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# Computational Modeling of Algal Growth in Open Ponds

Jessica Drewry

Patricia Gharagozloo

# Algal biofuels benefit the environment

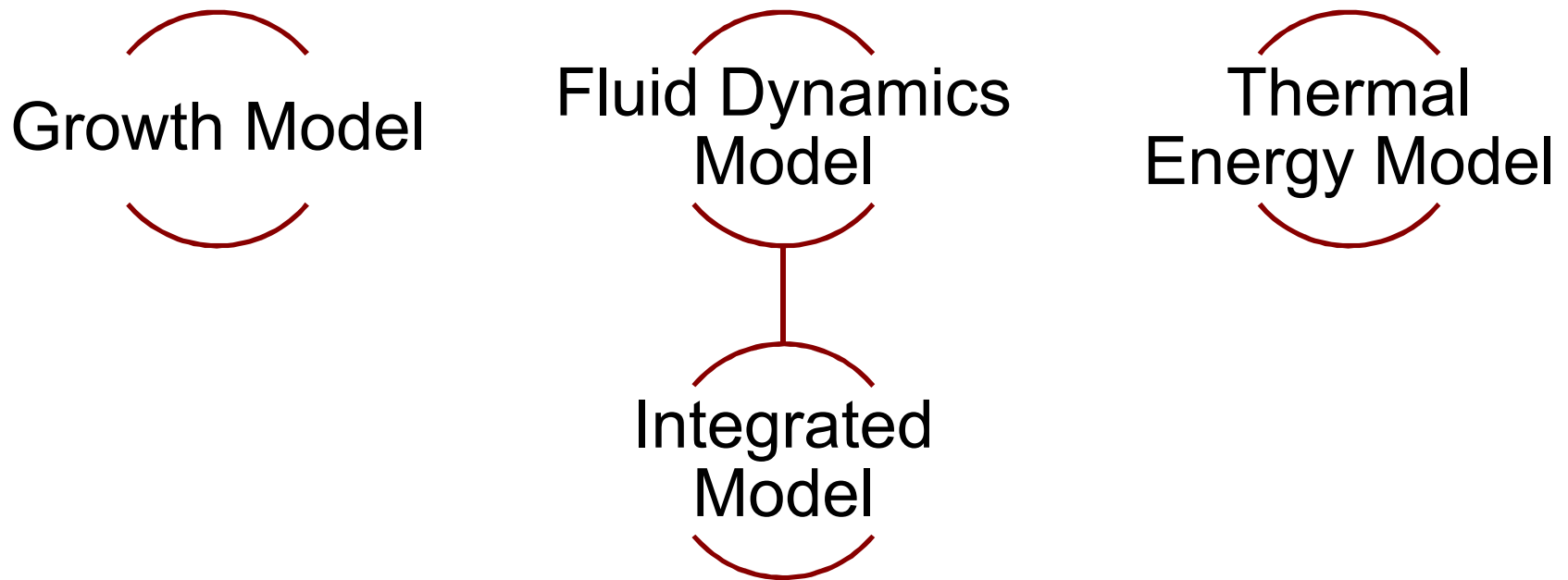
- Help meet the demand for alternative energy
- Grown on non-arable land
- Utilize wastewater
- Consume CO<sub>2</sub>



# Computational modeling streamlines optimization

- Make cultivation more environmentally and economically feasible
- Account for a large number of variables
  - Algal strain
  - Environmental conditions
  - Pond design
  - Mixing
  - Geographic location
- Reduce experimentation cost and time

# Components of an effective model



# Growth Model

$$S_{algae} = K_{ag} \Phi_a - K_{ar} \Phi_a - K_{am} \Phi_a - \omega_a \frac{d\Phi_a}{dz} - \sum Z_\mu \Phi_{zoo} \frac{\sigma_a \Phi_a}{\sum \sigma_a \Phi_a + \sigma_{pom} \Phi_{lpom} + \sum \sigma_{zoo} \Phi_{zoo}}$$

$$K_{ag} = P_m \lambda_{temp} \lambda_{light} \lambda_{nutreints} \lambda_{pH}$$

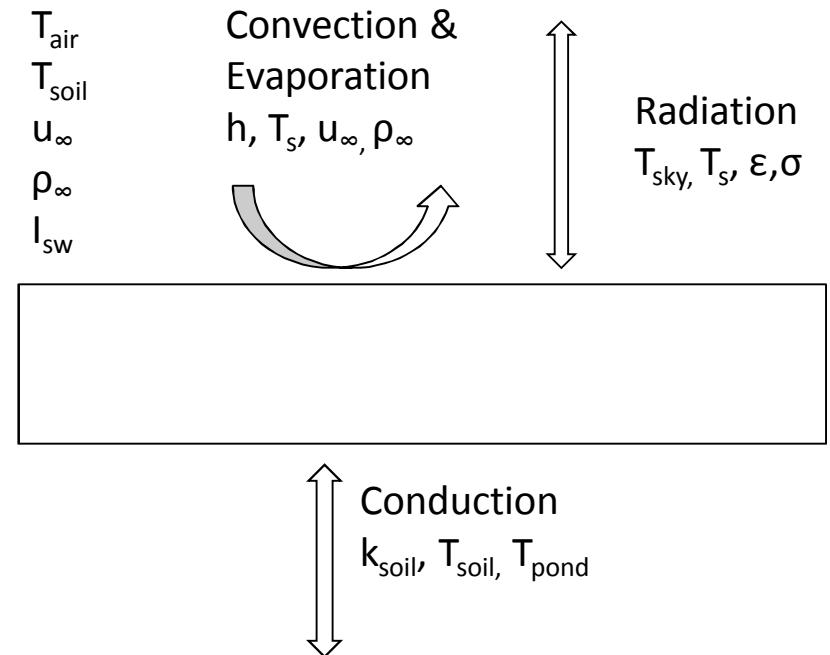
$$\lambda_{temp} = \begin{cases} \exp(-K_1(T_{opt,1} - T)^2) & \text{for } T < T_{opt,1} \\ 1 & \text{for } T_{opt,1} \leq T \leq T_{opt,2} \\ \exp(-K_2(T - T_{opt,2})^2) & \text{for } T_{opt,2} < T \end{cases} \quad \lambda_{nutrients} = \min\left(\left(\frac{\phi_n}{\phi_n + K_n}\right), \left(\frac{\phi_p}{\phi_p + K_p}\right), \left(\frac{\phi_c}{\phi_c + K_c}\right)\right)$$

$$\lambda_{light} = \left(\frac{I}{I_s} \exp\left(-\frac{I}{I_s} + 1\right)\right)$$

$$\lambda_{pH} = \frac{[H^+]}{[H^+] + k_{OH} + [H^+]^2/k_H}$$

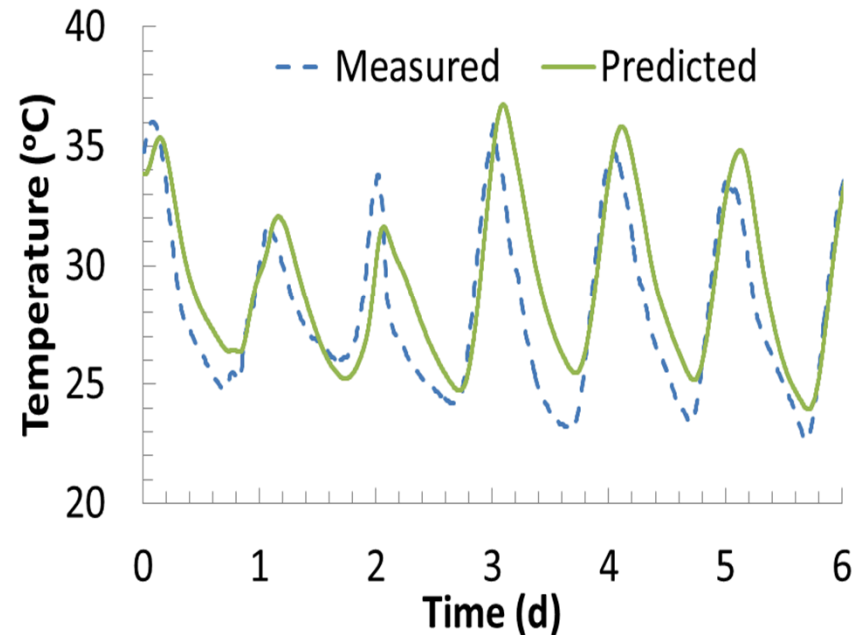
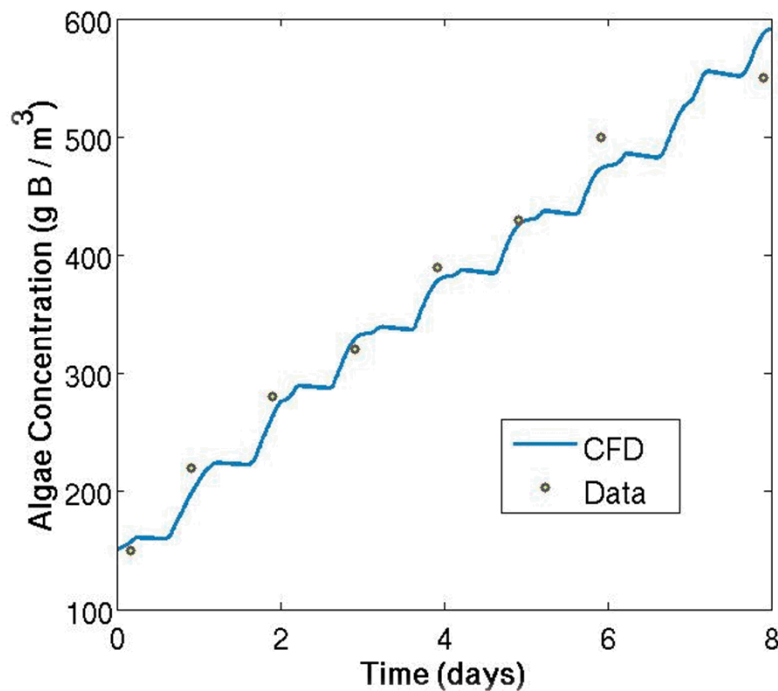
# Energy Model

- $q''_{lw} = \varepsilon\sigma(T_{sky}^4 - T_{surface}^4)$
- $q''_{conv} = \bar{h}(T_{\infty} - T_s)$
- $q''_{evap} = h_{fg}h_m(\rho_{sat} - \rho_{\infty})$
- $q''_{cond} = k(T_{pond} - T_{soil})$
- $q''_{sw}$ , from weather data



# Previous experimental validation

- 2D model
- Experimental data from ASU



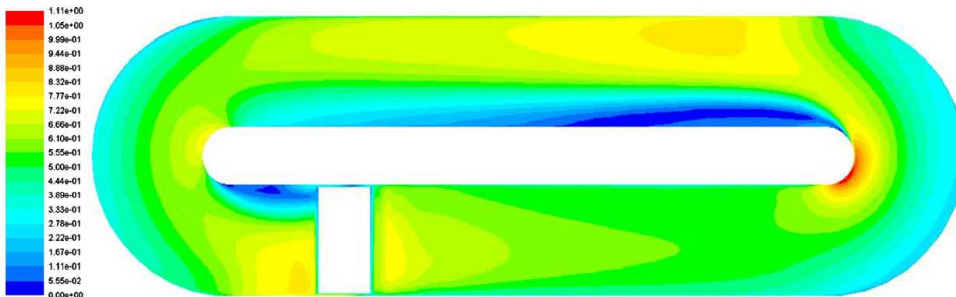
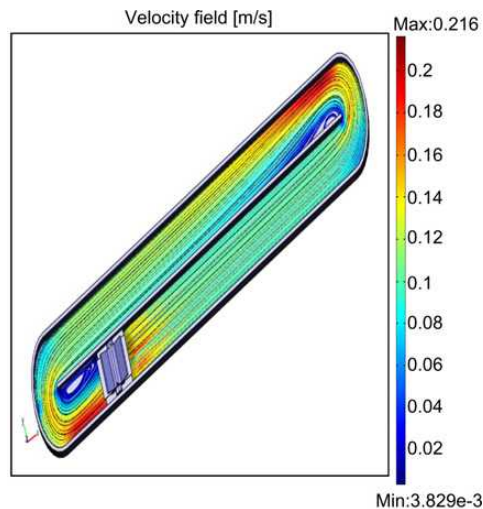
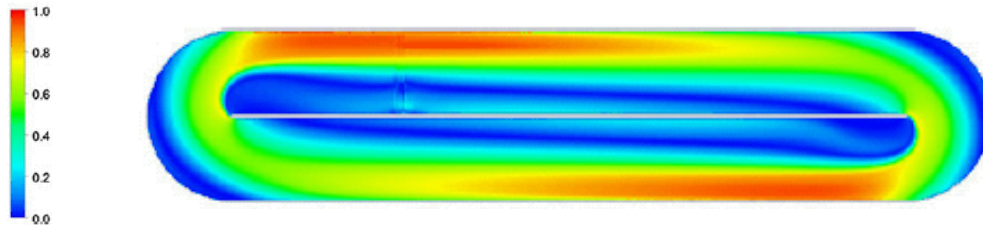
# Design and operation of ponds can affect algal growth

- Commercial ponds are typically mixed by paddle wheels and 180° bends
- Fluid dynamics affect algal growth
  - Species transport
  - Thermal energy transport
  - Exposure to solar irradiation





# Assumptions for modeling paddle wheels



- Momentum Source

- Liffman et al. 2013

- Inlet/ Outlet

- Hadiyanto et al. 2013

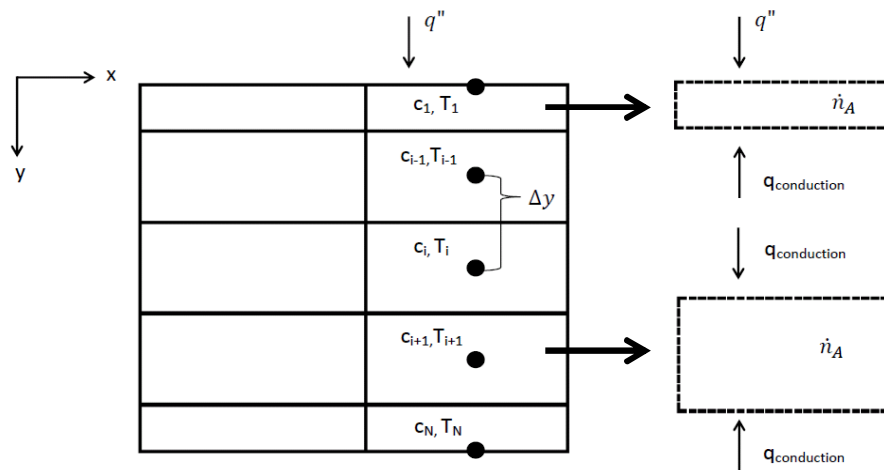
- Movable Mesh

- Hreiz et al. 2014

# Goals to implement and validate the computational model

- Determine if computational growth models can capture the effects of mixing
- Quantify the effect of model assumptions on computational growth models
  - Compare 2D unmixed 2D repeating boundary, 3D momentum source, and 3D inlet/ outlet models
- Compare computational results with experimental data
  - Data from the ATP<sup>3</sup> project
  - 1000 L ponds
  - Mesa, AZ
  - *Nannochloropsis oceanica*

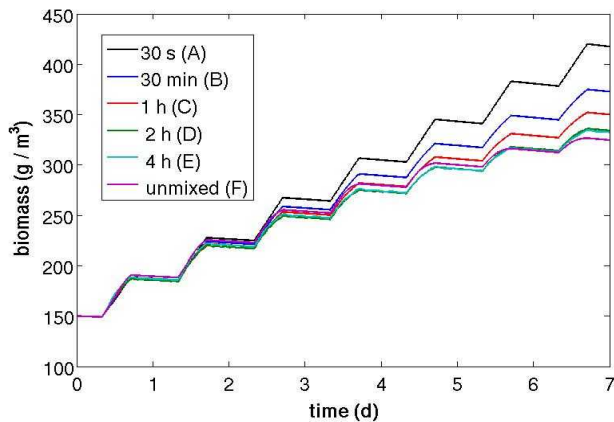
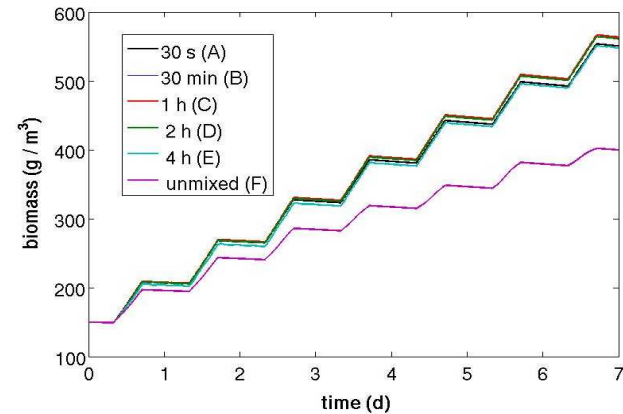
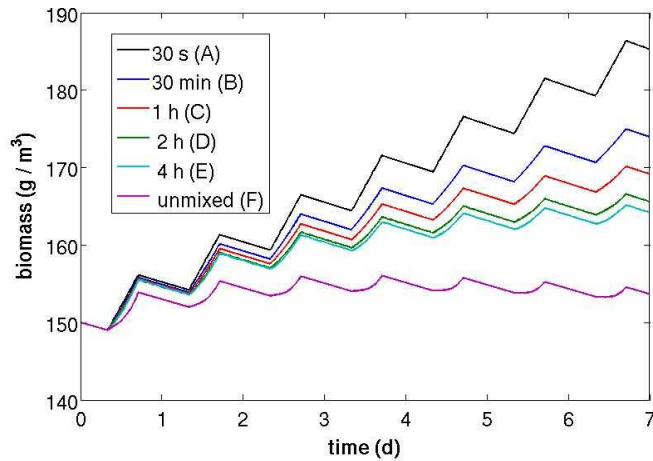
# Finite difference mixing model



Low Medium High

Temperature [C]	$12 \pm 2$	$22 \pm 2$	$32 \pm 2$
Intensity [ $\text{W m}^{-2}$ ]	300	600	900
Mixing time	30 s (A)	30 min (B)	1 h (C)
Mixing time	2 h (D)	4 h (E)	unmixed (F)

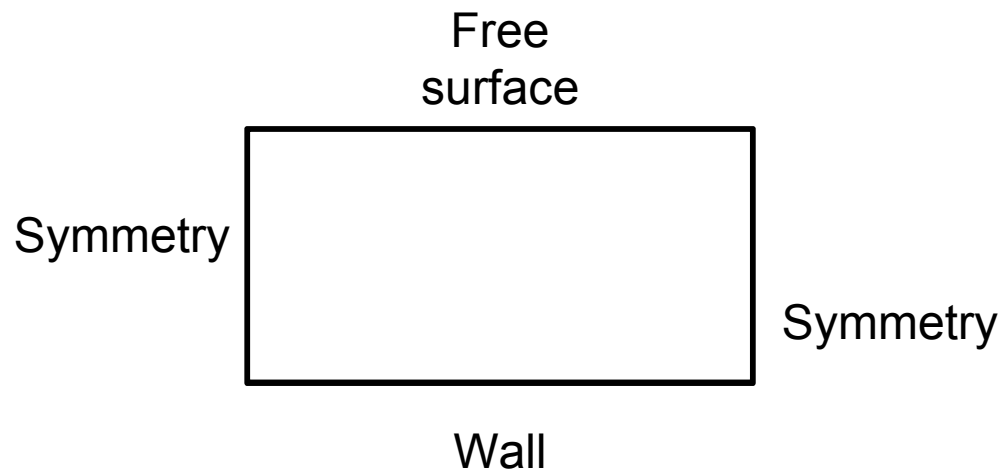
# Mixing affect on algal growth



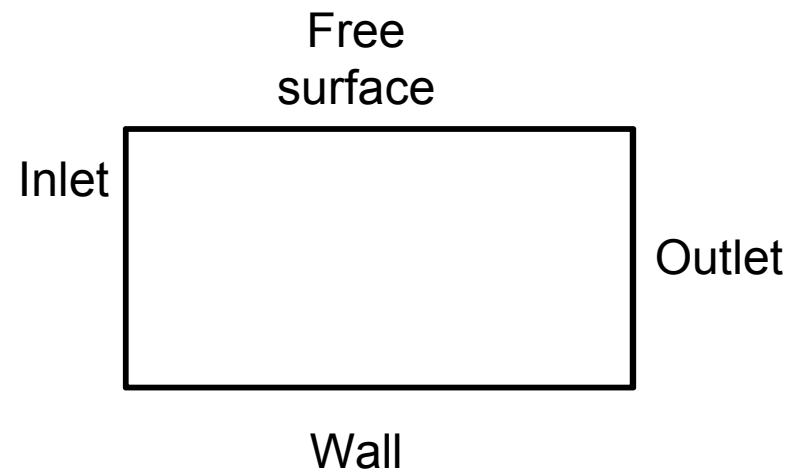
Biomass concentration as a function of time with both temperature and light held at low, medium, and high levels, respectively for ease of visualization.

# 2D Models

## Unmixed

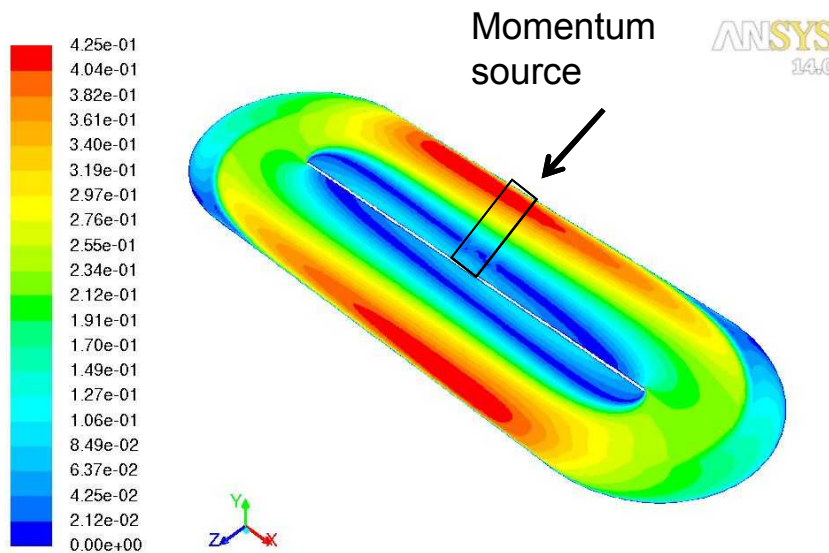


## Repeating Boundary

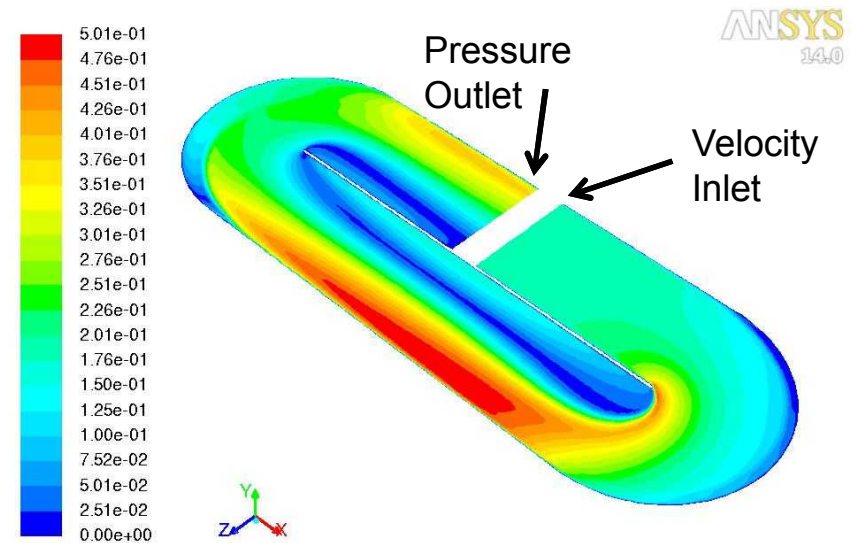


# 3D Models

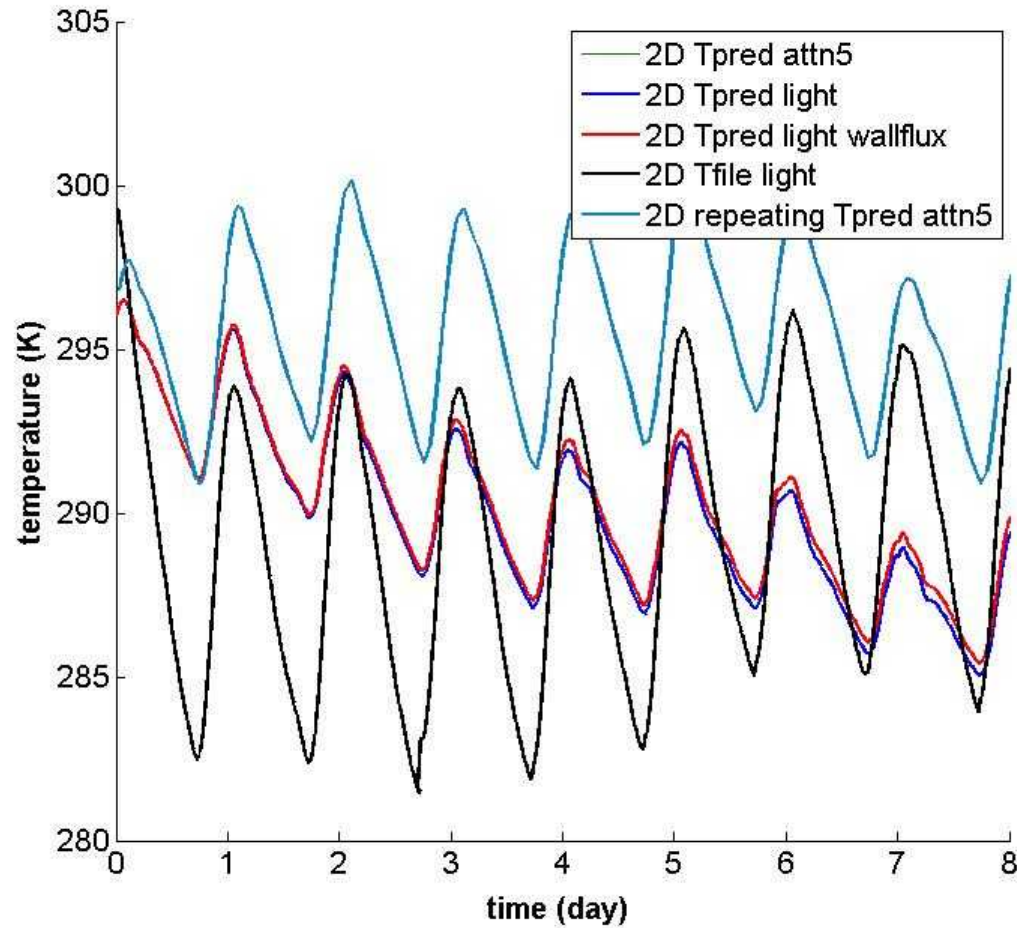
## Momentum Source



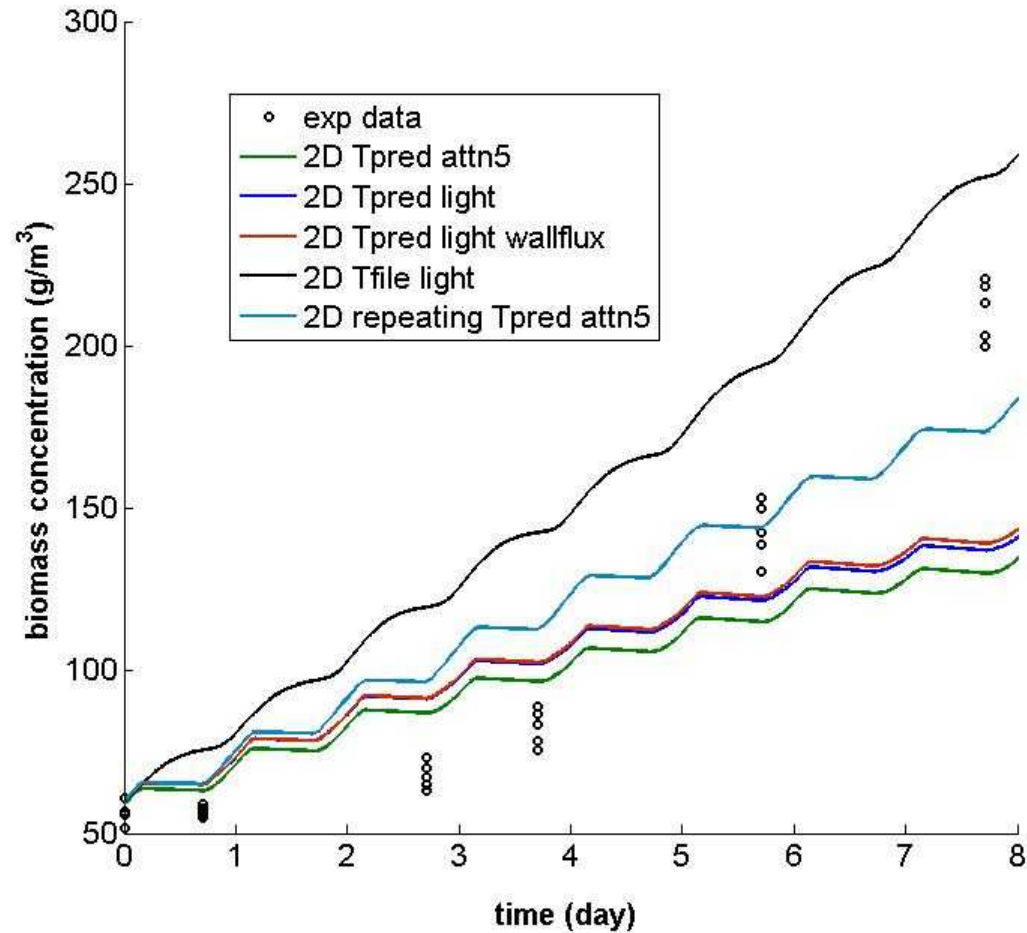
## Inlet/ Outlet



# Pond Temperature



# Biomass Concentration





# Conclusions

- Computational modeling is an effective tool in modeling and optimizing algal growth
- 2D models give good results for large ponds
- 3D models are most likely needed to model detailed hydrodynamic and temperature effects in small or well mixed ponds