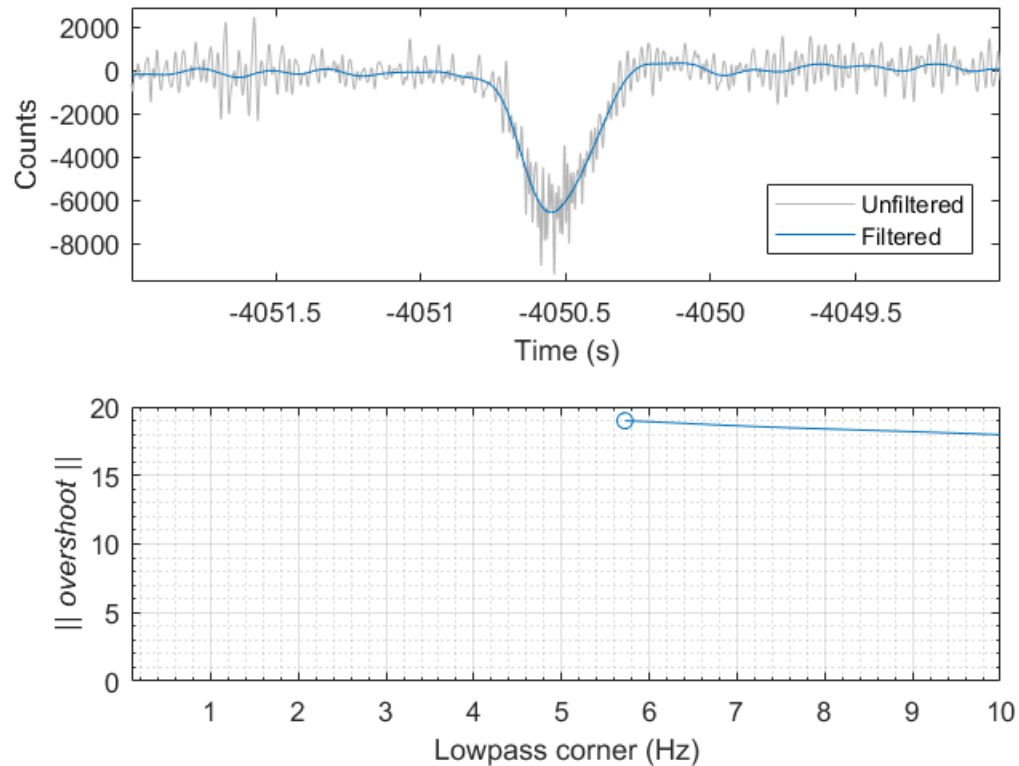
2. Recover the weight lift



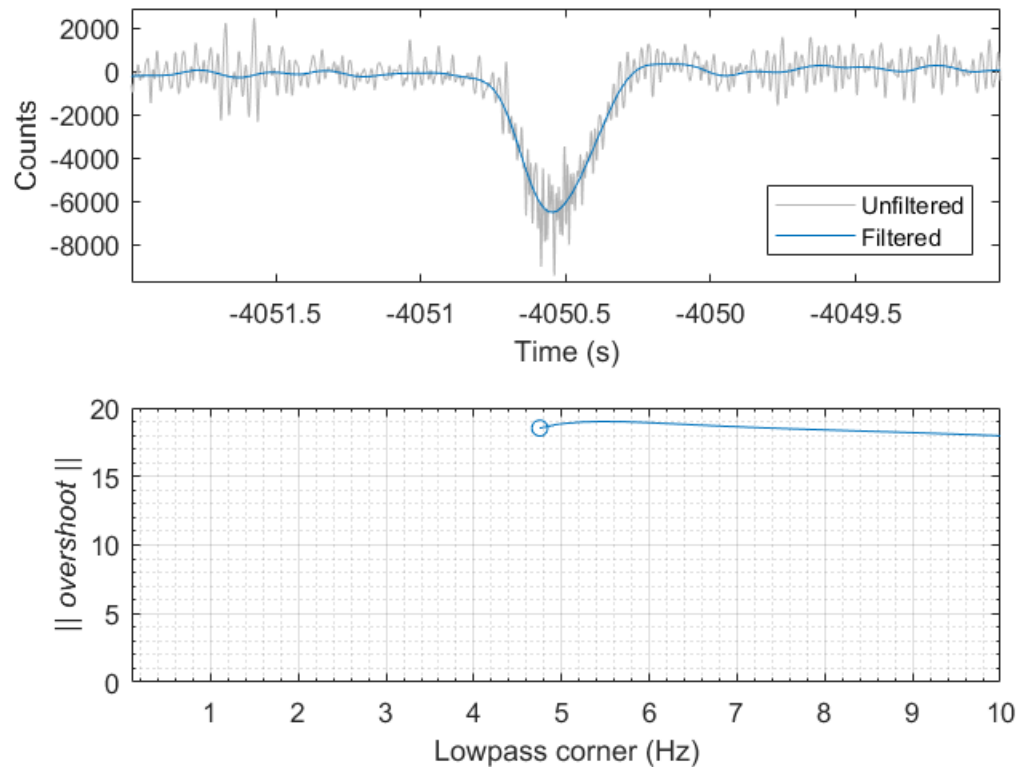
2. Recover the weight lift



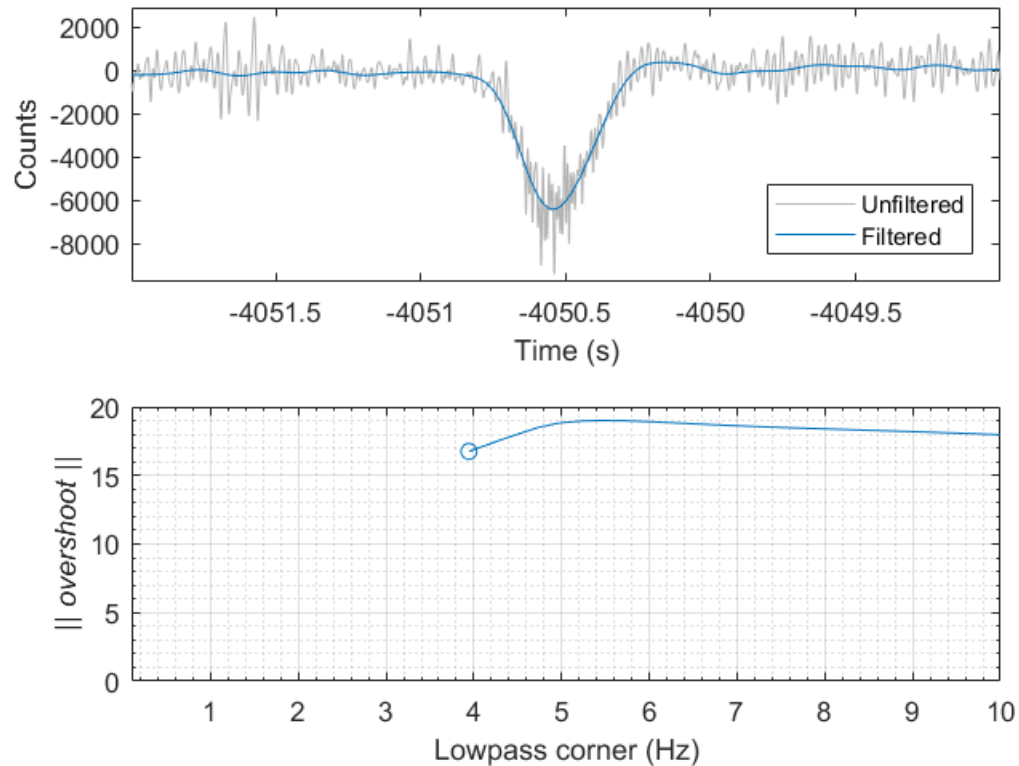
2. Recover the weight lift



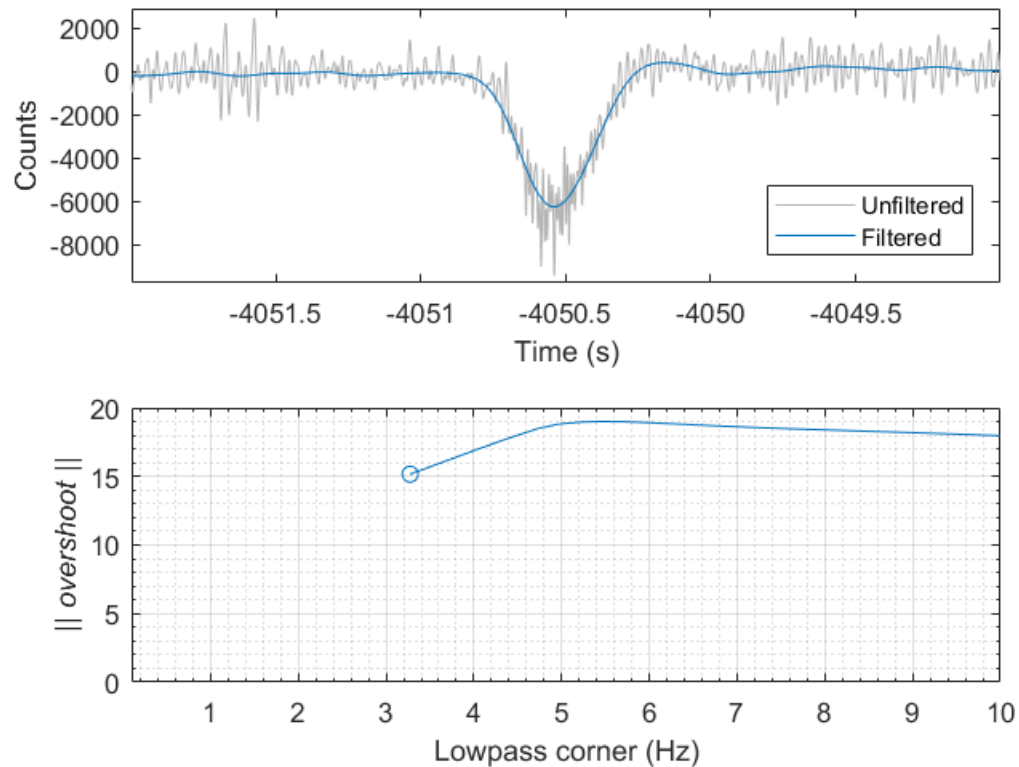
2. Recover the weight lift



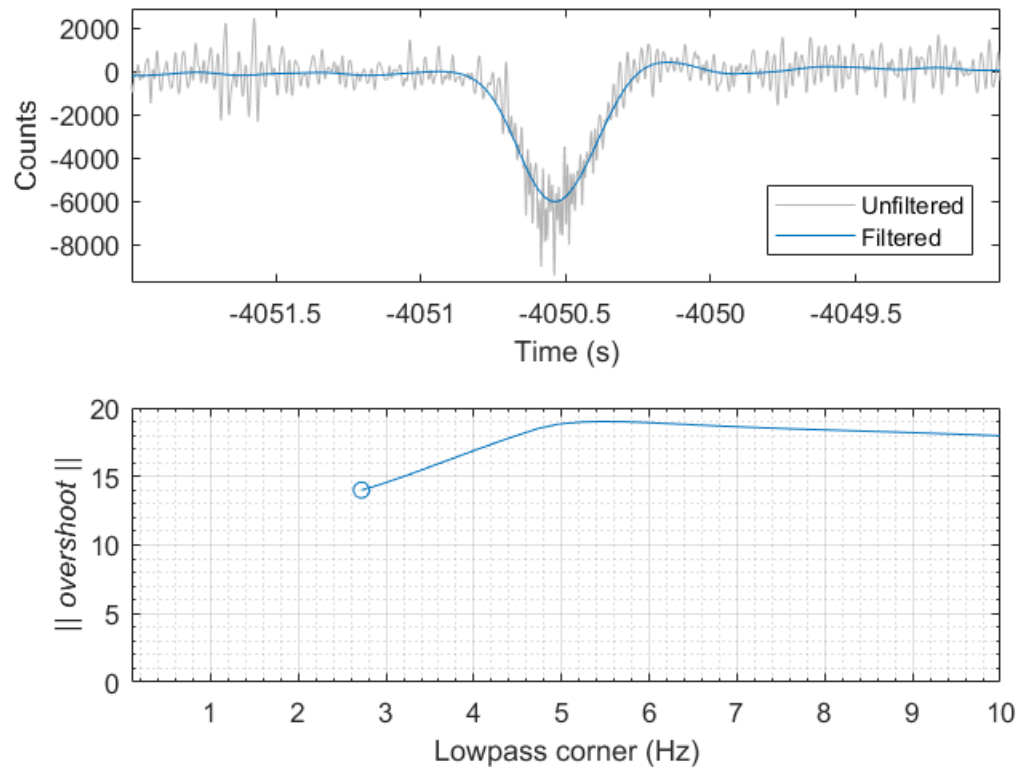
2. Recover the weight lift



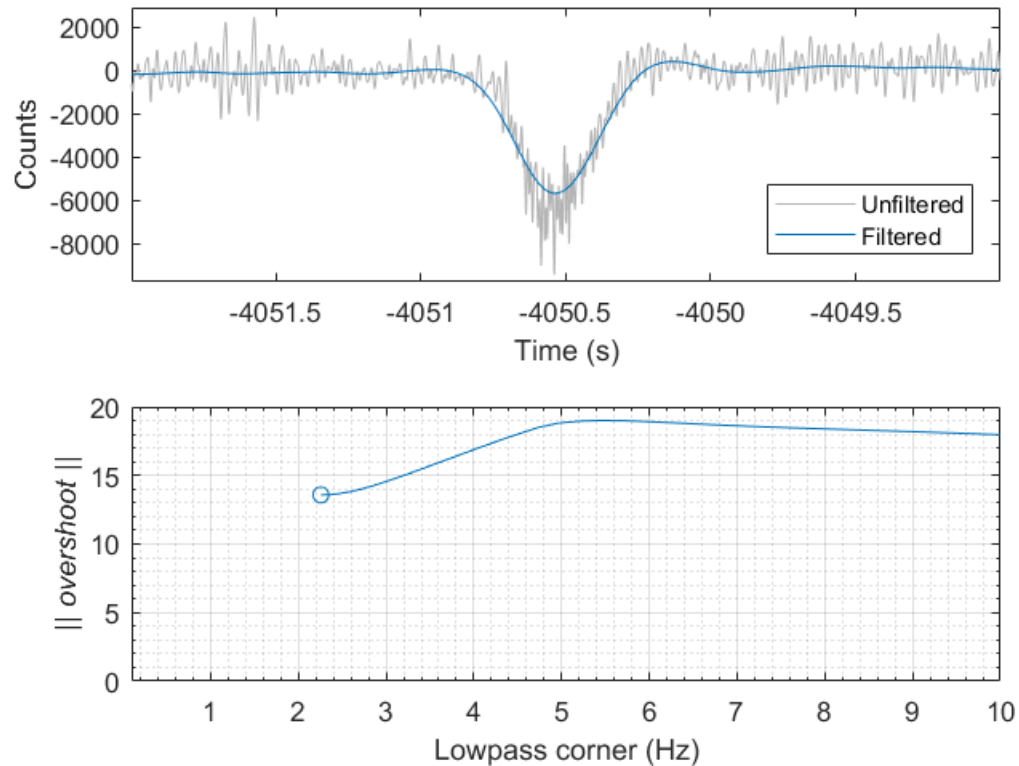
2. Recover the weight lift



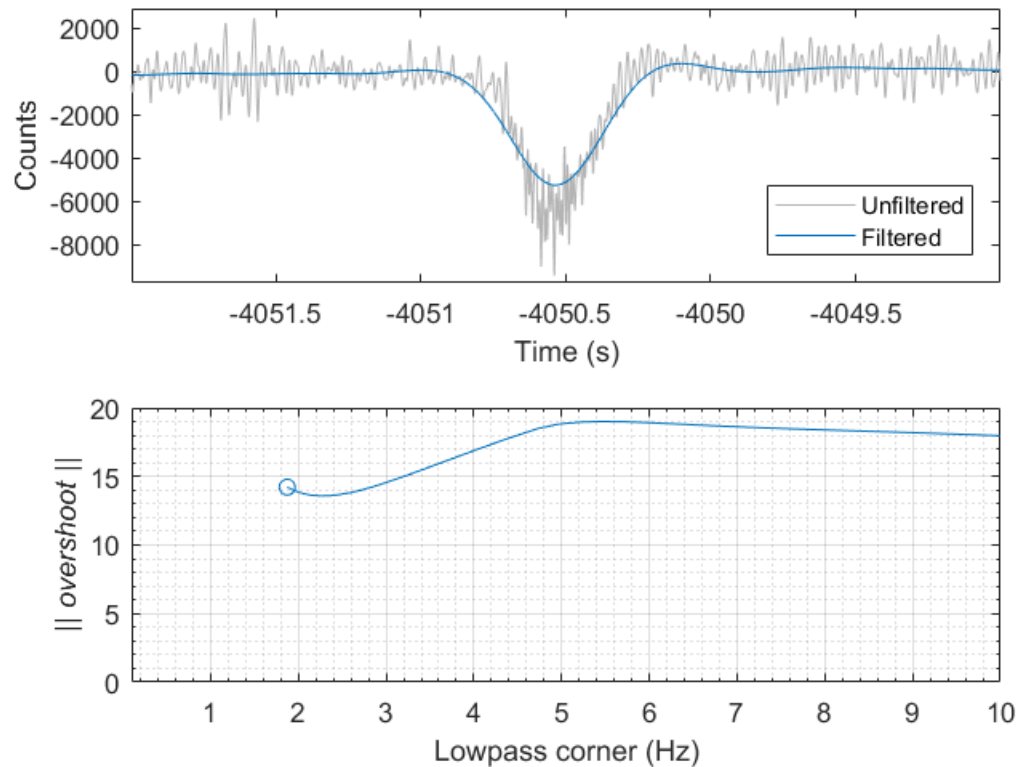
2. Recover the weight lift



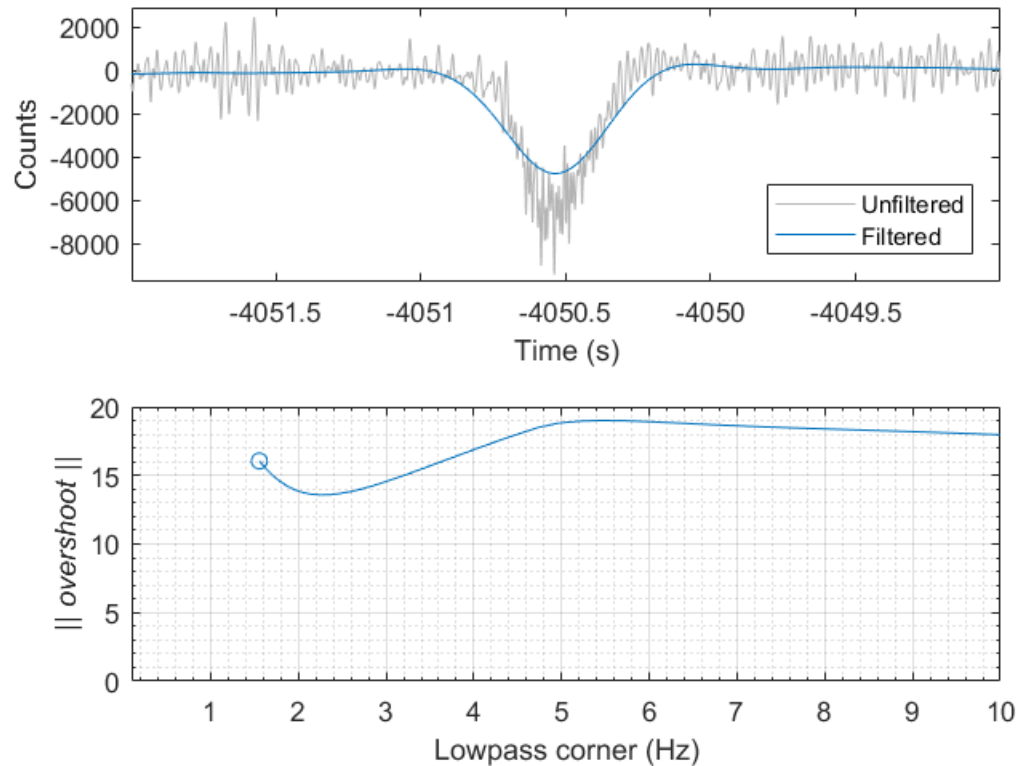
2. Recover the weight lift



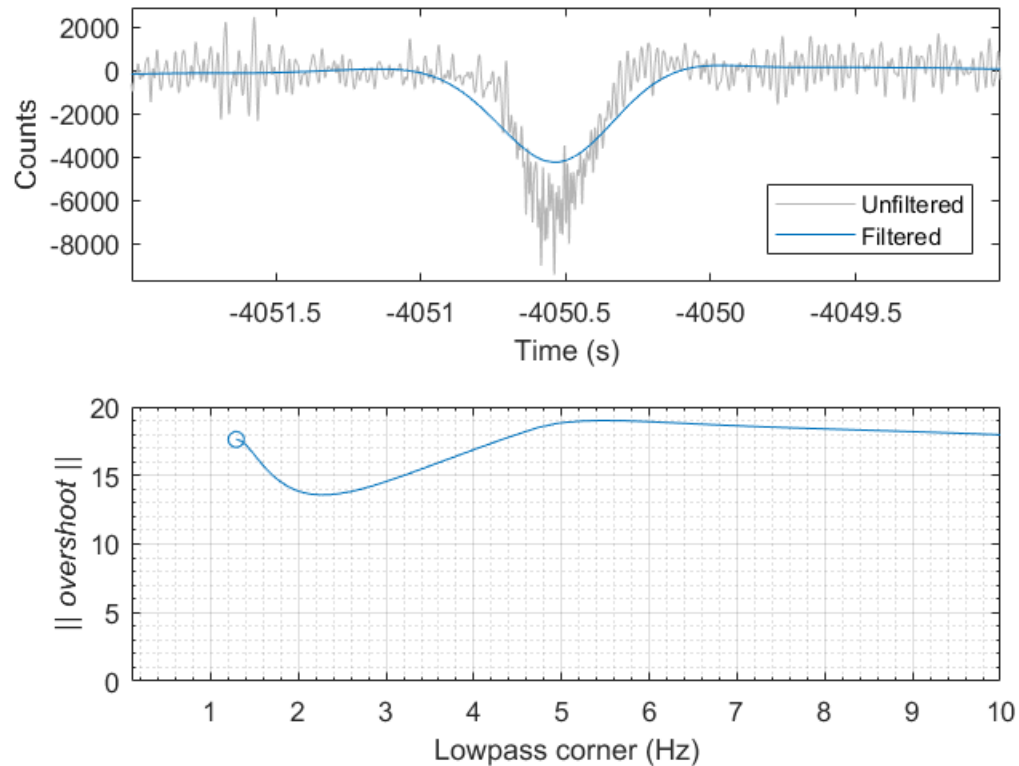
2. Recover the weight lift



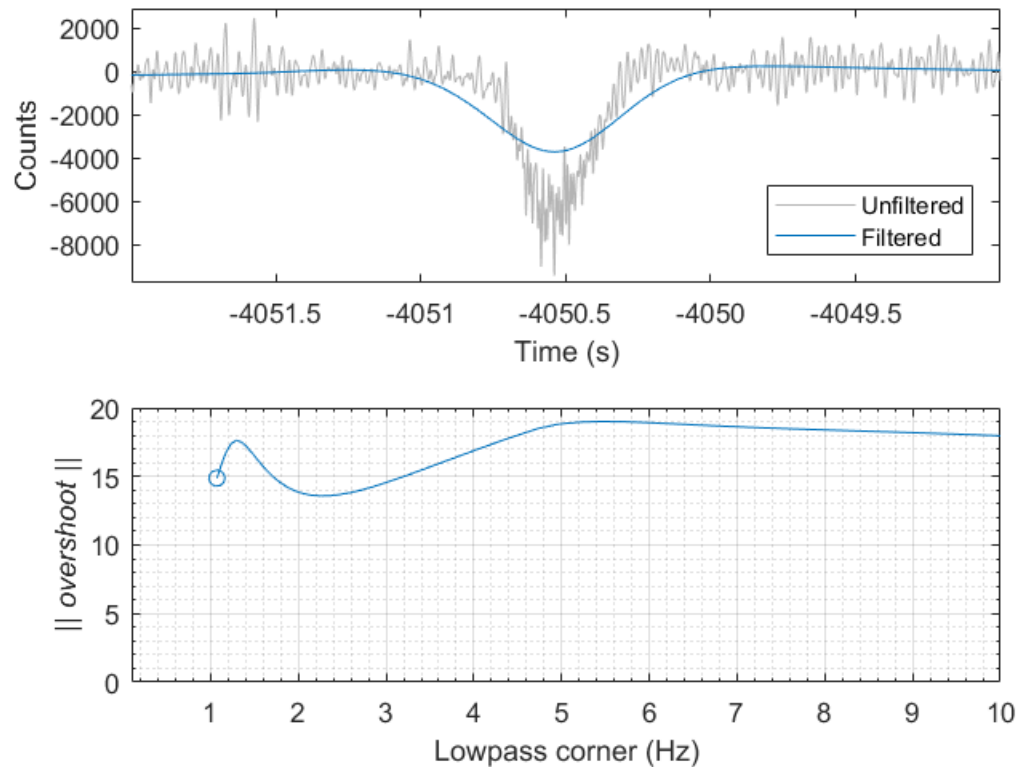
2. Recover the weight lift



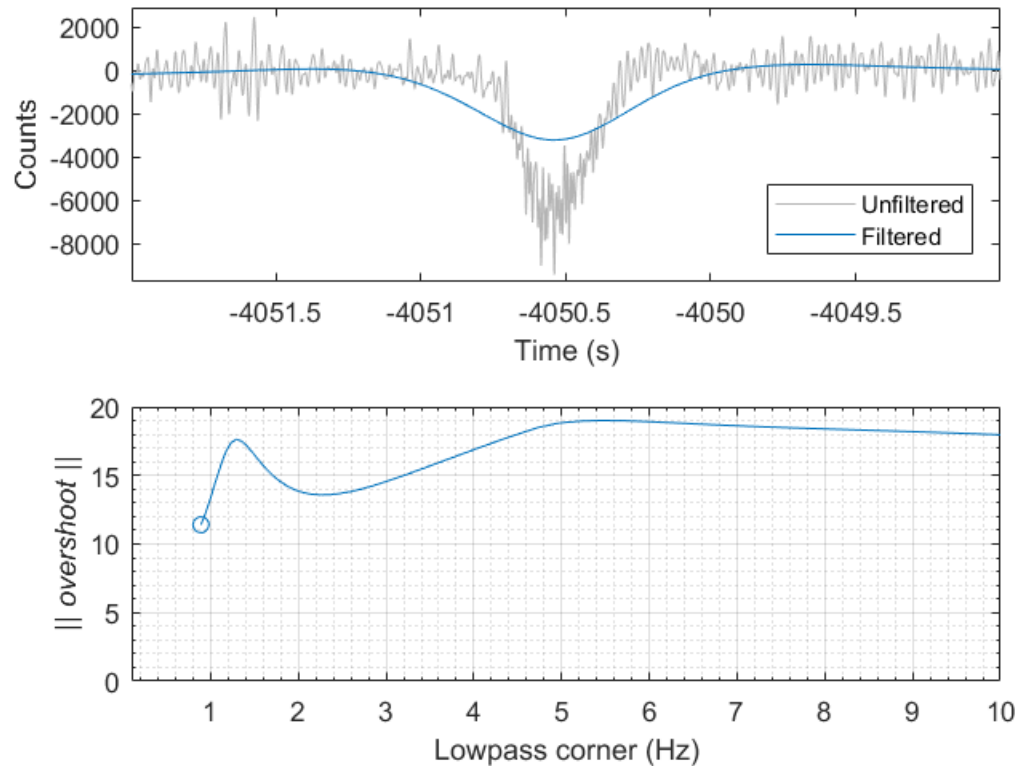
2. Recover the weight lift



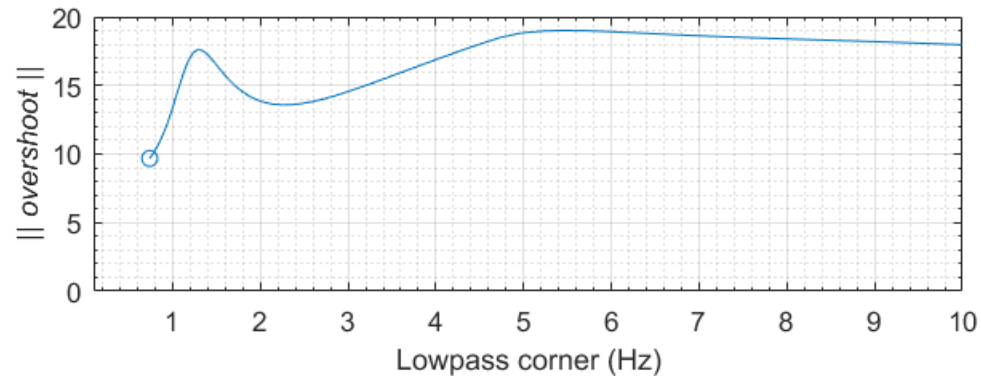
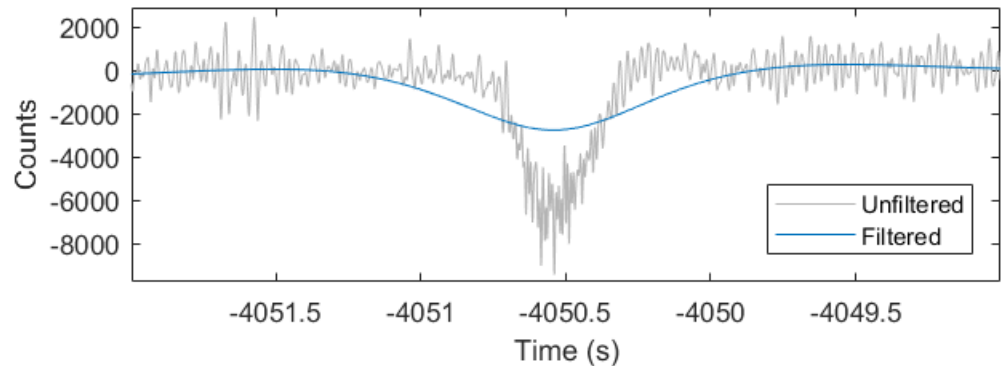
2. Recover the weight lift



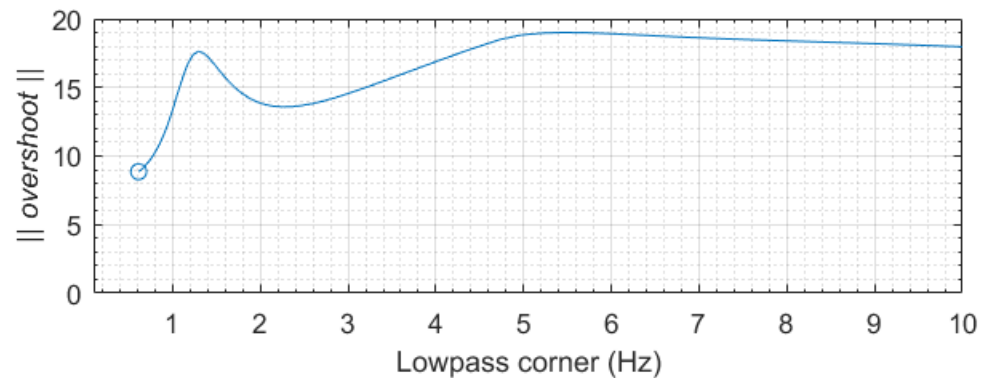
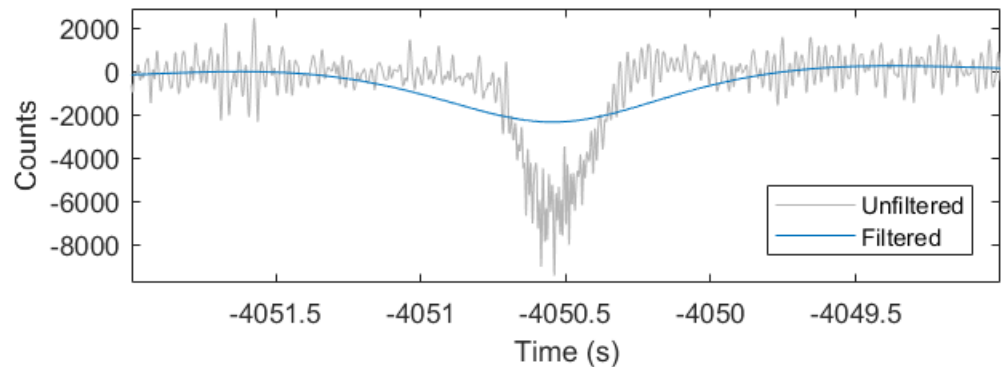
2. Recover the weight lift



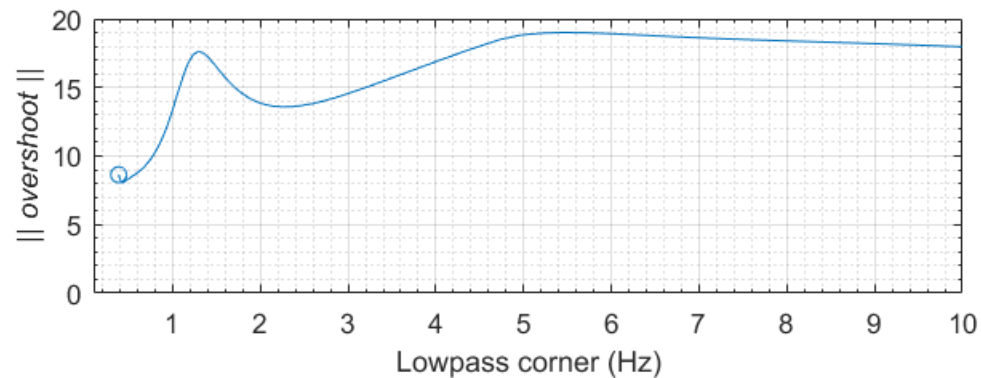
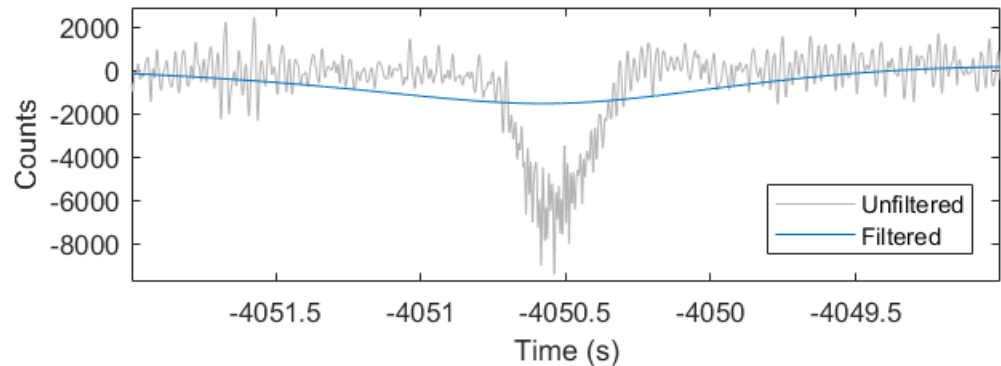
2. Recover the weight lift



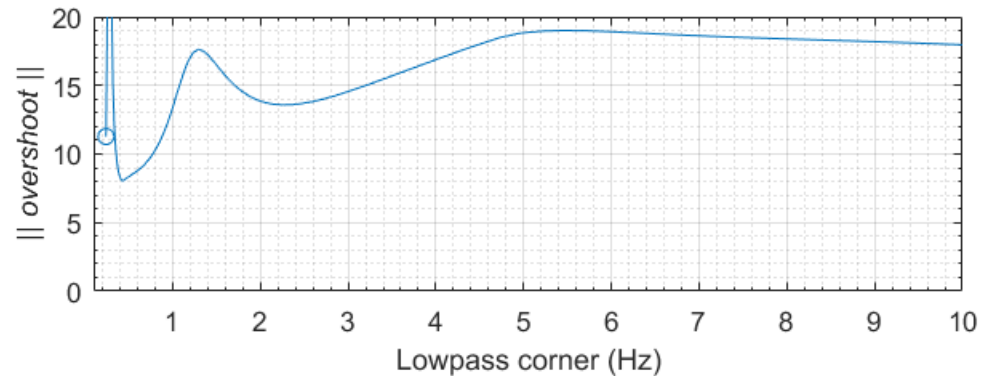
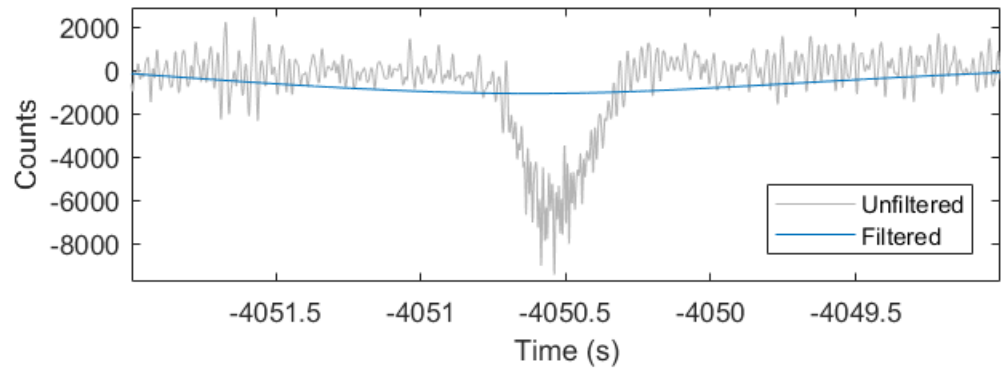
2. Recover the weight lift



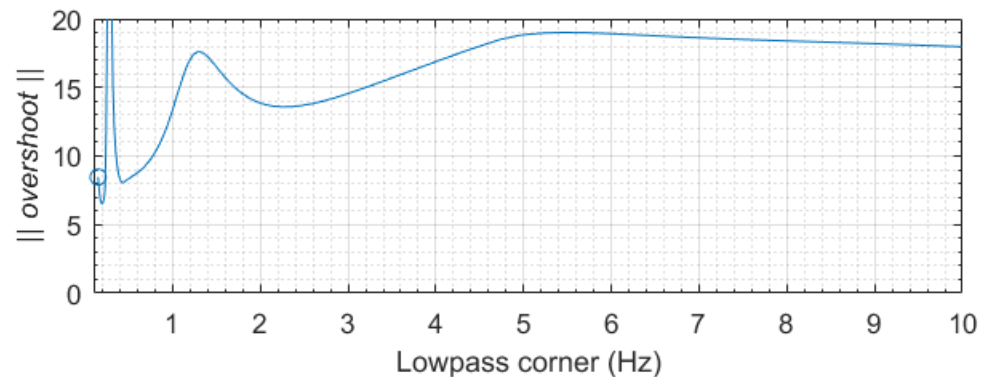
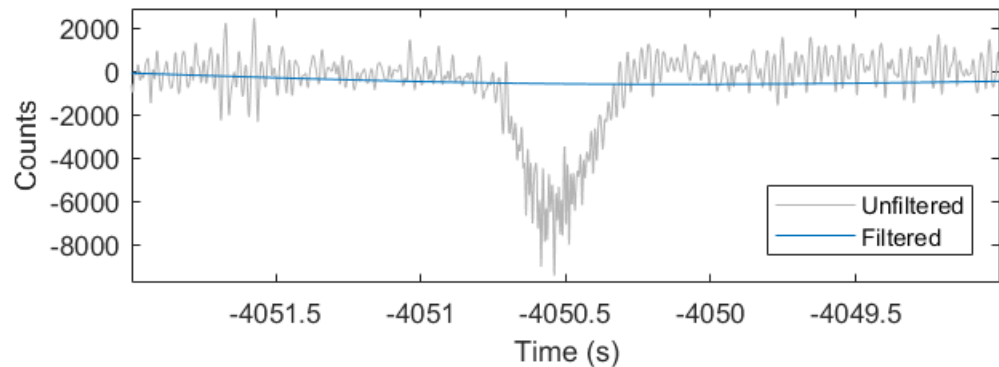
2. Recover the weight lift



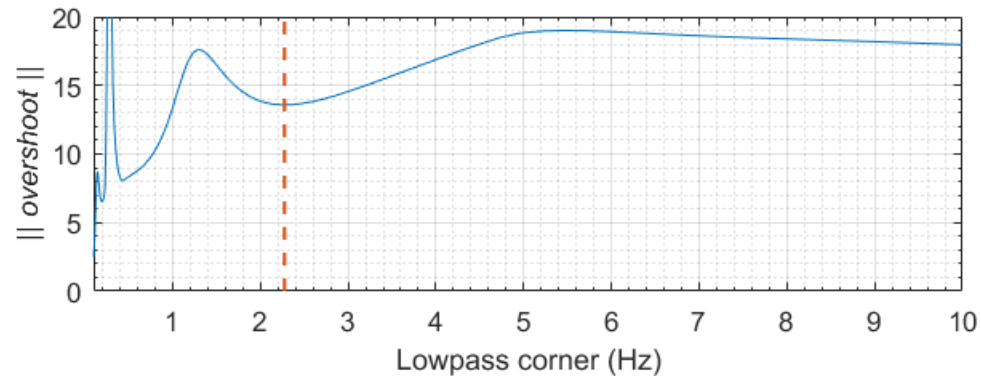
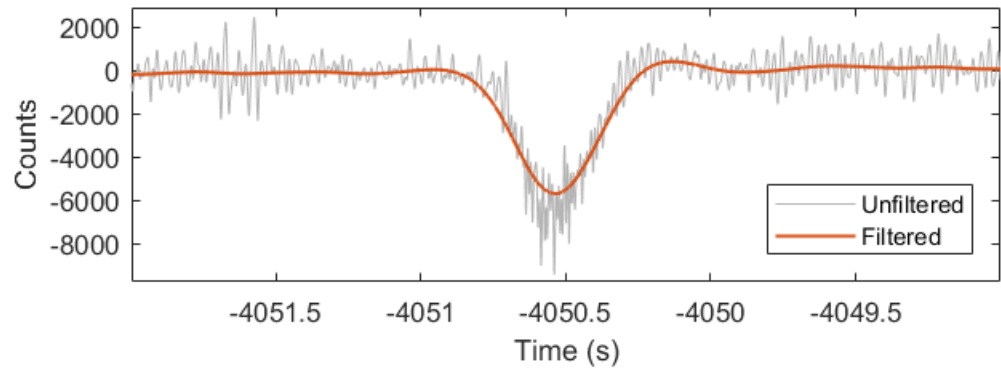
2. Recover the weight lift



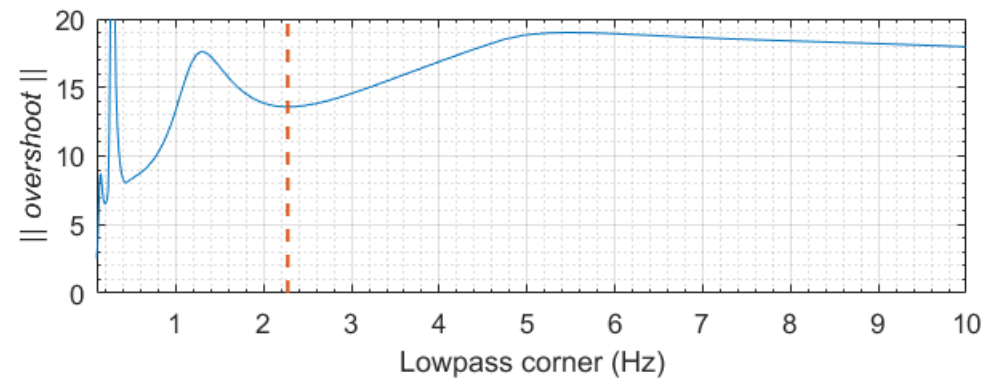
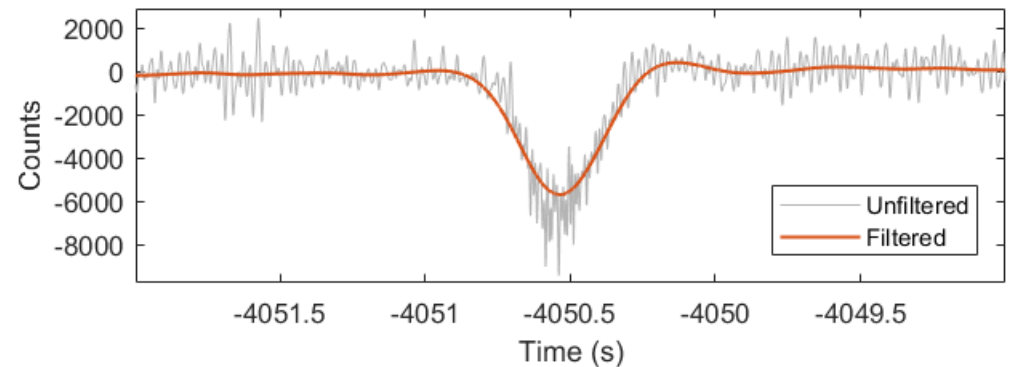
2. Recover the weight lift



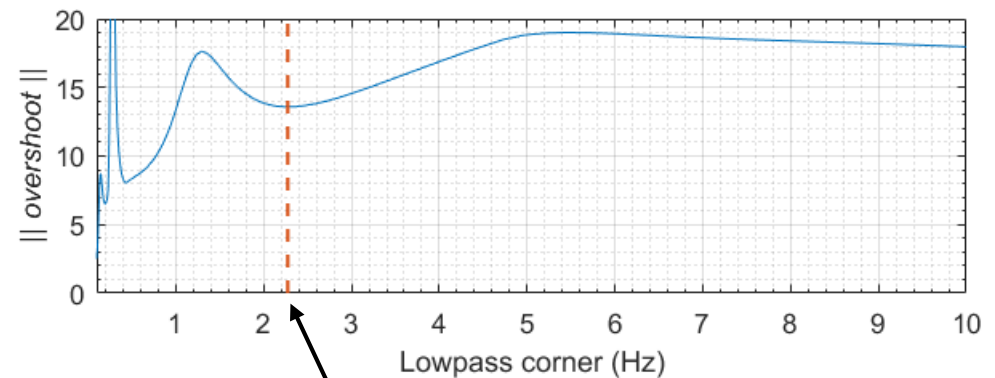
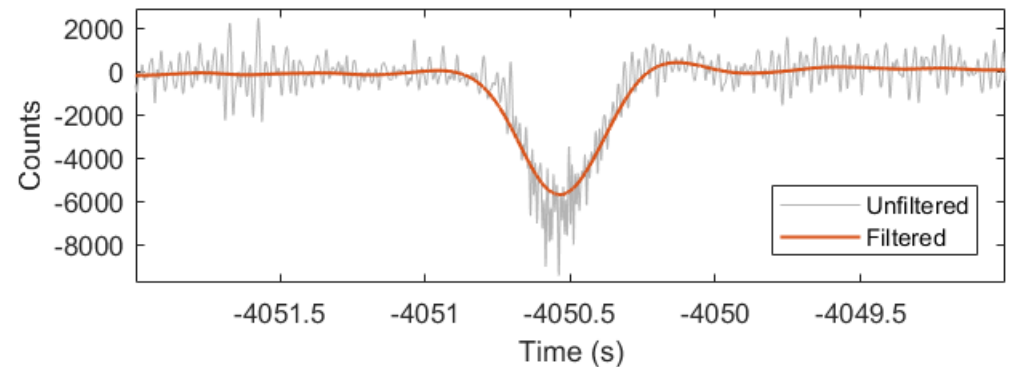
2. Recover the weight lift



3. Measure instrument constants



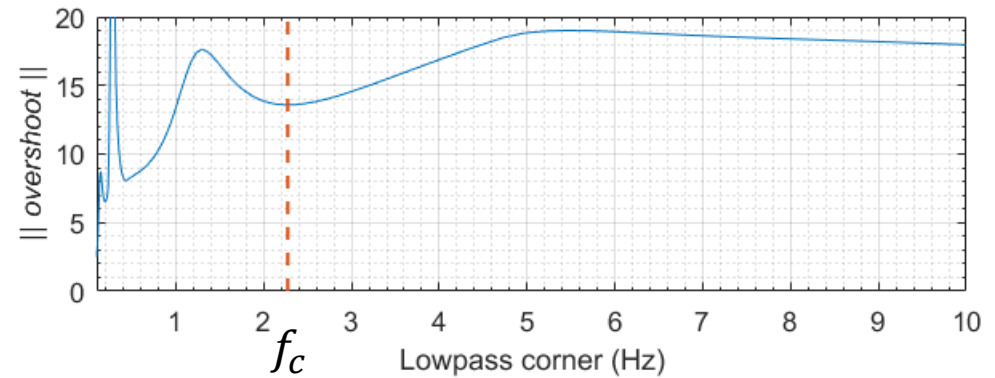
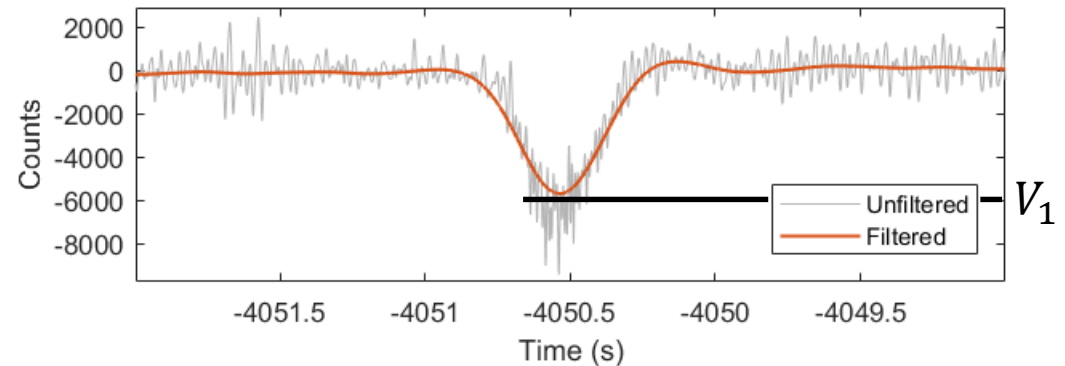
3. Measure instrument constants



$$f_c \approx 2.3 \text{ Hz}$$

3. Measure instrument constants

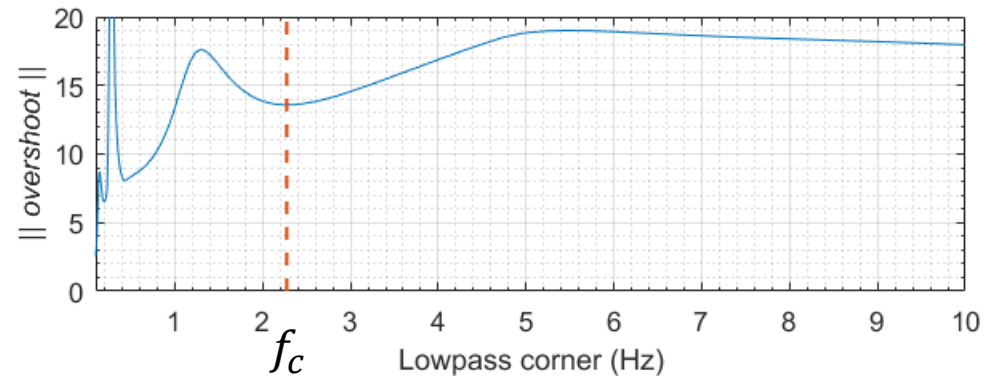
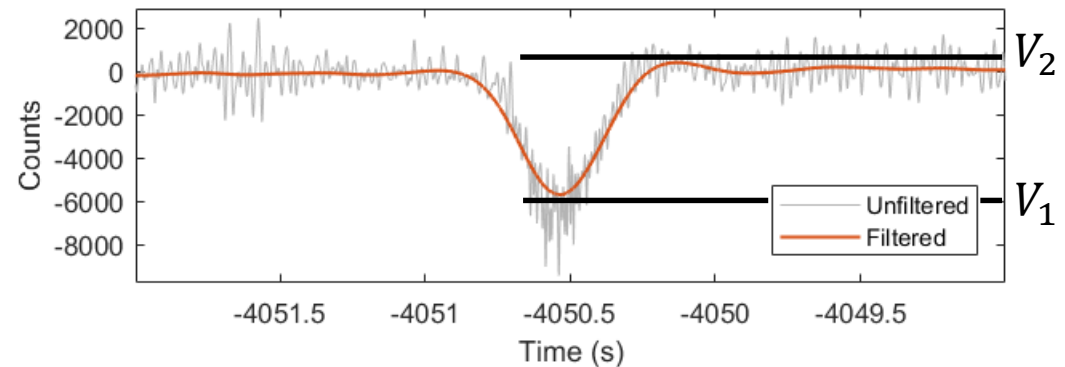
$$f_c \approx 2.3 \text{ Hz}$$



3. Measure instrument constants

$$f_c \approx 2.3 \text{ Hz}$$

$$V_1 = -5692 \text{ cts}$$

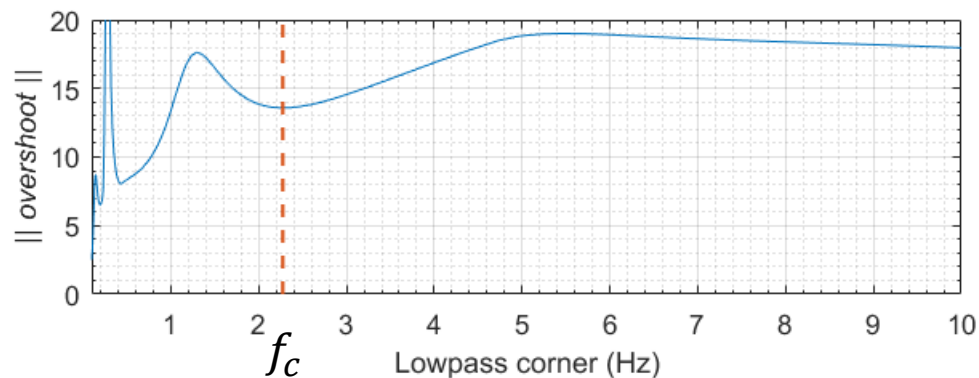
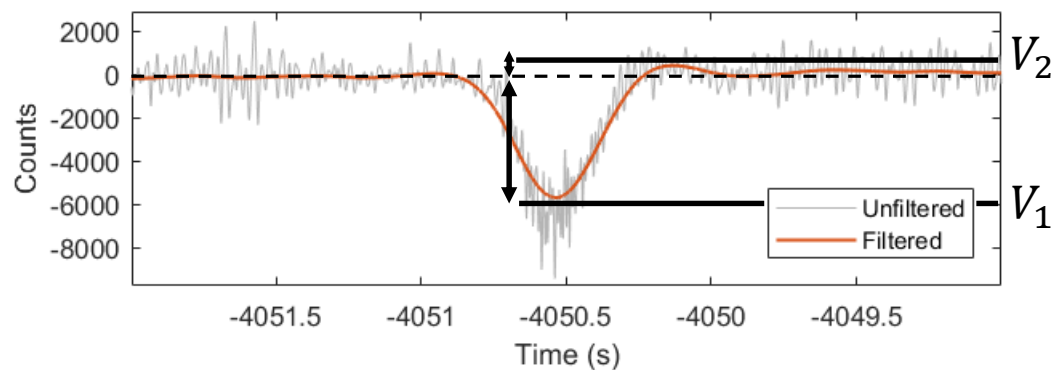


3. Measure instrument constants

$$f_c \approx 2.3 \text{ Hz}$$

$$V_1 = -5692 \text{ cts}$$

$$V_2 = 419 \text{ cts}$$



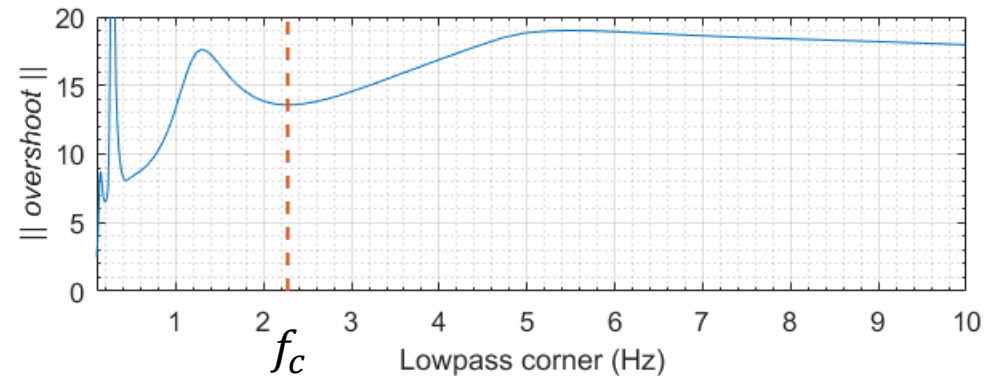
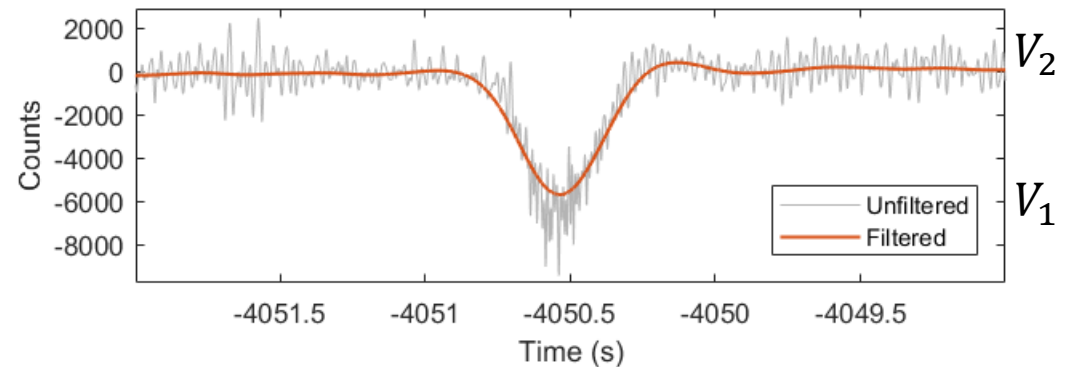
3. Measure instrument constants

$$f_c \approx 2.3 \text{ Hz}$$

$$V_1 = -5692 \text{ cts}$$

$$V_2 = 419 \text{ cts}$$

$$\left| \frac{V_1}{V_2} \right| = 13.58$$



3. Measure instrument constants

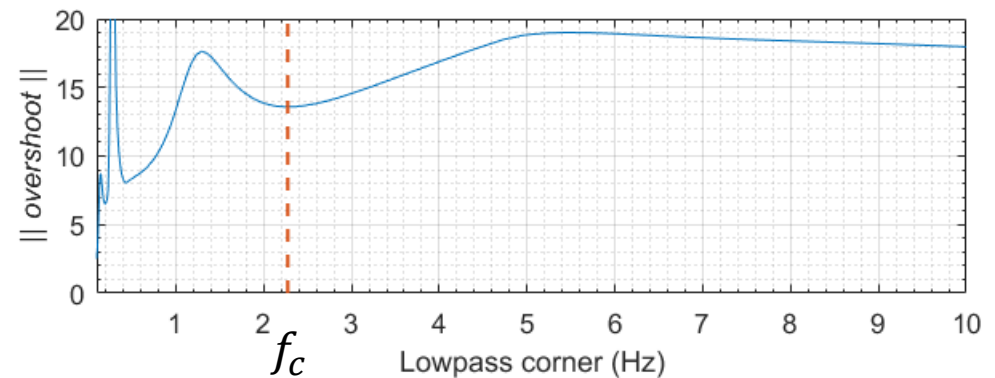
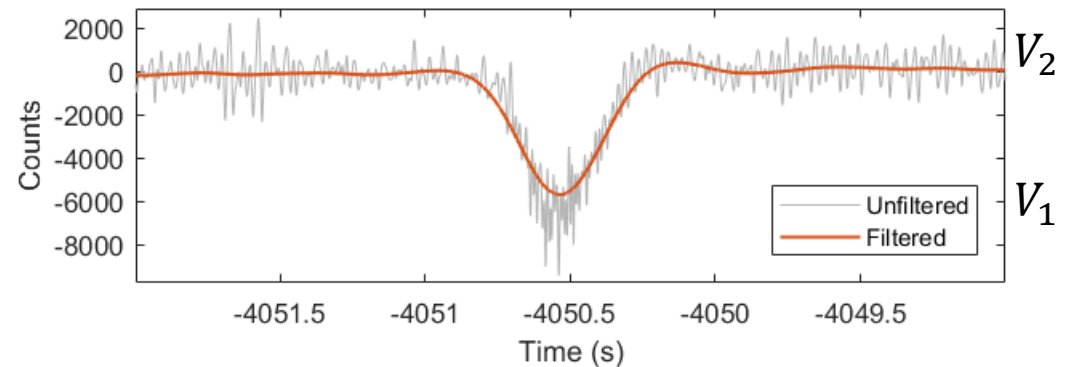
$$f_c \approx 2.3 \text{ Hz}$$

$$V_1 = -5692 \text{ cts}$$

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$$\left| \frac{V_1}{V_2} \right| = 13.58$$

$$\delta = \ln \left| \frac{V_1}{V_2} \right| = 2.61$$



3. Measure instrument constants

$$f_c \approx 2.3 \text{ Hz}$$

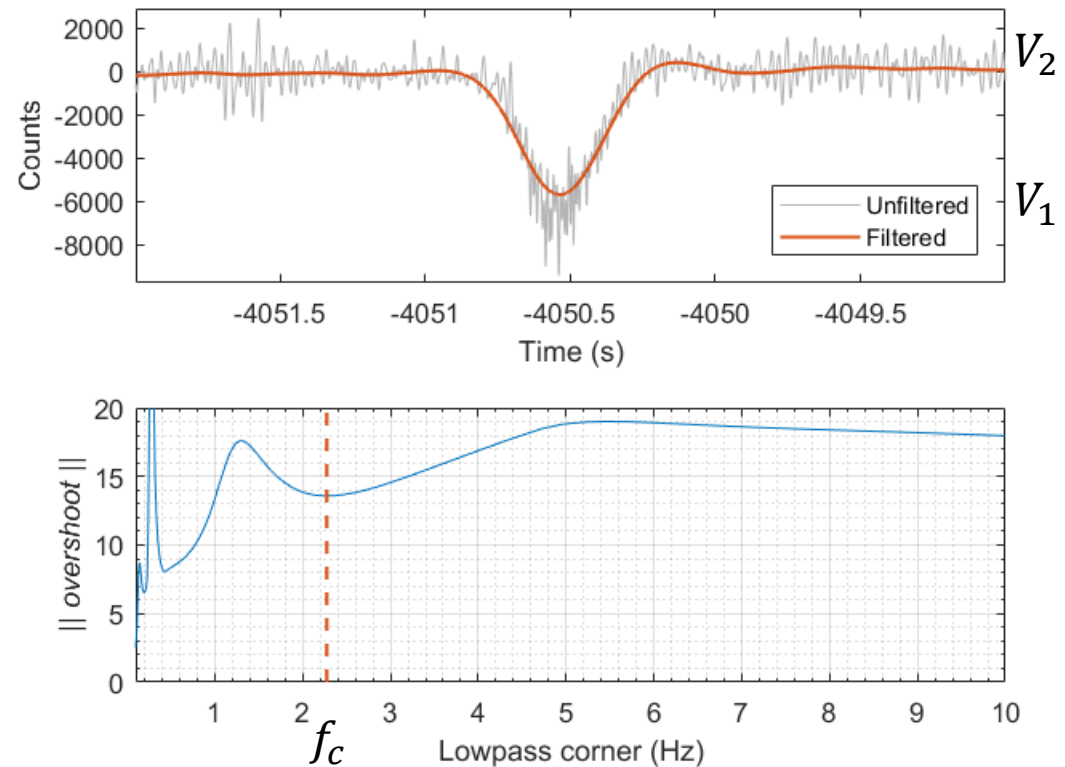
$$V_1 = -5692 \text{ cts}$$

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$$\left| \frac{V_1}{V_2} \right| = 13.58$$

$$\delta = \ln \left| \frac{V_1}{V_2} \right| = 2.61$$

$$\lambda = \frac{\delta}{\sqrt{\pi^2 + \delta^2}} = 0.6389$$



3. Measure instrument constants

$$f_c \approx 2.3 \text{ Hz}$$

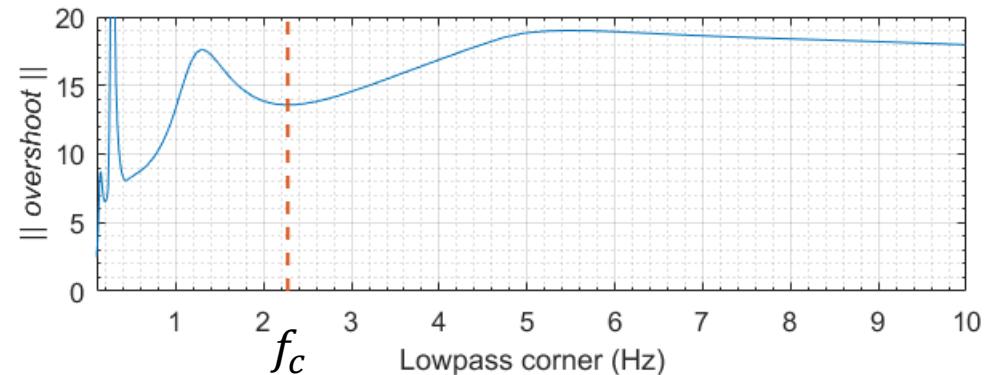
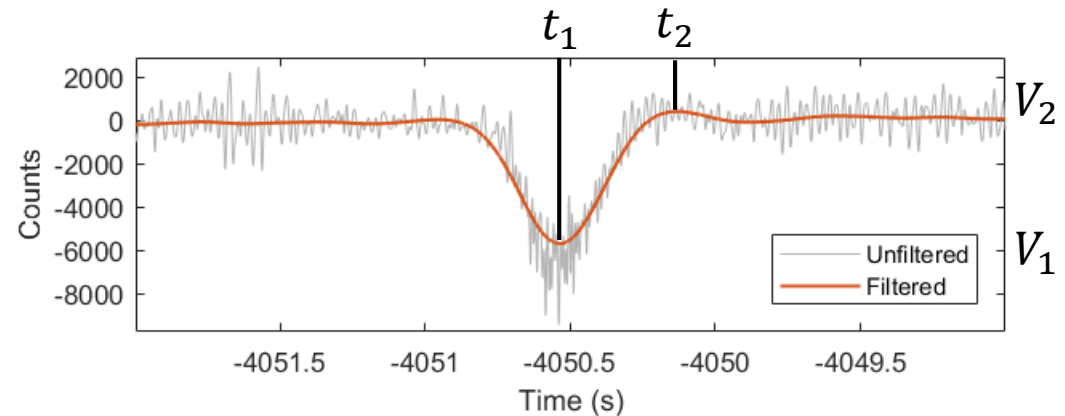
$$V_1 = -5692 \text{ cts}$$

$$V_2 = 419 \text{ cts}$$

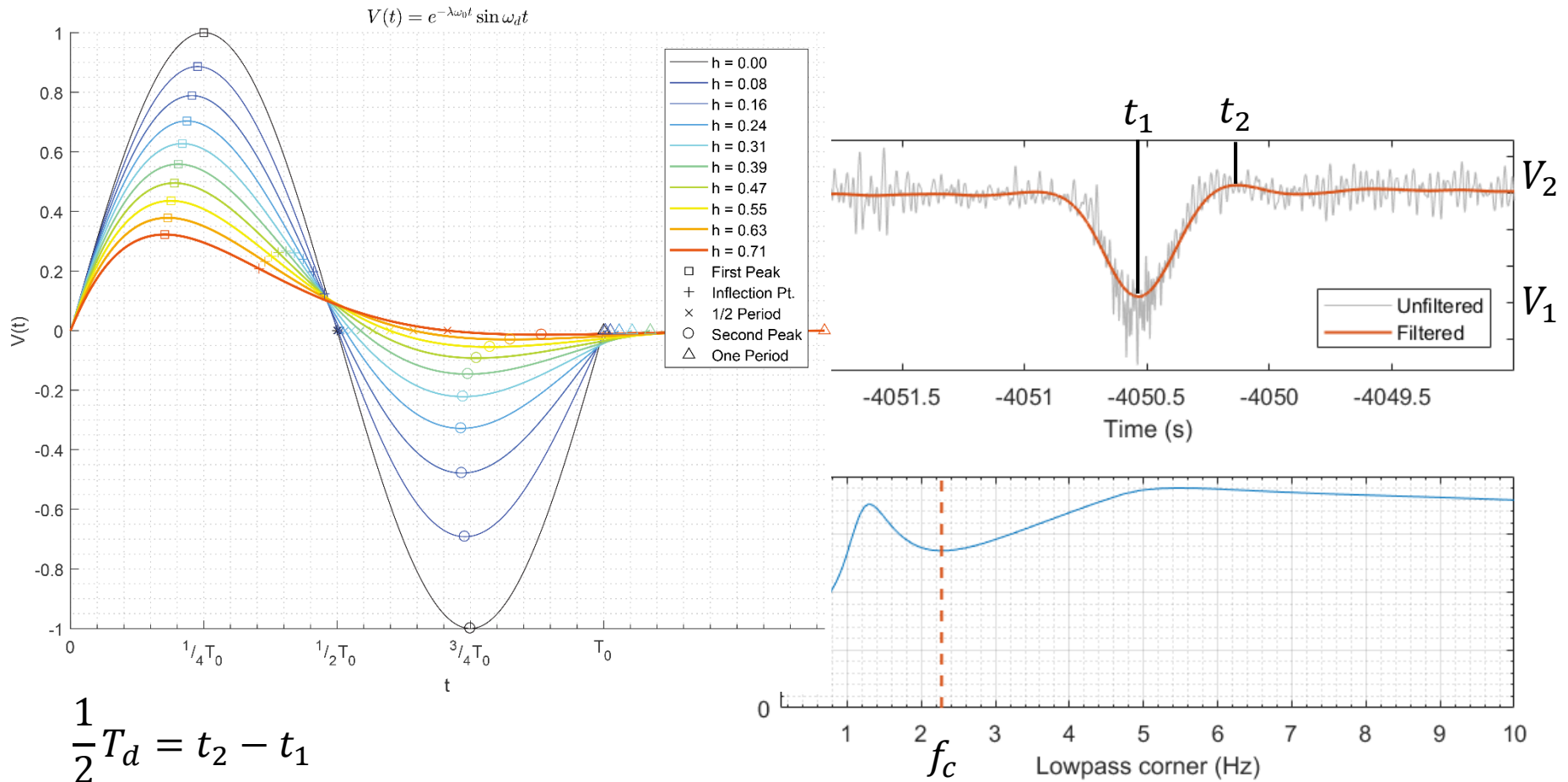
$$\left| \frac{V_1}{V_2} \right| = 13.58$$

$$\delta = \ln \left| \frac{V_1}{V_2} \right| = 2.61$$

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3. Measure instrument constants



3. Measure instrument constants

$$f_c \approx 2.3 \text{ Hz}$$

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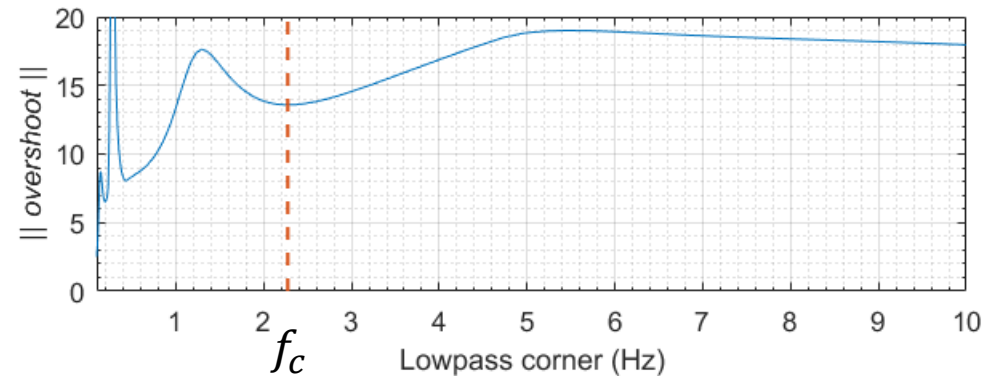
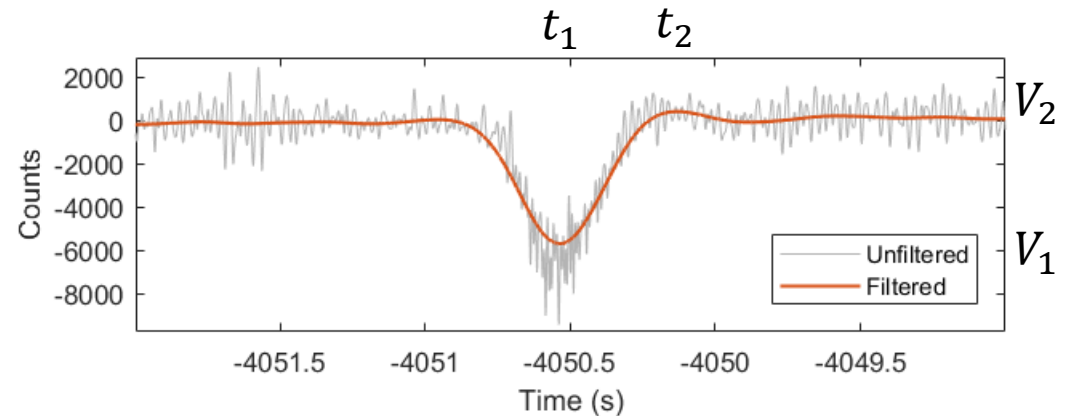
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$$\lambda = \frac{\delta}{\sqrt{\pi^2 + \delta^2}} = 0.6389$$

$$\frac{1}{2} T_d = t_2 - t_1 = 0.42 \text{ s}$$

$$\omega_d = 2\pi f_d = \frac{2\pi}{T_d} = 7.48$$



3. Measure instrument constants

$$f_c \approx 2.3 \text{ Hz}$$

$$V_1 = -5692 \text{ cts}$$

$$V_2 = 419 \text{ cts}$$

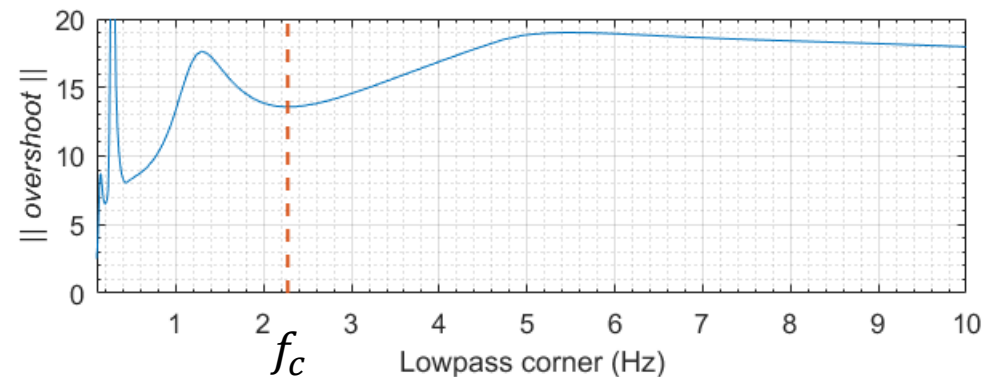
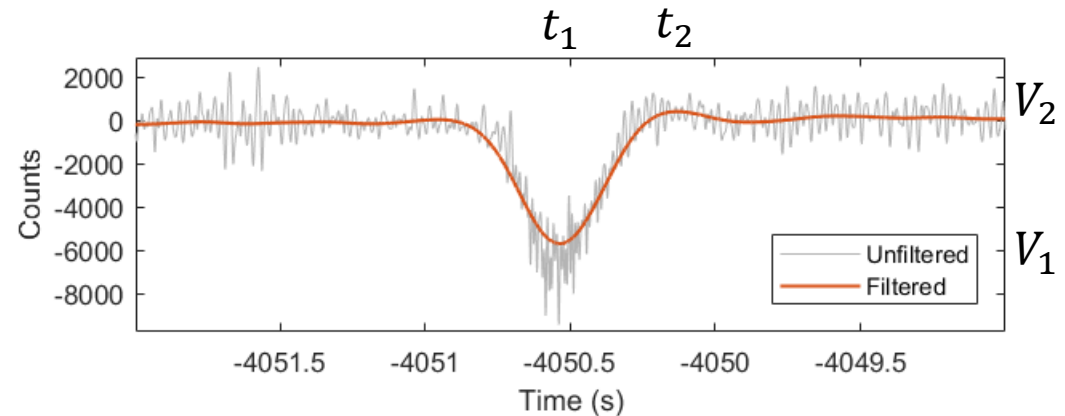
$$\left| \frac{V_1}{V_2} \right| = 13.58$$

$$\delta = \ln \left| \frac{V_1}{V_2} \right| = 2.61$$

$$\lambda = \frac{\delta}{\sqrt{\pi^2 + \delta^2}} = 0.6389$$

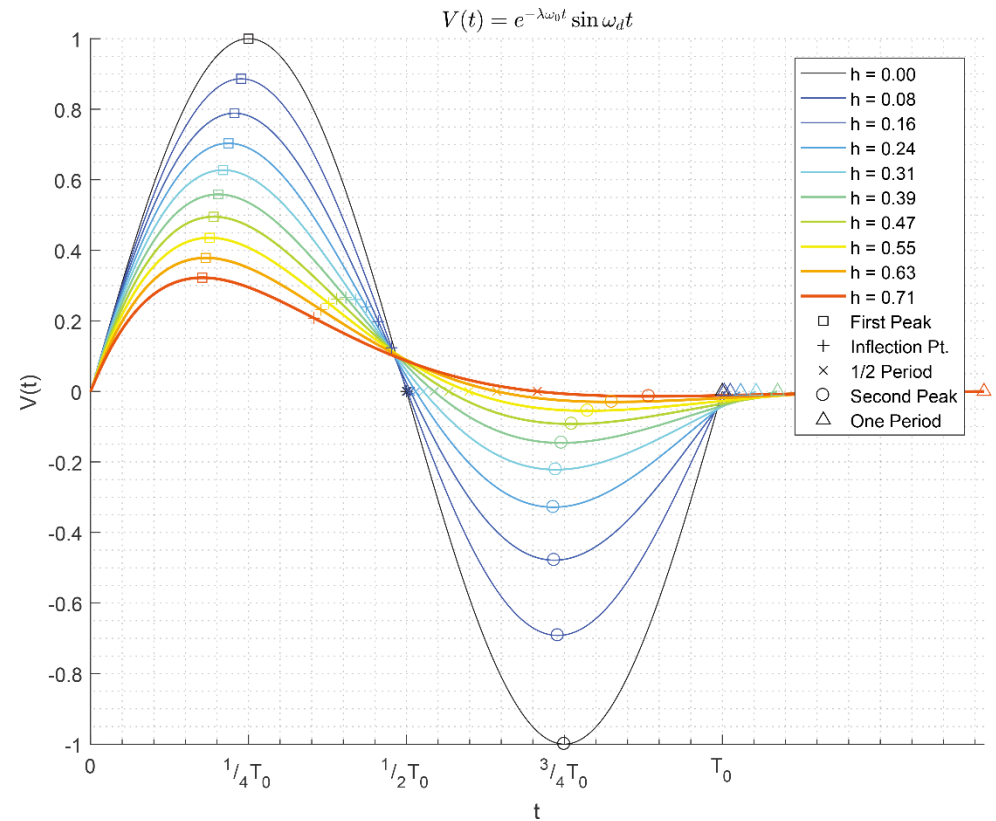
$$\frac{1}{2} T_d = t_2 - t_1 = 0.42 \text{ s}$$

$$\omega_d = 2\pi f_d = \frac{2\pi}{T_d} = 7.48 \quad \omega_d = \omega_0 \sqrt{1 - \lambda^2} \quad \omega_0 = 9.72 \quad f_0 = 1.54 \text{ Hz}$$



4. Solve for generator constant

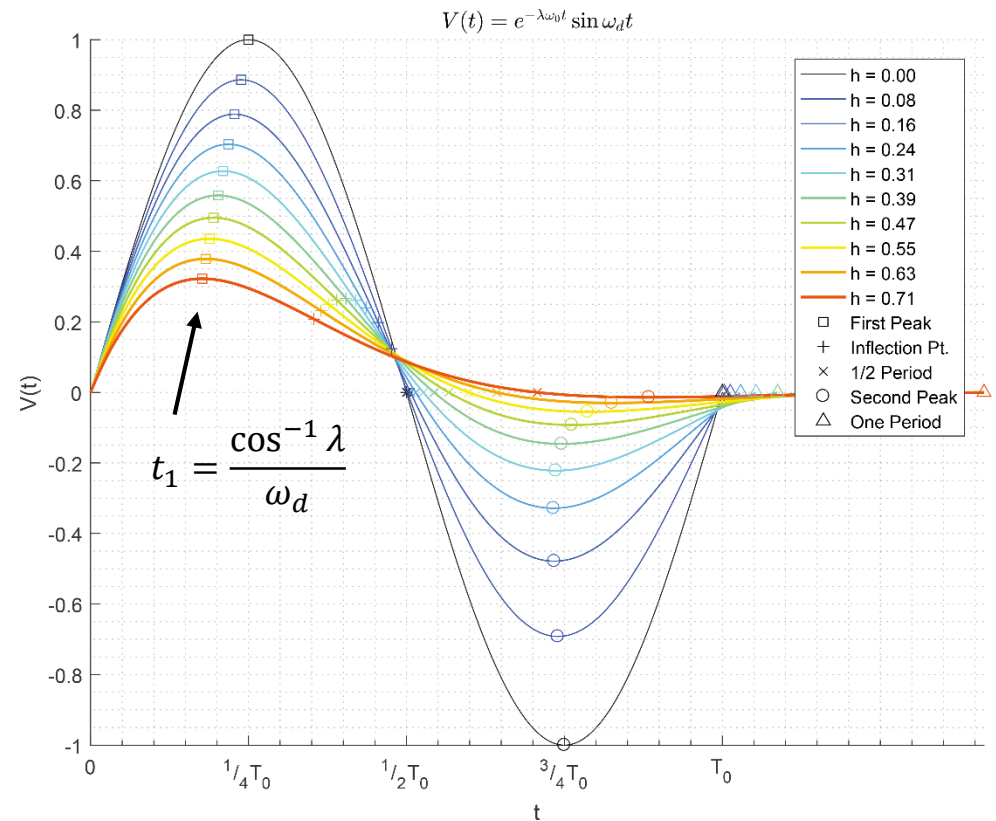
$$V(t) = -G \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t} \sin \omega_d t$$



4. Solve for generator constant

$$V(t) = -G \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t} \sin \omega_d t$$

$$V(t_1) = -G_1 \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t_1} \sin \omega_d t_1$$

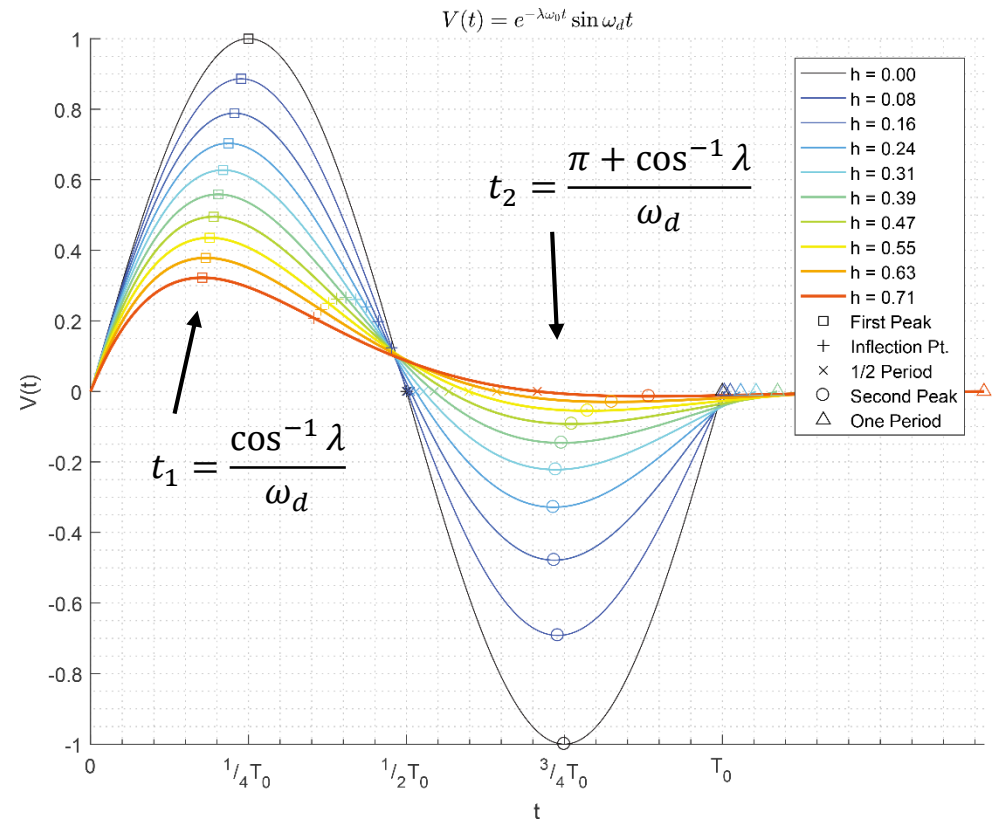


4. Solve for generator constant

$$V(t) = -G \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t} \sin \omega_d t$$

$$V(t_1) = -G_1 \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t_1} \sin \omega_d t_1$$

$$V(t_2) = -G_2 \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t_1} \sin \omega_d t_2$$



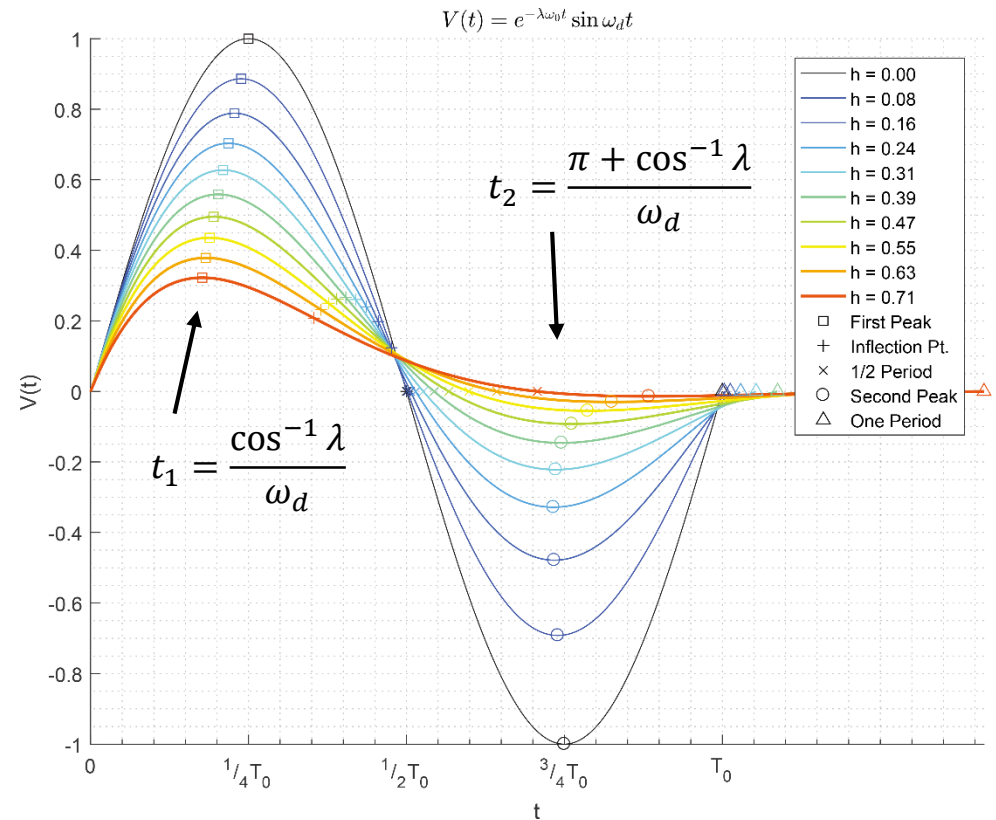
4. Solve for generator constant

$$V(t) = -G \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t} \sin \omega_d t$$

$$V(t_1) = -G_1 \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t_1} \sin \omega_d t_1$$

$$V(t_2) = -G_2 \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t_1} \sin \omega_d t_2$$

$$G = \frac{G_1 + G_2}{2} \left[\frac{\text{cts}}{\text{m/s}} \right]$$



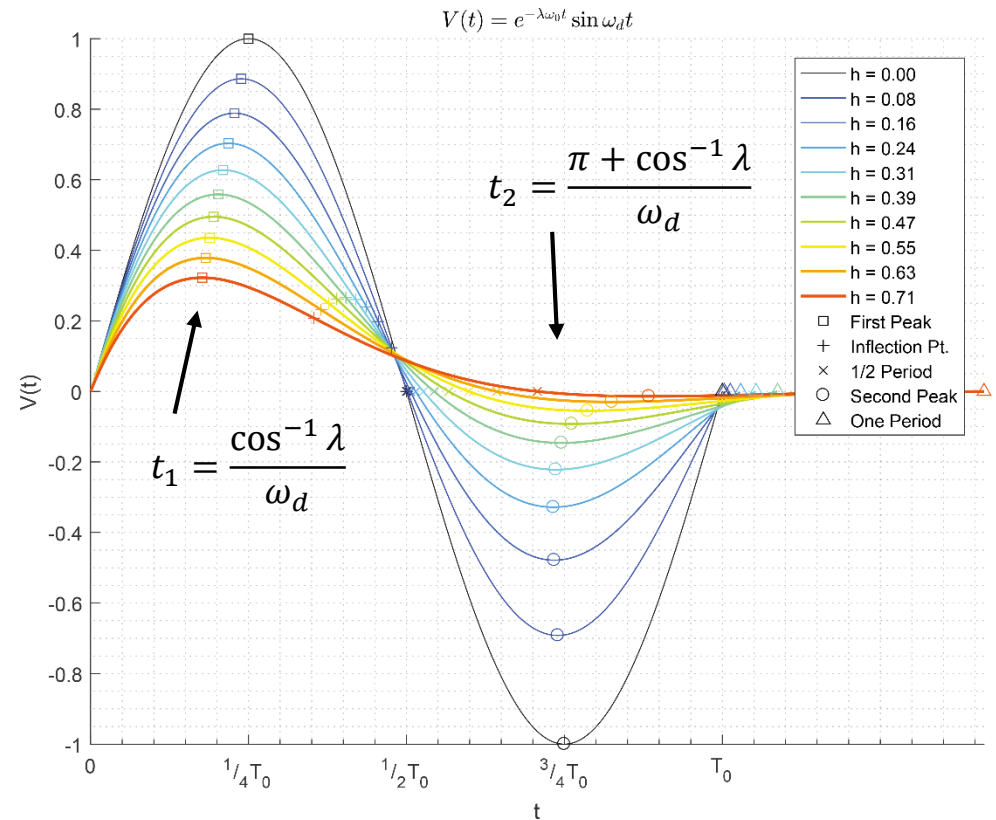
4. Solve for generator constant

$$V(t) = -G \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t} \sin \omega_d t$$

$$V(t_1) = -G_1 \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t_1} \sin \omega_d t_1$$

$$V(t_2) = -G_2 \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t_2} \sin \omega_d t_2$$

$$G = \frac{G_1 + G_2}{2} \left[\frac{\text{cts}}{\text{m/s}} \right]$$



$$m_w = 0.255 \text{ [g]}$$

$$m_s = 107.5 \text{ [kg]}$$

$$g = 9.80665 \text{ [m/s}^2\text{]}$$

5. Dynamic magnification

- G is units of *digital counts per velocity*
 - per velocity of seismic mass motion
- Seismic mass doesn't move 1:1 with ground motion
 - It moves less

Undriven seismometer:

$$\ddot{x} + 2\lambda\omega_0\dot{x} + \omega_0^2x = 0$$

Driven seismometer:

$$\ddot{x} + 2\lambda\omega_0\dot{x} + \omega_0^2x = -\ddot{u}$$

Arbitrary acceleration
(Earth ground motion)



5. Dynamic magnification

Driven seismometer:

Arbitrary acceleration
(Earth ground motion)

$$\ddot{x} + 2\lambda\omega_0\dot{x} + \omega_0^2x = -\ddot{u}$$



Fourier Transform:

$$\mathcal{F}[\ddot{x} + 2\lambda\omega_0\dot{x} + \omega_0^2x] = \mathcal{F}[-\ddot{u}]$$

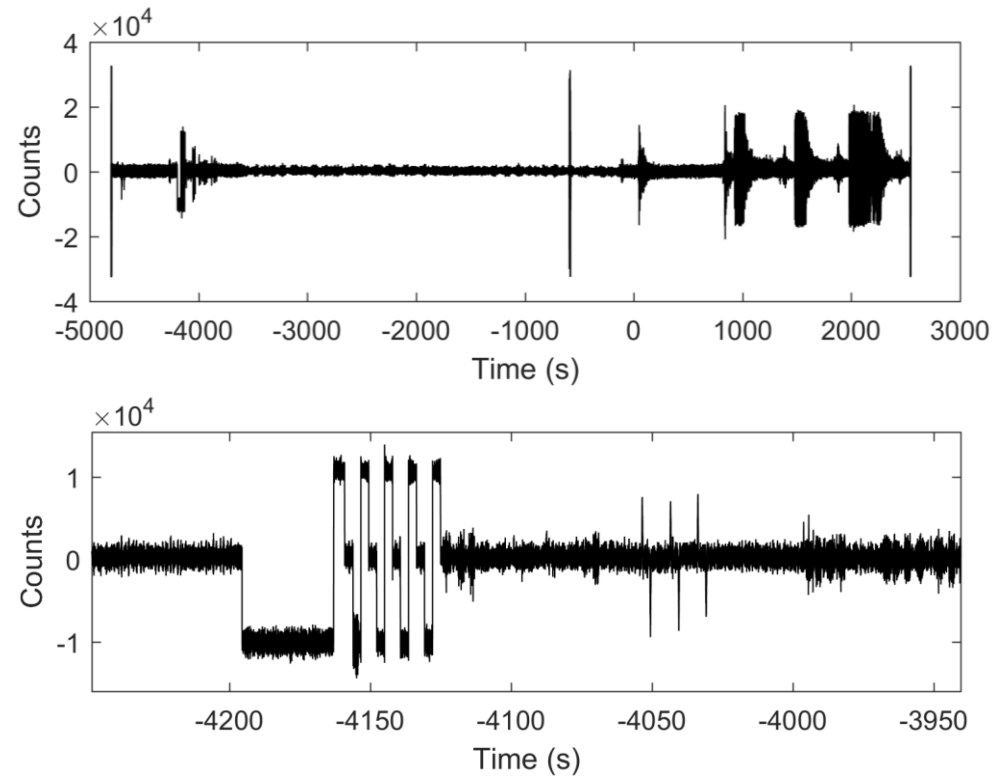
$$\Rightarrow (-\omega^2 + i2\lambda\omega_0\omega + \omega_0^2)\hat{x} = \omega^2\hat{u}$$

Solve for *Earth movt* per *mass movt*

$$\left| \frac{\hat{u}}{\hat{x}} \right|^2 = \left(\frac{\omega_0^2}{\omega^2} - 1 \right)^2 + 4\lambda^2 \frac{\omega_0^2}{\omega^2}$$

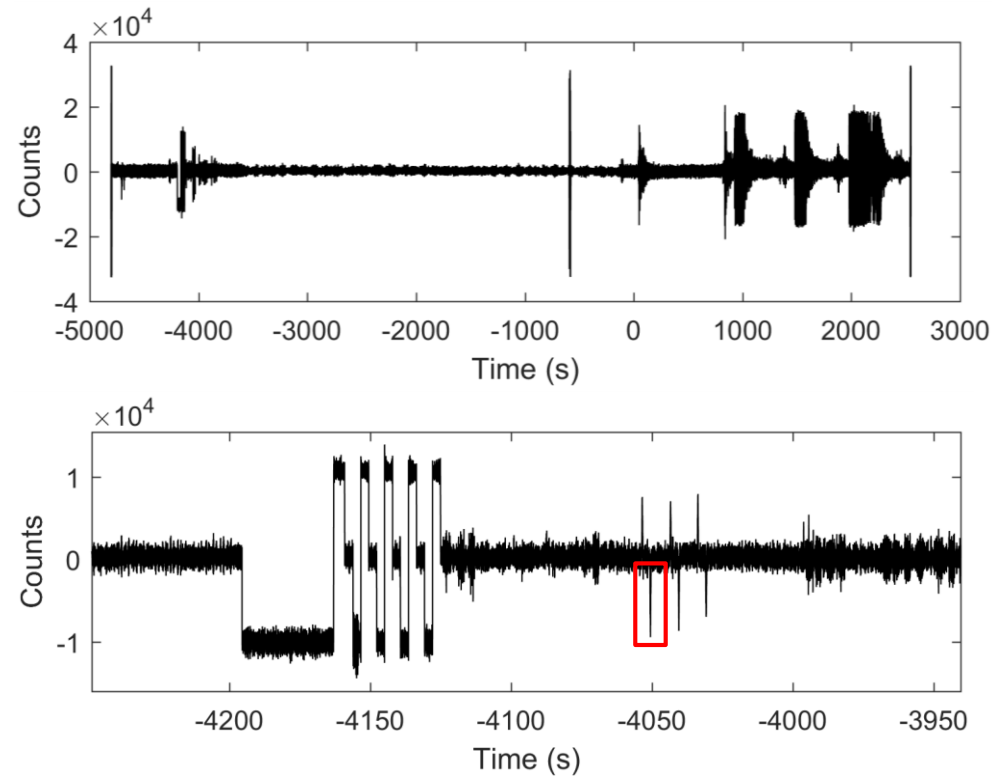
Magnitude as a
function of *frequency* ...in units of $\left[\frac{\text{earth movt}}{\text{mass movt}} \right]$

Let's calibrate some data



Boxcar – Leeds – VSP÷5

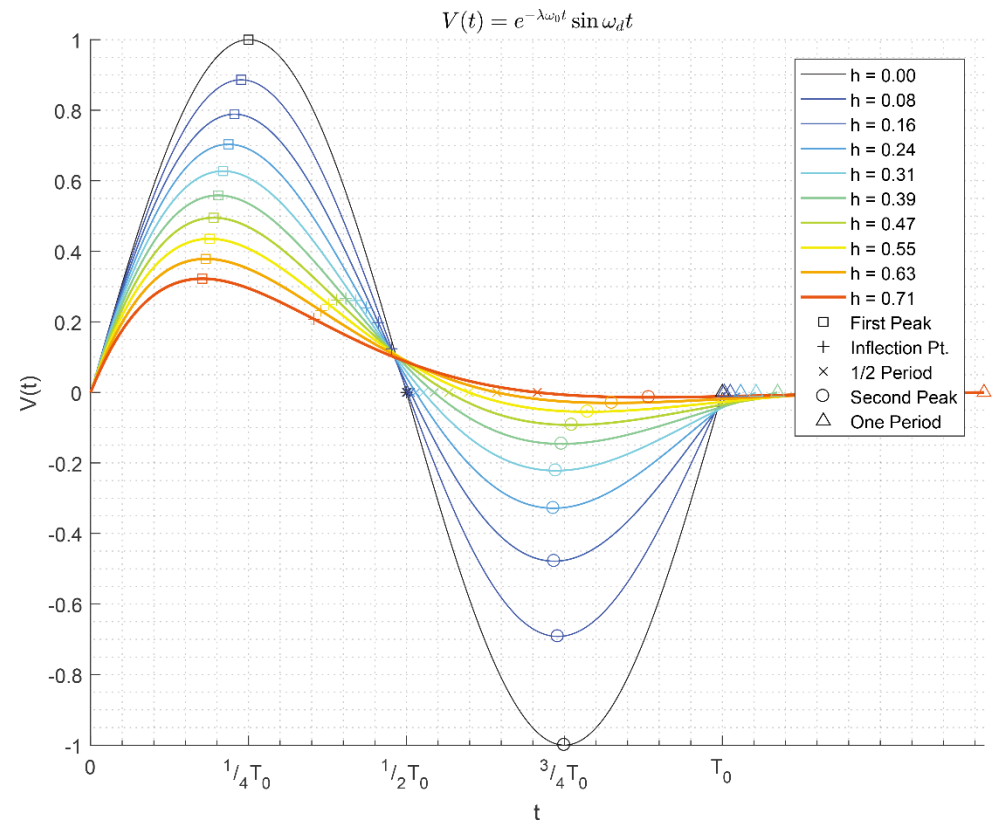
Let's calibrate some data



Boxcar – Leeds – VSP÷5

Let's calibrate some data

$$V(t) = -G \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t} \sin \omega_d t$$



$$m_w = 0.255 \text{ [g]}$$

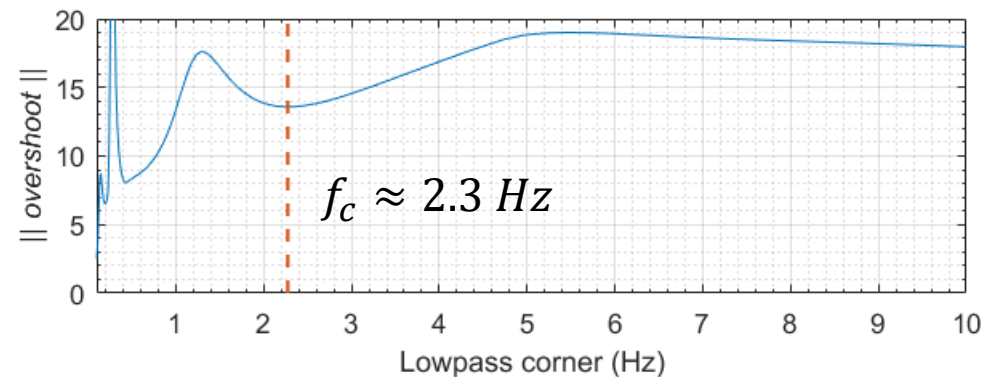
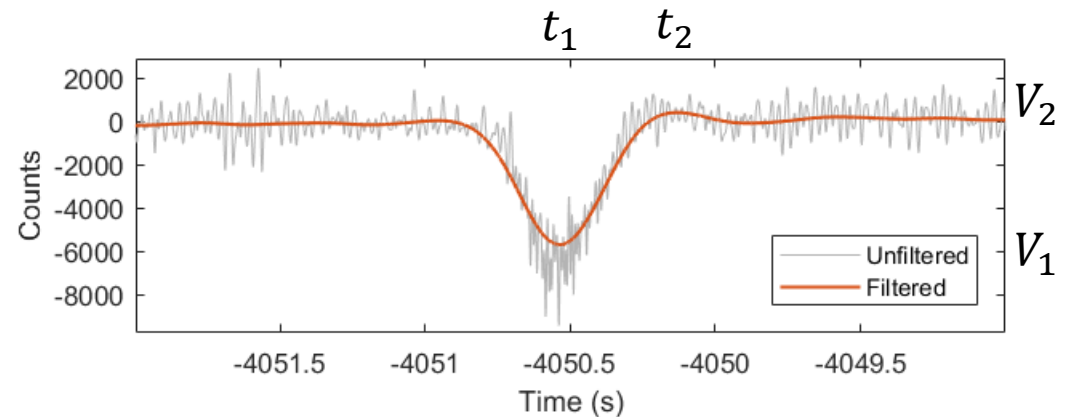
$$m_s = 107.5 \text{ [kg]}$$

$$g = 9.80665 \text{ [m/s}^2\text{]}$$

Let's calibrate some data

$$V(t) = -G \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t} \sin \omega_d t$$

$$V_1 = -5692 \text{ cts} \quad V_2 = 419 \text{ cts}$$



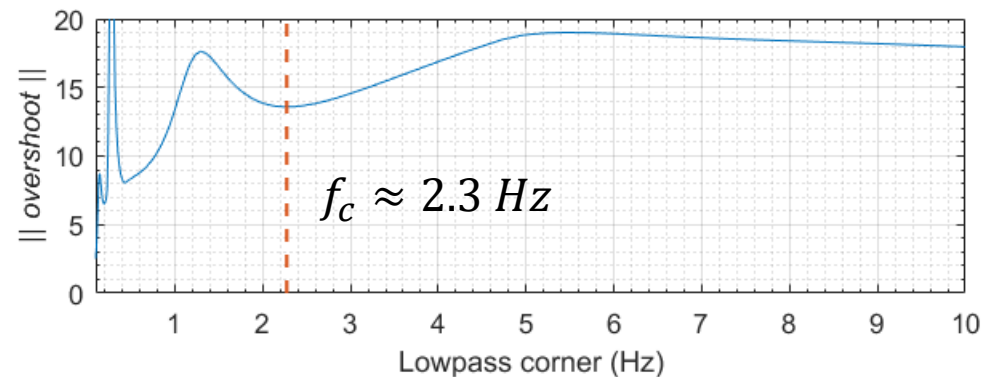
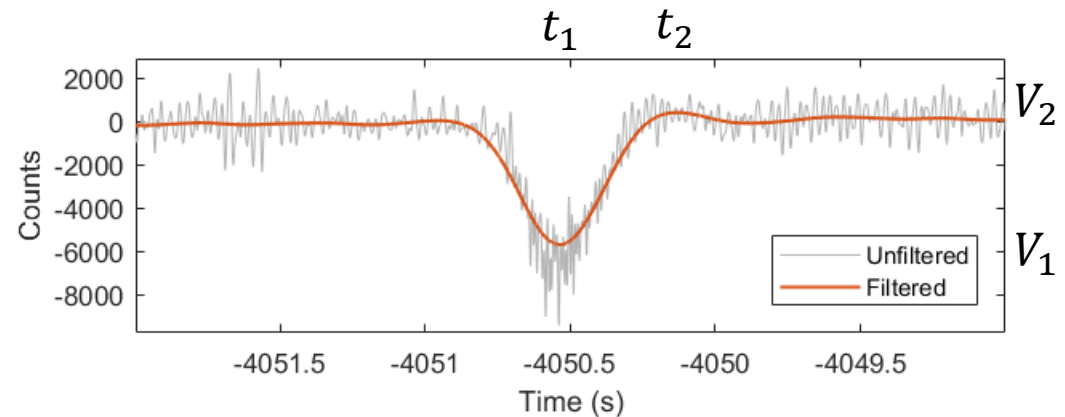
Let's calibrate some data

$$V(t) = -G \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t} \sin \omega_d t$$

$$V_1 = -5692 \text{ cts} \quad V_2 = 419 \text{ cts}$$

$$\left| \frac{V_1}{V_2} \right| = 13.58 \quad \delta = \ln \left| \frac{V_1}{V_2} \right| = 2.61$$

$$\lambda = \frac{\delta}{\sqrt{\pi^2 + \delta^2}} = 0.6389$$



Let's calibrate some data

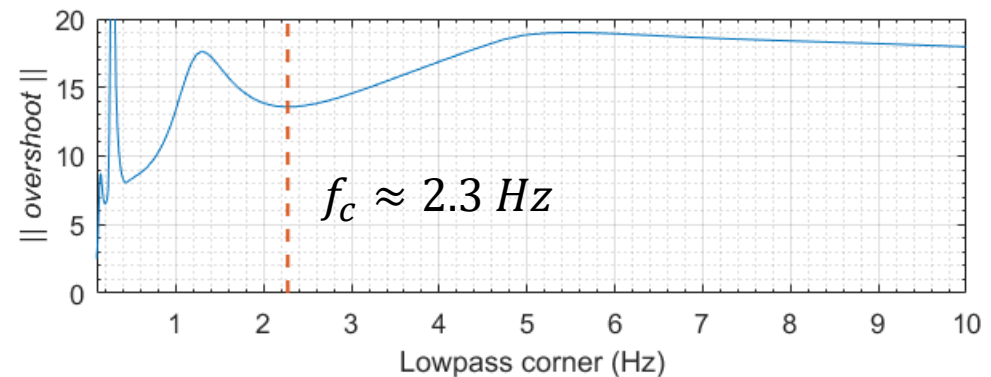
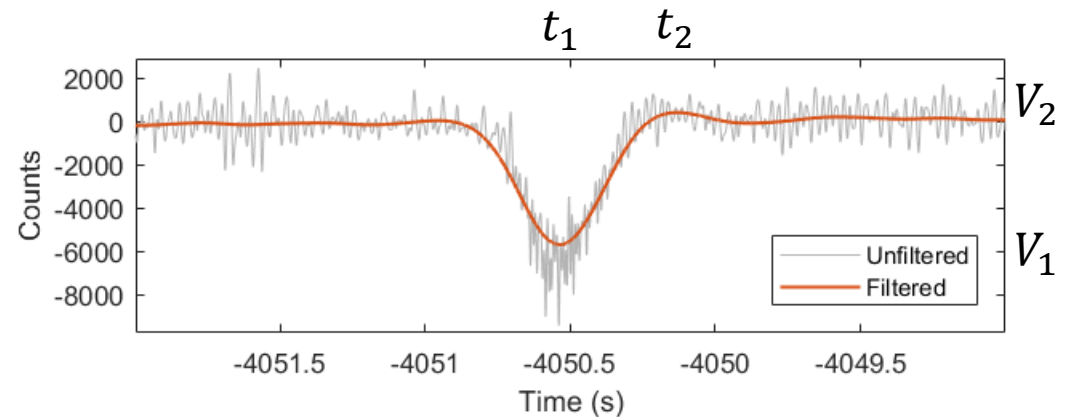
$$V(t) = -G \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t} \sin \omega_d t$$

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$$\frac{1}{2} T_d = 0.42 \text{ s} \quad T_d = 0.84 \text{ s}$$



Let's calibrate some data

$$V(t) = -G \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t} \sin \omega_d t$$

$$V_1 = -5692 \text{ cts} \quad V_2 = 419 \text{ cts}$$

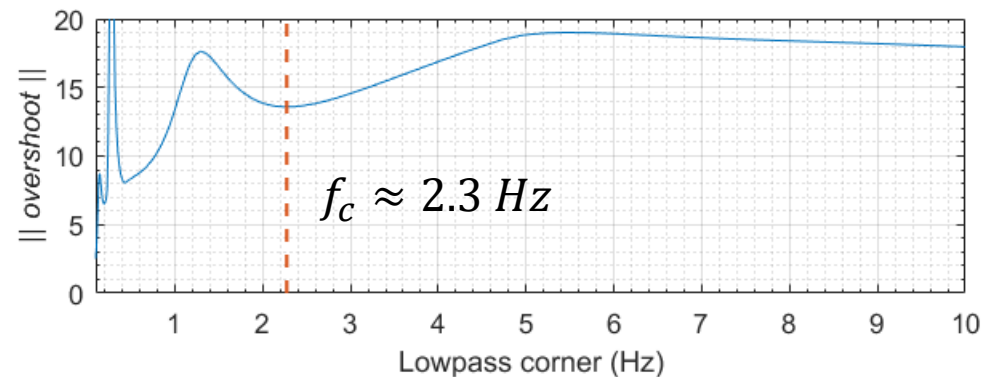
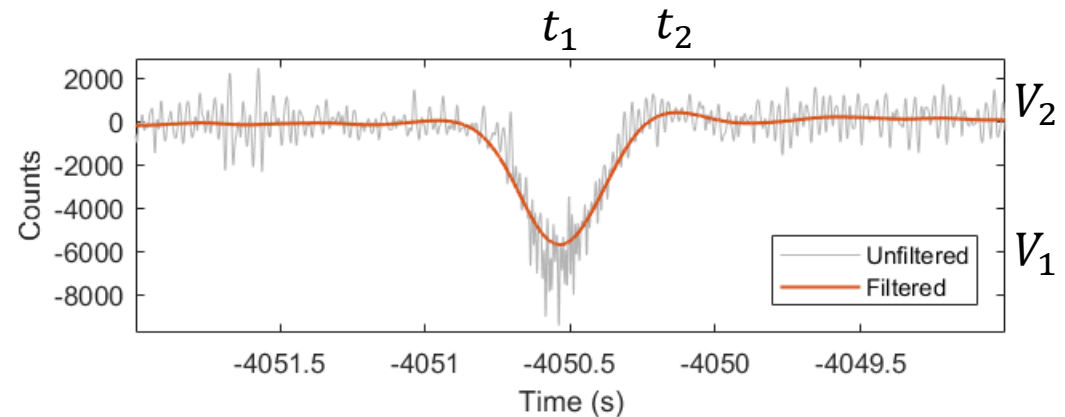
$$\left| \frac{V_1}{V_2} \right| = 13.58 \quad \delta = \ln \left| \frac{V_1}{V_2} \right| = 2.61$$

$$\lambda = \frac{\delta}{\sqrt{\pi^2 + \delta^2}} = 0.6389$$

$$\frac{1}{2} T_d = 0.42 \text{ s} \quad T_d = 0.84 \text{ s}$$

$$\omega_d = 7.48$$

$$\omega_d = \omega_0 \sqrt{1 - \lambda^2} \Rightarrow \omega_0 = 9.72$$



Let's calibrate some data

$$V(t) = -G \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t} \sin \omega_d t$$

$$V_1 = -5692 \text{ cts} \quad V_2 = 419 \text{ cts}$$

$$\left| \frac{V_1}{V_2} \right| = 13.58 \quad \delta = \ln \left| \frac{V_1}{V_2} \right| = 2.61$$

$$\lambda = \frac{\delta}{\sqrt{\pi^2 + \delta^2}} = 0.6389$$

$$\frac{1}{2} T_d = 0.42 \text{ s} \quad T_d = 0.84 \text{ s}$$

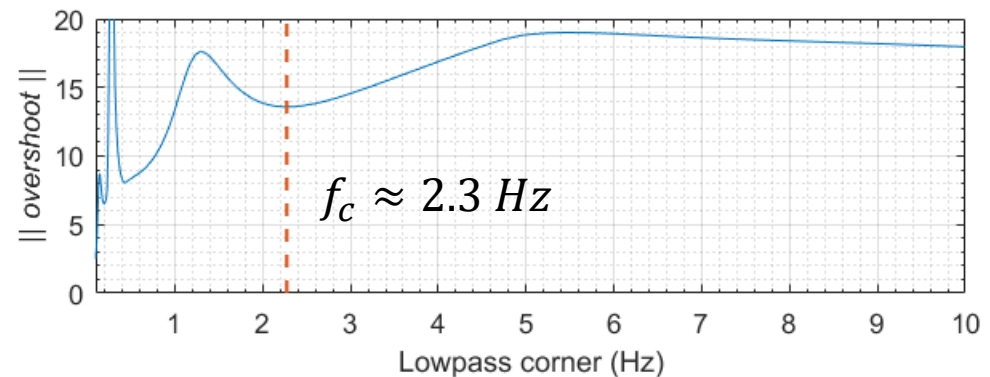
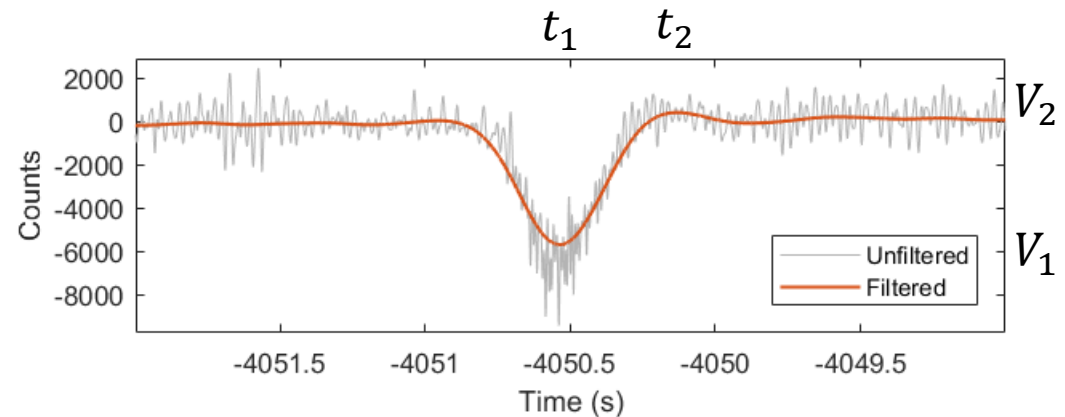
$$\omega_d = 7.48$$

$$\omega_d = \omega_0 \sqrt{1 - \lambda^2} \Rightarrow \omega_0 = 9.72 \quad t_1 = \frac{\cos^{-1} \lambda}{\omega_d} = 0.12 \text{ [s]} \quad t_2 = \frac{\pi + \cos^{-1} \lambda}{\omega_d} = 0.54 \text{ [s]}$$

$$m_w = 0.255 \text{ [g]}$$

$$m_s = 107.5 \text{ [kg]}$$

$$g = 9.80665 \text{ [m/s}^2\text{]}$$

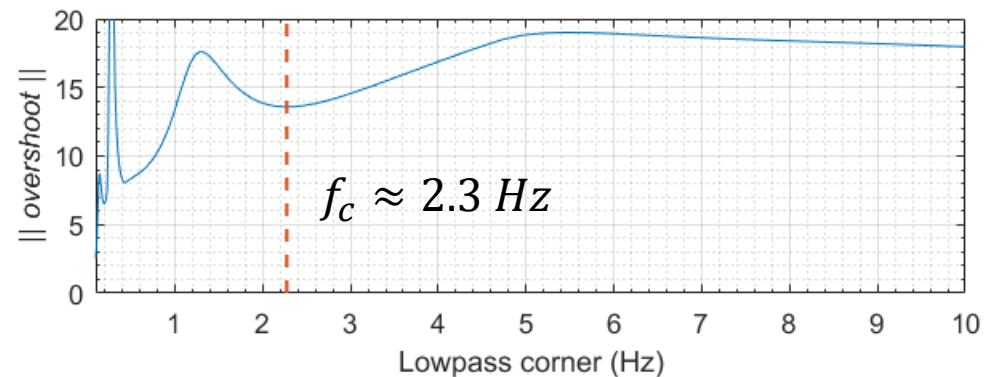
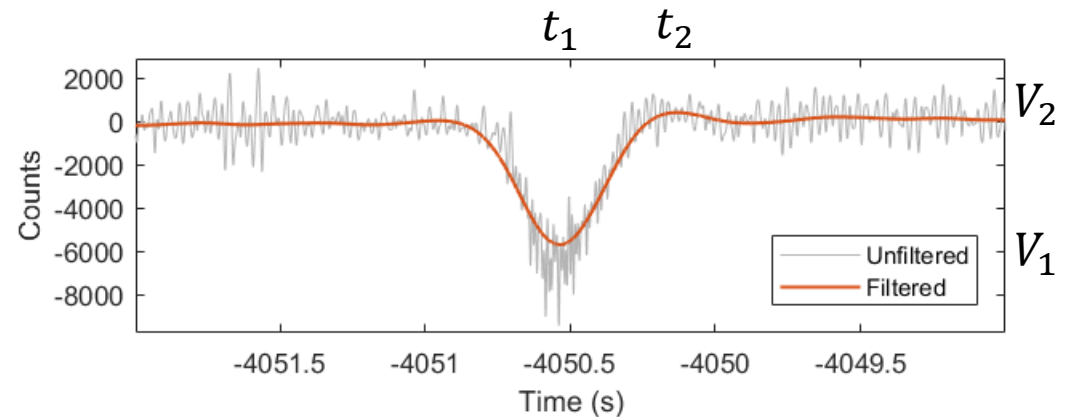


Let's calibrate some data

$$V(t) = -G \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t} \sin \omega_d t$$

$$V(t_1) = -G_1 \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t_1} \sin \omega_d t_1$$

$$G_1 = 4.9327 \times 10^9$$



Let's calibrate some data

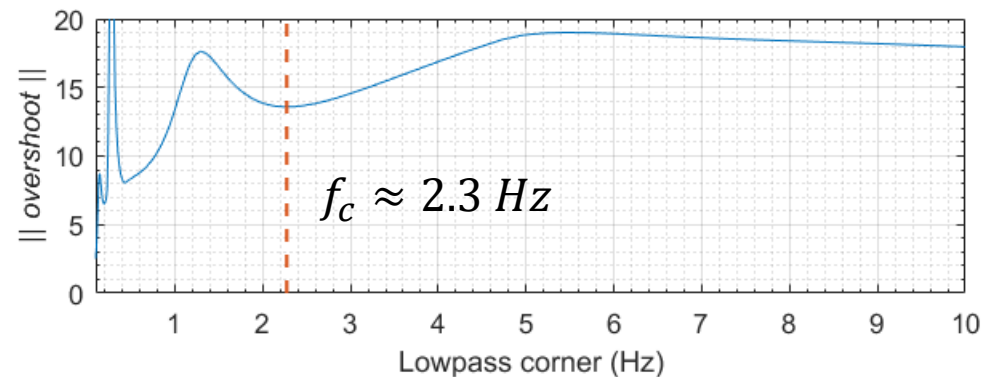
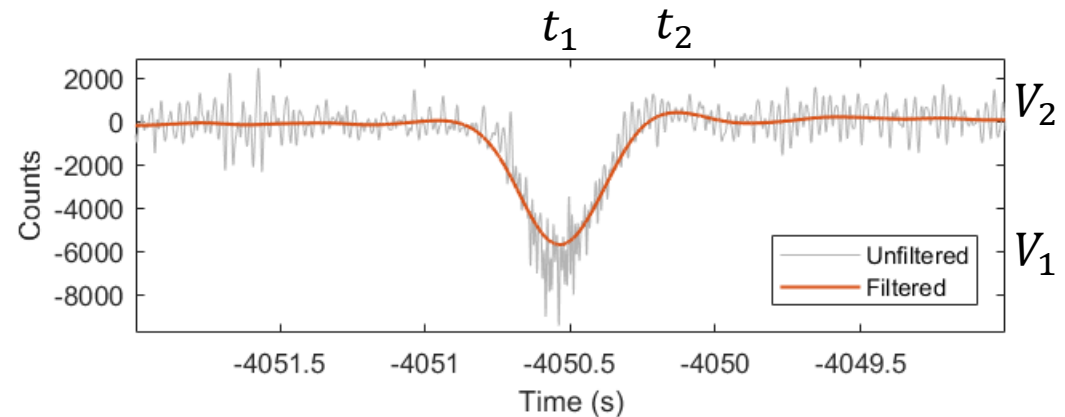
$$V(t) = -G \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t} \sin \omega_d t$$

$$V(t_1) = -G_1 \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t_1} \sin \omega_d t_1$$

$$G_1 = 4.9327 \times 10^9$$

$$V(t_2) = -G_2 \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t_2} \sin \omega_d t_2$$

$$G_2 = 4.9327 \times 10^9$$



Let's calibrate some data

$$V(t) = -G \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t} \sin \omega_d t$$

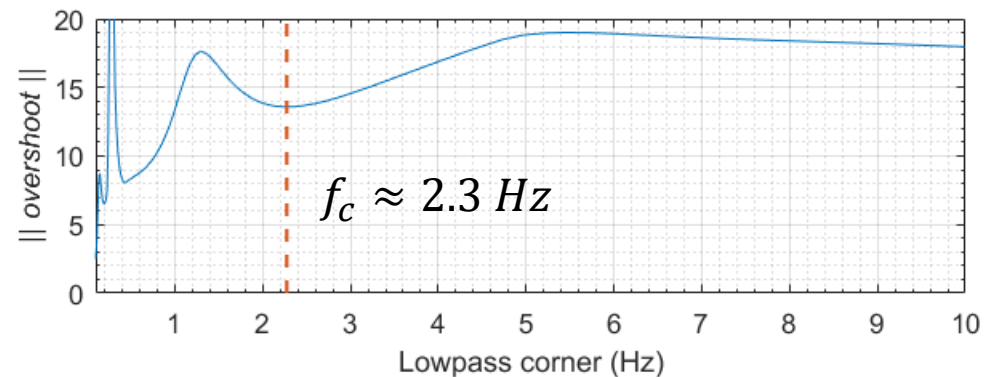
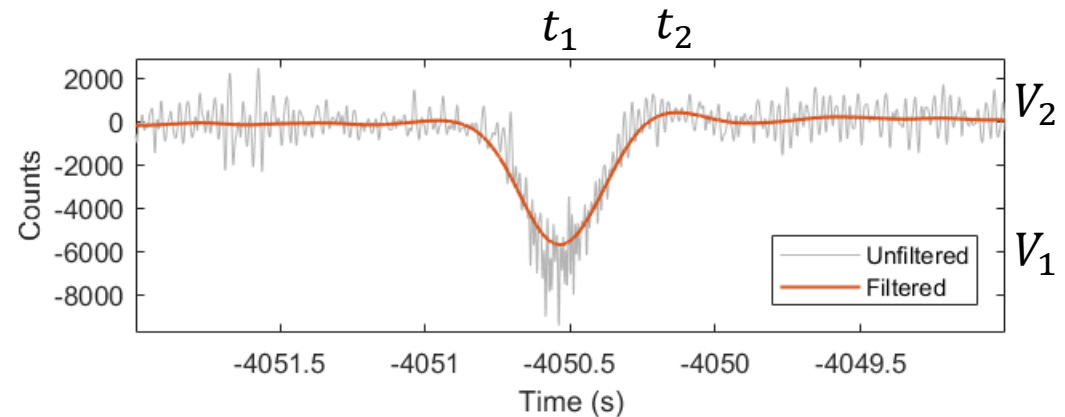
$$V(t_1) = -G_1 \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t_1} \sin \omega_d t_1$$

$$G_1 = 4.9327 \times 10^9$$

$$V(t_2) = -G_2 \frac{m_w g}{m_s \omega_d} e^{-\lambda \omega_0 t_2} \sin \omega_d t_2$$

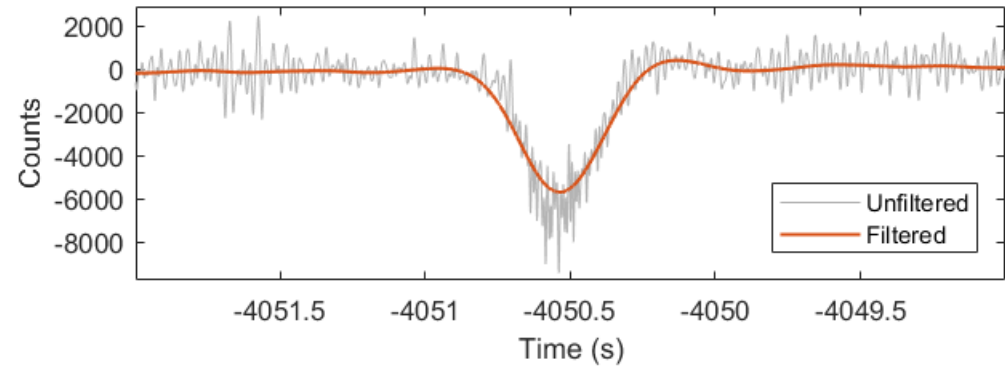
$$G_2 = 4.9327 \times 10^9$$

$$G = \frac{G_1 + G_2}{2} = 4.9327 \times 10^9 \left[\frac{\text{cts}}{\text{m/s}} \right]$$



Let's calibrate some data

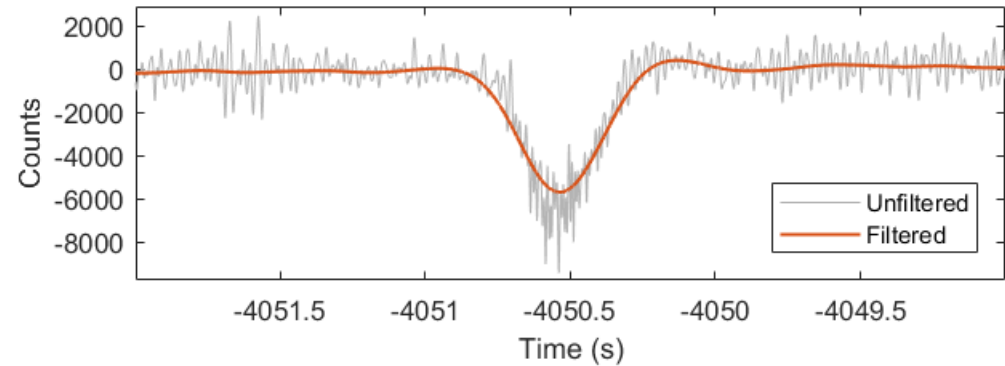
$$G = 4.9327 \times 10^9 \left[\frac{\text{cts}}{\text{m/s}} \right]$$



$$M^2(\omega) = \left| \frac{\hat{u}}{\hat{x}} \right|^2 = \left(\frac{\omega_0^2}{\omega^2} - 1 \right)^2 + 4\lambda^2 \frac{\omega_0^2}{\omega^2} \left[\frac{\text{earth movt}}{\text{mass movt}} \right]$$

Let's calibrate some data

$$G = 4.9327 \times 10^9 \left[\frac{\text{cts}}{\text{m/s}} \right]$$

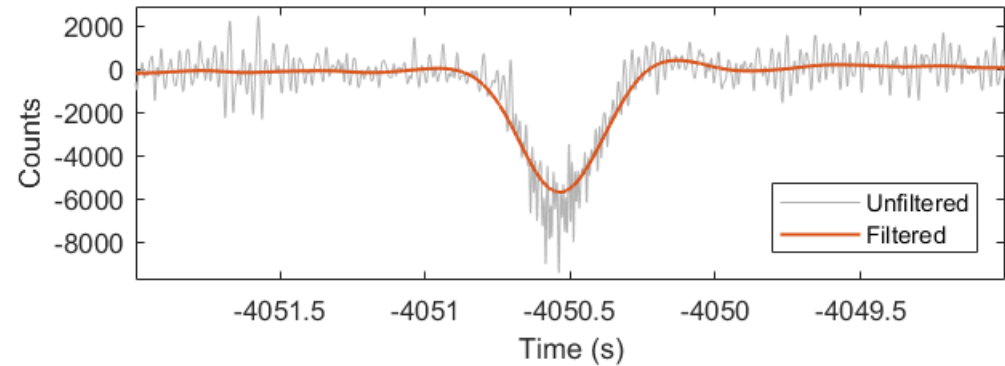


$$M^2(\omega) = \left| \frac{\hat{u}}{\hat{x}} \right|^2 = \left(\frac{\omega_0^2}{\omega^2} - 1 \right)^2 + 4\lambda^2 \frac{\omega_0^2}{\omega^2} \left[\frac{\text{earth movt}}{\text{mass movt}} \right]$$

$$M^2(\omega_d) = \left| \frac{\hat{u}}{\hat{x}} \right|^2 = \left(\frac{\omega_0^2}{\omega_d^2} - 1 \right)^2 + 4\lambda^2 \frac{\omega_0^2}{\omega_d^2}$$

Let's calibrate some data

$$G = 4.9327 \times 10^9 \left[\frac{\text{cts}}{\text{m/s}} \right]$$



$$M^2(\omega) = \left| \frac{\hat{u}}{\hat{x}} \right|^2 = \left(\frac{\omega_0^2}{\omega^2} - 1 \right)^2 + 4\lambda^2 \frac{\omega_0^2}{\omega^2} \left[\frac{\text{earth movt}}{\text{mass movt}} \right]$$

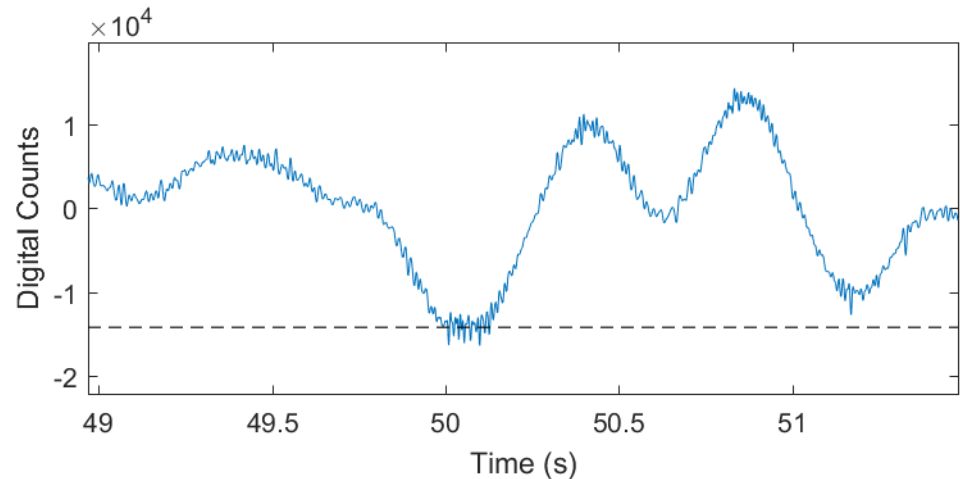
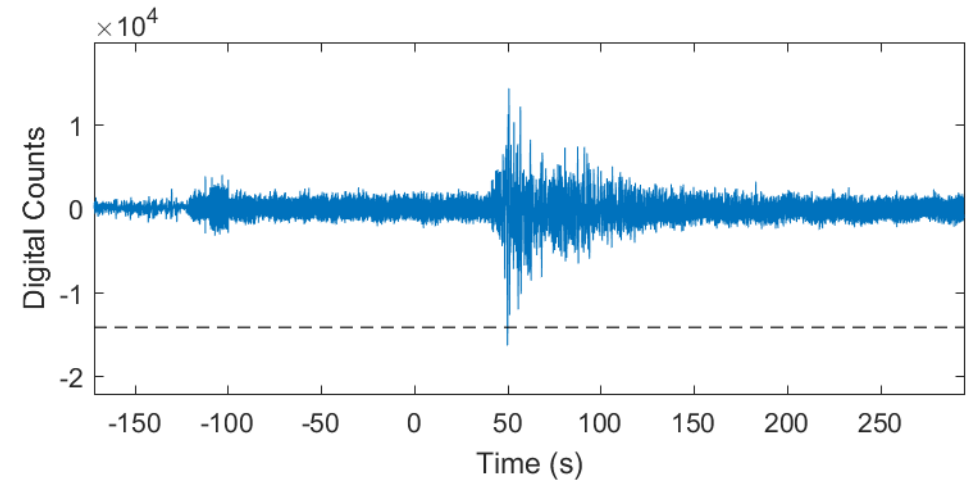
$$M^2(\omega_d) = \left| \frac{\hat{u}}{\hat{x}} \right|^2 = \left(\frac{\omega_0^2}{\omega_d^2} - 1 \right)^2 + 4\lambda^2 \frac{\omega_0^2}{\omega_d^2}$$

$$M(\omega_d) = 1.7985 \left[\frac{\text{earth movt}}{\text{mass movt}} \right]$$

Let's calibrate some data

$$G = 4.9327 \times 10^9 \left[\frac{\text{cts}}{\text{m/s}} \right]$$

$$M(\omega_d) = 1.7985 \left[\frac{\text{earth movt}}{\text{mass movt}} \right]$$



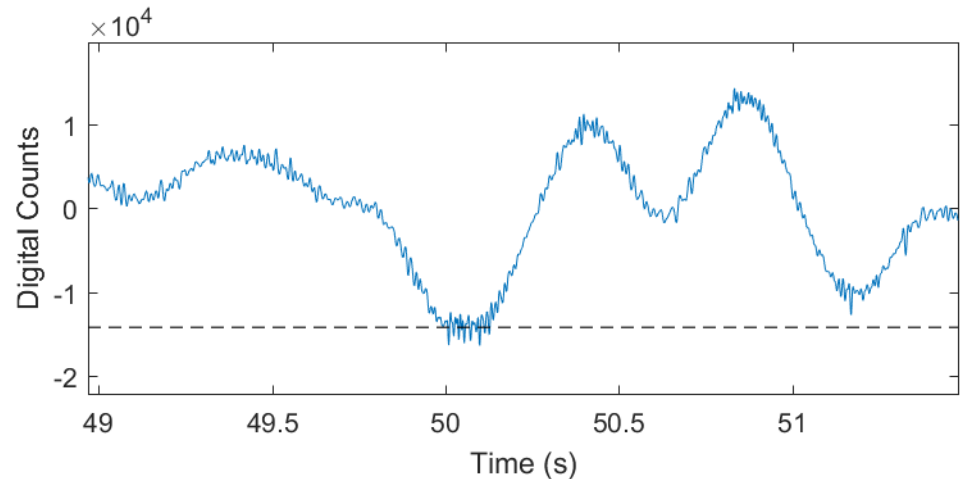
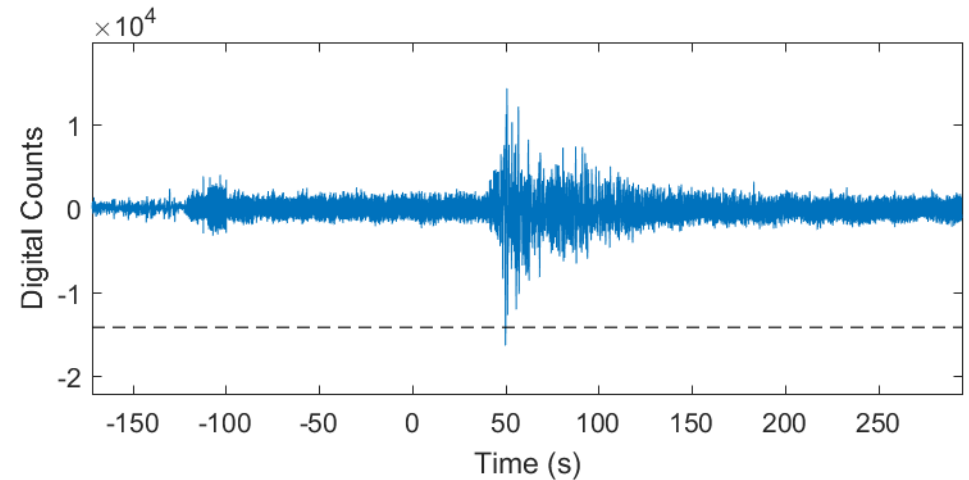
Peak ground velocity (PGV)

Let's calibrate some data

$$G = 4.9327 \times 10^9 \left[\frac{\text{cts}}{\text{m/s}} \right]$$

$$M(\omega_d) = 1.7985 \left[\frac{\text{earth movt}}{\text{mass movt}} \right]$$

$$PGV = 14233 \text{ [cts]}$$



Peak ground velocity (PGV)

Let's calibrate some data

REVISED 10/17/67

$$G = 4.9327 \times 10^9 \left[\frac{\text{cts}}{\text{m/s}} \right]$$

$$M(\omega_d) = 1.7985 \left[\frac{\text{earth movt}}{\text{mass movt}} \right]$$

$$PGV = 14233 [\text{cts}]$$

SEISMIC FIELD SHEET...Page 5

TAPE CHANNEL 5 DATA

6819-1

VCO FREQUENCY in CPS	INSTRUMENT	CAL db PDA PAD	RUN db PDA PAD	BAND EDGE SENS.*	ELECTR. GAIN	CAL BATT. VOLTS
1120	TSP÷5	48	96	.5v		.45v
1300	TSP×1		↓			
1480	RSP÷25		84			
1660	RSP÷5		↓			
1840	RSP×1		↓			
2030	VSP÷25		84			
2230	VSP÷5		↓			
2450	VSP×1		↓			

* Band Edge = 100% of bandwidth

SHORT PERIOD WEIGHT LIFTS

VERTICAL	<u>10.8</u>	DIV. @	<u>48</u> db	<u>13:1</u>
RADIAL	<u>14.9</u>	DIV. @	<u>48</u> db	<u>11:1</u>
TANGENTIAL	<u>12</u>	DIV. @	<u>48</u> db	<u>12:1</u>

DAMPING

SHORT PERIOD WEIGHT/MICRONS

VERTICAL	<u>.255</u> gms.	=	<u>.319</u> u
RADIAL	<u>2.000</u> gms.	=	<u>.250</u> u
TANGENTIAL	<u>2.000</u> gms.	=	<u>.250</u> u

NGC-23 CALIBRATION

VERTICAL	<u> </u>	DIV. @	<u> </u> db
RADIAL/STS	<u> </u>	DIV. @	<u> </u> db
RADIAL/NTS	<u> </u>	DIV. @	<u> </u> db

Seismic Arrival Time*

* Ely and Battle Mt. only. Other stations are noted on Field Data Sheet

$$PGV = \frac{14233 \times 5 [\text{cts}]}{10^{-\frac{84 [\text{dB}]}{20}}} \times \frac{1 [\text{m/s}]}{4.9327 \times 10^9 [\text{cts}]} \times \frac{1.7985 [\text{earth movt}]}{1 [\text{mass movt}]} = 0.1637 [\text{cm/s}]$$

Let's calibrate some data

$$G = 4.9327 \times 10^9 \left[\frac{\text{cts}}{\text{m/s}} \right]$$

$$M(\omega_d) = 1.7985 \left[\frac{\text{earth movt}}{\text{mass movt}} \right]$$

$$PGV = 14233 [\text{cts}] = 0.1637 [\text{cm/s}]$$

Murphy & Lahoud (1969)

$$PGV = 31.1W^{.505}R^{-1.58}$$

Analysis of seismic peak amplitudes from underground nuclear explosions. *Bull. Seismo. Soc. Am.*, 59(6).

Let's calibrate some data

$$G = 4.9327 \times 10^9 \left[\frac{\text{cts}}{\text{m/s}} \right]$$

$$M(\omega_d) = 1.7985 \left[\frac{\text{earth movt}}{\text{mass movt}} \right]$$

$$PGV = 14233 \text{ [cts]} = 0.1637 \text{ [cm/s]}$$

Murphy & Lahoud (1969)

$$PGV = 31.1W^{.505}R^{-1.58} = 0.1620 \text{ [cm/s]}$$

BOXCAR Leeds, UT

$$W = 1300 \text{ [kt]} \quad R = 276 \text{ [km]}$$

Let's calibrate some data

$$G = 4.9327 \times 10^9 \left[\frac{\text{cts}}{\text{m/s}} \right]$$

$$M(\omega_d) = 1.7985 \left[\frac{\text{earth movt}}{\text{mass movt}} \right]$$

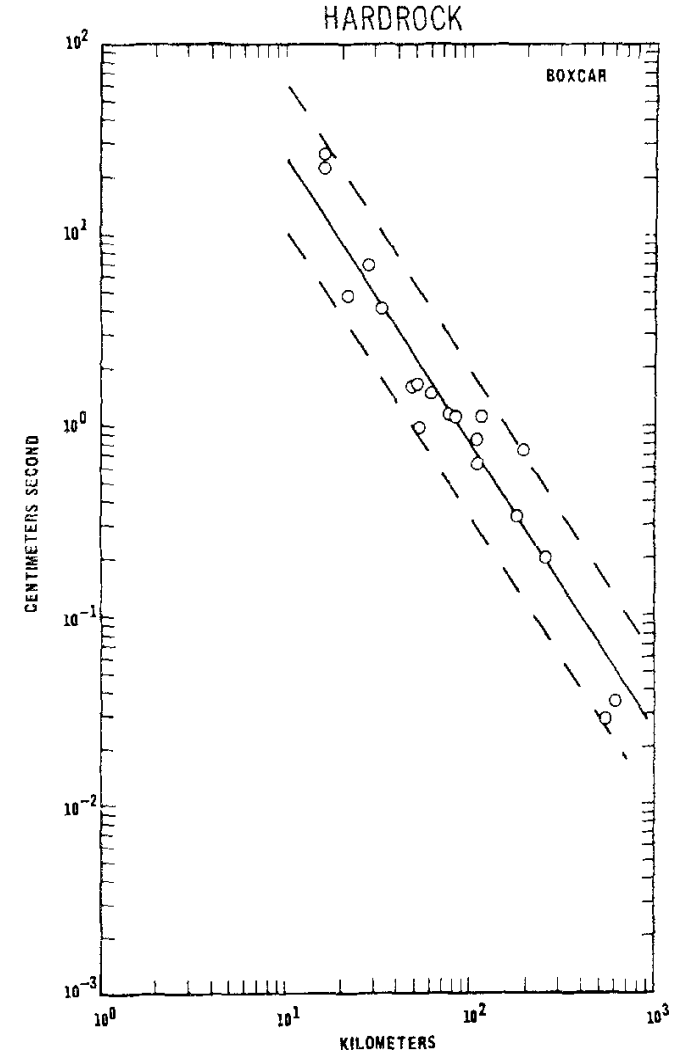
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BOXCAR Leeds, UT

$W = 1300 [\text{kt}]$ $R = 276 [\text{km}]$



Let's calibrate some data

$$G = 4.9327 \times 10^9 \left[\frac{\text{cts}}{\text{m/s}} \right]$$

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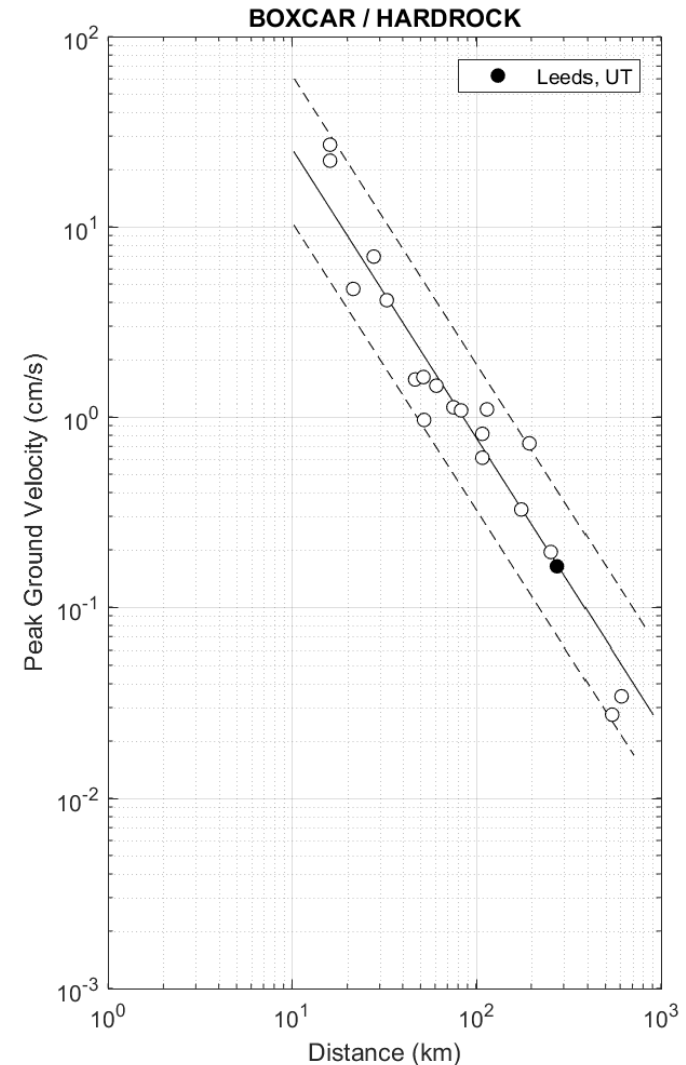
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Murphy & Lahoud (1969)

$$PGV = 31.1W^{.505}R^{-1.58} = 0.1620 [\text{cm/s}]$$

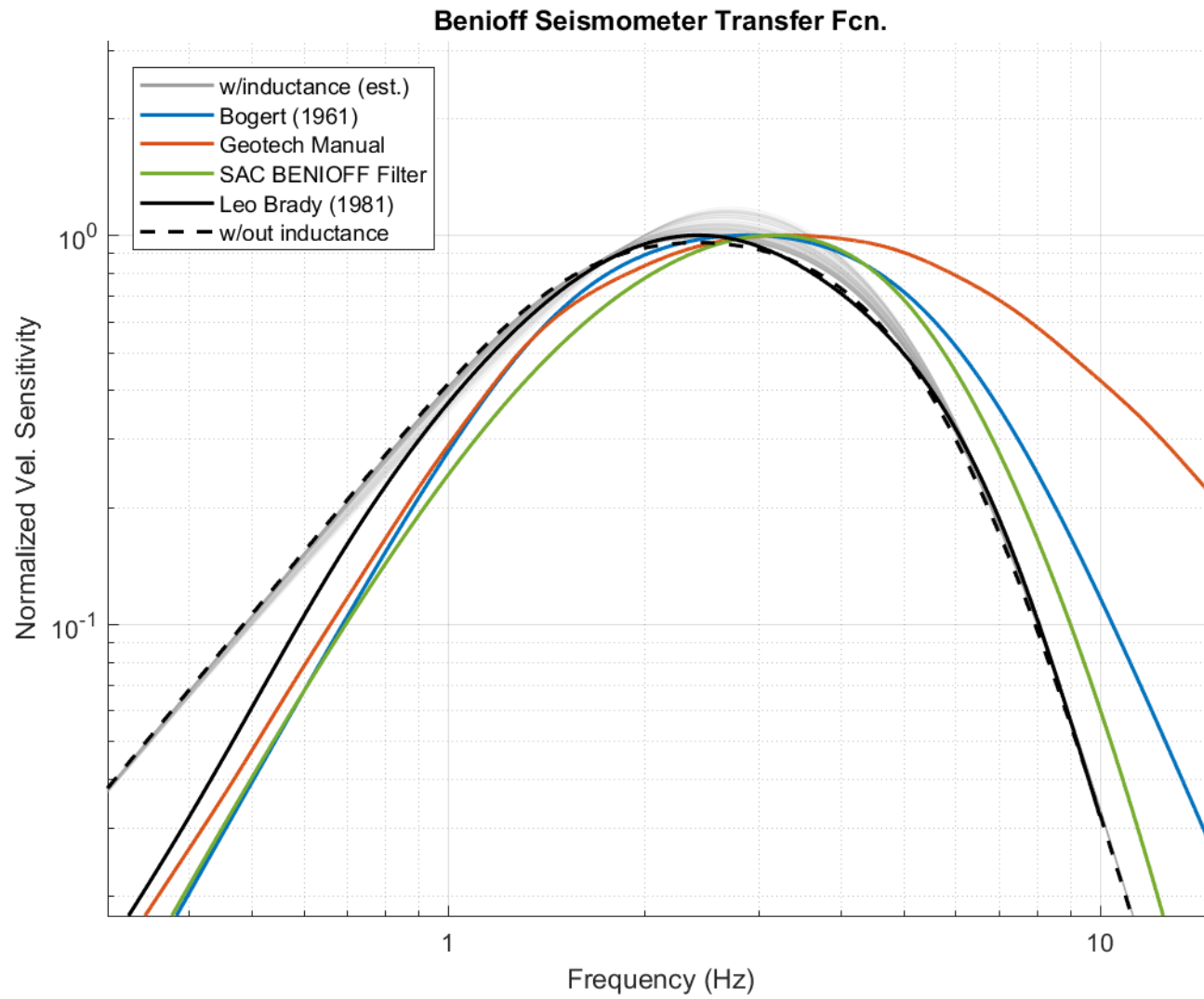
BOXCAR Leeds, UT

$W = 1300 [\text{kt}]$ $R = 276 [\text{km}]$

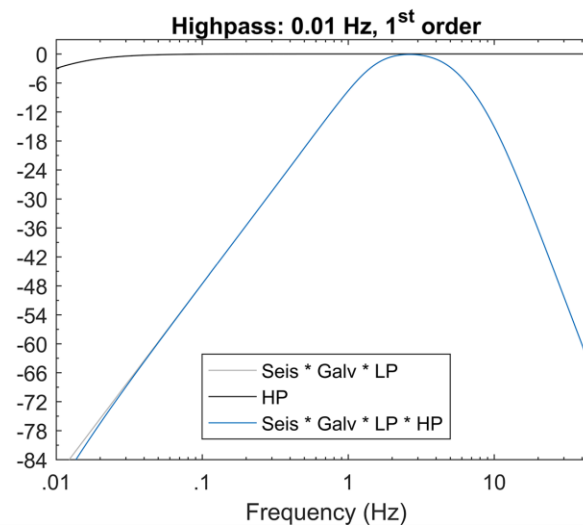
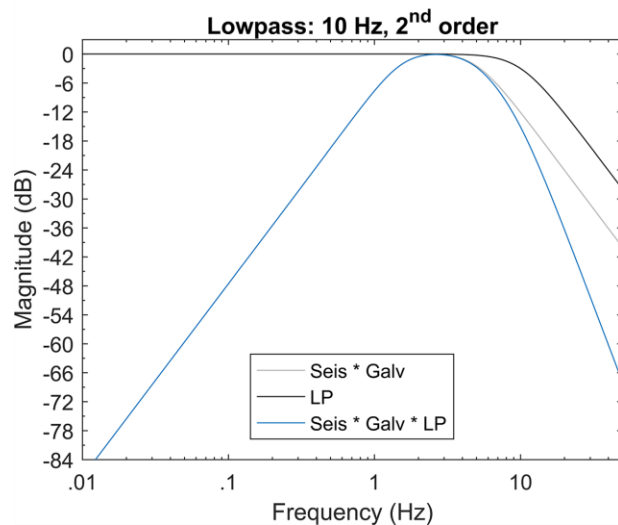
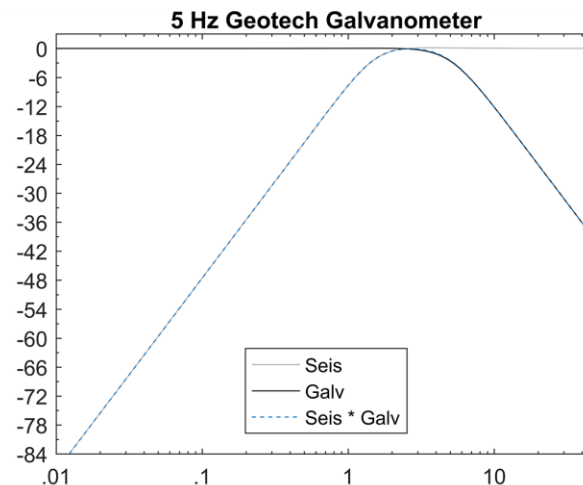
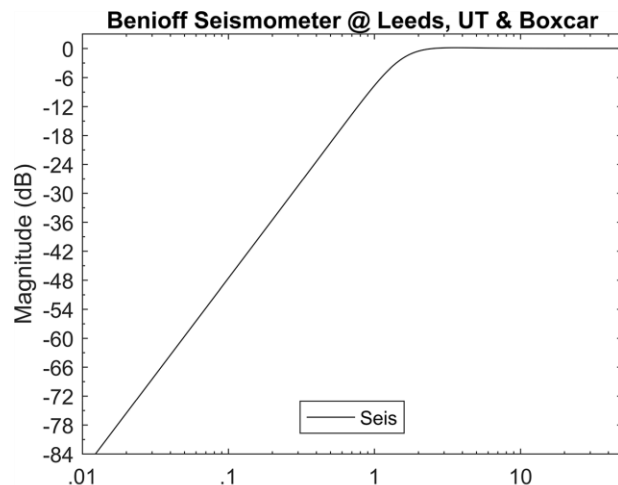


Instrument Response

Comparison of freq. resposnes



Building an instrument response



Building an instrument response

Velocity
transfer function

$$\hat{T}_V(\omega) = \frac{\omega^2}{\omega_s^2 - \omega^2 + i2\lambda_s\omega_s\omega} \cdot \frac{1}{\omega_g^2 - \omega^2 + i2\lambda_g\omega_g\omega}$$

Seismometer Galvanometer
(Benioff 1051/1101) (Geotech Model 4100-13)

$$\omega_s = 2\pi \cdot 1.54 \text{ [Hz]} \quad \omega_g = 2\pi \cdot 5 \text{ [Hz]}$$

$$\lambda_s = 0.6389 \quad \lambda_g = 0.675$$

Building an instrument response

Velocity
transfer function

$$\hat{T}_V(\omega) = \frac{\omega^2}{\omega_s^2 - \omega^2 + i2\lambda_s\omega_s\omega} \cdot \frac{1}{\omega_g^2 - \omega^2 + i2\lambda_g\omega_g\omega}$$

Seismometer

(Benioff 1051/1101)

Galvanometer

(Geotech Model 4100-13)

$$\cdot \frac{i\omega Q\sqrt{2}}{\omega_{c,hp} + i\omega} \cdot \frac{\omega_{c,lp}^2}{\omega_{c,lp}^2 - \omega^2 + i\omega\omega_{c,lp}Q^{-1}}$$

1st order

highpass

2nd order

lowpass

$$Q = -3 \text{ [dB]}$$

$$\omega_c = 0.01 \text{ [Hz]}$$

$$Q = -3 \text{ [dB]}$$

$$\omega_c = 8 \text{ [Hz]}$$

Filter FL201
*(Geotech PTA Model
4300 Manual, Fig. 4)*

Building an instrument response

Velocity
transfer function

$$\hat{T}_V(\omega) = \frac{\omega^2}{\omega_s^2 - \omega^2 + i2\lambda_s\omega_s\omega} \cdot \frac{1}{\omega_g^2 - \omega^2 + i2\lambda_g\omega_g\omega}$$

Seismometer Galvanometer
(Benioff 1051/1101) (Geotech Model 4100-13)

$$\cdot \frac{i\omega Q\sqrt{2}}{\omega_{c,hp} + i\omega} \cdot \frac{\omega_{c,lp}^2}{\omega_{c,lp}^2 - \omega^2 + i\omega\omega_{c,lp}Q^{-1}}$$

1st order 2nd order
highpass lowpass

Filter FL201
(Geotech PTA Model
4300 Manual, Fig. 4)

$$\cdot \frac{i\omega Q\sqrt{2}}{\omega_{c,hp} + i\omega} \cdot \frac{\omega_{c,lp}^2}{\omega_{c,lp}^2 - \omega^2 + i\omega\omega_{c,lp}Q^{-1}}$$

Phototube Amp
(Geotech PTA Model
4300 Manual, Fig. 11)

$$Q = -3 \text{ [dB]} \quad Q = -3 \text{ [dB]}$$

$$\omega_c = 0.01 \text{ [Hz]} \quad \omega_c = 5 \text{ [Hz]}$$

Building an instrument response

Velocity
transfer function

$$\hat{T}_V(\omega) = \frac{\omega^2}{\omega_s^2 - \omega^2 + i2\lambda_s\omega_s\omega} \cdot \frac{1}{\omega_g^2 - \omega^2 + i2\lambda_g\omega_g\omega}$$

Seismometer

(Benioff 1051/1101)

Galvanometer

(Geotech Model 4100-13)

$$\cdot \frac{i\omega Q\sqrt{2}}{\omega_{c,hp} + i\omega} \cdot \frac{\omega_{c,lp}^2}{\omega_{c,lp}^2 - \omega^2 + i\omega\omega_{c,lp}Q^{-1}}$$

1st order
highpass

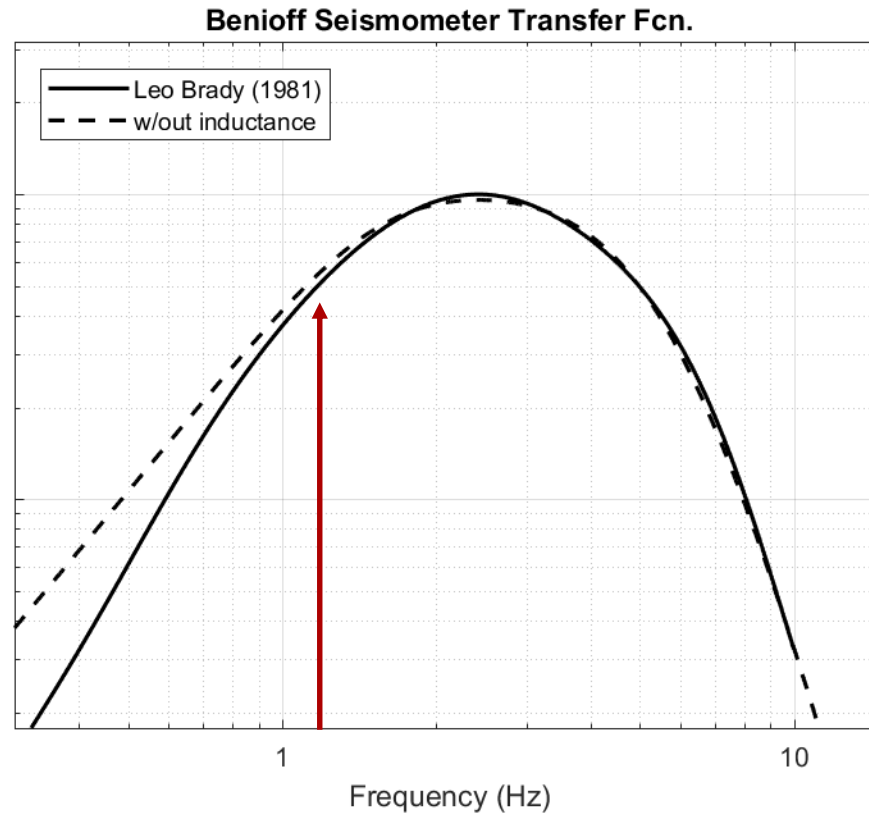
2nd order
lowpass

Filter FL201
*(Geotech PTA Model
4300 Manual, Fig. 4)*

$$\cdot \frac{i\omega Q\sqrt{2}}{\omega_{c,hp} + i\omega} \cdot \frac{\omega_{c,lp}^2}{\omega_{c,lp}^2 - \omega^2 + i\omega\omega_{c,lp}Q^{-1}}$$

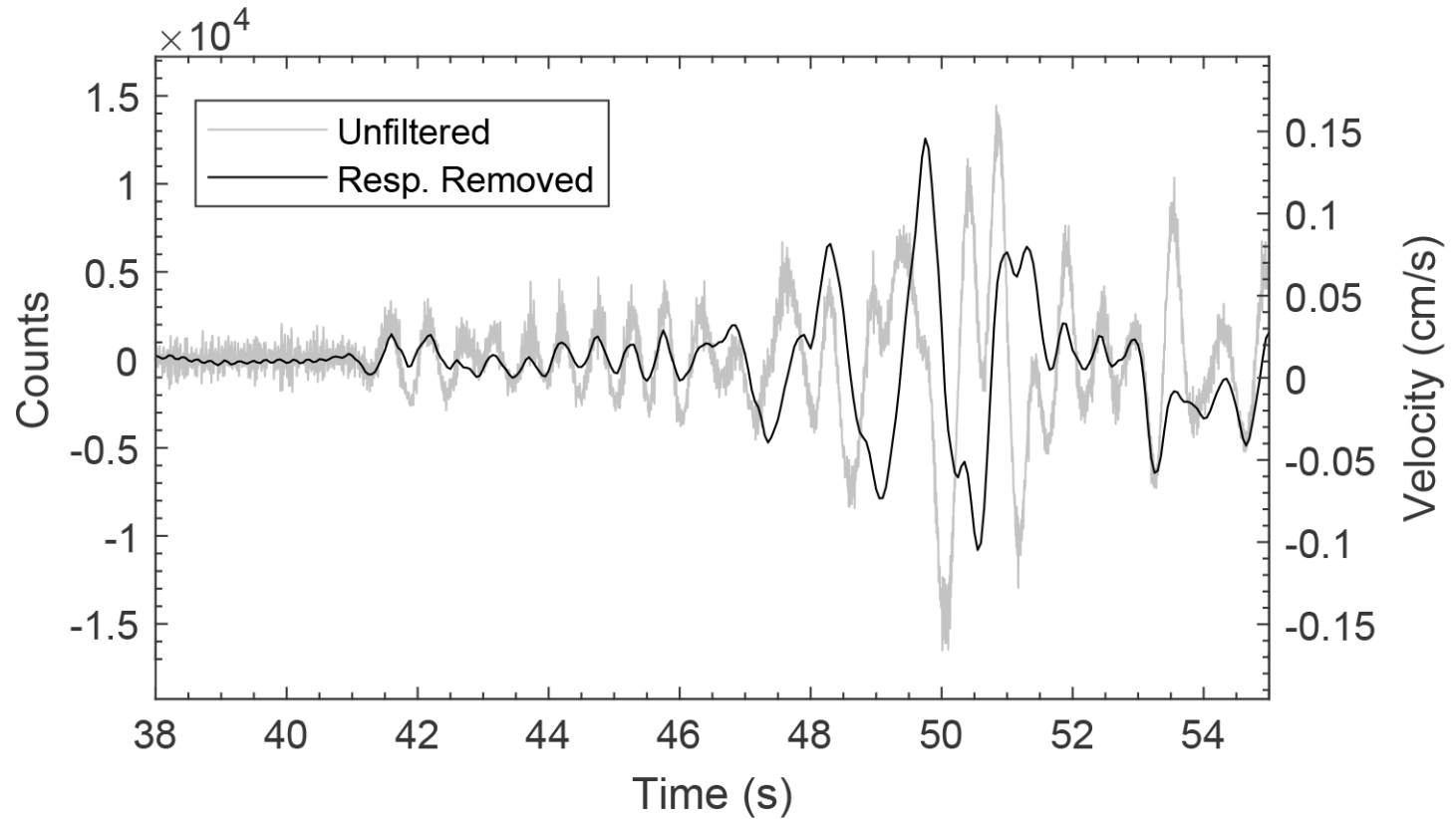
Phototube Amp
*(Geotech PTA Model
4300 Manual, Fig. 11)*

Final calibration



$$f_d = 1.1905 \text{ [Hz]}$$

Final calibration



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Legacy Data project: An SNL multi-department effort!

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