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# Rotational excitation of the interstellar $\text{NH}_2$ radical by $\text{H}_2$

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We present quantum close-coupling calculations for the rotational excitation of the interstellar amidogen radical  $\text{NH}_2$  due to collisions with  $\text{H}_2$  molecules. The calculations are based on a recent, high-accuracy full-dimensional  $\text{NH}_4$  potential energy surface adapted for rigid-rotor scattering calculations. The collisional cross section calculations are performed for all transitions among the first 15 energy levels of both *ortho*- and *para*- $\text{NH}_2$  and for total energies up to  $1500\text{ cm}^{-1}$ . Both *para*- and *ortho*- $\text{H}_2$  colliding partners are considered. The cross sections for collision with *para*- and *ortho*- $\text{H}_2$  are found to differ significantly, the magnitude of the *ortho*- $\text{H}_2$  ones being dominant. No strong propensity rules are observed but transitions with  $\Delta k_c = 0$  are slightly favored. *Published by AIP Publishing.* [<http://dx.doi.org/10.1063/1.4975324>]

## I. INTRODUCTION

Neutral nitrogen hydrides ( $\text{NH}$ ,  $\text{NH}_2$ , and  $\text{NH}_3$ ) are highly abundant species in a variety of astrophysical regions. Among them, the  $\text{NH}_2$  radical, even if not generally the most abundant one, is of key importance for the chemistry of these media. It was detected for the first time in the interstellar medium (ISM) by van Dishoeck *et al.*<sup>1</sup> who pointed out that this simple hydride is crucial for testing the production pathways of nitrogen-bearing molecules. Indeed, the  $\text{NH}_2$  chemistry is directly related to that of the abundant and ubiquitous ammonia,  $\text{NH}_3$ . In addition,  $\text{NH}_2$  exhibit spin symmetry states whose relative abundances are sensitive to the  $\text{H}_2$  *ortho*-to-*para* ratio (OPR) in the gas phase.  $\text{NH}_2$  observations<sup>2</sup> may be able to put constraints on the  $\text{H}_2$  OPR in dense gas.

The Infrared Space Observatory was later used to observe infrared absorption lines of  $\text{NH}_2$ <sup>3,4</sup> and recently, the Herschel Space Observatory<sup>5</sup> with the Heterodyne Instrument for the Far-Infrared (HIFI)<sup>6</sup> allowed the observation of several low-lying rotational transitions of  $\text{NH}_2$  at a very high spectroscopic resolution.<sup>7</sup> These (absorption) lines were employed to derive  $\text{NH}:\text{NH}_2:\text{NH}_3$  abundance ratios of  $\sim 2:1:1$  in lukewarm diffuse clouds<sup>8</sup> and  $\sim 3:1:20$  in the colder envelope of low-mass protostars.<sup>9</sup> Emission lines were also detected more recently in denser and hot ISM regions.<sup>2</sup> In addition, anomalous (non statistical) *ortho*-to-*para* ratios of  $\text{NH}_2$  and  $\text{NH}_3$  were derived in the diffuse gas.<sup>2,10</sup> These ratios were successfully reproduced by gas-phase models including a rigorous nuclear-spin chemistry,<sup>9,11</sup> suggesting that  $\text{NH}_2$ , just like  $\text{NH}_3$ , is mainly formed in the

gas-phase via a series of successive hydrogen abstraction reactions  $\text{NH}_n^+ + \text{H}_2$  ( $n = 0-3$ ) followed by electronic dissociative recombination. A recent study has also emphasized the importance of the H-exchange reaction  $\text{NH}_2 + \text{H}$  in the *ortho*-*para* conversion of  $\text{NH}_2$ .<sup>12</sup>

However, the analysis of the  $\text{NH}_2$  rotational spectra, especially those in emission, was hampered by the lack of collisional rate coefficients. Without these data, only approximate estimates of the molecular column density are possible assuming local thermodynamic equilibrium (LTE), which is generally not a good approximation. Persson *et al.*<sup>2</sup> estimated collisional rate coefficients assuming quenching rate coefficient of  $5 \times 10^{-11}\text{ cm}^3\text{ s}^{-1}$  and state-specific downward rates for radiatively allowed transitions that scale in proportion to radiative line strengths. Such estimates are very approximate and the accurate determination of the  $\text{NH}_2$  abundance would greatly benefit from accurate collisional data. The main collider in the dense ISM is generally molecular hydrogen,  $\text{H}_2$ .

Scattering studies implying nonlinear polyatomic molecules and  $\text{H}_2$  are still sparse. To date, calculations of rate coefficients for the collisional excitation by *para*- and *ortho*- $\text{H}_2$  (hereafter *p*- $\text{H}_2$  and *o*- $\text{H}_2$ , respectively) have been performed only for the four interstellar molecules  $\text{H}_2\text{CO}$ ,<sup>13</sup>  $\text{NH}_3$ ,<sup>14</sup>  $\text{CH}_3\text{OH}$ ,<sup>15</sup>  $\text{H}_2\text{O}$ ,<sup>16</sup> and  $\text{SO}_2$ .<sup>17</sup>

To the best of our knowledge, there are no collisional data available for the  $\text{NH}_2$ - $\text{H}_2$  system. The only relevant study for astrophysics implying the  $\text{NH}_2$  molecules is the measurement of integral cross sections for  $\text{NH}_2$ -He rotational transitions performed by Dagdigan.<sup>18</sup> However, no rate coefficients were given in this work.  $\text{NH}_2$ -H collisions were also studied<sup>19</sup> but the  $\text{NH}_2$  molecule was in its first excited electronic state that is negligibly populated in astrophysical media.

$\text{NH}_2$  is an asymmetrical rotor with two forms caused by the different relative orientations of the hydrogen nuclear

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spins. In collision with  $\text{H}_2$ , the two forms behave like two distinct species: *ortho*- $\text{NH}_2$  and *para*- $\text{NH}_2$  (hereafter denoted as *o*- $\text{NH}_2$  and *p*- $\text{NH}_2$ , respectively). In addition,  $\text{NH}_2$  has a complex rotational structure resulting from the open-shell character of the  $\text{NH}_2$  ground electronic state  $^2B_1$ . Hence, each rotational level is split by spin-rotation interaction in a fine structure of two sublevels identified by the total angular momentum  $j_1$  with  $\vec{j}_1 = \vec{N}_1 + \vec{S}$  (where  $N_1$  is the rotational angular momentum and  $S$  is the electronic spin). Moreover, fine structure levels are further split into three components through hyperfine interactions, due to the coupling between the nitrogen nuclear spin and the total angular momentum  $j_1$ . Finally, a second hyperfine structure resulting from the coupling between the nuclear spins of the hydrogen nuclei splits all *o*- $\text{NH}_2$  sublevels into three new sublevels.

The calculation of collisional cross sections taking into account this complex structure is an extremely challenging task. Calculations of collisional data for open-shell molecules in collision with  $\text{H}_2$  have been achieved only recently<sup>20</sup> for linear molecules and cannot be easily extended to a polyatomic top. This is why, in the present work, we neglect the fine and hyperfine structure of the  $\text{NH}_2$  target and we provide data for transitions between rotational levels. Collisional data including these specific structures may be deduced from the present calculations using decoupling approximations.<sup>21,22</sup>

In this paper, we used a new accurate full-dimensional  $\text{NH}_4$  potential energy surface (PES)<sup>23</sup> to compute the cross sections for the collisional excitation of the first 15 rotational levels of both *o*- and *p*- $\text{NH}_2$  by  $\text{H}_2$ . The paper is organized as follows. The PES and the scattering calculations are presented in Section II. In Section III, we report state-to-state resolved cross sections for the rotational excitation of  $\text{NH}_2$  by  $\text{H}_2$ . Concluding remarks are drawn in Section IV.

## II. METHODS

### A. Potential energy surface

The  $\text{NH}_2$  radical is known to react with  $\text{H}_2$  to form  $\text{NH}_3$  through an exothermic pathway by a direct hydrogen abstraction mechanism. This reactive channel  $\text{NH}_2 + \text{H}_2 \rightarrow \text{NH}_3 + \text{H}$  was found to have a barrier of  $3340 \text{ cm}^{-1}$ .<sup>23</sup> The reaction is thus quite slow with rate coefficients lower than  $10^{-15} \text{ cm}^3 \text{ s}^{-1}$  for temperatures lower than 500 K.<sup>23,24</sup> Under such circumstances, neglecting the reactive pathway in the treatment of the  $\text{NH}_2\text{--H}_2$  collision should have only a small influence on the description of the inelastic processes,<sup>25,26</sup> as long as low to moderate collision energies are considered. We also note that the hydrogen exchange process is also negligibly small under such conditions.

An accurate rigid-rotor five-dimensional PES was then constructed for the  $\text{NH}_2\text{--H}_2$  system in its electronic and vibrational ground state, suitable for low-energy inelastic rotational calculations, from the recently computed nine-dimensional global PES of  $\text{NH}_4$ .<sup>23</sup> This PES was determined at the UCCSD(T)-F12a/aug-cc-pVTZ level of theory and the *ab initio* points were fitted using the permutation-invariant polynomial neutral network (PIP-NN) method<sup>27</sup> with a root mean squared error (RMSE) of  $27 \text{ cm}^{-1}$ . The RMSE of  $27 \text{ cm}^{-1}$  is for the full nine-dimensional PES (including the reactive path).

The fitting RMSE for the non-reactive  $\text{NH}_2\text{--H}_2$  region relevant for this work is much smaller, of the order of few  $\text{cm}^{-1}$ .

In this work, the intermolecular potential is described as a function of five coordinates, namely, the intermolecular distance  $R$  from the  $\text{NH}_2$  center of mass to the  $\text{H}_2$  center of mass, and four relative angles ( $\theta$ ,  $\varphi$ ) and ( $\theta'$ ,  $\varphi'$ ) which describe, respectively, the collision direction and the  $\text{H}_2$  orientation relative to the  $\text{NH}_2$  body-fixed system. The body-fixed Jacobi coordinate system used in our calculations is presented in Fig. 1.

As the original routine from Li and Guo<sup>23</sup> employs internuclear coordinates, the following transformation was employed to determine the Cartesian positions of the two hydrogen atoms ( $\text{H}_a$  with coordinates  $x_a, y_a, z_a$  and  $\text{H}_b$  with coordinates  $x_b, y_b, z_b$ ) of the  $\text{H}_2$  molecule in the  $\text{NH}_2$  body-fixed coordinate system:

$$x_a = R \sin \theta \cos \varphi + r_{\text{H}_2} \sin \theta' \cos \varphi' \frac{m_{\text{H}}}{2m_{\text{H}}}, \quad (1)$$

$$y_a = R \sin \theta \sin \varphi + r_{\text{H}_2} \sin \theta' \sin \varphi' \frac{m_{\text{H}}}{2m_{\text{H}}}, \quad (2)$$

$$z_a = R \cos \theta + r_{\text{H}_2} \cos \theta' \frac{m_{\text{H}}}{2m_{\text{H}}}, \quad (3)$$

$$x_b = R \sin \theta \cos \varphi - r_{\text{H}_2} \sin \theta' \cos \varphi' \frac{m_{\text{H}}}{2m_{\text{H}}}, \quad (4)$$

$$y_b = R \sin \theta \sin \varphi - r_{\text{H}_2} \sin \theta' \sin \varphi' \frac{m_{\text{H}}}{2m_{\text{H}}}, \quad (5)$$

$$z_b = R \cos \theta - r_{\text{H}_2} \cos \theta' \frac{m_{\text{H}}}{2m_{\text{H}}}, \quad (6)$$

where  $r_{\text{H}_2}$  is the bond length of  $\text{H}_2$  fixed at its vibrationally averaged distance  $\langle r_{\text{H}_2} \rangle_0 = 1.449 a_0$ . The  $\text{NH}_2$  molecule, which lies in the (*xoz*) plane (see Fig. 1), was also kept rigid with an averaged geometry taken from the experimental work of Davies *et al.*:<sup>28</sup>  $\langle r_{\text{NH}} \rangle_0 = 1.936 a_0$  and  $\langle \text{HNH} \rangle_0 = 103.33^\circ$ . We note that employing state-averaged geometries is a reliable approximation for including zero-point vibrational effects within a rigid-rotor PES, as discussed in previous studies on  $\text{H}_2\text{O--H}_2$ .<sup>29,30</sup> In addition, it was shown recently for the  $\text{CO--H}_2$  system that state-averaged geometries also give scattering results very close to full-dimensional calculations.<sup>31</sup>

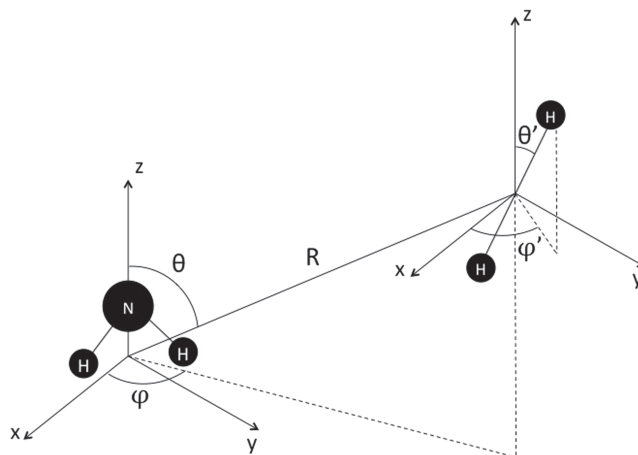


FIG. 1. Jacobi coordinate system of the  $\text{NH}_2\text{--H}_2$  complex.

Here, the lowest vibrational bending frequency of  $\text{NH}_2$  is  $\approx 1500 \text{ cm}^{-1}$ .<sup>32</sup> Hence, vibrational excitation is closed at the investigated energies and can be safely neglected in the scattering calculations.

The original fit of Li and Guo<sup>23</sup> was employed to generate interaction energies on a very dense grid of 81 000 geometries in  $R, \theta, \varphi, \theta'$ , and  $\varphi'$ . An asymptotic potential of  $2062.47 \text{ cm}^{-1}$  (corresponding to the above monomer averaged geometries) was subtracted from these interaction energies. 27 values in  $R$  were selected in the range  $[3.75\text{--}20.00]a_0$  and this radial grid was combined with 3000 random angular geometries  $\theta, \varphi, \theta', \varphi'$ . The PES  $V(R, \theta, \varphi, \theta', \varphi')$  was expanded over angular functions for all  $R$ -distances using the following expression:<sup>33</sup>

$$V(R, \theta, \varphi, \theta', \varphi') = \sum v_{p_1 q_1 p_2 p}(R) t_{p_1 q_1 p_2 p}(\theta, \varphi, \theta', \varphi'), \quad (7)$$

where

$$t_{p_1 q_1 p_2 p}(\theta, \varphi, \theta', \varphi') = (1 + \delta_{q_1 0})^{-1} \sum \begin{pmatrix} p_1 & p_2 & p \\ r_1 & r_2 & r \end{pmatrix} \times Y_{p_2 r_2}(\theta', \varphi') Y_{p r}(\theta, \varphi) \times \left[ \delta_{q_1 r_1} + (-1)^{p_1 + q_1 + p_2 + p} \delta_{-q_1 r_1} \right], \quad (8)$$

where  $(3j)$  is a “3- $j$ ” symbol,  $Y_{pq}$  is a spherical harmonic,  $\delta_{ij}$  is a Kronecker delta, equal to one if  $i = j$  and to zero otherwise, and the sum is over  $r_1, r_2, r$ . The indices  $p_1, p_2$ , and  $p$  refer to the tensor ranks of the angle dependence of the  $\text{NH}_2$  orientation, the  $\text{H}_2$  orientation, and the collision vector orientation, respectively. In Eq. (8), the index of the  $C_{2v}$  symmetry of  $\text{NH}_2$  requires that  $q_1$  be even and the homonuclear symmetry of  $\text{H}_2$  similarly constrains  $p_2$  to be even. The expansion coefficients  $v_{p_1 q_1 p_2 p}(R)$  were obtained through a least-squares fit on the random grid of 3000 orientations at each intermolecular separation. We initially included all anisotropies up to  $p_1 = 10$ ,  $p_2 = 6$ , and  $p = 16$ , resulting in 810 basis functions. We then selected only significant terms using a Monte Carlo error estimator (defined in the work of Rist and Faure<sup>34</sup>), resulting in a final set of 146 expansion functions with anisotropies up to  $p_1 = 10$ ,  $p_2 = 6$ , and  $p = 13$ . The RMSE was found to be lower than  $1 \text{ cm}^{-1}$  for  $R > 4.75 a_0$ . A cubic spline interpolation of the coefficients  $v_{p_1 q_1 p_2 p}(R)$  was finally performed over the whole  $R$  range and it was smoothly connected using a switching function to standard extrapolations (exponential and power laws at the short and long-range, respectively) in order to provide continuous radial expansion coefficients for the scattering calculations. Figure 2 shows a sample of expansion coefficients ( $v_{p_1 q_1 p_2 p}$ ) of the  $\text{NH}_2\text{--H}_2$  PES, as a function of intermolecular distance  $R$ .

Two-dimensional plots of the  $\text{NH}_2\text{--H}_2$  PES are presented in Figs. 3–5.

The global minimum of the 5D fitted PES is located at  $\theta = \theta' = 0^\circ$  with a depth of  $-213.00 \text{ cm}^{-1}$  and at an intermolecular distance  $R = 6.05 a_0$ . This minimum corresponds to the most stable configuration of the  $\text{NH}_2\text{--H}_2$  complex so that  $\text{H}_2$  is approaching the N atom of the  $\text{NH}_2$  molecule along the  $C_2$  axis.

In Fig. 3, we show a contour plot of the interaction energy for fixed  $\theta' = \varphi = \varphi' = 0^\circ$ . This plot shows the anisotropy of the interaction with respect to the  $\text{NH}_2$  rotation.

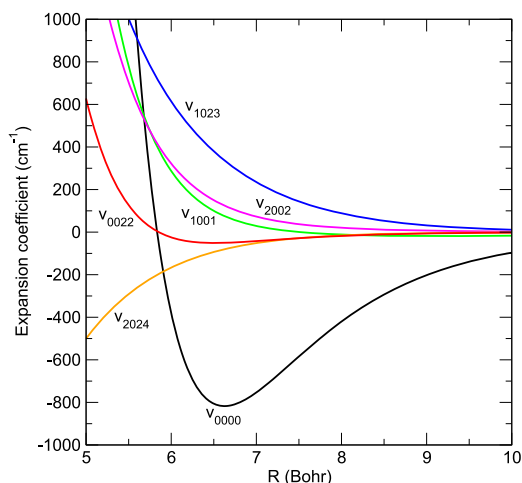


FIG. 2. Sample of expansion coefficients ( $v_{p_1 q_1 p_2 p}$ ) of the  $\text{NH}_2\text{--H}_2$  PES, as function of intermolecular distance  $R$ , for  $p_1 = 0, 1, 2$  and  $p_2 = 0, 2$ .

Figure 4 shows the interaction energies for  $\varphi = \varphi' = 0^\circ$  and  $R = 6.05 a_0$ . We found a relatively strong anisotropy of the PES with respect to the  $\text{NH}_2$  and  $\text{H}_2$  rotation. It means that the rotational state of  $\text{H}_2$  will probably influence the magnitude of the  $\text{NH}_2$  excitation cross sections.

A secondary minimum is found at  $\theta = 113^\circ$ , with an energy deduced from our fit of  $-122.29 \text{ cm}^{-1}$ . It occurs when  $\text{H}_2$  is approaching along the direction of the  $\text{NH}$  bond and  $\text{H}_2$  is perpendicular to the  $\text{NH}_2$  plane ( $\theta' = \varphi' = 90^\circ$ ). The contour plot is displayed in Fig. 5.

Finally, it is interesting to compare the  $\text{NH}_2\text{--H}_2$  with the  $\text{H}_2\text{O--H}_2$  PES of Valiron *et al.*<sup>29</sup> The shape of the two PESs is quite similar. Indeed, Valiron *et al.*<sup>29</sup> reported that the  $\text{H}_2\text{O--H}_2$  global minimum is at the same configuration than that of  $\text{NH}_2\text{--H}_2$ , the well depth of  $\text{H}_2\text{O--H}_2$  and  $\text{NH}_2\text{--H}_2$  PESs being similar ( $-235.14 \text{ cm}^{-1}$  for the  $\text{H}_2\text{O--H}_2$  complex vs.  $-213 \text{ cm}^{-1}$  for the  $\text{NH}_2\text{--H}_2$  complex).

Furthermore, for both  $\text{NH}_2\text{--H}_2$  and  $\text{H}_2\text{O--H}_2$  PESs, a secondary minimum is found when  $\text{H}_2$  is approaching along the direction of the  $\text{NH}$  ( $\text{OH}$ ) bond with the  $\text{H}_2$  molecule perpendicular to the  $\text{NH}_2$  ( $\text{H}_2\text{O}$ ) plane). The  $\text{H}_2\text{O--H}_2$  secondary minimum found at  $\theta = 119^\circ$  and  $\theta' = 90^\circ$  with a well depth equal to  $-199.40 \text{ cm}^{-1}$  is, however, deeper than that of  $\text{NH}_2\text{--H}_2$  ( $-122.29 \text{ cm}^{-1}$ ) found at  $\theta = 113^\circ$  and  $\theta' = 90^\circ$ .

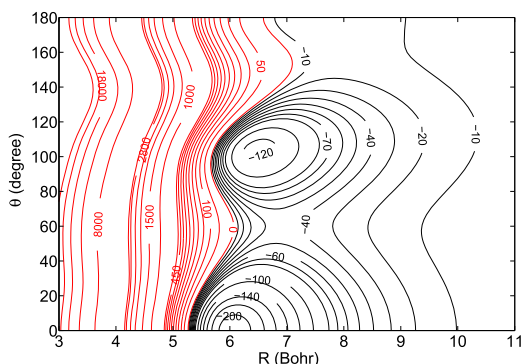


FIG. 3. Contour plot of the 5D PES as function of  $R, \theta$  for fixed  $\theta' = \varphi = \varphi' = 0^\circ$ . Energy is in  $\text{cm}^{-1}$ .

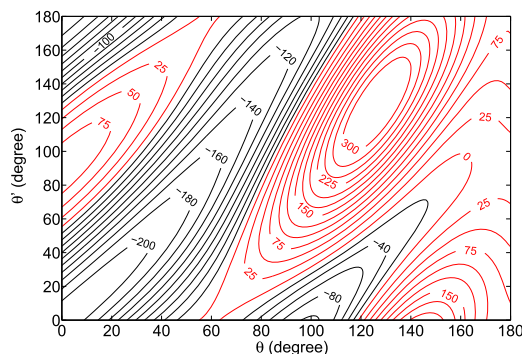


FIG. 4. Contour plot of the 5D PES as function of  $\theta$ ,  $\theta'$  for fixed  $\varphi = \varphi' = 0^\circ$  at an intermolecular separation of  $R = 6.05 a_0$ . Energy is in  $\text{cm}^{-1}$ .

## B. Scattering calculations

We used the fitted  $\text{NH}_2\text{-H}_2$  PES to study the rotational excitation of  $\text{NH}_2$  by  $\text{H}_2$ .

We focus only on the collisional excitation of the rotational states of  $\text{NH}_2$ , since the computation of fine/hyperfine structure resolved cross sections is a true challenge. The rotational energy levels of  $\text{NH}_2$  are labelled by three numbers: the angular momentum  $N_1$  and the pseudo-quantum numbers  $k_a$  and  $k_c$  which correspond to the projection of  $N_1$  along the axis of the least and greatest moments of inertia, respectively. The *para* states correspond to  $k_a + k_c$  odd and the *ortho* states to  $k_a + k_c$  even. Extension to the fine/hyperfine structure using approximate treatment will be considered in a future study.

The rotational levels of  $\text{NH}_2$  were obtained using the rotational constants from Müller *et al.*<sup>35</sup> Figure 6 shows the rotational energy levels of both *o*- and *p*- $\text{NH}_2$ . For the  $\text{H}_2$

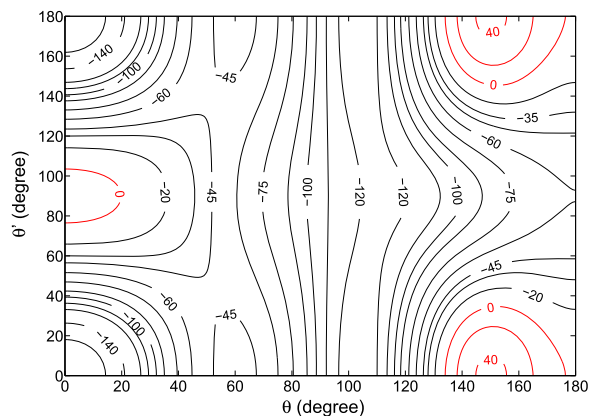


FIG. 5. Contour plot of the 5D PES for fixed  $\varphi = 0^\circ$ ,  $\varphi' = 90^\circ$ , and  $R = 6.61 a_0$  corresponding to the secondary minimum. Energy is in  $\text{cm}^{-1}$ .

molecule, the rotational states are denoted by  $j_2$  throughout this paper. The *para* states of  $\text{H}_2$  have even rotational states  $j_2 = 0, 2, \dots$  and the *ortho* states have odd rotational states,  $j_2 = 1, 3, \dots$

As inelastic (nonreactive) collisions cannot interconvert the *ortho*- and *para*-forms, the calculations were done separately for the four spin combinations, namely, *p*- $\text{NH}_2$ -*p*- $\text{H}_2$ , *p*- $\text{NH}_2$ -*o*- $\text{H}_2$ , *o*- $\text{NH}_2$ -*p*- $\text{H}_2$ , and *o*- $\text{NH}_2$ -*o*- $\text{H}_2$ .  $\text{NH}_2$  molecule is treated as a rigid rotor. We used the quantum close-coupling (CC) approach to obtain the inelastic cross sections as described in Phillips *et al.*<sup>36</sup> All scattering calculations have been performed with the version 14 of the MOLSCAT code.<sup>37</sup> The coupled equations were solved using the modified log-derivative airy propagator of Alexander and Manolopoulos.<sup>38</sup> The reduced mass of the system is 1.790 367 amu.

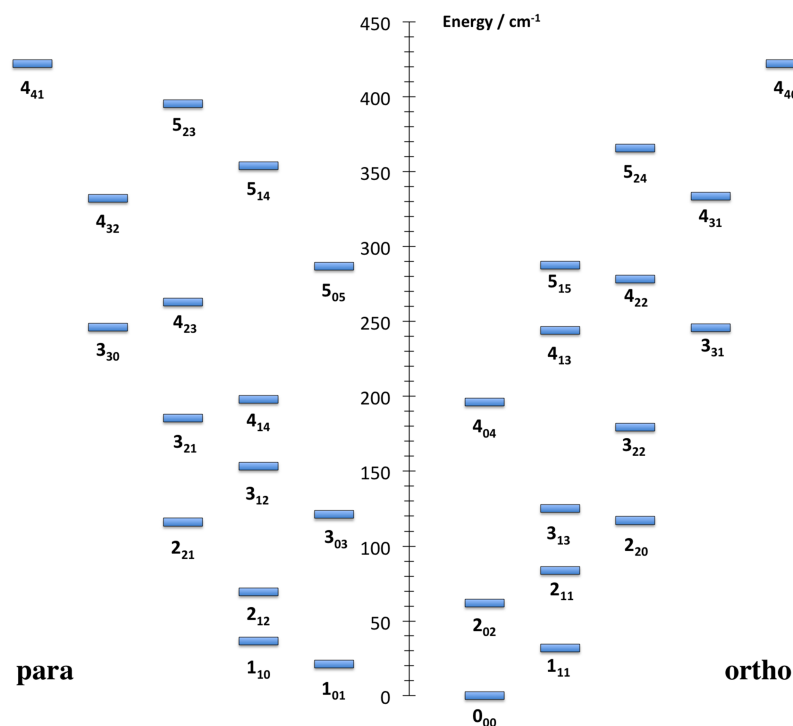


FIG. 6. Diagram of the rotational energy levels of  $\text{NH}_2$ . The levels are labelled by the  $N_{1k_a k_c}$  quantum numbers.

Inelastic cross sections were obtained between levels with a rotational energy  $E_{\text{rot}} \leq 422 \text{ cm}^{-1}$ , that is, up to  $N_{1k_a k_c} = 4_{40}$  for *o*-NH<sub>2</sub> and  $N_{1k_a k_c} = 4_{41}$  for *p*-NH<sub>2</sub>.

The collisions were studied for the total energy ranging from 32 to  $1500 \text{ cm}^{-1}$ . The integration parameters were chosen to ensure convergence of the cross sections in this range. We carefully spanned the energy range to guarantee a good description of the resonances. For collision with *p*-H<sub>2</sub>, the energy steps are  $0.2 \text{ cm}^{-1}$  below  $100 \text{ cm}^{-1}$ ,  $0.5 \text{ cm}^{-1}$  from 100 to  $200 \text{ cm}^{-1}$ ,  $1.0 \text{ cm}^{-1}$  from 200 to  $500 \text{ cm}^{-1}$ ,  $2.0 \text{ cm}^{-1}$  from 500 to  $700 \text{ cm}^{-1}$ ,  $5.0 \text{ cm}^{-1}$  from 700 to  $1000 \text{ cm}^{-1}$ , and  $20 \text{ cm}^{-1}$  from 1000 to  $1500 \text{ cm}^{-1}$ . For collision with *o*-H<sub>2</sub>, the energy steps are  $0.2 \text{ cm}^{-1}$  below  $300 \text{ cm}^{-1}$ ,  $1.0 \text{ cm}^{-1}$  from 200 to  $500 \text{ cm}^{-1}$ ,  $2.0 \text{ cm}^{-1}$  from 500 to  $700 \text{ cm}^{-1}$ ,  $5.0 \text{ cm}^{-1}$  from 700 to  $1000 \text{ cm}^{-1}$ , and  $20 \text{ cm}^{-1}$  from 1000 to  $1500 \text{ cm}^{-1}$ . At each collision energy, the total angular momentum  $J_{\text{tot}}$  was set large enough to converge cross sections, the value of  $J_{\text{tot}}$  varies from 19 at low energies to 64 for energies larger than  $1000 \text{ cm}^{-1}$ .

Since a given  $N_1$  rotational number includes a large number of NH<sub>2</sub> sub-rotational energy, rotational levels with internal energies above  $E_{\text{max}} = 650 \text{ cm}^{-1}$  were eliminated for total energies  $E_{\text{tot}} \leq 200 \text{ cm}^{-1}$ . This  $E_{\text{max}}$  parameter was progressively increased up to  $E_{\text{max}} = 2200 \text{ cm}^{-1}$  for  $E_{\text{tot}} = 1500 \text{ cm}^{-1}$ . These large values of  $E_{\text{max}}$  are needed to converge cross sections. A similar effect was previously observed for methyl-formate (HCOOCH<sub>3</sub>) colliding with helium<sup>39</sup> and for formaldehyde (H<sub>2</sub>CO) colliding with H<sub>2</sub>.<sup>40</sup>

It was also crucial to optimize the rotational basis of H<sub>2</sub> in order to keep calculations feasible in terms of both central processing unit (CPU) time and memory. Tests of the *p*-H<sub>2</sub> and *o*-H<sub>2</sub> basis were performed at different values of total energy. For collisions with *p*-H<sub>2</sub> ( $j_2 = 0$ ), the inclusion of the H<sub>2</sub> ( $j_2 = 2$ ) level was necessary to obtain cross sections converged to better than 5%, even when these channels were energetically closed. For *o*-H<sub>2</sub> ( $j_2 = 1$ ), it was found that inclusion of the H<sub>2</sub> ( $j_2 = 3$ )

level in the basis does not have a noticeable influence on the magnitude of the cross sections. Hence, for the determination of rotational excitation cross section of NH<sub>2</sub> in collision with *o*-H<sub>2</sub>, only the H<sub>2</sub> ( $j_2 = 1$ ) basis was retained.

### III. RESULTS

Figure 7 shows the collisional energy dependence of the de-excitation integral cross sections of *o*- and *p*-NH<sub>2</sub> in collision with *o*-H<sub>2</sub> ( $j_2 = 1$ ) and *p*-H<sub>2</sub> ( $j_2 = 0$ ). One can first observe resonances that appear for energies lower than  $250 \text{ cm}^{-1}$ . These resonances in the de-excitation cross sections are related to the presence of the attractive potential well with a depth of  $-213 \text{ cm}^{-1}$  that allows the H<sub>2</sub> molecule to be temporarily trapped and hence quasi-bound states to be formed before the complex dissociates. The cross sections for collisions with *p*-H<sub>2</sub> ( $j_2 = 0$ ) seem to display a richer resonance structure than the cross sections for collisions with *o*-H<sub>2</sub> ( $j_2 = 1$ ) that appear to have a smoother energy dependence. Actually, there are many more, and hence overlapping, resonances for the cross sections for collisions with *o*-H<sub>2</sub> ( $j_2 = 1$ ) because of a larger number of (quasi-)bound states due to the contribution of an additional coupling term  $N_1 + j_2 = j_{12}$  absent in collisions with *p*-H<sub>2</sub> ( $j_2 = 0$ ). Second, regarding the magnitude of the cross sections, we observe a global decrease of their intensity with increasing  $\Delta N_1$ . However it is interesting to note that for collisions with *p*-H<sub>2</sub> ( $j_2 = 0$ ), the magnitude of cross sections with  $\Delta N_1 = 2$  can be larger than those with  $\Delta N_1 = 1$ , while the trend is a rather monotonic decrease for *o*-H<sub>2</sub> ( $j_2 = 1$ ).

Also, when the collisional energy increases, the magnitude of the cross sections for  $\Delta N_1 = 1$  and  $\Delta N_1 > 1$  tends to be closer whether for collisions with *p*- or *o*-H<sub>2</sub>. This behavior is expected and observed for many systems like HNC-H<sub>2</sub>,<sup>41</sup> HCl-H<sub>2</sub>,<sup>42</sup> and O<sub>2</sub>-H<sub>2</sub>.<sup>43</sup>

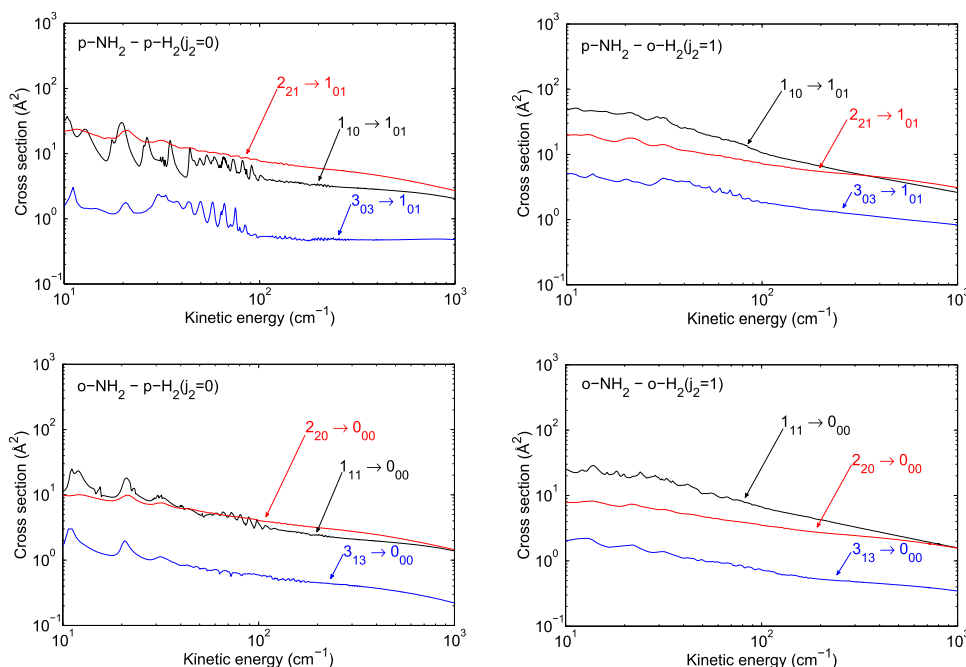


FIG. 7. Rotational de-excitation cross sections of *para*- and *ortho*-NH<sub>2</sub> by *para*- and *ortho*-H<sub>2</sub>. For collisions with both *p*- and *o*-H<sub>2</sub>,  $j_2$  is unchanged.

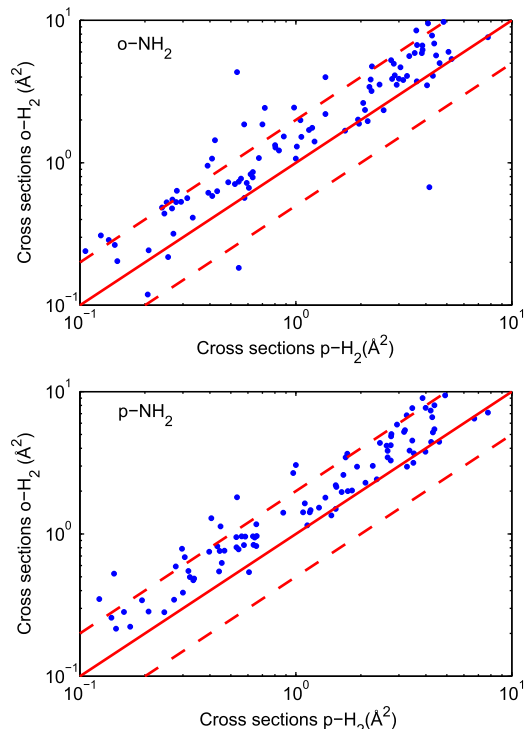


FIG. 8. Comparison between  $p$ - and  $o$ -H<sub>2</sub> de-excitation cross sections for  $o$ -NH<sub>2</sub> (upper panel) and  $p$ -NH<sub>2</sub> (lower panel) at a collision energy of 100 cm<sup>-1</sup>. The horizontal axis represents the collisional cross sections with  $p$ -H<sub>2</sub> ( $j_2 = 0$ ) and the vertical axis represents the corresponding collisional cross sections with  $o$ -H<sub>2</sub> ( $j_2 = 1$ ). The two dashed lines in each panel delimit the region where the cross sections differ by less than a factor 3.

In order to have an overview of the differences that exist between the excitation cross sections with  $p$ - and  $o$ -H<sub>2</sub> colliders, we show, in Fig. 8, a comparison between the two sets of cross sections for all the de-excitation transitions from all initial levels up to  $N_{1k_a k_c} = 4_{40}$  for  $o$ -NH<sub>2</sub> and up to  $N_{1k_a k_c} = 4_{41}$  for  $p$ -NH<sub>2</sub> at a fixed collision energy of 100 cm<sup>-1</sup>. The horizontal axis presents the cross sections for collisions with  $p$ -H<sub>2</sub> ( $j_2 = 0$ ) whereas the vertical axis presents the cross sections for collisions with  $o$ -H<sub>2</sub> ( $j_2 = 1$ ).

Examination of the plots for collisions of  $o$ - and  $p$ -NH<sub>2</sub> with both  $o$ - and  $p$ -H<sub>2</sub> shows that the two sets of data agree generally within a factor of 3. The largest cross sections are those for collision with  $o$ -H<sub>2</sub>, with only a few exceptions. This trend was already observed for several interstellar species like SiS,<sup>44</sup> HCl,<sup>42</sup> SO<sub>2</sub>,<sup>45</sup> or H<sub>2</sub>O.<sup>46</sup>

This behavior can also be explained by looking at the radial coefficients  $v_{p_1 q_1 p_2 p}$  of the expansion Equation (7), as plotted in Fig. 2. The radial coefficients contributing to cross sections with  $j_2 \rightarrow j'_2$  transitions are those with  $p_2$  in the range  $j_2 - j'_2 < p_2 < j_2 + j'_2$ . Then, for collisions with  $p$ -H<sub>2</sub> ( $j_2 = 0$ ) only the terms with  $p_2 = 0$  contribute whereas for collisions with  $o$ -H<sub>2</sub> ( $j_2 = 1$ ) the  $p_2 = 0, 2$  terms contribute. The radial coefficients with  $p_2 = 2$  are not negligible compared to the one with  $p_2 = 0$  explaining why the cross sections for collisions with  $o$ -H<sub>2</sub> ( $j_2 = 1$ ) are larger than the ones for collisions with  $p$ -H<sub>2</sub> ( $j_2 = 0$ ). The non-negligible contribution of the radial coefficients with  $p_2 = 2$  can be explained notably by the dipole-quadrupole interaction that exists for collisions with  $o$ -H<sub>2</sub> and that vanishes for collisions with  $p$ -H<sub>2</sub>.

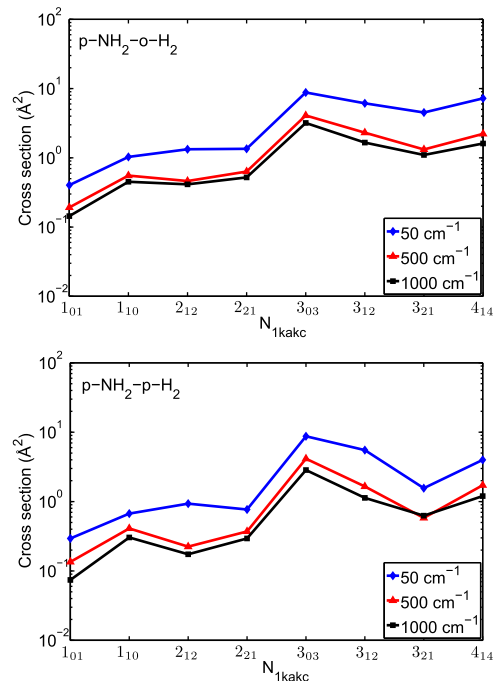


FIG. 9. Propensity rules for transitions out of the initial  $N_{1k_a k_c} = 4_{23}$  state of the  $p$ -NH<sub>2</sub> molecule in collision with  $p$ -H<sub>2</sub> ( $j_2 = 0$ ) (bottom panel) and  $o$ -H<sub>2</sub> ( $j_2 = 1$ ) (top panel), for kinetic energies = 50, 100, and 1000 cm<sup>-1</sup>.

Then, we were interested in the propensity rules in the NH<sub>2</sub>-H<sub>2</sub> collisional system. Figures 9 and 10 show, at 3 different collisional energies (50, 500, and 1000 cm<sup>-1</sup>), the rotational de-excitation cross sections from  $p$ -NH<sub>2</sub> ( $N_{1k_a k_c} = 4_{23}$ ) and  $o$ -NH<sub>2</sub> ( $N_{1k_a k_c} = 4_{13}$ ) for both  $p$ - and  $o$ -H<sub>2</sub> collisions.

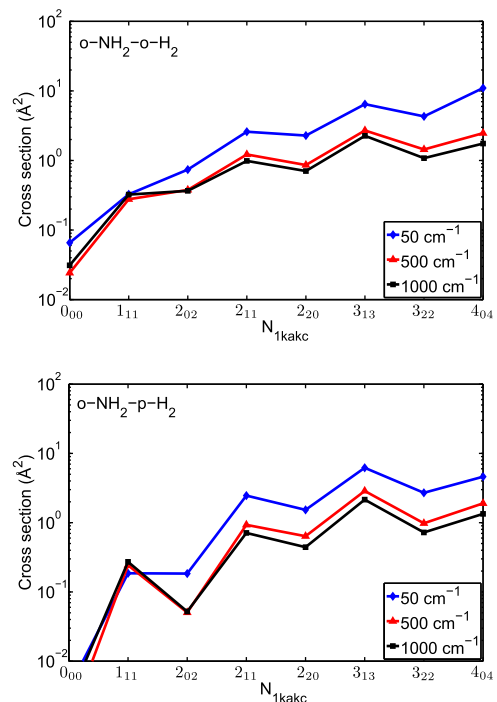


FIG. 10. Propensity rules for transitions out of the initial  $N_{1k_a k_c} = 4_{13}$  state of the  $o$ -NH<sub>2</sub> molecule in collision with  $p$ -H<sub>2</sub> ( $j_2 = 0$ ) (bottom panel) and  $ortho$ -H<sub>2</sub> ( $j_2 = 1$ ) (top panel), for kinetic energies = 50, 100, and 1000 cm<sup>-1</sup>.

TABLE I. Comparison of cross sections for transitions out of  $o$ -NH<sub>2</sub> ( $N_{1k_a k_c} = 0_{00}$ ) rotational level induced by collisions with  $p$ -H<sub>2</sub> ( $j_2 = 0$ ) and He.<sup>18</sup>  $E_{col} = 467$  cm<sup>-1</sup>.

Final level	Cross sections	
	$o$ -NH <sub>2</sub> - $p$ -H <sub>2</sub>	$o$ -NH <sub>2</sub> -He
1 <sub>11</sub>	(1) <sup>a</sup>	(1) <sup>a</sup>
2 <sub>02</sub>	(1) <sup>a</sup>	(1) <sup>a</sup>
2 <sub>11</sub>	0.01	$\leq 0.05 \pm 0.02$
3 <sub>13</sub>	0.37	$0.07 \pm 0.02$
4 <sub>04</sub>	0.23	$0.06 \pm 0.02$

<sup>a</sup>Cross sections are separately normalized for each  $k'_a = 0$  and 1 manifold.

Despite the fact that no strong propensity rules are present, we actually observe a slight propensity rule in favor of transitions with odd  $\Delta k_a$  and  $\Delta k_c$  which is seen for  $p$ -NH<sub>2</sub> in collision with both  $p$ -H<sub>2</sub> and  $o$ -H<sub>2</sub>, while for collisions of  $o$ -NH<sub>2</sub> with both  $p$ -H<sub>2</sub> and  $o$ -H<sub>2</sub> we notice a more marked propensity in favor of even  $\Delta k_a$  and  $\Delta k_c$ . Furthermore, a propensity rule in favor of transitions with  $\Delta k_c = 0$  exists for collisions of both  $o$ - and  $p$ -NH<sub>2</sub> with both  $o$ - and  $p$ -H<sub>2</sub>. This propensity is pointed out in Figs. 9 and 10 where the transitions 4<sub>13</sub>-3<sub>13</sub> of  $o$ -NH<sub>2</sub> and 4<sub>23</sub>-3<sub>03</sub>  $p$ -NH<sub>2</sub> are indeed found to be favored. This trend may be explained by the difficulty of reorienting the angular momentum vector with respect to the axis of the greatest moment of inertia.

Because of the similarity of molecular geometries of H<sub>2</sub>O and NH<sub>2</sub>, it is interesting to compare the propensity properties of the two systems. From the propensity rules found for the H<sub>2</sub>O-H<sub>2</sub> system<sup>47</sup> ( $\Delta N_1 = 0, \pm 1$ ;  $\Delta k_a = 0, \pm 1$ ;  $\Delta k_c = 0, \pm 1$ ), it can be seen that transitions with conservation of  $k_c$  or small variation of  $k_c$  are also favored for this system, which might be general to C<sub>2v</sub> molecules.

Finally, as collisions with helium are often used to model collisions with  $p$ -H<sub>2</sub> ( $j_2 = 0$ ), it is interesting to compare our theoretical results with the experimental state resolved cross sections for rotationally inelastic collisions of NH<sub>2</sub> ( $^2B_1$ ) with He measured by Dagdigian.<sup>18</sup> Dagdigian used a crossed beam experiment and resolved fluorescence spectroscopy to study rotational energy transfer within the NH<sub>2</sub> electronic state. Table I presents close-coupling calculation for NH<sub>2</sub> with  $p$ -H<sub>2</sub> ( $j_2 = 0$ ) collisions at the kinetic energy 467 cm<sup>-1</sup> used in experiment. By comparing our results with the experimental relative cross sections out of the NH<sub>2</sub> ( $N_{1k_a k_c} = 0_{00}$ ) state induced by collision with He,<sup>18</sup> we found that the  $p$ -H<sub>2</sub> collisional partner is much more efficient than He for inducing  $\Delta N_1 > 1$  transitions. This probably mainly reflects the difference in the interaction potential where the NH<sub>2</sub>-H<sub>2</sub> well depth is expected to be much larger than the NH<sub>2</sub>-He one. Then we confirm again that for hydrides molecules, He cannot be used as a model for H<sub>2</sub>, as already found for HCl<sup>42</sup> or H<sub>2</sub>O.<sup>46</sup>

#### IV. CONCLUSION

We have presented in this paper a study of the interaction between NH<sub>2</sub> and hydrogen molecules. Cross sections for the rotational (de)excitation of  $o$ - and  $p$ -NH<sub>2</sub> colliding with both  $p$ -H<sub>2</sub> ( $j_2 = 0$ ) and  $o$ -H<sub>2</sub> ( $j_2 = 1$ ) have been computed. All

transitions among both the 15 lowest levels of  $o$ -NH<sub>2</sub> and  $p$ -NH<sub>2</sub> were considered.

The cross sections for collisions with *para*- and *ortho*-H<sub>2</sub> differ, the magnitude of the *ortho*-H<sub>2</sub> ones being dominant. Propensity rules are discussed and it is found that no rigorous selection rules are defined although transitions with  $\Delta k_c = 0$  seem to be slightly favored.

The present results should therefore be adopted in any radiative transfer model of NH<sub>2</sub> in environments with  $T \leq 150$  K. In particular, Persson *et al.*<sup>2</sup> used a non-LTE radiative transfer model using rate coefficients estimated from an assumed quenching rate coefficient of  $5 \times 10^{-11}$  cm<sup>3</sup> s<sup>-1</sup> and radiative selection rules, i.e.,  $\Delta N_1 = 0, \pm 1$ ;  $\Delta k_a = \pm 1, \pm 3$ , etc.;  $\Delta k_c = \pm 1, \pm 3$ , etc. Our results indicate that inelastic cross sections corresponding to radiatively forbidden transitions (e.g.,  $\Delta k_c = 0$ ) can be as probable as (or even stronger than) those corresponding to radiatively allowed transitions. Hence, previously published NH<sub>2</sub> abundance should be revised accordingly, using our new data.

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