

# A Stochastic Programming Approach to the Design Optimization of Layered Physical Protection Systems

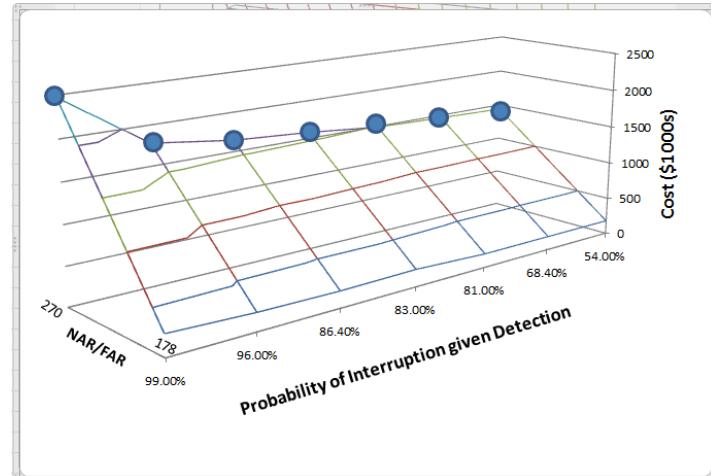
*Nathanael Brown, Katherine Jones, Alisa Bandlow, Lucas Waddell, and Linda Nozick*  
Sandia National Laboratories and Cornell University

# Optimization for Risk Analysis

- Research project was focused on likelihood of adversary success given an attack, not analyzing the likelihood of attack or consequence evaluation.
- Optimization model helps compare different risk mitigation strategies and includes representation of attacker strategy given those mitigations.
- Instead of an event tree or fault tree, represent all possible paths the attacker could take and use 1) probability of detection and 2) uncertain travel time at points along the paths to determine likelihood that the attacker reaches their target before interception, and trade off that likelihood against other metrics (cost, nuisance/false alarms)
- For integrated 3S analysis, useful to think about PRA extensions which:
  - Incorporate attacker capability and strategy in different environments
  - Use optimization or simulation optimization to recommend mitigation strategies that best represent the risk preferences of stakeholders (for example, balancing security and safety risk)

# Research Goals

- Create a mathematical framework to represent a multi-layered security system as a complex system
- Provide insight into the trade-off between performance and cost
- Requires:
  - Model of security architecture of a Physical Protection System (PPS)
  - Representation of intruder behavior
  - Consideration of Nuisance Alarm/False Alarm Rates (NAR/FAR) and impact on Alarm Station Operators (ASOs)
  - Optimization to estimate triple objective trade-off frontier



# Previous Work Referenced

- Bennett, H.A., The “EASI” Approach to Physical Security Evaluation (NUREG-760145), U.S. Nuclear Regulatory Commission, Washington, D.C., 1977.
  - Seminal work which defines calculation for probability of interruption ( $P_I$ )
- Garcia, M., The Design and Evaluation of Physical Protection Systems, Butterworth-Heinemann, Oxford, 2007.
  - Describes established approach to evaluating a PPS (Physical Protection System) using adversary sequence diagrams (ASDs) which describe the layers of protection that the attacker must pass through in order to reach a target
- Jang, S., S. Kwak, H. Yoo, J. Kim, and W. Yoon, Development of a Vulnerability Assessment Code for a Physical Protection System: Systematic Analysis of Physical Protection Effectiveness (SAPE), *Nuclear Engineering and Technology*, 41(5), 2009.
  - Develops a shortest path algorithm to determine the MVP (Most Vulnerable Path) in a security system

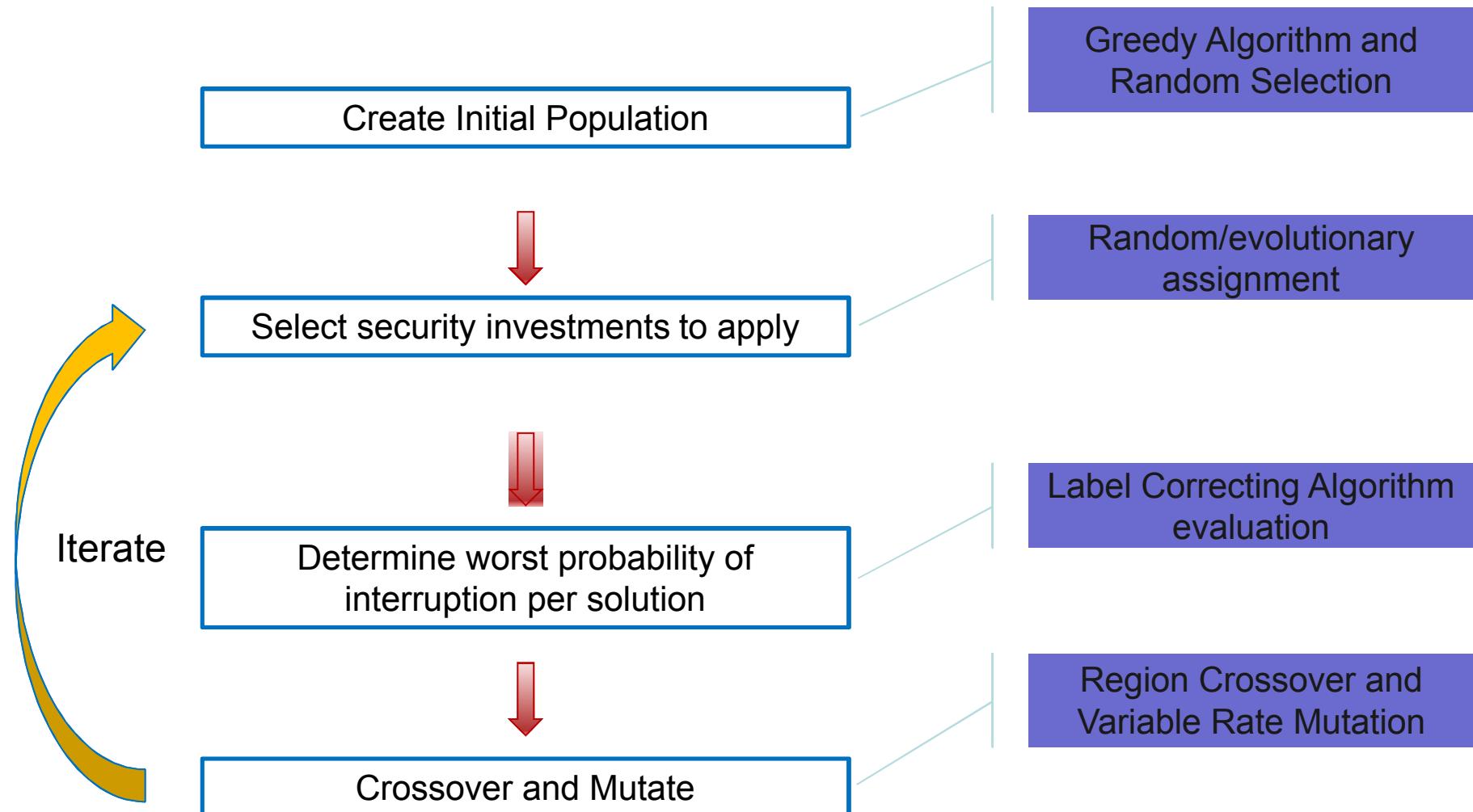
# Investment Optimization

- **Intruder goal:** Minimize the probability that the time remaining after detection will exceed the response time of the protective force (probability of interruption)
- **System owner goal:** Maximize the probability that the intruder will be interrupted given that the intruder can adapt to different investment strategies
- **System owner decision:** What technologies and physical barriers to invest in and where to place them subject to budget and false alarm rate limits



<http://levgrossman.com/tag/spy-vs-spy/>

# Defender Investment Optimization

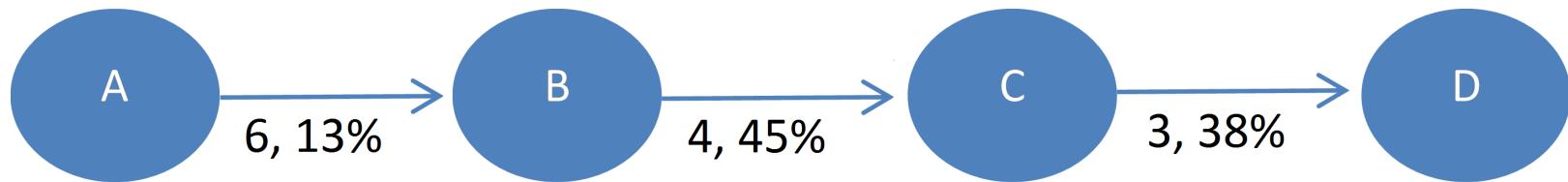


# Creating a (more) Realistic Model

| Characteristic                              | Simplified Model | Realistic Model  | Impact  |
|---|------------------|--|---|
| <b>Response force/intruder travel times</b> | Constant         | Variable (Gaussian)                                    | Addresses uncertainty; Gaussian improves computational efficiency |
| <b>Lighting/weather effects</b>             | None             | Decreases sensor detection probability                 | Improves system resiliency to multiple environmental scenarios    |
| <b>Effect of NAR/FAR on ASOs</b>            | None             | Longer assessment time (increased response force time) | Realistic NAR/FAR degradation with mitigation strategy            |
| <b>Variable Intruder Capabilities</b>       | None             | Intruders can degrade certain sensors/barriers         | Improves system resiliency to multiple intruder types             |

# Intruder path selection – Constant vs. Variable Time

- Intruder's objective is to minimize the probability of interruption ( $P_I$ ) which is the probability that the delay time after detection exceeds the response force time (RFT)



- If RFT is 6 minutes and *constant*, detection on link C-D leaves insufficient time to respond (and hence is irrelevant)


$$P_I = P_{D(AB)} + \bar{P}_{D(AB)} * P_{D(BC)} = 0.13 + (1-0.13)*0.45 = 0.52$$

- If RFT is 6 minutes and *Gaussian* with link travel times that are also *Gaussian*, must consider all links


$$P_I = P_{D(AB)} * P_{(RFT < T_{AD})} + \bar{P}_{D(AB)} * P_{D(BC)} * P_{(RFT < T_{BD})} + \bar{P}_{D(AB)} * \bar{P}_{D(BC)} * P_{D(CD)} * P_{(RFT < T_{CD})}$$

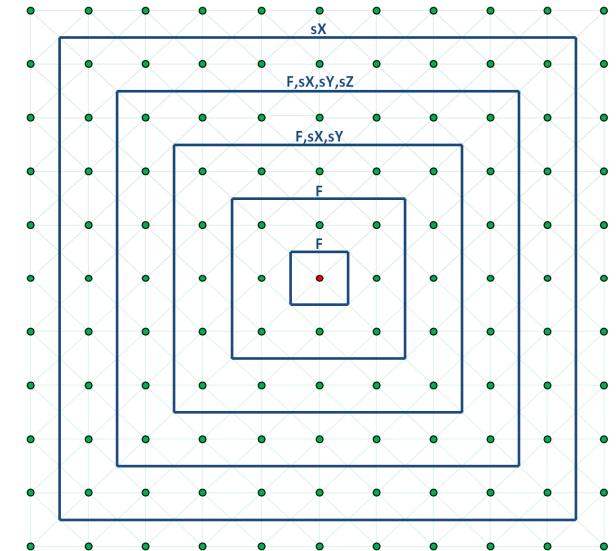
$$P_I = 0.44 \text{ (15% standard deviation)}$$

# Accounting for Alarm Queueing

- If NAR/FAR is high enough, ASOs (Alarm Station Operators) won't be able to process alarms "immediately"
  - ASOs will also likely not respond as quickly to alarms that are perceived as unreliable (trust lag time)
  - The *effective* RFT is increased by alarm queue time plus assessment time
- Probability of Interruption becomes:
  - $P_I = D_1 P(T_1) + \sum_{i=2}^n D_i P(T_i) \prod_{j=1}^{i-1} (1 - D_j)$
- Where
  - $P(T_i) = P(T_{R+AS} < T_{AT}) = \varphi \left[ \frac{\sum_{j \geq i} \mu_j - (\mu_R + \mu_{AS})}{\sum_{j \geq i} \sigma_j^2 + (\sigma_R^2 + \sigma_{AS}^2)} \right]$
  - $D_i$  = probability of detection on link  $i$
  - $R$  = Response Force Time (RFT)
  - $AS$  = ASO assessment time plus queue time
  - $AT$  = Attacker travel time

# Accounting for Multiple Scenarios

- Create multiple environmental effects (e.g., day, night, precipitation) which lowers the  $P_D$  (probability of detection) of certain sensors
- Allow “smart” intruders to degrade certain sensors (decrease the  $P_D$ ) and/or barriers (decrease travel time)
- Optimization evaluates a candidate architecture against all scenarios to determine the worst case  $P_I$  and best complementary investments
- A naïve designer might choose to create an “average” architecture which uses the average sensor/barrier values (across all scenarios) to conduct a single scenario optimization

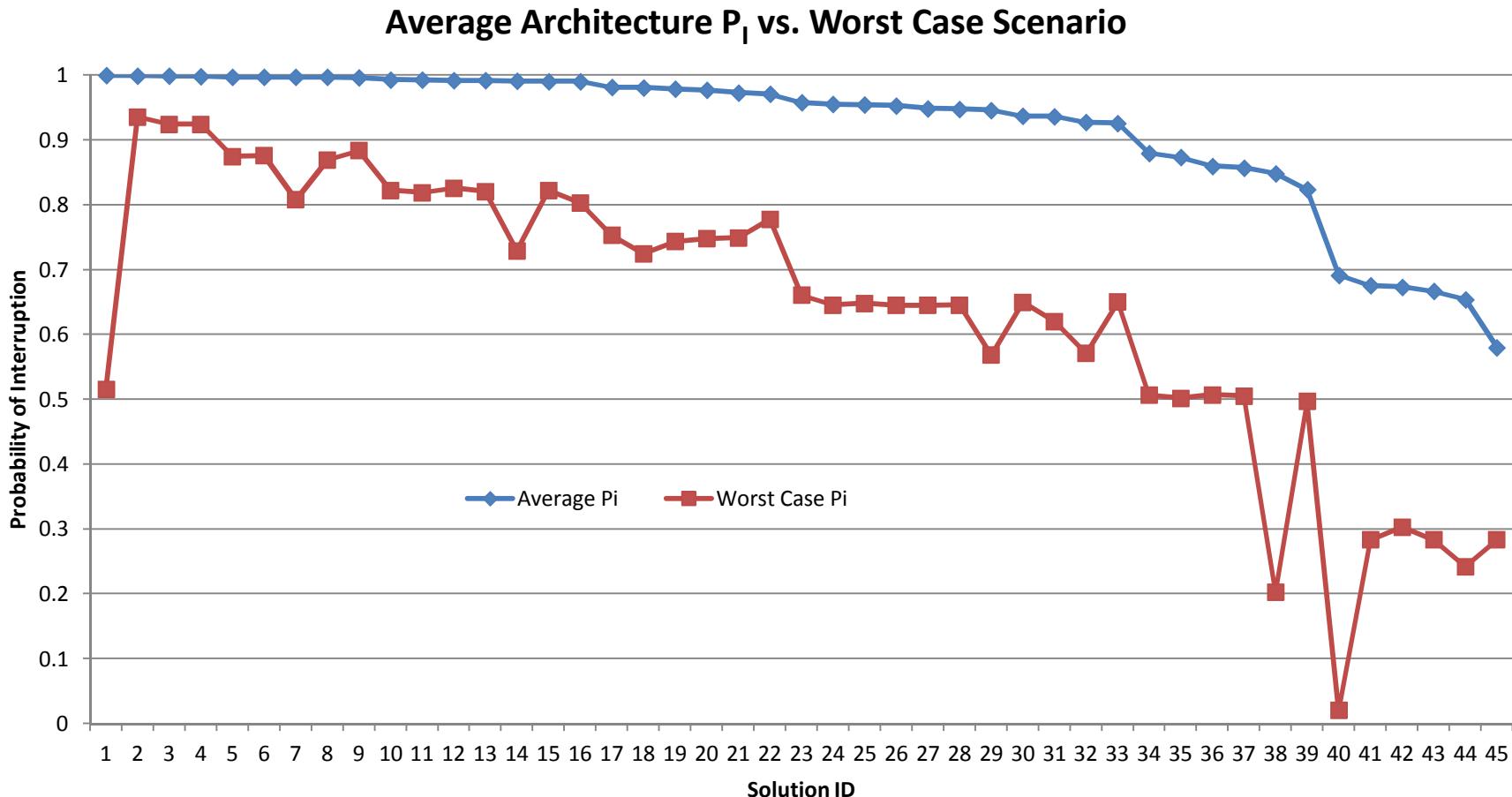


**Notional Security Architecture**

# Results

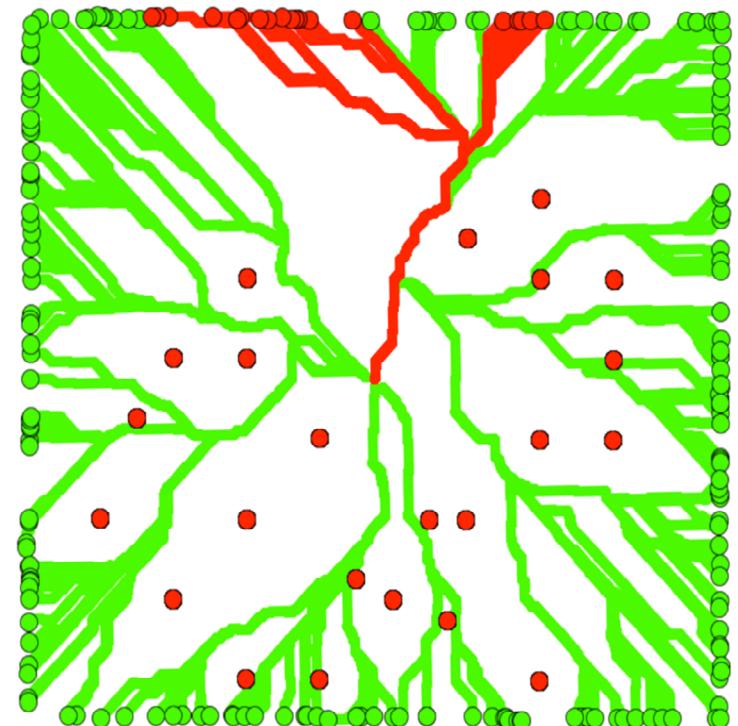
# Average Architecture Optimization

- Run single-scenario optimization against “average” architecture
  - Technology parameters have average value across all scenarios
- Average architecture performs poorly against worst case scenario



# Validation: Dante Simulation from MLS Input

- Use solutions from MLS engine to seed Dante scenarios
  - Perform batch analyses on solutions with random start positions for attacker
  - Allow human-in-the-loop to adjust scenarios for further examination
  - Comparison of  $P_i$  simulated value is within 1-2% of MLS calculation



# Summary

- Use an adaptive game-theoretic approach combined with stochastic optimization, so that the PPS design changes based on varying conditions and available options
- Create designs that are symmetric with respect to  $P$ , even when the physical layout is asymmetric
- Provides greater resiliency to variable:
  - Travel/response times
  - Environmental effects
  - Intruder behavior and/or abilities
  - ASO (Alarm Station Operator) behavior
- Allows a decision maker to choose architectures that trade off performance versus cost

# Backup

# Case Study – Multi-Scenario vs. Average

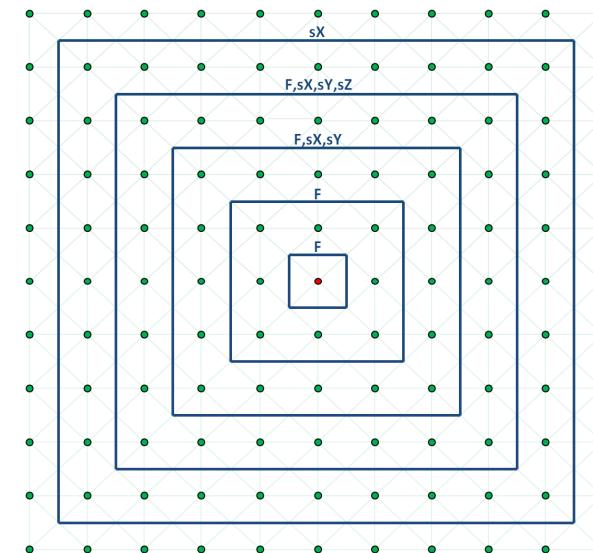
- Scenarios consist of four different environmental scenarios in combination with an intruder which is either uninformed or “smart”
- The smart intruder is able to degrade all site technologies
- Designer can choose from 3 different types of sensor (sX, sY and sZ) and 1 type of barrier (Fence) to be placed throughout the facility

| Environmental Conditions     | Abbreviation | Probability of Occurrence |
|------------------------------|--------------|---------------------------|
| Daytime No Precipitation     | DNP          | 0.5                       |
| Daytime With Precipitation   | DWP          | 0.1                       |
| Nighttime No Precipitation   | NNP          | 0.3                       |
| Nighttime With Precipitation | NWP          | 0.1                       |

Notional Environmental Scenarios

| Tech. | 10-year Cost (\$1000s) | NAR /FAR | Average | Worst Case |
|-------|------------------------|----------|---------|------------|
| sX    | \$100                  | 3        | 0.58    | 0.3        |
| sY    | \$200                  | 6        | 0.64    | 0.3        |
| sZ    | \$300                  | 12       | 0.61    | 0.47       |
| F     | \$3                    | 0        | 51.5    | 30         |
| ASO   | \$10,000               | N/A      | N/A     | N/A        |

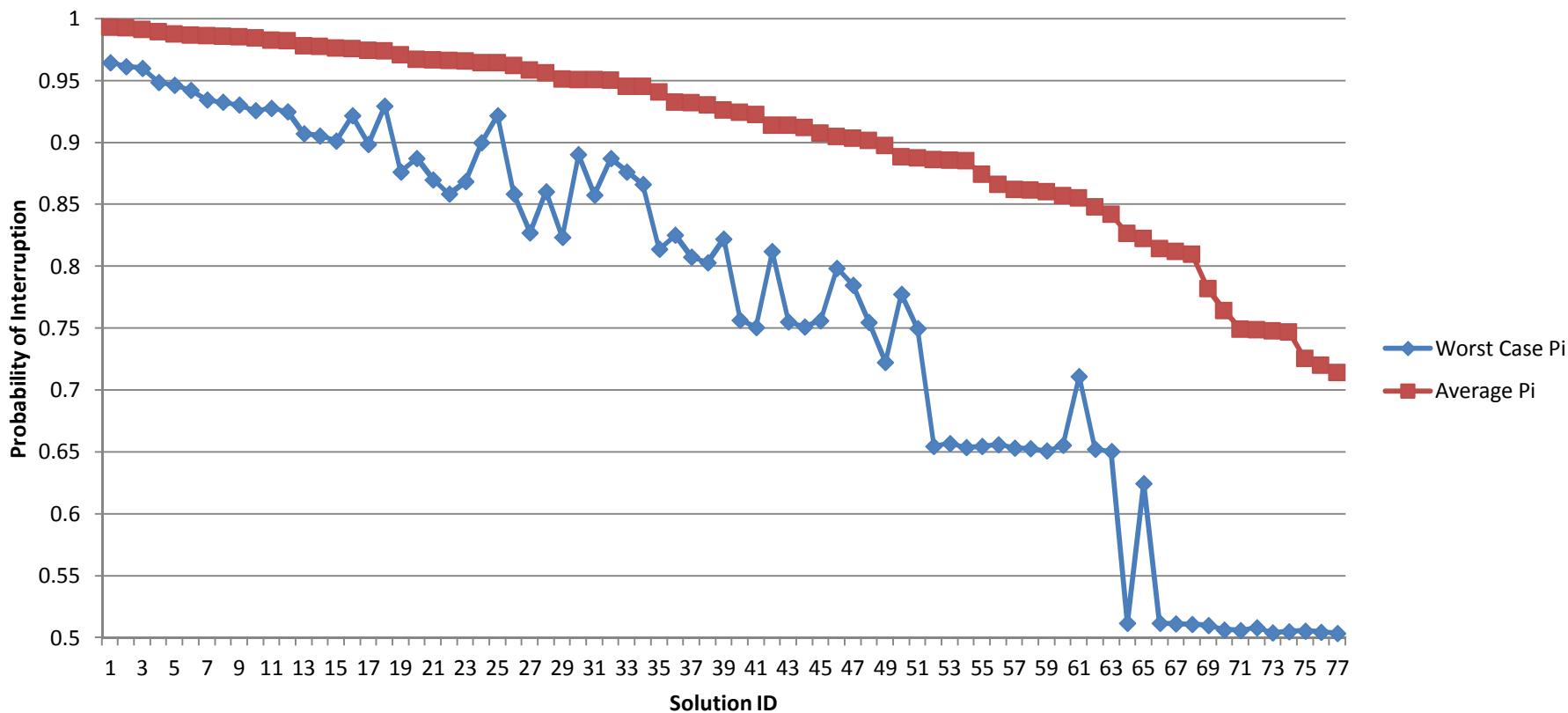
Notional Technology Investments



Notional Security Architecture

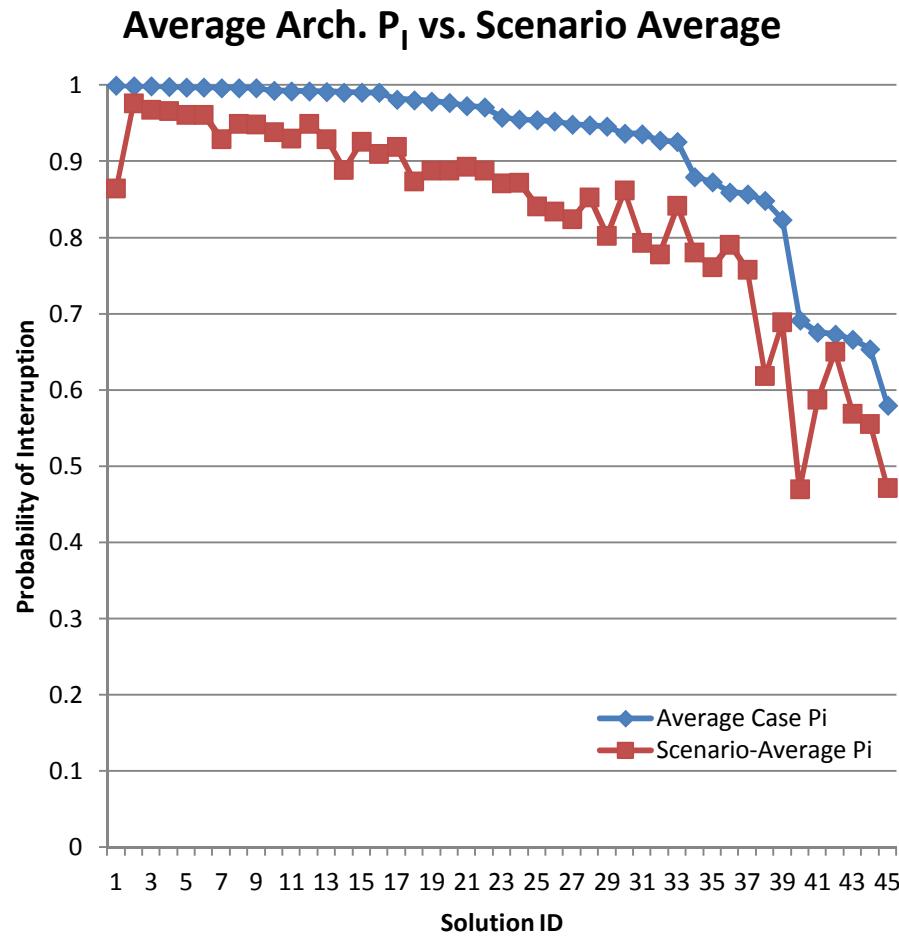
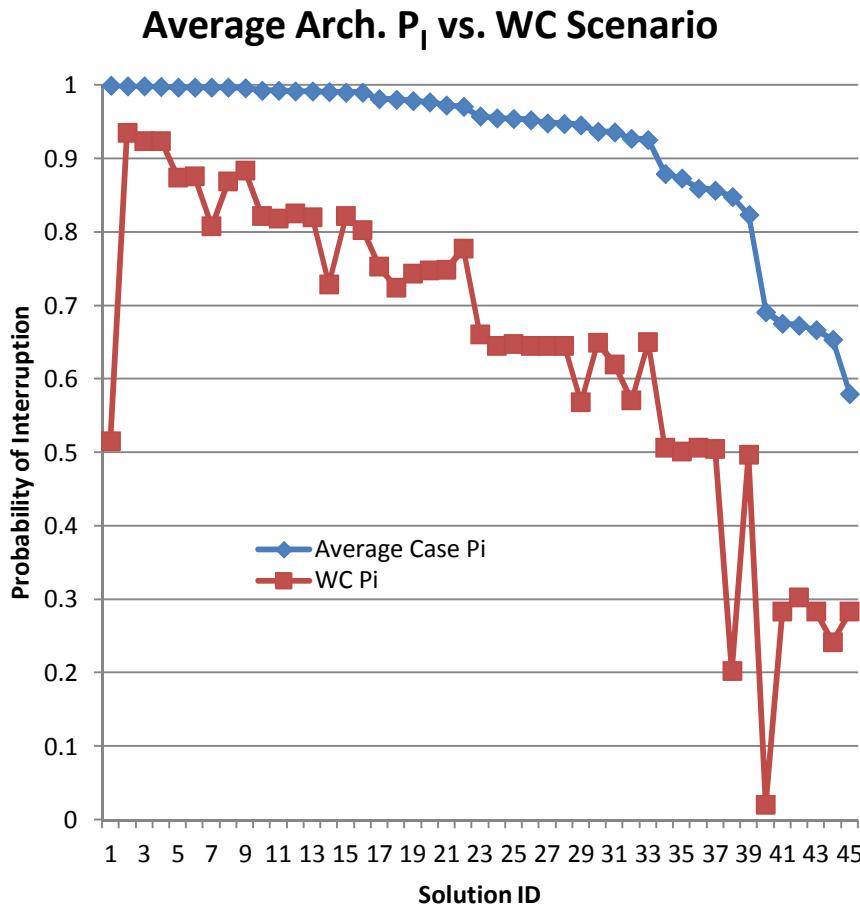
# Case Study – Worst Case vs. Average

- Run multi-scenario optimization where technology parameters vary according to the scenario
- Optimize against worst case  $P_i$  (Probability of Interruption)
- Average  $P_i$  across all scenarios is higher (often substantially)



# Average Architecture Optimization

- Run single-scenario optimization against “average” architecture
  - Technology parameters have average value across all scenarios
- Average architecture performs poorly against worst case scenario



# Technology Attributes by Scenario

- Eight different scenarios with different sensor and barrier performance characteristics
- The “average” value is weighted by the probability of each scenario
  - Probability of each type of intruder is equally likely (50%)
  - For example, NNP with no degradation has probability  $0.3*0.5 = 0.15$

## Notional intruder sensor/barrier degrade capabilities under different environmental conditions

| Tech. | DNP  |      | DWP  |      | NNP  |      | NWP  |      | Average | Worst Case |
|-------|------|------|------|------|------|------|------|------|---------|------------|
|       | N    | D    | N    | D    | N    | D    | N    | D    |         |            |
| sX    | 0.80 | 0.70 | 0.70 | 0.60 | 0.4  | 0.30 | 0.35 | 0.30 | 0.58    | 0.30       |
| sY    | 0.85 | 0.75 | 0.82 | 0.75 | 0.45 | 0.30 | 0.50 | 0.47 | 0.64    | 0.30       |
| sZ    | 0.60 | 0.55 | 0.95 | 0.8  | 0.53 | 0.47 | 0.85 | 0.75 | 0.61    | 0.47       |
| Fence | 60   | 30   | 70   | 40   | 70   | 40   | 80   | 60   | 51.5    | 30         |

\*Technology Impact: N = Normal, D = Degraded by Intruder