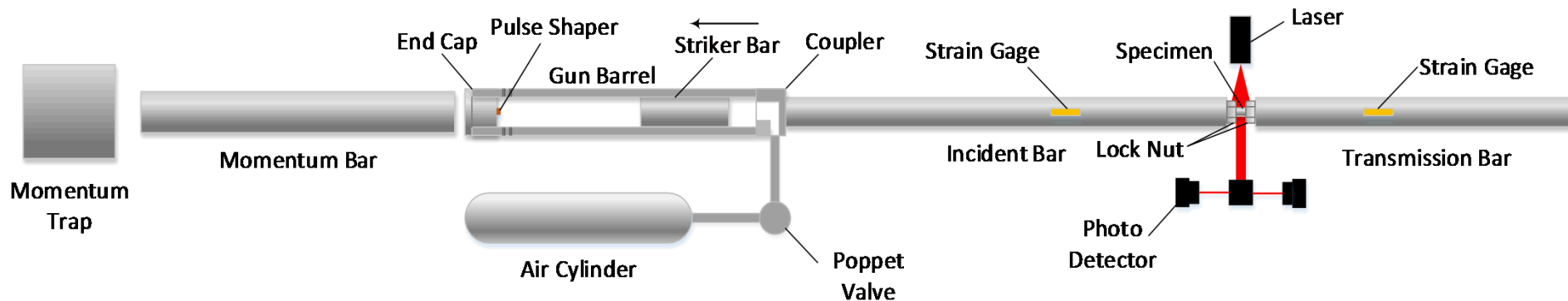


High Strain Rate Tensile Response of A572 and 4140 Steel

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# A572 and 4140 Steels

- American Society for Testing and Materials (ASTM) **A572 steel**
  - Columbium-Vanadium Steel
  - Minimum yield stress of ~400 MPa (quasi-static)
  - Good corrosion resistance

- Used in:
  - Building structures
  - Anchoring systems
  - Bridges
  - Boom sections



ASTM A572-50 steel beam for a bridge.

[www.steel-sections.com](http://www.steel-sections.com)

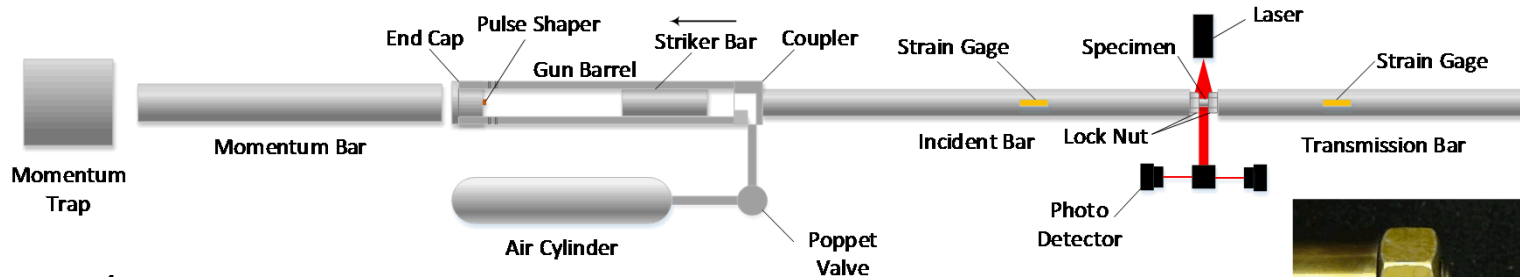
- American Iron and Steel Institute (AISI) **4140 Alloy**
  - Chromium-Molybdenum
  - Yield Strength ~650 MPa (quasi-static)
  - Excellent corrosion resistance

- Used in:
  - Hydraulic Shafts
  - Boring bars
  - Axles
  - Roll Cages
  - Bolts



# Scope of Work

- Dynamic tensile material characterization at high strain rates
  - $\sim 500, 1500, 3000 \text{ s}^{-1}$



$$\sigma_E = E \frac{A_0}{A_s} \varepsilon_t$$

$$\varepsilon_E = \begin{cases} c' \frac{L_1 - L_2}{L_s} & (\sigma \leq \sigma_y) \\ \frac{L_1 - L_2 - (1 - c')(L_1 - L_2)_{yield}}{L_s} & (\sigma > \sigma_y) \end{cases}$$

$$c' = \frac{\Delta L_s}{\Delta L + \Delta L_s} = 0.62$$



Available online at [www.sciencedirect.com](http://www.sciencedirect.com)

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DYMAT 23<sup>rd</sup> Technical Meeting

Dynamic Fracture of Ductile Materials

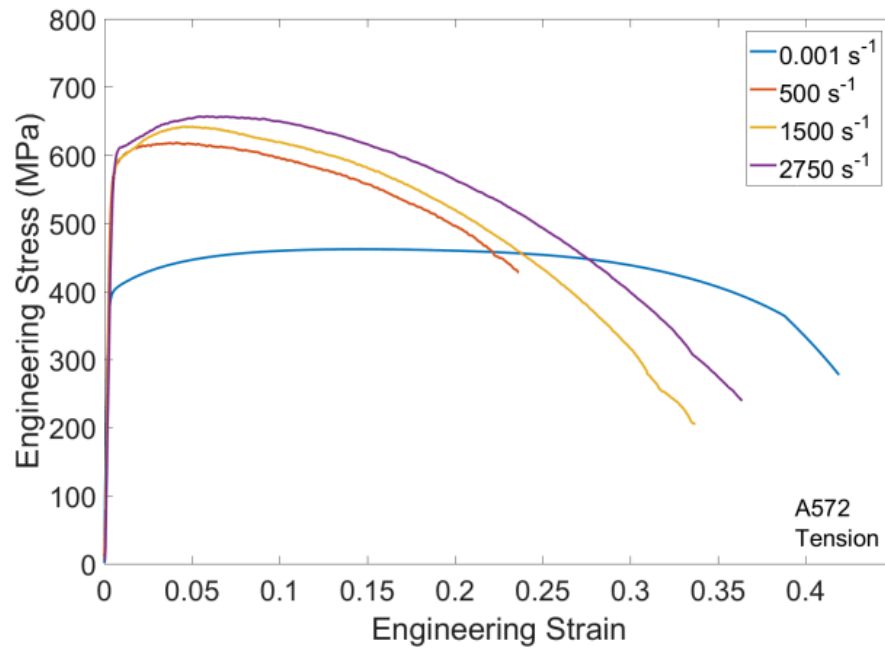
High Strain Rate Tensile Response of A572 and 4140 Steel

Brett Sanborn<sup>a,\*</sup>, Bo Song<sup>a</sup>, Andrew Thompson<sup>a</sup>, Blake Reece<sup>a</sup>, Stephen Attaway<sup>a</sup>

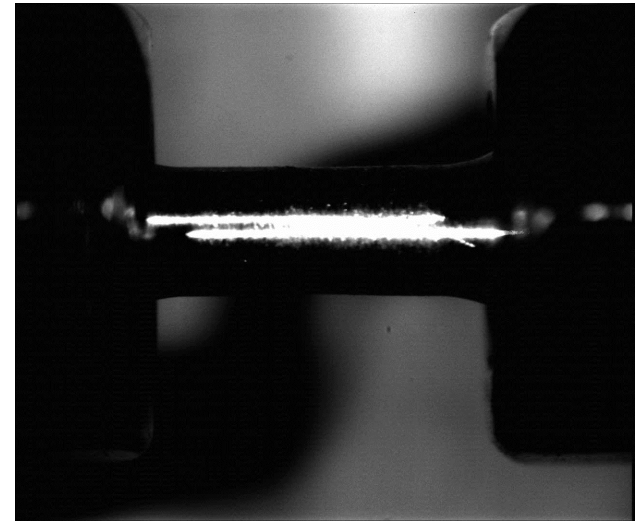
<sup>a</sup> Sandia National Laboratories, 1515 Eubank SE, Albuquerque, NM 87122, USA

- Rate-dependent material modeling
  - Modified Johnson-Cook model

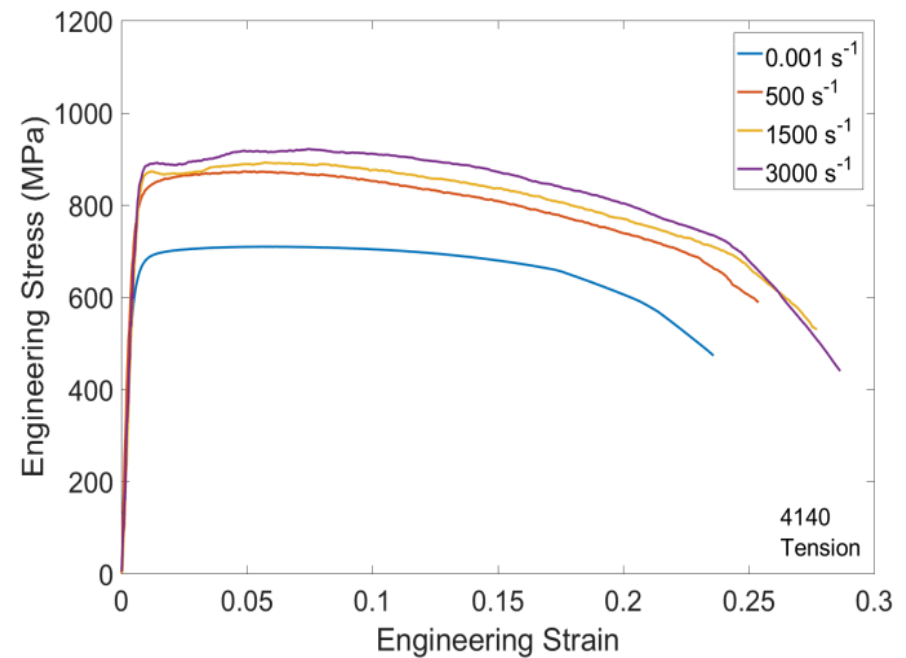
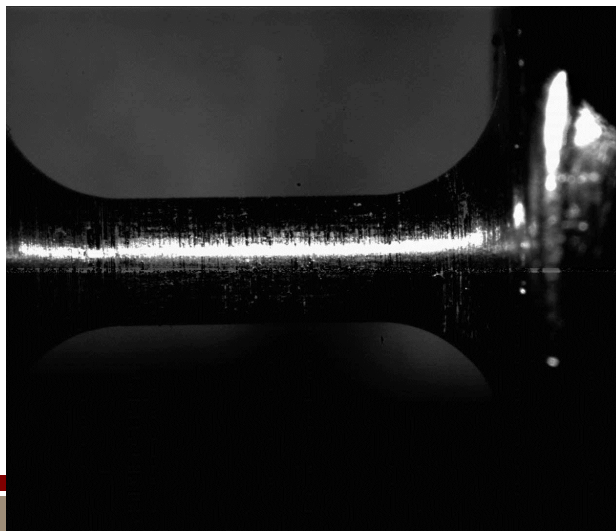
# Experimental Results



A572 #19



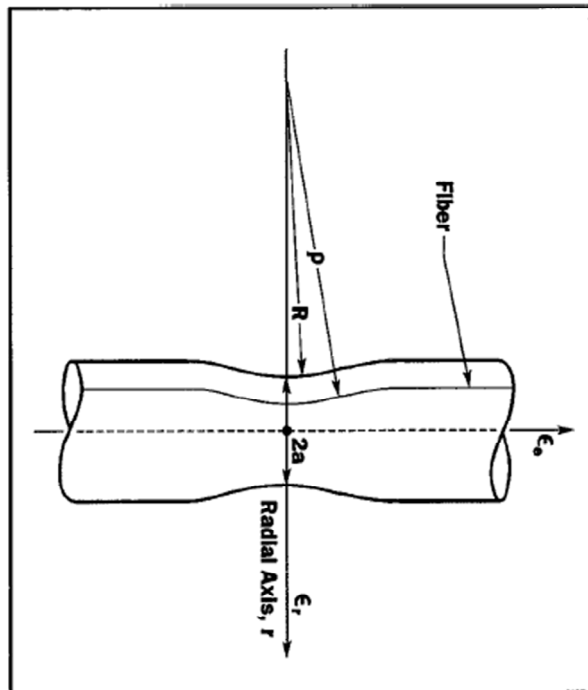
4140 #12



# Bridgman Correction for Necking

## Bridgman Correction

- Assumptions:
  - Uniform strain distribution in the minimum section
  - A longitudinal grid line deformed into a curve at the neck
- Good for rod



- True strain  $\epsilon_T = \ln \frac{A_0}{A}$
- Average true axial stress at the smallest cross section

$$(\sigma_a)_{av} = \frac{F}{A} = \sigma_E \frac{A_0}{A}$$

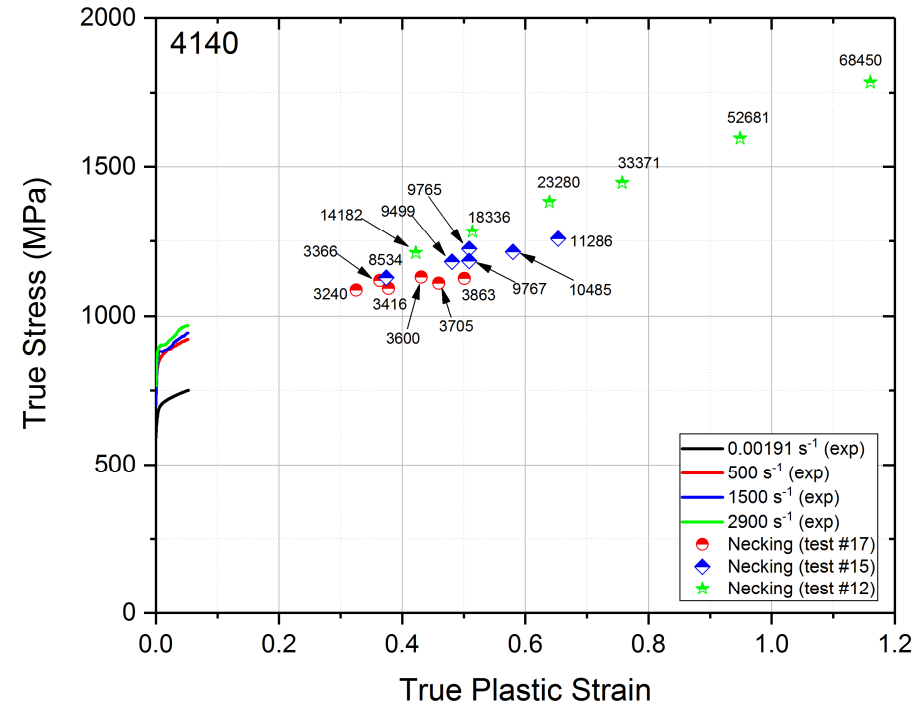
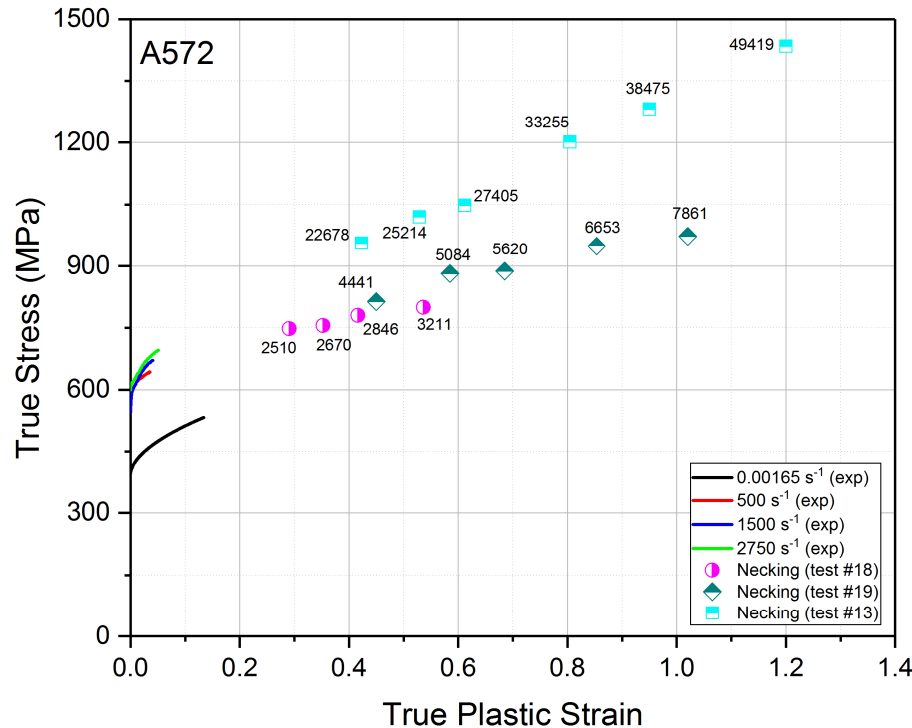
- Uniaxial stress correction

$$\sigma_T = k(\sigma_a)_{av}$$

$$k = \left[ \left( 1 + \frac{2R}{a} \right) \ln \left( 1 + \frac{a}{2R} \right) \right]^{-1}$$

- Requires instantaneous measurements of minimum cross sectional area,  $A$ , and radius,  $R$ .

# True Stress-Strain Response



## During necking

- True plastic strain becomes significantly higher
  - *More than 10 times elongated*
- Strain rate becomes significantly higher
  - *More than 10 times higher*

# Johnson-Cook Model

$$\sigma = \left( A + B \varepsilon^n \right) \cdot \left( 1 + C \ln \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) \cdot \left( 1 - T^{*m} \right)$$



Strain (work) hardening



Strain-rate effect (scaling)

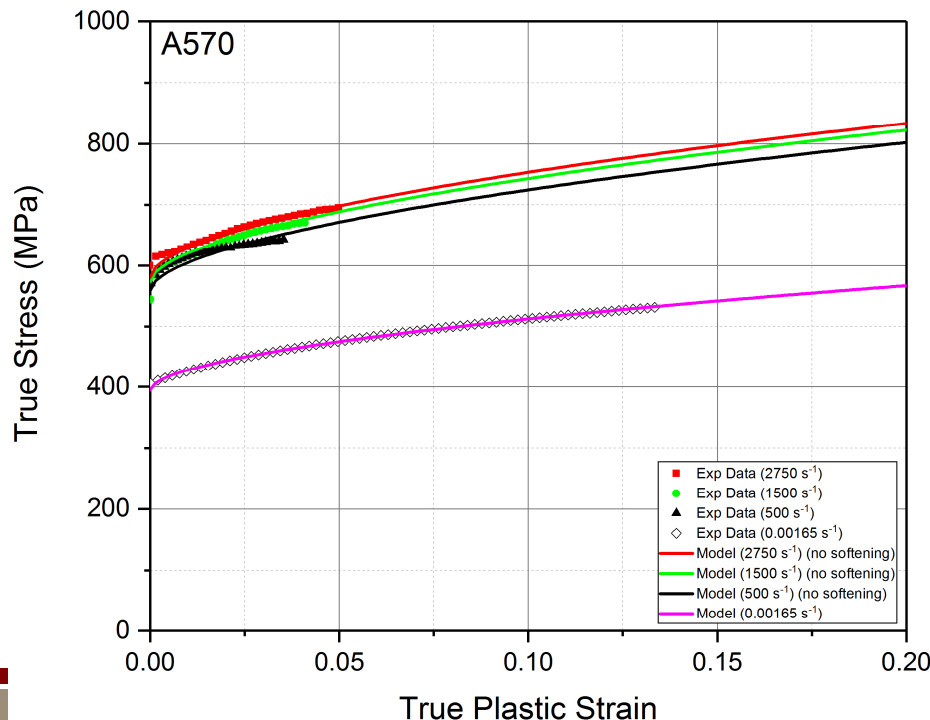


Temperature effect (thermal-softening)

$$T^* = \frac{T - T_0}{T_m - T_0}$$



The most difficult part !

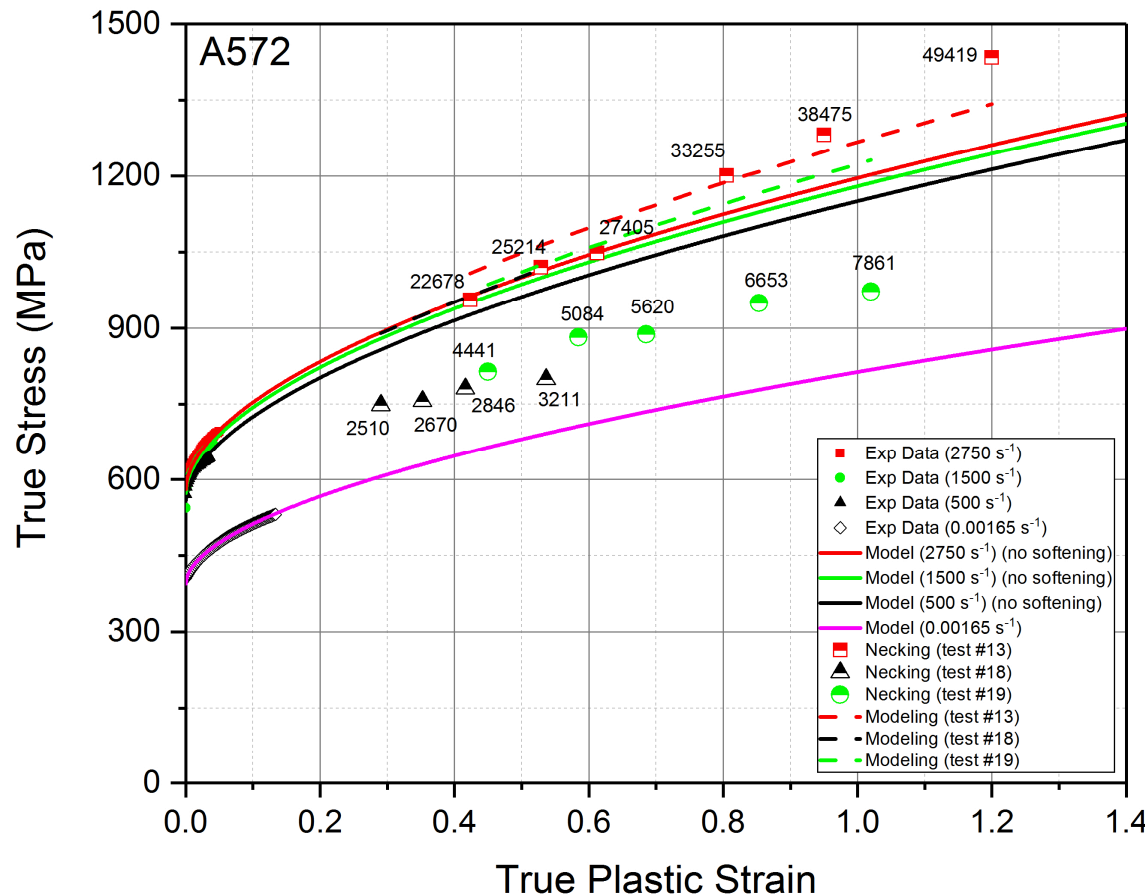


- May be neglected for room-temperature quasi-static tests
- What about room-temperature dynamic tests?

# Johnson-Cook Model (Temperature Effect)

$$\sigma = \left( A + B \varepsilon^n \right) \cdot \left( 1 + C \ln \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) \cdot \left( 1 - T^{*m} \right)$$

$$T^* = \frac{T - T_0}{T_m - T_0}$$



*What about room-temperature dynamic tests?*

➤ *Adiabatic heating must be considered*

➤ *In-situ temperature measurement*

➤ *Temperature effect on quasi-static material properties*

➤ *Uncertainties?*

$$\Delta T = \frac{\beta}{\rho C} \cdot \int \sigma d\varepsilon$$

*Where is “adiabatic”?*



# Modified Johnson-Cook Model for Thermal Softening

$$\sigma = \left( A + B \varepsilon^n \right) \cdot \left( 1 + C \ln \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) \cdot \left( 1 - T^{*m} \right)$$



$$T^* = (T_m - T_0) \cdot \Delta T = f(\varepsilon, \dot{\varepsilon}) \propto \varepsilon \cdot \ln \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0}$$

$$\sigma = \left( A + B \varepsilon^n \right) \cdot \left( 1 + C \ln \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) \cdot \left( 1 - D \left( \varepsilon \cdot \ln \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right)^m \right)$$

when  $\varepsilon = 0 \longrightarrow T^* = 0$

when  $\dot{\varepsilon} = \dot{\varepsilon}_0 \longrightarrow T^* = 0$

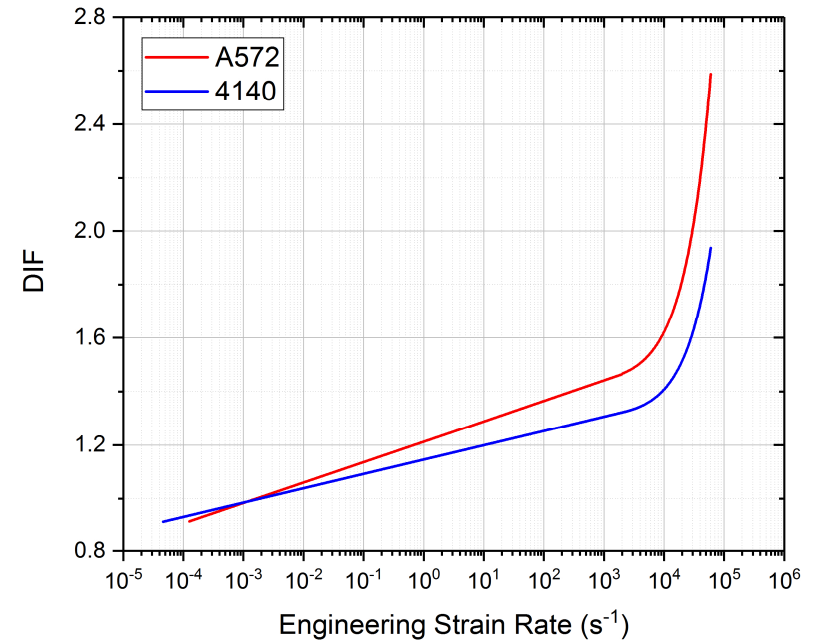
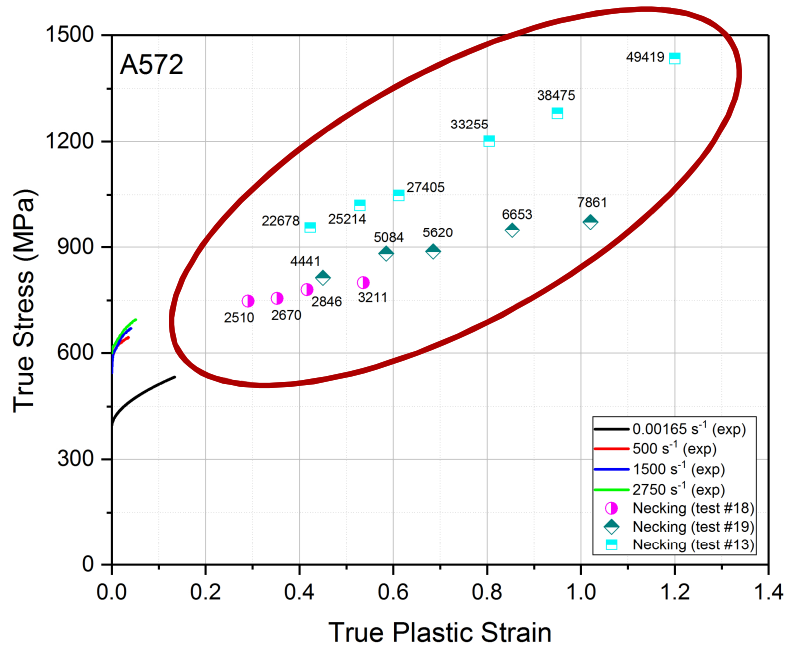
**No temperature rise**

$\dot{\varepsilon}_0$  is reference strain rate which is sufficiently low to be considered isothermal.

**Showing adiabatic heating at higher strain rates**



# Modified Johnson-Cook Model For Strain-Rate Effect

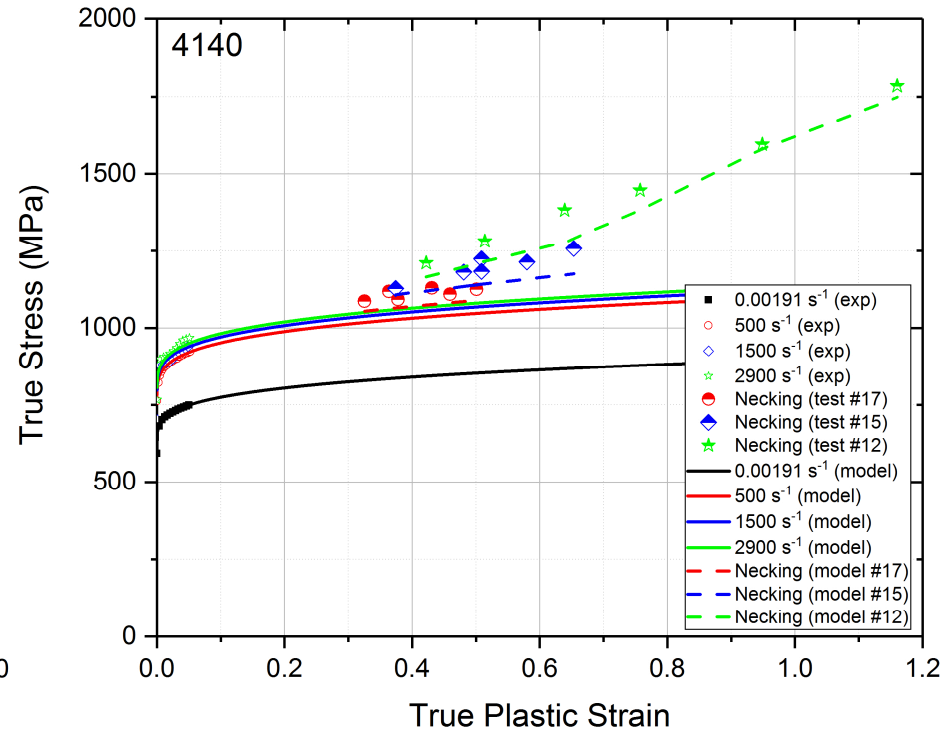
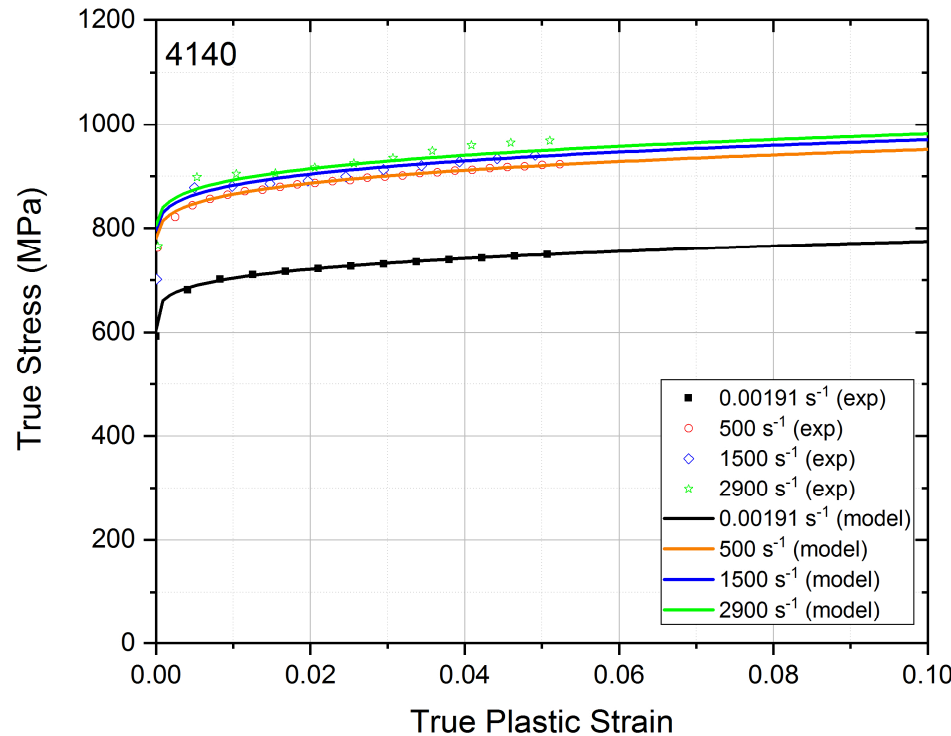


$$\sigma = \left( A + B \varepsilon^n \right) \cdot f \left( \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) \cdot \left( 1 - D \left( \varepsilon \cdot \ln \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right)^m \right)$$

$$f \left( \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) = \begin{cases} 1 + C_0 \ln \left( \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) & \dot{\varepsilon} \leq \dot{\varepsilon}^* \\ C_1 + C_2 \cdot \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} & \dot{\varepsilon} > \dot{\varepsilon}^* \end{cases}$$

$\dot{\varepsilon}^* = 2500 \text{ s}^{-1}$

# Modified Johnson-Cook Model for A572 Steel

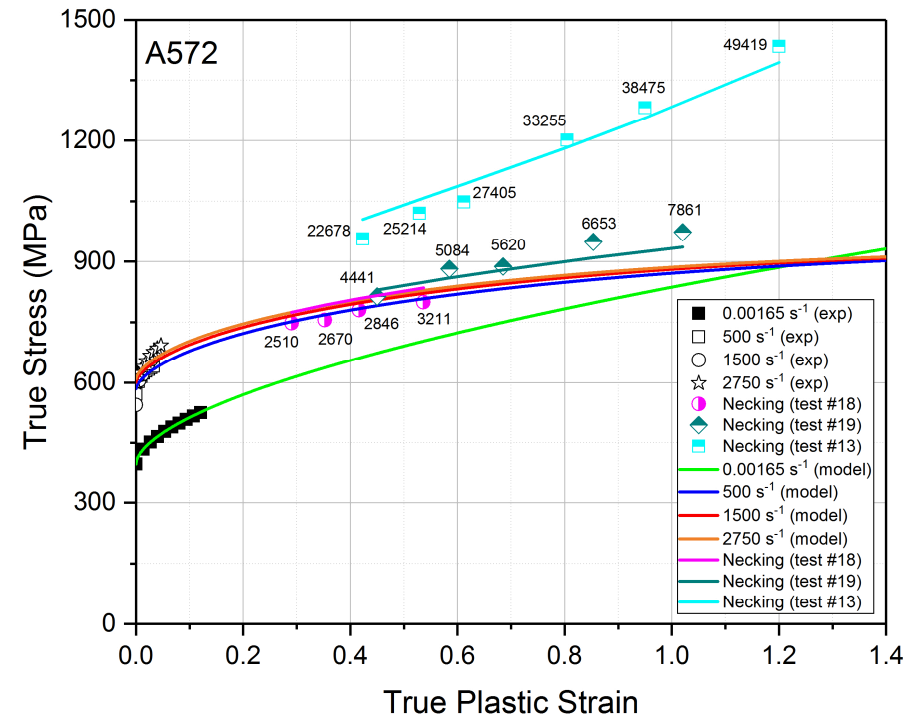
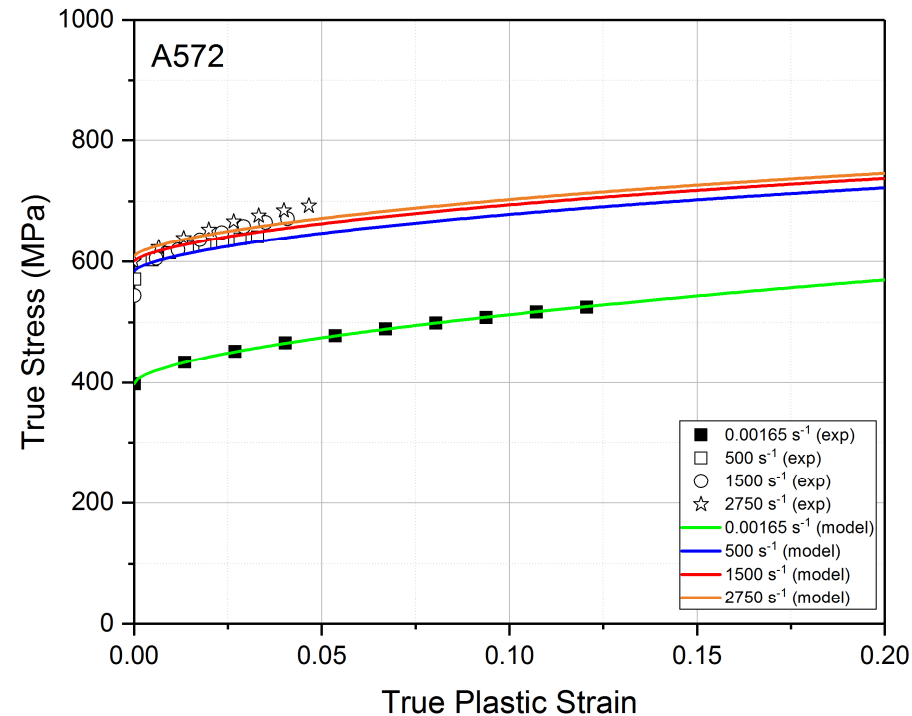


$$A = 605.53 \text{ MPa} \quad B = 291.31 \text{ MPa} \quad n = 0.2375 \quad D = 0.04739$$

$$m = 0.01235 \quad C_0 = 0.02327 \quad C_1 = 1.3016 \quad C_2 = 3.0583 \times 10^{-8}$$

$$\dot{\epsilon}_0 = 0.00191 \text{ s}^{-1} \quad \dot{\epsilon}^* = 2500 \text{ s}^{-1}$$

# Modified Johnson-Cook Model for 4140 Steel



$$A = 397.82 \text{ MPa} \quad B = 438.77 \text{ MPa} \quad n = 0.5821 \quad D = 0.08893$$

$$m = 0.4676 \quad C_0 = 0.03714 \quad C_1 = 1.4807 \quad C_2 = 3.3551 \times 10^{-8}$$

$$\dot{\epsilon}_0 = 0.00165 \text{ s}^{-1} \quad \dot{\epsilon}^* = 2500 \text{ s}^{-1}$$

# Conclusion

- A572 and 4140 steels were characterized in tension using Kolsky tension bar at high strain rates.
- The tensile stress and strain data during necking were obtained through high-speed measurement of necking geometries and corrected with Bridgman correction.
- The experimental data were used to modify Johnson-Cook model to reflect strain-rate and thermal-softening effect prior to and after necking.

$$\sigma = \left( A + B \varepsilon^n \right) \cdot f \left( \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) \cdot \left( 1 - D \left( \varepsilon \cdot \ln \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right)^m \right) \quad f \left( \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) = \begin{cases} 1 + C_0 \ln \left( \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} \right) & \dot{\varepsilon} \leq \dot{\varepsilon}^* \\ C_1 + C_2 \cdot \frac{\dot{\varepsilon}}{\dot{\varepsilon}_0} & \dot{\varepsilon} > \dot{\varepsilon}^* \end{cases}$$