



# An Active Thevenin Equivalent Circuit Approach to Problems with Non-Linear Circuit Loads

*Jeffery T. Williams, Fred J. Zutavern,  
and Larry D. Bacon*

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Antennas and  
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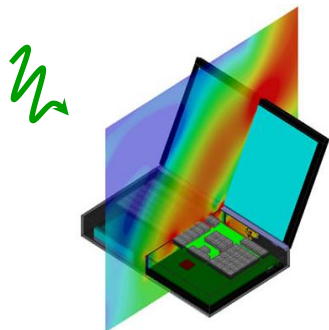
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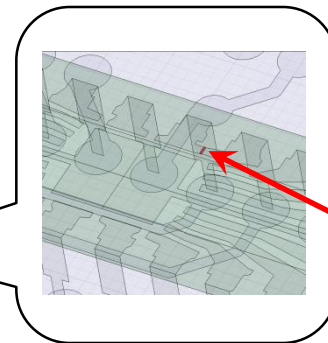
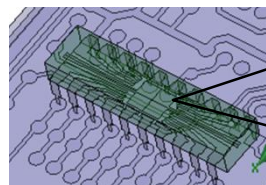
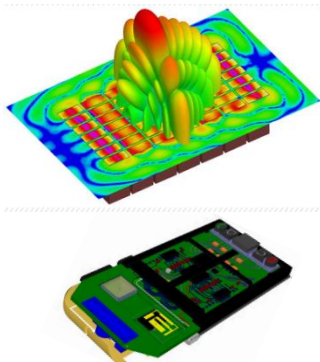


# EMI & IEMI Effects Process

## Coupling

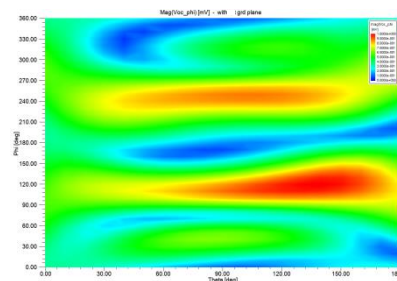


## Energy Distribution



port

## Device Response

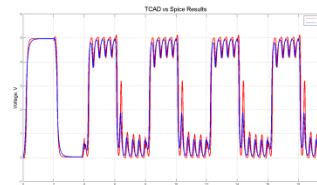
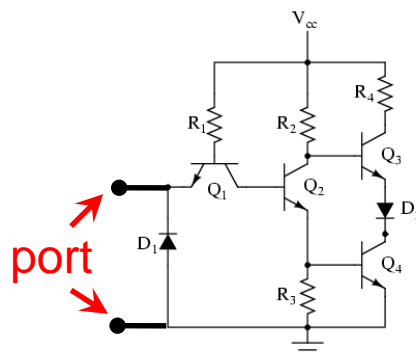
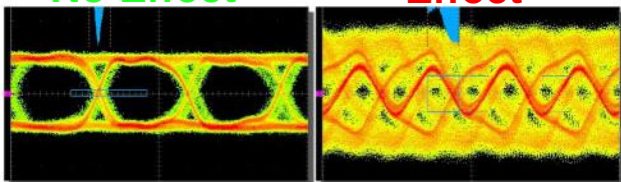


available power at port

## System Impact

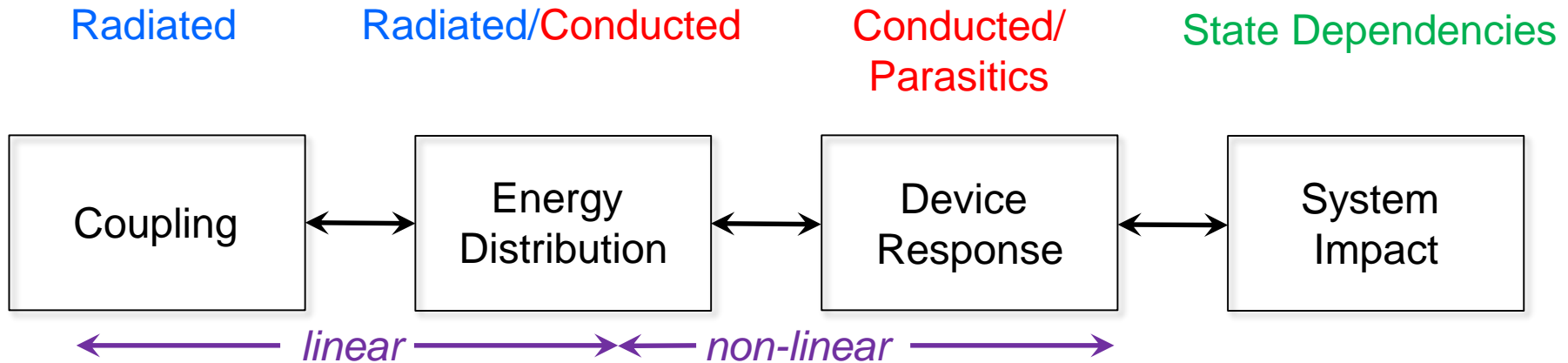
No Effect

Effect

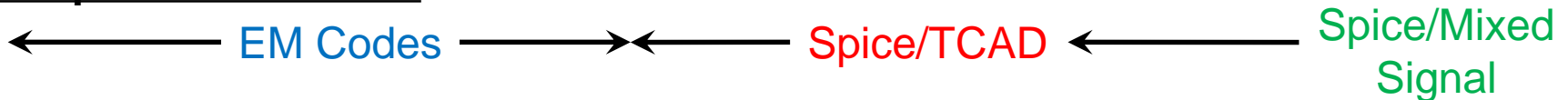


# Computing EMI & IEMI Effects

## Mechanisms:



## Computational Tools:



*We need an efficient and accurate approach for linking these different computations together in a self-consistent manner.*



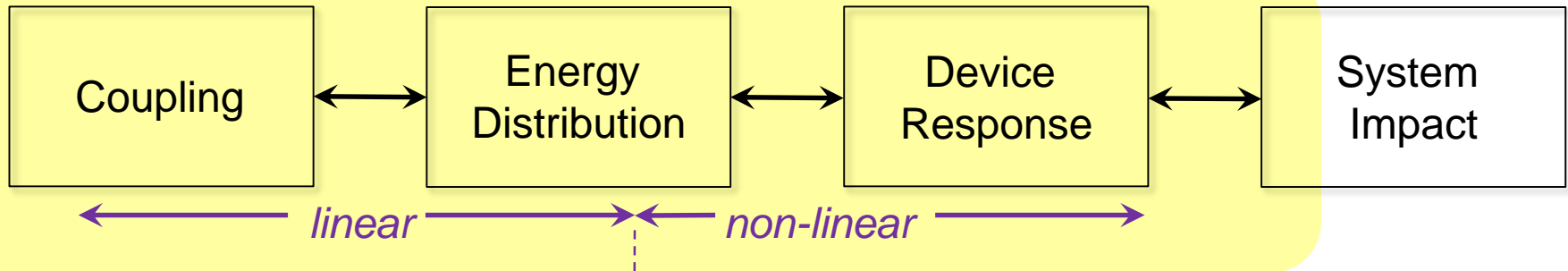
# Our Approach: ATHENA

## Computational Tools:

EM Codes

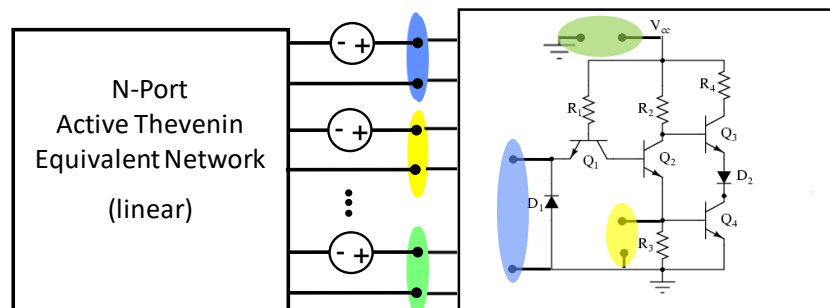
Spice/TCAD

Spice/Mixed  
Signal



ATHENA

Active THevenin Equivalent Network Approach

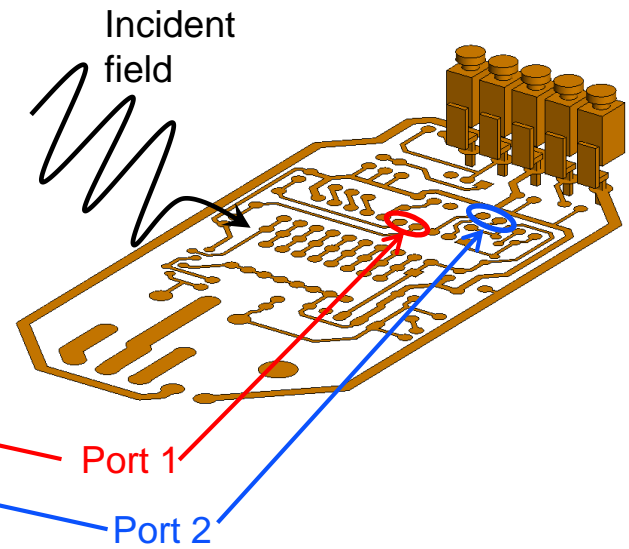
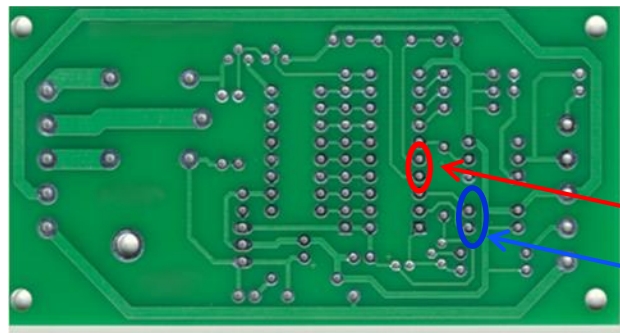


Circuit for demonstration only

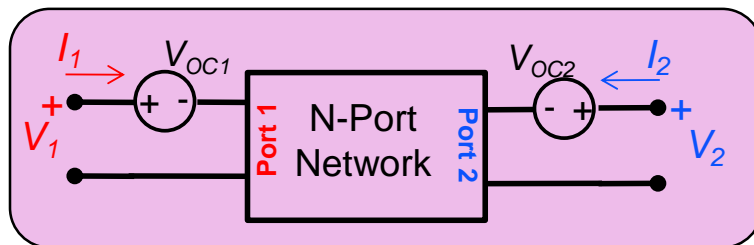
# Active Thevenin Equivalent Network

Ports are essentially terminal pairs defined at reference planes where quasi-static voltages and currents can be defined.

## 2-Port Example



Excluding the port loads, **linear** time or frequency domain EM simulators are used to determine the **open-circuit voltage** and **impedance parameters** at the ports.

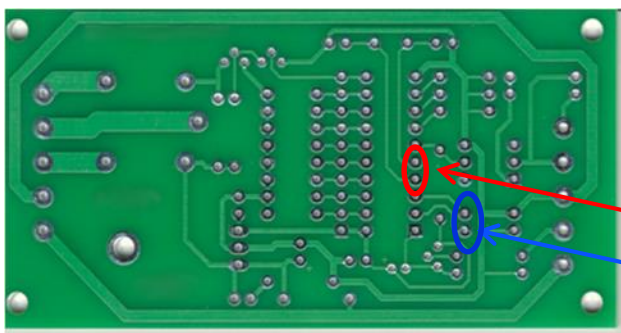


Active Thevenin Equivalent Network = “ATHENA device”



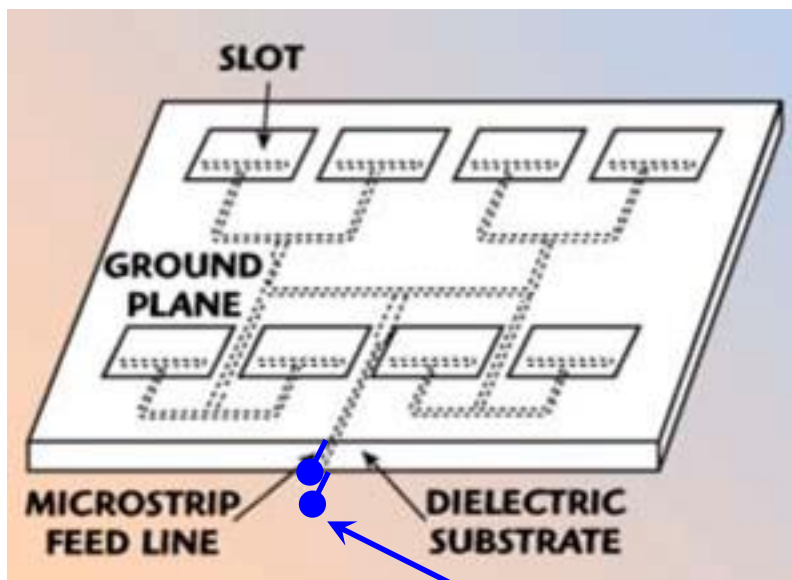


# Port Examples

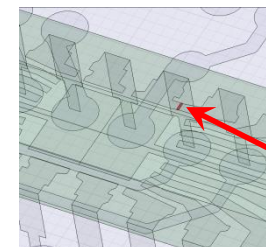
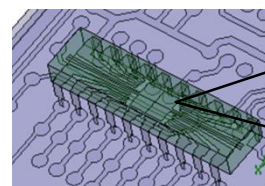


Port 1

Port 2



port



port



# General Aspects of ATHENA

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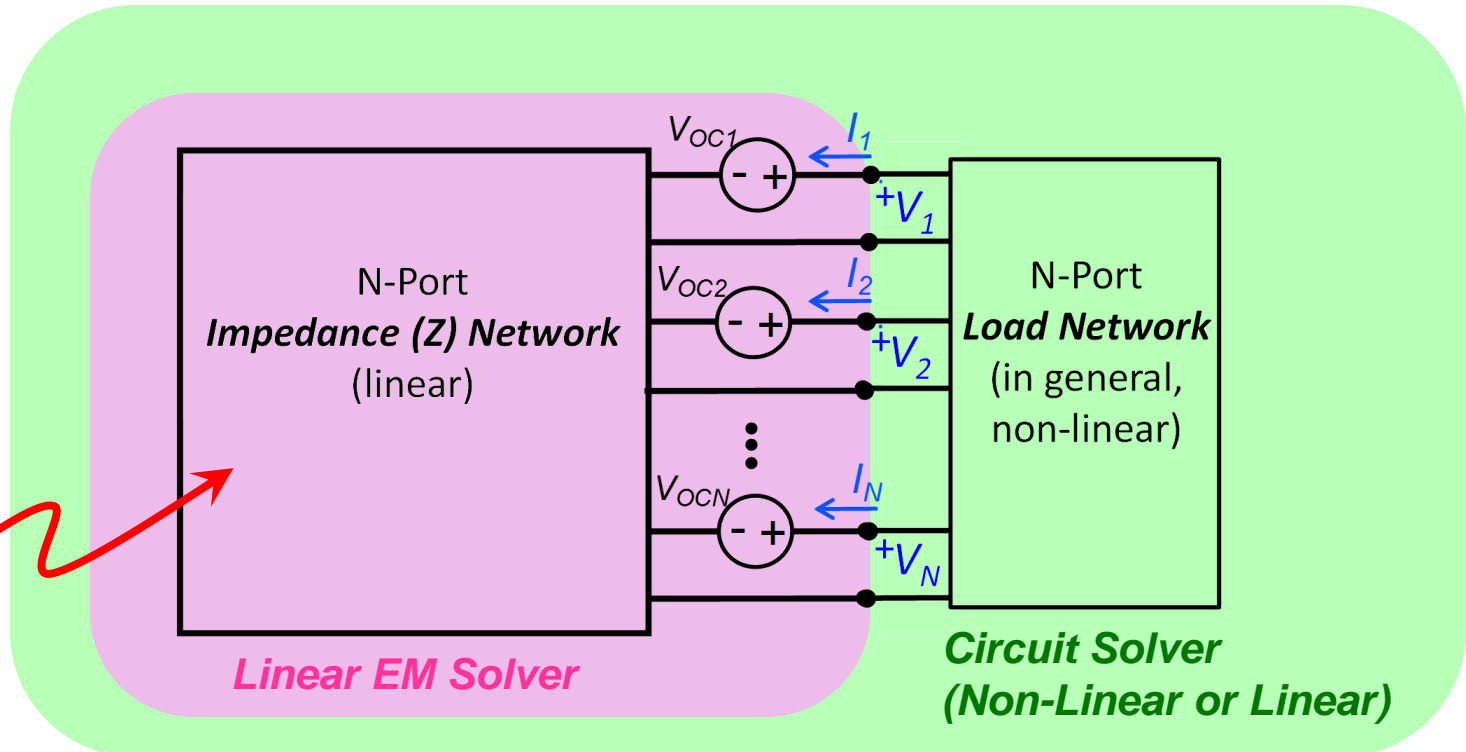
The overriding goals in developing ATHENA are to

- not be restricted to specific EM simulators
  - time domain (FDTD, TLM,...)
  - frequency domain (FEM, MOM, ...)
- be general enough to be implemented in any linear/non-linear circuit solver
  - transient time domain
  - harmonic balance



# Coupling of ATHENA Device to a Load Network

*Only needs to be calculated once.*



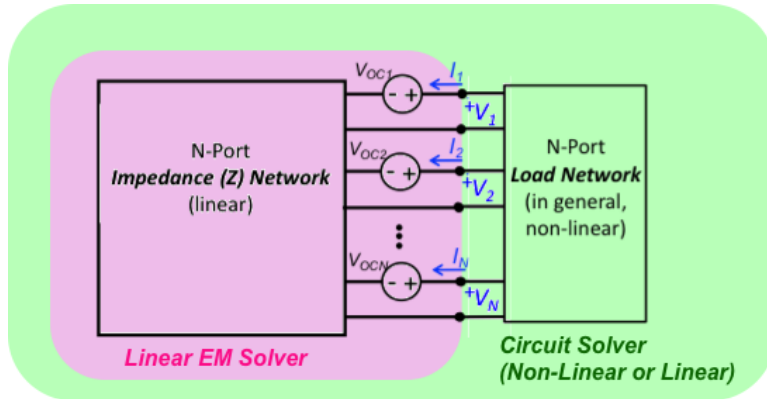
- Implicitly, for non-linear loads this coupling is performed in the time-domain. Hence, any frequency domain quantities have to be inverse-Fourier transformed to the time-domain.





# ATHENA Device

$$V_m^{OC} = \frac{1}{j\omega\mu_0} (4\pi r e^{+jk_0 r}) (\mathbf{p} \cdot \mathbf{E}_m^T(\theta, \phi))$$



Using reciprocity, the open-circuit voltage at  $m^{\text{th}}$ -port due to an incident wave from a far-field source

$$V_m^{OC} = \mathbf{h}_m(\theta, \phi) \cdot \mathbf{E}_{\text{inc}}$$

where

$$\mathbf{h}_m(\theta, \phi) = \frac{1}{j\omega\mu_0} \left( \frac{4\pi r e^{+jkr}}{I_m} \right) \mathbf{e}_m^T(\theta, \phi)$$

*Radiated field from current  $I_m$  driving port  $m$ .*

Freq. Domain

$$[\mathbf{V}] = [\mathbf{Z}][\mathbf{I}] + [\mathbf{V}^{OC}]$$

Time Domain

$$[v(t)] = [z(t)] \otimes [i(t)] + [v^{OC}(t)]$$

*Convolution operator*

**2-Port Example:**

$$\begin{bmatrix} v_1(t) \\ v_2(t) \end{bmatrix} = \begin{bmatrix} \int_0^t z_{11}(t-\tau) i_1[v_1(\tau)] d\tau + \int_0^t z_{12}(t-\tau) i_2[v_2(\tau)] d\tau \\ \int_0^t z_{21}(t-\tau) i_1[v_1(\tau)] d\tau + \int_0^t z_{22}(t-\tau) i_2[v_2(\tau)] d\tau \end{bmatrix} + \begin{bmatrix} v_1^{OC}(t) \\ v_2^{OC}(t) \end{bmatrix}$$

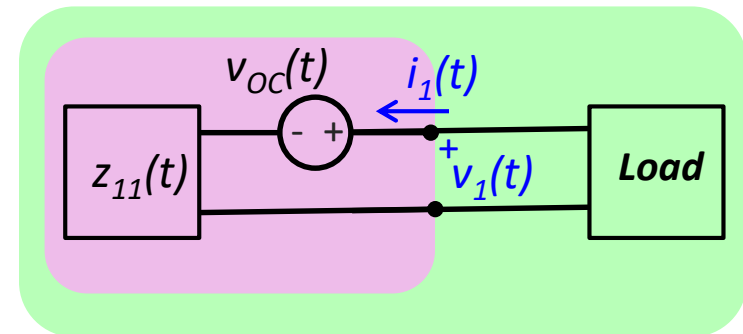
*Relationships between port voltages and currents dictated by the Load Network*

# Surge Impedance



To discuss details associated with implementation, consider a **one-port network** example:

$$v_1(t) = \int_0^t z_{11}(t - \tau) i_1[v_1(\tau)] d\tau + v_1^{OC}(t)$$



For distributed coupling problems the self-impedances ( $z_{mm}$ ) are impulsive near  $t=0$ .

$$v_1(t) - \int_{t_-}^t z_{11}(t - \tau) i_1[v_1(\tau)] d\tau = \int_0^{t_-} z_{11}(t - \tau) i_1[v_1(\tau)] d\tau + v_1^{OC}(t)$$

$$v_1(t) - z_{11}(t) i_1[v_1(t)] = \int_0^{t_-} z_{11}(t - \tau) i_1[v_1(\tau)] d\tau + v_1^{OC}(t)$$

$$t_- = \lim_{\delta \rightarrow 0} (t - \delta)$$

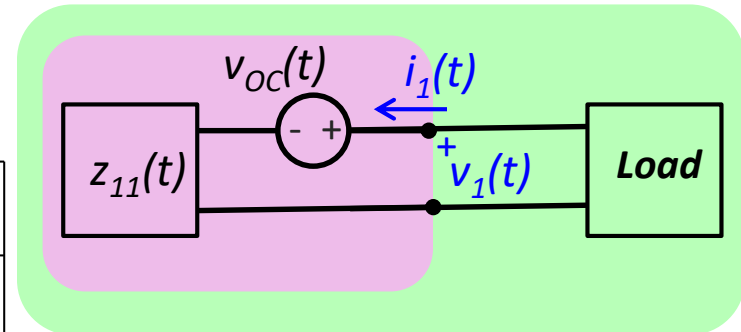
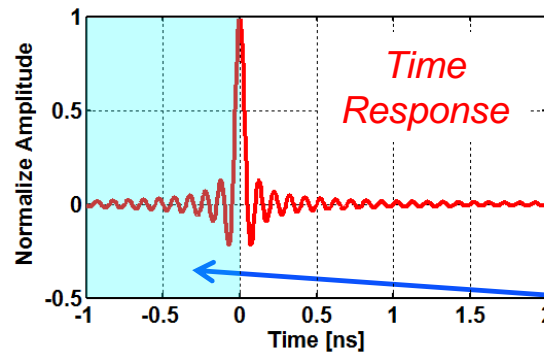
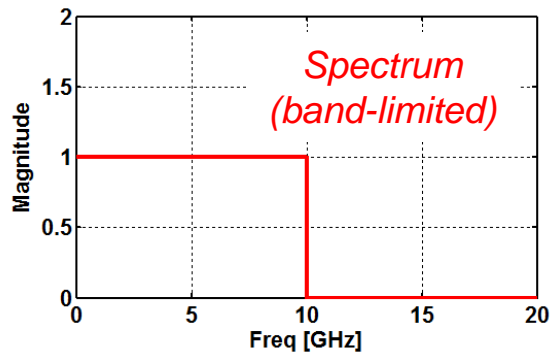
*Surge impedance*

- Time domain simulations typically capture this response.
- Frequency domain simulations must be corrected.



# When using Frequency Domain Simulations

Frequency domain simulations are band-limited.  
Hence, impulse-like responses in the  
time-domain appear as *sinc* functions.



*Non-Causal*

If the surge impedance is not corrected

- causality errors
- aliasing errors
- instability in non-linear solvers

$$v_1(t) - z_{11}(t) i_1[v_1(t)] = \int_0^{t_-} z_{11}(t - \tau) i_1[v_1(\tau)] d\tau + v_1^{OC}(t)$$

Since the impulsive nature of surge impedance is known, it is evaluated analytically and *sinc* behavior is analytically removed.



# Non-Impulsive Surge Impedance

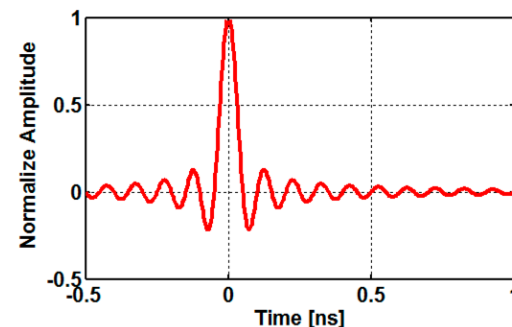
This is a continuing area of investigation.

- Windowing (filtering) frequency response to reduce amplitude of time domain “ripples.”

➤ relaxes required time resolution

- Extract reactive parasitic effects near the port.

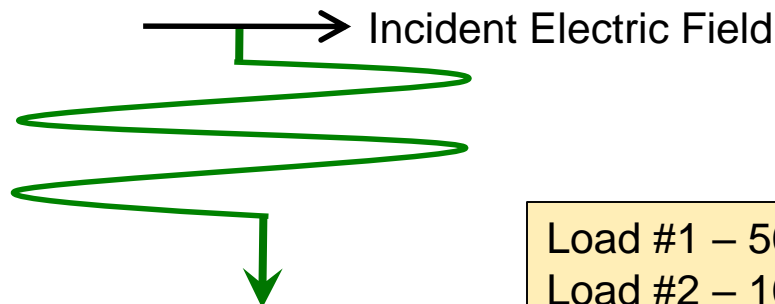
➤ have successfully employed this technique by “manually” identifying reactive elements



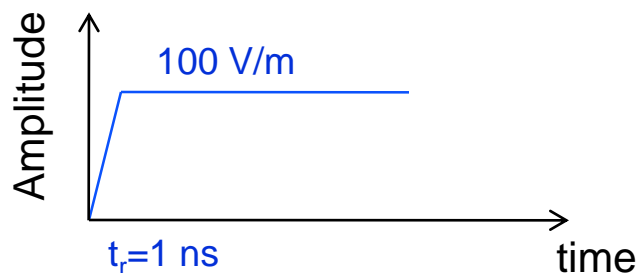
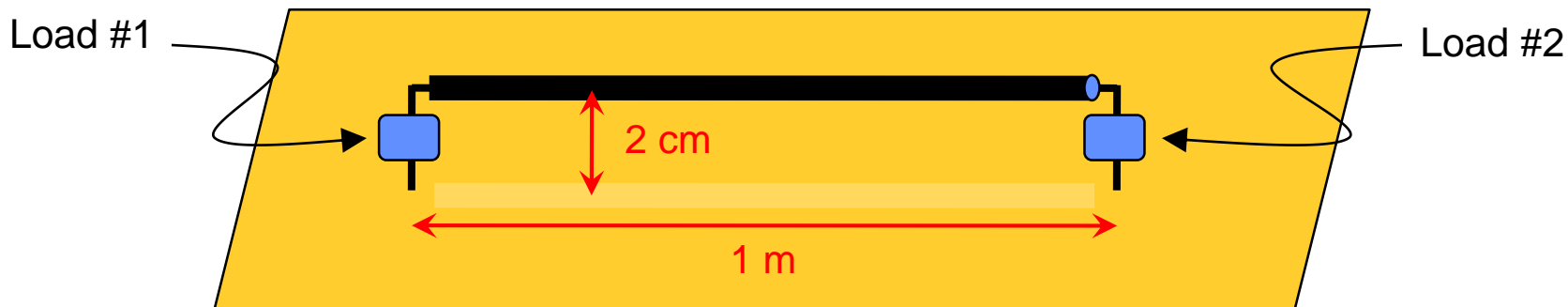


# Example Problem Geometry (Intentionally Simple!)

Wire above ground plane  
with end terminations



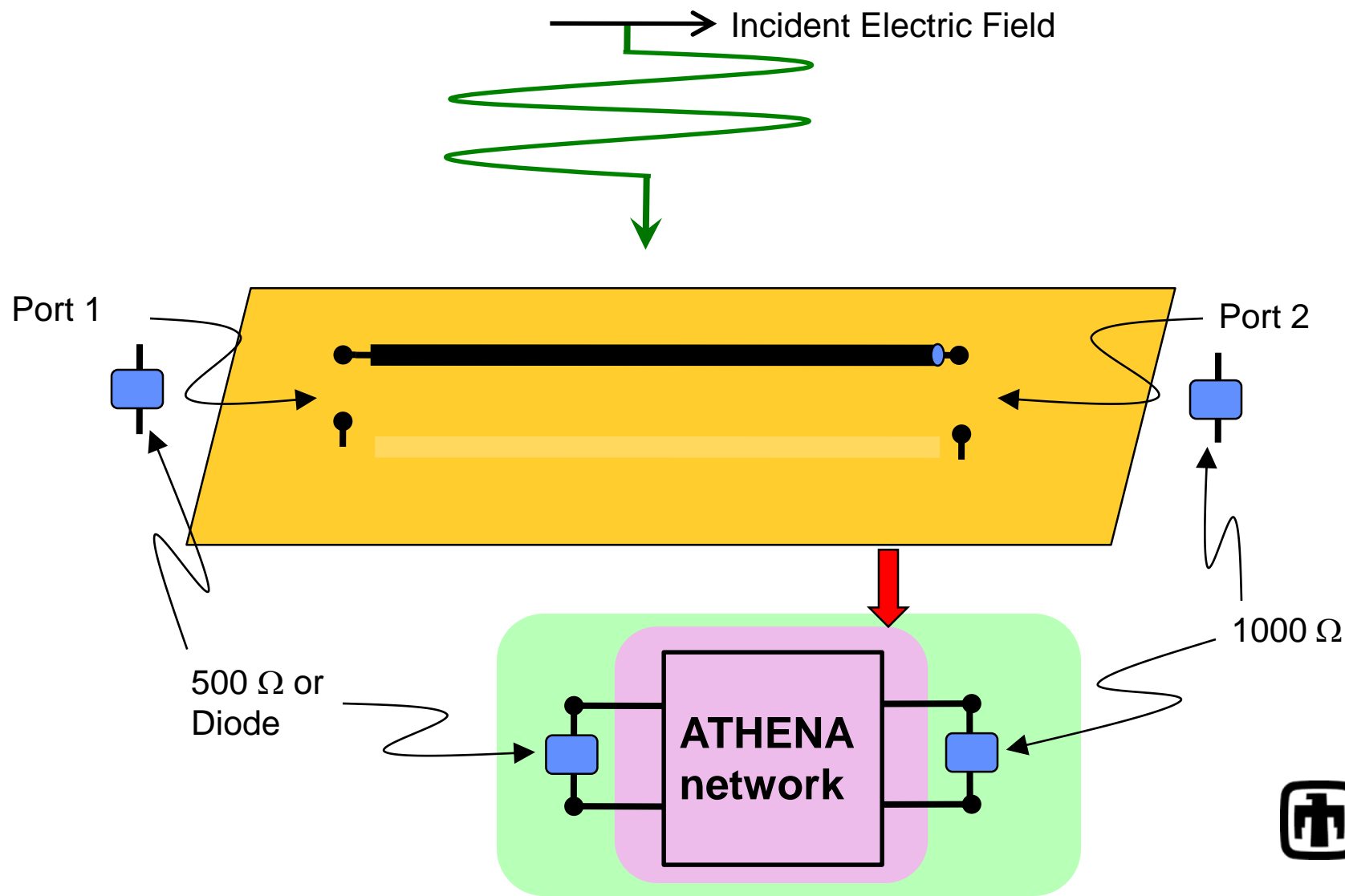
Load #1 – 500  $\Omega$  or Diode  
Load #2 – 1000  $\Omega$



Not to scale

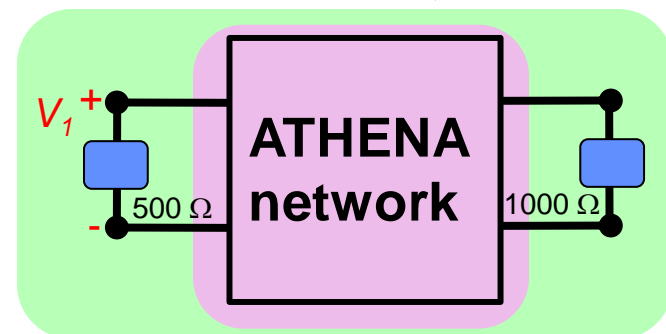
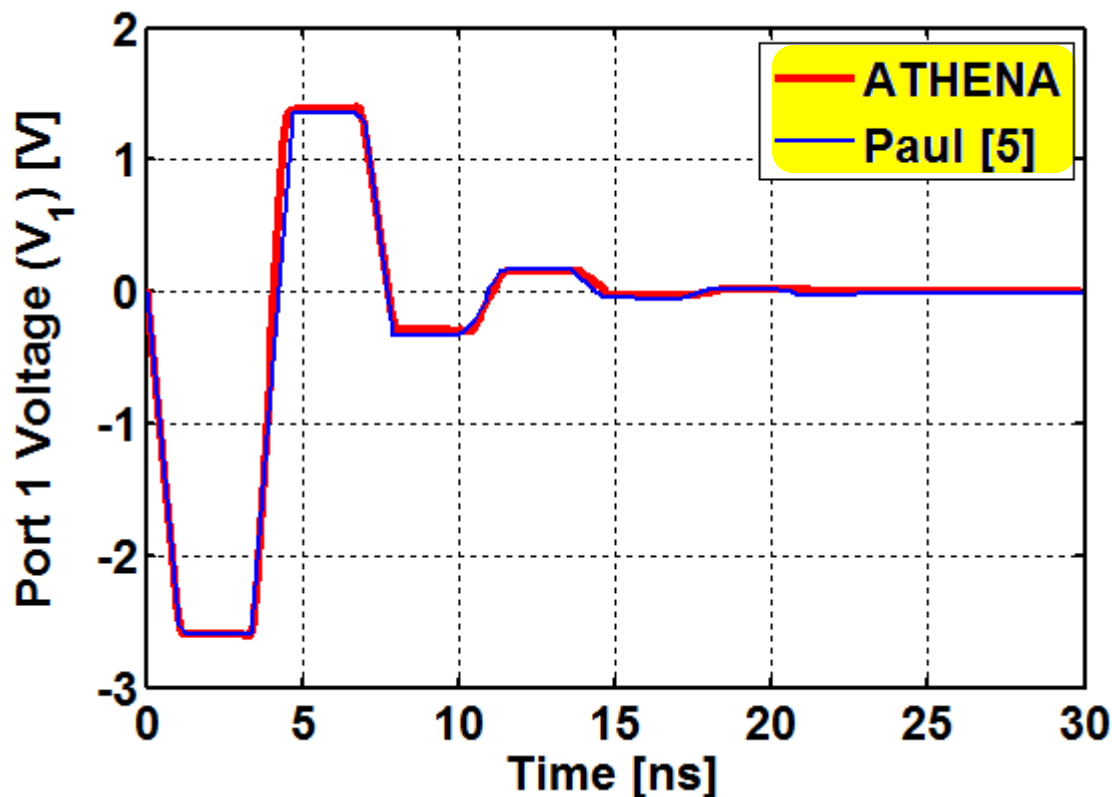


# Example: 2-Port Network





## 2-Port : Linear Loads (500 $\Omega$ and 1000 $\Omega$ )

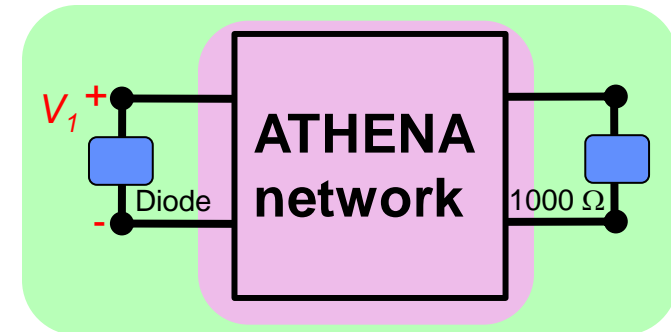
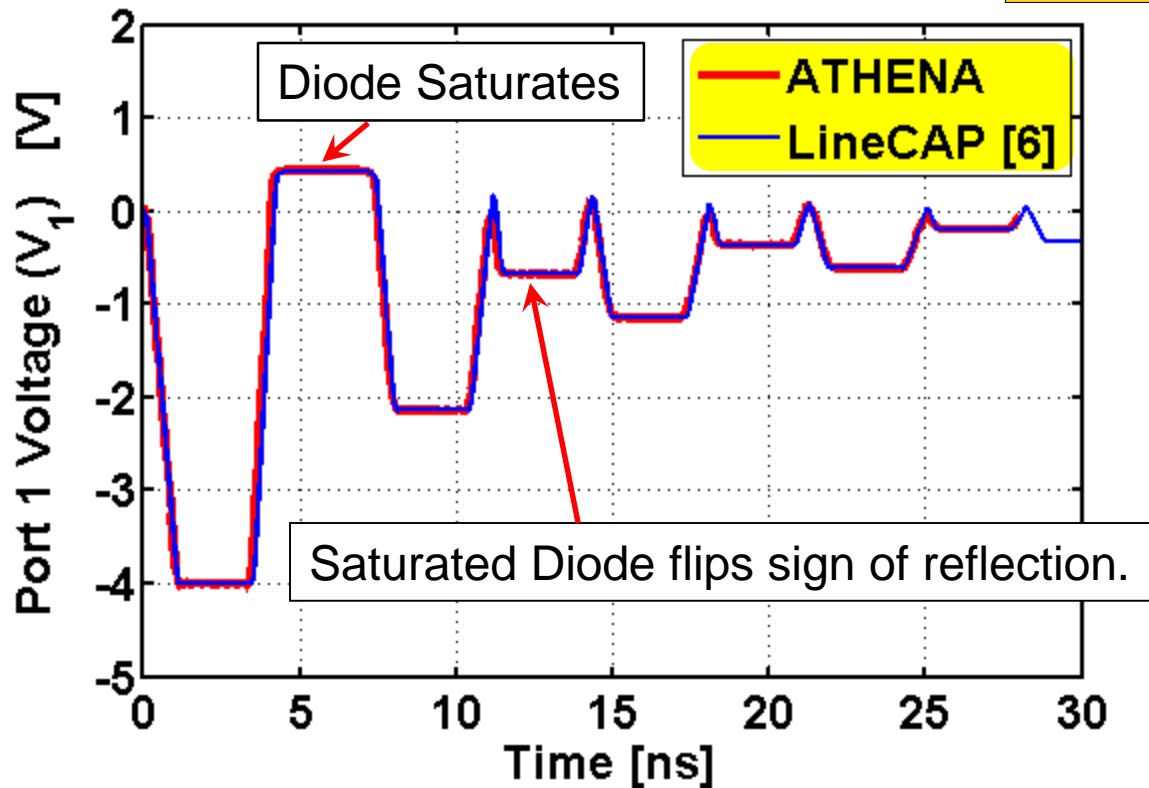


$$E_{\max} = 100 \text{ V/m}$$

*Parameters of ATHENA device  
determined using the freq.  
domain MOM code FEKO.*

*ATHENA device implemented  
in Xyce.*

## 2-Port : Linear ( $500\ \Omega$ ) and Non-Linear (Diode) Loads



$$E_{\max} = 100\ \text{V/m}$$

*Parameters of ATHENA device determined using the freq. domain MOM code FEKO.*

*ATHENA device implemented in Xyce.*

Athena allows us to feed back nonlinear electronic response into the coupling problem.



# Summary and Next Steps

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- The **Active Thevenin Equivalent Network Approach (ATHENA)** allows us to link EMI & IEMI coupling to nonlinear circuit simulations in a fully consistent, bidirectional way.
- The ATHENA approach is general. It can utilize both time and frequency domain linear EM simulators, and harmonic balance and transient time domain non-linear circuit solvers.
- ATHENA is now implemented in the Spice code *ngspice* and Sandia's parallelized circuit code *Xyce*.
- Test cases (numerical and experimental) are continually being investigated to further the validation and development of the approach.
- Investigating causality issues associated this approach with the EM simulations are done in the frequency domain.