

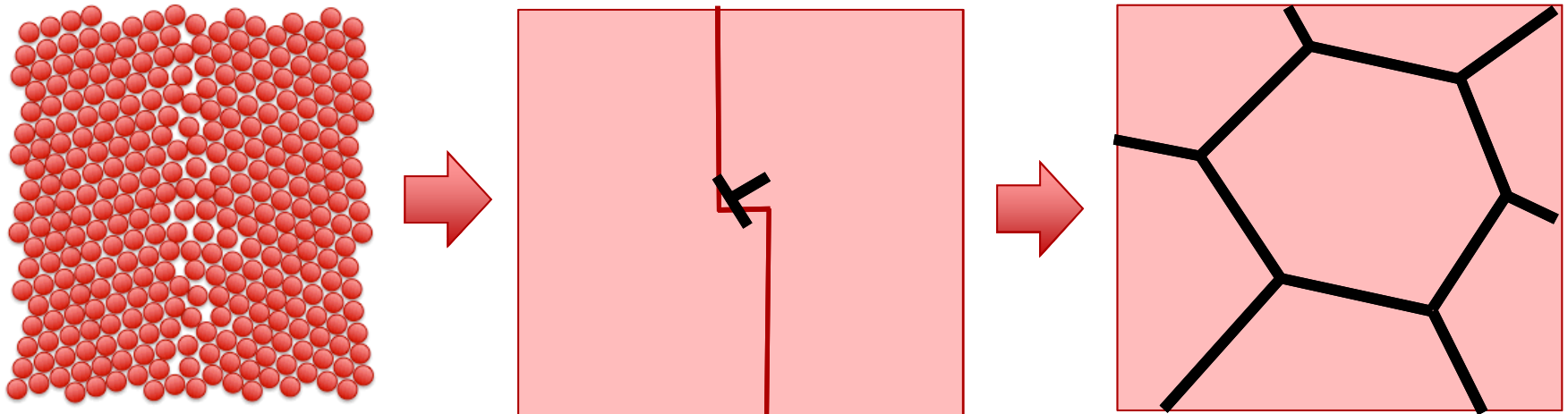
Interfacial Line Defects:

Bridging Structural Information Between Atomic and Continuum Length Scales

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Interfacial Line Defects:

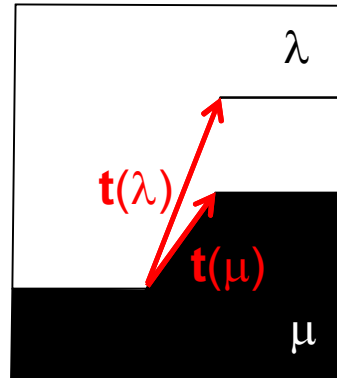
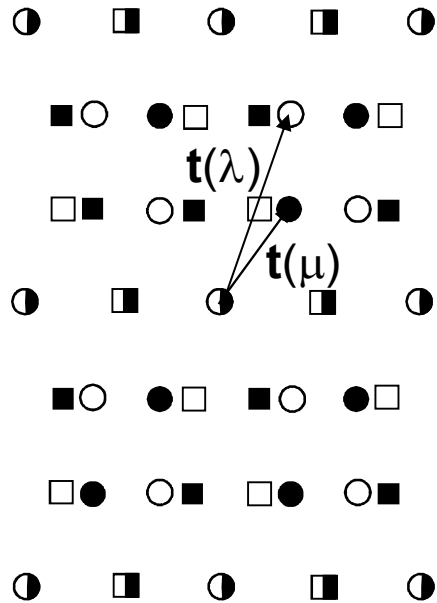
An important bridging concept



- **Connection between details of atomic structure and larger-scale structure and behavior of interfaces.**
- **Essential to extending from specific boundaries to more general boundaries**
- **Clues to essential physics and mechanisms controlling behavior and properties of interfaces.**

In general interfacial line defects have both dislocation and step content

Dichromatic Pattern Volterra Operation



$$t(\lambda) = \frac{1}{2}[1\bar{2}1]_{\lambda}$$

$$t(\mu) = \frac{1}{2}[101]_{\mu}$$

$$\mathbf{b} = \frac{1}{3}[1\bar{1}1]_{\lambda}$$

"disconnection" :
both step and dislocation content

R.C. Pond, Dislocations in Solids, Chapter 38 (1989)
J. Hirth & R.C. Pond, Acta Materialia (1996)

Crystal lattice translation vectors

$$\mathbf{b}_{ij} = \mathbf{t}(\lambda)_{ij} - \mathbf{P} \mathbf{t}(\mu)_{ij}$$

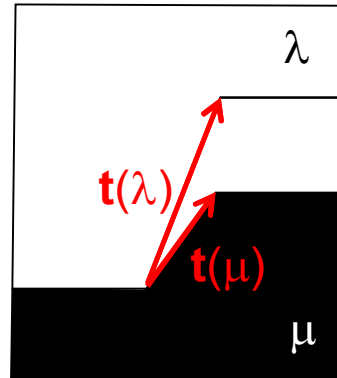
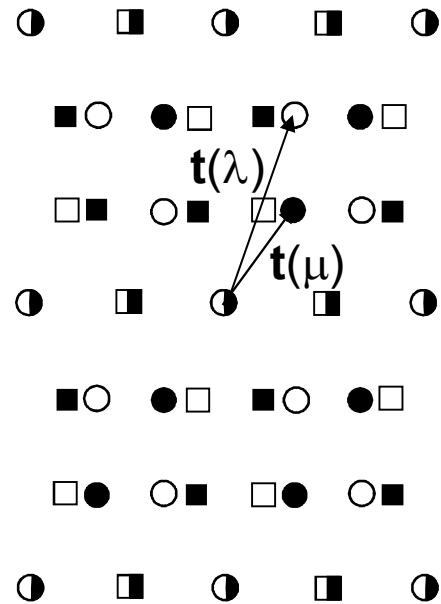
Burgers
vectors of
the set of
"admissible"
defects

Matrix converts
from μ to λ crystal
coordinates

**Definition of a
physically
meaningful
reference state
is critical.**

In general interfacial line defects have both dislocation and step content

Dichromatic Pattern Volterra Operation

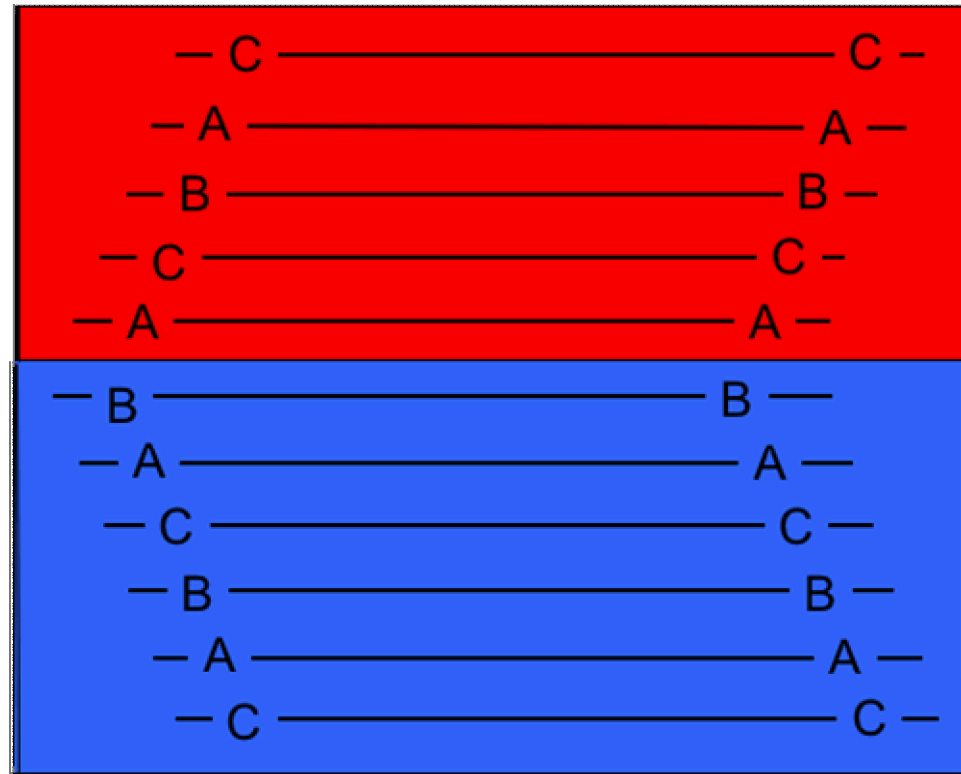


$$t(\lambda) = \frac{1}{2}[1\bar{2}1]_{\lambda}$$

$$t(\mu) = \frac{1}{2}[101]_{\mu}$$

$$\mathbf{b} = \frac{1}{3}[1\bar{1}1]_{\lambda}$$

Example: $(1/3)\langle 111 \rangle$ disconnection:
FCC $\{111\}$ twin boundary ($\Sigma=3$)



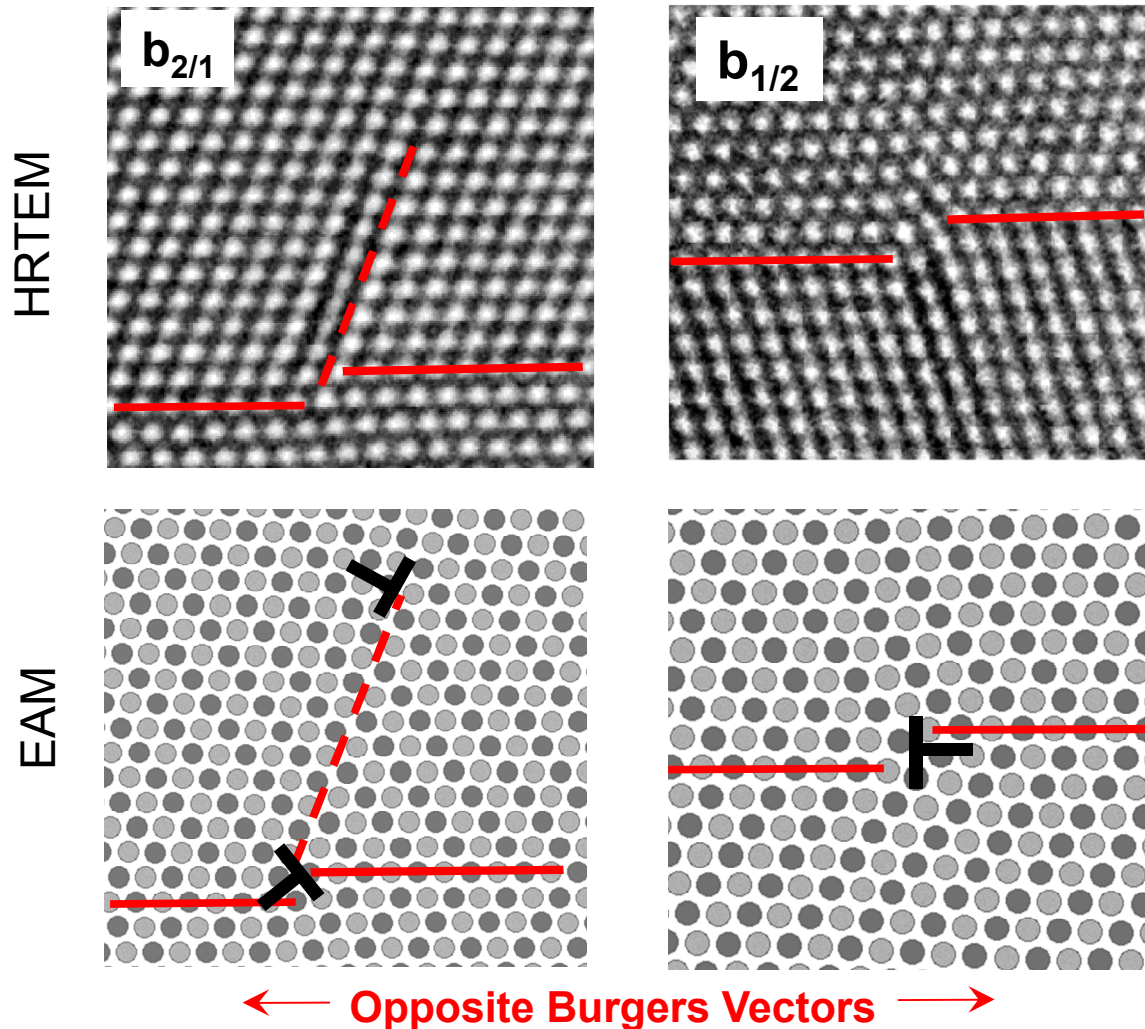
"disconnection" :
both step and dislocation content

R.C. Pond, Dislocations in Solids, Chapter 38 (1989)

J. Hirth & R.C. Pond, Acta Materialia (1996)

(1/3) $\langle 111 \rangle$ Disconnection at twin in Au: Sandia National Laboratories

Core-relaxation by stacking fault emission



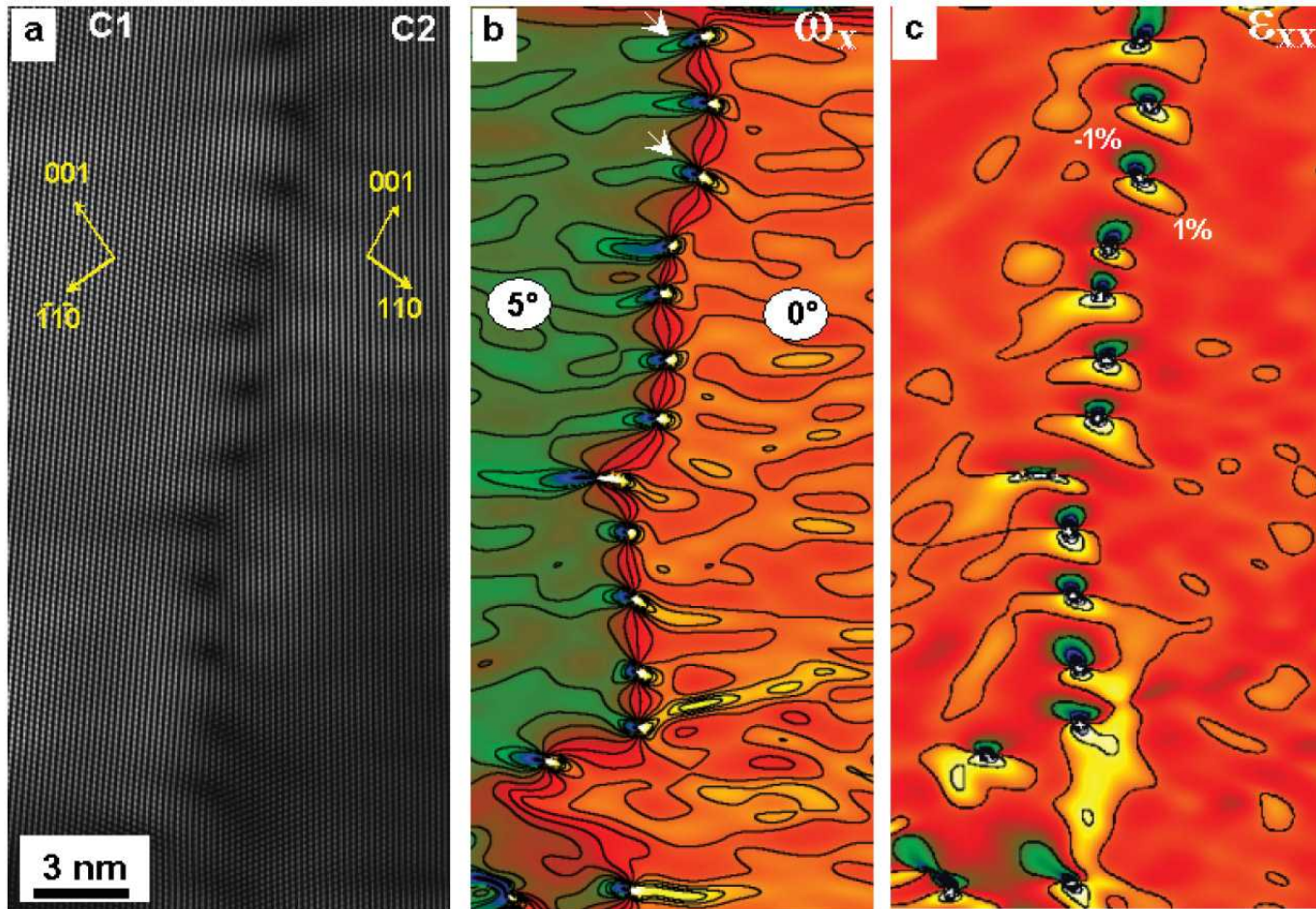
- Interface breaks symmetry of dislocation.

- $b_{2/1}$ reduces strain energy by dissociating into Shockley and stair rod dislocations.

- $b_{1/2}$ disconnection cannot dissociate without creating unfavorable “AA” stacking.

E.A. Marquis and D.L. Medlin, Phil. Mag. Letters (2005).

$(1/3)\langle 111 \rangle$ dislocations accommodating misorientation at $\Sigma=3$ twin boundary



Deformed
Ultra Fine
Grained
(UFG) Copper

HRTEM
Strain analysis
from Geometric
Phase Analysis
(GPA)

M. Sennour, S. Lartigue-Korinek, Y. Champion, M.J. Hytch, Phil Mag (2007)

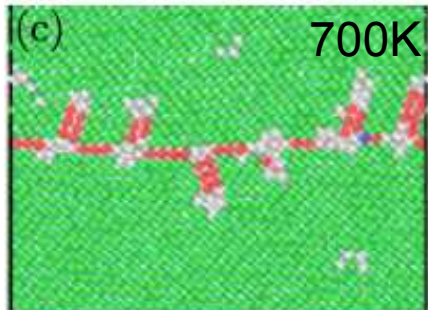
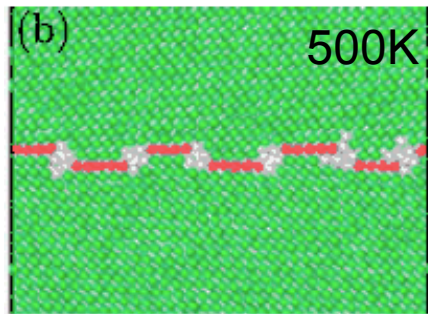
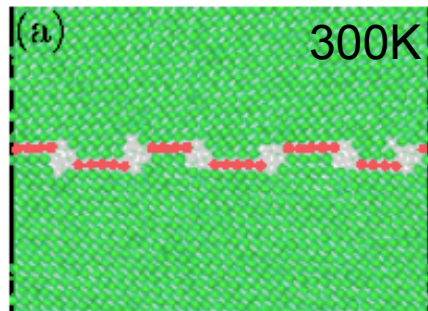
Grain Boundary Structural Transition: dissociation of $(1/3)\langle 111 \rangle$ disconnections with compact core

$(1/3)\langle 111 \rangle$ Disconnections

$\Delta\theta = +8.98^\circ$ from exact $\Sigma=3$

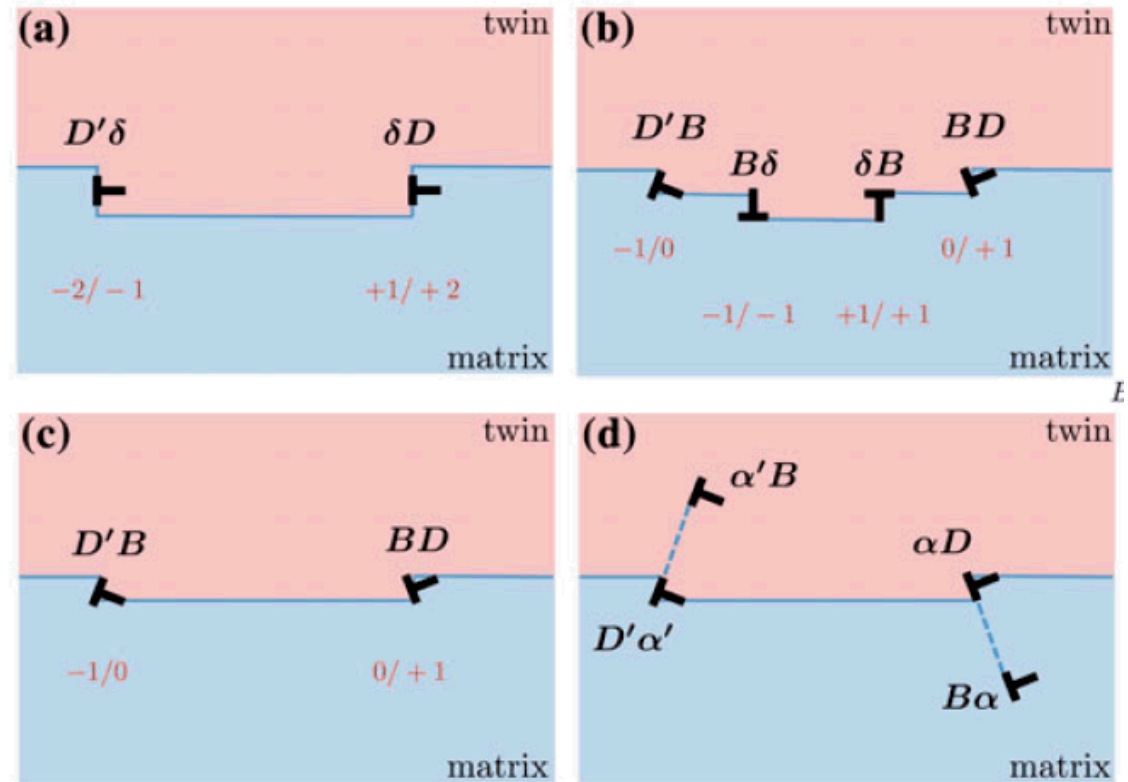
Compact Core

Dissociated



GB Free Energy vs Misorientation from $\Sigma=3$

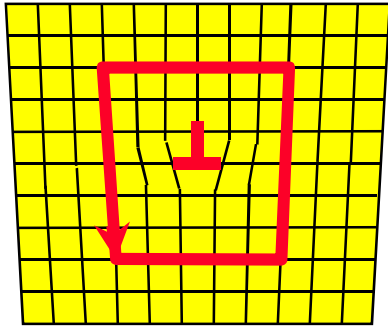
$(1/3)\langle 111 \rangle$ disconnections emit oppositely signed $(1/6)\langle 112 \rangle$ disconnections on twin terraces



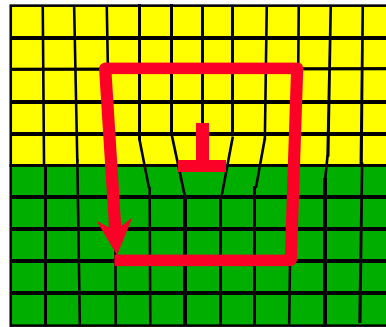
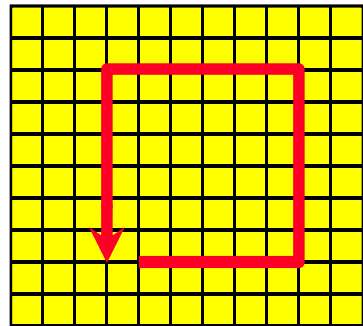
C.J. O'Brien, D.L. Medlin, S.M. Foiles,
Philosophical Magazine (2016)

Misfit Dislocations: topological analysis in *coherent* reference frame

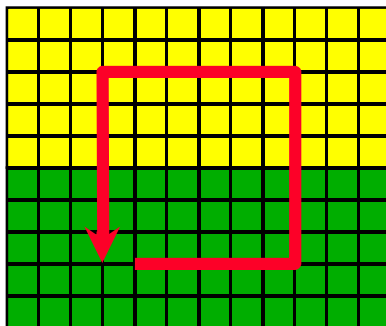
Bulk Lattice Dislocation. Heteroepitaxial Misfit Dislocation.



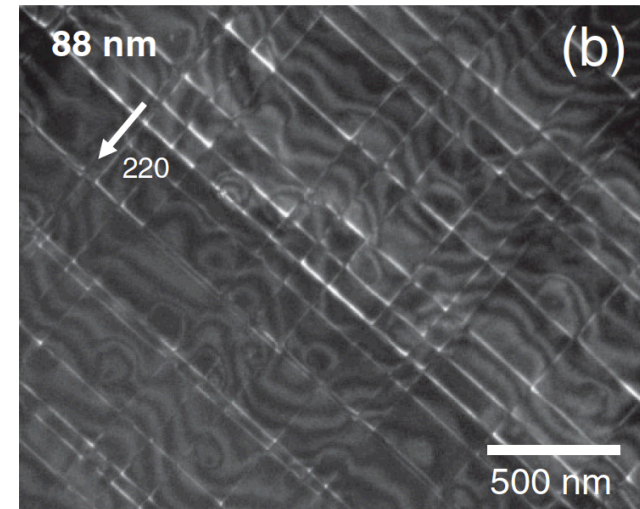
Reference Frame:
Perfect Crystal



Reference Frame:
Coherently Strained Interface



**Example: Misfit dislocations
Si/Si_{0.8}Ge_{0.2} interface
(Plan-view TEM)**



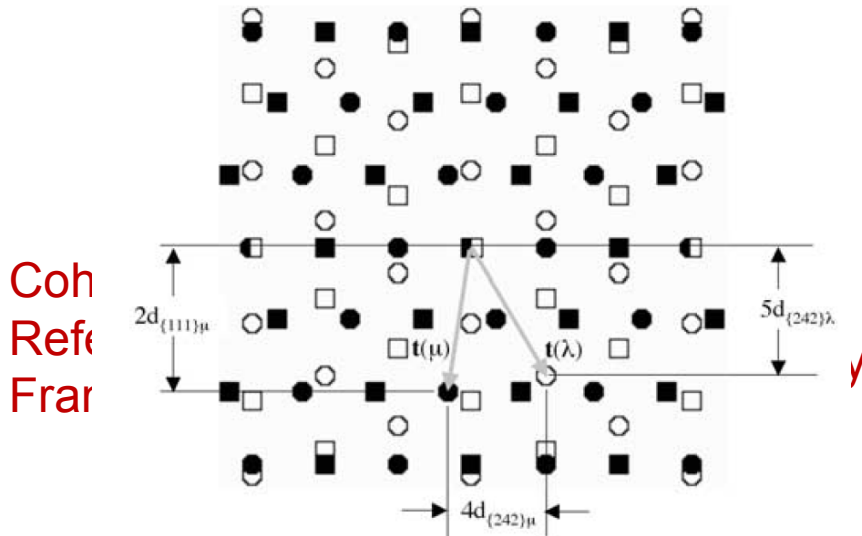
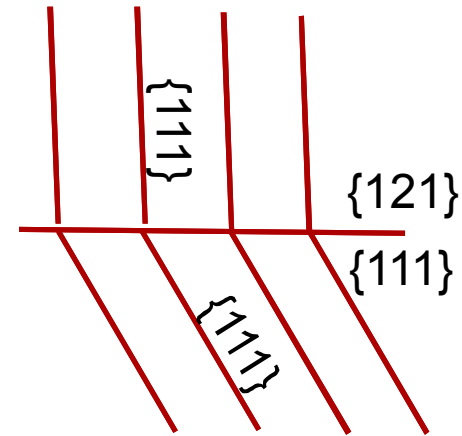
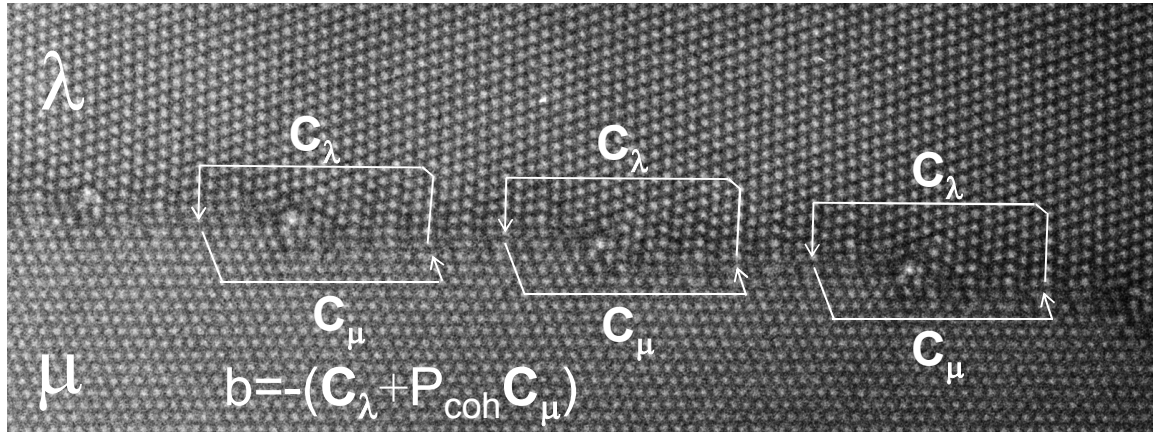
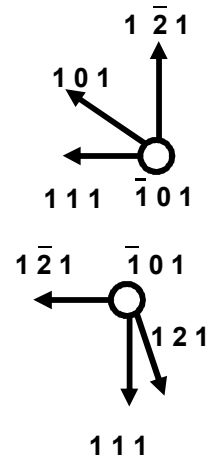
Cheaito, Duda, Beechem, Hattar, Ihlefeld, Medlin, Rodriguez, Campion, Piekos, Hopkins, Phys. Rev. Letts., **109**, 195901 (2012)

**Equilibrium density of misfit dislocations
cancels the long range coherency strain**

Accommodation of Grain Boundary Coherency Strain by Disconnections

90° Boundary in Gold

5.7% strain across terraces

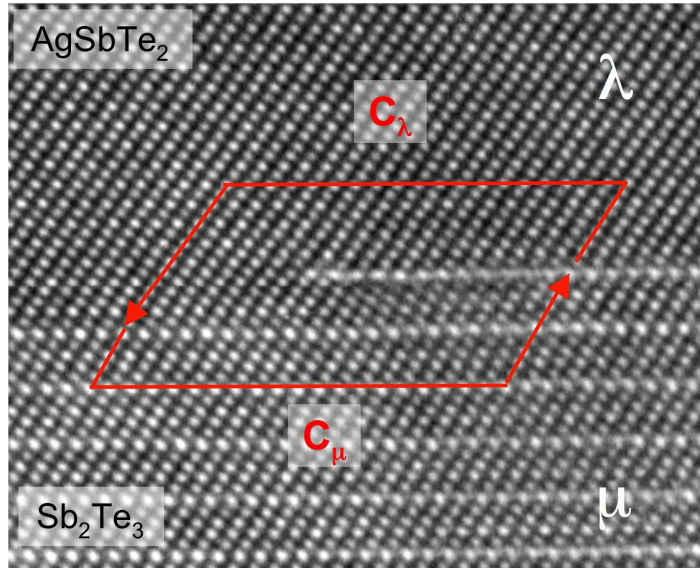


- P_{coh} describes 90° crystal rotation and strain to bring λ and μ into coherency.
- Defects efficiently accommodate the 5.7% misfit on the $\{111\}/\{112\}$ facets.
- Nearest CSL is $\Sigma=99$

Disconnections in Phase Transformations

Example: Sb_2Te_3 precipitate in AgSbTe_2 thermoelectric

Burgers vector:



Upper crystal
circuit

Lower crystal
circuit

$$\mathbf{b} = -(\mathbf{C}_\lambda + \mathbf{P}\mathbf{C}_\mu)$$

- Coordinate Transformation from Tetradymite to Rock-salt.
- Coherently strained reference frame

Resolve \mathbf{b} into components normal and parallel to interface

$$\mathbf{b}_n = (a_{cub} - c_{hex} / 3\sqrt{3})[111]$$

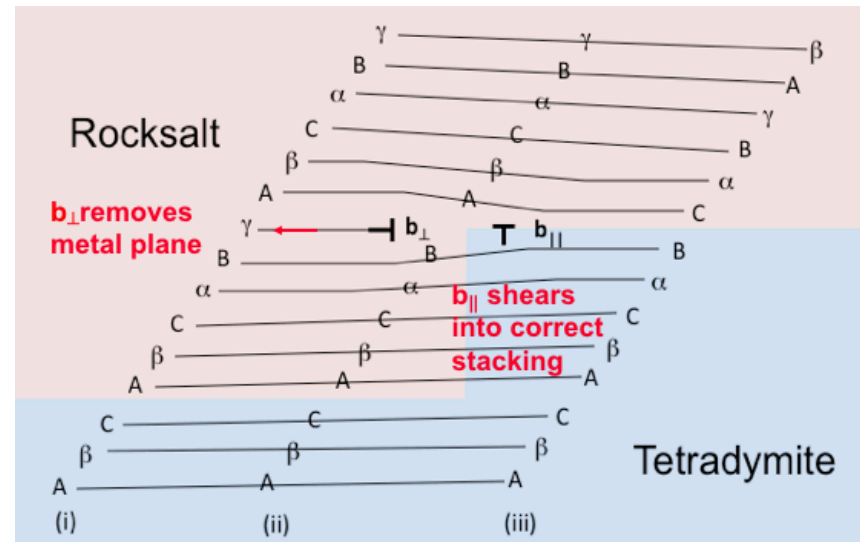
•mismatch of step heights.

$$|\mathbf{b}_n| = 0.3747\text{\AA}$$

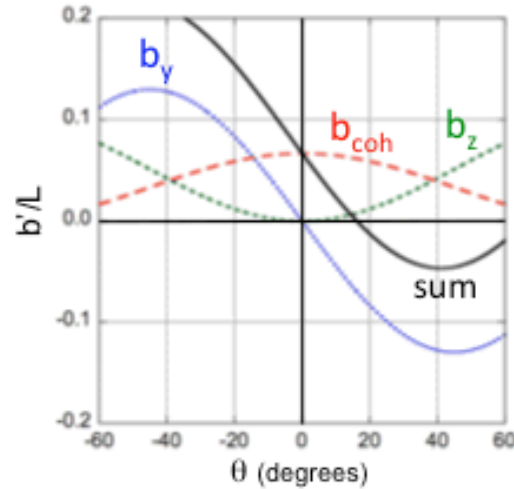
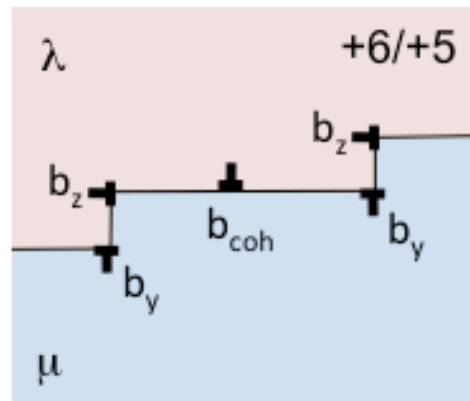
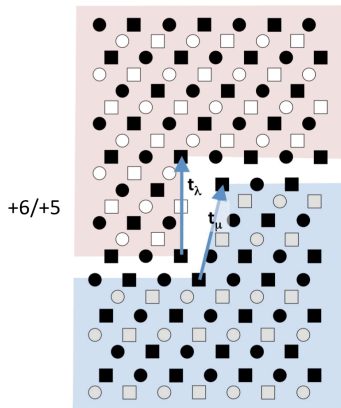
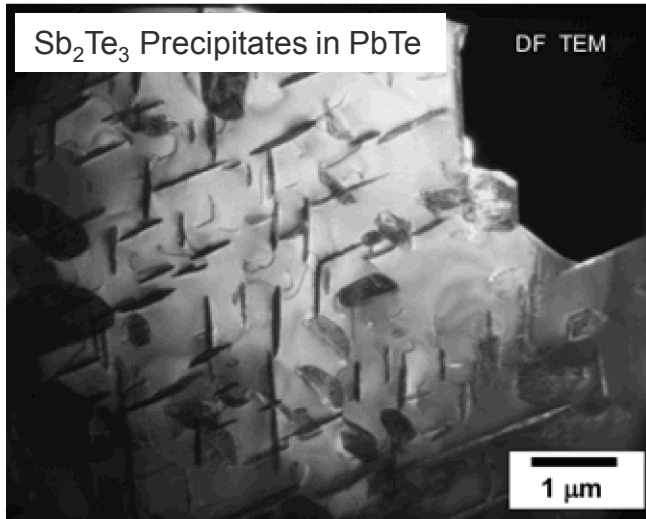
$$\mathbf{b}_\parallel = \frac{a_{cub}}{6}[\bar{1}2\bar{1}]$$

•Analogous to Shockley partial Dislocation

$$|\mathbf{b}_\parallel| = 2.48\text{\AA}$$



A system with larger misfit: PbTe/Sb₂Te₃

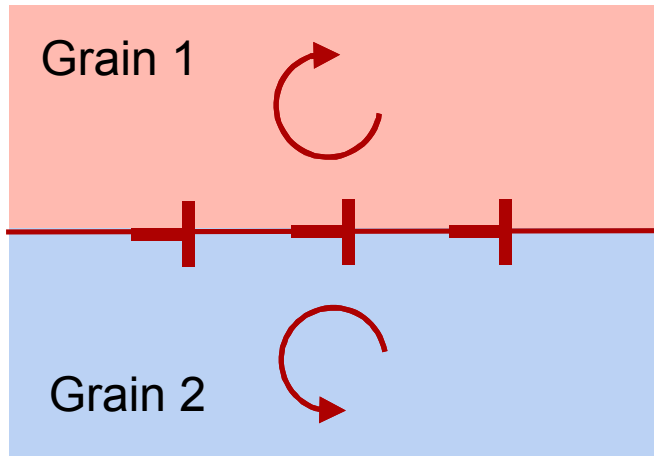


Habit plane inclination:

Measured: 14.8°
Predicted: 16.2°

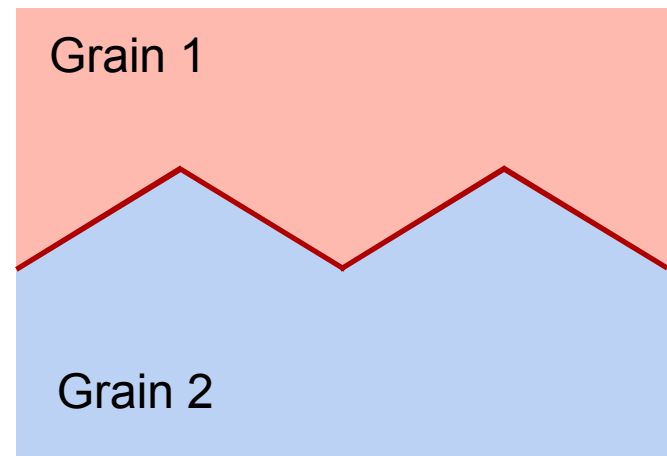
Defect spacing accommodates the (111)/(0001) coherency strain.

Facet Junctions and Grain Boundary Dislocations: Accommodating deviations from low energy interfaces



- **Misorientation:**

- Accomodate deviation with grain boundary dislocations



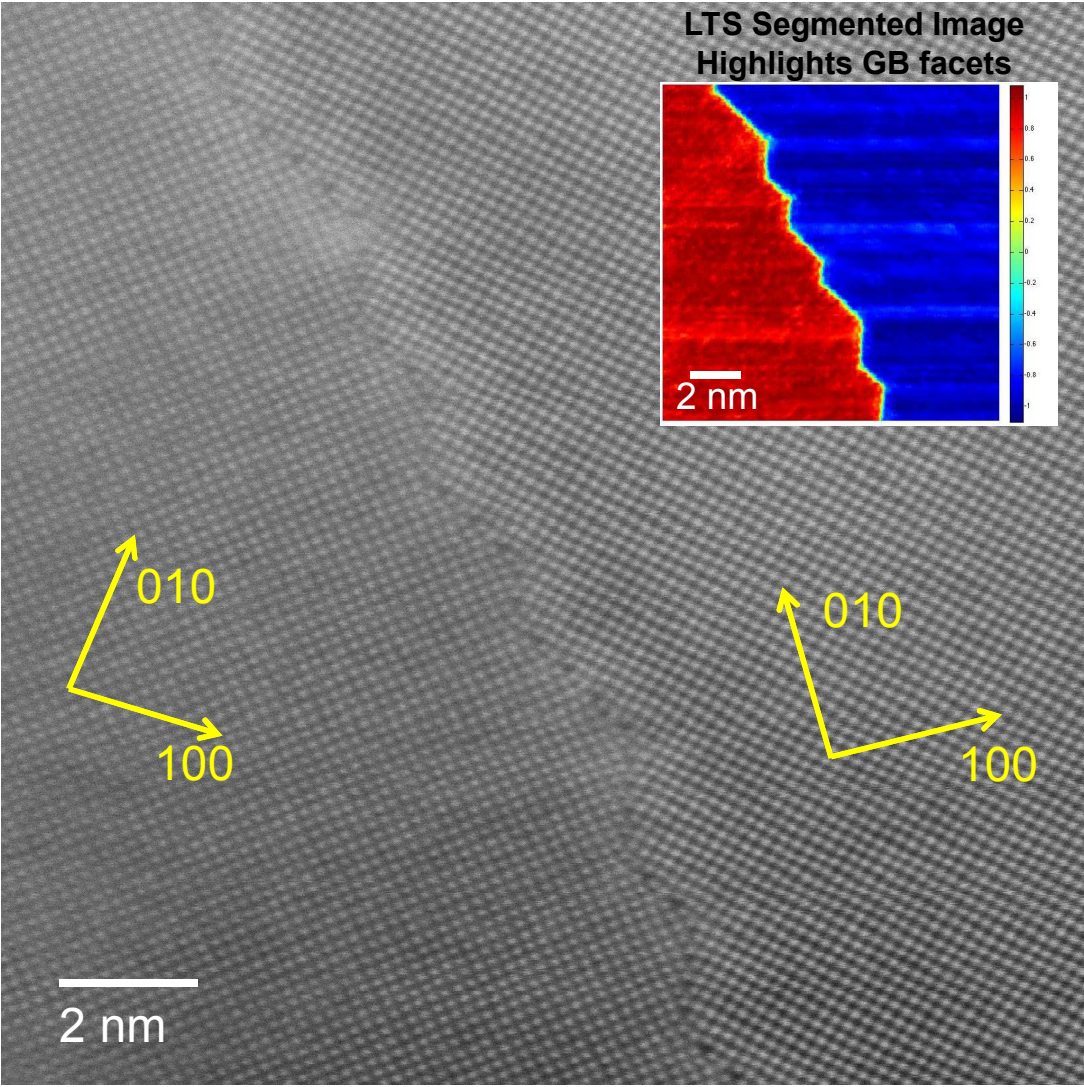
- **Inclination:**

- Reduce energy by faceting on lower energy planes
- Facet junctions.

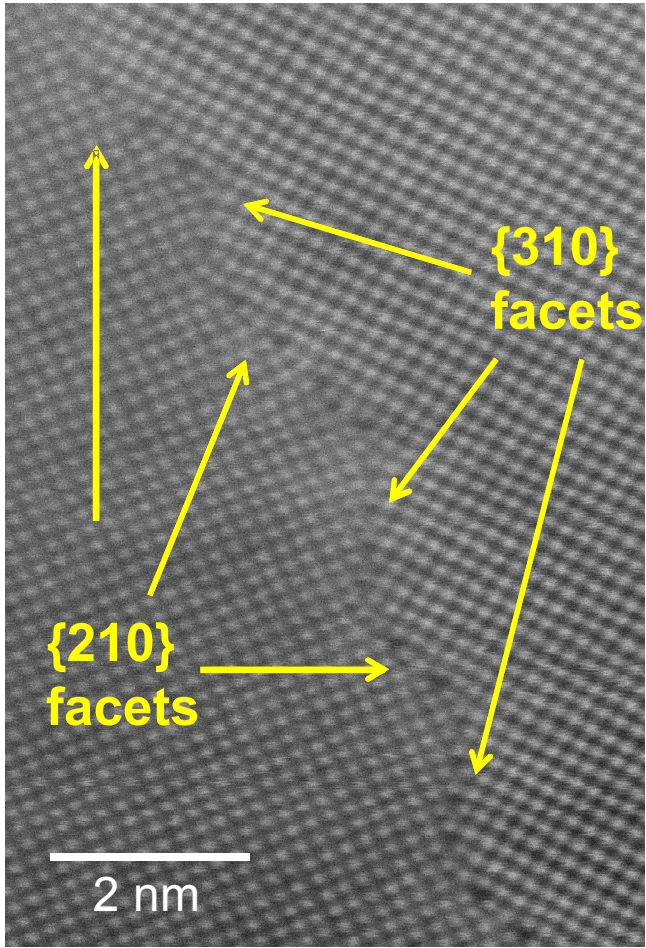
Interaction of grain boundary dislocation and facet junctions?

HRSTEM shows nanoscale faceting at Grain boundary

HAADF-STEM $\Sigma=5$ $\langle 001 \rangle$ Boundary in Fe



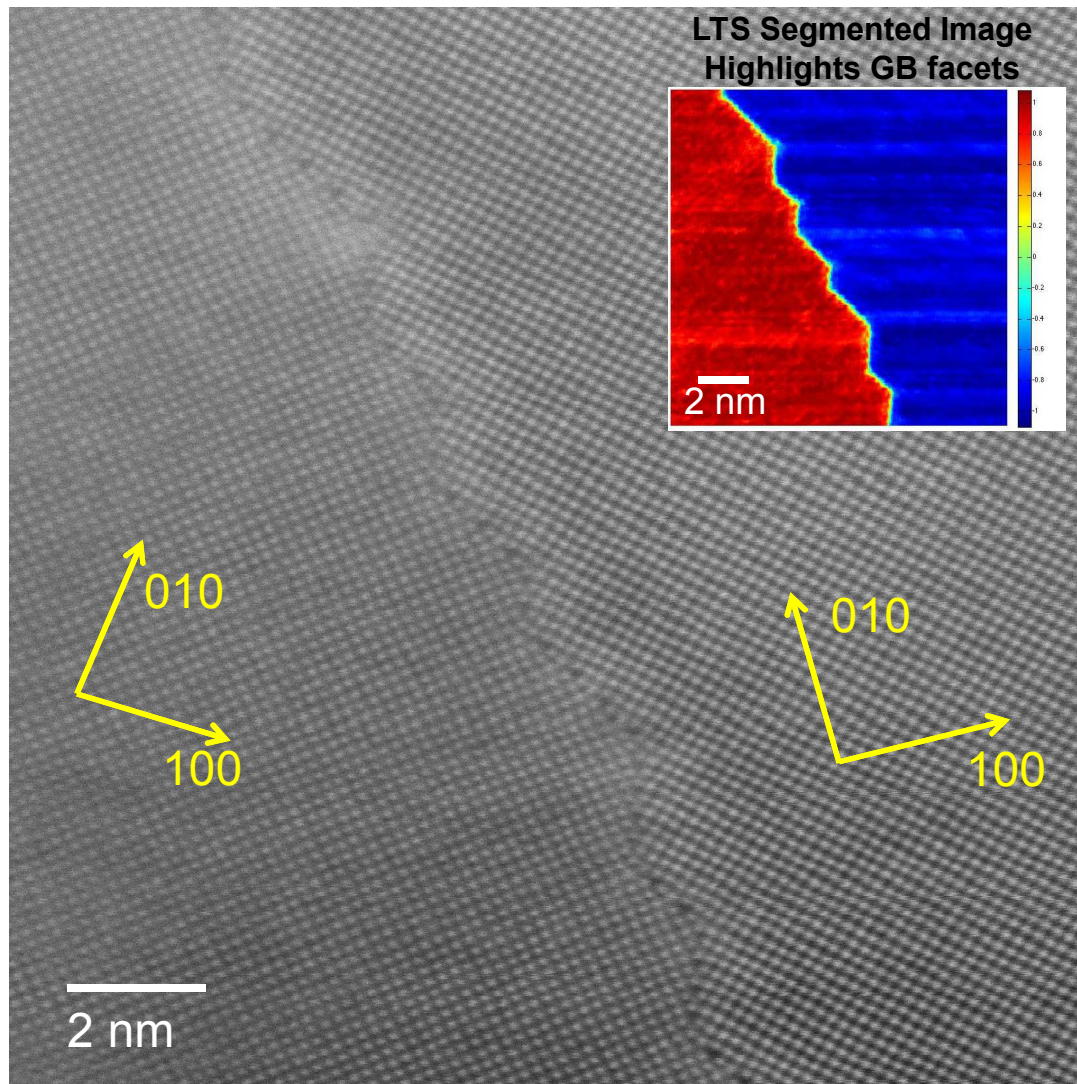
Boundary is faceted on $\{210\}$ and $\{310\}$ type inclinations



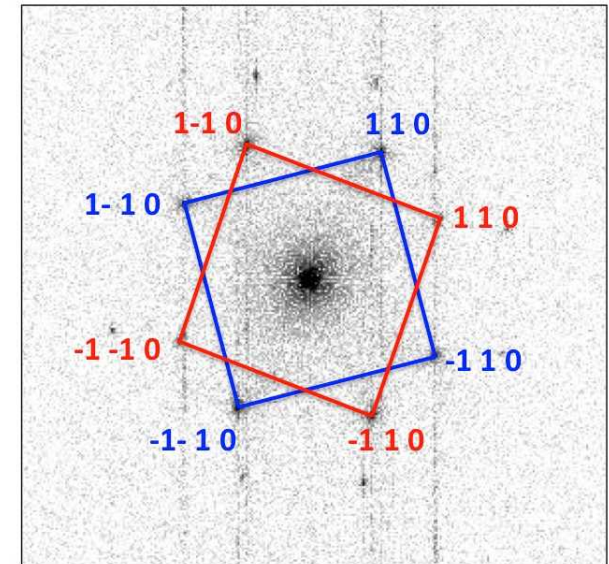
Pulsed Laser Deposited Fe on Rocksalt (NaCl).
36 nm thickness. Specimen released and annealed
on Mo grid 675°C, 2 hours, under vacuum

HRSTEM shows nanoscale faceting at Grain boundary Sandia National Laboratories

HAADF-STEM $\Sigma=5$ $\langle 001 \rangle$ Boundary in Fe



Boundary Geometry



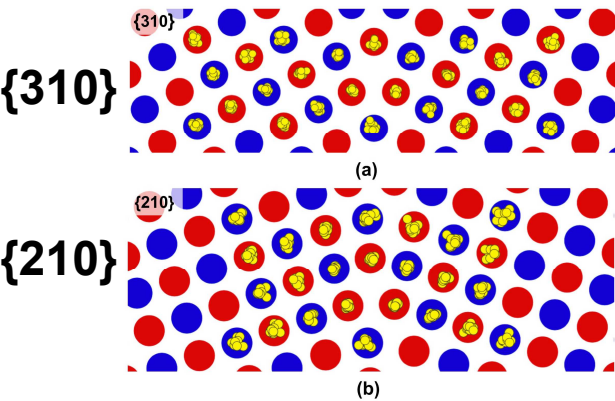
Inclination from $\{310\}$:
 $\phi = 26.3^\circ \pm 1^\circ$

Misorientation:
 $\theta = 34.49 \pm 0.75^\circ$

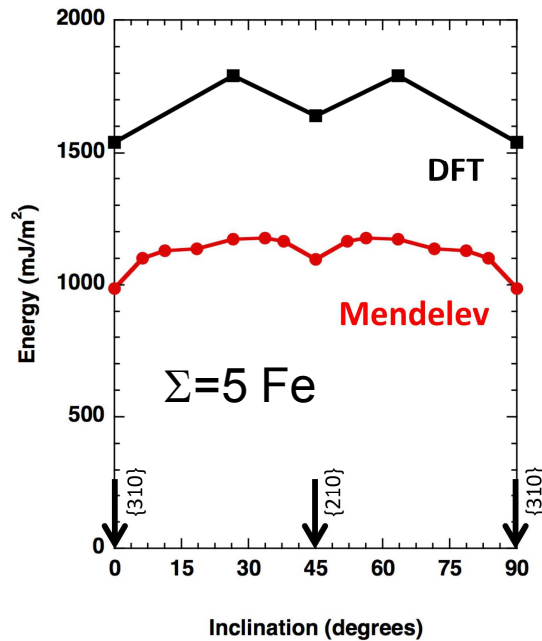
$\Delta\theta = -2.38 \pm 0.75^\circ$
from exact $\Sigma=5$

Energetics predict growth of {210} and {310} facets

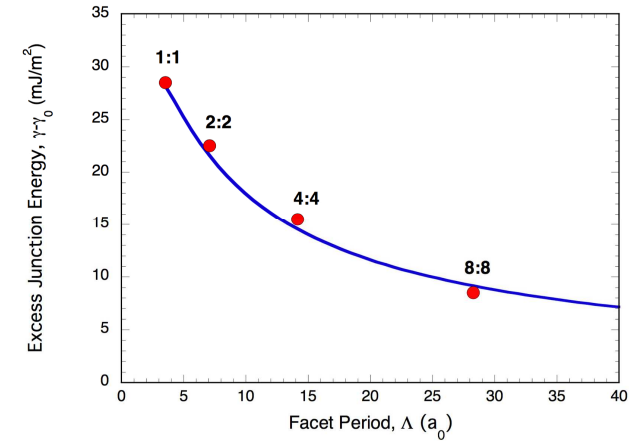
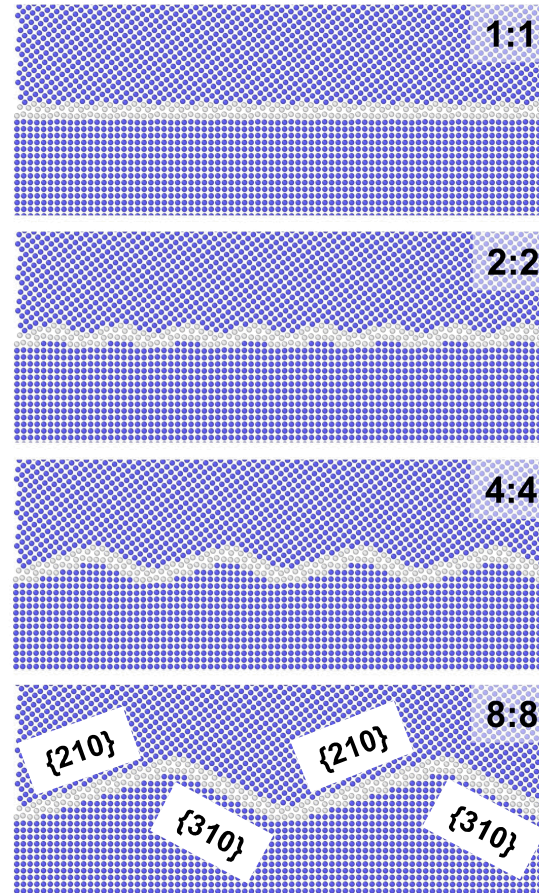
Atomistic Simulation
(HAADF-STEM peak positions overlaid)



Energy vs Boundary Inclination



Reduction of Energy with Facet Coarsening

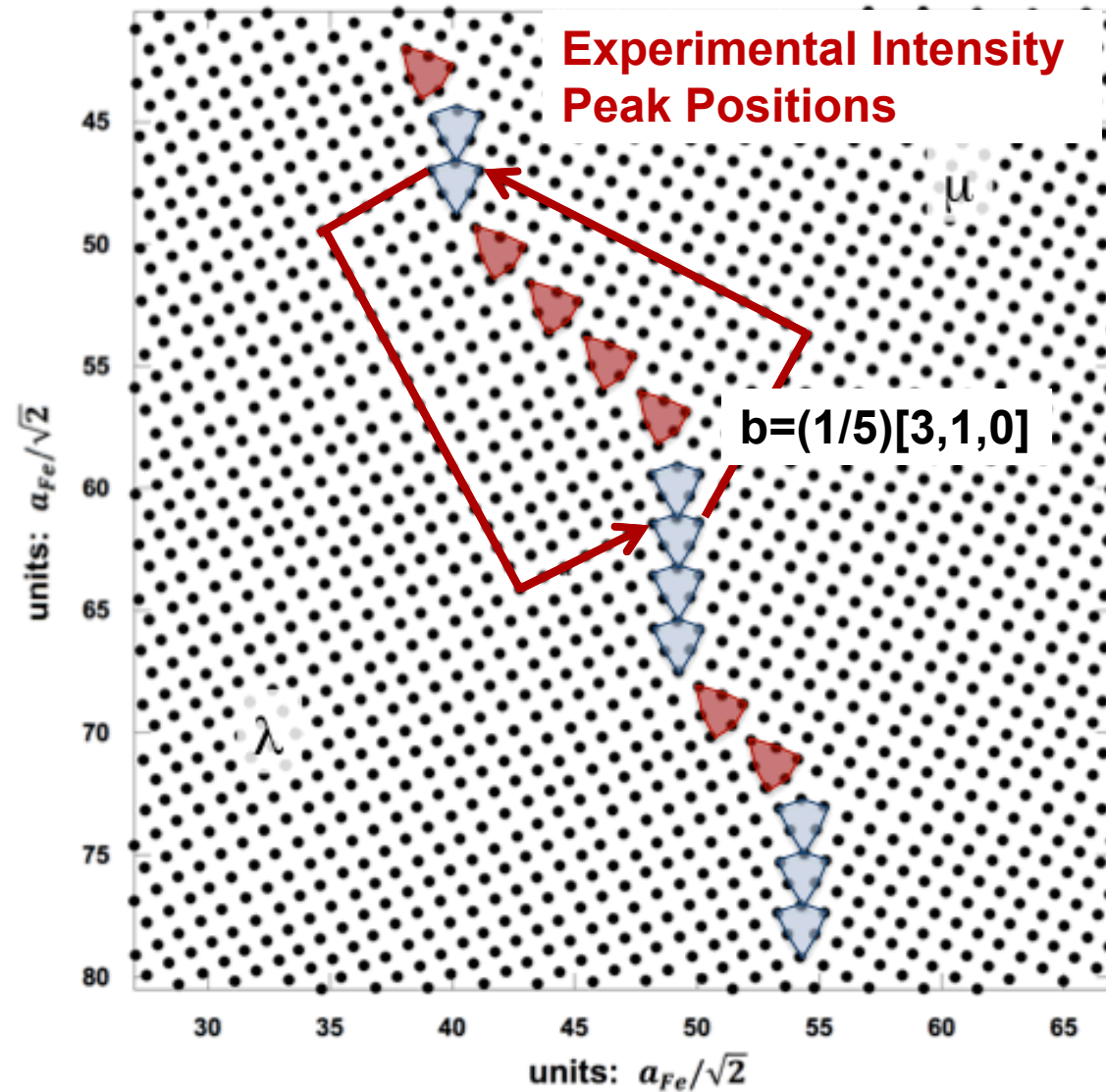


$$(\gamma - \gamma_0) = (C_1/\Lambda)\ln\Lambda + C_2/\Lambda$$

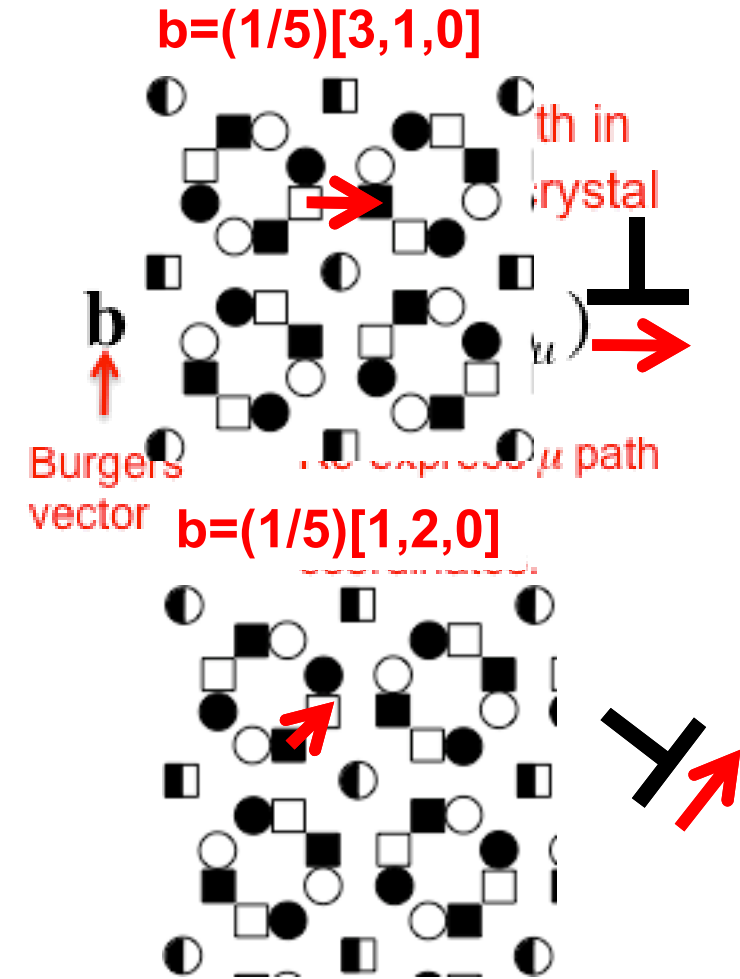
Stable facets only for $C_1 < 0$

fit: $C_1 = +76.55$ mJ/m²
 $C_2 = +2.94$ mJ/m²

Circuit Mapping: Grain Boundary Disconnections at all Facet Junction Pairs



Two types of defect observed:



Defect spacing accounts for misorientation and boundary inclination

Observed SGBD Density Accommodates Deviation from Exact $\Sigma=5$ Misorientation

Dislocation Content Required is function of both Misorientation *and* Inclination

Frank-Bilby Equation:

$$\mathbf{b}\text{-vector density} \rightarrow \mathbf{B} = (\mathbf{I} - \mathbf{P}^{-1}) \mathbf{v} \leftarrow \text{Interface vector, defining inclination}$$

Matrix defining misorientation from reference

Predicted Burgers Vector Density:

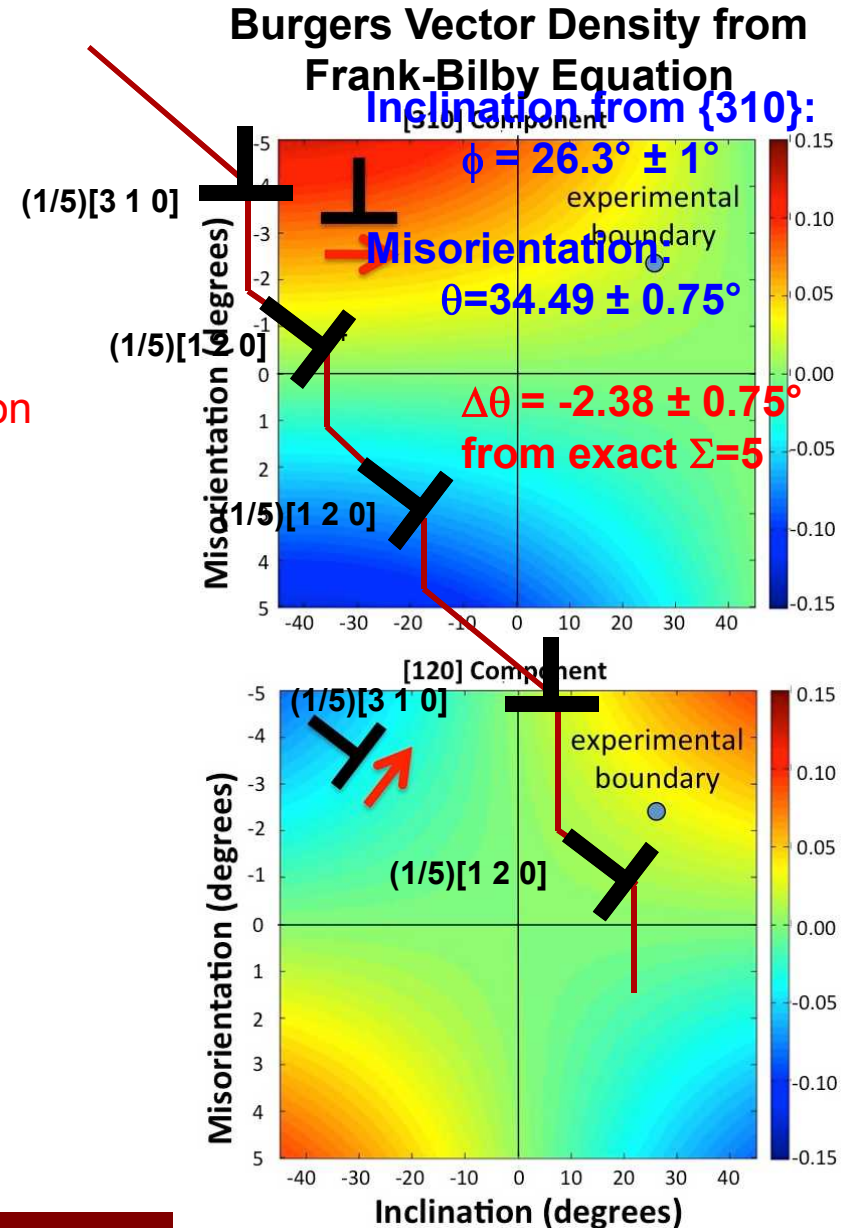
$$\mathbf{B} = [0.029 \pm 0.010, 0.030 \pm 0.010, 0]$$

Observed Burgers Vector Density:

$$\mathbf{B} = [0.030 \pm 0.002, 0.027 \pm 0.002, 0]$$

(b per unit length of boundary)

Coupling of SGBDs and junctions dictates the facet length scale



Conclusions

Rich set of phenomena associated with interfacial line defects

- Strain accomodation.***
- Interfacial motion***
- Phase transformation.***
- Interfacial properties.***

Interfacial defect crystallography provides a framework for evaluating and interpreting complex interfacial structures.

- Determining interfacial mechanisms.***
- Informing and guiding modeling.***

Collaborators

Sandia National Laboratories

J. Hamilton
E.A. Marquis (now Univ. Michigan)
D. Cohen
J.D. Sugar
S.M. Foiles

J. Zimmerman
K. Hattar
F. Abdeljawad
C. O'Brien

University of Exeter

R.C. Pond

California Institute of Technology

J. Snyder (now Northwestern University)
N. Heinz
T. Ikeda (now Ibaraki University)

Acknowledgement

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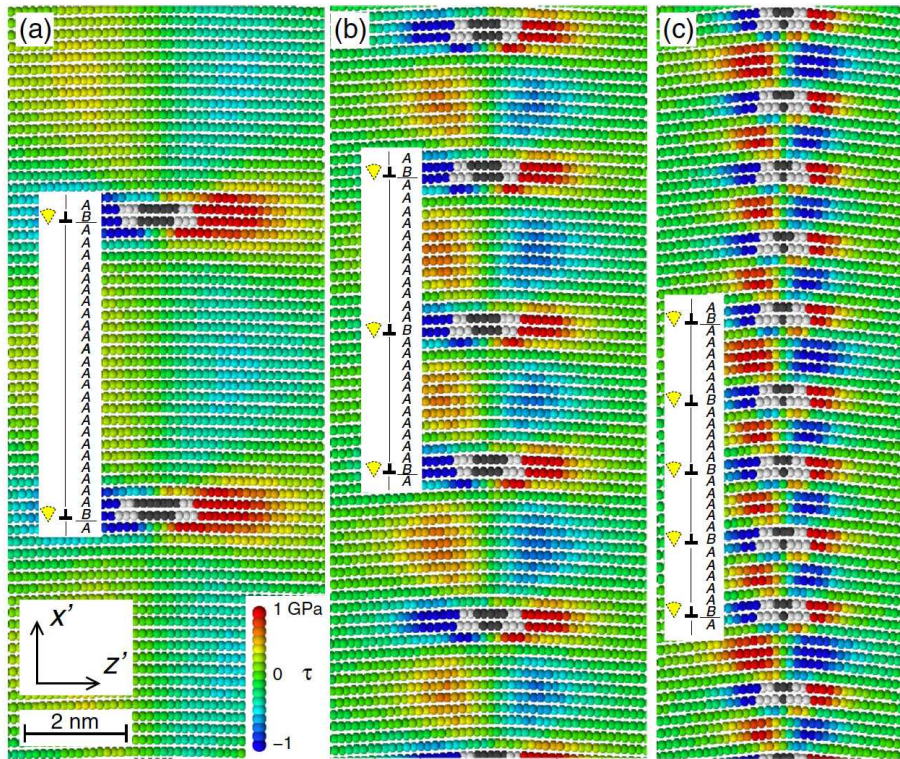
EXTRA

Grain Boundaries: Lattice Dislocation

Description limited by overlap of defect cores

Example: Atomistic simulations LAGB in Al

$\theta = 2.81^\circ$ $\theta = 5.61^\circ$ $\theta = 11.91^\circ$

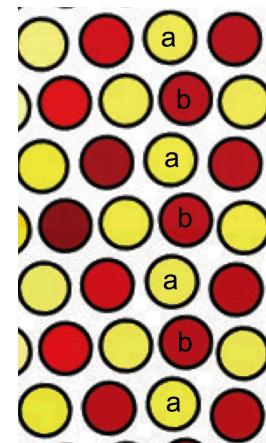
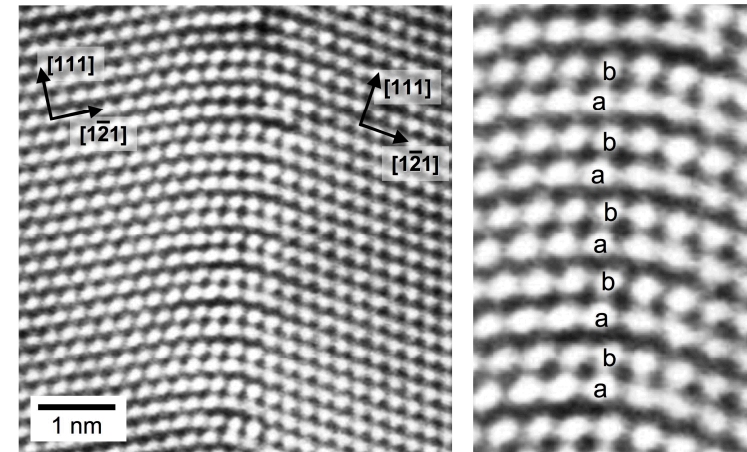


T. Shimokawa, PRB (2010)

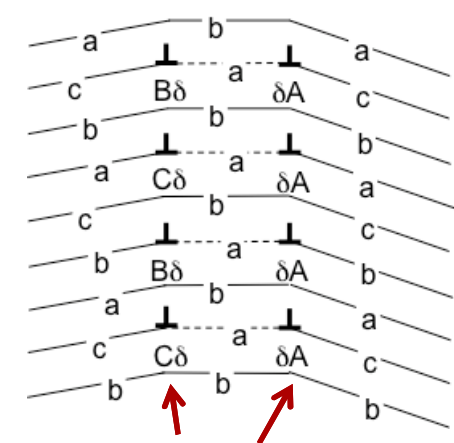
Low Angle Grain Boundary cut-off
typically between 5° and 15°

Example: HCP Stacking at Au GB

$\theta = 29^\circ$: Dislocations separated
by 1 atomic plane



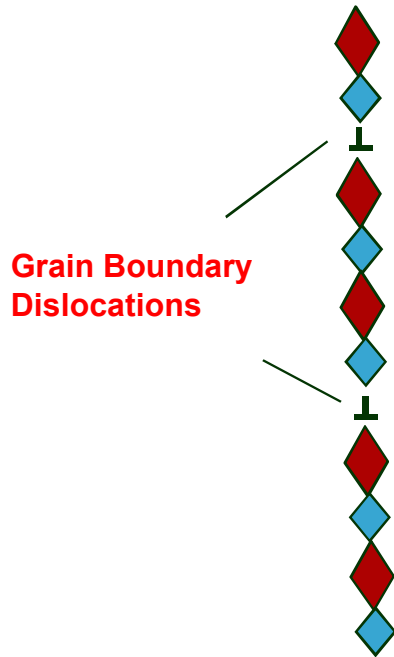
Medlin & Hamilton,
J. Mat Sci 2009.



**Dissociated dislocations give
stacking faults every other plane**

Dislocations in High Angle Boundaries

High Angle GB

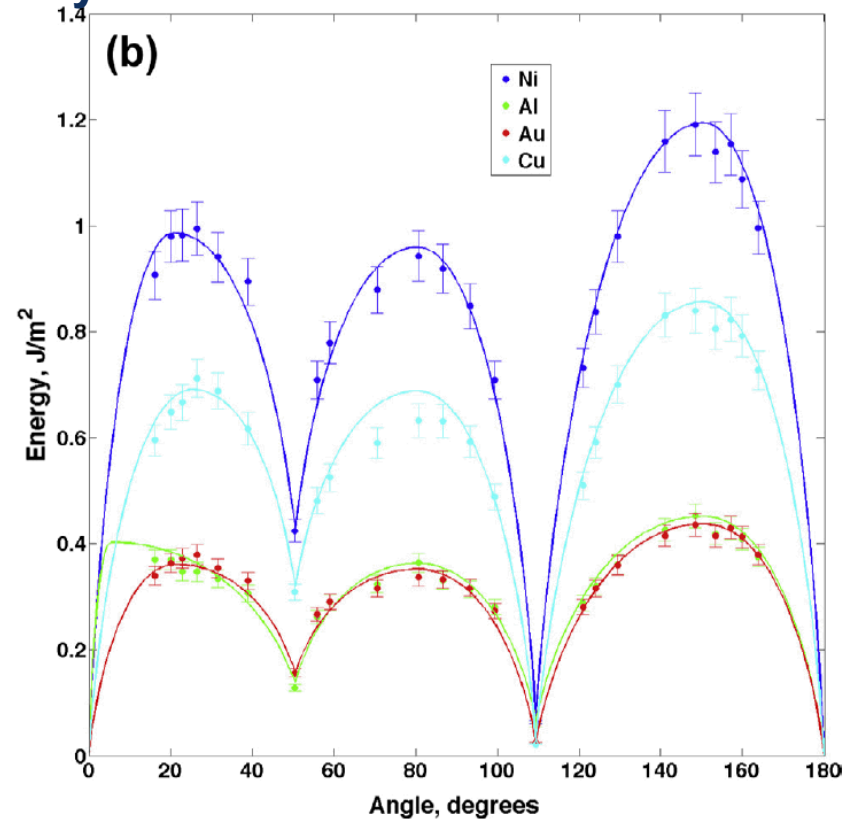


Reference Frame:

Typically choose energy minimum in misorientation/inclination space.

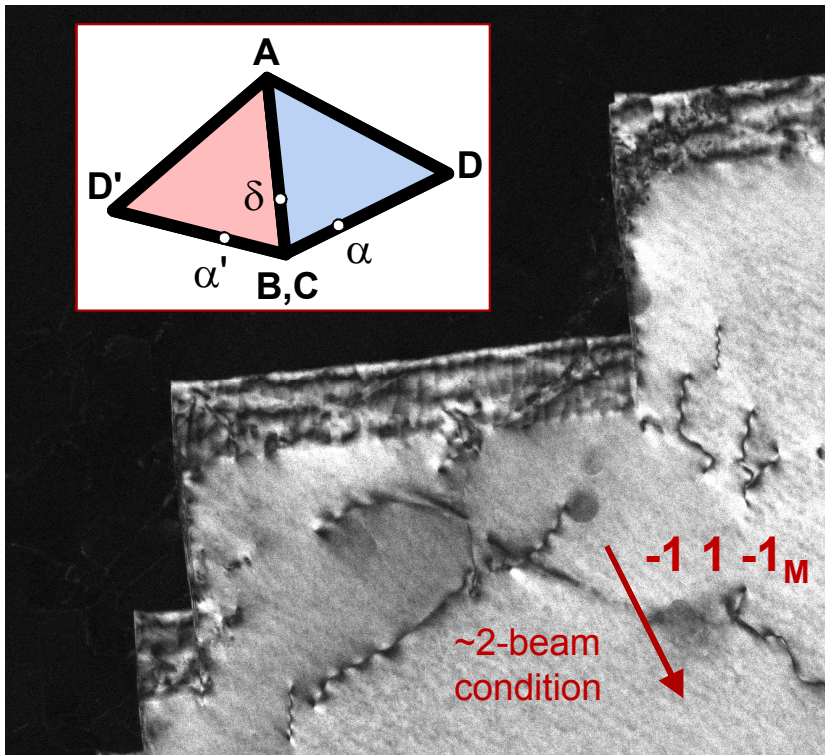
Often a low CSL boundary, but not always!

Energy vs misorientation Symmetric FCC $\langle 110 \rangle$ tilt boundaries

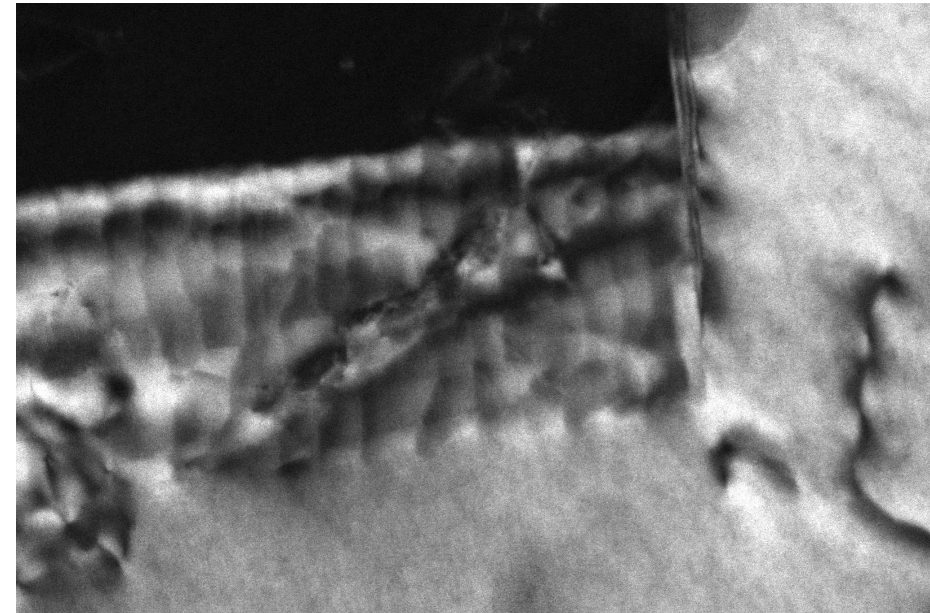


V.V. Bulatov, B.W. Reed, M. Kumar,
Acta Mat 2014

Example: GB dislocation network at $\Sigma=3$ boundary facets in Nickel (Diffraction Contrast STEM)



200 nm



100 nm

Average dislocation spacing: $\sim 15 \pm 2$ nm

Measured misorientation from exact $\Sigma=3$: 0.41°

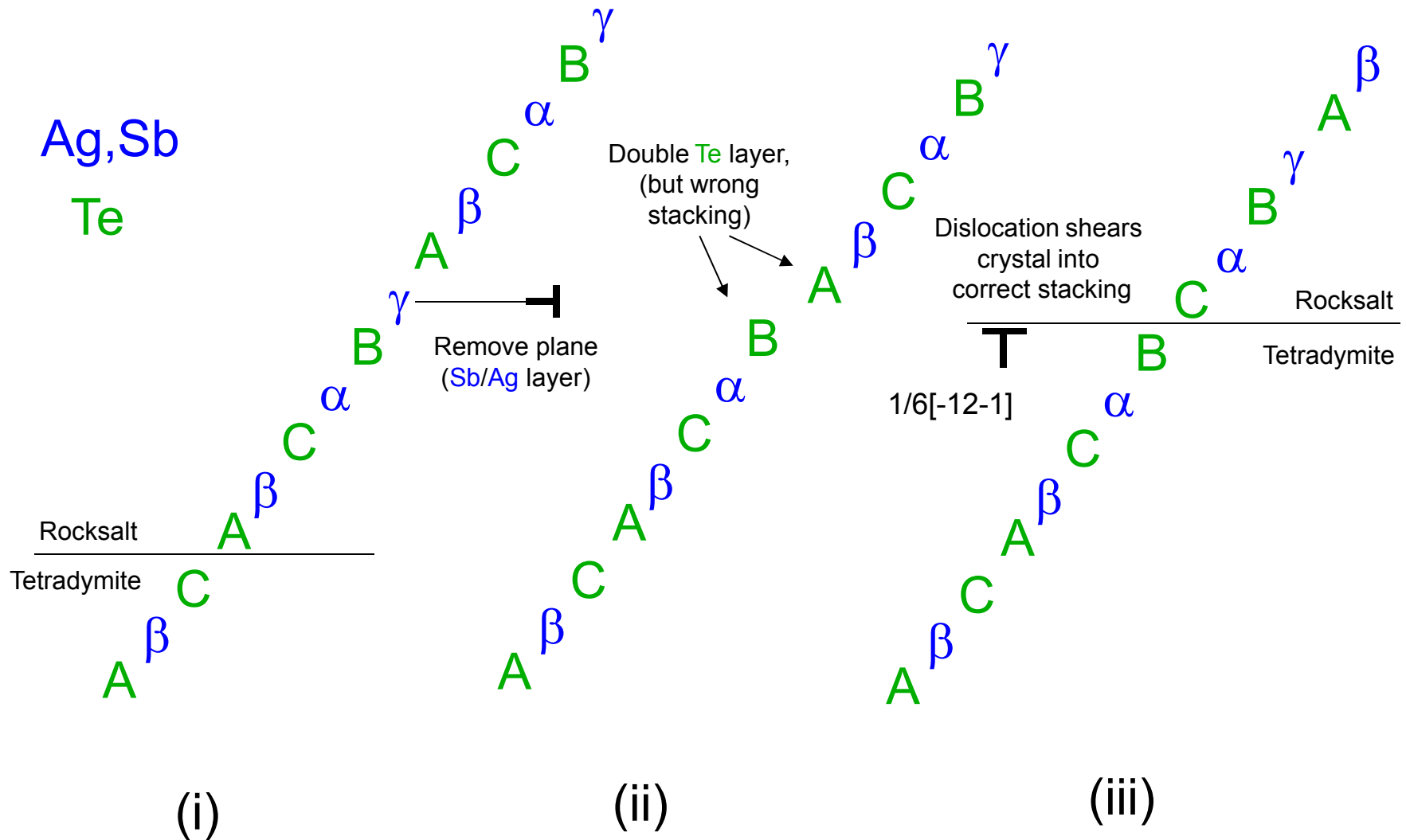
$$d \approx |b| / (2 \sin(\theta/2))$$

$$|b| \ (a/6) < 112 > = 0.14 \text{ nm}$$



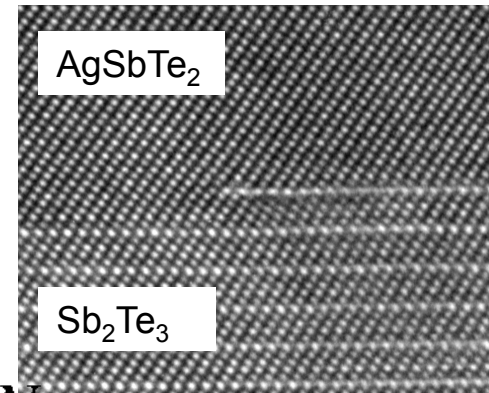
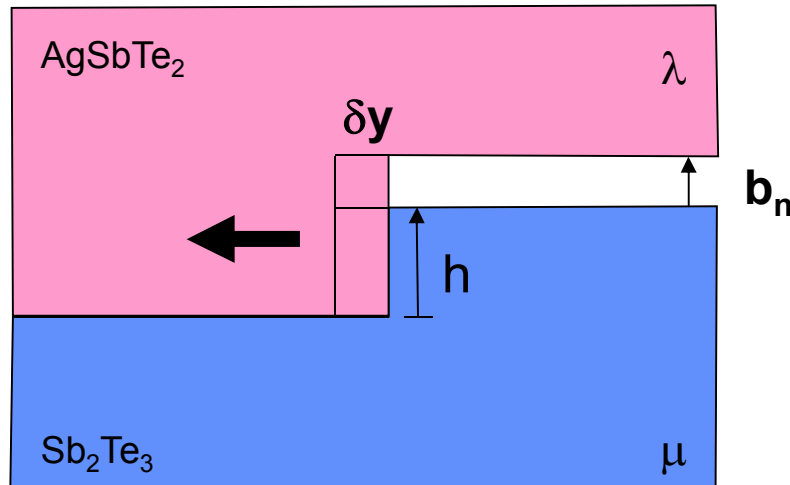
Dislocation spacing to accommodate misorientation: ~ 20 nm

Schematic of Transformation Sequence



Defect properties give local mass flux required for transformation

Partition flux for defect motion into step and dislocation components



$$\frac{\Delta N_i}{L\delta y} = \underbrace{(\chi_i^\lambda - \chi_i^\mu)h}_{\text{step}} + \underbrace{\chi_i^\lambda b_n}_{\text{dislocation}}$$

Hirth & Pond, Acta Mat 1996

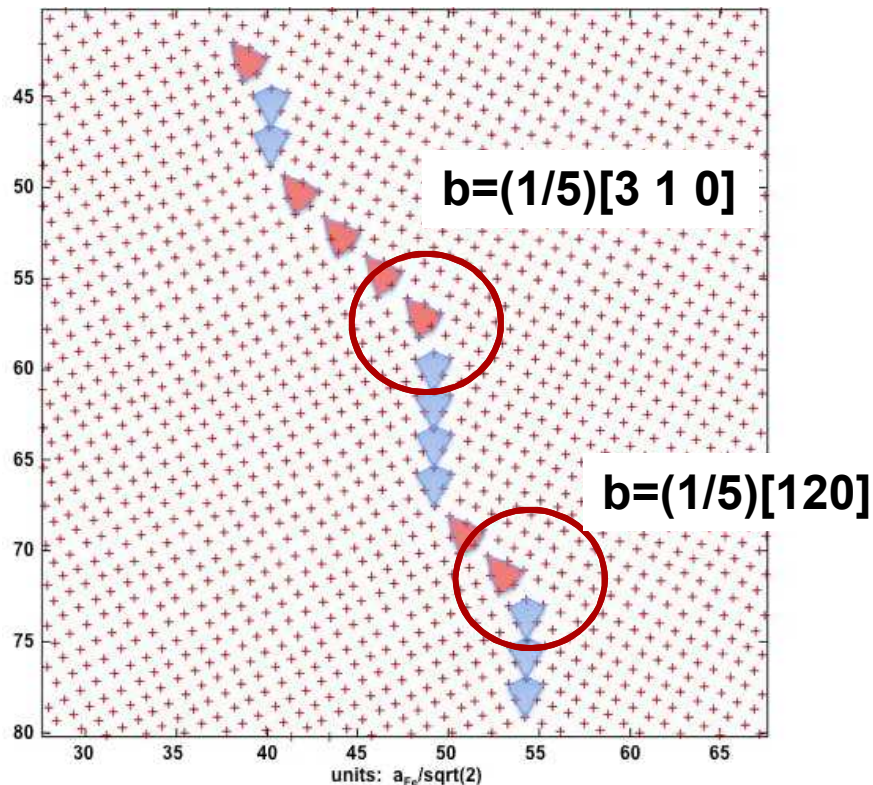
**Reject Ag and Incorporate Sb
in ratio of 3:1**

**Tellurium:
Step and Dislocation fluxes cancel.
No long-range Te transport required.**

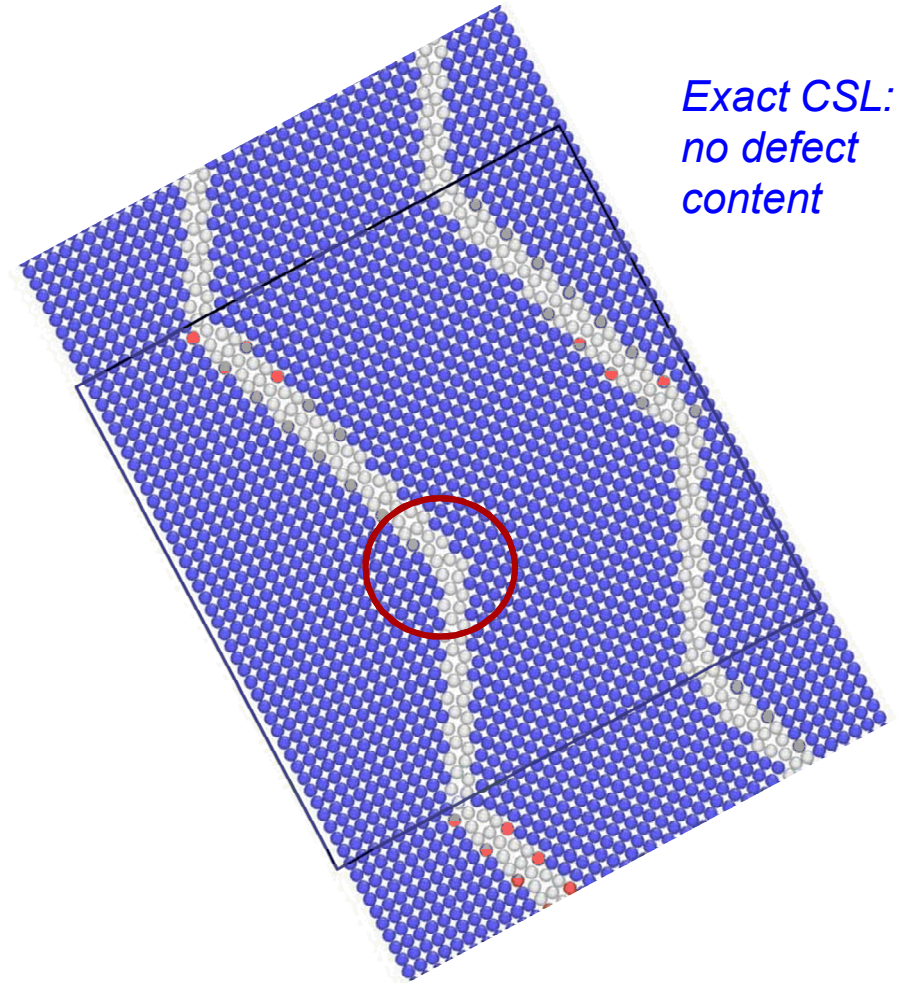
Species	Step flux (atoms/Å ²)	Dislocation flux (atom/Å ²)	Total flux (atom/Å ²)
Ag	$\frac{2 c_{hex}}{3 a_{cub}^3}$ +0.09043	$\frac{2}{a_{cub}^3}(\sqrt{3}a_{cub} - c_{hex}/3)$ +0.00334	$\frac{2\sqrt{3}}{a_{cub}^2}$ +0.09377
Sb	$\frac{2 c_{hex}}{3 a_{cub}^3} - \frac{8\sqrt{3}}{3 a_{cub}^2}$ -0.03459	$\frac{2}{a_{cub}^3}(\sqrt{3}a_{cub} - c_{hex}/3)$ +0.00334	$-\frac{2\sqrt{3}}{3 a_{cub}^2}$ -0.03126
Te	$-\frac{4}{a_{cub}^3}(\sqrt{3}a_{cub} - c_{hex}/3)$ -0.00668	$+\frac{4}{a_{cub}^3}(\sqrt{3}a_{cub} - c_{hex}/3)$ +0.00668	0

How are the grain boundary dislocations manifested in the junction structure?

Experimental Junctions
 $b=(1/5)(120)$ and $(1/5)(310)$



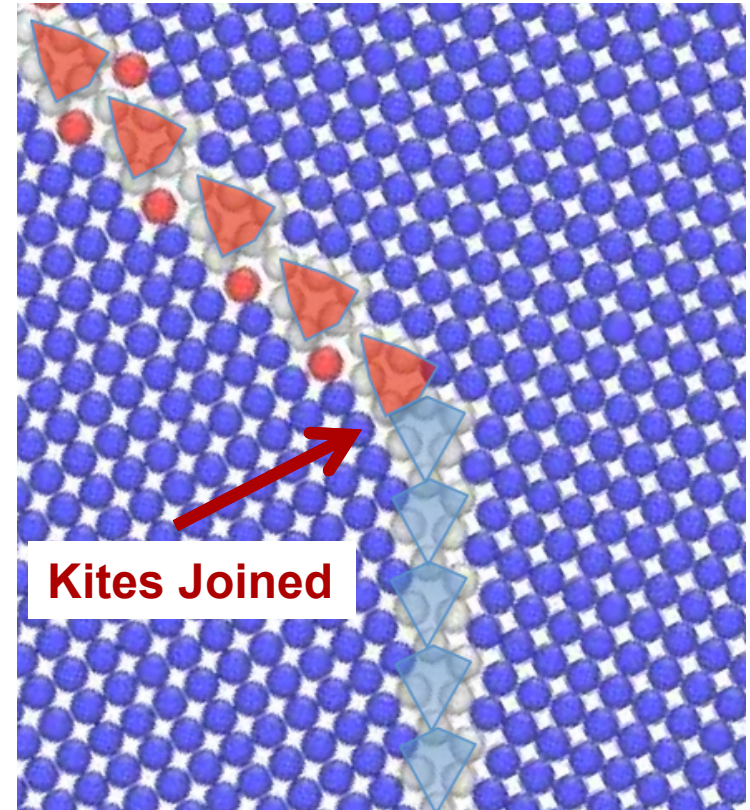
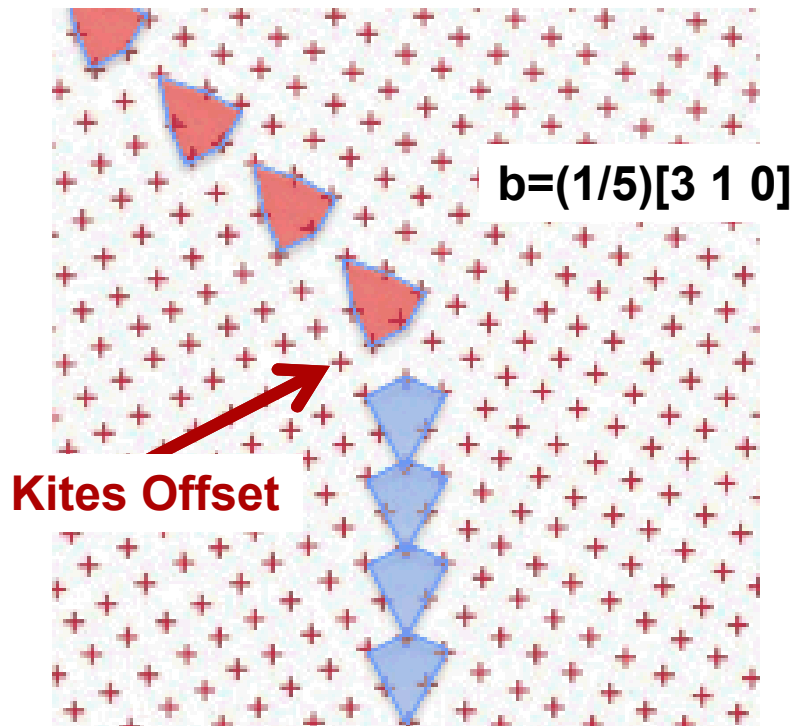
Relaxed Periodic Atomistic Structure



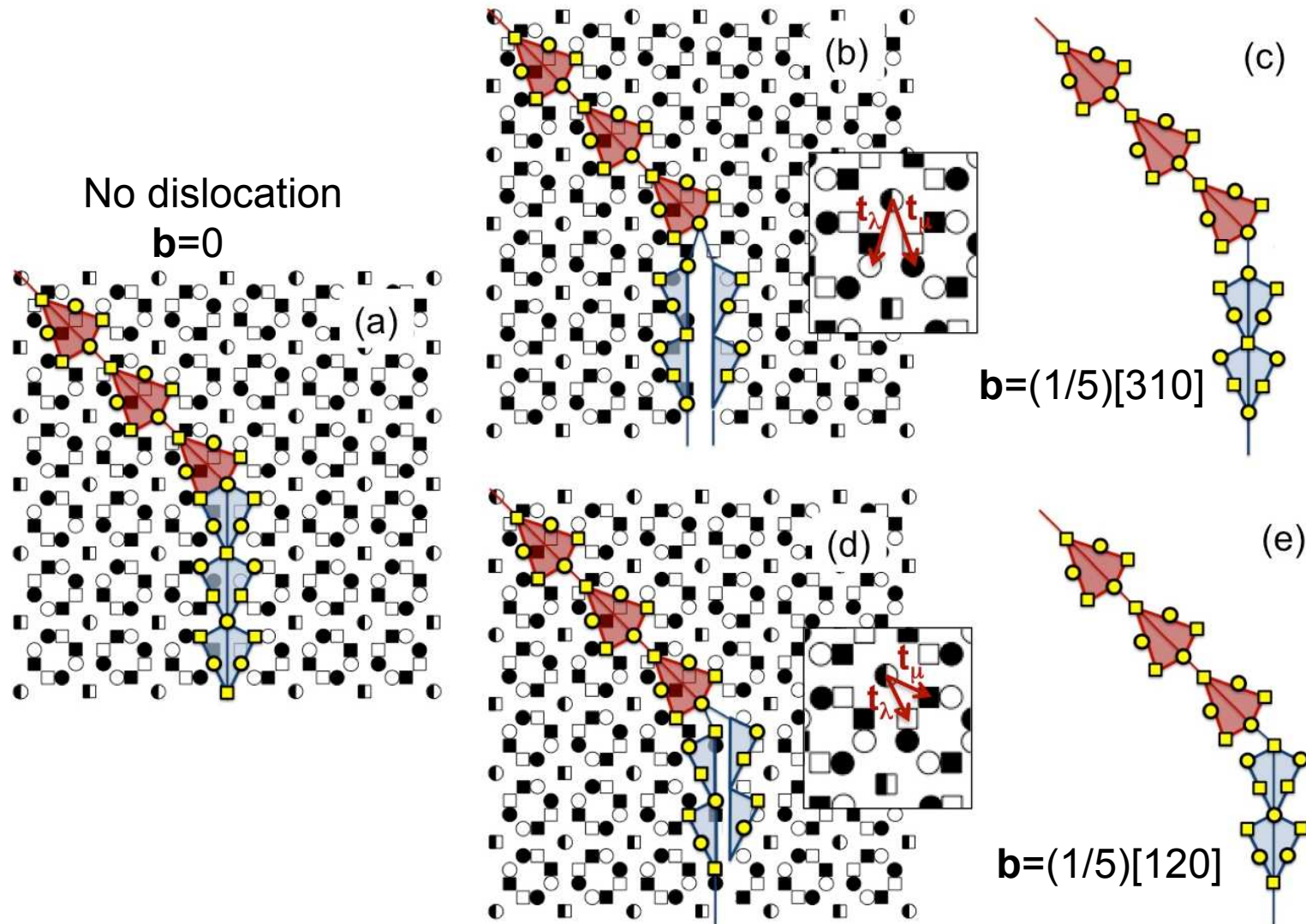
How are the grain boundary dislocations manifested in the junction structure?

Experimental Junctions
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Relaxed Periodic Atomistic Structure

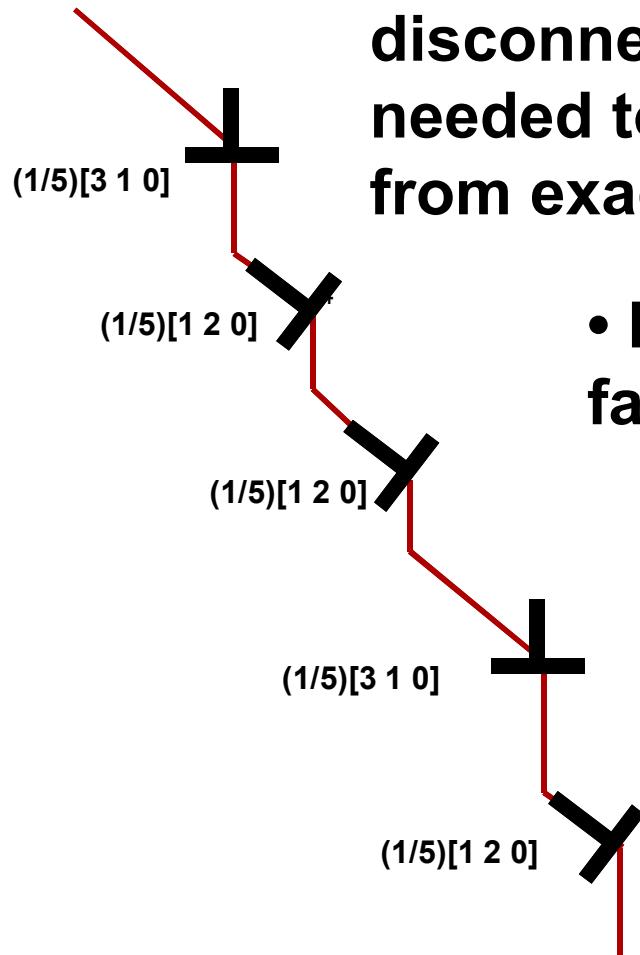


Geometric construction links junction core structure to defect content



Impact on facet length scale

- Distribution of grain boundary disconnections consistent with that needed to accommodate misorientation from exact $\Sigma=5$ misorientation.



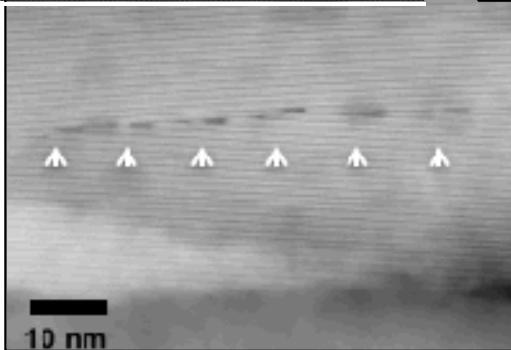
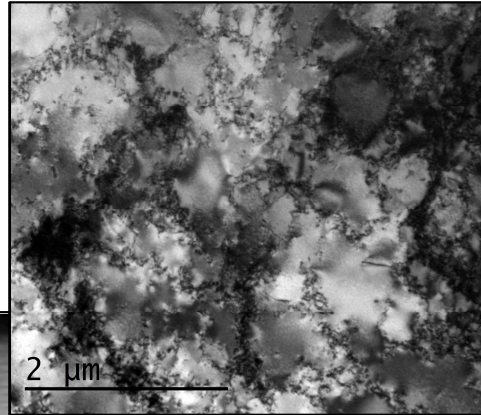
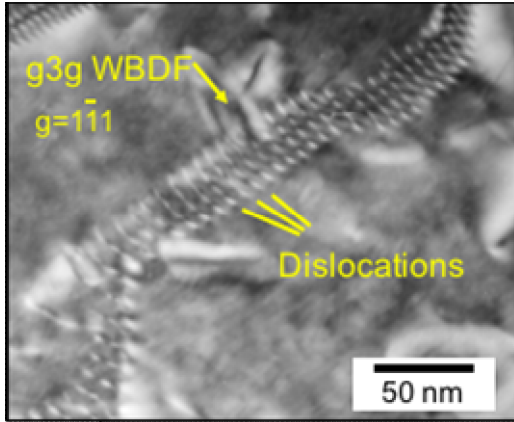
- Disconnection cores located at facet junctions.

- Suggests that facet length scale here is tied to misorientation/inclination via dislocation content.

Low angle boundaries: Arrays of dislocations

Low angle GB in Al thin film

Dislocation Cells in Ni



Low Angle grain boundary in Bi_2Te_3 Nanowire

Crystal Lattice Dislocations



Reference Frame:
Single Crystal

Symmetric tilt boundaries:

$$\theta = 2\sin^{-1}(b/2D)$$

Misorientation

Burgers vector

Spacing

Dislocation density depends on misorientation and inclination (Frank-Bilby Equation)

$$\mathbf{B} = (\mathbf{I} - \mathbf{P}^{-1})\mathbf{v}$$

\mathbf{b} -vector density \rightarrow \mathbf{B} \leftarrow Interface vector, defining inclination

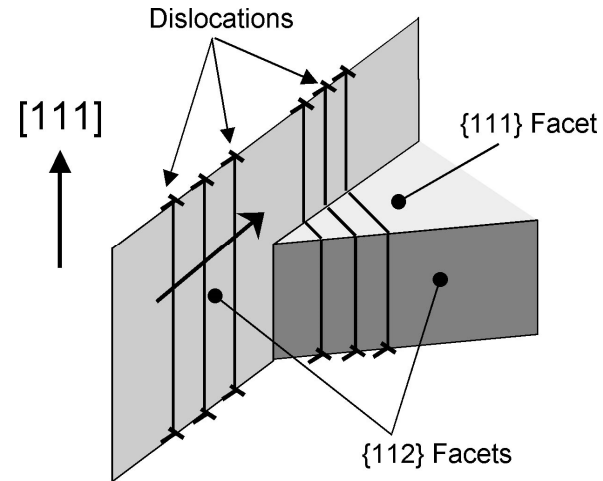
Matrix defining misorientation

Coupling of GBD's with facet junctions



$T=550^{\circ}\Delta t=400$ sec
Movie is repeated

20 nm



- $-(1/6)\langle 112 \rangle$ dislocations climb on $\Sigma=3$ {112} facets**
 - Segments on horizontal {111} facets move by glide.
- Climb is driven by repulsive elastic interactions between the dislocations**
 - Finite tilt wall, un-relaxed long-range stresses

Understanding dislocation/junction interactions important to relating grain evolution to local plastic strain.



50 nm

$T=490^{\circ}\text{C}$

185
minutes

31