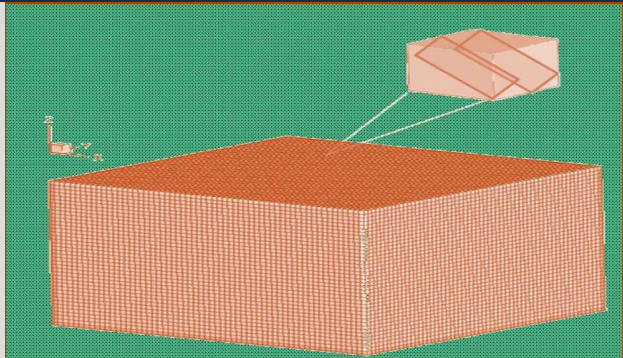
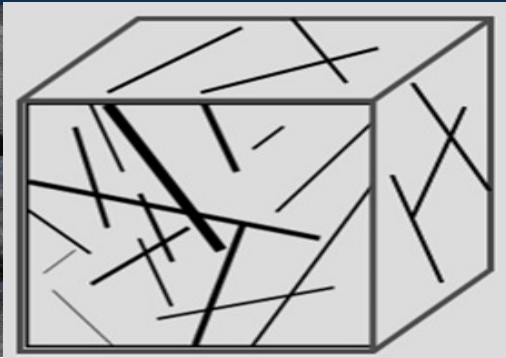




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# NUMERICAL MODELING OF FLOW AND TRANSPORT IN FRACTURED CRYSTALLINE ROCK

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# Disposal Concept for Crystalline Repository

- Crystalline rocks are common in many stable continental regions
- Low permeability matrix rock and sparse fracture system
- Geochemically reducing conditions
- Rock characteristics favorable for repository construction

# Fracture Characterization Methods

- A realistic representation of fractures in granite rock is needed
- Discrete Fracture Network and Equivalent Continuum Methods used
- The Fractured Continuum Model (FCM) used in this study
- FCM based on discrete fracture and effective continuum approaches (McKenna and Reeves, 2005, Kalinina et al. 2012, and Hadgu et al. 2016)

# Flow and Transport Simulations

- Test case simulations of flow and transport in crystalline rock
- Relevant fracture data used
- Specified simulation domain and grid discretization
- FCM used to generate permeability and porosity of selected number of realizations
- Effective permeability and breakthrough curves evaluated
- PFLOTRAN (Lichtner et al., 2015) massively parallel subsurface flow and reactive transport code used in a high performance computing environment

# Test Case Fracture Parameters

Fracture statistics used for test case:

Fracture Set	Mean trend (degrees)	Mean plunge (degrees)	$\kappa$	$\alpha$	$R_u$ (m)	$R_0$ (m)	Number of fractures
North-South Vertical	90	0	22	2.5	500	15	2,100
East-West Vertical	0	0	22	2.7	500	15	2,000
West-East Horizontal	360	90	10	2.4	500	15	2,300

Fracture radius R follows a truncated power law distribution:

$$R = R_0 \cdot \left[ 1 - u + u \cdot \left( \frac{R_0}{R_u} \right)^\alpha \right]^{-1/\alpha}$$

Fracture orientation  $\Theta$  follows Fisher distribution:

$$f(\theta) = \frac{\kappa \cdot \sin \theta \cdot e^{\kappa \cdot \cos \theta}}{e^\kappa - e^{-\kappa}}$$

$\alpha$  = scaling factor,  $R_0$  = radius lower limit,  $R_u$  = radius upper limit,  $\kappa$  = concentration parameter

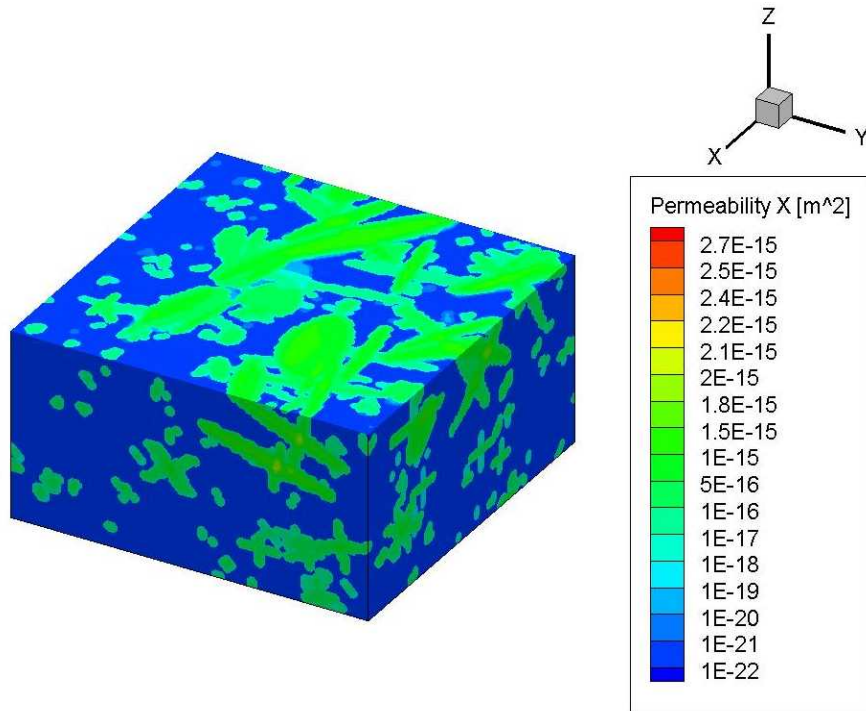
# Simulation Model Setup

- Domain: 1000 m x 1000 m x 1000 m
  - Grid block size: 10 m x 10 m x 10 m
  - Number of grid blocks: 1,000,000
- Porosity: Anisotropic
- Permeability: Anisotropic
- Initial Conditions: Hydrostatic pressure
- Isothermal Conditions ( $T = 25\text{ }^{\circ}\text{C}$ )
- Boundary Conditions:
  - Pressure at West Face: 1.001 MPa
  - Pressure at East Face: 1.0 MPa

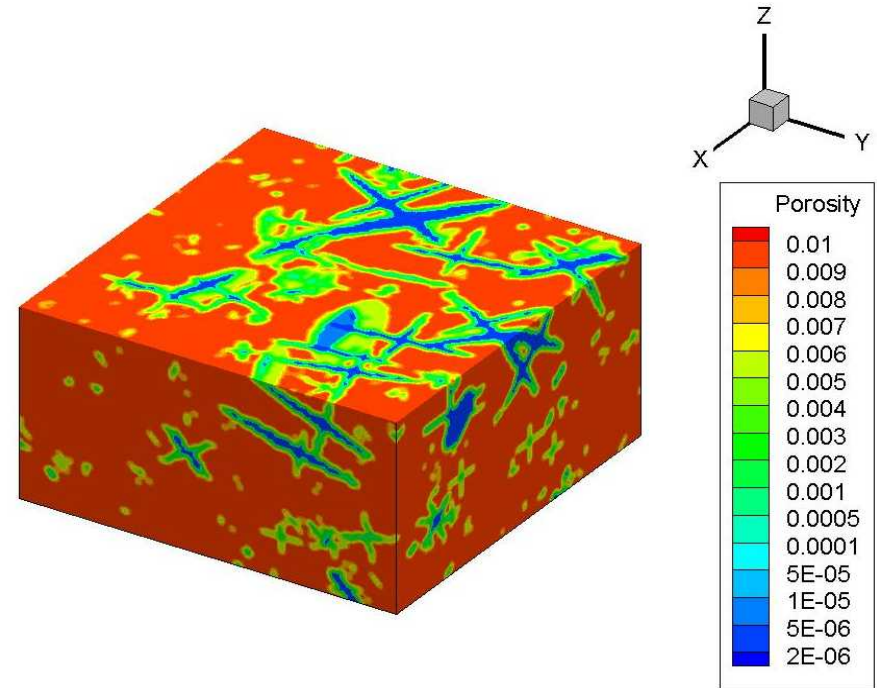
# Generation of Permeability and Porosity Fields Sandia National Laboratories

- Permeability and porosity fields generated using FCM with ELLIPSIM
- Specified fracture parameter distributions used in geostatistical representation of fractured domain
- Two sets of 25 realizations were selected
- Matrix rock permeability of  $10^{-22}$  m<sup>2</sup> used to suppress matrix flow
- Matrix rock porosity of 0.01 used

# Example Permeability and Porosity Fields



Permeability of a Realization



Porosity of a Realization

- Steady state flow utilized
  - to estimate effective permeability for each realization
  - To generate flow field for transport simulation
- Darcy's law and east face flux used to calculate effective permeability

$$q = \frac{-k_{eff} \Delta P}{\mu L}$$

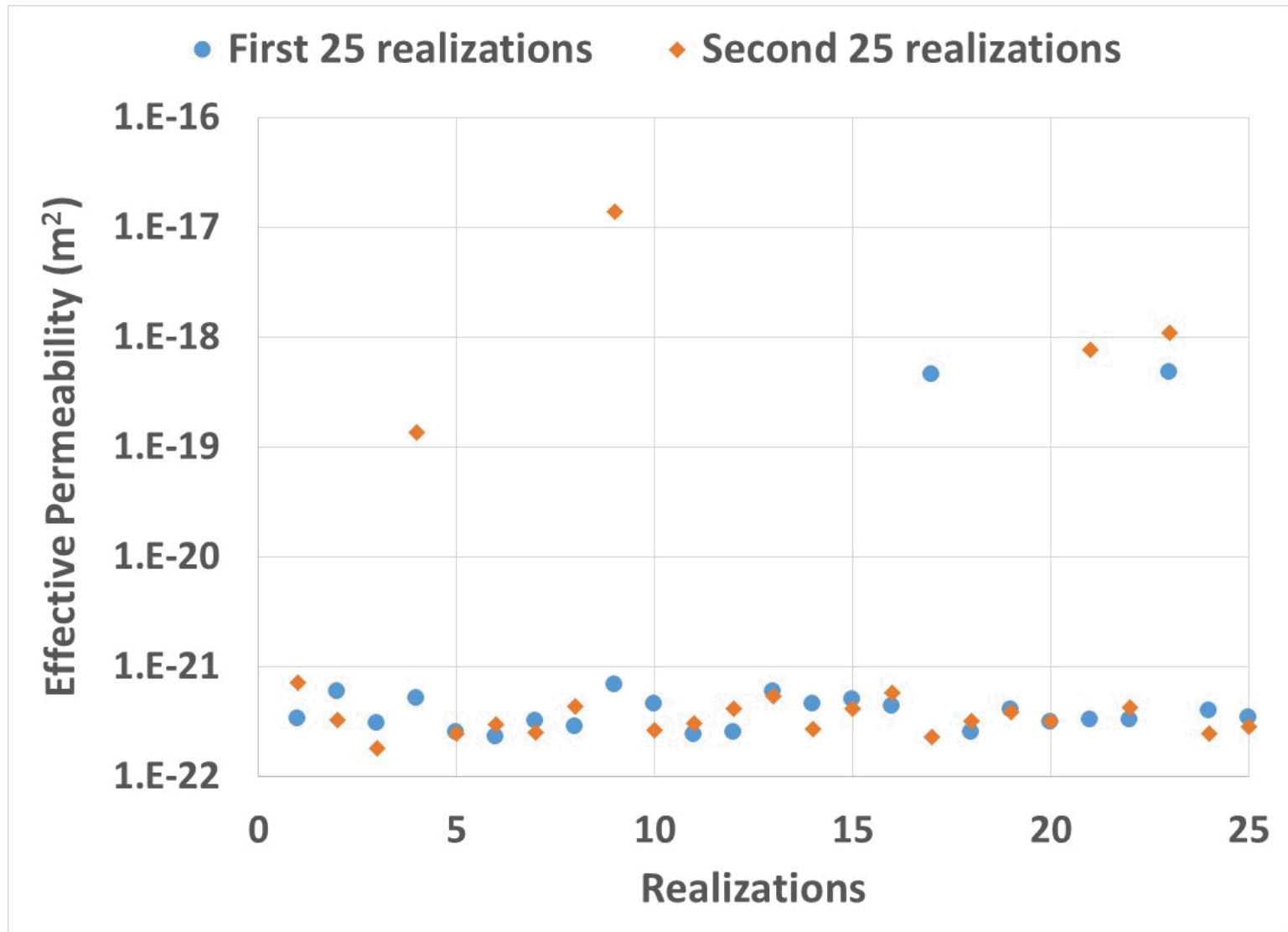
$q$  = flux,

$k_{eff}$  = effective permeability,

$\Delta P$  = pressure difference,  $\mu$  = dynamic viscosity

$L$  = distance between west and east faces

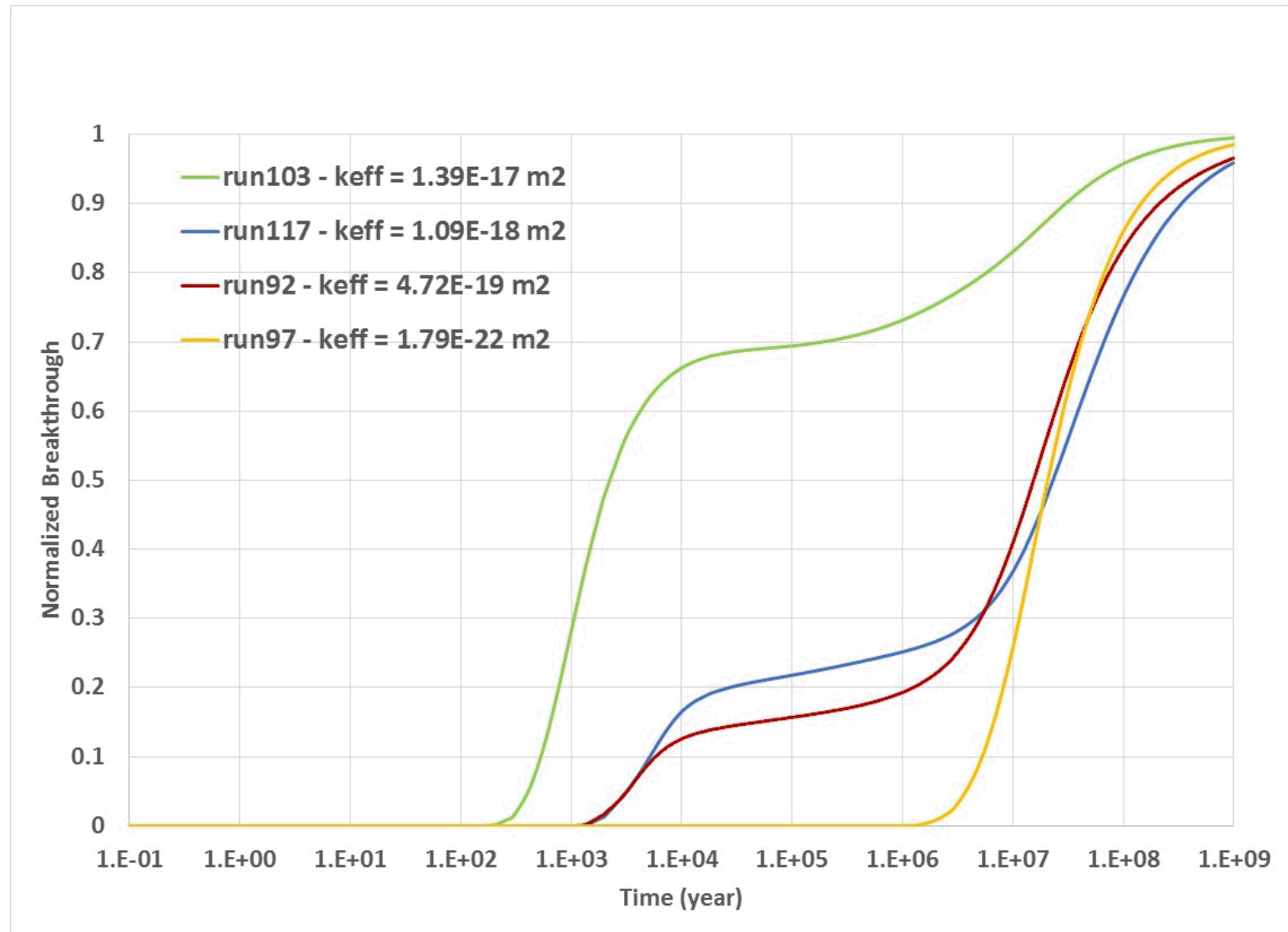
# Effective Permeability Evaluation



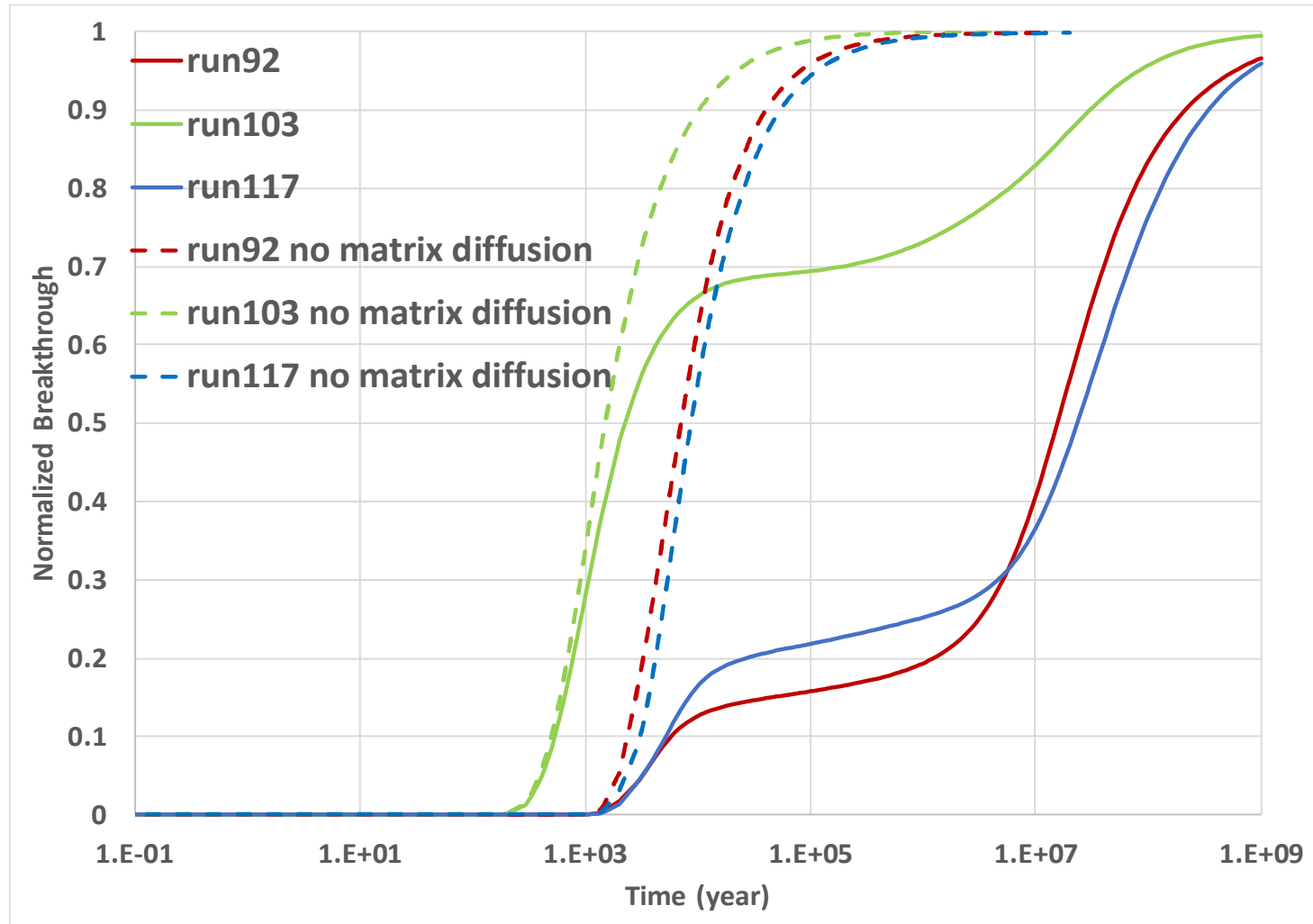
# Transport Simulations: Tracer Breakthrough Curves Evaluation:

- PFLOTRAN numerical simulator used (advection-diffusion)
- Porosity and steady state flow fields for each realization utilized as input to transport simulations
- Transport of dissolved, nonreactive tracer through domain
- Tracer transport simulated with and without matrix diffusion
- Output used to calculate normalized breakthrough curve for each realization

# Tracer Breakthrough Curves

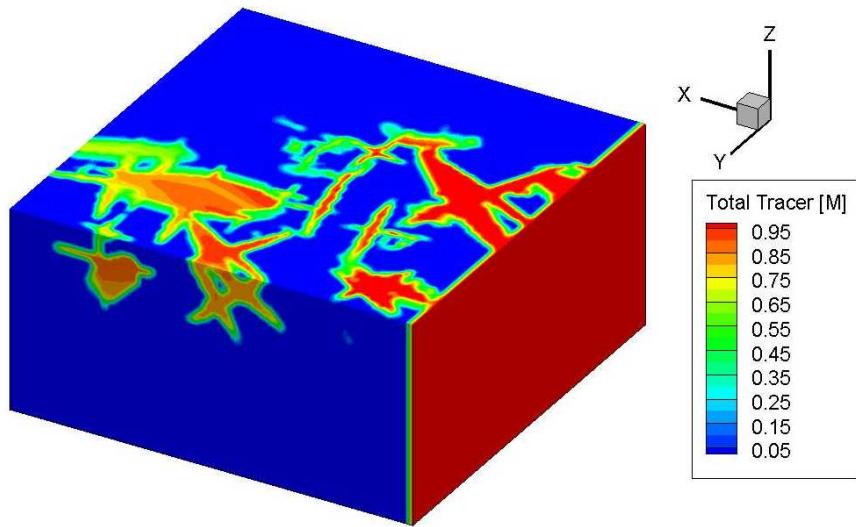


# Tracer Breakthrough Curves: Effect of Matrix Diffusion

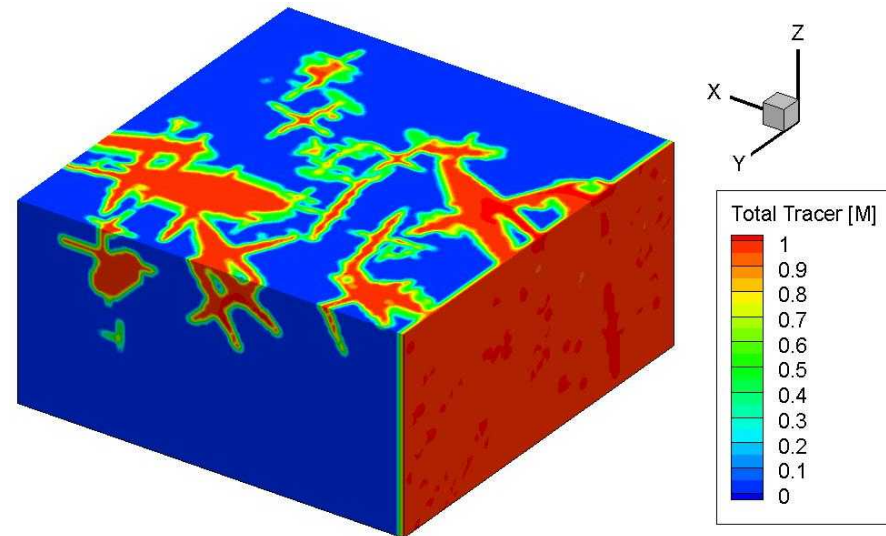


# Tracer Distributions: No Matrix Diffusion

- Matrix Diffusion Excluded
- FCM Tracer Transport Results (after  $1 \times 10^3$  and  $1 \times 10^5$  years simulation time)



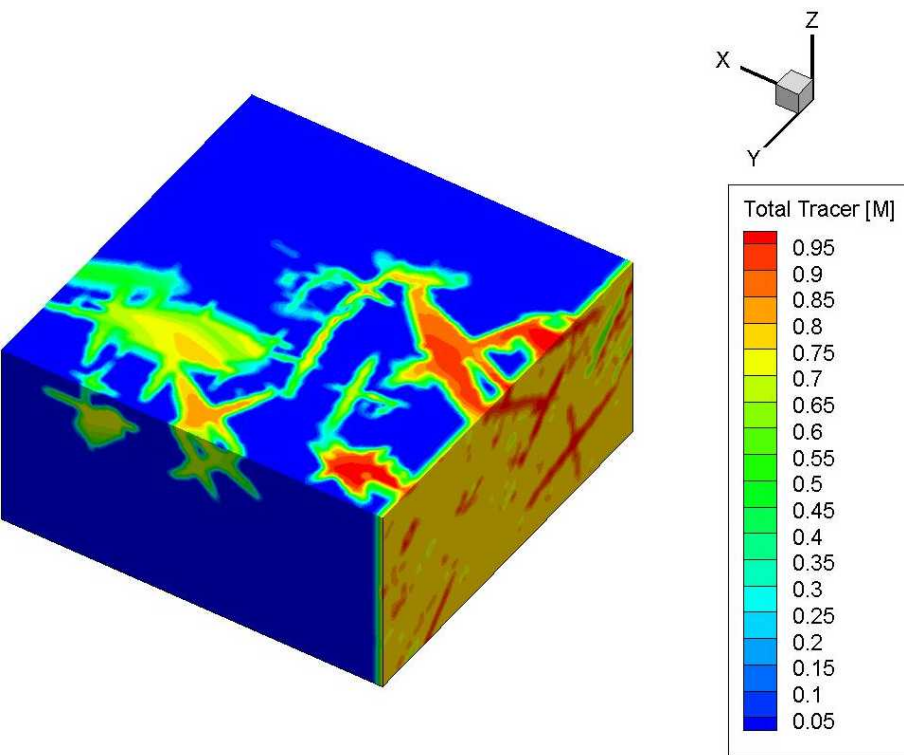
Tracer distributions after  $10^3$  years



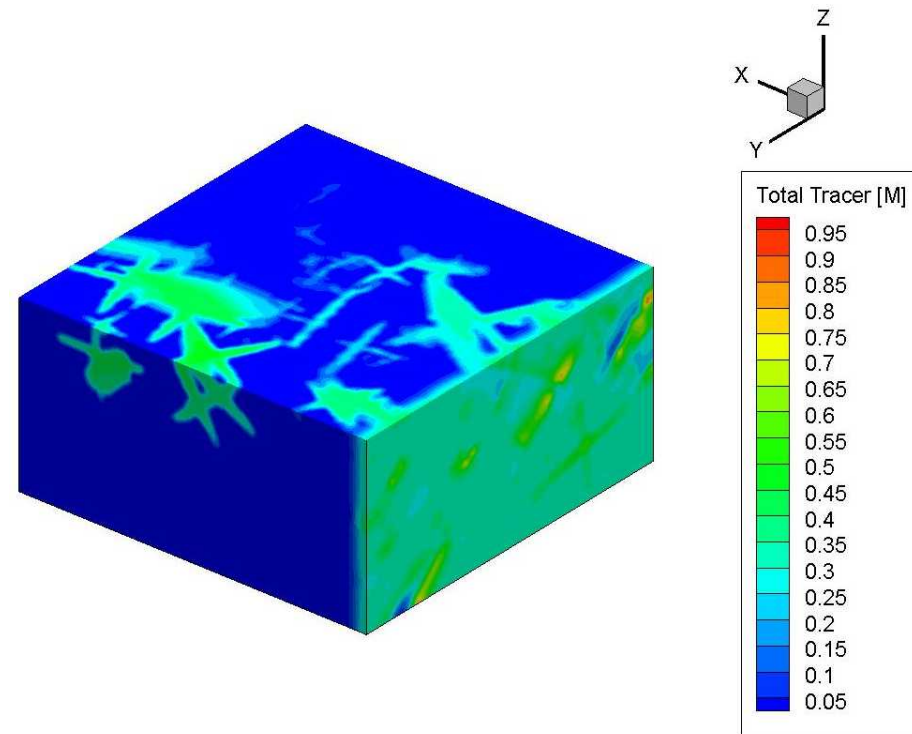
Tracer distributions after  $10^5$  years

# Tracer Distributions: With Matrix Diffusion

- Matrix Diffusion included
- FCM Tracer Transport Results (after  $1 \times 10^3$  and  $1 \times 10^5$  years simulation time)



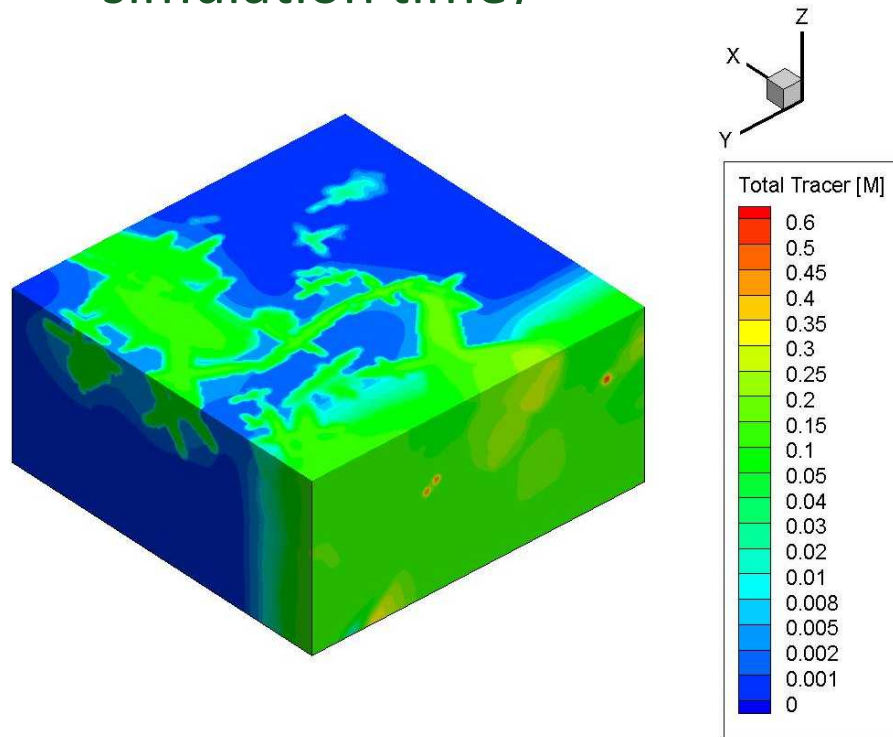
Tracer distributions after  $10^3$  years



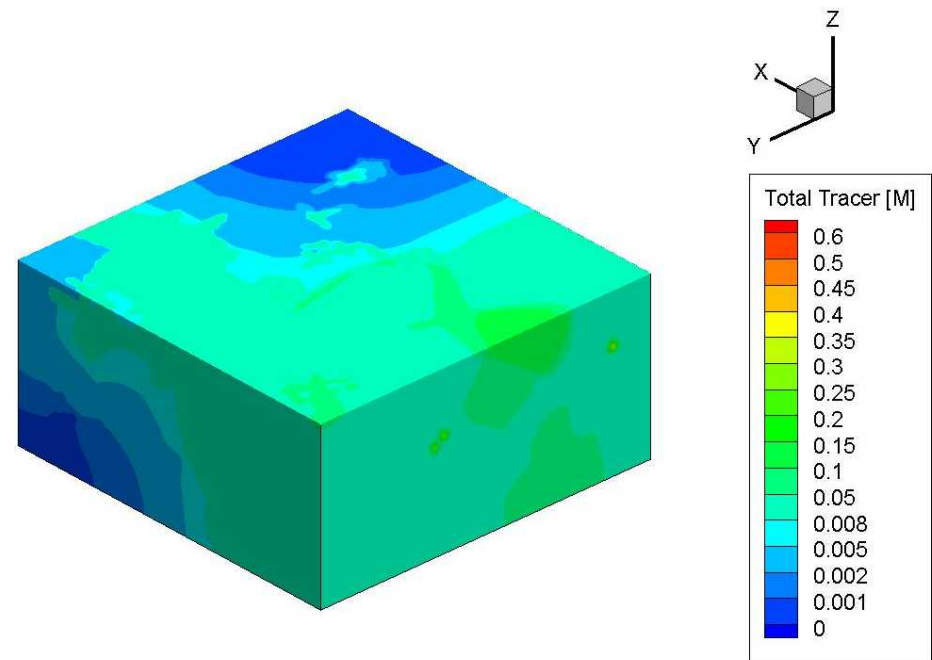
Tracer distributions after  $10^4$  years

# Tracer Distributions: With Matrix Diffusion, Contd.

- Matrix Diffusion included
- FCM Tracer Transport Results (after  $1 \times 10^5$  and  $1 \times 10^6$  years simulation time)



Tracer distributions after  $10^5$  years



Tracer distributions after  $10^6$  years

# Conclusions

- Flow and Transport simulations conducted using the FCM with applications to a generic nuclear waste repository in crystalline rock
- Advection in matrix rock excluded using low permeability
- Transport simulations conducted with and without matrix diffusion
- Inclusion of advection and diffusion through small fractures and matrix are important
- FCM can be applied to large domains with large number of fractures
- Further testing of FCM to be based on measured field data

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