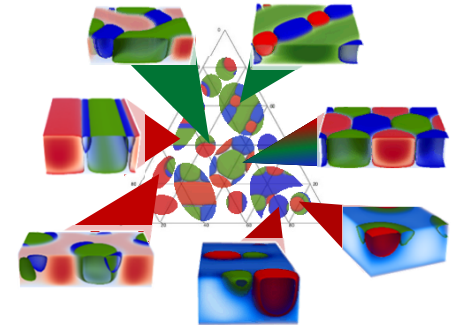
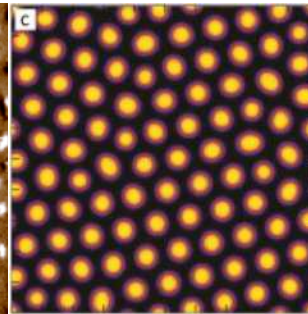
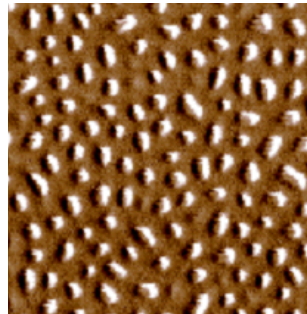


Pattern Formation and Particle Assembly
with Mixed Polymer Brushes

Amalie L. Frischknecht

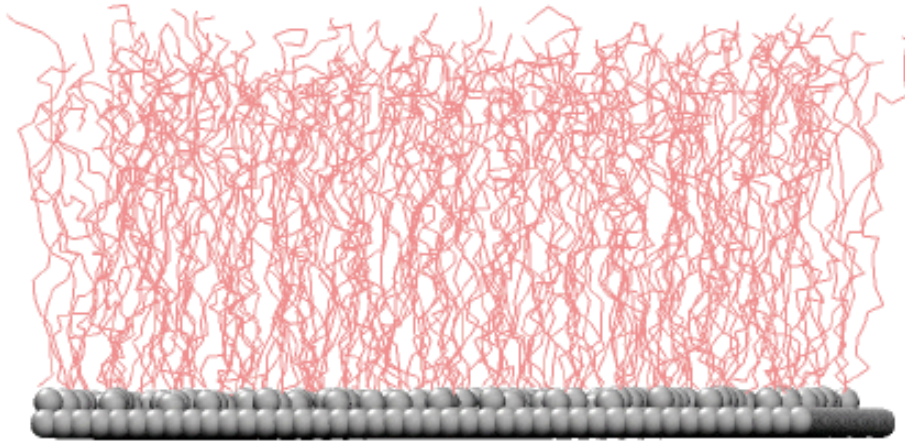


Pattern Formation and Particle Assembly with Mixed Polymer Brushes

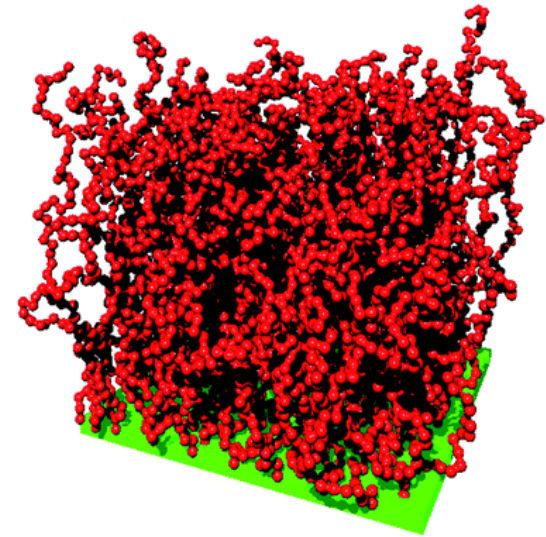
Amalie L. Frischknecht

What is a polymer brush?

polymer chains covalently bonded to a surface



Polymer brush

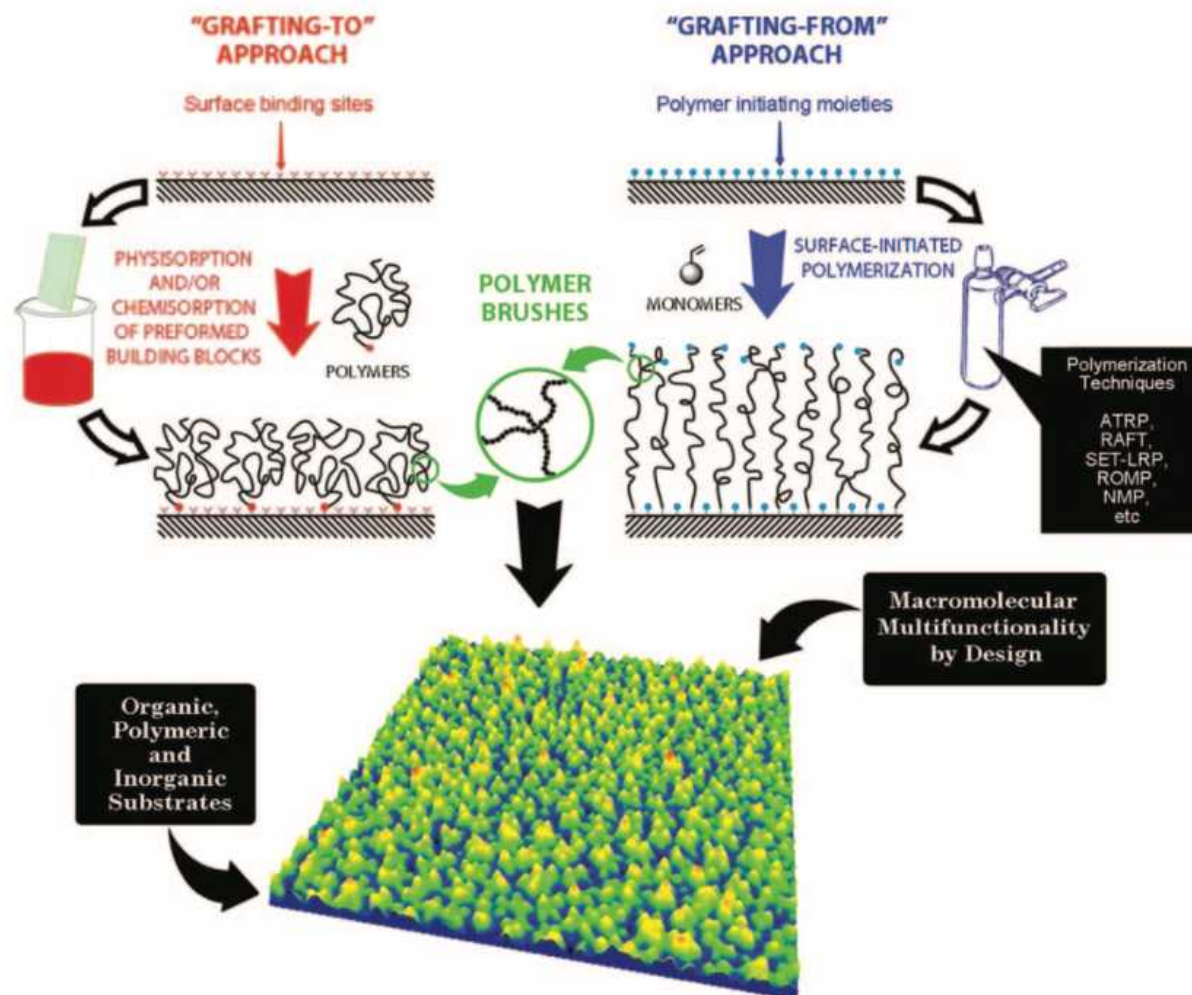


<http://erbas.web.unc.edu>

A. Milchev and K. Binder, *Soft Matter* **10**, 3783 (2014).

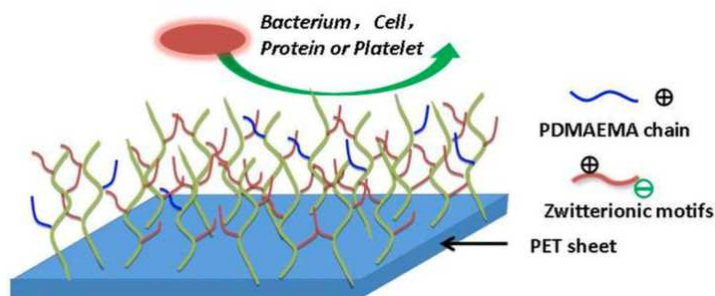


How to make polymer brushes



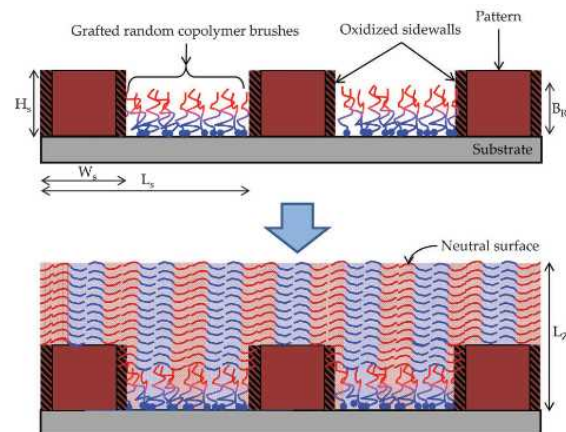
Applications of polymer brushes

antifouling surfaces



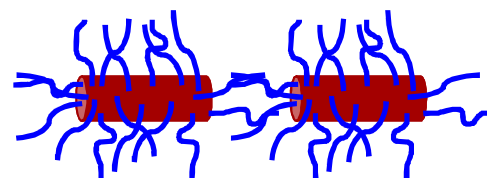
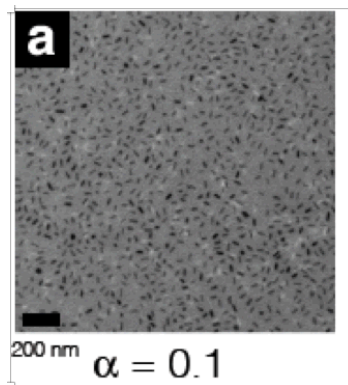
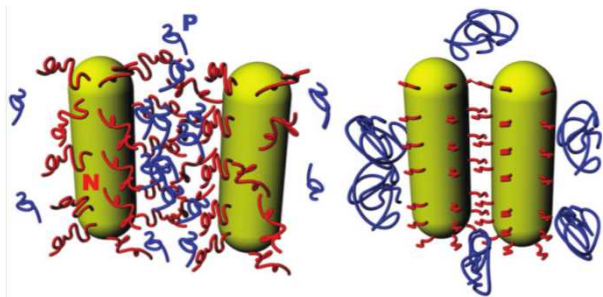
X. Jin, J. Yuan, and J. Shen, *Colloids and Surfaces B: Biointerfaces* **145**, 275 (2016).

block copolymer assembly



G. Pandav, W.J. Durand, C.J. Ellison, C.G. Willson, and V. Ganesan, *Soft Matter* **11**, 9107 (2015).

controlling particle stability



C.L. Ting, R.J. Composto, and A.L. Frischknecht, *Macromolecules* **49**, 1111 (2016).

Structure of polymer brushes

free polymers are random walks

$$R_e \sim N^{1/2}$$

brush: put σ chains/unit area

if close enough in a brush,
polymers must stretch:

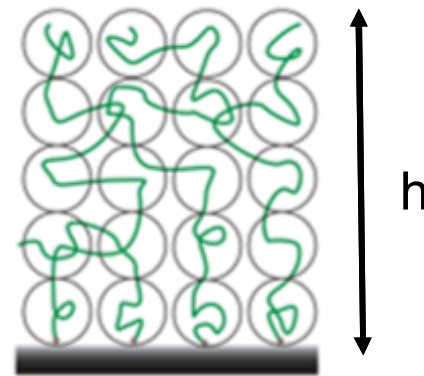
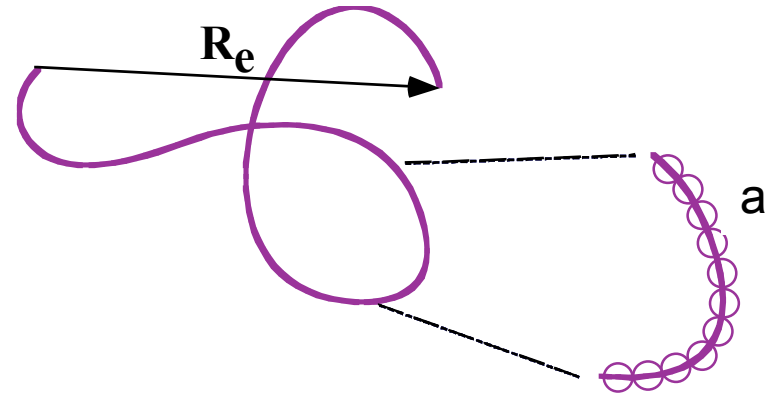
$$F = k_B T \left[\underbrace{\frac{3h^2}{2Na^2}}_{\text{stretching entropy}} + \underbrace{\frac{wN^2\sigma}{h}}_{\text{interactions}} \right]$$

stretching entropy

interactions

minimize free energy:

$$h \sim N(\sigma w)^{1/3}$$



Structure of polymer brushes

free polymers are random walks

$$R_e \sim N^{1/2}$$

brush: put σ chains/unit area

if close enough in a brush,
polymers must stretch:

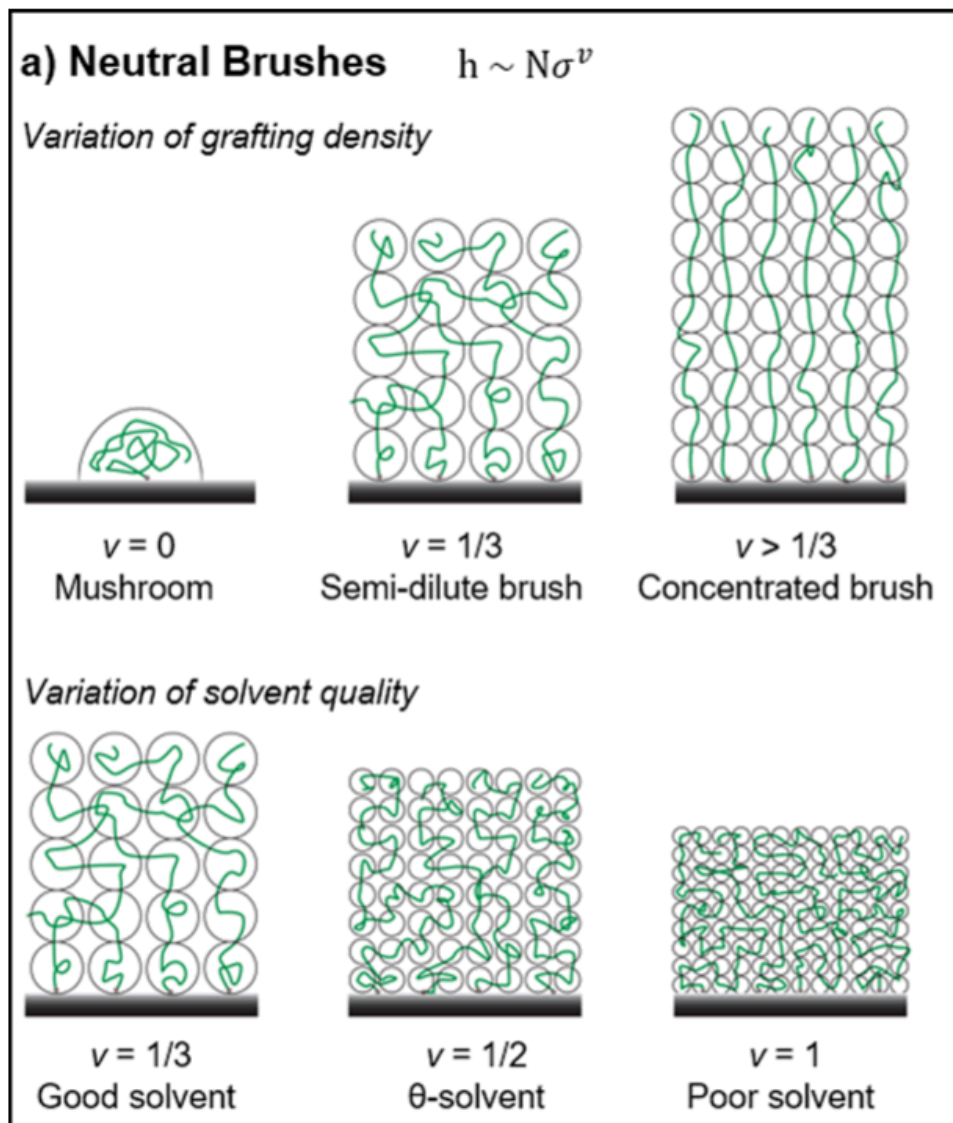
$$F = k_B T \left[\underbrace{\frac{3h^2}{2Na^2}}_{\text{stretching entropy}} + \underbrace{\frac{wN^2\sigma}{h}}_{\text{interactions}} \right]$$

stretching entropy

interactions

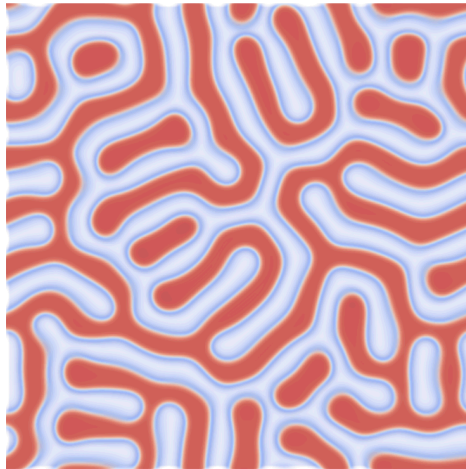
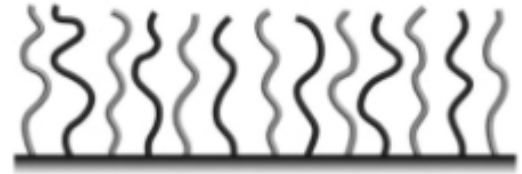
minimize free energy:

$$h \sim N(\sigma w)^{1/3}$$

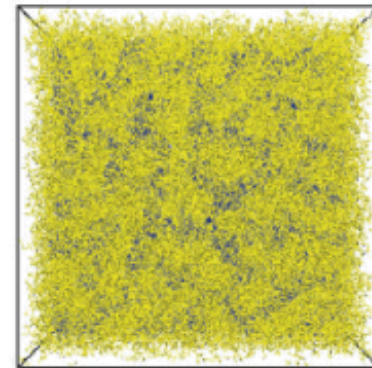
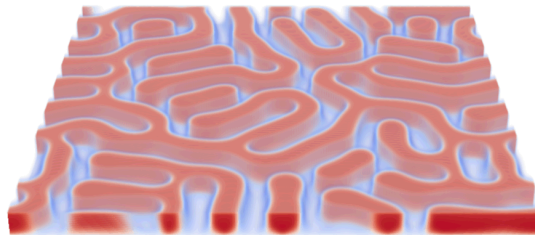


Mixed Polymer Brushes

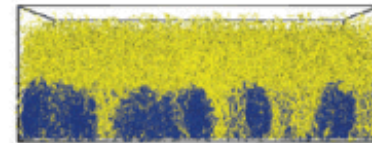
- multiple polymer species grafted to surface
- melt: highly stretched
- microphase separation
 - lateral
 - vertical



lateral phase separation

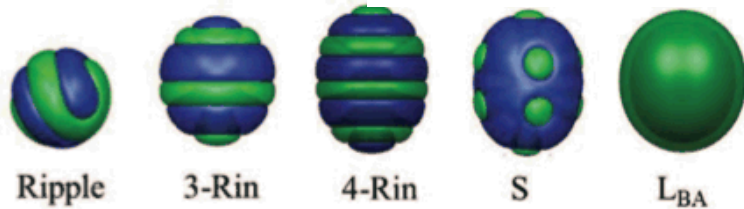
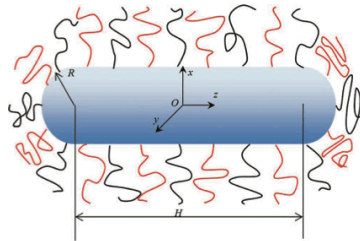


vertical
phase
separation



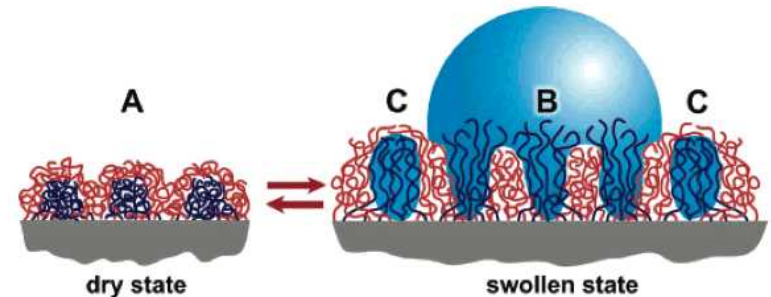
Applications for mixed brushes

patchy
nanoparticles



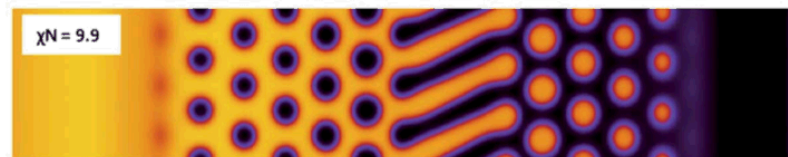
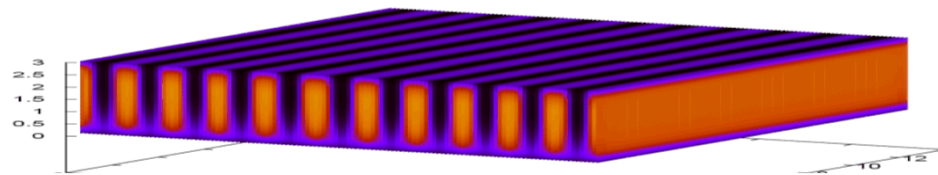
X. Ma, et al J Chem Phys **139**, 214902 (2013).

switchable surfaces



Motornov, M., Sheparovych, R., Tokarev, I.,
Roiter, Y. & Minko, S. *Langmuir* **23**, 13–19 (2007).

surface patterning

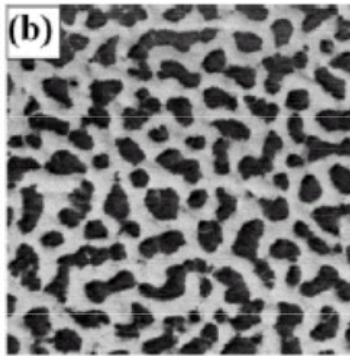


S-M. Hur, et al, *Soft Matter* **7**, 8776 (2011);
Soft Matter **9**, 5341 (2013).

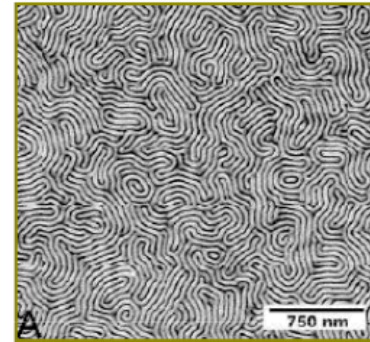
Binary brushes for nanolithography?

binary brushes phase separate similarly to diblock copolymer thin films

- “Ripple” phase of symmetric mixed brush (PS – PMMA) under non-selective solvent
- Perpendicular lamella of PS-b-PMMA block copolymer thin film



Usov et al., *Macromolecules*, **2007**, 40, 8774-8783

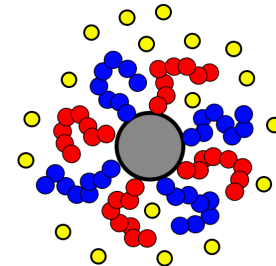
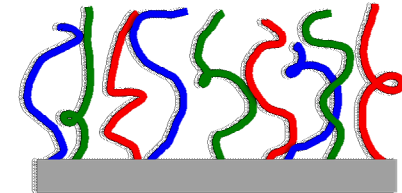
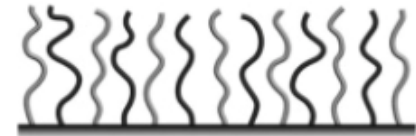
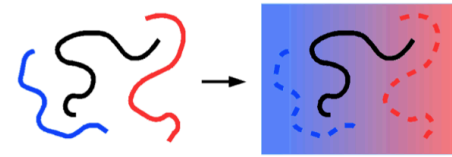


Daniel J.C. Herr, *Future Fab. Intl. Sec.5*, **2005**, Issue 18

use brushes for patterning?
can we get long-range order?

Rest of the Talk

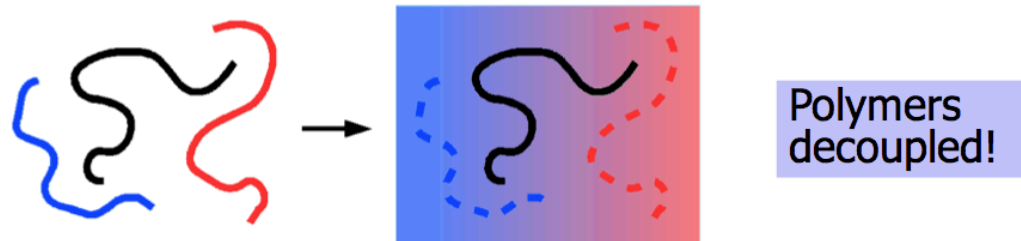
- polymer field theory
- binary brushes
- ternary brushes
- binary brushes on nanoparticles



theme: effects of fluctuations

Self-Consistent Field Theory

- standard technique in polymer science
- replace interactions with many other polymers with interactions between 1 polymer and a field



interaction free energy between different polymers A and B:

$$U_{AB}/kT = \chi_{AB} \int d\mathbf{r} \rho_A(\mathbf{r}) \rho_B(\mathbf{r})$$



Flory χ parameter

Types of polymer field theory

1. a mean-field theory (SCFT) by making a *saddle point* approximation:

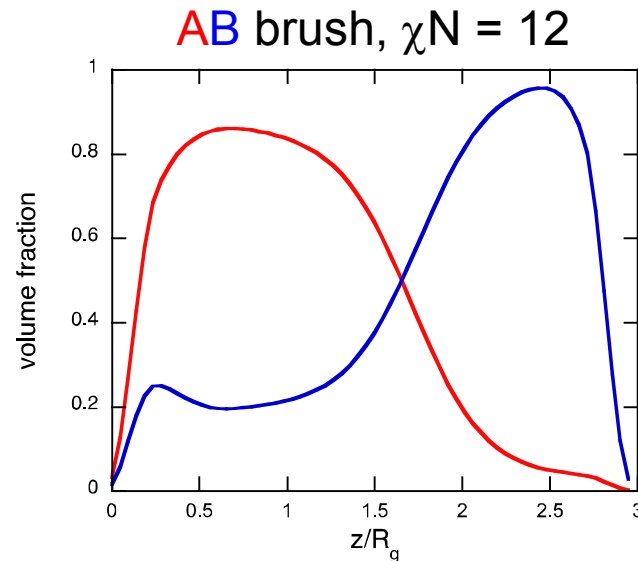
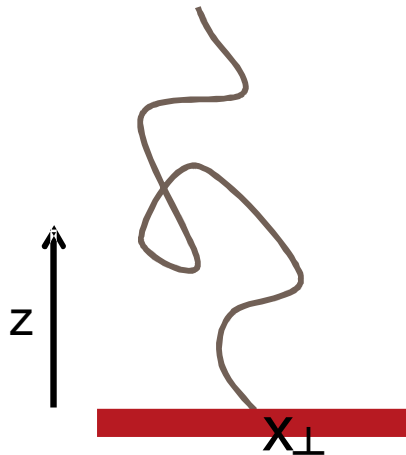
$$e^{-F} = Z = \int \mathcal{D}w e^{-H[w]} \approx e^{-H[w^*]} \quad \left. \frac{\delta H[w]}{\delta w(r)} \right|_{w^*} = 0$$

- evaluate the partition function at the mean-field w^* : $F \approx H[w^*]$
 - accurate for high molecular weight melts
2. sample the entire partition function Z
“field-theoretic simulations”
 3. “dynamic mean field theory” (DMFT)—later in the talk

SCFT for Melt Polymer Brushes

- melt with high grafting density
- graft polymers of length N to surface
- large polymer/air surface tension so flat top surface
 - “walls” in z -direction (substrate + top surface)
 - assume brush height $h = 3R_g$
- periodic boundaries in (x,y)
- polymers interaction strength: χN

calculate minimum free energy from field theory

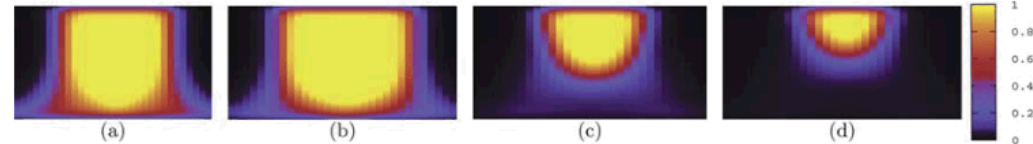


Calculation details

unit cell calculations

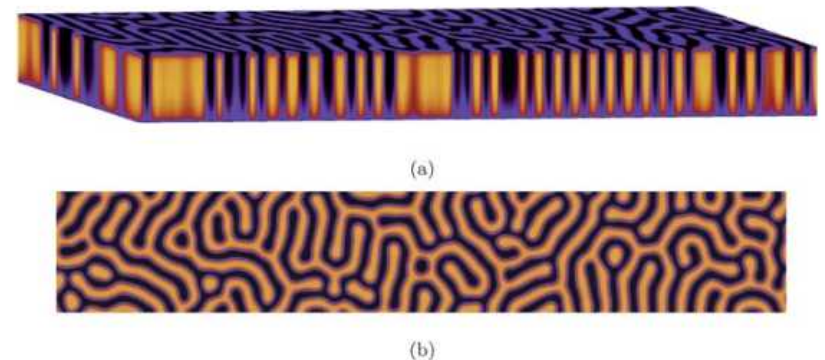
perform in small region

find box size in x, y dimensions with lowest free energy

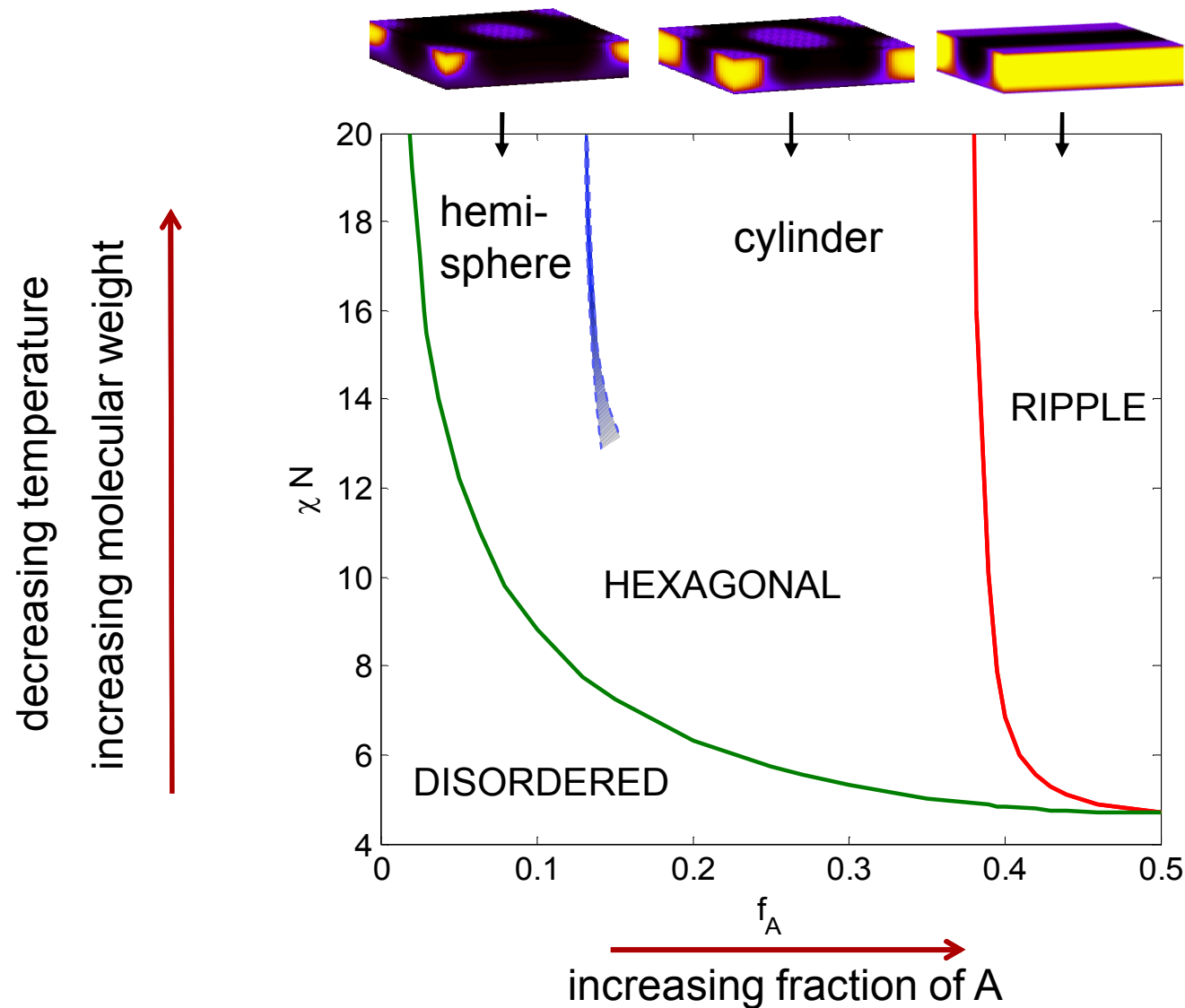


large cell simulations

start with random field configuration
iterate until free energy is “small”
equivalent to fast quench



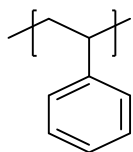
Phase Diagram of a Binary Melt Brush



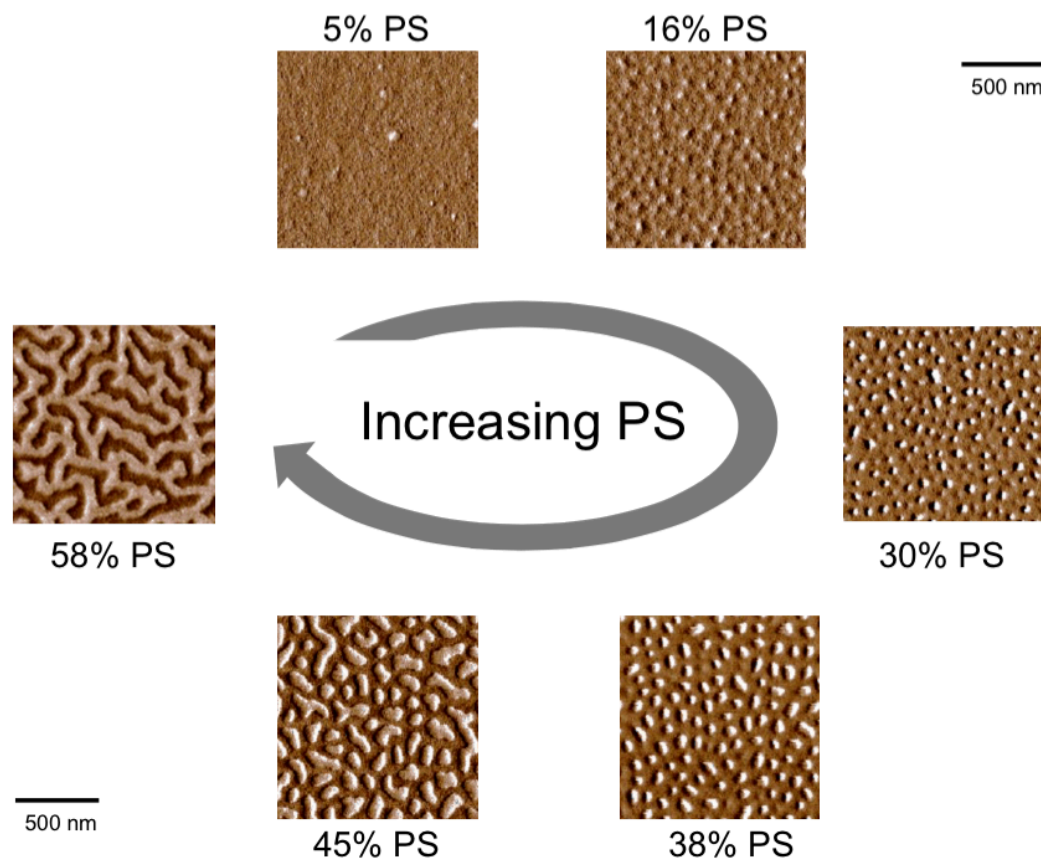
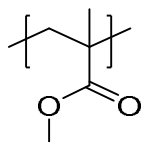
Experimental Verification

High Mw PS-PMMA mixed brushes
brush heights ≈ 30 nm

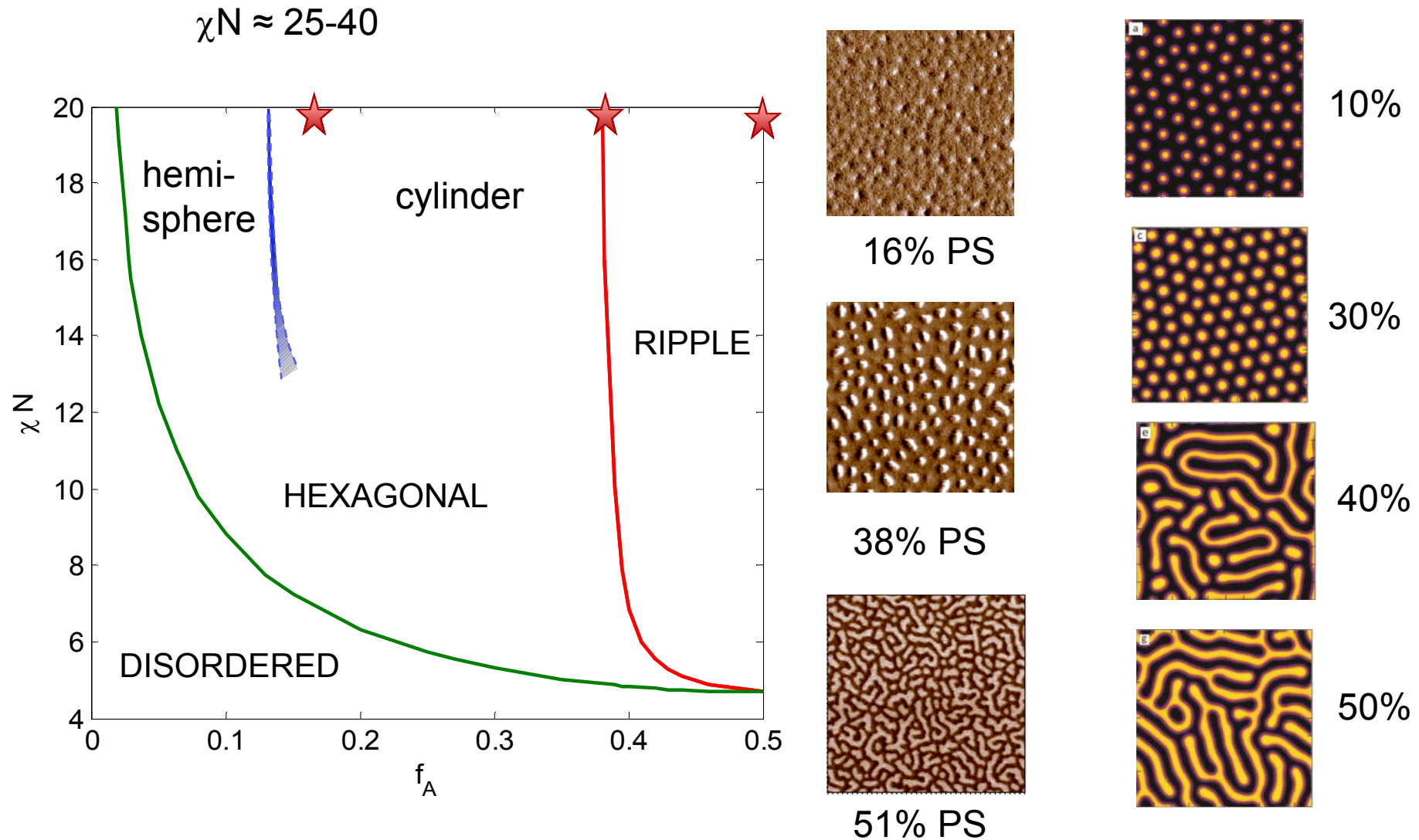
Polystyrene



Poly(methyl methacrylate)



Experimental Phases Similar to Theory

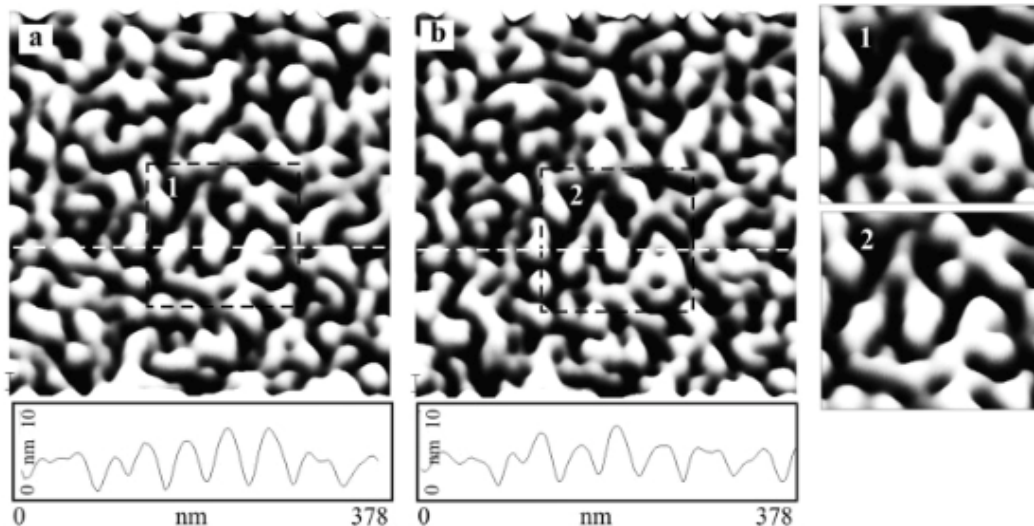


Why no long range order?

theory assumes *uniform* distribution of grafting sites

experimentally: *random* is not the same as *uniform*

fluctuations in grafting density lead to disorder in lateral structure



memory effect: domains reform in same location after solvent cycle

Grafting density fluctuations

incorporate spatial variations in
grafting density in theory

SCFT

uniform grafting density

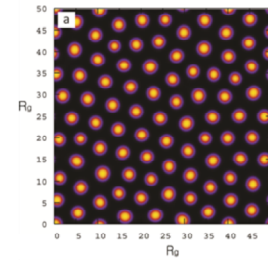
$$g_A(\mathbf{x}_\perp) = f_A$$

Gaussian random distribution of
grafting sites

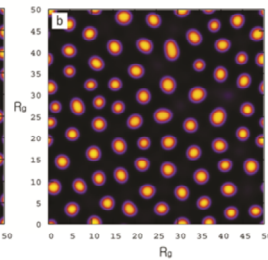
$$\langle (g_A(\mathbf{x}_\perp) - f_A)(g_A(\mathbf{x}'_\perp) - f_A) \rangle = \Lambda^2 \exp(-|\mathbf{x}_\perp - \mathbf{x}'_\perp|^2 / 2\sigma^2)$$

$$\sigma = 0.5R_g, \Lambda^2 = 0.02$$

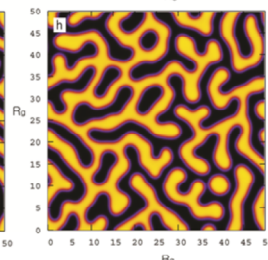
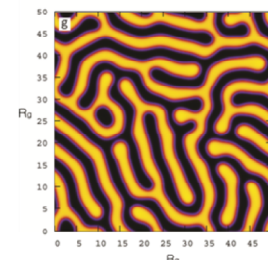
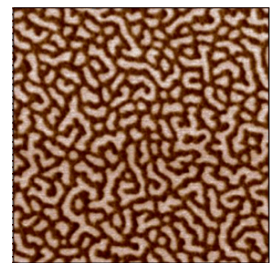
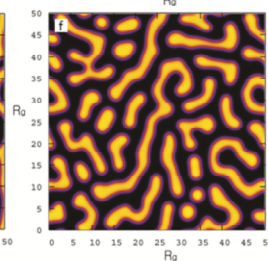
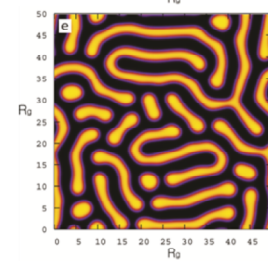
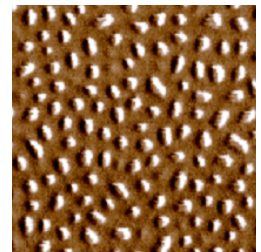
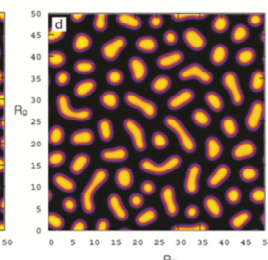
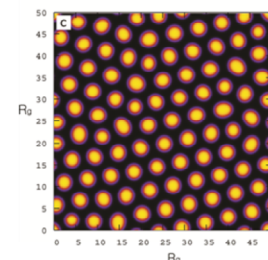
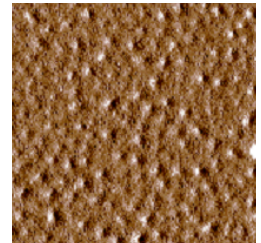
uniform



correlated



experiment



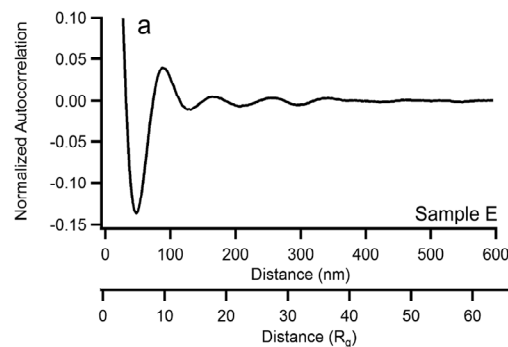
Price et al., *Macromolecules* **45**, 510 (2012); Hur et al.,
Soft Matter **9**, 5341 (2013)

Similar amounts of order

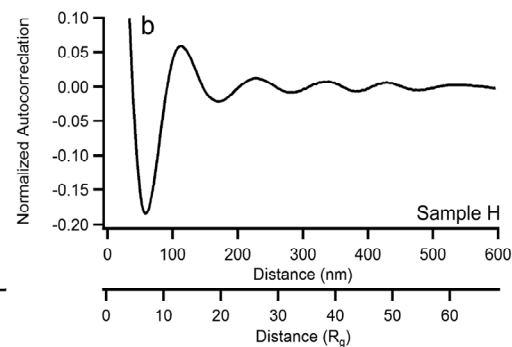
experiment

Cylindrical Phase

Experiment

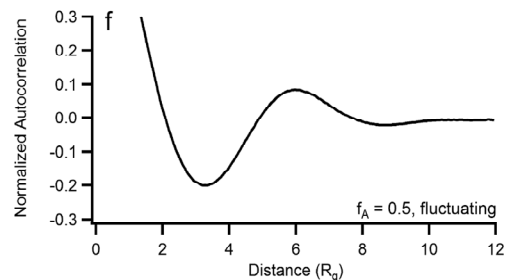
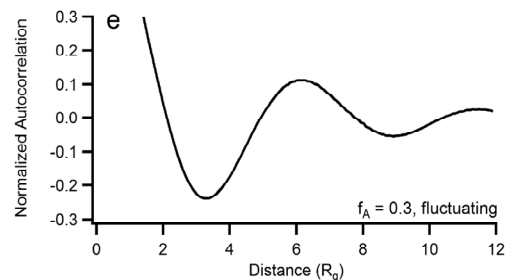
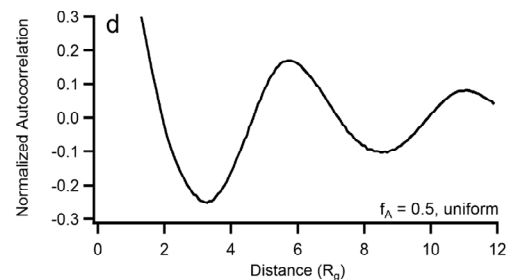
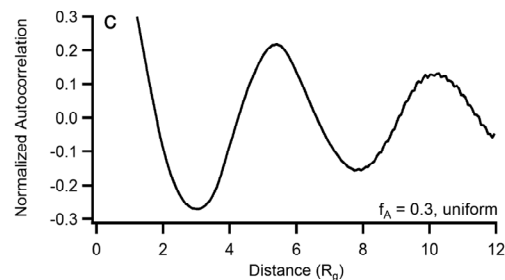


Ripple Phase



simulations

SCFT Simulation



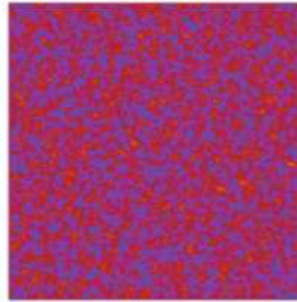
Correlations in grafting density

grafting

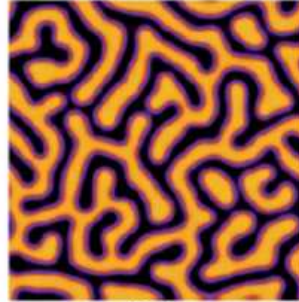
top of brush

$$\langle (g_A(\mathbf{x}_\perp) - f_A)(g_A(\mathbf{x}'_\perp) - f_A) \rangle = \Lambda^2 \exp(-|\mathbf{x}_\perp - \mathbf{x}'_\perp|^2 / 2\sigma^2)$$

$\sigma = 0.4$

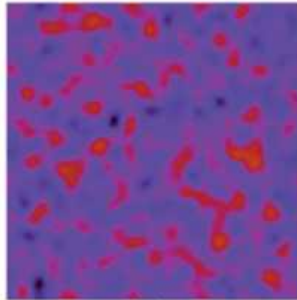


(a)

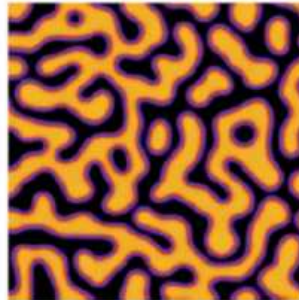


(b)

$\sigma = 1.4$

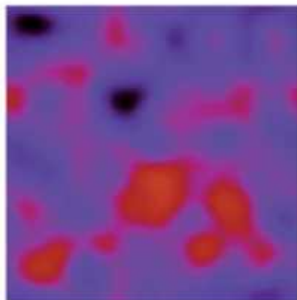


(d)

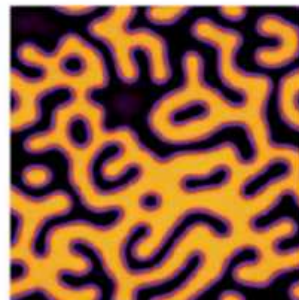


(e)

$\sigma = 3.5$

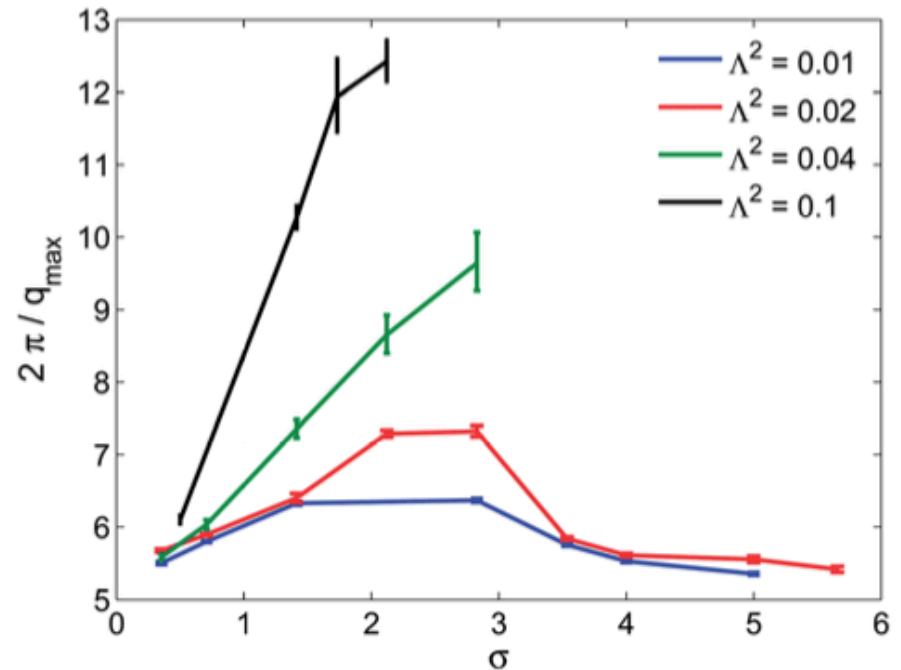


(g)



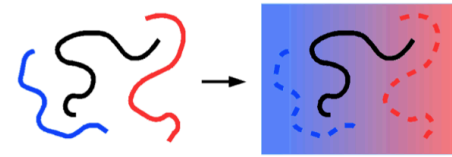
(h)

domain size

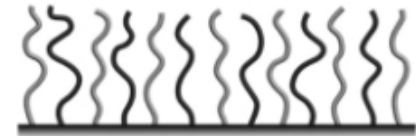


Rest of the Talk

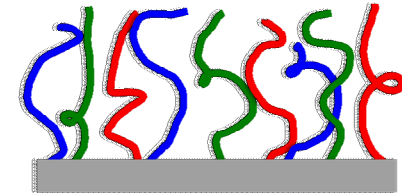
- polymer field theory



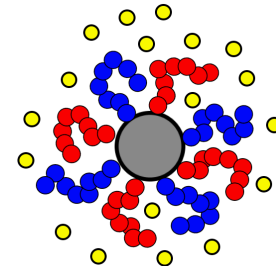
- binary brushes



- ternary brushes



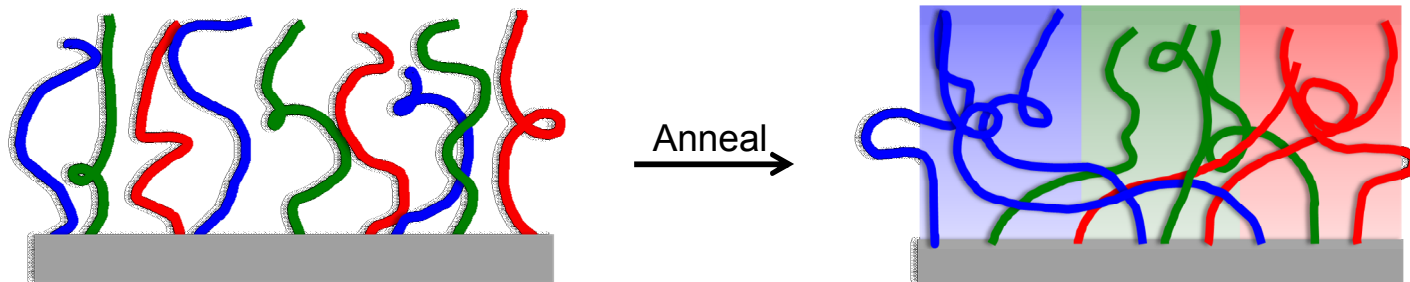
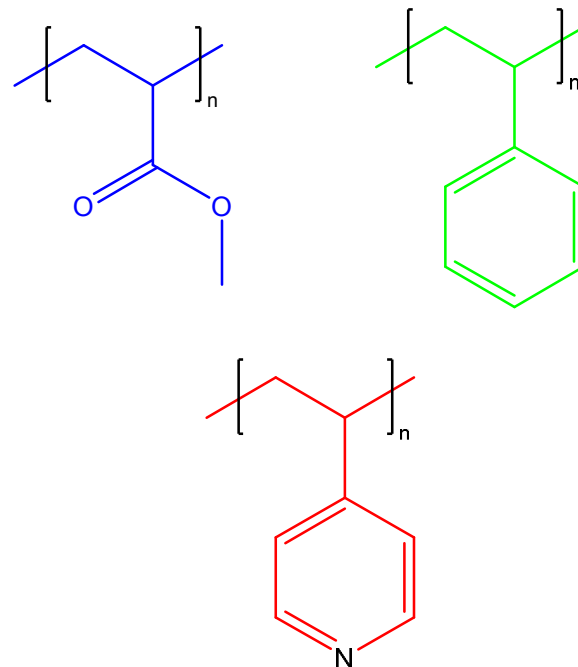
- binary brushes on nanoparticles



theme: effects of fluctuations

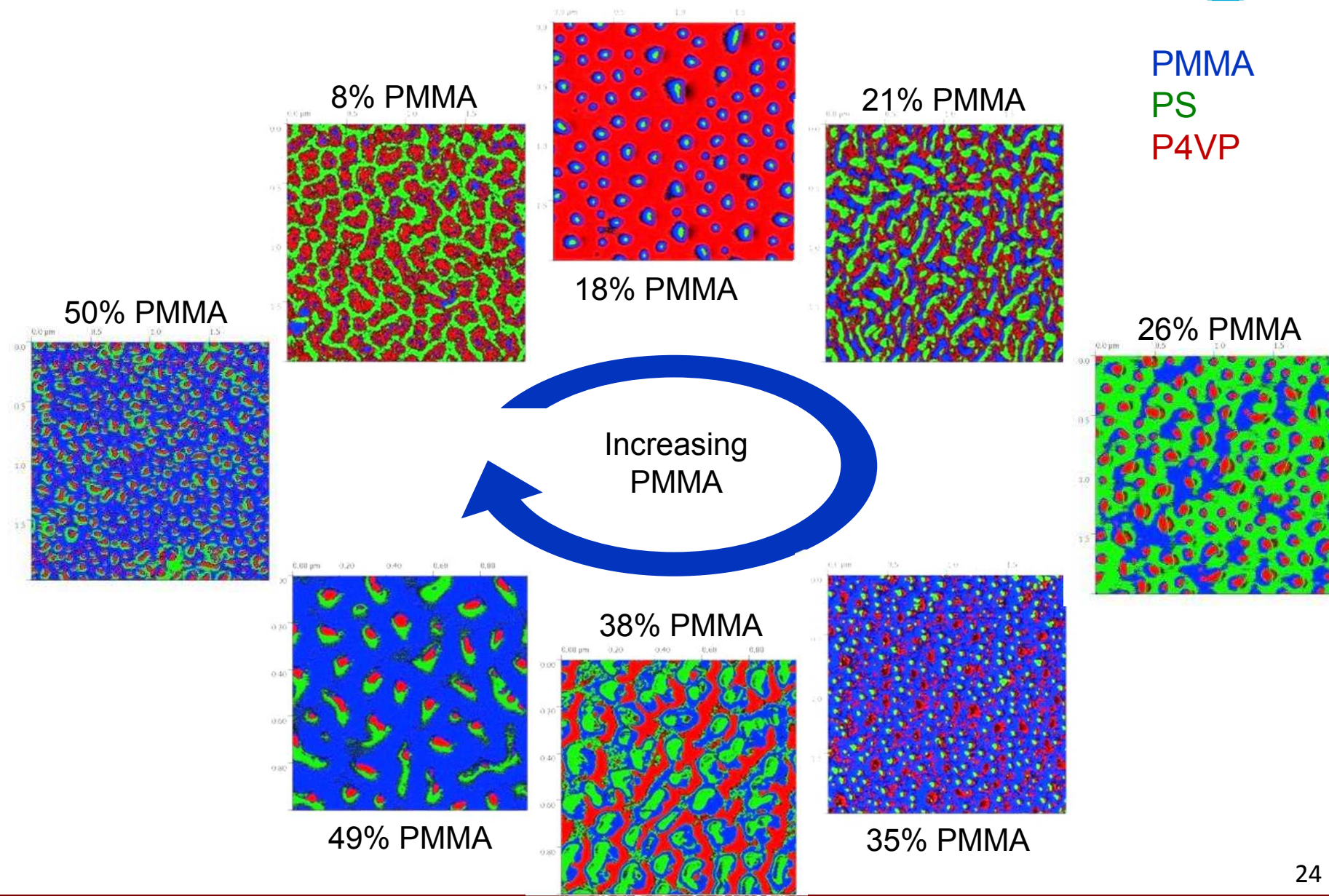
Ternary Polymer Brushes

- PMMA, PS, and P4VP
- Strongly segregating system
 - $\chi N_{\text{PS-PMMA}} \approx 18$
 - $\chi N_{\text{PMMA-P4VP}} \approx 65$
 - $\chi N_{\text{PS-P4VP}} \approx 320$
- AFM was used to analyze phase behavior



Experimental Phase Behavior

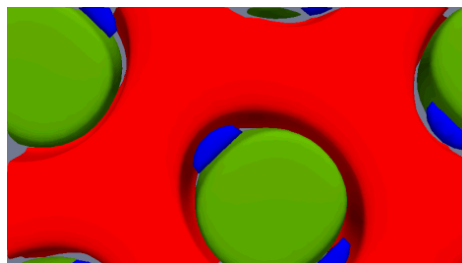
PMMA
PS
P4VP



Unit Cell SCFT Calculations

set $\chi N_{AB} = 10$, $\chi N_{AC} = 12$, $\chi N_{BC} = 16$

10% PMMA



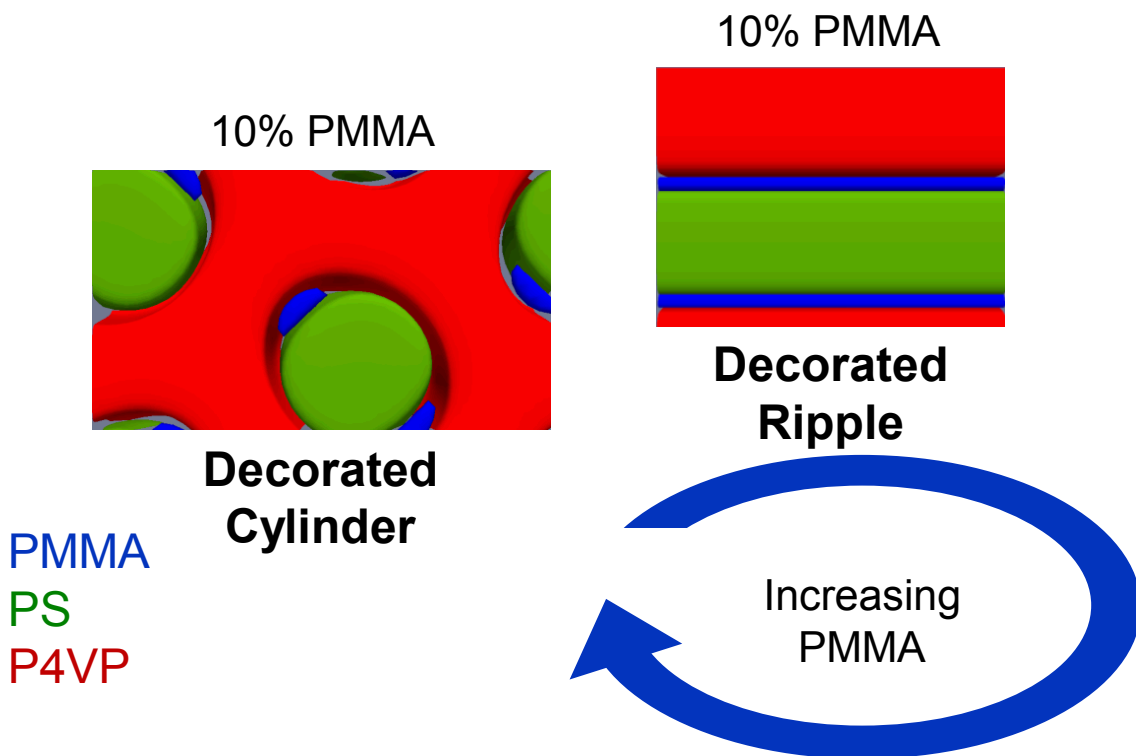
**Decorated
Cylinder**

PMMA
PS
P4VP

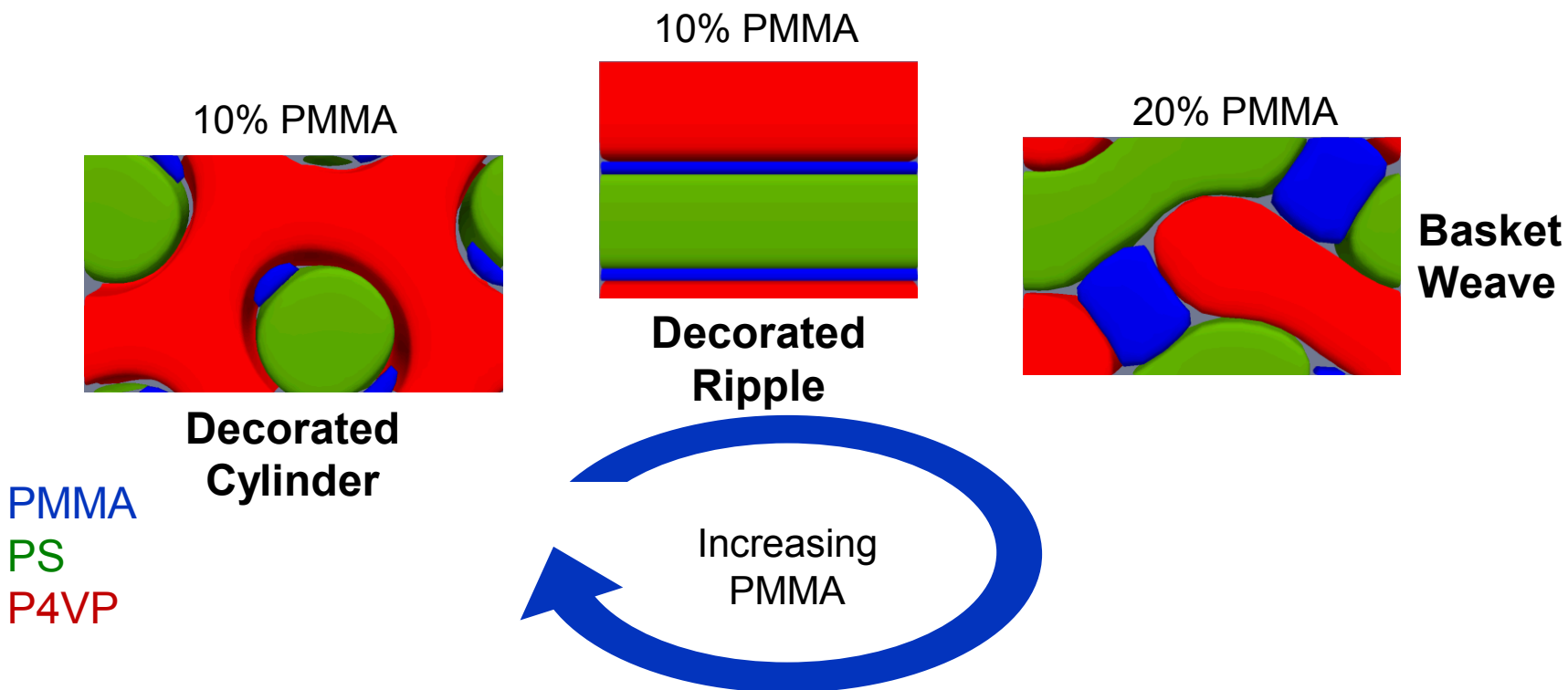


Increasing
PMMA

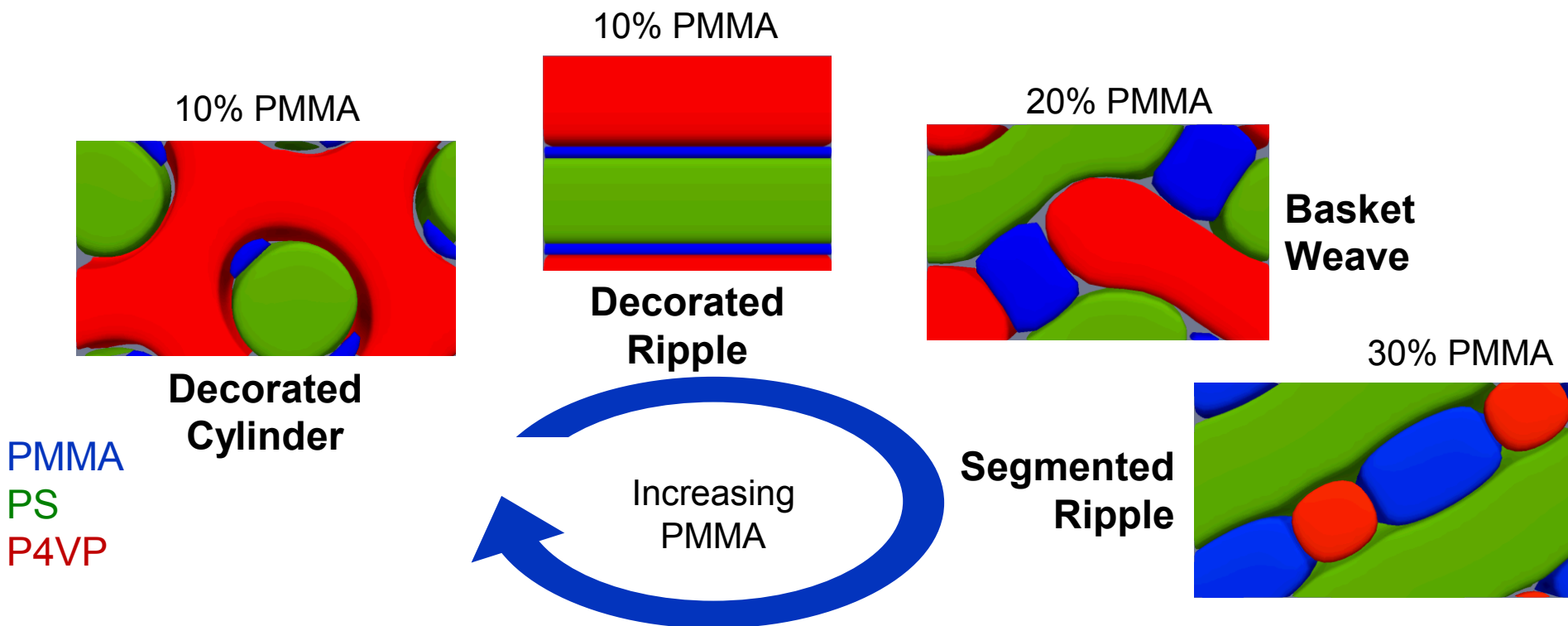
Unit Cell SCFT Calculations



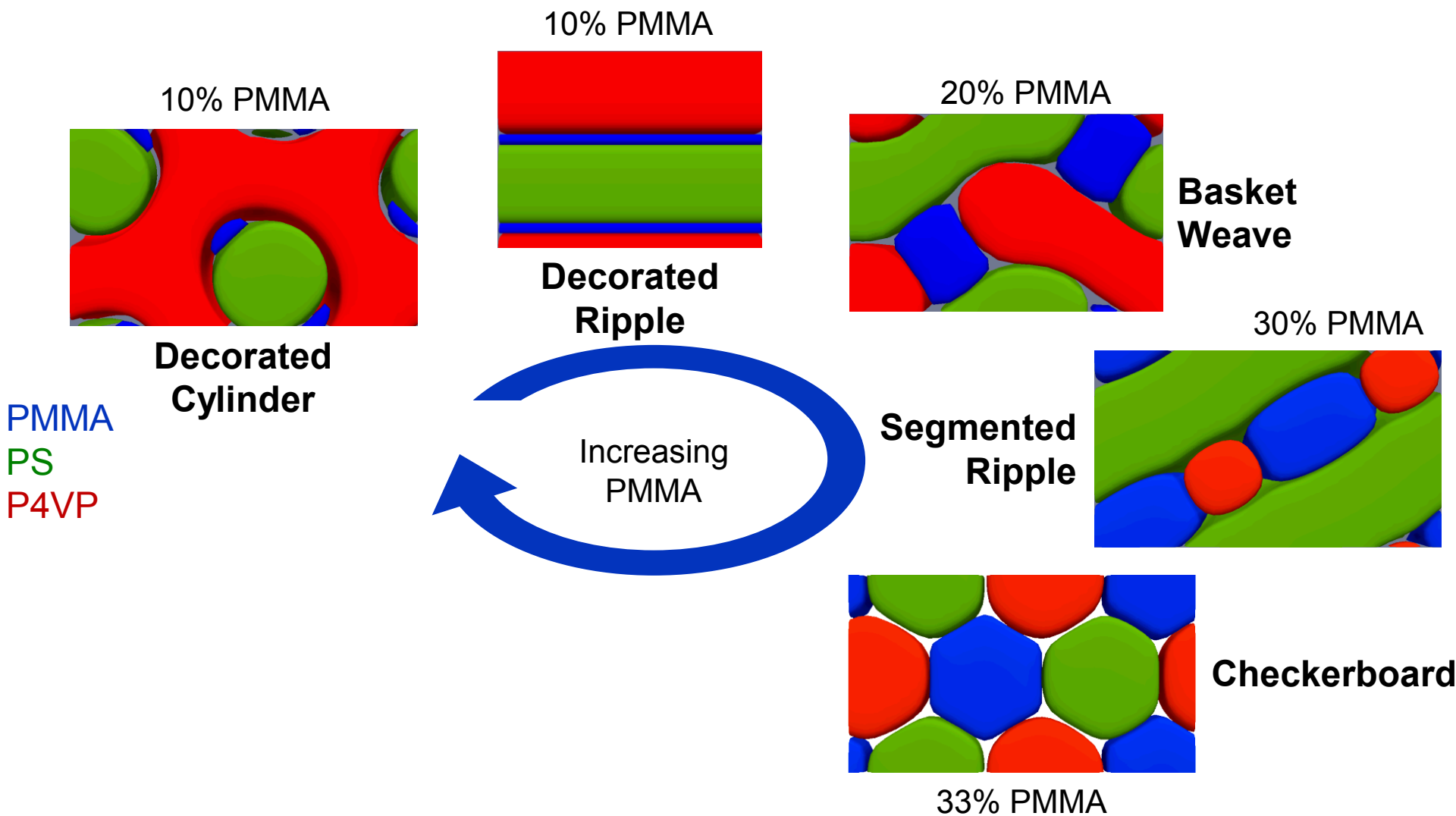
Unit Cell SCFT Calculations



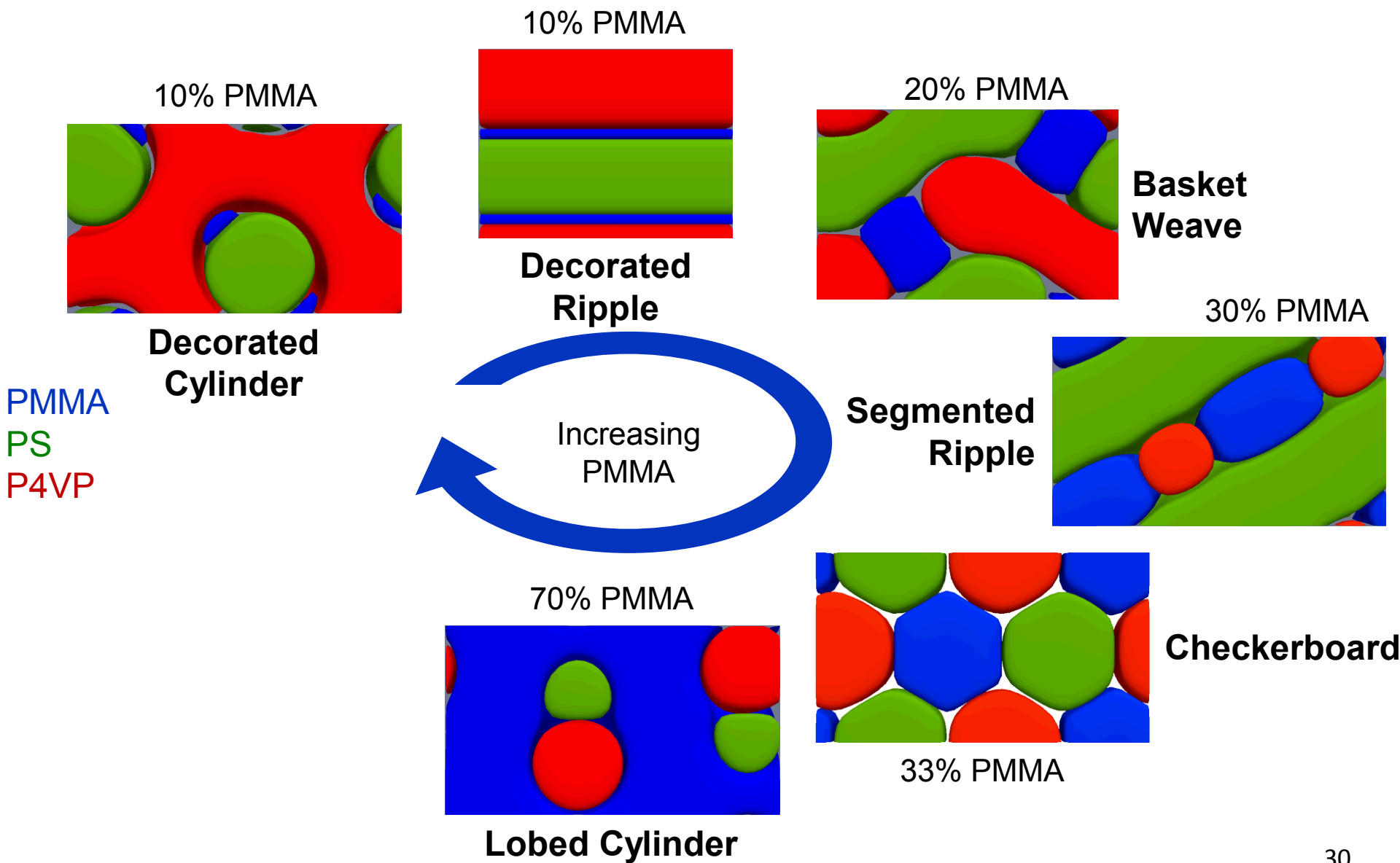
Unit Cell SCFT Calculations



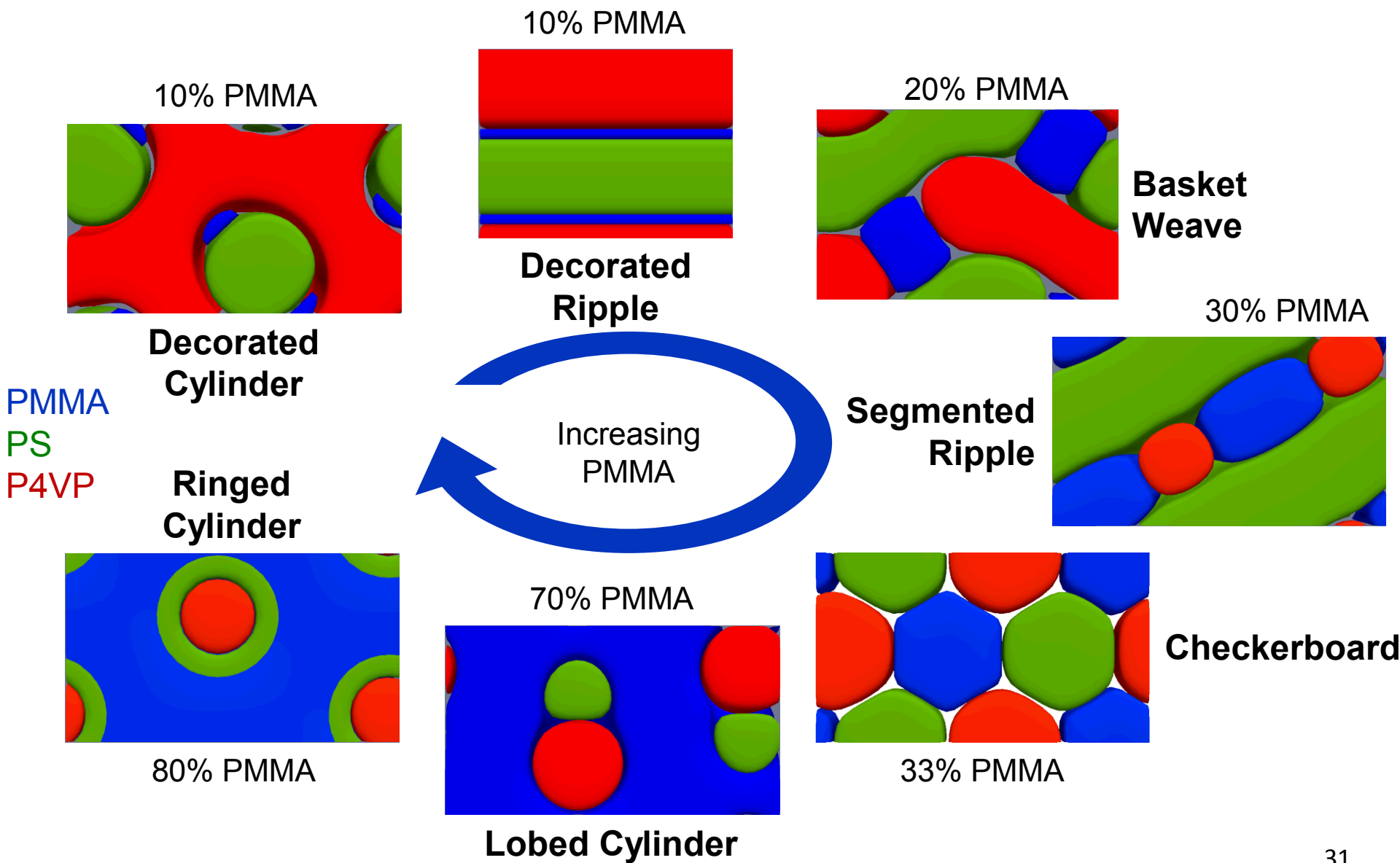
Unit Cell SCFT Calculations



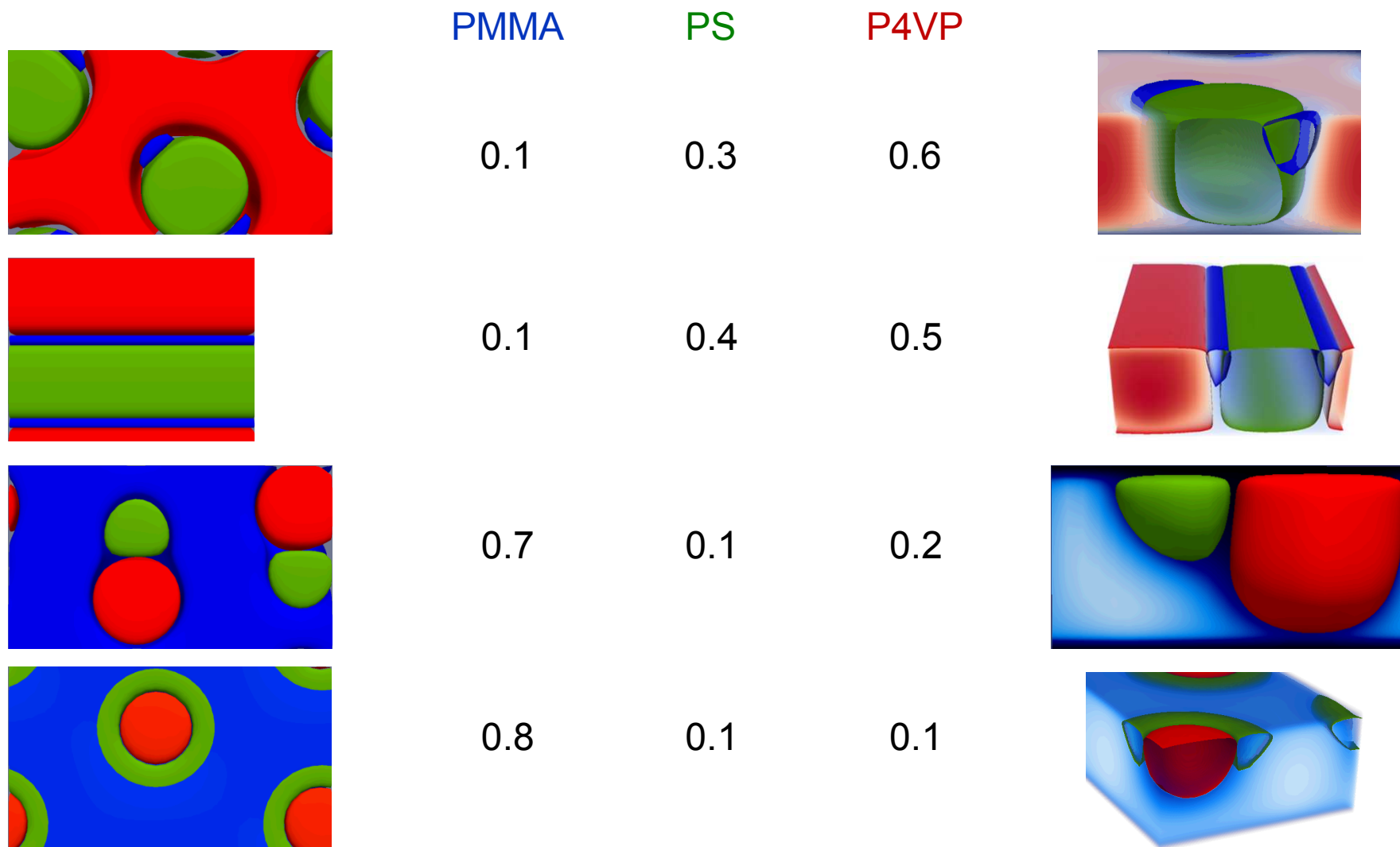
Unit Cell SCFT Calculations



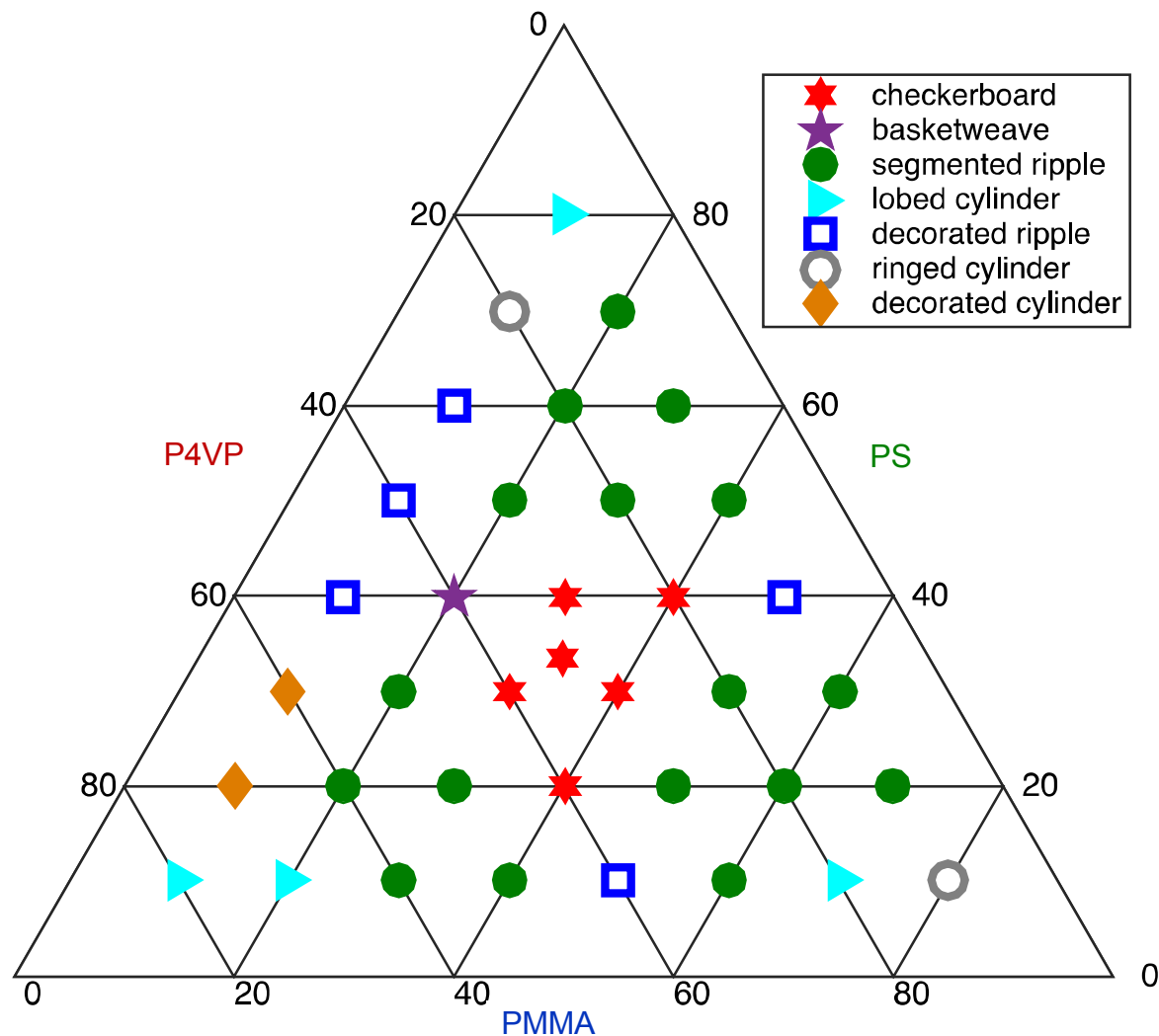
Unit Cell SCFT Calculations



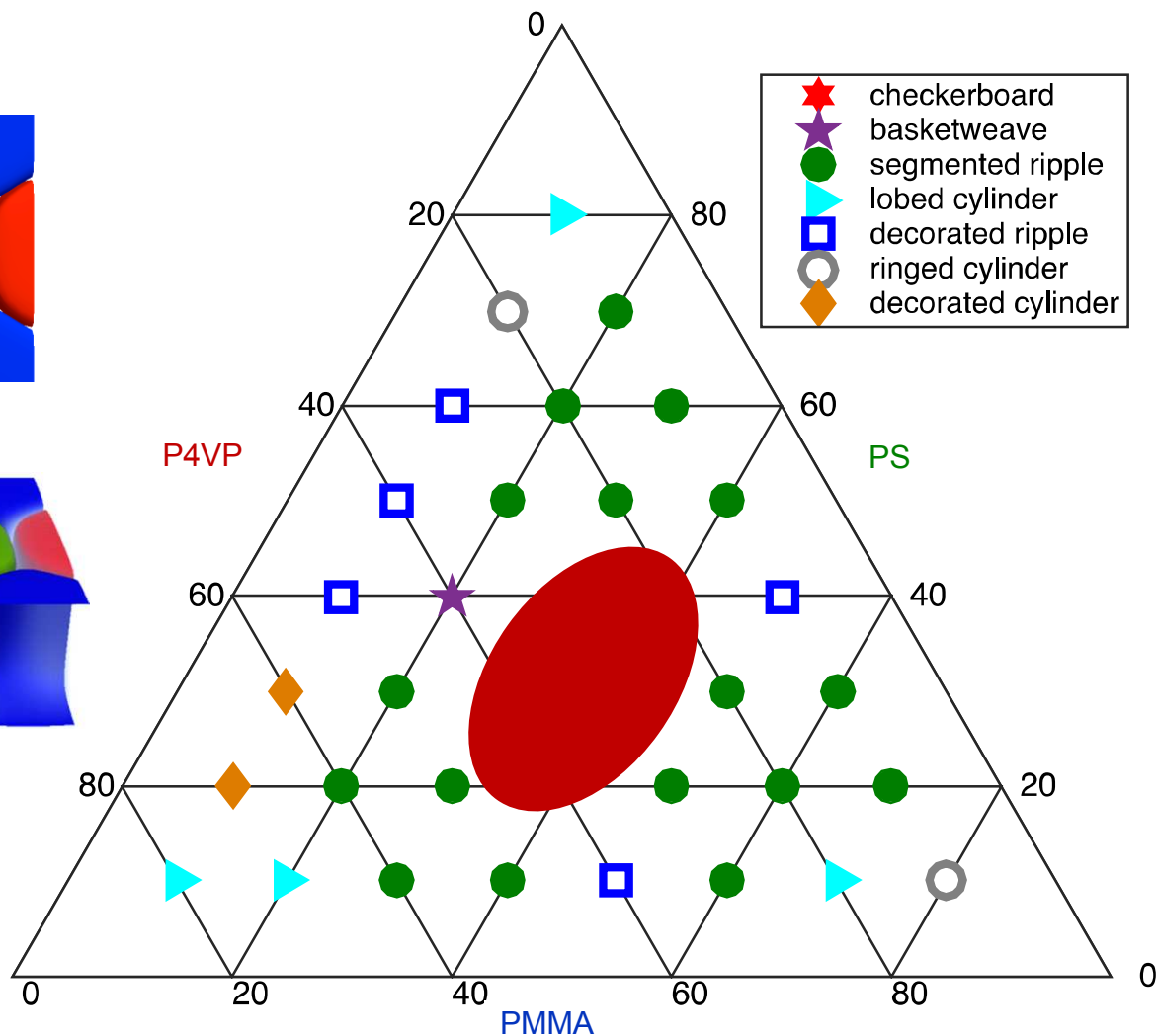
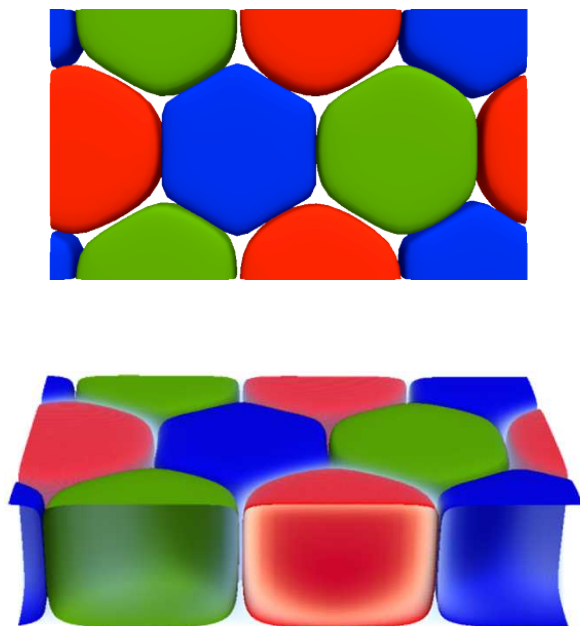
Below the Surface



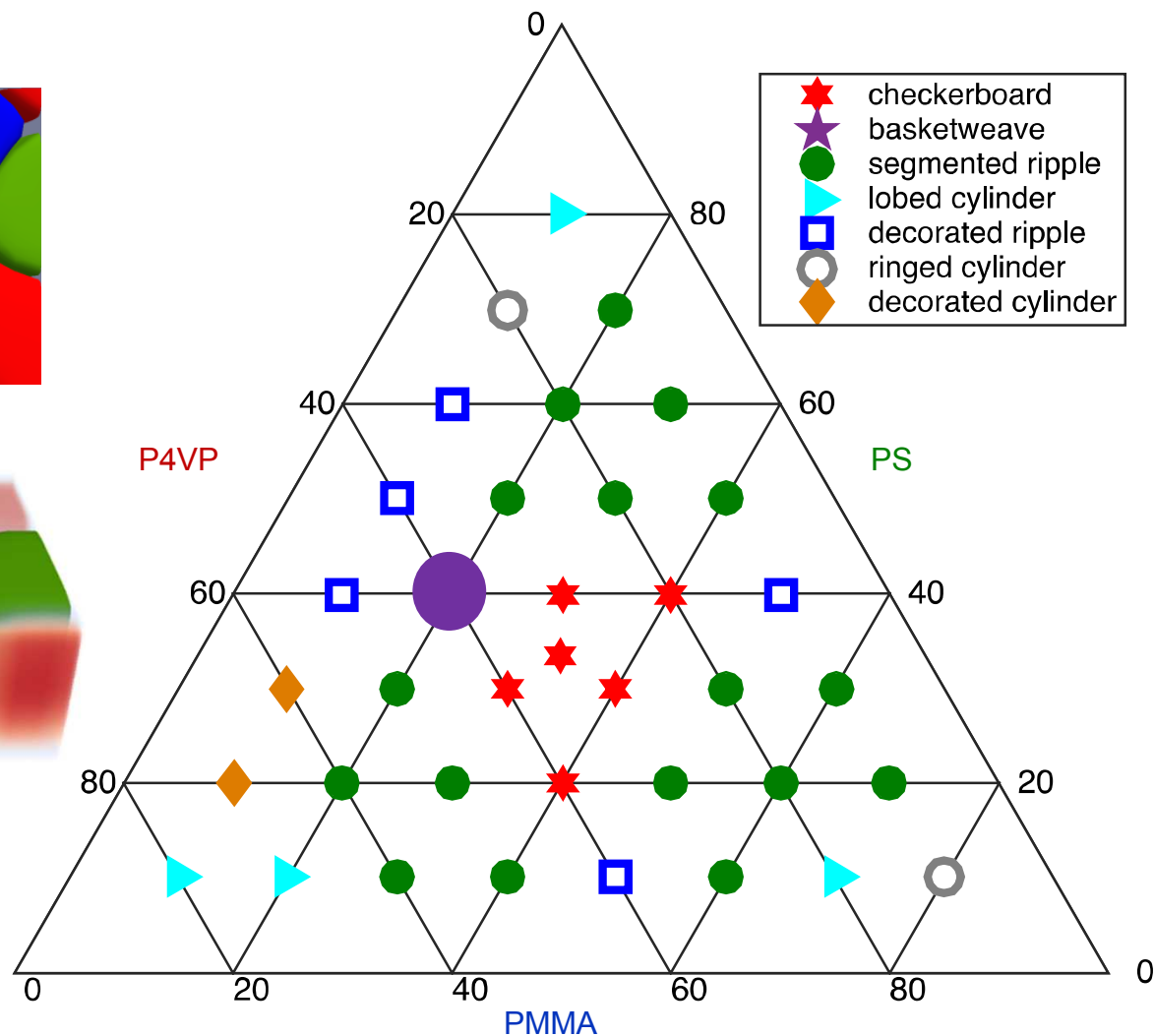
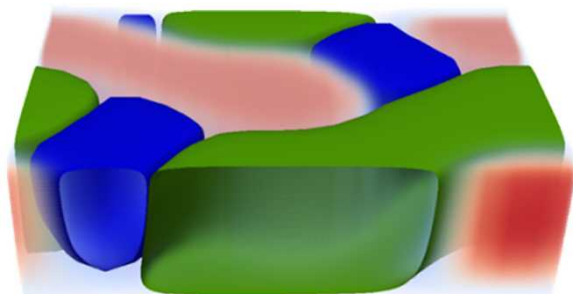
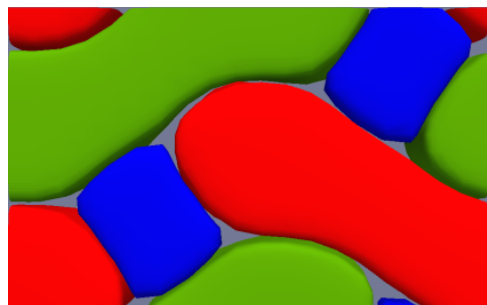
Phase Diagram



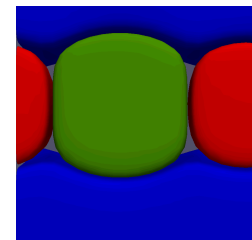
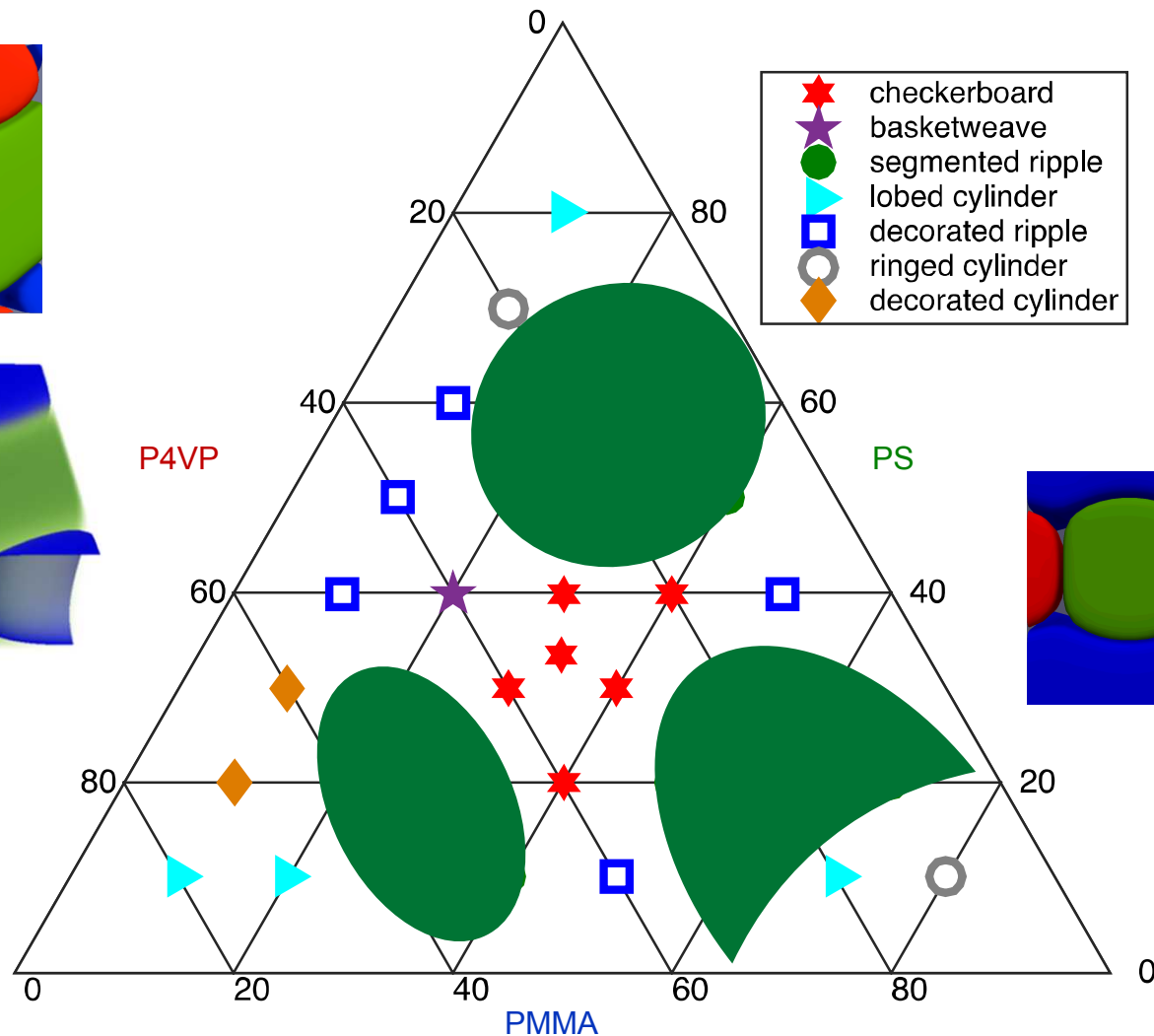
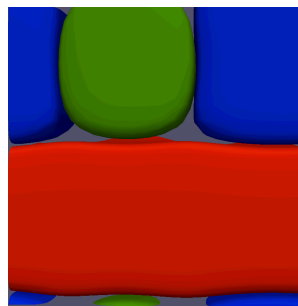
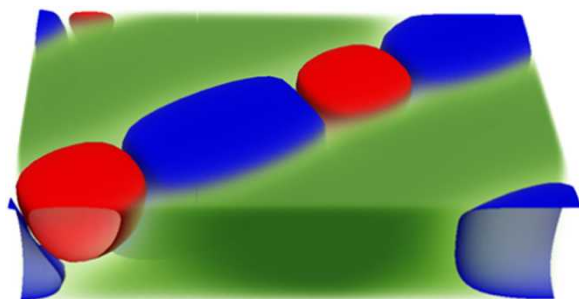
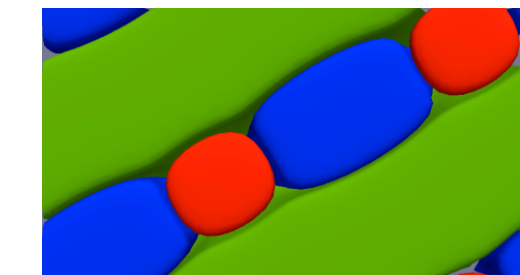
Phase Diagram



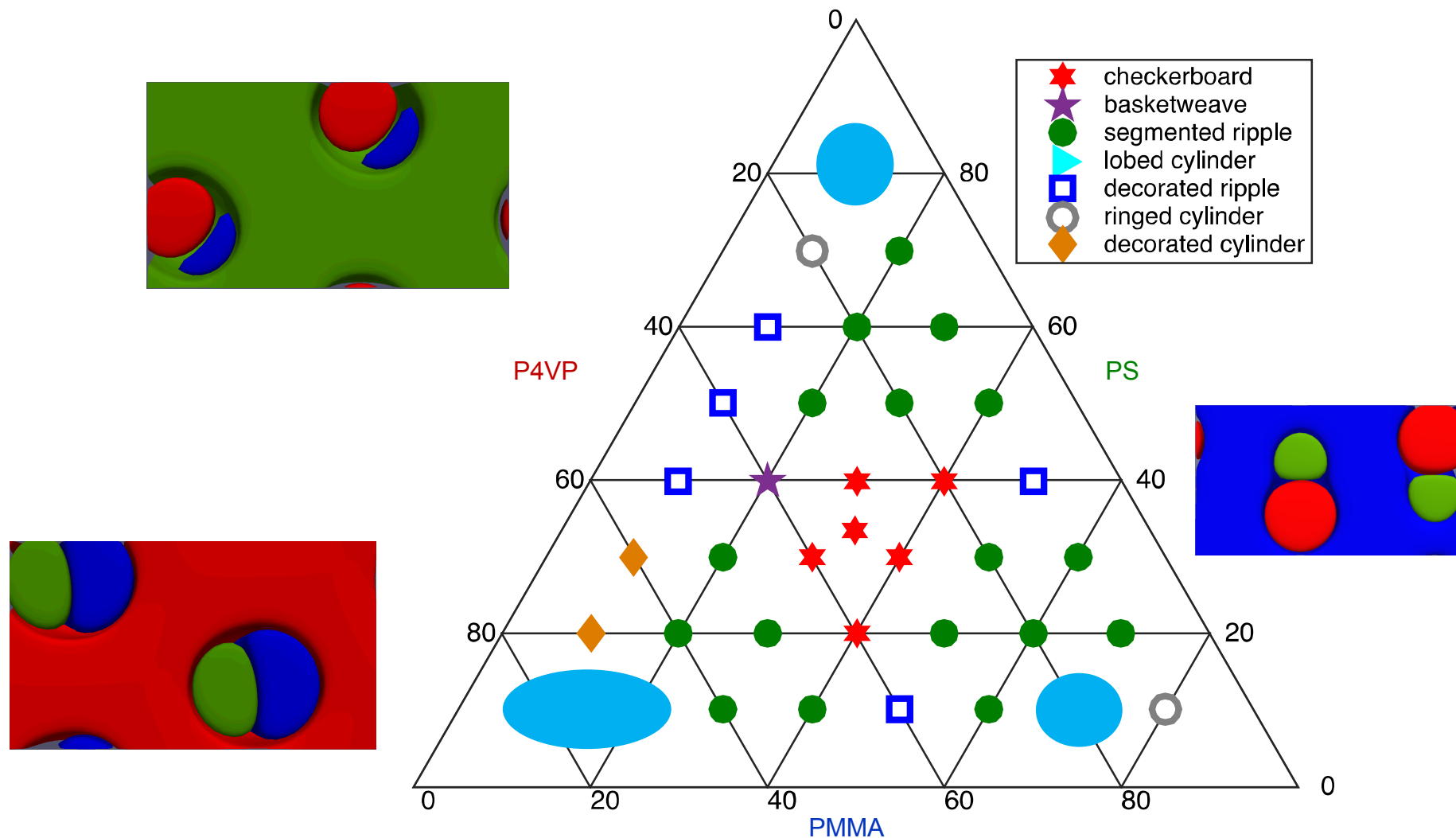
Phase Diagram



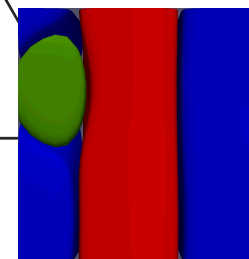
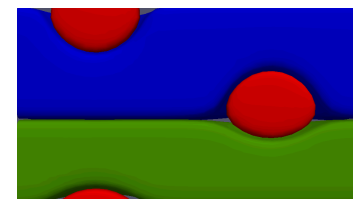
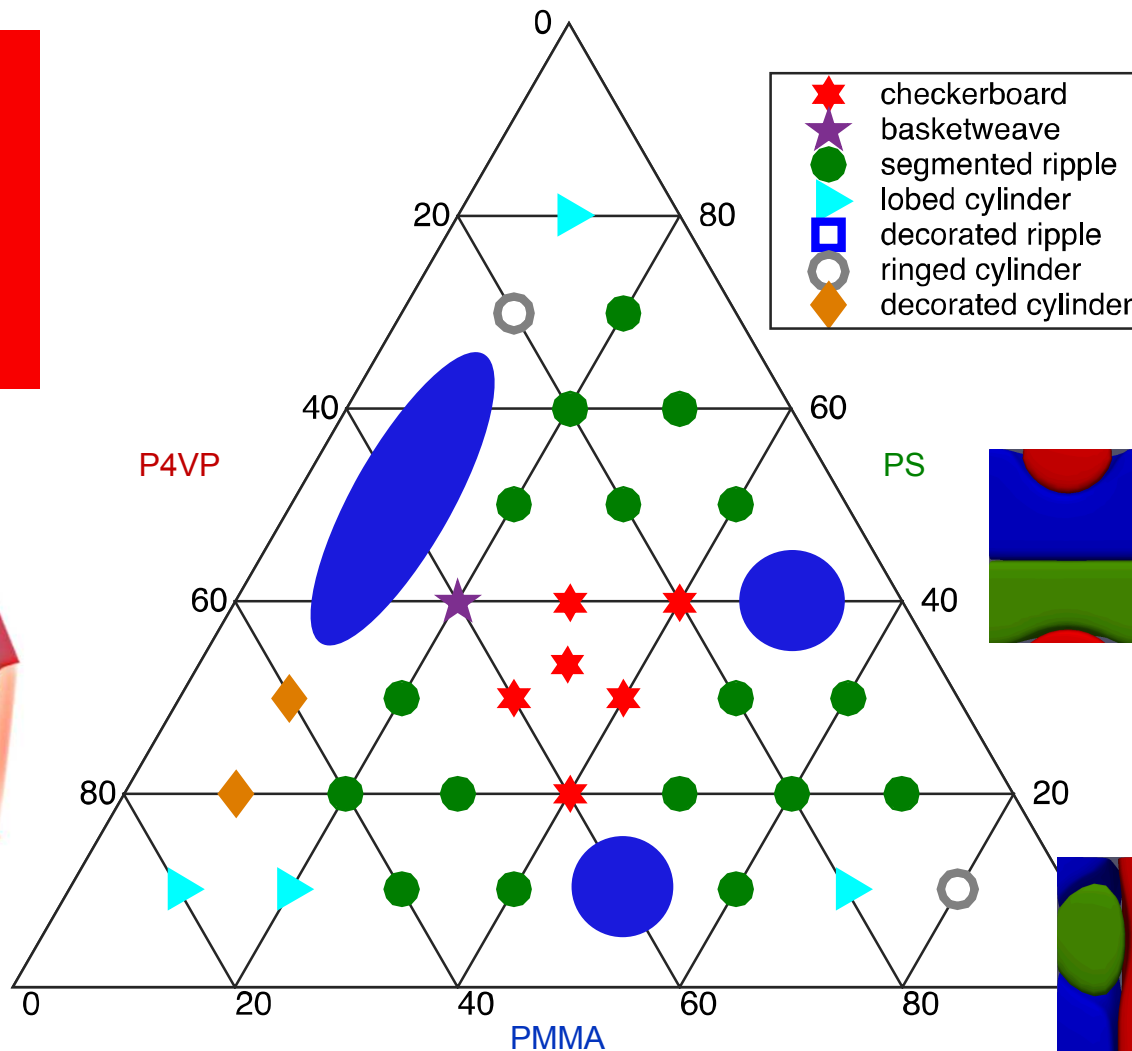
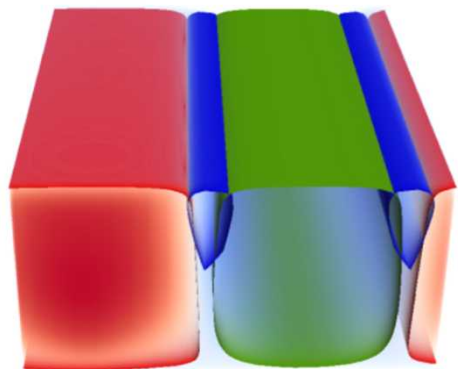
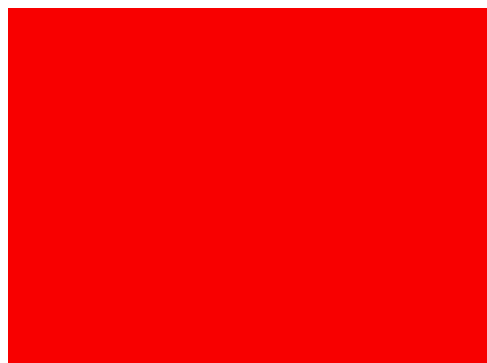
Phase Diagram



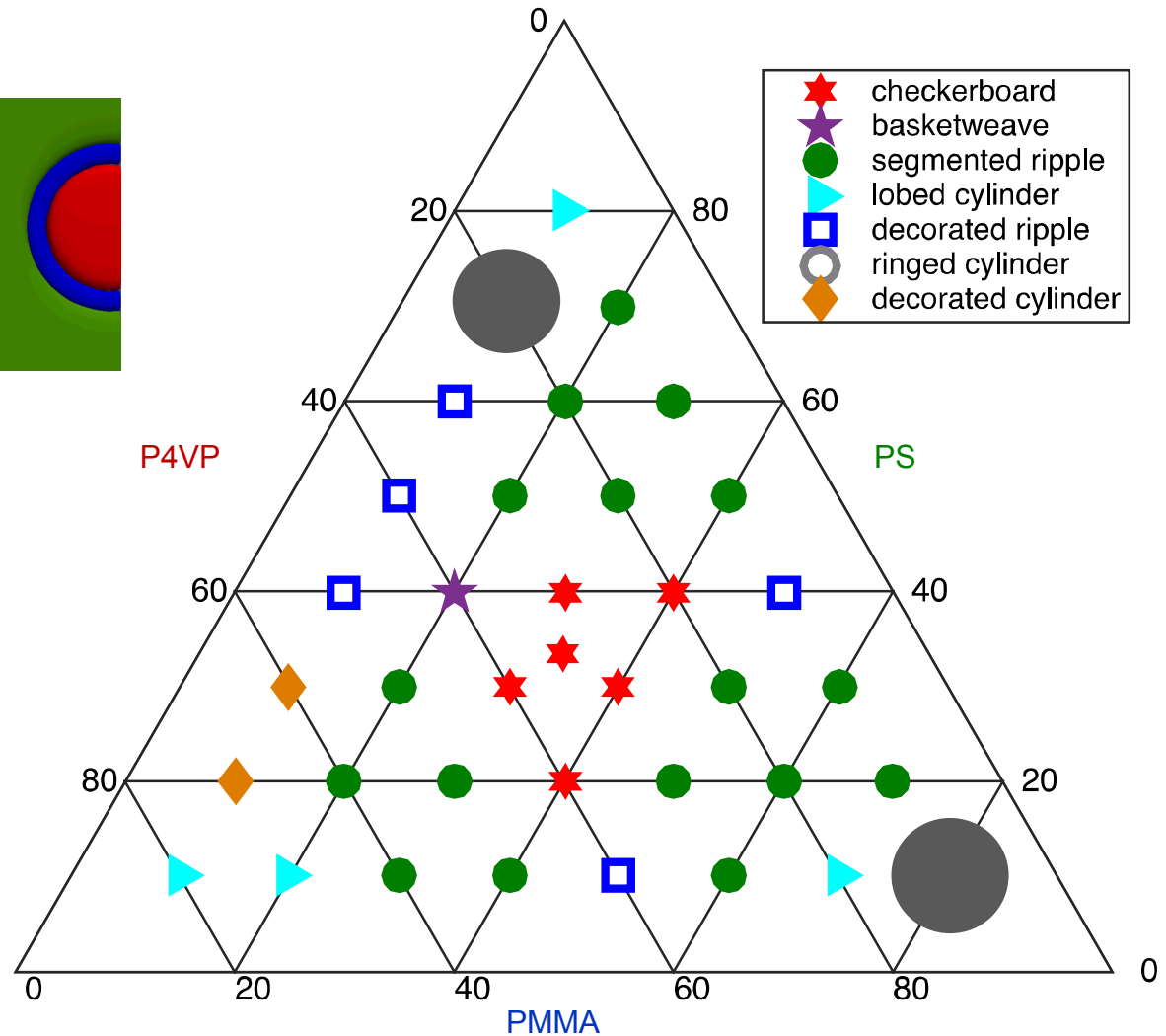
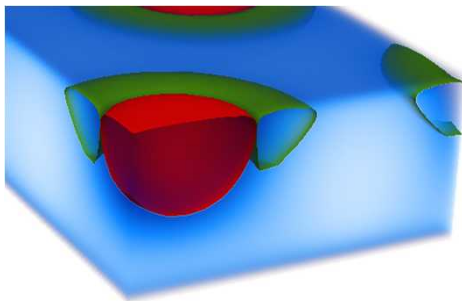
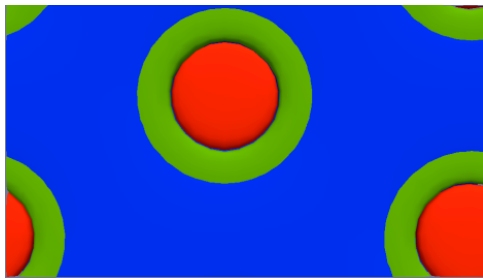
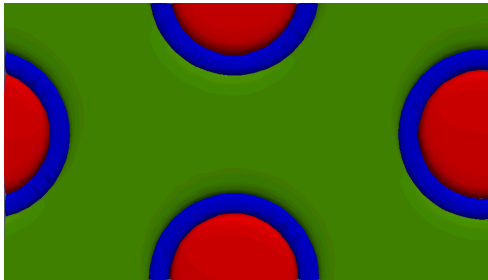
Phase Diagram



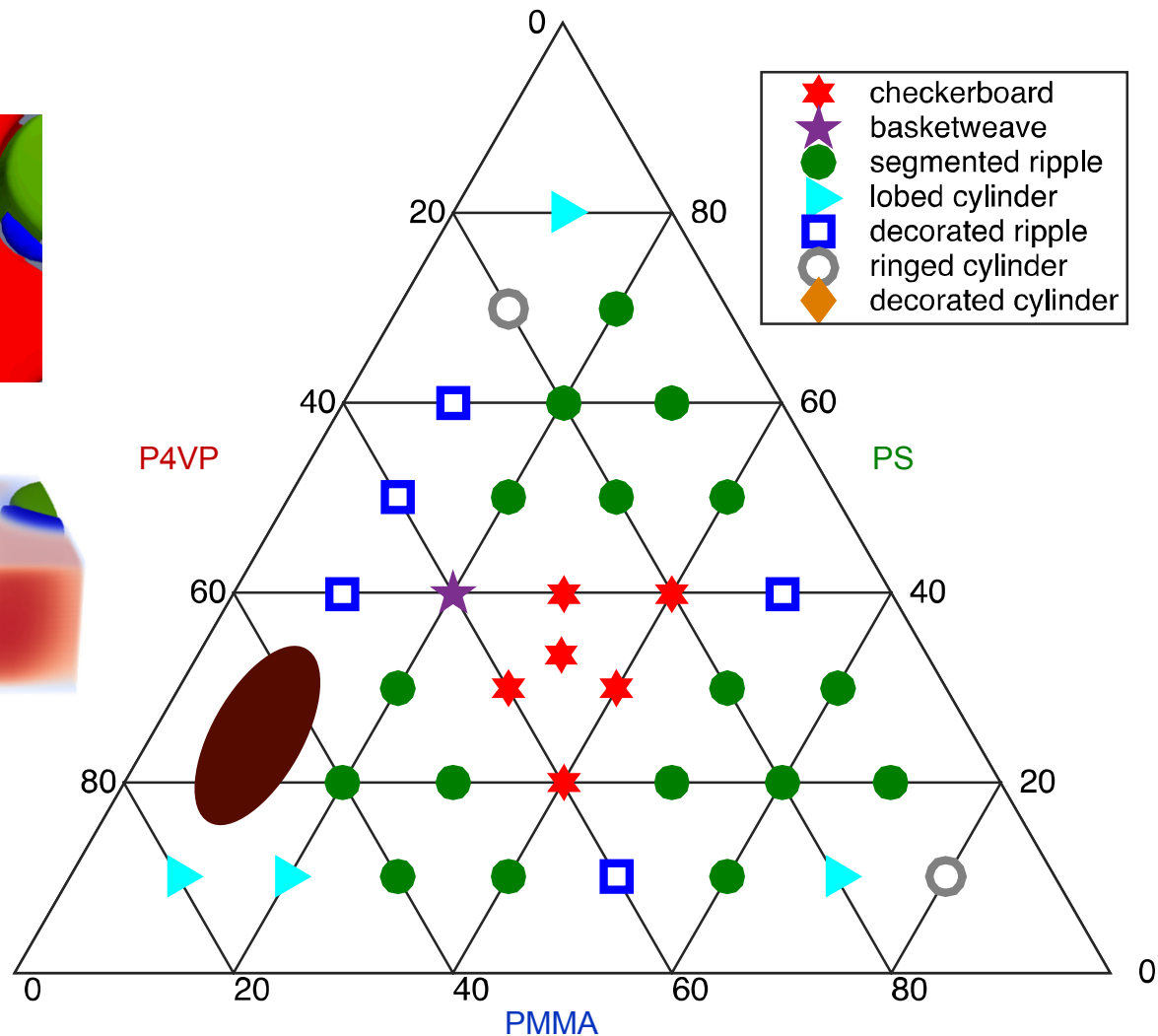
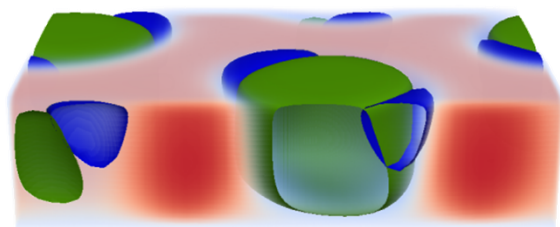
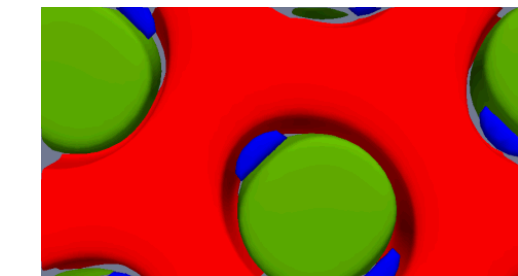
Phase Diagram



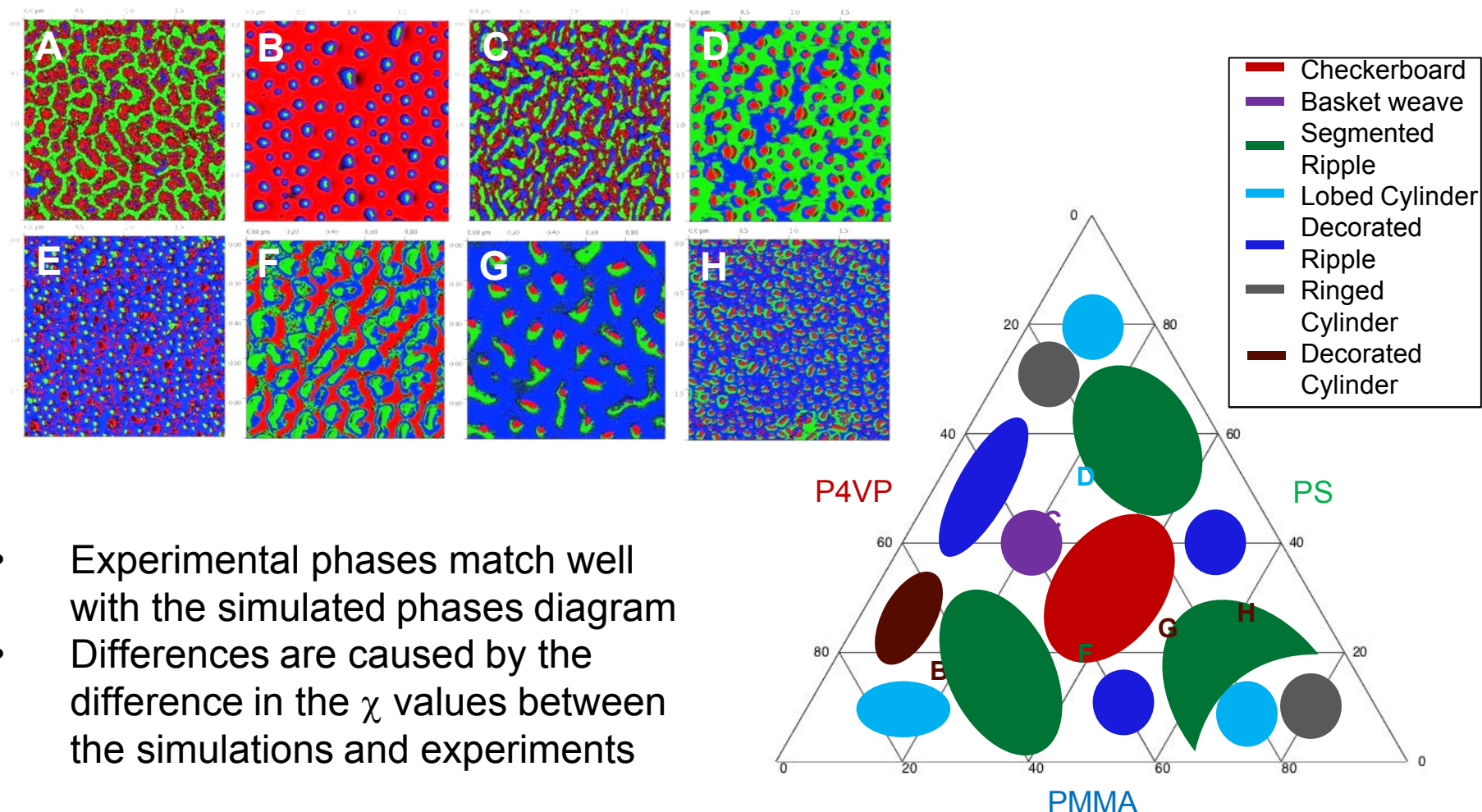
Phase Diagram



Phase Diagram



Matching Experiment to Theory



- Experimental phases match well with the simulated phases diagram
- Differences are caused by the difference in the χ values between the simulations and experiments

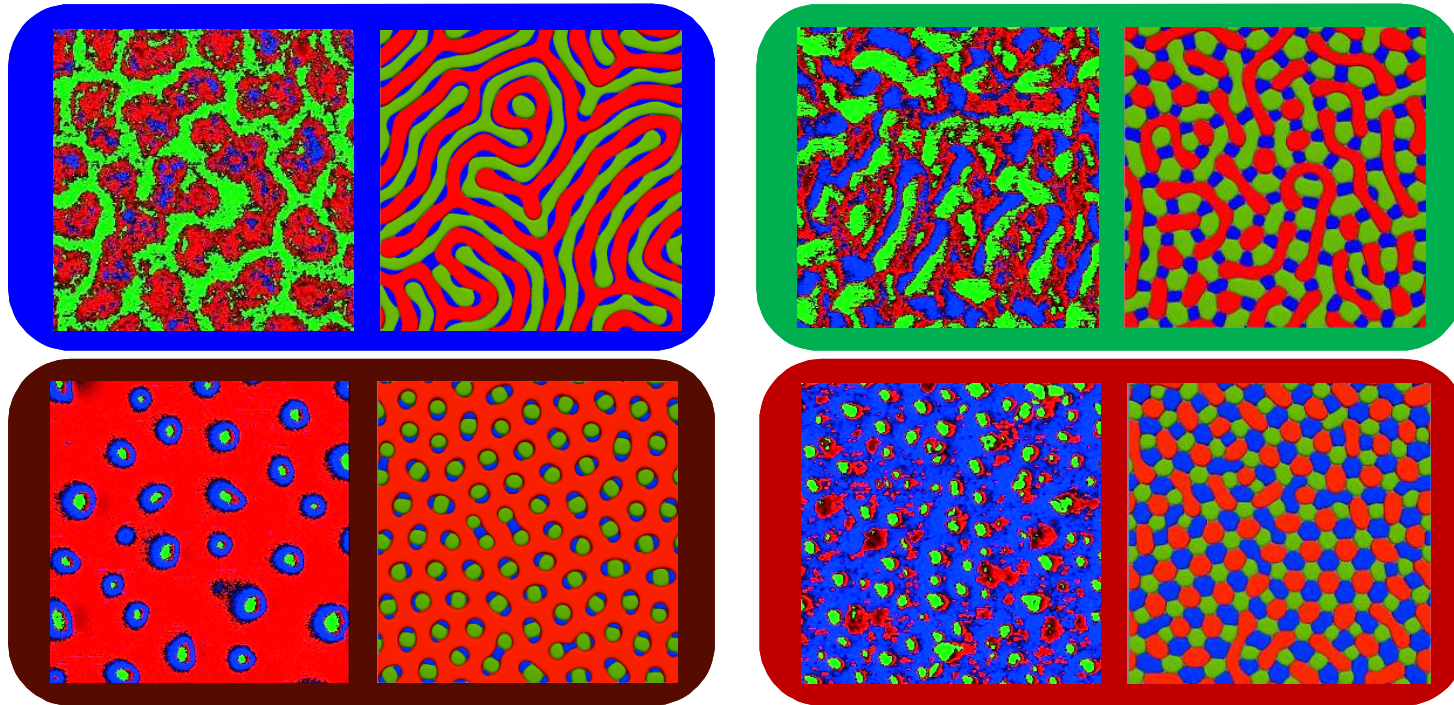
Large cell SCFT compared to experiment

experimental images $1 \times 1 \mu\text{m}$

simulation images $50 \times 50 R_g$

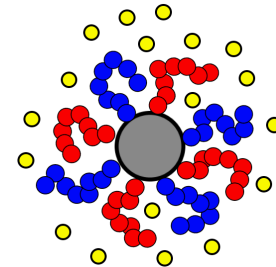
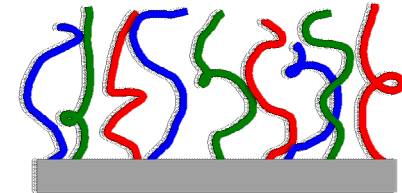
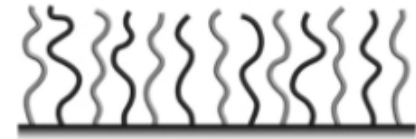
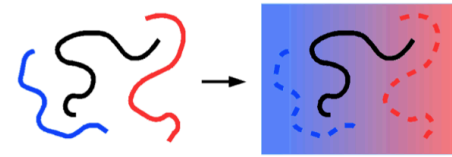
qualitative agreement

no grafting density fluctuations in SCF



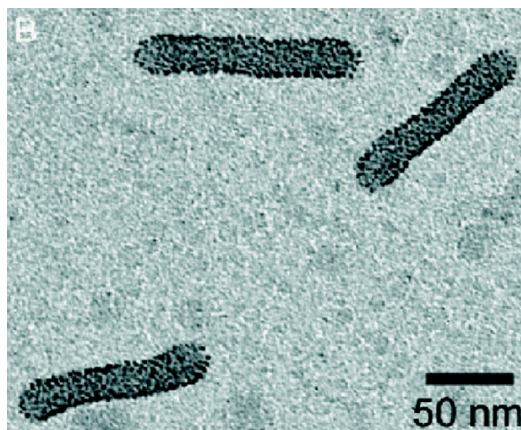
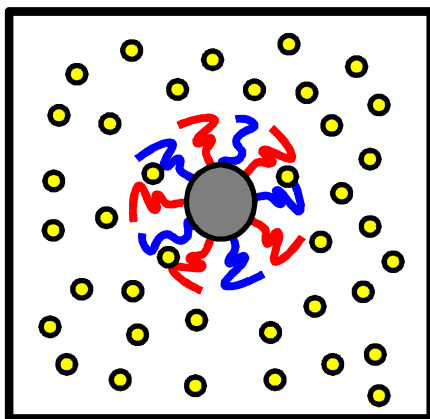
Rest of the Talk

- polymer field theory
- binary brushes
- ternary brushes
- binary brushes on nanoparticles

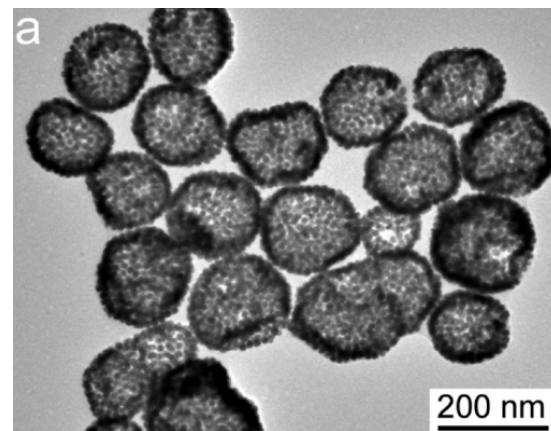


theme: effects of fluctuations

Mixed Brush on Nanoparticle in Solvent



Zubarev, *et al.*, JACS, 2006



Song, *et al.*, JACS, 2012

what brush structure do we expect on 1 particle?

how will many particles assemble?

SCF Brush Profiles

assume: $N_A = N_B$

$$f_A = f_B$$

$$\chi_{AS} = \chi_{BS} = \chi_S$$

to compare to experiment

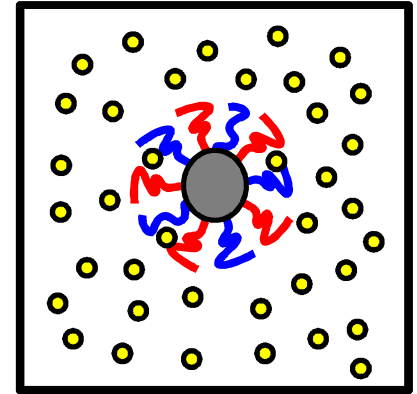
$N = 60$ kg/mol

PS-PMMA at 100°C, $\chi N = 18.9$

$R_p = 4.4$ nm

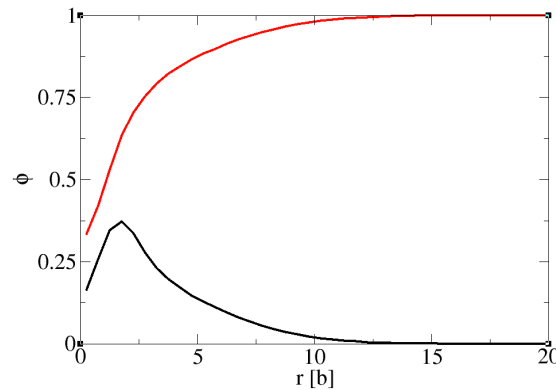
vary: R_p/R_g , σ , χ_{AB} , χ_S

R_p = nanoparticle radius

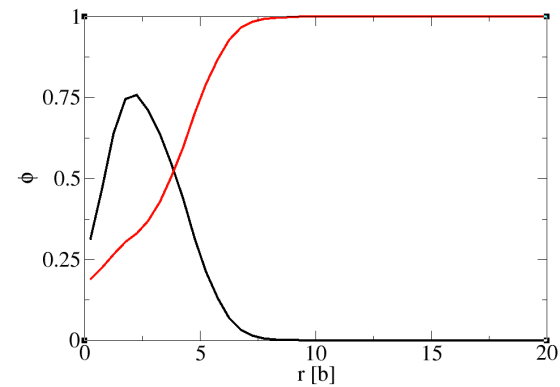


$$\chi_{AB}N = 28.3$$

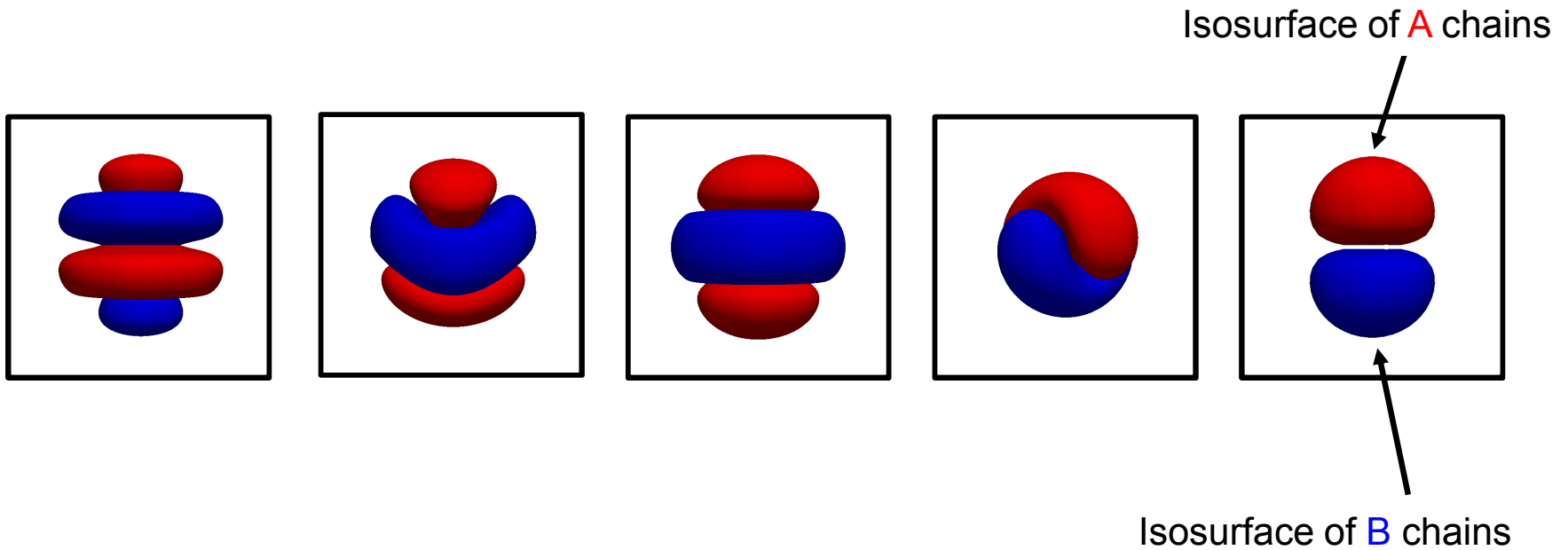
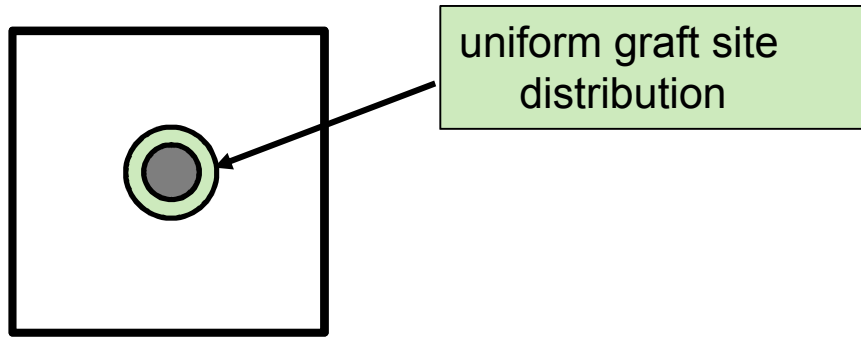
$$\chi_S = 0.5$$



$$\chi_S = 1.0$$



Ordered Brush Isosurfaces from SCFT



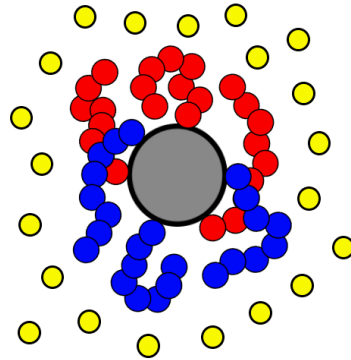
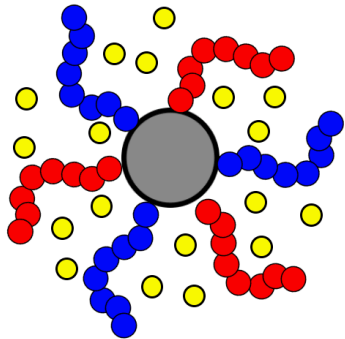
Effect of solvent quality

$$\chi_{AB}N = 18.9$$

$$R_P = (2/3)R_g$$

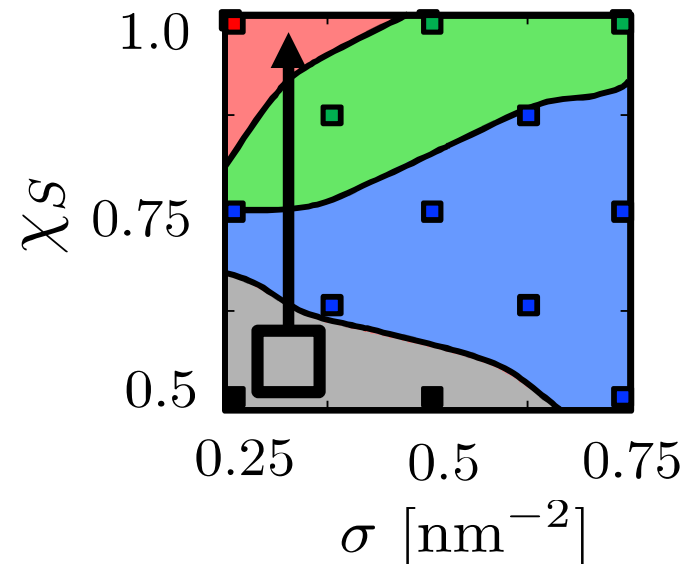
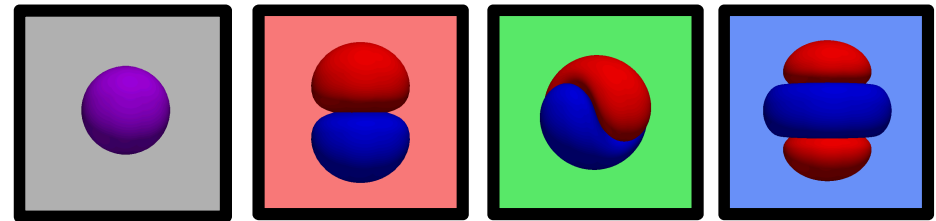
Low χ_s

High χ_s



- High chain entropy
- Low enthalpy

- Low chain entropy
- High enthalpy

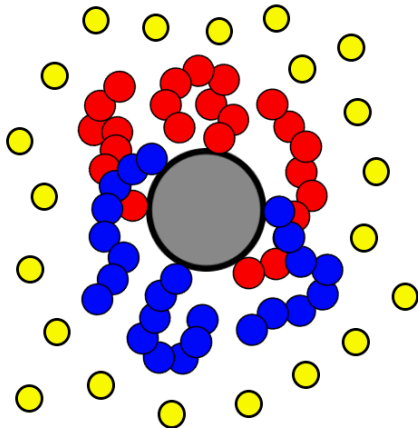
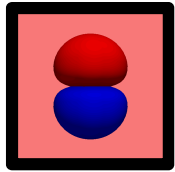


Effect of grafting density

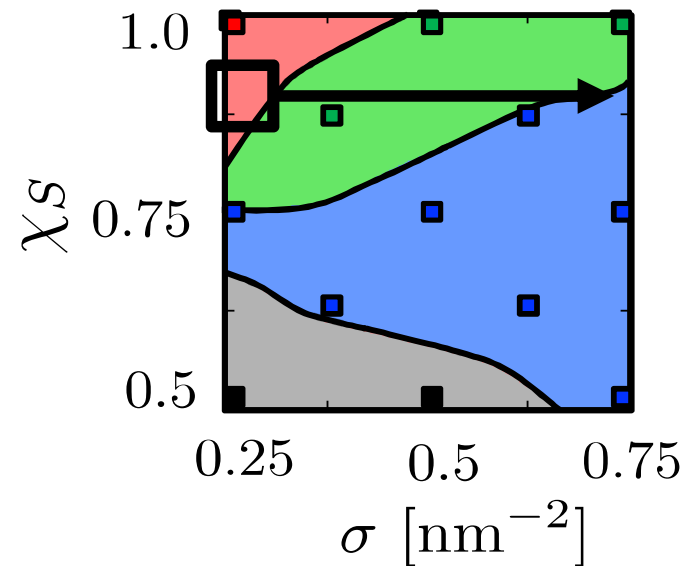
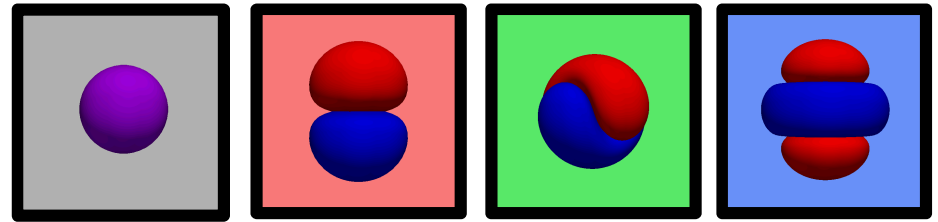
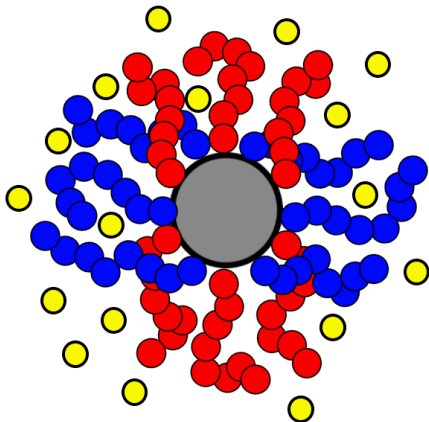
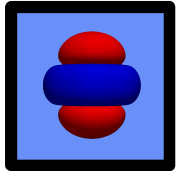
$$\chi_{AB}N = 18.9$$

$$R_P = (2/3)R_g$$

Low σ

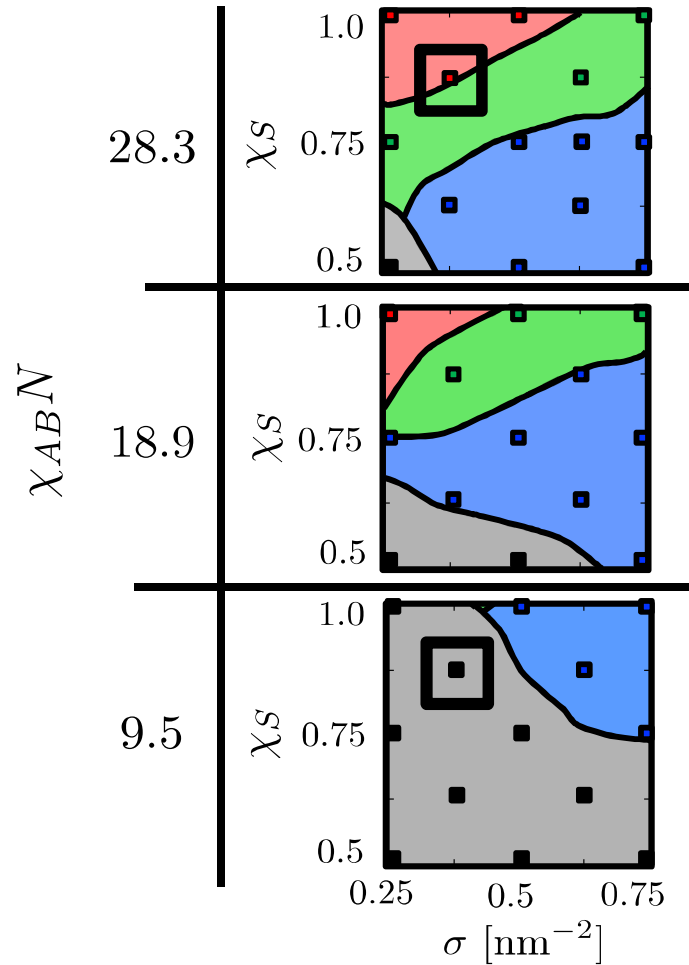
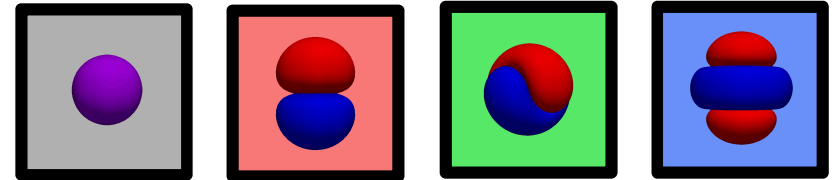
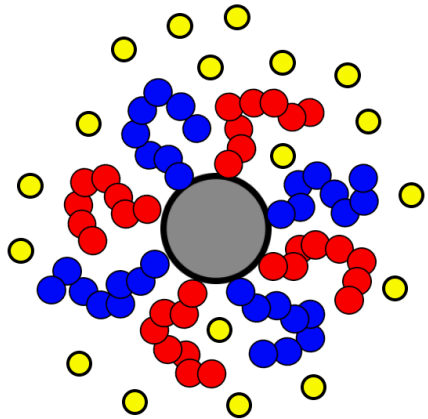
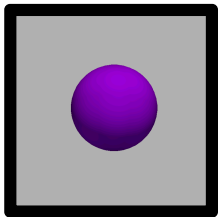
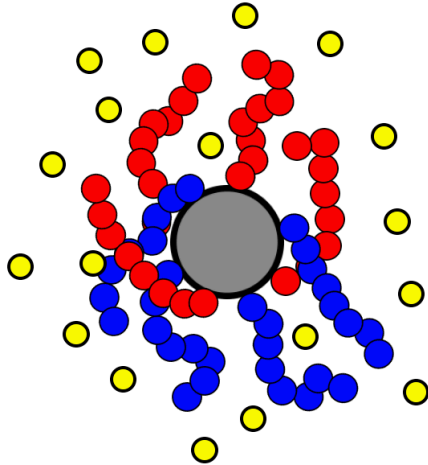
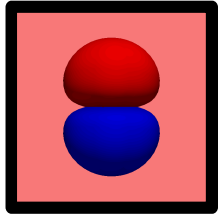


High σ



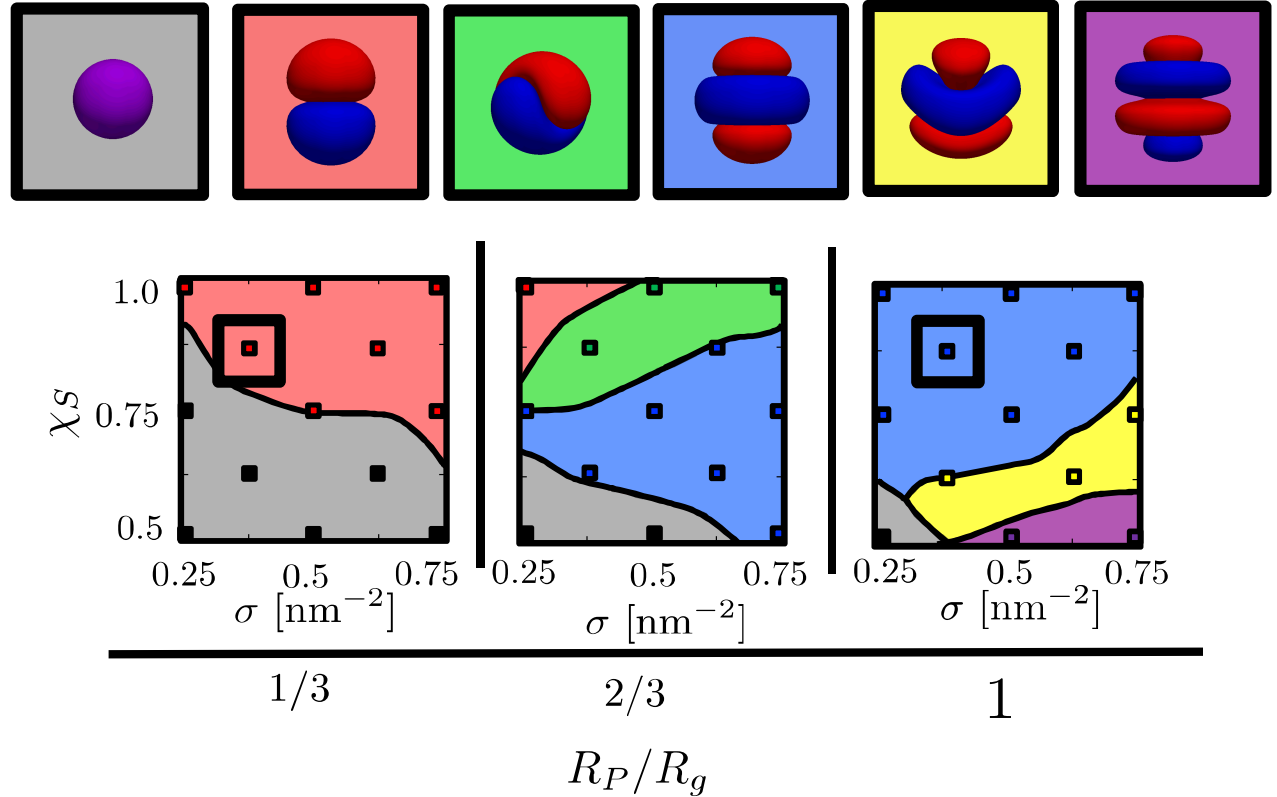
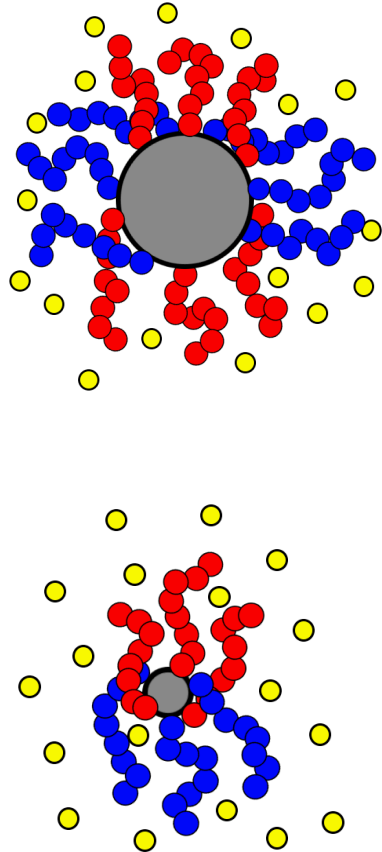
Effect of enthalpic repulsion

$$R_P = (2/3)R_g$$

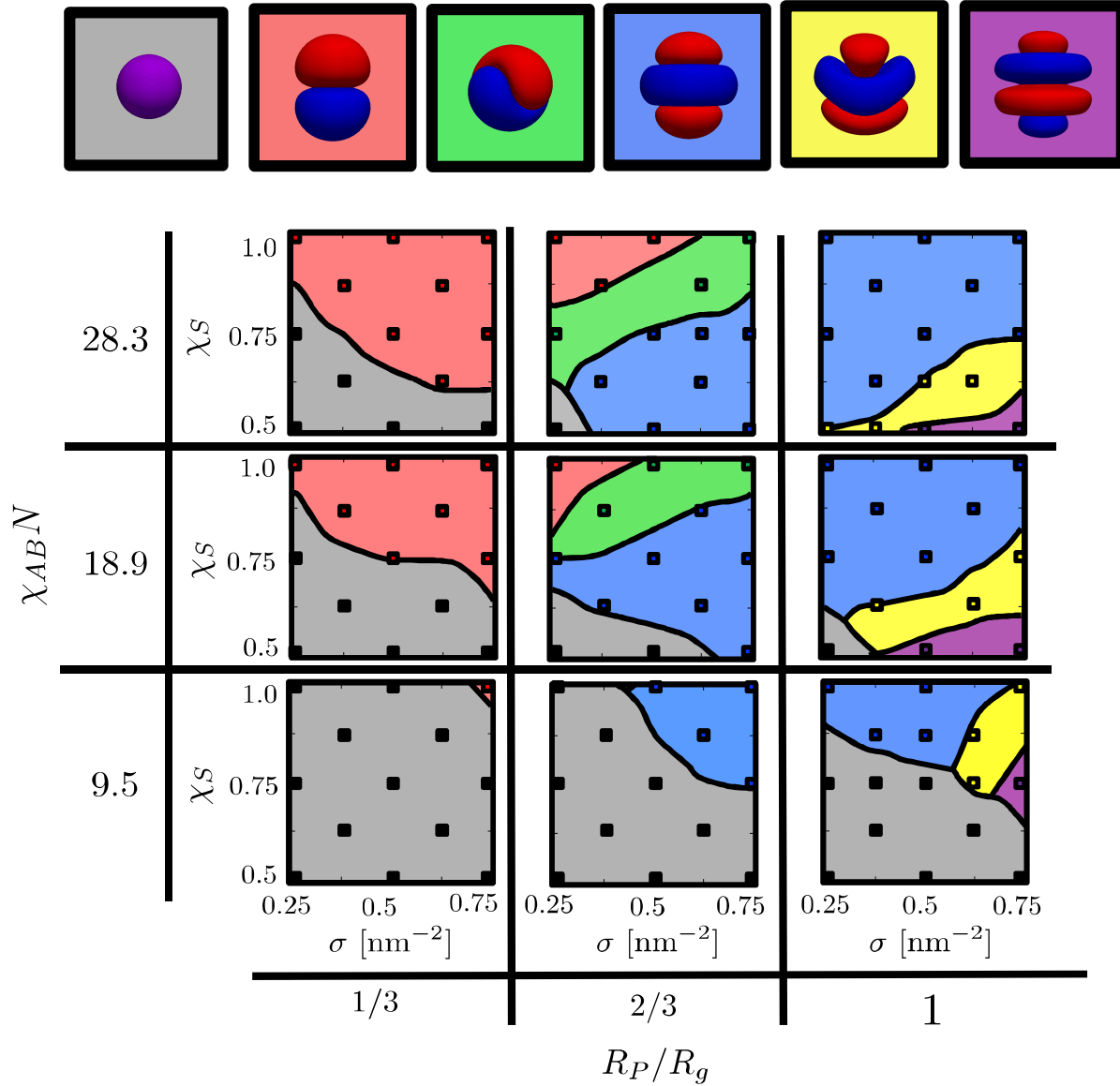


Effect of nanoparticle size

$$\chi_{AB}N = 18.9$$

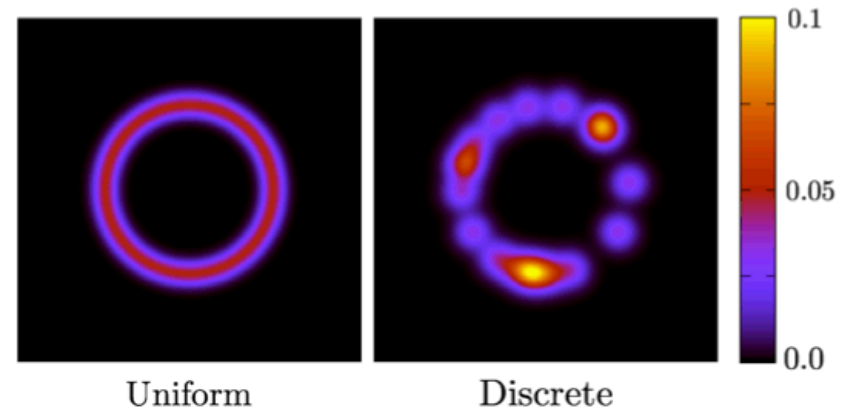


Full phase SCF diagram

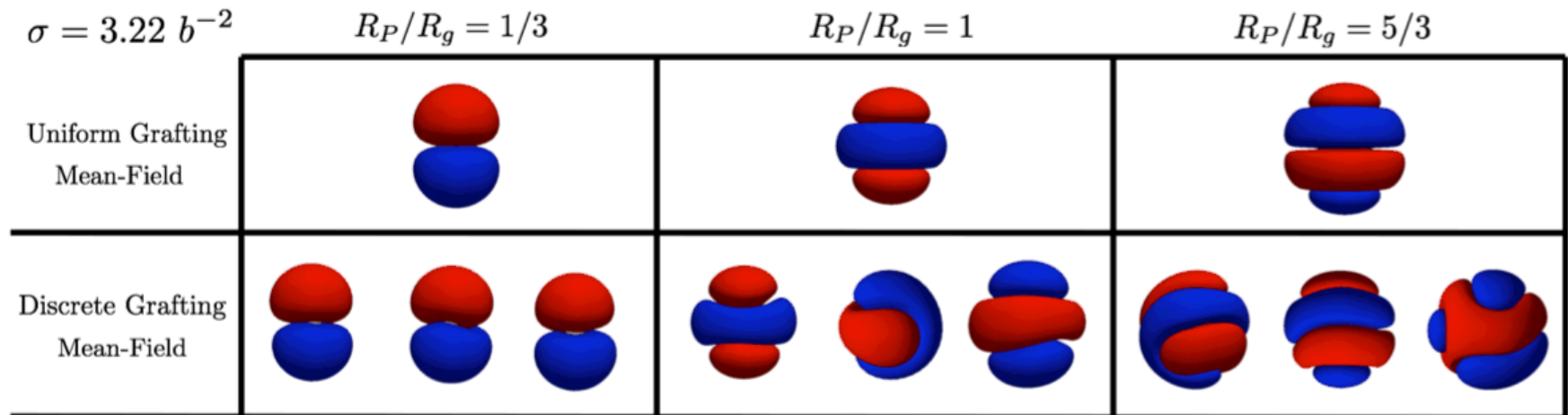


Fluctuation effects

uniform grafting is unlikely
allow discrete grafting



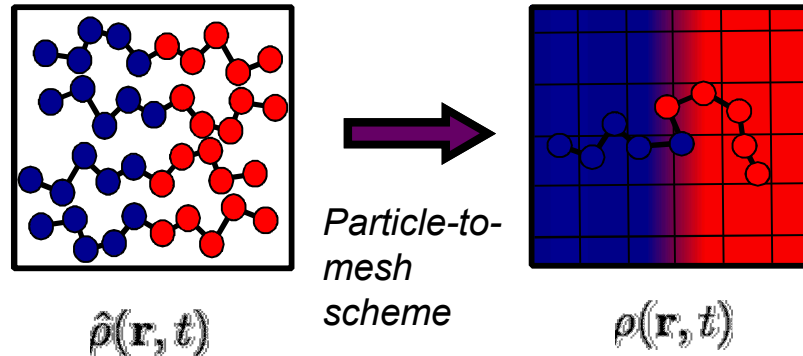
SCF structures less ordered



Dynamic Mean Field Theory

$$\mathcal{Z} = \prod_i^n \int \mathcal{D}r_i(t)$$

Rouse dynamics



Explicit access to
particle positions

Efficient calculation of
non-bonded forces

- Lose direct access to free energy
- Computationally expensive relative to SCFT
- Includes thermal fluctuations
- Includes randomness in grafting density

Fredrickson, Orland, *J. Chem. Phys.* 2014

Chao, Koski, Riggleman, *Soft Matter*, 2014

Thermal fluctuations

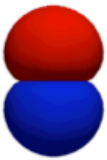




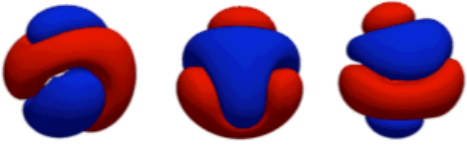


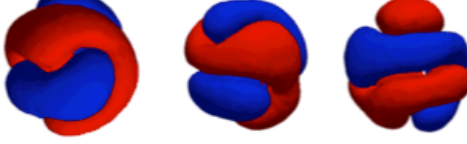
particularly important in solvent

$$\sigma = 1.07 \, b^{-2}$$

$$R_P/R_g = 1/3$$






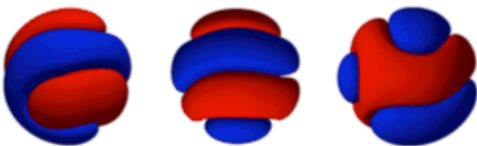
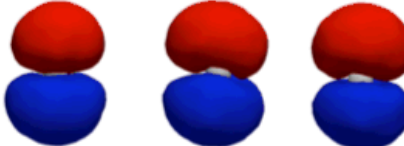
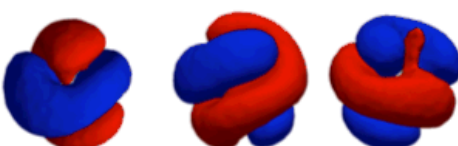

$$R_P/R_g = 1$$

$$R_P/R_g = 5/3$$

Uniform Grafting Mean-Field			
Discrete Grafting Mean-Field			
Discrete Grafting Fluctuations			

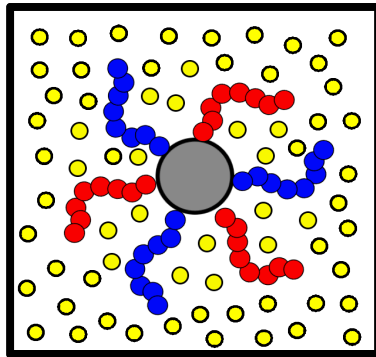
Thermal fluctuations

particularly important in solvent

$\sigma = 3.22 \, b^{-2}$	$R_P/R_g = 1/3$	$R_P/R_g = 1$	$R_P/R_g = 5/3$
Uniform Grafting Mean-Field			
Discrete Grafting Mean-Field			
Discrete Grafting Fluctuations			

prediction: Janus phase robust to fluctuations!

Mixed brush particle assembly



Yellow: Solvent
Red: "Hates Solvent"
Blue: "Loves Solvent"
Silver: Neutral Particle

DMFT calculations

80 nanoparticles in a box

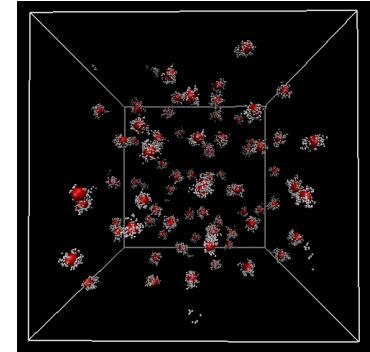
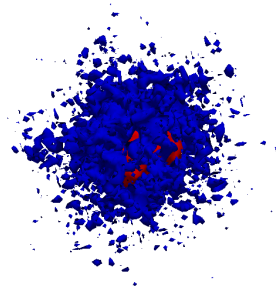
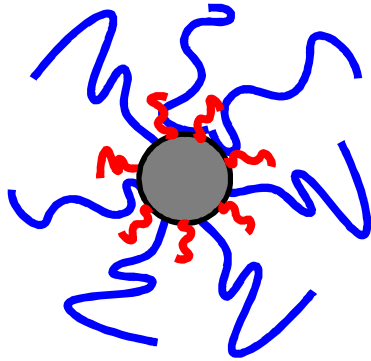
$$R_p = 2b$$

$$\sigma = 1 \text{ chain}/b^2$$

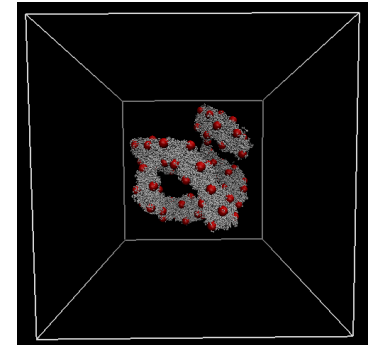
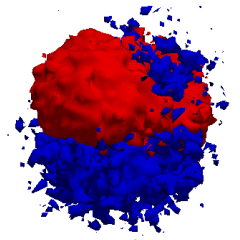
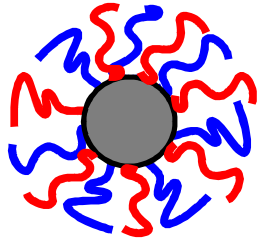
Mixed brush assembly, $f = 0.5$

Long
'Loves Solvent'

Short
'Hates Solvent'

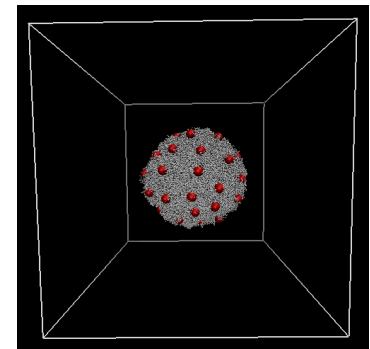
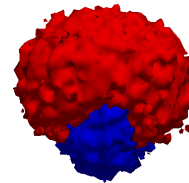
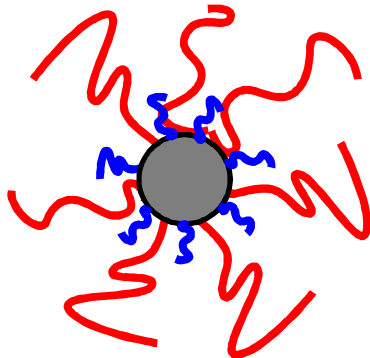


Equal Size
'Loves Solvent'
and
'Hates Solvent'



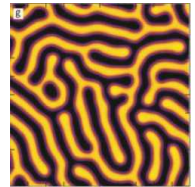
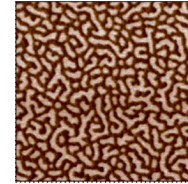
Long
'Hates Solvent'

Short
'Loves Solvent'

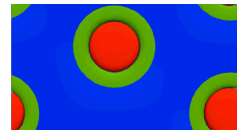
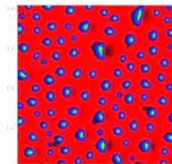


Conclusions

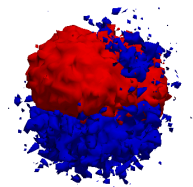
- binary melt brushes
 - SCFT phase diagram in good agreement with experiment
 - excellent lateral phase sep.
 - long-range order hindered by random grafting distributions



- ternary melt brushes
 - range of phase behavior with many laterally phase-separated patterns
 - all phase behaviors observed experimentally were observed in simulations

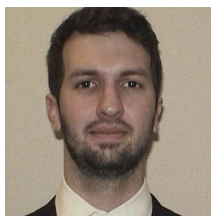
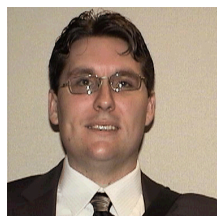
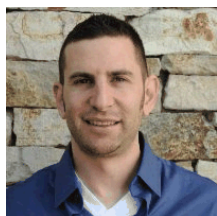


- mixed brush particles
 - Janus phase robust to fluctuations
 - interesting self-assembly

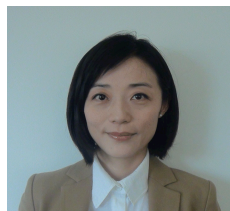


often must include fluctuations in modeling!

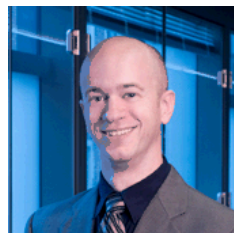
Acknowledgments



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Sandia National Labs



Glenn Fredrickson, Su-Mi Hur
UC Santa Barbara



Rob Riggelman, Russ Composto
U Penn



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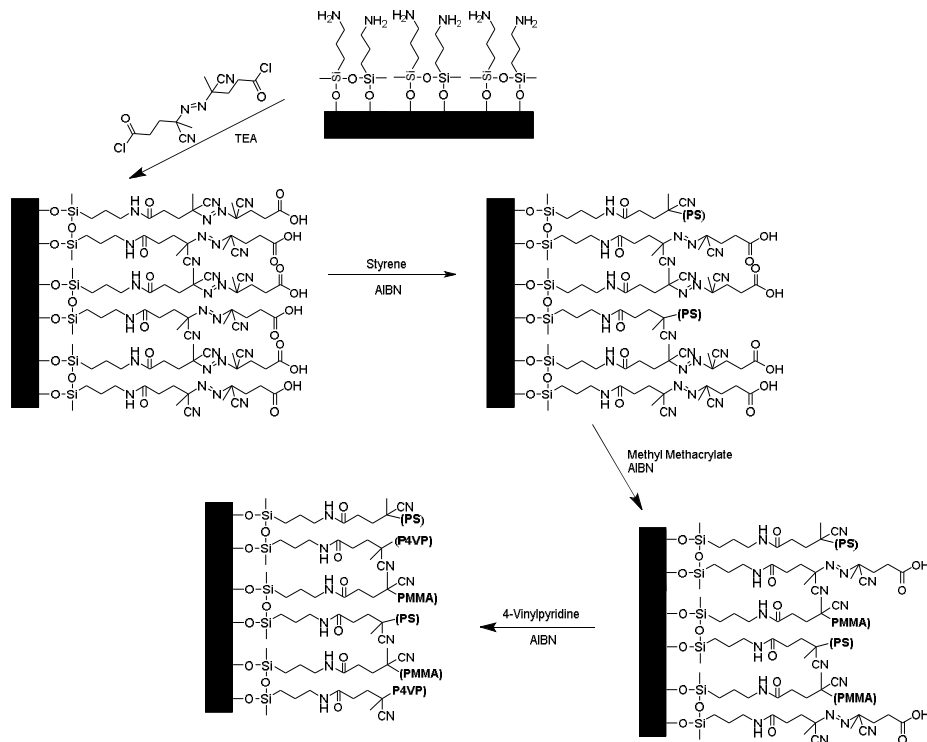


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Backup

Surface Initiated Growth

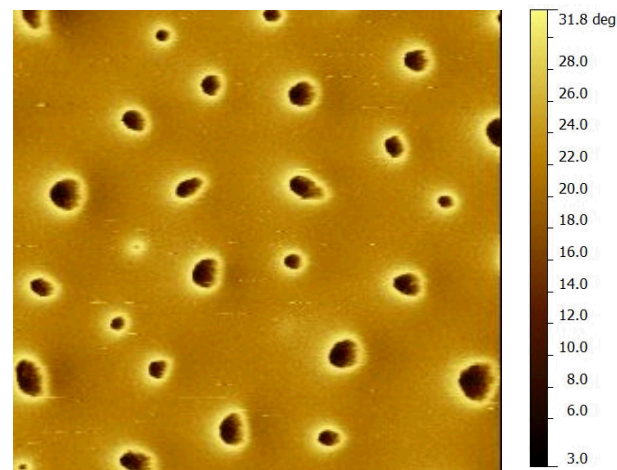


M_n : 56 – 130 kDa

brush thicknesses: 2.6 – 6 R_g

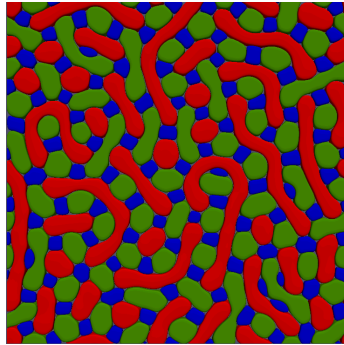
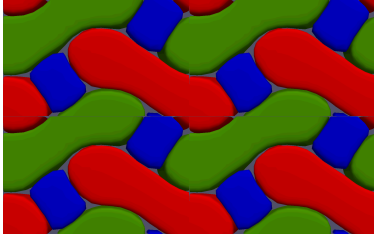
grafting density: 0.14 – 0.44 chains/nm²

AFM phase contrast

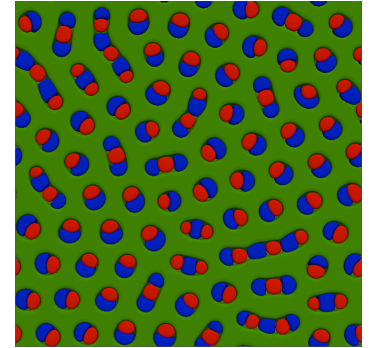
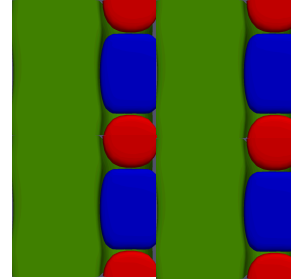


Results from fast quenches

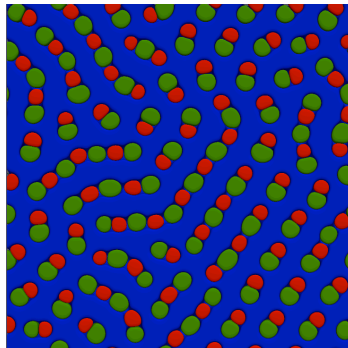
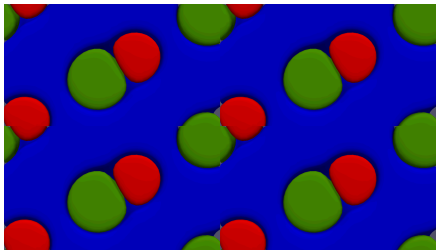
basketweave



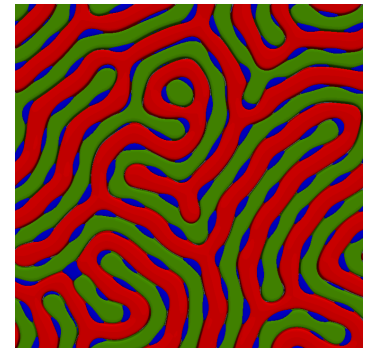
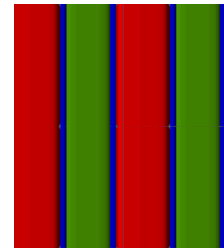
segmented ripple



lobed cylinder

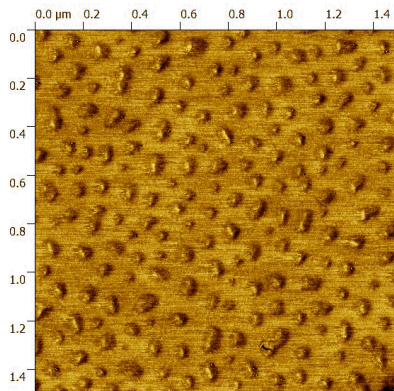
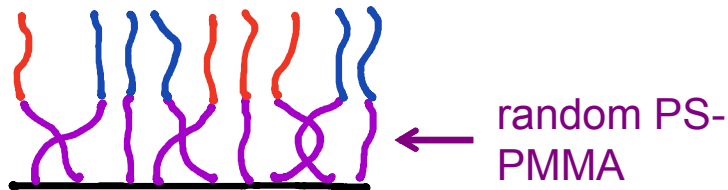


decorated ripple

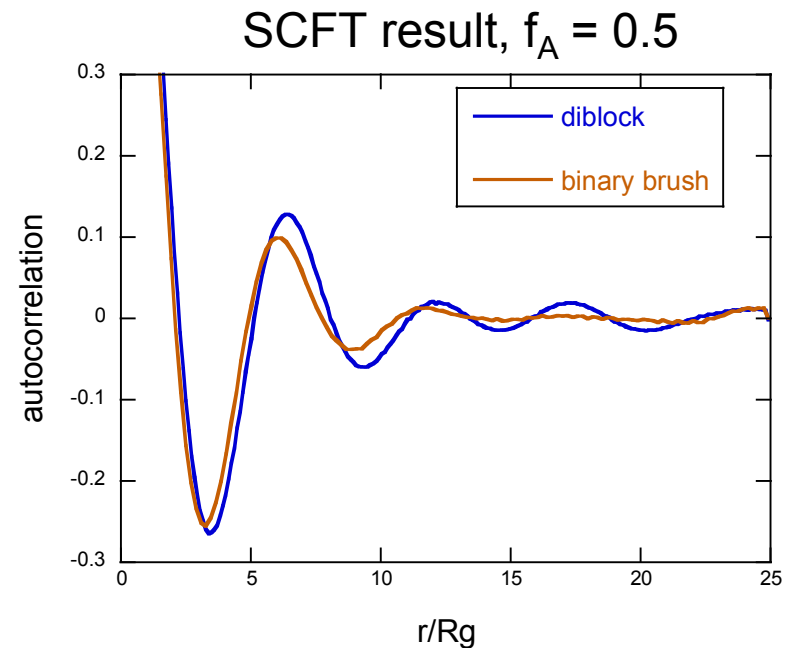


Summary of binary mixed brushes

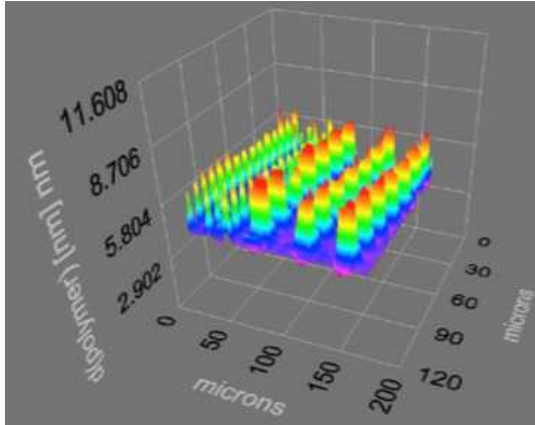
- in ideal case, directed assembly works for mixed brushes
- spatial variations in grafting prevent long-range order
- ideas for improved long-range order
 - better annealing methods for graphoepitaxy
 - random diblock copolymers to relax grafting correlations



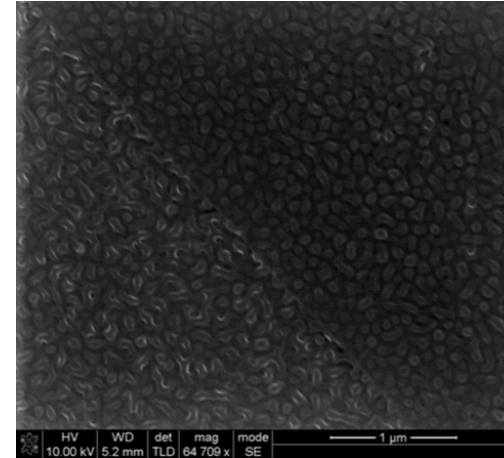
12% PS-
88% PMMA



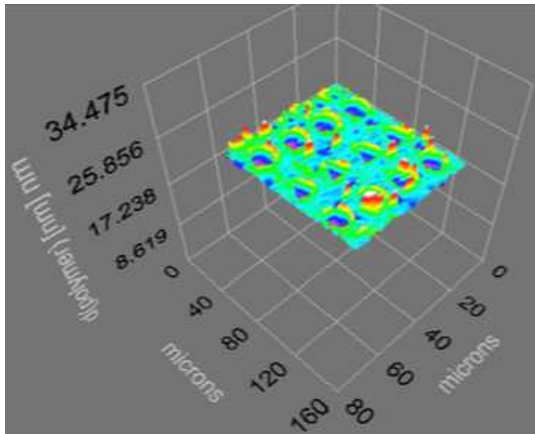
DSA attempts



patterned PMMA brushes



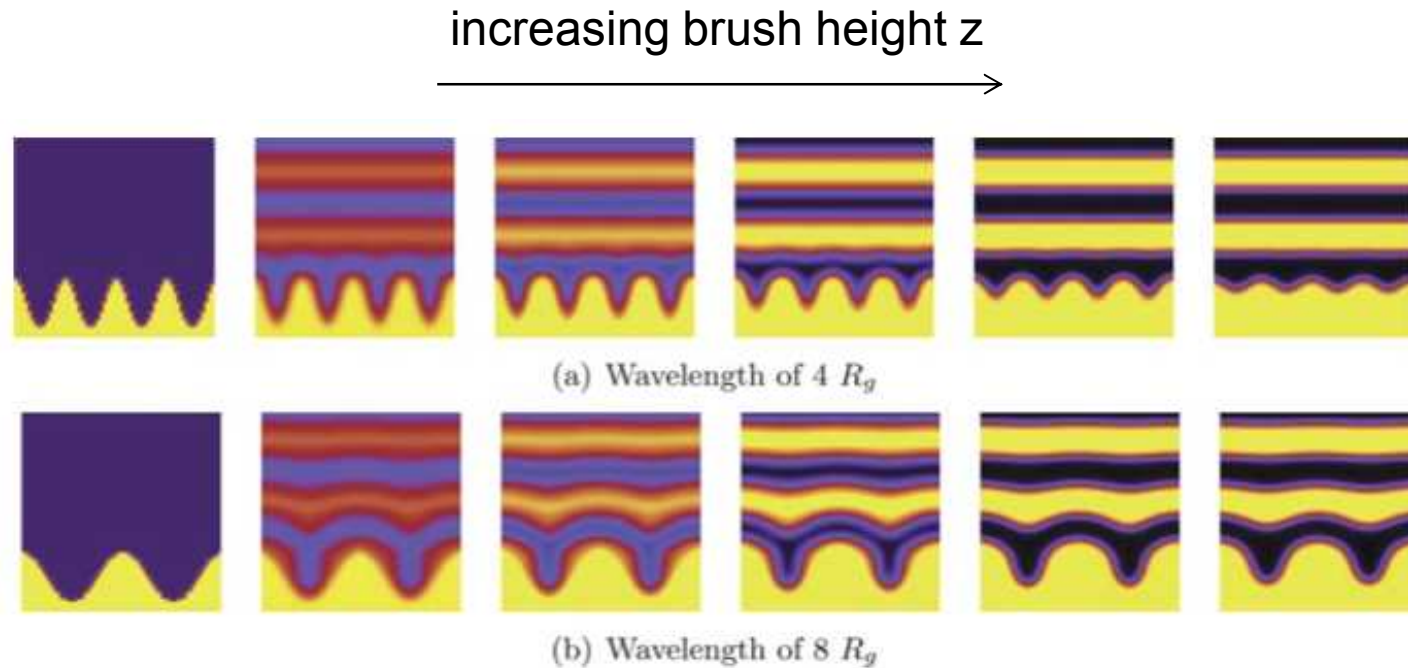
55%PMMA-45%PS next to
75% PMMA-25%PS



mixed PMMA-PS brushes

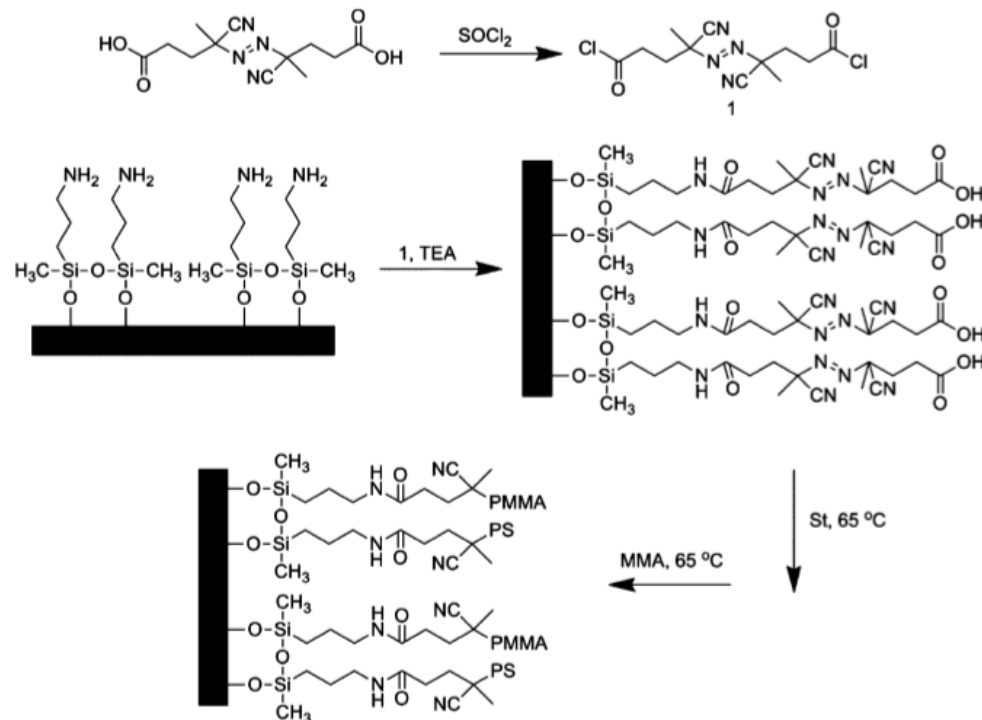
“pure” region is $\approx 15\%$
PMMA due to chain transfer

Line Edge Roughness in SCFT



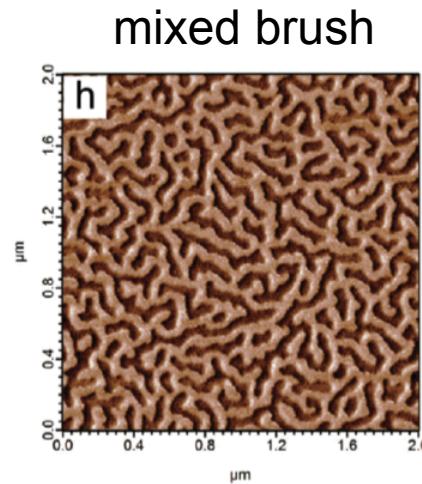
mixed brush maintains long-range order
better than block copolymer films

Synthesis of Mixed Brushes

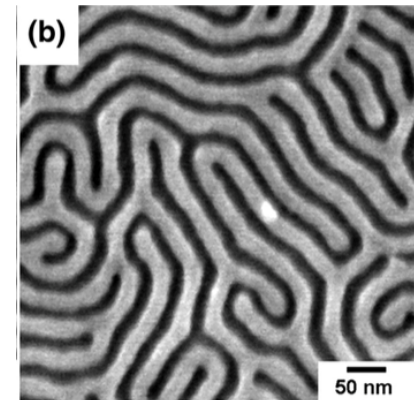


Mixed Brushes for Lithography?

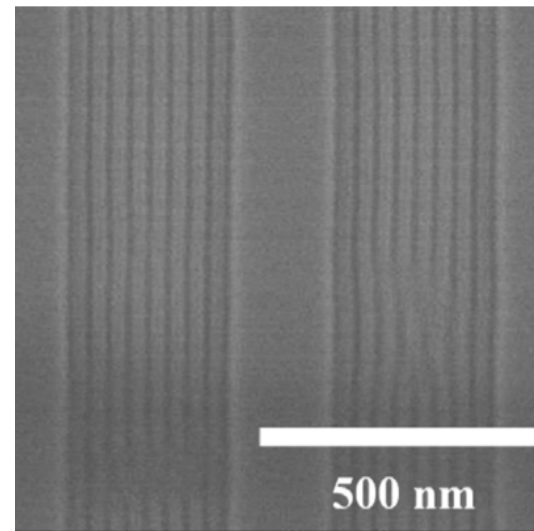
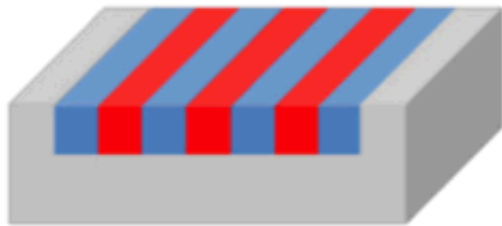
lateral phase separation
in PS-PMMA



block copolymer



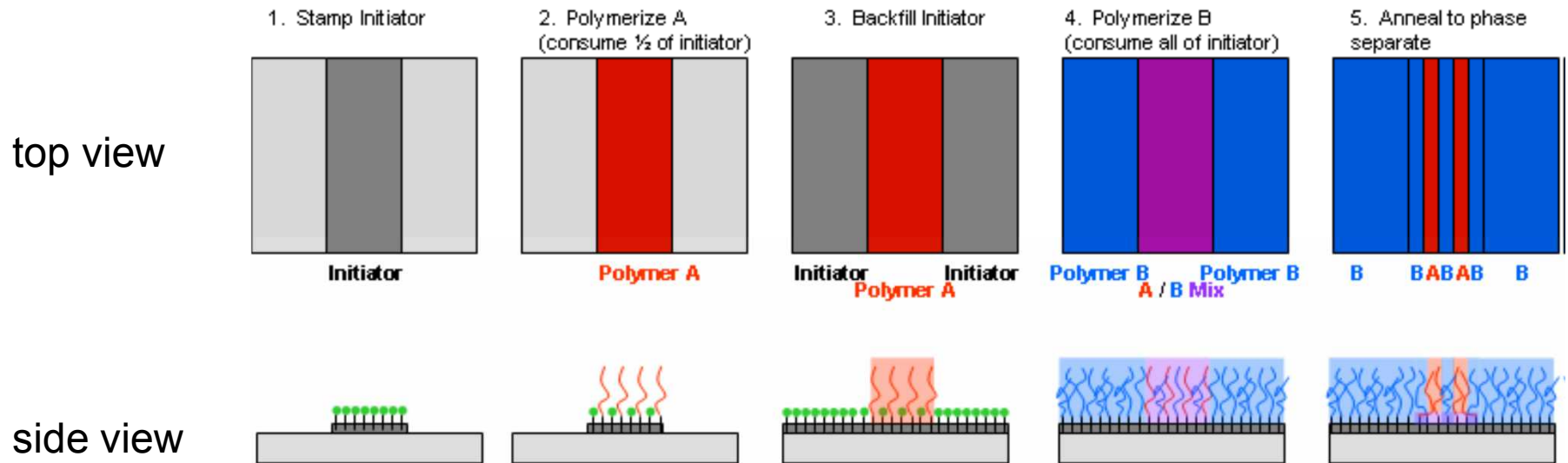
alignment by graphoepitaxy in
block copolymer thin films



Mixed brushes vs BCP thin films

- block copolymer thin films
 - advantages
 - 25+ years of research and development
 - use beginning in semiconductor industry for lines, vias (hole shrink)
 - disadvantages
 - spin-casting limited to planar surfaces
 - difficult to turn sharp corners, make square patterns
- polymer brushes
 - advantages
 - could be made on any substrate, i.e. non-planar
 - chip-relevant architectures (e.g. 90 degree turns)
 - multiple patterns on same chip
 - potentially cheaper synthesis than BCP's; fast annealing
 - disadvantages
 - research still at early stages
 - more defects

Nanolithography using Directed Self-Assembly



first: calculate phase diagram for melt mixed brush

D. L. Huber and A. Frischknecht. Nanopatterns by phase separation of patterned mixed polymer monolayers. US Patent 8652768 B1, February 18, 2014.

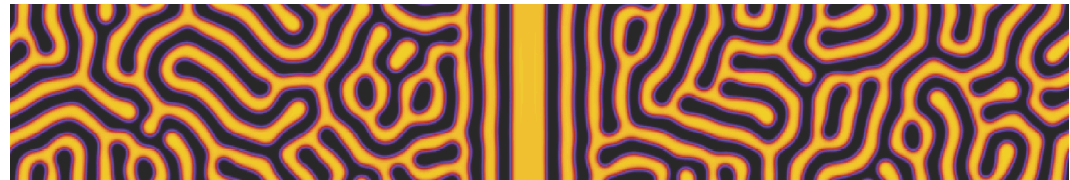
Does lithography idea work?

bulk,
quenched

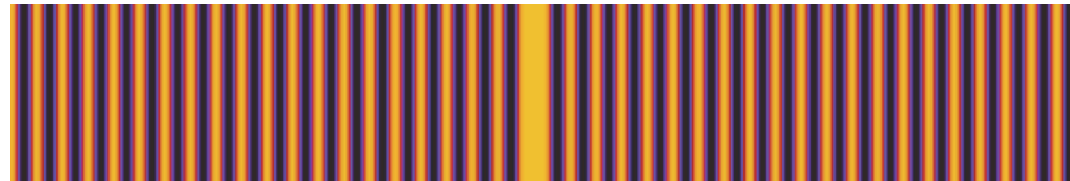


↓ pure A region

patterned,
quenched



patterned,
slowly annealed



➡ get long range ordered ripple phase in simulation

Directed Assembly

aligned cylinder phase



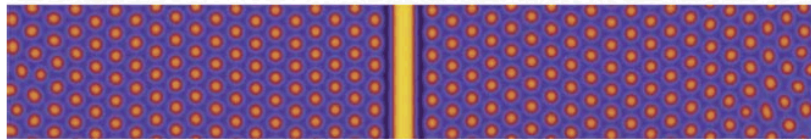
(a)



(b)



(c)



(d)

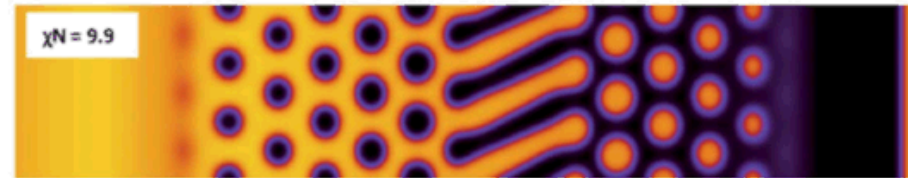
linear ramp in grafting density



A-rich domain

B-rich domain

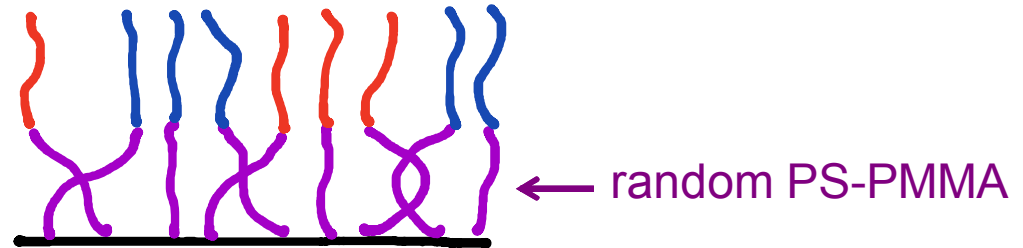
Increasing B homopolymer fraction



different shape features in one system

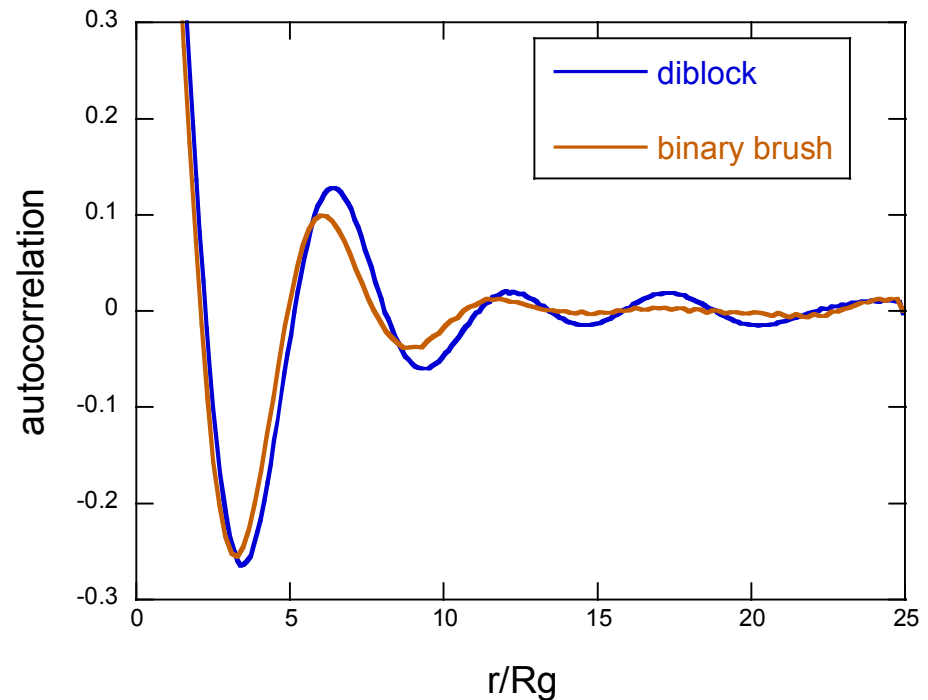
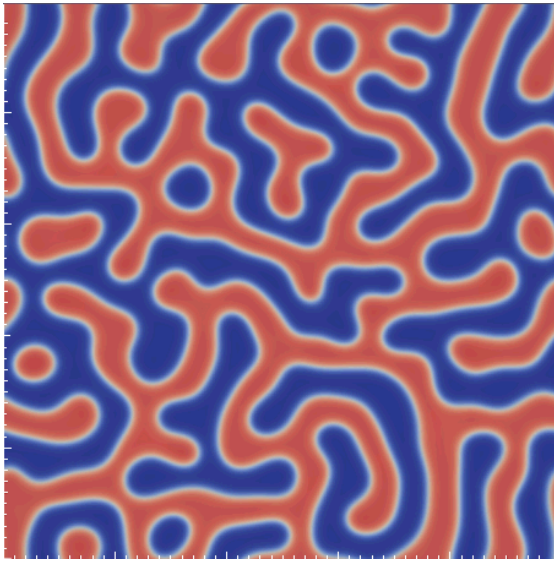
Improve order with diblocks?

diblock mixed brush?

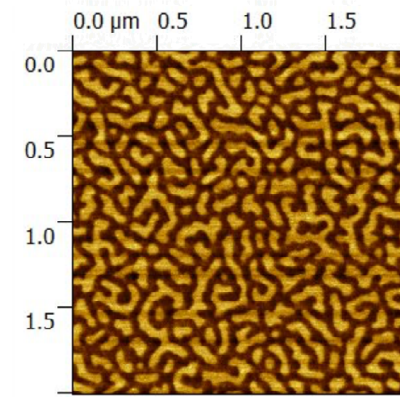
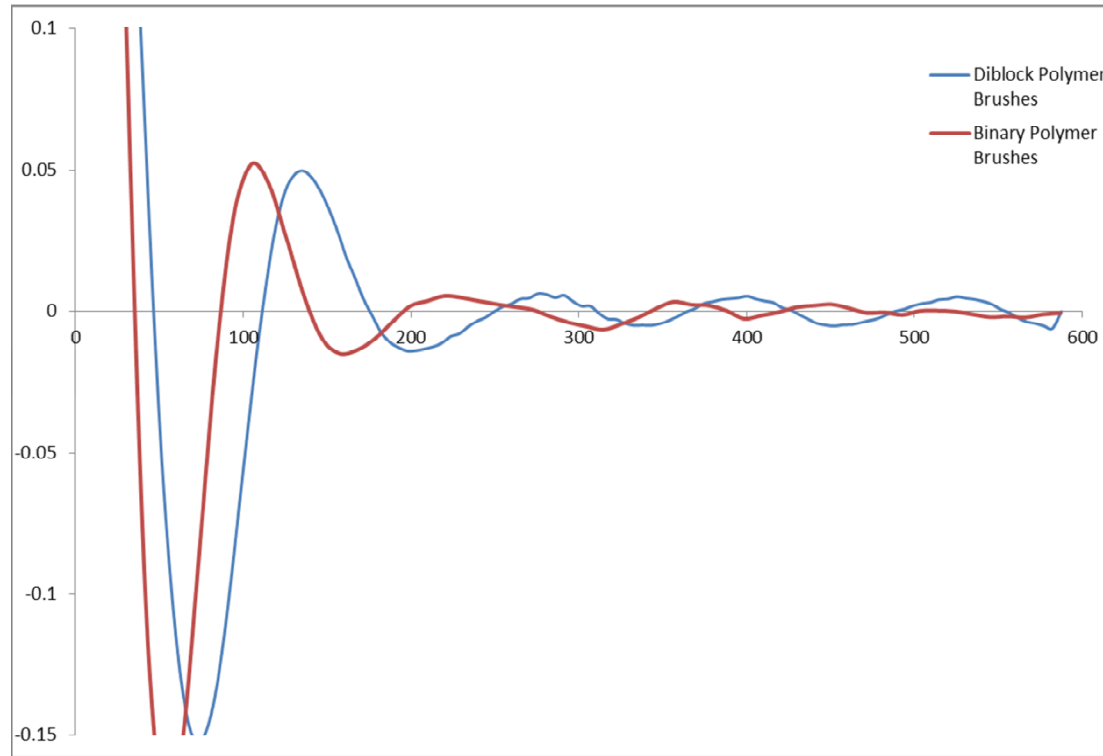


50% random copolymer, $f_{\text{PS}} = 0.5$

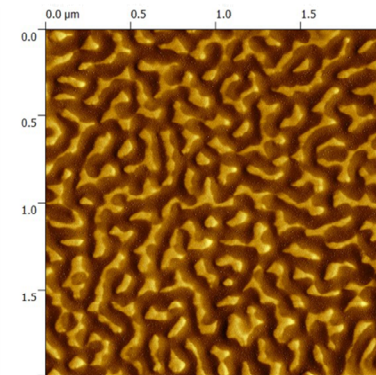
$\chi N = 16$ $\sigma = 0.5R_g$, $\Lambda^2 = 0.02$



Experimental results



binary brush



diblock
binary brush

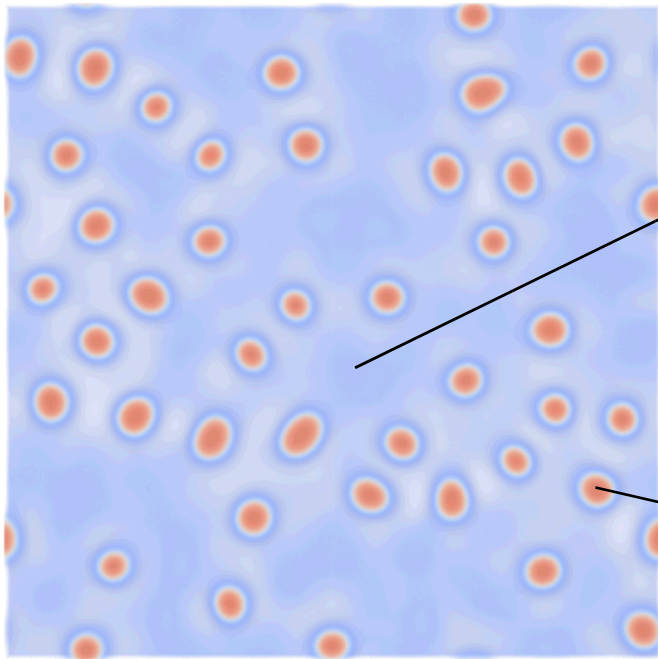
slightly more long range order

Diblock Mixed Brush

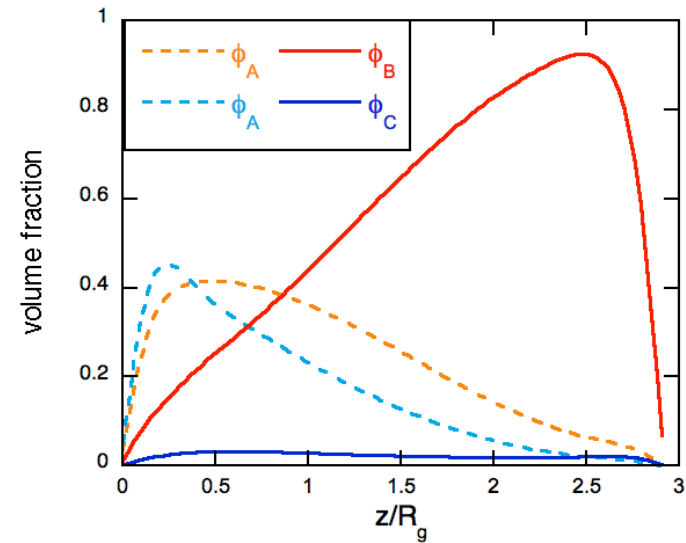
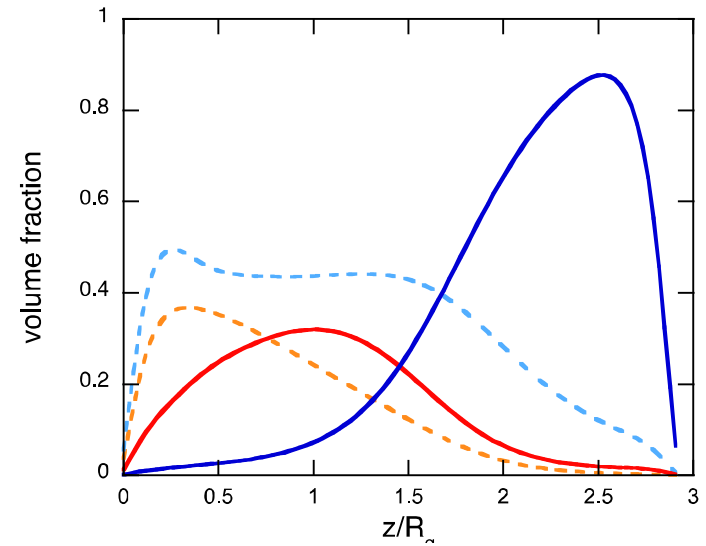
strong tendency to vertically phase separate

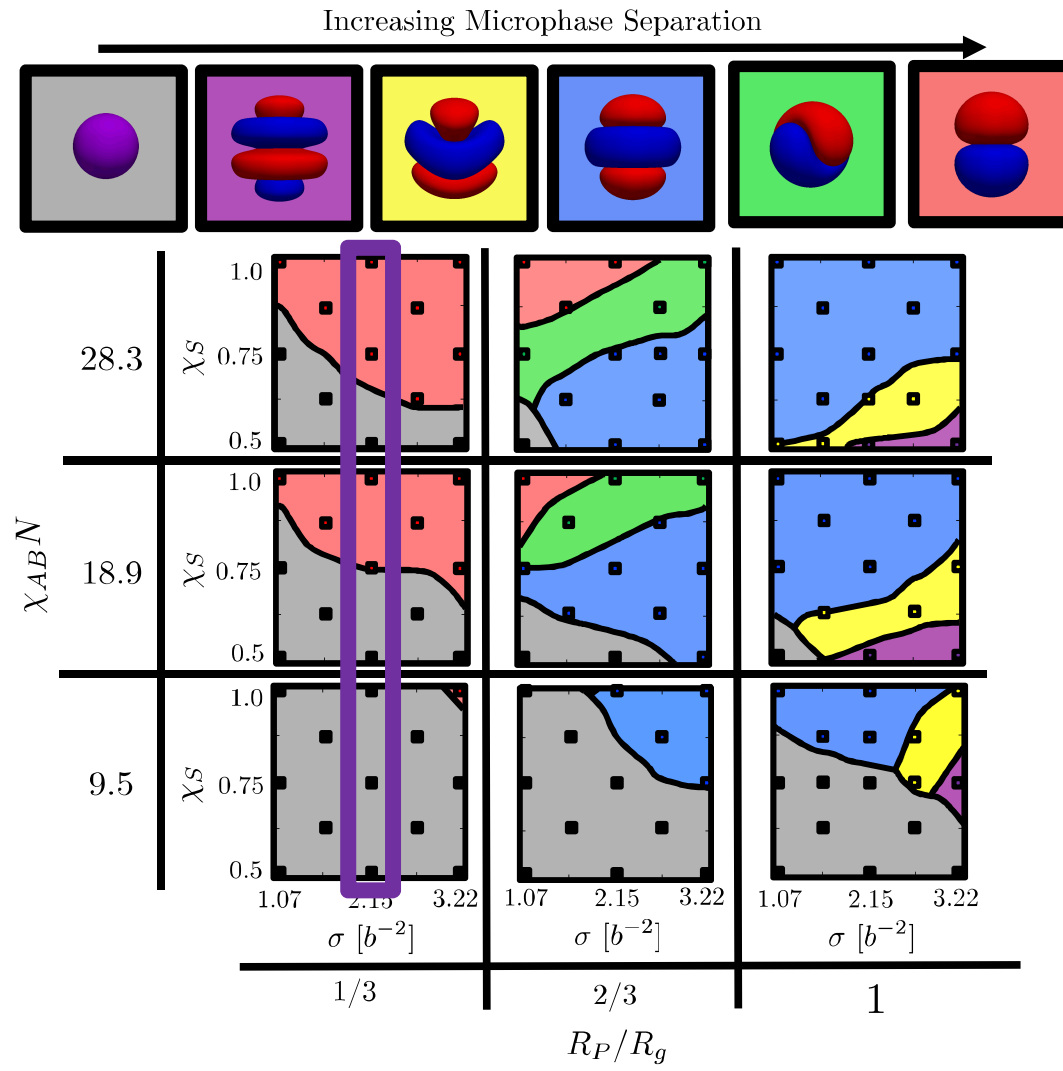
50% copolymer, $f_{PS} = 0.3$

$\chi N = 16$



$\sigma = 0.5R_g$, $\Lambda^2 = 0.02$

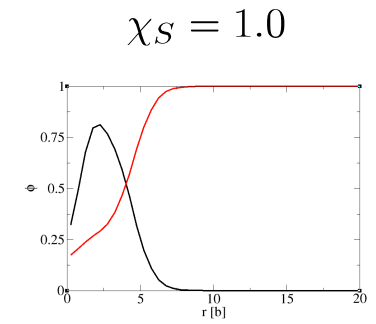
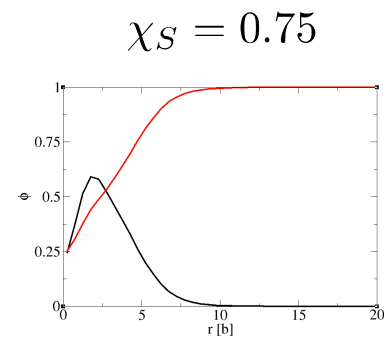
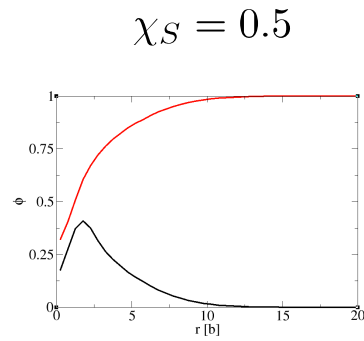




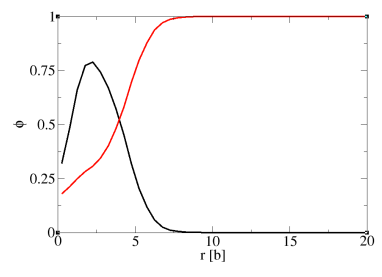
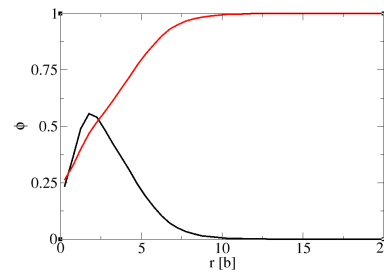
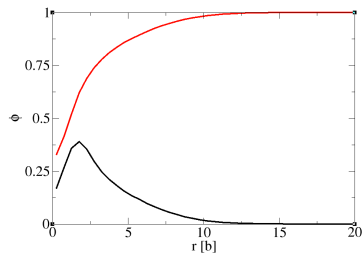
$$\sigma = 2.15 \, b^{-2}$$

$$R_P/R_g = 1/3$$

$$\chi_{AB}N = 9.5$$



$$\chi_{AB}N = 18.9$$



$$\chi_{AB}N = 28.3$$

