

DYNAMIC MODEL OF A PARTICLE/SCO₂ HEAT EXCHANGER FOR TRANSIENT ANALYSIS AND CONTROL

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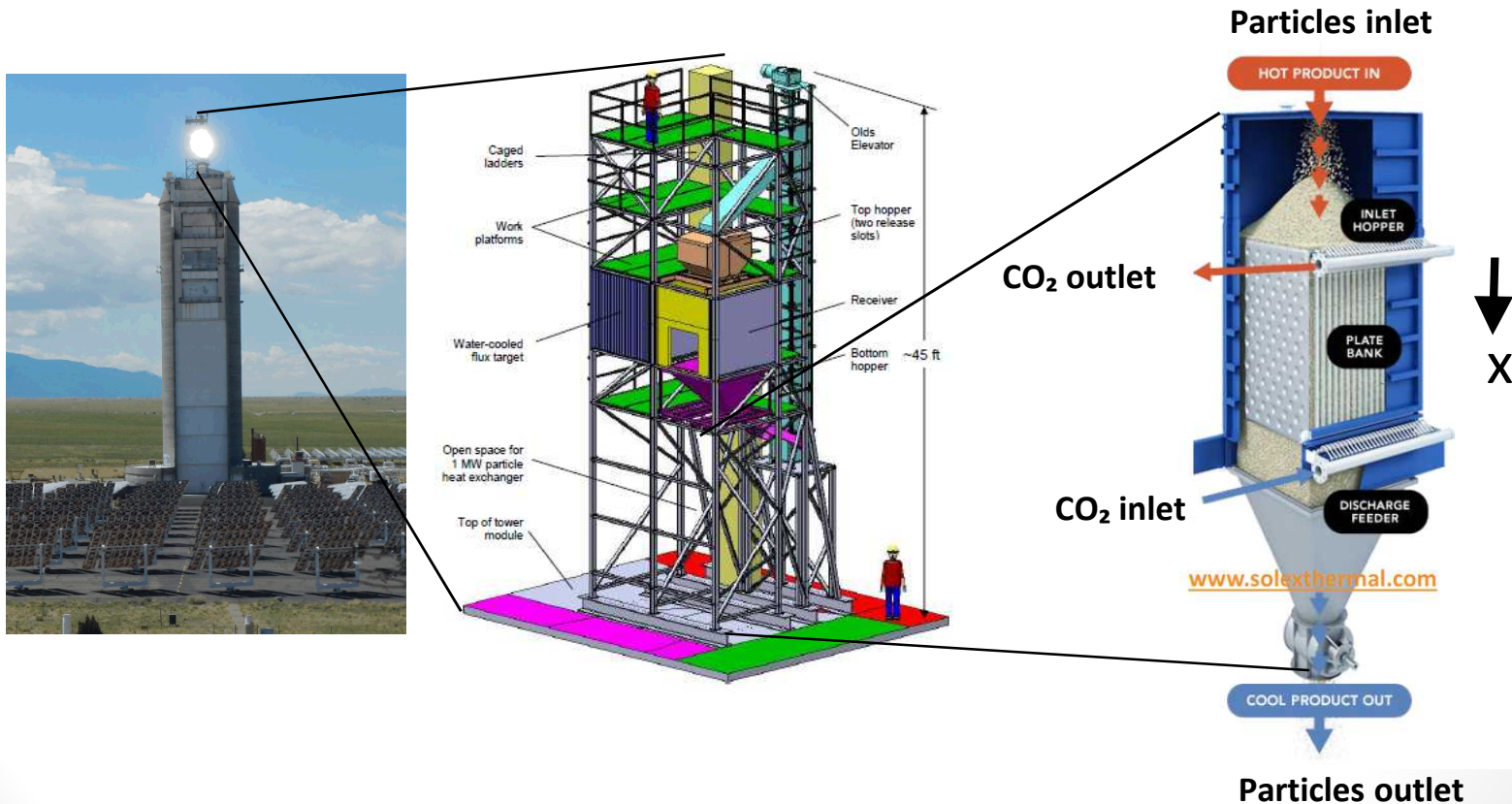
1. Introduction and objectives
2. Numerical model
3. Sensitivity analysis
4. Transient analysis
5. Control strategies
6. Conclusions

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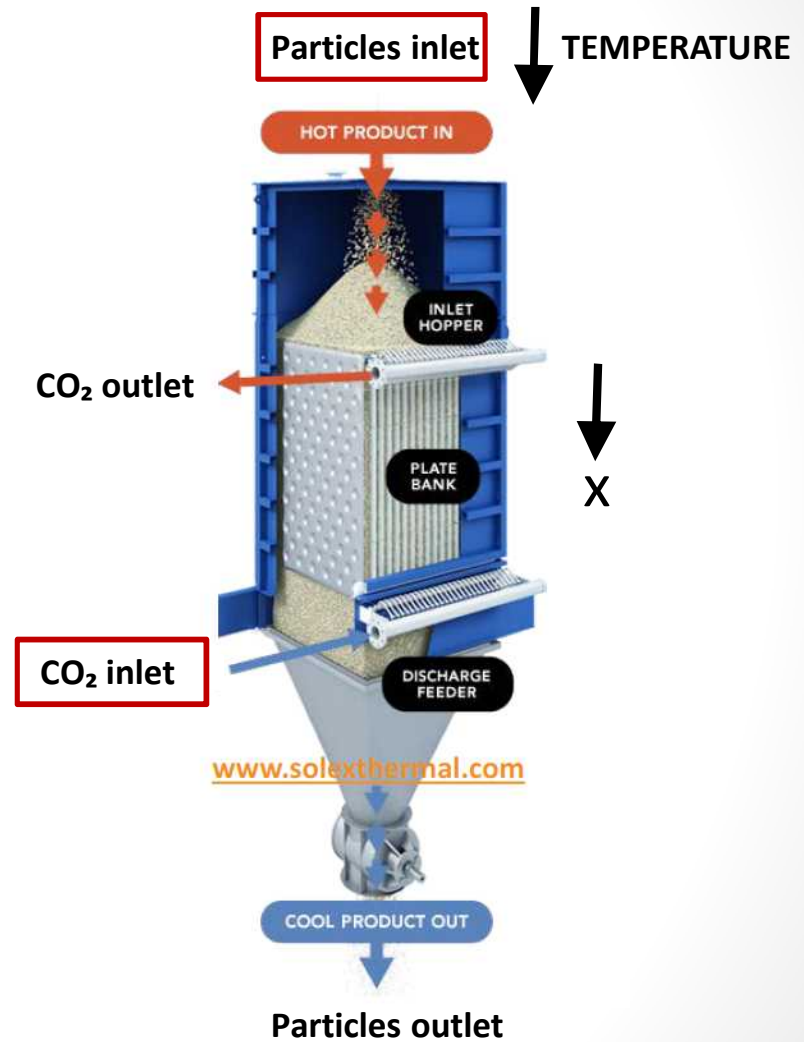
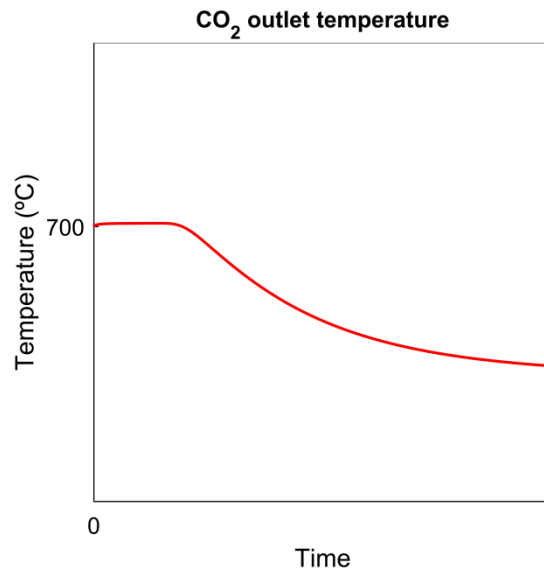
1. Introduction and objectives

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- Solid particle receivers integrated with sCO_2 power cycles: $\uparrow T \uparrow$ efficiency
- The design of particle-to- sCO_2 is necessary $\Rightarrow$ Shell and plate moving packed bed HX



1. Introduction and objectives

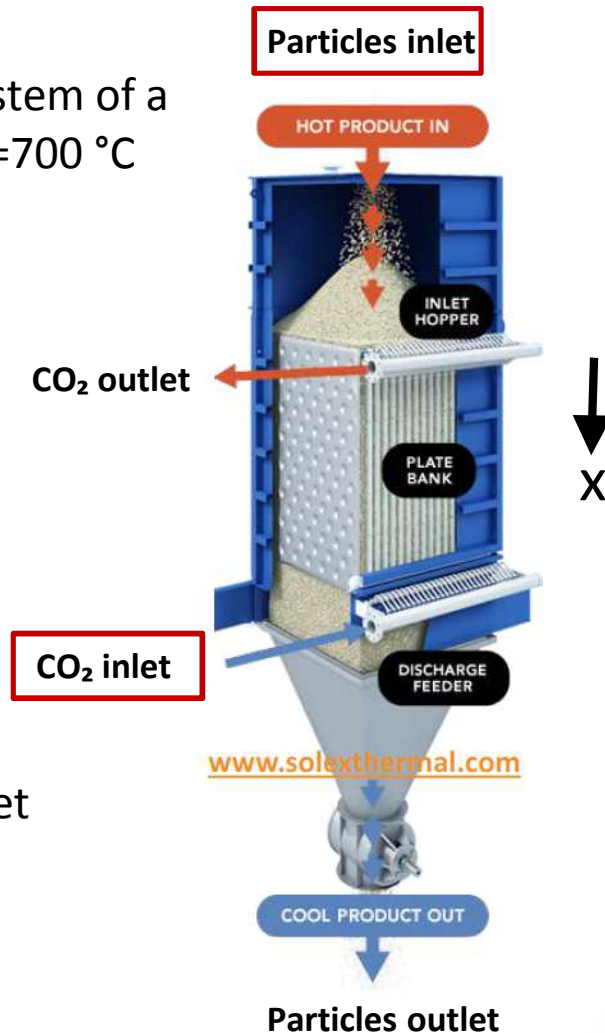


1. Introduction and objectives

- Main objective: to design the control system of a particle-to-sCO₂ HX to maintain $T_{\text{out,sCO}_2} = 700\text{ }^{\circ}\text{C}$

Steps:

1. To study the transient response of the HX in presence of inlet conditions deviations from the design point
2. To investigate the control system to minimize both particles and sCO₂ outlet temperature deviations



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2. Numerical model

3. 1D transient conservation of energy equations

Particles

$$\rho_s \cdot c_{p,s} \cdot \frac{\partial T_s}{\partial t} = -\rho_s \cdot c_{p,s} \cdot u_s \cdot \frac{\partial T_s}{\partial x} + \frac{2 \cdot \overline{h_{sw}}}{hc_s} \cdot (T_w - T_s)$$

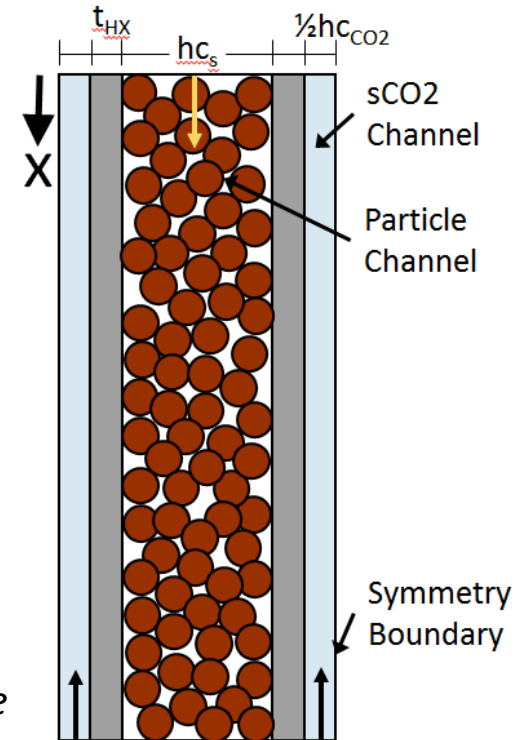
sCO₂

$$\rho_{CO_2} \cdot c_{p,CO_2} \cdot \frac{\partial T_{CO_2}}{\partial t} = -\rho_s \cdot c_{p,s} \cdot u_s \cdot \frac{\partial T_{CO_2}}{\partial x} + \frac{2 \cdot h_{CO_2}}{hc_{CO_2}} \cdot (T_w - T_{CO_2})$$

Wall

$$\rho_w \cdot c_{p,w} \cdot \frac{\partial T_w}{\partial t} = \frac{\overline{h_{sw}}}{t_{HX}} \cdot (T_s - T_w) + \frac{h_{CO_2}}{t_{HX}} \cdot (T_{CO_2} - T_w)$$

- $\overline{h_{sw}}$ is considered to be 150 W/(m²·K) in accordance to previous 2D steady state calculations (*"Heat transfer models of moving packed-bed particle-to-sCO₂ heat exchangers"*, Albrecht, K., Ho, Clifford, *Proceedings of the ASME 2017 Power and Energy Conference*)
- h_{CO_2} according to Gnielinsky correlation
- Implicit method MATLAB



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3. Sensitivity analysis

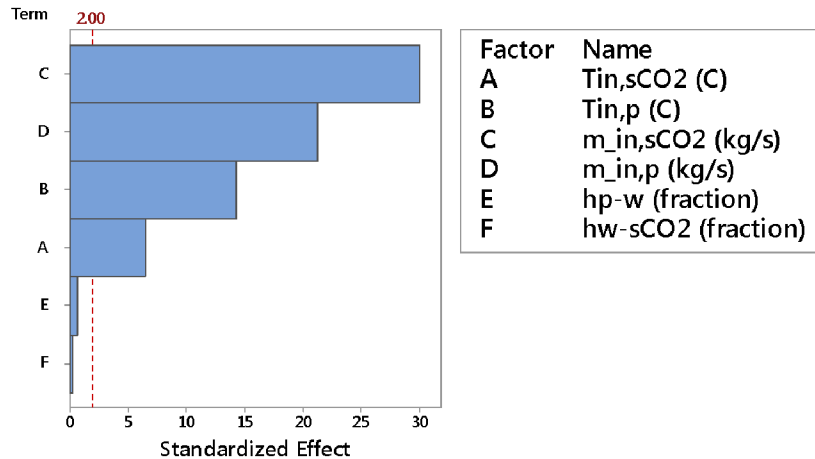
4. Sensitivity analysis – design of experiments

- DoE: which variables have a strong influence on HX response?
- Analysis of variance (ANOVA)
 - Independent variables:
 - Inlet conditions: T_{in,sCO_2} , $T_{in,p}$, m_{sCO_2} , m_p (changes during plant operation)
 - Heat transfer coefficients: $\overline{h_{sw}}$ and h_{sCO_2} (correlations uncertainty)
 - Dependent variables:
 - Time to reach equilibrium
 - $\Delta T = T_{out,sCO_2} - 700^\circ C$

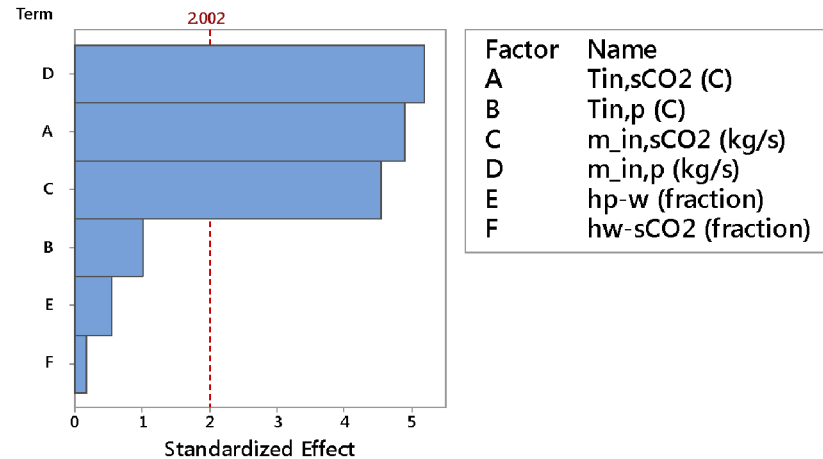
	Design point	Deviations	Final value
Particle inlet temperature ($T_{in,p}$) ($^\circ C$)	775	↓ 50	725
sCO2 inlet temperature (T_{in,sCO_2}) ($^\circ C$)	550	↓ 50	500
sCO2 mass flow rate (m_{sCO_2}) (kg/s)	0.0267	↓ 50%	0.0133
Particle mass flow rate (m_p) (kg/s)	0.02	↓ 50%	0.01
Average particle-wall convection coeff ($\overline{h_{sw}}$) (W/(m ² ·K))	150	↓ 10%	135
sCO2-wall convection coeff (h_{sCO_2}) (W/(m ² ·K))	600	↓ 10%	540

4. Sensitivity analysis results

Pareto Chart of the Standardized Effects
(response is deltaT, $\alpha = 0.05$)



Pareto Chart of the Standardized Effects
(response is Time (s), $\alpha = 0.05$)



- Conclusions:
 - A 10% change in $\overline{h_{sw}}$ and h_{sCO2} does not strongly affect the HX response
 - HX response is strongly affected by changes in inlet temperature and mass flow rates of sCO2 and particles

OUTLINE

1. Introduction

2. Steady-state analysis

3. Frequency response

4. Transient analysis

4. Transient analysis

- 6 different cases varying T_{in,CO_2} , $T_{in,p}$, m_{sCO_2} along the time

Design point					
$T_{in,p}$ (°C)	T_{in,CO_2} (°C)	m_{CO_2} (kg/s)	m_p (kg/s)	$(\overline{h_{sw}})$ (W/(m ² ·K))	h_{sCO_2} (W/(m ² ·K))
775	550	0.0267	0.02	150	600

Case	$T_{in,p}$ (°C)		T_{in,CO_2} (°C)		m_{sCO_2} (kg/s)	
	Deviation	Value	Deviation	Value	Deviation	Value
1	↓50 °C	725	↓50 °C	500	↓50 %	0.0133
2	↓25 °C	750	=	550	↓50 %	0.0133
3	=	775	↓50 °C	500	↓50 %	0.0133
4	=	775	=	550	↓50 %	0.0133
5	↓25 °C	750	↓50 °C	500	=	0.0267
6	=	775	↓50 °C	500	=	0.0267

- 2 different change rates:
 - Instantaneous
 - Linearly decreasing in 30 min

Transient results with change in sCO₂ temperature and mass flow rate

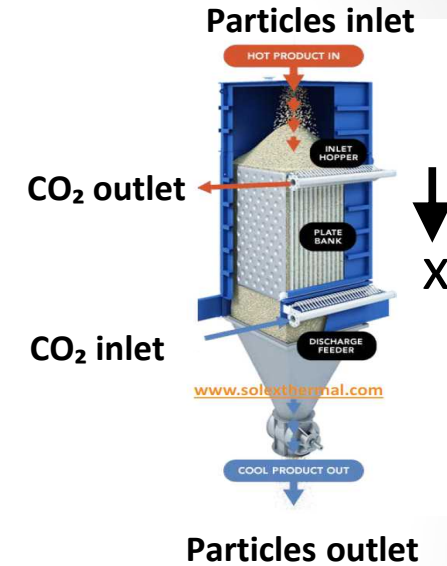
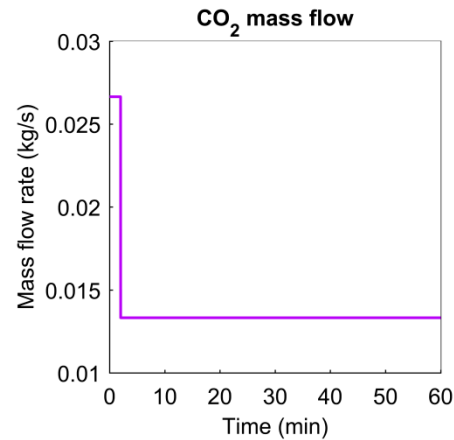
Inlet conditions

$$T_{in,p} = 775\text{ }^{\circ}\text{C}$$

$$T_{in,sCO_2} = 500\text{ }^{\circ}\text{C} (\downarrow 50\text{ }^{\circ}\text{C})$$

$$m_{sCO_2} = 0.0133\text{ kg/s} (\downarrow 50\text{ \%})$$

Step change



Transient results with change in sCO₂ temperature and mass flow

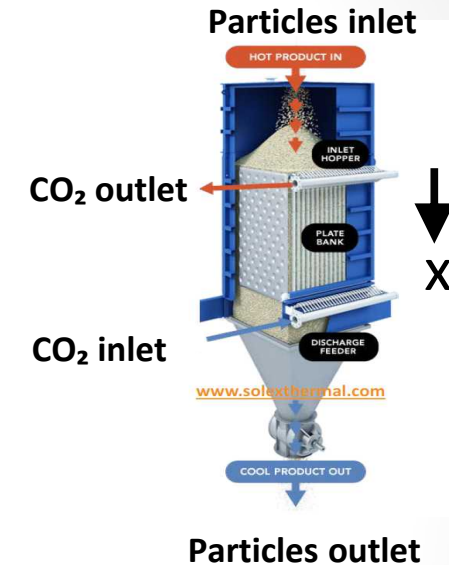
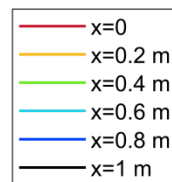
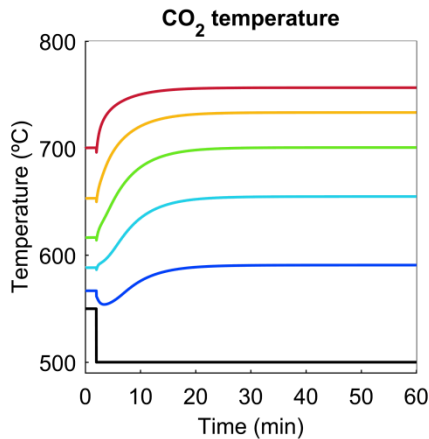
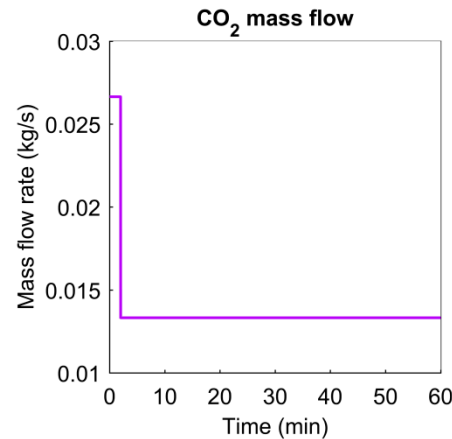
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Transient results with change in sCO₂ temperature and mass flow

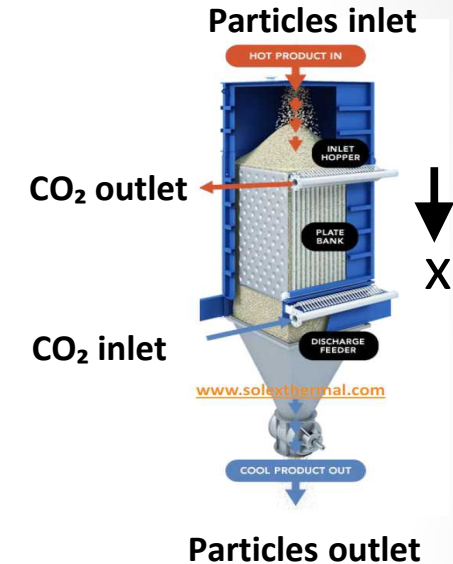
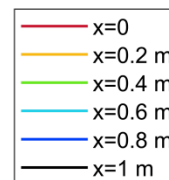
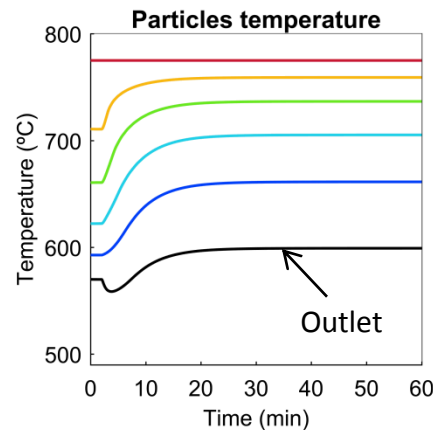
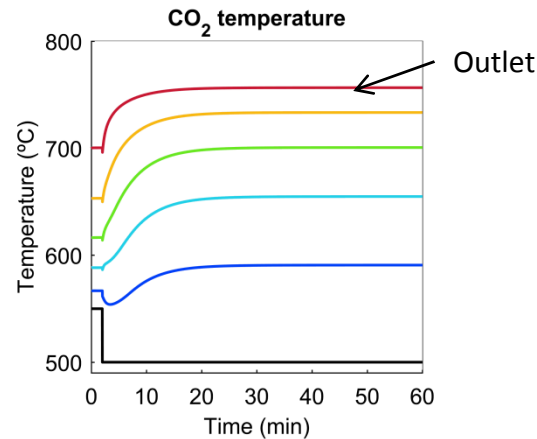
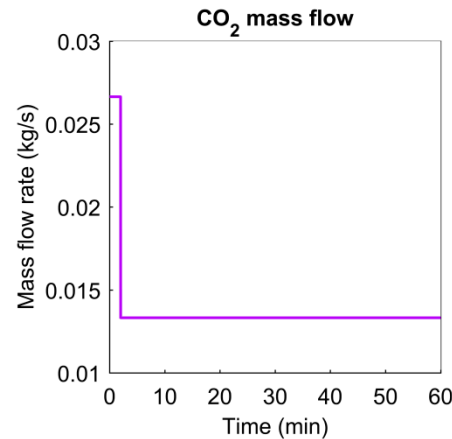
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Step change



Temperature deviations:

30 °C in $T_{out,p}$

60 °C in T_{out,sCO_2}



A control system
is necessary

Transient results with change in sCO₂ temperature and mass flow

Inlet conditions

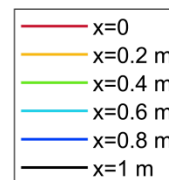
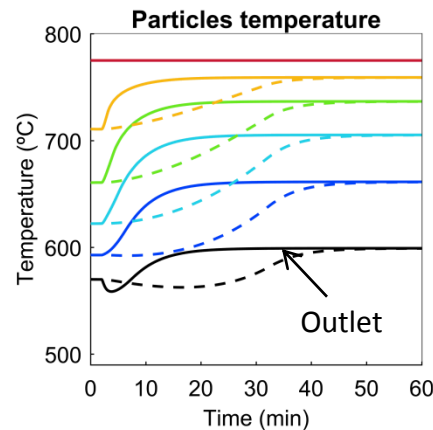
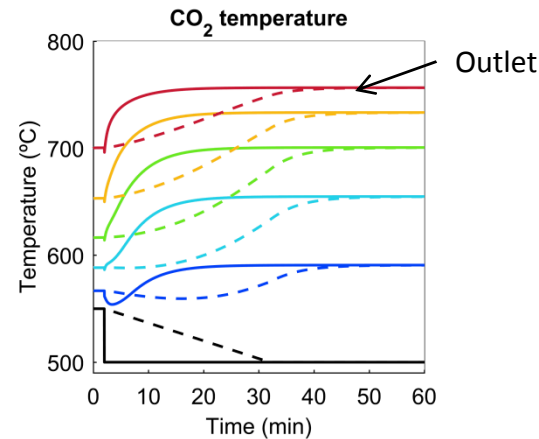
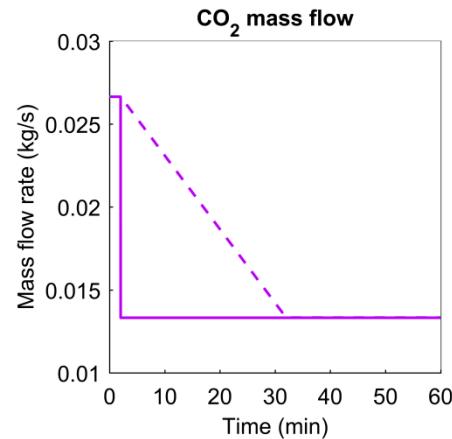
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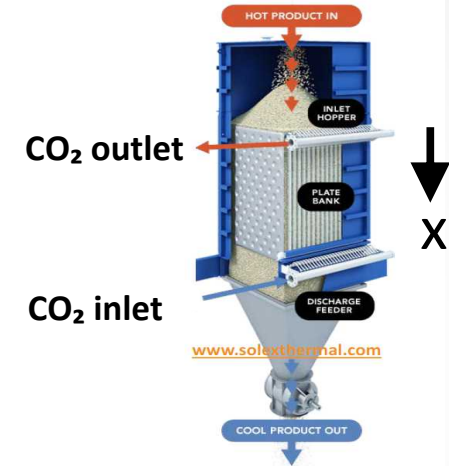
$$m_{sCO_2} = 0.0133\text{ kg/s} (\downarrow 50\text{ \%})$$

Step change

30 min change



— — — Particles inlet



Temperature deviations:

30 °C in $T_{out,p}$

60 °C in T_{out,sCO_2}



A control system
is necessary

OUTLINE

5. Control strategies

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- Goal: to maintain both T_{out,sCO_2} and $T_{out,p}$ deviations from the desired values (700 °C and 570 °C respectively) below 1°C when modifying T_{in,sCO_2} , $T_{in,p}$, m_{sCO_2} (cases 1-6)

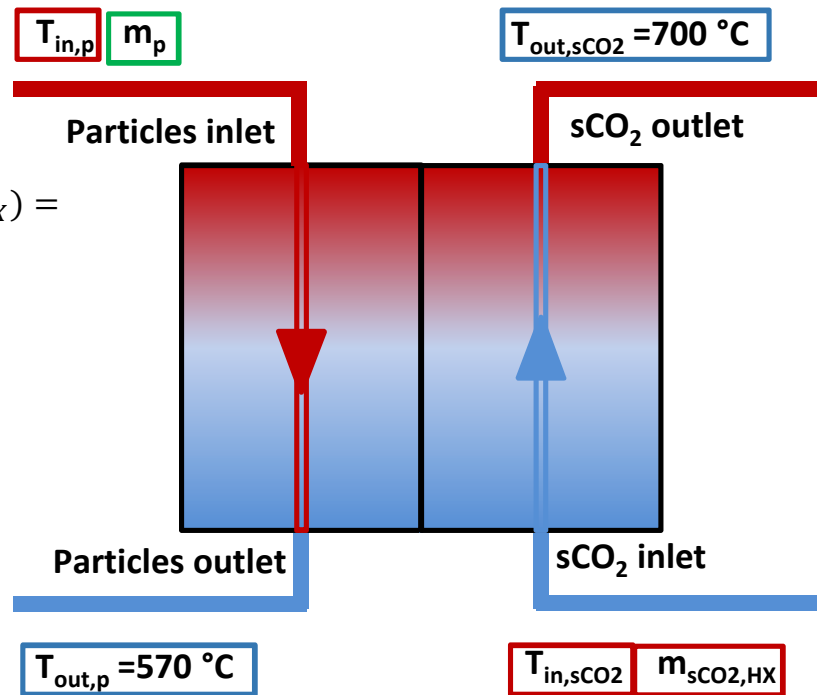
- Steady state equations

1) Heat exchanger energy balance

$$m_{sCO_2,HX} \cdot c_{p,sCO_2} \cdot (T_{out,sCO_2,HX} - T_{in,sCO_2,HX}) = m_p \cdot c_{p,p} \cdot (T_{in,p} - T_{out,p})$$

2) ΔT mean log equation

$$m_p \cdot c_{p,p} \cdot (T_{in,p} - T_{out,p}) = U \cdot A \cdot \Delta T_{lm}$$



5. Control strategies

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- Steady state equations

- 1) Heat exchanger energy balance

$$m_{sCO_2,HX} \cdot c_{p,sCO_2} \cdot (T_{out,sCO_2,HX} - T_{in,sCO_2,HX}) = m_p \cdot c_{p,p} \cdot (T_{in,p} - T_{out,p})$$

- 2) ΔT mean log equation

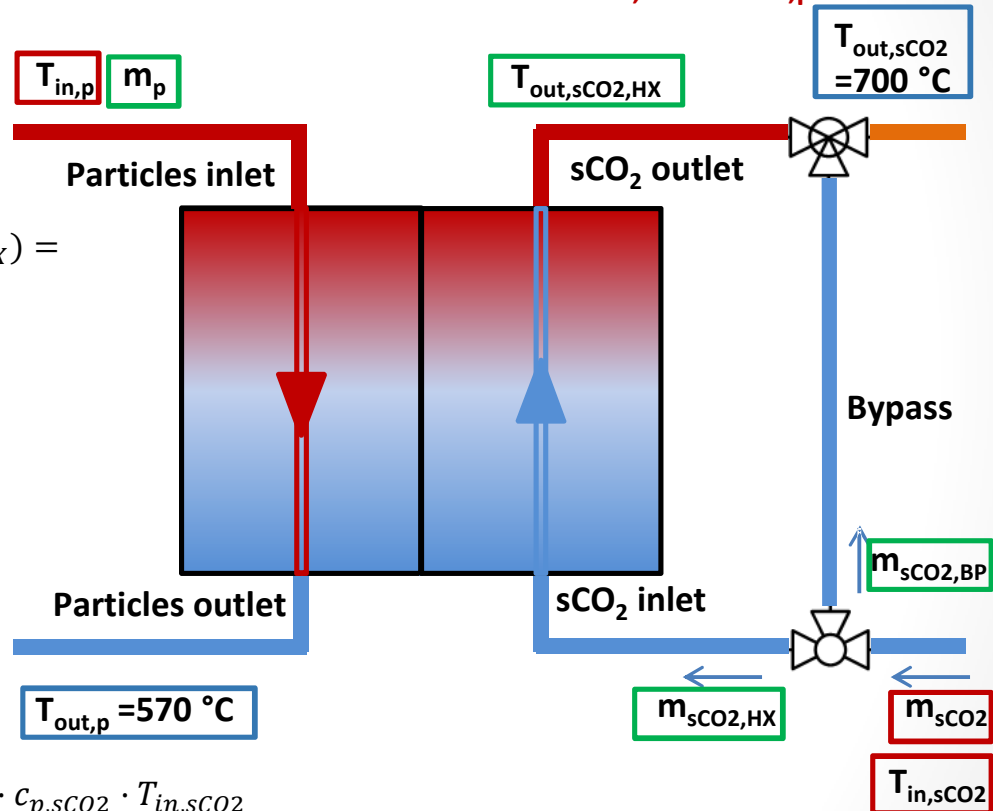
$$m_p \cdot c_{p,p} \cdot (T_{in,p} - T_{out,p}) = U \cdot A \cdot \Delta T_{lm}$$

- 3) Bypass mass balance

$$m_{sCO_2} = m_{sCO_2,BP} + m_{sCO_2,HX}$$

- 4) Bypass energy balance

$$m_{sCO_2} \cdot c_{p,sCO_2} \cdot T_{out,sCO_2} = m_{sCO_2,HX} \cdot c_{p,sCO_2} \cdot T_{out,sCO_2,HX} + m_{sCO_2,BP} \cdot c_{p,sCO_2} \cdot T_{in,sCO_2}$$



4 equations-4 unknown variables: $m_{sCO_2,HX}$, $m_{sCO_2,BP}$, m_p , $T_{out,sCO_2,HX}$

5. Control strategies

- Steady state: for the inlet conditions of the 6 cases studied, $m_{sCO_2,HX}$ and m_p can be calculated to obtain the desired temperatures
- Transient solution: **steady state solution** + **proportional correction**

$$m_{sCO_2,HX}(t) = m_{sCO_2,HX,ste}(t) - K_{sCO_2} \cdot (T_{out,sCO_2}(t) - 700)$$

$$m_p(t) = m_{p,ste}(t) - K_p \cdot (T_{out,p}(t) - 570)$$

Proportional correction:

- To reduce T_{out,sCO_2} and $T_{out,p}$ deviations from the desired value
- K_{sCO_2} and K_p depends on the T_{in,sCO_2} , $T_{in,p}$, m_{sCO_2} change rate

Case	K_{sCO_2}			K_p		
	Step	30 min	60 min	Step	30 min	60 min
1	1.00E-04	5.00E-04	1.00E-04	0.02	5.00E-04	1.00E-04
2	1.00E-04	0	0	1.00E-04	0	0
3	1.00E-04	1.00E-04	1.00E-04	0.1	7.00E-03	7.00E-03
4	1.00E-04	1.00E-04	1.00E-04	0.1	1.50E-04	1.50E-04
5	1.00E-04	1.00E-04	1.00E-04	0.02	7.00E-03	7.00E-03
6	1.00E-04	1.00E-04	1.00E-04	0.02	7.00E-03	7.00E-03

Control results with change in sCO₂ temperature and mass flow in 30 min

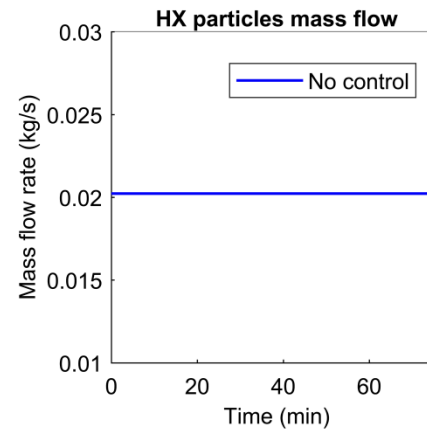
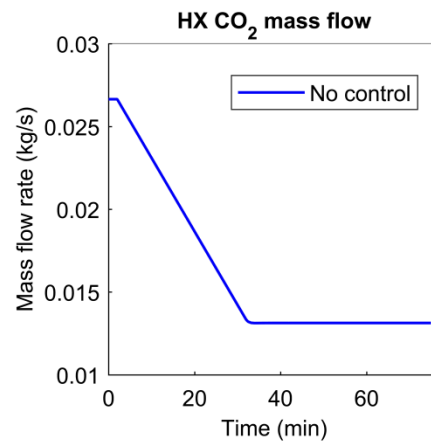
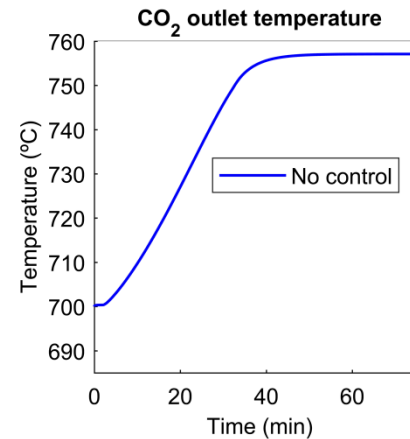
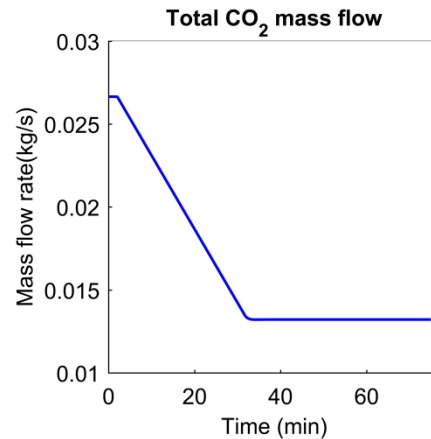
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$$m_{sCO_2} = 0.0133\text{ kg/s} (\downarrow 50\text{ \%})$$

No control $\Delta T_{out,sCO_2} = 60\text{ }^{\circ}\text{C}$



Control results with change in sCO₂ temperature and mass flow in 30 min

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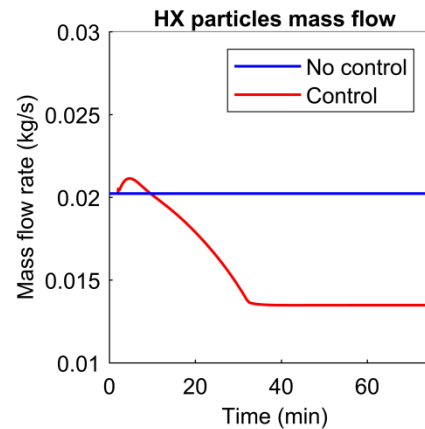
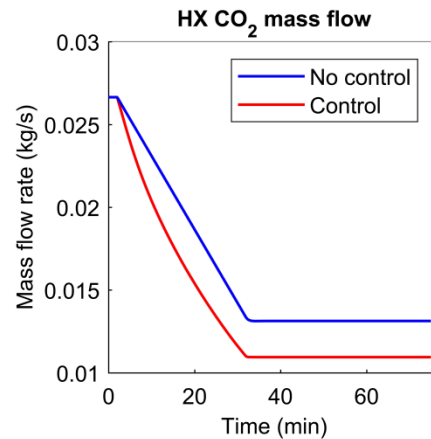
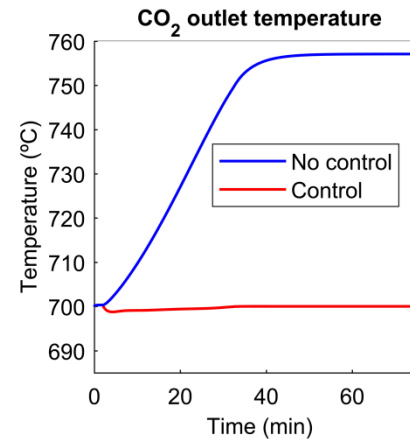
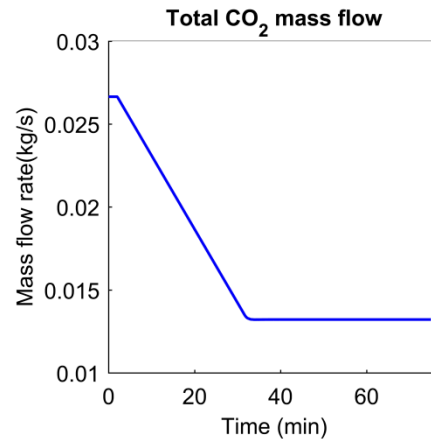
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No control $\Delta T_{out,sCO_2} = 60\text{ }^{\circ}\text{C}$

Control $\Delta T_{out,sCO_2} = 1\text{ }^{\circ}\text{C}$



OUTLINE

6. Conclusions

5. Conclusions

- The transient response of moving packed bed particles-to-sCO₂ HX in presence of inlet conditions deviations was analyzed
- A control system is needed to maintain the desired outlet temperatures during transient response
- The control system is based on installing a bypass in the sCO₂ side. Particles and sCO₂ mass flow rates through the HX are adjusted to maintain the desired outlet temperatures
- The control system developed maintains outlet temperature deviations below 1C

Acknowledgements

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Thank you for your attention