

Real-time TDDFT beyond the linear response regime

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Overview

TDDFT is a promising capability for *ab initio* linear response calculations in WDM

- Dynamic structure factor [1]
- Optical conductivity
- Stopping power* [2]

* Technically beyond linear response, but existing adiabatic functionals work well

Using XRTS calculations as a motivator, we will:

- See what happens beyond linear response (naively)
- Point to deficiencies in TDDFT, as implemented
- Sketch out a framework for *ab initio* x-ray heating

To describe non-LTE properties, we need to go beyond adiabatic TDDFT

Linear response in real-time

Time-evolve orbitals from Mermin Kohn-Sham DFT

$$i\frac{\partial}{\partial t}\phi_{n,\mathbf{k}}(\mathbf{r},t) = \left(-\frac{\nabla^2}{2} + v_S[\rho](\mathbf{r},t)\right)\phi_{n,\mathbf{k}}(\mathbf{r},t)$$

Weak perturbation looks like **probe x-ray envelope**

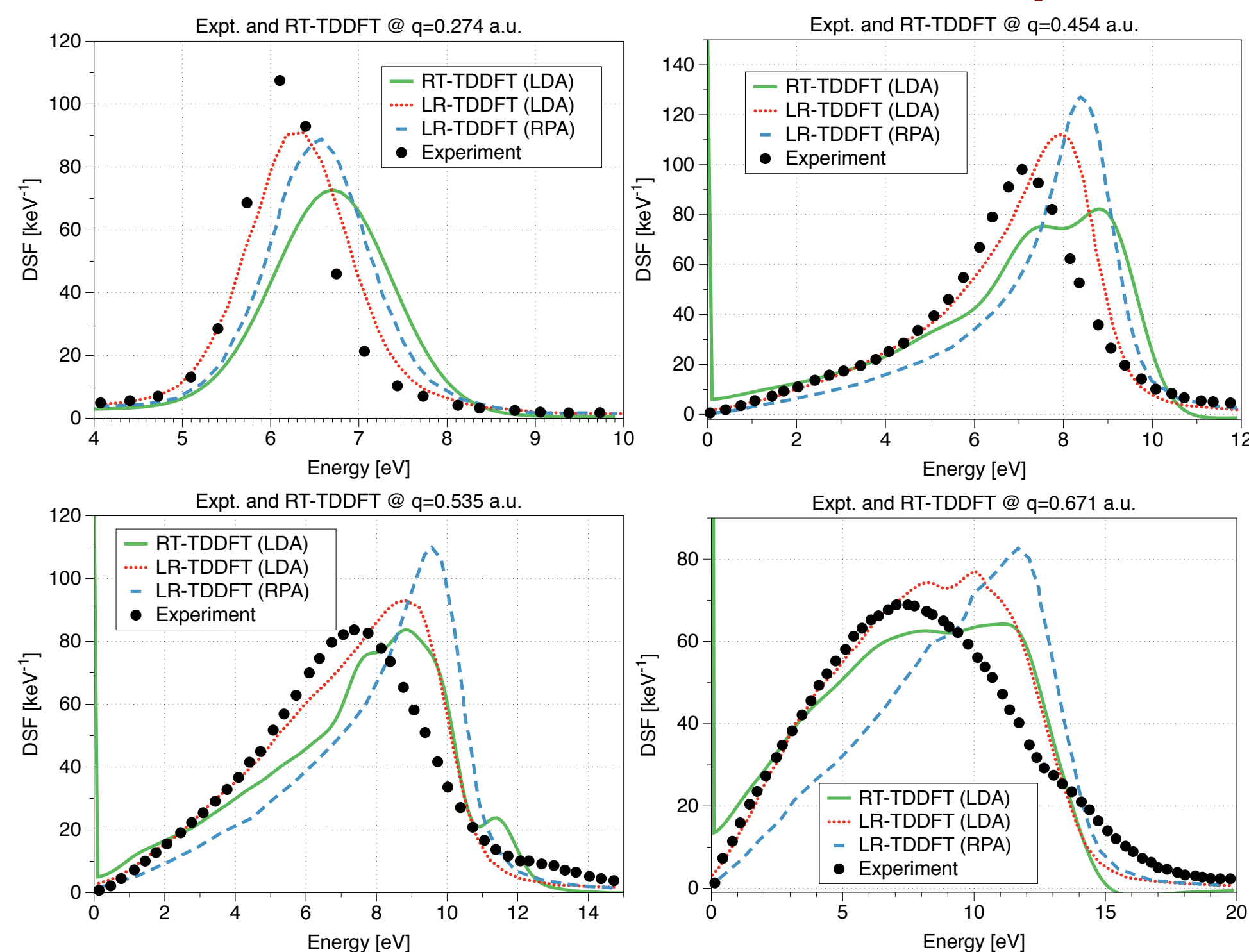
$$v_S[\rho](\mathbf{r},t) = v_{ext}(\mathbf{r},t) + v_H[\rho](\mathbf{r},t) + v_{xc}[\rho](\mathbf{r},t)$$

Build density from **TD orbitals + fixed Mermin weights**

$$\rho(\mathbf{r},t) = \sum_{n,\mathbf{k}} f_{n,\mathbf{k}}(T_e) |\phi_{n,\mathbf{k}}(\mathbf{r},t)|^2$$

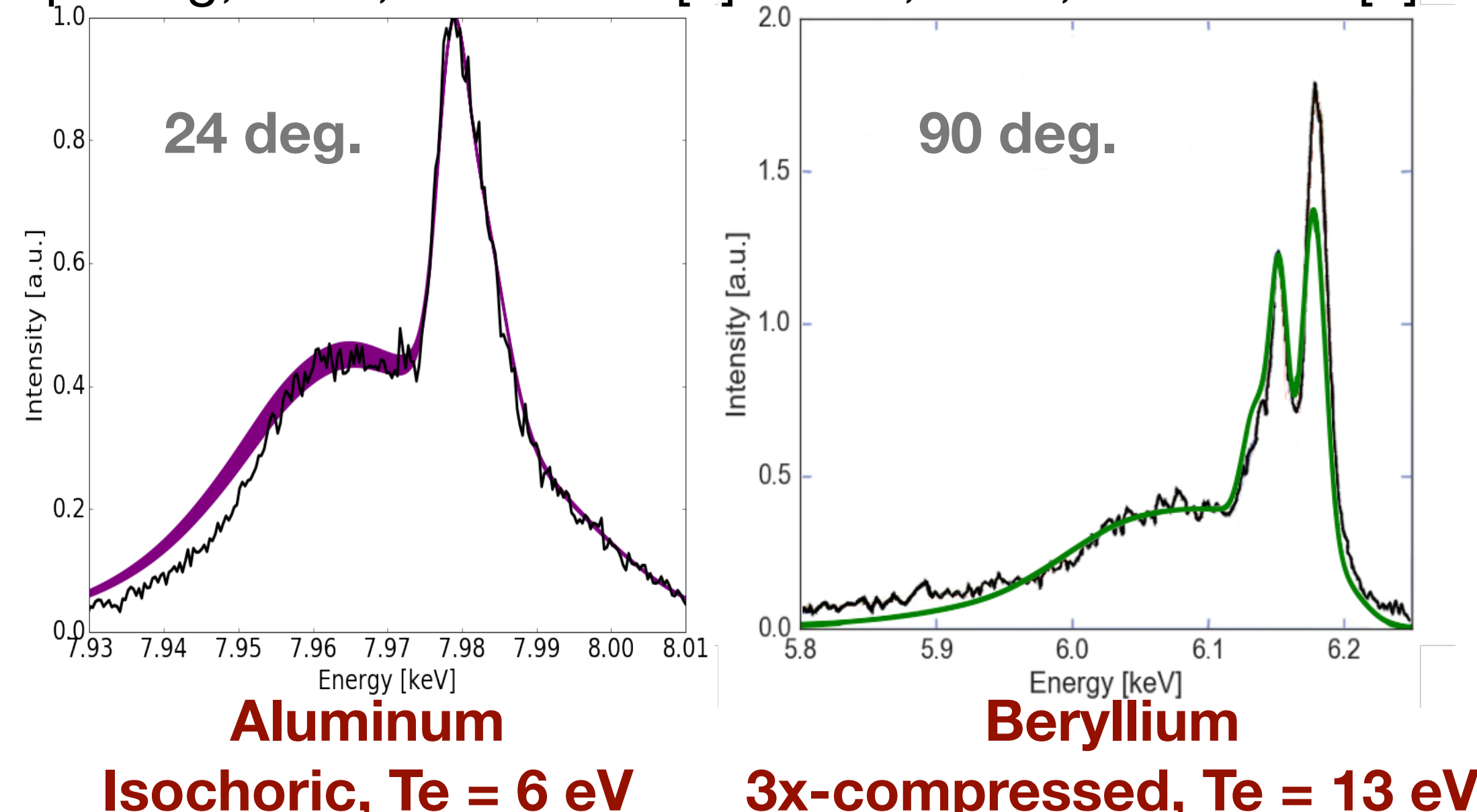
$$\chi_{\rho,\rho}(\mathbf{q},-\mathbf{q},\omega) = \frac{\delta\rho(\mathbf{q},\omega)}{\delta v_{ext}(\mathbf{q},\omega)} \longrightarrow S(\mathbf{q},\omega) = -\frac{1}{\pi} \frac{\Im[\chi_{\rho,\rho}(\mathbf{q},-\mathbf{q},\omega)]}{1 - e^{-\omega/k_B T_e}}$$

Methods consistent with each other & experiment [x]



Ambient crystalline sodium

Sperling, et al., PRL 2015 [3] Lee, et al., PRL 2009 [4]



Aluminum

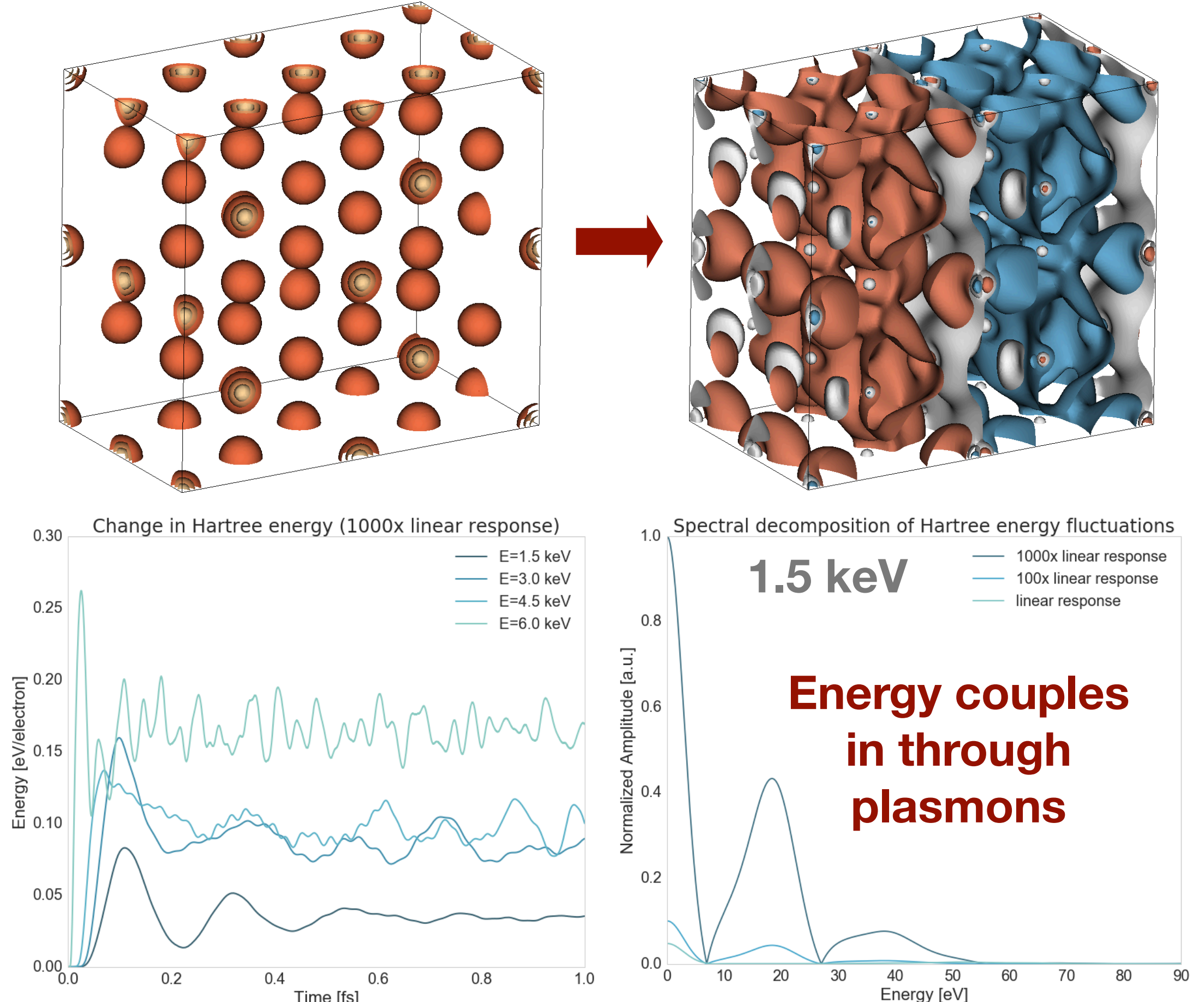
Isochoric, Te = 6 eV

Beryllium

3x-compressed, Te = 13 eV

Beyond linear response

Can we isochorically heat beryllium in TDDFT?



X-ray directly drives plasmons, but TDDFT (as implemented) is missing physics:

- Kohn-Sham occupancies don't know how to change
- No direct core excitations
- No Auger processes
- Ejected high energy electrons cannot drive plasmons

How can we proceed?

State-of-the-art Kinetics

- Multi-configuration atoms
- Electrons equilibrate instantaneously
- Heuristic treatment of coupling to environment
- Partition Hamiltonian into low and high energy sectors:

Real-time TDDFT

- Single configuration atoms
- Electrons can't equilibrate on their own
- Consistent treatment of coupling to environment

$$\mathcal{H}_{KS}(\text{Be}^{n+}) + \mathcal{H}_{HE} + \mathcal{H}_{KS,HE}(\text{Be}^{n+})$$

KS-DFT Hamiltonian for each charge config.

Quasi-free electrons

Coupling at fixed total charge

- Integrate out high energy sector / create self-energy

$$\mathcal{G}(\text{Be}^{n+}) = \mathcal{G}_{KS}(\text{Be}^{n+}) + \mathcal{G}_{KS}(\text{Be}^{n+})\Sigma(\text{Be}^{n+})\mathcal{G}(\text{Be}^{n+})$$

Art is in creating an efficient approximation
Another self-energy couples charge configs.

- Solve Kadanoff-Baym equations with x-ray drive and ambient initial condition

$$\left[i\frac{d}{dz} - \bigoplus_{n=0}^4 \mathcal{H}_{TDKS}(\text{Be}^{n+}, z)\right] \mathcal{G}^<(z, z') = \delta(z, z') + \int_{\gamma} dz' \tilde{\Sigma}(z, z') \mathcal{G}^<(z, z')$$

Adiabatic TDDFT Hamiltonian in each charge sector

Self-energy approximation bootstraps in non-adiabatic effects

References

- [1] Baczewski, et al., Phys. Rev. Lett. **116**, 115004 (2016)
- [2] Magyar, et al., Cont. Plas. Phys. **56**, 459 (2016)
- [3] Cazzaniga, et al., Phys. Rev. B **84**, 075109 (2011)
- [4] Sperling, et al., Phys. Rev. Lett. **115**, 115001 (2015)
- [5] Lee, et al., Phys. Rev. Lett. **102**, 115001 (2009)