

### Team members

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# Entangling atomic spins with a strong Rydberg-dressed interaction

Grant Biedermann



**LDRD**

Laboratory Directed Research and Development

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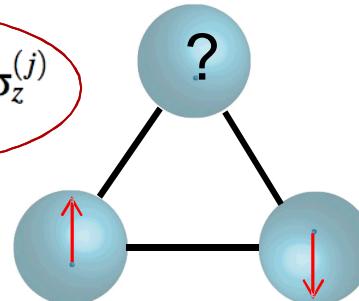
# Outline

- Introduction to Rydberg-dressed atoms and the Sandia Rydberg atom experiment
- Rydberg dressed physics and entangling gates
- Study of a controlled-phase (CPHASE) gate
- Extension to trap arrays

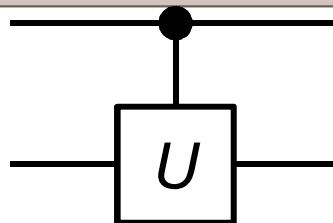
# Motivation

Quantum simulation

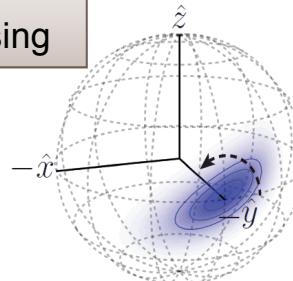
$$H_P = \sum_{i=1}^N \tilde{h}_i \sigma_z^{(i)} + \sum_{i,j=1}^N \tilde{J}_{ij} \sigma_z^{(i)} \otimes \sigma_z^{(j)}$$



Pairwise entangling gates  
between two neutral  
atoms



Large-scale/rapid  
entanglement for sensing



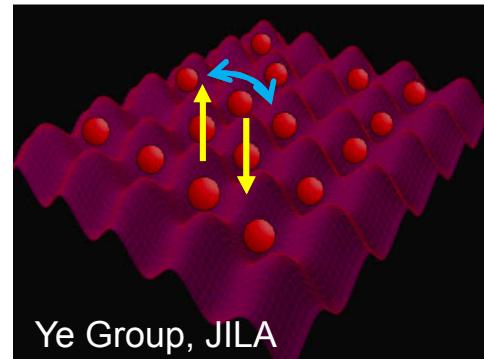
# Interaction between *neutral* atoms

Atom 1                    Atom 2



$$U = \frac{4\pi a \hbar^2}{m} \times \bar{n}$$

$$J_{ex} \propto J^2 / U$$



- Interaction between ground state atoms is small  $\sim 100$  Hz
  - Thermal energy scales too large (e.g., QSIM)
  - Long gate times (e.g., QIP)

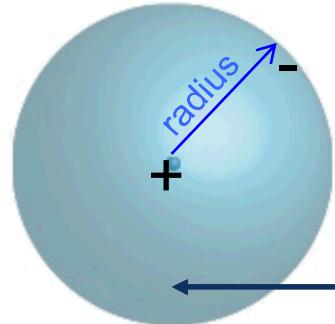
One solution: use Rydberg states

S. Trotzky *et al.*, Science **319**, 295-299 (2008)

I. Bloch, J. Dalibard, and S. Nascimbène, Nat. Phys. **8**, 267-276 (2012)

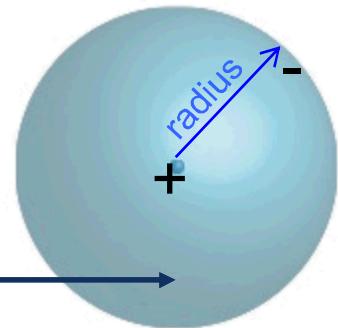
# Interaction between *neutral* atoms

Valence electron  
in Rydberg state



orbital radius  $\propto n^2$

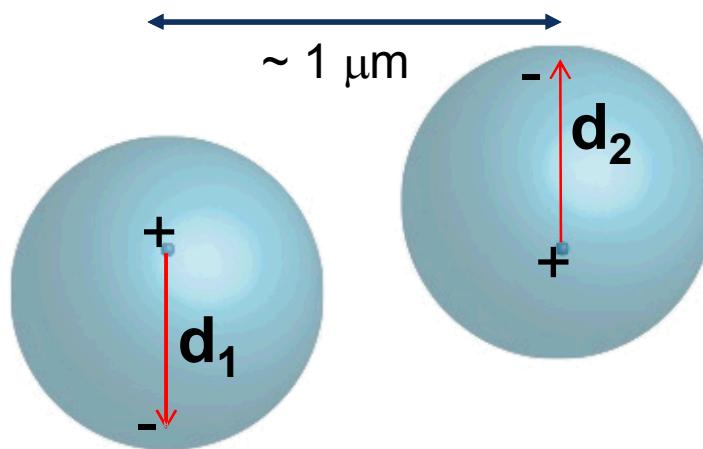
Valence electron  
in Rydberg state



$\sim 10 \mu\text{m}$

- Excite valence electron to Rydberg state—nearly ionized
- Atom becomes highly polarizable—strong interactions

# Interaction between *neutral* atoms



van der Waals interaction

## Parameter scaling

van der Waals

$$U \propto n^{11}$$

Lifetime

$$\tau \propto n^3$$

DC polarizability

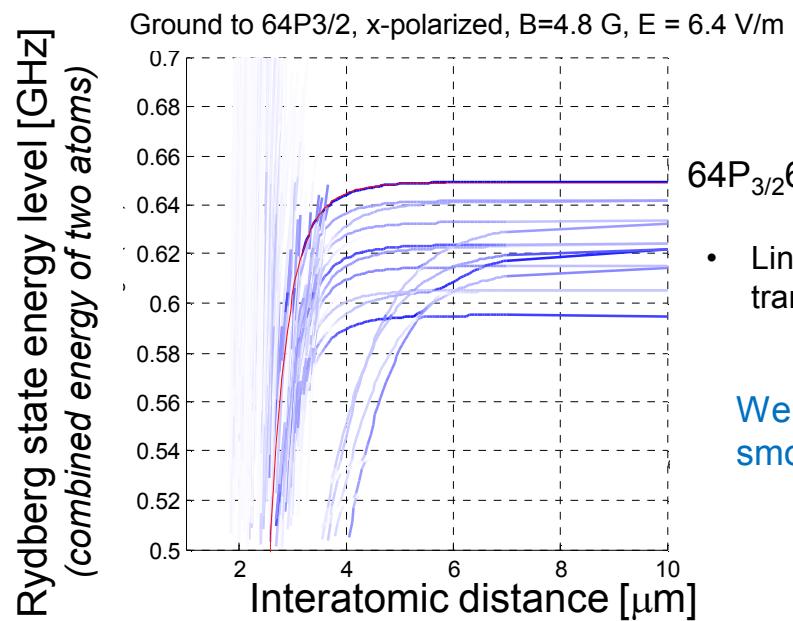
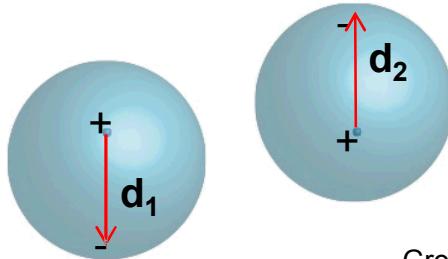
$$\alpha(0) \propto n^7$$

- Even the presence of another atom can cause a massive response  $\gg 10$  MHz
- Induced Electric Dipole-Dipole Interaction  $\propto 1/r^6$

## Entanglement demonstrations

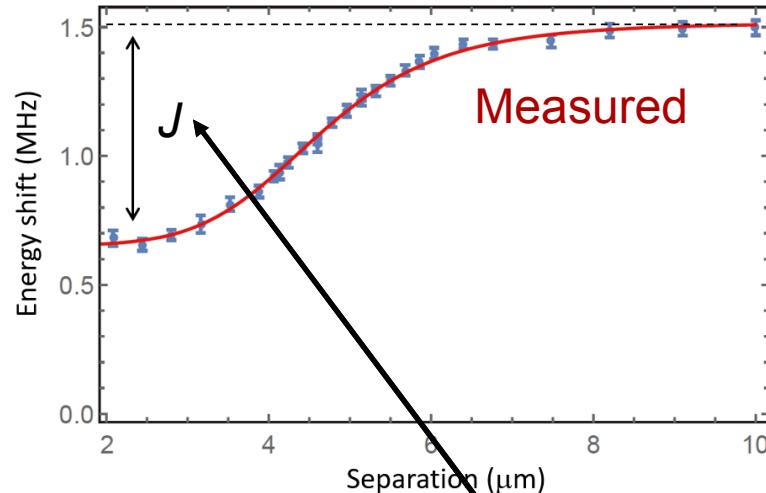
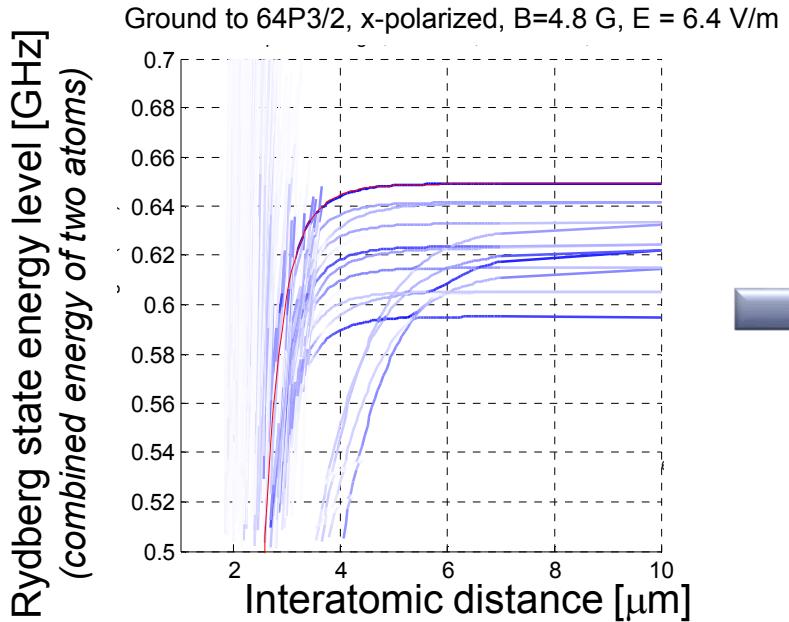
- Madison: Phys. Rev. Lett. 104, 010503 (2010)
- Paris: Phys. Rev. Lett. 104, 010502 (2010)

# Rydberg blockade—the nitty gritty



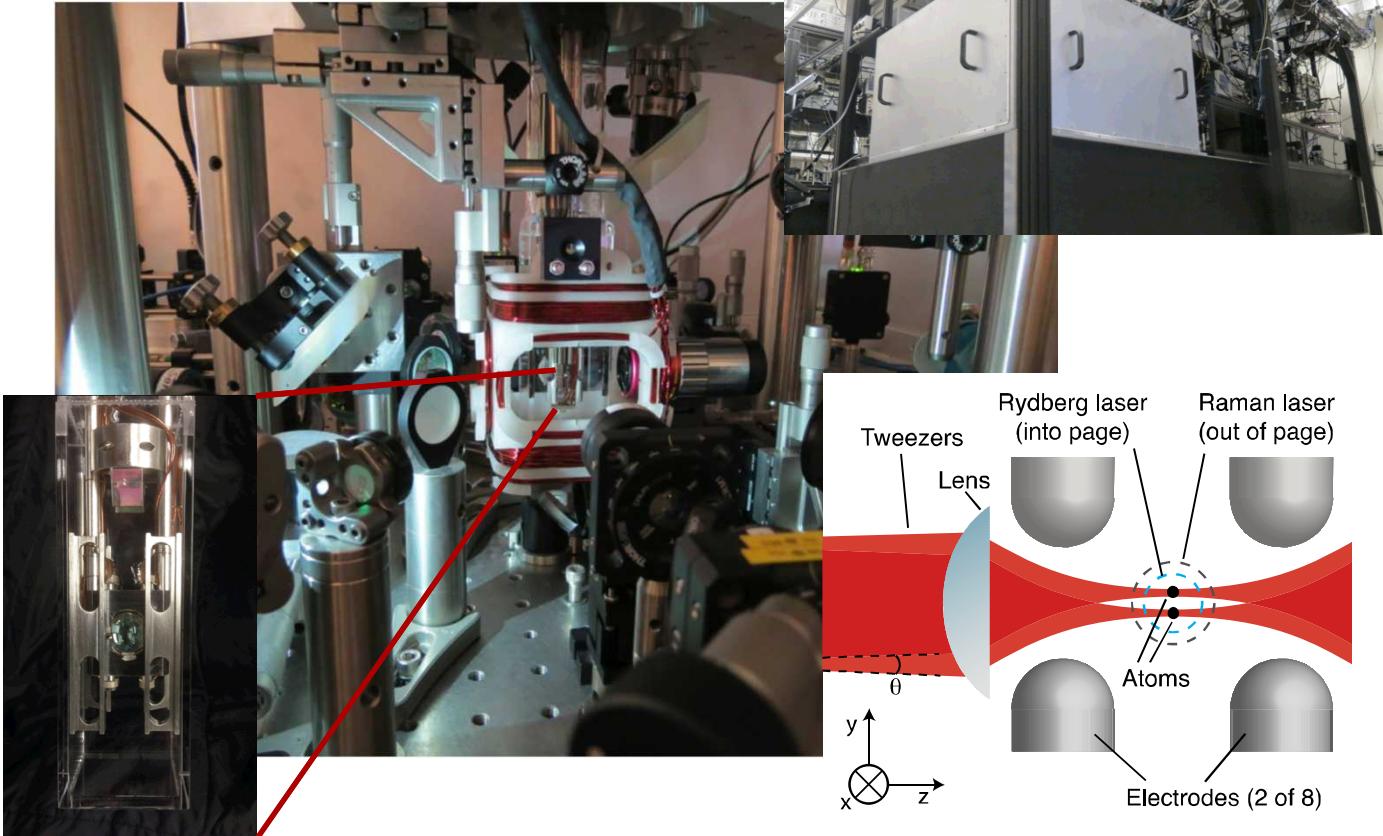
We want something smooth and tunable

# Direct Rydberg $\rightarrow$ Rydberg-Dressed

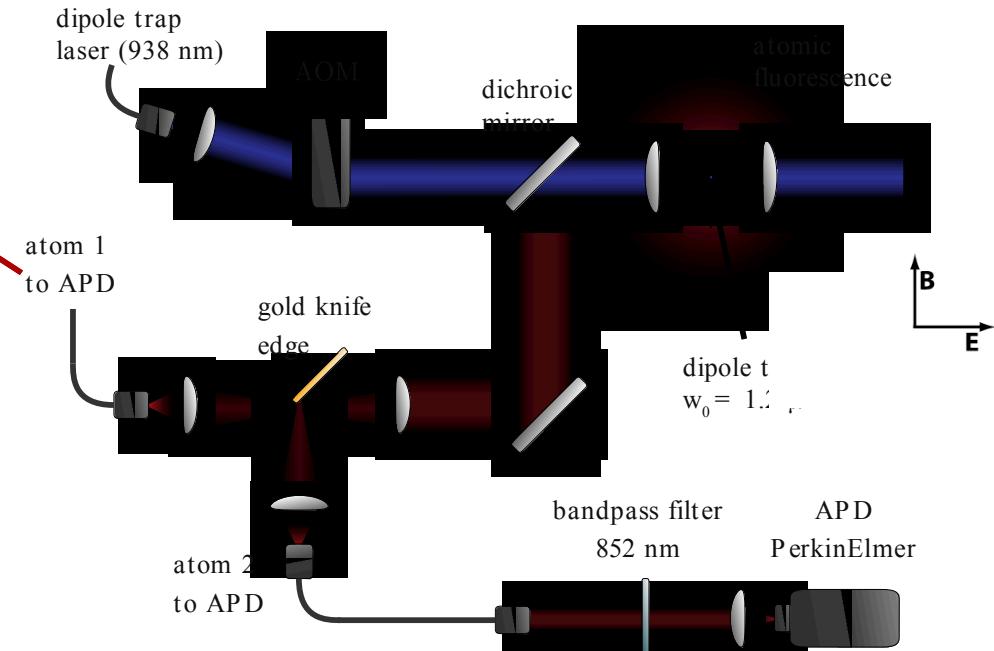
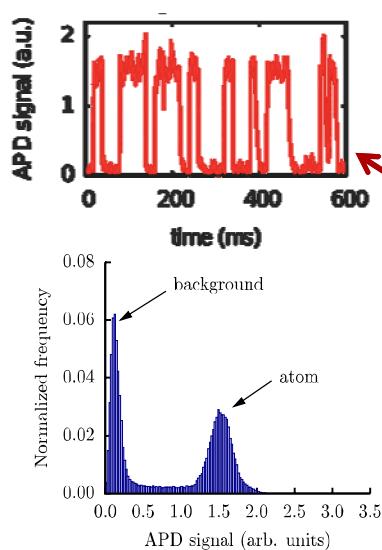


$$H_P = \sum_{i=1}^N \tilde{h}_i \sigma_z^{(i)} + \sum_{i,j=1}^N \tilde{J}_{ij} \sigma_z^{(i)} \otimes \sigma_z^{(j)}$$

# Rydberg experiment

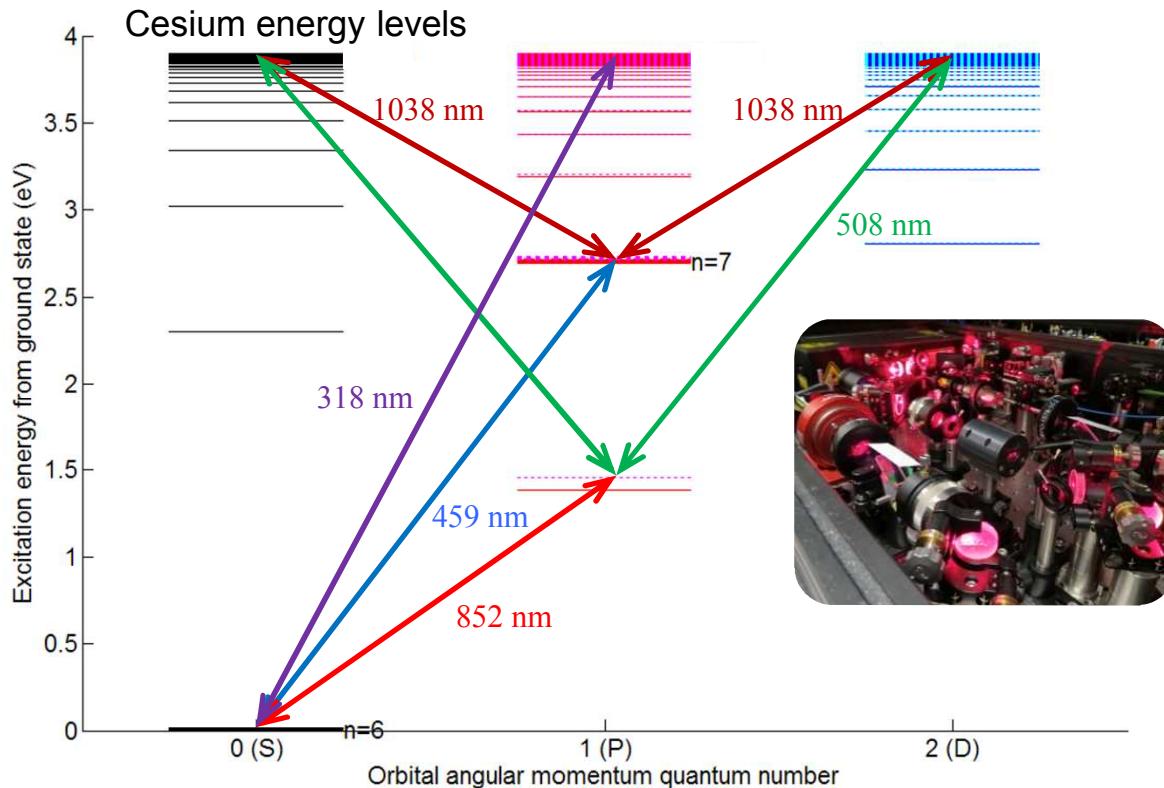


# Single atom control of 2 atoms

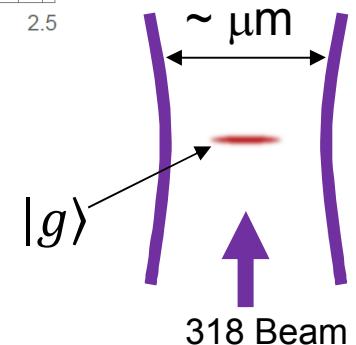
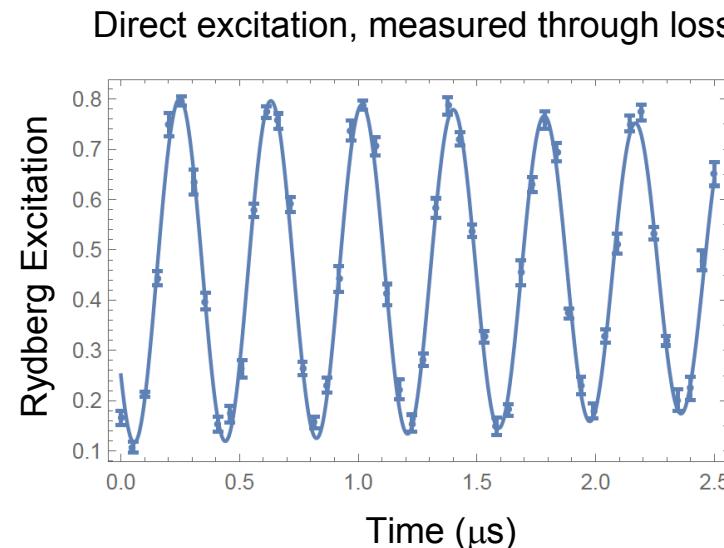
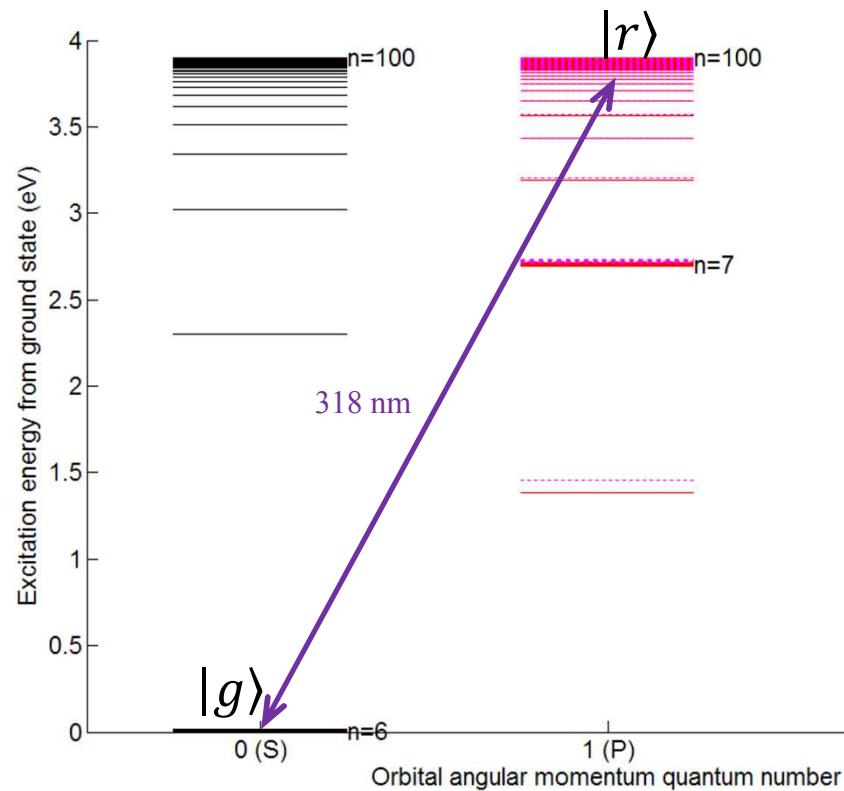


- Optical tweezers
- Trap single Cs atoms
- Laser cooling to load traps
- AOM deflection controls trap position
- Photon counters for detection

# Rydberg excitation laser



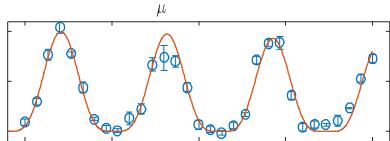
# Direct excitation 318 nm Rydberg Rabi flopping



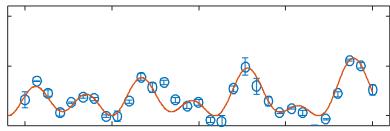
# Rydberg blockade

Weak ( $U_{RR} < 100$  kHz)

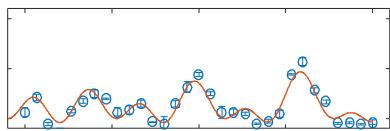
$P_{rr}$



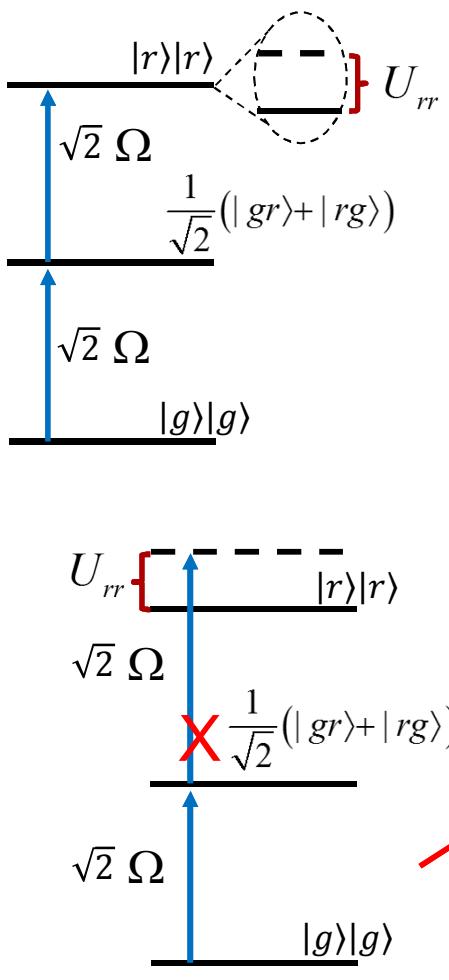
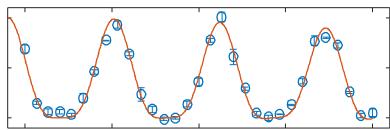
$P_{r1}$



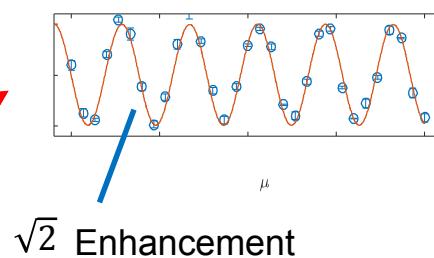
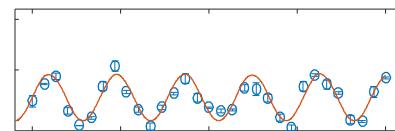
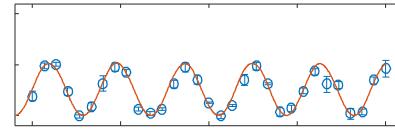
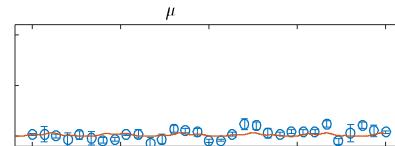
$P_{1r}$



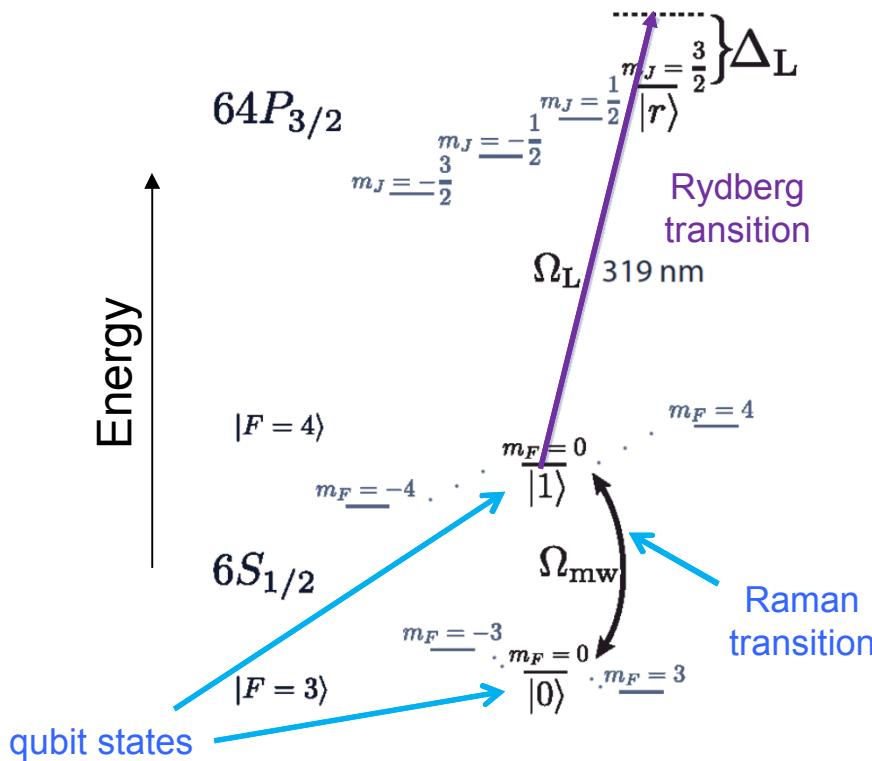
$P_{11}$



Strong ( $U_{RR} > 6$  MHz)

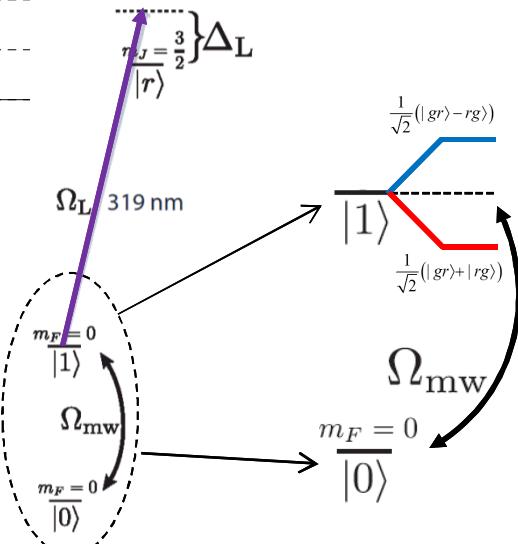
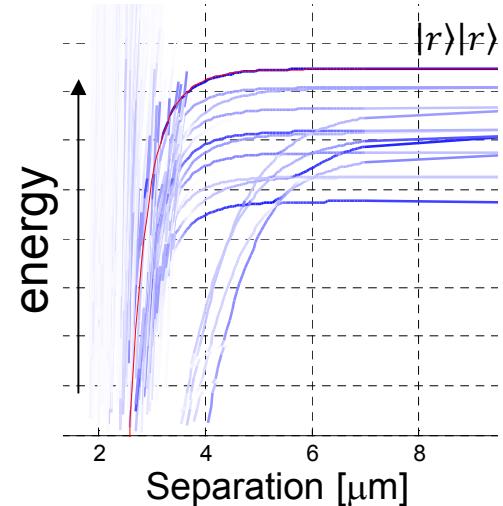


# Creating Rydberg-Dressed states

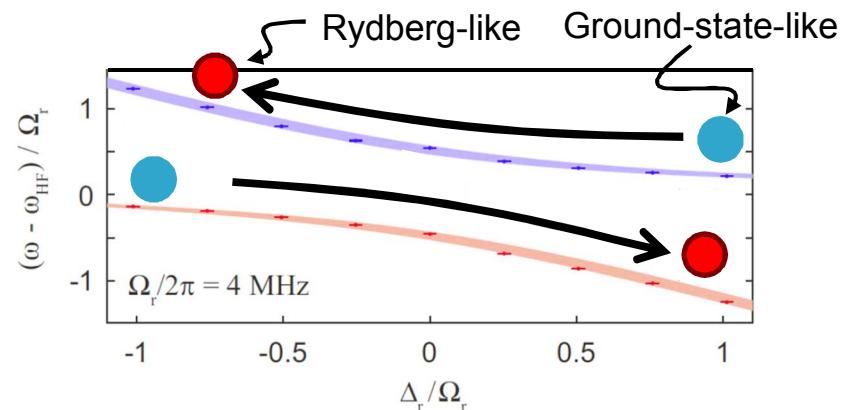
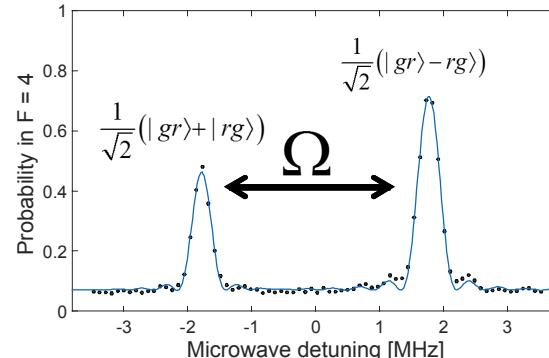


- 1-S scale coherence time. Neutral atoms define the SI second!
- Form the basis of sensors and clocks that use measurements of  $\sim 10^6$  atoms.

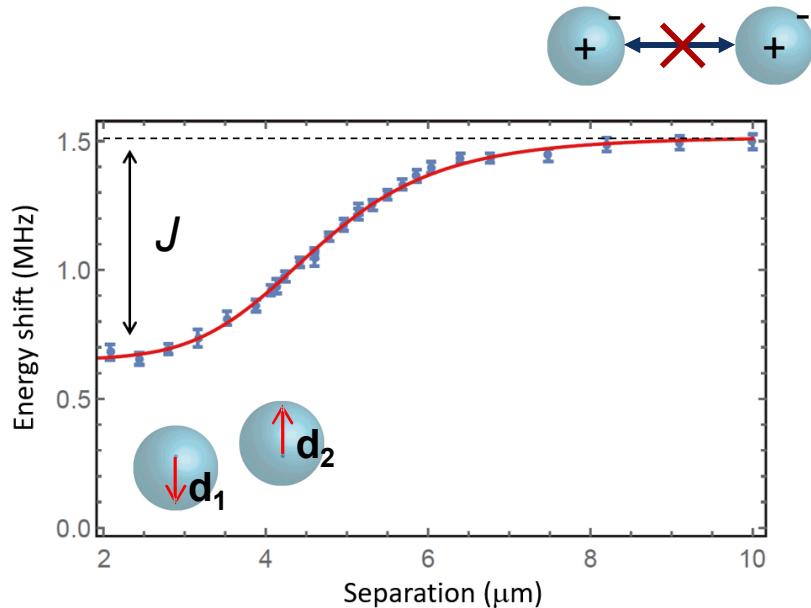
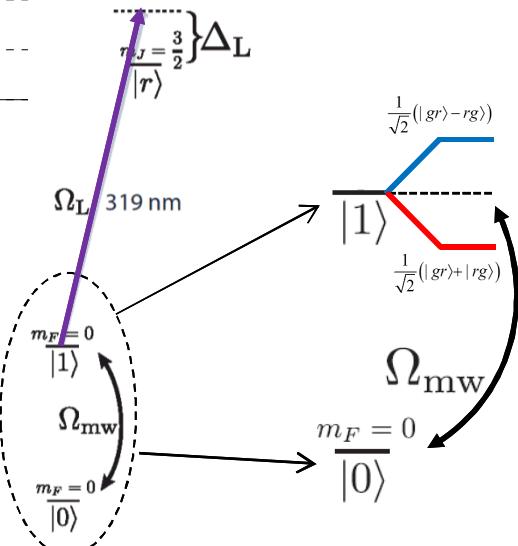
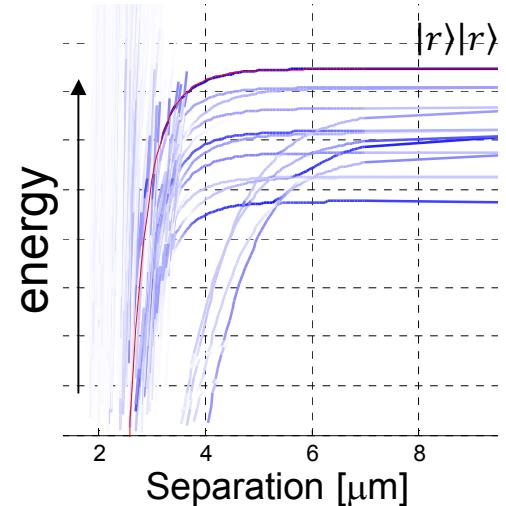
# 1-atom Rydberg-dressed states



Dressed F=4 state Autler-Townes splitting



# Rydberg-Dressed interaction



# Rydberg-dressed interactions

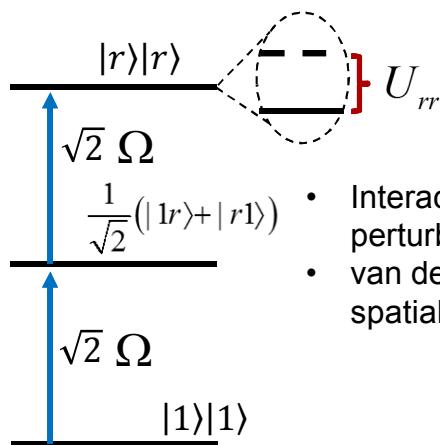
$U_{rr} \ll \Omega_r$  (atoms far apart)



$U_{rr} \gg \Omega_r$  (atoms close)

$$|\psi\rangle = \alpha |1\rangle + \beta |r\rangle$$

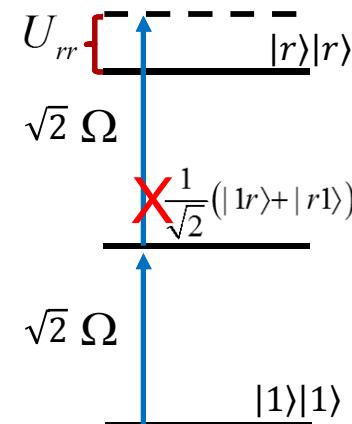
$$J \rightarrow |\beta|^4 \times U_{rr}$$



- Interaction is perturbative
- van der Waals spatial dependence

$$|\psi\rangle = \alpha' |11\rangle + \frac{\beta'}{\sqrt{2}} (|1r\rangle + |r1\rangle)$$

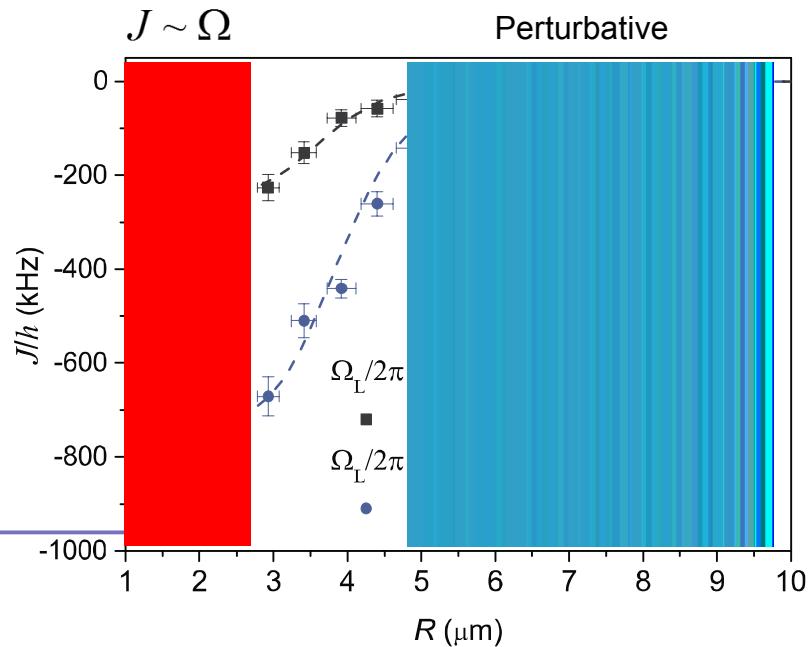
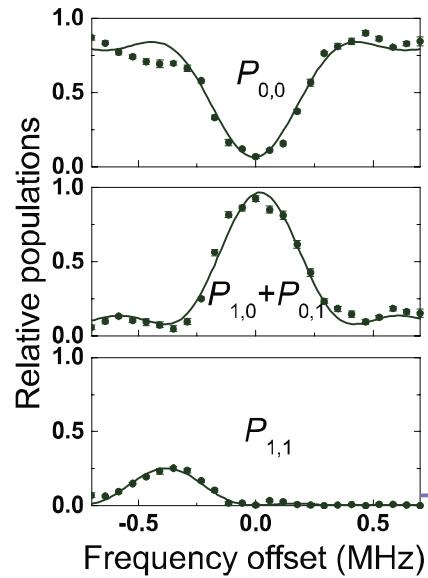
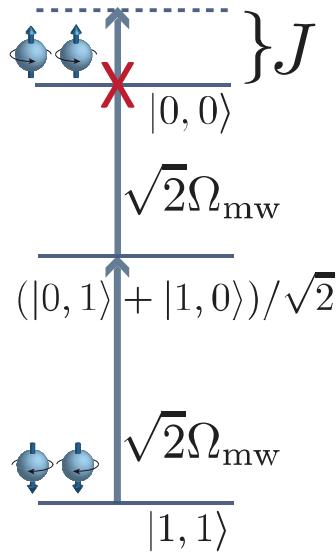
$$J \sim \Omega$$



- Interaction non-perturbative
- Blockade truncates Hilbert space for light shift Hamiltonian

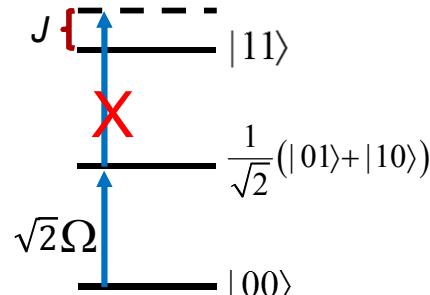
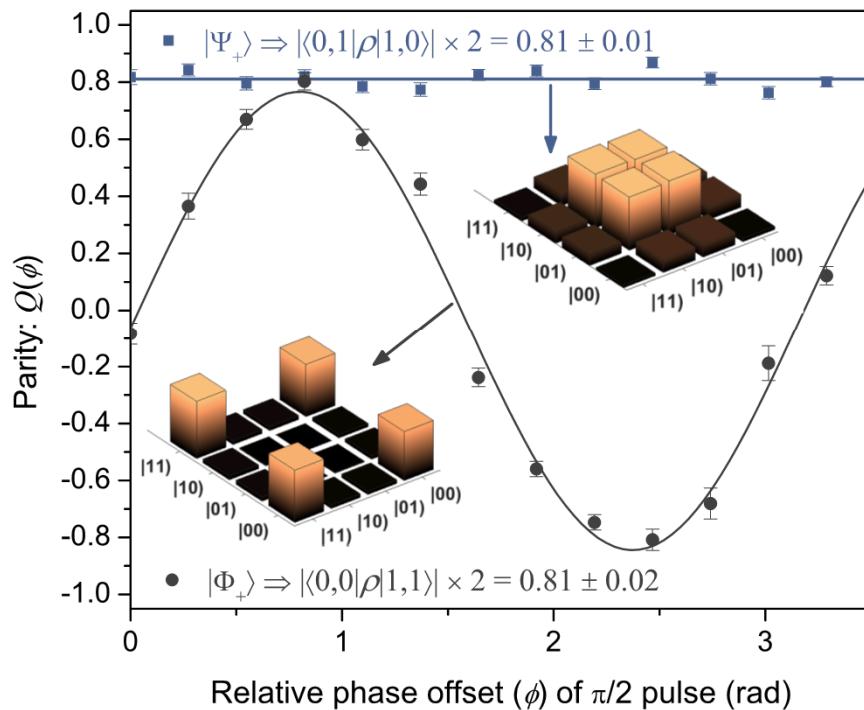
# Observing blockade on hyperfine qubit

Direct measurement of two-qubit interaction strength  $J$  as a function of two-atom separation with different dressing conditions.



# Spin-flip blockade

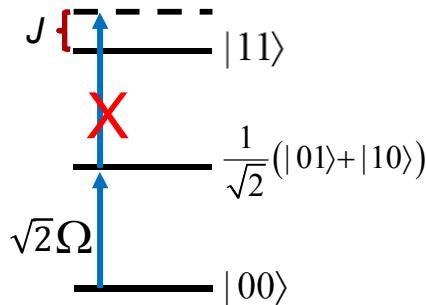
Verify the entanglement via parity measurements



1. Prepare Bell state
2. Apply global  $\pi/2$  with given phase
3. Measure parity  $Q$
4. Obtain bound on fidelity = 0.81(2)

# Spin-flip blockade vs. CPHASE

## Blockade



- Conditional  $\pi$  phase shift can be used to generate controlled-Z and CNOT gates via direct excitation

## Controlled Phase (CPHASE)

- Use nonlinear Hamiltonian:

$$\hat{H}_{DD} = J |11\rangle\langle 11|$$

(+ single-atom light shift terms)

- States acquire nonlinear phase shift:

$$|\psi_0\rangle = \frac{1}{2}(|0\rangle + |1\rangle) \otimes (|0\rangle + |1\rangle)$$

$$\rightarrow \frac{1}{2}(|00\rangle + |10\rangle + |01\rangle + e^{i\phi} |11\rangle)$$

- $\pi$  phase shift as a special case can be used to generate controlled-Z and CNOT gates between hyperfine qubits.
- Nonlinear Hamiltonians for larger systems

# Generating Entanglement

Phase:



$$\hat{H}_{DD} = J |11\rangle\langle 11|$$

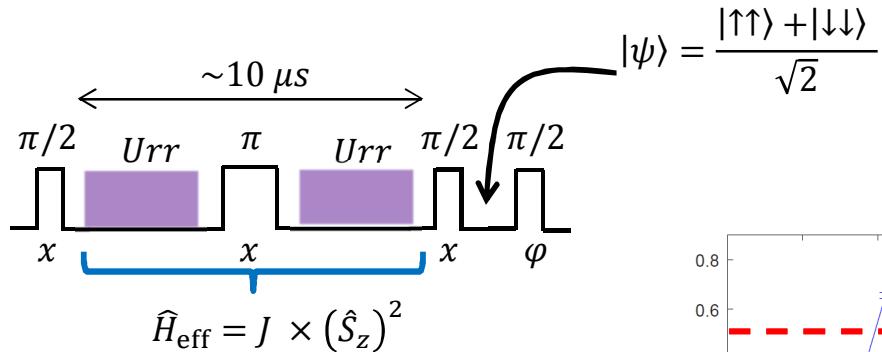
Laser **ON**

— |11\rangle

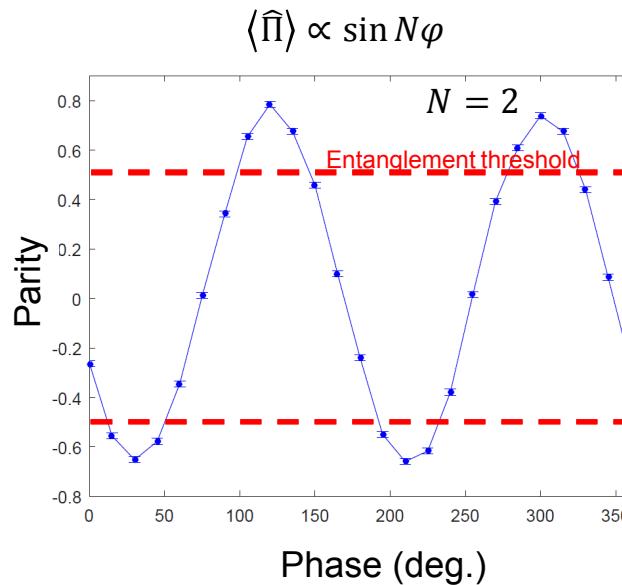


— |01\rangle |10\rangle  
and |00\rangle

# Dressed CPHASE gate



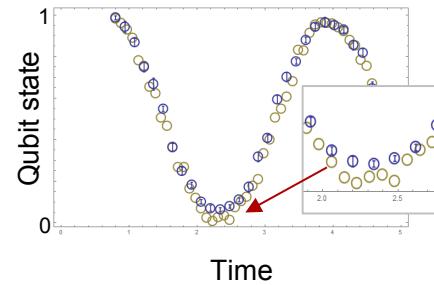
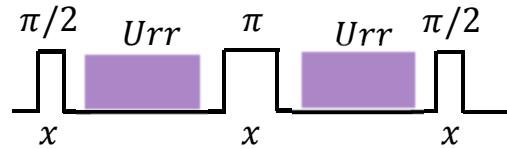
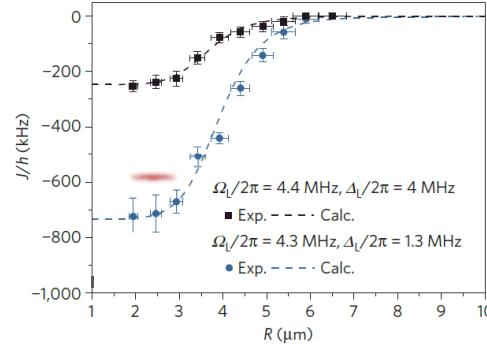
- Single-atom effects removed by echo pulse



J. J. Bollinger *et al.*, “Optimal frequency measurements with maximally correlated states.” Phys. Rev. A **54**(6) (1996).

# Potential limitations

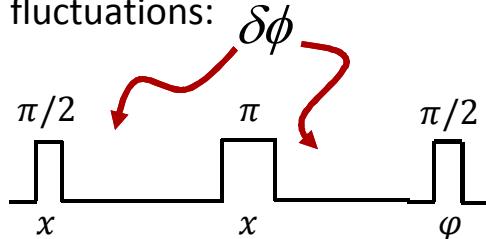
- Thermal, shot-to-shot, position spread
  - Measured position spread, currently limiting at the 3% level
  - “Fine structure” in dressed Rydberg potential still a possible limitation
- Doppler noise
  - Motion-dependent single-atom light shift
  - Mitigated by echo to <0.1%
- State purity
  - Implemented extra state purification
  - >97% purity demonstrated
- Rydberg laser phase and amplitude noise
  - Characterized for current operating parameters: contributes <1%



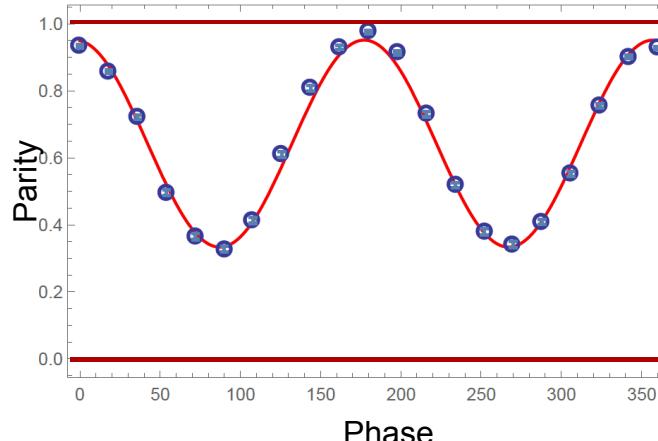
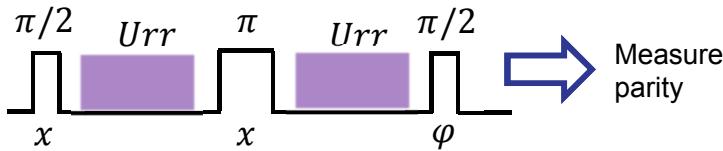
# Local oscillator noise

- Sequence to test qubit rotation operations:
- Expect sine wave with peak-to-peak amplitude of 1

- Measured results consistent with 0.5 rad RMS phase fluctuations:



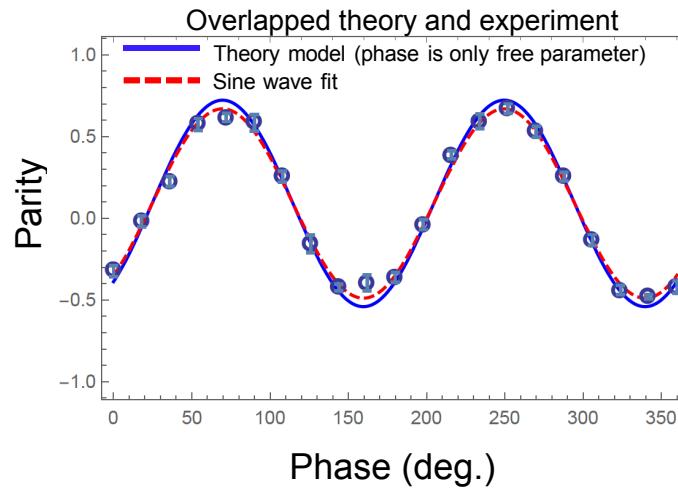
- Potential sources: **Raman Laser linewidth** and **near-resonant amplified spontaneous emission pedestal**



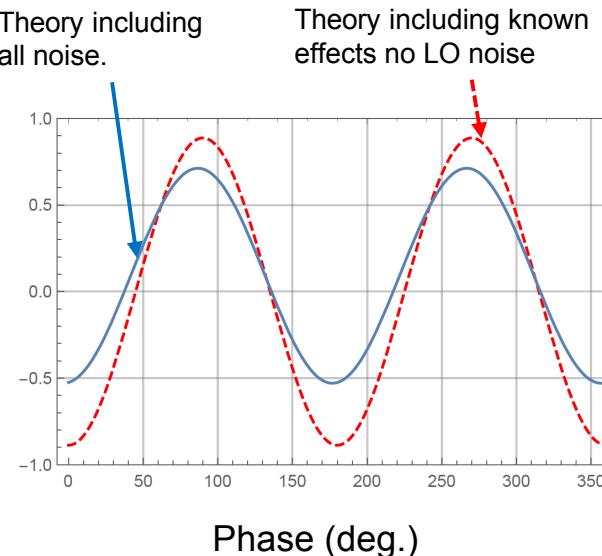
# CPHASE limitations

- Calculated the effect of :
  - Atomic position spread
  - Atomic velocity distribution
  - Effective local oscillator phase noise

→ Theory model with measured noise parameters matches data.



Theory including all noise.

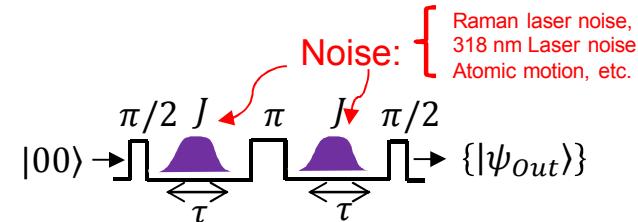


# Error budget for CPHASE gate

## Error budget: informing an experimental strategy

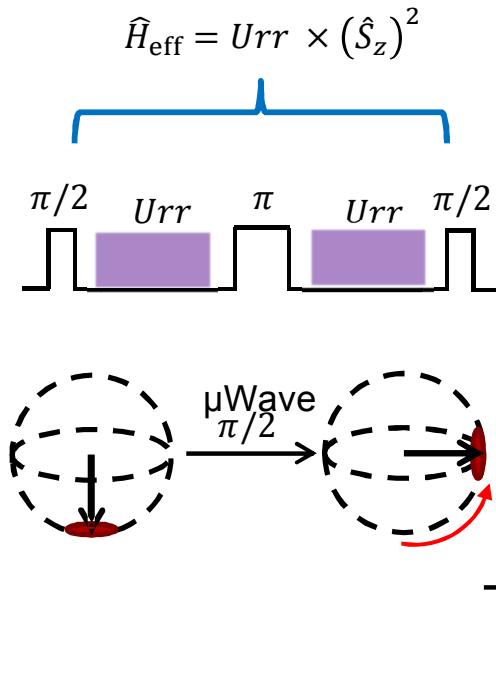
- Trace over external parameters to calculate effect on state fidelity, using measured parameters.

$$\text{Fidelity} = \langle \psi_{tar} | \rho_{out} | \psi_{tar} \rangle$$



Effect	Fidelity reduction	Mitigation
LO noise	$10\% \pm 0.1\%(\text{stat.}) \pm 2\%(\text{sys.})$	Clean Raman laser/μWave cavity
State purity	<3%	Clean Raman laser/μWave cavity
Atomic position spread	$3\% \pm 0.5\%$	Increase blockade radius, increase confinement
Wave-packet overlap	<0.1%	Sideband cooling to ground state
Atomic velocity spread	<0.1%	Sideband cooling to ground state
318 nm Laser frequency noise	$0.2\% \pm 0.1\%$	Pre-stabilized seed lasers, different detuning, dynamical decoupling
Spontaneous emission	$0.4\% \pm 0.2\%$	Higher principal quantum #
318 nm laser amplitude noise	<0.1%	Install "noise eater" on laser

# Scaling to $N$ atoms



- $\hat{S}_z$  is the collective  $S_z$  spin operator for the pseudospin  $N/2$  system.
- For  $N$  atoms all within a blockade radius, an  $N$ -atom cat state forms at  $J \times \tau = \pi/2$

(2-atom case)

$$\frac{| \uparrow \downarrow \rangle + | \downarrow \uparrow \rangle}{\sqrt{2}}$$

y-GHZ

(2-atom case)

$$\frac{| \uparrow \uparrow \rangle + | \downarrow \downarrow \rangle}{\sqrt{2}}$$

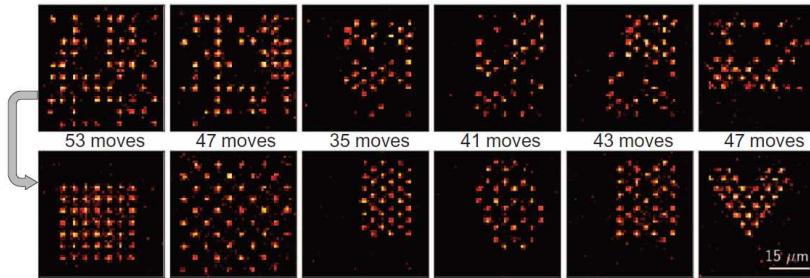
z-GHZ

# Defect-free neutral atom arrays

Lukin group, Harvard<sup>1</sup>

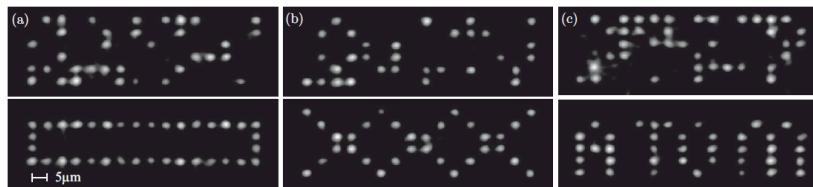


Browaeys group, Institut d'Optique (France)<sup>2</sup>



- There has been a revolution in creating defect free, controllable arrays of neutral atoms.
- 1D and 2D arrays demonstrated. 3D arrays are imminent.
- This capability makes scaling to a many qubit simulator a possibility.

Ahn Group, KAIST (South Korea)<sup>3</sup>



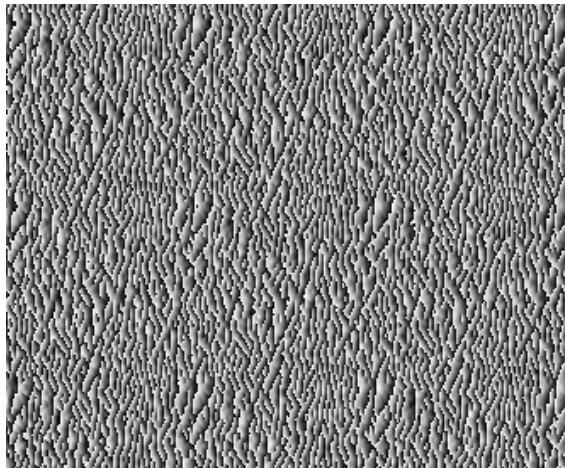
1. M. Endres et al., Science 354, 1024 (2016)
2. D. Barredo et al., Science 354, 1021 (2016)
3. W. Lee et al., Phys. Rev. A 95, 053424 (2017)

# Generation and control of >500 of individual traps

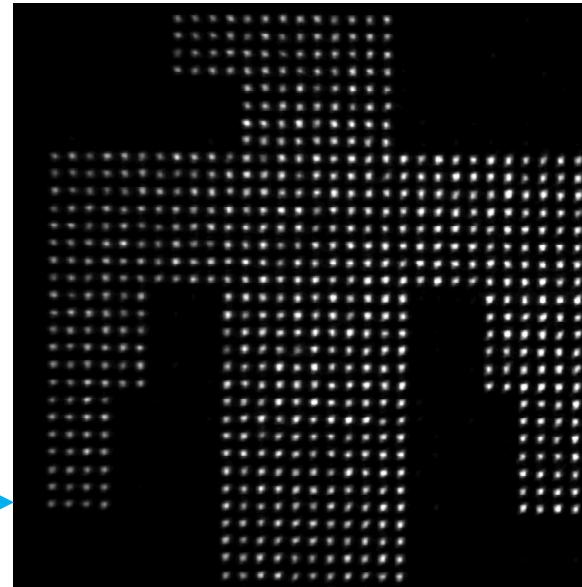
Gerchberg-Saxton algorithm  
With GPU compute acceleration  
(~50 Hz hologram calculation)



Phase to SLM



Intensity profile (measured)

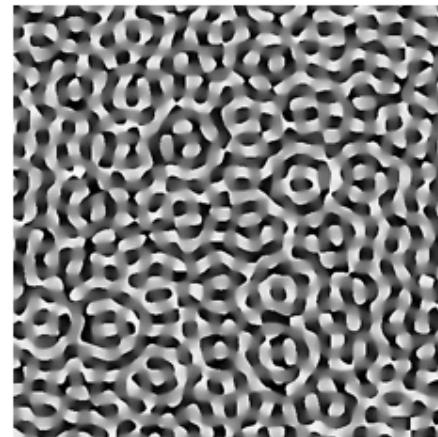


# Dynamic control of hologram-generated traps

30 fps, real time



Phase hologram



# Dynamic control of hologram-generated traps

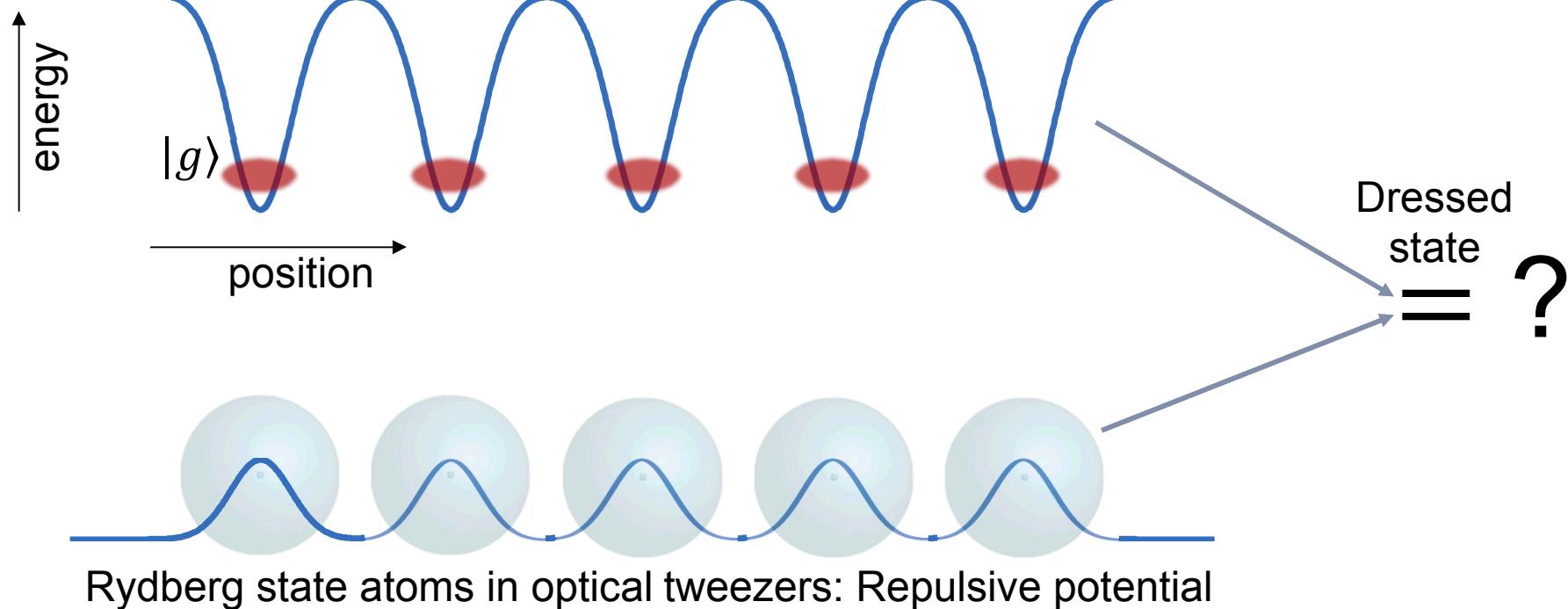
500 fps



-Optimize techniques for calculating hologram with as little phase discontinuity between frames as possible.

# Trapping Rydberg-Dressed atoms

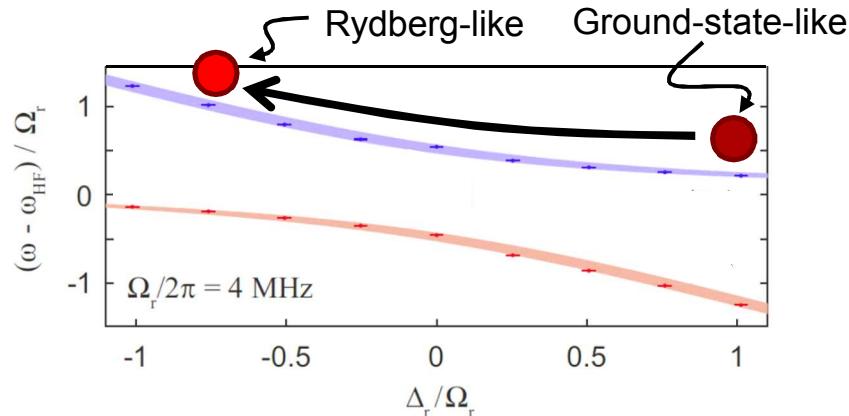
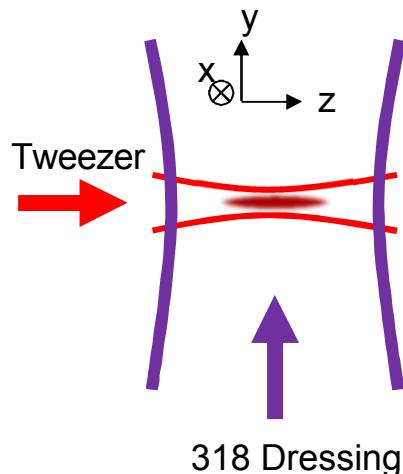
Ground state atoms in optical tweezers: Attractive potential



Rydberg state atoms in optical tweezers: Repulsive potential

# Preparing a trapped, dressed-state

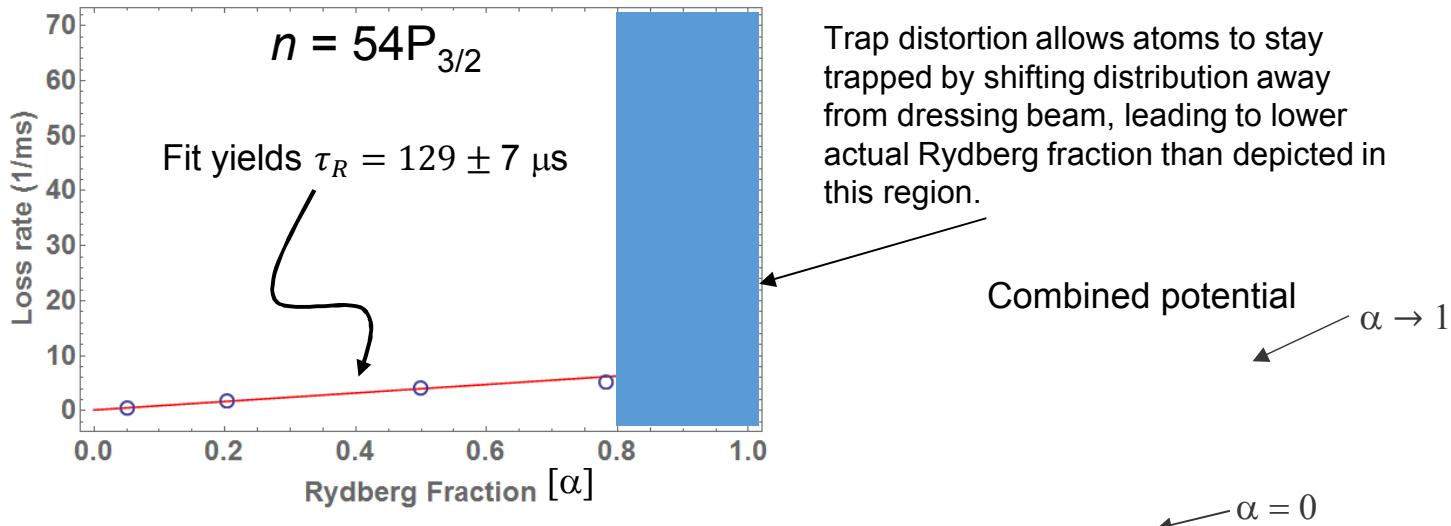
- Sweep Rydberg laser frequency and amplitude to prepare dressed, trapped final state.



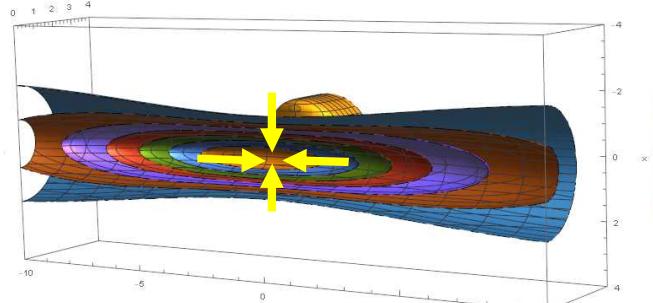
Test lifetime of dressed state in trap

# Long-lived & trapped, Rydberg-dressed states

- loss rate depends linearly on Rydberg admixture
- consistent with theoretical Rydberg state lifetime of 121  $\mu$ s



# Equipotential surfaces for the blue sideband for different dressing conditions.



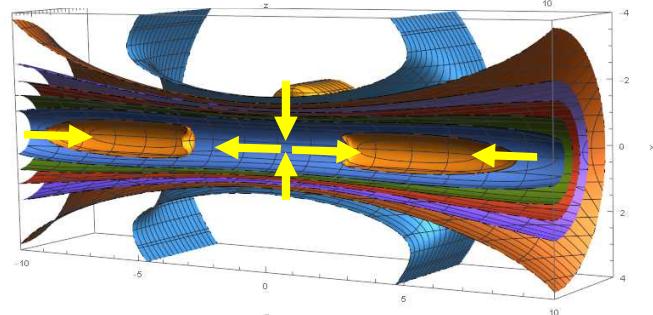
Rydberg Rabi freq.  $\Omega_R = 2.2$  MHz

Bare trap depth  $U_0 = 5$  MHz

$\Delta/\Omega_R = 0$

50% Rydberg admixture at trap center

Center is stable minimum.



Rydberg Rabi freq.  $\Omega_R = 2.2$  MHz

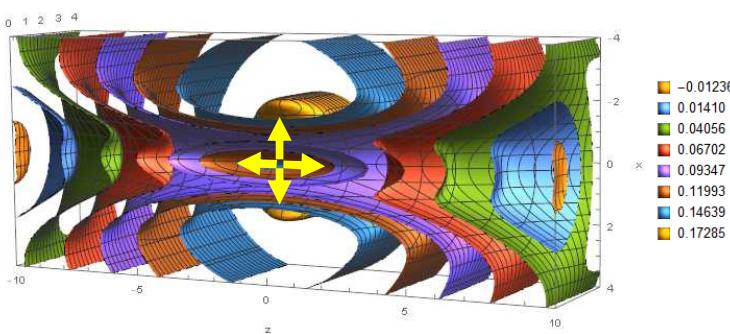
Bare trap depth  $U_0 = 5$  MHz

$\Delta/\Omega_R = -1.75$

93% Rydberg admixture at trap center

Center is not stable minimum.

Trap closed.



Rydberg Rabi freq.  $\Omega_R = 2.2$  MHz

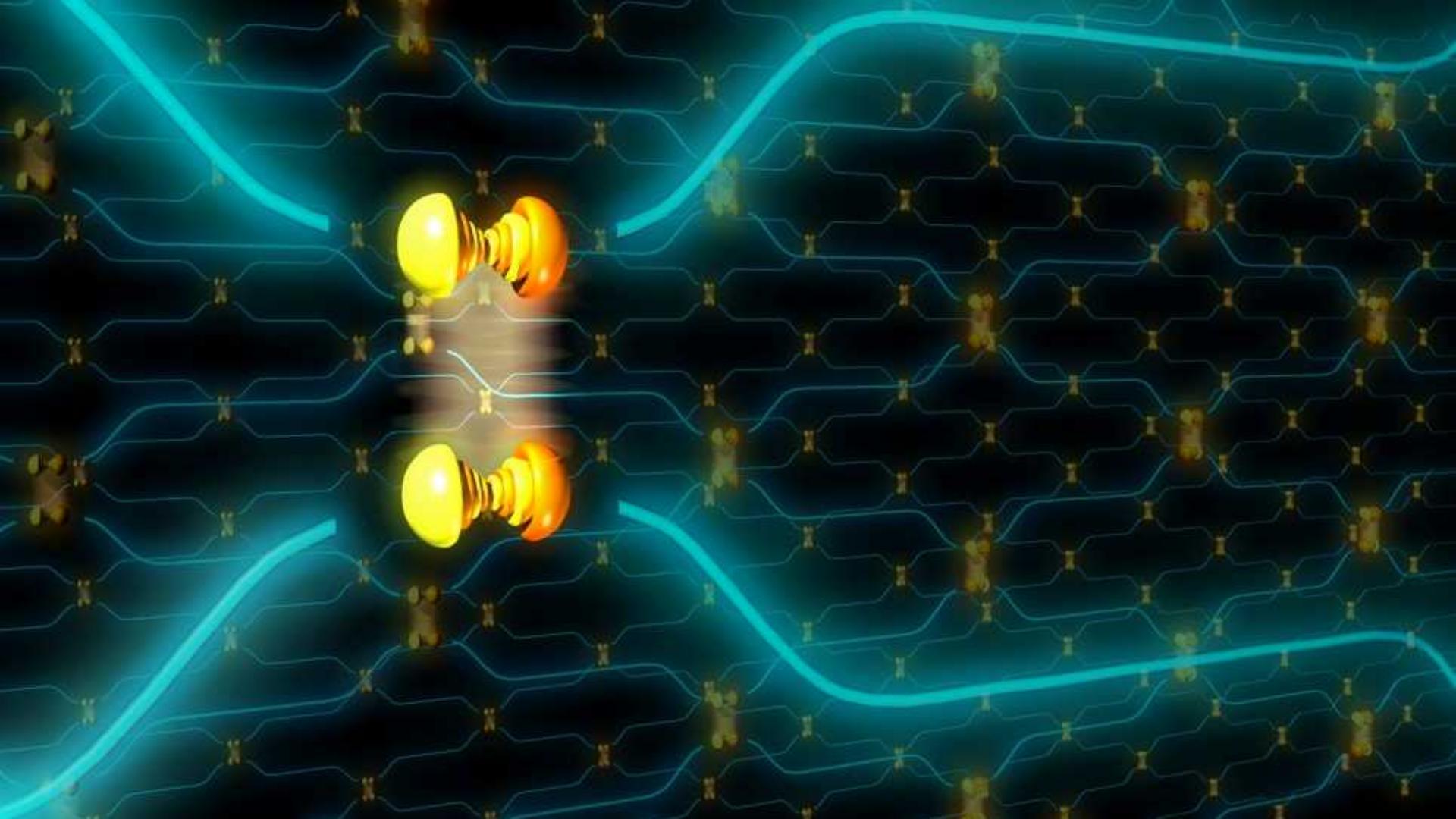
Bare trap depth  $U_0 = 5$  MHz

$\Delta/\Omega_R = -2.5$

96% Rydberg admixture at trap center

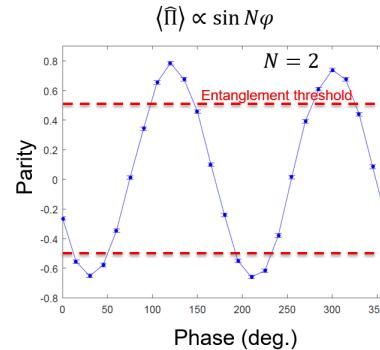
Center is not stable minimum.

Trap open.

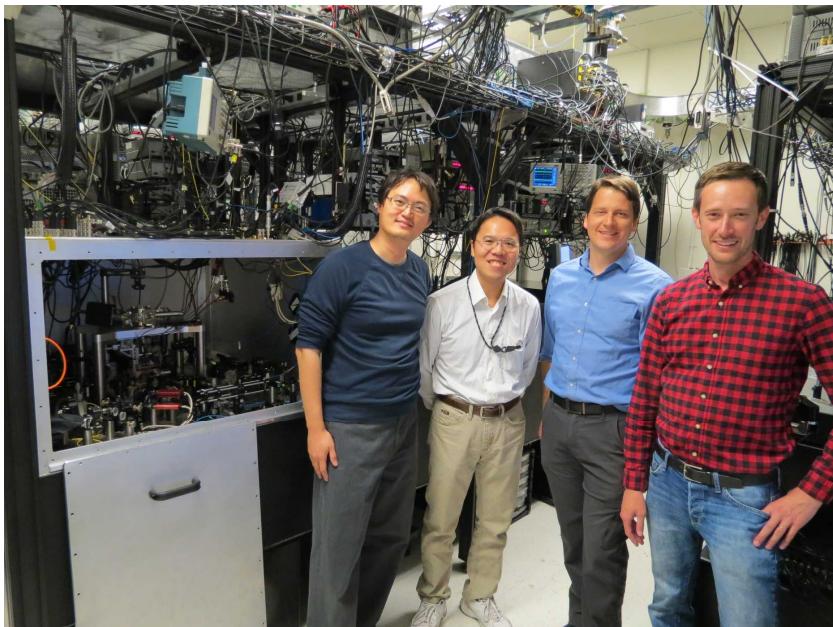


# Recap

- Demonstrated both spin-flip and CPHASE gates between two Rydberg-dressed hyperfine qubits.
  - CPHASE functionality will permit useful quantum operations between atoms.
  - **Tracking down systematic effects!**
- Single-photon Rydberg dressing opens up possibilities for large-scale entanglement and quantum simulation.
  - **Work towards larger systems is ongoing.**



# Sandia Rydberg Team



Sandia mountains viewed from the Rio Grande near Albuquerque, New Mexico



**LDRD**

Laboratory Directed Research and Development



Postdoc position available. Contact me!