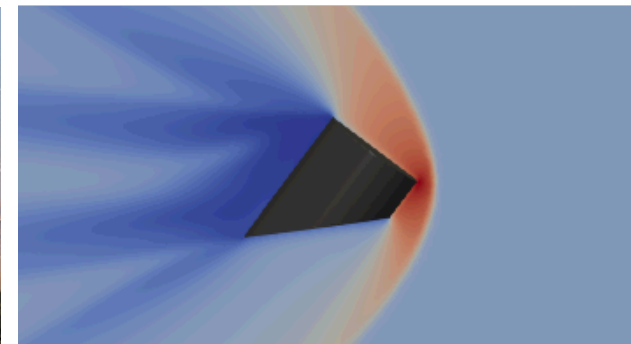




11/24/2017



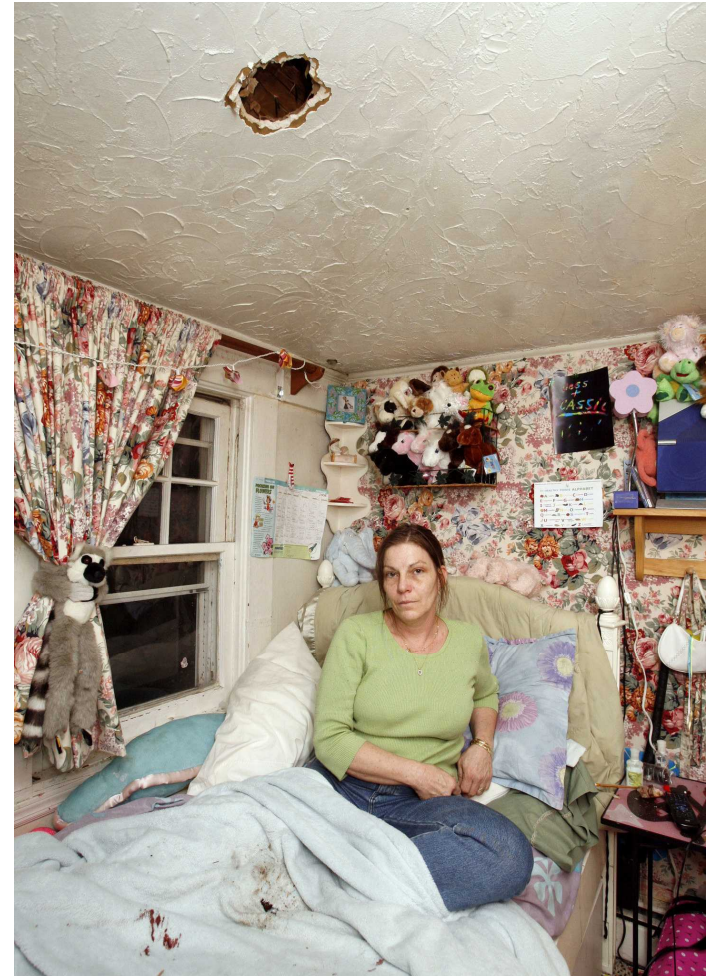
Simulations of High Speed Fragment Trajectories

Peter D. Yeh, Stephen Attaway,
Srinivasan Arunajatesan, Travis Fisher

Why is understanding fragment flight important?

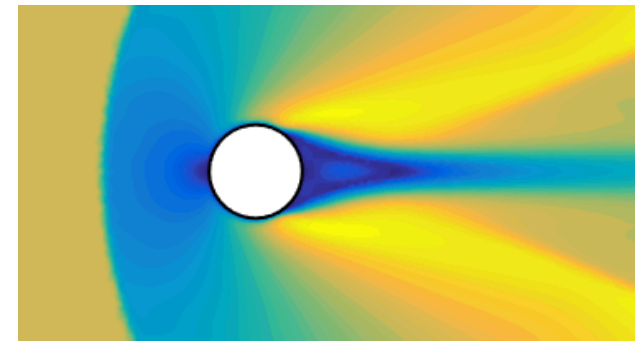
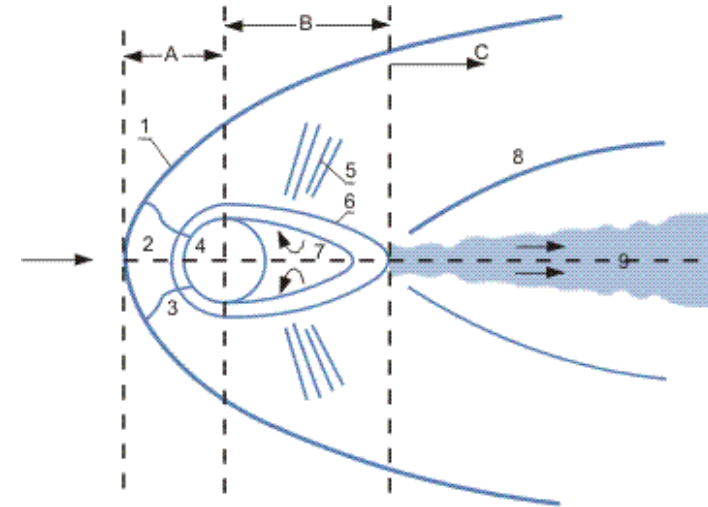


Picatinny Arsenal Accident, 2008

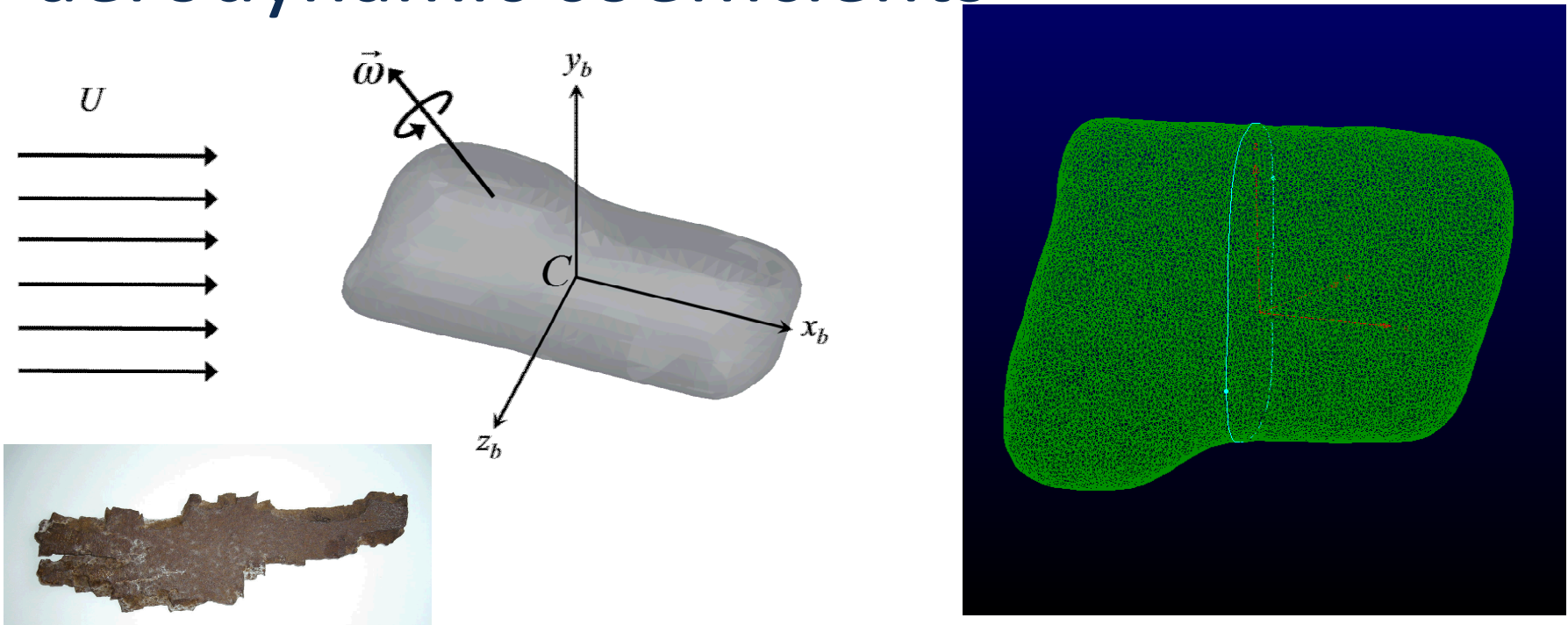


Fragment flight involves complex physics

- Fragments fly at supersonic speeds
- Geometry is complicated, high aspect ratio
- Fragment-air interaction creates tumbling and chaotic motion
- Cylinder flow field has multiple features needed to be captured
- **Approach: Computational modeling with validation by experimental testing**



Step 1: Build database of aerodynamic coefficients



- Example fragment (output from CTH calculation)
- Unstructured tet mesh of fragment surrounded by spherical far-field
- RANS compressible flow solver with SST turbulence model
- Pressure is integrated across surface to determine forces/moments

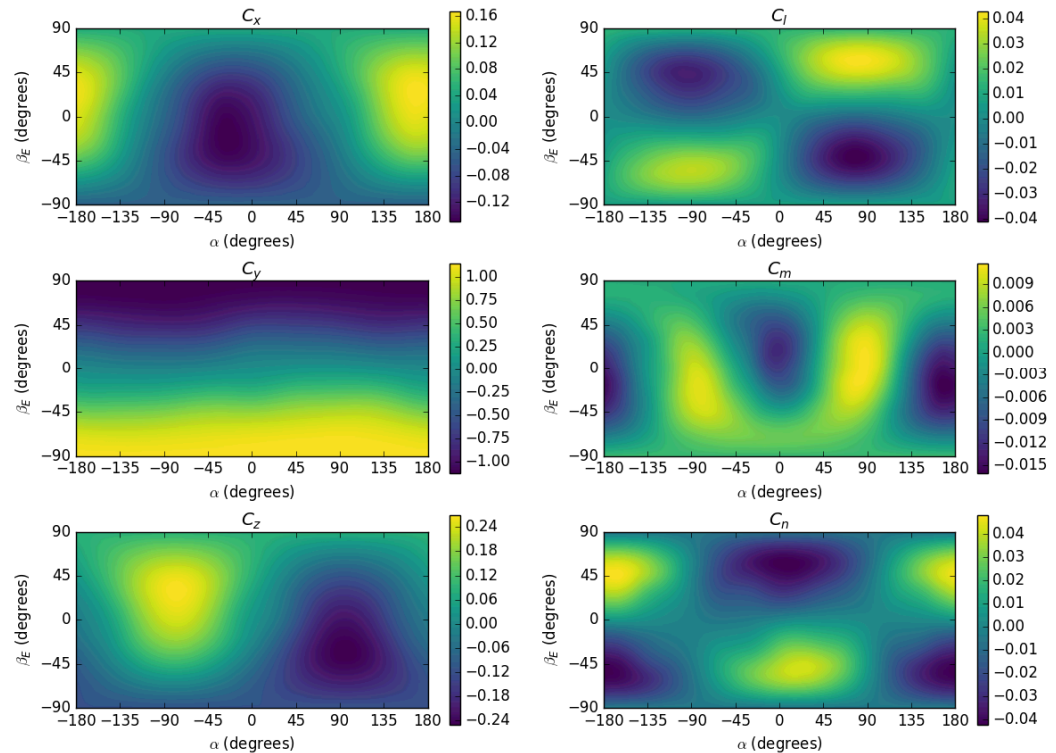
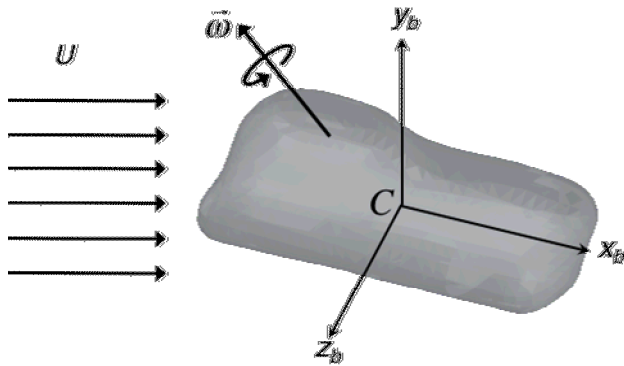
Example flow solution



- Contour of $Ma = 1$ shows 3D bow shock and rarefaction wave
- Calculated drag matched literature values for simple shapes (cube, sphere)

Aerodynamic database

Fragment Aerodynamic Coefficients



- Orientation characterized by 2 angles
- 6 contour plots of each force/moment coefficient, 1 set per fragment

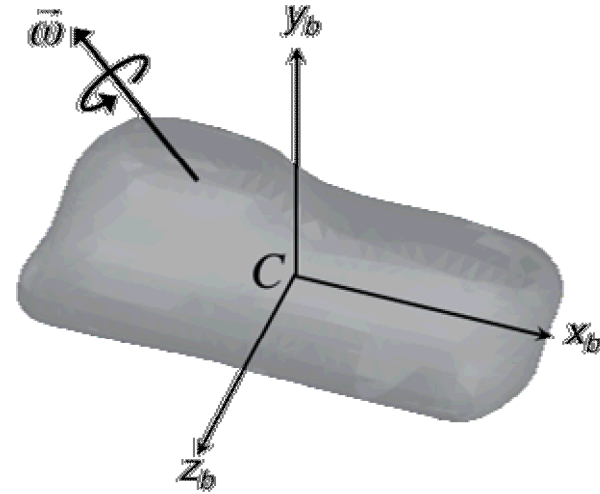
Step 2: Integrate trajectories

- Trajectory of example fragment
- Newton-Euler equations of motion

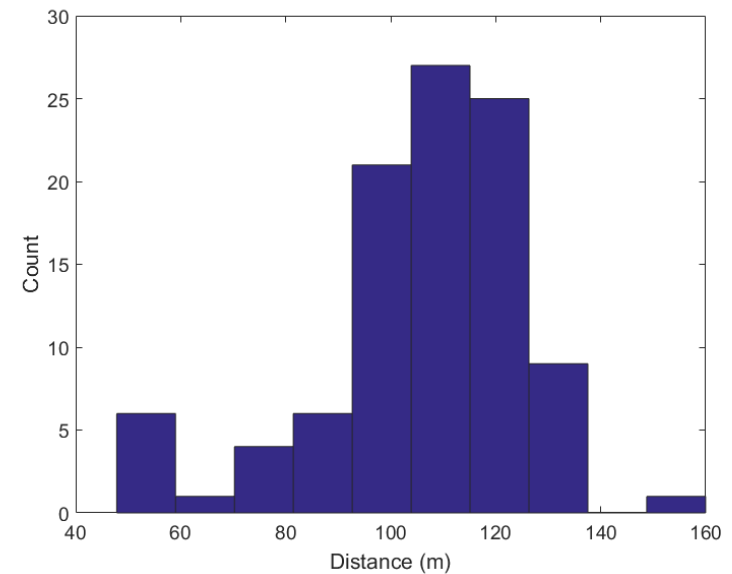
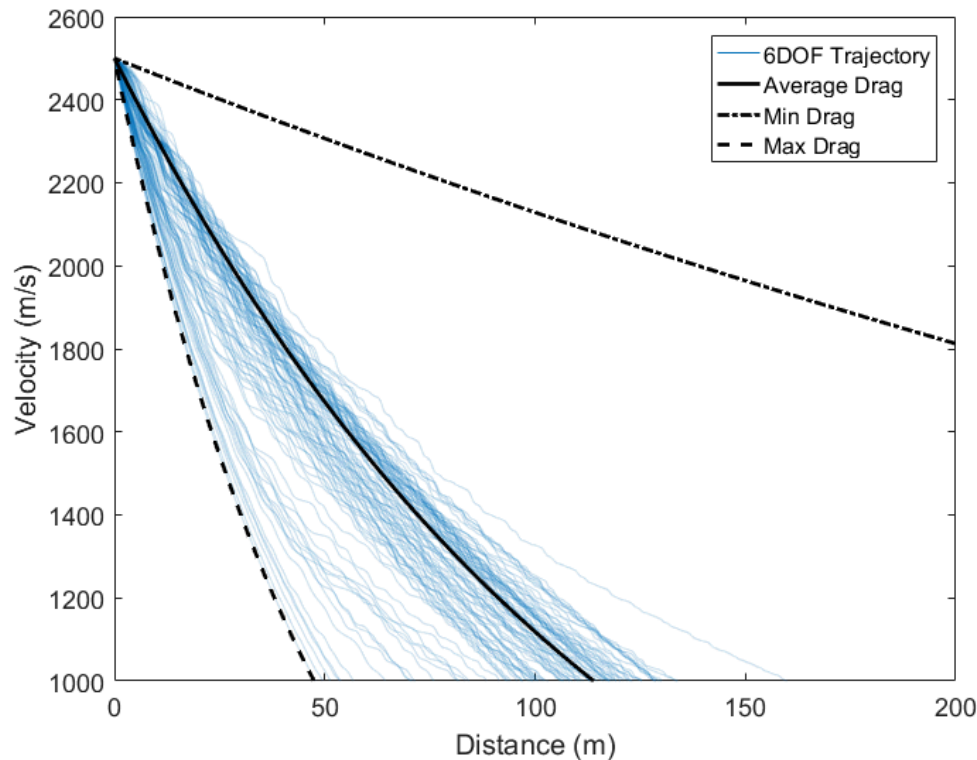
$$\sum \bar{F} = m\bar{a}_C$$

$$\sum \bar{M}_C = \frac{d\bar{L}_C}{dt} \quad \bar{L}_C = \bar{I}_C \bullet \bar{\omega}$$

- Forces and moments used from database built by CFD simulations
 - Assume force/moment coefficients not function of Ma (Ma ≥ 3)
- Steel fragment, initial velocity 2500 m/s, no rotation, ~4.5 cm long

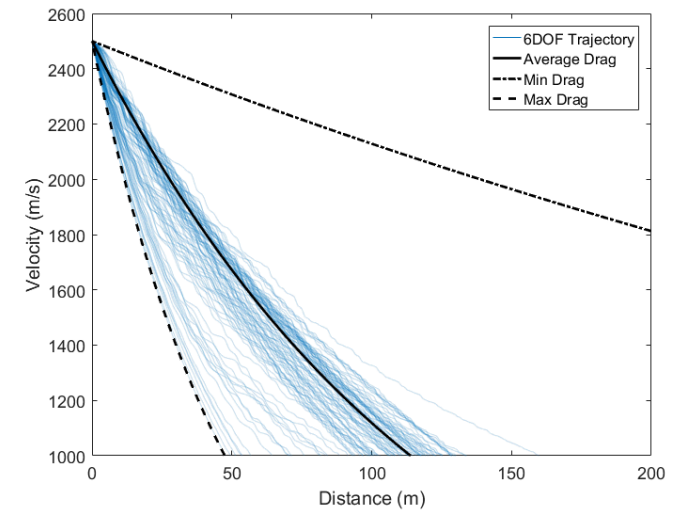
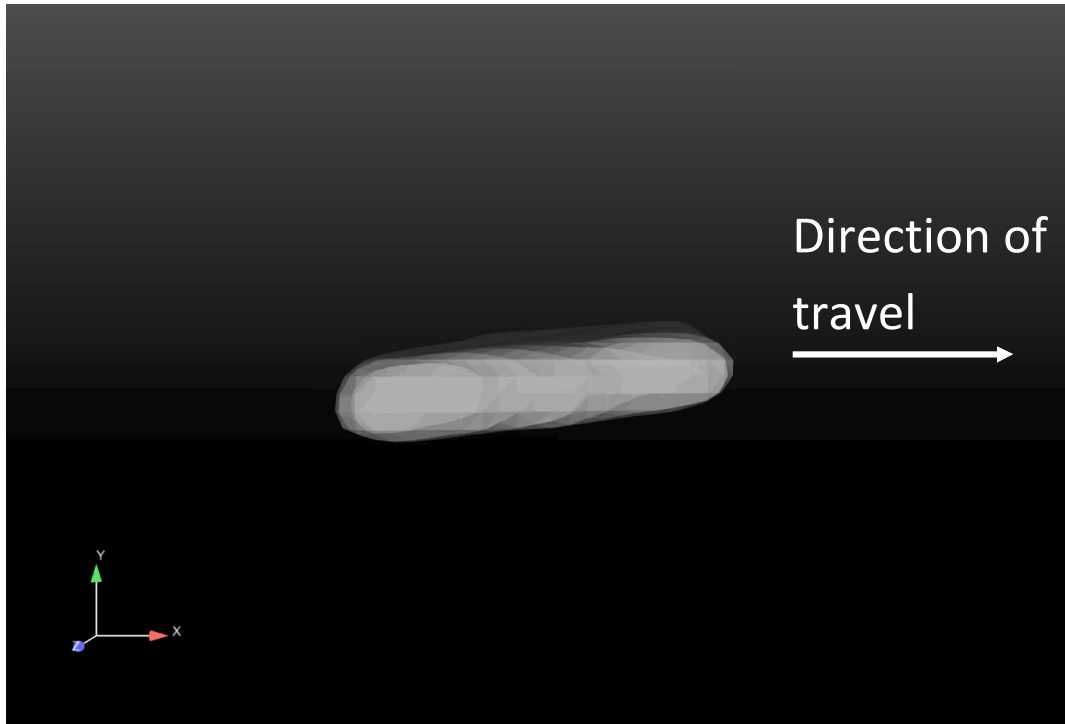


How far can fragments fly?



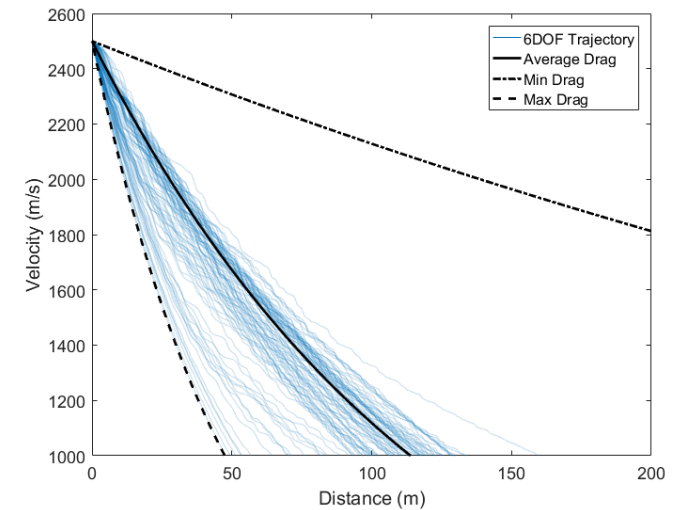
- 100 trajectories sampled with different initial orientations
- Average drag coefficient approximates most likely trajectory
- Distance ranges from 50 to 160 m!

Average trajectory



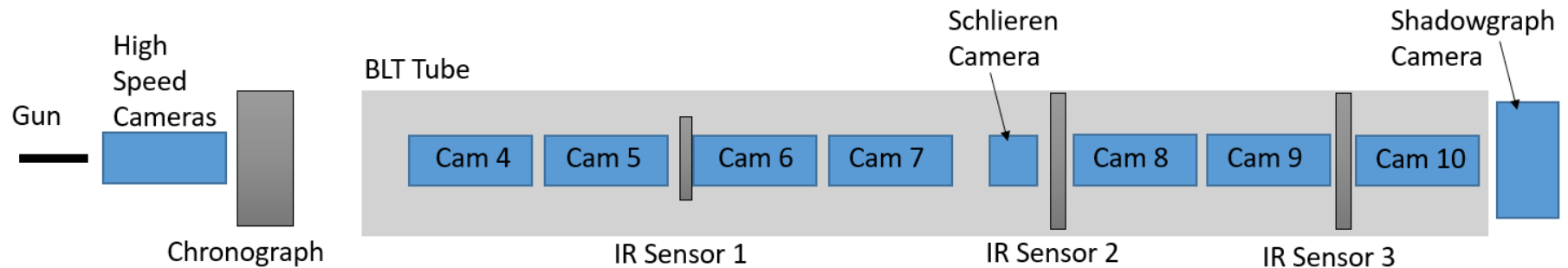
- Chaotic behavior, although seems to settle on a spin/precession

Far flying fragment



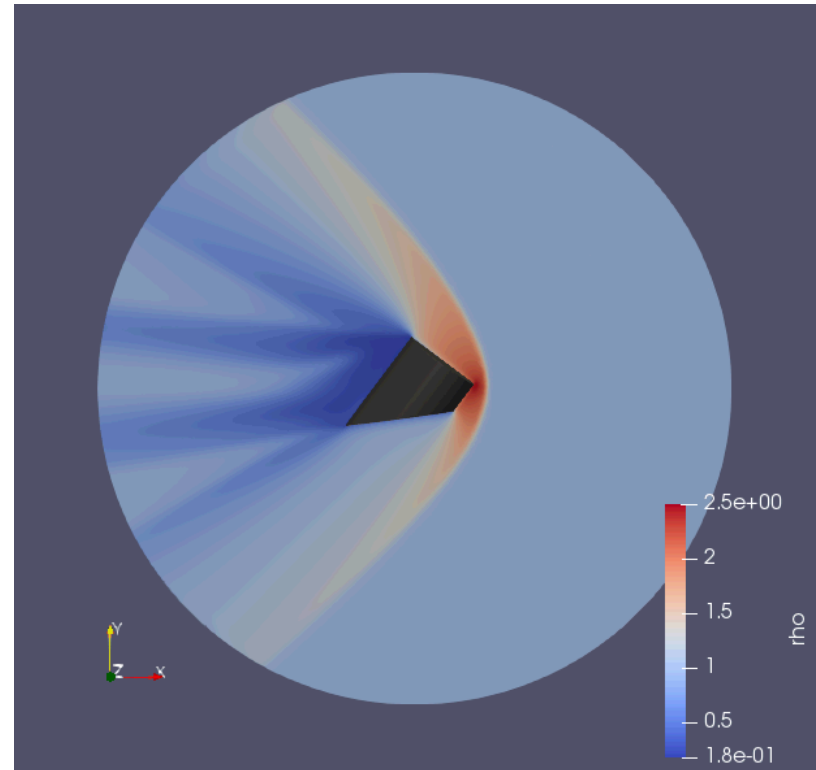
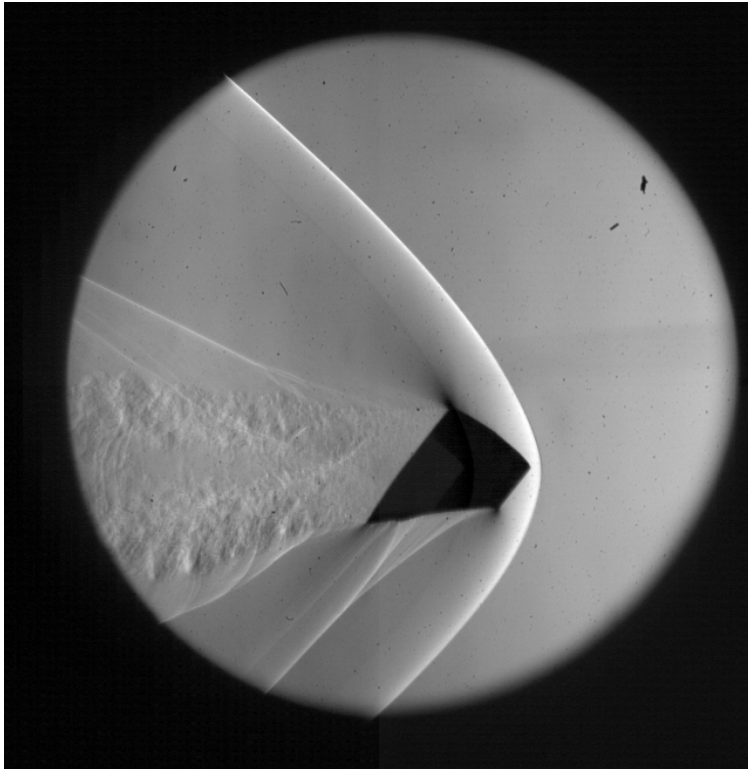
- Settles on a spin with thin edge in direction of travel (like a Frisbee)
- Experiences lower drag for longer portion of trajectory

Experimental Setup

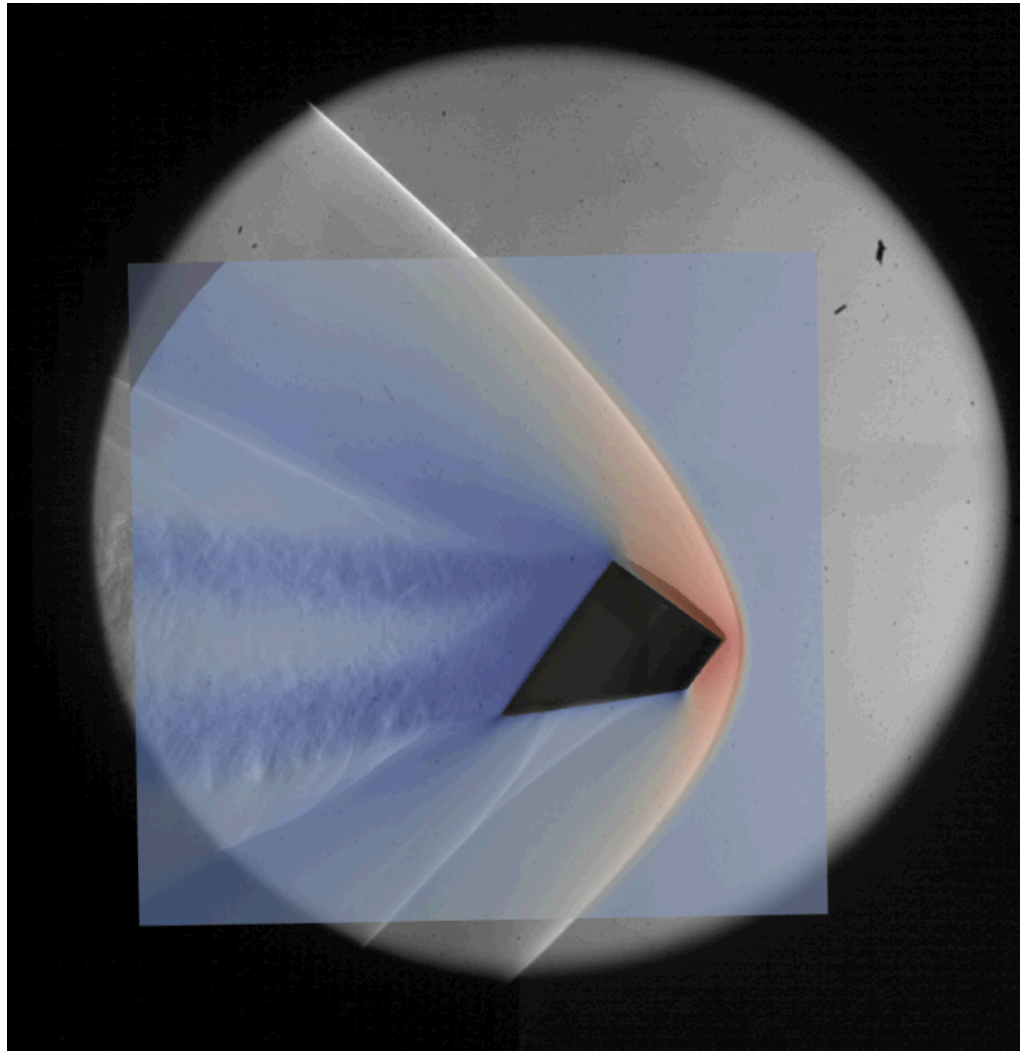


- **Approach: Shoot projectiles in unstable flight and track trajectories using series of camera stations and computer vision algorithms for simulation validation**

Comparison to CFD Simulations

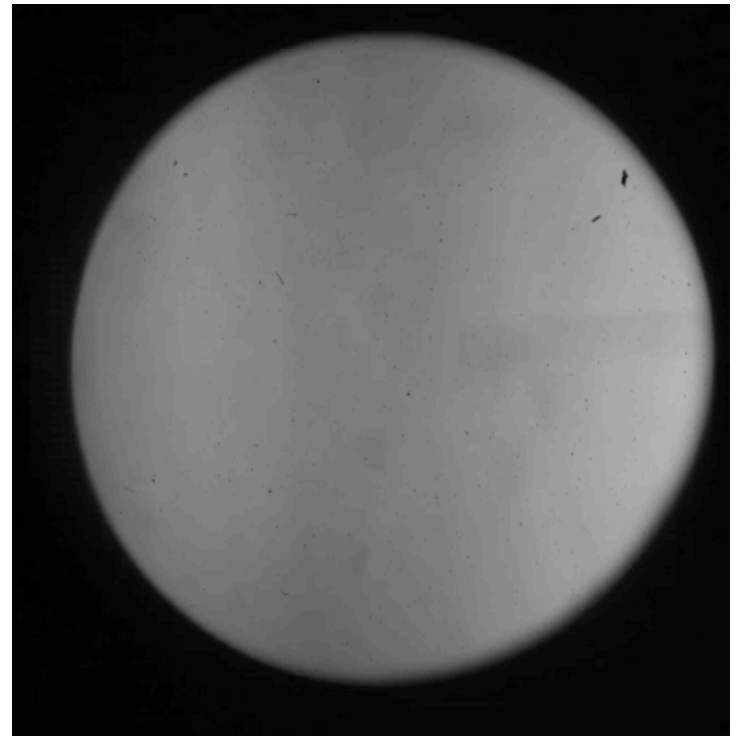


Flow Structures Line Up



Summary/Future Work

- Used simulations to determine trajectory distribution and flight dynamics of example fragment
- Experiments show promise in validating flow field and trajectory
- Future Work
 - Experimental data analysis
 - Effects of fragment shapes and sizes

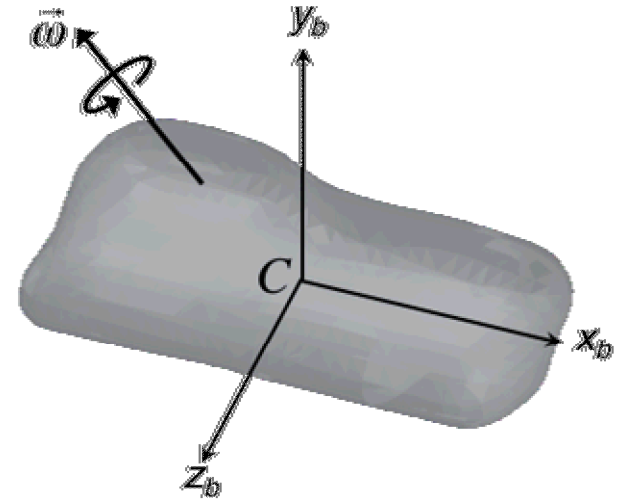


How to characterize tumbling?

- Angular velocity vector

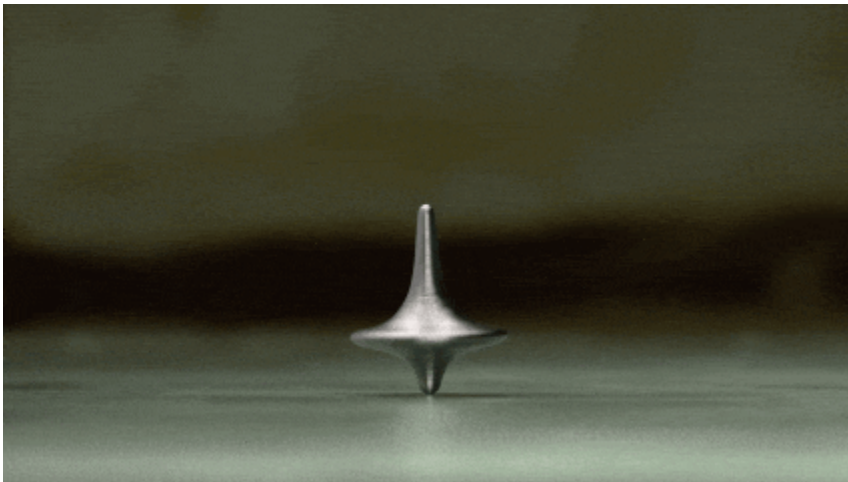
$$\vec{\omega} = p\hat{x}_b + q\hat{y}_b + r\hat{z}_b$$

- Plot (p, q, r) components in 3D pqr -space
- “Rotation trajectories”



Pure spin

pqr -space : Point



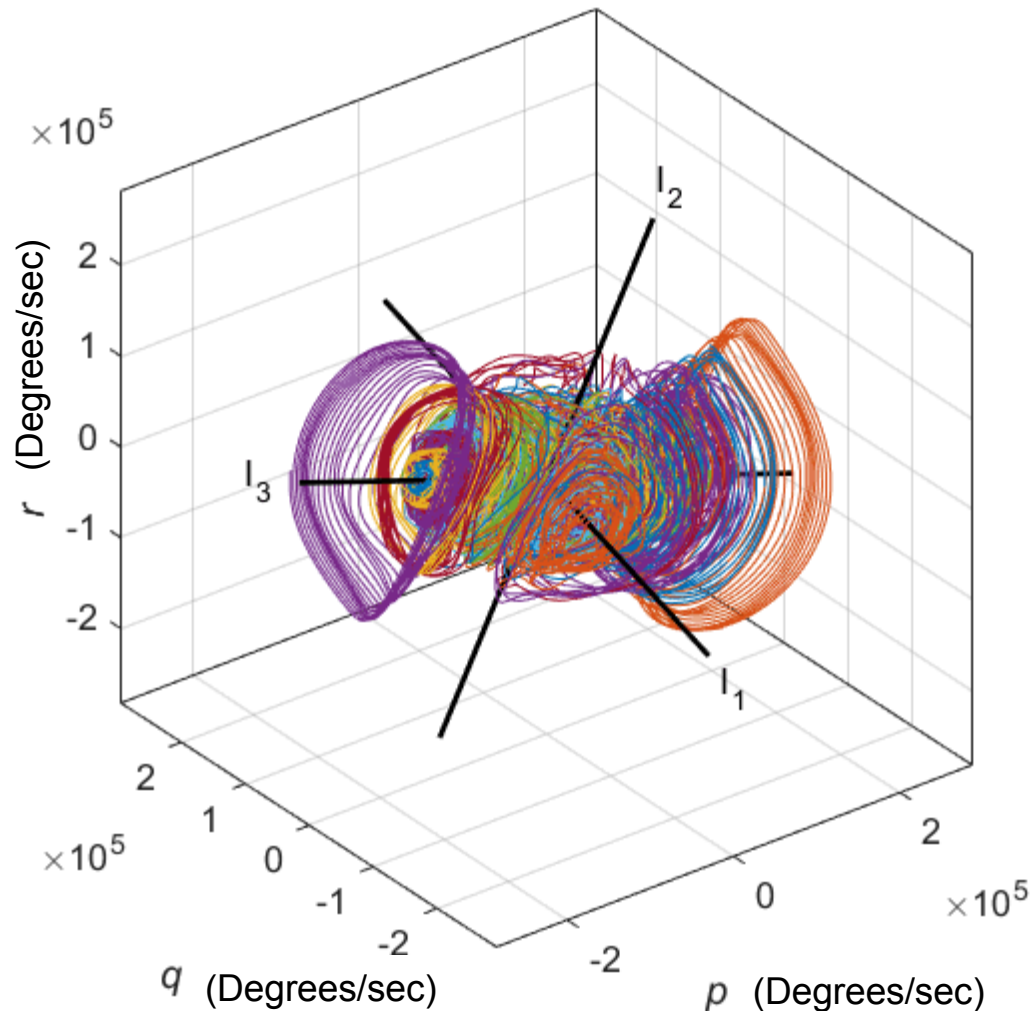
Spin + Precession

pqr -space: Orbit about spin axis



Inception. Warner Bros. Pictures, 2010.

“Rotation Trajectories” for Fragment

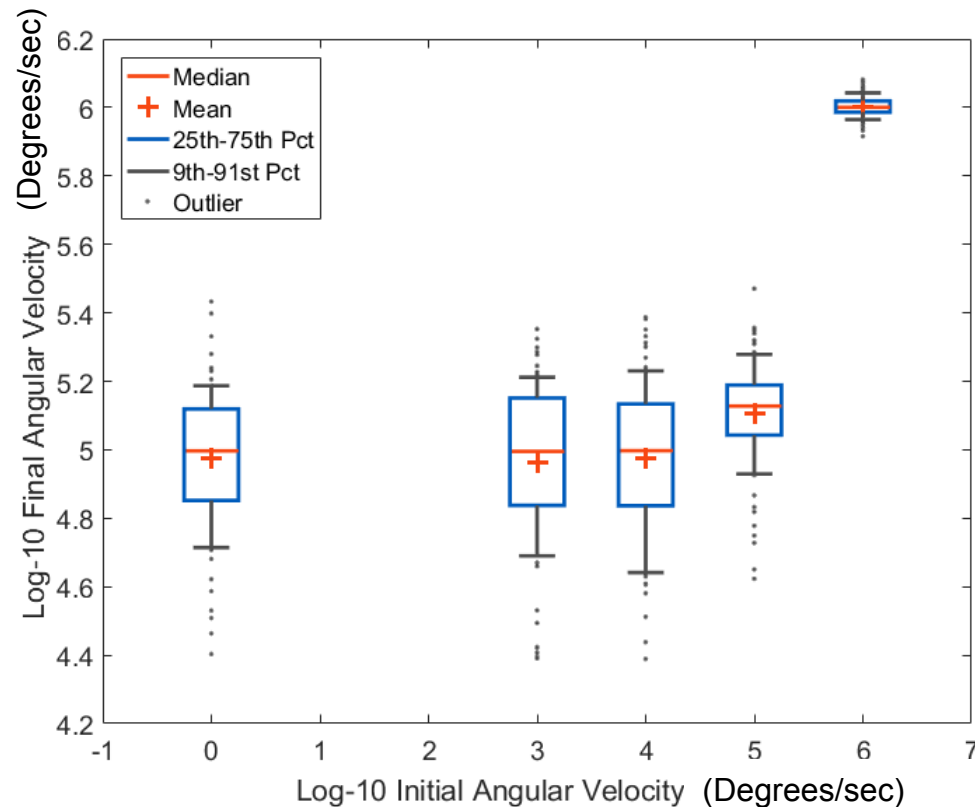


I_1, I_2, I_3 : Principal axes of rotation

- Spin + Precession about I_1, I_3
- Rotation about I_2 is unstable
 - “Intermediate Axis Theorem”

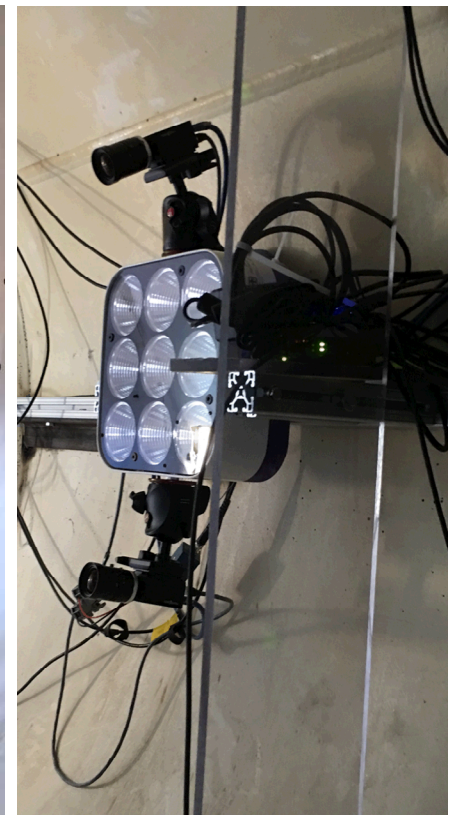
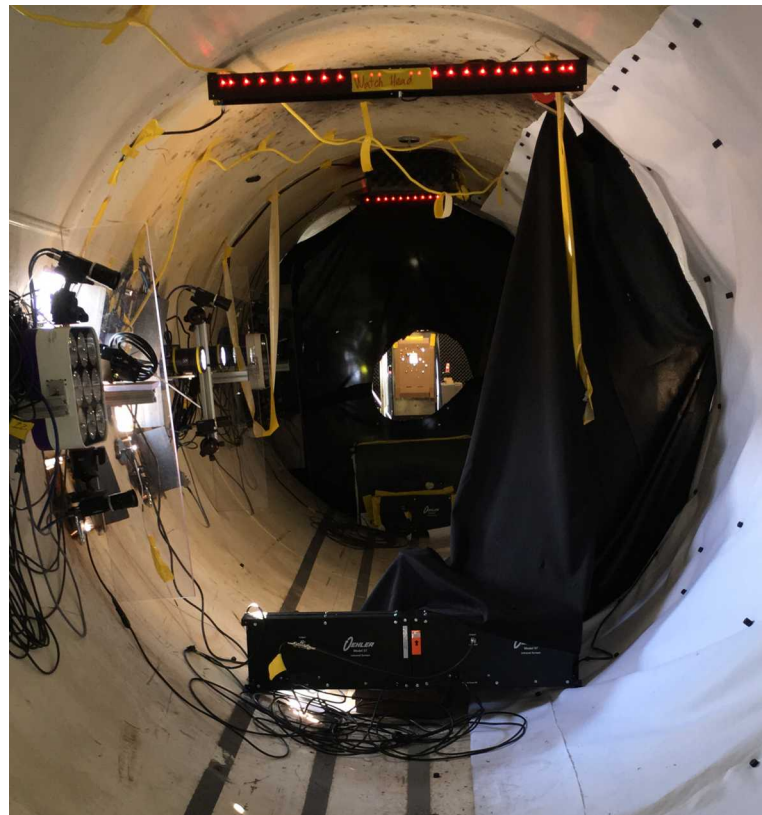
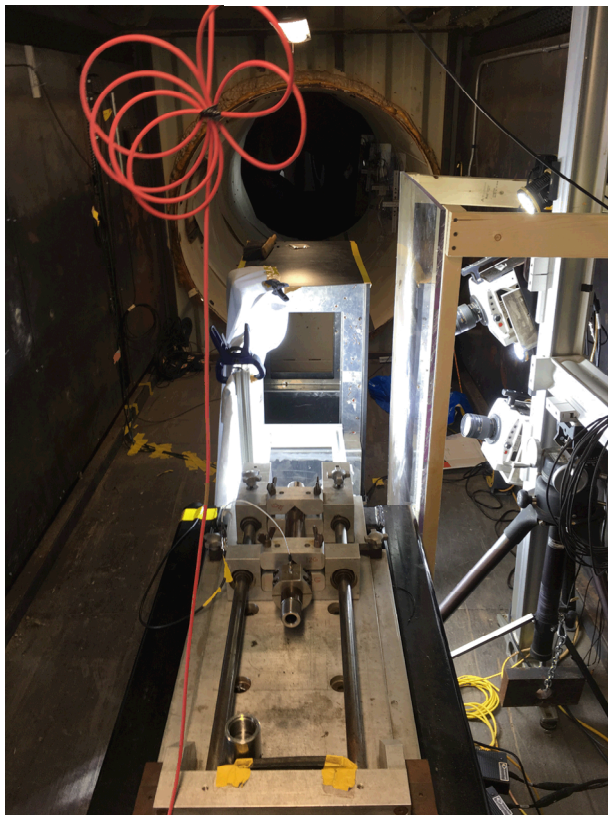
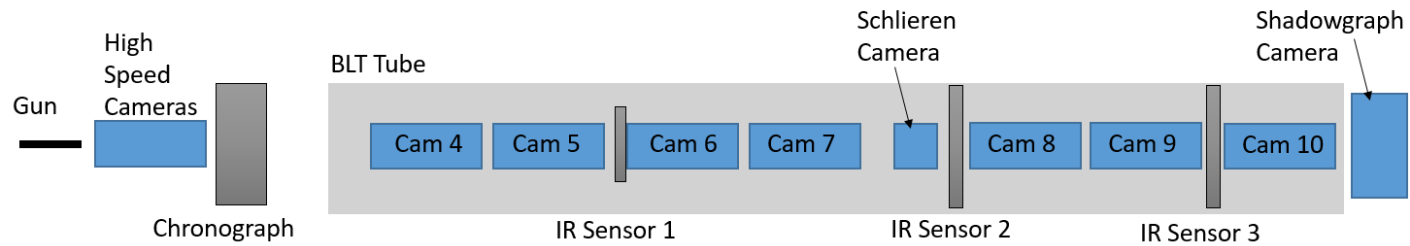
Steady Tumbling Rate

Random initial orientation
Random spin axis
100 samples per angular velocity



- Fragment reaches steady tumbling rate of $\sim 10^5$ deg/s (3.6 ms period)
- Higher initial tumbling rate is not dissipated in time

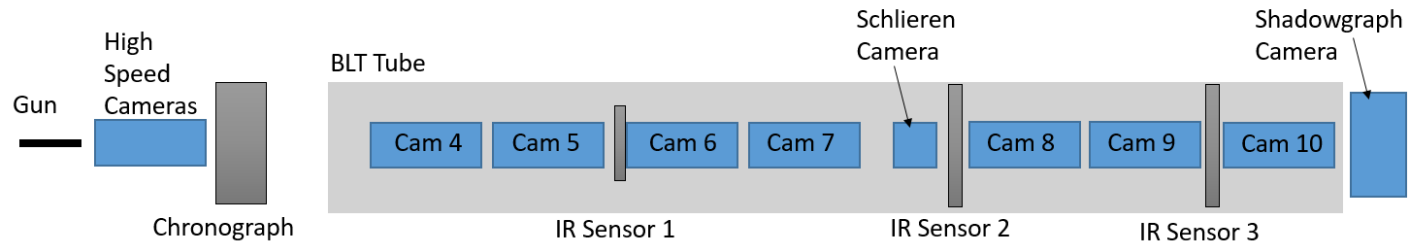
Stereo Systems



High Speed Stereo System



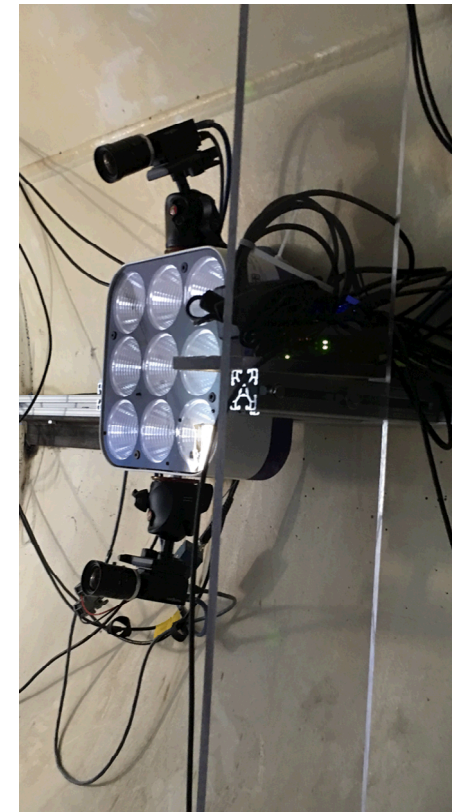
Stroboscopic Camera System



- Open shutter, light pulsed technique
- Need very high frequency light pulses for projectile



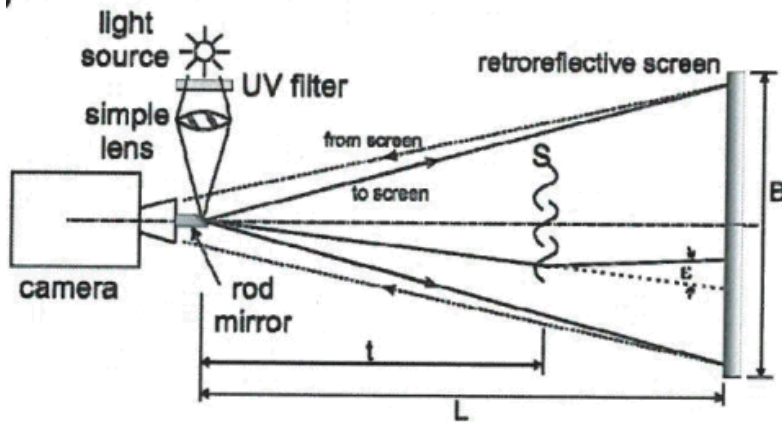
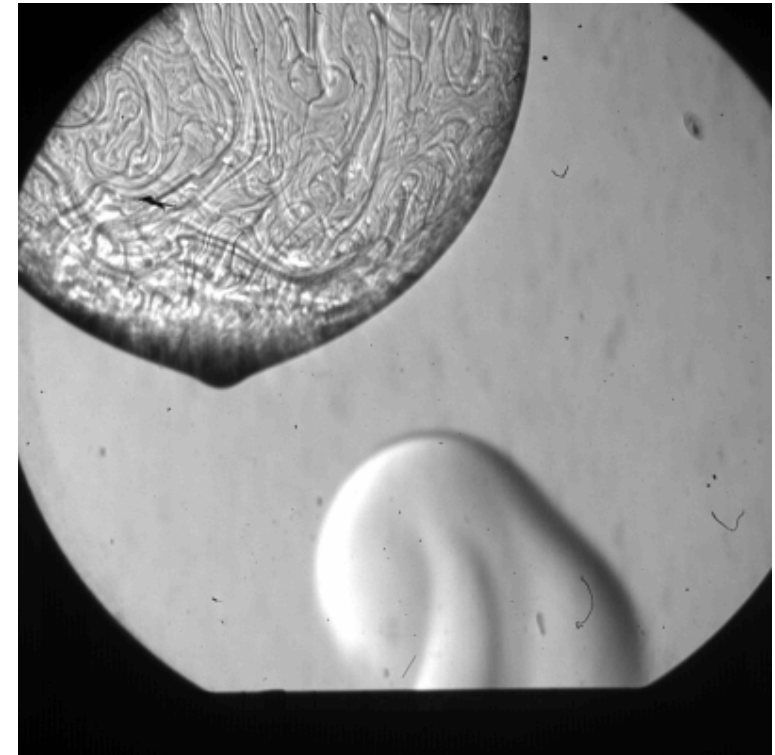
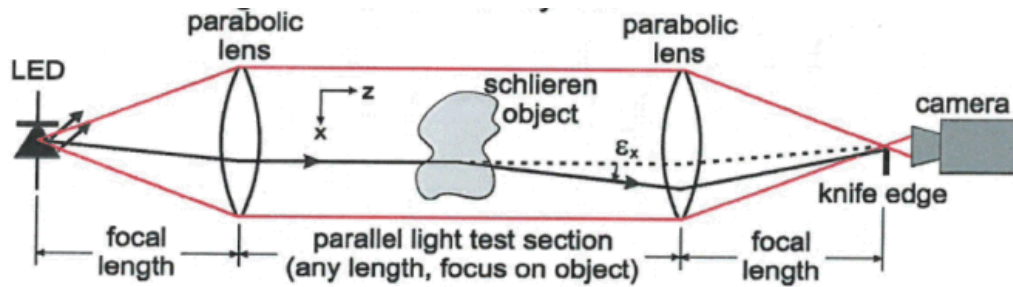
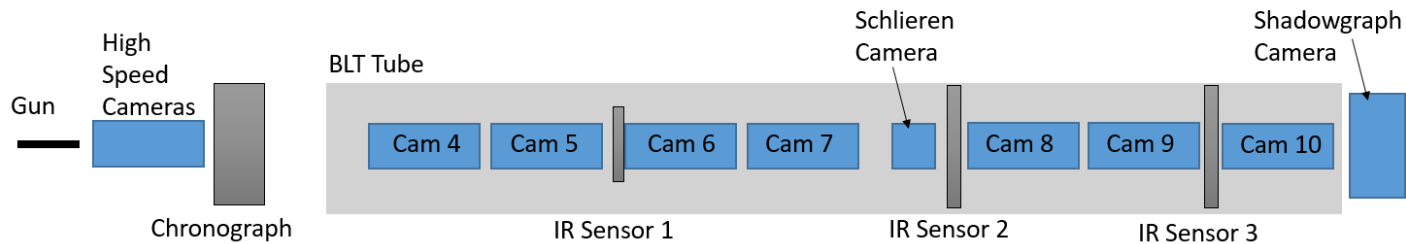
Wikipedia



Stroboscopic Images



Schlieren & Shadowgraph Imaging

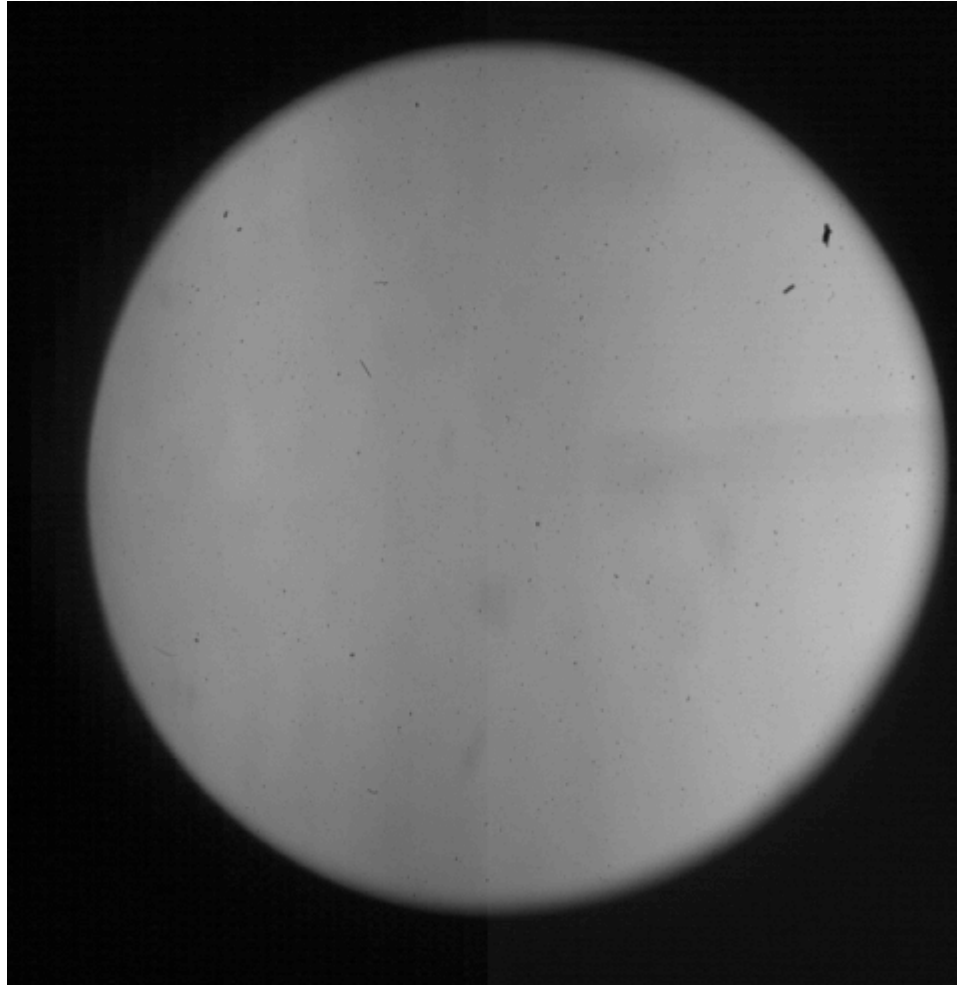


Michael Hargather, New Mexico Tech

Shadowgraph



Schlieren



Questions?

