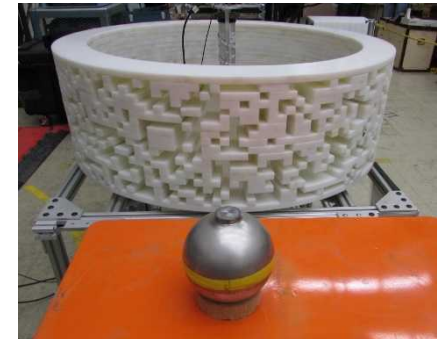
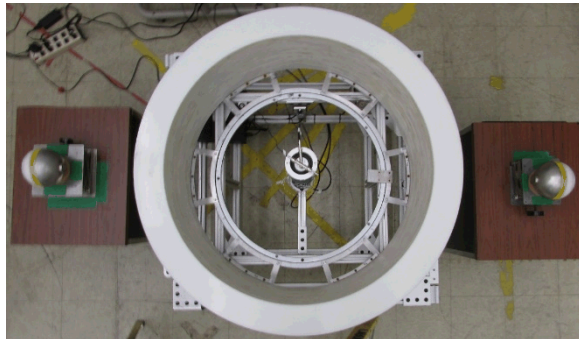
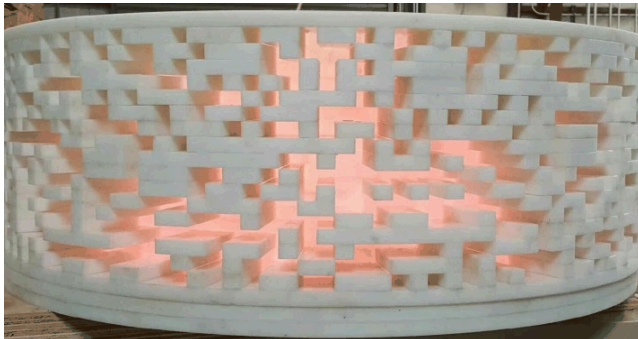


CONFIDENTIAL

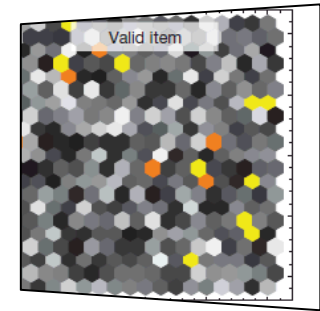
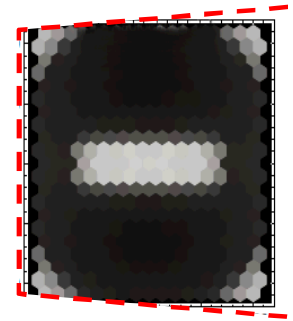
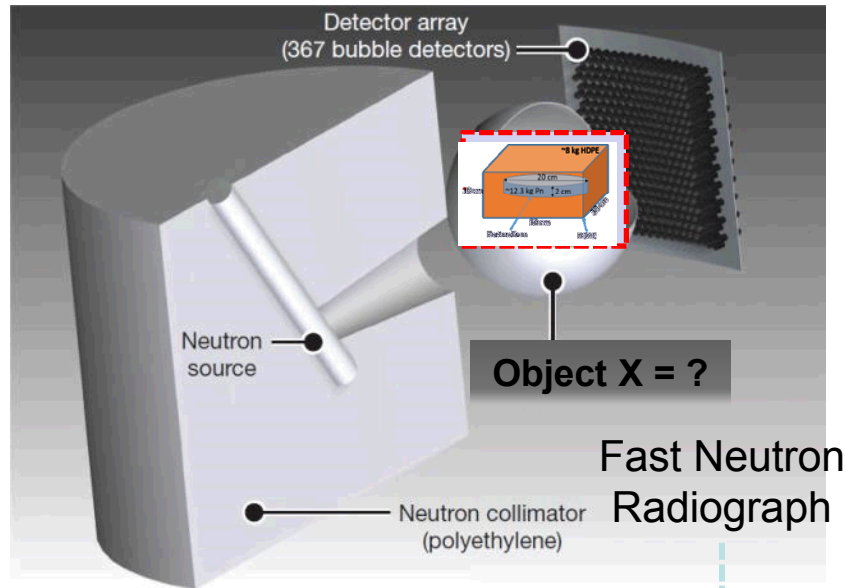
CONFIDENTIAL



CONFIDANTE Research Questions

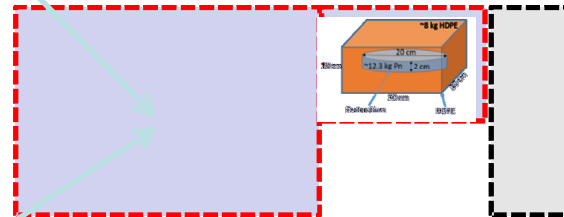
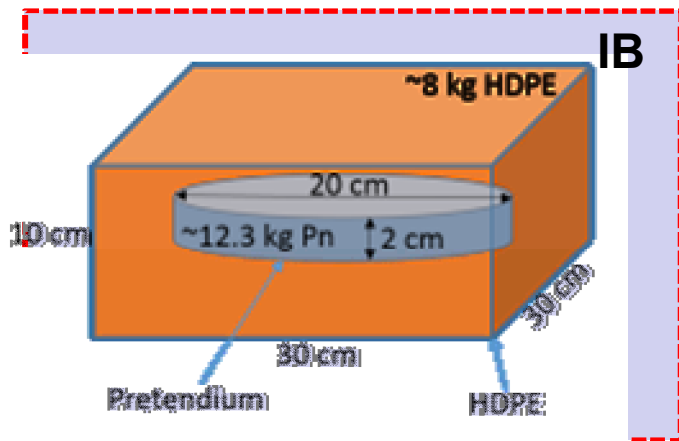
Peter Marleau

Zero Knowledge Protocols – Glaser, Barak, and Goldston



Analog bubble detectors with preloaded complement "template"

Flat featured image (NULL) indicates a true positive.

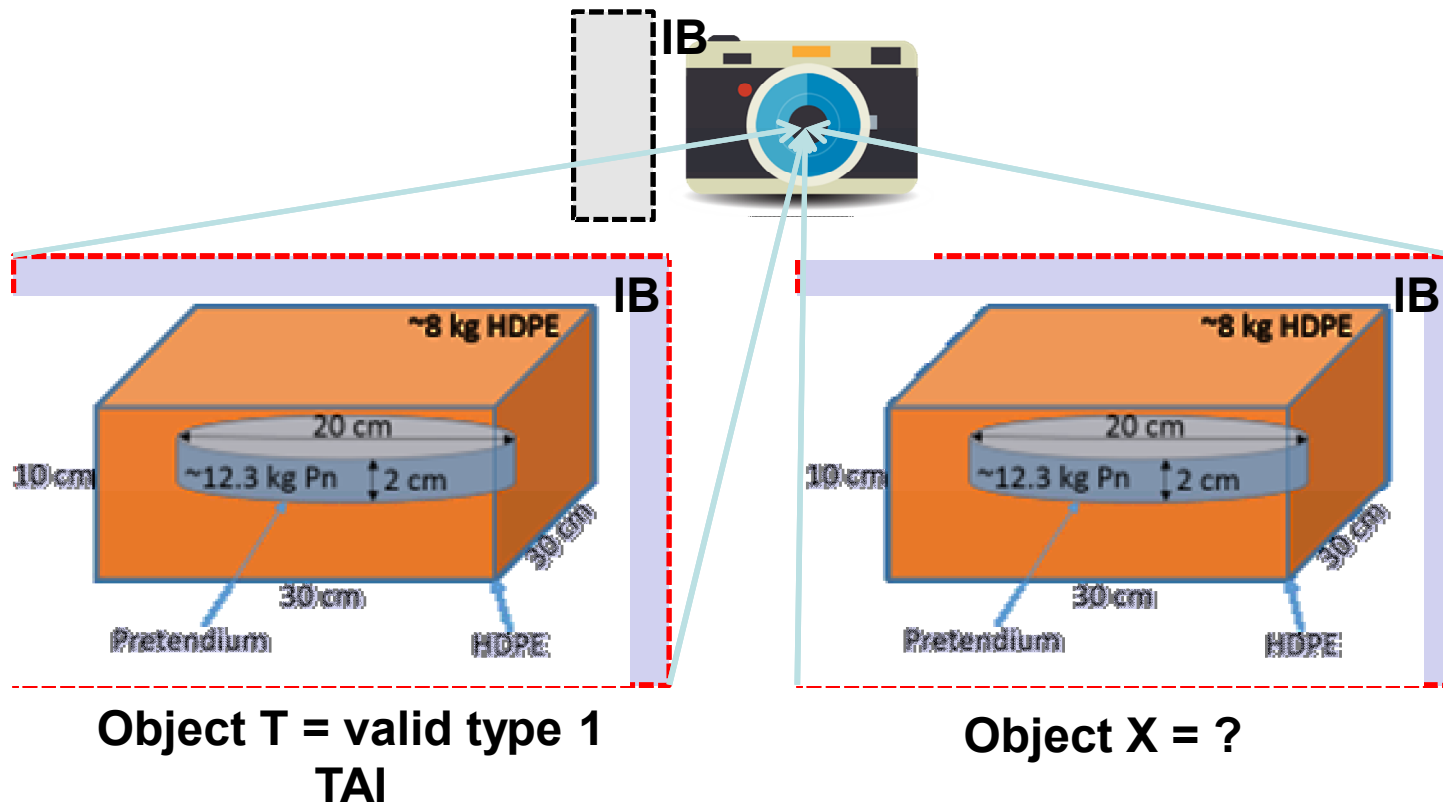


PASS/FAIL

Has this boundary moved?

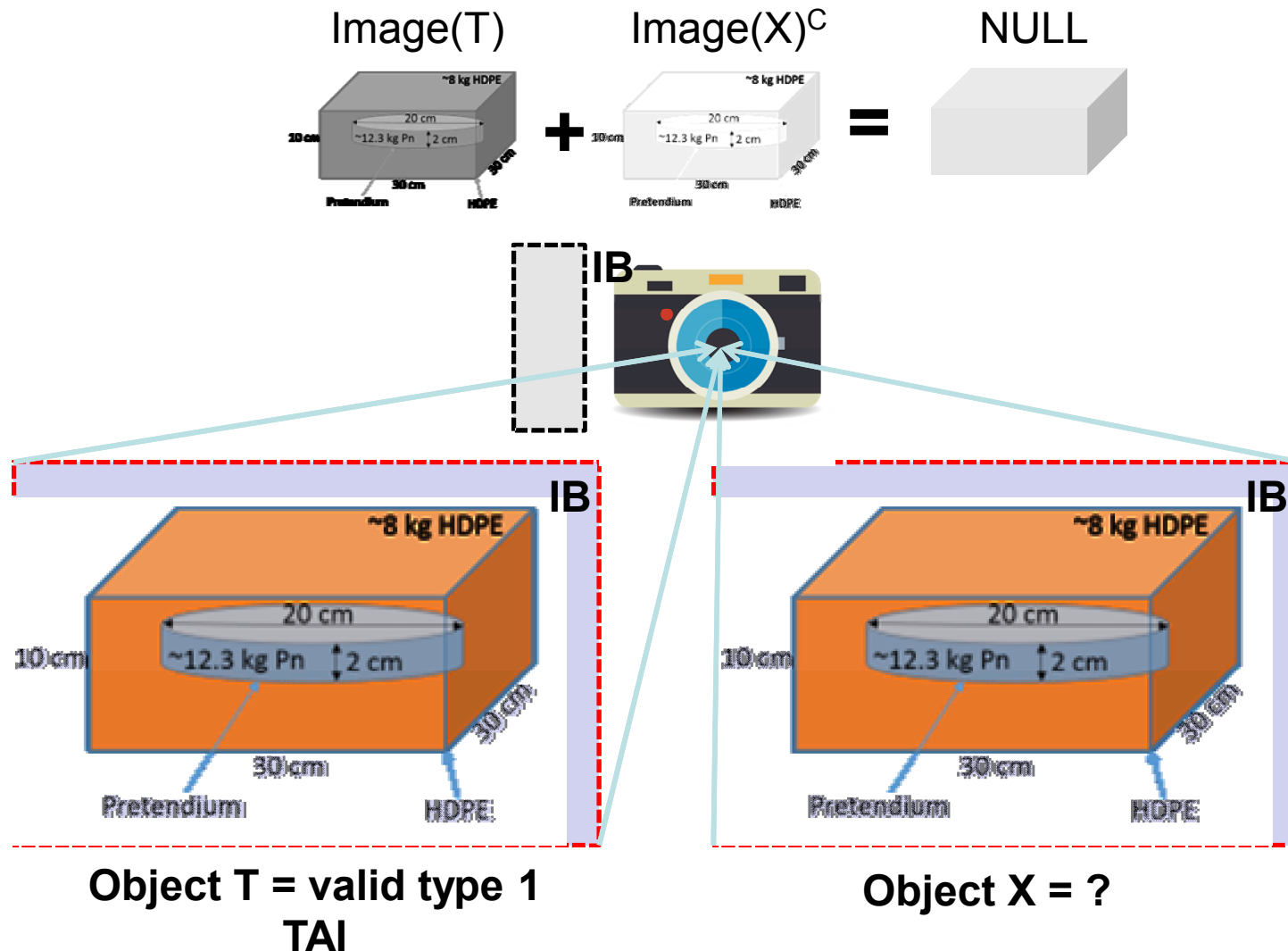
Zero Knowledge comparison measurement?

- Is there a physical implementation of the confirmation measurement that an inspecting party can watch and authenticate?
- **It would be great if we could get a physical NULL as an indication of positive confirmation at all times, *not just at the end.***

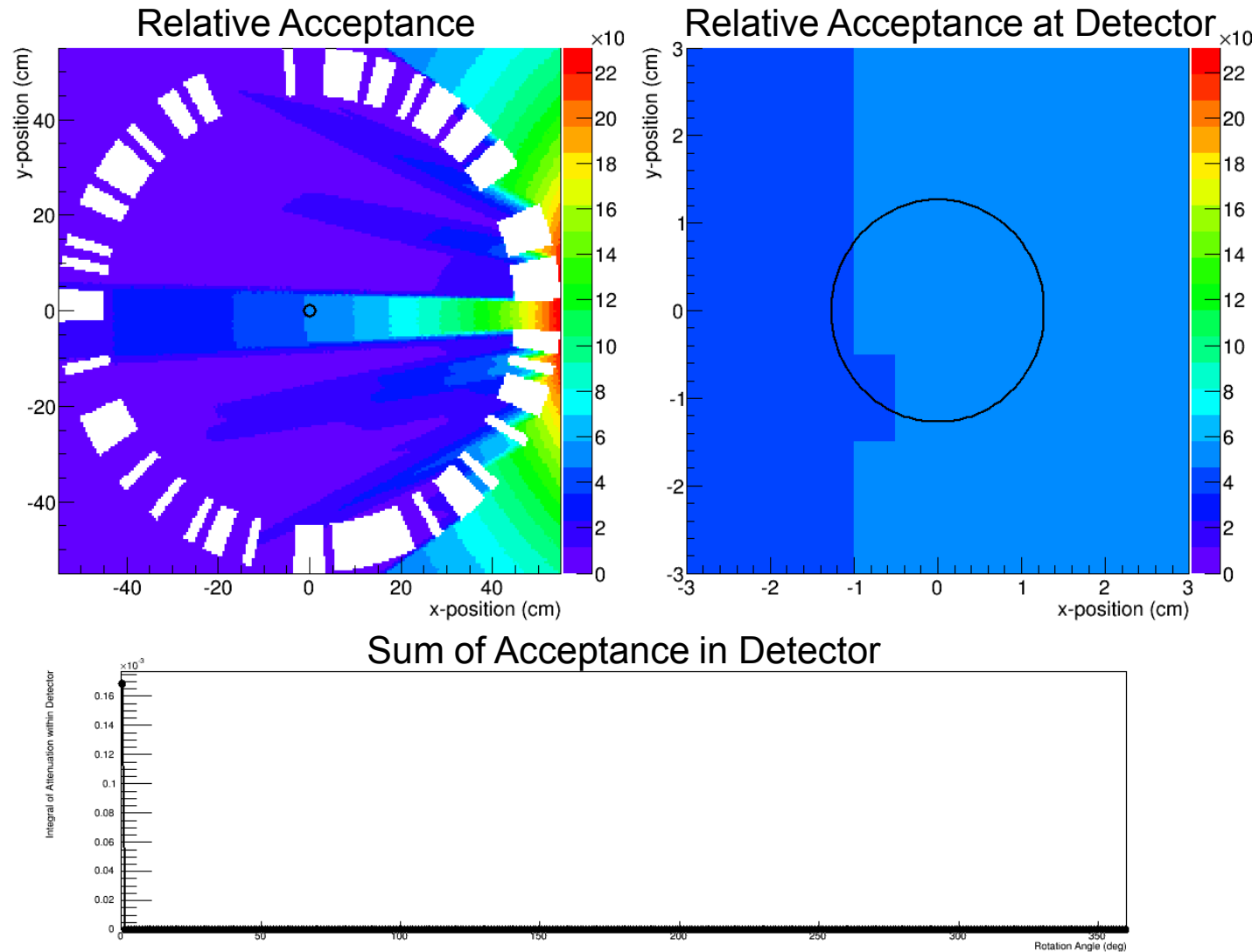


Proposal – complementary comparison

- What we need is to turn one image into its complement ***at all times***.



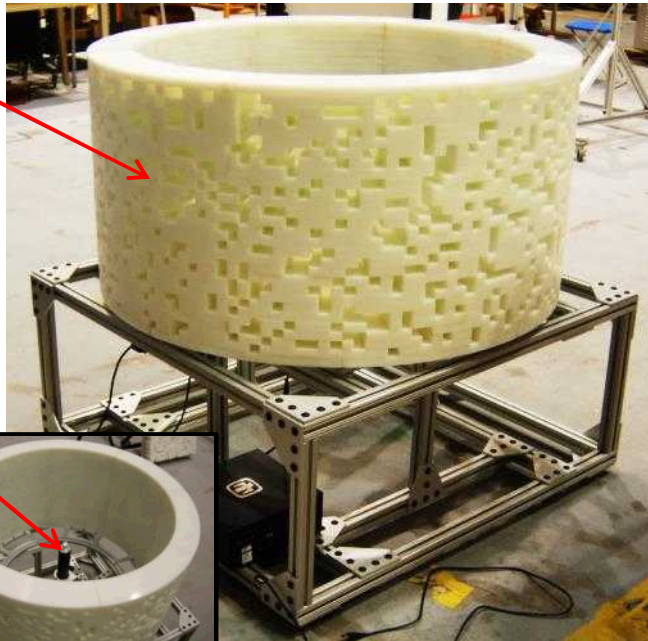
Time Encoded Imaging



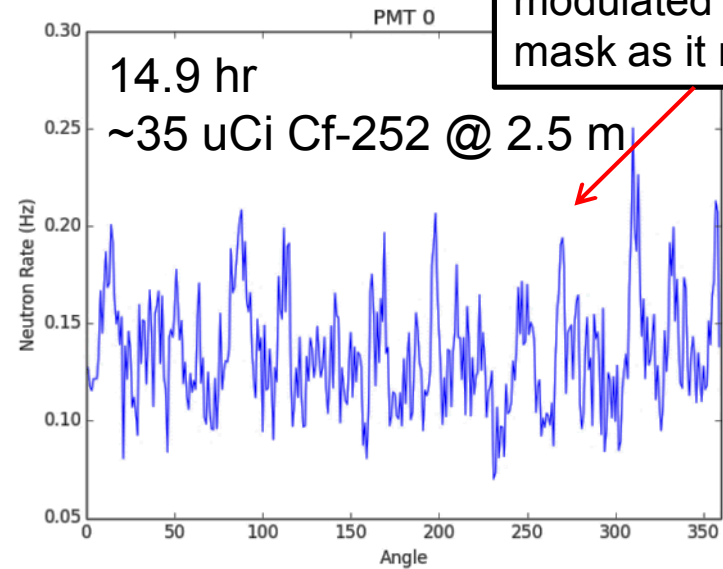
2D Time-encoded Imaging (TEI)

J. Brennan, E. Brubaker, M. Gerling, P. Marleau, K. McMillan, A. Nowack, N. LeGalloudec, M. Sweany,
"Demonstration of Two-dimensional Time-encoded Imaging of Fast Neutrons", Nuclear Instruments and Methods A, 2015

2-d
coded
mask



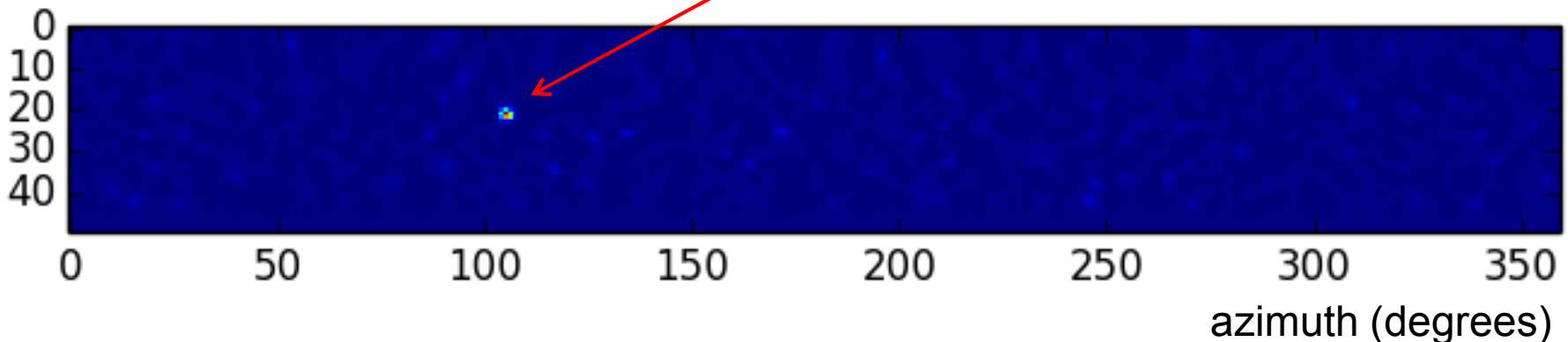
Single
1"D x 1"
LS pixel



Single pixel rate is
modulated by the
mask as it rotates.

Modulation pattern is unfolded to 2-D image

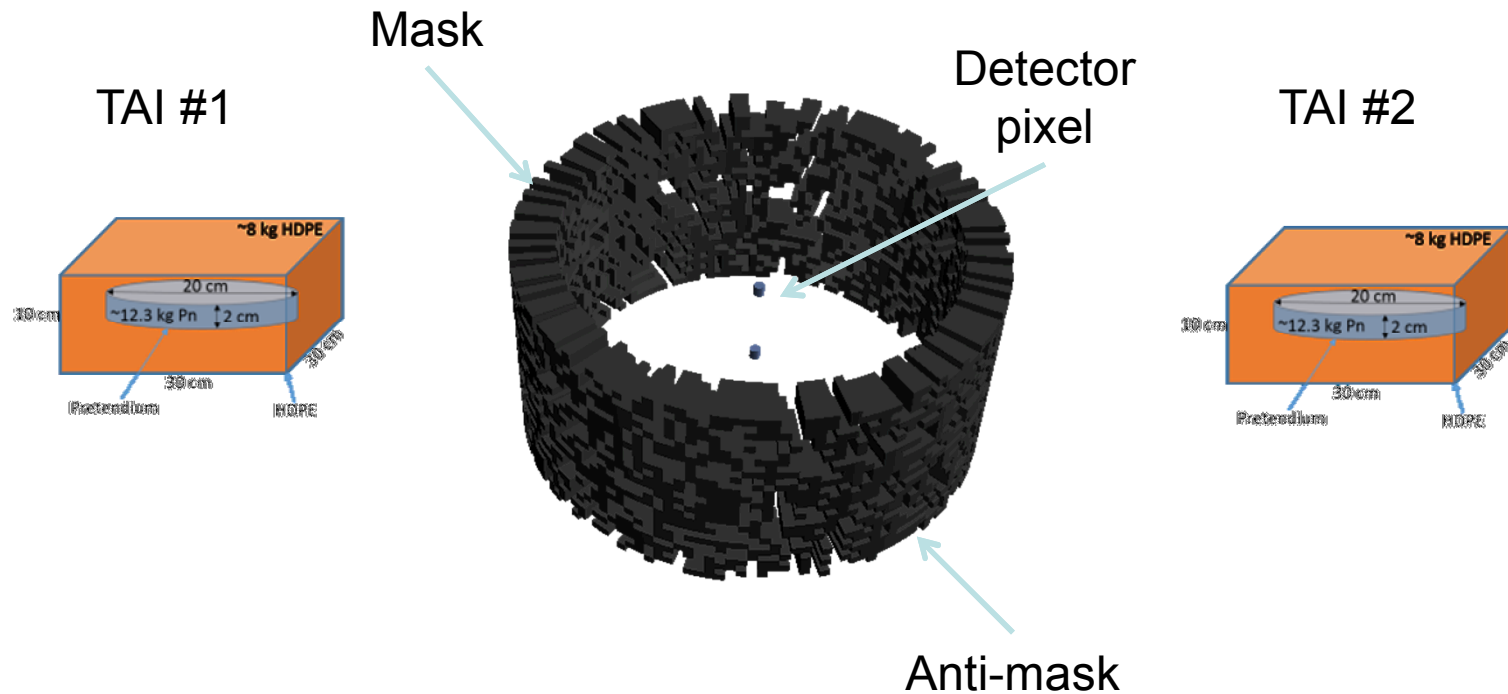
Arb. Bin idx in [-1 m, 1 m]



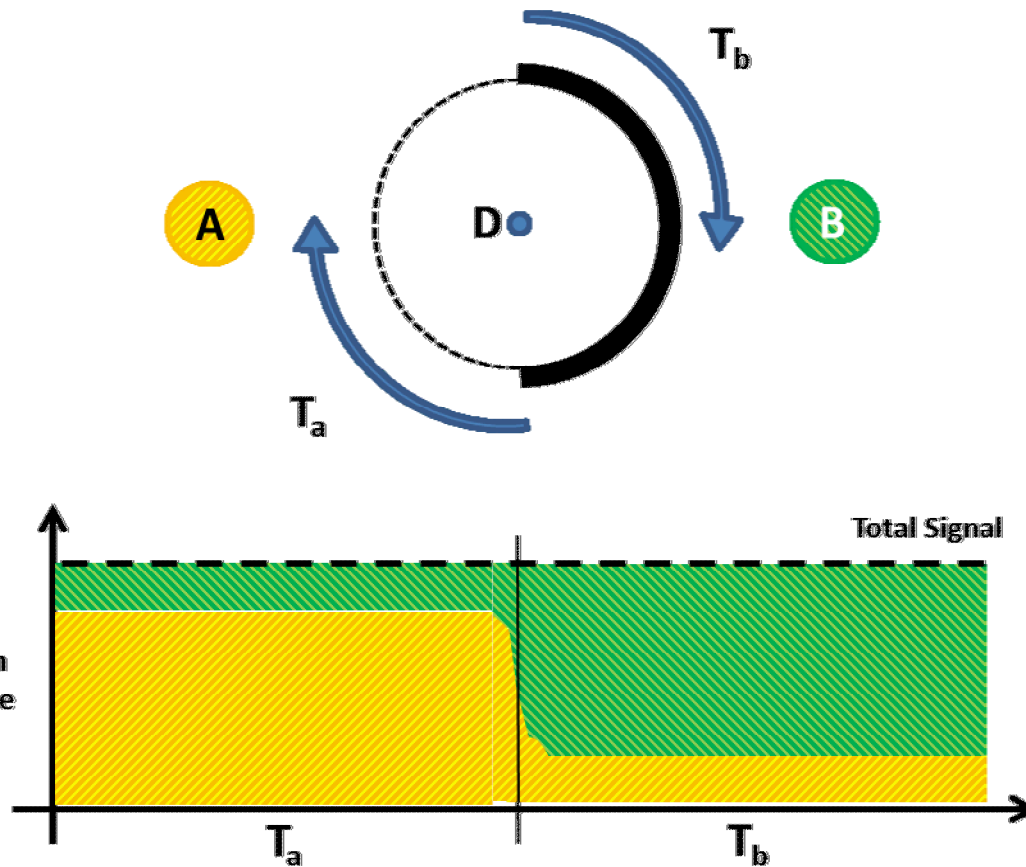
Here's where the magic happens ...

If the mask is designed such that one side is the anti-mask of the other, then **TAI #2 projects the anti-image of TAI #1 at all times**

if and only if they are identical!

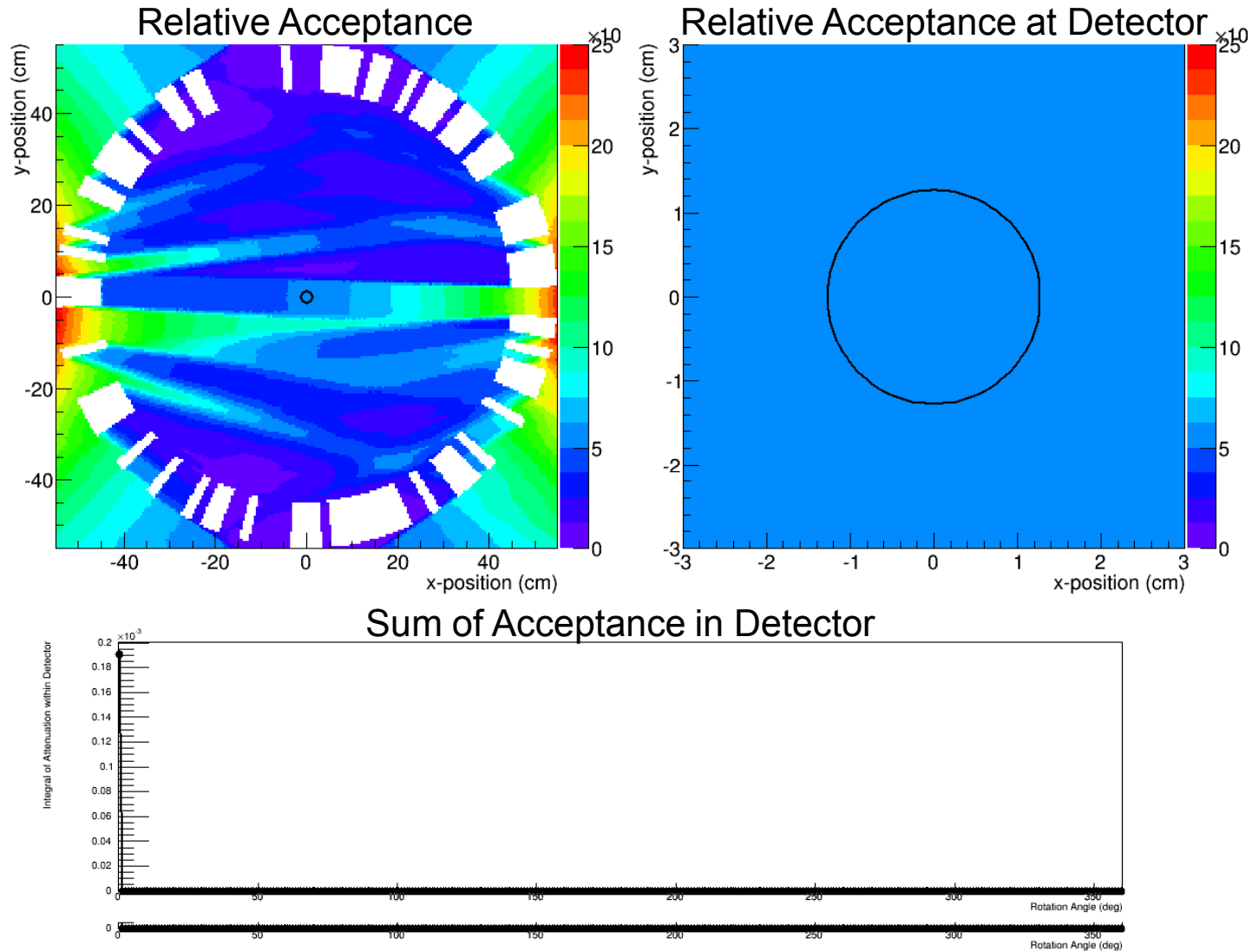


A very simple example

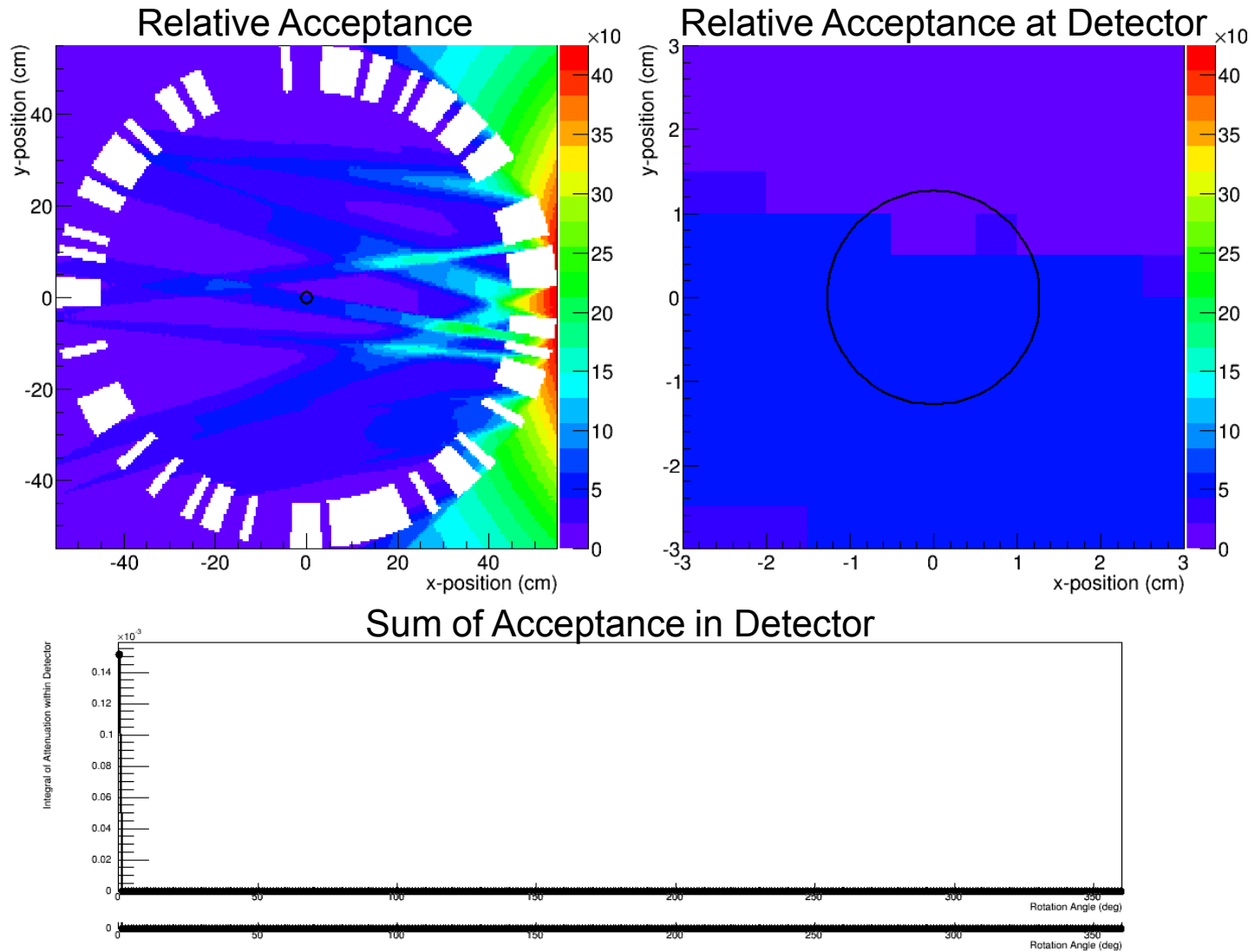


- The simplest possible mask with this property: half mask, half aperture.
- The fraction of total count rate coming from A and B is unknown at any given angle.
- In this example, the location (and shape) of the boundary between regions is not revealed.

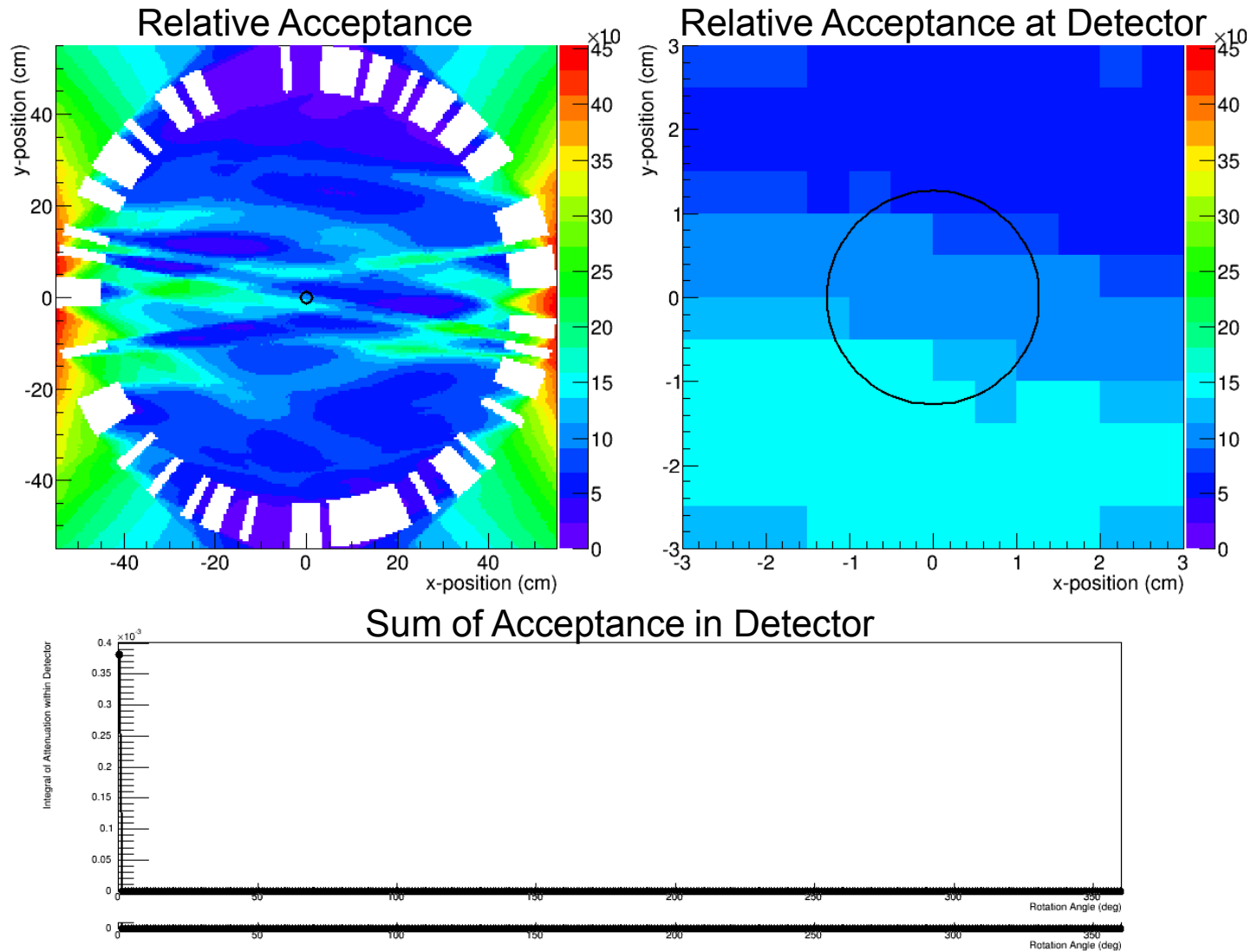
Single Point Source on opposite sides



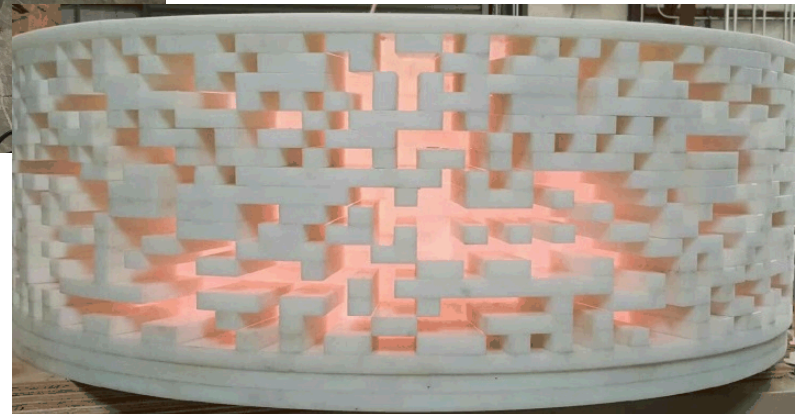
Two Point Sources on one side



Two Point Sources on opposite sides

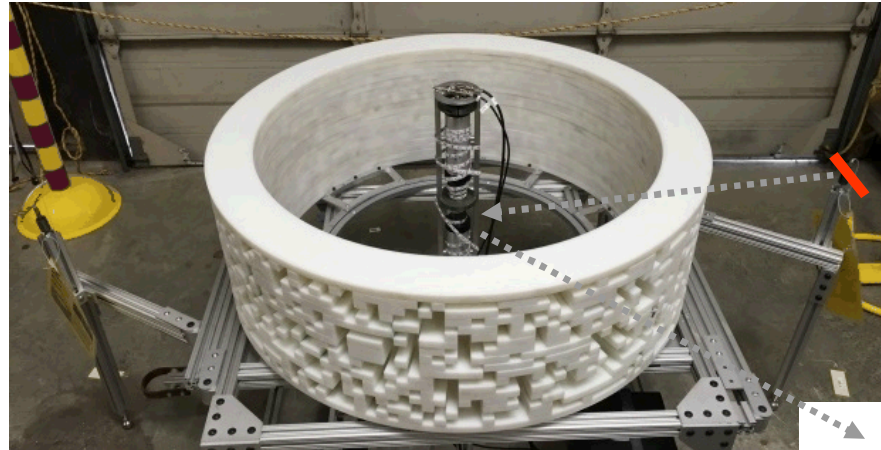


CONFIDANTE

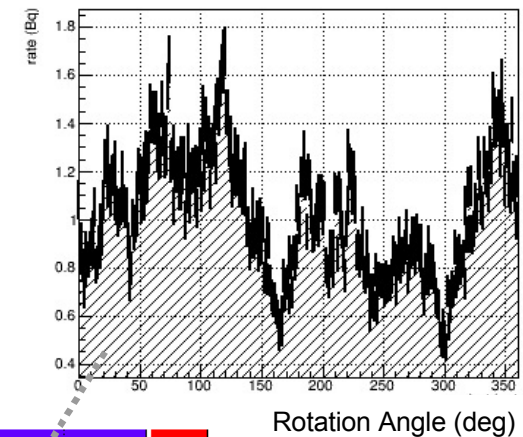


Results – Double point source measurements

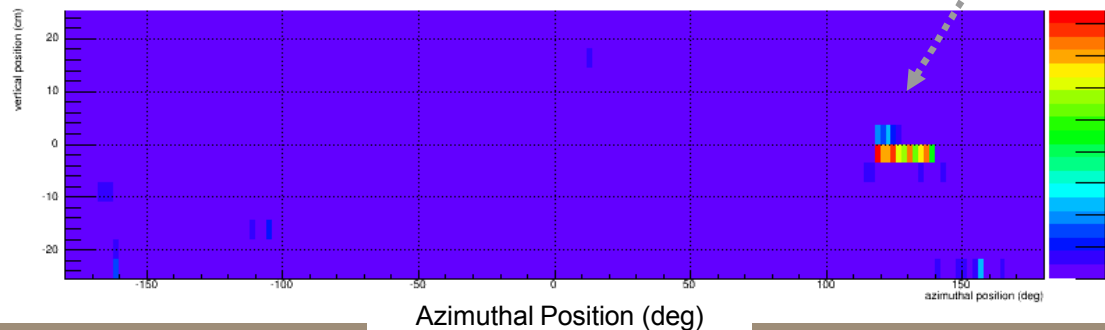
Measurement of a double “line” source on one side (~20 hours)



Neutron Rate

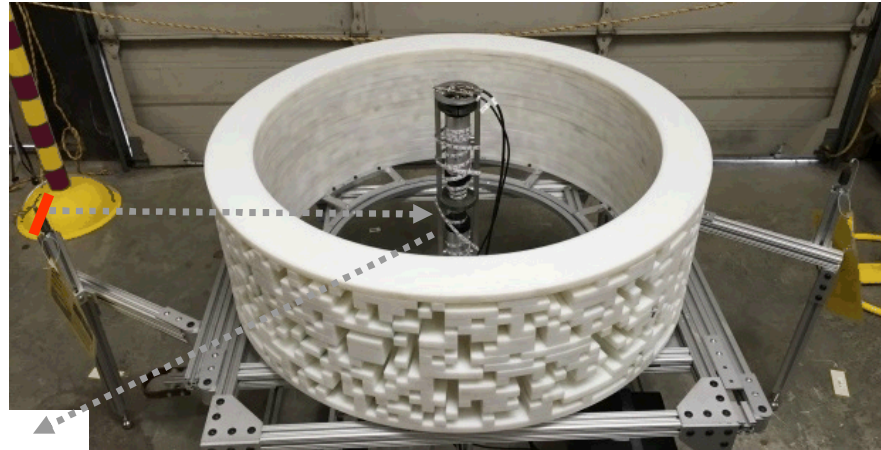


MLEM Reconstruction

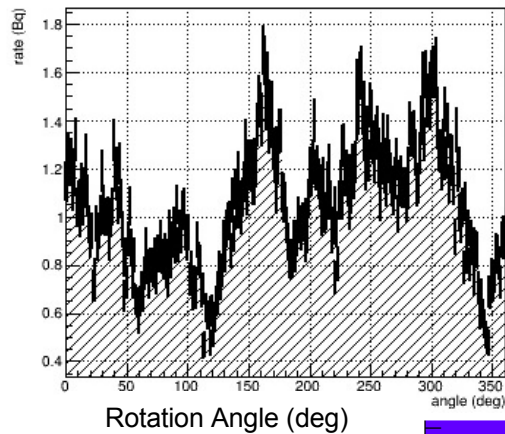


Results – Double point source measurements

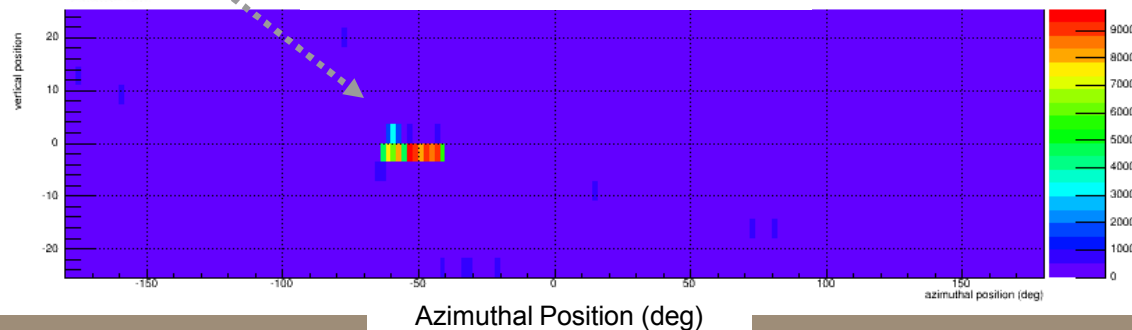
Measurement of a double “line” source on the opposite side (~20 hours)



Neutron Rate

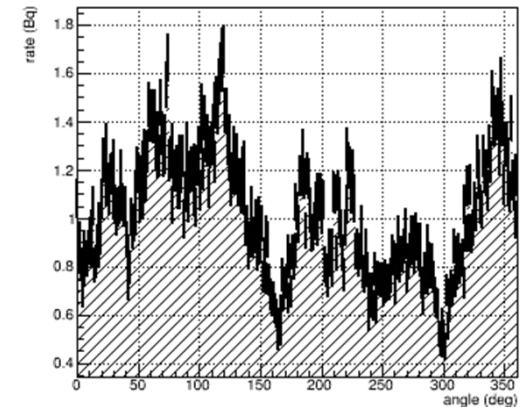
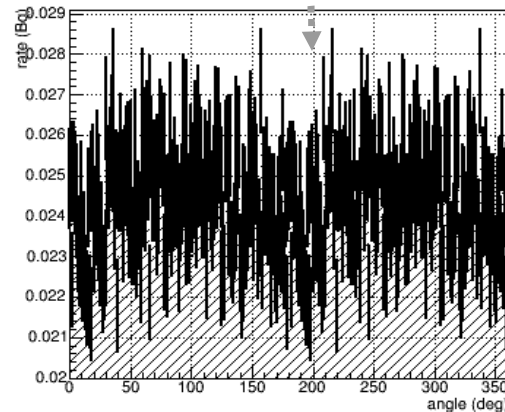
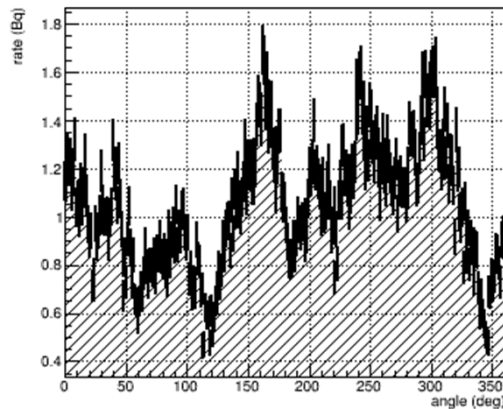
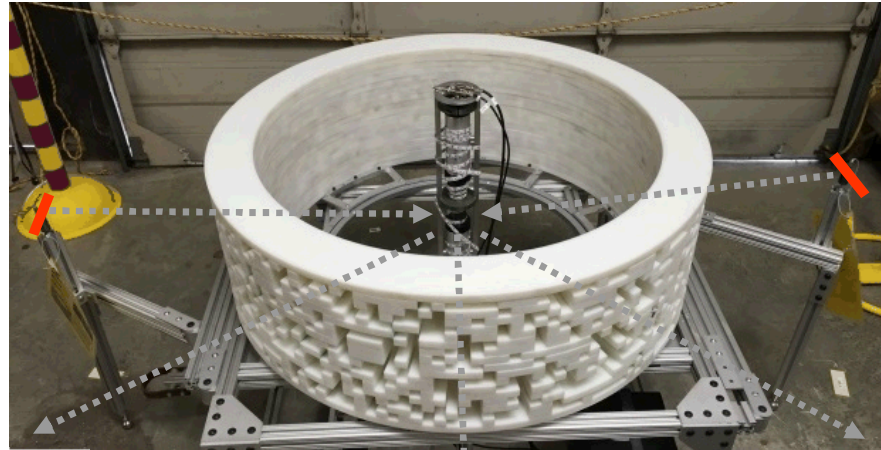


MLEM Reconstruction



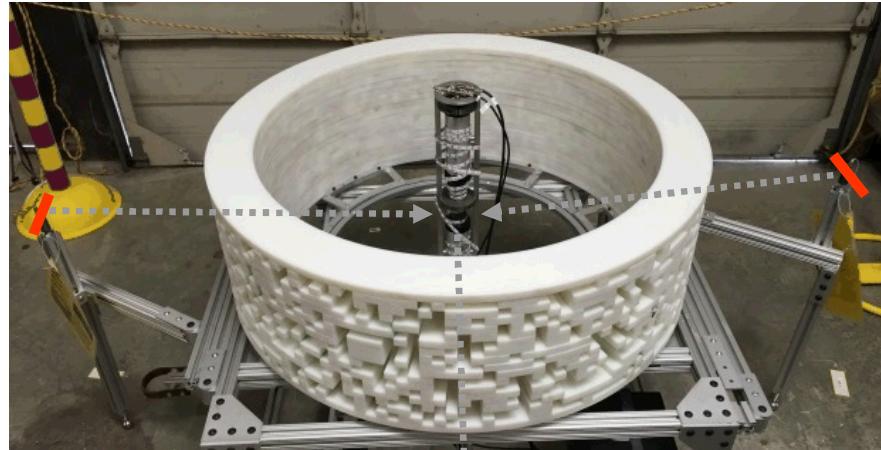
Results – Double point source measurements

Measurement of
two double “line”
sources on
opposite sides
(~20 hours)



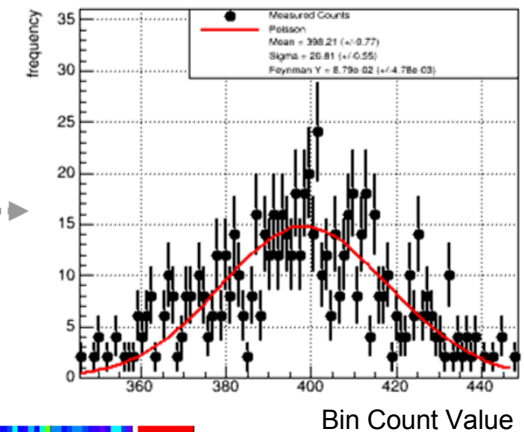
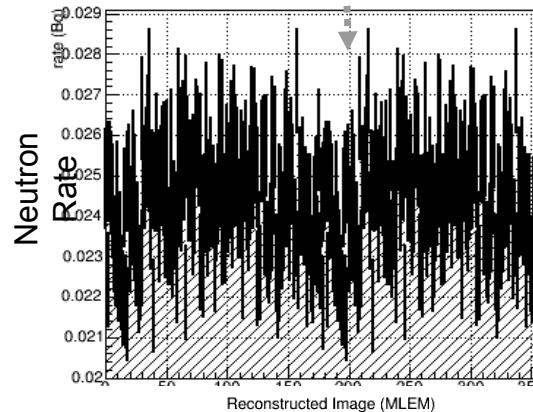
Results – Double point source measurements

Measurement of
two double “line”
sources on
opposite sides
simultaneously
(~20 hours)

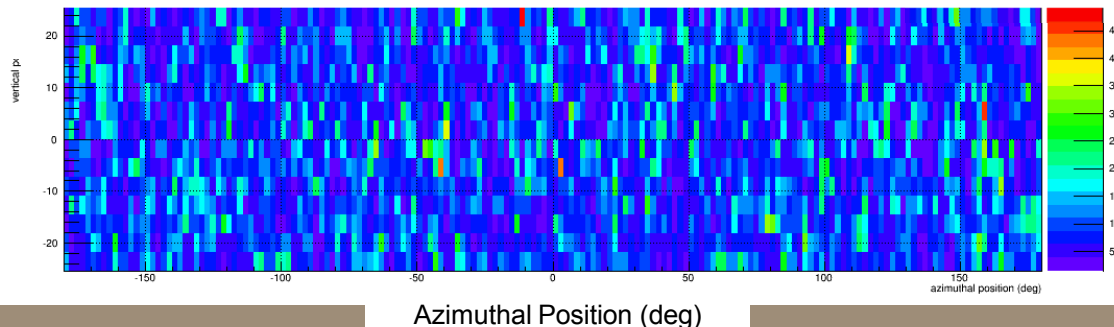


$$\begin{aligned}\text{Feynman } Y \\ &= \left(\frac{\text{variance}}{\text{mean}} - 1 \right) \\ &= 0.0354\end{aligned}$$

Count Distribution
(Poisson – red curve)

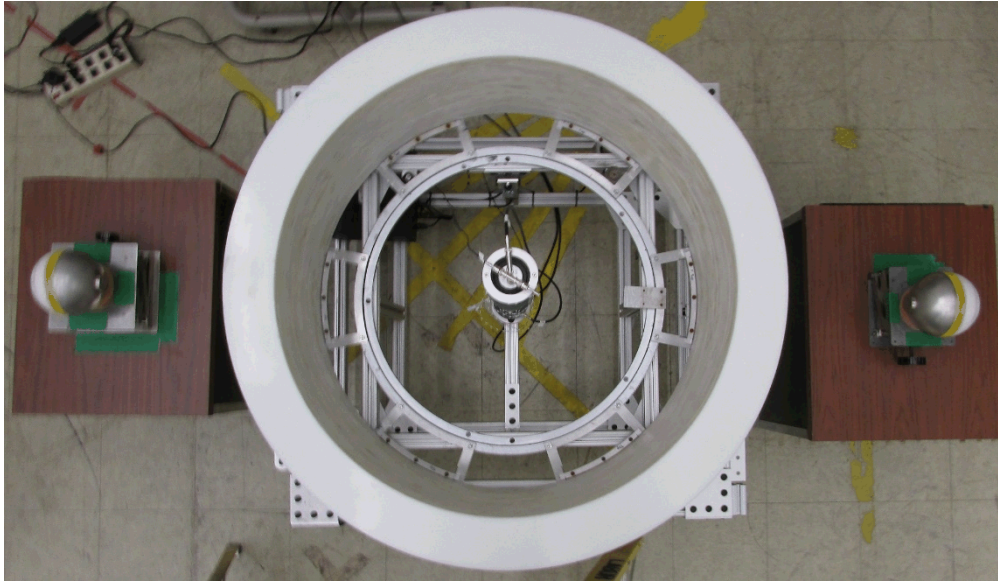


MLEM
Reconstruction



Azimuthal Position (deg)

LLNL's PuO₂ Hemisphere comparison



- One hemisphere was placed on either side of CONFIDANTE (180 deg. apart).
- ~68 hours of data was taken.

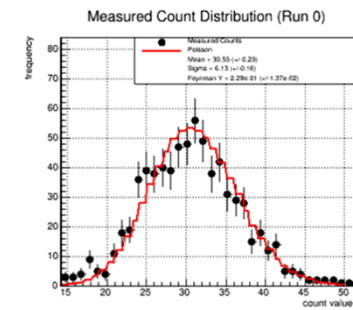
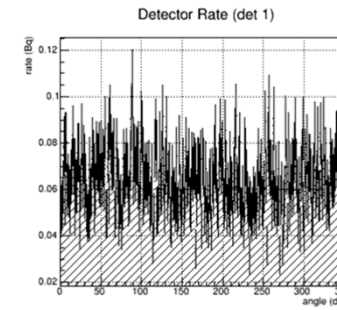
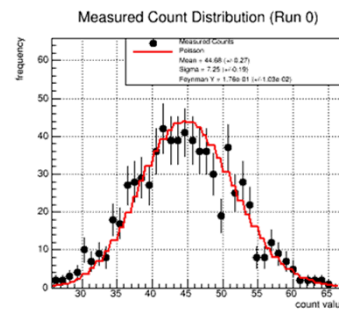
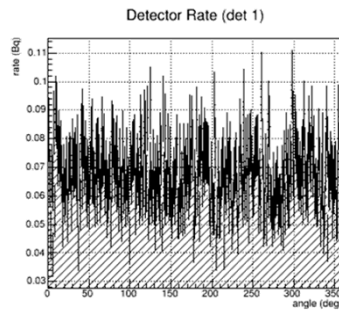


Feynman Y Test Statistic – 10,000 bootstrapped trials

Identical Hemis



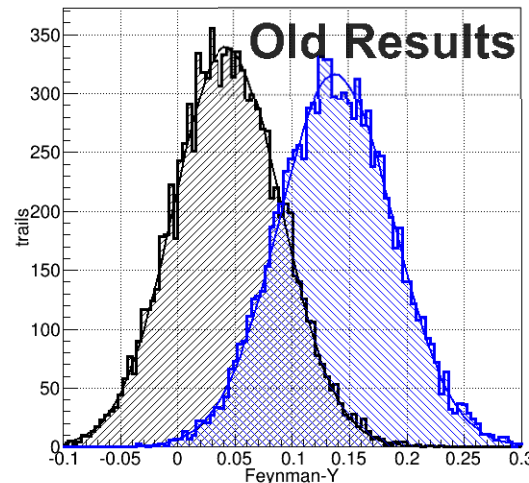
Misaligned Hemis



$$\begin{aligned} \text{Feynman Y} &= \left(\frac{\text{variance}}{\text{mean}} - 1 \right) \\ &= 0.0209 \end{aligned}$$

Black – 10,000 bootstrapped trials of two “identical” PuO₂ hemispheres (~48 hours)

Distribution of Feynman-Y Test Statistics



$$\begin{aligned} \text{Feynman Y} &= \left(\frac{\text{variance}}{\text{mean}} - 1 \right) \\ &= 0.324 \end{aligned}$$

Blue – 10,000 bootstrapped trials of two “non-identical PuO₂ hemispheres (~48 hours)

Statistical null hypothesis test results

Object 1	Object 2	mean counts /deg	σ^2/deg	χ^2/NDF	$P(\chi^2, \text{NDF})$
	Two ^{252}Cf at 130°	202.61	872.25	4.39	9E-152
Two ^{252}Cf at -50°		228.17	1219.55	5.43	2E-216
Two ^{252}Cf at -50°	Two ^{252}Cf at 130°	377.92	391.31	1.05	0.25
	PuO_2 hemi at 130°	9.97	12.45	1.28	3E-4
PuO_2 hemi at -50°		24.73	47.77	1.98	2E-25
PuO_2 hemi at -50°	PuO_2 hemi at 130°	19.16	19.56	1.04	0.27
PuO_2 hemi at -50°	PuO_2 hemi rotated by 90° at 130°	30.00	39.73	1.36	7E-6

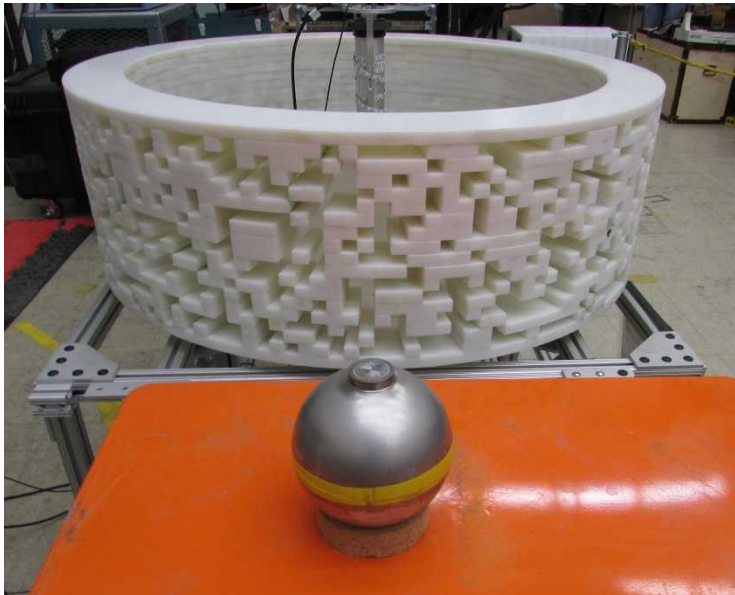
Research Questions

- Considering the concept and associated CONOPS, what sensitive information might be at risk?
 - Is there any remaining information in the measurement results that should be protected?
 - Are there particular design features to worry about?
 - Is there expected variability to worry about?
 - Between treaty accountable items.
 - Between containers or environments.
 - Are there other factors that can cause variability between items or measurements?
- Are there further steps that can be taken to mitigate information risk?
 - Changes to hardware, firmware, software.
 - Procedural changes.

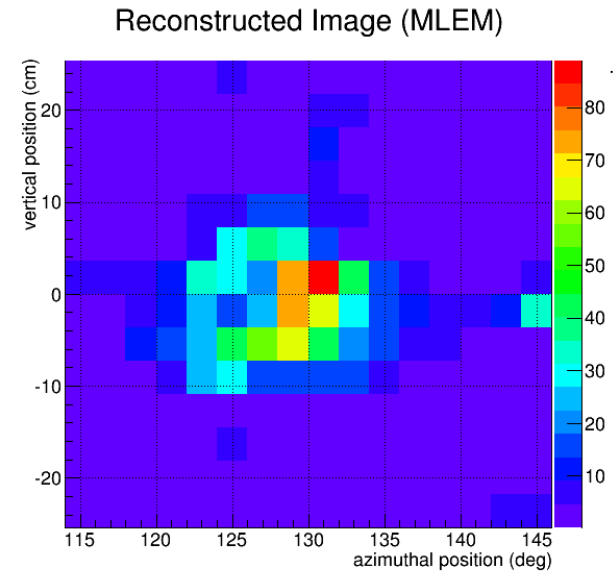
Additional Slides

LLNL's PuO₂ Hemispheres

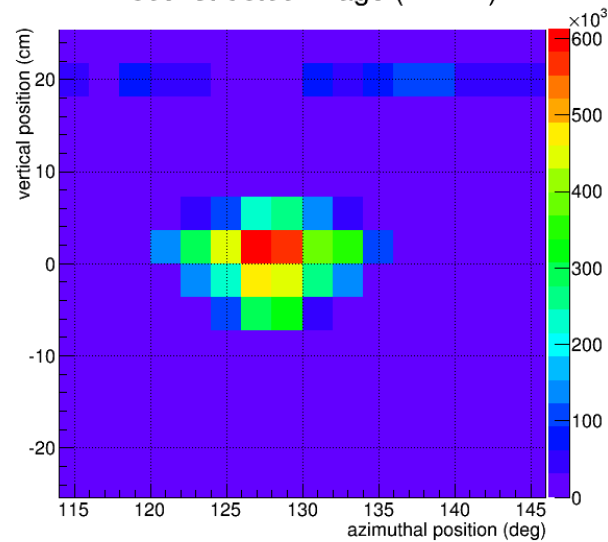
Measurement of plutonium dioxide hemispherical shells at LLNL.



Neutron Image



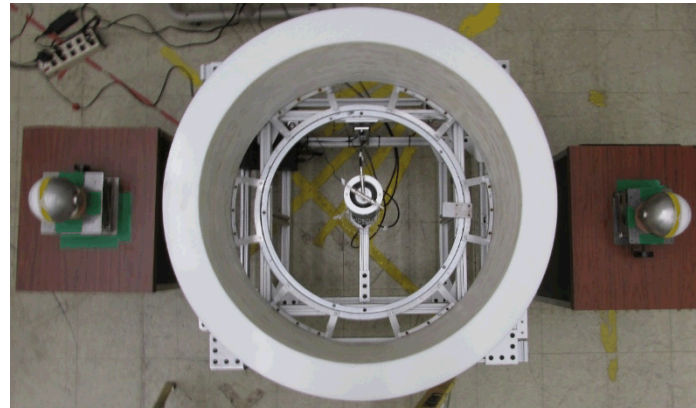
Reconstructed Image (MLEM)



Gamma-ray Image

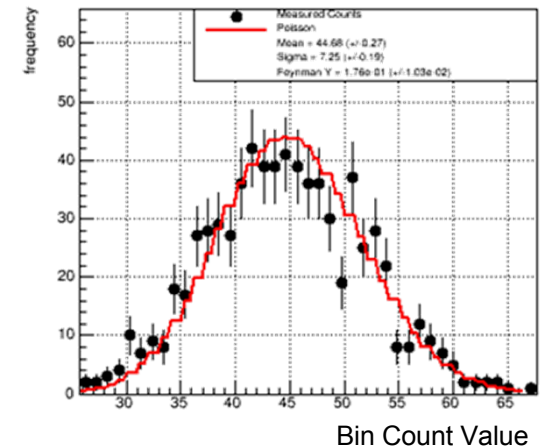
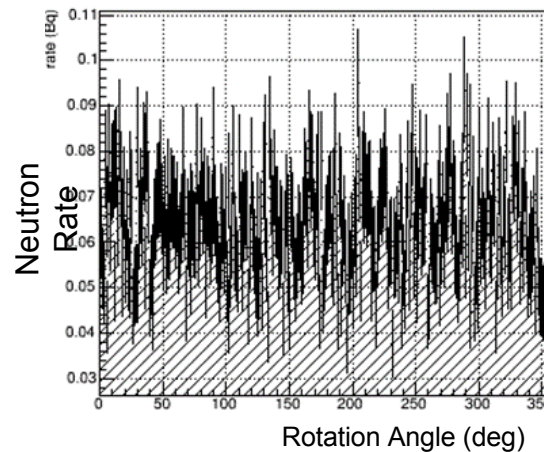
LLNL's PuO₂ Hemi positive measurement

- One hemisphere was placed on each side (180 deg) of CONFIDANTE.
- ~68 hours of data was taken.

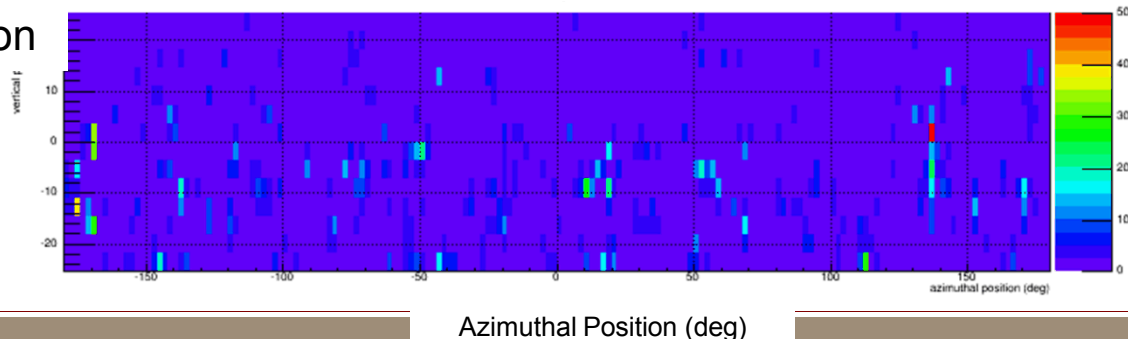


$$\begin{aligned} \text{Feynman } Y &= \left(\frac{\text{variance}}{\text{mean}} - 1 \right) \\ &= 0.0176 \pm 0.00103 \end{aligned}$$

Count Distribution
(Poisson – red curve)



MLEM
Reconstruction



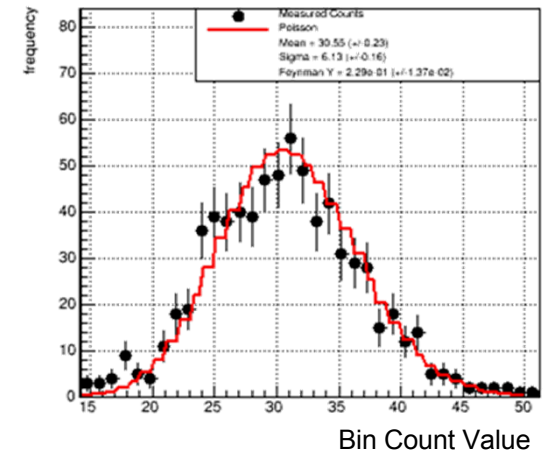
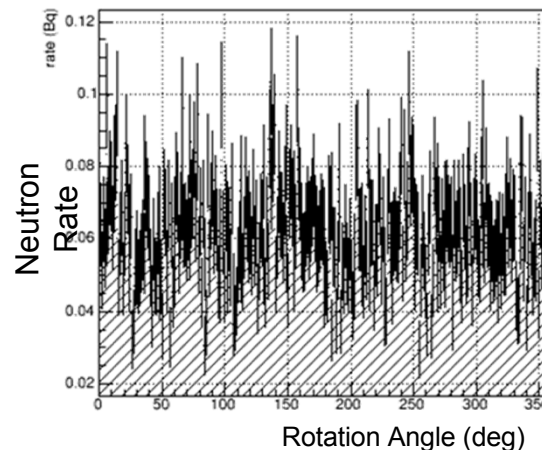
LLNL's PuO₂ Hemi negative measurement

- One hemisphere was placed on each side (180 deg) of CONFIDANTE.
- One was rotated by 90 degrees.
- ~48 hours of data was taken.



$$\begin{aligned}\text{Feynman Y} &= \left(\frac{\text{variance}}{\text{mean}} - 1 \right) \\ &= 0.229 \pm 0.0137\end{aligned}$$

Count Distribution
(Poisson – red curve)



MLEM
Reconstruction

