

# Fluid Dynamics Model for Pore-Scale Wetting Phenomena

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## Introduction

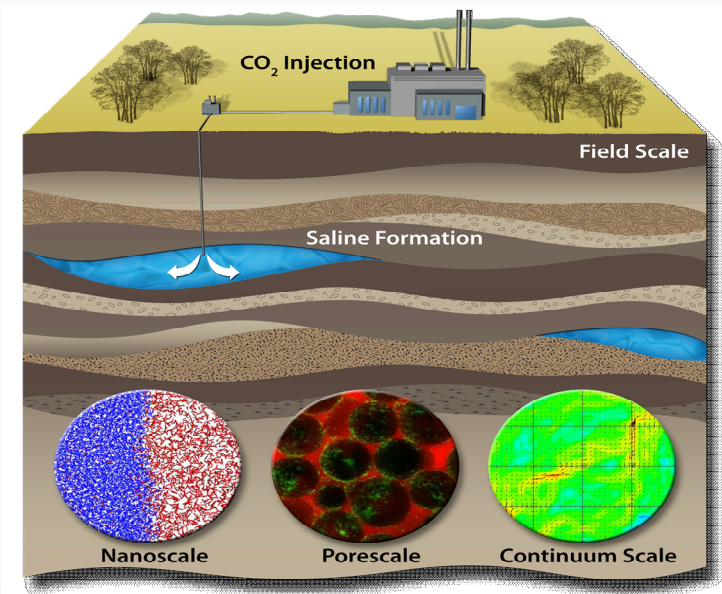
### Motivation



Moving Contact Line (MCL) problems are important to model the migration of wetting/non-wetting fluids through reservoir rocks.

### Scientific Objective:

Understand and control *emergent behavior* arising from *coupled physics* in *heterogeneous geomaterials* associated with injection for CCS, especially at *intermediate length scales* (cm to m) where geologic variability plays a decisive role. Processes and strategies are based on mesoscale science from which non-equilibrium and emergent behaviors arise over a large range of time and length scales.



## Computational Model

### Navier-Stokes Equation

$$\nabla \cdot \mathbf{u} = 0$$

$$\rho(\mathbf{x}) \left( \frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} \right) = -\nabla p + \nabla \cdot (\mu(\mathbf{x}) (\nabla \mathbf{u} + \nabla \mathbf{u}^T))$$

### Level Set Equation

$$\frac{\partial \phi}{\partial t} + \mathbf{u} \cdot \nabla \phi = 0$$

### Interface Boundary Conditions

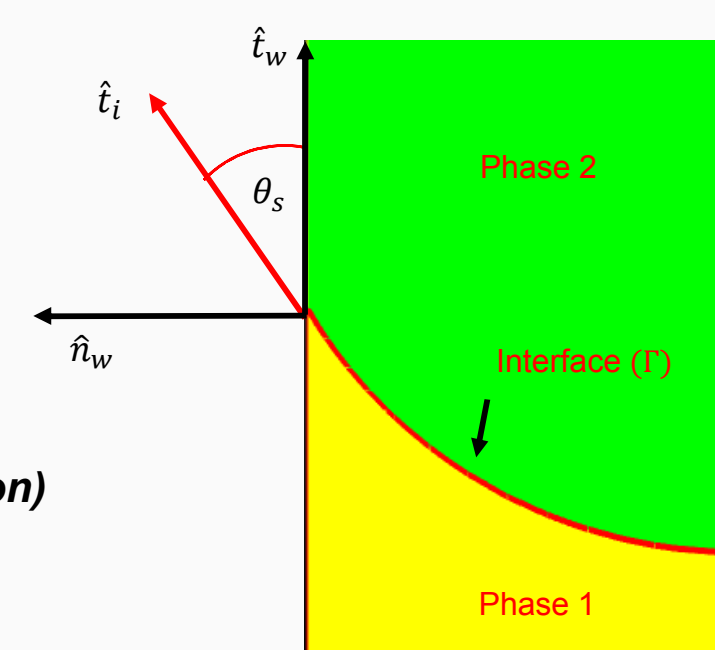
$$[\mathbf{u}]_{\Delta} = 0, \quad \mathbf{x} \in \Gamma \quad (\text{continuity})$$

$$[-p\mathbf{I} + \mu(\mathbf{x}) (\nabla \mathbf{u} + \nabla \mathbf{u}^T)]_{\Delta} \cdot \hat{\mathbf{n}} = -\gamma \kappa \hat{\mathbf{n}}, \quad \mathbf{x} \in \Gamma \quad (\text{surface tension})$$

### Wetting Line Model

$$\int_{\Gamma^{n+1}} \sigma (\cos(\theta_s) \mathbf{t}_w + \sin(\theta_s) \mathbf{n}_w) \cdot \mathbf{w}_i d\Gamma$$

$$\int_{\Gamma^{n+1}} \frac{\mu}{\beta^*} (\mathbf{u}_w - \mathbf{u}^{n+1}) \cdot \mathbf{w}_i d\Gamma$$



Finite Element Method (FEM) is used to model the interface dynamics

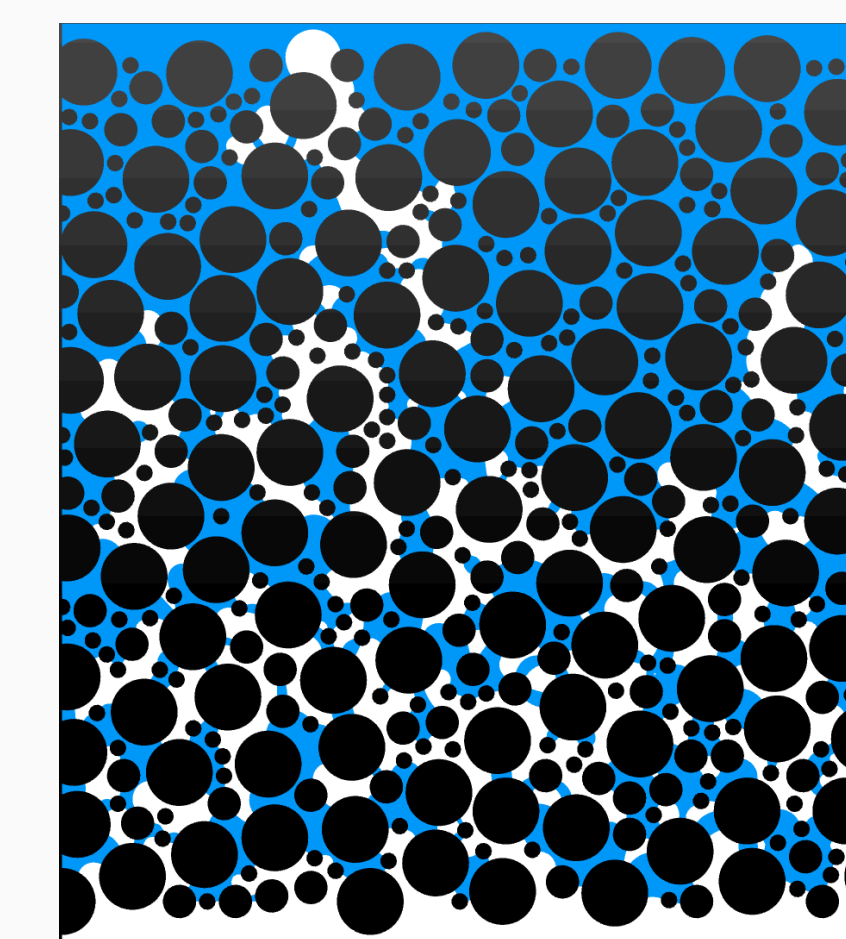
- Conformal decomposition FEM (CDFEM) uses the level-set method to model two-phase interface
- CDFEM allows for a sharp-interface between the immiscible phases, providing exact location of the contact line
- Contact line model determined completely by equilibrium properties (must fit a slip coefficient)

## Model Applications for GCS

### Drainage in Disordered Media

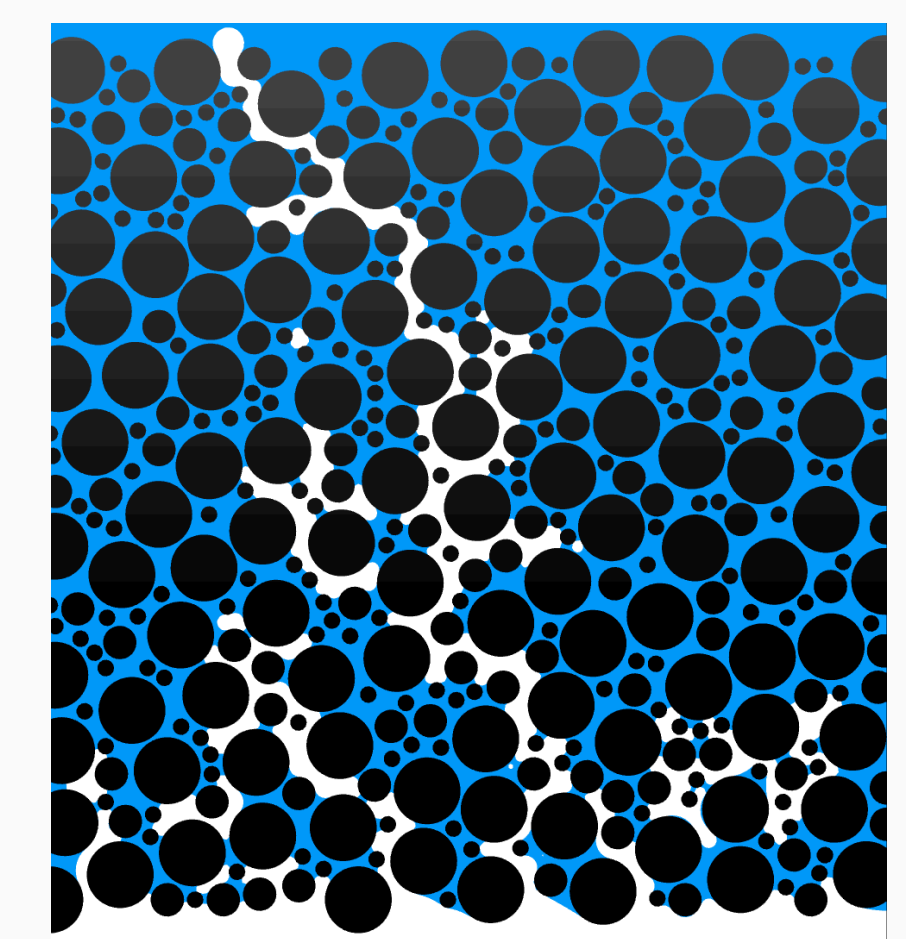
Capillary Number,  $Ca = 1 \times 10^{-5}$

Weakly Wetting ( $\theta_s = 80^\circ$ )



Brine – blue phase

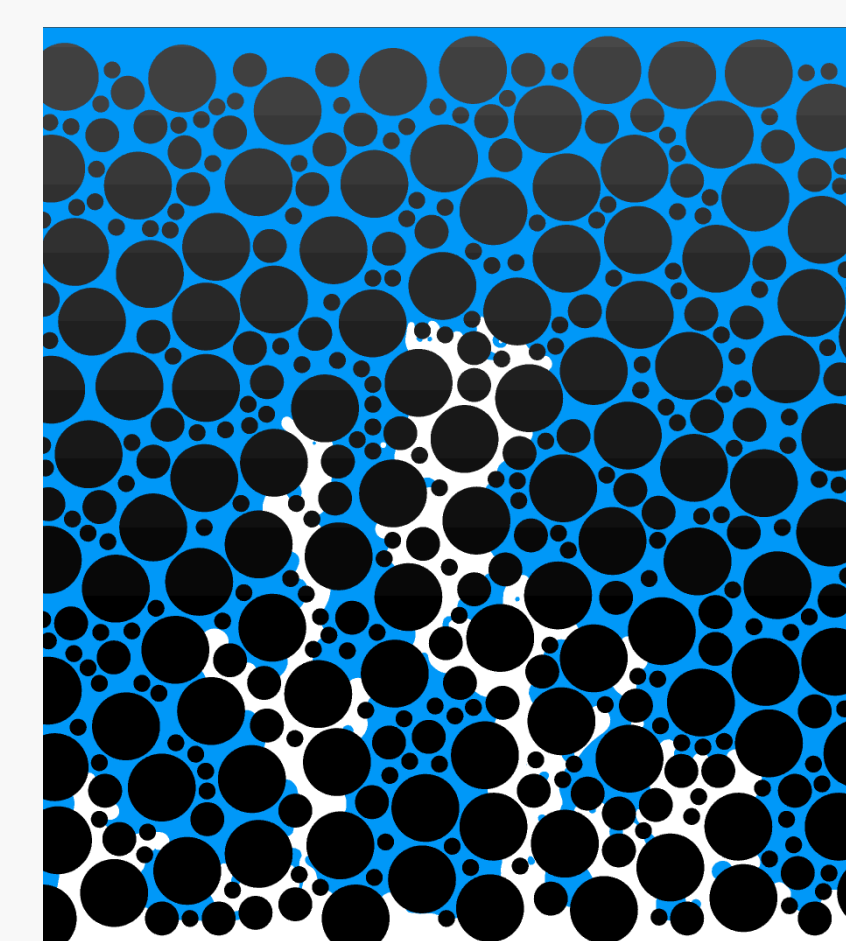
Strongly Wetting ( $\theta_s = 0^\circ$ )



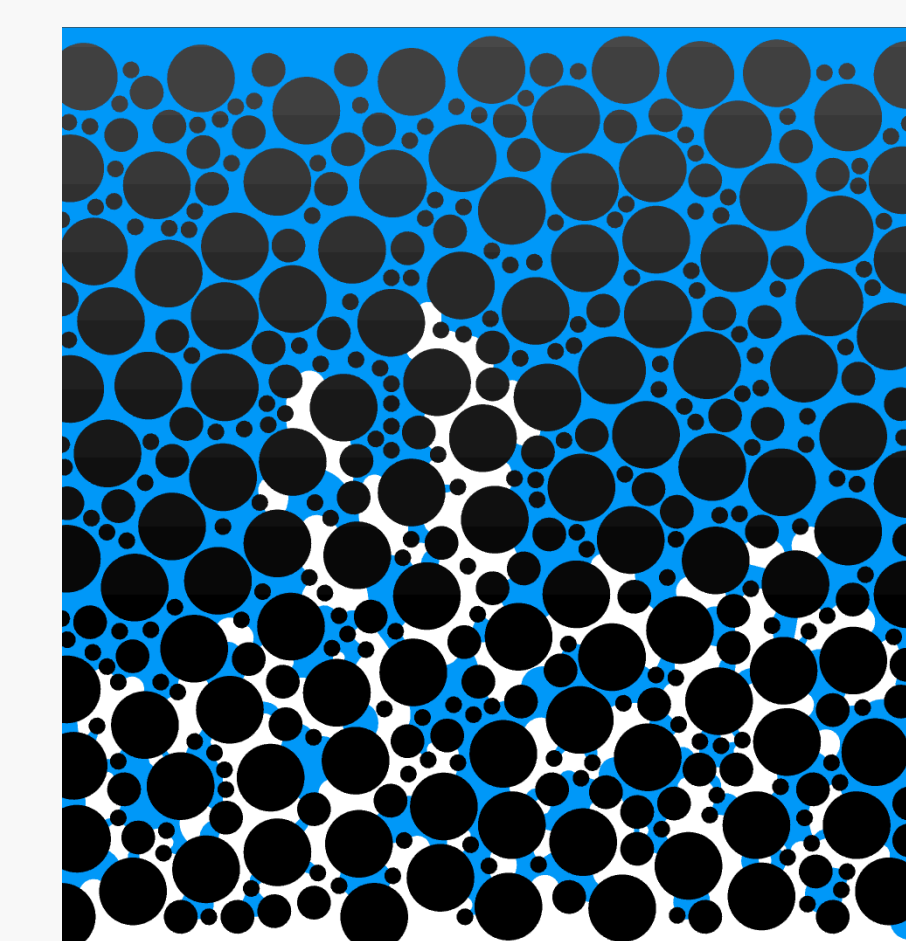
CO<sub>2</sub> – white phase

Wetting Angle  $\theta = 80^\circ$  (Weakly Wetting)

Capillary Number,  $Ca = 1 \times 10^{-4}$



Capillary Number,  $Ca = 1 \times 10^{-5}$



### Brine drainage by CO<sub>2</sub> injection

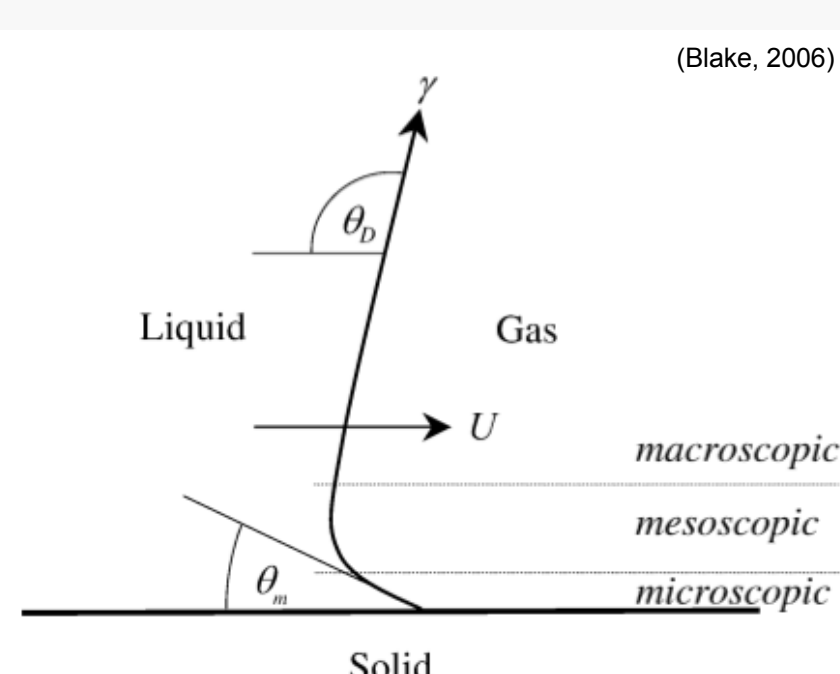
- Wetting model captures viscous and capillary fingering configurations
- At fixed capillary number, increased brine wettability promotes fingering, lowers final saturation (lower sweep efficiency)
- For weakly wetting brine, increasing capillary number promotes viscous fingering

## Contact Line Modeling

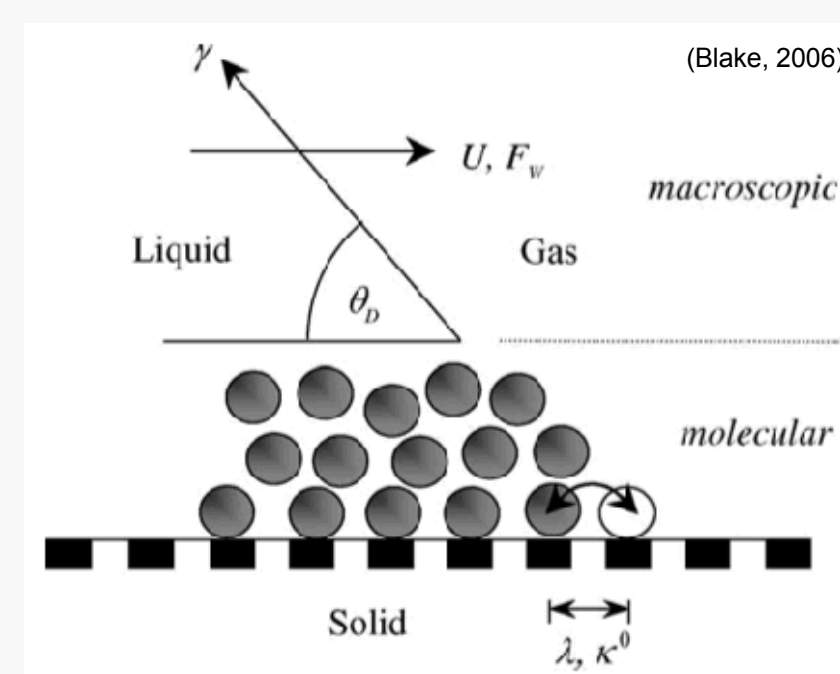
### Moving Contact Lines

- Two immiscible fluids in contact with a solid surface in equilibrium form a static contact angle
- When this equilibrium is disturbed, the contact angle becomes dynamic and the contact line moves
- Must model relationship between contact angle and contact line velocity as the physics are poorly understood

### Hydrodynamic Models



### Molecular Models



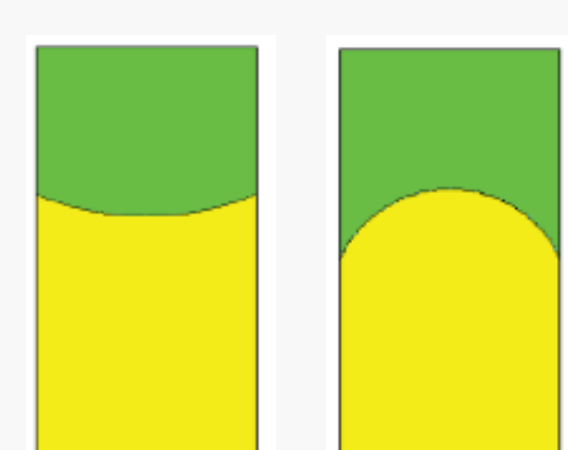
- Three length scales near the contact line: macroscopic, mesoscopic, and microscopic
- Changes in experimentally observed macroscopic dynamic contact angle is attributed to viscous bending of the interface in the mesoscopic region
- Microscopic angle is usually assumed as the static angle and velocity independent
- Voinov, 1976; Cox, 1989; Huh & Scriven, 1971.

- Two length scales: macroscopic and molecular
- Contact line motion is determined by the statistical dynamics of the molecules at the molecular scale
- Driving force of contact line is proportional to the disturbed and equilibrium contact angles.
- Blake, 1969

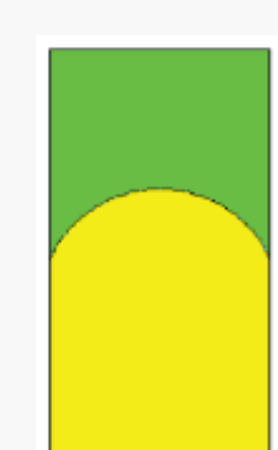
## Verification & Validation

### Capillary Injection

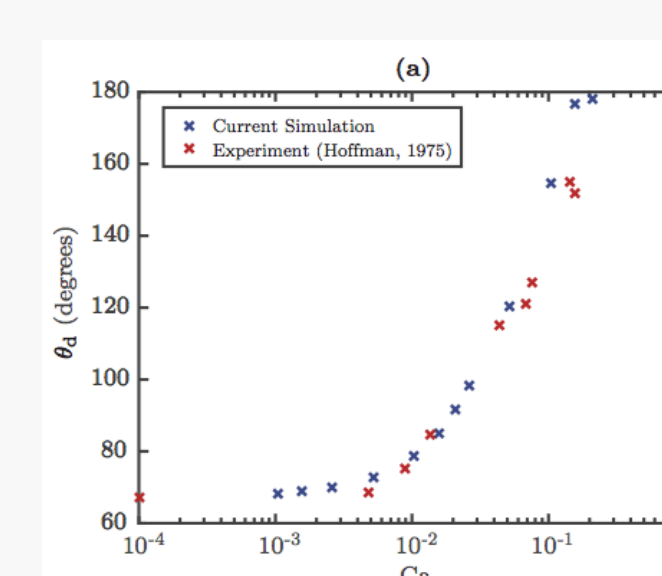
$Ca = 5.2e-3$  (low)



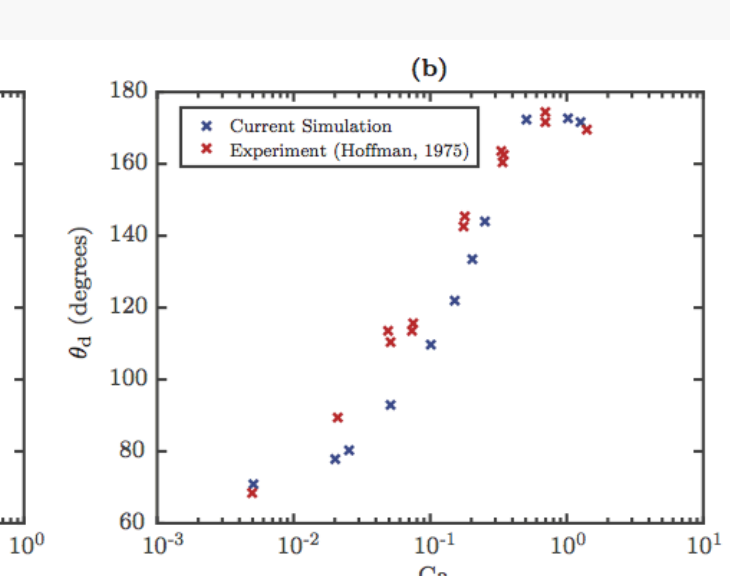
$Ca = 4.4e-2$  (high)



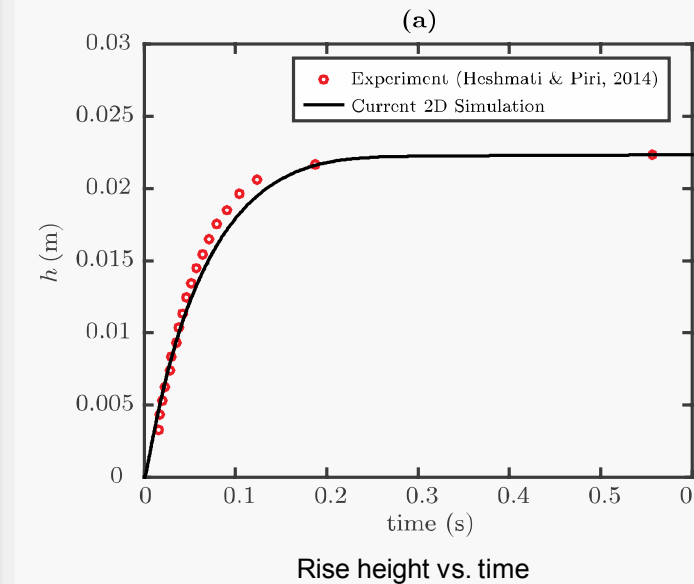
Sancitizer 405 ( $\theta_s = 67^\circ$ )



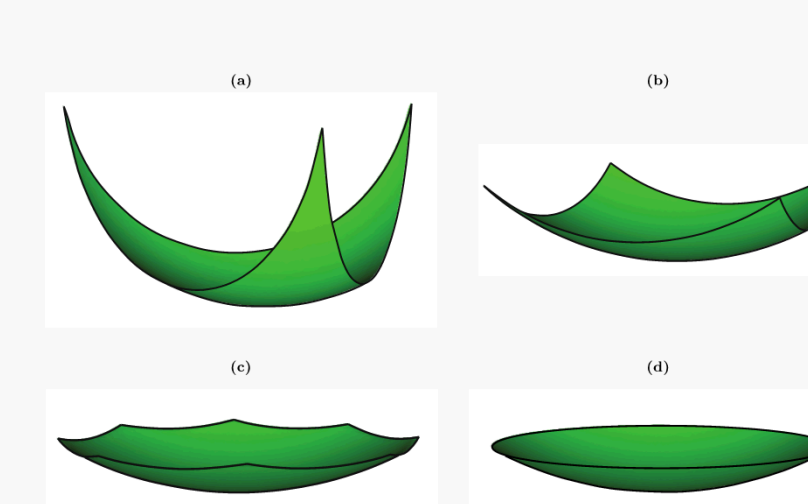
Amdex 760 ( $\theta_s = 69^\circ$ )



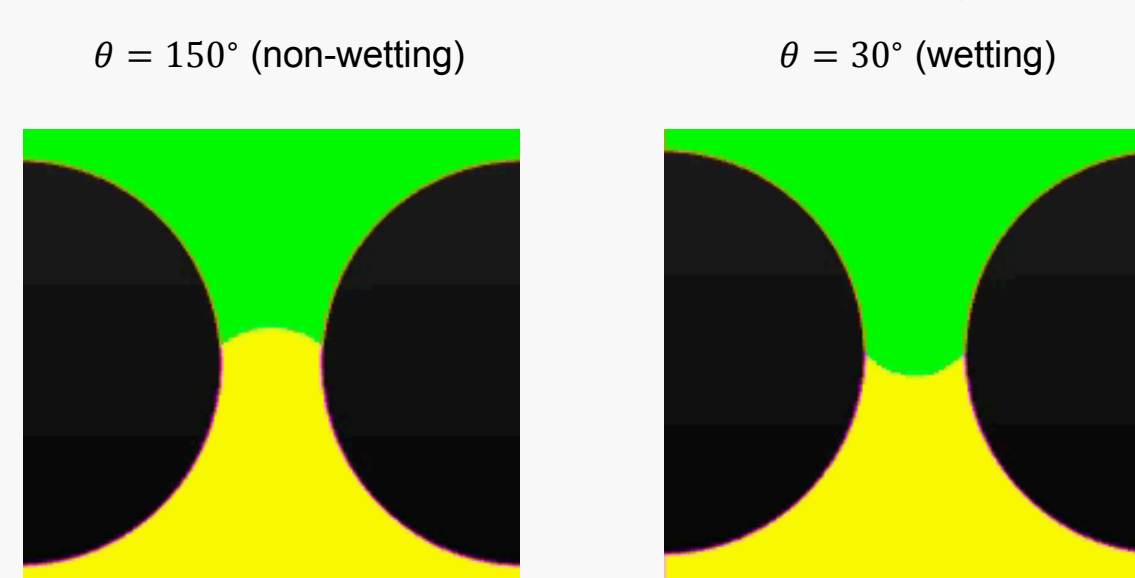
### Capillary Rise



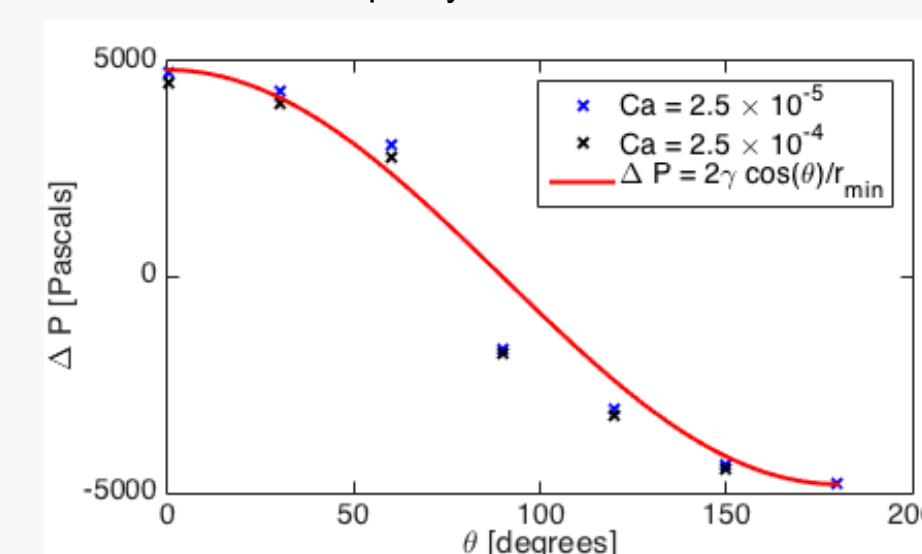
### 3D Interfaces



### Flow Through a Pore Throat



Capillary Pressure Curve



## Concluding Remarks

- Improvement in MCL models can be used to accurately predict CO<sub>2</sub> migration in reservoir rocks
- CO<sub>2</sub> saturation profiles influenced on static wetting properties of the reservoir
- Mixed-wettability within a pore-network may impact sweep efficiency