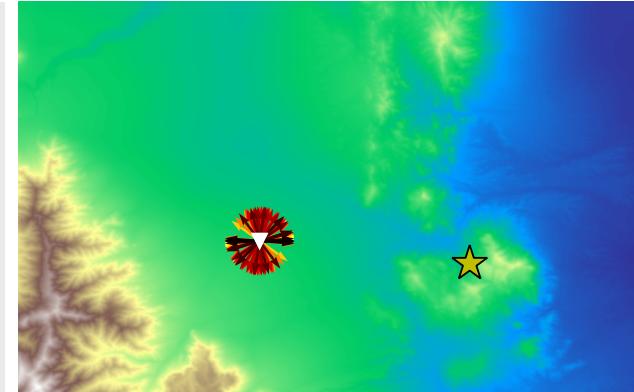
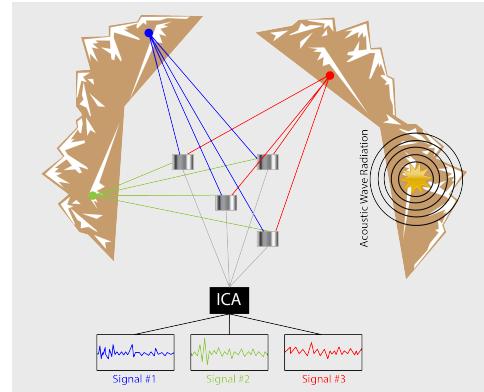
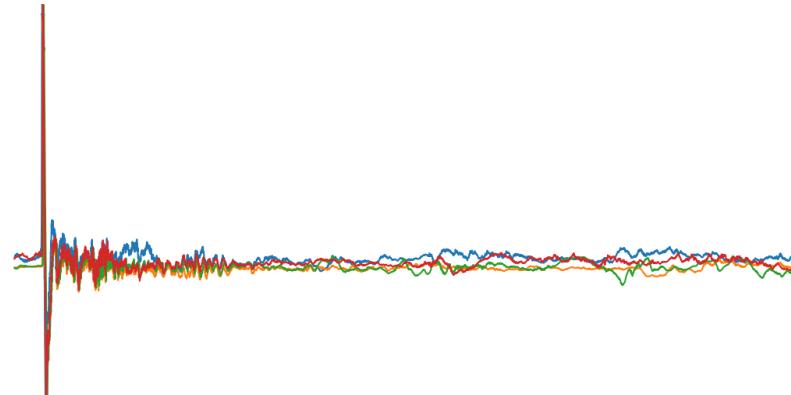


Exceptional service in the national interest



Tracking Scattered Signals in the Acoustic Coda Using Independent Component Analysis

Sarah Albert, Daniel Bowman



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Motivation

- Acoustic waves travel various paths from source to sensor
 - Direct arrival
 - Arrivals from reflections off scatterers
- Each interaction with a scatterer alters the shape of the acoustic coda
 - Consider each interaction statistically independent
 - Can use Independent Component Analysis (ICA) to separate signals
- Implications for a variety of studies
 - Volcano infrasound
 - Waveform inversion
 - Yield estimation

Independent Component Analysis

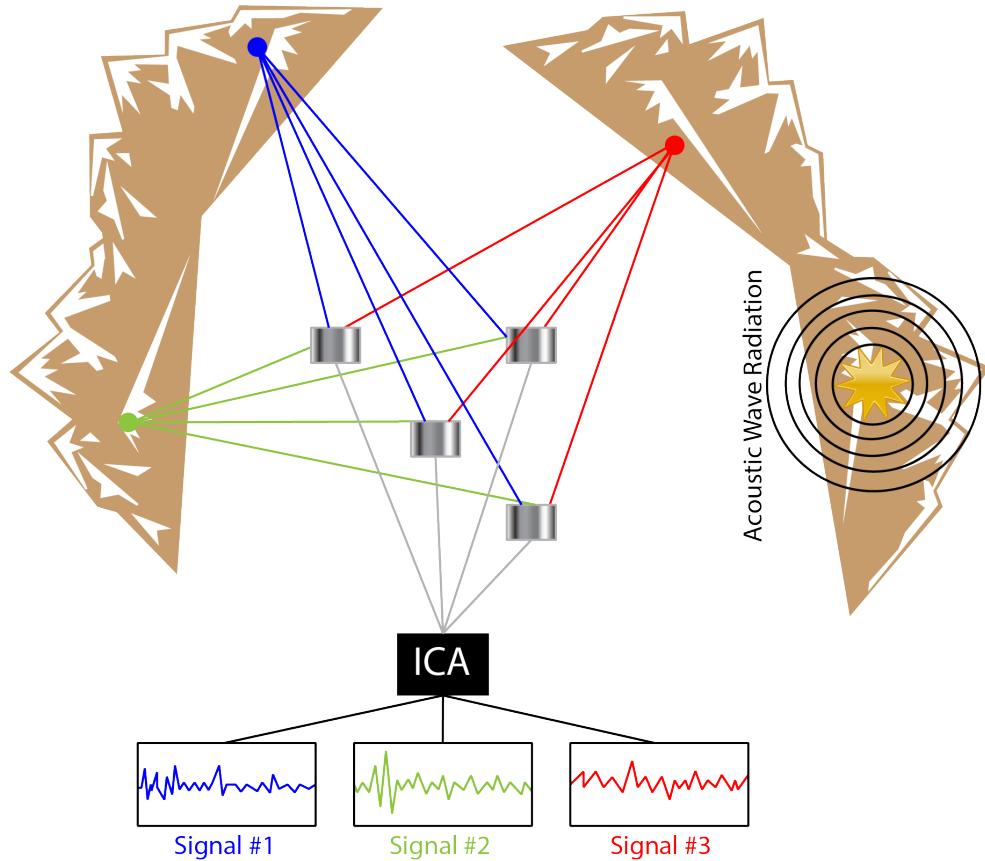


Image not to scale.

Independent Component Analysis

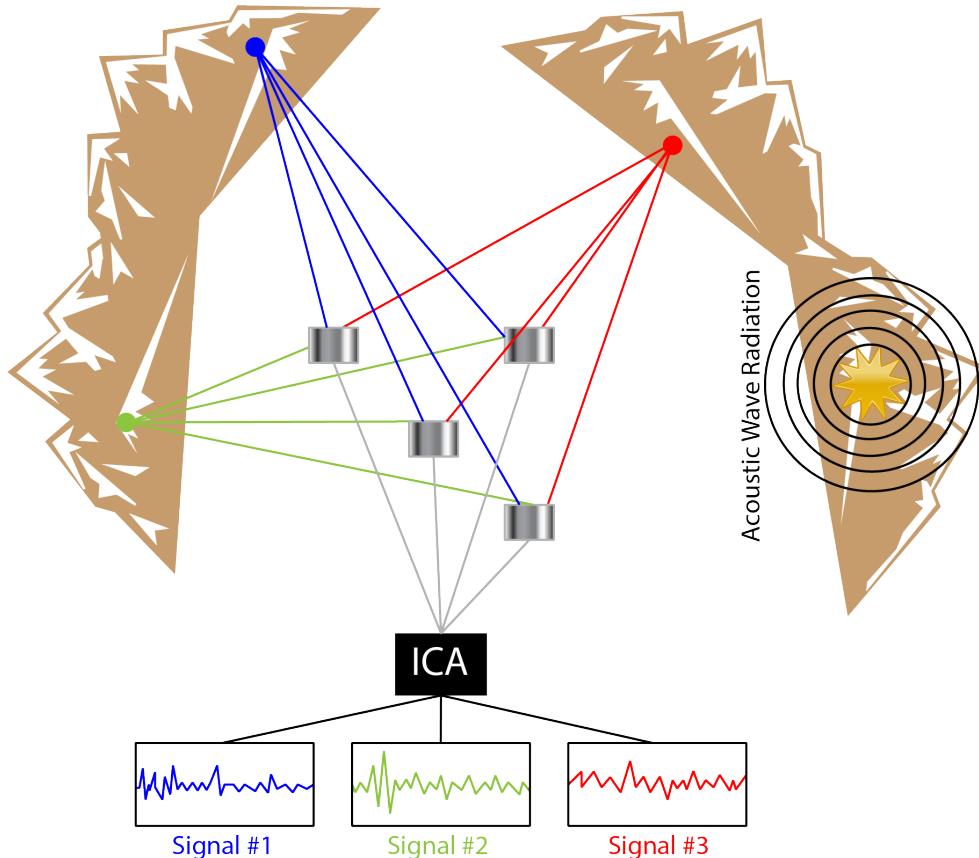


Image not to scale.

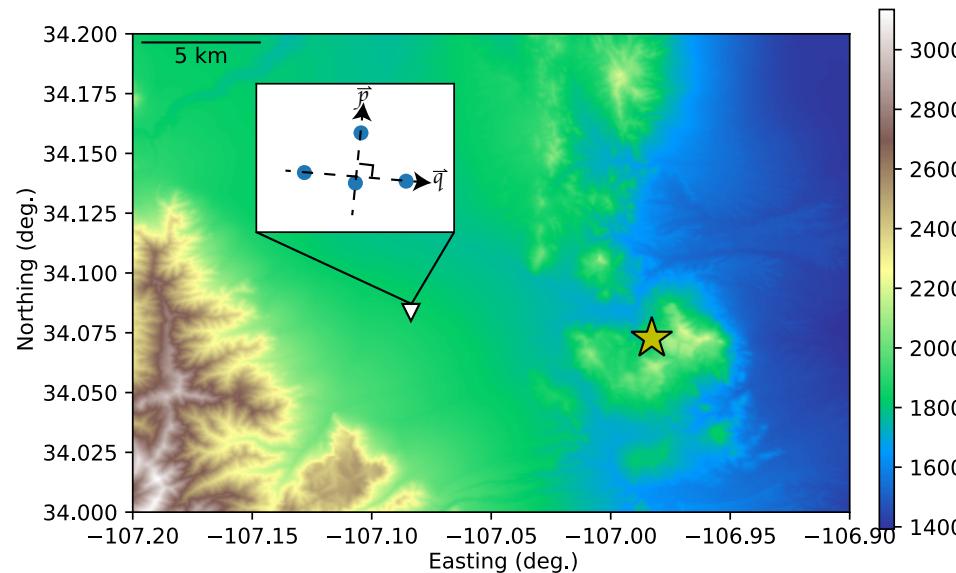
Mixed signal vector

Vector of source signals

Weight vectors describing how signals are mixed (a.k.a “mixing” matrix)

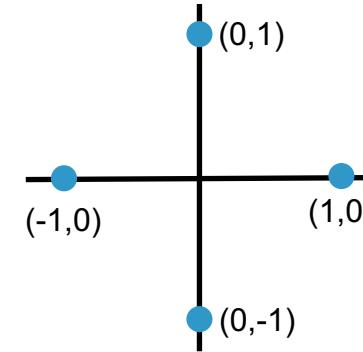
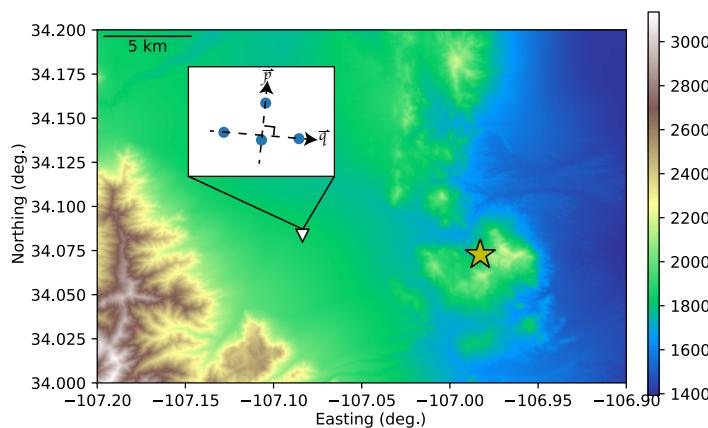
$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} = \begin{bmatrix} A_{11} & \cdots & A_{14} \\ \vdots & \ddots & \vdots \\ A_{41} & \cdots & A_{44} \end{bmatrix} \begin{bmatrix} s_1 \\ s_2 \\ s_3 \\ s_4 \end{bmatrix}$$

Gradient Flow ICA



- Closely-spaced array (10 m separation)
- Take spatial time derivatives of signal mixtures along position coordinates
 - Leads to backazimuth calculations
- Overcomplete ICA bases so we use symmetric quasi-decorrelation

Signal Backazimuth Calculation



- Spatial derivatives:

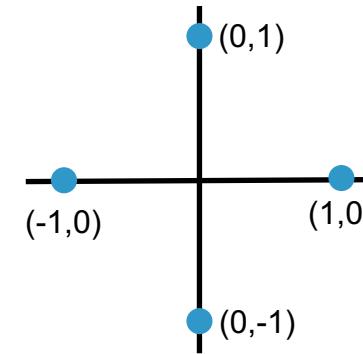
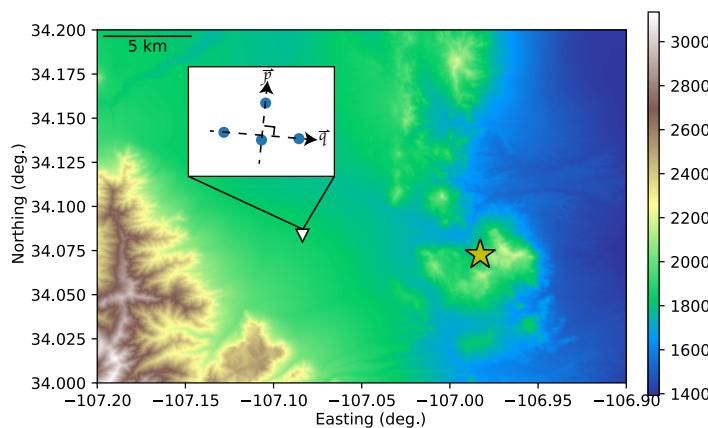
$$\xi_{00} \approx \frac{1}{4} (x_{-1,0} + x_{0,-1} + x_{0,1})$$

$$\xi_{10} \approx \frac{1}{2} (x_{1,0} - x_{-1,0})$$

$$\xi_{01} \approx \frac{1}{2} (x_{0,1} - x_{0,-1})$$

- Forms x in the equation, $\vec{x} = A\vec{s}$

Signal Backazimuth Calculation



- Use inter-station time differences between sensors:

$$\tau_1^\ell = \frac{1}{c} \vec{q} \cdot \vec{u}_x^\ell$$

$$\tau_2^\ell = \frac{1}{c} \vec{p} \cdot \vec{u}_y^\ell$$

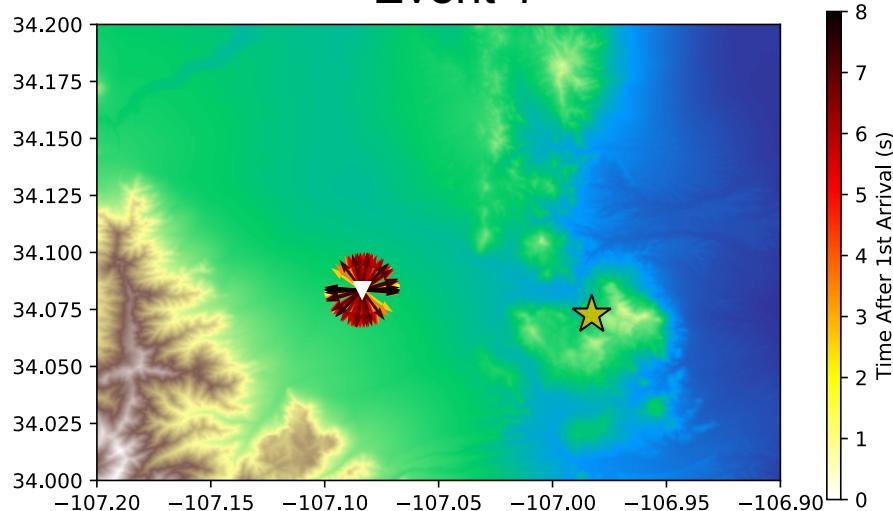
$$\tan^{-1} \frac{\vec{u}_x^\ell}{\vec{u}_y^\ell} = \theta$$

Direction vectors
for source ℓ

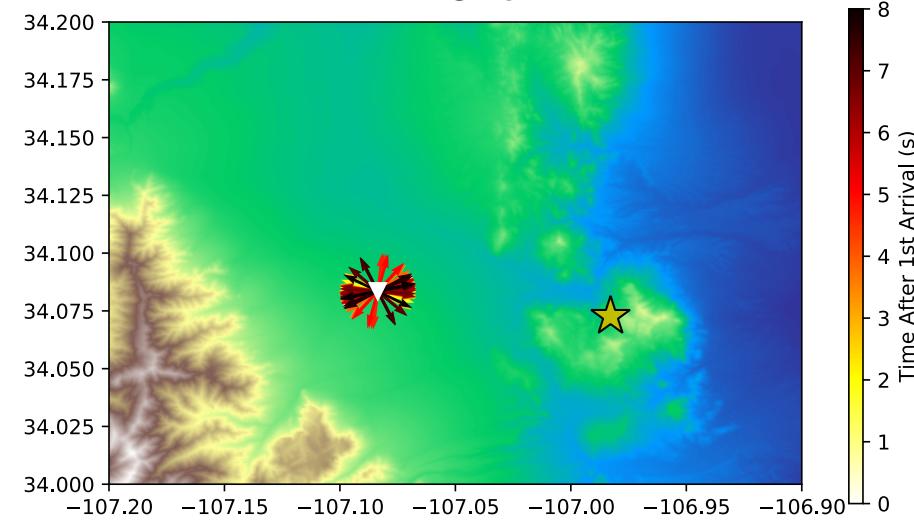
Signal backazimuth

Results (0 – 30 s after direct arrival)

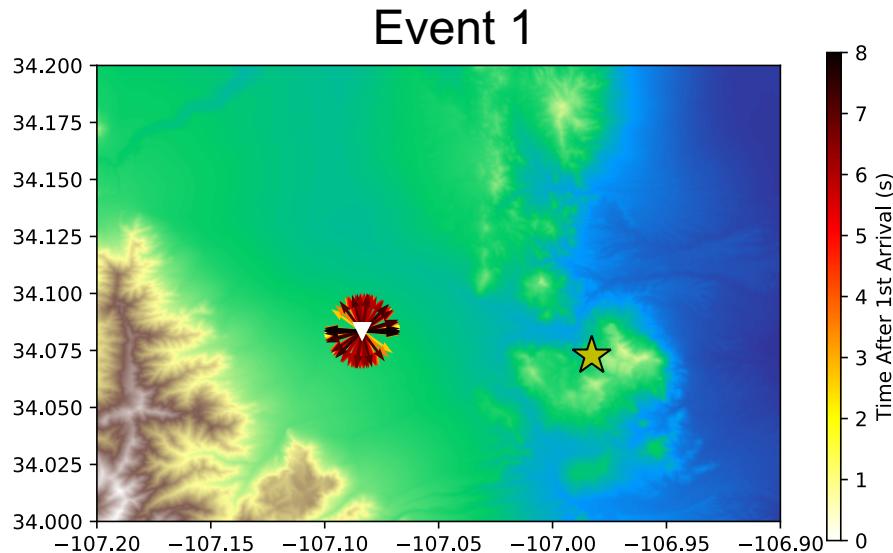
Event 1



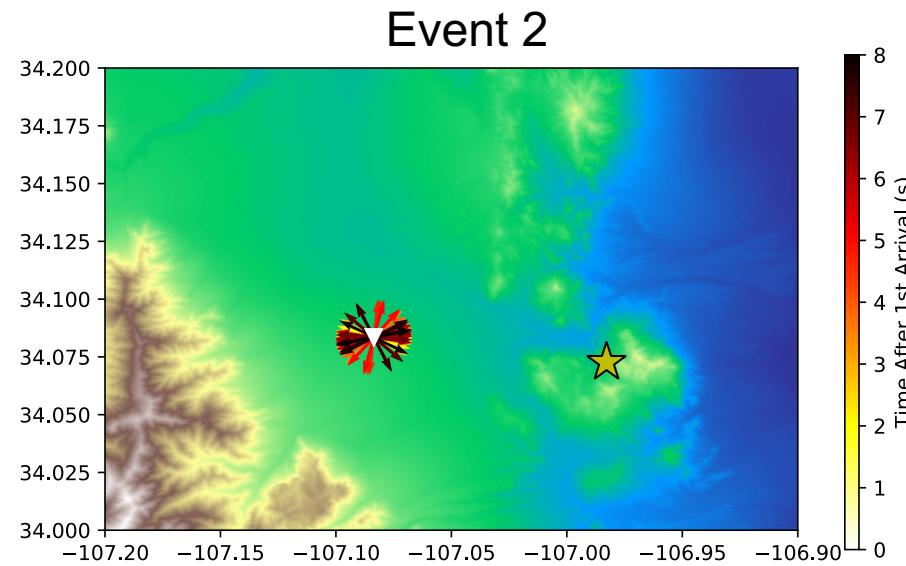
Event 2



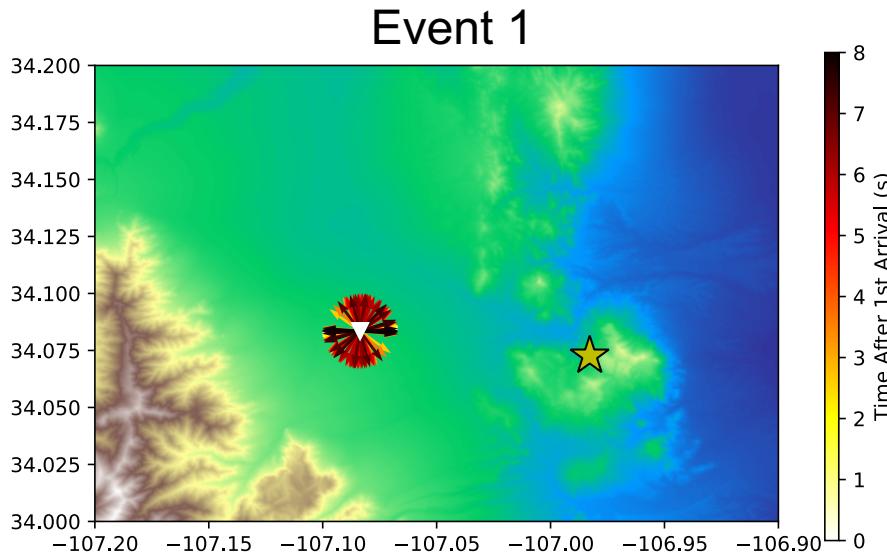
Results (0 – 30 s after direct arrival)



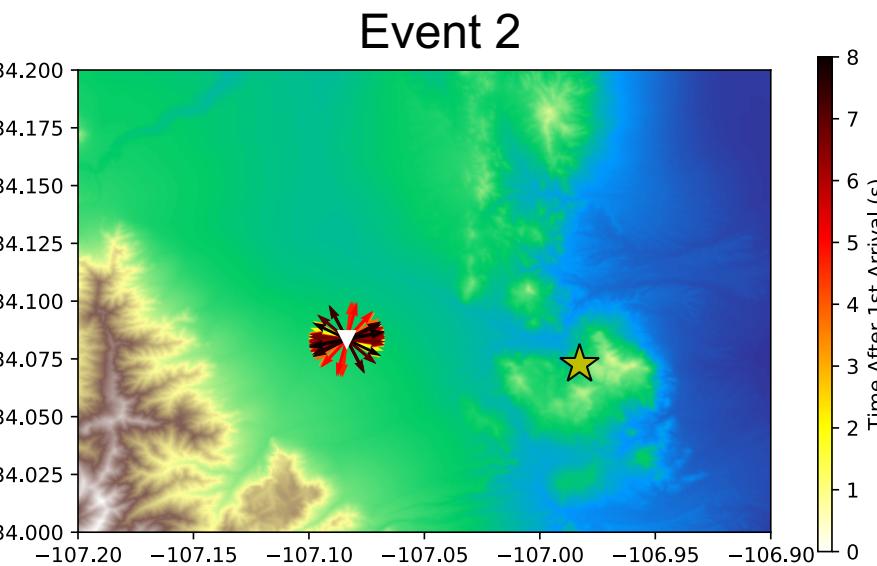
- Backazimuths point towards surrounding mountains
- Correct direct arrival backazimuth



Results (0 – 30 s after direct arrival)



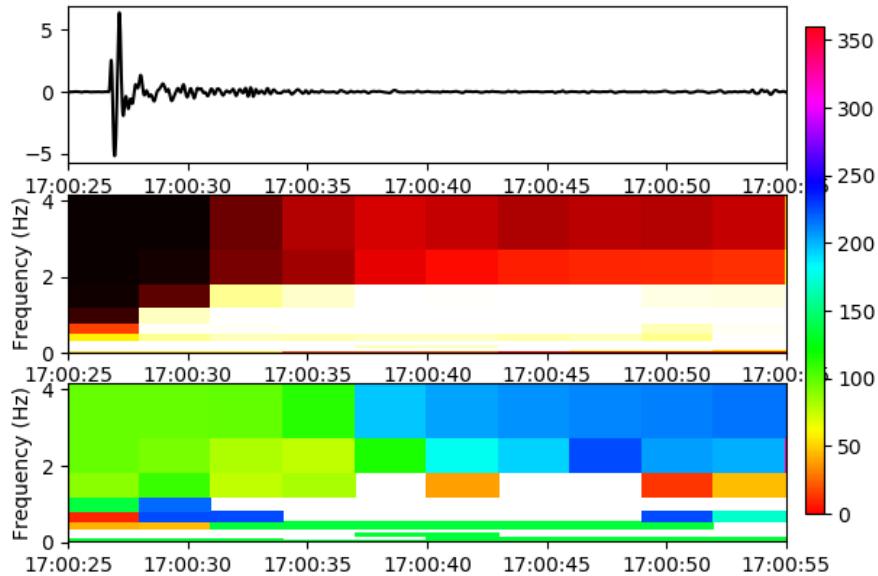
- Backazimuths point towards surrounding mountains
- Correct direct arrival backazimuth



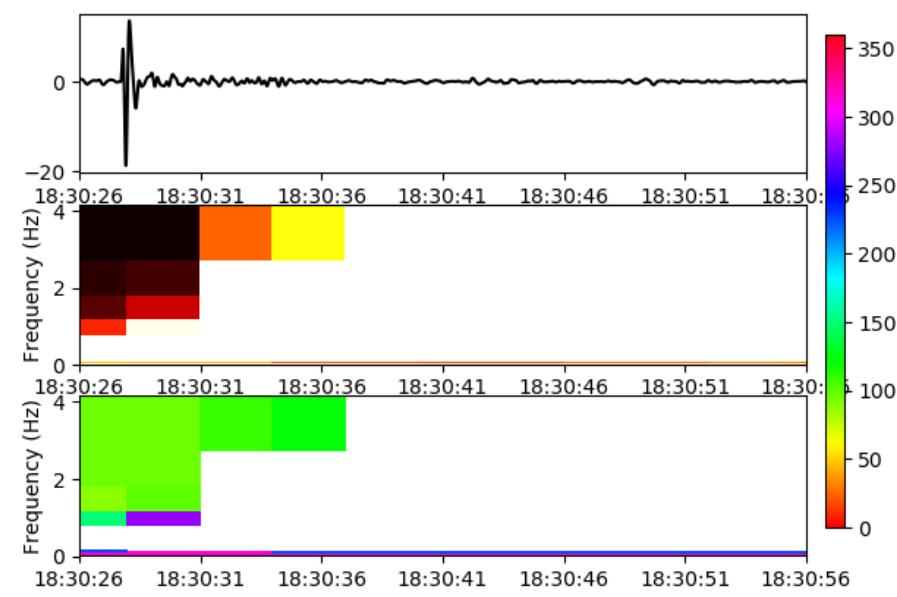
- Backazimuths point towards surrounding mountains, but shifted
- Generally correct direct arrival backazimuth

PMCC Comparison

Event 1



Event 2

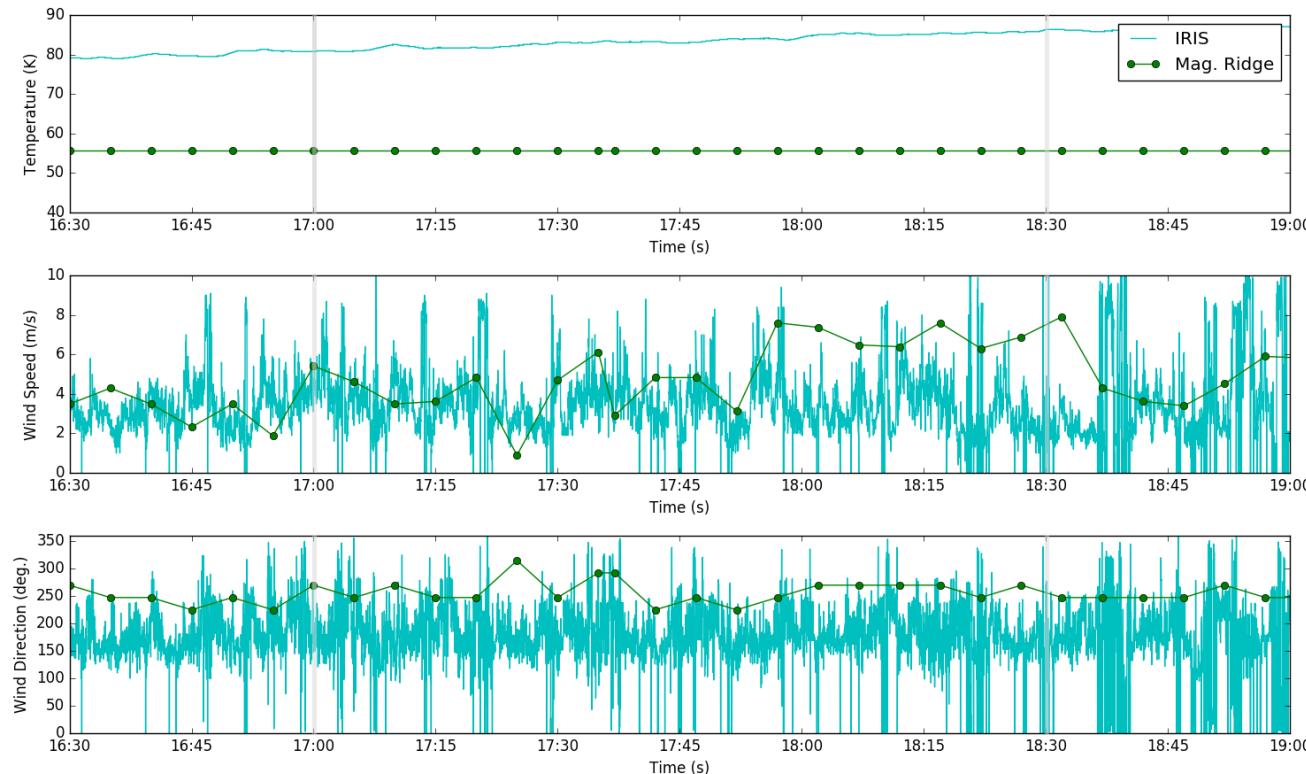


Conclusions

Strengths	Limitations
<ul style="list-style-type: none">■ Correctly identifies backazimuths from the direct arrival and scattered signals■ Only requires one explosion and four microphones■ Outperforms traditional methods in scattered signal identification	<ul style="list-style-type: none">■ Effectiveness with time decreases due to attenuation (30 s in our case)■ Must be done in an area with close, complex, topography (or other scatterers)■ Backazimuths are aliased, require analyst input

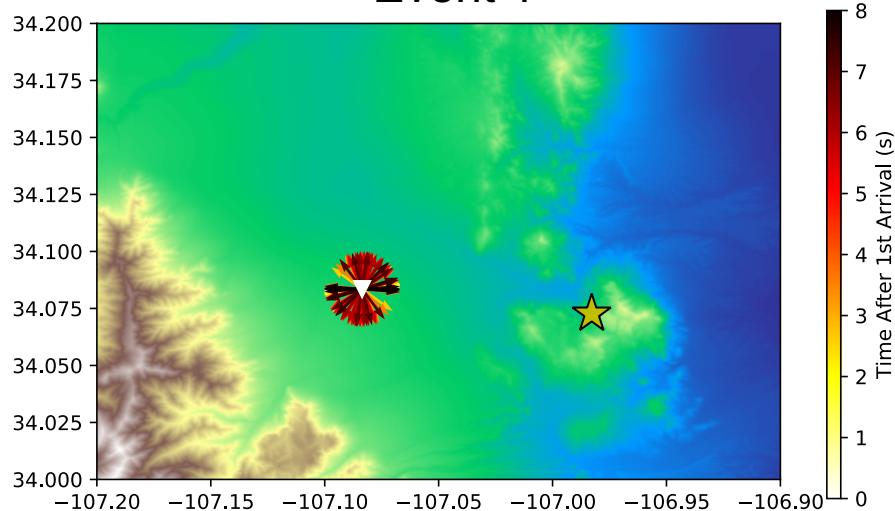
Future Work

- Publication in GRL or GJI
- Use this method with a larger array (50-100 sensors)
- Incorporate weather to explain “shifted” backazimuths during Event 2



Thank You

Event 1



Event 2

