

Code to code comparison on hypersonic high enthalpy transitional boundary layers

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In the present study three boundary layer stability codes are compared based on hypersonic high enthalpy boundary layer flows around a 7° blunted cone. The code to code comparison is conducted between the following codes: the NOnLocal Transition analysis code (NOLOT) of the German Aerospace Center (DLR), the Stability and Transition Analysis for hypersonic Boundary Layers code (STABL) of University of Minnesota and the VKI Extensible Stability and Transition Analysis code (VESTA) of the von Karman Institute. The comparison focuses on the role of real gas effects on the second mode instability, in particular the disturbance frequency. The experimental test cases for the code to code comparison are provided by the DLR High Enthalpy Shock Tunnel Göttingen (HEG) and the JAXA High Enthalpy Shock tunnel (HIEST).

Abbreviations

| | |
|-------|--|
| DLR | German Aerospace Center |
| HEG | DLR High Enthalpy Shock Tunnel Göttingen |
| HIEST | JAXA High Enthalpy Shock tunnel |
| JAXA | Japan Aerospace Exploration Agency |
| NOLOT | NOnLocal Transition analysis code |
| STABL | Stability and Transition Analysis for hypersonic Boundary Layers |
| VESTA | VKI Extensible Stability and Transition Analysis toolkit |
| VKI | von Karman Institute for Fluid Dynamics |

I. Introduction

Laminar to turbulent transition in high speed boundary layers is of high importance for re-entry vehicles since early transition can increase the surface heat transfer by a factor of 3 to 8. The uncertainty on the

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transition location usually leads to an oversized thermal protection system, adding extra costs and reducing the payload of a hypersonic system. The second mode instability, commonly referred to as second mode or Mack mode,¹⁰ is the dominant boundary layer instability for essentially 2D boundary layers at high local Mach number ($Ma_e > 4$) and/or cold walls.¹⁰ Therefore, the second mode is the main focus of the investigations in this paper. High speed vehicles and re-entry vehicles operate in a high enthalpy range. In this range, real gas effects occur, which can include molecular rotation, molecular vibration, chemical dissociation and exchange, electronic excitation, radiation and ionization. In this paper, the high enthalpy effects on second mode instabilities are investigated. The numerical investigations are performed with three different stability codes, which are compared against each other: the NOLOT code of the DLR, the STABL code from the University of Minnesota and the VESTA code of VKI, which are described in section III.

The stability results are compared against low and high enthalpy experiments, which were performed on a blunted 7° half-angle cone model. The two high enthalpy shock tunnels (HEG and Hiest), in which the experiments were conducted, are described in section II.

The mean flow as well as the stability calculations themselves are performed with and without real gas effects to isolate the high enthalpy effect on the instability. Currently, the NOLOT stability code is limited to caloric or thermal perfect gas assumptions. Thus, an essential element of the paper is to assess the effect of real gas effects during the stability analysis.

II. Ground test facility and cone test article

The experimental data referred to in the present study were obtained in two free-piston driven reflected shock tunnels, the DLR High Enthalpy Shock Tunnel Göttingen (HEG)³ and the JAXA High Enthalpy Shock tunnel (HIEST).⁵ Similar test conditions were chosen with respect to unit Reynolds number, Mach number and total enthalpy. Table 1 provides a low enthalpy test condition from HEG and two comparable high enthalpy test conditions of both tunnels. The HEG conditions were derived by nozzle computations using the DLR TAU code^{11,21,25} in combination with a one temperature model, thus, assuming thermal equilibrium, which was shown to be a reasonable approach.^{26,30} The HIEST test conditions were calculated using a two temperature model. As shown in table 1 the rotational and vibrational temperatures are almost identical which supports the before mentioned assumption.

| Condition | HEG-Low-E | HEG-High-E | HIEST-High-E |
|--------------------------------------|-------------------|-------------------|-------------------|
| p_0 [MPa] | 7.1 | 38.8 | 46.8 |
| T_0 [K] | 2680 | 6690 | 6370 |
| h_0 [MJ · kg ⁻¹] | 3.1 | 11.6 | 10.9 |
| M_∞ [-] | 7.35 | 6.09 | 6.05 |
| T_∞ (1T) [K] | 264 | 1268 | - |
| T_{vib} (2T) [K] | - | T_∞ | 1192 |
| T_{rot} (2T) [K] | - | T_∞ | 1185 |
| ρ_∞ [g · m ⁻³] | 10.7 | 17.1 | 19 |
| u_∞ [m · s ⁻¹] | 2399 | 4354 | 4246 |
| Re_m [m ⁻¹] | $1.55 \cdot 10^6$ | $1.52 \cdot 10^6$ | $1.71 \cdot 10^6$ |

Table 1. HEG and HIEST test conditions used in the present study. The model wall temperature is assumed to be isothermal at 293 K.

All tests were conducted on separate 7° half-angle blunted cones with a nose tip radius of 2.5 mm and an overall length of about 1 m. Each model was supported by a sting at a nominal angle of attack of 0° . Further, both models were equipped with thermocouples and PCB flush mounted pressure transducers. The latter transducer have a response time of $\approx 1 \mu s$ and were used to capture the second mode frequencies for later comparison with stability analysis. On the cone model used in HIEST the PCB transducers were positioned between 0.412 m to 1.012 m, measured from the sharp tip, with a spacing of 0.04 m.²⁷ On the HEG model the PCB transducers were placed at 0.650 m, 0.785 m and 0.965 m from the sharp tip.²⁹

III. Numerical methods

III.A. Mean flow solver

The laminar base flows \bar{q} , which are required for the stability analysis, are calculated by different CFD solvers, which are not described in detail here. The DLR TAU code is a three-dimensional parallel hybrid multi-grid code and has been validated for hypersonic flows (see e.g.^{11,21,25}). The base flow calculations account for real gas effects, based on non-equilibrium gas modeling with 5 species for air: N_2 , O_2 , NO , N , O . Different assumption are applied: thermal equilibrium and chemical non-equilibrium (one temperature model) and thermochemical non-equilibrium (two and three temperature model). Constant free stream conditions, which are listed in table 1, are used. Additional mean flow calculations with perfect gas assumption are performed to isolate the real gas effects. Figure 1 shows the Mach number distribution of the low-enthalpy test case (see also table 1: HEG-Low-E) as an example of the base flow calculations.

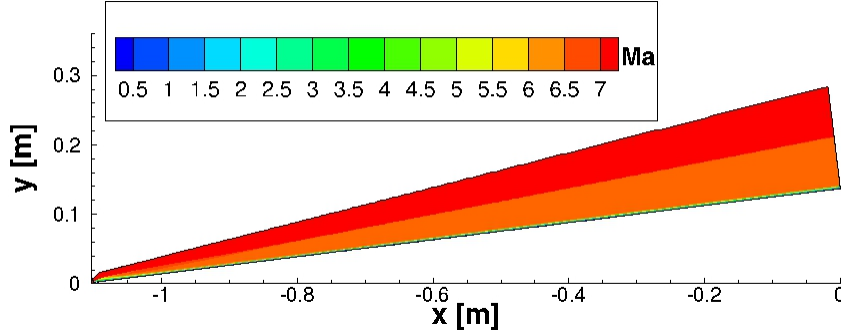


Figure 1. Example of mean flow: HEG-Low-E test case (CFD solver: TAU)

The stability simulations obtained with the VESTA toolkit are based on mean flow computations with the second order finite volume solvers CFD++[®] (see for instance Perroomian and Chakravarthy¹⁶) and COOLFluiD (Lani *et al.*,⁹ Degrez *et al.*²). Grid convergence studies were conducted for each code as described in section IV.A.1.

The STABL software suite contains a structured, axisymmetric CFD solver, which solves the reacting Navier-Stokes equations and is maintained by Dr. Heath Johnson.⁷ This flow solver is based on the finite-volume formulation. The inviscid fluxes are based on the modified Steger-Warming flux vector splitting method and are second-order accurate with a MUSCL limiter as the TVD scheme. The viscous fluxes are second order accurate. The time integration method is the implicit, first-order DPLR method. The simulated gas is a mixture of ideal gases using N_2 , O_2 , NO , N , and O in chemical and thermal non-equilibrium. The viscosity law uses Blottner curve fit data for species viscosities and the Wilke mixing rule for mixture viscosity. The heat conductivity is calculated using Eucken's relation.

III.B. LST / PSE solver

The equations of the stability codes are derived from the conservation equations of mass, momentum and energy, which govern the flow of a viscous, compressible gas. All flow and material quantities are decomposed into a steady laminar base flow \bar{q} and an unsteady disturbance flow \tilde{q}

$$q(x, y, z, t) = \bar{q}(x, y) + \tilde{q}(x, y, z, t). \quad (1)$$

The laminar mean flows \bar{q} are calculated by different CFD codes (see previous section) and can be used without and with chemistry. The disturbance \tilde{q} is represented as a harmonic wave

$$\tilde{q}(x, y, z, t) = \hat{q}(x, y) \exp[i(\alpha x + \beta z - \omega t)] \quad (2)$$

with the complex-valued amplitude function \hat{q} .

The stability codes applied in this paper are: the NOOnLocal Transition analysis code (NOLOT⁴) of the German Aerospace Center, the Stability and Transition Analysis for hypersonic Boundary Layers code (STABL⁷) of the University of Minnesota and the VKI Extensible Stability and Transition Analysis (VESTA) toolkit,^{19, 2018} of the von Karman Institute. All codes can be used for Linear Stability Theory (LST) as well as Parabolized Stability Equations (PSE) analyses. Both approaches are applied in this paper. In contrast to STABL and VESTA,¹⁷ which can account for real gas effects, NOLOT is limited to a calorically or thermally perfect gas.

The stability analyses performed using the STABL software suite are calculated with the PSE-Chem solver.⁷ PSE-Chem solves the reacting, two-dimensional, axisymmetric, linear parabolized stability equations (PSE) to predict the amplification of disturbances as they interact with the boundary-layer. The PSE-Chem solver includes finite-rate chemistry and translational-vibrational energy exchange.

Due to the similarity of the stability codes, only the VESTA code is described here in detail.

The VESTA code is made of different components dealing with the different aspects of the stability equations solution: derivation of a generic set of equations, generation of an automated implementation and a set of solution algorithms associated to different ansatz. In order to perform the different tasks the VESTA toolkit is coded in MAXIMA, MATLAB[®] and FORTRAN. The toolkit has been tested against several cases available in the literature such as the one in Malik,¹³ Arnal¹ and Özgen and Kırcah.¹⁴

Several solvers are available within VESTA, namely LST, PSE and BiGlobal. They are all able to cope with different regimes from incompressible to compressible flows with LST and PSE dealing with chemical reactions. The numerical method currently in use is based on a Chebyshev collocation method similar to the one described by Malik.¹³ A set of Gauss-Chebyshev-Lobatto points has been chosen

$$x_j = \cos\left(\frac{j\pi}{N}\right). \quad (3)$$

Given a function v defined on the aforementioned points, it is possible to obtain its derivative by defining a polynomial p that satisfy the usual condition for an interpolation problem $p(x_j) = v_j$ for $j = 0, \dots, N$ and then computing its derivative $w_j = p'(x_j)$. This is a linear operation and it could be represented as a simple multiplication by an $(N+1) \times (N+1)$ matrix $w = D_N \cdot v$. Note that m -th order derivative could be easily computed by $(D_N)^m$.

The algebraic mapping proposed by Malik¹³ has been used to transform Chebyshev polynomials defined in $x = [-1, 1]$ to the physical domain $y = [0, \infty]$ (truncated arbitrarily in $y = [0, y_{max}]$)

$$y = a \frac{1+x}{b-x}, \quad (4)$$

where $b = 1 + 2a/y_{max}$ and $a = y_i y_{max} / (y_{max} - 2y_i)$ with y_i corresponding to the location $x = 0$.

For the current set of calculations four homogeneous boundary conditions are applied to \tilde{u} , \tilde{v} , \tilde{w} , \tilde{T} . These homogeneous Dirichlet b.c. can be easily plugged into the collocation method by skipping the first and the last rows and columns [D_N becomes a $(N-1) \times (N-1)$ matrix]. Two zeros at the extremities of the resulting w could be appended so that the final vector has the correct dimension.

In case of a Neumann boundary conditions the problem could be stated by extracting the corresponding row from the matrix D_1 . As nothing is prescribed on pressure, one could either use a staggered grid as in Khorrami *et al.*⁸ or introduce a compatibility condition on pressure. This could be achieved by re-writing the y-momentum equation at the boundaries and adding them to the system as new equations to be solved:

$$\left. \frac{\partial \tilde{p}}{\partial y} \right|_{y=0, y_{max}} = X_{0,m}. \quad (5)$$

The variable vector gains two more variables, namely \tilde{p}_0 and \tilde{p}_N , and two new equations are introduced by appending two rows and two columns to the matrices reaching a final dimension of $(5N-3)$.

IV. Results

Three test cases are chosen for the analyses of the chemical effects on the second mode: a low enthalpy experiment is conducted as reference case and two high enthalpy experiments as main test cases for the investigations of the chemical effects. See also table 1.

IV.A. Low enthalpy test case (HEG)

The chosen reference test case is an experiment, which was performed in HEG. This low enthalpy test case, HEG-Low-E, was conducted at a total enthalpy of 3.1 MJ/kg (table 1), at which the gas can be assumed to be thermally perfect.

IV.A.1. Grid convergence

Different grids are used for the base flow calculations: non-adapted grids as well as adapted grids. For the shock adapted grids with additional modulation of the outer grid limits, it is possible to reduce the number of points compared to the non-adapted grids. Apart from the number of grid points, also the wall normal distance of the first grid points has an effect.

On the right side (figure 2) the grid convergence study using the VESTA code based on LST perfect gas calculations is shown. The calculated maximum N-factors of the second mode is given as a function of the x-coordinate (axial distance measured from the blunt nose for this diagram as for all following pictures). Due to the minor differences of the one million point grid compared to the four and five million point grids, for the studies in this paper a grid with 1 million points is chosen (2600×450).

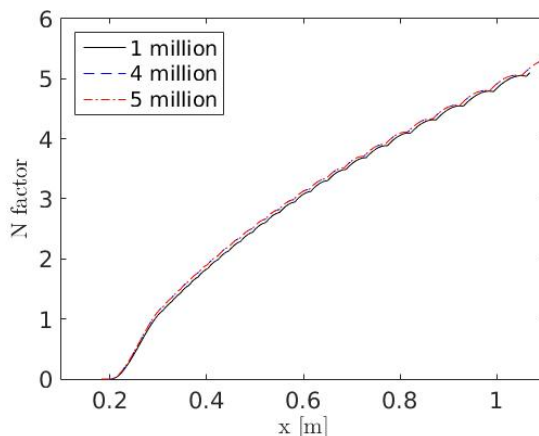


Figure 2. Maximal N-factor as function of x-coordinate - Grid convergence study with a perfect gas assumption (HEG-Low-E, LST, VESTA)

Due to the use of different CFD solver, the grid convergence study has to be done for each CFD solver separately. For the STABL code, Wagnild³¹ summarized a detailed grid convergence study using a comparable geometry as well as comparable free stream conditions. Different grids up to a cell count of over 15 million cells were investigated. Based on these previous grid studies a grid of 1215×350 is chosen. Detailed information on NOLOT grid studies are provided in Wartemann,³³ performed for the same geometry with similar free stream conditions. In the present study, as in Wartemann,³³ grid point clustering is applied towards the nose, the wall of the cone and the shock. The number of grid points are in the same range as for the STABL code.

IV.A.2. Chemical influence (HEG-Low-E)

In this subsection, PSE calculations performed with NOLOT are shown: in Figure 3a the calculated N-factors of the second mode as a function of the x-coordinate (axial distance measured from the blunt nose) for a frequency range from 200 up to 300kHz are depicted. The dashed lines in gray are based on perfect gas calculations, whereas the black lines are based on thermochemical non-equilibrium gas modeling (see also section III.A). Almost identical results were obtained confirming the assumption of thermally perfect gas for the low enthalpy test case.

As mentioned in section II, PCB sensors were used in the HEG experiments to measure the pressure fluctuations in the boundary layer, which are associated with second mode instabilities. From figure 3a the N-factors can be extracted at the transducer positions as shown in figure 3b for the three PCB sensor positions of the experiment. The calculated second mode is amplified in streamwise direction. Due to the

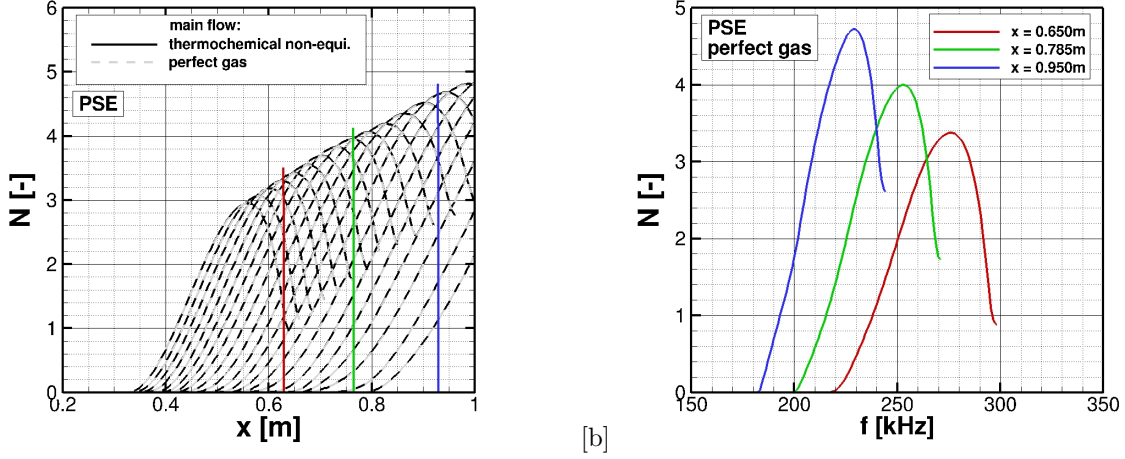


Figure 3. N-factor as a function of the x-coordinate (a), N-factor as function of the frequency (b) (HEG-Low-E, PSE, NOLOT)

increase of the boundary layer thickness in the downstream direction and the relation between the boundary layer thickness δ and the second mode wavelength, $\lambda \approx 2\delta$, the typical shift towards lower frequencies can be observed.

IV.A.3. LST comparison: VESTA / NOLOT (HEG-Low-E)

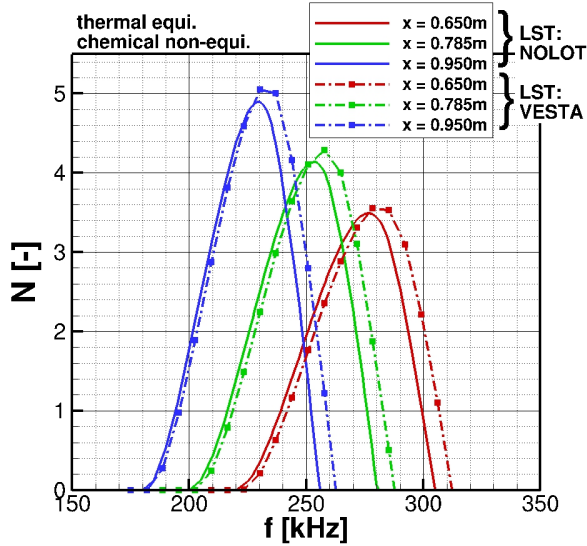


Figure 4. N-factor as function of frequency (HEG-Low-E, LST, NOLOT and VESTA)

mean flow solvers. These small deviations should mainly result from small mean flow variations. The effect of the different LST gas approaches should be negligible. To confirm this statement an LST code to code comparison based on the same base flow simulation is planned in the near future.

IV.A.4. PSE comparison: STABL / NOLOT (HEG-Low-E)

Previous investigations of the same geometry with a similar low enthalpy free stream condition, based on a comparison of the experimental / calculated growth rate of the second modes, shows that it is possible to apply LST instead of PSE.³³ Nevertheless, LST neglects the nonparallel nature of the boundary layer as well as nonlinear effects. Thus, PSE is in general the preferable method.

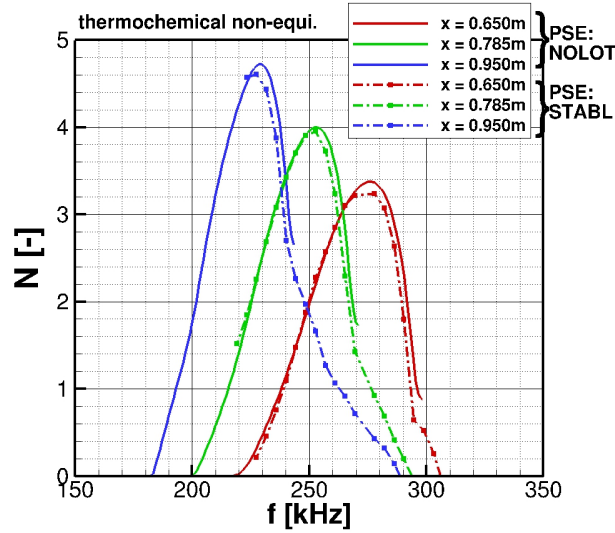


Figure 5. N-factor as function of frequency (HEG-Low-E, PSE, NOLOT and STABL)

The N-factor of the PSE calculations and consequently the differences between PSE and LST, depend on the chosen parameter for the PSE N-factor calculations, such as velocity or disturbance energy. For all PSE results in this paper, the N-factors are derived based on the disturbances energy.

Figure 5 shows that the STABL results (dashed lines with symbols) are in a good agreement with the NOLOT calculations (solid lines). The mean flow as well as the stability calculations of STABL are performed with thermochemical non-equilibrium based on a two temperature approach. In contrast, due to the limitation of the NOLOT code, only the base flow simulation was used thermochemical non-equilibrium. The differences between the code predictions are in the range of 1% comparing the maximum N-factors and the corresponding frequencies at the three sensor locations.

Furthermore, the results confirmed, as expected for the low enthalpy case, the neglect of the chemical effects for the low enthalpy case is possible.

IV.A.5. Comparison to experiment: HEG-Low-E

For the second mode comparison of the numerical data with the measurements, two requirements are necessary. First, the second mode at the PCB sensor position has to be strong enough, meaning it has to be higher than the background noise level. Second, the flow at the sensor position has to be laminar. In the current case, the measured second mode at the last position ($x = 950\text{mm}$) is in the transition region. Thus, for the comparison with the measured second mode, the first and second sensor positions ($x = 0.650\text{ m}$, red color; $x = 0.785\text{ m}$, green color) are used. For the comparison with the experimental data, the results of the NOLOT code of the previous section are used.

Figure 6 shows the measured amplitude spectra density (ASD) marked as symbols. N-factors, which are based on PSE NOLOT calculations, as a function of the frequency are shown as lines. As can be seen, the numerically predicted N-factor distribution is in acceptable agreement with the measured data. Differences of the peak frequencies are in the range of 10%. However, the frequency shift between the first and the second sensor positions is within about 22 kHz for both the experiment and the computations, $\Delta f_{s1 \text{ to } s2, \text{ Exp.}} = \Delta f_{s1 \text{ to } s2, \text{ PSE.}}$ Thus in principal a good agreement is visible, but with a small frequency shift.

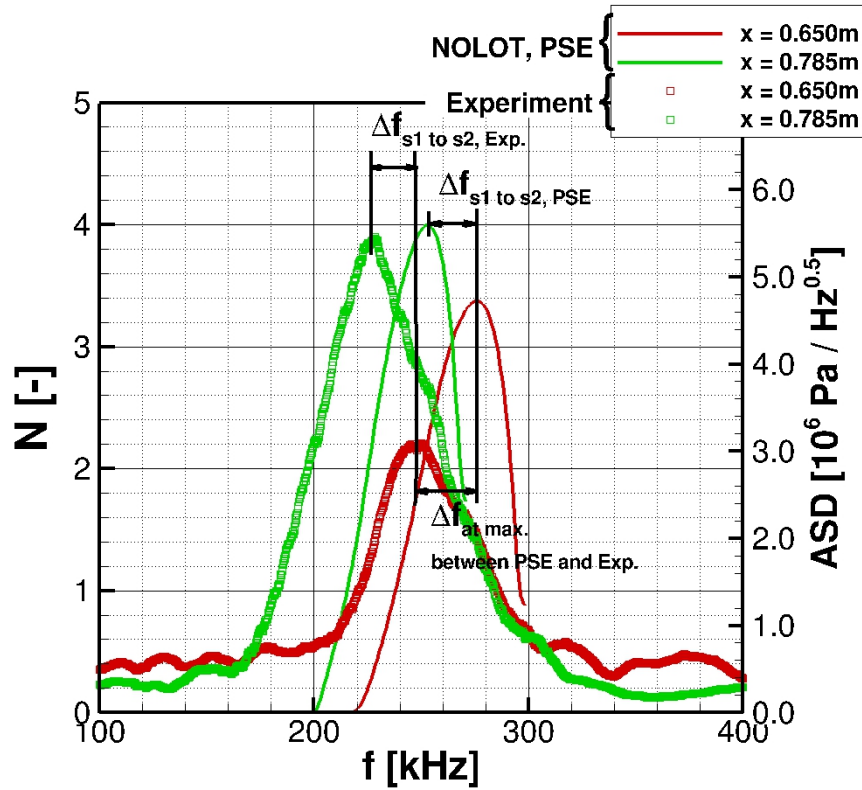


Figure 6. N-factor / ASD as function of frequency (HEG-Low-E, NOLOT and experimental data)

Several analyses were performed to investigate this frequency shift: Wagner et al.²⁸ investigated the influence of small deviations of the nose radius on the second mode. A change in the nose radius of 10% results in a frequency shift of about 10%. However, the nose is well proven for this test case. Further, Wagner et al.²⁸ investigated the influence of small variations of the angle of attack on the transition location and the second mode development. In two subsequent tests on the same model as used in the present study the angle of attack was varied in a range of $\pm 0.2^\circ$, which is a conservative estimation of angle of attack uncertainties. The analysis shows a negligible effect on the transition process and the second mode frequencies.

The good agreement in $\Delta f_{s1 \text{ to } s2}$ of the comparison makes small inaccuracies in the free stream condition the most likely reason for the Δf_{max} . In Wartemann et al.³² the influence of usual measurement inaccuracies in the determination of the free stream conditions on the maximum frequency of the second modes are investigated using a 3 half-angle sharp cone. In reference,³³ an investigation on the geometry used in the present study revealed, that a change of unit Reynolds number of about 5% results in a frequency shift of about 10%.

IV.B. First high enthalpy test case (HEG-High-E)

This section summarizes the comparison of the first high enthalpy test case: HEG-High-E with a total enthalpy of 11 MJ/kg.

IV.B.1. PSE comparison: STABL / NOLOT (HEG-High-E)

Figure 7 summarizes the PSE code to code analysis. The mean flow as well as the stability calculation of STABL, dashed lines with symbols, are performed with thermochemical non-equilibrium based on a two temperature model. For NOLOT (lines), different approaches are applied: data in Figure 7a are based on a calorically perfect gas assumption using a specific heat ratio of 1.4 for base flow as well as stability calculations. As expected, for the high enthalpy case major differences are visible. For all sensor positions a shift of the frequency range can be observed. Including chemistry reduces the boundary layer stability and increases

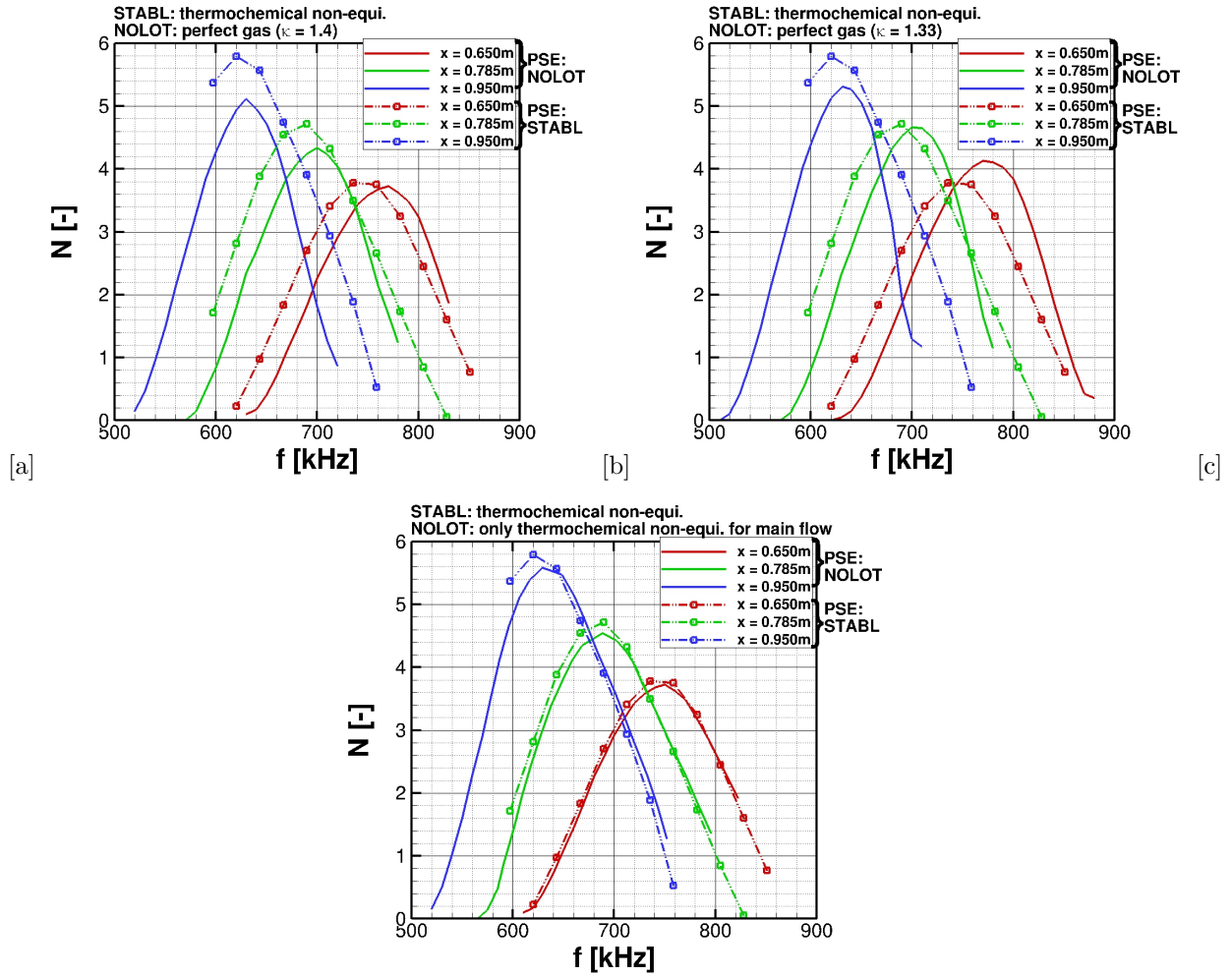


Figure 7. N-factor as a function of the frequency (HEG-High-E, PSE, NOLOT and STABL)

the calculated N-factors. The deviations of the N-factors at the maxima of each sensor position between the two approaches depend strongly on the sensor position itself: for the first sensor, almost the same maximum N-factor is predicted, while for the second position, the deviation increases to a ΔN_{max} of around 10% and for the last sensor position up to over 10%. Figure 7b considers variations of the specific heat ratio. One result of the calculations of the complete nozzle is, that the specific heat ratio κ is reduced to 1.33. Using this reduced κ for the calorically perfect gas simulation delivers the values in Figure 7b. This numerical test approach does not affect the frequency range. Looking at the frequencies, the same differences between STABL and NOLOT as in figure 7a are visible. Due to the dependency on the position, the maximum N-factor at the first sensor position is overestimated from NOLOT, the second position is similar to the STABL results, and the last sensor is underestimated. Thus, only an upgrade to thermochemical non-equilibrium base flow simulations make senses, which is summarized in figure 7c. Minor differences between STABL and NOLOT are still visible especially for the downstream sensor positions. The differences of the N-factor at the maximum for the last sensor is about 3%. Consequently, real gas effects have a higher effect on the mean flow, than on the stability calculations itself. The application of the thermochemical non-equilibrium for the base flow in combination with the perfect gas assumption for the stability calculations result in an acceptable agreement for the present test case. However, the error, due to the perfect gas assumption, propagates in streamwise direction and increases the discrepancy.

IV.B.2. Comparison to experiment: HEG-High-E

The code to code comparison of the previous section is based on a generic test case using the nominal free-stream conditions of table 1 to perform the simulations of the mean flow. For the comparison with the experimental data, the base flow simulation includes the nozzle, test camber and cone model.

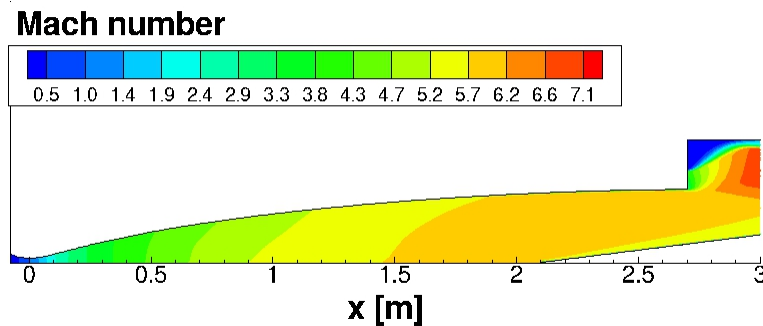


Figure 8. Base flow calculations of HEG-High-E test case (CFD solver: TAU)

The grid is axially-symmetric and has about four million points clustered to the laminar walls and the shock. Based on the nozzle calibration of Wagner,³⁰ the nozzle boundary layer is set turbulent. Due to the thermocouple measurements of the experiment, the boundary layer of the cone is known to be completely laminar. A thermochemical non-equilibrium approach based on a three temperature model is used. Figure 8 illustrates the Mach number distribution in the numerical nozzle - cone set up.

The second mode at the first PCB sensor position is not strong enough and still in the range of the background noise level. Thus, Figure 9 shows the measured amplitude spectra density (symbols) as function of the frequency for the second and third PCB sensor. The PSE results (N-factors) are based on NOLOT calculations using the mean flow simulation of figure 9. The numerically predicted N-factor distribution is in relatively good agreement with the measured data, but with visible differences. Although the nozzle, the test section, and the cone model are simulated together, there are still uncertainties in the free stream conditions, which could explain the remaining differences. Nevertheless, the numerical results are in acceptable agreement with the experimental data.

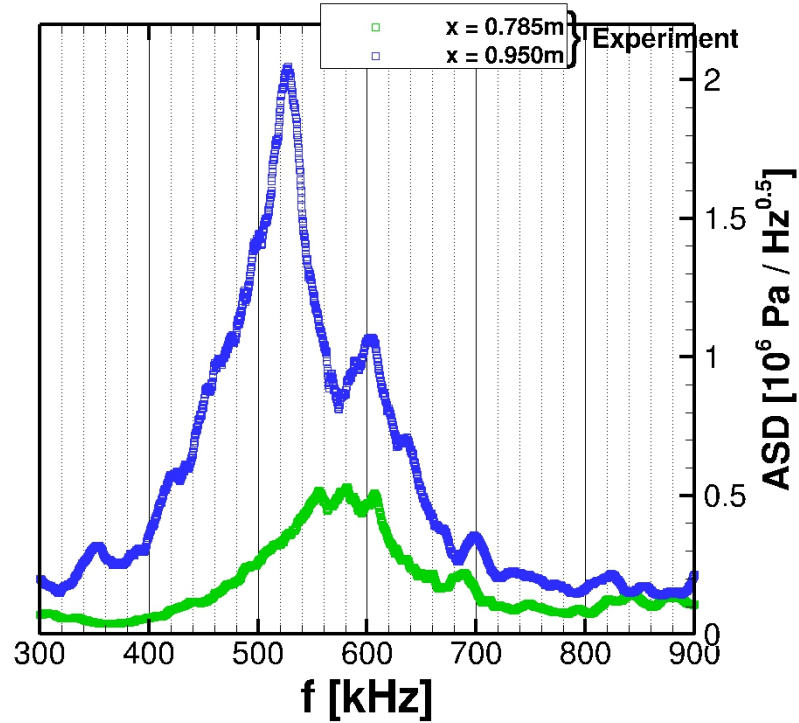


Figure 9. N-factor / ASD as function of frequency (HEG-High-E, NOLOT and experimental data)

IV.C. Second high enthalpy test case (HIEST-High-E)

This section summarizes the comparison of the second high enthalpy test case: HIEST-High-E with a total enthalpy of 10.9 MJ/kg. These test conditions for the second high-enthalpy case are chosen because of their similarity to the HEG-High-E test case, with respect to unit Reynolds number, Mach number and total enthalpy.

IV.C.1. PSE comparison: STABL / NOLOT (HIEST-High-E)

Figure 10a summarizes the PSE code to code analysis. The mean flow as well as the stability calculations of STABL, dashed lines with symbols, are performed with thermochemical non-equilibrium based on a two temperature model. For NOLOT (solid lines) the mean flow is also simulated with the thermochemical non-equilibrium approach based on a two temperature model in combination with the perfect gas assumption for the NOLOT stability calculations. Due to the increase of the error in streamwise direction, which was described in section IV.B, the last sensor position was chosen for the code to code comparison to provoke the worst case with maximal deviation for the present test case.

The predicted frequency range is similar to the previous test case (HEG-HIGH-E) due to the similarity of the free stream conditions, the total enthalpy and the wind tunnel model. The difference of the maximum N-factors as well as the corresponding most amplified frequency between NOLOT and STABL are found to be approximately 3%. This confirms the validity of the selected approach for the NOLOT analyses.

IV.C.2. Comparison to experiment: HIEST-High-E

The last two sensor positions are chosen for the comparison conducted in this section.

Figure 10b shows the measured power spectra density (PSD) marked as symbols. N-factors, which are based

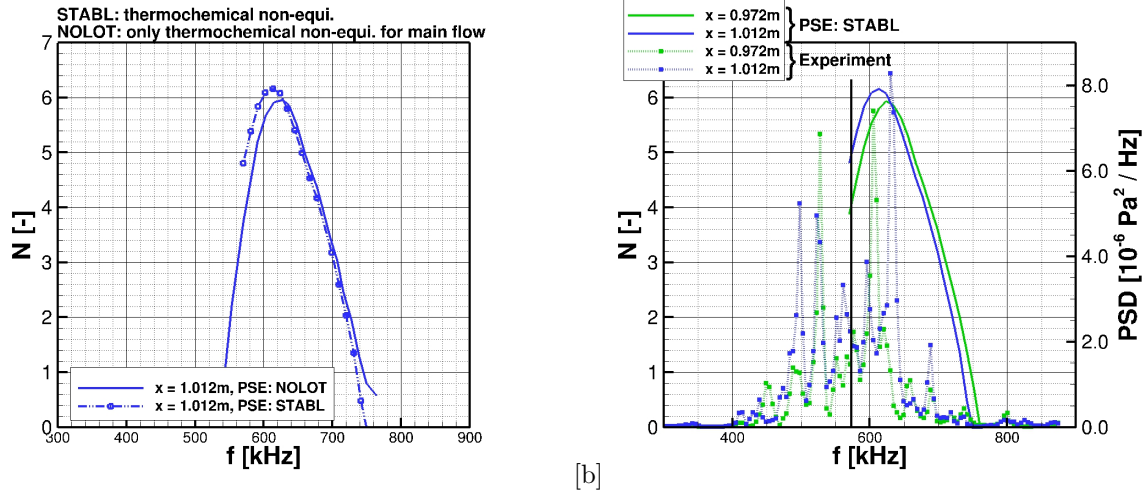


Figure 10. N-factor function of frequency (HIEST-High-E, NOLOT and STABL) (a), N-factor / PSD as function of frequency (HIEST-High-E, STABL and experimental data) (b)

on PSE STABL calculations of the previous section, are shown as solid lines.

The last two sensors of the HIEST-High-E case are with $x = 0.972m$ and $x = 1.012m$ very close together. Thus, the shift of frequencies due to the thickening of the boundary layer is only visible for the stability results. The predicted frequencies of the second modes are in a similar frequency range as the experimental PCB data. Due to the scatter of the PCB data for this short-time wind tunnel, the black line is used for the extraction of the frequencies for the maxima of the PSD functions. Compared to the numerical data, the differences are less than 10% for the frequencies at the maxima, which is a good agreement for the present comparison (see also section IV.B, where this differences were already discussed).

V. Conclusion

In the scope of the present study different stability codes were compared: the NONLocal Transition analysis code (NOLOT) of the German Aerospace Center (DLR), the Stability and Transition Analysis for hypersonic Boundary Layers code (STABL) of the University of Minnesota and the VKI Extensible Stability and Transition Analysis code (VESTA) of the von Karman Institute.

The code to code comparison revealed good agreement for the low enthalpy reference case. The deviations of the maximum N-factors and corresponding frequencies are around 1% and are expected to be mainly caused by using different CFD solvers for the mean flow computations. Since the gas can be considered being thermally perfect, the results obtained by using an thermochemical non-equilibrium approach for the mean flow and the stability code are almost identical to the approach of considering thermochemical non-equilibrium for the mean flow only.

The focus of this paper is the high enthalpy test cases. The main results of the code to code comparison at high enthalpy are the following:

- Real gas effects reduce the boundary layer stability and thus increase the N-factors.
- If real gas effects are of importance, it is essential to model those in the mean flow computations.
- For the present test cases only minor effects, with acceptable errors, were observed considering or neglecting real gas effects in the stability analysis.
- Nevertheless, it is important to remember that errors can built up with increasing flow length.

The comparison to the experiments shows a good agreement to the numerical data regarding the predicted / measured frequency shift between two sensor position: for example: $\Delta f_{s1 \text{ to } s2, \text{Exp.}} = \Delta f_{s1 \text{ to } s2, \text{PSE}}$ was almost the same for the low enthalpy references case. The differences of the frequency at the maxima Δf_{max} , comparing the maximum N-factors with measured PCB data, are about 10%. Thus in principal a good agreement is observed, however, with a small frequency shift. Inaccuracies in the free stream conditions are the most likely reason for this deviations since the predicted N-factors are extremely sensitive towards small changes of the free stream condition and the corresponding base flow calculations. Nevertheless, the differences of the frequency range is in an usual, acceptable range for this kind of comparison.

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