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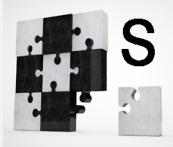
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# PRACTICAL PERIDYNAMIC MODELING FOR DAMAGE AND FAILURE PREDICTION

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 **Sandia National Laboratories**



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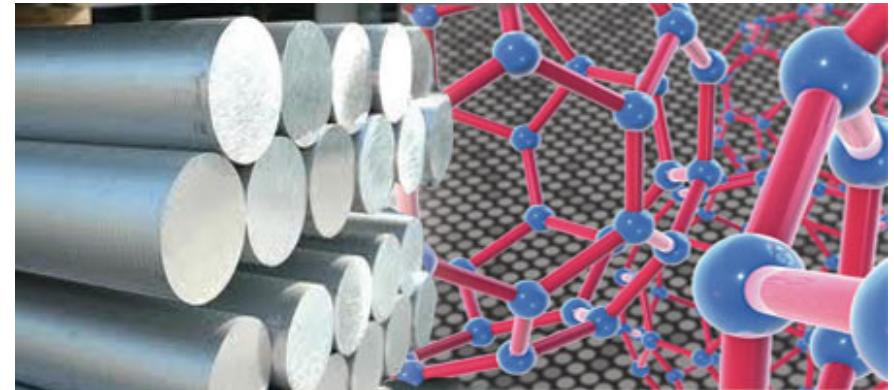
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# PROBLEM

- Predictive analysis of material damage and failure is a critical challenge in several industries (e.g., aerospace, automotive, medical devices, design, fashion and jewelry)
- Existing computer-aided engineering software based on the Finite Element Method (FEM) have received widespread acceptance for macroscale materials and traditional manufacturing processes
- Such software must deal with ambiguity of derivatives of displacement at discontinuities
- Damage models in existing software impose requirements on mesh size



- New materials damage analysis is critically needed for products of additive manufacturing which comprise 3-D heterogeneities and discontinuities (e.g., composites, porous metals/alloys)



# SOLUTION: COMMERCIALIZE PERIDYNAMICS

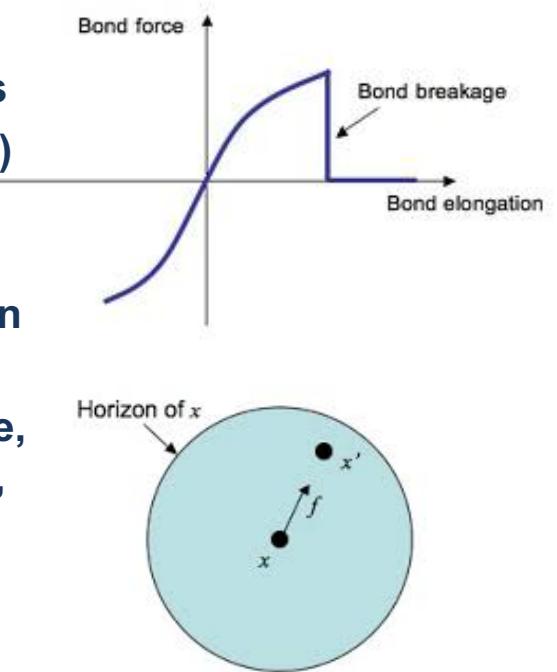


- Stewart Silling

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- Peridynamic theory originated at Sandia is based on direct interactions between points
- The maximum interaction distance (horizon) provides a length scale for the material model
- Peridynamics use displacements rather than displacement derivatives
- Peridynamic equations are valid everywhere, including discontinuities (e.g., voids, pores, pre-cracks)
- Peridynamic tensor converges to a Piola-Kirchhoff stress tensor when horizon  $\rightarrow 0$



# PERIDIGM

- Sunergolab Inc. in collaboration with Sandia National Laboratories commercialize the Peridigm peridynamic software
- Peridigm (<https://github.com/peridigm/Peridigm>) is an open-source, highly efficient, massively-parallel C++ simulation code for solving 3-D problems in structural mechanics and material failure
- Peridigm heavily leverages Sandia's Trilinos software project (e.g., parallel data structures, solvers, automatic differentiation package, I/O)
- Wide adoption of Peridigm is limited by
  - Lack of integration with commercial software
  - Difficulties with installation and use
  - Differences in the discretization process, selection of model parameters, and application of initial and boundary conditions from standard approaches
  - Computational cost



<https://peridigm.sandia.gov/>



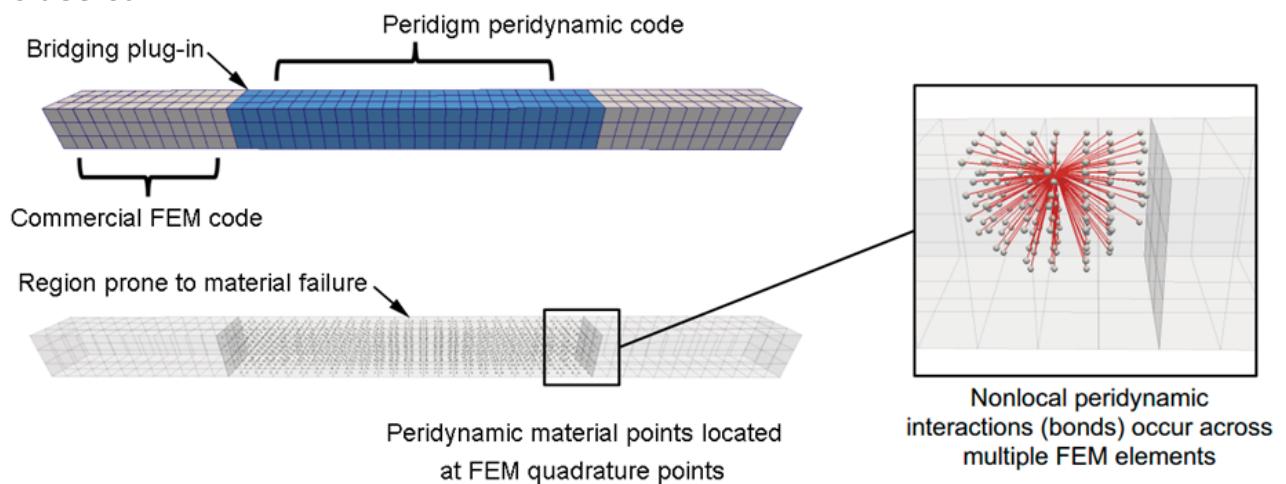
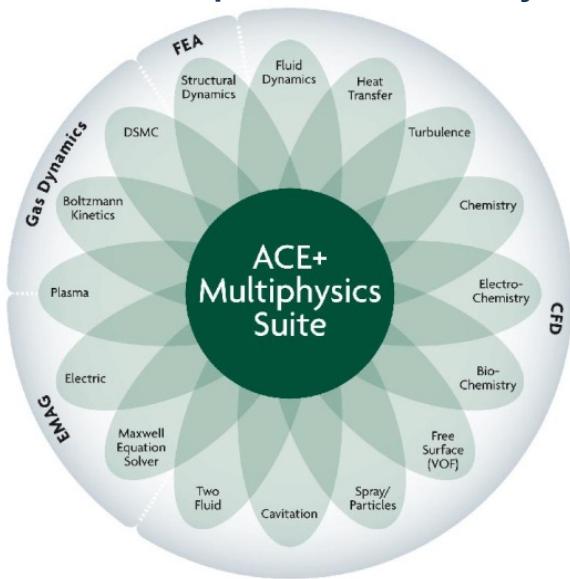
# CURRENT USE OF PERIDYNAMICS IN INDUSTRY

- Peridynamic model called PDIFEA (Peridynamics Implemented Finite Element Analysis) was implemented in ABAQUS
- A few small-businesses pursue peridynamic approach:
  - 1) Global Engineering Research and Technologies, <http://www.gertinnovation.com/>, commercializing university's code
  - 2) Technical Data Analysis, Inc. (TDA), <http://www.tda-i.com/>, focusing on providing solutions using peridynamics to extend the useful life of aircraft
  - 3) Advanced Cooling Technologies, Inc., <http://www.1-act.com/>, develops thermal protection materials with peridynamic analysis
- Existence of direct competitors demonstrates the interest of potential customers to peridynamics software and reflects urgency in commercializing Peridigm



# BLENDING PERIDIGM IN FEM SOFTWARE<sup>6</sup>

- Nonlocal-local coupling is currently being investigated as means to embed a peridynamic modeling within a larger ACE+ multi-physics simulation
- Such coupled approach achieves a desirable balance between the high fidelity of the peridynamic model and the computational efficiency of classical FEM



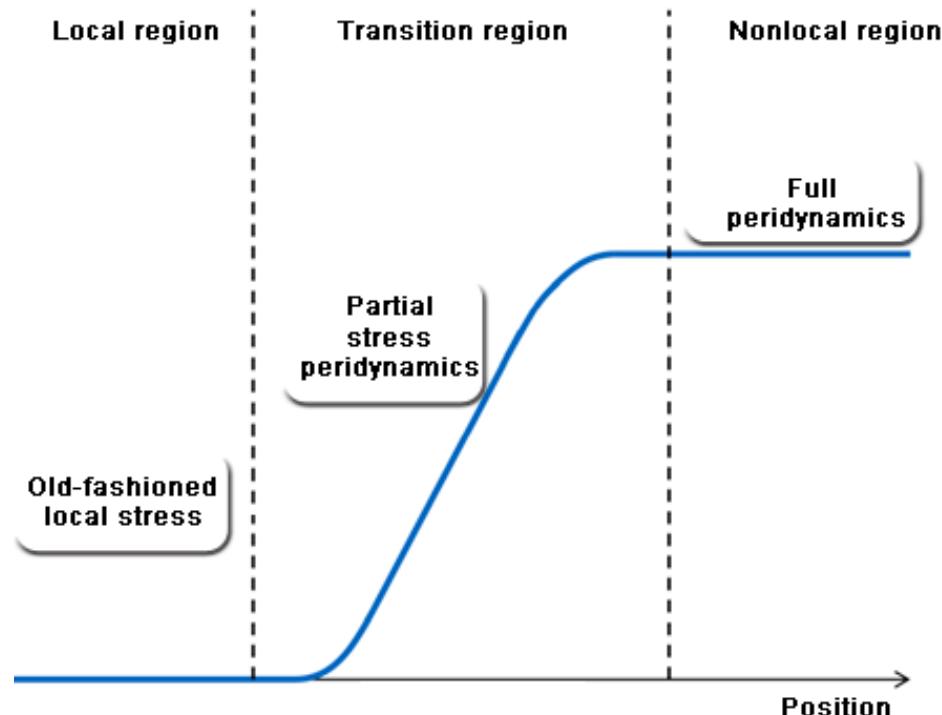
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# LOCAL/NONLOCAL COUPLING

- Fundamental challenge is discrepancy between finite length scale in peridynamics and zero-length scale of FEM
- This challenge was addressed with peridynamic partial stress approach that supports the use of variable horizon
- Here, peridynamic horizon can be reduced in the direct vicinity of the nonlocal-local interface, thus mitigating the discrepancy between local/nonlocal approaches

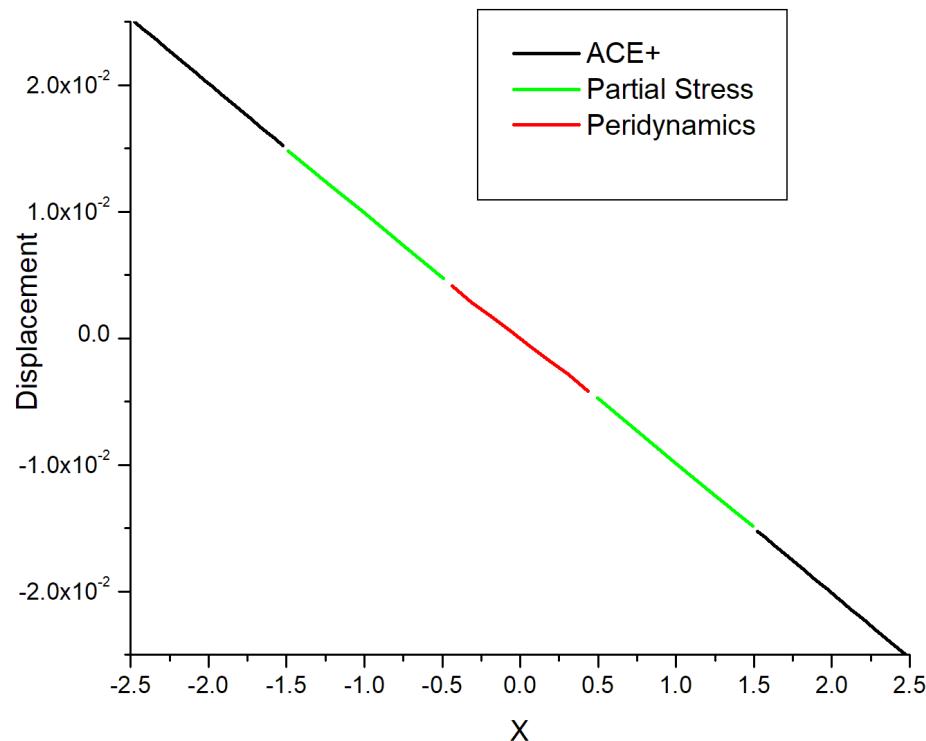


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# PERIDIGM/FEM COUPLING

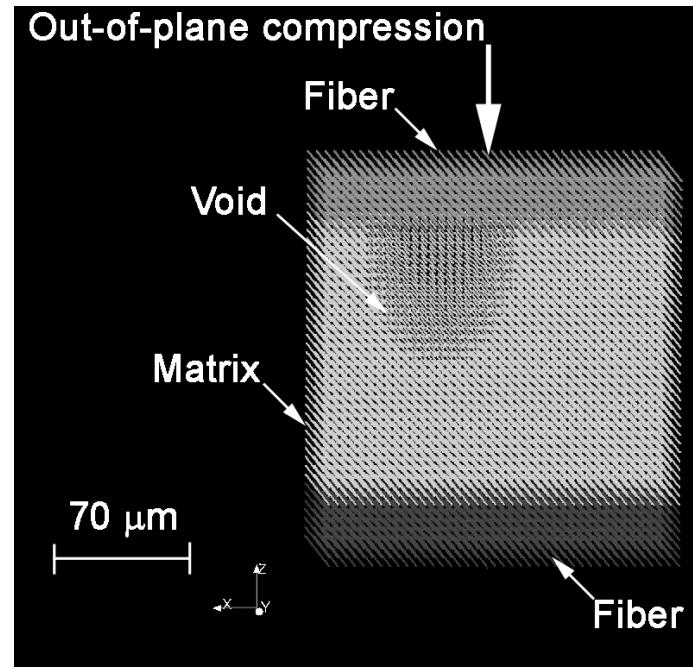


- Coupled ACE+/Peridigm simulation was demonstrated for a bar under tension problem
- A bar was discretized into five domains:
  - Meshfree peridynamics at the center
  - Peridynamic partial stress regions between FEM (ACE+) and meshfree peridynamics domains
  - Classical continuum mechanics regions at the ends of the bar
- Boundary conditions were applied in ACE+ software
- Simulation was performed with a linear elastic material model



# CARBON FIBER-REINFORCED SiC-MATRIX COMPOSITE

- Carbon fiber-reinforced SiC-matrix composite (C/SiC) is a key material for thermal protection in aeronautics and astronautics
- Geometry represents a slice of unidirectional C/SiC, where fibers are aligned along the longitudinal direction
- Time-dependent displacement boundary conditions were prescribed at the top of domain, while the bottom boundary was fixed in transverse direction
- The anisotropic bond-based model was used to model interactions between points in the fiber regions
- A peridynamic plasticity model was used in the matrix region
- The plasticity model includes an explicit dependence on collective effects such as a shear band of plastic nature, which typically develop during severe deformation of the matrix ductile material



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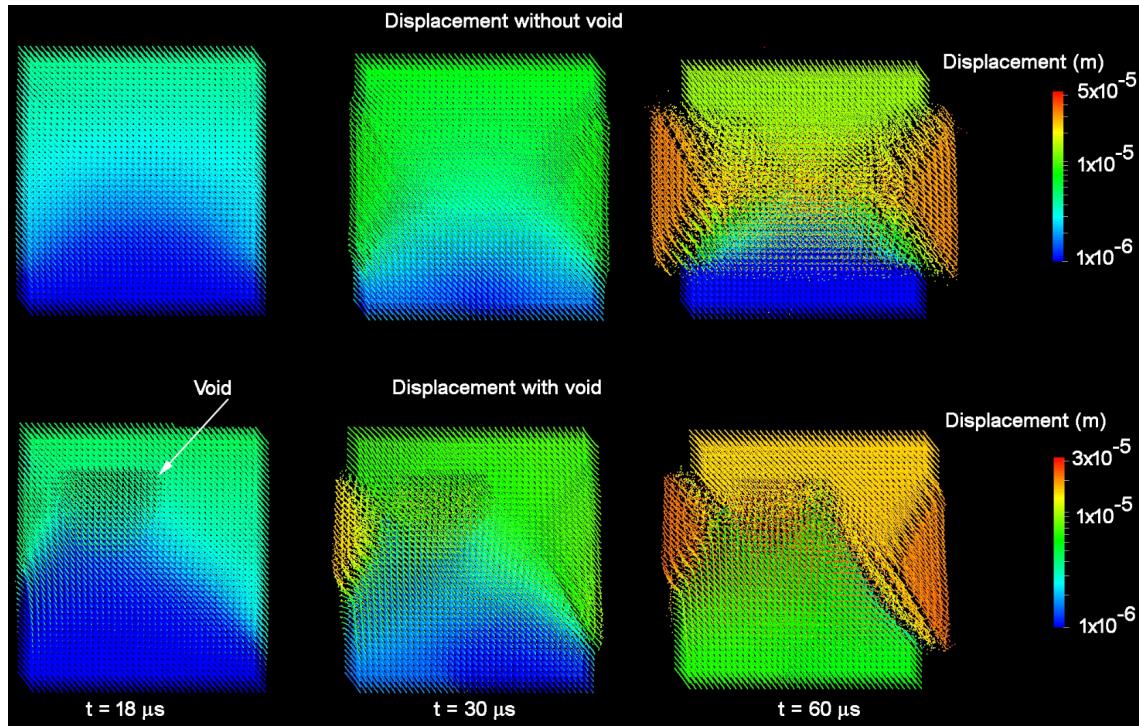


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# OUT-OF-PLANE COMPRESSION LOADING: DISPLACEMENT

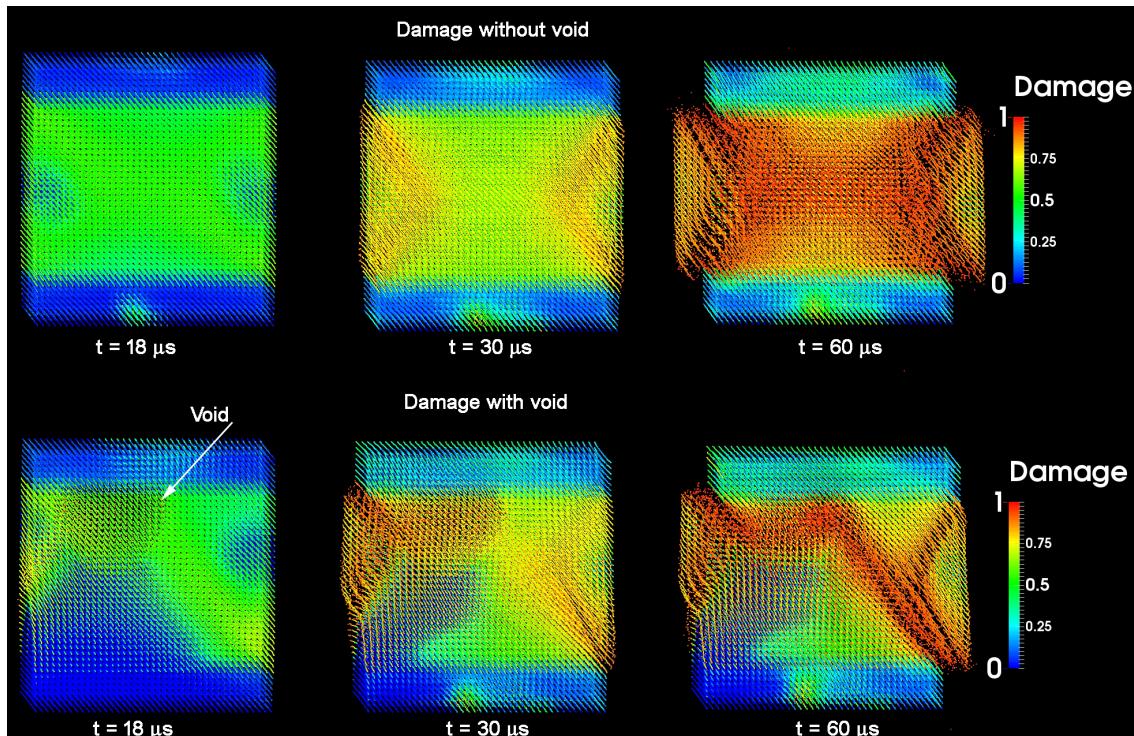
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- At 18  $\mu$ s, displacement peaks near the void due to inhomogeneous deformation
- At 30  $\mu$ s, systems are visibly deformed with a pronounced peak of displacement in matrix in comparison to the fiber regions due to a larger longitudinal elastic modulus in latter
- At 60  $\mu$ s, damage for systems without and with void is clearly pronounced along the peak of shear stress direction that is about 45 degrees relative to the loading direction

# OUT-OF-PLANE COMPRESSION LOADING: DAMAGE

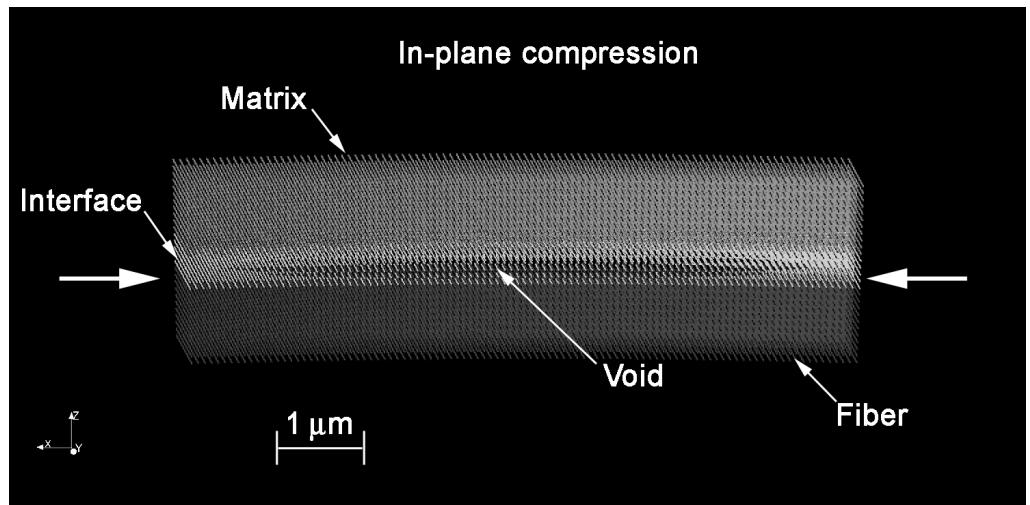
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- At  $18 \mu\text{s}$ , damage is spatially homogeneous for a system without void owing to homogeneous deformation
- At  $30 \mu\text{s}$ , damage is concentrating near the void boundary when the void is present
- At  $60 \mu\text{s}$ , damage for the system without void spreads to the center of the system owing to inhomogeneous deformation
- For the system with void, a fracture is visible along the peak of shear stress direction, while damage in the fiber regions remains relatively low

# IN-PLANE COMPRESSION LOADING OF C/SiC

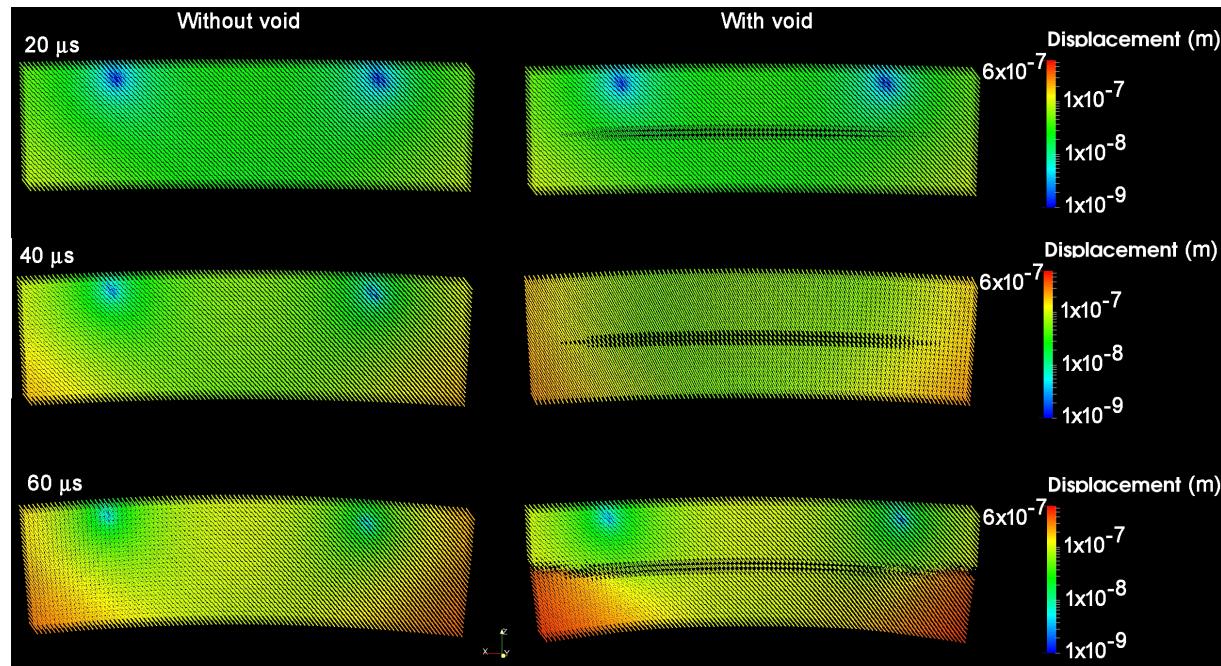
- Time-dependent external force at the side boundaries was used to represent an in-plane loading
- Fiber was aligned along the compression direction shown by the thick arrows
- An isotropic bond-based peridynamic model was used to model interactions between points in the matrix region
- An anisotropic bond-based peridynamic model was used in the fiber and interface regions
- Stiffness of interface structure was represented by a combination of fiber bonds along the compression direction and matrix bonds in all other directions



- Damage processes in the fiber-interface-matrix system were resolved by iterating fast implicit quasi-static time integration with slow explicit dynamics



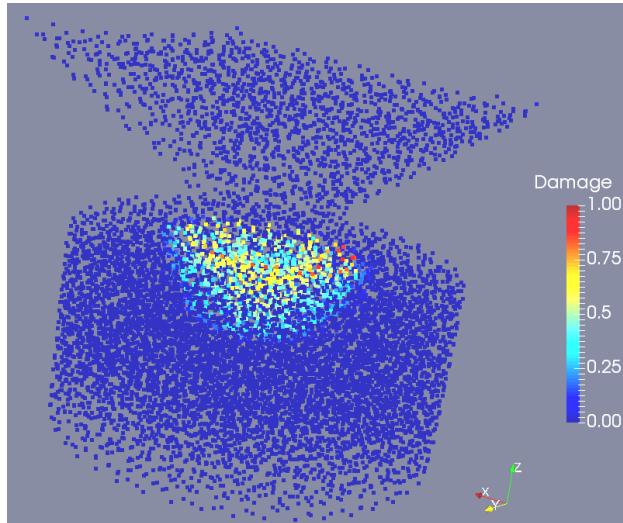
# IN-PLANE COMPRESSION LOADING



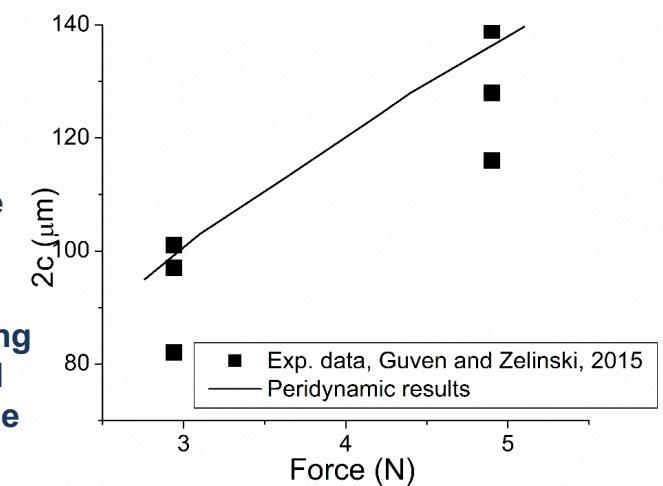
- At 20  $\mu$ s, displacement is spatially homogeneous except the region near the side boundaries where displacement peaks due to the directional deformation
- There are two spots with low displacement magnitude where deformation along the longitudinal direction is negated by that along the transverse direction
- Systems are deformed at 40  $\mu$ s with a pronounced peak of displacement in the fiber region due to the small transverse elastic modulus
- At 60  $\mu$ s, fracture is visible in the case of the system with void, while the system without void is deformed, but not cracked

# MODELING ELASTO-PLASTIC INDENTATION ON ZnS SUBSTRATE

14



- Structural virtual analysis of missile materials was conducted in past using empirical impact material response models
- However, such models were developed only for simple materials such as metals
- Advanced materials including ceramic composites can fail due to microcracks with little appreciable mass loss

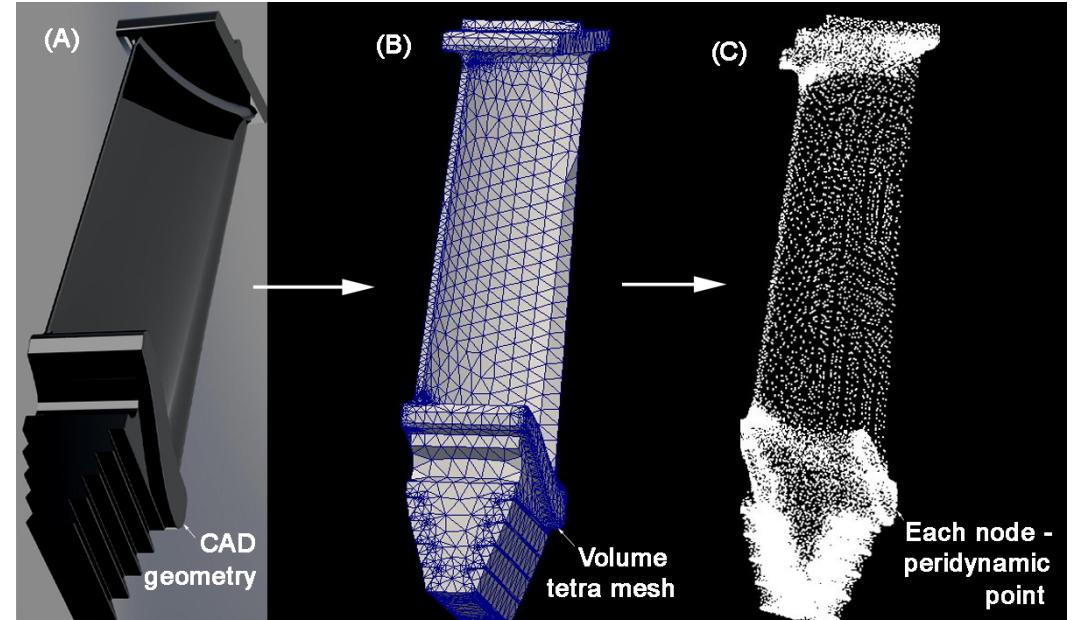


- Vickers hardness test measurements reported by Guven and Zelinski, 2015 were used to validate peridynamics results
- Peridynamic model consisted of an indentor and a ZnS ceramic substrate
- A peridynamic plasticity model was used for the substrate



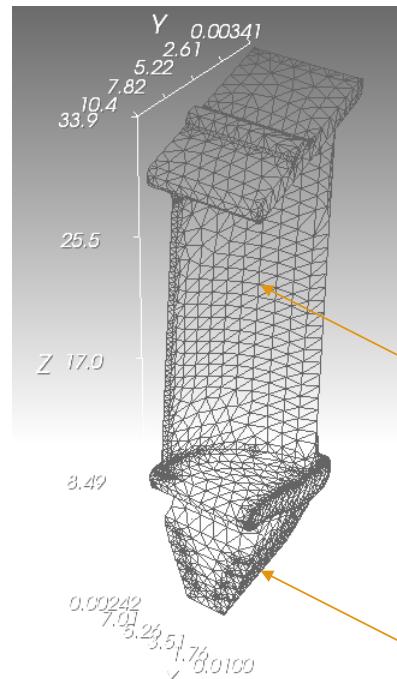
# FATIGUE DAMAGE ANALYSIS OF GAS TURBINE BLADE

- Peridynamic calculations are almost always done for mesh with nearly constant node spacing
- This makes peridynamic simulation unpractical for complex geometry
- Peridigm can handle a non-uniform mesh provided in Exodus/Genesis mesh input
- This feature is demonstrated by fracture analysis of a blade of gas-turbine engine
- (A) - CAD geometry
- (B) - Unstructured grid
- (C) – Peridynamic points



# SET-UP AND BOUNDARY CONDITIONS

- Modeling was performed for a blade made from a Ti–6Al–4V alloy
- Temperature was prescribed as a function of height
- Temperature varied from 400°C at the bottom to 500°C at the top
- Single cycle was modelled with explicit Verlet integration method with a stable time step of  $2.0 \times 10^{-7}$
- Explicit solution provided an initial guess to the implicit method



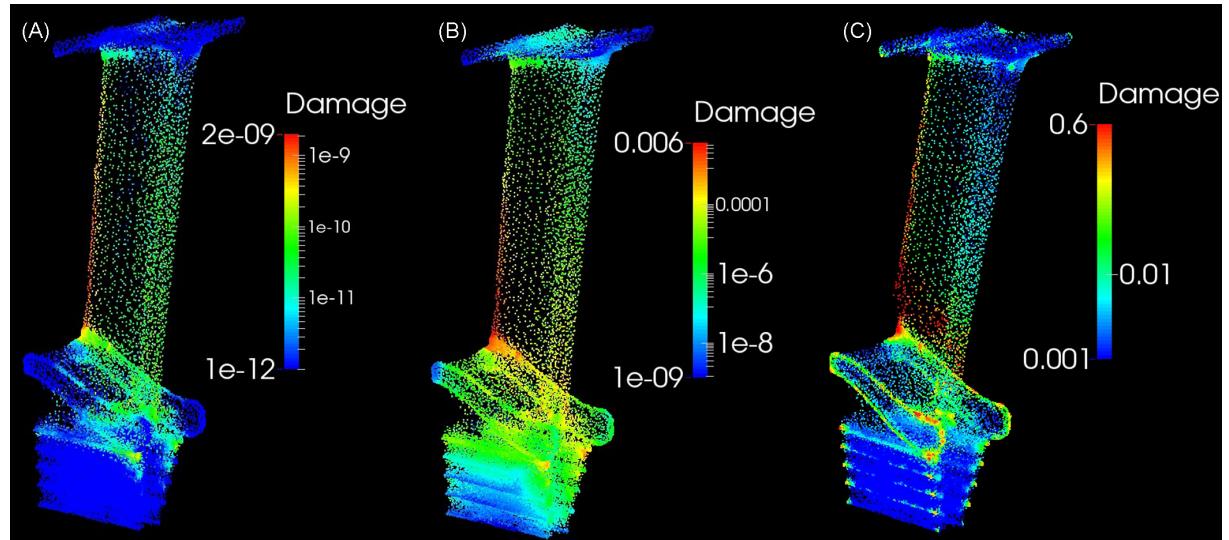
Prescribed Force of  
 $F_x = 10^3 \sin(2\pi \text{ RPM } t)$  [Lift]  
 $F_y = 10^3 \cos(2 \pi \text{ RPM } t)$  [Drag]

Prescribed zero displacement  
 for disk/blade segment



# DAMAGE VS NUMBER OF CYCLES (N)

- Damage resulting from fatigue of blade had a strong dependence on the number of cycles
- Damage peaked at the bottom of the trailing edge of the blade
- It is likely that cracks would form in this area at a larger number of cycles
- There was also some damage accumulated at the blade/disk interface



- (A) - N=1
- (B) - N=1,000
- (C) - N=30,000
- RPM - 15,000
- Prescribed Force:
  - $F_x = 10^3 \sin(2\pi \text{ RPM } t)$  [Lift]
  - $F_y = 10^3 \cos(2 \pi \text{ RPM } t)$  [Drag]



# SUMMARY

- Peridynamics is a novel mathematical theory that unifies the mechanics of continuous media, cracks and discrete particles
- Peridynamic damage analysis is particularly valuable for products of additive manufacturing which comprise 3-D heterogeneities and discontinuities
- Nonlocal-local coupling was demonstrated as means to embed peridynamic modeling within a larger FEM simulation
- Peridynamic software was used to reproduce trends from the literature for fracture formation during the out-of-plane and in-plane compression loadings
- For out-of-plane loading, fracture was formed via void collapse and shear damage banding owing to compression
- For in-plane loading, fracture was caused by the directional delamination
- Peridynamic modeling can provide predictive insight to composite nosecones and radomes applications
- The use of non-uniform node spacing made the peridynamic simulations practical for high-cycle fatigue damage analysis of a turbine blade

