

Exceptional service in the national interest



Development of Large-Scale Inverse Methods in Sierra-SD

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Outline

- Inverse problems in computational mechanics
- Discussion of inverse methods in Sierra-SD
- Connections with design of materials and acoustic metamaterials

What is an Inverse Problem?

What is an Inverse Problem?

Inverse problems arise when we have partial information and indirect observations of a system and need to infer (hidden) quantities of interest of the system.

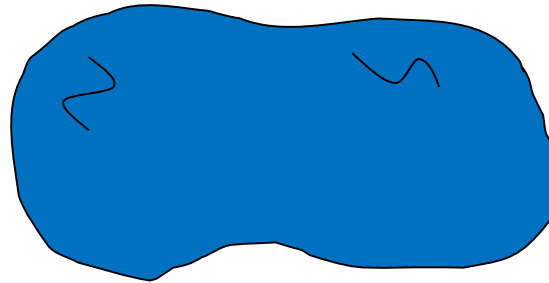
An inverse problem can be viewed as a quest for information that is not directly available from observations or measurements.

The pursuit of a solution to an inverse problem calls for a balance synergy between analysis and experimentation.

Inverse Problems: Observing the Unobservable

Suppose we have a “black box” system in the *as-manufactured* state that has only partially known parameters

Question: can we *non-destructively* interrogate the system to “see what is inside”?



Typical unknown parameters:

- Material properties
- Loads
- Boundary conditions
- Residual stresses
- Size/shape/location of inclusions (e.g. composite materials)

Example applications:

- Seismic imaging
- Medical imaging
- Non-destructive evaluation

Challenges

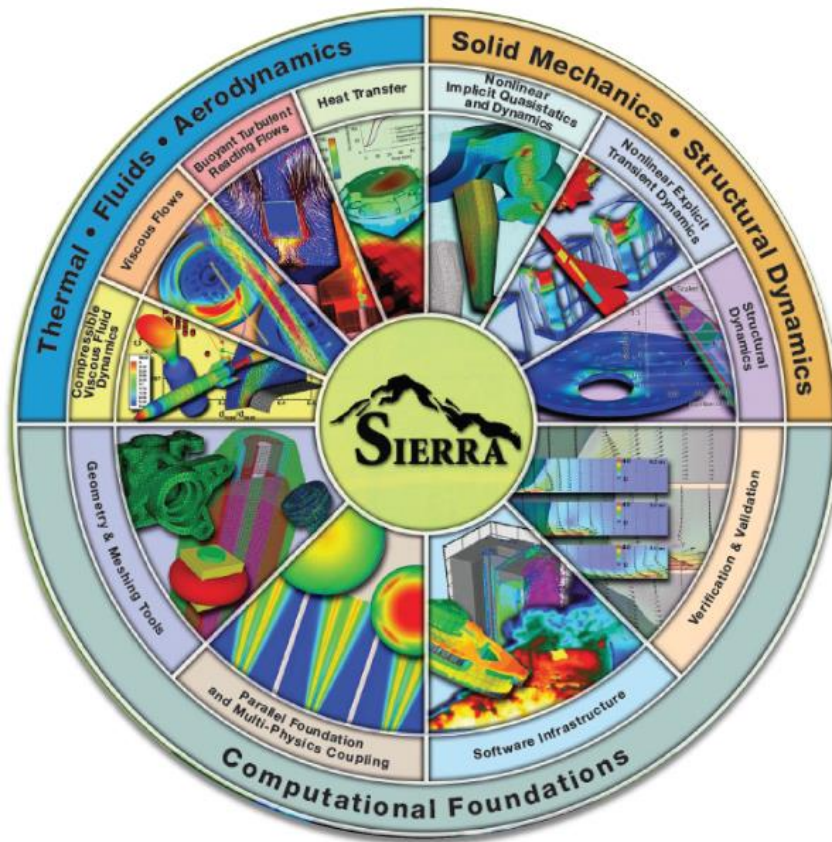
- Inverse problems can be ill-posed.
 - Solution may not exist.
 - Solution may not be unique.
 - Solution may be unstable. That is, it may be sensitive to small changes in the input data.
- Can be very computationally demanding.
- But... regularization can be used to mitigate these issues
- Or we can re-formulate the problem (different objective)

Categories of Inverse Problems

- Imaging
 - Ultrasound medical
 - seismic
- Calibration of material models
 - Structural material properties, circuits, thermal properties, etc.
- Optimal Experimental Design
 - Best placement of sensors, test fixture setups
- Shape reconstruction
 - E.g. inverse scattering
- Design of materials
 - Design material microstructure to achieve desired properties
 - E.g. Cloaking, camouflage, noise suppression, etc

Inverse Problems - Motivation

For long-term monitoring of structural systems, parallel multiphysics forward solvers (Sierra Mechanics) are not enough



Partially known information:

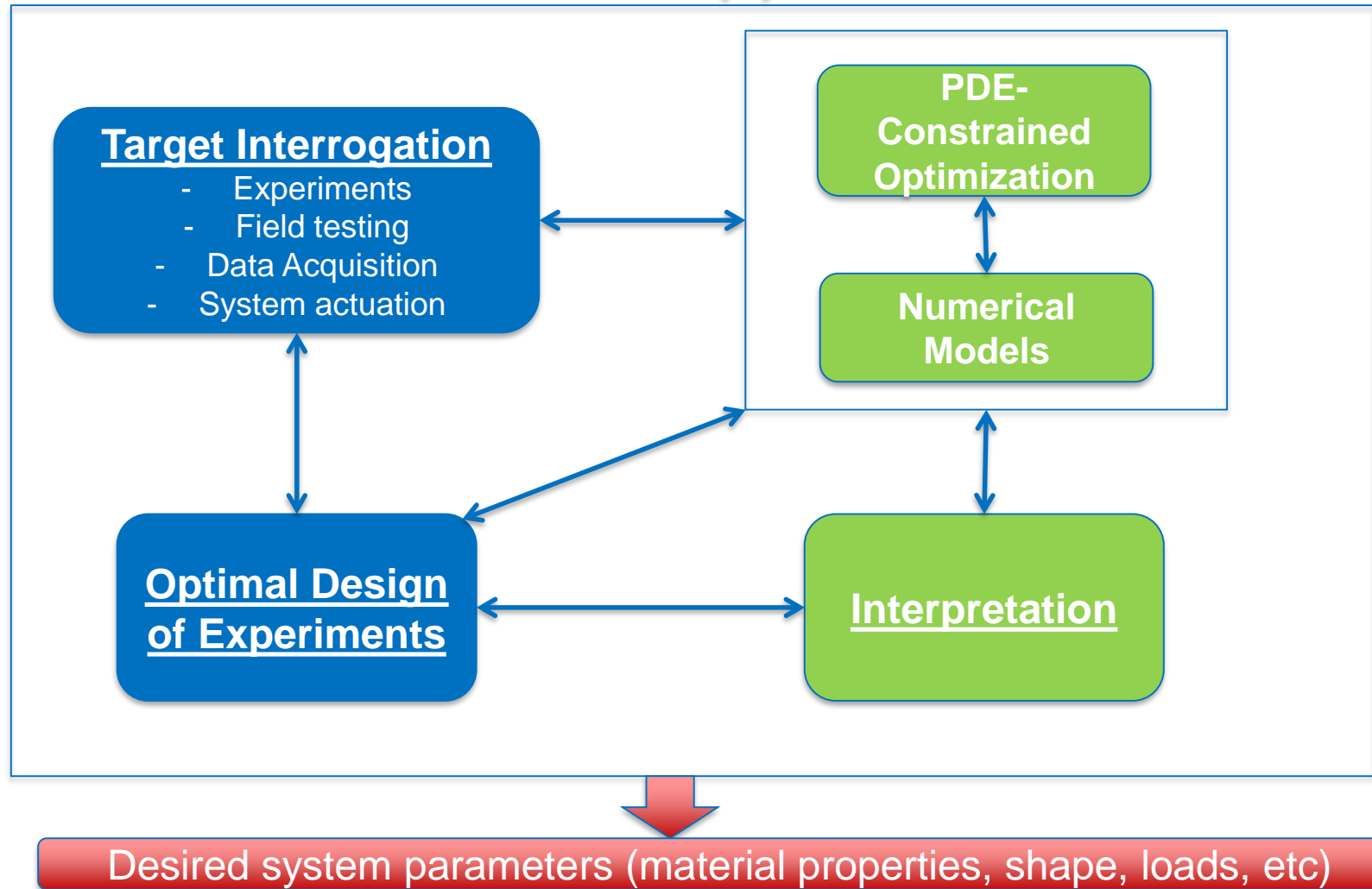
- material properties?
- boundary conditions?
- loading conditions?
- Internal flaws from aging?
- Preloading effects?

The missing link:

Experimental measurements and solution of inverse problem

Inverse Problems - The Interaction of Experiments and Simulation

Experimental data ↔ *inverse problem*



PDE-Constrained Optimization Formulation

Abstract
optimization
formulation

$$\underset{u, p}{\text{minimize}} \quad J(u, p)$$

$$\text{subject to} \quad g(u, p) = 0$$

$$\mathcal{L}(u, p, w) := J + w^T g$$

Objective function

PDE constraint

Lagrangian

$$\begin{Bmatrix} \mathcal{L}_u \\ \mathcal{L}_p \\ \mathcal{L}_w \end{Bmatrix} = \begin{Bmatrix} J_u + g_u^T w \\ J_p + g_p^T w \\ g \end{Bmatrix} = \{0\}$$

First order optimality
conditions

$$\begin{bmatrix} \mathcal{L}_{uu} & \mathcal{L}_{up} & g_u^T \\ \mathcal{L}_{pu} & \mathcal{L}_{pp} & g_p^T \\ g_u & g_p & 0 \end{bmatrix} \begin{Bmatrix} \delta u \\ \delta p \\ w^* \end{Bmatrix} = - \begin{Bmatrix} J_u \\ J_p \\ g \end{Bmatrix}$$

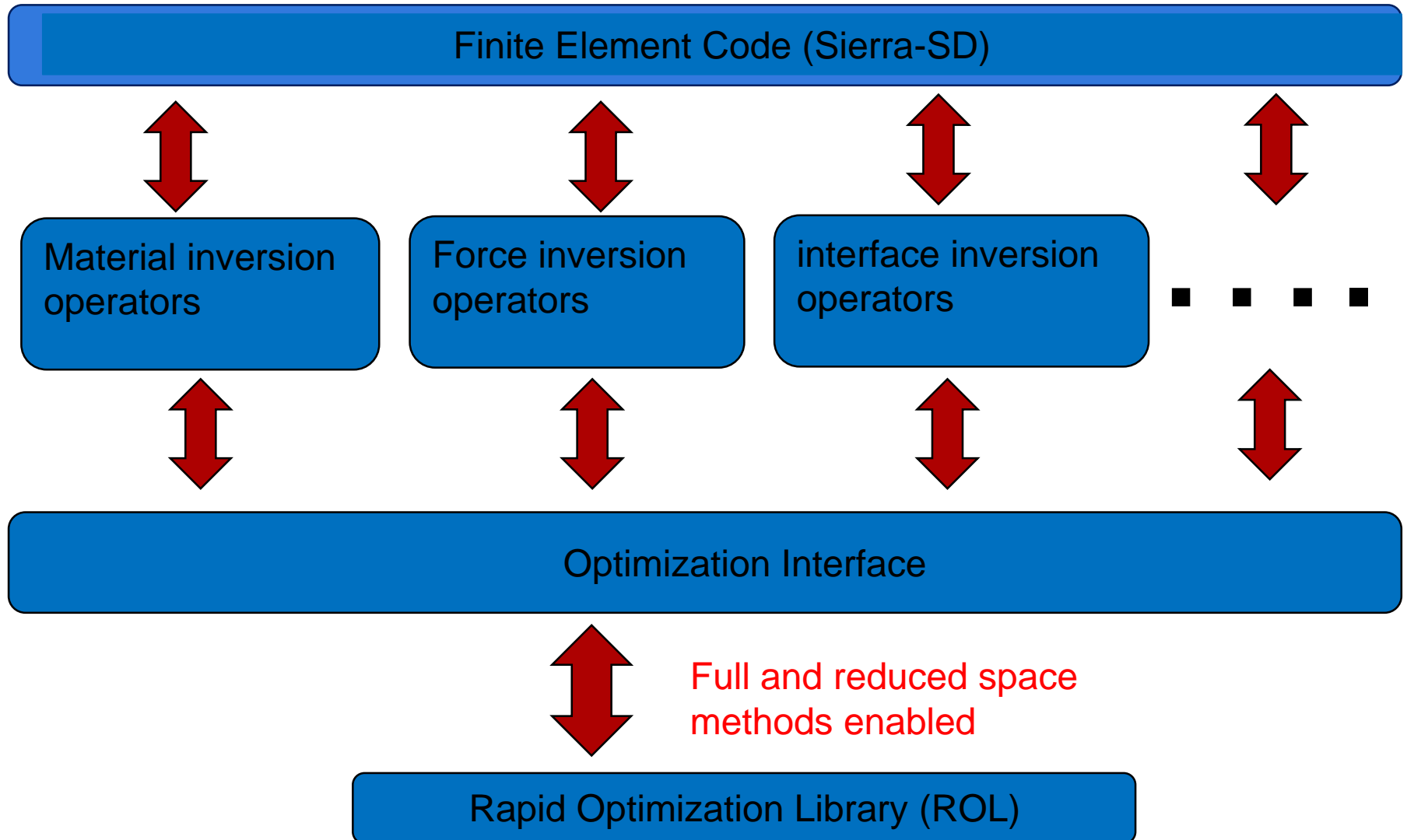
Newton iteration

$$W \Delta p = -\hat{J}',$$

$$W = g_p^T g_u^{-T} (\mathcal{L}_{uu} g_u^{-1} g_p - \mathcal{L}_{up}) - \mathcal{L}_{pu} g_u^{-1} g_p + \mathcal{L}_{pp}$$

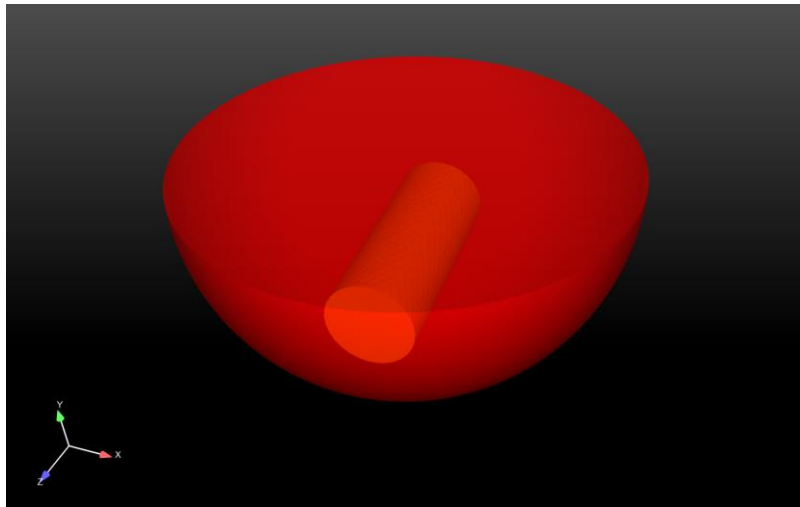
Hessian calculation

Operator-Based Inverse Problems



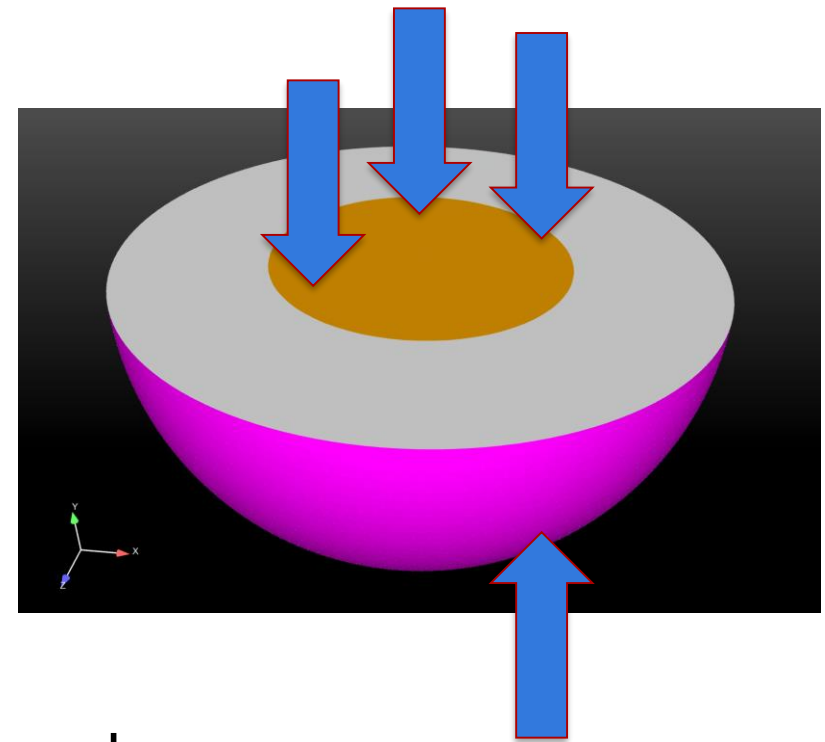
Buried Tunnel Model – MECE vs Least Squares Objectives

Buried inclusion model



Goal: locate buried inclusion and surrounding material properties

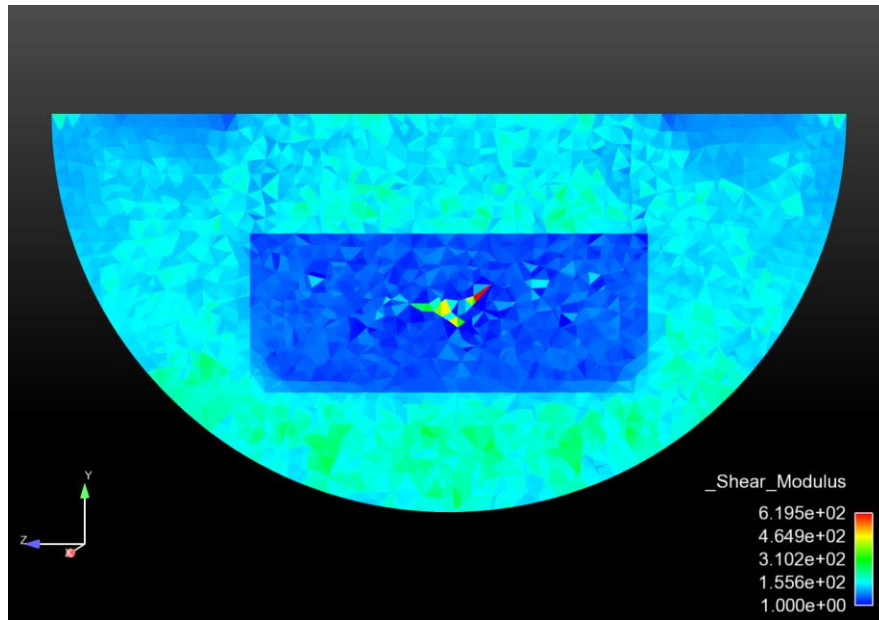
Applied pressure



Fixed boundary

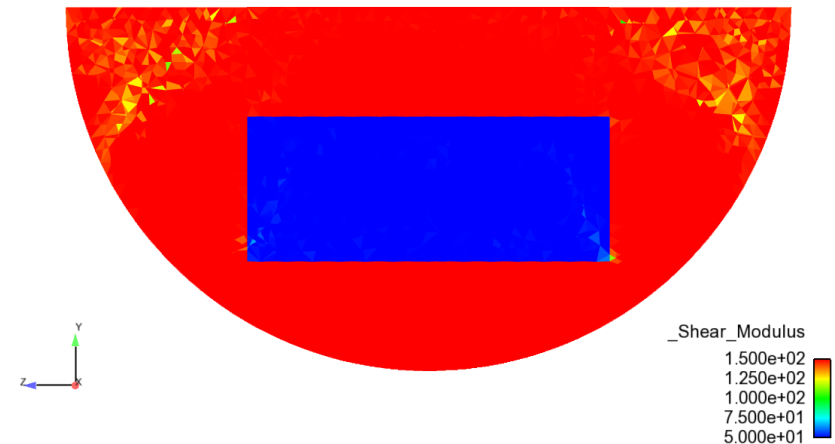
Shear Modulus – MECE vs Least Squares Objectives

Least Squares



1000 iterations

MECE



30 iterations

Exact bulk moduli: 50 (matrix), 150 (inclusion)

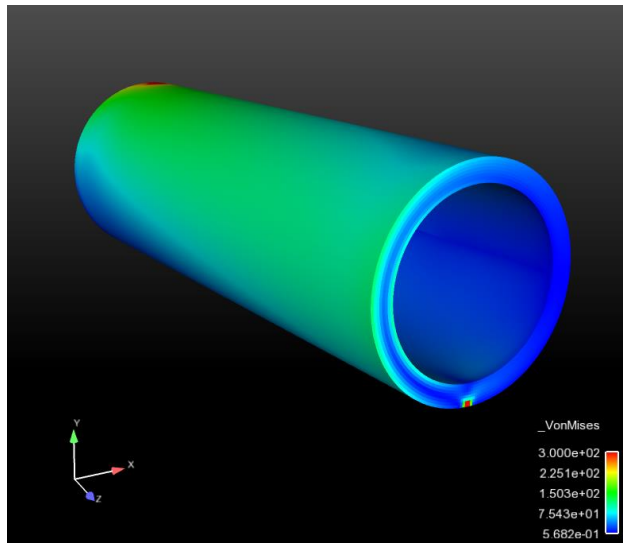
Residual Stress Inversion

Equilibrium constraint: $\nabla \cdot \sigma = 0$

Approach: source inversion for tractions on cut-plane

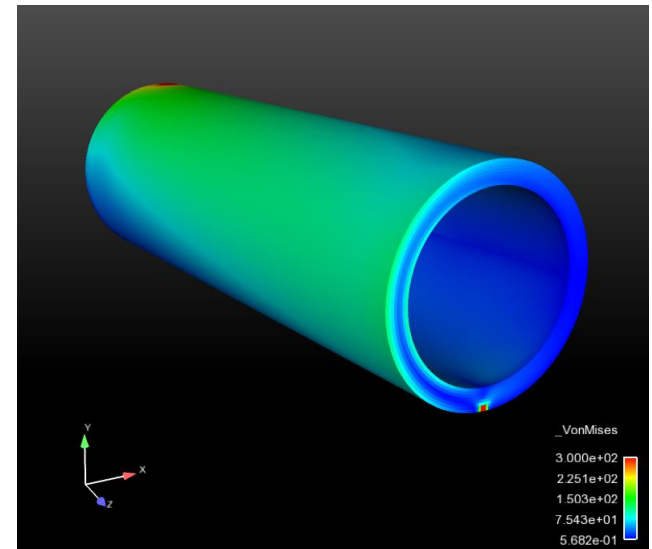
Prestressed Tube Example

Exact stress field (from forward solution)



Stress concentrated around fixed points

Stress field from inverted tractions

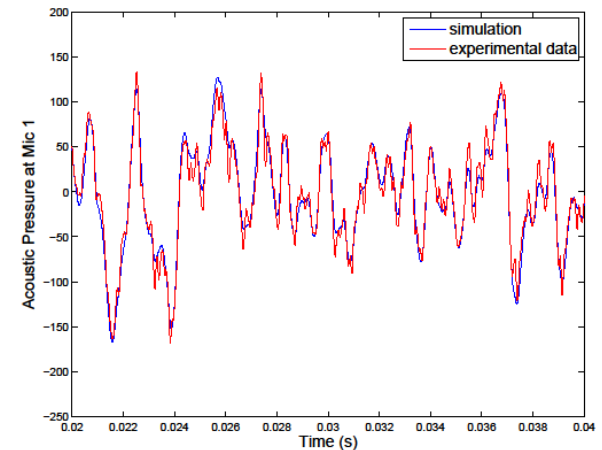
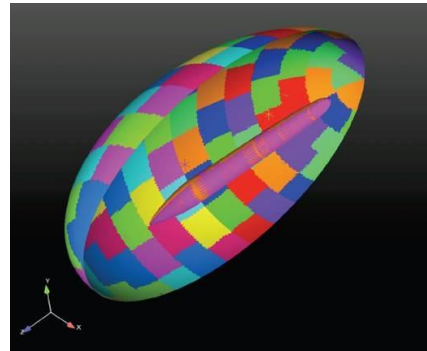
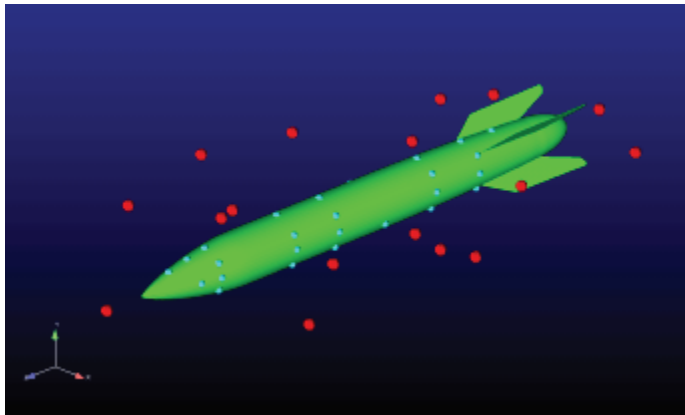


Inverted stresses

*Joint work with Joe Bishop (1554)

Source Inversion in Sierra-SD

- Goal: reconstruct acoustic field using inverse problem to obtain acoustic patch inputs that produce the given microphone measurements

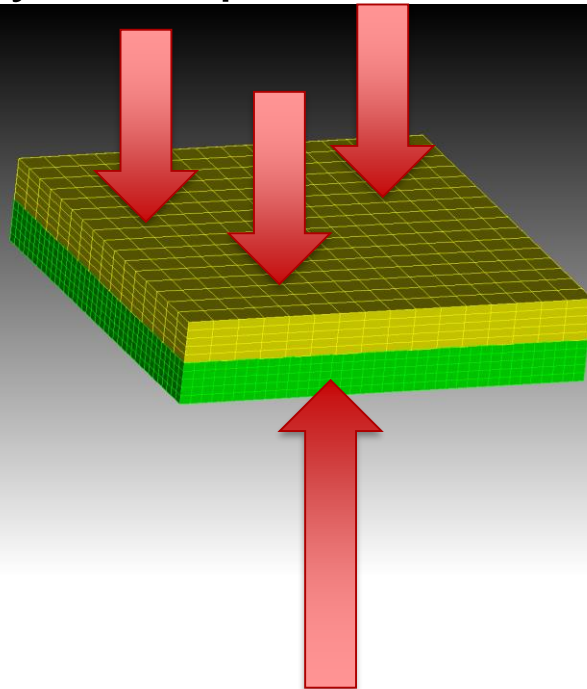


- Additional research on-going
- How to regularize the inverse problem – gradient regularization (penalize jumps across neighboring patches)
- How to place microphones

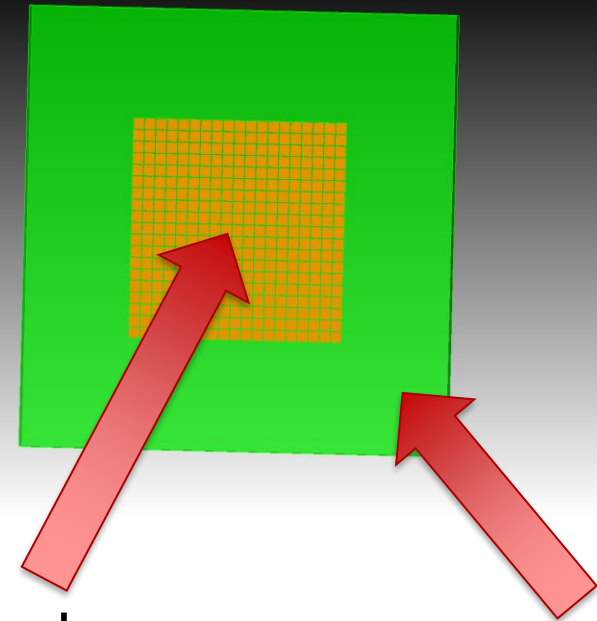
Delamination Detection

Partially-bonded plates – can we invert for the bonded/debonded regions?

Steady-state pressure load at 2000Hz



Simply supported
on bottom



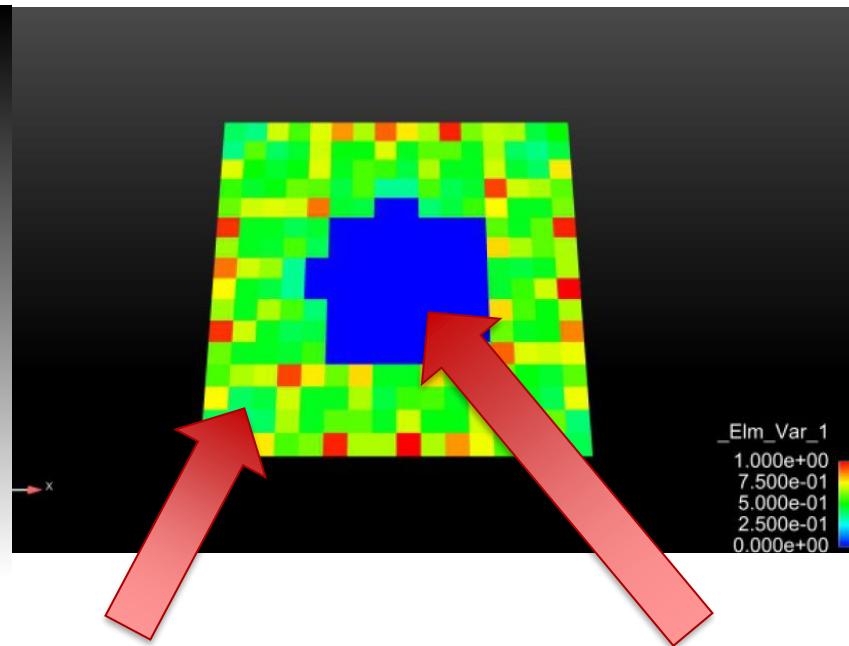
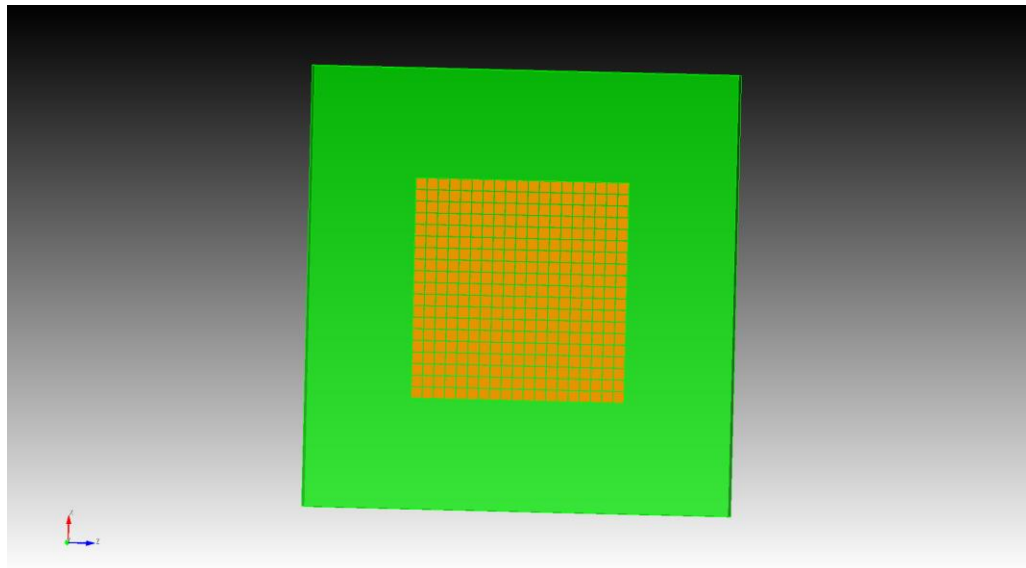
Bonded area

De-bonded
area

Delamination Example

Partially-bonded plates – can we invert for
the bonded/debonded regions?

Exact bonded/de-bonded areas



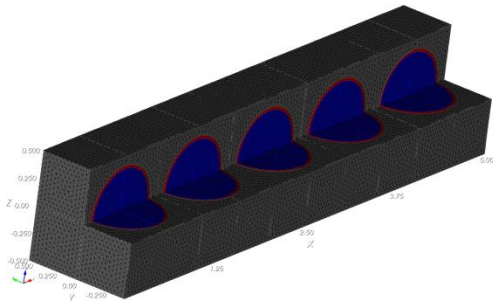
Initial guess for optimization:
Completely de-bonded

Bonded area
(penalty=1)

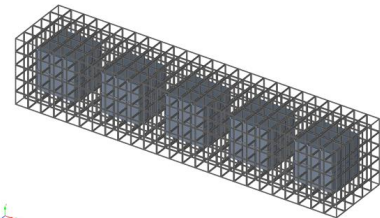
De-bonded
Area (penalty=0)

A Revolution in Acoustic Metamaterials

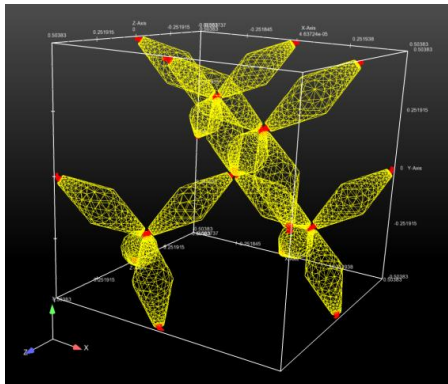
Breakthrough technology could allow us to **mitigate harsh vibration environments**



Multiphase composite



Lattice with embedded masses

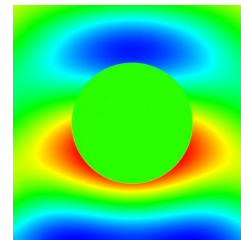
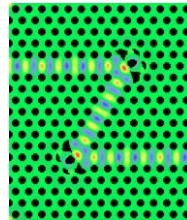


Pentamode lattice

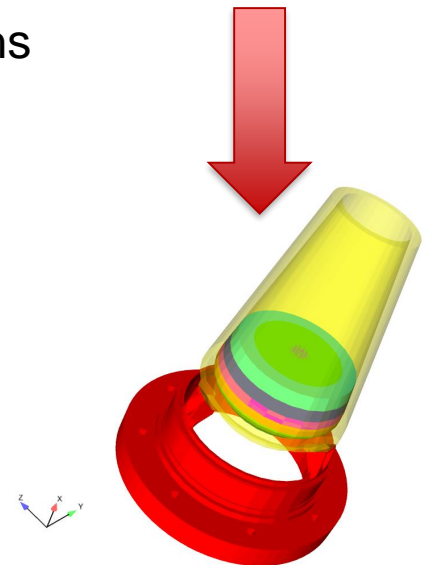
Transformative technology



Re-directed load paths



cloaking



Vibration isolation

Vibration Control with Acoustic Metamaterials

Problem: Harsh vibration environments pose serious threat to sensitive components in structural systems.

Challenge:

- Existing damping materials only provide limited vibration protection and cannot re-direct energy

As a Result:

- Sensitive components are exposed to potentially damaging vibration profiles.
 - Electronics packages, accelerometers, etc

Proposal: Large-scale optimization and multi-material additive manufacturing to design **acoustic metamaterials** for vibration control.

What is an acoustic metamaterial

- Acoustic metamaterials: Multiphase composite materials designed to produce dynamic material properties not found in individual materials themselves
 - Negative moduli, negative density, negative refractive index, imaginary speed of sound!!! (not possible in traditional composite materials)
- First demonstrated in 2000 by Liu et al, *Science*

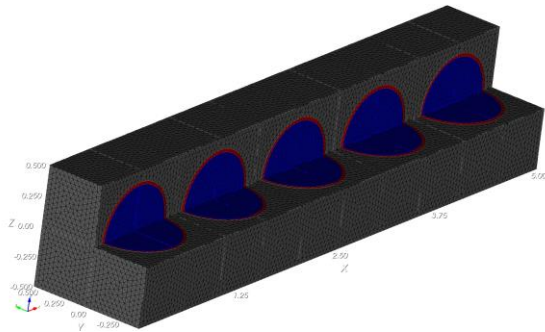
Mechanical Filter Design

Uniqueness of metamaterials – allow for frequency-selective designs!

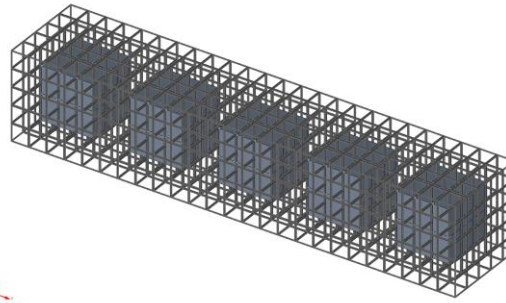
- Broadband – goal is to eliminate vibration in wide (or entire) frequency band - foam pads work well for this
- Band-stop – negative stiffness or negative density
- Band-pass – negative stiffness AND negative density (see paper on sharepoint)
- Notch – only filter at one particular frequency

Candidate Metamaterial Designs

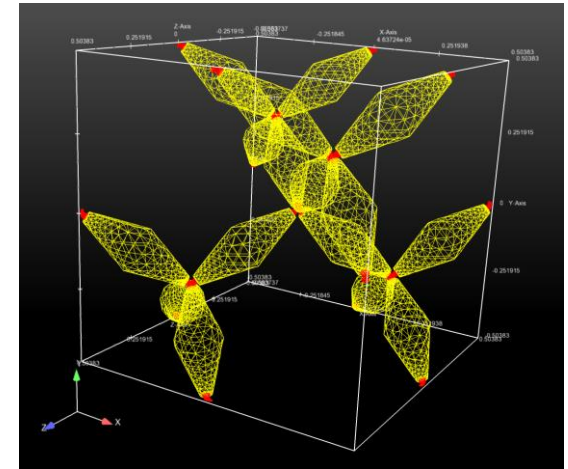
Finite element models have been developed and analysis is on-going for 3 classes of metamaterial designs. In all cases, local resonating elements are embedded in a host material.



Multiphase composite



Lattice with
embedded
masses



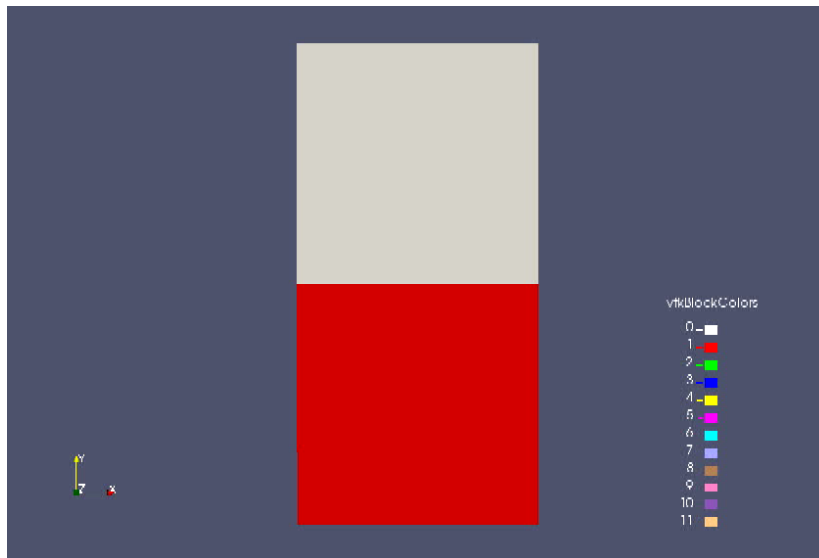
Pentamode lattice

Inverse homogenization – to achieve spatially distributed material properties

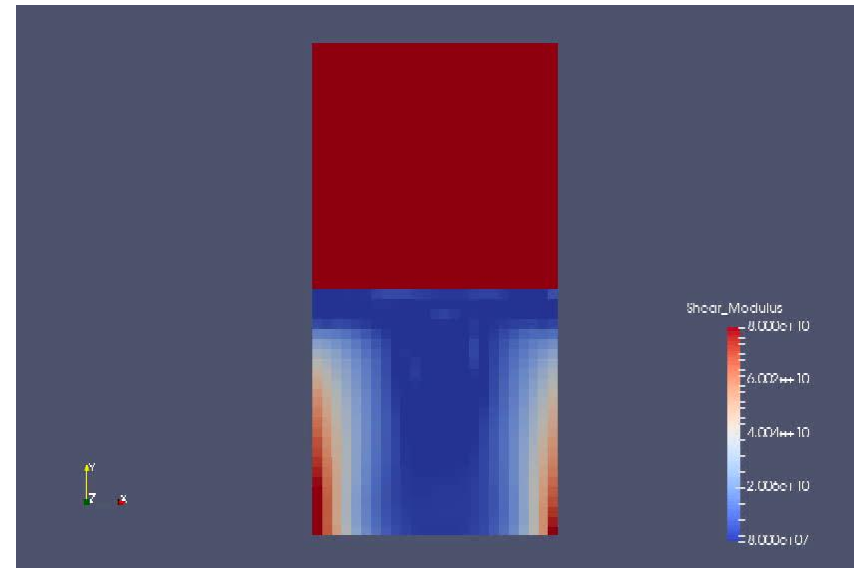
Transient Shock Isolation

Goal: design the bottom material such that the top block does not move

Initial guess



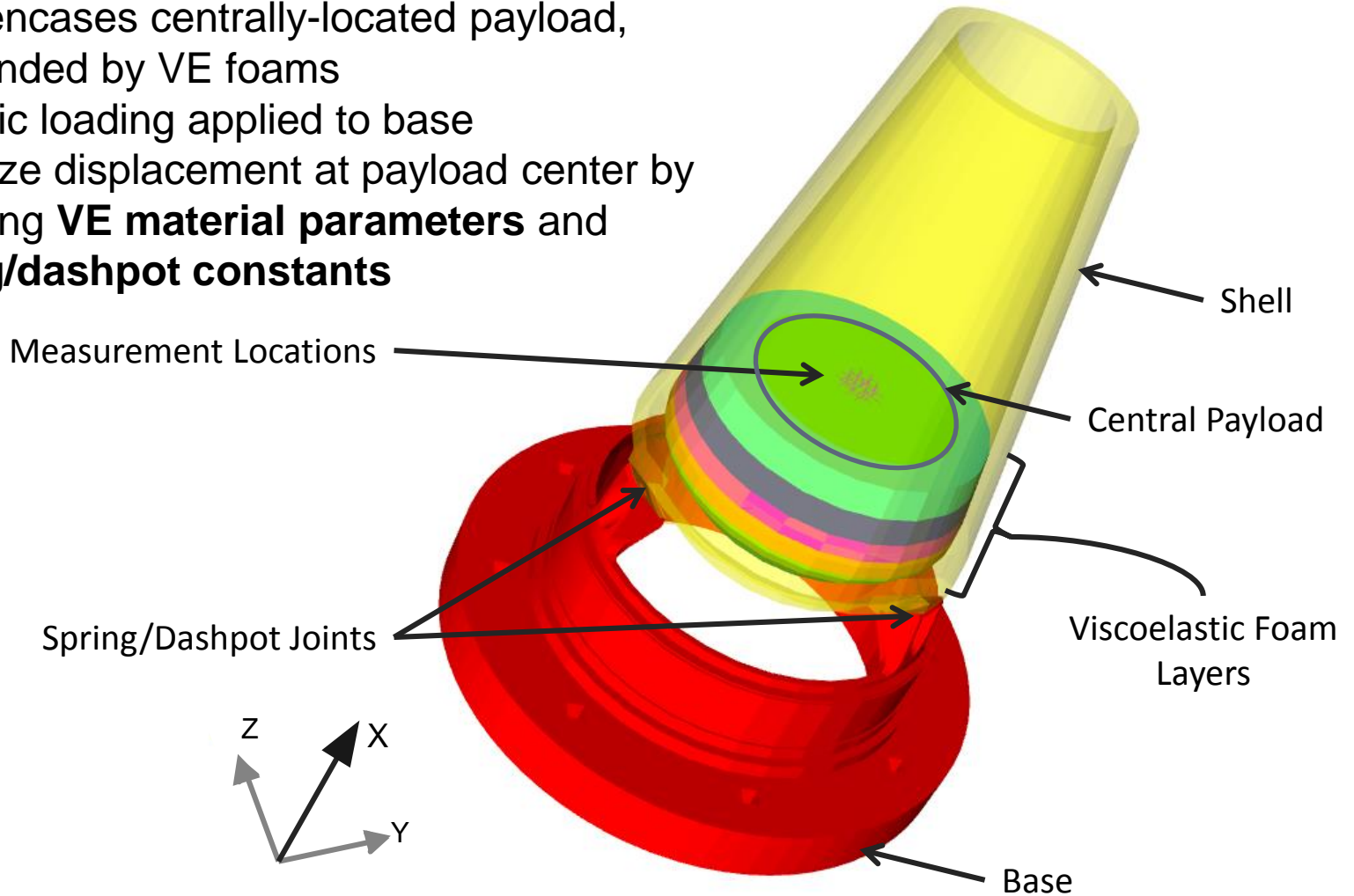
optimized



Top block: steel
Bottom block: single phase fixed, two-phase,
multi-phase

Inverse Problems: *Mechanical Vibration Reduction*

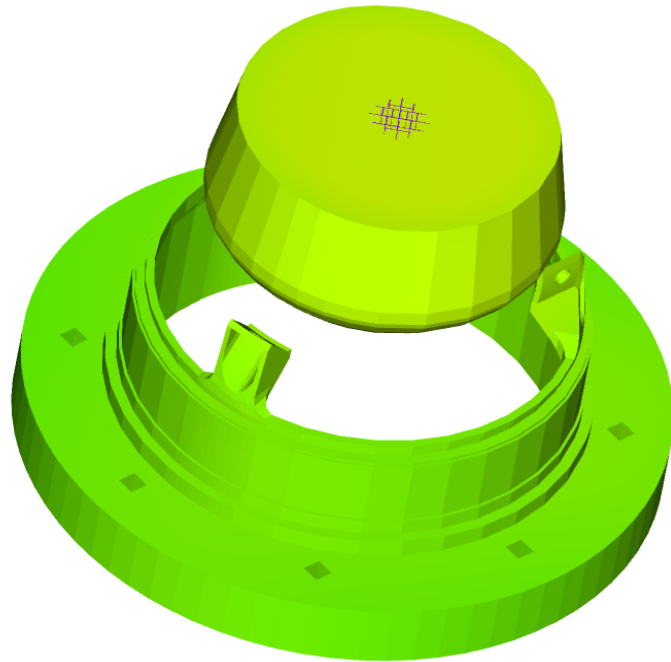
- Shell encases centrally-located payload, surrounded by VE foams
- Periodic loading applied to base
- Minimize displacement at payload center by adjusting **VE material parameters** and **spring/dashpot constants**



Case Study 1: *Mechanical Vibration Reduction*

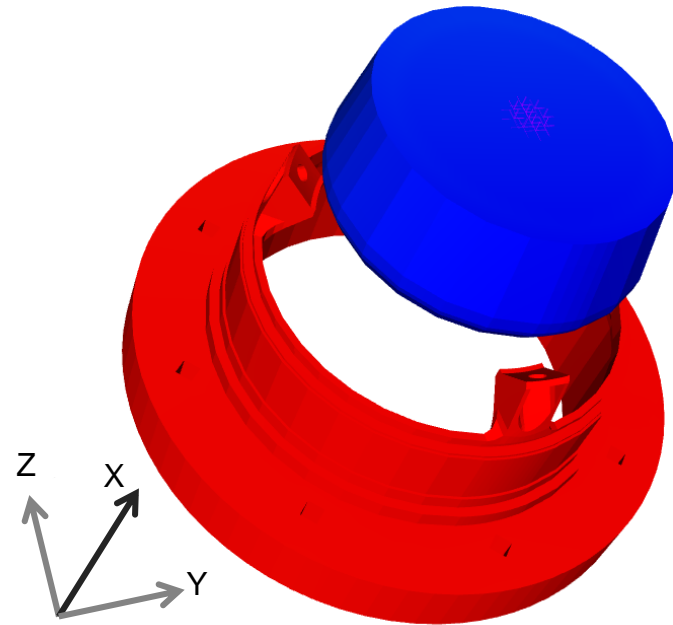
- Displacement at measurement locations minimized (dependent on frequency)

Initial Guess



_DispX
3.387e-05
1.818e-05
9.761e-06
5.240e-06
2.813e-06

Optimized

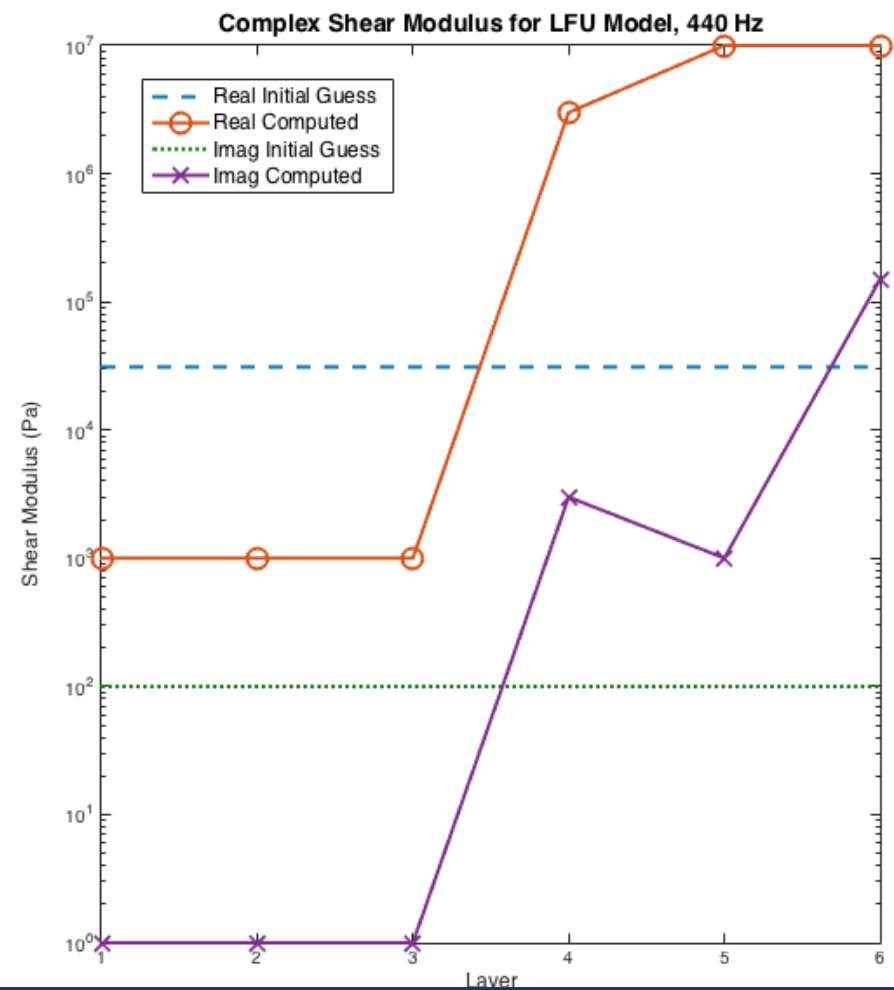
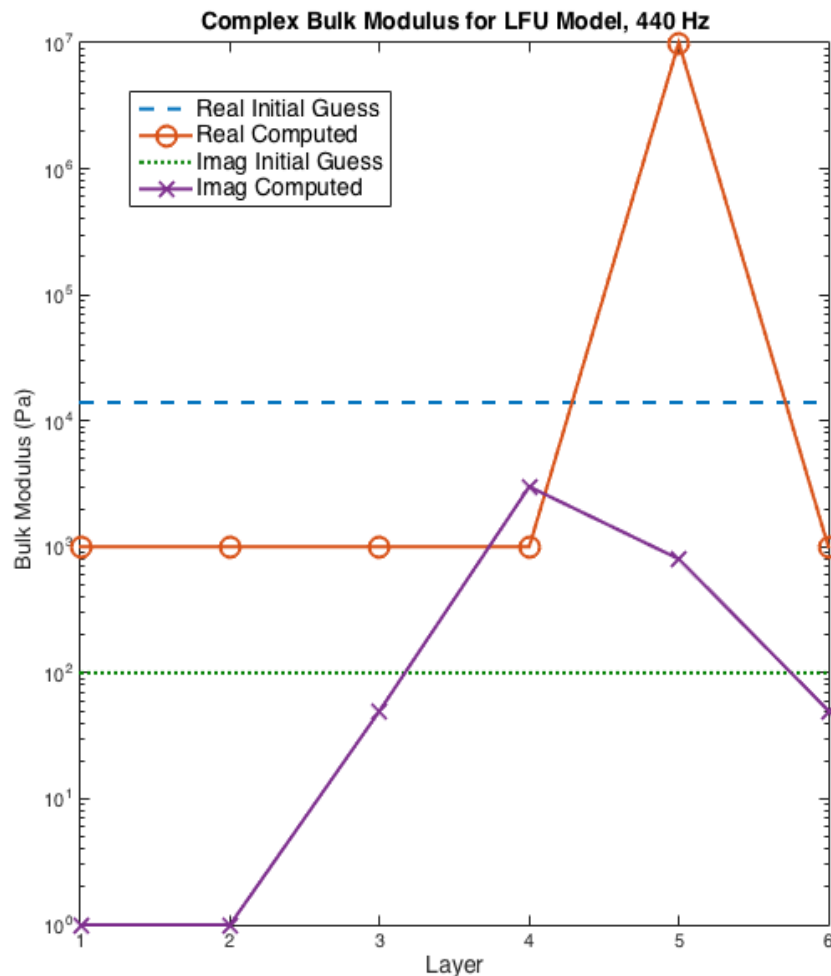


_DispX
3.387e-05
1.818e-05
9.761e-06
5.240e-06
2.813e-06

Left: X-displacement in base and payload with initial material guesses, 440 Hz loading;

Right: X-displacement in design

Case Study 1: *Mechanical Vibration Reduction*

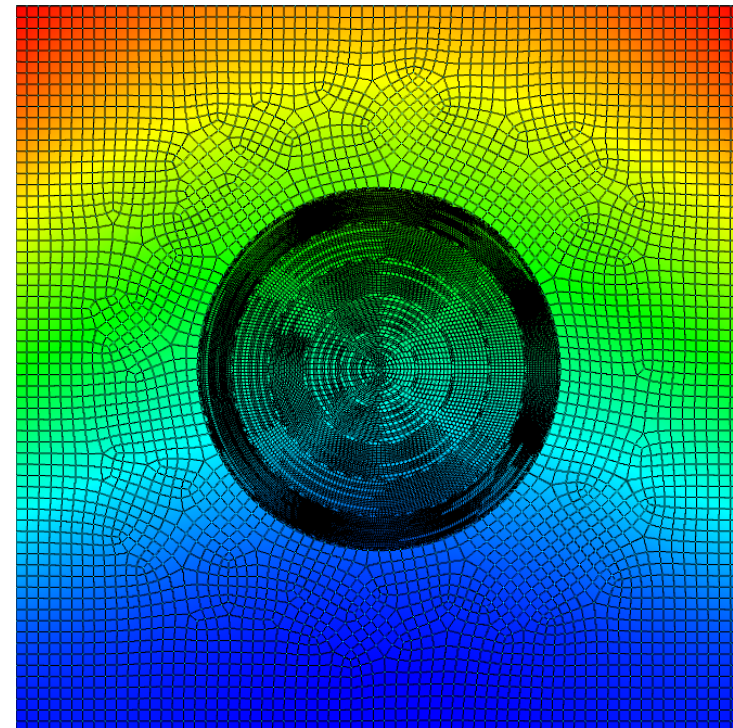
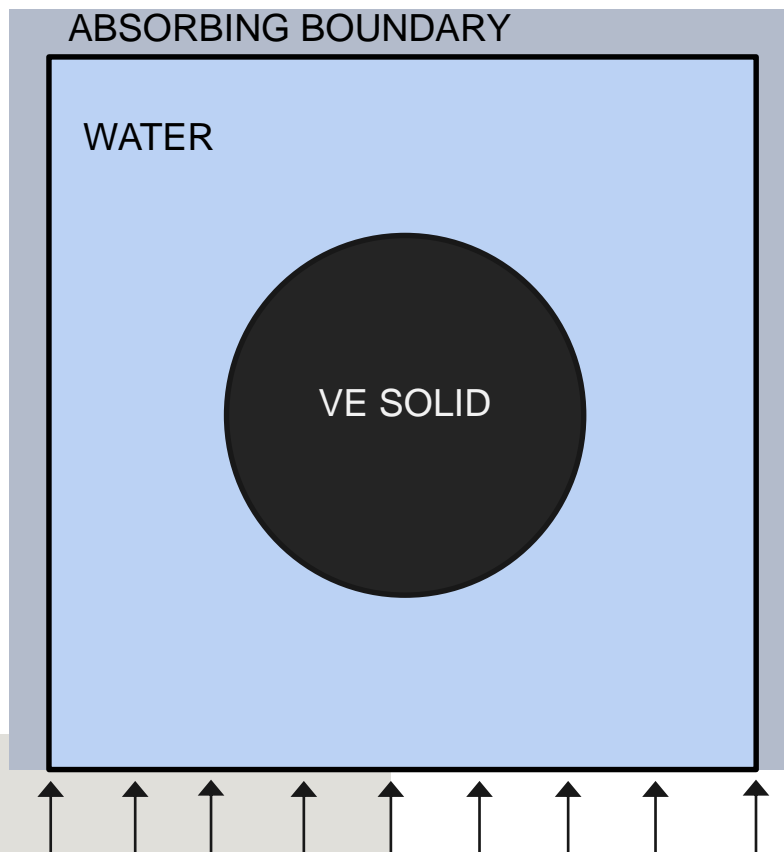


OBSERVATIONS:

- Elastic Properties: Soft materials selected towards top, stiffer materials near base
- Viscous Properties: Damping is added towards base of viscoelastic region

Inverse Problems: *Acoustic Cloaking*

- 2-D fluid region with circular VE solid inclusion
- Inclusion consists of concentric rings w/ distinct material properties
- Periodic acoustic load applied to end
- Match forward problem pressure distribution by adjusting **VE material parameters**



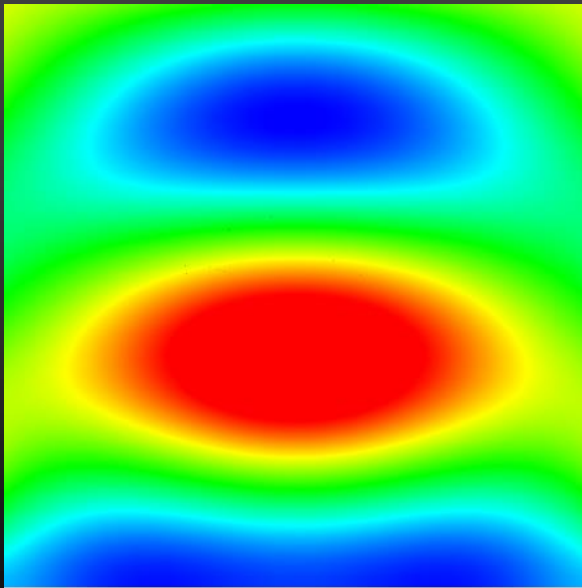
Left: Model Set up

Right: Forward problem pressure distribution (500 Hz loading) in model with 50 layers

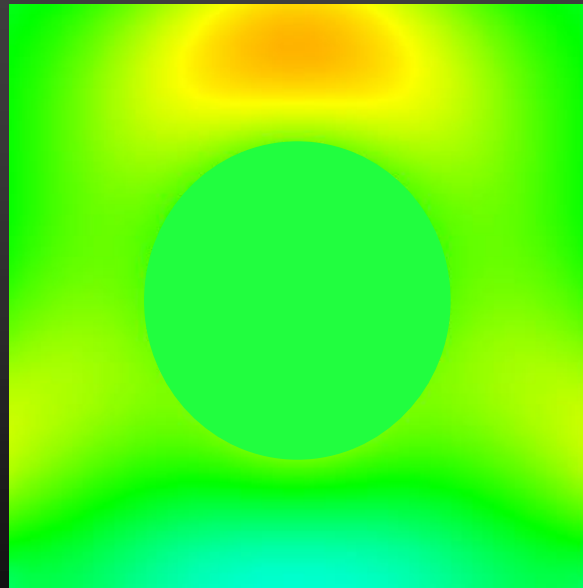
Acoustic Cloaking

- Optimized VE foams allow recovery of desired pressure distribution

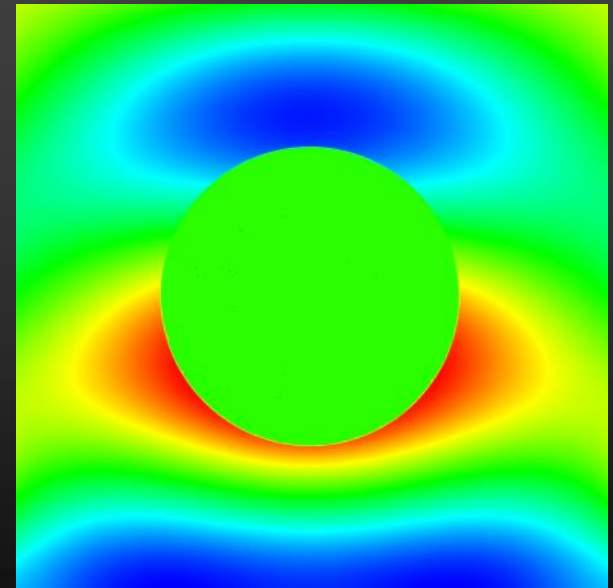
Forward



Initial Guess



Optimized



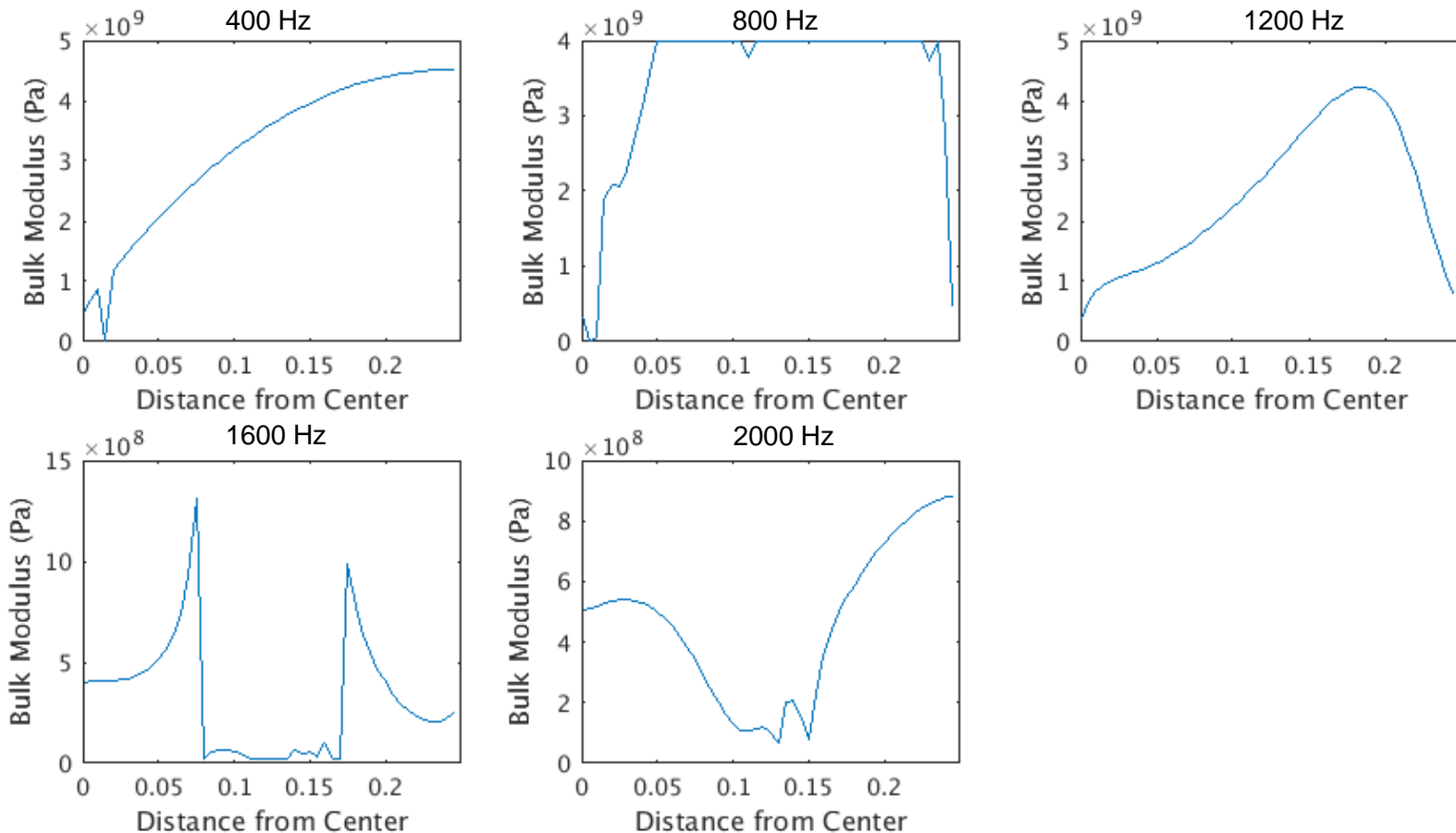
Left: Target acoustic pressure distribution, from forward problem

Center: Acoustic pressure distribution with initial material guess (2000 Hz Loading)

Right: Pressure distribution after convergence to optimized design

Acoustic Cloaking Results: Bulk Modulus

Bulk modulus sensitive to frequency, and varies nontrivially along disk radius



Figures: Real component of bulk modulus along radius, for various frequency