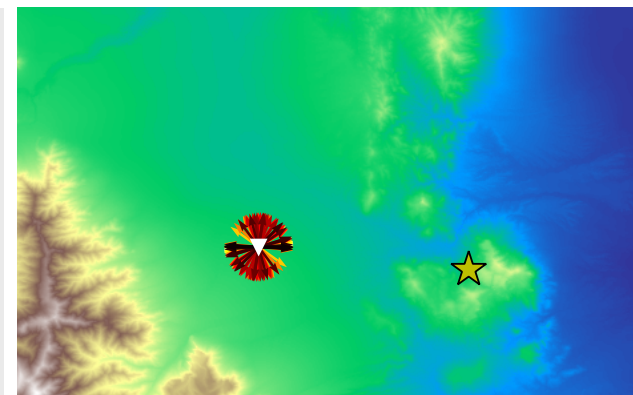
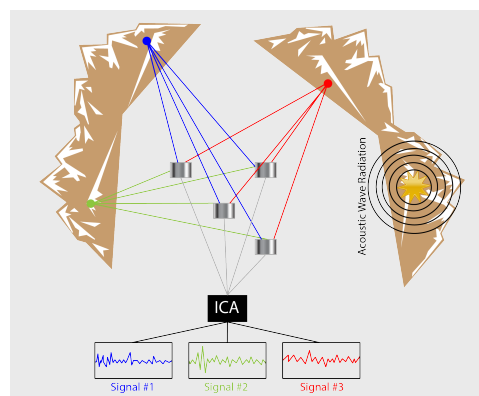
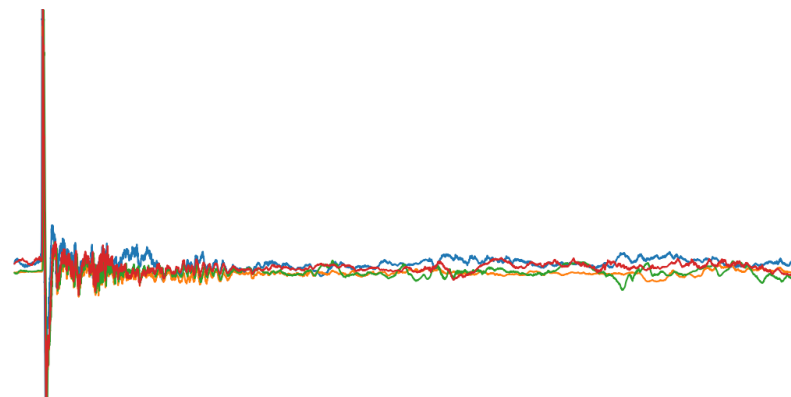


Exceptional service in the national interest



Tracking Scattered Signals in the Acoustic Coda Using Independent Component Analysis

Sarah Albert, Daniel Bowman

Motivation

- Acoustic waves travel various paths from source to sensor
 - Direct arrival
 - Arrivals from reflections off scatterers
- Each interaction with a scatterer alters the shape of the acoustic coda
 - Consider each interaction statistically independent
 - Can use Independent Component Analysis (ICA) to separate signals
- Implications for a variety of studies
 - Volcano infrasound
 - Waveform inversion
 - Yield estimation

Independent Component Analysis

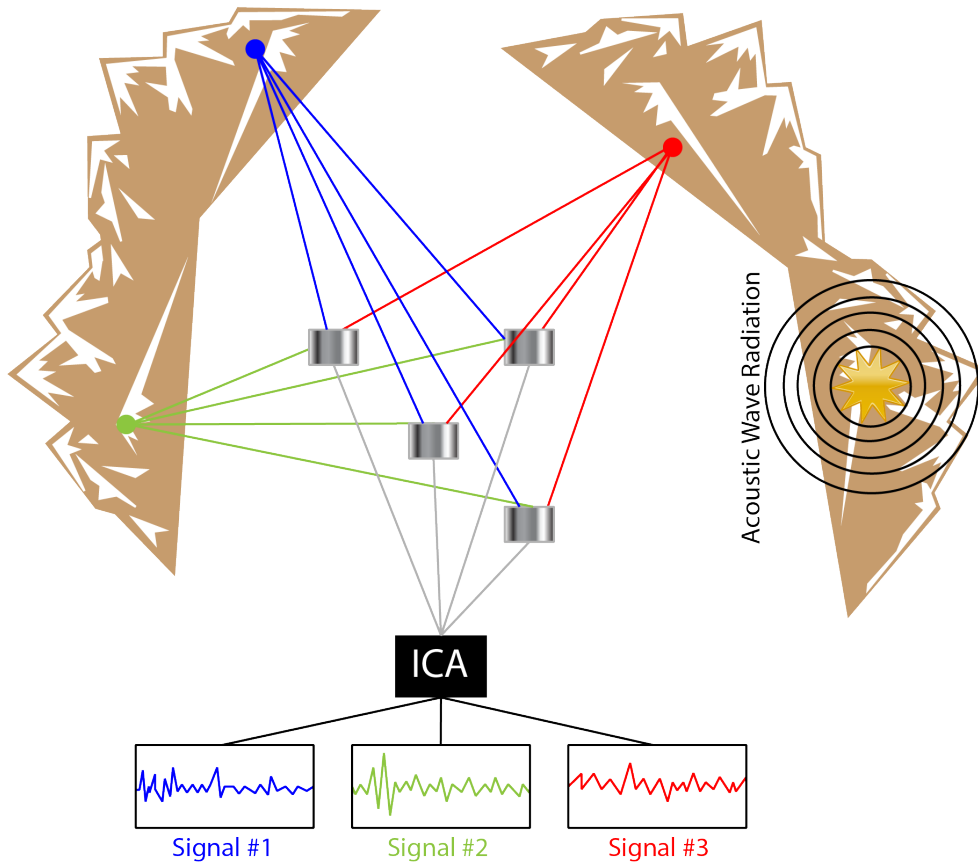


Image not to scale.

Independent Component Analysis

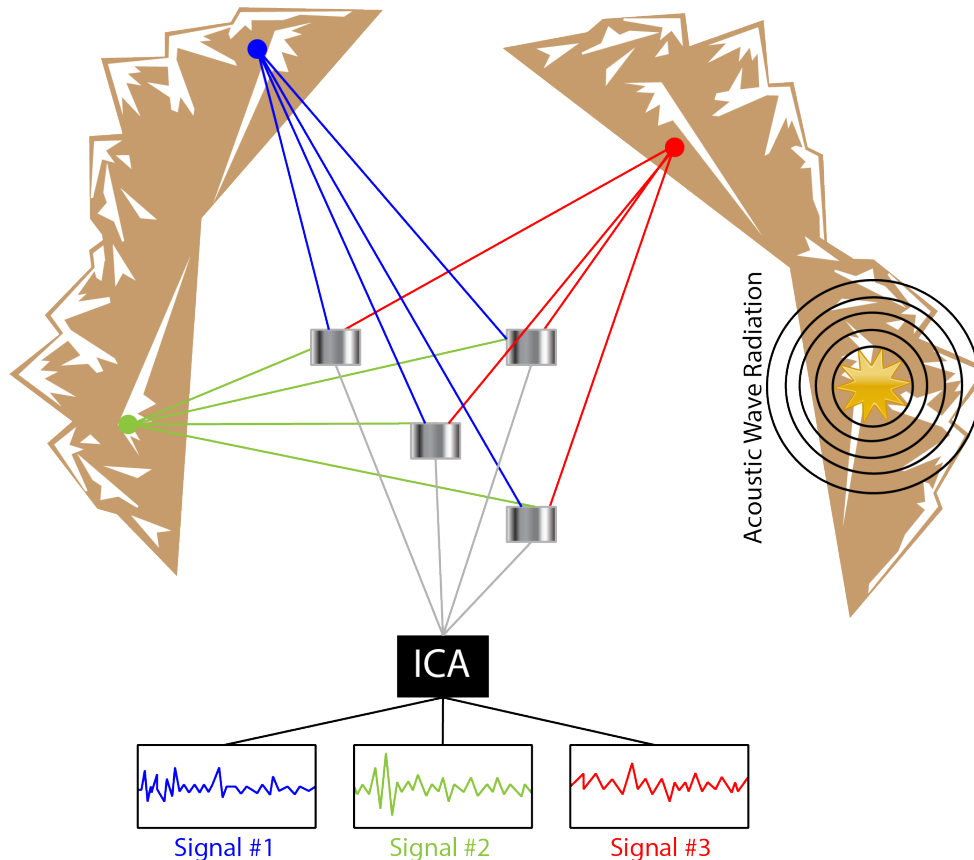


Image not to scale.

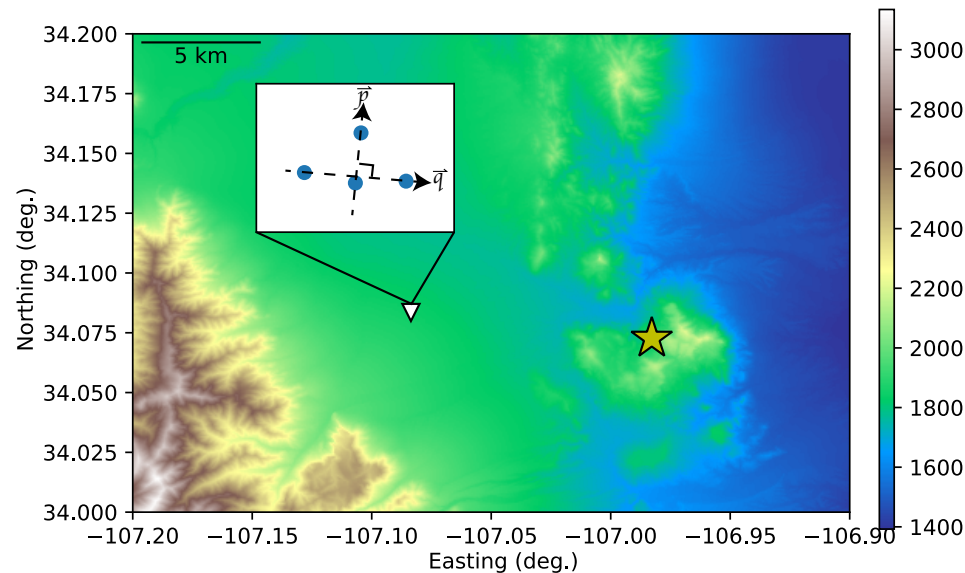
Mixed signal vector

Vector of source signals

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} = \begin{bmatrix} A_{11} & \cdots & A_{14} \\ \vdots & \ddots & \vdots \\ A_{41} & \cdots & A_{44} \end{bmatrix} \begin{bmatrix} s_1 \\ s_2 \\ s_3 \\ s_4 \end{bmatrix}$$

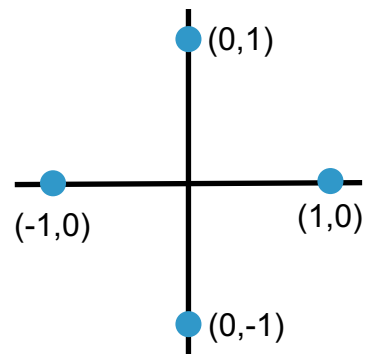
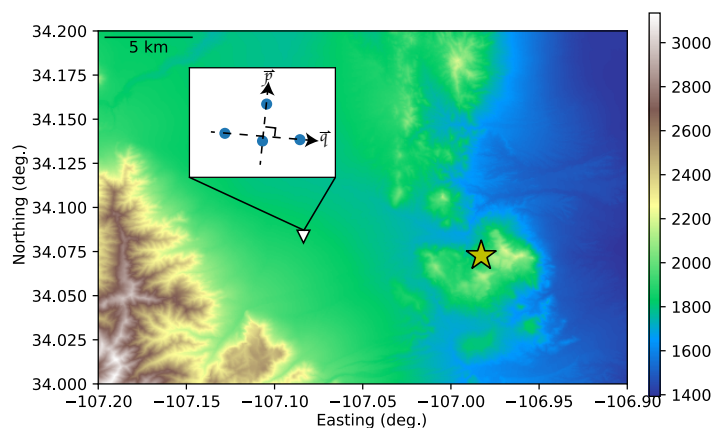
Weight vectors describing how signals are mixed (a.k.a "mixing" matrix)

Gradient Flow ICA



- Closely-spaced array (10 m separation)
- Take spatial time derivatives of signal mixtures along position coordinates
 - Leads to backazimuth calculations
- Overcomplete ICA bases so we use symmetric quasi-decorrelation

Signal Backazimuth Calculation



- Spatial derivatives:

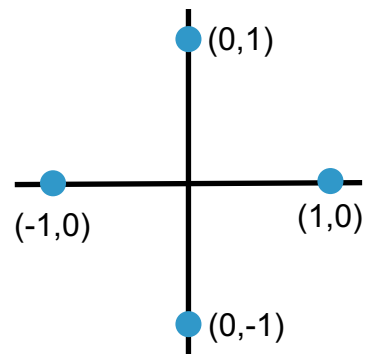
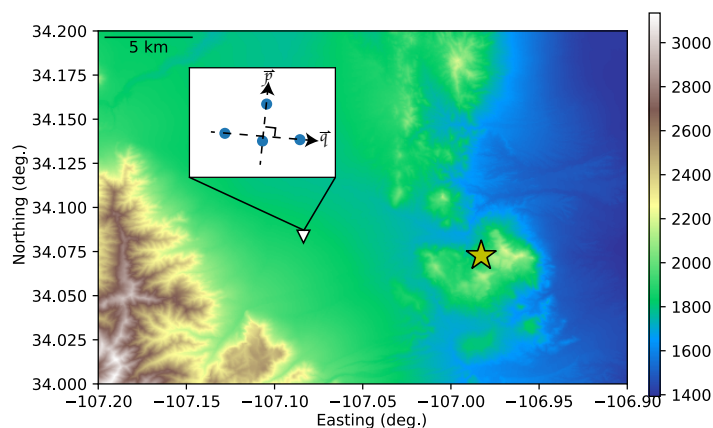
$$\xi_{00} \approx \frac{1}{4}(x_{-1,0} + x_{0,-1} + x_{0,1})$$

$$\xi_{10} \approx \frac{1}{2}(x_{1,0} - x_{-1,0})$$

$$\xi_{01} \approx \frac{1}{2}(x_{0,1} - x_{0,-1})$$

- Forms x in the equation, $\vec{x} = A\vec{s}$

Signal Backazimuth Calculation



- Use inter-station time differences between sensors:

$$\tau_1^\ell = \frac{1}{c} \vec{q} \cdot \vec{u}_x^\ell$$

$$\tau_2^\ell = \frac{1}{c} \vec{p} \cdot \vec{u}_y^\ell$$

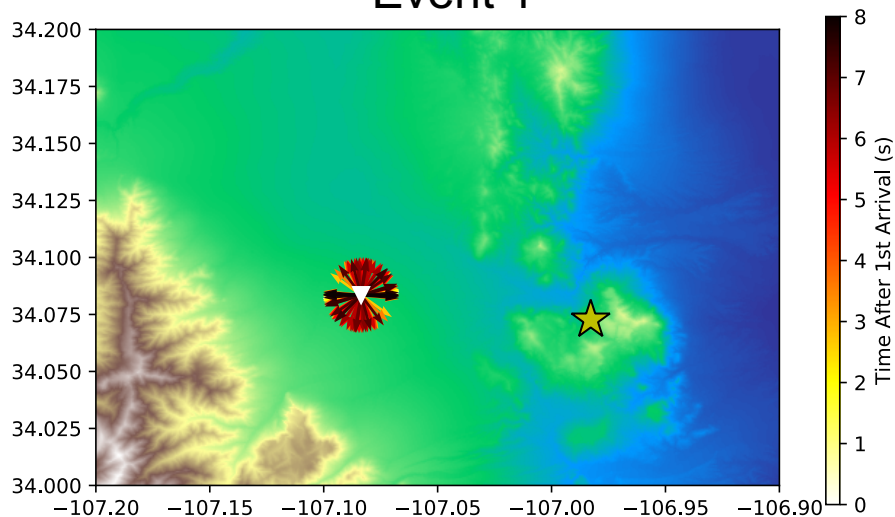
$$\tan^{-1} \frac{\vec{u}_x^\ell}{\vec{u}_y^\ell} = \theta$$

Direction vectors
for source ℓ

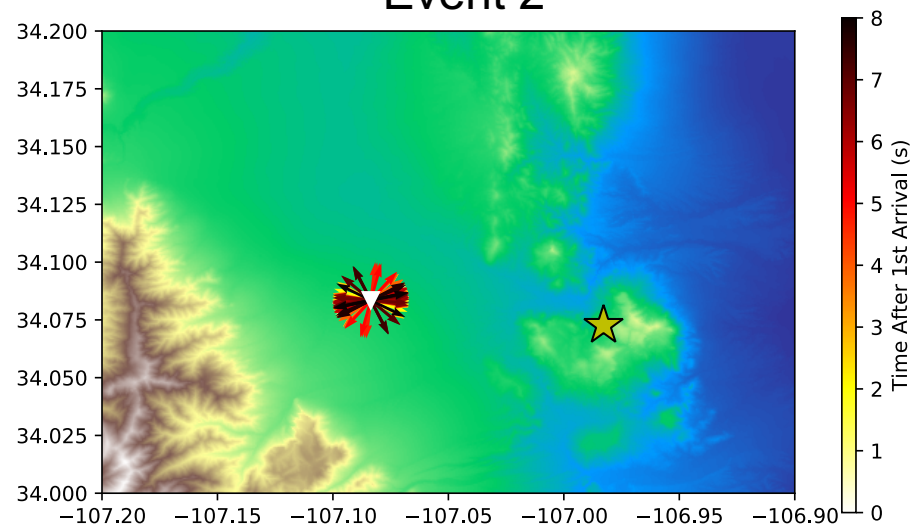
Signal backazimuth

Results (0 – 30 s after direct arrival)

Event 1

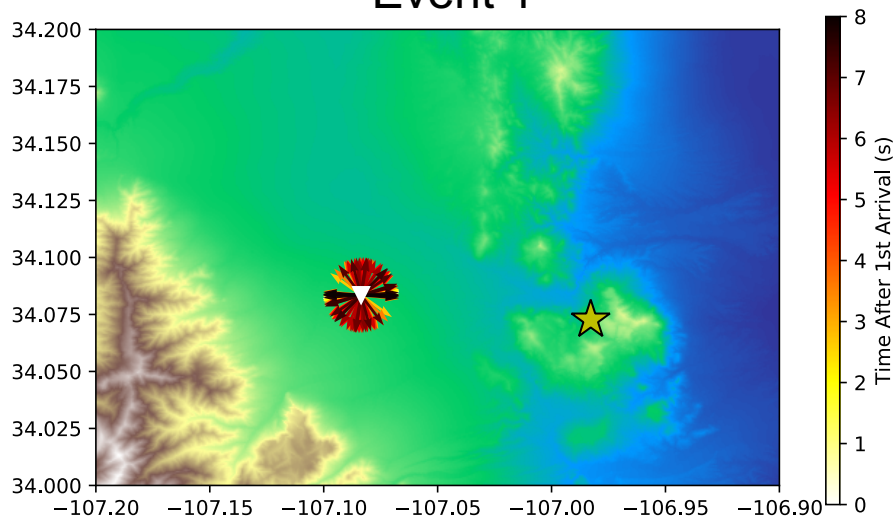


Event 2



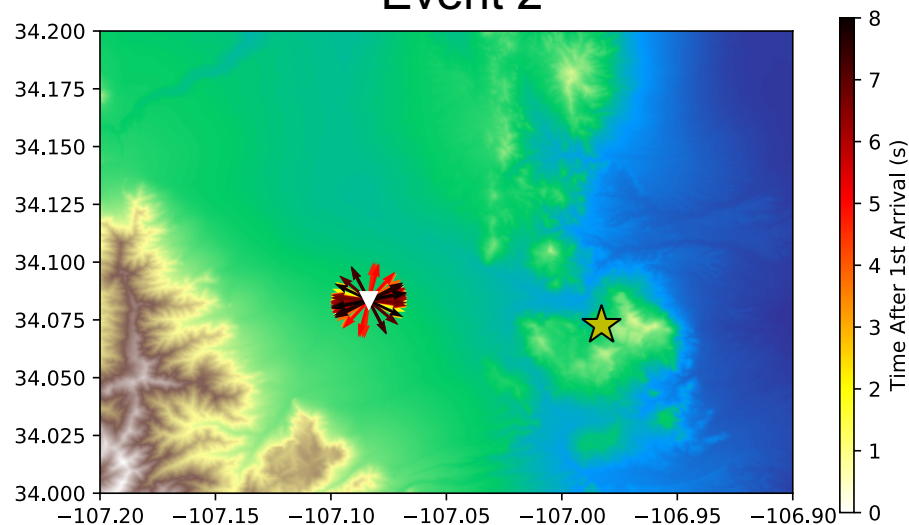
Results (0 – 30 s after direct arrival)

Event 1



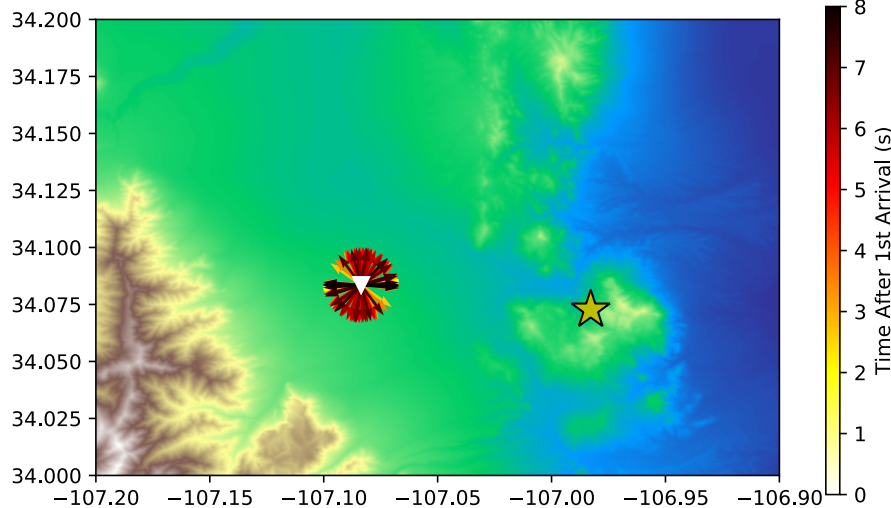
- Backazimuths point towards surrounding mountains
- Correct direct arrival backazimuth

Event 2



Results (0 – 30 s after direct arrival)

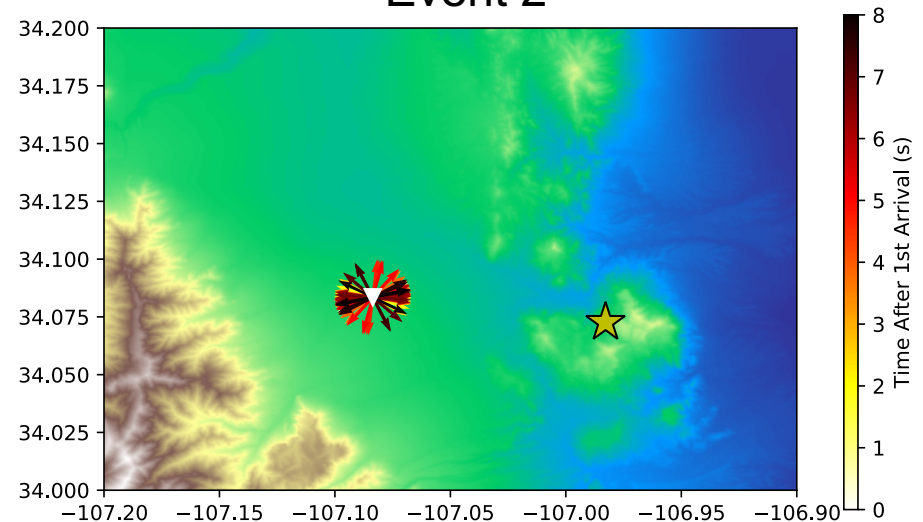
Event 1



- Backazimuths point towards surrounding mountains
- Correct direct arrival backazimuth

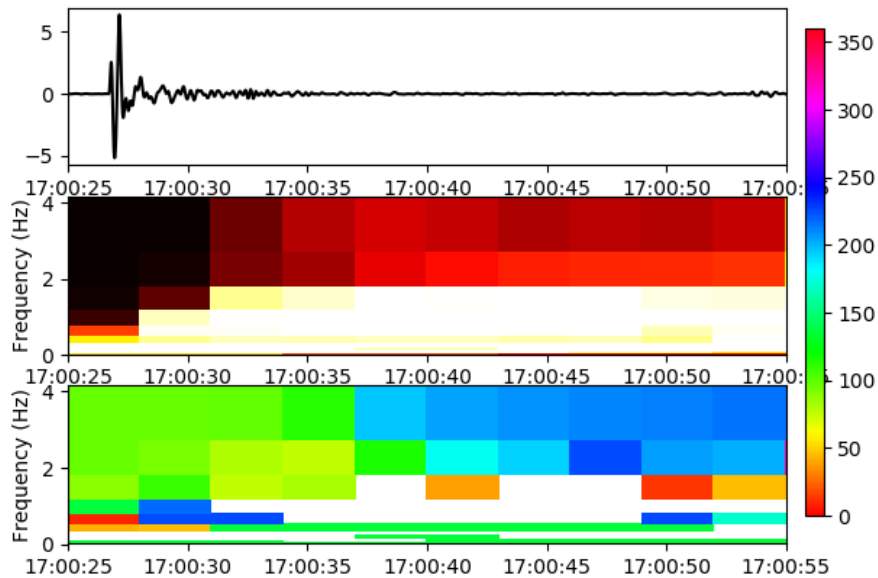
- Backazimuths point towards surrounding mountains, but shifted
- Generally correct direct arrival backazimuth

Event 2

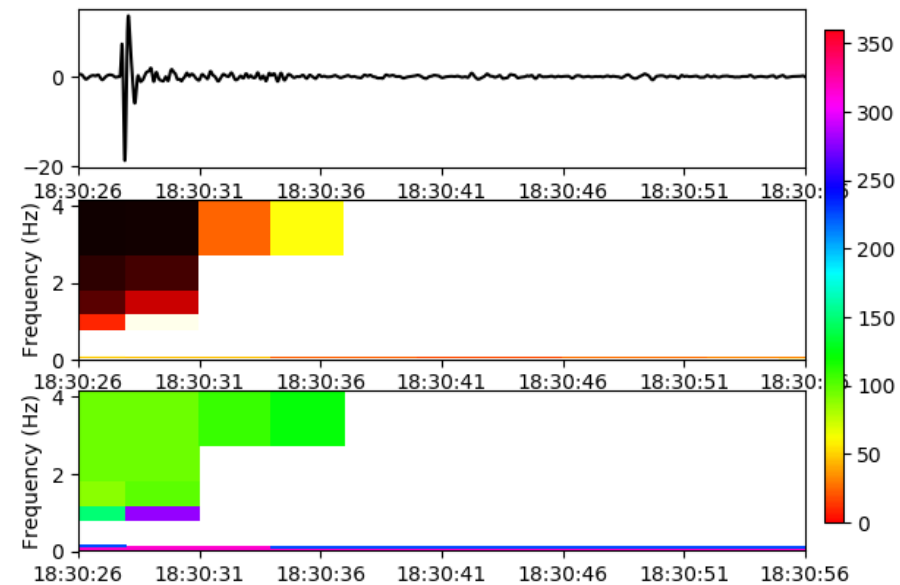


PMCC Comparison

Event 1



Event 2

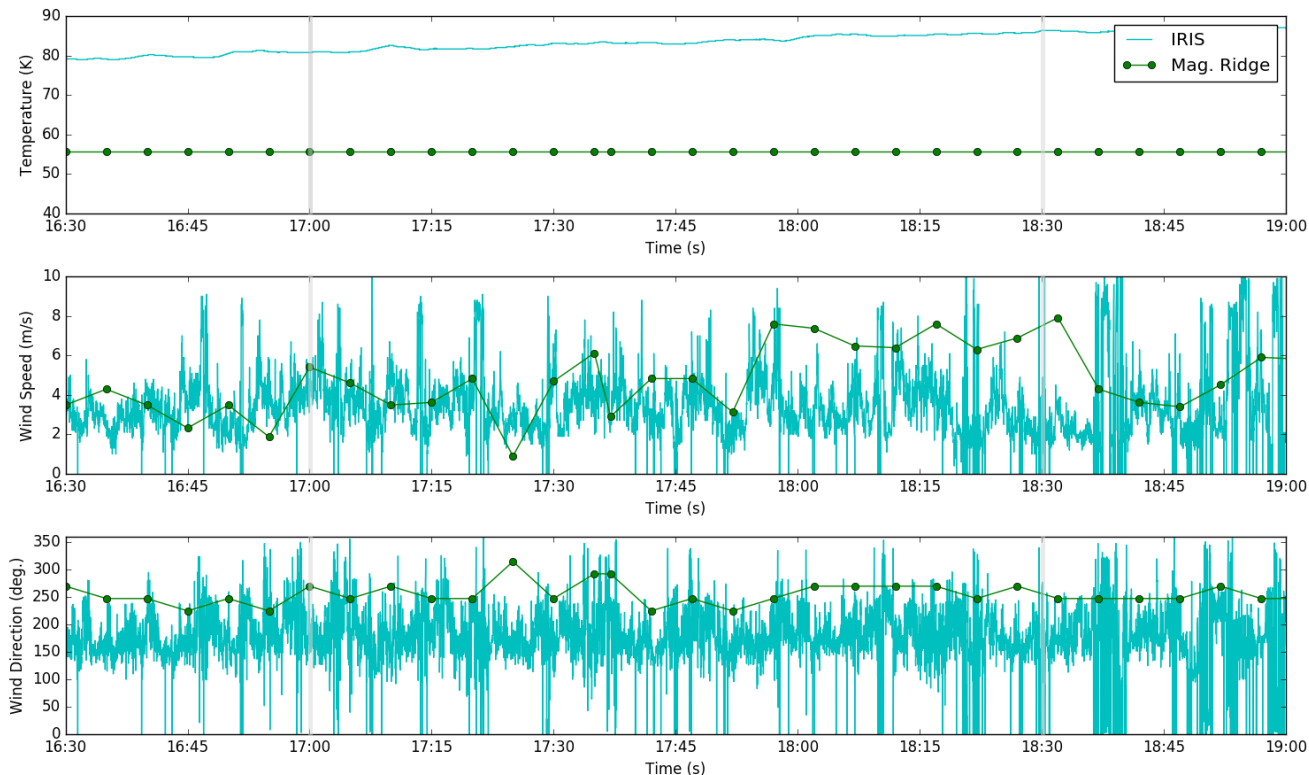


Conclusions

Strengths	Limitations
<ul style="list-style-type: none">■ Correctly identifies backazimuths from the direct arrival and scattered signals■ Only requires one explosion and four microphones■ Outperforms traditional methods in scattered signal identification	<ul style="list-style-type: none">■ Effectiveness with time decreases due to attenuation (30 s in our case)■ Must be done in an area with close, complex, topography (or other scatterers)■ Backazimuths are aliased, require analyst input

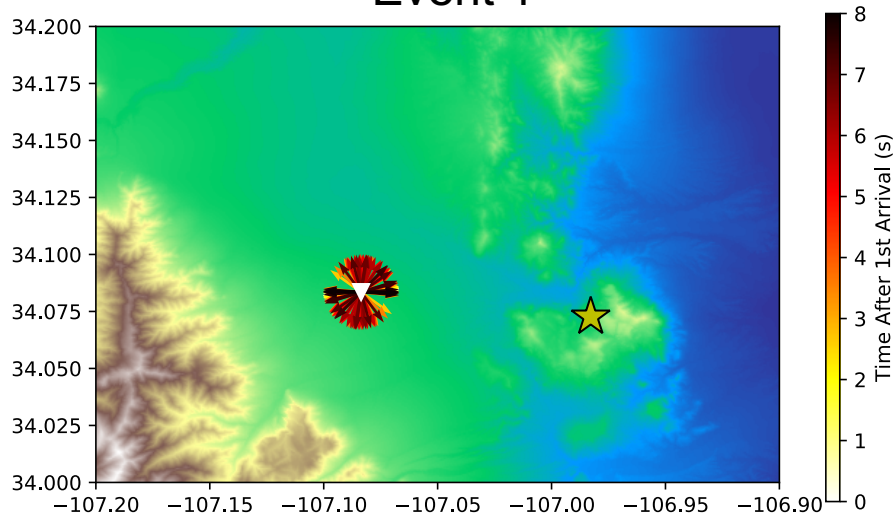
Future Work

- Publication in GRL or GJI
- Use this method with a larger array (50-100 sensors)
- Incorporate weather to explain “shifted” backazimuths during Event 2



Thank You

Event 1



Event 2

