

An Active Thevenin Equivalent Circuit Approach to Problems with Non-Linear Circuit Loads

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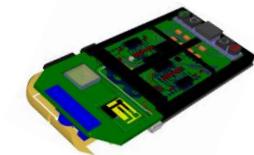
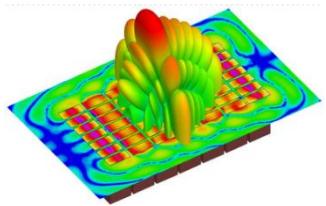
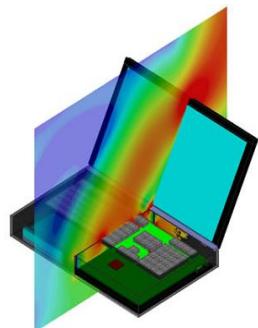
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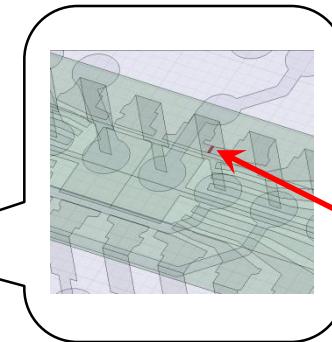
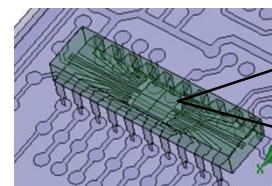


EMI & IEMI Effects Process

Coupling

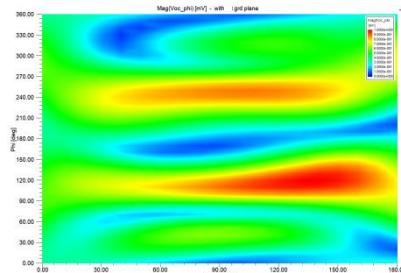


Energy Distribution



port

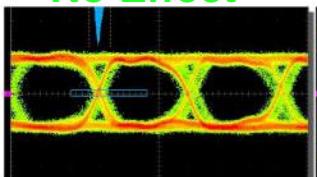
Device Response



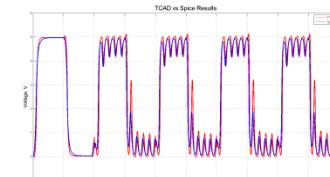
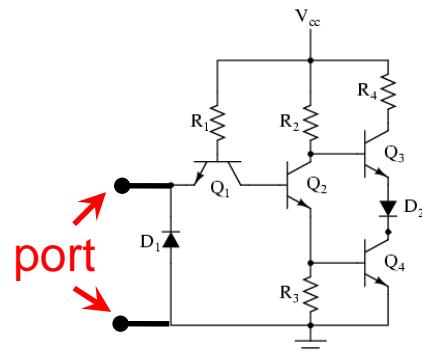
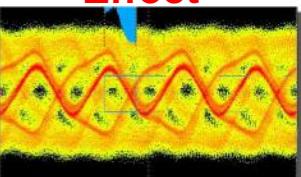
available power at port

System Impact

No Effect



Effect



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Computing EMI & IEMI Effects

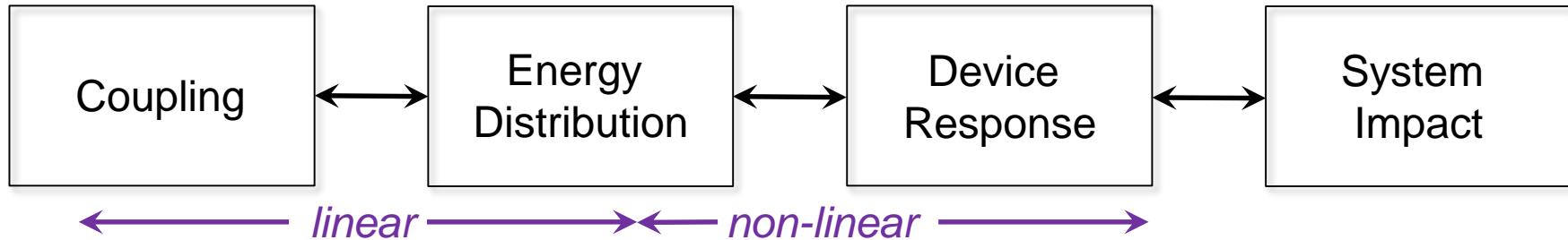
Mechanisms:

Radiated

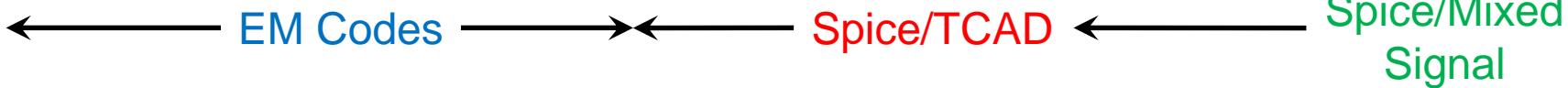
Radiated/Conducted

Conducted/
Parasitics

State Dependencies



Computational Tools:

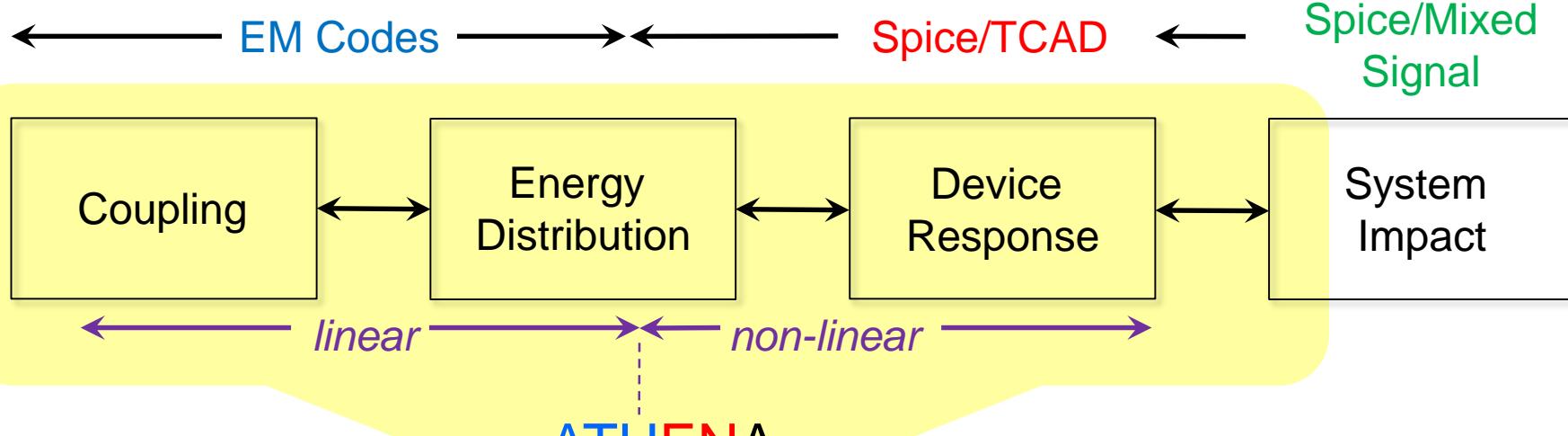


*We need an efficient and accurate approach
for linking these different computations
together in a self-consistent manner.*

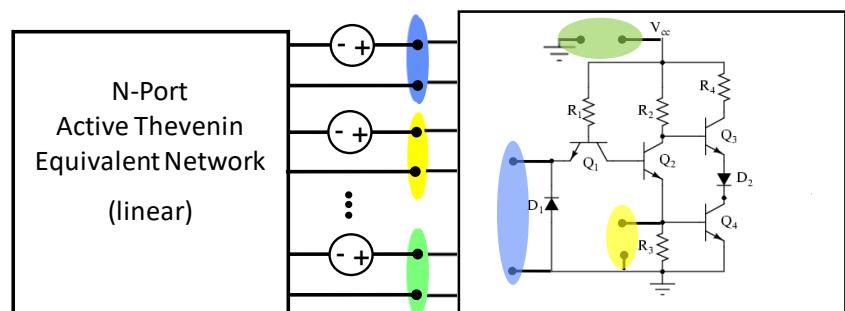


Our Approach: ATHENA

Computational Tools:



Active THevenin Equivalent Network Approach



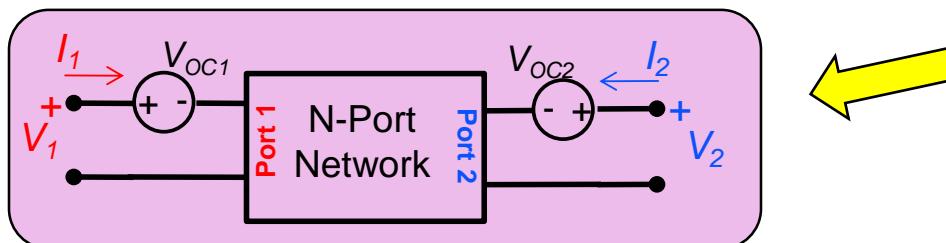
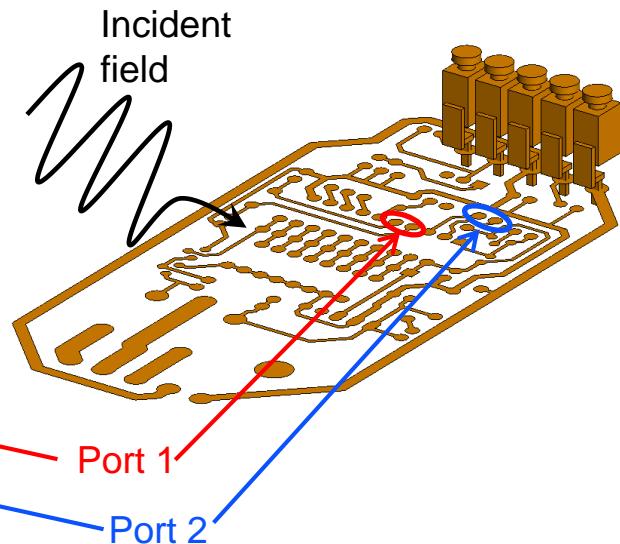
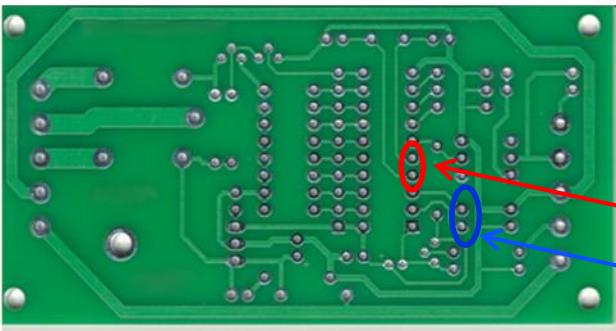
Circuit for demonstration only

Active Thevenin Equivalent Network



Ports are essentially terminal pairs defined at reference planes where quasi-static voltages and currents can be defined.

2-Port Example

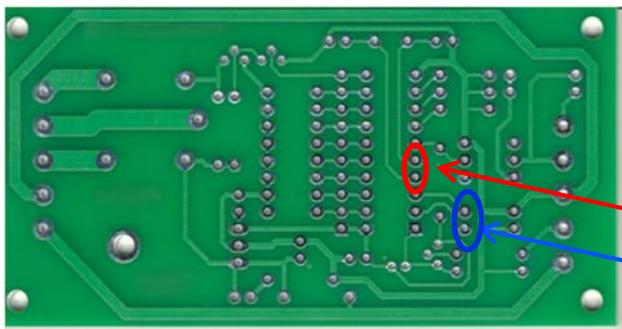


Excluding the port loads, **linear** time or frequency domain EM simulators are used to determine the **open-circuit voltage** and **impedance parameters** at the ports.

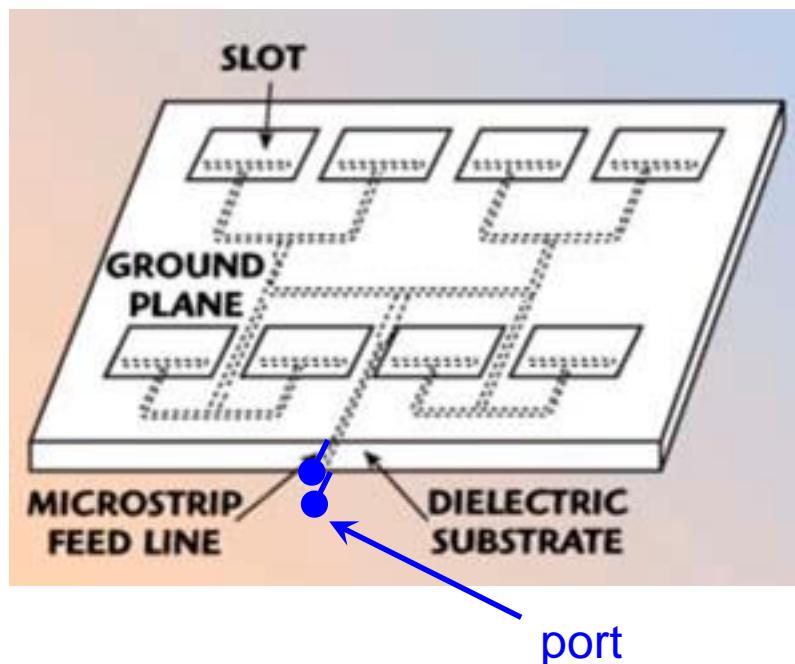
Active Thevenin Equivalent Network = “ATHENA device”



Port Examples



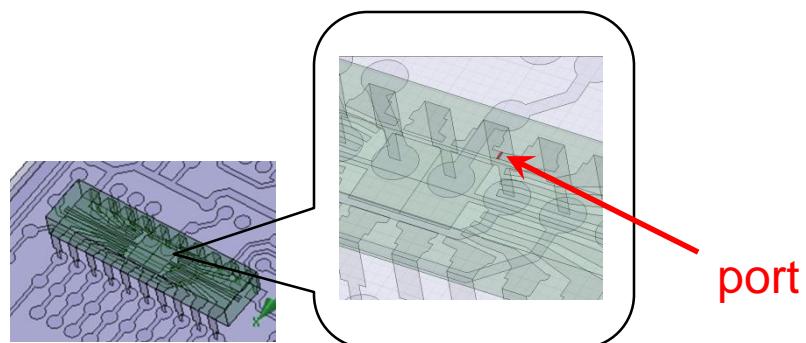
Port 1
Port 2



MICROSTRIP
FEED LINE

DIELECTRIC
SUBSTRATE

port





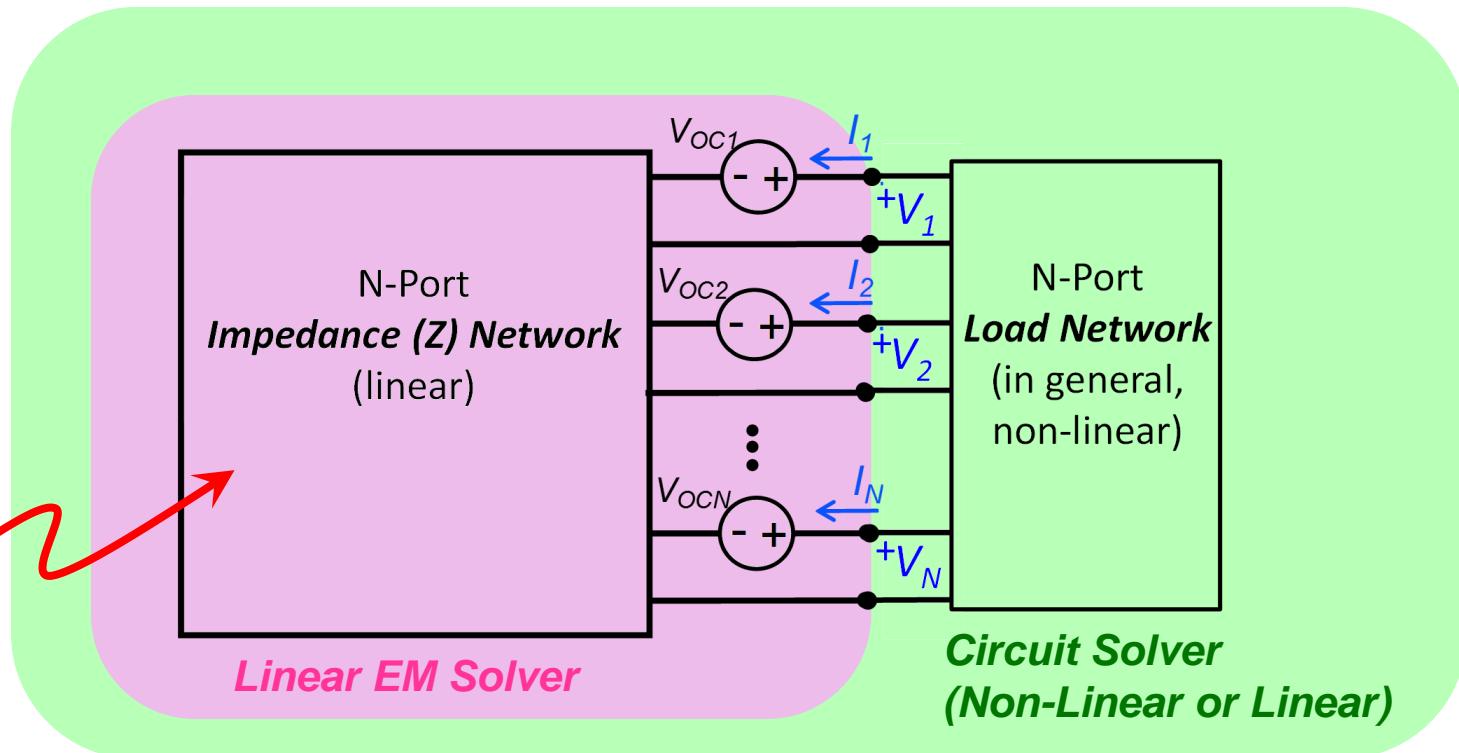
General Aspects of ATHENA

The overriding goals in developing ATHENA are to

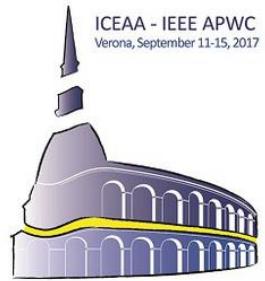
- not be restricted to specific EM simulators
 - time domain (FDTD, TLM, ...)
 - frequency domain (FEM, MOM, ...)
- be general enough to be implemented in any linear/non-linear circuit solver
 - transient time domain
 - harmonic balance



Coupling of ATHENA Device to a Load Network

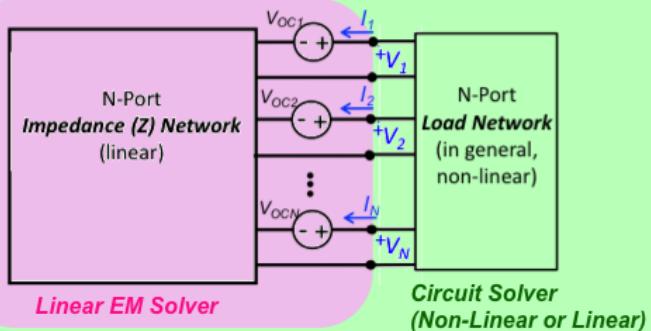


- Implicitly, for non-linear loads this coupling is performed in the time-domain. Hence, any frequency domain quantities have to be inverse-Fourier transformed to the time-domain.



$$V_m^{OC} = \frac{1}{j\omega\mu_0} (4\pi r e^{+jk_0 r}) (\mathbf{p} \cdot \mathbf{E}_m^T(\theta, \phi))$$

ATHENA Device



Using reciprocity, the open-circuit voltage at m^{th} -port due to an incident wave from a far-field source

$$V_m^{OC} = \mathbf{h}_m(\theta, \phi) \cdot \mathbf{E}_{\text{inc}}$$

where

$$\mathbf{h}_m(\theta, \phi) = \frac{1}{j\omega\mu_0} \left(\frac{4\pi r e^{+jk_0 r}}{I_m} \right) \mathbf{e}_m^T(\theta, \phi)$$

Radiated field from current I_m driving port m .

Freq. Domain

$$[\mathbf{V}] = [\mathbf{Z}] [\mathbf{I}] + [\mathbf{V}^{OC}]$$

Time Domain

$$[\mathbf{v}(t)] = [\mathbf{z}(t)] \otimes [\mathbf{i}(t)] + [\mathbf{v}^{OC}(t)]$$

Convolution operator

2-Port Example:

$$\begin{bmatrix} v_1(t) \\ v_2(t) \end{bmatrix} = \begin{bmatrix} \int_0^t z_{11}(t-\tau) i_1[v_1(\tau)] d\tau + \int_0^t z_{12}(t-\tau) i_2[v_2(\tau)] d\tau \\ \int_0^t z_{21}(t-\tau) i_1[v_1(\tau)] d\tau + \int_0^t z_{22}(t-\tau) i_2[v_2(\tau)] d\tau \end{bmatrix} + \begin{bmatrix} v_1^{OC}(t) \\ v_2^{OC}(t) \end{bmatrix}$$



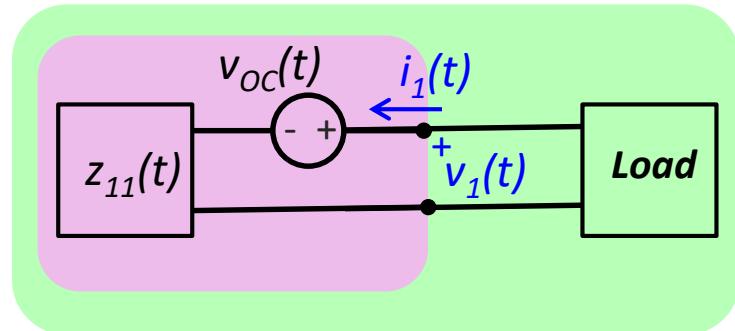
Relationships between port voltages and currents dictated by the Load Network



Surge Impedance

To discuss details associated with implementation, consider a **one-port network** example:

$$v_1(t) = \int_0^t z_{11}(t - \tau) i_1[v_1(\tau)] d\tau + v_1^{OC}(t)$$



For distributed coupling problems the self-impedances (z_{mm}) are impulsive near $t=0$.

$$v_1(t) - \int_{t_-}^t z_{11}(t - \tau) i_1[v_1(\tau)] d\tau = \int_0^{t_-} z_{11}(t - \tau) i_1[v_1(\tau)] d\tau + v_1^{OC}(t) \quad t_- = \lim_{\delta \rightarrow 0} (t - \delta)$$

$$v_1(t) - z_{11}(t) i_1[v_1(t)] = \int_0^{t_-} z_{11}(t - \tau) i_1[v_1(\tau)] d\tau + v_1^{OC}(t)$$

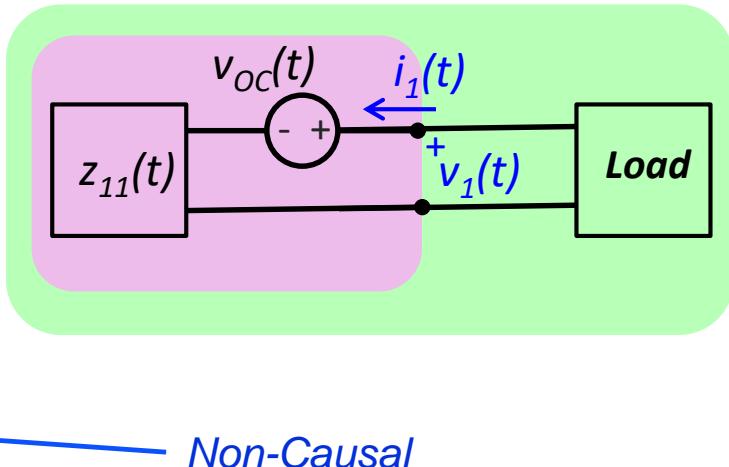
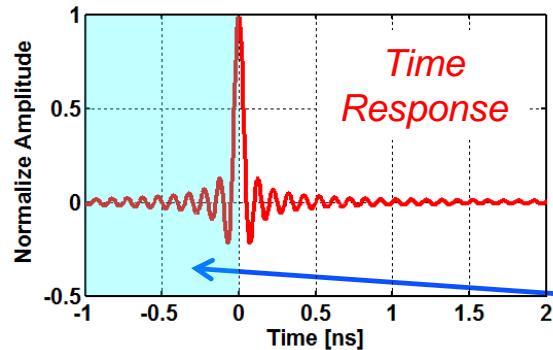
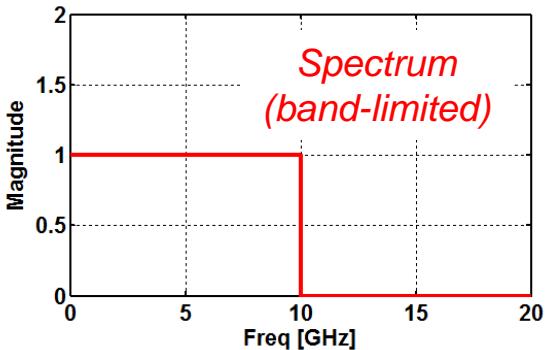
Surge impedance

- Time domain simulations typically capture this response.
- Frequency domain simulations must be corrected.



When using Frequency Domain Simulations

Frequency domain simulations are band-limited.
Hence, impulse-like responses in the time-domain appear as *sinc* functions.

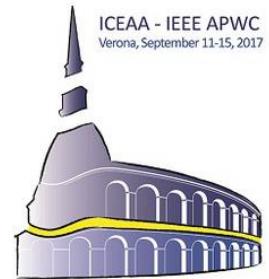


If the surge impedance is not corrected

- causality errors
- aliasing errors
- instability in non-linear solvers

$$v_1(t) - z_{11}(t) i_1[v_1(t)] = \int_0^{t_-} z_{11}(t - \tau) i_1[v_1(\tau)] d\tau + v_1^{OC}(t)$$

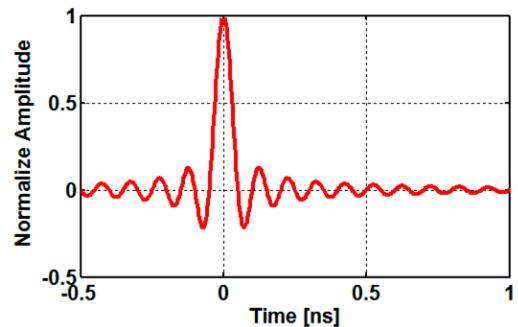
Since the impulsive nature of surge impedance is known, it is evaluated analytically and *sinc* behavior is analytically removed.

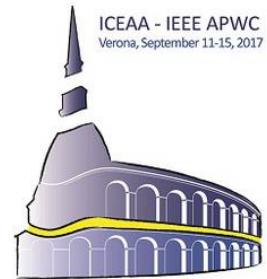


Non-Impulsive Surge Impedance

This is a continuing area of investigation.

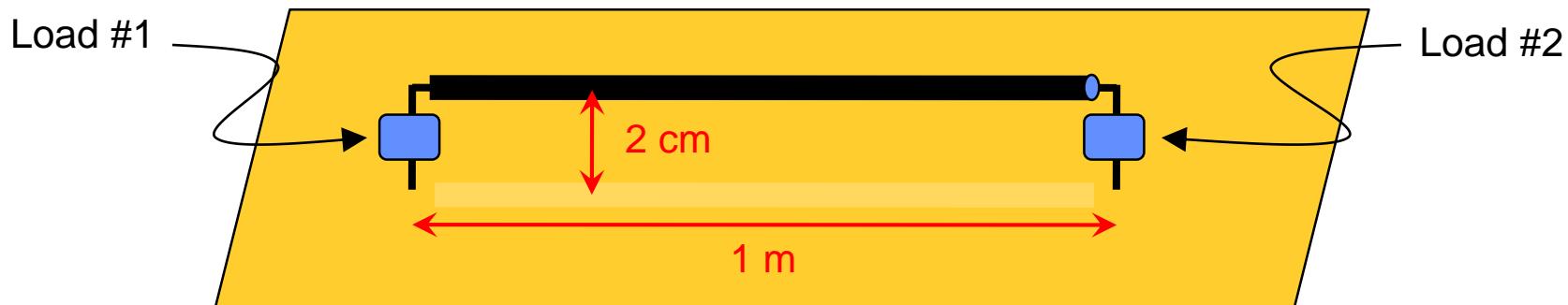
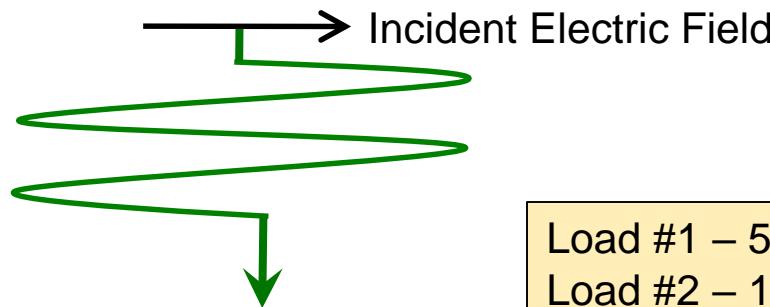
- Windowing (filtering) frequency response to reduce amplitude of time domain “ripples.”
 - **relaxes required time resolution**
- Extract reactive parasitic effects near the port.
 - **have successfully employed this technique by “manually” identifying reactive elements**



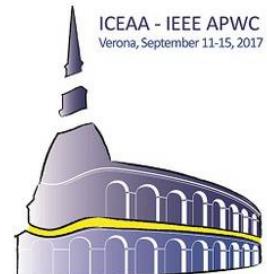


Example Problem Geometry (Intentionally Simple!)

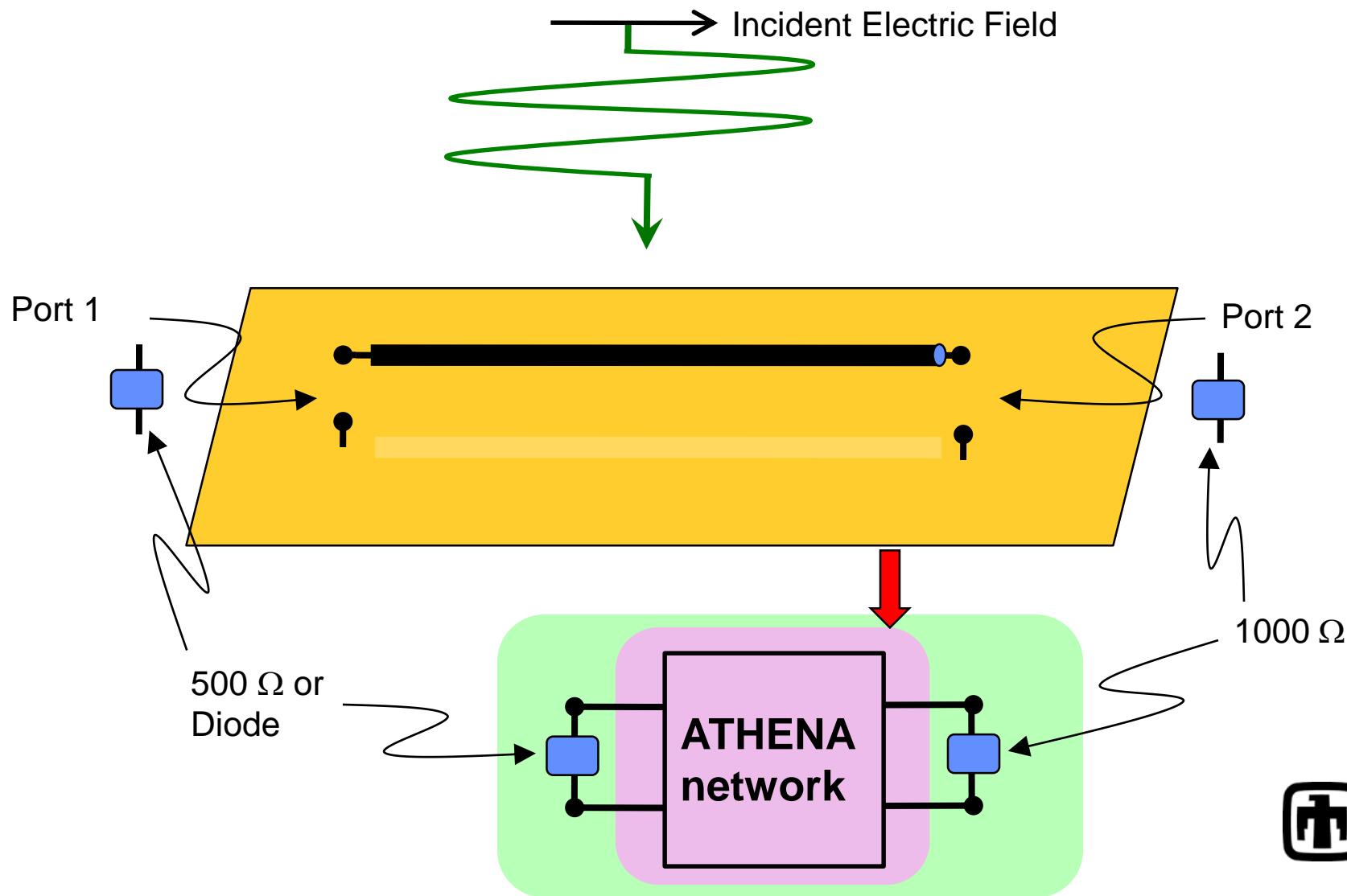
Wire above ground plane
with end terminations



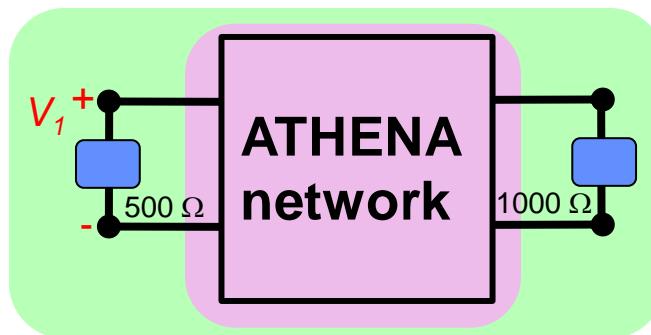
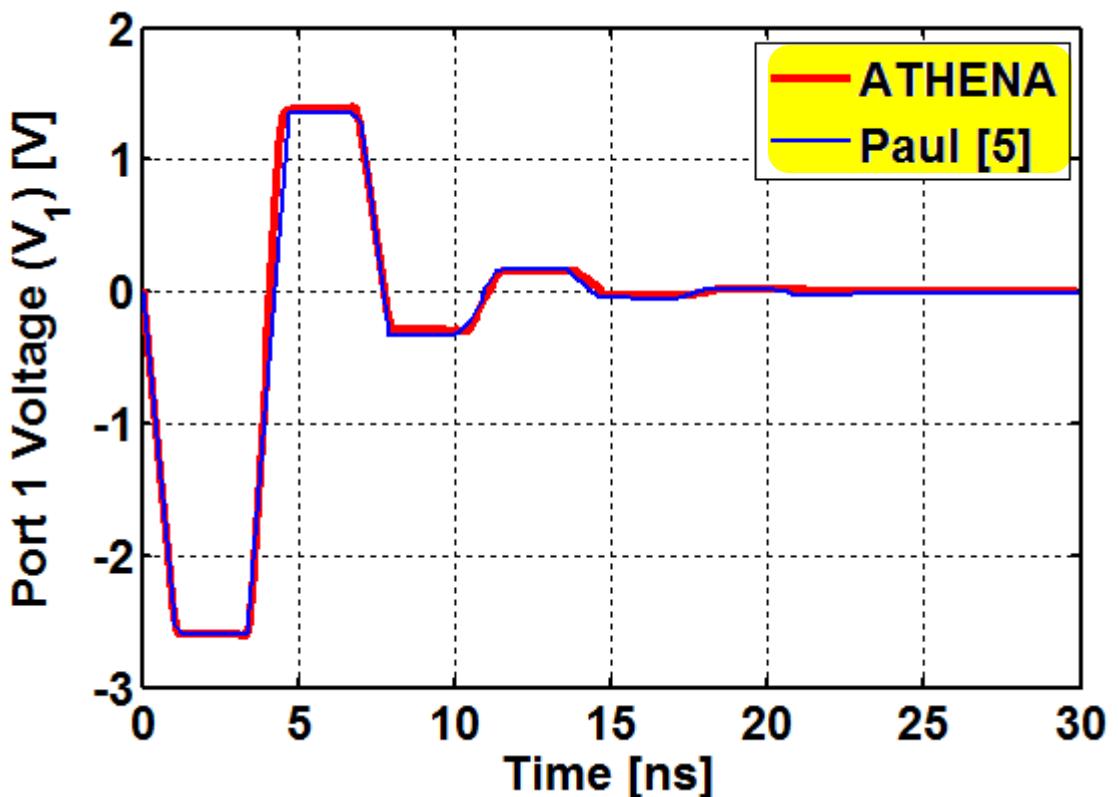
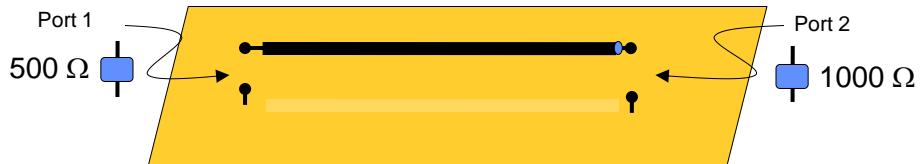
Not to scale



Example: 2-Port Network



2-Port : Linear Loads (500 Ω and 1000 Ω)

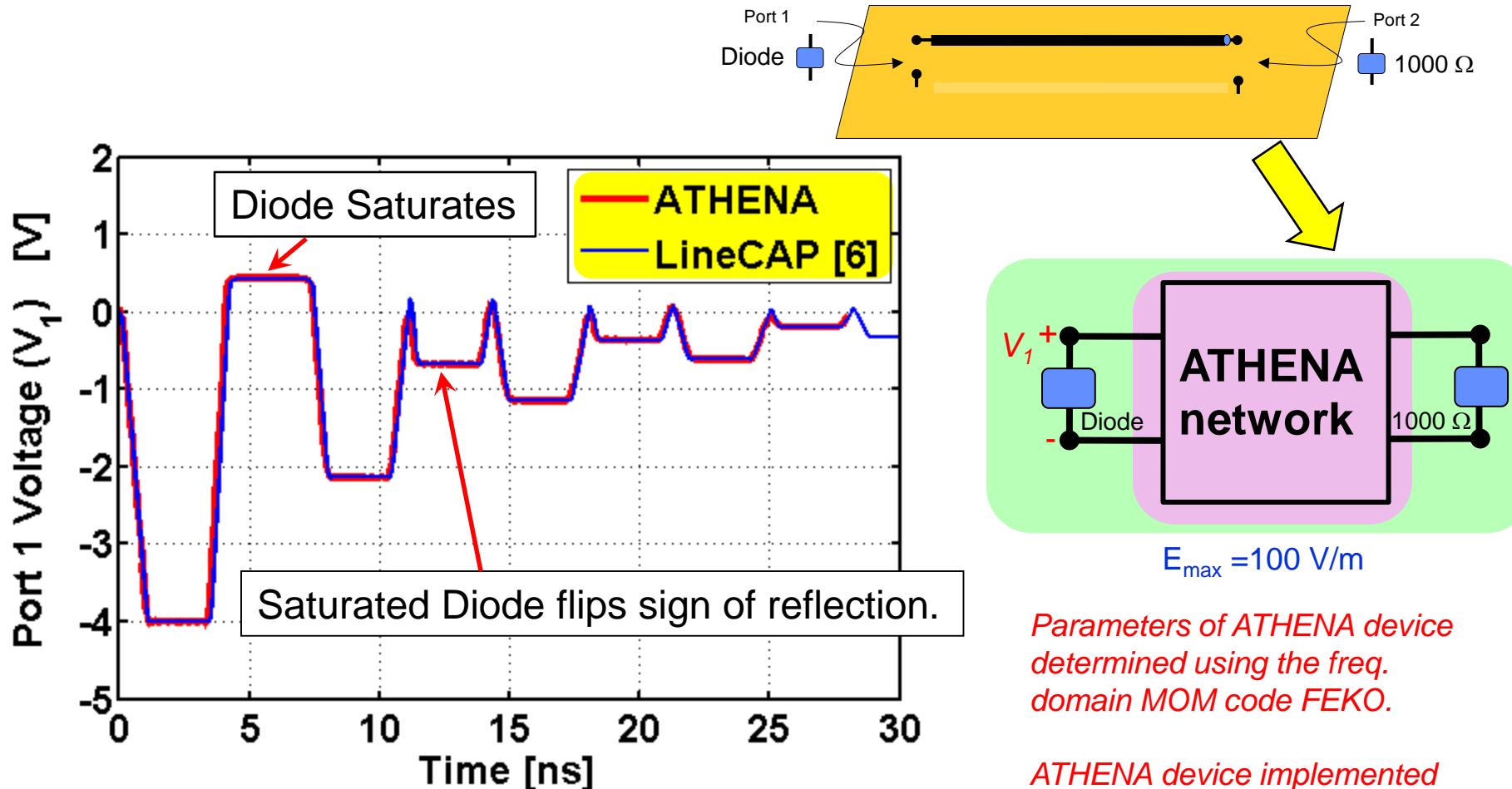


$$E_{\max} = 100 \text{ V/m}$$

Parameters of ATHENA device determined using the freq. domain MOM code FEKO.

ATHENA device implemented in Xyce.

2-Port : Linear (500Ω) and Non-Linear (Diode) Loads



Athena allows us to feed back nonlinear electronic response into the coupling problem.



Summary and Next Steps

- The **Active Thevenin Equivalent Network Approach (ATHENA)** allows us to link EMI & IEMI coupling to nonlinear circuit simulations in a fully consistent, bidirectional way.
- The ATHENA approach is general. It can utilize both time and frequency domain linear EM simulators, and harmonic balance and transient time domain non-linear circuit solvers.
- ATHENA is now implemented in the Spice code *ngspice* and Sandia's parallelized circuit code *Xyce*.
- Test cases (numerical and experimental) are continually being investigated to further the validation and development of the approach.
- Investigating causality issues associated this approach with the EM simulations are done in the frequency domain.