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# Which Models Matter: Uncertainty and Sensitivity Analysis for Photovoltaic Power Systems

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# Outline

- Uncertainty and Sensitivity Analysis
- Methodology
- Models and uncertainty quantification for each model
- Analysis results
- Next steps

# Uncertainty and Sensitivity Analysis

- If we have perfect data  $X$  and an exact model  $F(X)$  :

$$X \rightarrow \boxed{F(X)} \rightarrow Y \text{ is known exactly}$$

- But we don't have perfect information or exact models:

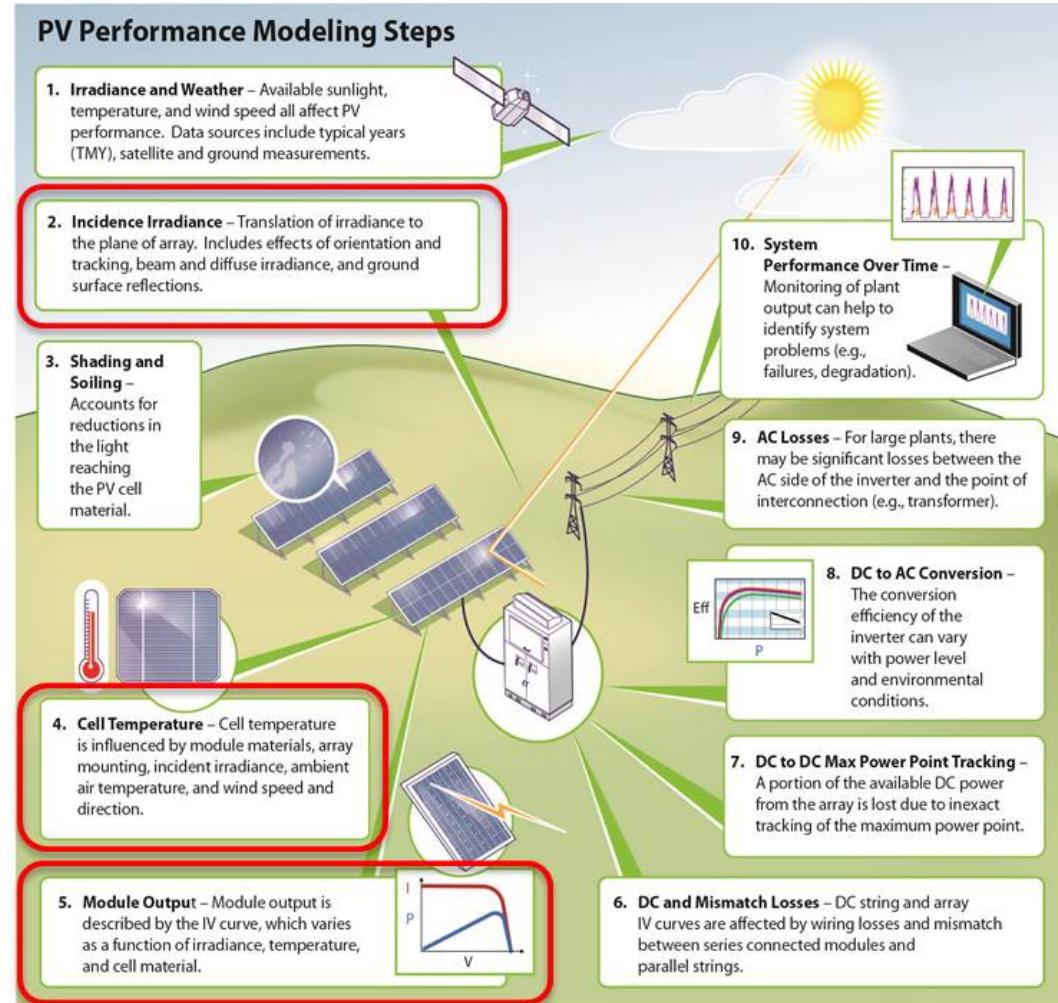
$$X_i \rightarrow \boxed{F(X_i)} \rightarrow Y_{F,i}, i = 1, \dots,$$

$$X_i \rightarrow \boxed{G(X_i)} \rightarrow Y_{G,i}, i = 1, \dots,$$

- Uncertainty analysis quantifies the uncertainty in  $Y$  resulting from uncertainty in data  $X$  and models  $F, G, \dots$
- Sensitivity analysis explores the relationship between uncertainty in  $Y$  and uncertainty in data  $X$

# Models considered

- GHI, DNI and DHI to POA:
  - Isotropic sky, Hay and Davies, Perez, Sandia
- POA to effective irradiance:
  - Accounts for spectral mismatch, reflections and soiling
  - Polynomial in AM
- Cell temperature:
  - Sandia model
- Module DC output:
  - Sandia model
- cSi and CdTe modules
- Meteorological data from Albuquerque and Golden, CO



# Limitations

- We deliberately do NOT consider uncertainty in measured irradiance
  - Uncertainty in irradiance translates proportionally to uncertainty in power and energy
  - Would obscure effects of other uncertainties, which we want to understand
- We do not consider effect of measurement error in other quantities (e.g., temperature, voltage)
  - Would add greatly to complexity of analysis
  - But they are anticipated to have small effects
- We do not consider uncertainty in calibration of models
  - Most models used for PV system analysis (e.g., Hay and Davies sky diffuse model) are calibrated to a specific set of historic data
  - A different 'Hay and Davies' model would result from different data

# Methodology

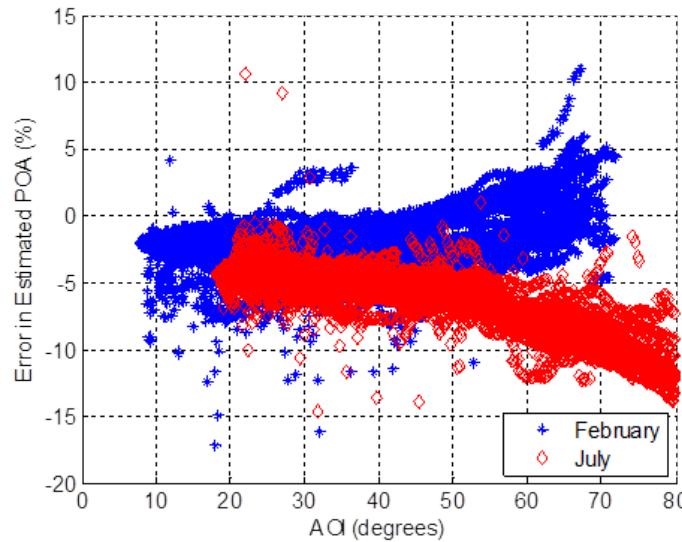
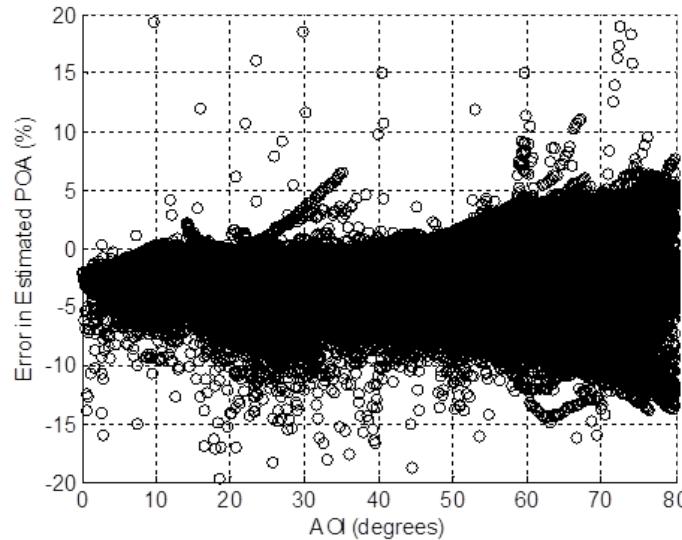
- Obtain measured inputs  $X$  and concurrently measured output  $Y$  for each model  $f(X)$
- Define model residuals, e.g., :  $\varepsilon_f(X) = f(X) - Y$

The distributions of  $\varepsilon_f(X)$  characterize the aggregate uncertainty in  $f(X)$  over the range of  $X$

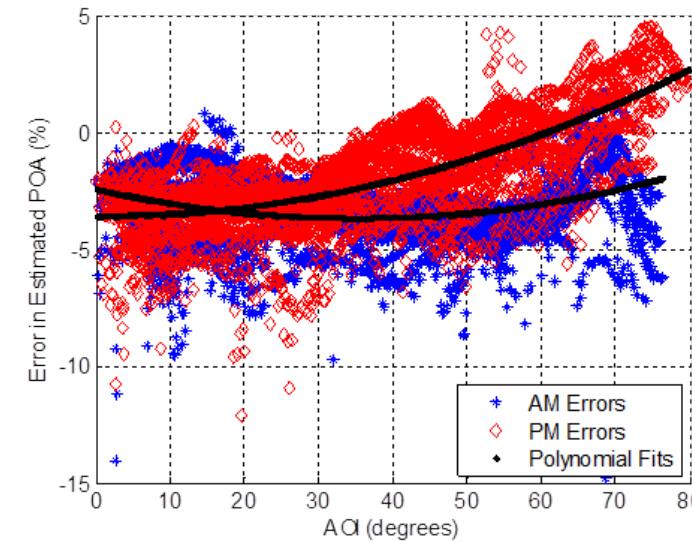
- Build a probability model for each  $\varepsilon_f$
- Need to detrend and account for correlations
- Generate samples  $\varepsilon_{f,i}(X)$
- Propagate samples through the sequence of models:

$$\begin{aligned} P_{DC}(X) &= P_{DC}(Ee(X) + \varepsilon_{Ee,i}(X), Tc(X) + \varepsilon_{Tc,i}(X)) \\ &= \dots \end{aligned}$$

# Uncertainty Quantification: Isotropic sky diffuse model



- Partition residuals by month, sky condition and time of day; detrend
- Create and sample stochastic process model for detrended residuals

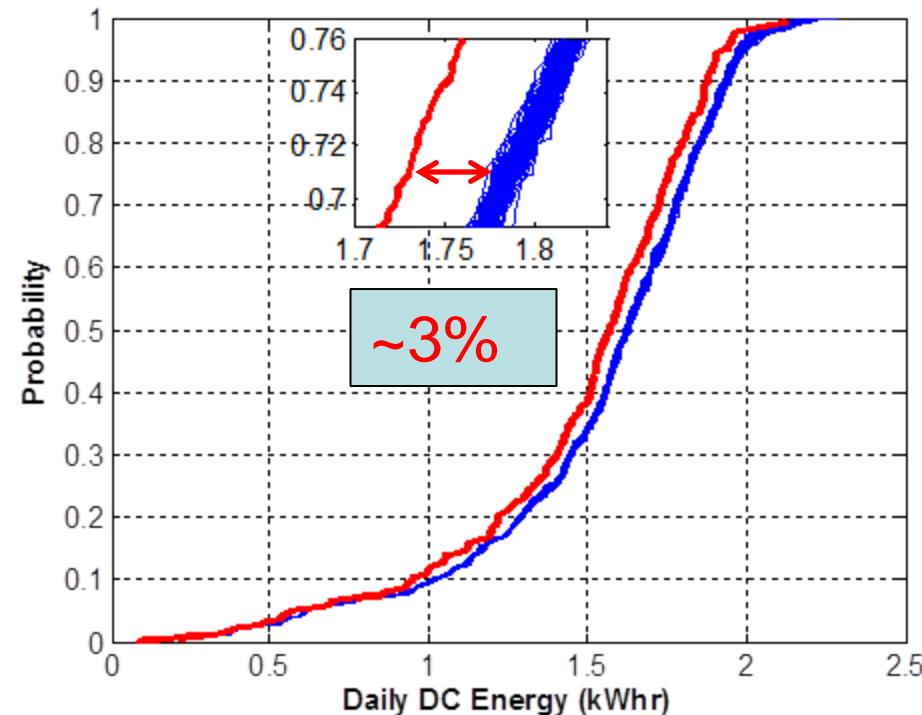


# Uncertainty in daily energy

- Red curve is ‘baseline’ : model results without applying sampled errors
- 100 blue curves result from 100 error samples
- Shift indicates an overall bias toward overestimating energy
- But small variation among blue curves

Models are consistent but also consistently wrong

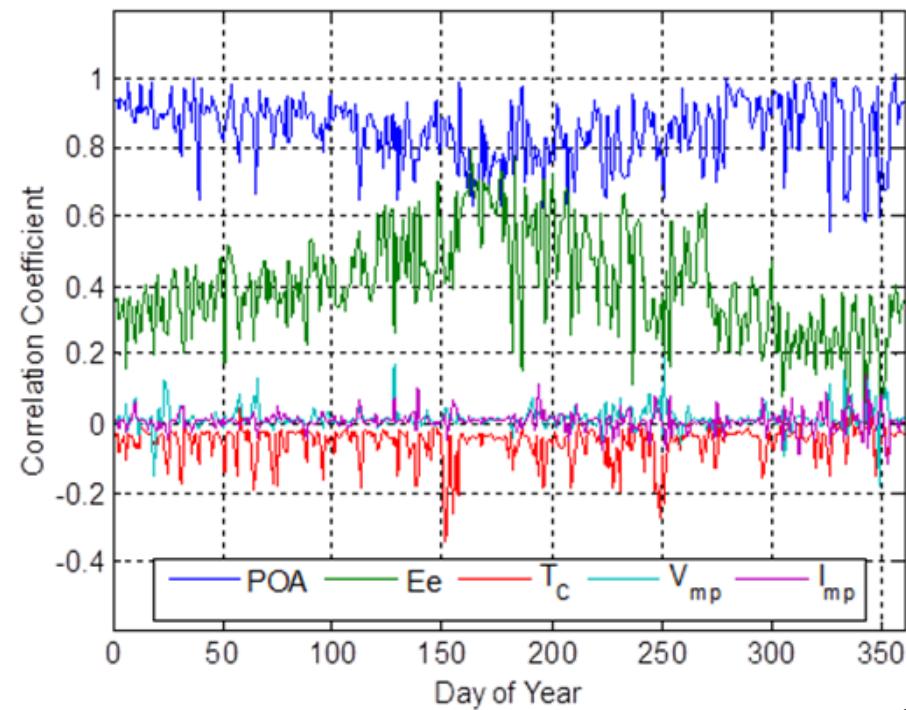
Distributions of daily energy: cSi module, isotropic sky model, Albuquerque data (other module, models, and data similar)



# Which models drive uncertainty?

- Uncertainty in POA model dominates (relative to uncertainty in other models)
- Independent of module type, POA model and data source
- Uncertainty distributions for POA models aren't that different

Stepwise rank regression of deviations in daily energy onto errors: cSi module, isotropic sky model, Albuquerque data (other modules, models, and data similar)



# Conclusions

- Given what we have considered (POA, Ee, Tc, DC output), uncertainty in modeled energy is relatively small ~3%
- Analysis indicates POA model uncertainty dominates
- POA model error appears to be systematic

See Lave, Hansen, Hayes, et al., PVSC 40, for analysis of POA models

## Future work:

- Consider remaining modeling steps : e.g., effective irradiance separately broken down into reflection losses, spectral mismatch, soiling
- Research to improve POA models

# Thank you