

Exceptional service in the national interest



https://en.wikipedia.org/wiki/Sandia_Mountains

***Digital Image Correlation
at Sandia National Laboratories:
Emphasizing material characterization
and finite-element model validation***

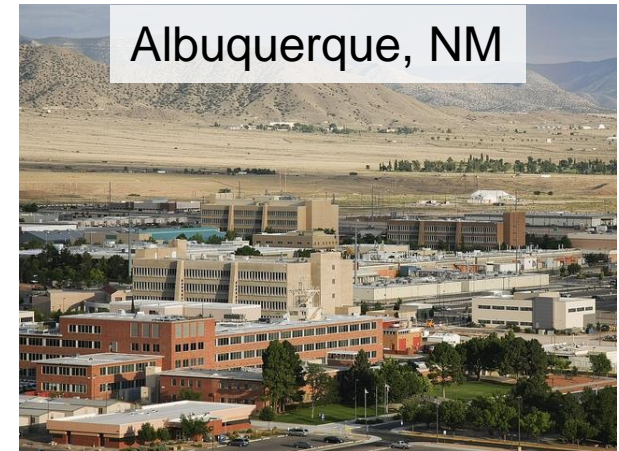
Elizabeth M. C. Jones, Ph.D.

Diagnostic Science and Engineering



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- SNL is a federally-funded research and development center:
 - Nuclear Weapons
 - Defense Systems and Assessments
 - Energy and Climate
 - Global Security
- Engineering Science, Center 1500
 - Revolutionizing the fundamental understanding of complex engineered systems
 - solid mechanics
 - fluid mechanics
 - structural dynamics
 - thermal and combustion sciences
 - aerodynamics
 - shock physics and energetics
 - electromagnetic sciences
 - <https://www.youtube.com/watch?v=o1qAjLSEv0A>

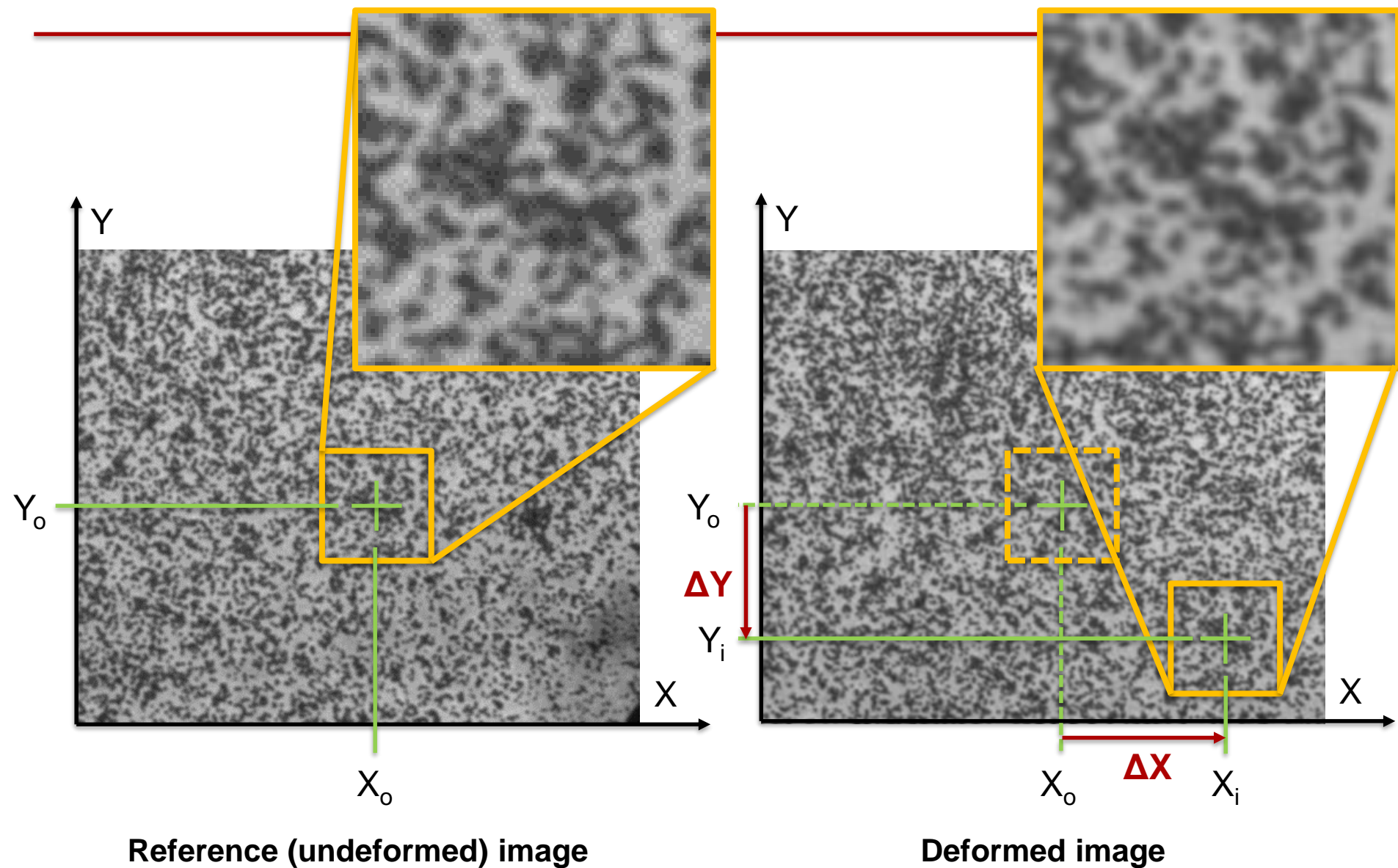


- Digital Image Correlation
 - Fundamentals
 - International DIC Society (iDICs)
 - Applications at Sandia
- Material Characterization
 - Background
 - Viscoplastic Material Model
 - Traditional Calibration Technique
 - Advanced, Full-Field Calibration Technique
- Finite-Element Model Validation
 - Global Data
 - Full-Field Data
 - Boundary Conditions
- Conclusions and Future Work

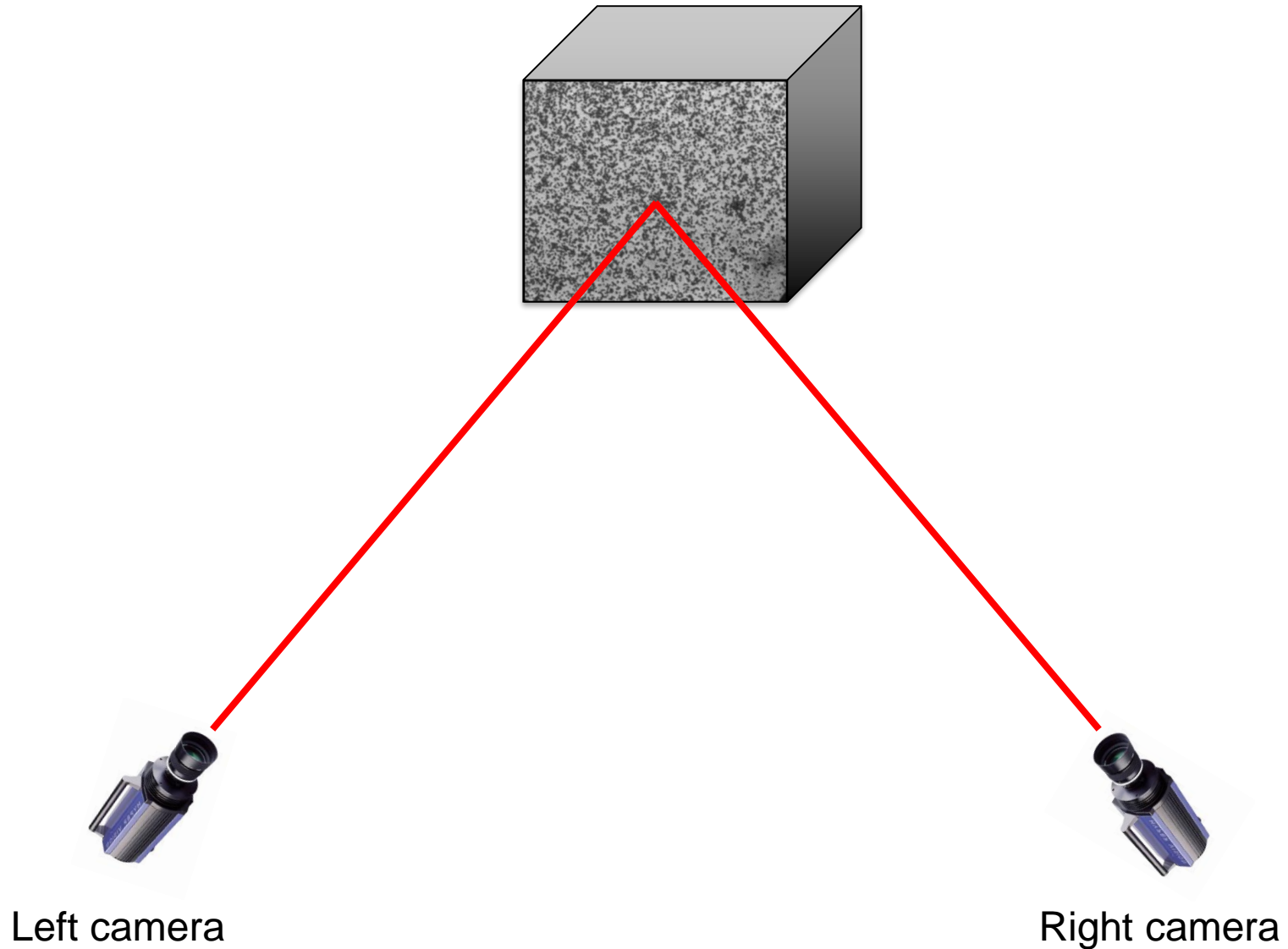
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- Diagnostic technique providing full-field shape, displacement and strain measurements on the surface of a solid specimen
- Optical (non-contact)
- Length scale independent
- “Keep the dots in the box”* (Prof. Samantha Daly)

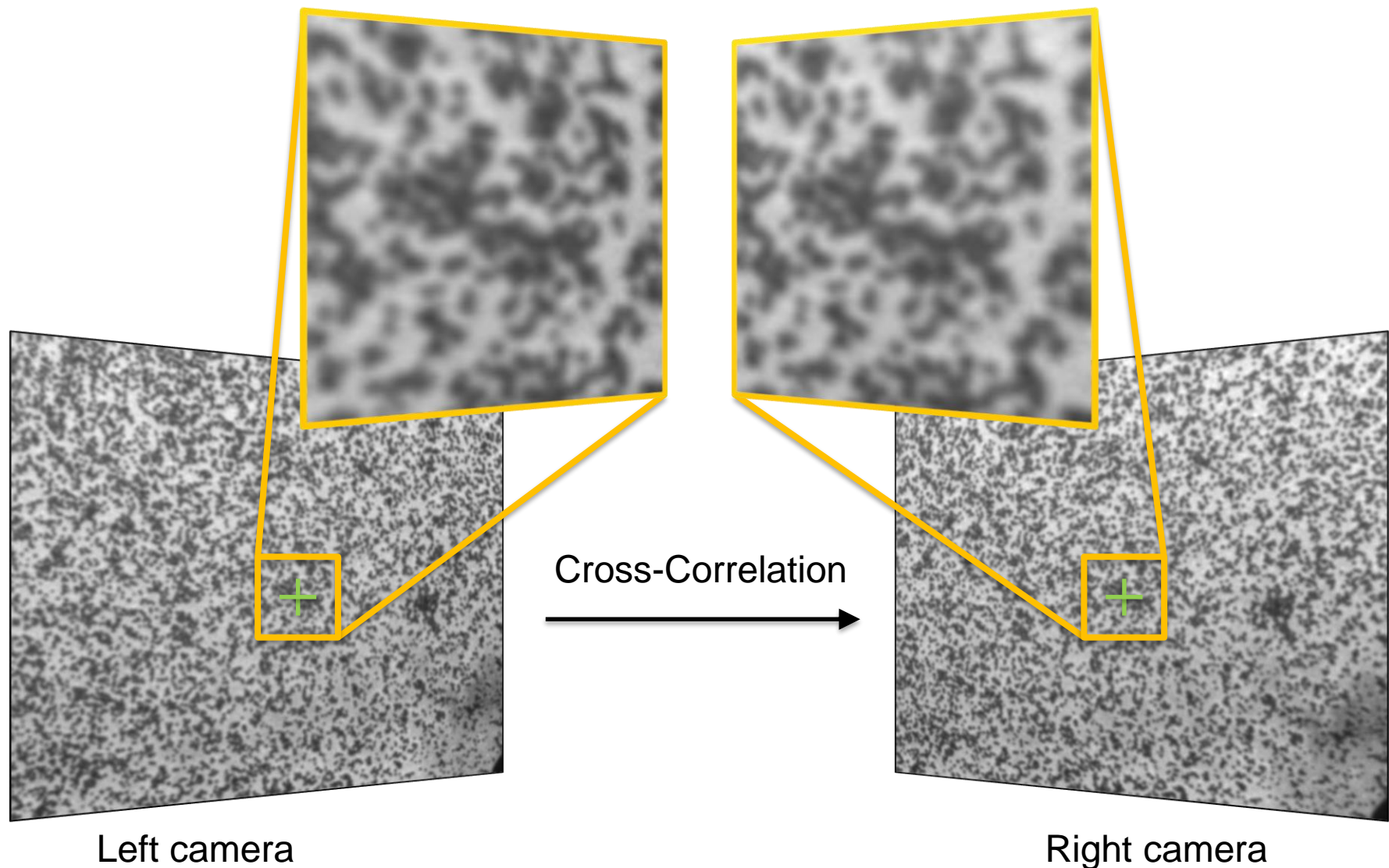
Digital Image Correlation (DIC)



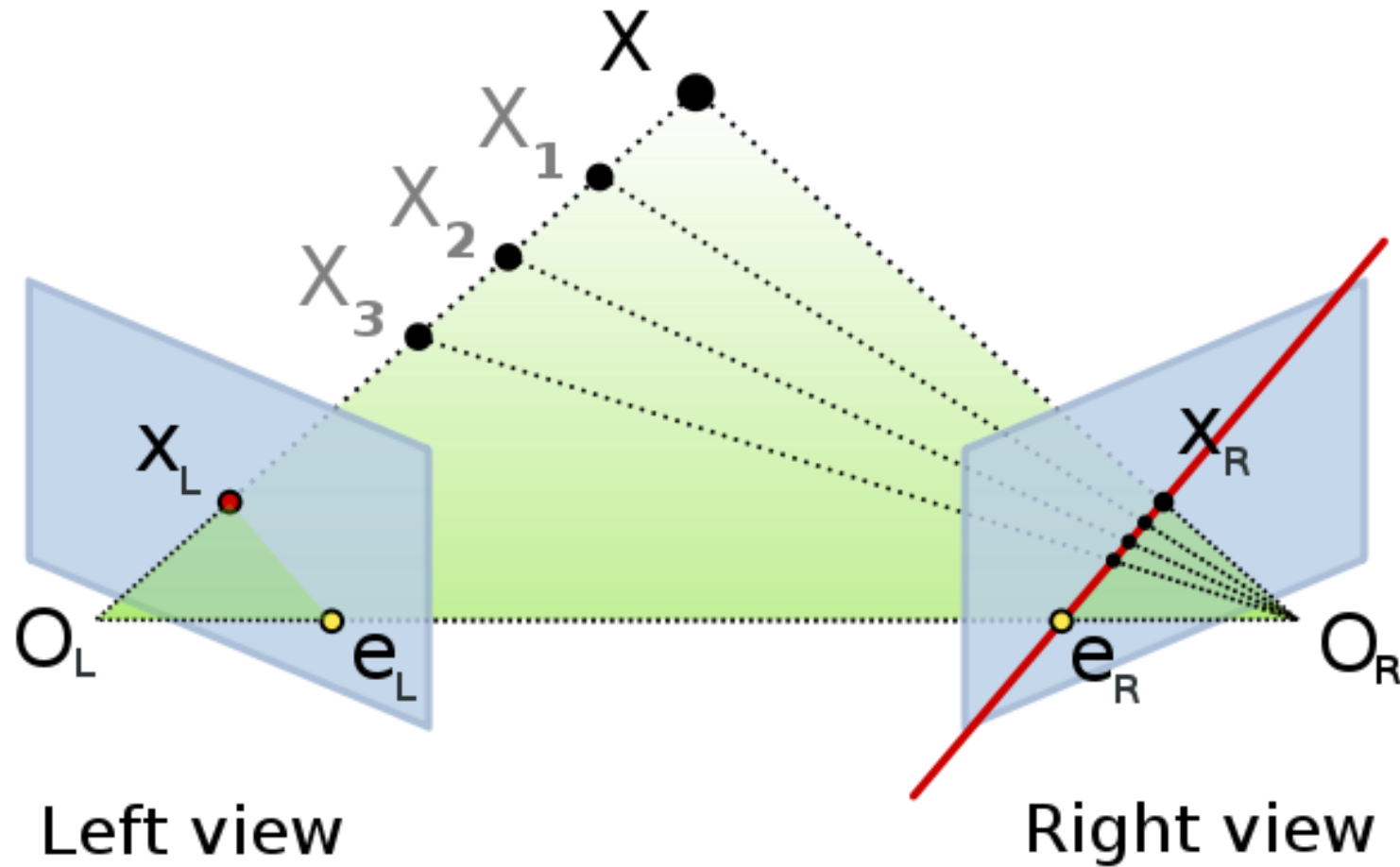
Stereo DIC provides locations and displacements in three dimensions.



Stereo DIC provides locations and displacements in three dimensions.



Stereo DIC provides locations and displacements in three dimensions.



- Founded in 2015
- Composed of members of academia, government, and industry
- Developing world-recognized DIC training, certification, and standardization
- www.idics.org

iDICS INTERNATIONAL
DIGITAL IMAGE CORRELATION
SOCIETY

A Good Practices Guide for Digital Image Correlation

Standardization, Best Practices, and Uncertainty Quantification Committee

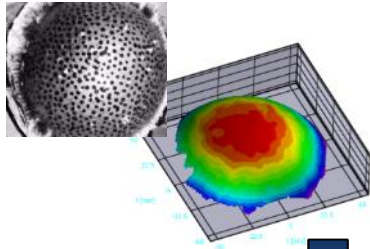
November 2017

This is a pre-release copy of the work titled "A Good Practice Guide for Digital Image Correlation". Permission to review this document is given solely to the original recipient of this document. This pre-published copy of the document may not be distributed. If you are not the original recipient of this document, contact guide@idics.org and either return this document to the original recipient or destroy this document.

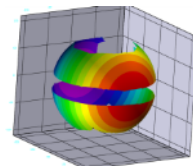


Digital Image Correlation at Sandia

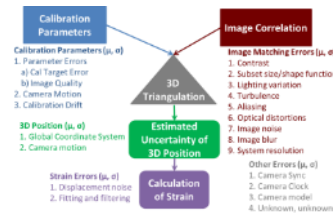
Displacement, velocity
and strain



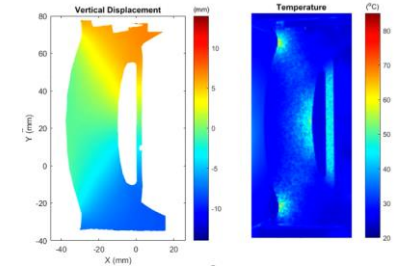
360° coverage



Stereo-DIC Uncertainty Quantification
From colors to metrology.

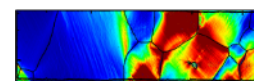


Advanced Material Testing



Volumetric DIC

Grain Scale strain



2005

2007

2009

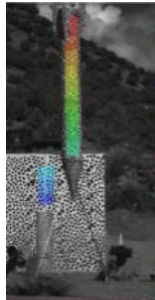
2011

2013

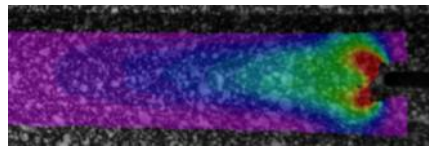
2015

2017

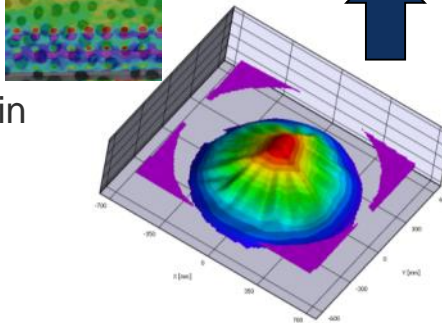
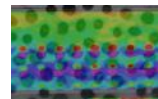
Introduction of
DIC to Sandia



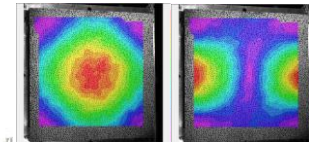
Crack-tip and Fracture Strain



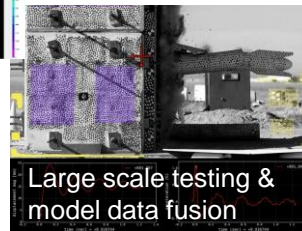
0% 5% ϵ 15%



Explosive Panel Deformation



Modal Testing



Large scale testing &
model data fusion

Credit: Phillip Reu

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Special thanks goes to...

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Kyle N. Karlson, Ph.D.

Jay Carroll, Ph.D.

William M. Scherzinger, Ph.D.

Paul A. Farias

Darren L. Pendley

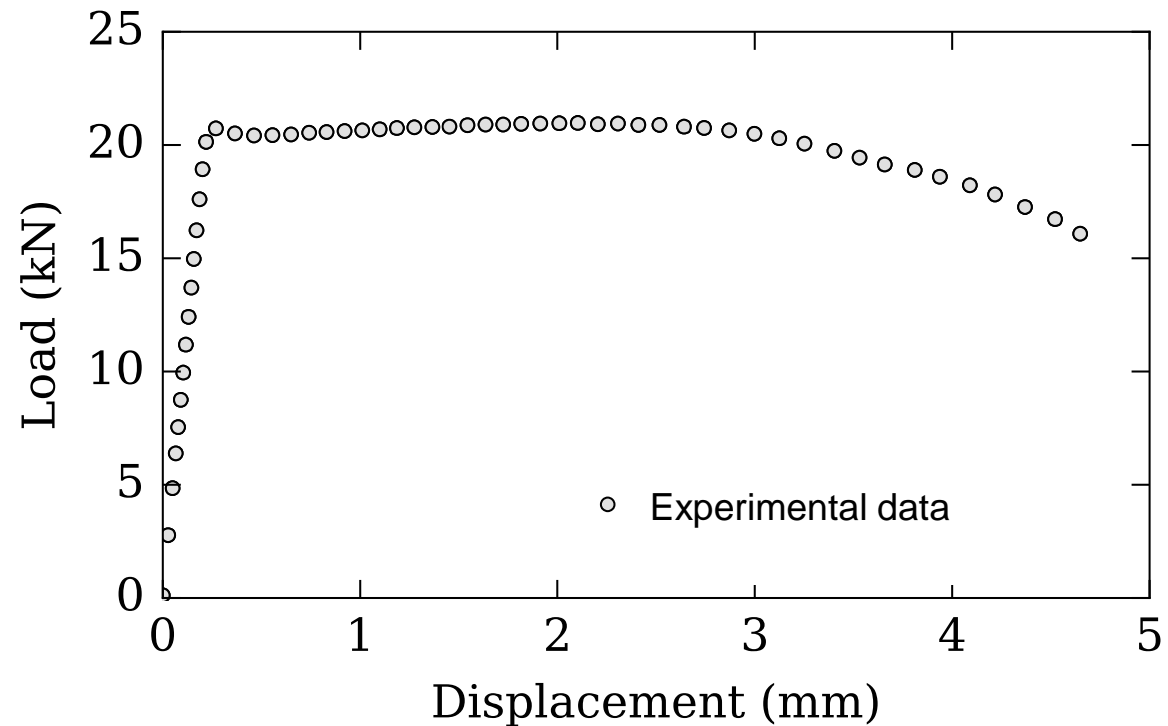
Modeling material and component behavior is critical for modern engineering.

- Material model:

$$\sigma = f(\underbrace{\zeta(\varepsilon, p, \dot{p}, T)}_{\text{loading conditions}}, \underbrace{\xi(E, \nu, \sigma_o, H)}_{\text{model parameters}})$$

- Model parameters \neq material properties
- Finding model parameters:
 - Model calibration
 - Material identification
 - Material characterization

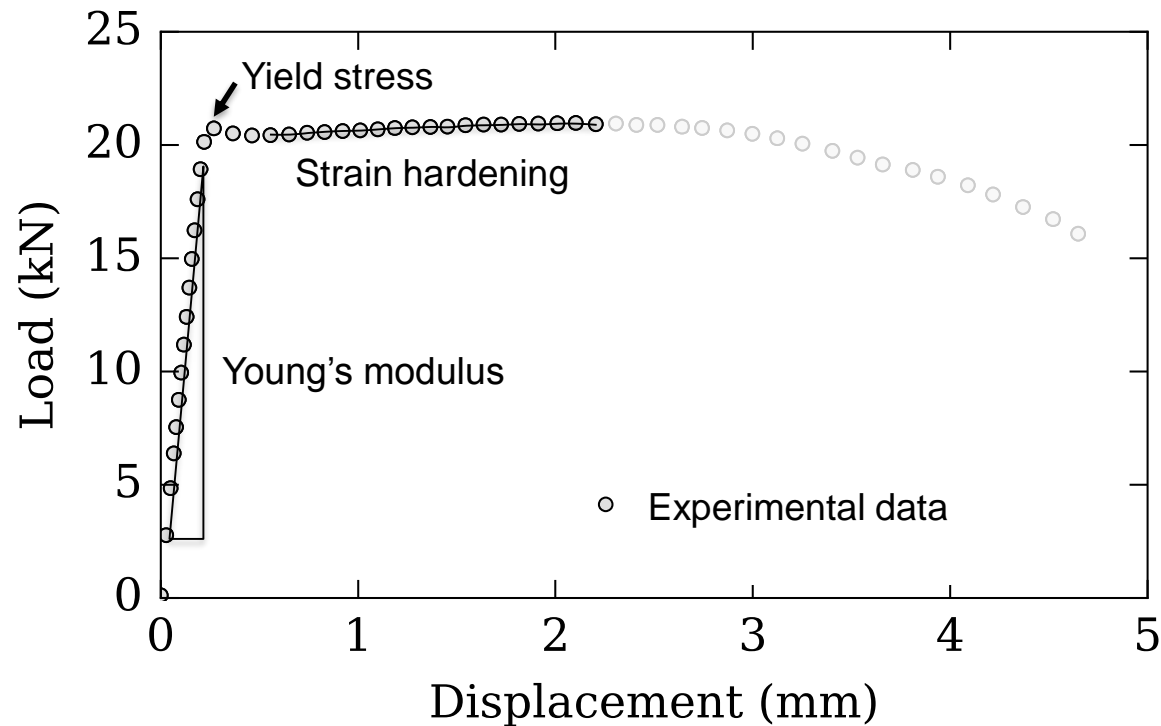
Material models are **traditionally** calibrated from **global, homogeneous** data.



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Low strain regime:

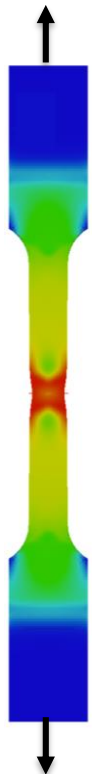
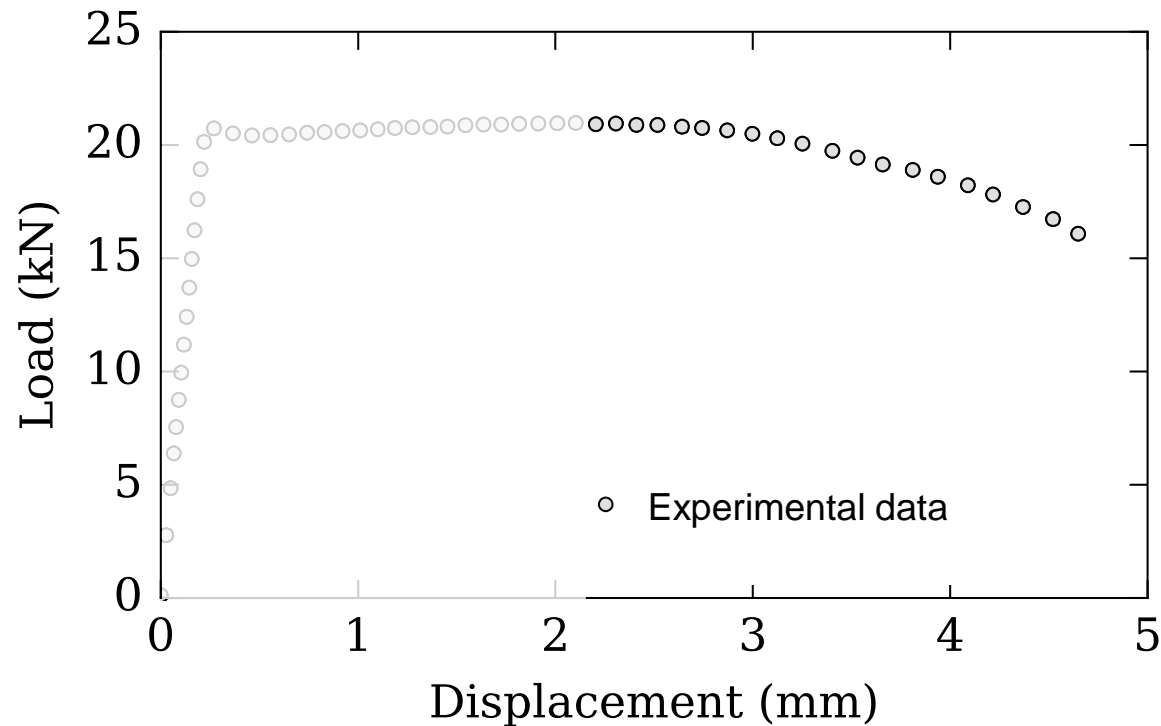
- Uniaxial tension
- Identification of model parameters accomplished analytically



Material models are **traditionally** calibrated from **global, homogeneous** data.

High strain regime:

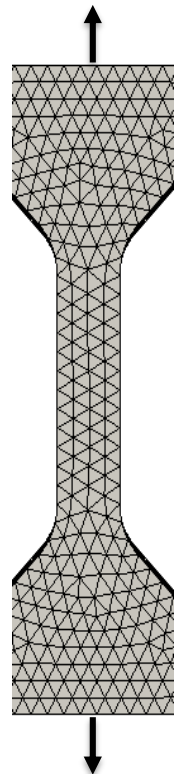
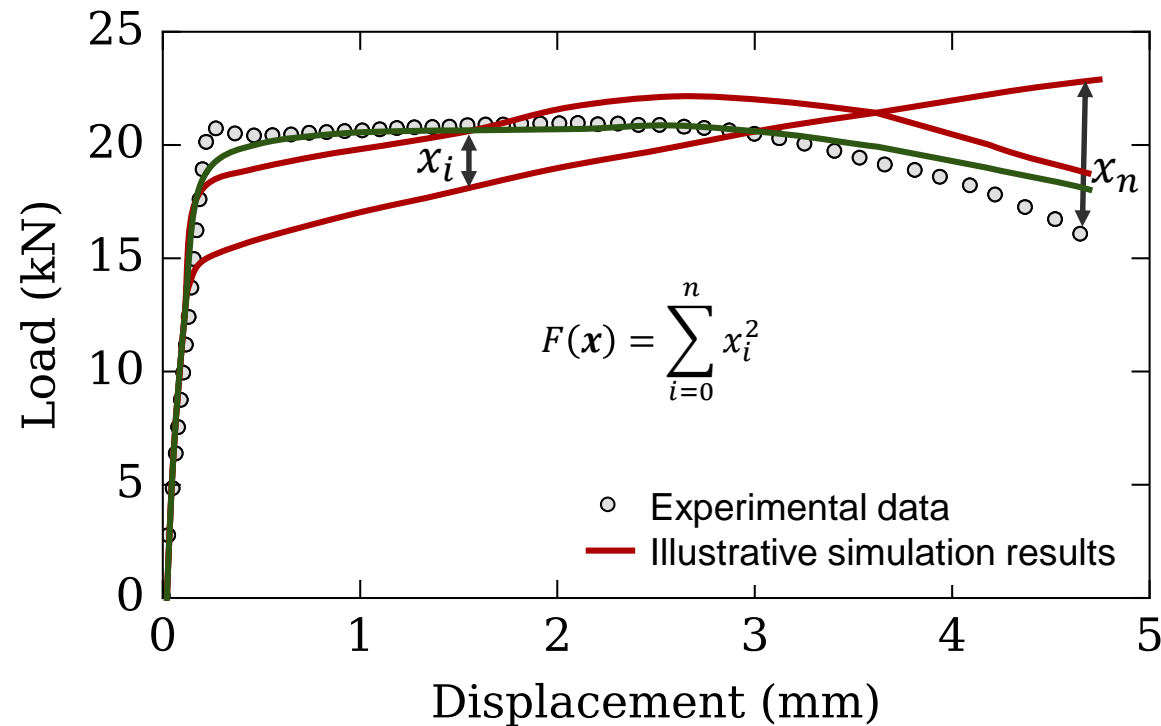
- Multiaxial stress state
- Identification of model parameters requires inverse problem



Material models are **traditionally** calibrated from **global, homogeneous** data.

High strain regime:

- Multiaxial stress state
- Identification of model parameters requires inverse problem



Traditional material identification has **limitations**.

- Global information misses local deformation
- Many tests required to calibrate complex models
- Simple stress state does not reflect complex, real-world loading conditions



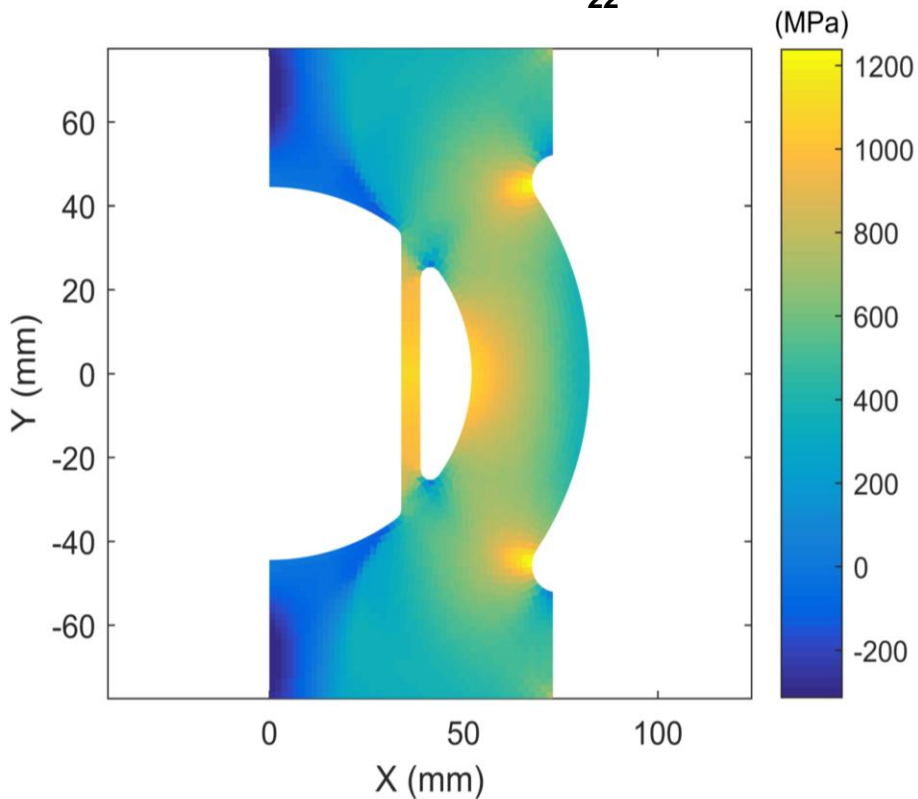
≠



<http://money.cnn.com/2014/01/22/autos/small-car-crash-test/>
Accessed 29 Aug 2016

High-throughput, high-quality material identification addresses limitations of traditional material ID.

Contour Plot of σ_{22}



Capitalize on:

- Full-field deformation measurements: Digital Image Correlation (DIC)
- Inverse techniques: Virtual Fields Method (VFM)

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Strain-rate dependence is modeled with the Bammann-Chiesa-Johnson (BCJ) material model.

$$\sigma_f(p, \dot{p}, \xi) = \dots$$

$$\sigma_Y \left\{ 1 + a \sinh \left[\left(\frac{\dot{p}}{b} \right)^{1/m} \right] \right\} + \dots \quad \leftarrow \text{Strain-rate dependence of initial yield stress}$$

$$\frac{H}{R_d} [1 - \exp(-R_d p)] \quad \leftarrow \text{Voce-type hardening}$$

σ_f flow stress

p equivalent plastic strain

\dot{p} equivalent plastic strain rate

σ_Y quasi-static yield stress

b rate-dependent coefficient

m rate-dependent exponent

H hardening variable

R_d dynamic recovery

Strain-rate dependence is modeled with the Bammann-Chiesa-Johnson (BCJ) material model.

$$\sigma_f(p, \dot{p}, \xi) = \dots$$

$$\sigma_Y \left\{ 1 + \operatorname{asinh} \left[\left(\frac{\dot{p}}{b} \right)^{1/m} \right] \right\} + \dots$$

$$\frac{H}{R_d} [1 - \exp(-R_d p)]$$

σ_f flow stress

p equivalent plastic strain

\dot{p} equivalent plastic strain rate

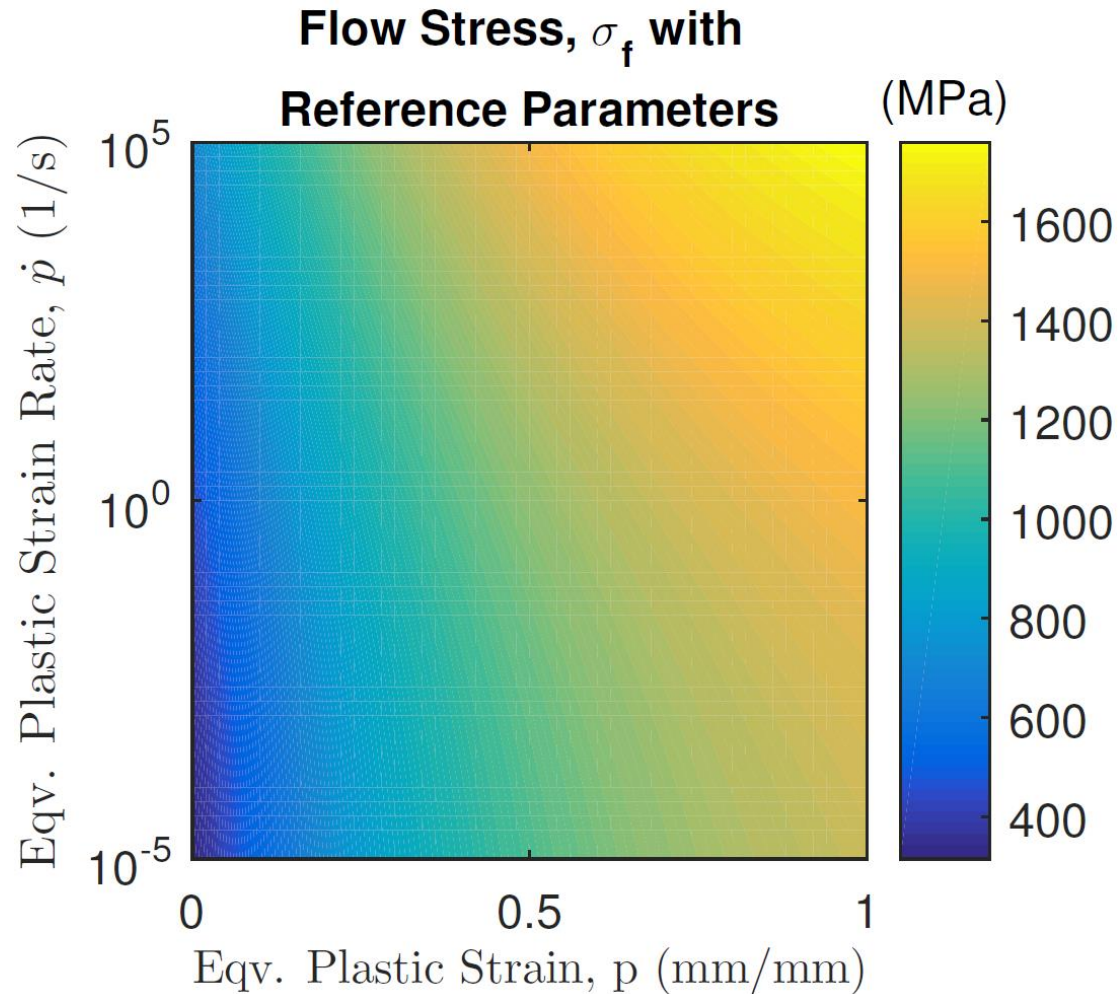
σ_Y quasi-static yield stress

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m rate-dependent exponent

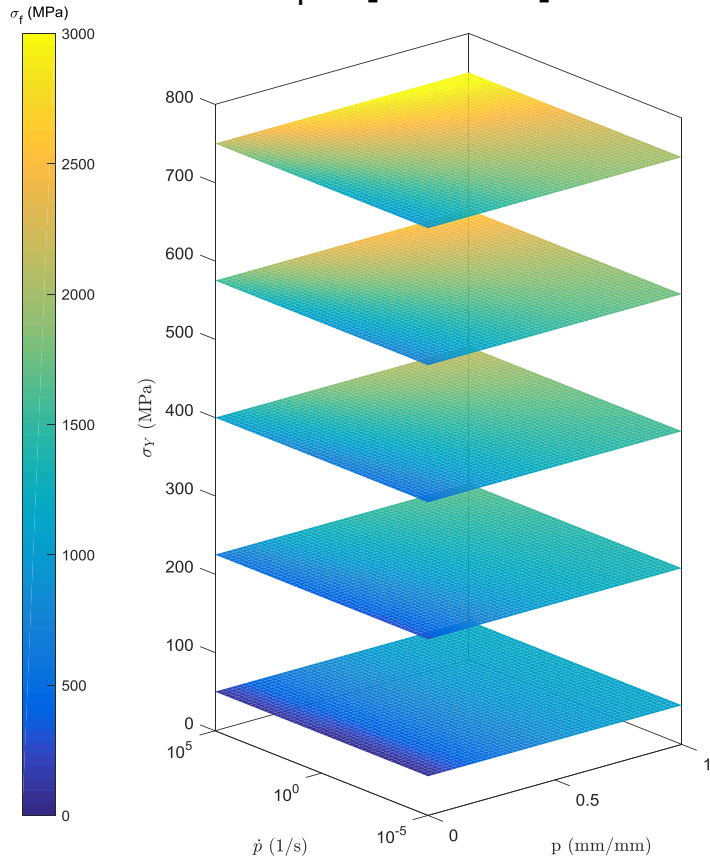
H hardening variable

R_d dynamic recovery

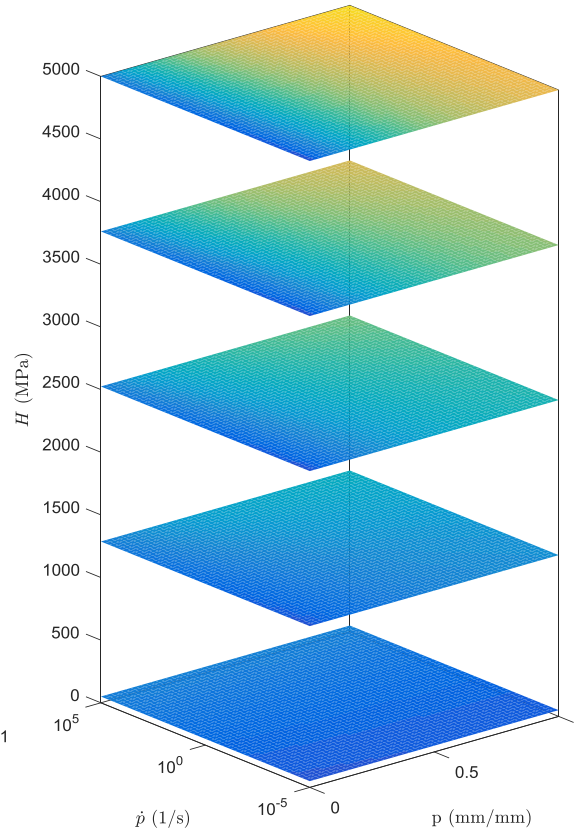


The influence of model parameters is complex and **multidimensional**.

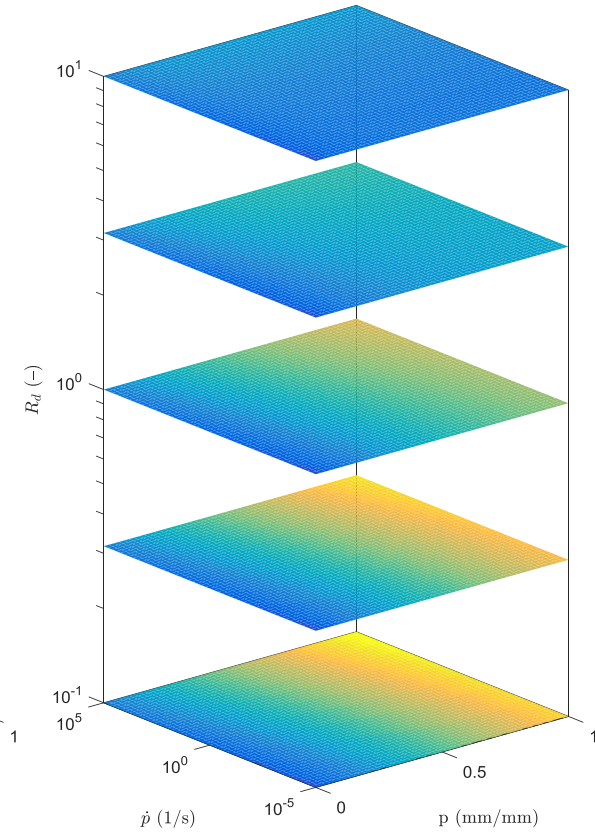
$\sigma_Y = [50, 750] \text{ MPa}$



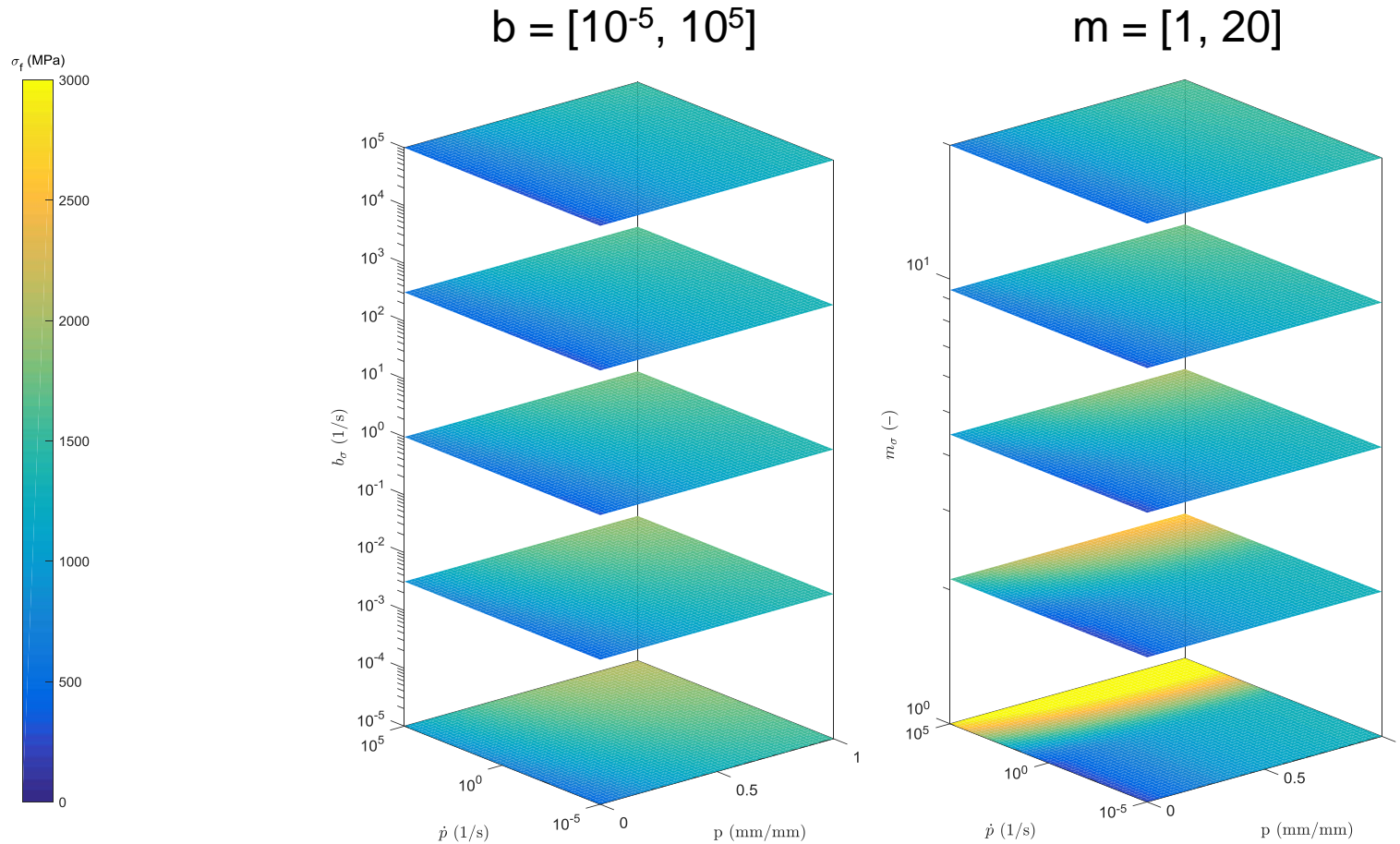
$H = [50, 5000] \text{ MPa}$



$R_d = [0.1, 10]$



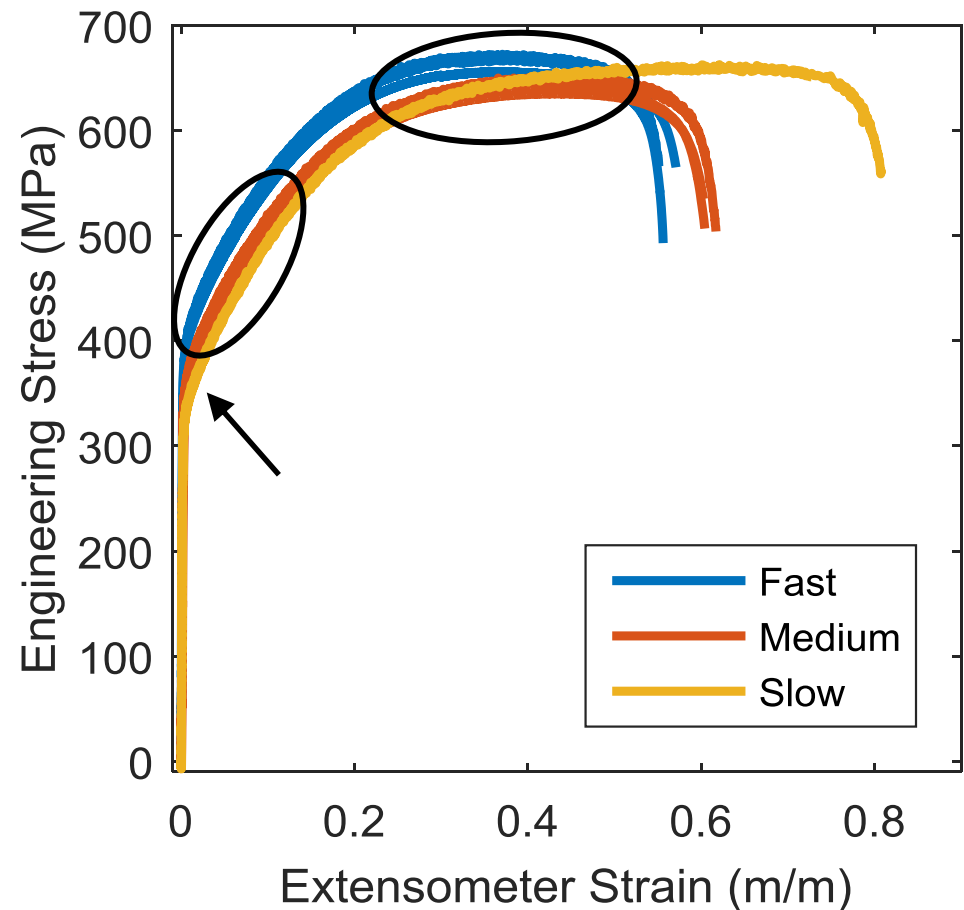
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Tensile dog bones were tested experimentally.

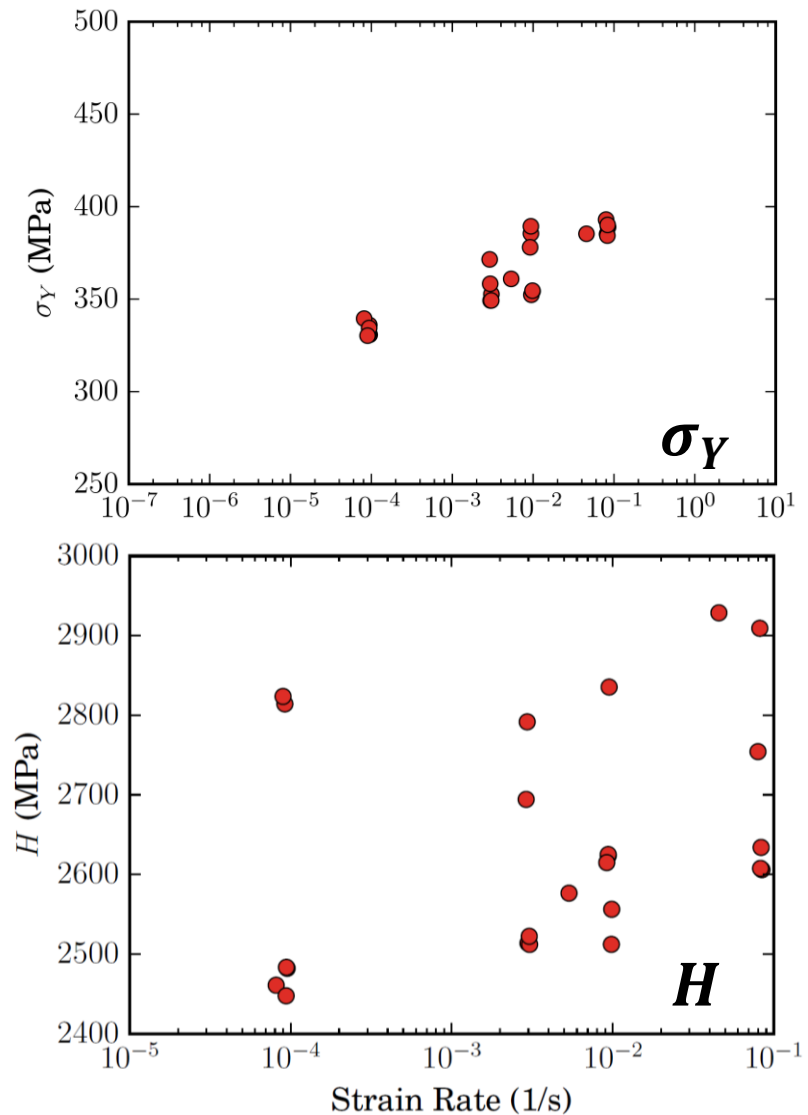
- Material:
 - 304L stainless steel rolled sheet, 1.5 mm thick
- Dog bone gauge section:
 - 50.8 mm x 12.7 mm
- Three nominal strain rates (s^{-1}):
 - $1.0 \cdot 10^{-4}$
 - $3.2 \cdot 10^{-3}$
 - $1.0 \cdot 10^{-1}$
- Virtual extensometer from DIC
 - 22 mm gauge section



Because of material model complexity,
data is fit in **successive steps**.

Step 1:

- Each tensile test is fit individually to a rate-independent model:
 - $\sigma_f(p, \dot{p}, \xi) = \sigma_Y + \dots$
 $\frac{H}{R_d} [1 - \exp(-R_d p)]$
- Actual strain rate is calculated from DIC extensometer data



Initial guesses are found for all five parameters.

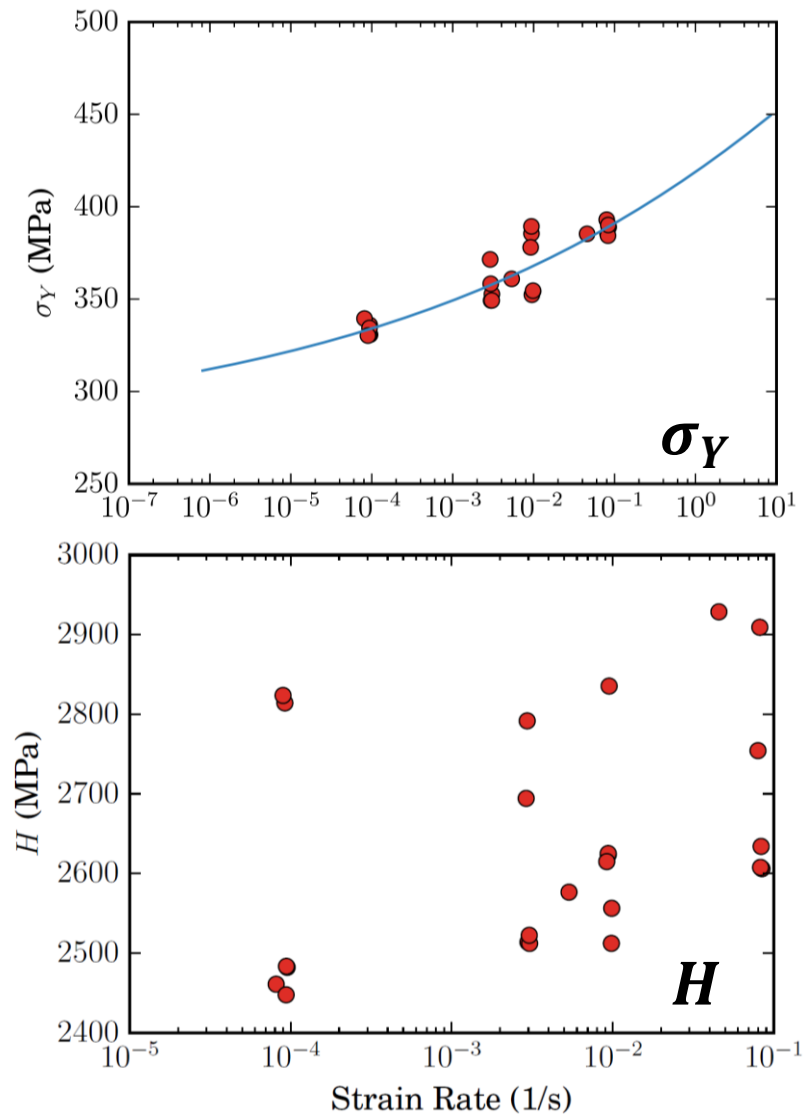
Step 2:

- σ_Y, b, m :

- $\sigma_f = \sigma_Y \left\{ 1 + \text{asinh} \left[\left(\frac{\dot{p}}{b} \right)^{1/m} \right] \right\}$

- H, R_D :

- No significant rate-dependence
 - Averaged from step 1



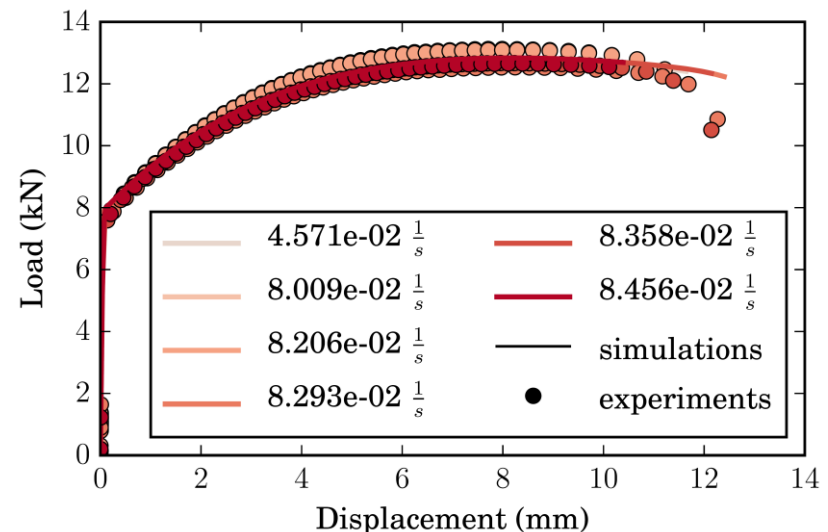
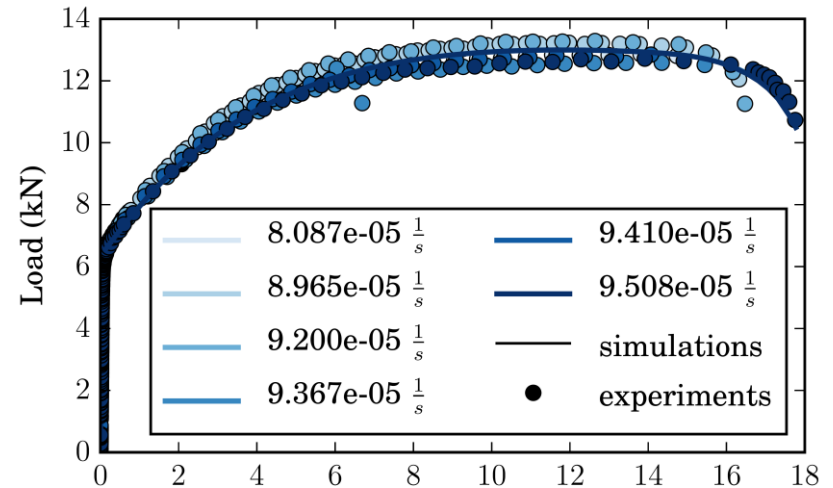
Finite-element method updating (FEMU) is used for final traditional calibration.

Step 3:

- FEA model is created for each tensile specimens
- Cost function is built as the error between experimental and FE uniaxial stress-strain curves

$$\sigma_f(p, \dot{p}, \xi) = \sigma_Y \left\{ 1 + \operatorname{asinh} \left[\left(\frac{\dot{p}}{b} \right)^{1/m} \right] \right\} + \frac{H}{R_d} [1 - \exp(-R_d p)]$$

Parameter	Symbol	Value	Units
Quasi-static Yield Stress	σ_y	253.8	MPa
Hardening Variable	H	2538	MPa
Dynamic Recovery	R_d	2.110	--
Rate-Dependent Coefficient	b	4.728	s^{-1}
Rate-Dependent Exponent	m	9.229	--



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Virtual Fields Method is a powerful inverse technique.

Principle of Virtual Power

$$\underbrace{\int_{V_o} ((\det \mathbf{F}) \boldsymbol{\sigma} \mathbf{F}^{-T}) : \dot{\mathbf{F}}^* dV}_{\text{Internal Power, } P_{int}} = \underbrace{\mathbf{f} \cdot \overline{\mathbf{v}}^*}_{\text{External Power, } P_{ext}}$$

σ	Cauchy Stress
F	Deformation Gradient
f	Resultant Load
V_o	Sample Volume (Reference)
\mathbf{v}^*	Virtual Velocity
$\dot{\mathbf{F}}^*$	Virtual Velocity Gradient

Material Identification Procedure

1. Select material model and specimen geometry
2. Measure specimen deformation during loading
3. Calculate stress with initial guess of model parameters
4. Select one or more kinematically-admissible virtual velocity fields
5. Compute internal and external power
6. Compute cost function: $\Phi = \sum_{\text{time}} [P_{int} - P_{ext}]^2$
7. Iterate on model parameters until cost function is minimized

Pierron and Grédiac (2012) *The Virtual Fields Method*. Springer.
Rossie, Pierron, Štamborská (2016) *Int. J. Solids Struct.*
Kramer and Scherzinger (2014) SAND2014-17871

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σ Cauchy Stress
 F Deformation Gradient
 f Resultant Load

VFM utilizes
heterogeneous calibration data
and requires fewer tests than
traditional calibration techniques.

Material

- 1.
- 2.
- 3.
- 4.

5. Compute cost function

$$\Psi = \sum_{\text{time}} [P_{\text{int}} - P_{\text{ext}}]^2$$

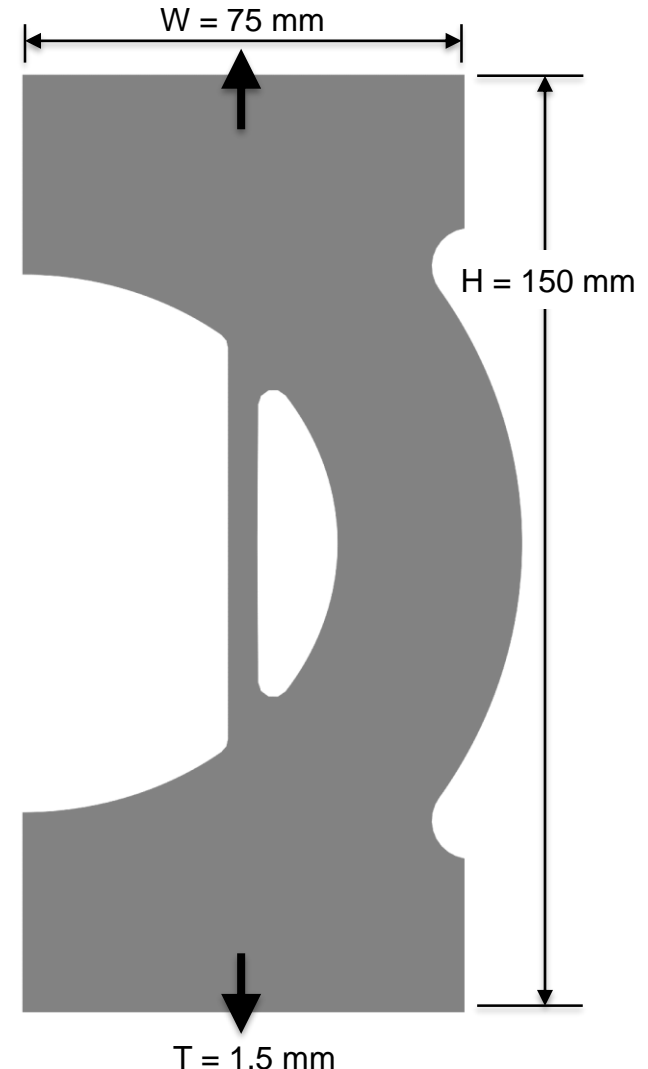
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Kramer and Scherzinger (2014) SAND2014-17871

Complex specimen geometry is available when using full-field diagnostics.

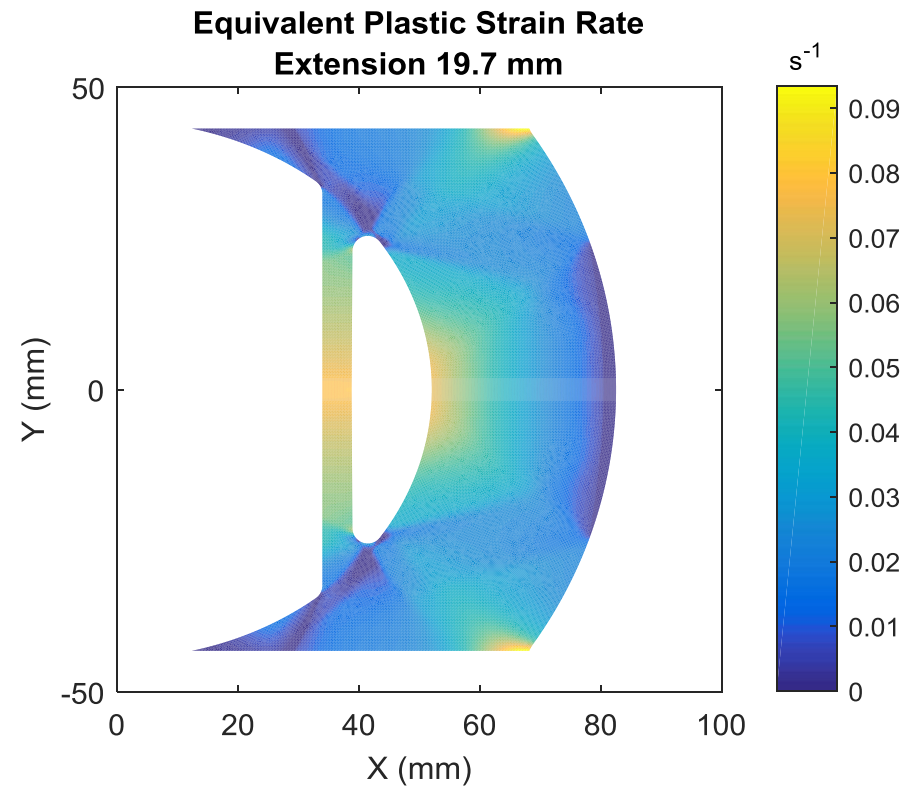
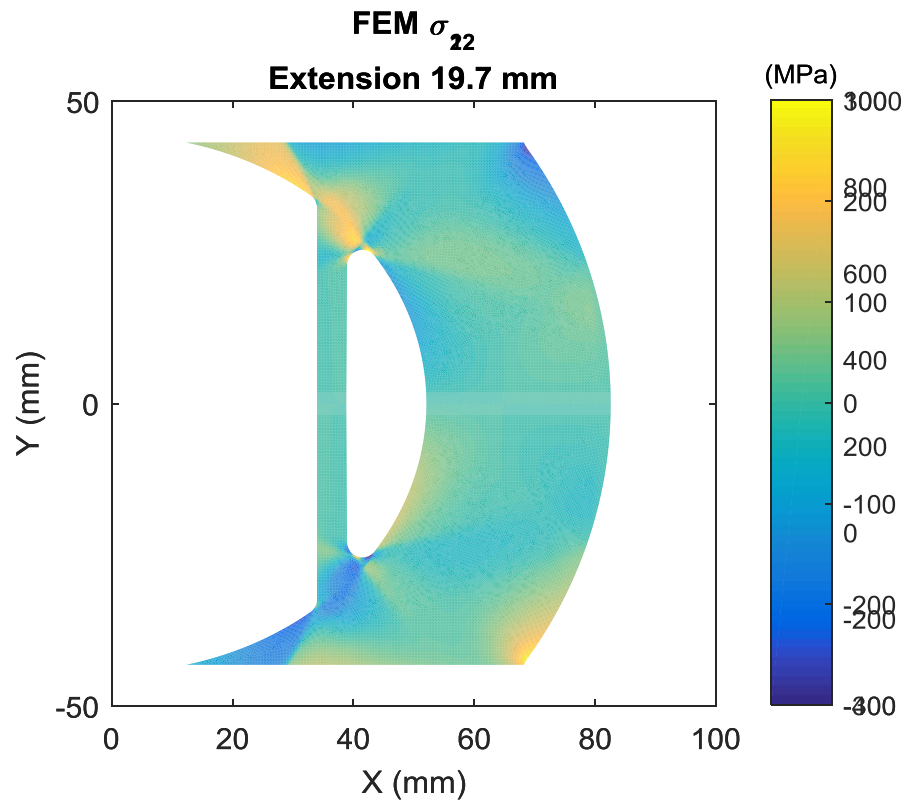
Design Criteria

- Objective:
 - Maximize strain/stress heterogeneity
 - Maximize range of strain rates
- Constraints:
 - Minimize large gradients near sample edges
 - Uniaxial loading
 - Planar sample

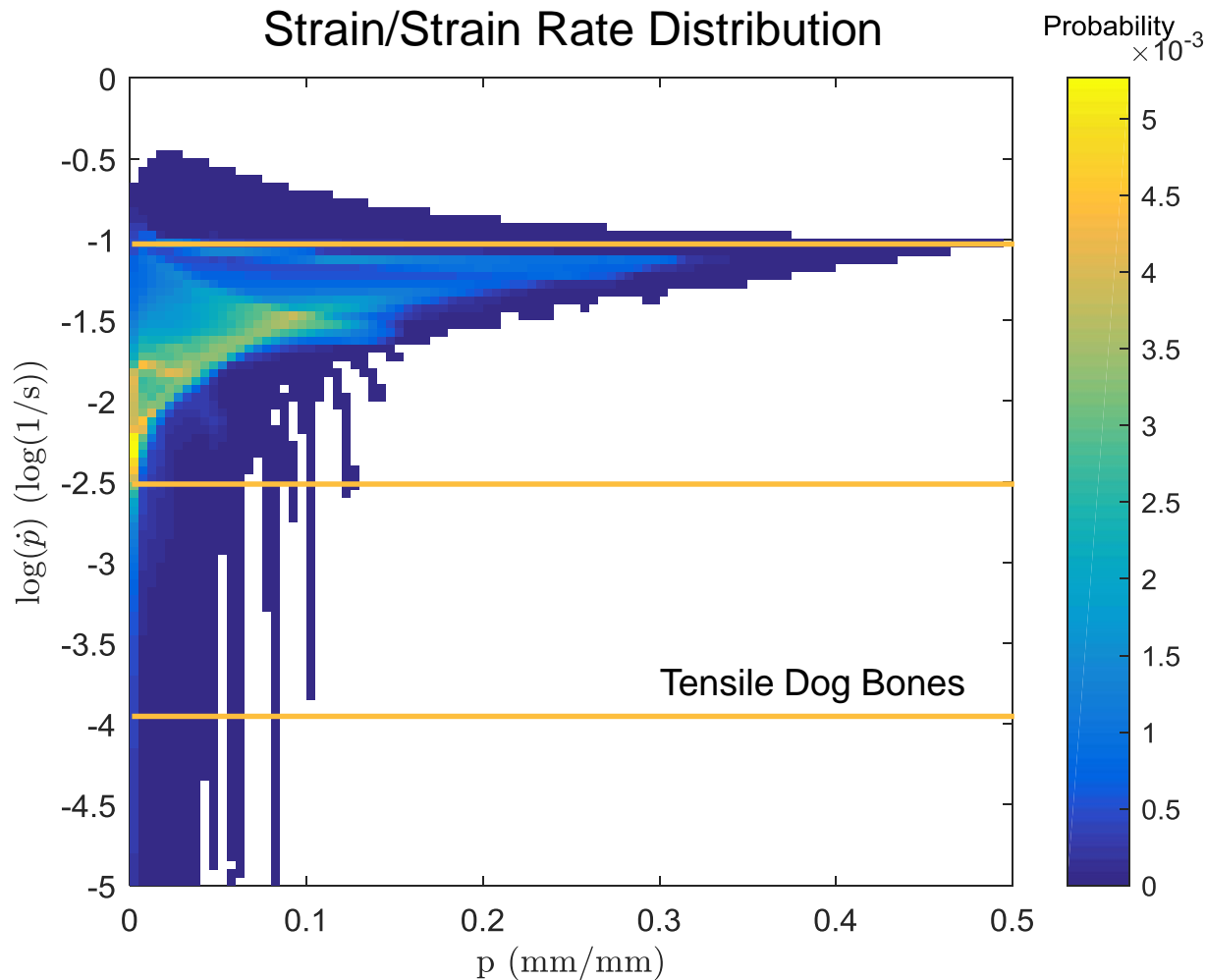


Complex specimen geometry induces stress and strain rate **heterogeneity** in sample.

Predicted Results from FEM Simulation

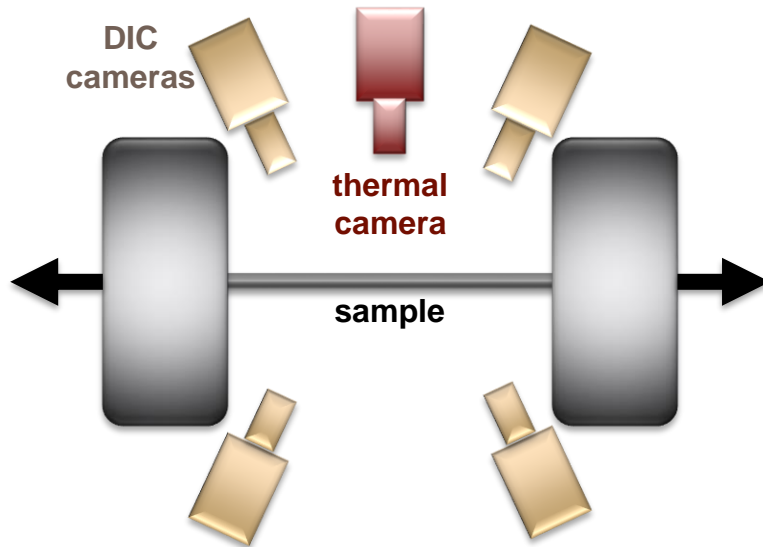


Complex specimen geometry induces stress and strain rate **heterogeneity** in sample.



Specimen deformation, temperature and applied load are measured **experimentally**.

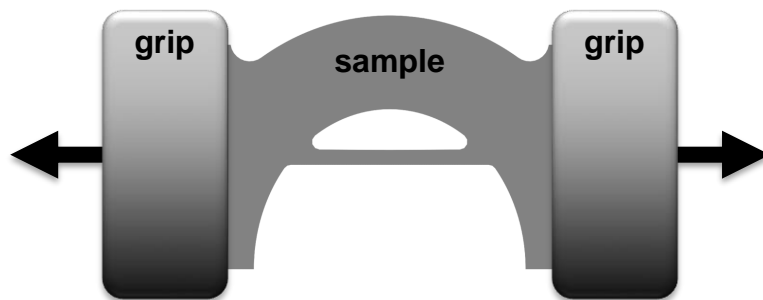
Top View



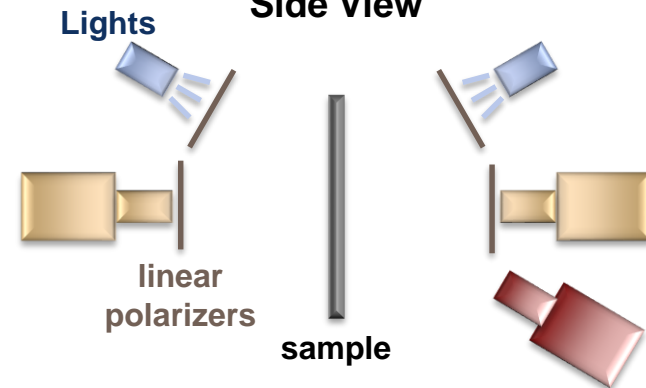
Key Features

- Dual actuator load frame
- Stereo DIC on both sides of specimen
- Rigid camera mounts
- Thermal camera on one side of specimen
- Cross-polarized light

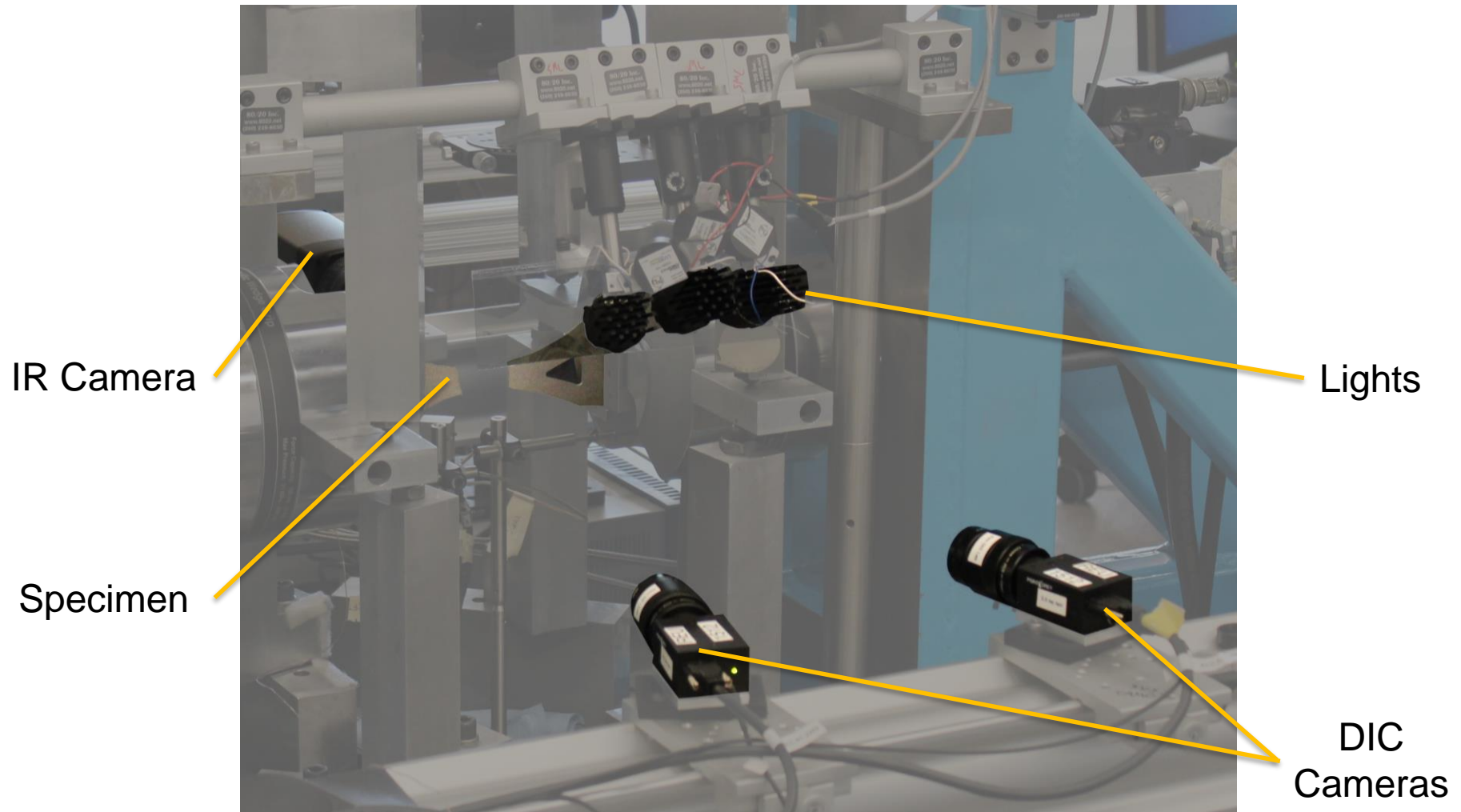
Front View



Side View



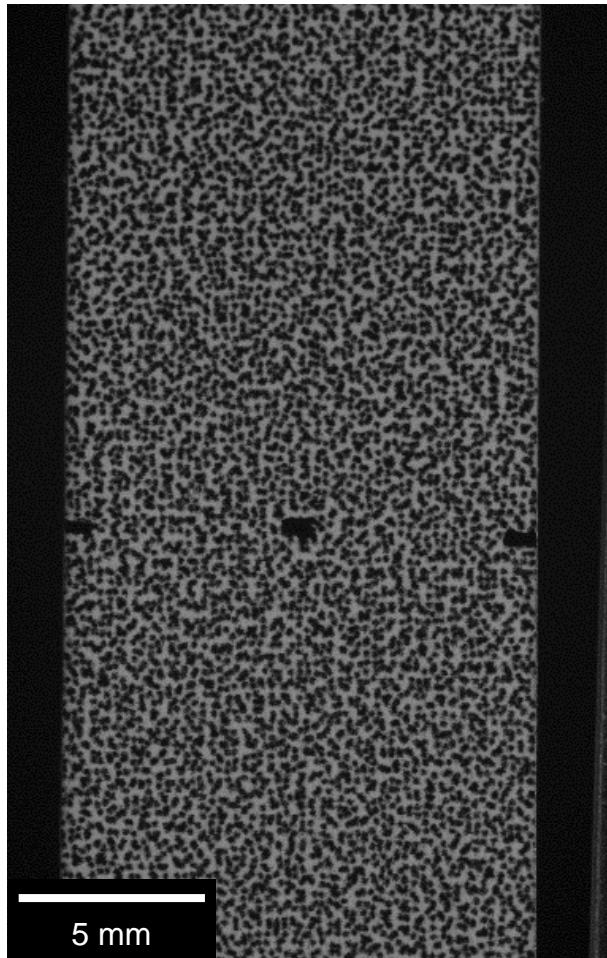
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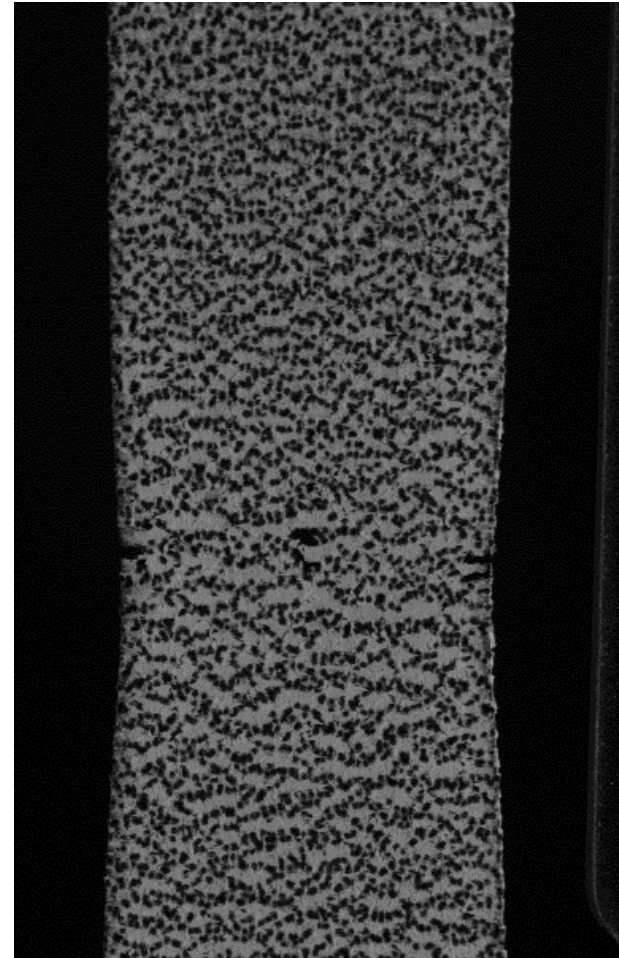
Standard speckling techniques fail at high strain.

Speckle Pattern 1: White base paint with black speckles

Undeformed Specimen



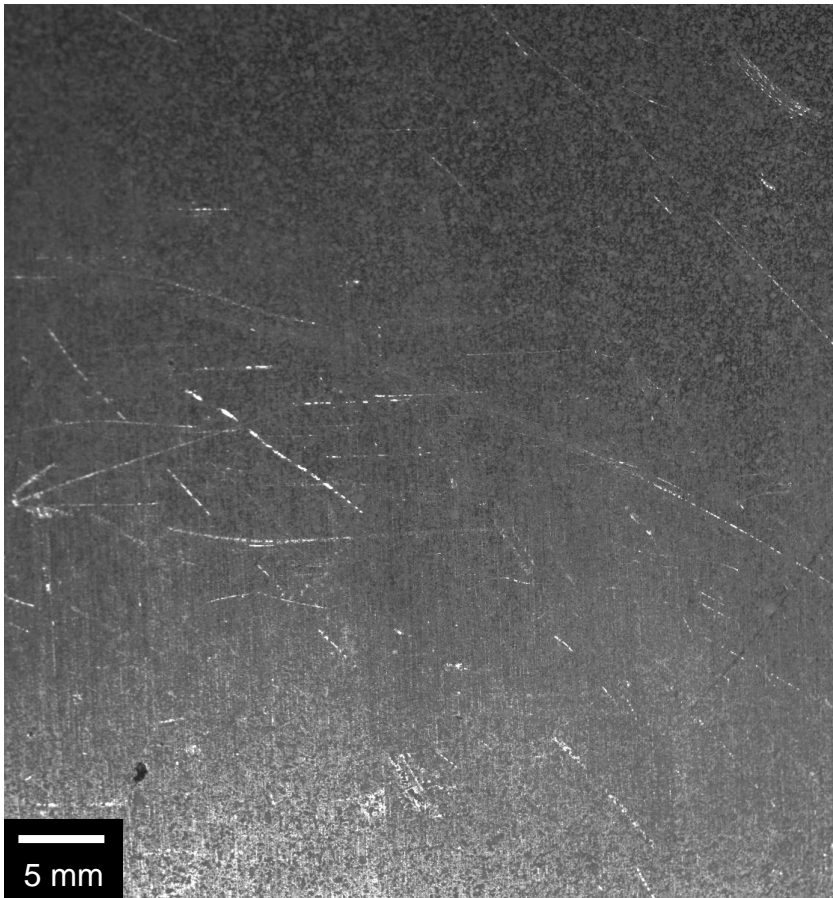
Deformed Specimen



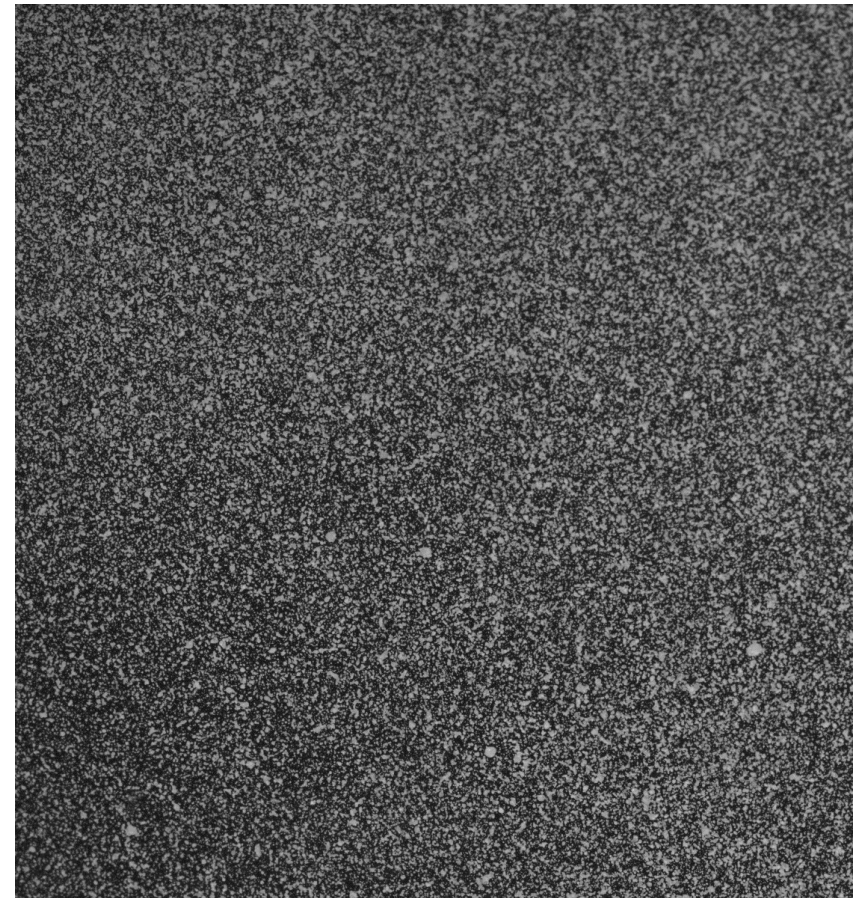
Cross-polarized light creates a robust speckle pattern.

Speckle Pattern 2: White speckles on bare metal

Unpolarized Light



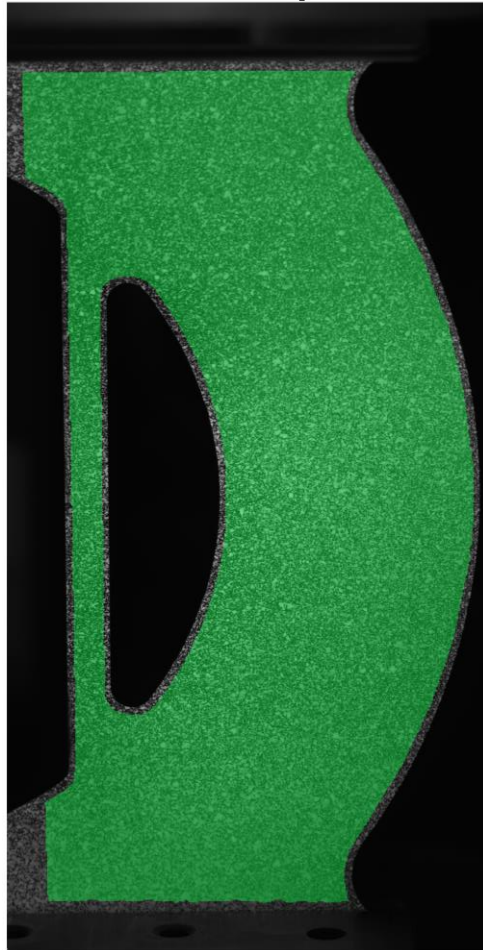
Cross-Polarized Light



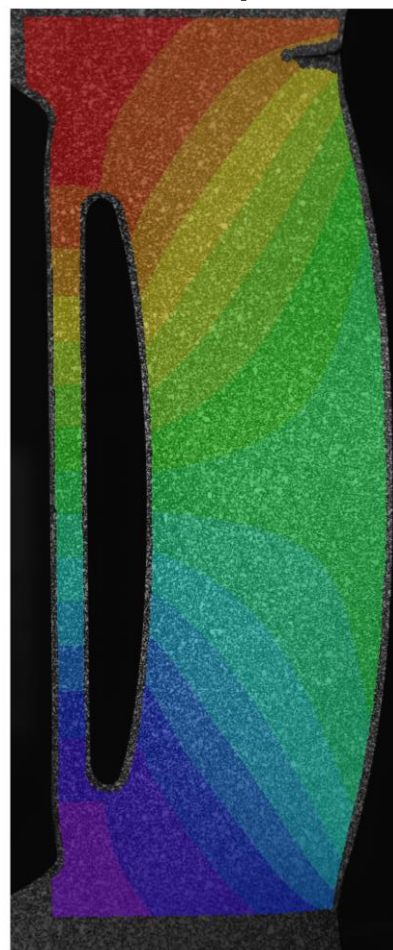
W. LePage, S. Daly, J. Shaw (2016) *Exp. Mech.*

Full-field displacements are measured using DIC.

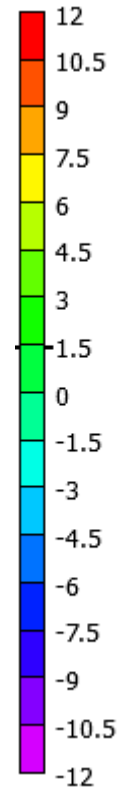
Undeformed Specimen



Deformed Specimen

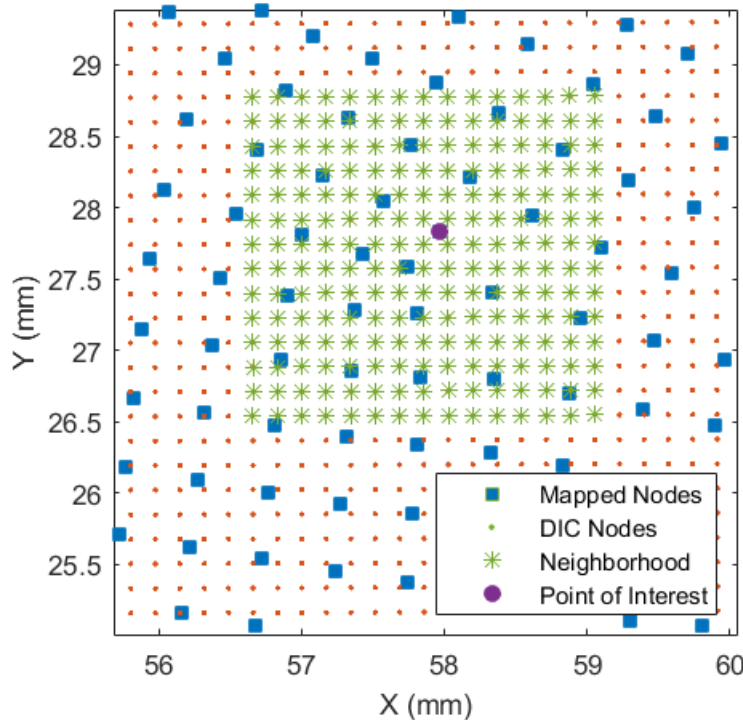


V (mm)



Parameter	Value
Camera	2.3 MP Grasshopper
Lens	35 mm Edmund Optics
Stereo Angle	~ 20°
Field of View	~ 100 mm
Image Scale	~ 17 px/mm
Frame Rate	85 Hz
Software	Vic3D
Subset Size	23 x 23 px
Step Size	5 px
Subset Shape Function	Affine
Displacement Noise Floor	~ 0.01 mm

Kinematics calculated from a least-squares polynomial fit to displacement data.



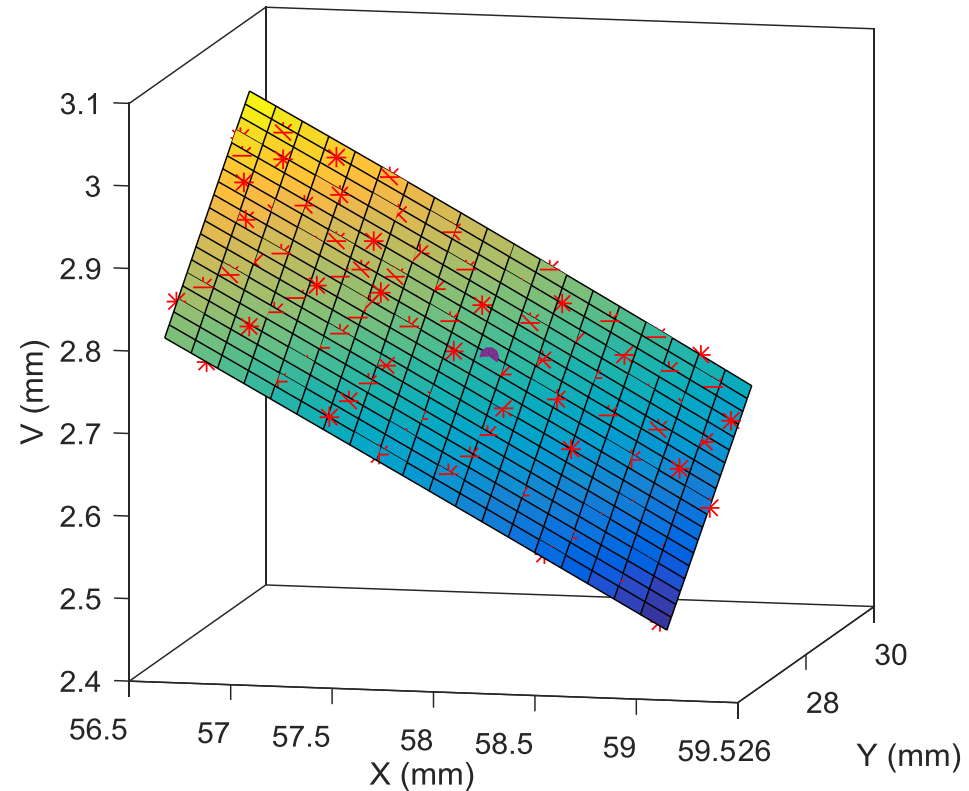
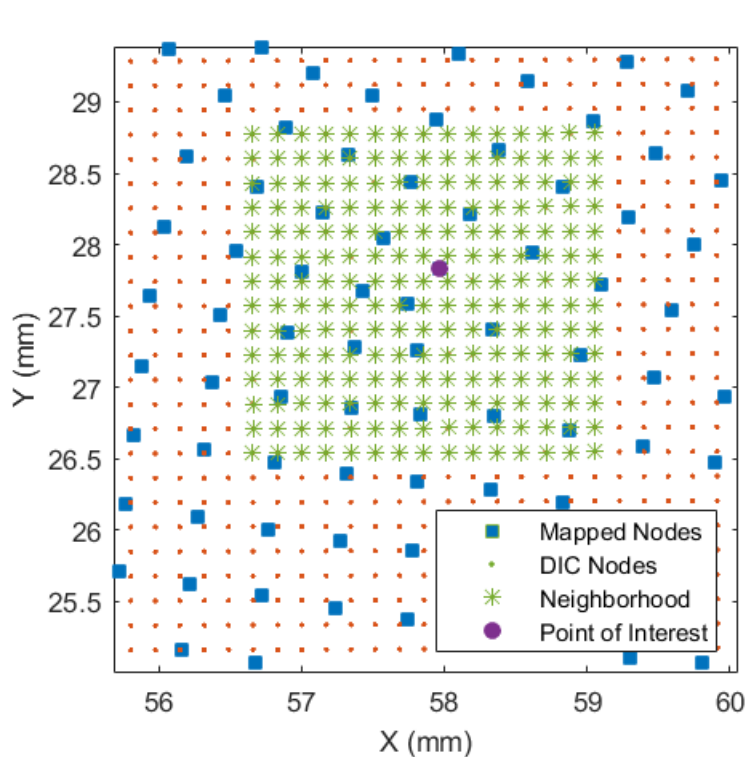
$$u_i = C_1 + C_2x + C_3y + C_4x^2 + C_5y^2 + C_6xy + C_7x^3 + C_8y^3 + C_9x^2y + C_{10}xy^2$$

$$\frac{\partial u_i}{\partial x} = C_2 + 2C_4x + C_6y + 3C_7x^2 + 2C_9xy + C_{10}y^2$$

$$\frac{\partial u_i}{\partial y} = C_3 + 2C_5y + C_6x + 3C_8y^2 + C_9x^2 + 2C_{10}xy$$

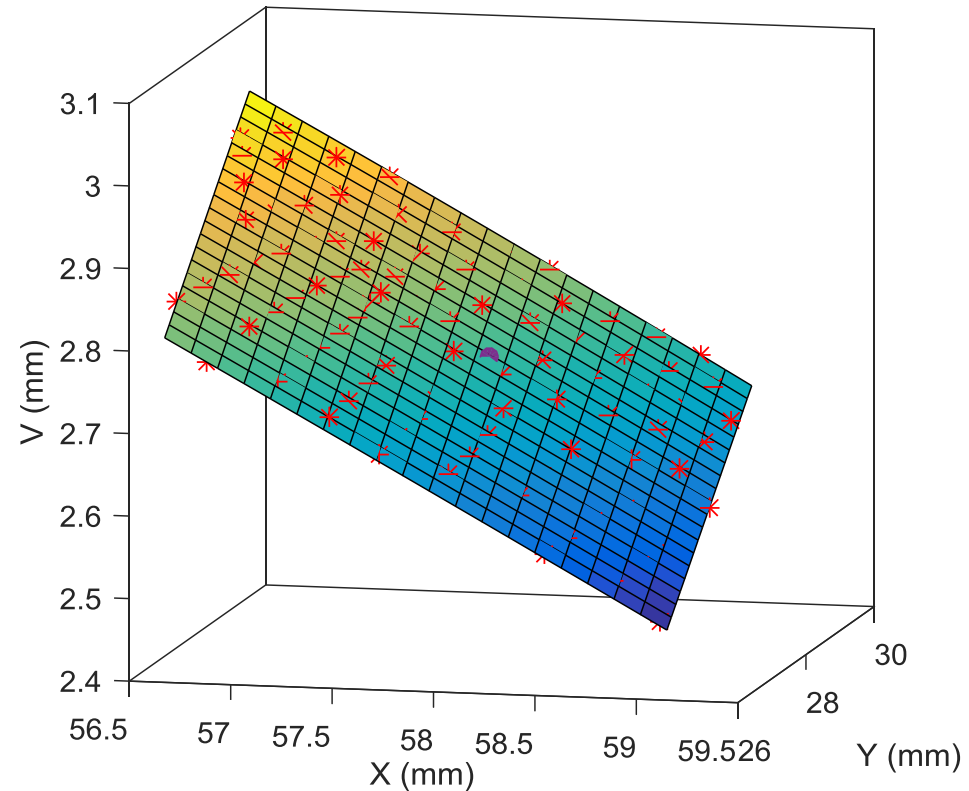
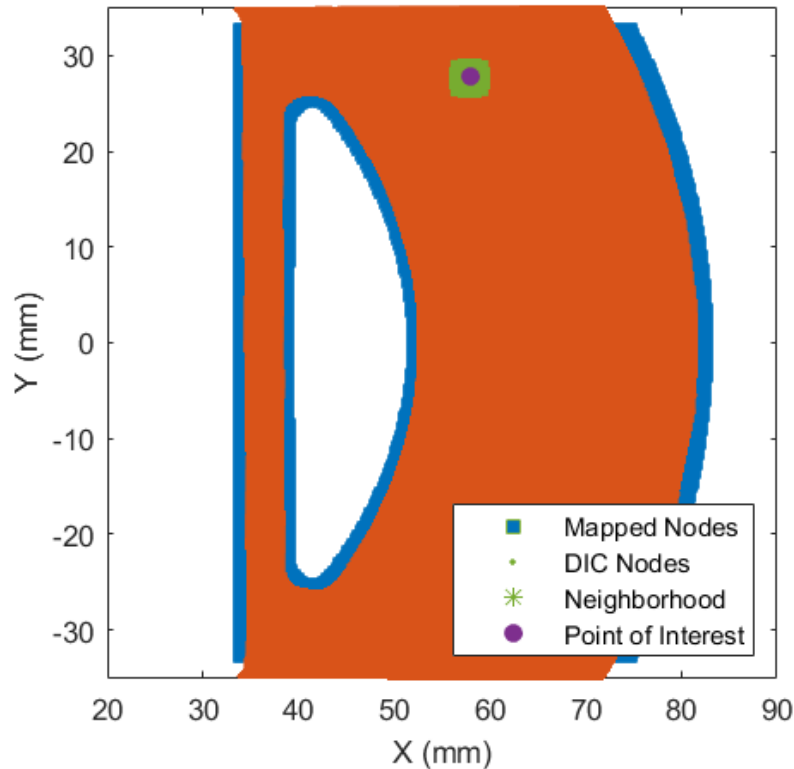
- 2D polynomial surface fitted to neighborhood of displacement nodes.
- Deformation gradient obtained directly from coefficients of polynomial fit.

Kinematics calculated from a least-squares polynomial fit to displacement data.



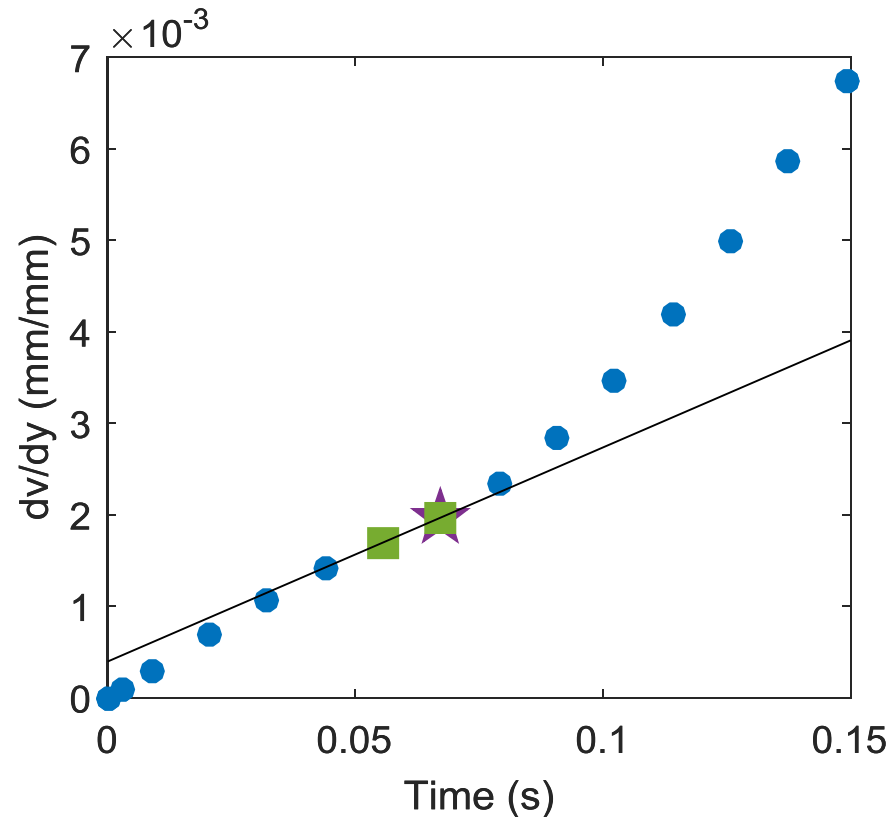
- 2D polynomial surface fitted to neighborhood of displacement nodes.
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- Spatially filters noise in DIC displacements.

Kinematics calculated from a least-squares polynomial fit to displacement data.



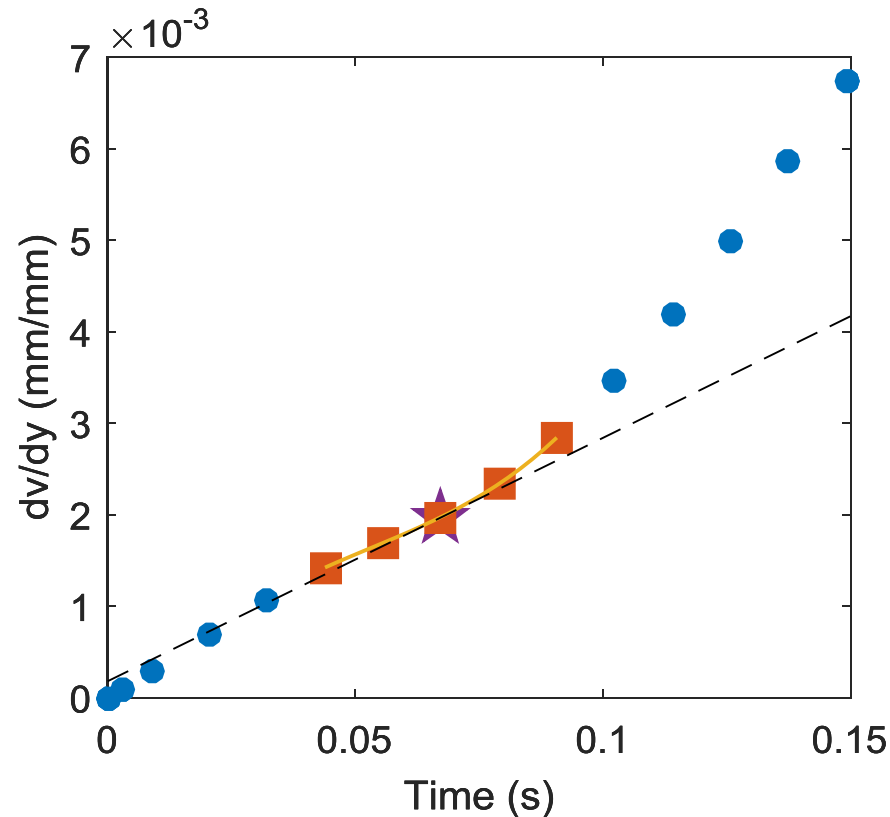
- 2D polynomial surface fitted to neighborhood of displacement nodes.
- Deformation gradient obtained directly from coefficients of polynomial fit.
- Spatially filters noise in DIC displacements.
- Extrapolate data to sample edges.

Rate of deformation is approximated using finite differences.



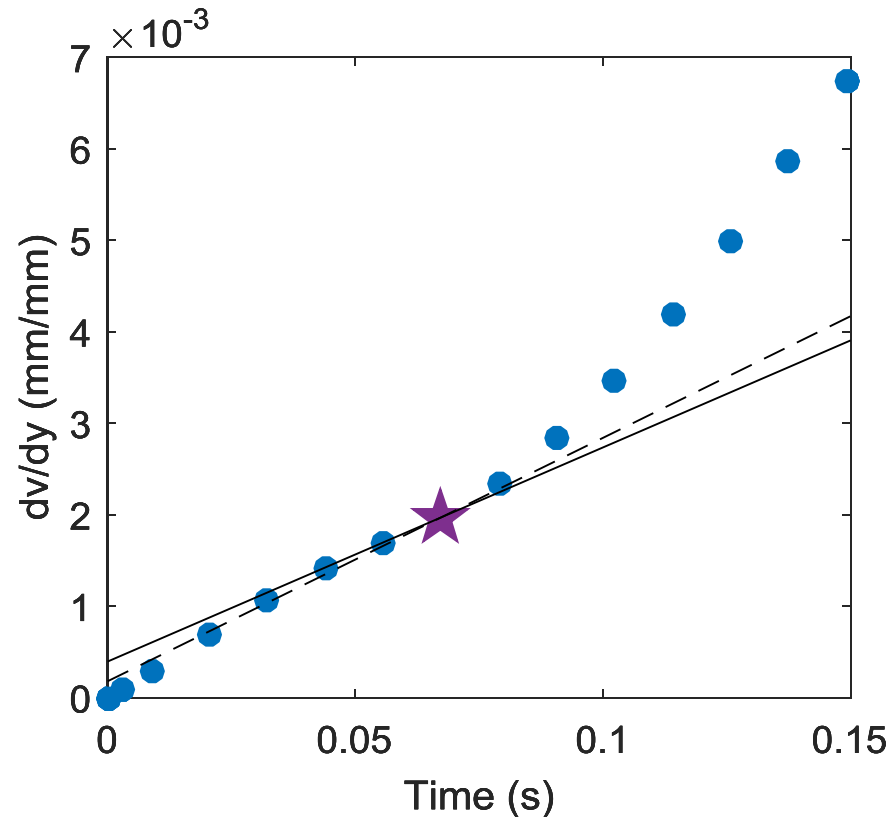
- Rate of deformation can be calculated via:
 - Backward difference

Rate of deformation is approximated using finite differences.



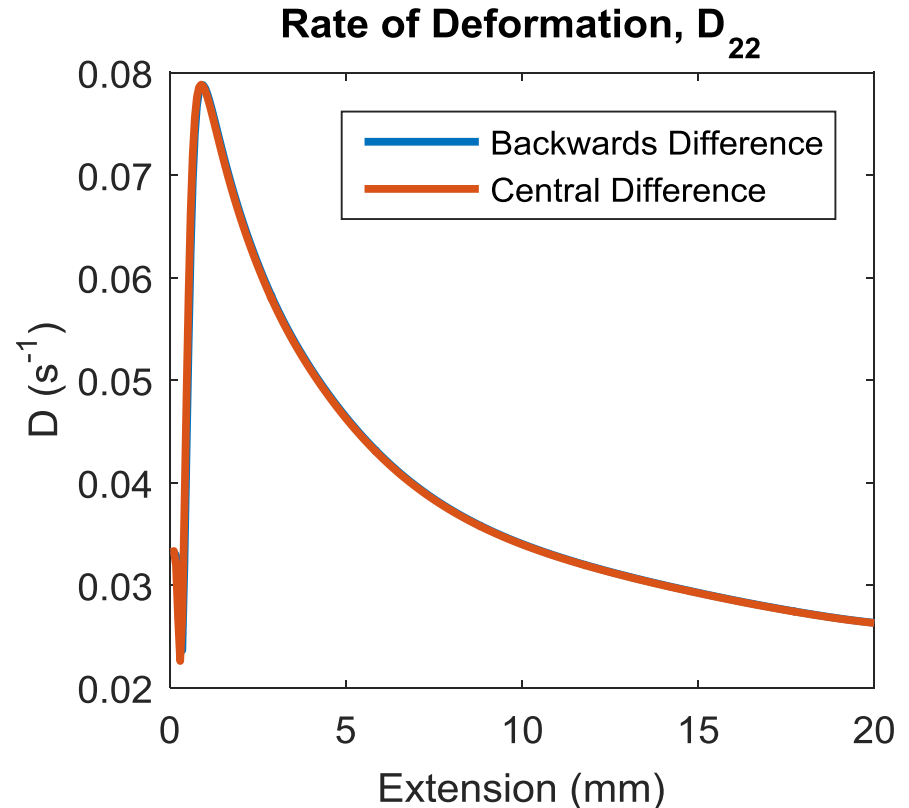
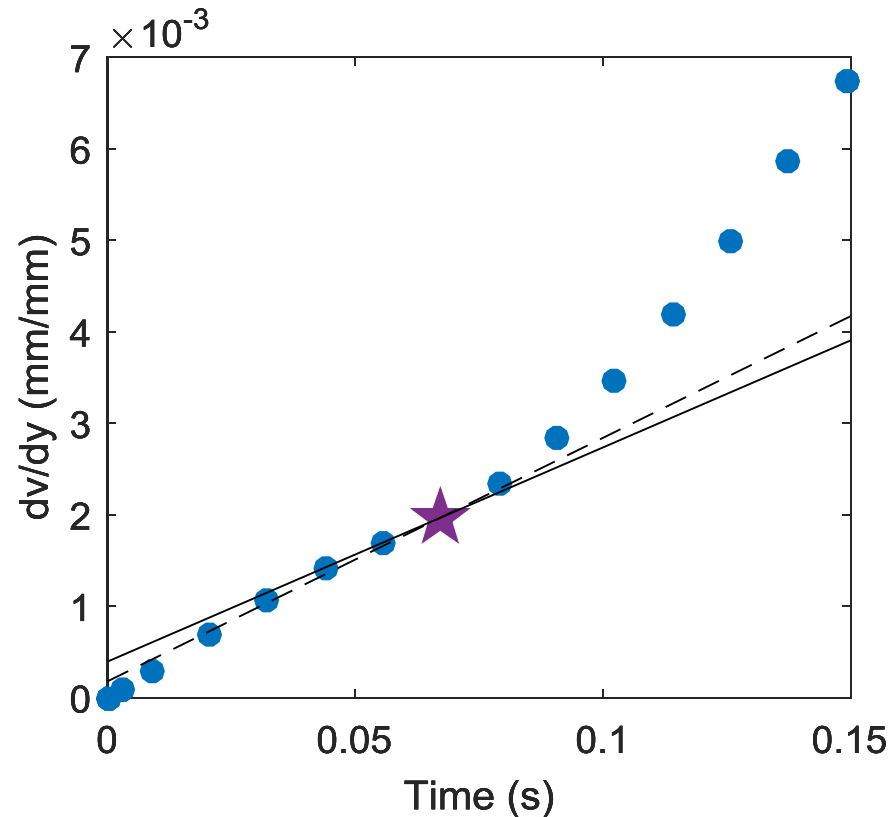
- Rate of deformation can be calculated via:
 - Backward difference
 - Central difference

Rate of deformation is approximated using finite differences.



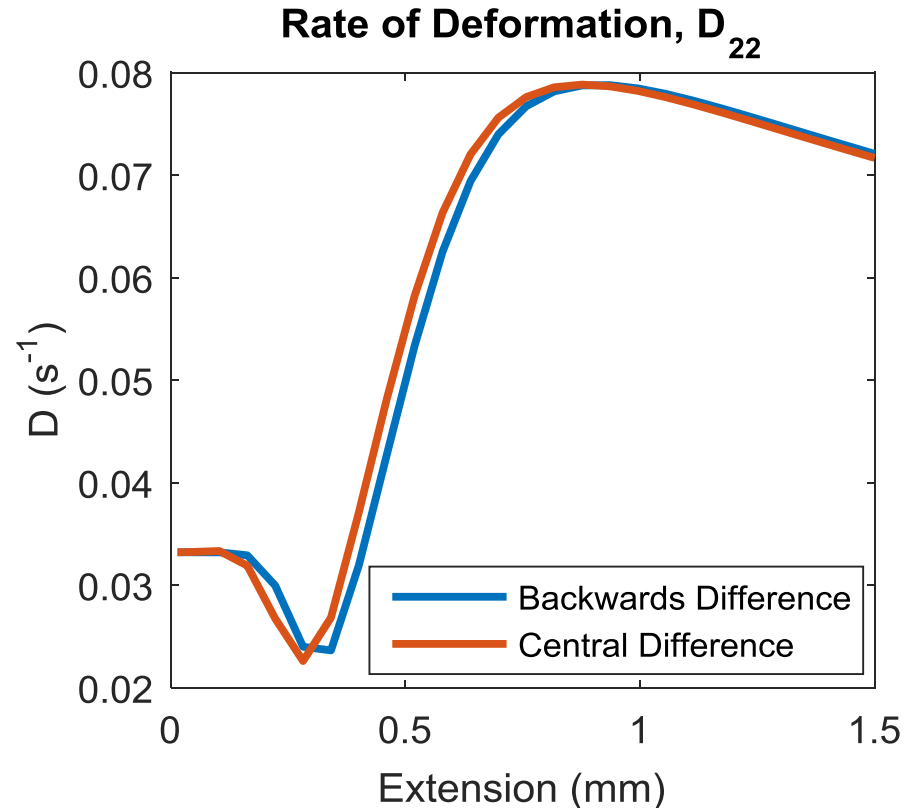
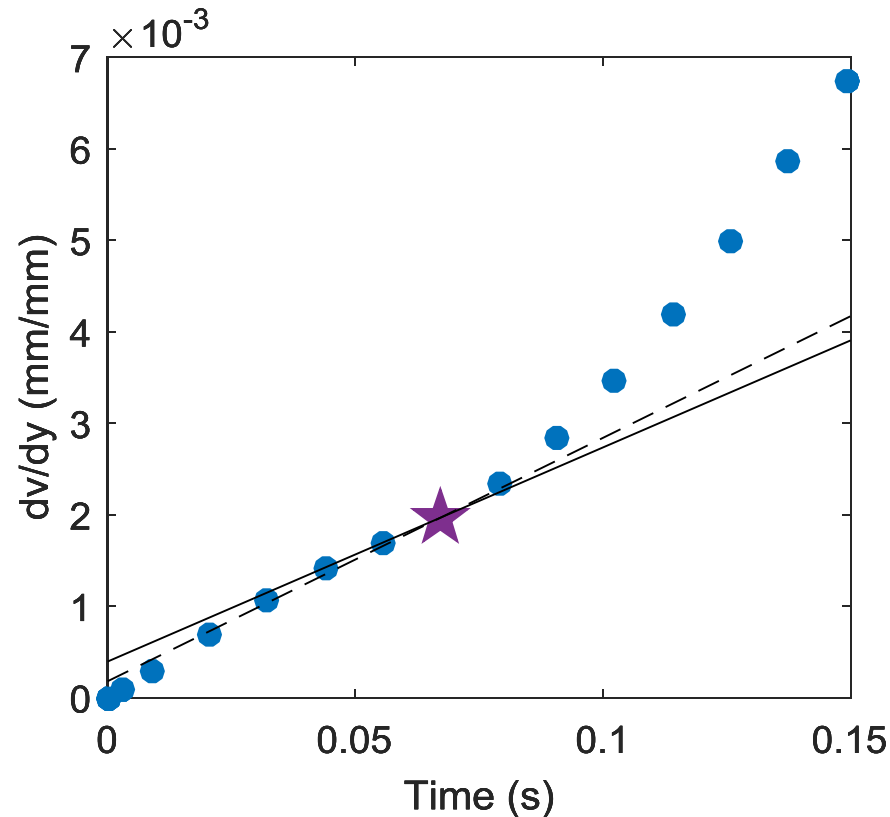
- Rate of deformation can be calculated via:
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 - Central difference

Rate of deformation is approximated using finite differences.



- Rate of deformation can be calculated via:
 - Backward difference
 - Central difference

Rate of deformation is approximated using finite differences.



- Rate of deformation can be calculated via:
 - Backward difference
 - Central difference
- Significant difference near yield

Stresses are **reconstructed** using the radial return method.

- Non-trivial, but direct, computation

- Material Model

- Flow stress:

$$\sigma_f = g_0(\xi)$$

- Von Mises Flow Criterion

- Equivalent Stress:

$$\bar{\sigma} = \sqrt{\frac{3}{2} s:s} \quad \left(s = \sigma - \frac{1}{3} \text{tr}(\sigma) I \right)$$

- Equivalent Plastic Strain Rate:

$$\dot{p} = \sqrt{\frac{2}{3} \dot{\epsilon}^p : \dot{\epsilon}^p}$$

- Flow Criterion:

$$f_c = \bar{\sigma} - \sigma_f = 0$$

- Cauchy Stress:

$$\sigma = g_1(\sigma_f(\xi), \dot{p})$$

Cost function is the balance between internal and external virtual work.

- Kinematically-admissible virtual fields
 - Virtual Velocity: $v_x^* = \cos\left(\frac{\pi y}{H}\right); v_y^* = \frac{2y+H}{2H}$
 - Kim et al (2014) *Exp Mech*
 - Virtual Velocity Gradient: $\dot{\mathbf{F}}^* = \begin{bmatrix} \frac{\partial v_x^*}{\partial x} & \frac{\partial v_x^*}{\partial y} \\ \frac{\partial v_y^*}{\partial x} & \frac{\partial v_y^*}{\partial y} \end{bmatrix}$
- Internal and external virtual work
 - $W_{int} = \int \int_{V_0} ((\det \mathbf{F}) \boldsymbol{\sigma}(\boldsymbol{\xi}) \mathbf{F}^{-T}) : \dot{\mathbf{F}}^* dV dt$
 - $W_{ext} = \int \mathbf{f} \cdot \overline{\mathbf{v}}^* dt$
- Cost function
 - $\Phi = (W_{int}(\boldsymbol{\xi}) - W_{ext})^2$

Parameters must be **scaled** for a more tractable optimization.

Bounds: Chosen such that $\sim 50 < \sigma_f < \sim 3000$ MPa over $p = [0,1]$ and $\dot{p} = [10^{-5}, 10^5]$

	Lower Bound, ξ_L	Upper Bound, ξ_H	Scaling	Parameter scaling \rightarrow			Lower Bound, ξ_L	Upper Bound, ξ_H	Scaling
σ_Y	50	750	Linear	$\hat{\xi} = \frac{\xi - \xi_L}{\xi_H - \xi_L}$ $\hat{\xi} = \frac{\log(\xi) - \log(\xi_L)}{\log(\xi_H) - \log(\xi_L)}$		$\hat{\sigma}_y$	0	1	Linear
H	50	5000	Linear			\hat{H}	0	1	Linear
R_d	0.1	10	Log			\hat{R}_d	0	1	Linear
b	10^{-5}	10^5	Log			\hat{b}	0	1	Linear
m	1	20	Log			\hat{m}	0	1	Linear

Initial guess: Latin Hyper Cube sampling

	Run 1	Run 2	Run 3	Run 4	Run 5	Run 6
$\hat{\sigma}_y$	0.2911	0.6644	0.5895	0.0398	0.2643	0.8108
\hat{H}	0.5025	0.1817	0.4183	0.2980	0.6770	0.9368
\hat{R}_d	0.6621	0.3845	0.0299	0.9711	0.7259	0.4755
\hat{b}	0.5675	0.0005	0.8965	0.2019	0.7547	0.5204
\hat{m}	0.7418	0.2607	0.7871	0.4505	0.9159	0.0377

Parameters must be **scaled** for a more tractable optimization.

Bounds: Chosen such that $\sim 50 < \sigma_f < \sim 3000$ MPa over $p = [0,1]$ and $\dot{p} = [10^{-5}, 10^5]$

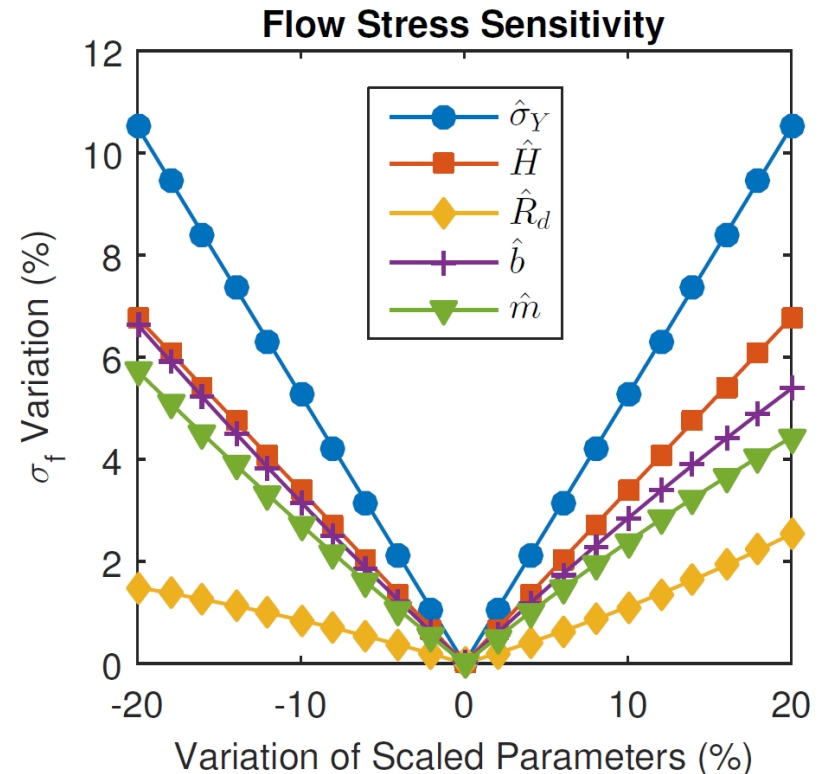
	Lower Bound, ξ_L	Upper Bound, ξ_H	Scaling	Parameter scaling \rightarrow			Lower Bound, ξ_L	Upper Bound, ξ_H	Scaling
σ_Y	50	750	Linear	$\hat{\xi} = \frac{\xi - \xi_L}{\xi_H - \xi_L}$ $\hat{\xi} = \frac{\log(\xi) - \log(\xi_L)}{\log(\xi_H) - \log(\xi_L)}$		$\hat{\sigma}_y$	0	1	Linear
H	50	5000	Linear			\hat{H}	0	1	Linear
R_d	0.1	10	Log			\hat{R}_d	0	1	Linear
b	10^{-5}	10^5	Log			\hat{b}	0	1	Linear
m	1	20	Log			\hat{m}	0	1	Linear

Initial guess: Latin Hyper Cube sampling

	Run 1	Run 2	Run 3	Run 4	Run 5	Run 6
σ_Y	253.8	515.1	462.7	77.86	235.0	617.6
H	2538	949.4	2121	1525	3401	4687
R_d	2.110	0.5875	0.1148	8.754	2.830	0.8933
b	9.229	1.01e-5	9.23e3	1.04e3	352.4	1.600
m	4.728	2.184	10.57	3.856	15.55	1.120

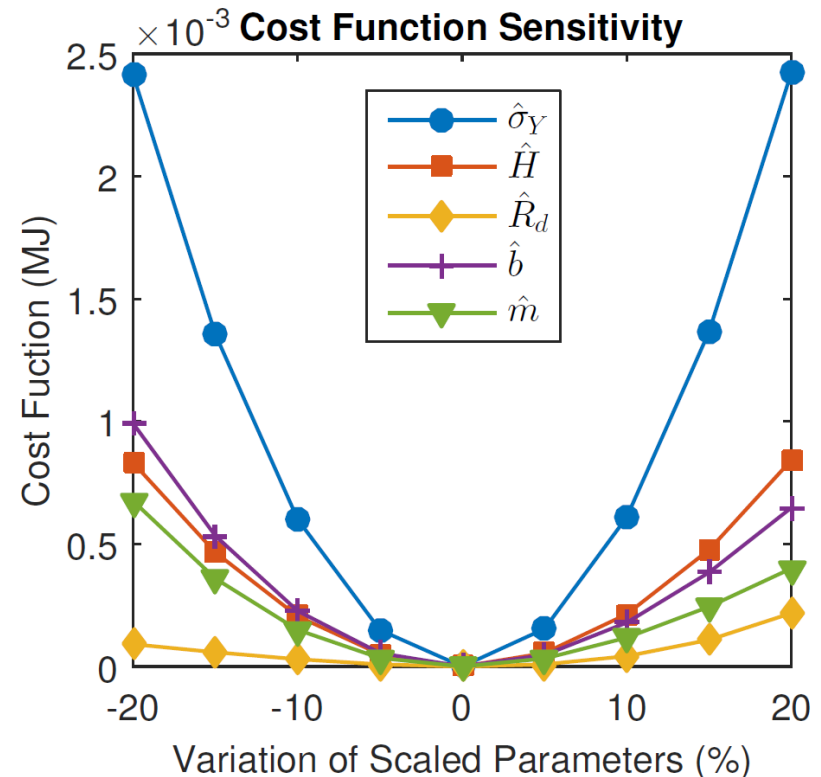
Cost function is **sensitive** to all parameters.

- Sensitivity of flow stress, σ_f
 - $\sigma_f = g_0(\xi)$
 - Function of mathematical form of material model only
 - Parameter scaling required
- Sensitivity of cost function, Φ
 - $\Phi = g_2(W_{int}(\dot{p}, \mathbf{v}^*), W_{ext}(\mathbf{v}^*))$
 - Function of data richness
 - Function of virtual fields

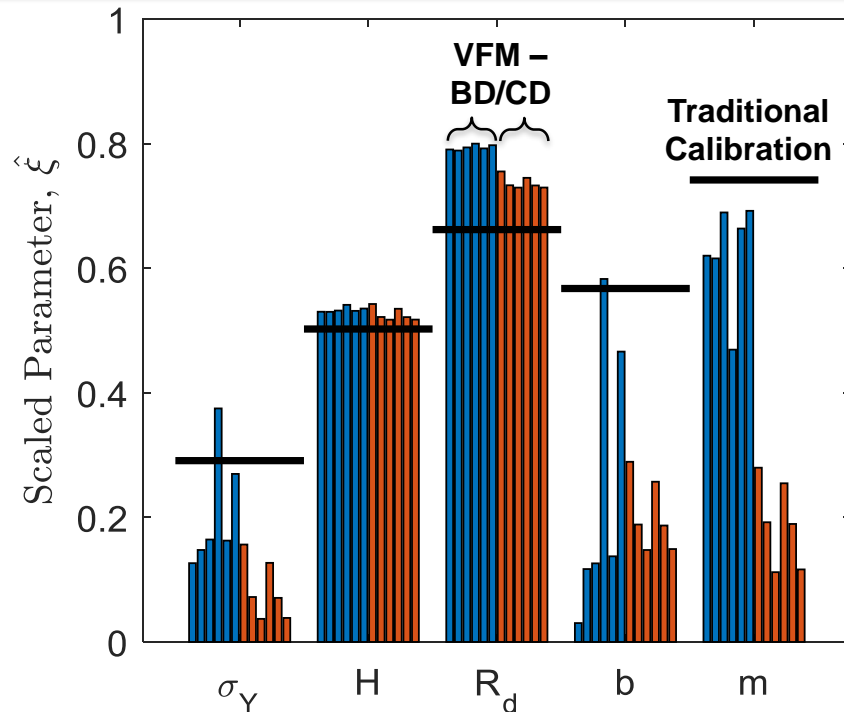


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 - Function of data richness
 - Function of virtual fields



Parameters are **identified** using a non-linear, gradient-based optimizer in Matlab.



$$\sigma_f(p, \dot{p}, \xi) = \sigma_Y \left\{ 1 + \operatorname{asinh} \left[\left(\frac{\dot{p}}{b} \right)^{1/m} \right] \right\} + \frac{H}{R_d} [1 - \exp(-R_d p)]$$

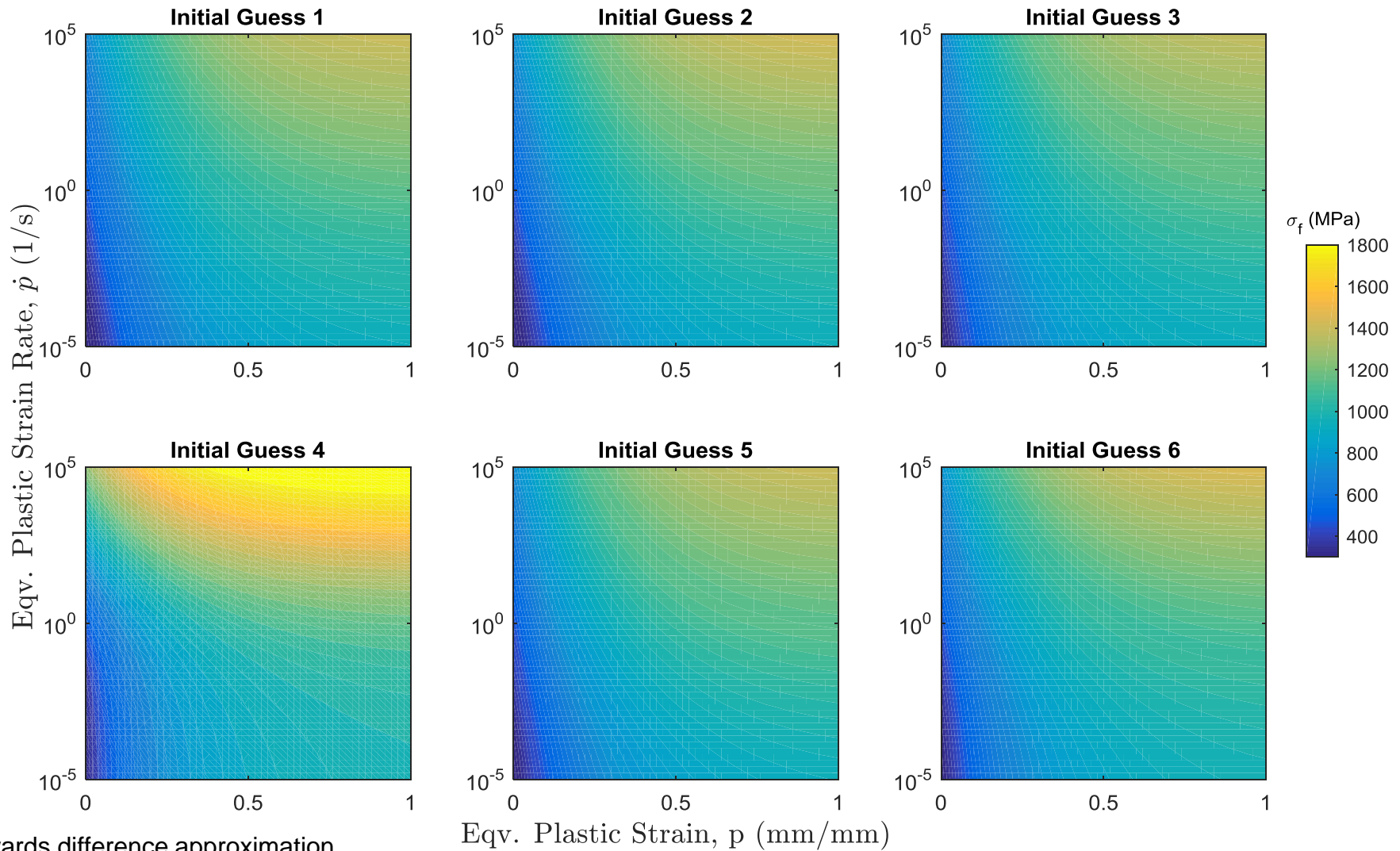
- 12 different parameter sets identified from VFM
 - 2 different approximations for the strain rate
 1. Backwards difference
 2. Central difference
 - 6 different initial guesses
 1. Reference parameters
 2. Latin hypercube sampling (5 sets)

- Hardening parameters (H , R_d) are relatively constant

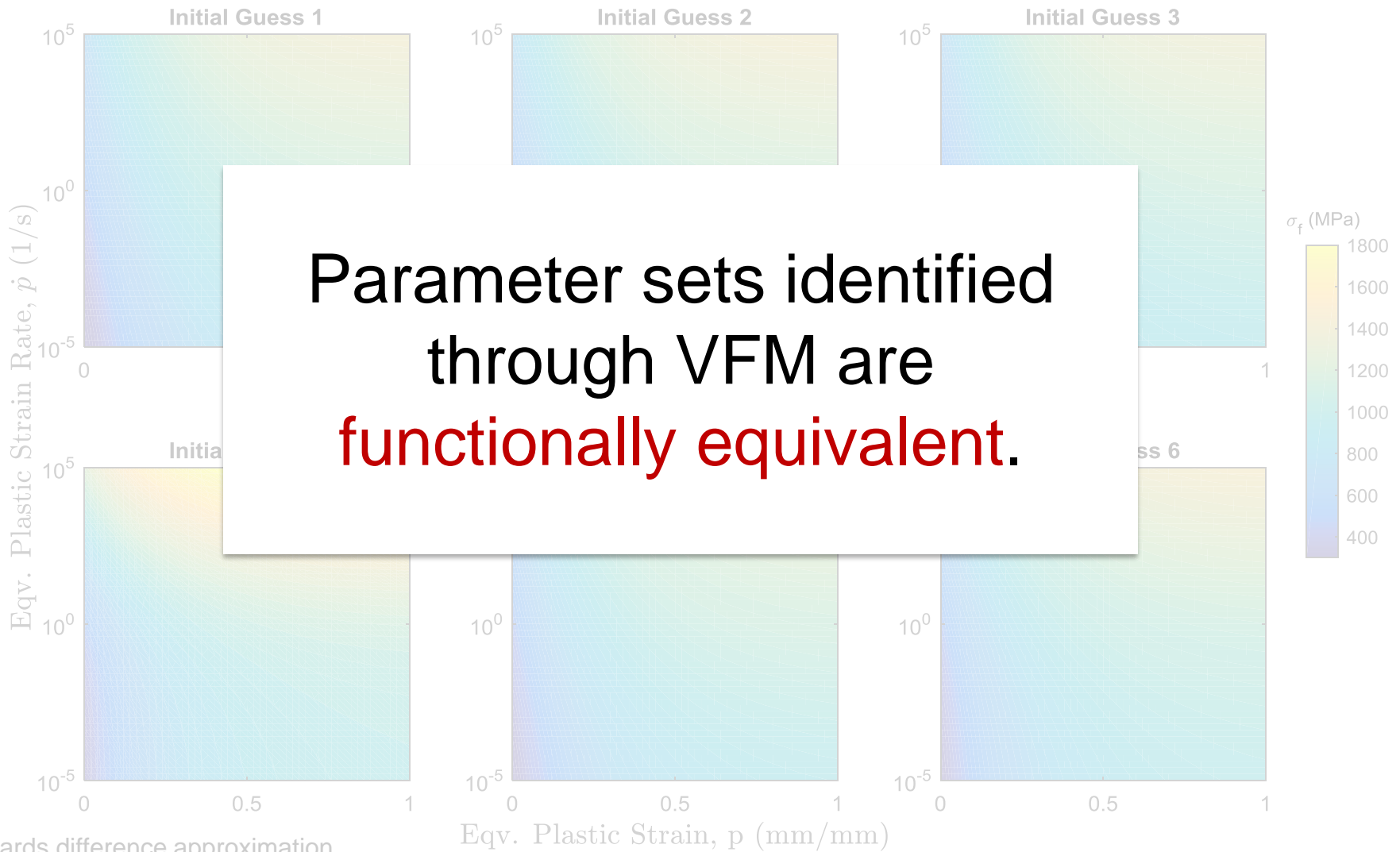
- Strain-rate dependent parameters (σ_Y , b , m) have significant variation.
 - Parameter co-variance!

Parameter	Symbol	Value	Units
Quasi-static Yield Stress	σ_y	253.8	MPa
Hardening Variable	H	2538	MPa
Dynamic Recovery	R_d	2.110	--
Rate-Dependent Coefficient	b	4.728	s^{-1}
Rate-Dependent Exponent	m	9.229	--

The flow stress is **invariant** with respect to the different parameter sets.

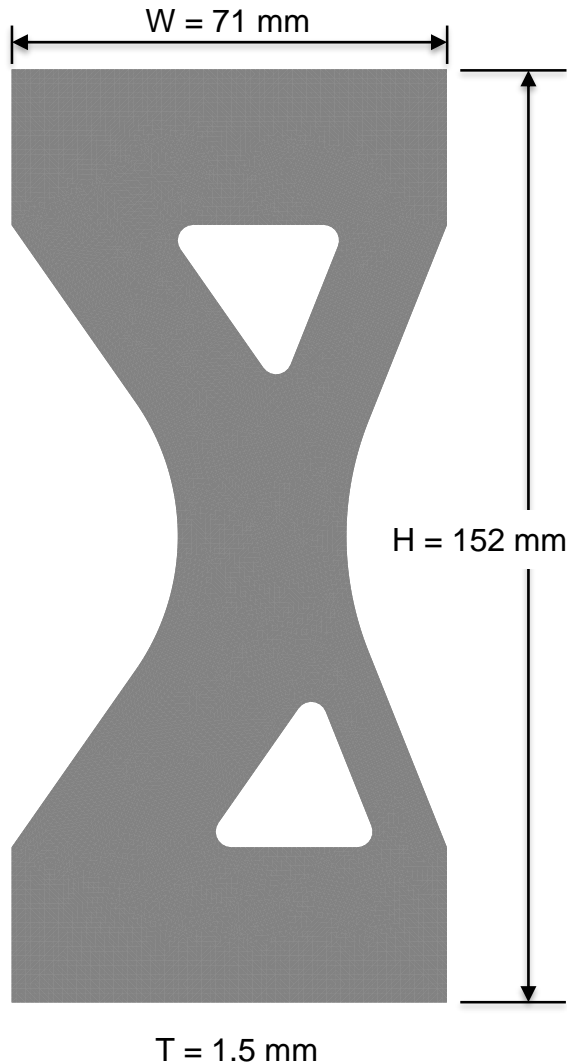


The flow stress is **invariant** with respect to the different parameter sets.



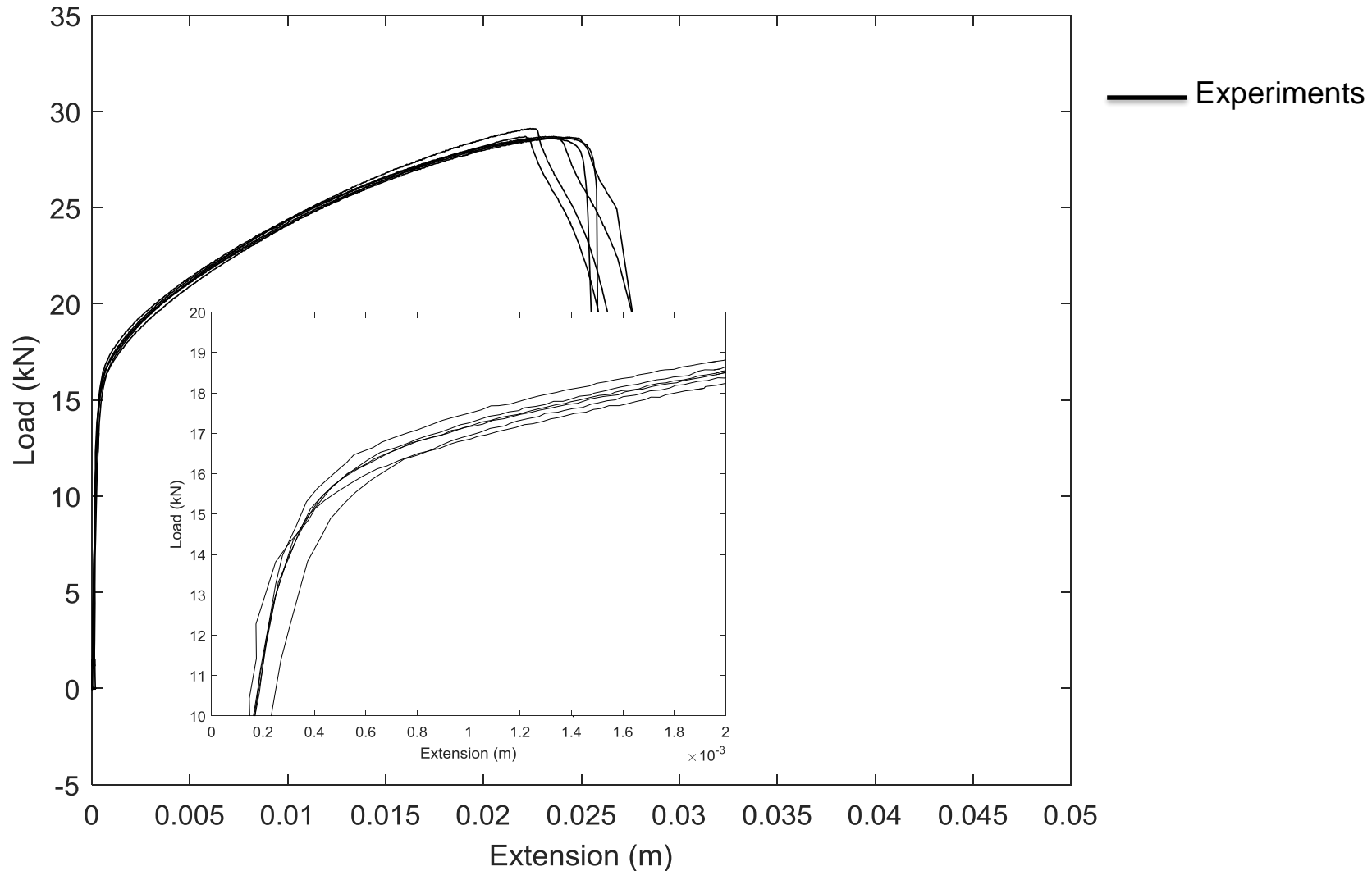
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 - Background
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 - Boundary Conditions
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Validation experiments conducted with an X-specimen.

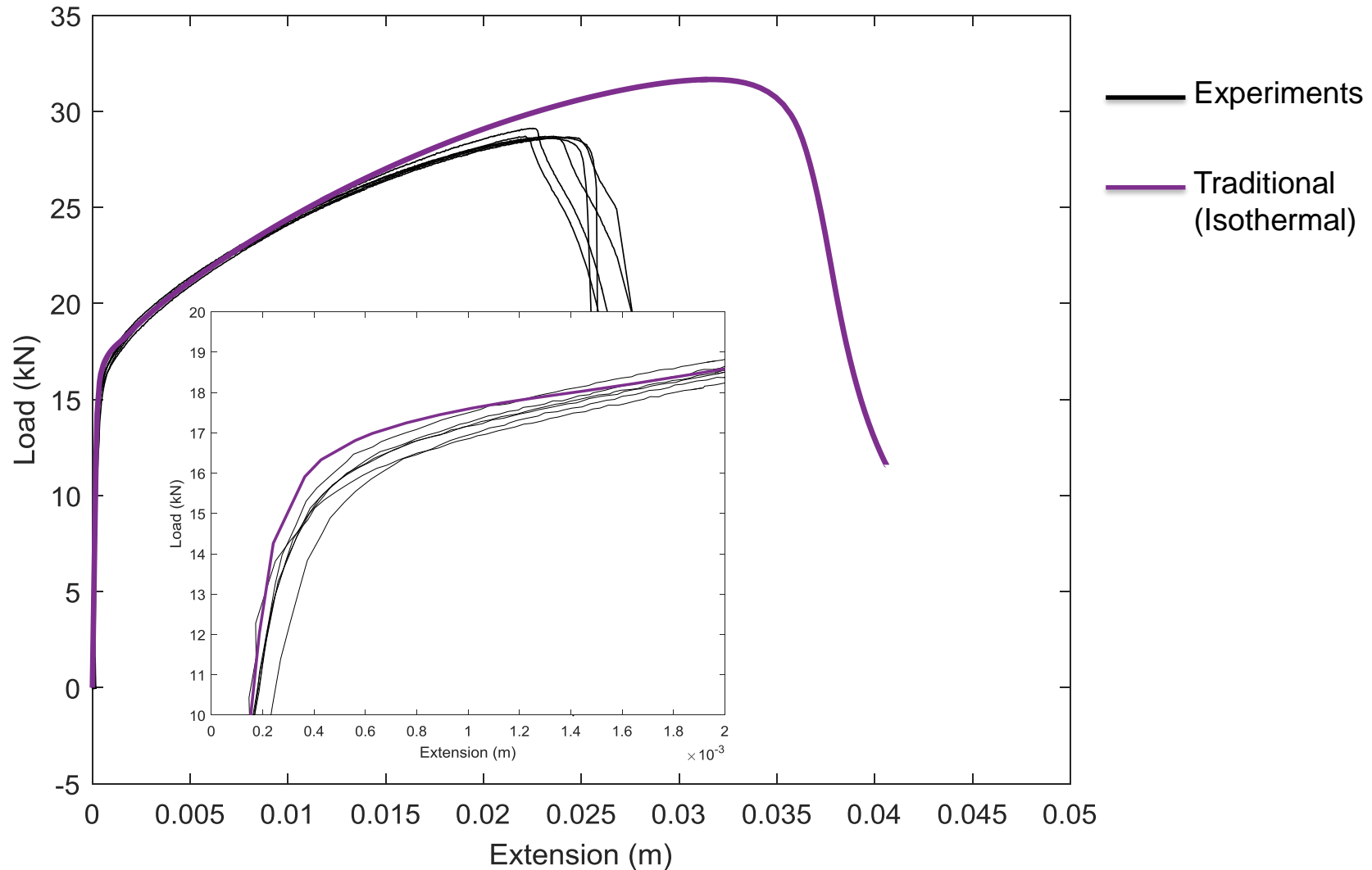


- Experimental DIC data of X-specimen with 6 repeats
- FEA of X-specimen using each of the different parameter sets
- Map FEA and Experimental displacement results to a common grid
- Green-Lagrangian finite strains computed from local polynomial fit
- Strains interpolated onto a common time vector

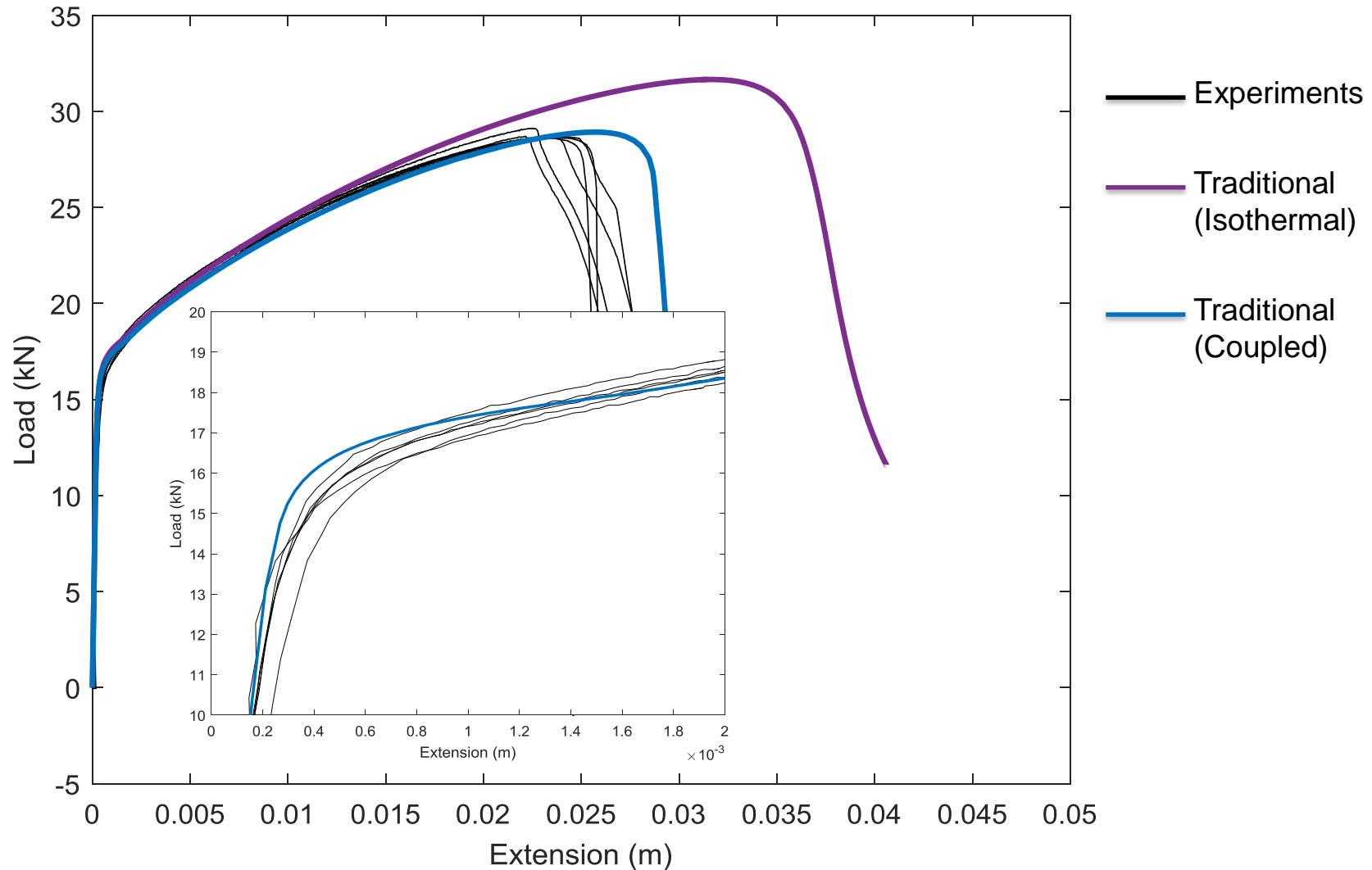
Global data is similar for all model parameter sets.



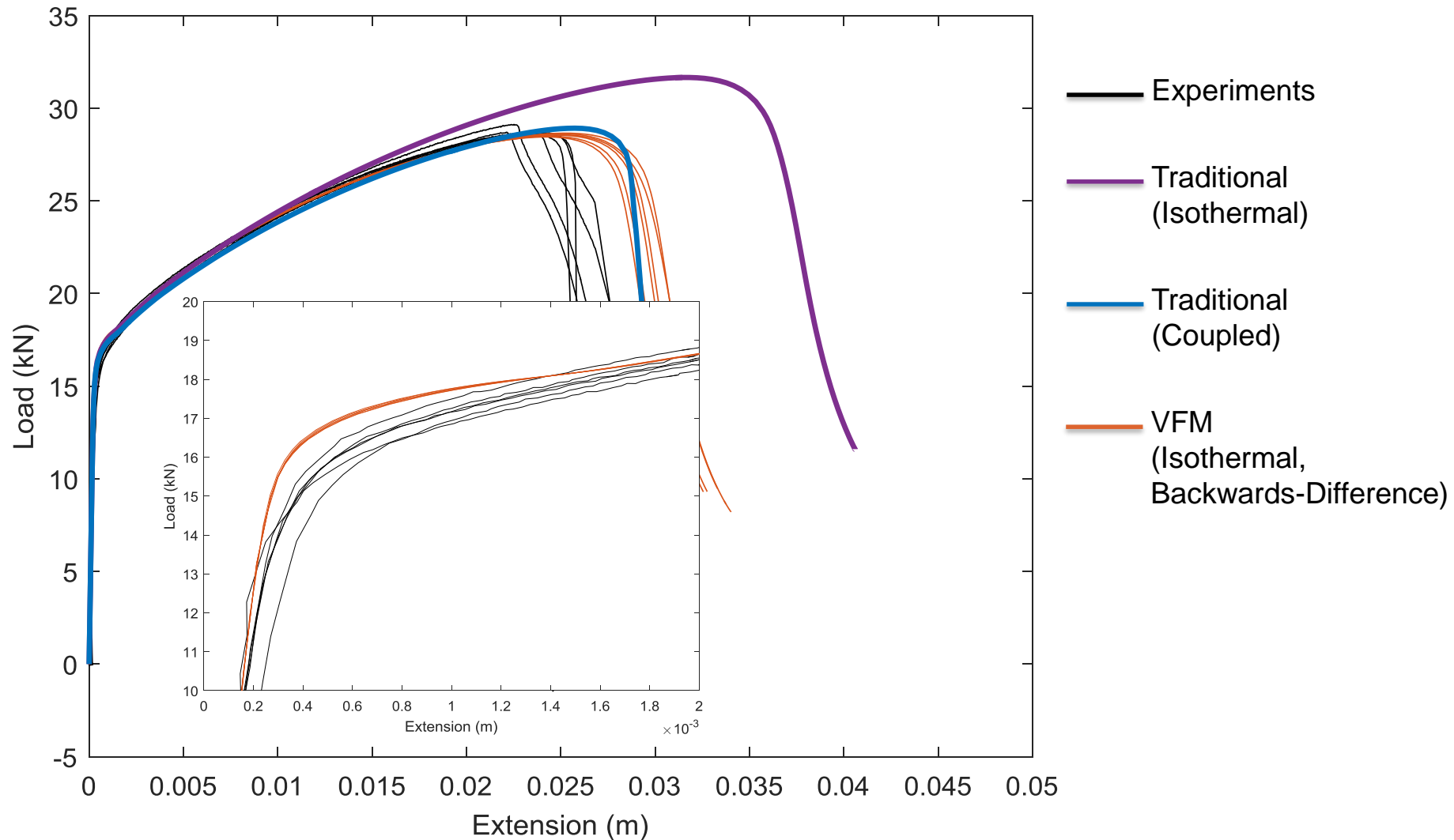
Global data is similar for all model parameter sets.



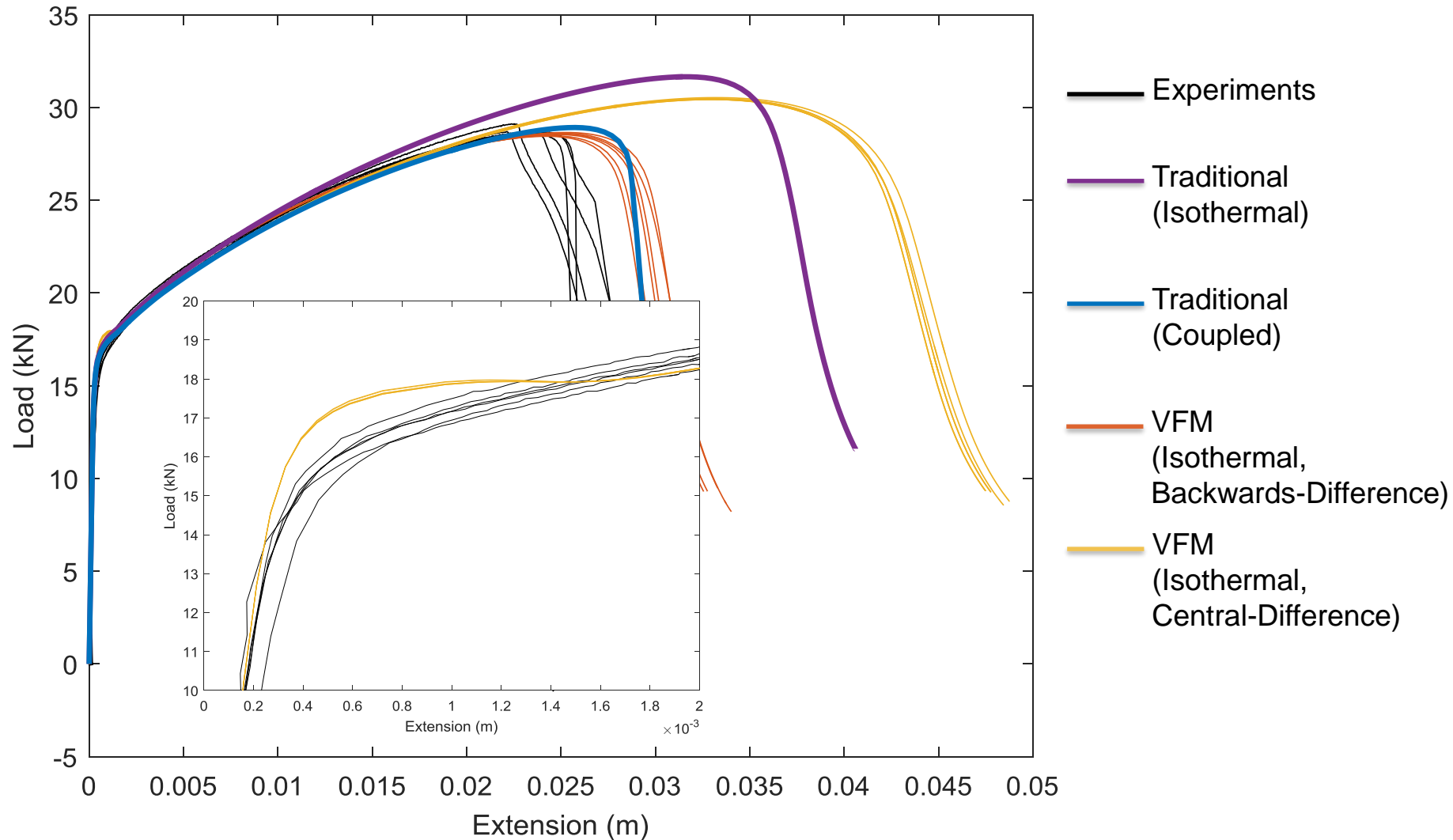
Global data is similar for all model parameter sets.



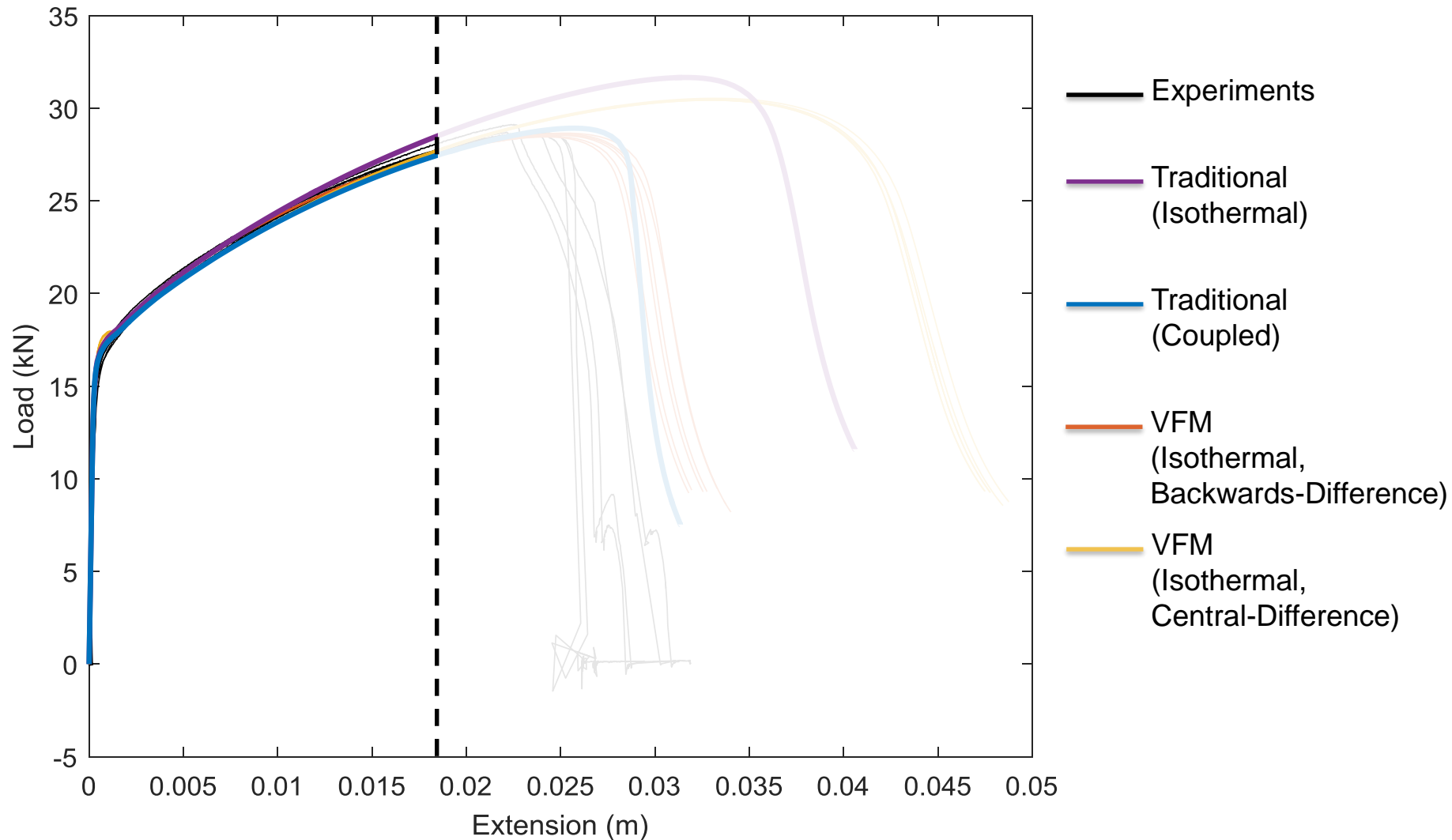
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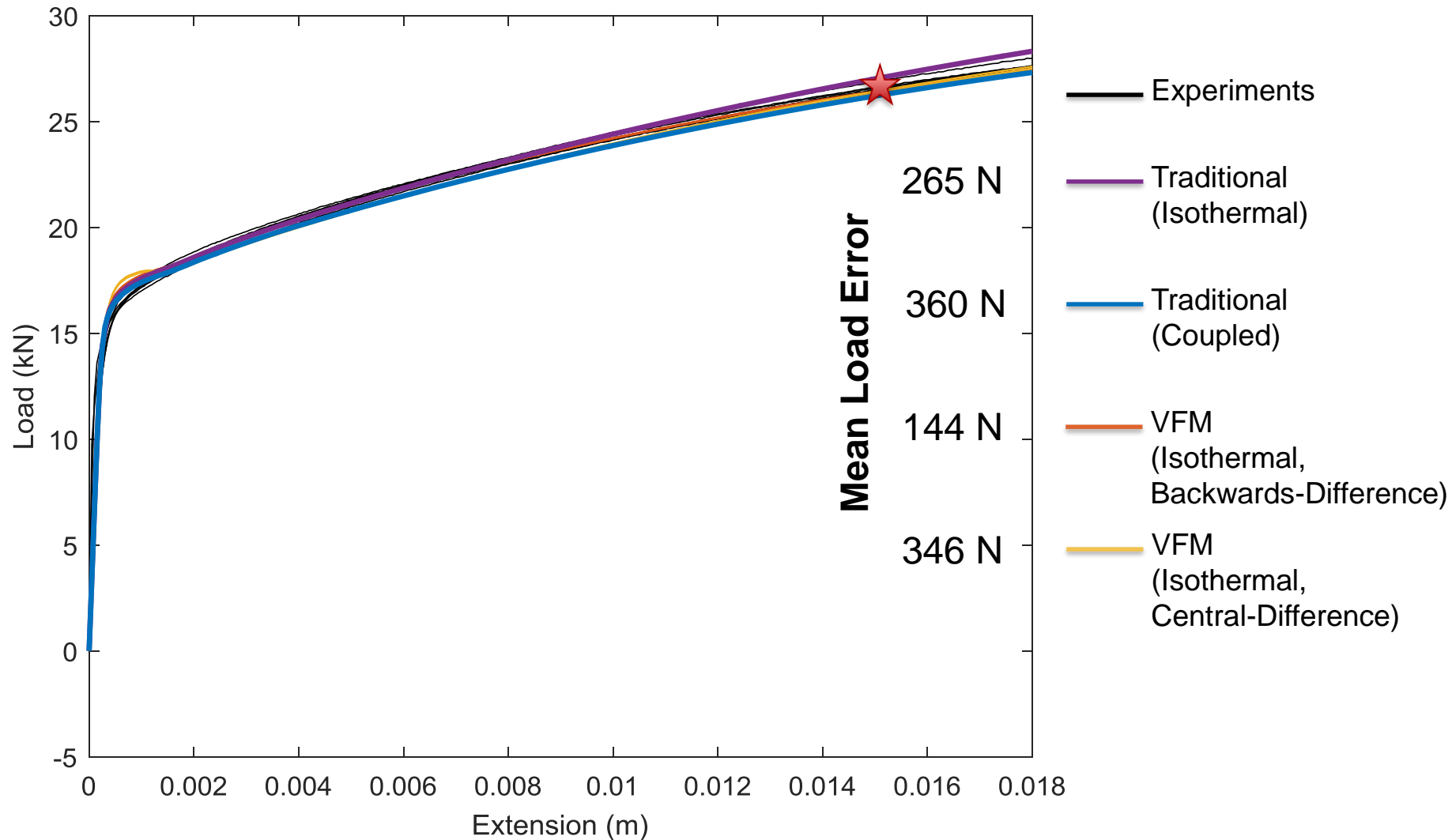
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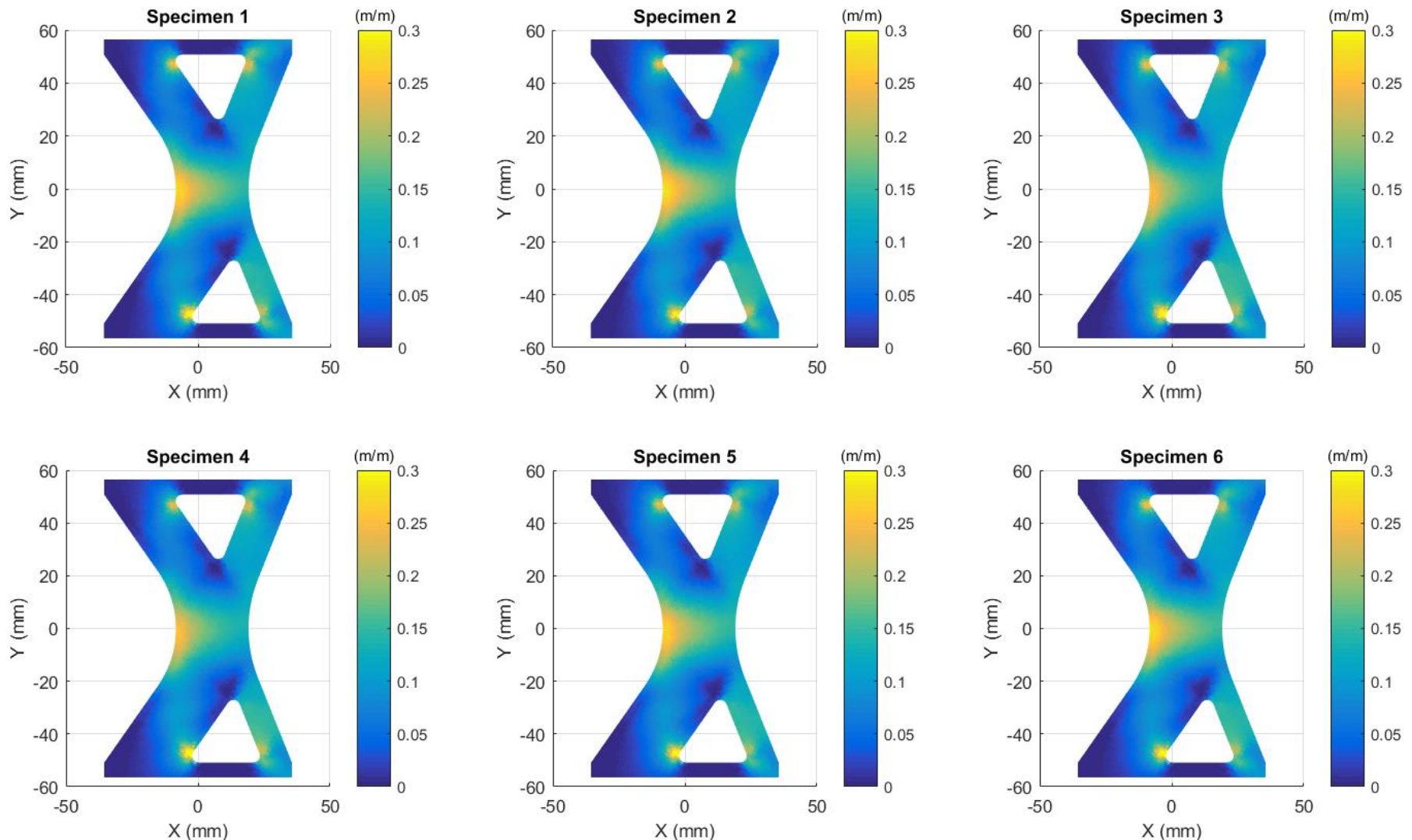


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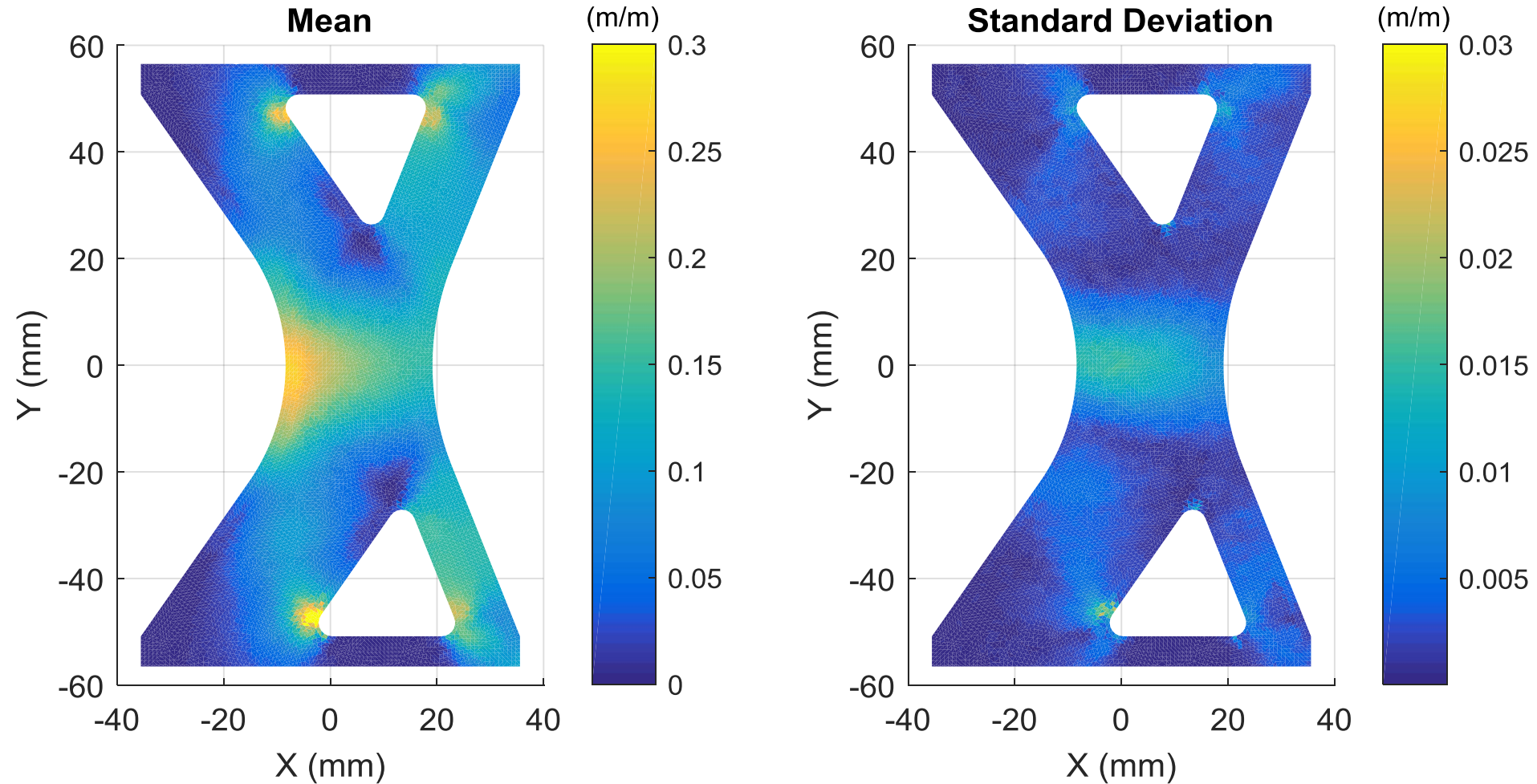
Experimental results are repeatable:

Vertical normal strain at 15 mm total extension.

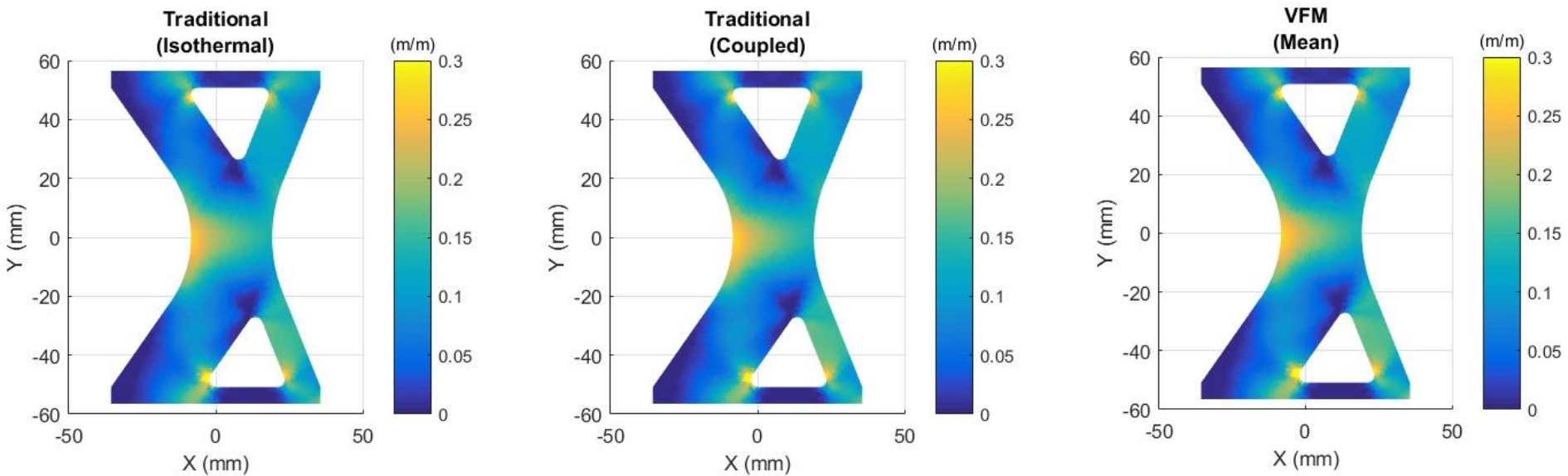


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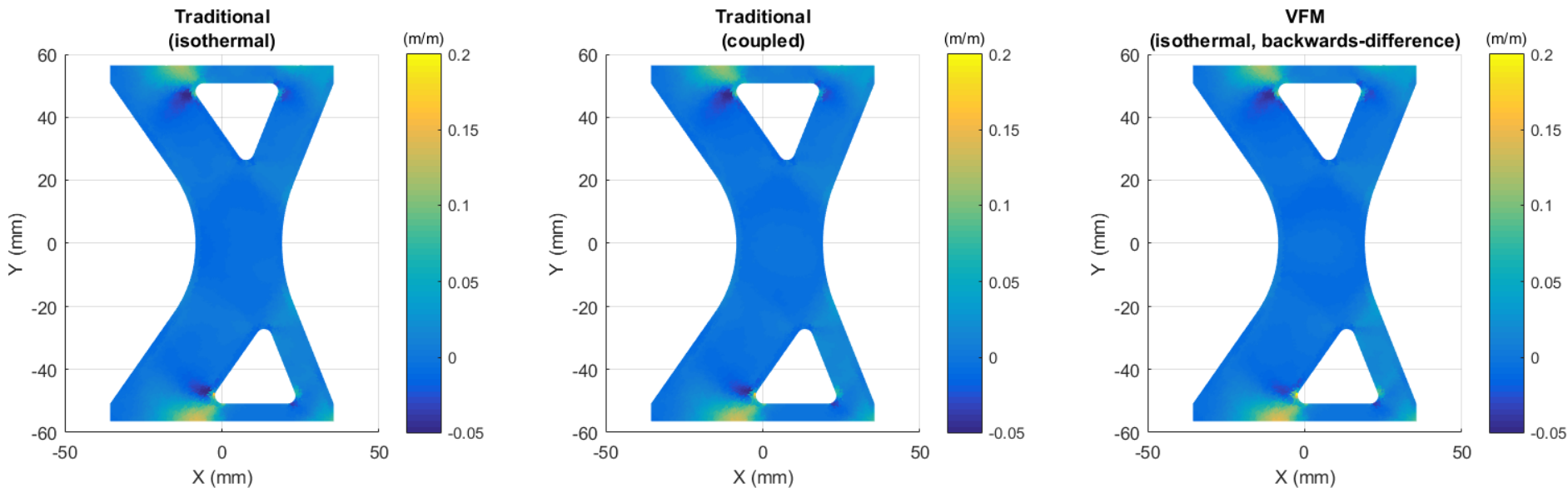


Finite-Element Models using different parameter sets are also very similar.



All material models have **similar errors** compared to experimental data.

Strain Error = FEM Strain – Experimental Strain



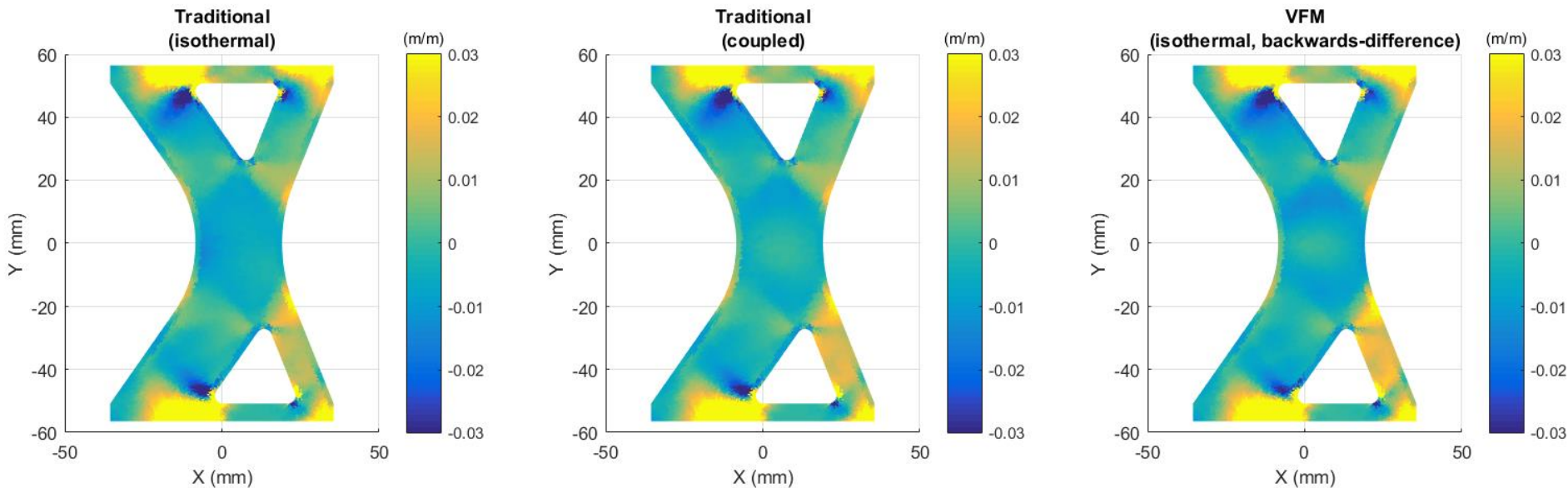
Average Strain Errors ($\mu\epsilon$)

	Traditional (isothermal)	Traditional (coupled)	VFM (backwards difference)
E_{11}	5450	5460	5480
E_{22}	8090	8030	8480
E_{12}	3020	3040	3050

- All material models have approximately the same error.
- Full-field data provides much more information for validation.

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Strain Error = FEM Strain – Experimental Strain



Average Strain Errors ($\mu\epsilon$)

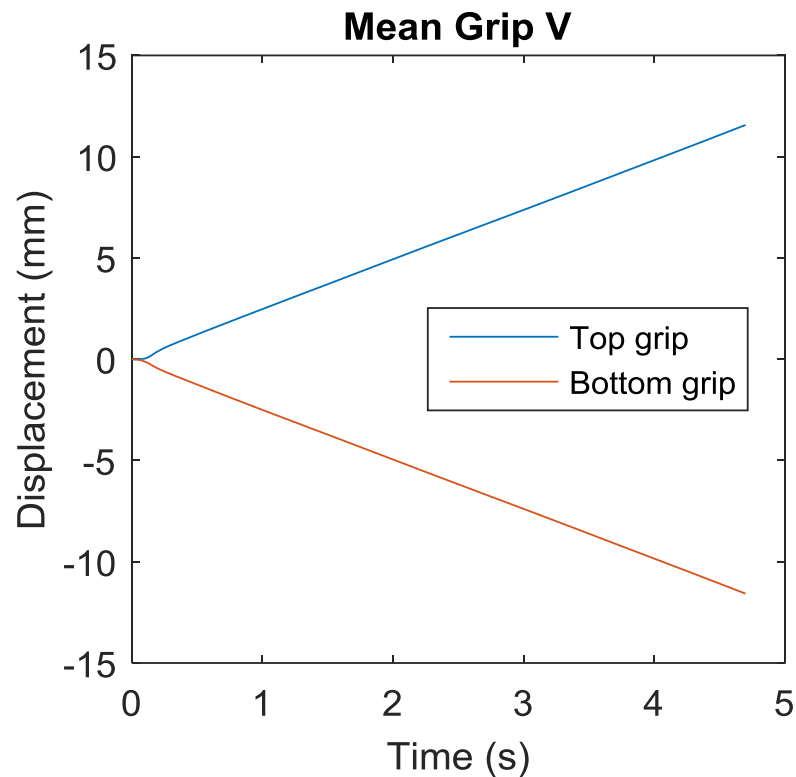
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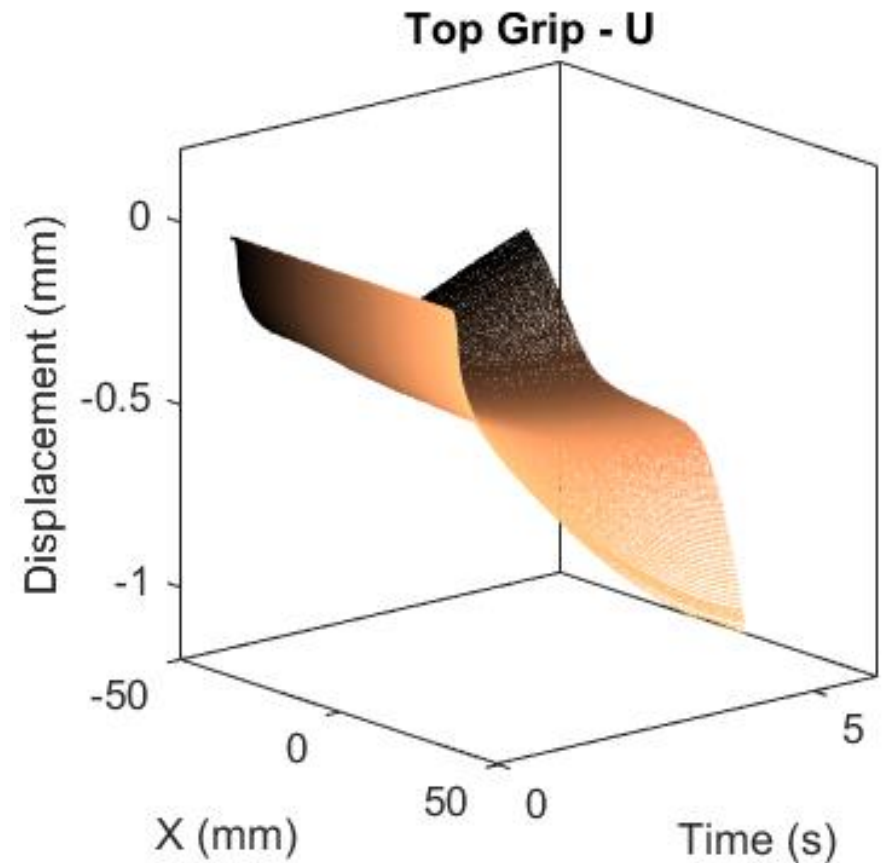
Experimental boundary conditions are not perfect.

FE Model BCs (Ideal)



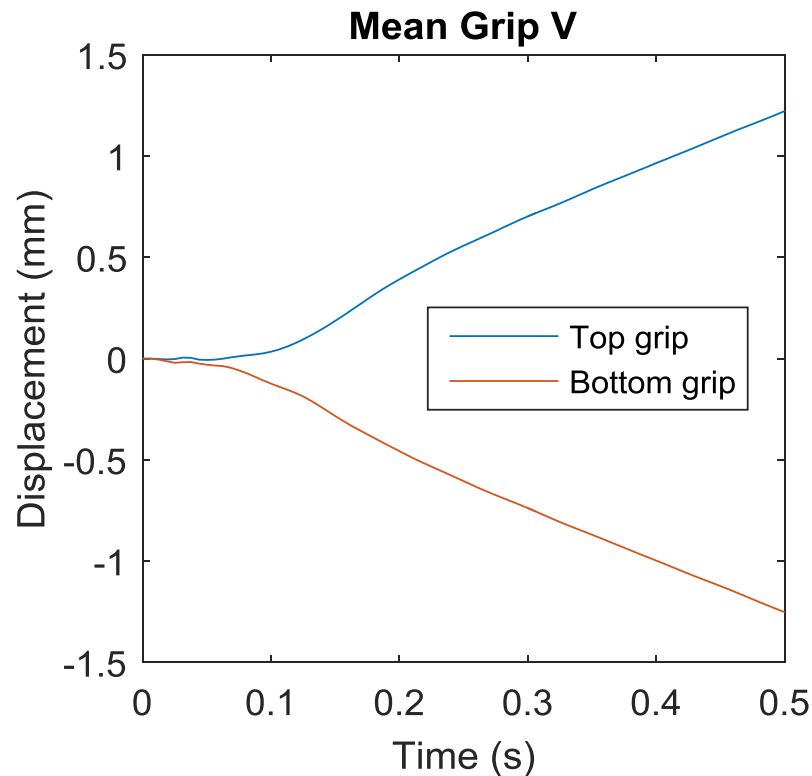
No displacement in U or W.

Experimental BCs



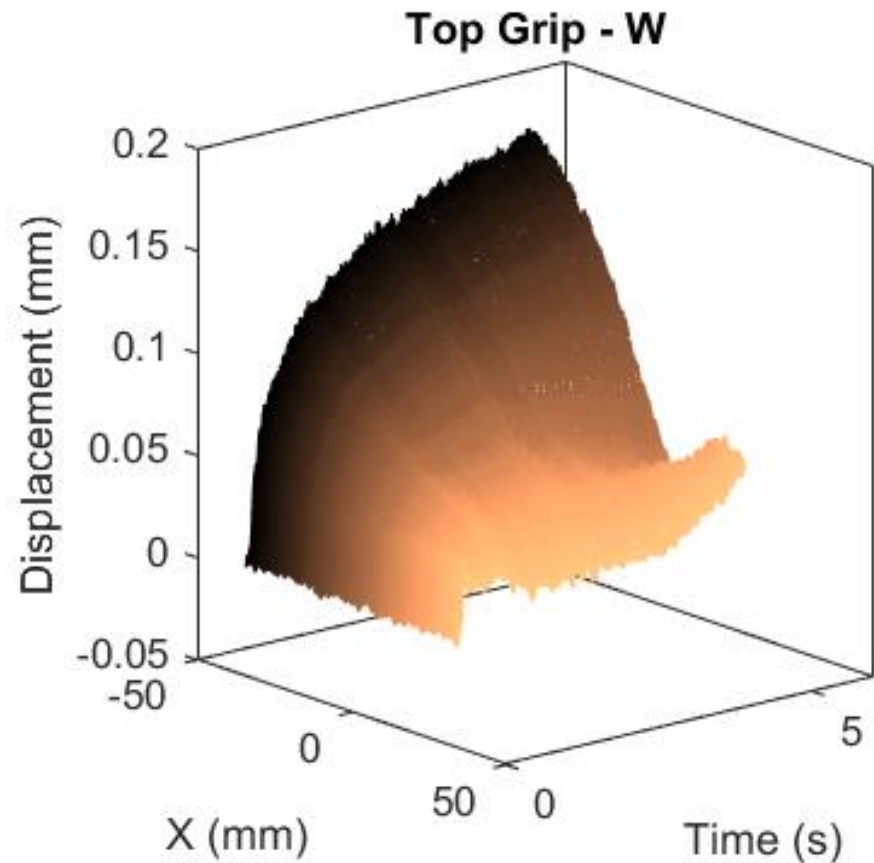
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FE Model BCs (Ideal)



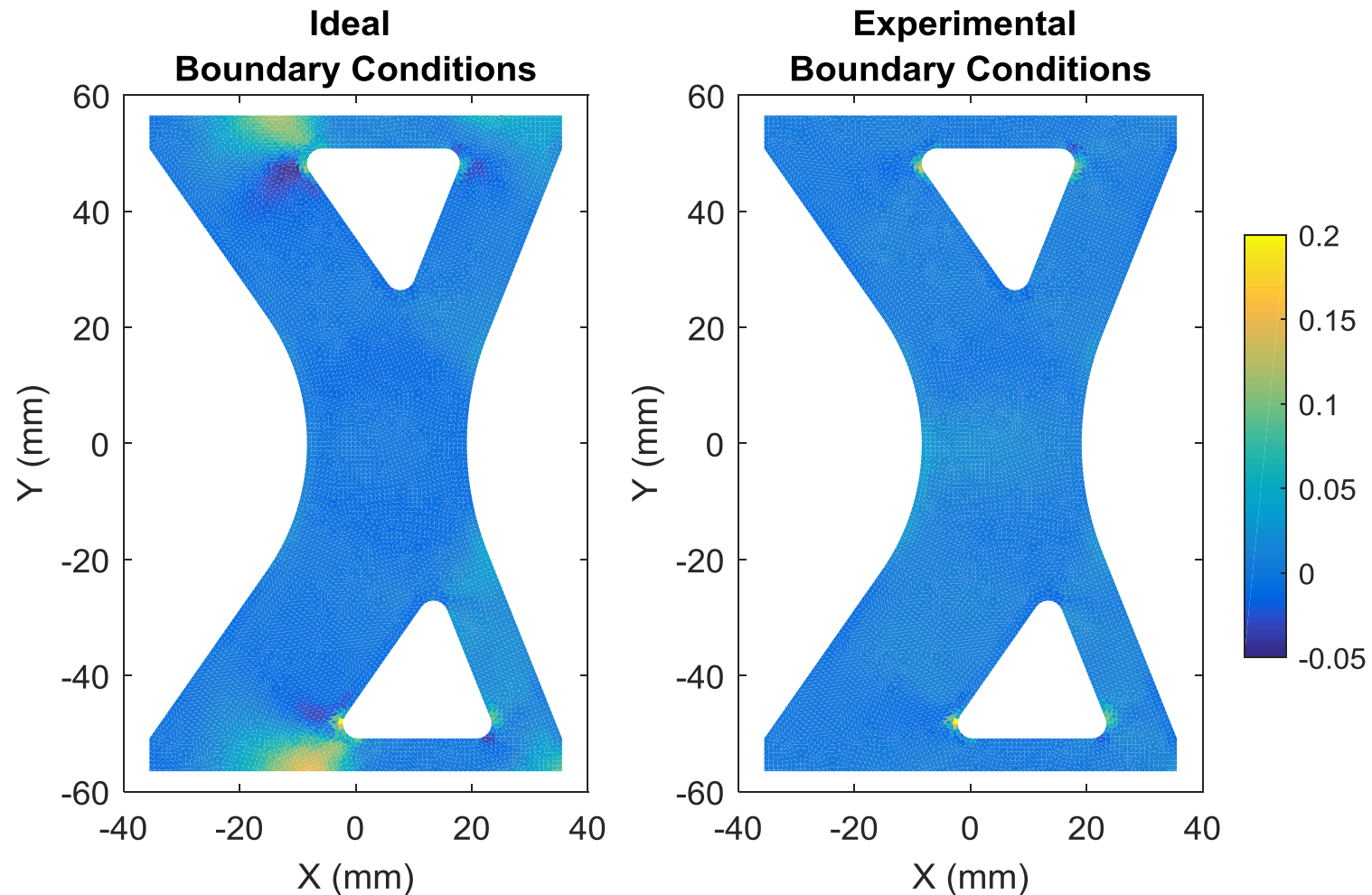
No displacement in U or W.

Experimental BCs



Modeling actual boundary conditions is critical for **FE model validation**.

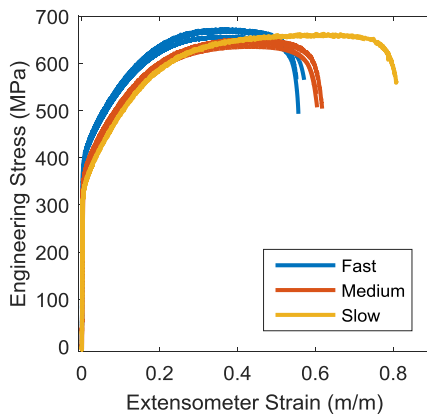
Strain Error = FEM Strain – Experimental Strain



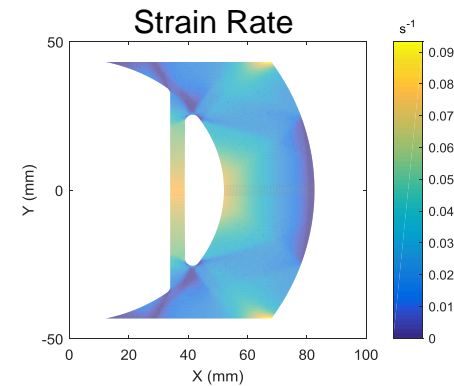
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Goal: Perform better material characterization by utilizing full-field data instead of only global measurements

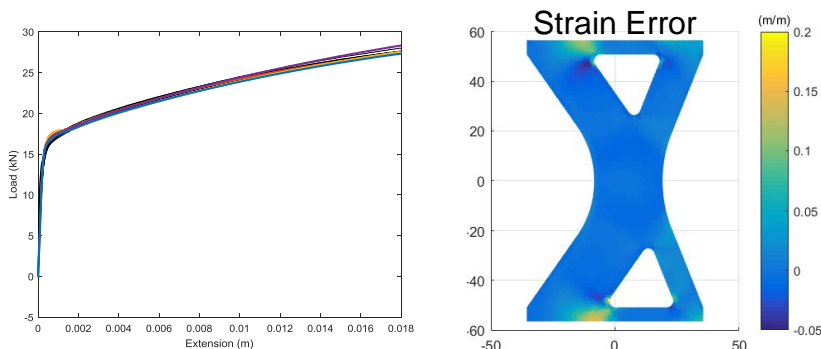
Calibrated a viscoplastic material model using traditional tensile tests.



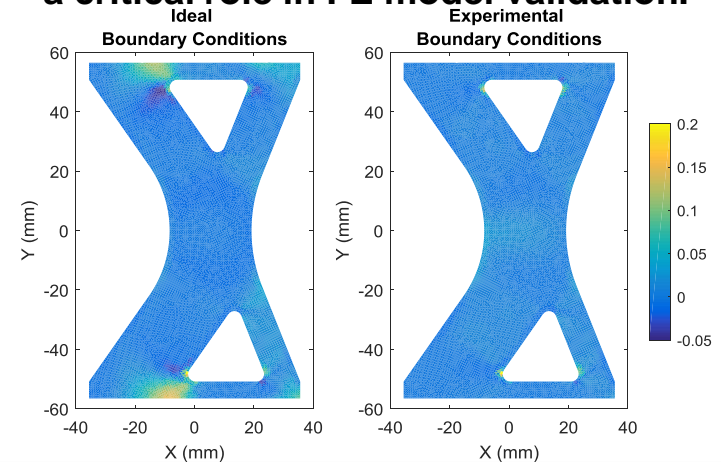
Calibrated a viscoplastic material model using a single specimen and VFM.



Validated FE models against experimental data – both global and full-field.



Determined that boundary conditions play a critical role in FE model validation.



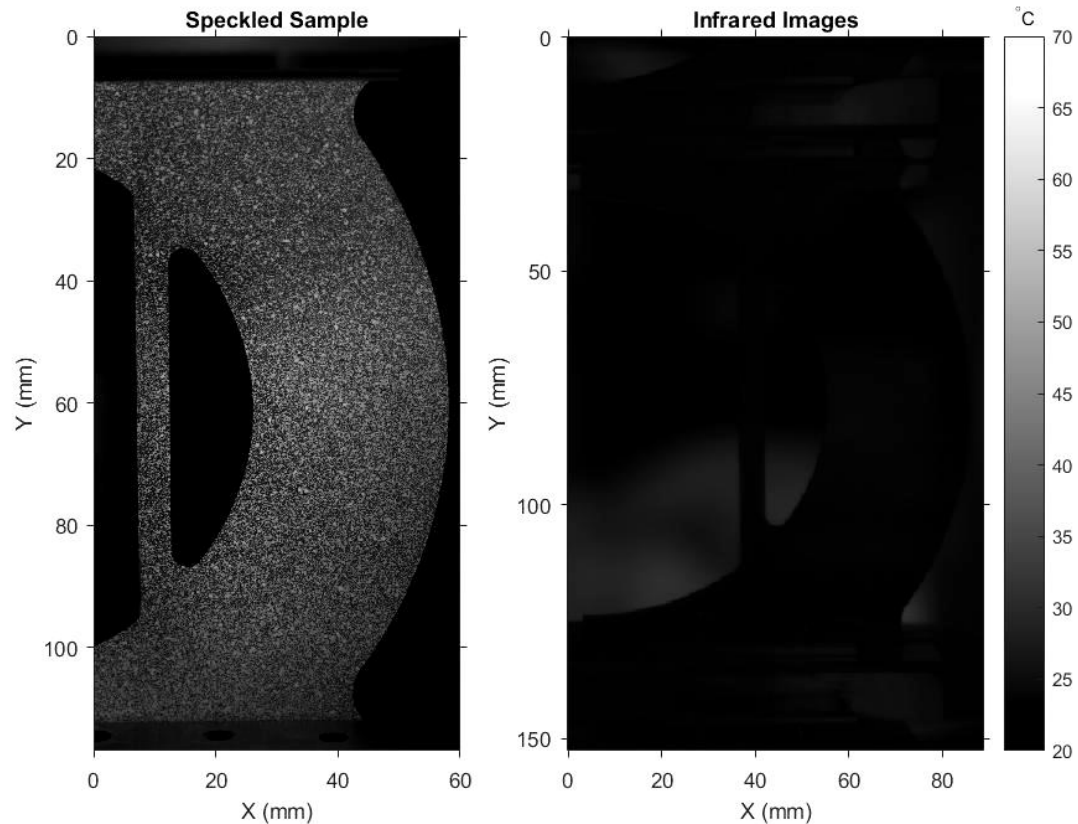
Much left to do

Near term:

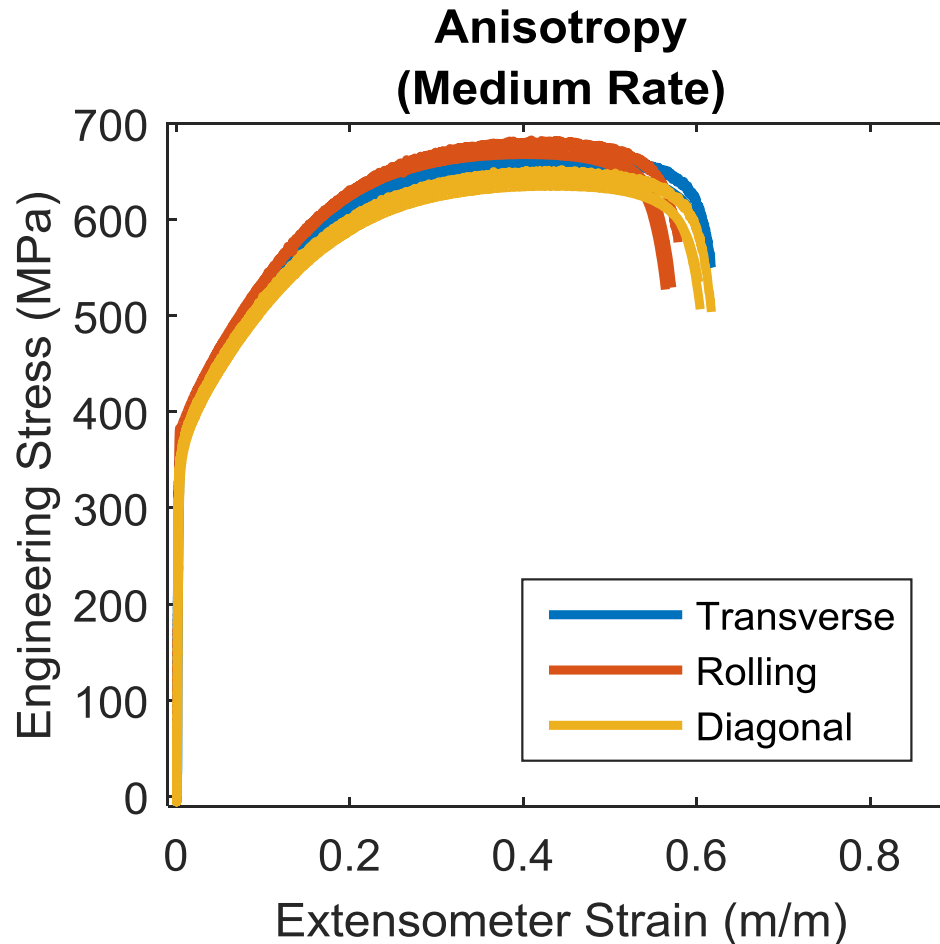
- Investigate effect of sample-to-sample variation on VFM model calibration
- Explore other material models (Johnson-Cook)
- Include temperature dependence and anisotropy in material model

Long term:

- Optimize specimen geometry
- Understand implications of non-unique parameters
- Determine advantages/disadvantages of VFM compared to traditional techniques



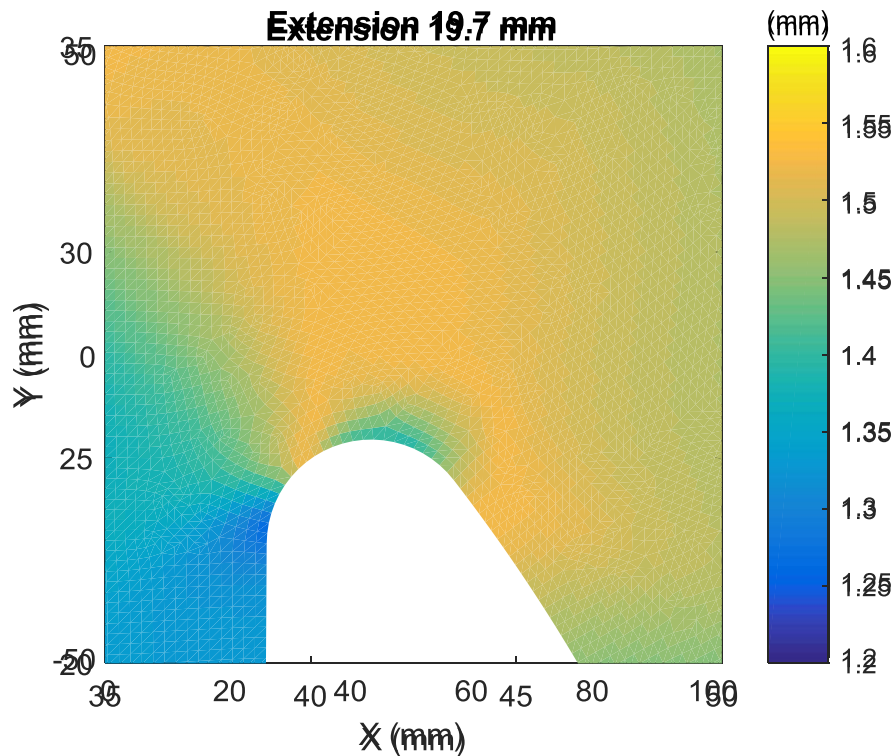
304L stainless steel sheet exhibits mild plastic anisotropy.



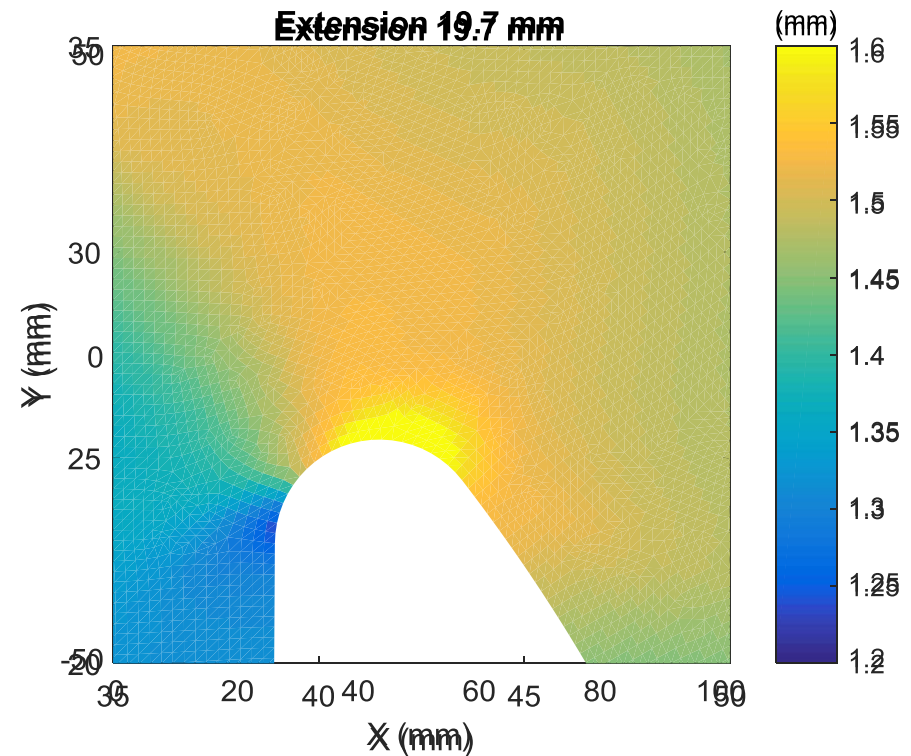
Thickness change must be measured or estimated.

- Internal power requires volume integral
- Plane stress assumption \rightarrow area integral times sample thickness
- Thickness can be computed by:
 - Measuring with DIC on both sides of the sample
 - Assuming incompressible plasticity and calculating from in-plane strains

FEM Thickness
Extension 19.7 mm



Reconstructed Thickness
Extension 19.7 mm

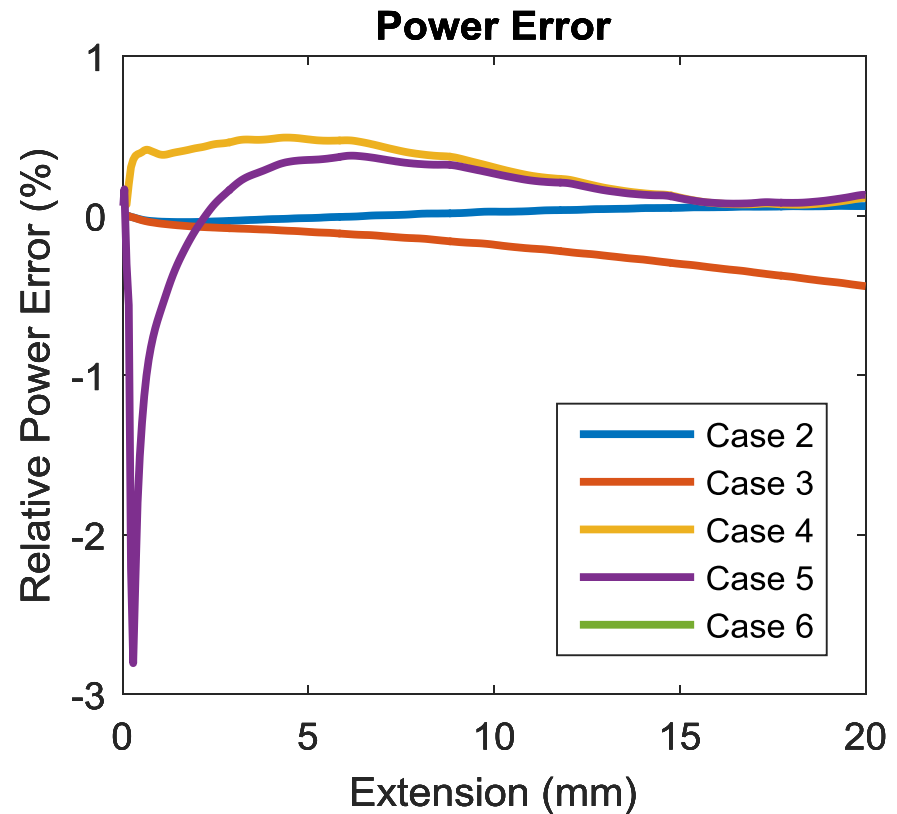


Accuracy of VFM algorithm quantified by error in internal vs. external power.

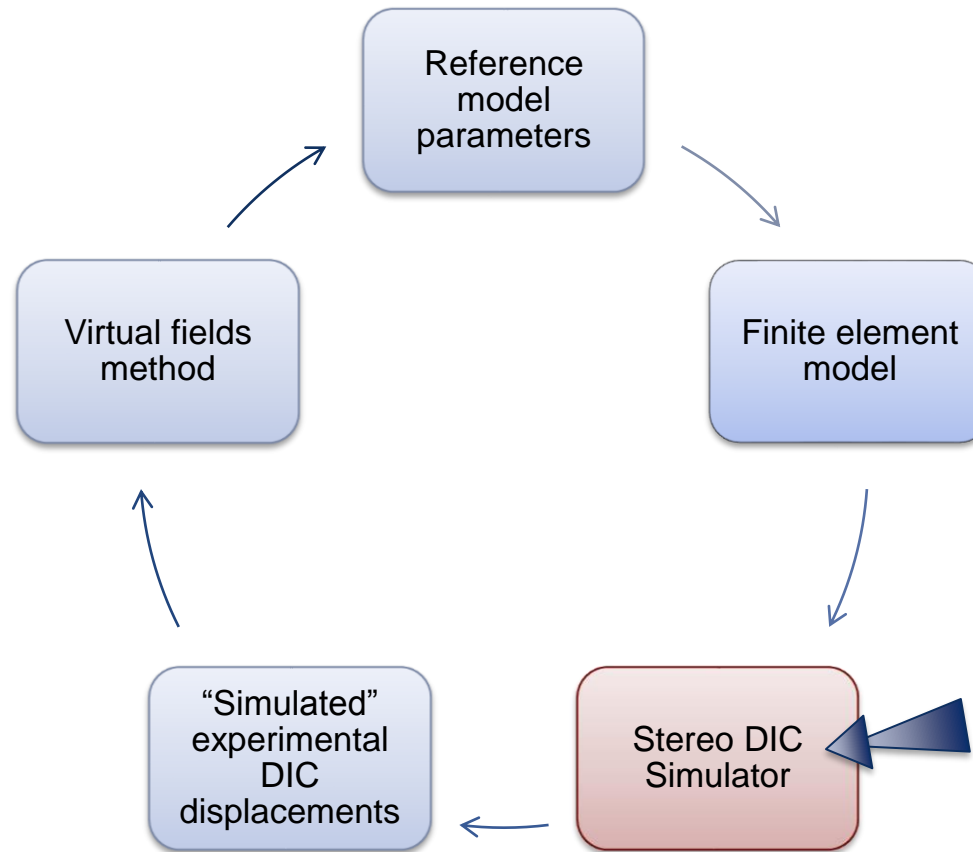
6 Cases

Increasing Realism for DIC
Decreasing Fidelity to FEA

1. FEA algorithms
2. Plane stress assumption;
discrete volume integral
approximation
3. Incompressible plasticity
4. Kinematics calculated from
polynomial fit, with
backward difference
temporal derivative
5. Central difference temporal
derivative

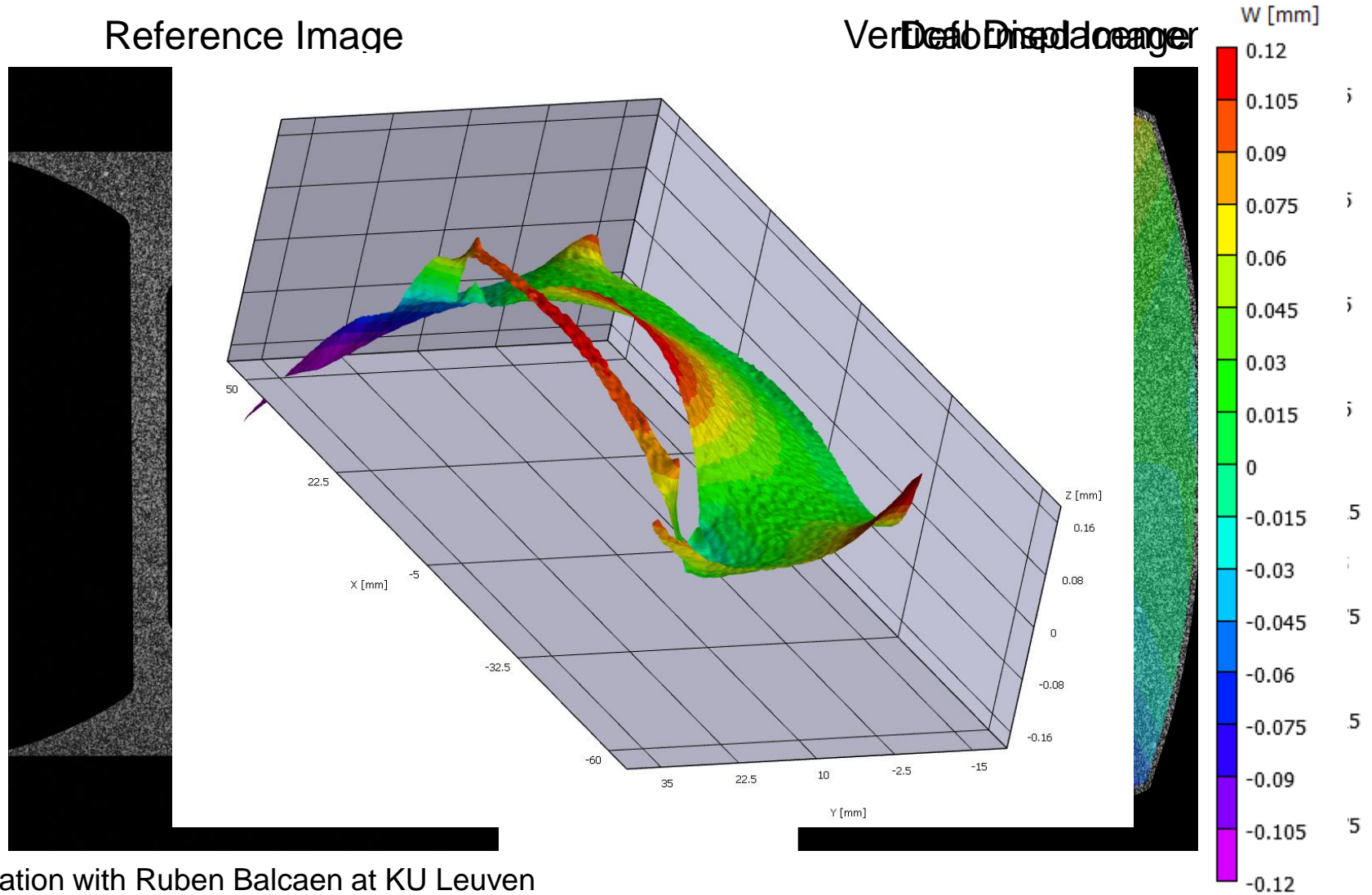


Stereo DIC simulator brings the simulated experiment one step closer to reality.



- Camera noise
- Matching error
- Spatial filtering
- Shape function
- Interpolation error

Stereo DIC simulator brings the simulated experiment one step closer to reality.



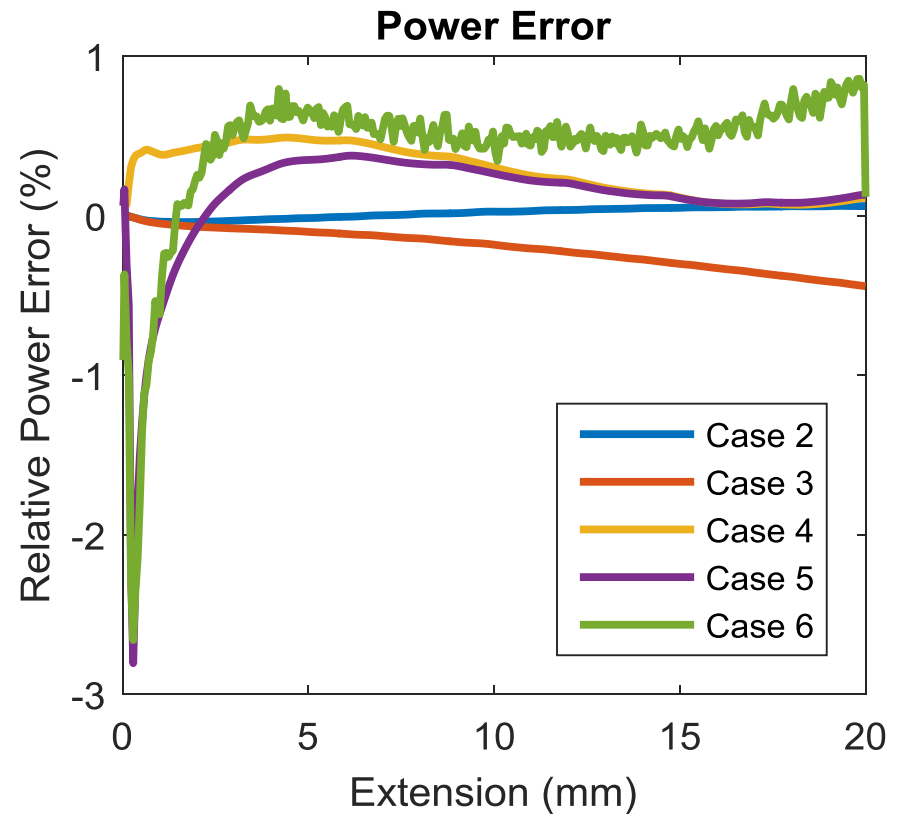
Collaboration with Ruben Balcaen at KU Leuven

Accuracy of VFM algorithm quantified by error in internal vs. external power.

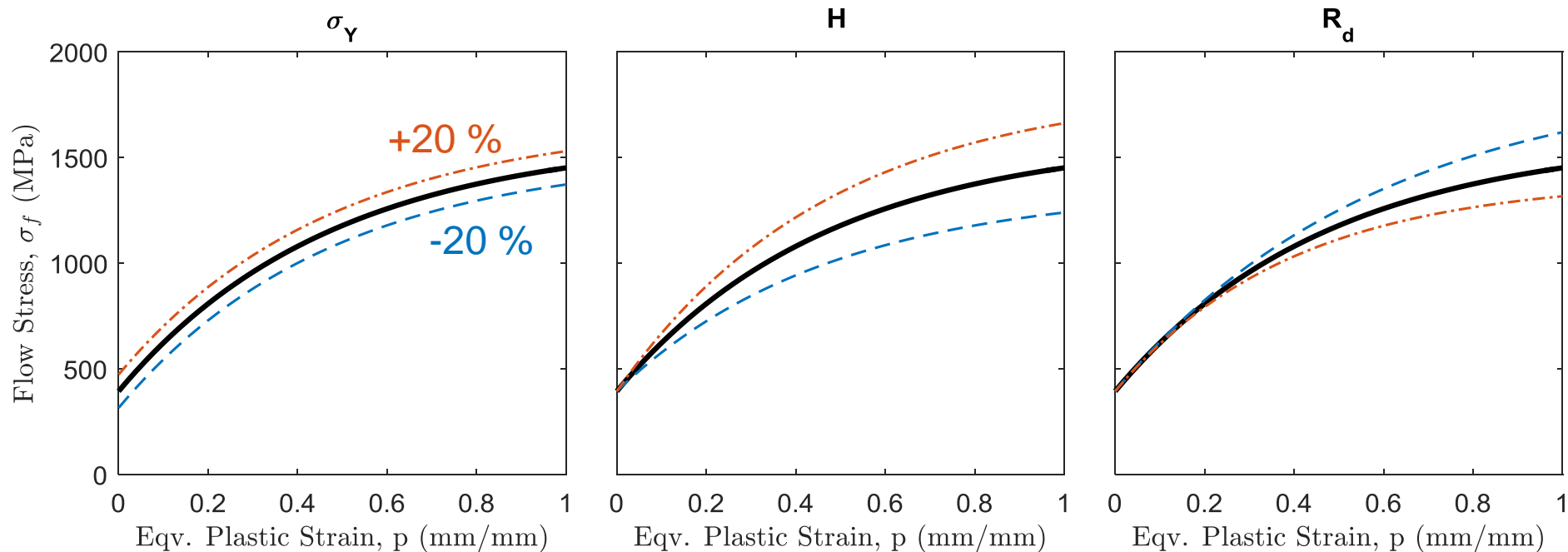
6 Cases

Increasing Realism for DIC
Decreasing Fidelity to FEA

1. FEA algorithms
2. Plane stress assumption; discrete volume integral approximation
3. Incompressible plasticity
4. Kinematics calculated from polynomial fit, with backward difference temporal derivative
5. Central difference temporal derivative
6. Simulated DIC images

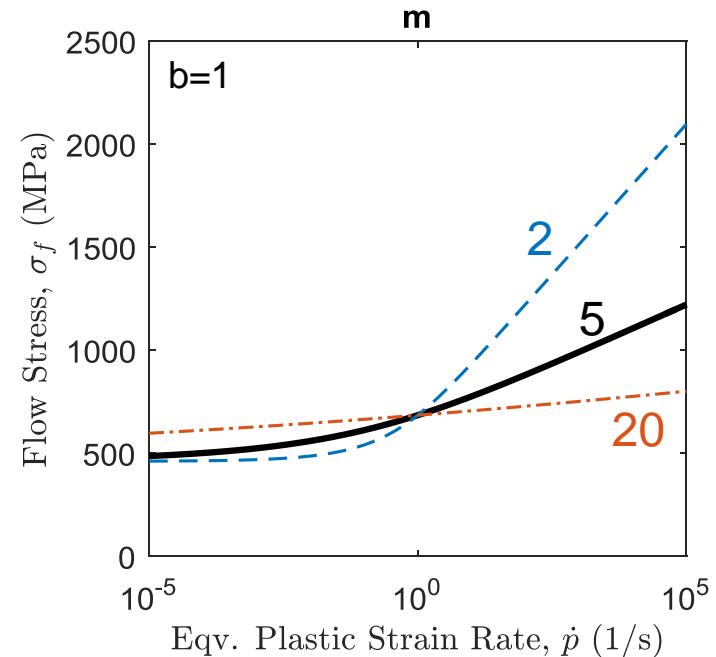
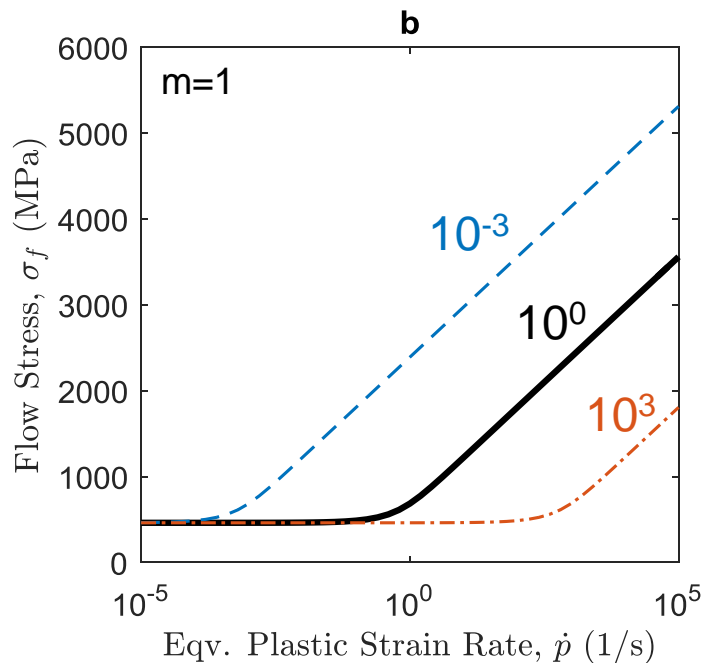


Simplified, 1D visualization of parameter effects



Constant strain rate, $\dot{p} = 10^{-1.5}$

Simplified, 1D visualization of parameter effects



Constant strain, $p = 0.09$

■ Von Mises Flow Criterion

- Equivalent Stress:

$$\bar{\sigma} = \sqrt{\frac{3}{2} s : s} \quad \left(s = \sigma - \frac{1}{3} \text{tr}(\sigma) I \right)$$

- Equivalent Plastic Strain Rate:

$$\dot{p} = \sqrt{\frac{2}{3} \dot{\varepsilon}^p : \dot{\varepsilon}^p}$$

- Flow Criterion:

$$f = \bar{\sigma} - \sigma_f = 0$$

■ Hardening Law

- $\sigma_f(p, \dot{p}, \xi) = \sigma_o \left\{ 1 + \text{asinh} \left[\left(\frac{\dot{p}}{b_\sigma} \right)^{1/m_\sigma} \right] \right\} + \kappa \left\{ 1 + \text{asinh} \left[\left(\frac{\dot{p}}{b_\kappa} \right)^{1/m_\kappa} \right] \right\}$

- $\dot{\kappa} = (H - R_d \kappa) \dot{p}$

- Constant strain rate: $\kappa = \frac{H}{R_d} [1 - \exp(-R_d p)]$

VFM utilizes multi-axial calibration data and requires **fewer tests** than traditional calibrations.

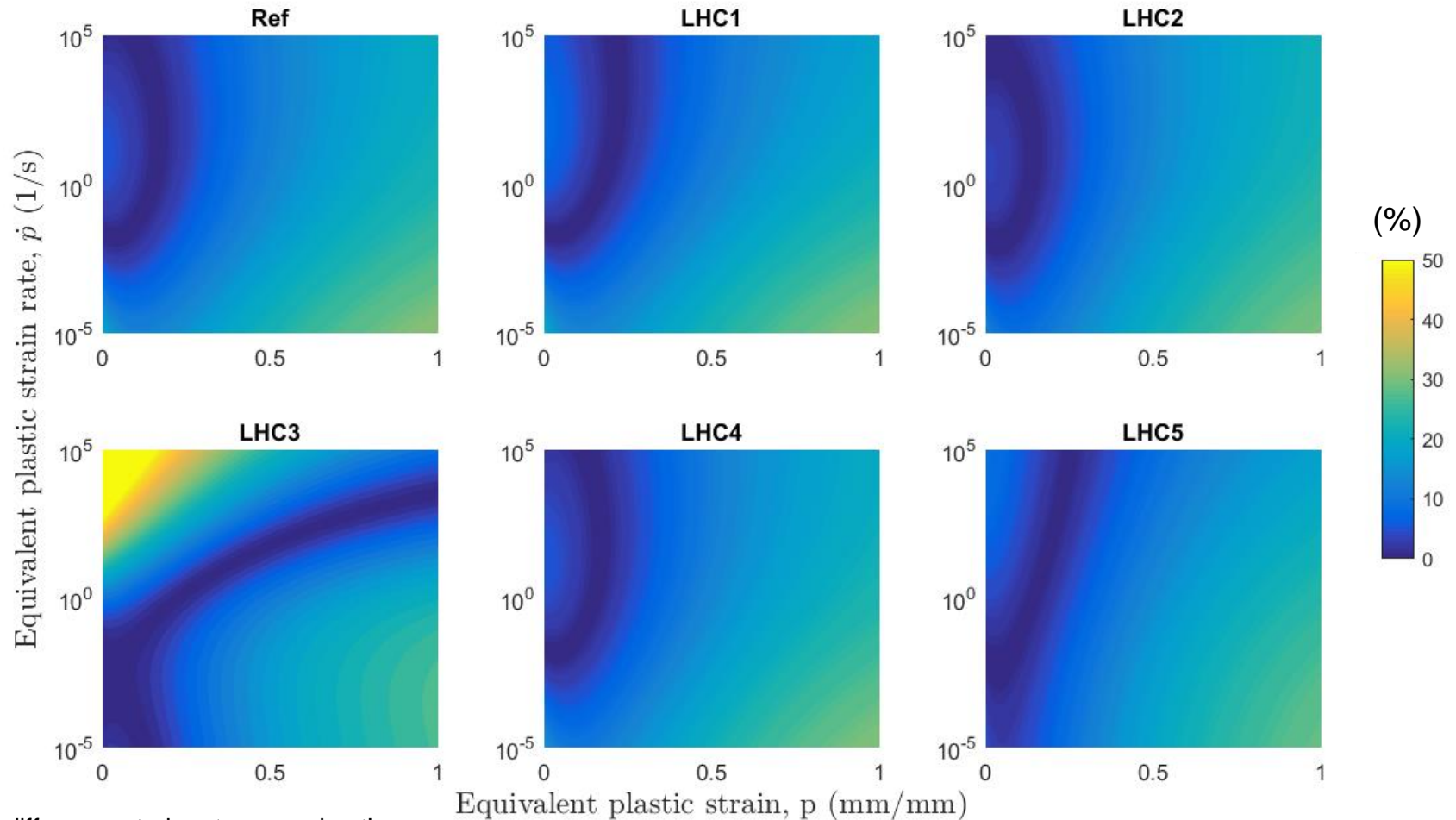
$$\sigma = f(\underbrace{\zeta(\varepsilon, p, \dot{p}, T)}_{\text{loading conditions}}, \underbrace{\xi(E, \nu, \sigma_o, H)}_{\text{model parameters}})$$

Techniques for Model Calibration (Material Characterization)

	Traditional	Advanced, Full-Field
Specimen Geometry	Tensile dog bones; torsion cylinders	Arbitrary
Type of Experimental Data	Global data → engineering stress and extensometer strain	Full-field data → DIC data over the entire specimen surface
Stress State	Uniaxial (tension only; shear only)	Multi-axial
Advantages	<ul style="list-style-type: none"> Simple experiments Data easier to interpret 	<ul style="list-style-type: none"> Loading conditions of calibration specimen reflect real-world Reduced number of experiments
Disadvantages	<ul style="list-style-type: none"> Uniaxial stress state does not reflect real-world conditions Multiple experiments required to fit complex model 	<ul style="list-style-type: none"> Experiments more complicated Data analysis more complicated

Parameter set is effectively not **unique**.

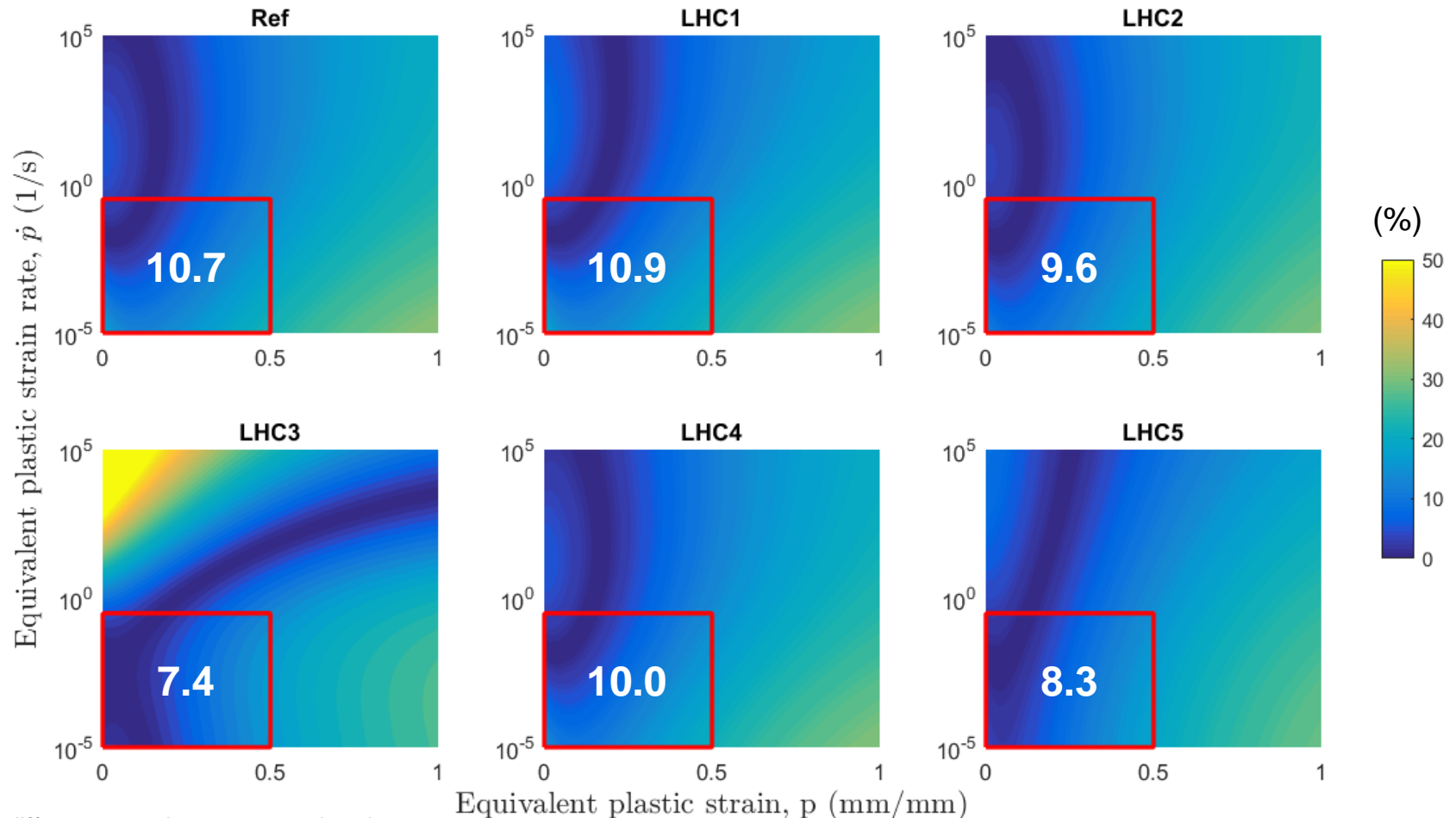
$$\text{Flow Stress Difference} = \frac{\sigma_f(p, \dot{p}, \xi_{\text{VFM}}) - \sigma_f(p, \dot{p}, \xi_{\text{traditional}})}{\sigma_f(p, \dot{p}, \xi_{\text{traditional}})}$$



Backwards-difference strain rate approximation

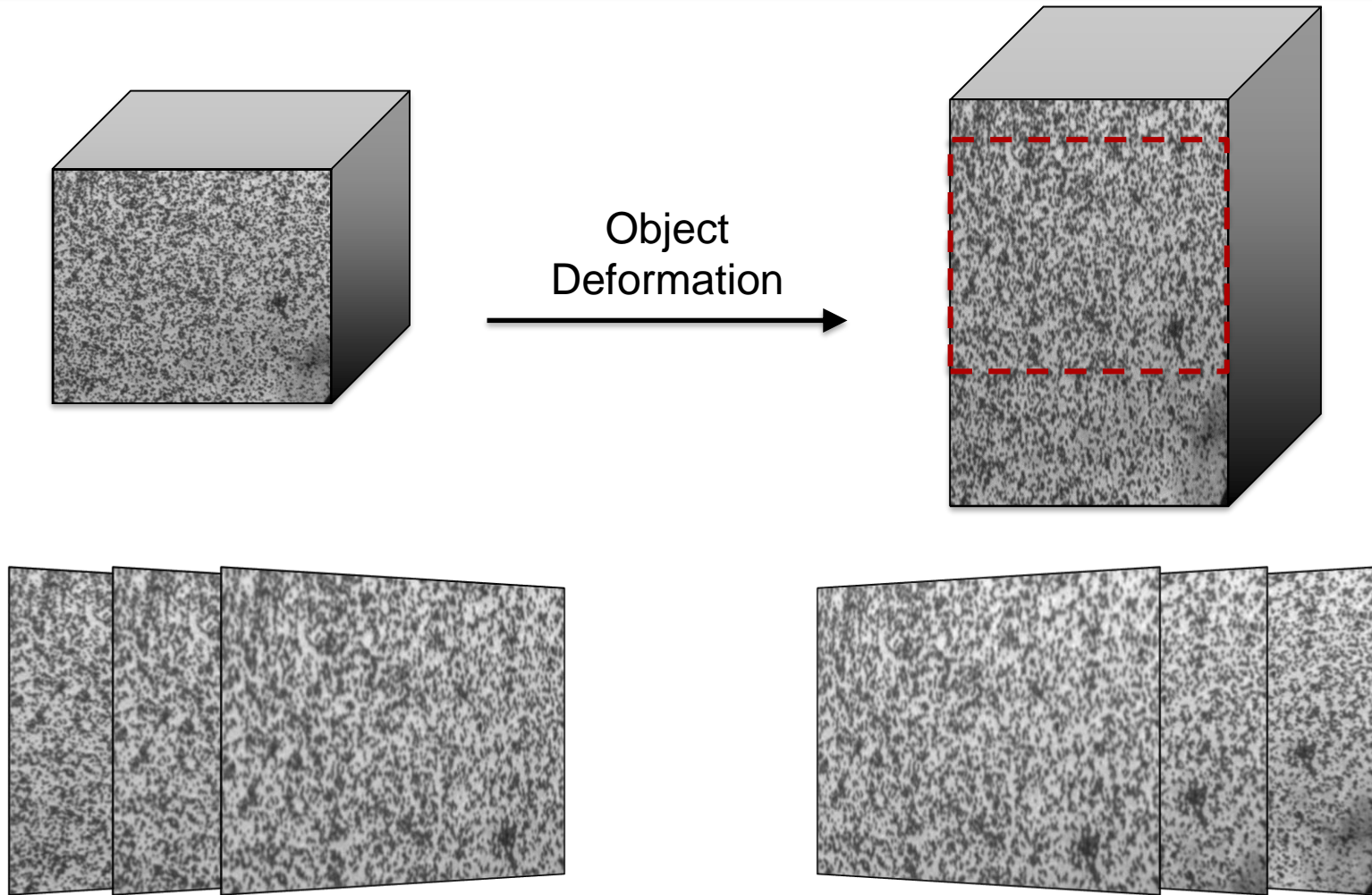
Parameter set is effectively not **unique**.

$$\text{Flow Stress Difference} = \frac{\sigma_f(p, \dot{p}, \xi_{\text{VFM}}) - \sigma_f(p, \dot{p}, \xi_{\text{traditional}})}{\sigma_f(p, \dot{p}, \xi_{\text{traditional}})}$$



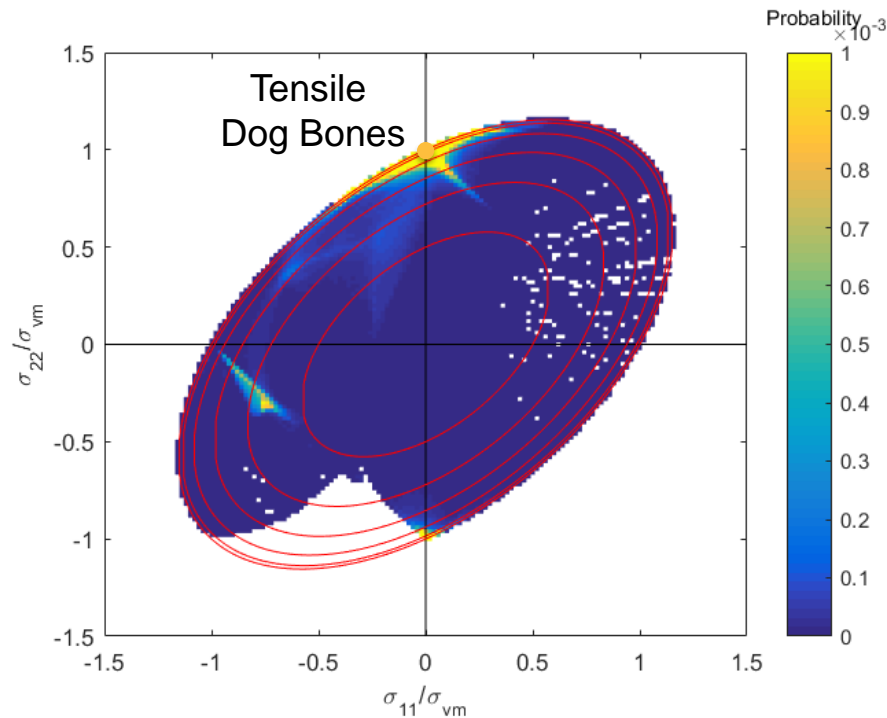
Backwards-difference strain rate approximation

Stereo DIC provides locations and displacements in three dimensions.



Complex specimen geometry induces stress and strain rate **heterogeneity** in sample.

Stress Distribution



Strain/Strain Rate Distribution

