

# Effect of Fracture Toughness Testing Geometry on Opening Style: Implications for Subsurface Crack Propagation

Alex Rinehart

E&ES (NMT) and Geomechanics (SNL)

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# Acknowledgements

## **Co-authors**

Thomas Dewers and Joseph Bishop

## **Laboratory Collaborators**

Alex Urquhart, Scott Broome and Greg Flint

## **Advisor**

Glenn Spinelli

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# To Begin....

**Mechanical strength of Lower Tuscaloosa  
Injection Horizon at CO<sub>2</sub> injection  
reservoir conditions.**

**Effect of fracture toughness testing  
geometry on opening style.**

**Automatic overlapping phase arrival  
picker: Picking P&S waves from acoustic  
emissions.**

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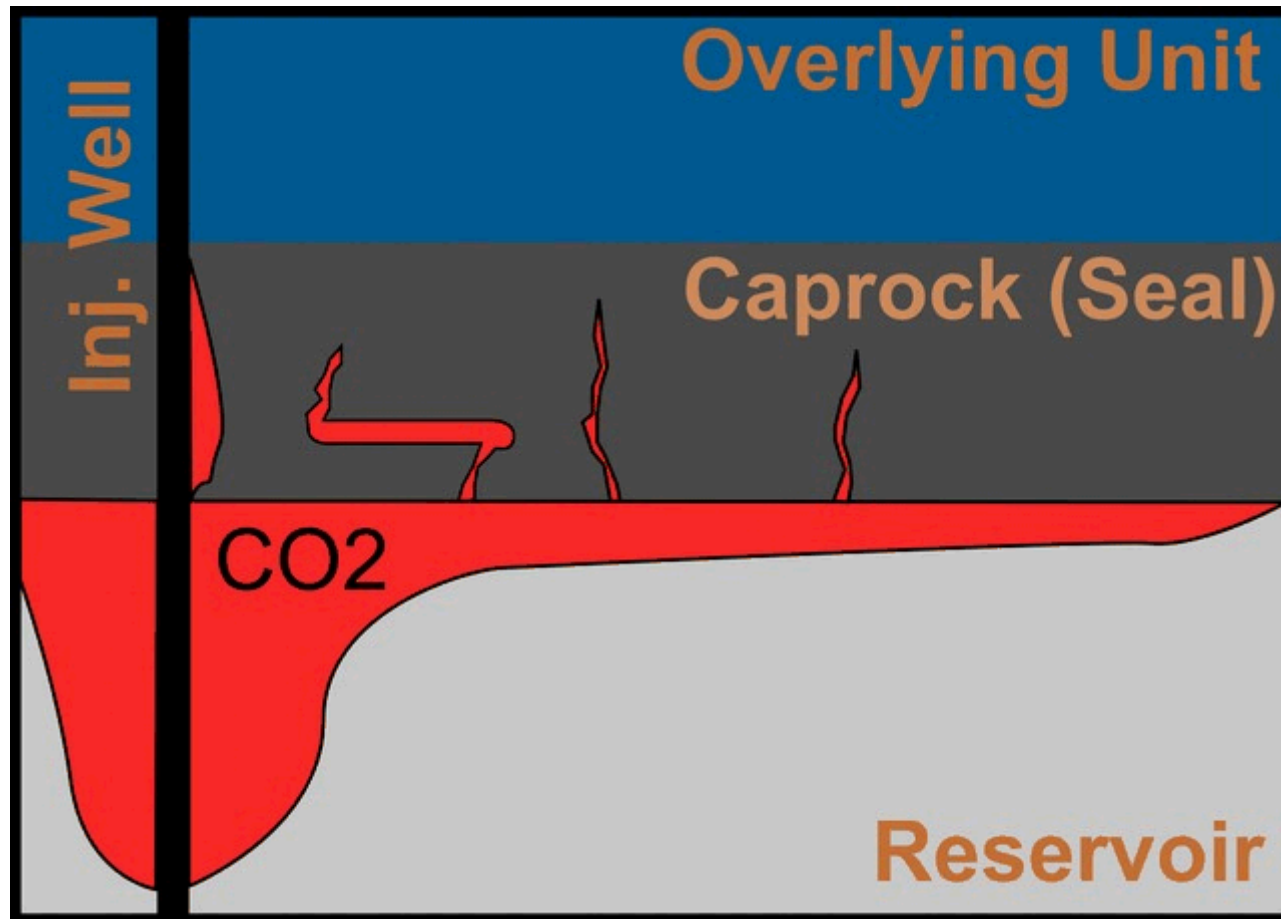
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# Why Care About Fractures?

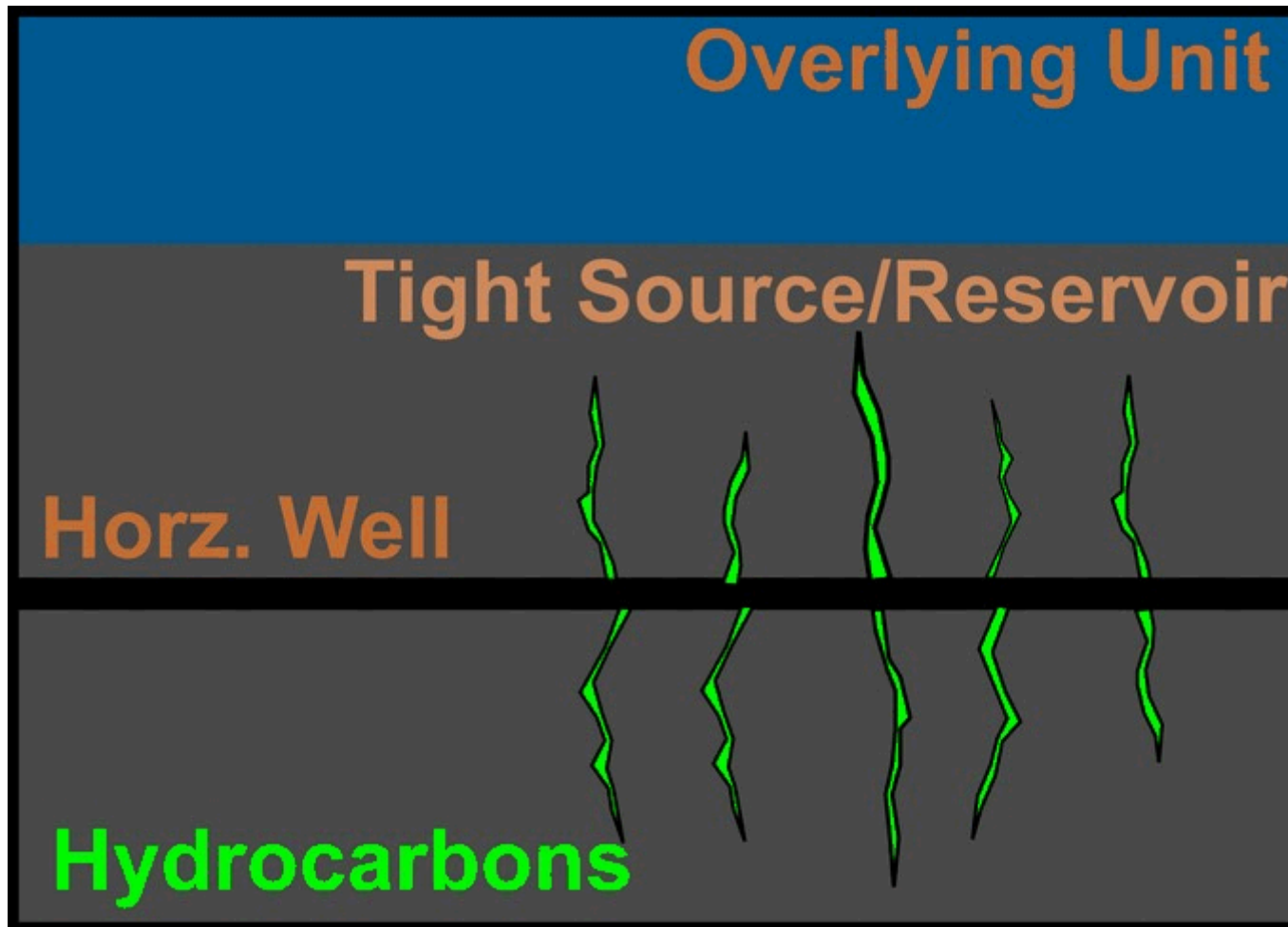
Fractures are a fast flow path in tight rocks.



Subsurface CO2 storage leakage pathway.

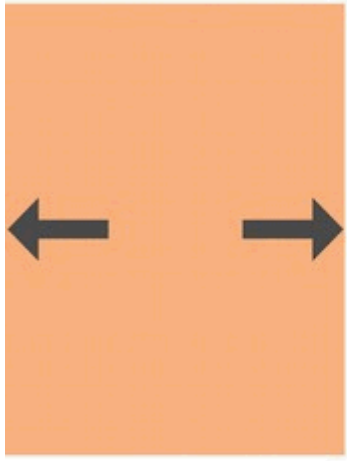
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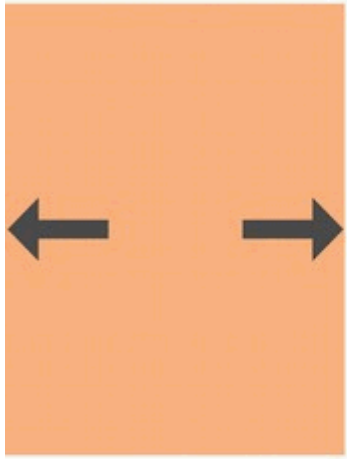
**Natural Gas Release in Shales**

# Fractures Defined



**Elastic**

# Fractures Defined



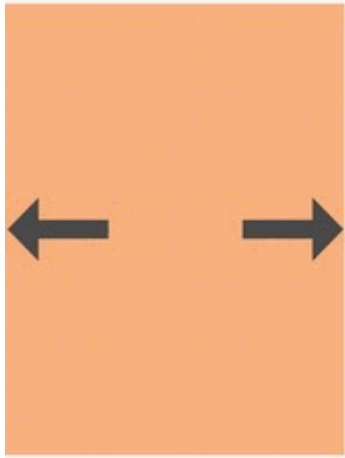
**Elastic**



**Distributed  
Damage  
(Yield)**



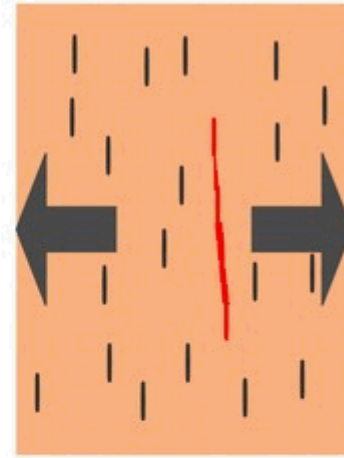
# Fractures Defined



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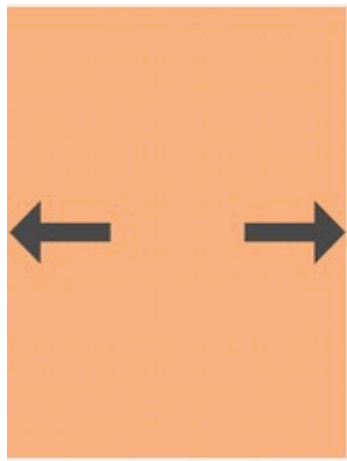


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**Coalescence  
of Damage  
(Peak Stress)**

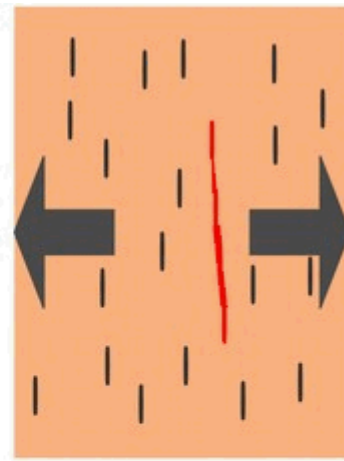
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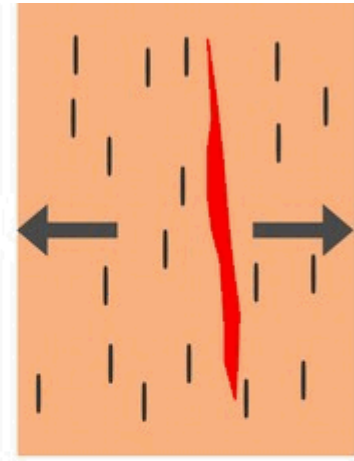
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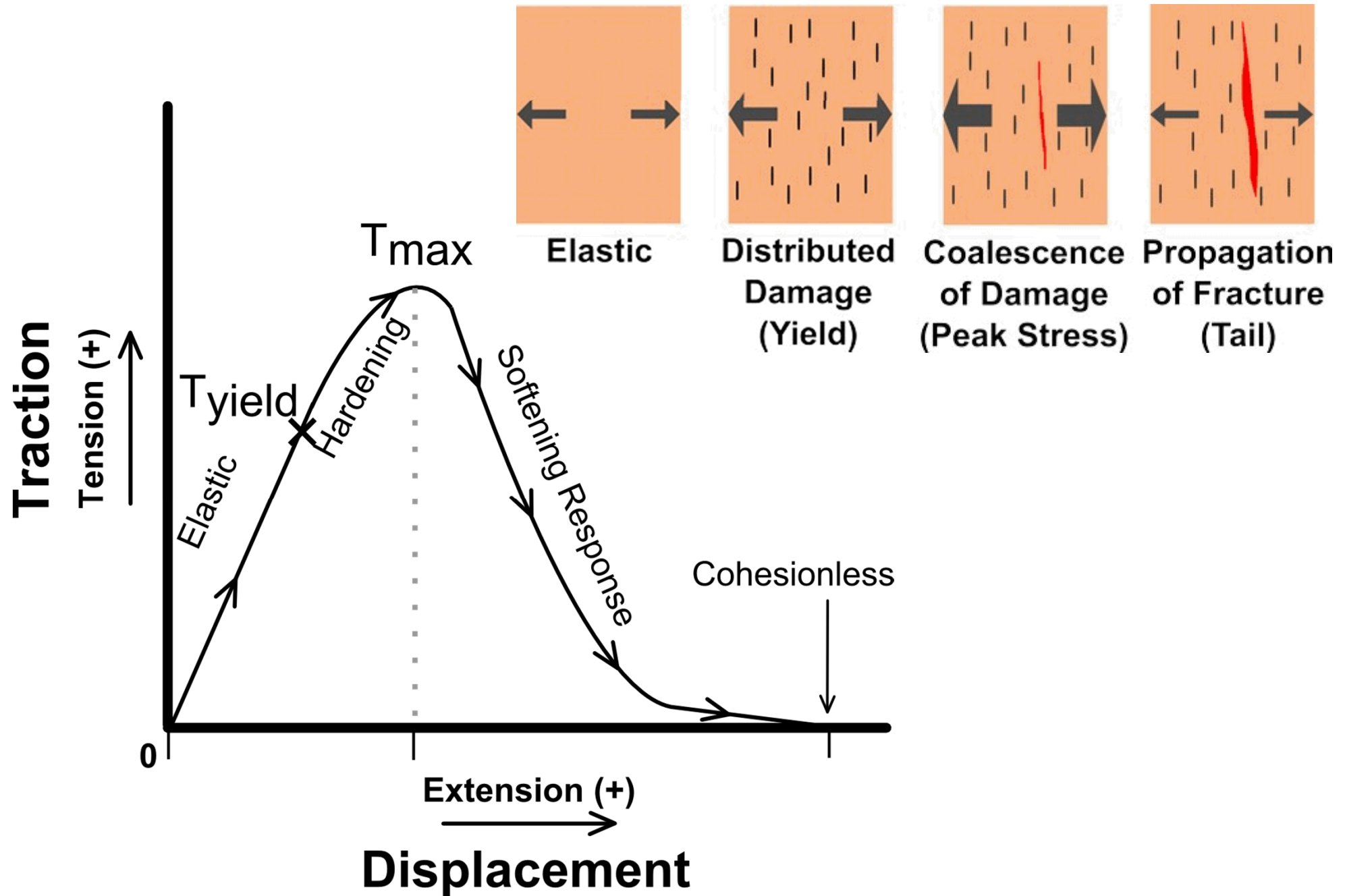
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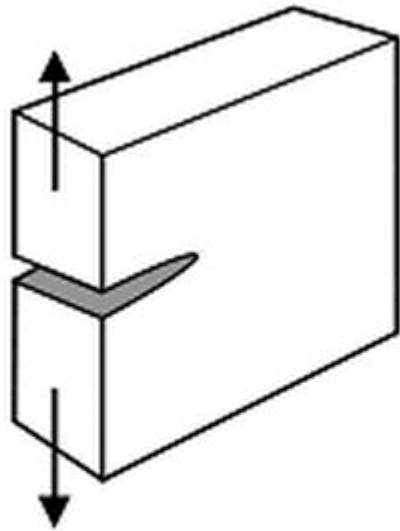
**Propagation  
of Fracture  
(Tail)**

**The coalescence of damage into a single roughly planar opening with limited surrounding damage.**

# Fractures Defined

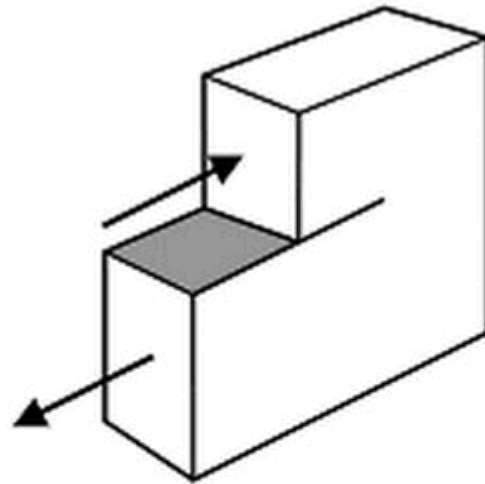


# Modes: Opening vs. Shear



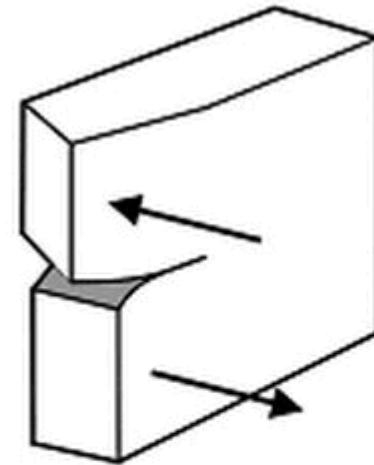
**I**

**Opening**



**II**

**Shear**

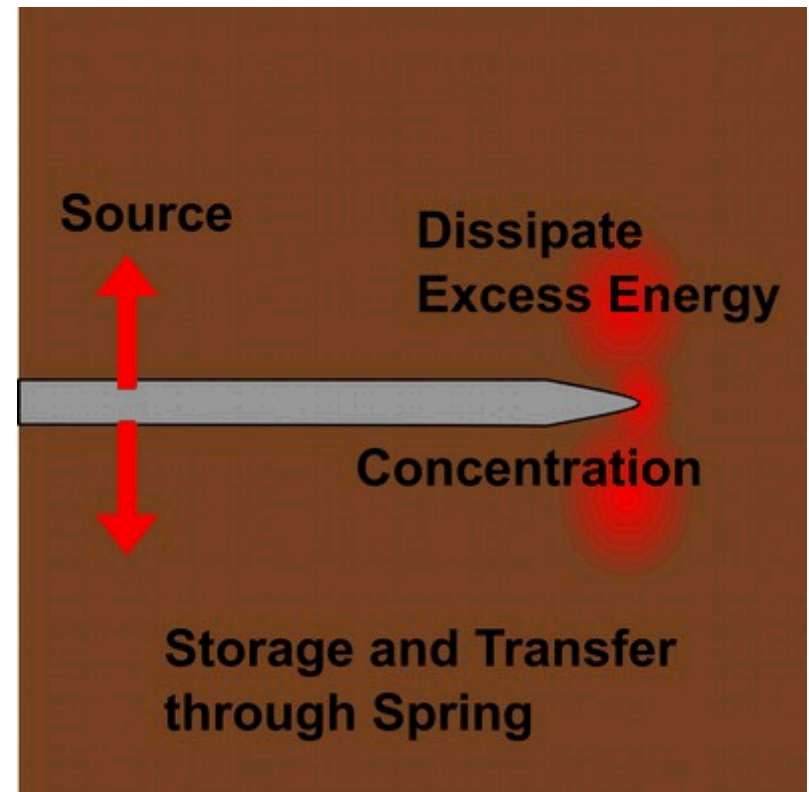
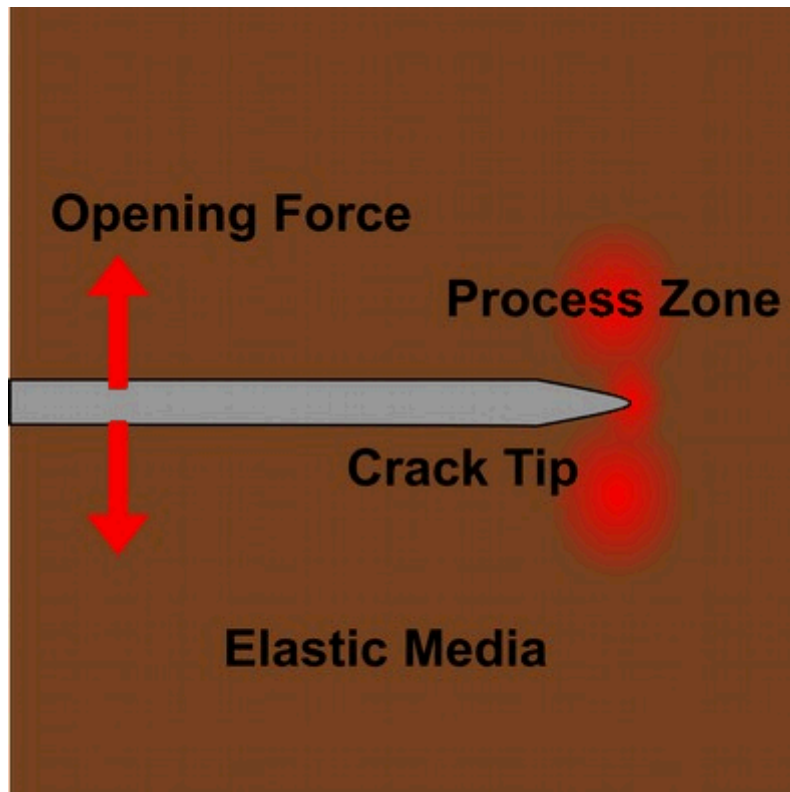


**III**

**For rocks, shear mode is often to 5x stronger than opening mode**

[http://www.doitpoms.ac.uk/tlplib/brittle\\_fracture/same.php](http://www.doitpoms.ac.uk/tlplib/brittle_fracture/same.php)

# The Parts of a Fracture



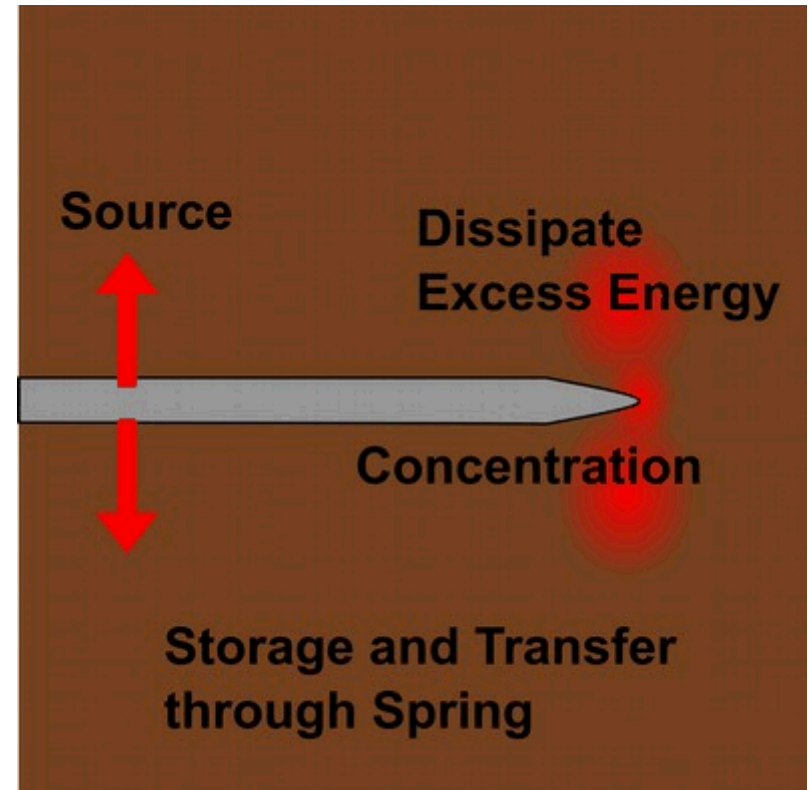
# The Energy Balance

**Softer the spring, the more displacement needed to get enough force (energy) to propagate fracture.**

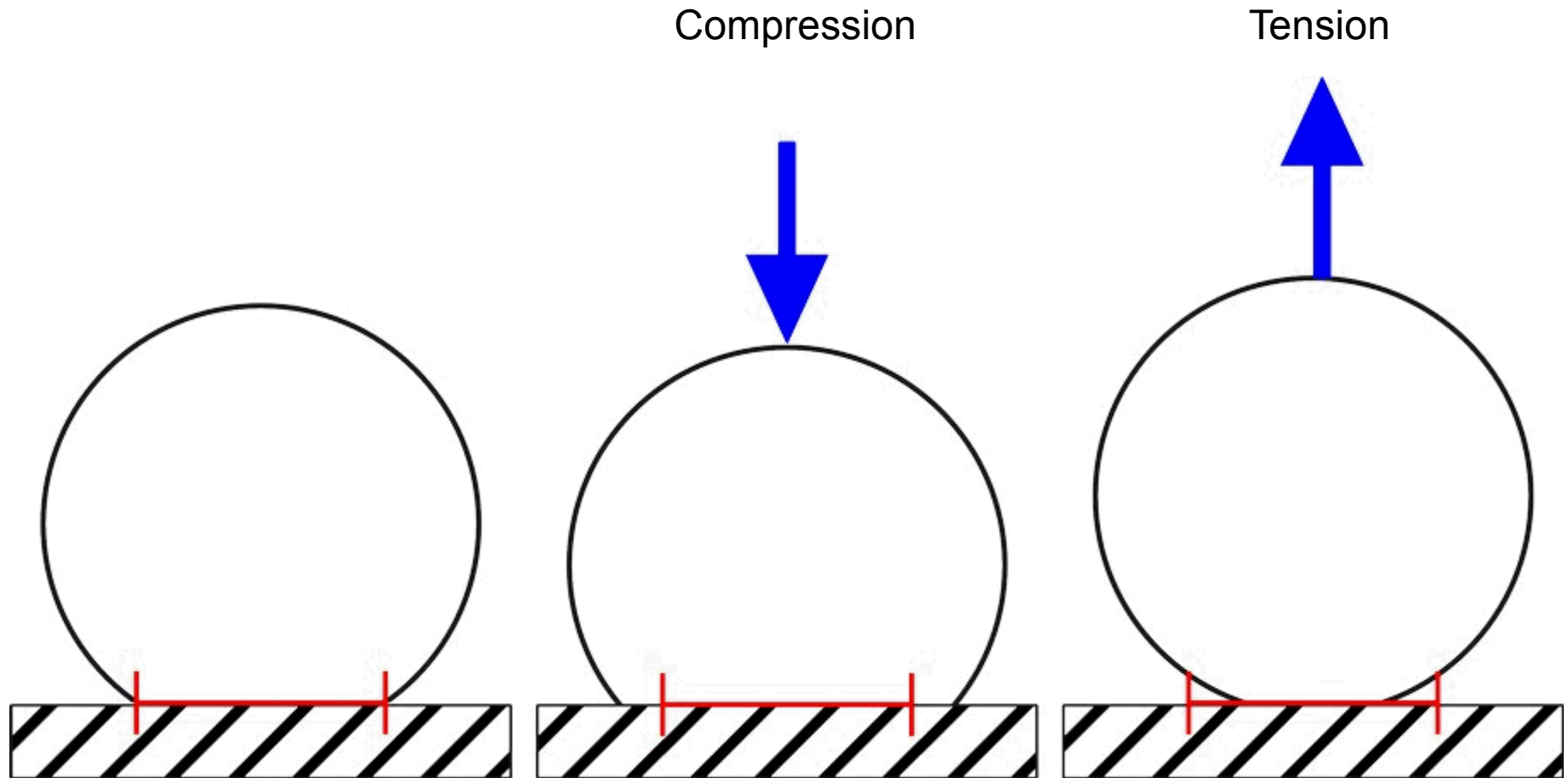
'Spring compliance' controlled by inherent material properties and tension/compression stress state.

**Magnitude of excess energy controlled by fracture mode:**

Shear Strength > Opening Strength

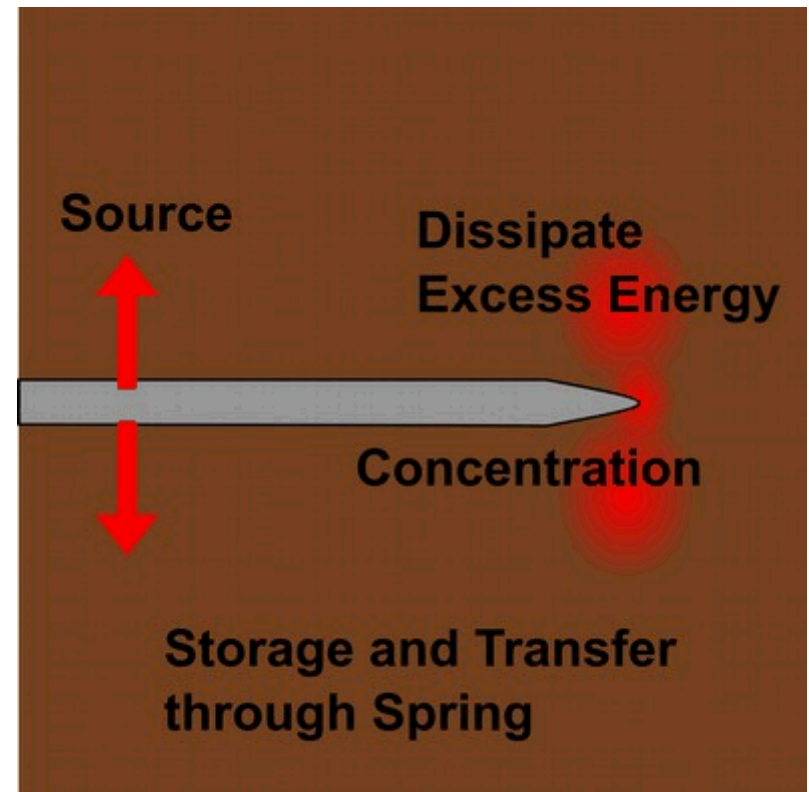
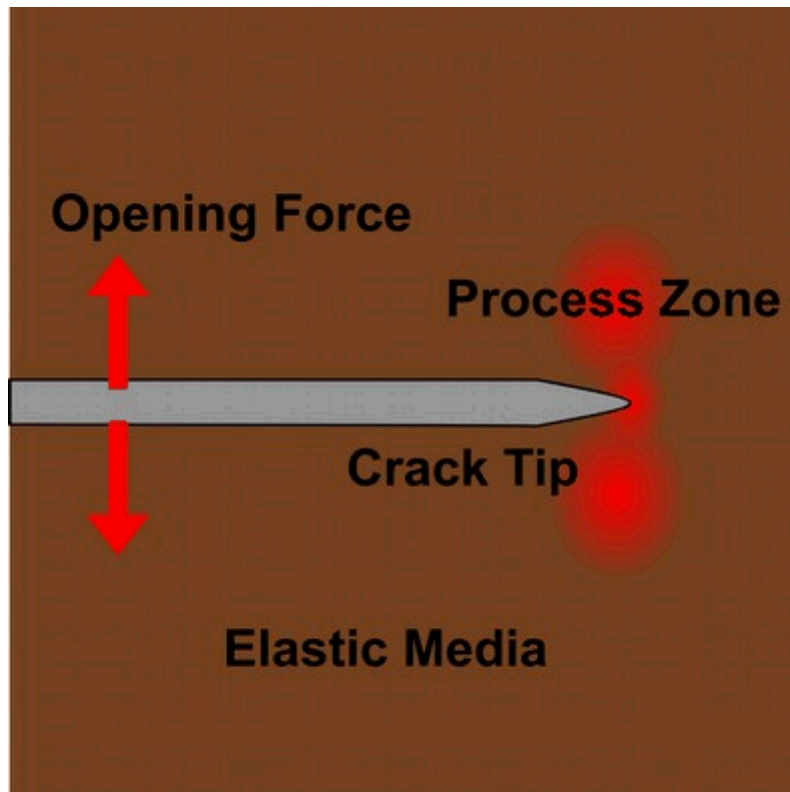


# Tension vs. Compression



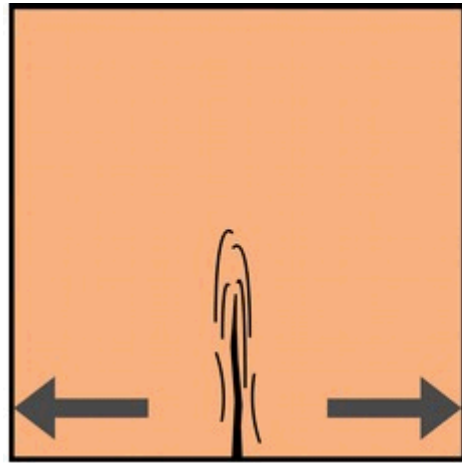
**Both b/c of pores closing and grain contacts, elastic moduli are less stiff in tension than in compression.**

# The Parts of a Fracture

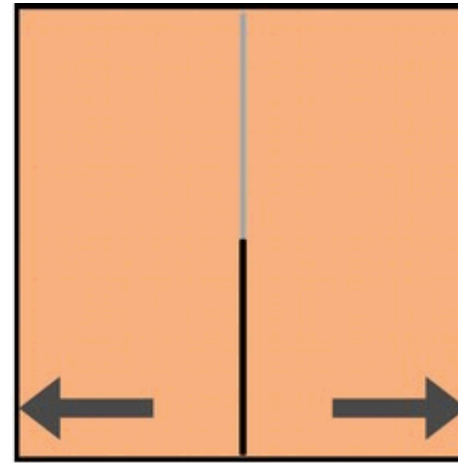




# Cohesive Fracture Approach



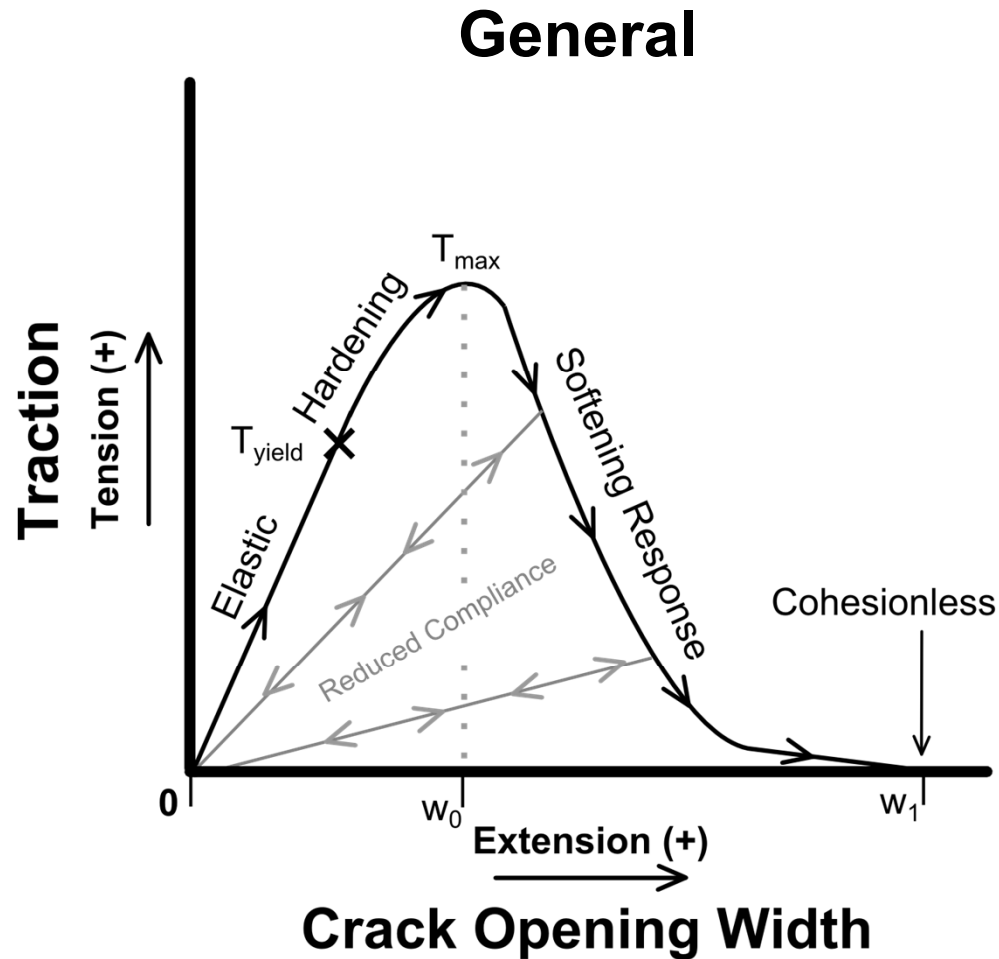
**'Real' Fracture  
w/ Distributed  
Damage and  
Complex  
Geometry**



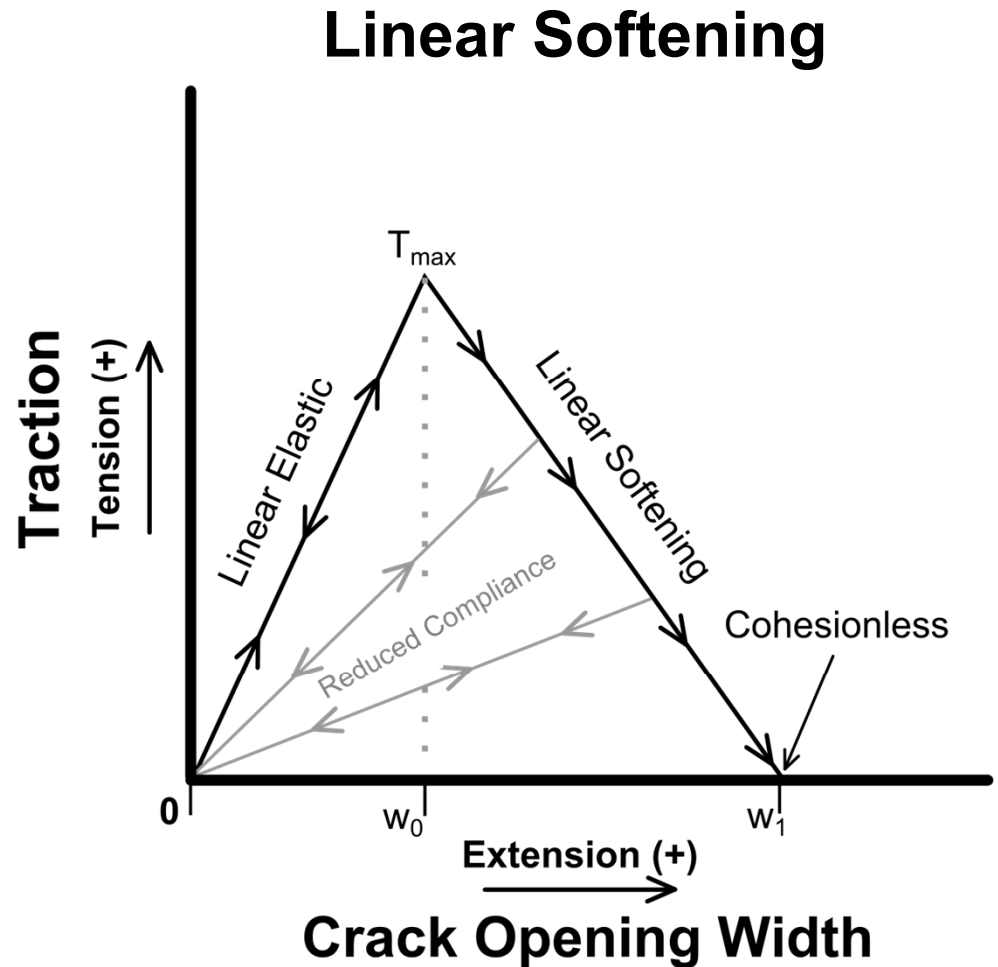
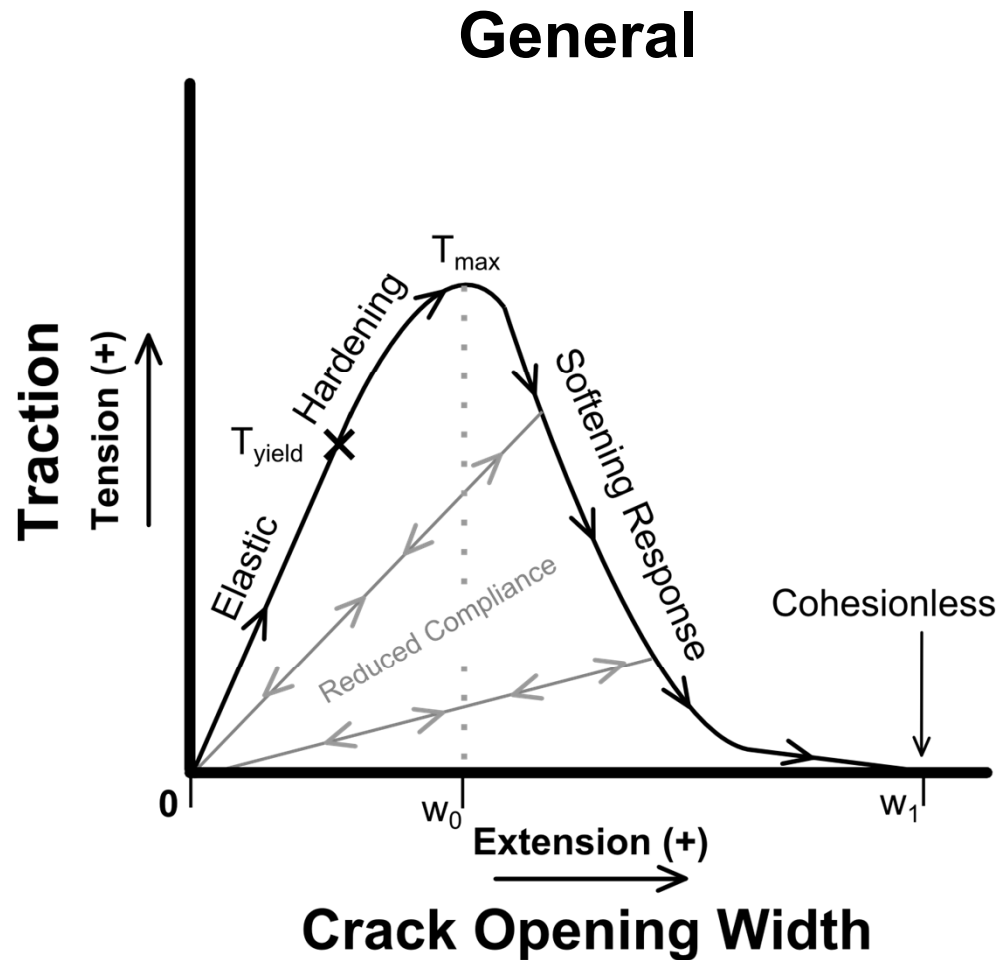
**Cohesive  
Fracture w/  
Finite Defined  
Zone of  
Damage**

**Cohesive fracture lumps all inelastic deformation into thin finite zone.**

# Cohesive Fracture Approach

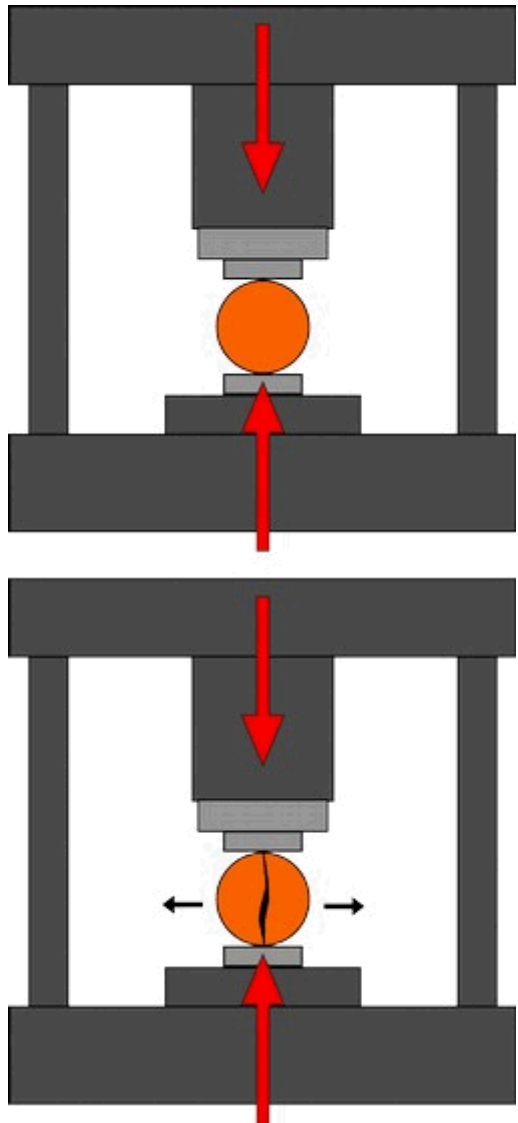


# Cohesive Fracture Approach



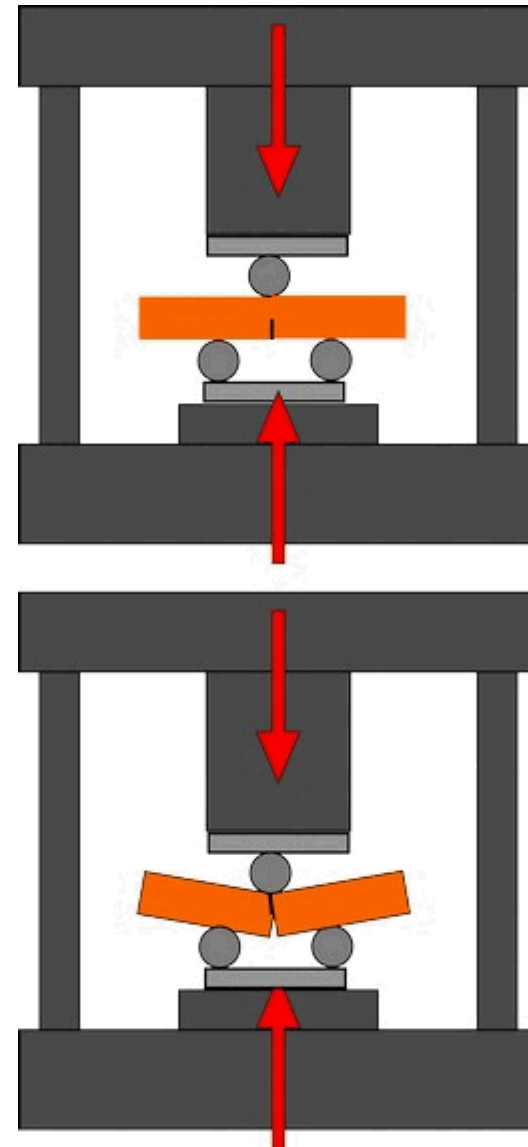
**Posited in geomaterials, but little work systematically confirming approach.**

# Approaches to Fractures (Testing)



**Brazil Test**

**Tensile Splitting Stress**



**Notched 3-Point-Bend**

**Fracture Toughness**

# Approaches to Fractures (Testing)

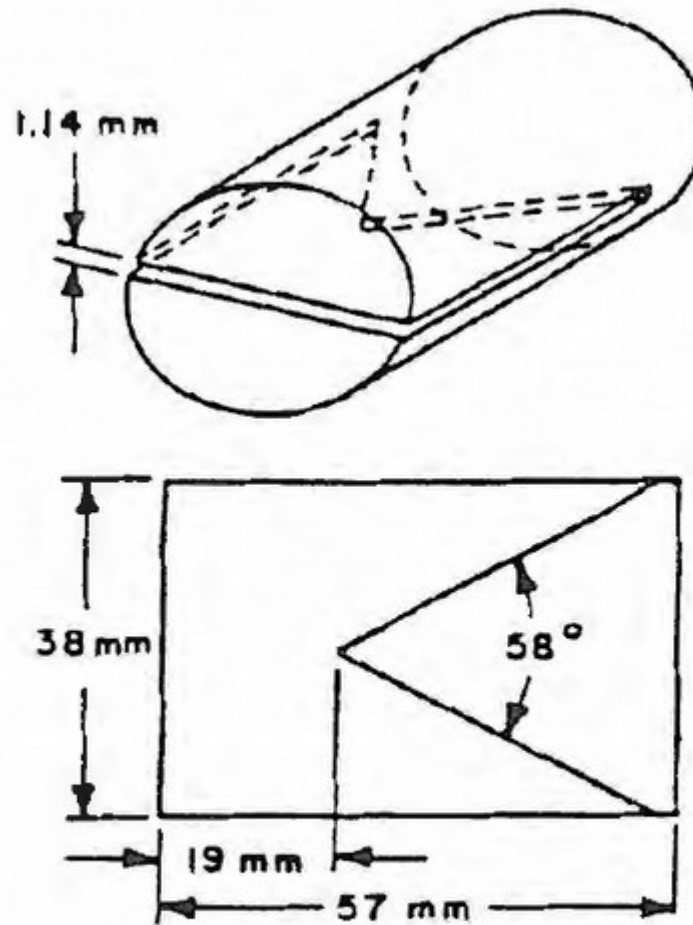
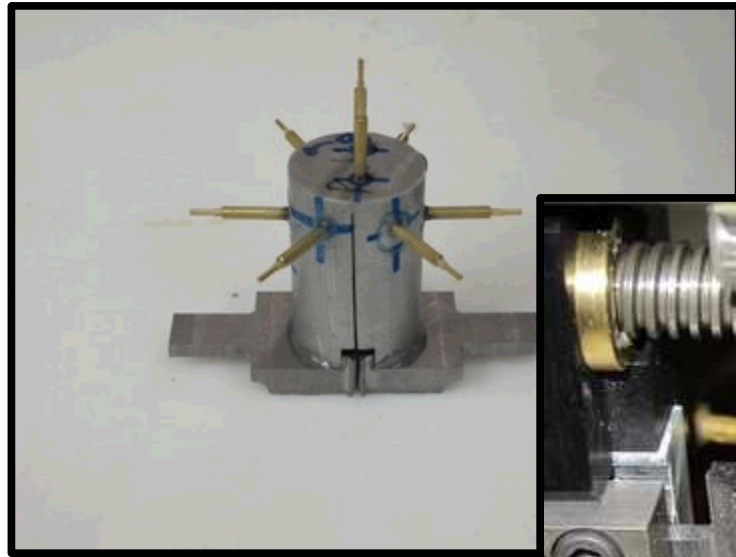


Fig.1 Specimen Geometry.

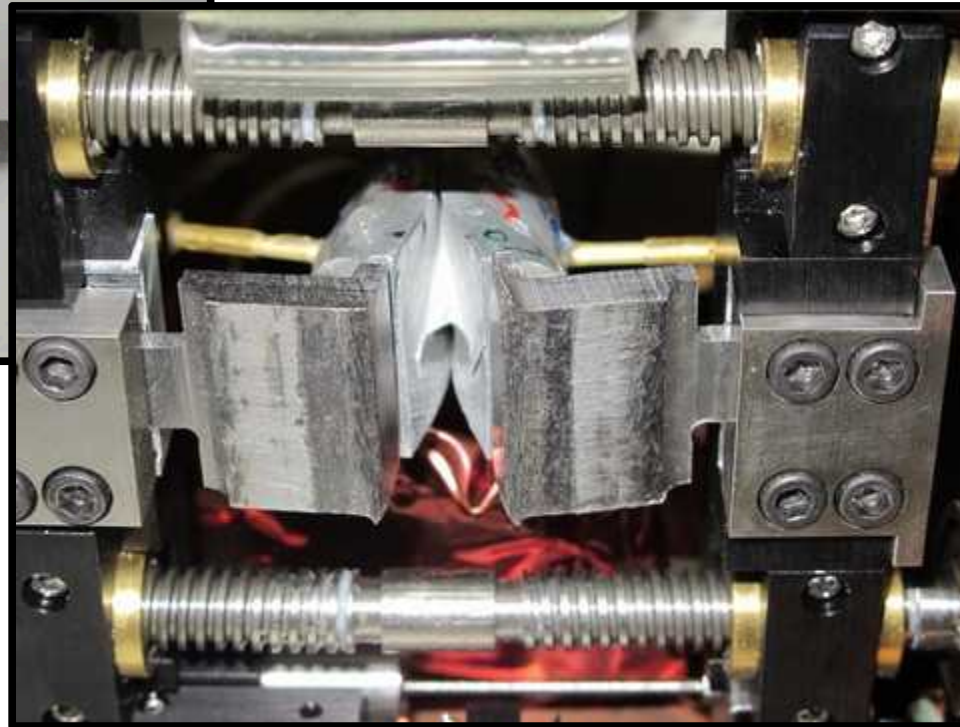
## Short-Rod Fracture Toughness

Senseny and Pfeifle (1987)

# Approaches to Fractures (Testing)



Pre-Test



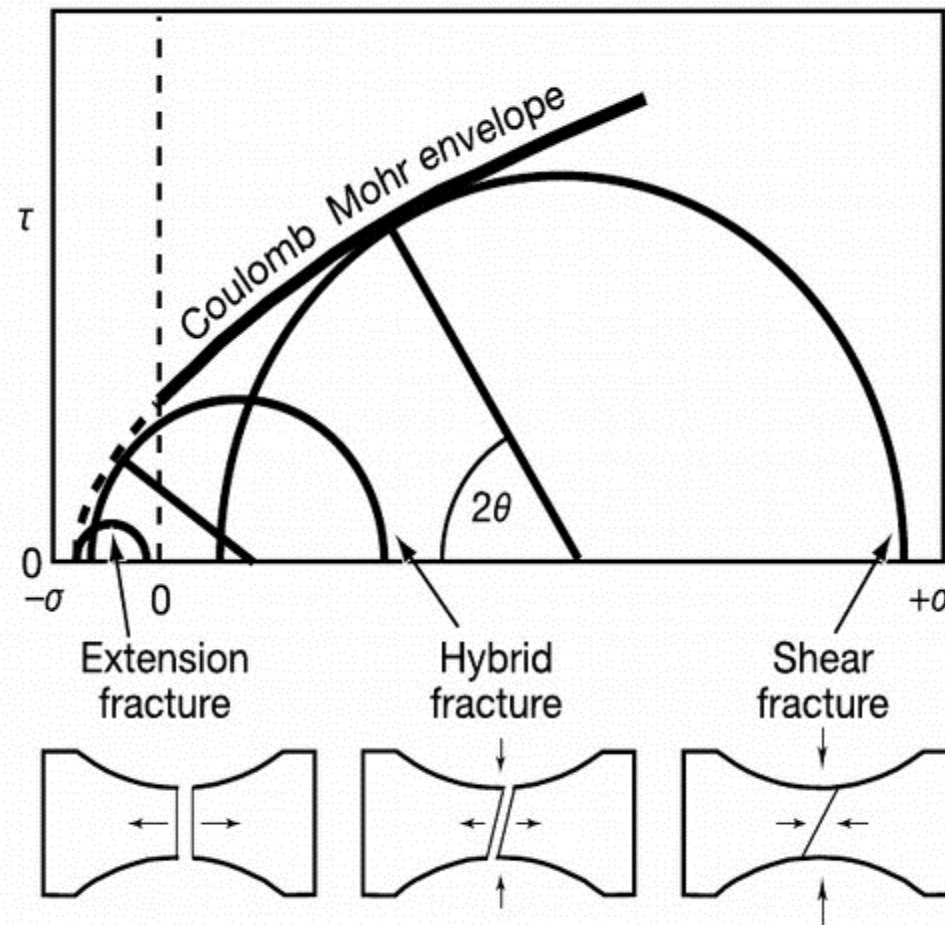
During Test

Post-Test



**Short-Rod  
Fracture Toughness**

# Subsurface Fractures in the Field



**Mixed-mode fractures predominate fracture propagation deep (3,000 m depth).**

**Extension (Mode I) fractures dominate at shallow depths (<1,000 m depth).**

# **The Big Question....**

**How sensitive are cohesive fracture model parameters to changes in geometry?**

**Do changing processes or simply changing stresses cause geometry dependence?**

**Which testing geometry is appropriate for parameterizing models for subsurface applications?**



# Calibration and Confirmation Outline

**Notched 3-point bend (N3PB) geometry, mesh and experiments.**

**Short-rod geometry, mesh and experiments.**

**Short-rod cohesive fracture modeling and calibration.  
Qualitative observations of deformation.**

**N3PB confirmation of cohesive fracture model.  
Qualitative observations of deformation.**

**Summary of pros and cons of cohesive fracture modeling for  
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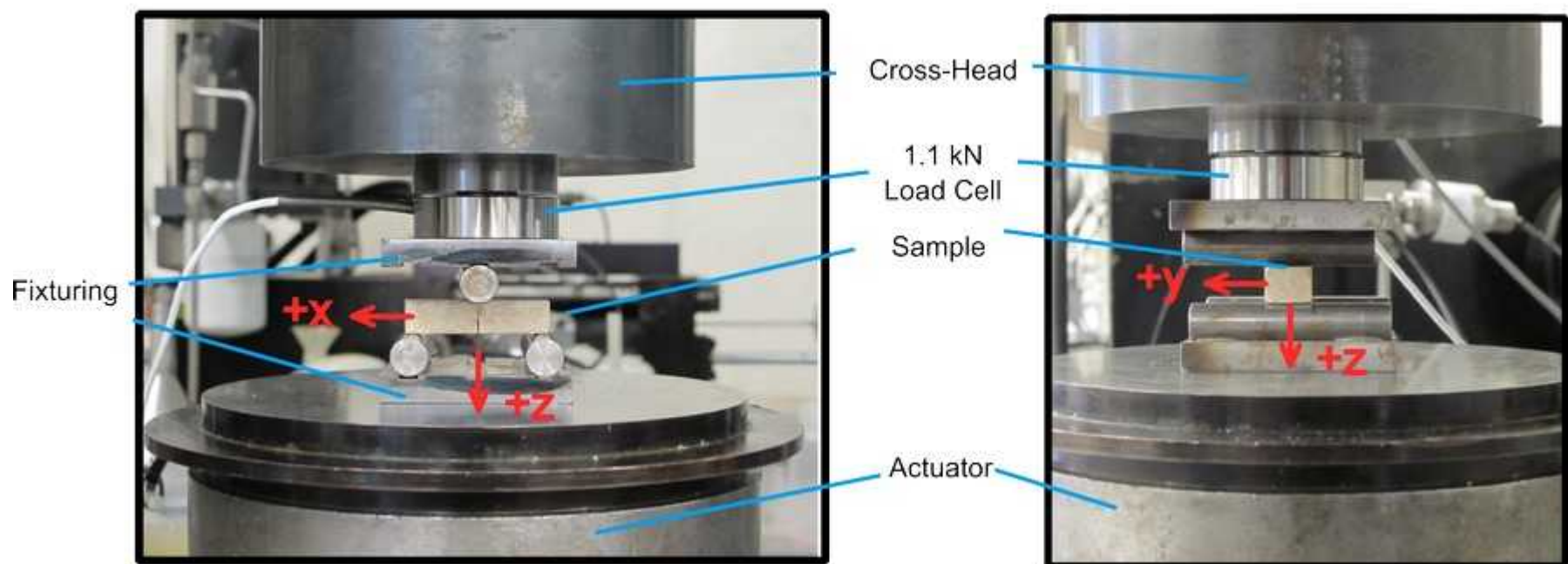
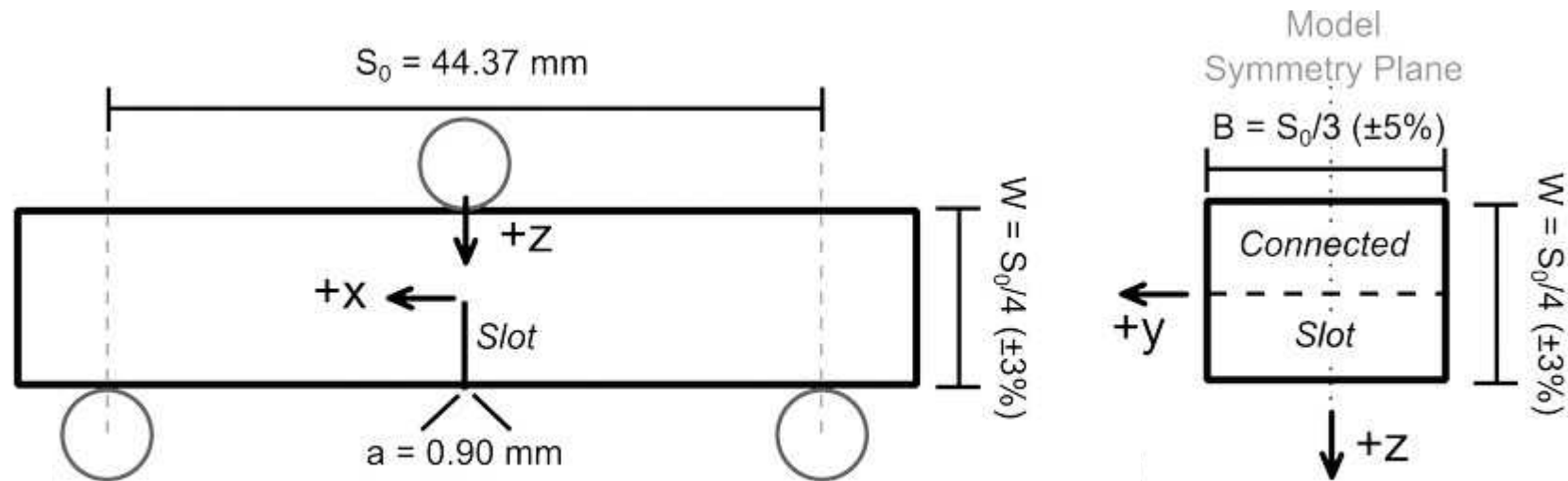
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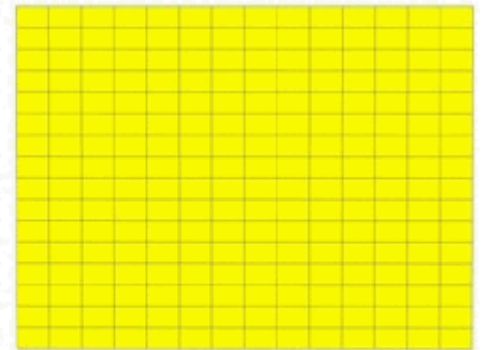
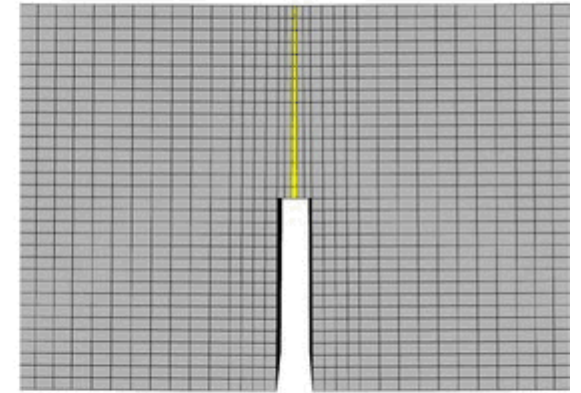
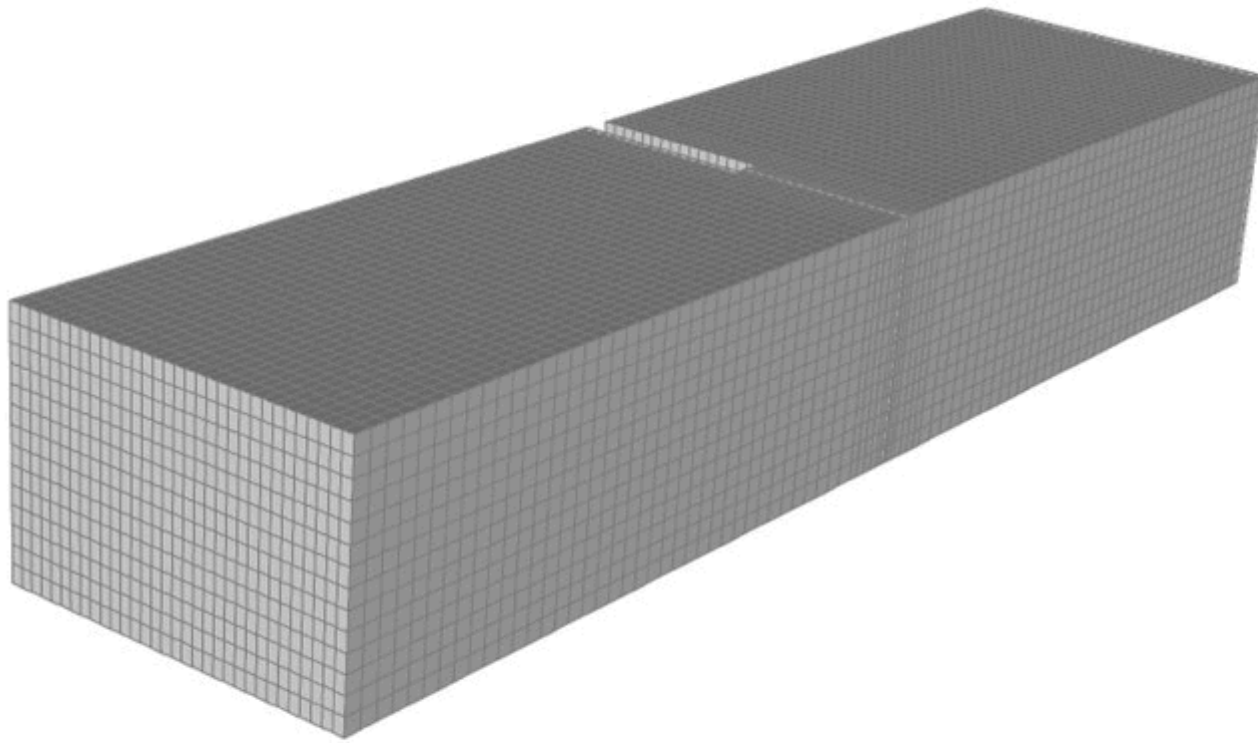
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# 3PB Tests and Geometry



# N3PB Mesh



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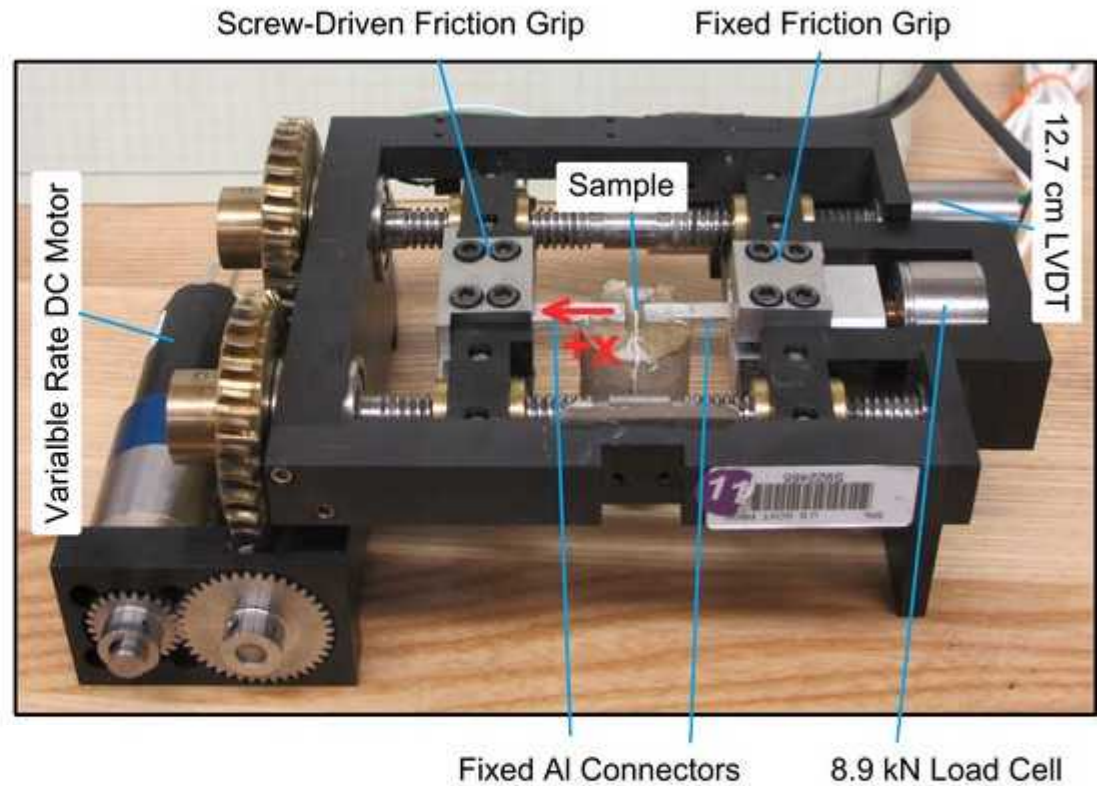
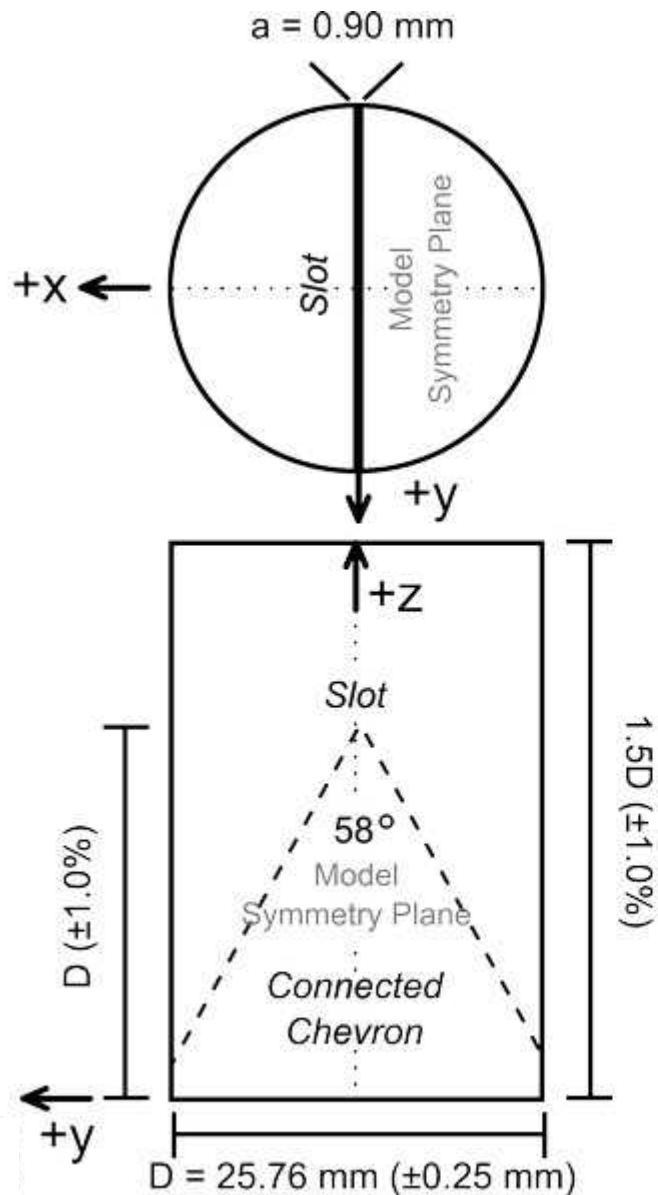
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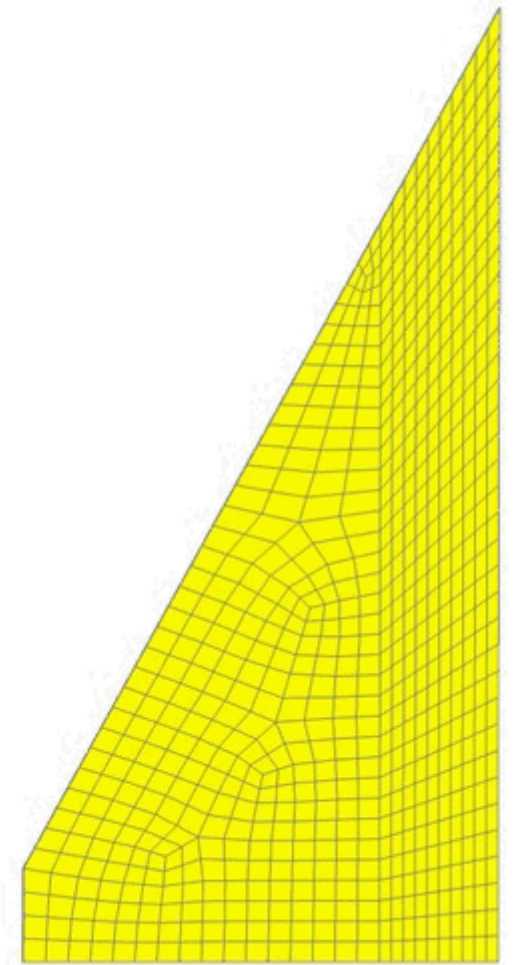
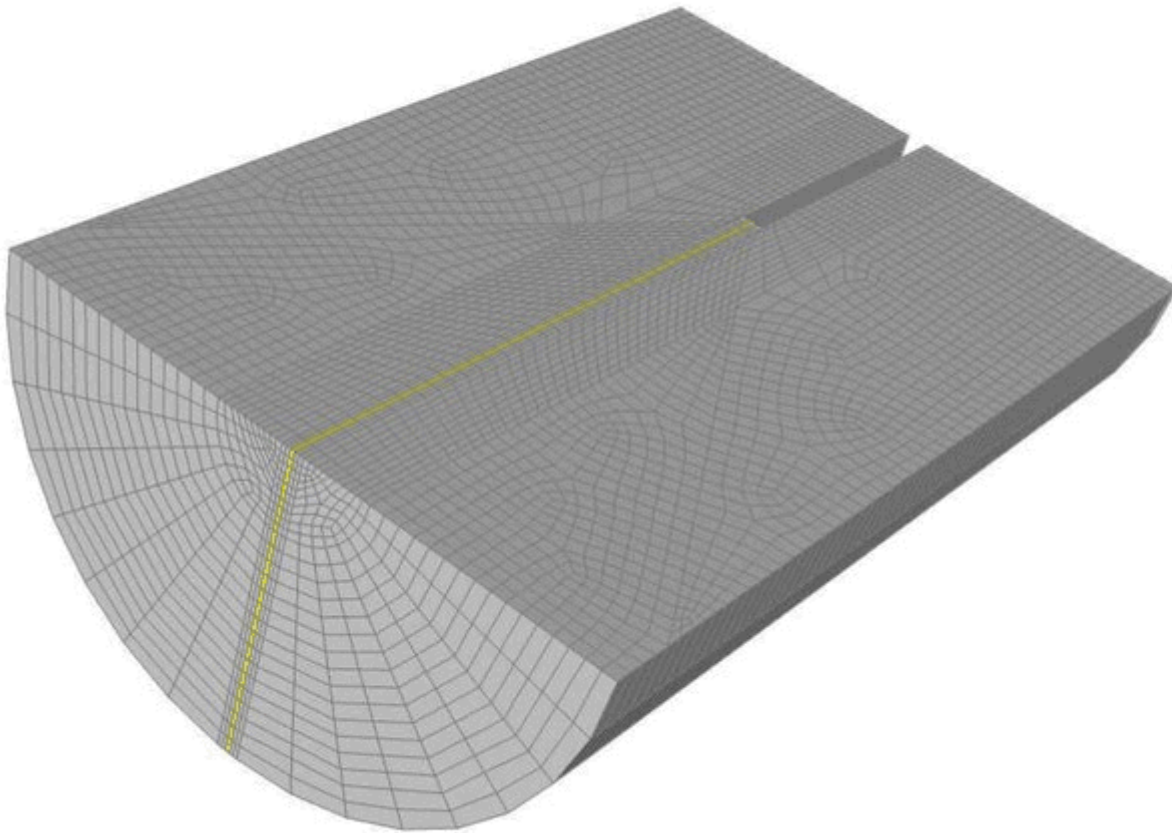
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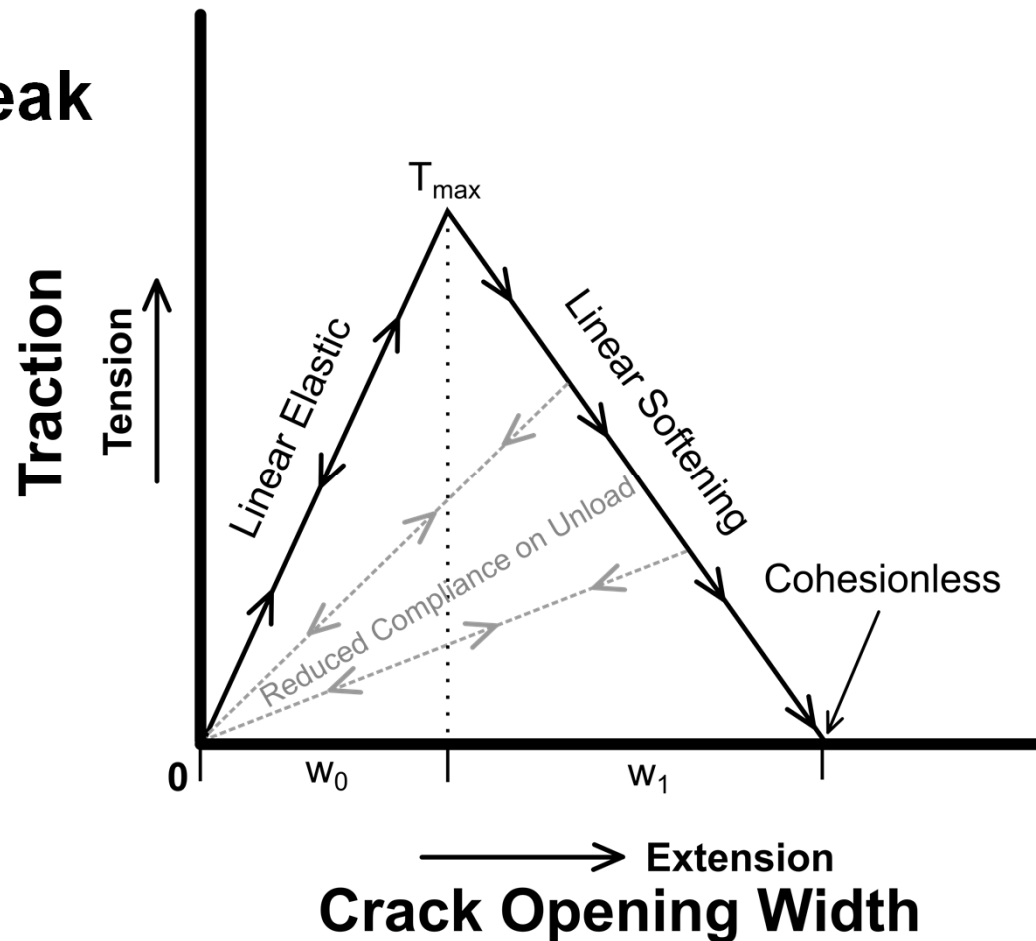


# Calibration Strategy

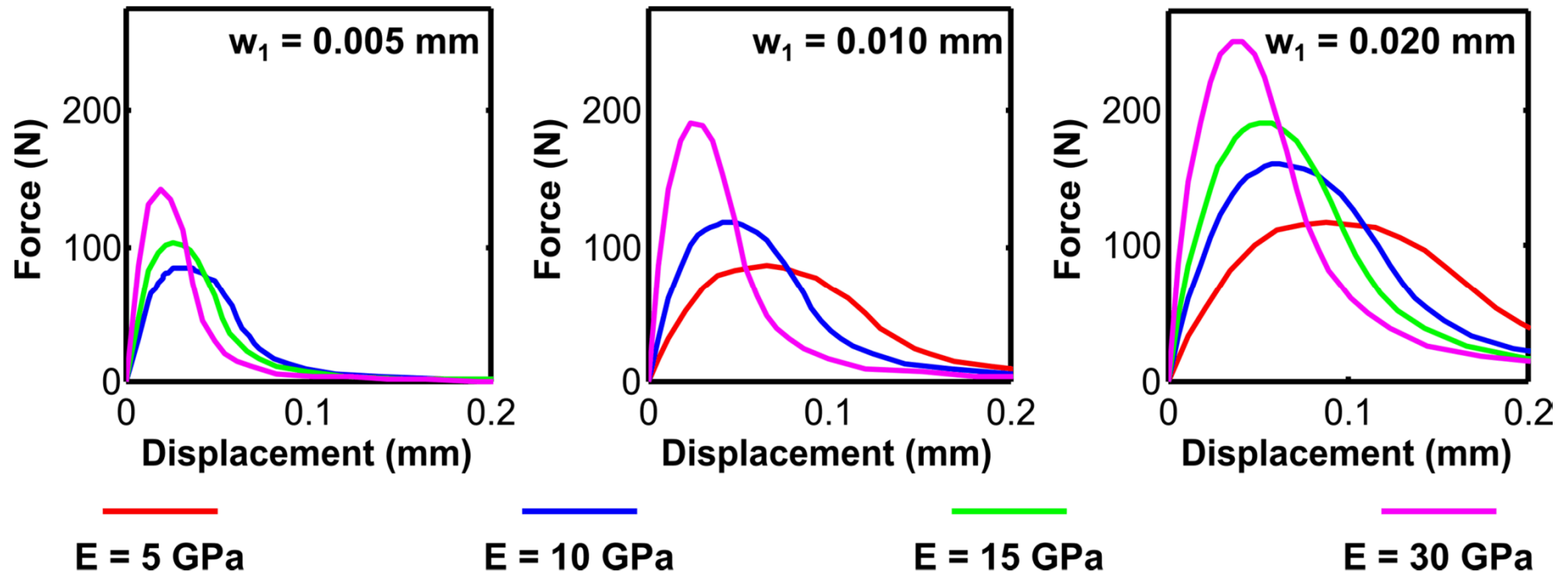
Fix  $\sigma_t = 5.9$  MPa from Brazil tests.

Begin with  $E=39$  GPa from UCS tests, vary to calibrate elastic response.

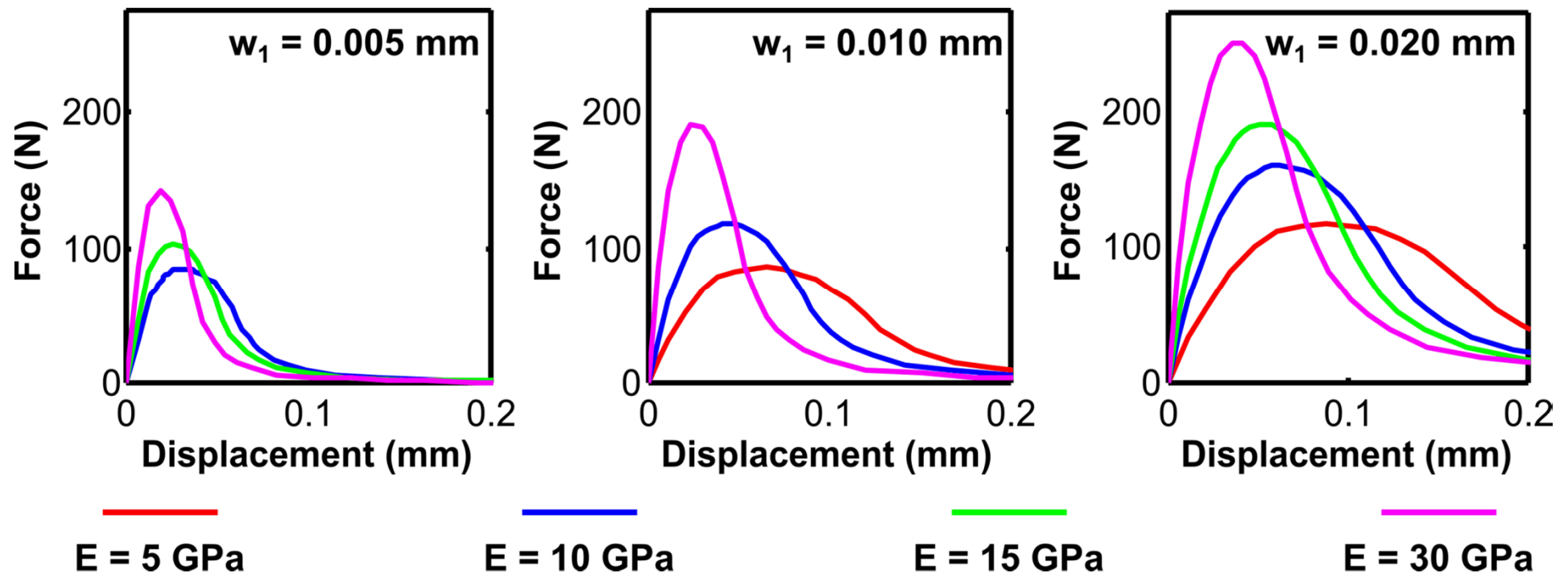
Vary  $w_1$  to match peak and softening.



# Parameters and Sensitivity



# Parameters and Sensitivity

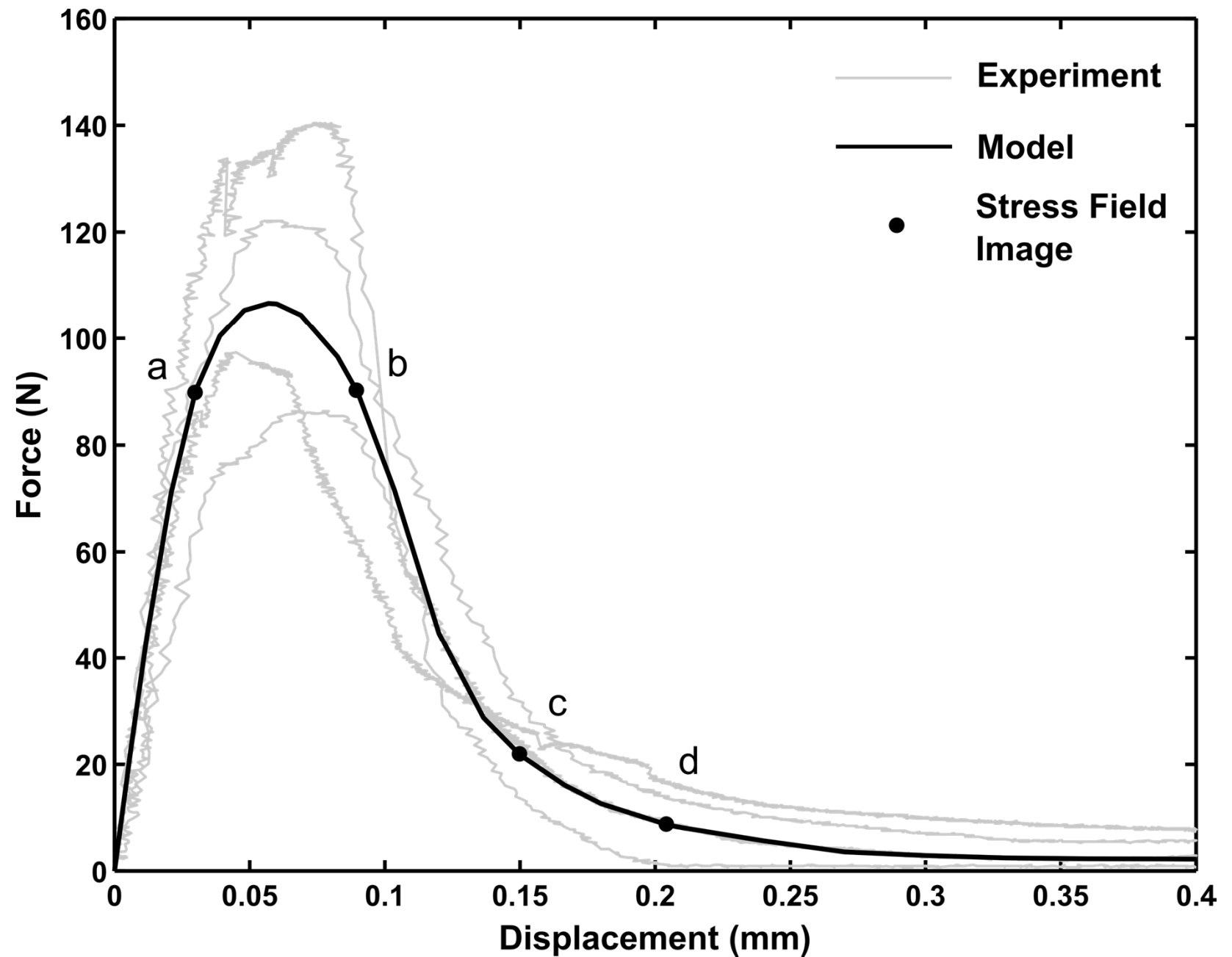


$\sigma_t = 5.9$  MPa fixed.

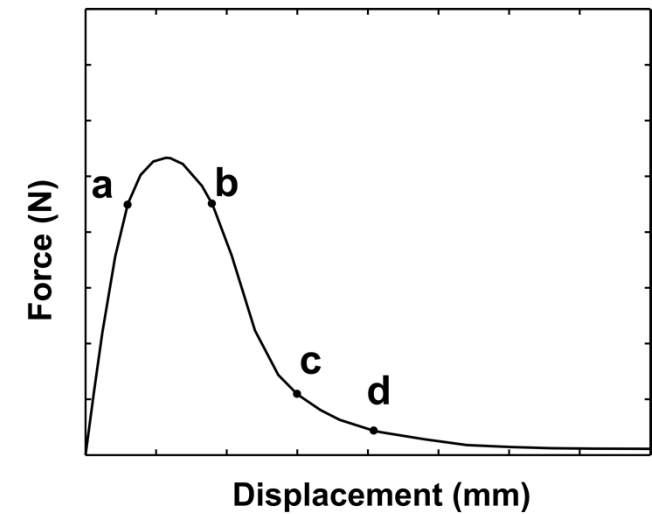
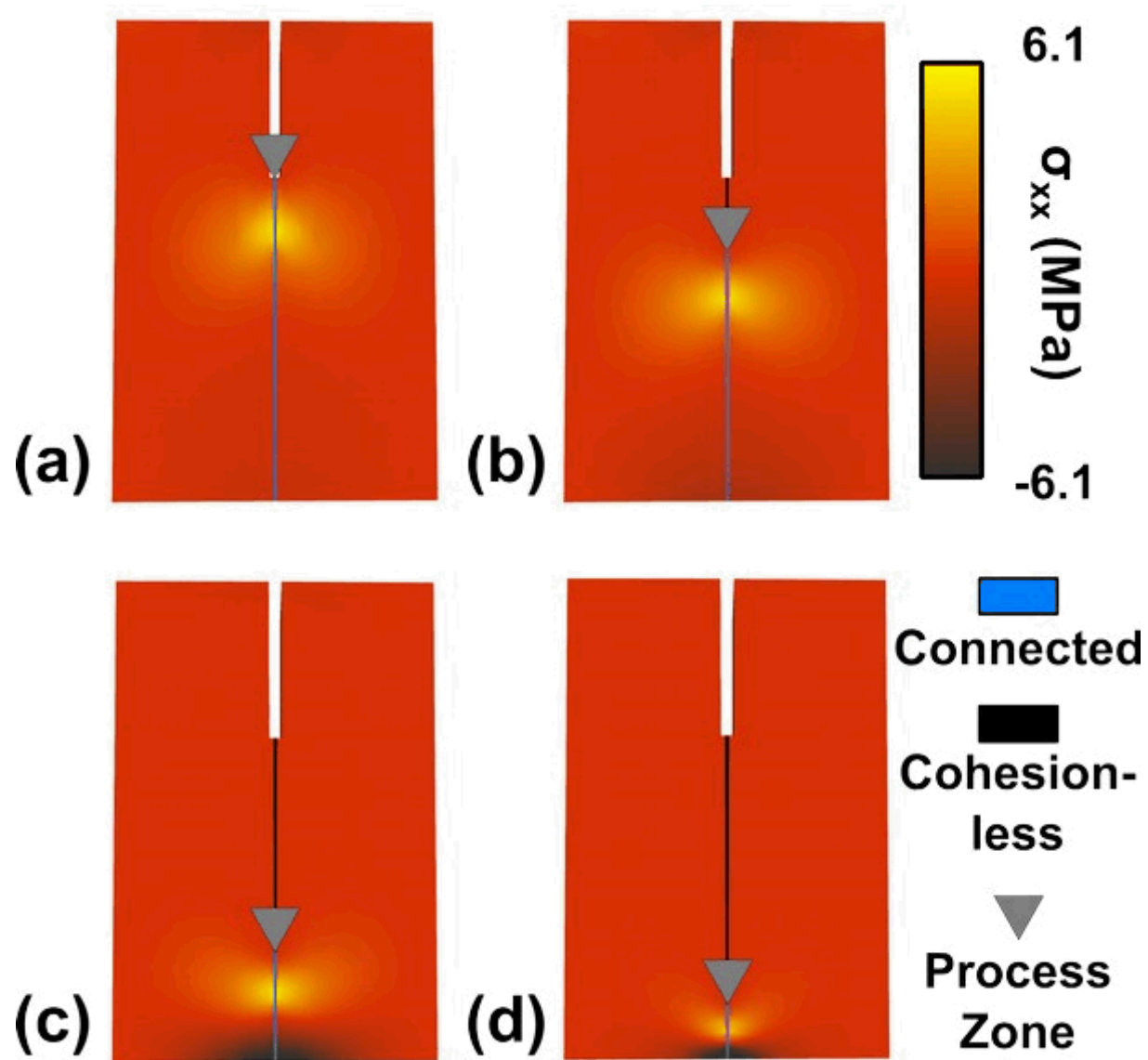
$E = 7.0$  GPa

$W_1 = 0.0115$  mm

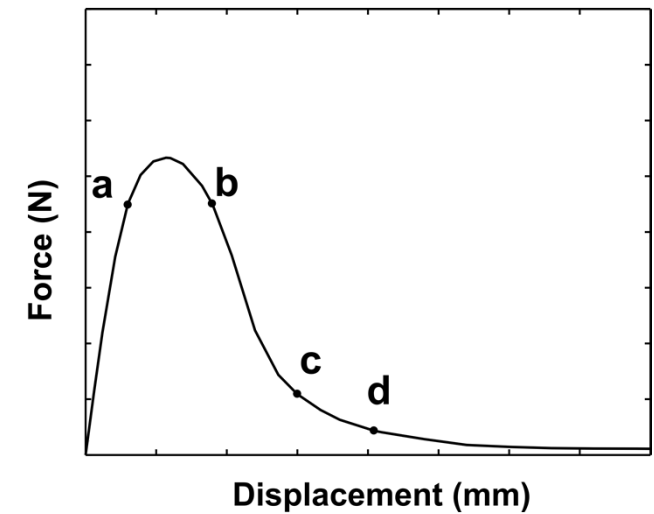
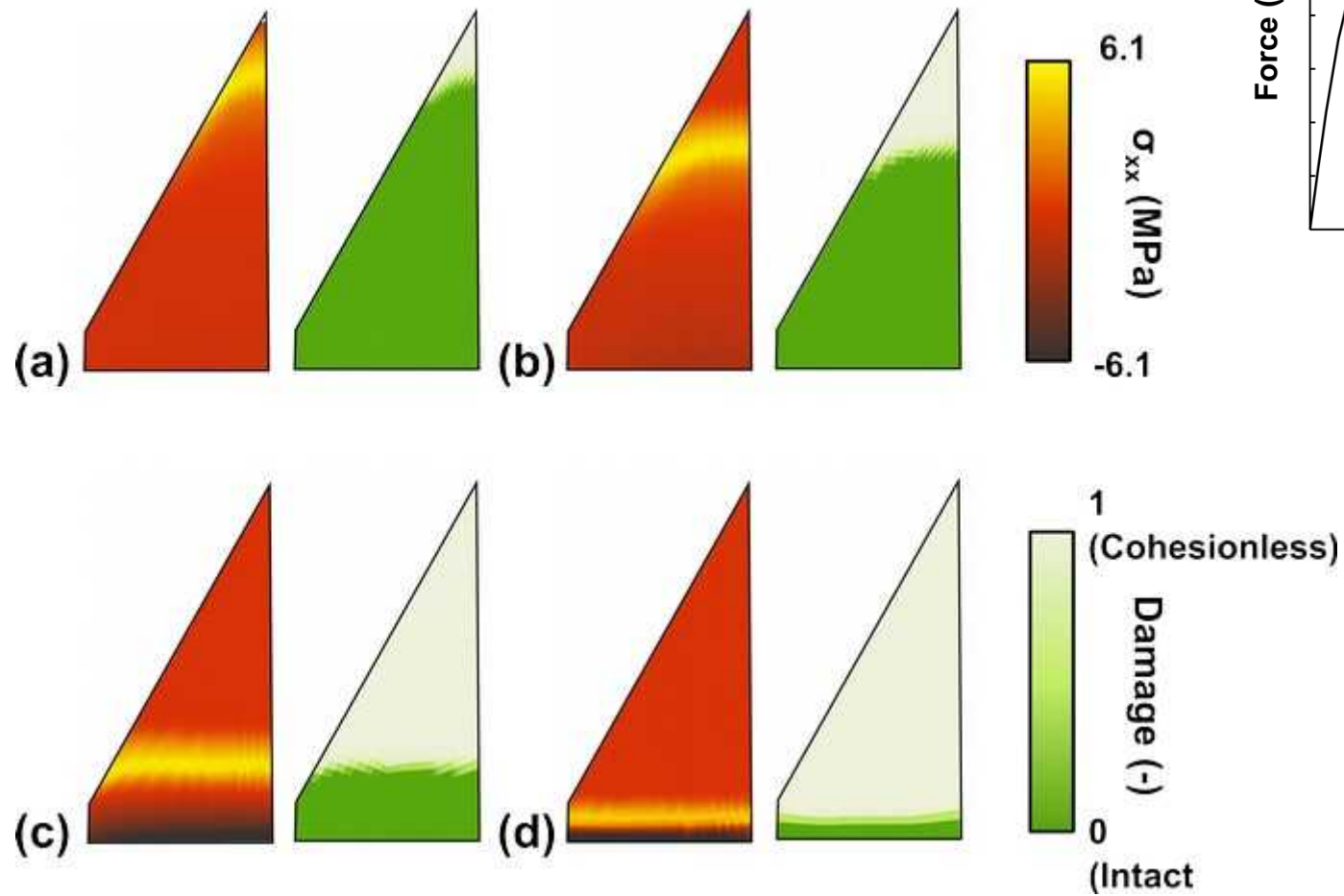
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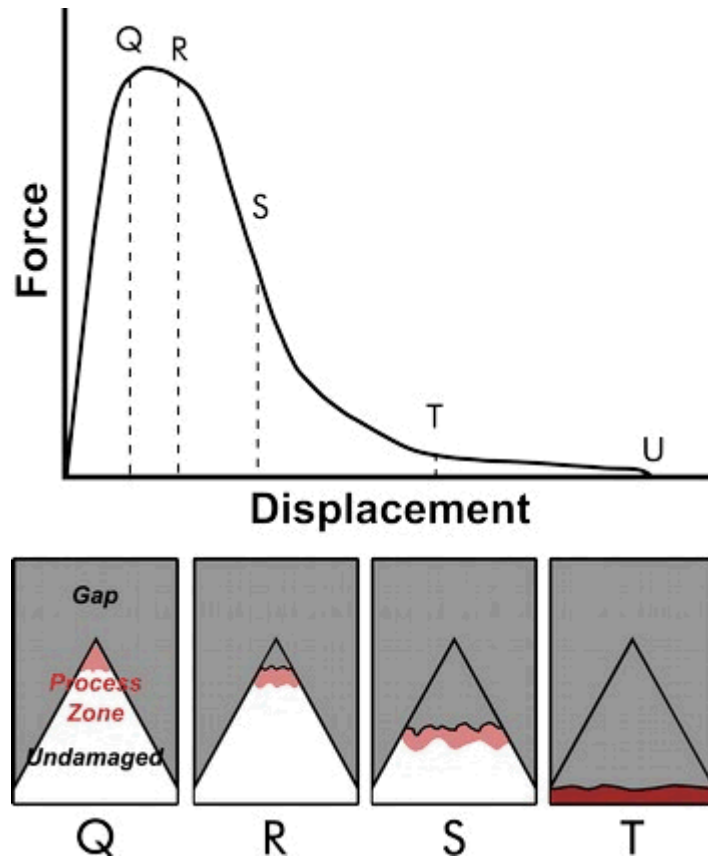


# Calibration Results



# Process Cartoon

## Short-Rod



# Calibration Summary

Cohesive fracture model can be calibrated to match elastic loading, yield, peak and **softening behavior** by

Fixing maximum tensile stress with Brazil tests.  
Varying  $E$  and  $w_1$  in order to calibrate.

Qualitative model fracture propagation similar to observed fracture propagation.

Matching softening behavior uncommon in other test geometries. May imply test geometry 'best at' separating Mode 1 behavior.

Large difference in elastic properties ( $E = 7$  GPa in tension vs.  $E = 39$  GPa in compression).



# Calibration and Confirmation Outline

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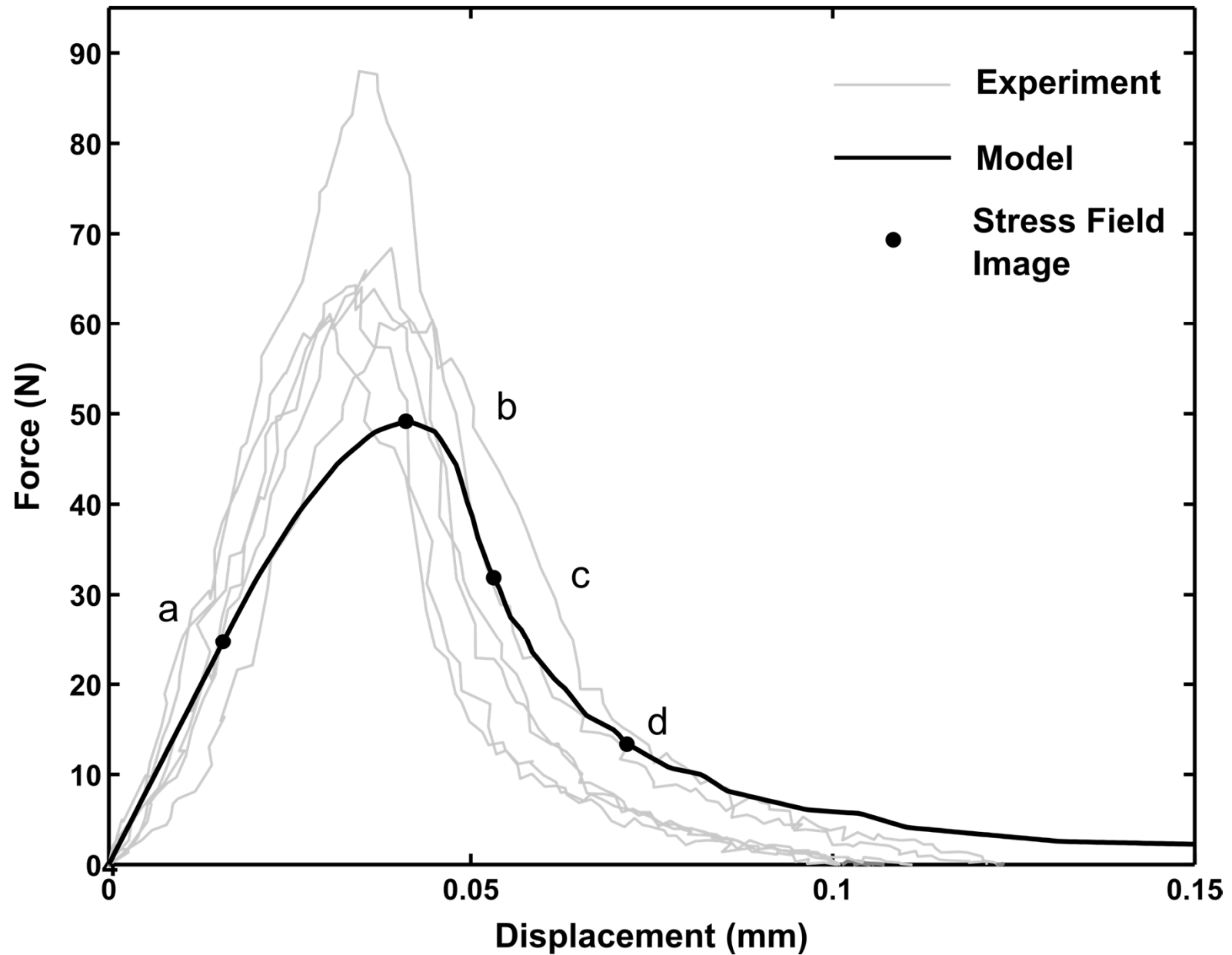
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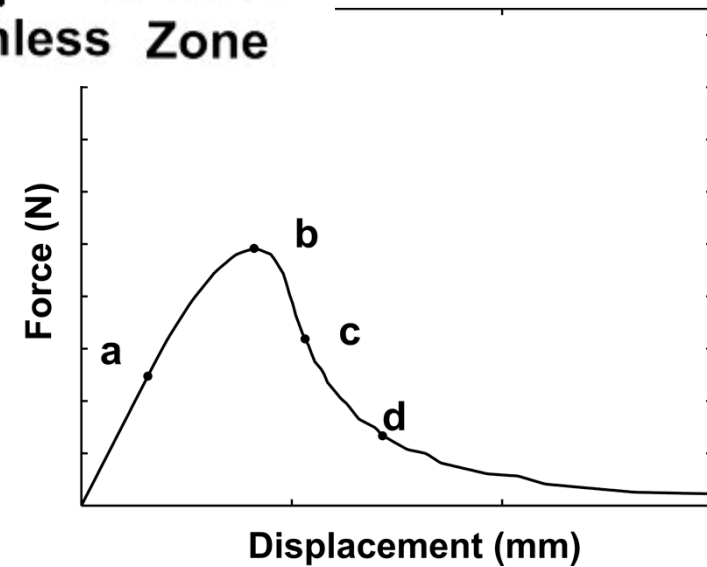
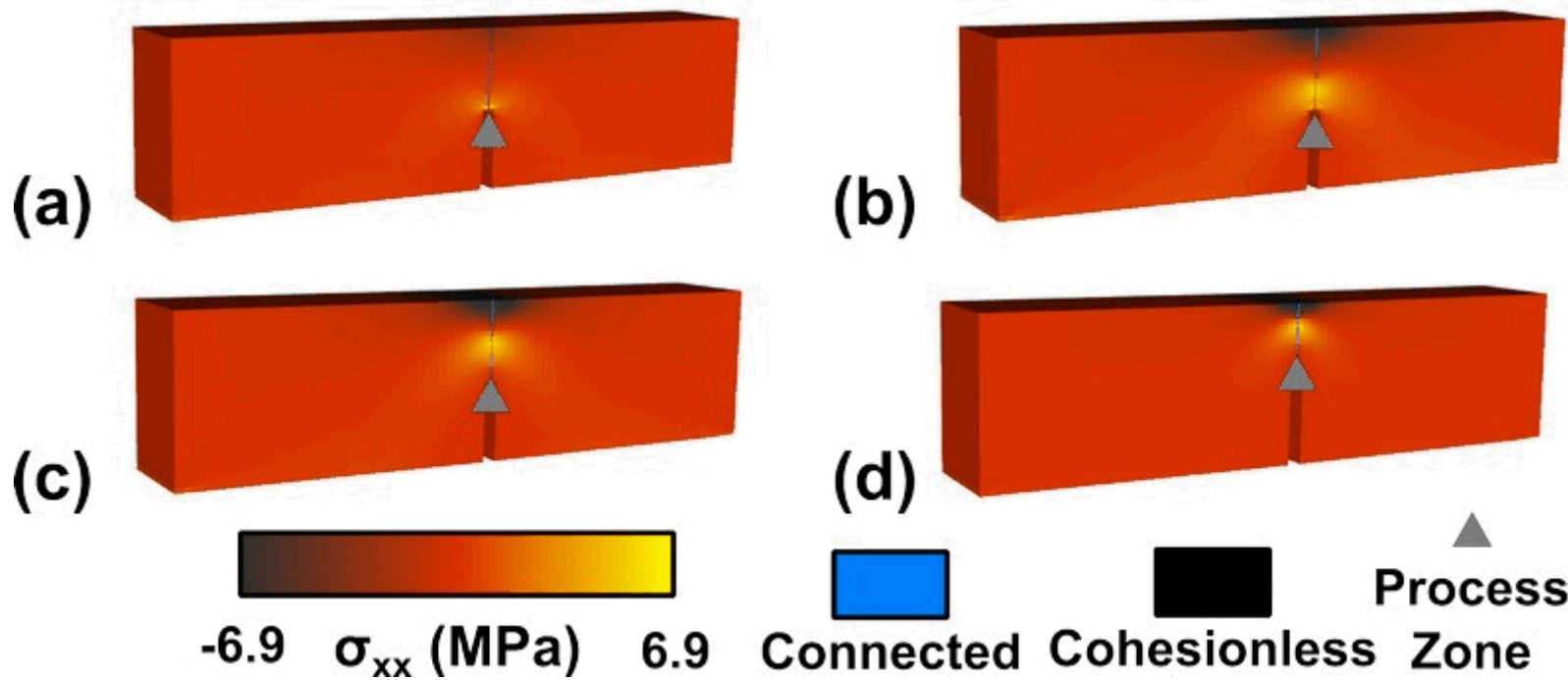
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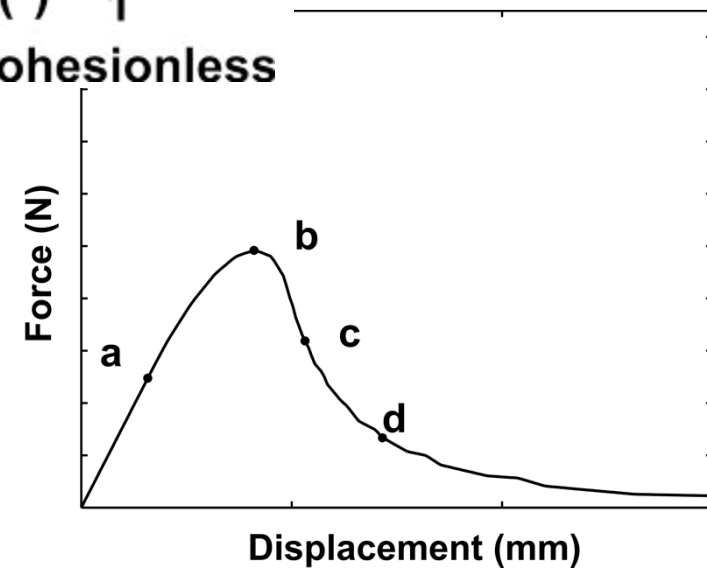
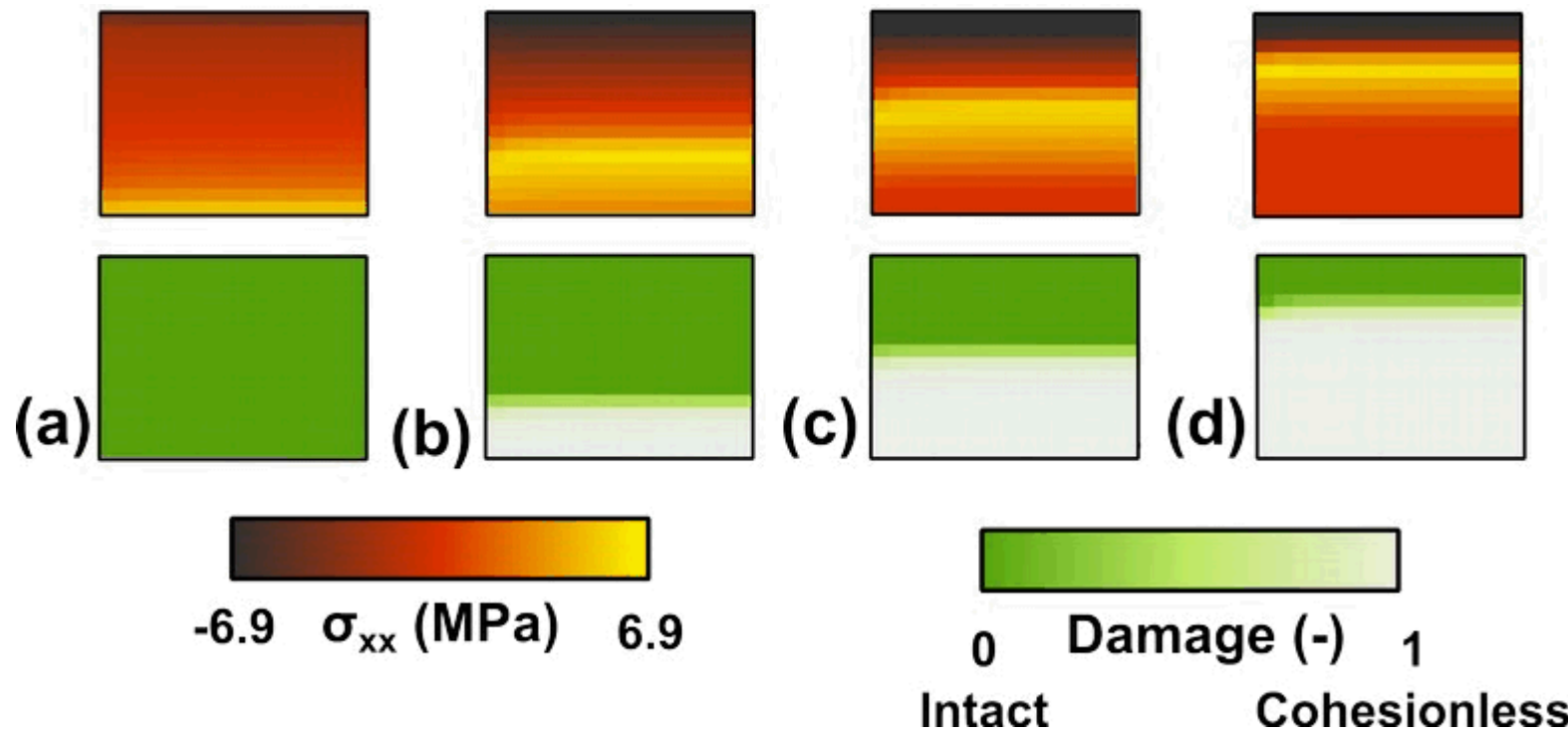
# Confirmation Results



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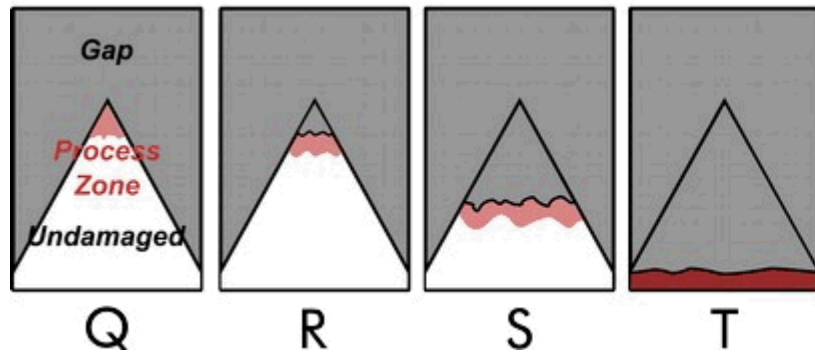
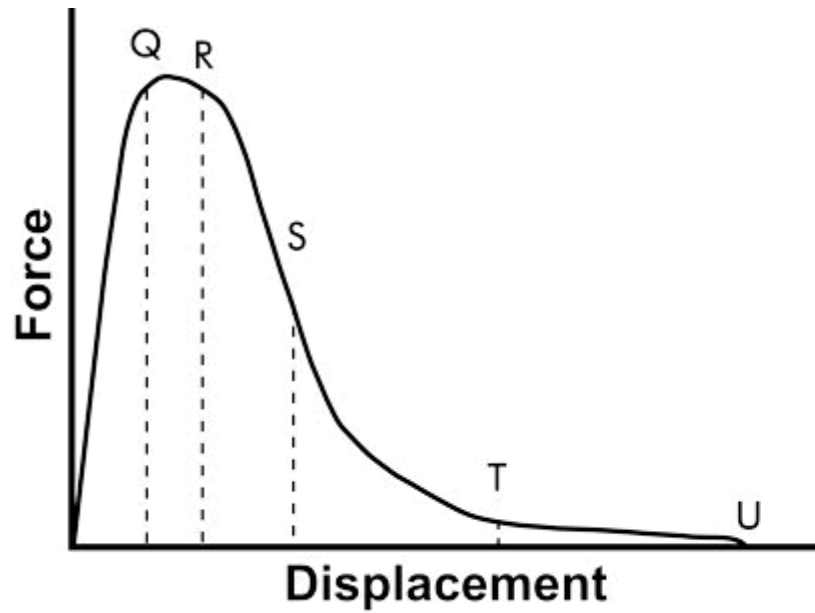


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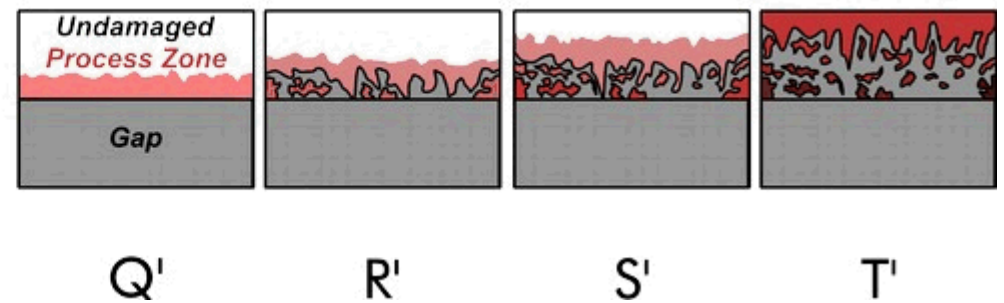
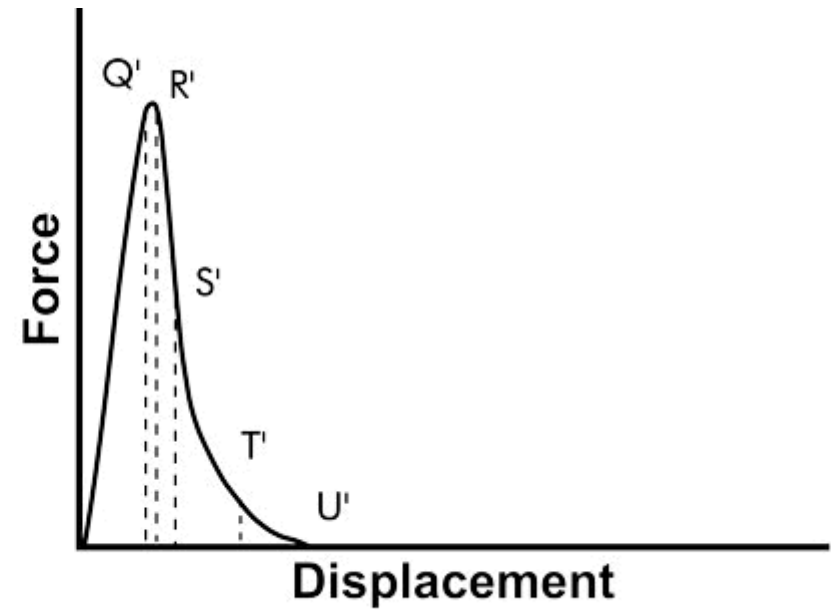


# Process Cartoon

## Short-Rod



## N3PB



# Confirmation Summary

Calibrated cohesive fracture model fell within uncertainty for peak stress and initial softening.

N3PB model initial elastic response 'softer' than measured.

N3PB response showed yielding pre-peak not observed.

N3PB model does not accurately depict large-displacement behavior.

Qualitative diffuse fracture pattern does not match modeled fracture propagation pattern.

**More volume immediately in compression and likely predominant shear failures in fracture both control change in response with geometry.**

# Conclusions

**Cohesive elements can, within  $O(1)$ , be used to predict crack propagation in different geometries.**

Varying stress state in Indiana limestone significantly affects effective elastic properties between short-rod and 3pb simulations.

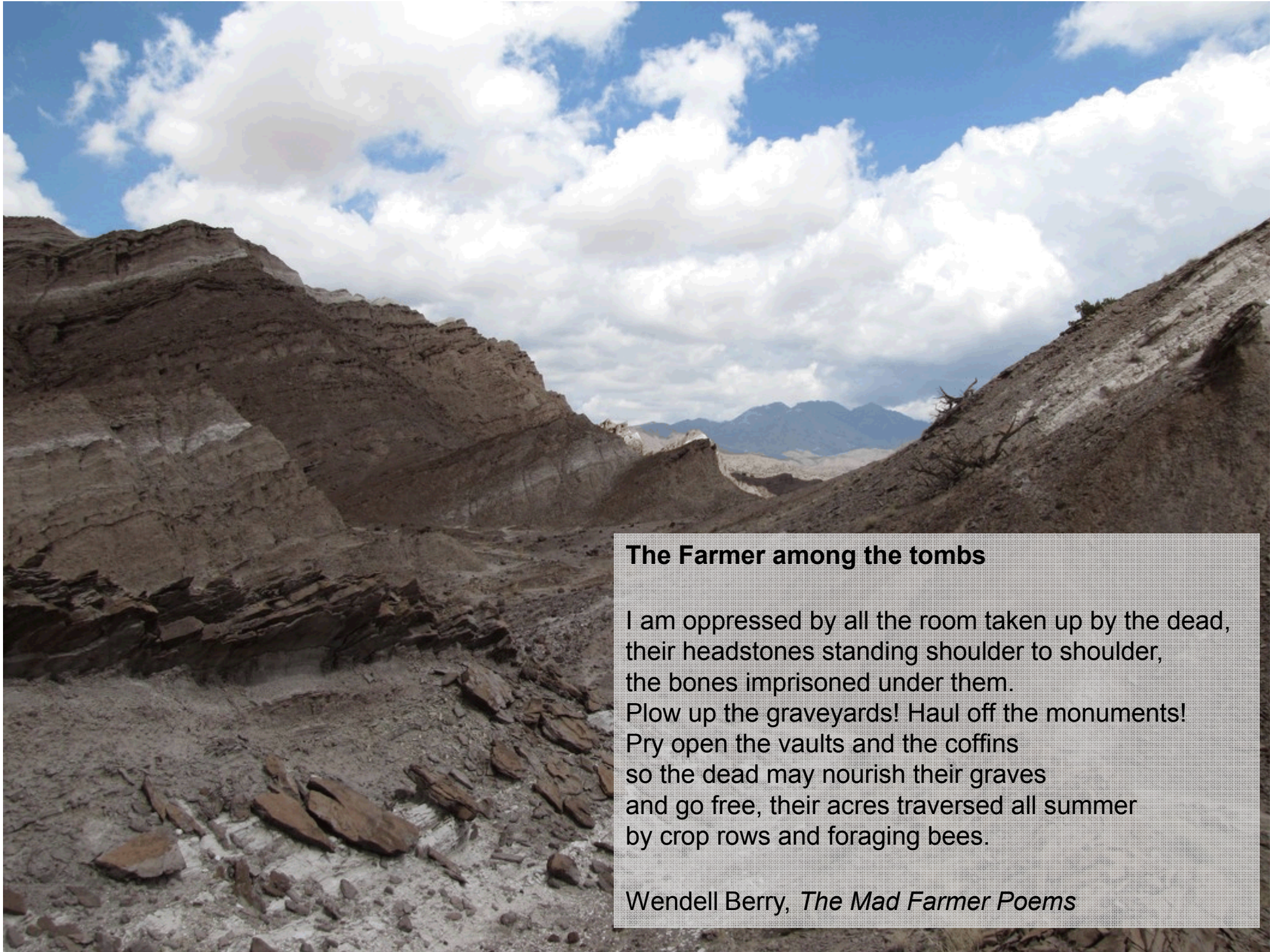
**Short-rod provides a more accurate Mode 1 fracture geometry than N3PB.**

Bulk plasticity or microcracking along edge of fracture needed to portray propagation.

Cohesive crack mimics tail in short-rod, not N3PB.

'Cold-runs' of 3pb fall within uncertainty, but display yielding before any of experiments.





### **The Farmer among the tombs**

I am oppressed by all the room taken up by the dead,  
their headstones standing shoulder to shoulder,  
the bones imprisoned under them.  
Plow up the graveyards! Haul off the monuments!  
Pry open the vaults and the coffins  
so the dead may nourish their graves  
and go free, their acres traversed all summer  
by crop rows and foraging bees.

Wendell Berry, *The Mad Farmer Poems*