

# **Impacts of Process and Prediction Uncertainties on Projected Hanford Waste Glass Amount**

**EWG-RPT-015, Rev 0.0 (PNNL-26996)**

Prepared for the U.S. Department of Energy  
Assistant Secretary for Environmental Management



**P.O. Box 450  
Richland, Washington 99352**

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Assistant Secretary for Environmental Management

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**February 2018**

V Gervasio  
JD Vienna

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Prepared for the U.S. Department of Energy  
under Contract DE-AC05-76RL01830

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## Abstract

Analyses were performed to evaluate the impacts of using the advanced glass models, constraints (Vienna et al. 2016), and uncertainty descriptions on projected Hanford glass mass. The maximum allowable waste oxide loading (WOL) was estimated for waste compositions while simultaneously satisfying all applicable glass property and composition constraints with sufficient confidence. Different components of prediction and composition/process uncertainties were systematically included in the calculations to evaluate their impacts on glass mass. The analyses estimated the production of 23,360 MT of immobilized high-level waste (IHLW) glass when no uncertainties were taken into account. Accounting for prediction and composition/process uncertainties resulted in 5.01 relative percent increase in estimated glass mass of 24,531 MT. Roughly equal impacts were found for prediction uncertainties (2.58 RPD) and composition/process uncertainties (2.43 RPD). The immobilized low-activity waste (ILAW) mass was predicted to be 282,350 MT without uncertainty and with waste loading “line” rules in place. Accounting for prediction and composition/process uncertainties resulted in only 0.08 relative percent increase in estimated glass mass of 282,562 MT. Without application of line rules the glass mass decreases by 10.6 relative percent (252,490 MT) for the case with no uncertainties. Addition of prediction uncertainties increases glass mass by 1.32 relative percent and the addition of composition/process uncertainties increase glass mass by an additional 7.73 relative percent (9.06 relative percent increase combined). The glass mass estimate without line rules (275,359 MT) was 2.55 relative percent lower than that with the line rules (282,562 MT), after accounting for all applicable uncertainties.

## **Quality Assurance**

This task was performed under the U.S. Department of Energy (DOE) Office of River Protection (ORP) Inter-Entity Work Order # M0ORV00020 and under Pacific Northwest National Laboratory's (PNNL's) Nuclear Quality Assurance Program (NQAP). The NQAP uses ASME NQA-1-2012, Quality Assurance Requirements for Nuclear Facility Applications as its consensus standard and NQA-1-2012 Subpart 4.2.1 as the basis for its graded approach to quality. The information in this report was produced under a grading of Basic Research.

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These calculations were based on the *Preliminary ILAW Formulation Algorithm* and the *Preliminary IHLW Formulation Algorithm* developed by the Bechtel National, Inc (BNI) as part of the WTP project. We are thankful to BNI for use of these algorithms.

The authors thank Hans Brandal for quality assurance support and Veronica Perez for records management.

## Acronyms and Abbreviations

|               |                                                                         |
|---------------|-------------------------------------------------------------------------|
| BNI           | Bechtel National, Inc.                                                  |
| CI            | confidence interval                                                     |
| $c_{sp}$      | equilibrium concentration of spinel in the melt                         |
| CRV           | concentrate receipt vessel                                              |
| DOE           | U.S. Department of Energy                                               |
| DWPF          | defense waste processing facility                                       |
| DWPF-EA       | defense waste processing facility environmental assessment              |
| EMF           | effluent management facility                                            |
| ETF           | effluent treatment facility                                             |
| GFC           | glass forming chemical                                                  |
| HBV           | HLW blend vessel                                                        |
| HLW           | high-level waste                                                        |
| IHLW          | immobilized high-level waste                                            |
| ILAW          | immobilized low-activity waste                                          |
| LAW           | low-activity waste                                                      |
| LAWPS         | low-activity waste pretreatment system                                  |
| MFPV          | melter feed preparation vessel                                          |
| MFV           | melter feed vessel                                                      |
| MT            | metric ton                                                              |
| NP            | nepheline                                                               |
| ORP           | Office of River Protection                                              |
| PCT           | Product Consistency Test                                                |
| PT            | pretreatment facility                                                   |
| RMSE          | root mean squared error                                                 |
| RPD           | relative percentage difference                                          |
| SCI           | simultaneous confidence interval                                        |
| $T_{2\%}$     | temperature at two volume percent crystals in equilibrium with the melt |
| $T_L$         | liquidus temperature                                                    |
| TOE           | total online efficiency                                                 |
| VHT           | Vapor Hydration Test                                                    |
| WOL           | waste oxide loading                                                     |
| WRPS          | Washington River Protection Solutions                                   |
| WTP           | Hanford Tank Waste Treatment and Immobilization Plant                   |
| $\eta_{1150}$ | melt viscosity at the processing temperature                            |

# Contents

|                                                                                 |     |
|---------------------------------------------------------------------------------|-----|
| Abstract.....                                                                   | iii |
| Quality Assurance.....                                                          | iv  |
| Acknowledgments.....                                                            | v   |
| Acronyms and Abbreviations .....                                                | vi  |
| 1.0 Background.....                                                             | 1   |
| 2.0 Waste Treatment Process Summary .....                                       | 2   |
| 3.0 Glass Constraints and Property Models.....                                  | 4   |
| 3.1 HLW Constraints and Property Models .....                                   | 4   |
| 3.2 LAW Constraints and Property Models .....                                   | 7   |
| 4.0 Uncertainty Estimates.....                                                  | 9   |
| 4.1 Model Prediction Uncertainties.....                                         | 10  |
| 4.2 Process/Composition Uncertainties.....                                      | 11  |
| 4.2.1 HLW Process/Composition Uncertainties.....                                | 12  |
| 4.2.2 LAW Process/Composition Uncertainties.....                                | 14  |
| 4.3 Estimation of Individual Uncertainty Impacts on Glass.....                  | 16  |
| 5.0 Waste Feeds.....                                                            | 17  |
| 6.0 HLW Calculation Results and Discussion.....                                 | 29  |
| 6.1 No Uncertainties.....                                                       | 29  |
| 6.2 Prediction Uncertainties Only .....                                         | 31  |
| 6.3 Evaluation of Individual Property Prediction Uncertainties .....            | 32  |
| 6.4 Prediction and Composition/Process Uncertainties .....                      | 33  |
| 6.5 Evaluation of Individual Sources of Composition/Process Uncertainty .....   | 35  |
| 7.0 LAW Calculation Results and Discussion.....                                 | 37  |
| 7.1 LAW Glass Mass with Waste Loading (‘Line’) Rules .....                      | 37  |
| 7.2 LAW Glass Mass without Waste Loading (‘Line’) Rules .....                   | 39  |
| 7.2.1 No Uncertainties.....                                                     | 40  |
| 7.2.2 Prediction Uncertainties Only .....                                       | 42  |
| 7.2.3 Evaluation of Individual Property Prediction Uncertainties .....          | 44  |
| 7.2.4 Prediction and Composition/Process Uncertainties.....                     | 45  |
| 7.2.5 Evaluation of Individual Sources of Composition/Process Uncertainty ..... | 46  |
| 7.2.6 Without VHT Constraint.....                                               | 48  |
| 7.2.7 Evaluation of Glass Mass for Initial Phase of LAW Processing.....         | 49  |
| 8.0 Summary and Conclusions .....                                               | 50  |
| 8.1 High-Level Waste .....                                                      | 50  |
| 8.2 Low-Activity Waste .....                                                    | 51  |
| 9.0 References .....                                                            | 53  |

|                                                                                                                                                                                 |     |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----|
| Appendix A.....                                                                                                                                                                 | A.1 |
| Appendix B.....                                                                                                                                                                 | B.1 |
| Appendix C Minimum, maximum, and most likely concentration of components in each GFC<br>(based on values reported in Table A-4 of Vienna and Kim 2014).....                     | C.1 |
| Appendix D Minimum, maximum, and most likely PERT distribution in $\ln \left[ \frac{1}{1 - \nu_i} \right]$ with<br>minimum, based on the values reported by Nelson (2013). .... | D.1 |

## Figures

|                                                                                                                                                               |    |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------|----|
| Figure 1. Schematic of the LAW and HLW vitrification process.....                                                                                             | 2  |
| Figure 2. Schematic Representation of the Hanford HLW Glass Processing Envelope, from<br>Vienna (2014). ....                                                  | 9  |
| Figure 3. Example Histogram of Predicted T <sub>2%</sub> Values from a 10,000 Run Monte Carlo<br>Calculation. ....                                            | 14 |
| Figure 4. Plot of Major HLW Component Concentrations vs Batch Number (~4000 batches) .....                                                                    | 17 |
| Figure 5. Plot of Major LAW Component Concentrations vs Batch Number (~28,500) .....                                                                          | 18 |
| Figure 6. Average Distance versus Number of HLW Clusters from Hierarchical Cluster Analysis. ....                                                             | 19 |
| Figure 7. Parallel Plots of 30 HLW Composition Clusters.....                                                                                                  | 23 |
| Figure 8. Average Distance versus Number of LAW Clusters from Hierarchical Cluster Analysis. ....                                                             | 24 |
| Figure 9. Parallel Coordinate Plots for 36 LAW Clusters. ....                                                                                                 | 28 |
| Figure 10. Waste Loading Limiting Factors (Glass Mass Basis) for HLW Glasses.....                                                                             | 30 |
| Figure 11. Comparison of the WTP Baseline and Proposed New Waste Loading Line Rules for<br>Normalized Alkali and Sulfur Content. (Vienna et al. (2016))...... | 37 |
| Figure 12. Distribution of LAW Glass Mass Limited by Various Line Rules.....                                                                                  | 39 |
| Figure 13. Waste Loading Limiting Factors for LAW Glasses without Line Rules.....                                                                             | 42 |
| Figure 14. Waste Loading Limiting Factors (Glass Mass Basis) for HLW Glasses.....                                                                             | 50 |

## Tables

|                                                                                                                                                                           |    |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----|
| Table 1. Summary of HLW Melt and Glass Constraints .....                                                                                                                  | 4  |
| Table 2. HLW Glass Component Concentration Constraints, in Mass Fractions .....                                                                                           | 6  |
| Table 3. Summary of LAW Melt and Glass Constraints .....                                                                                                                  | 7  |
| Table 4. LAW Glass Component Concentration Constraints, in Mass Fractions .....                                                                                           | 8  |
| Table 5. Summary of Predicted Properties and Associated Uncertainty Expressions .....                                                                                     | 11 |
| Table 6. Waste Mass, Maximum WOL, Glass Mass, and Limiting Factors for each of 30 HLW<br>Clusters with No Uncertainties .....                                             | 29 |
| Table 7. Waste Mass, Maximum WOL, Glass Mass, and Limiting Factors for 30 HLW Clusters<br>with Prediction Uncertainties.....                                              | 31 |
| Table 8. HLW Glass Masses Generated by Individually Excluding Prediction Uncertainties for<br>Various Properties.....                                                     | 32 |
| Table 9. Glass Mass and Limiting Factors for 30 HLW Clusters with Prediction and<br>Composition/Process Uncertainties .....                                               | 34 |
| Table 10. HLW Glass Masses Generated by Individually Excluding Prediction Uncertainties for<br>Various Properties, kg.....                                                | 35 |
| Table 11. Waste Mass, Maximum WOL, Glass Mass, and Limiting Factors for each of 36 LAW<br>Clusters with Line Rules .....                                                  | 38 |
| Table 12. Waste Mass, Maximum WOL, Glass Mass, and Limiting Factors for each of 36 LAW<br>Clusters with No Uncertainties and No Line Rules .....                          | 40 |
| Table 13. Waste Mass, Maximum WOL, Glass Mass, and Limiting Factors for 36 LAW Clusters<br>with Prediction Uncertainties without Line Rules .....                         | 43 |
| Table 14. LAW Glass Mass (MT) for Various Different Property Prediction Uncertainty Cases .....                                                                           | 44 |
| Table 15. Waste Mass, Maximum WOL, Glass Mass, and Limiting Factors for 36 LAW Clusters<br>with Prediction and Composition/Process Uncertainties without Line Rules ..... | 45 |
| Table 16. LAW Glass Mass (MT) for Full Prediction and Composition Uncertainty Compared to<br>Cases with Analytical and Mixing and Sampling Uncertainties Removed .....    | 47 |
| Table 17. Glass Mass (MT) Projected for the Full Mission for Each of the 12 Evaluated Cases.....                                                                          | 48 |
| Table 18. Glass Mass (MT) Projected for the Initial Phase of Processing and Full Mission for<br>Each of the 12 Evaluated Cases .....                                      | 49 |
| Table 19. LAW Glass Mass Estimates for Cases Including Various Uncertainty Terms.....                                                                                     | 51 |
| Table 20. Summary of Impacts of Line Rules and Uncertainties on LAW Glass Mass and<br>Containers (a).....                                                                 | 52 |

## 1.0 Background

The U.S. Department of Energy (DOE) Office of River Protection (ORP) is responsible for the safe retrieval, treatment, and disposal of this waste. For this scope ORP is contracting Bechtel National, Inc. (BNI) to design, construct, and commission the world's largest radioactive waste treatment plant: the Hanford Tank Waste Treatment and Immobilization Plant (WTP) - (DOE 2000). The plant will separate the tank waste into high-level waste (HLW) and low-activity waste (LAW) fractions through filtration, cesium ion exchange, and precipitation. Each fraction will be vitrified in separate facilities into borosilicate waste glass.

Waste glass data and property-composition models were developed for the commissioning of the WTP (Piepel et al. 2007; Piepel et al. 2008). These models with uncertainty descriptions and plant operating strategies and current estimated process data were used to develop glass formulation algorithms to be used in plant operation (Kim and Vienna 2012; Vienna and Kim 2014). The current WTP glass property models, constraints, and algorithms were intended to be used in plant commissioning and represent modest waste loading and relatively conservative constraints. Application of prediction and process uncertainties was found to have a negligible impact on the amount of glass to be produced at Hanford while using the conservative models (Nelson 2010; Nelson et al. 2007).

Since their development significant advancements in glass formulation and property modeling has been made (Muller et al. 2012; Vienna et al. 2013; Russell et al. 2017; Kim et al. 2008; Muller et al. 2010; Matlack et al. 2005a; Matlack et al. 2005b; Matlack et al. 2006a, b; Matlack et al. 2007; Matlack et al. 2009; Matlack et al. 2010c; Matlack et al. 2010a; Matlack et al. 2010b). These data were compiled and incorporated into sets of constraints and glass property models which are aimed at estimating the amount of glass that would be produced at Hanford upon successfully completion of the on-going studies (Vienna et al. 2016). As this latter set of models and constraints are intended to maximize waste loading in glass they are necessarily far less conservative than those intended for plant commissioning. It stands to reason that application of prediction and process/composition uncertainties would have a larger impact on the projected amount of glass produced during the Hanford mission than for the commissioning models and constraints.

The objective of this study is to quantify the expected changes in glass amount for the entire Hanford mission by applying these new models and constraints along with the anticipated prediction and process/composition uncertainties. The process is described that determined how the glass masses were obtained and the results from each type of calculation is summarized.

## 2.0 Waste Treatment Process Summary

A detailed description of the assumed waste treatment process is given elsewhere (Deng et al. 2016). This section summarizes the key aspects of that process that impacts the formulation of glass with its associated uncertainties. A schematic of the LAW and HLW vitrification process is shown in Figure 1. A feed preparation or pretreatment process will deliver waste to the vitrification plants. In the case used in this report, LAW feed is prepared for the first ten years of operation in a LAW Pretreatment System (LAWPS) with recycle streams from an Effluent Treatment Facility (ETF), not shown in Figure 1, and blended in the LAW Concentrate Receipt Vessel (CRV). After 10 years of operation the LAW feed is blended with recycle streams in the Pretreatment Facility (PT). The HLW feed including pretreated sludge and Cs ion exchange eluate are delivered to the HLW Melter Feed Preparation Vessel (MFPV) from the PT HLW Blend Vessel (HBV). The final glass formulations and ultimate WOL are determined for each batch of waste from samples taken from the HLW MFPV and the LAW CRV and analyzed.

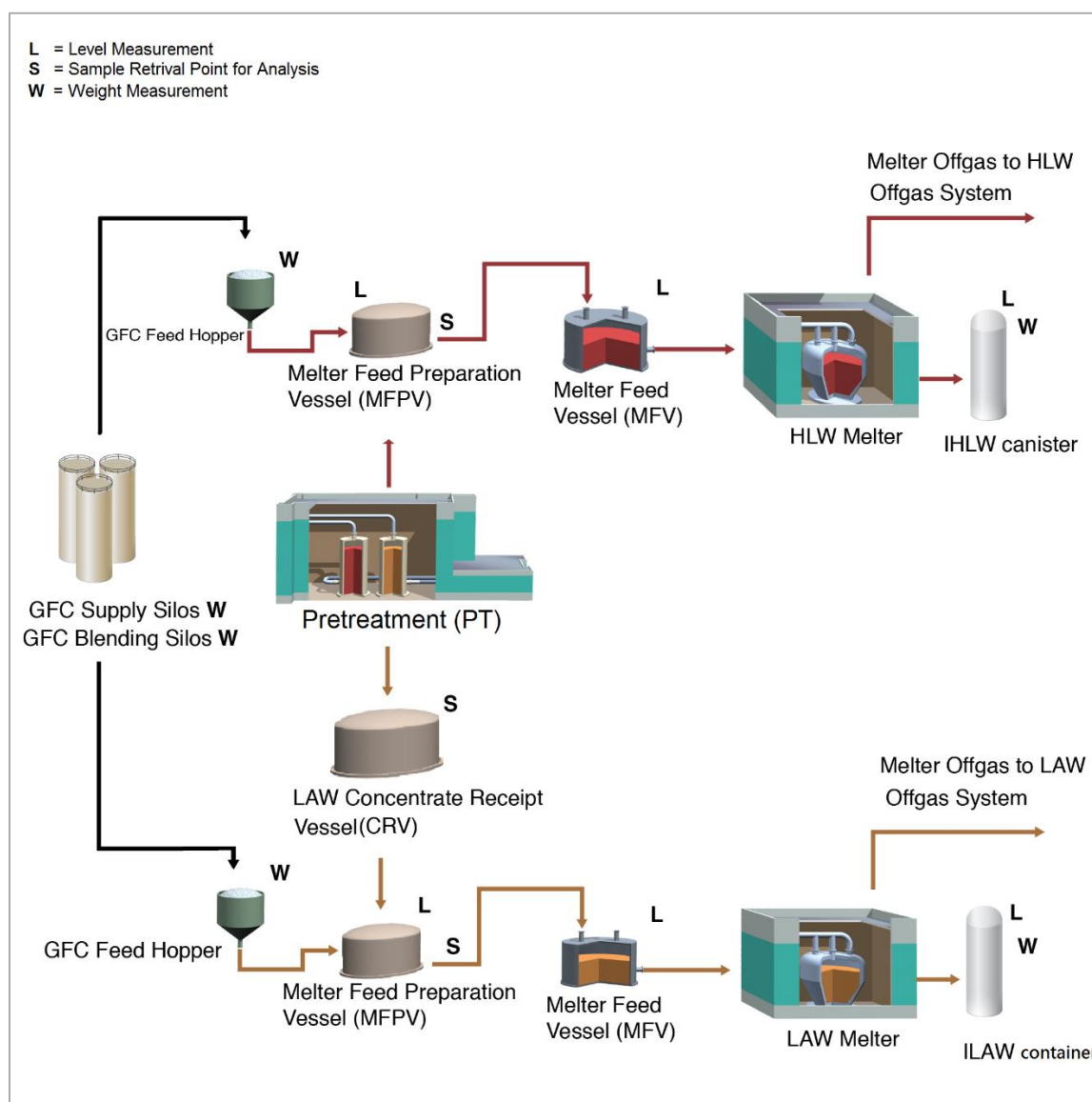


Figure 1. Schematic of the LAW and HLW vitrification process.

In the baseline flowsheet, the HLW vitrification plant will receive pretreated HLW from PT in the MFPV. The vessel content level will be measured before (heel level) and after (waste+heel level) waste addition to calculate the volume of waste and melter feed heel in each batch. The contents of the vessel will then be mixed, sampled, and analyzed for chemical and radiochemical concentrations. The current baseline is to analyze four samples of waste+heel for each MFPV batch. Based on the analyzed composition of waste+heel, glasses will be formulated to ensure the batch will meet all processing and product quality constraints with sufficient confidence. The associated mix of glass forming chemicals (GFC's) will be weighed, blended, and transferred into the MFPV. The level of slurry in the MFPV will be measured to determine melter feed volume and samples (nominally up to eight samples) will be taken and analyzed for chemical composition. The composition and associated predicted properties from this latter set of analyses will be used to qualify the glass to be produced and generate data for glass production records.<sup>1</sup> The melter feed will then be transferred as a batch to the melter feed vessel (MFV) where it will be continuously fed into the melter. The volumes of melter feed in both the MFPV and MFV will be measured before and after waste transfer to determine volume of melter feed in that batch.

The LAW vitrification plant will receive pretreated LAW from either LAWPS + effluent management facility (EMF) or PT in the CRV. The vessel content level will be measured after waste addition to estimate the volume of waste in each CRV batch. The contents of the vessel will then be mixed, sampled, and analyzed for chemical and radiochemical concentrations. The current baseline is to analyze three samples of waste for each CRV batch. Based on the analyzed composition, glasses will be formulated to ensure the melter feed batch will meet all processing and product quality constraints with sufficient confidence. The calculated volume of LAW for each MFPV batch from the CRV will be transferred into the MFPV. The mass of each glass forming chemicals (GFC's) to achieve the target glass composition will be weighed, blended, and transferred into the MFPV. The level of slurry in the MFPV will be measured to determine melter feed volume and a sample will be taken and analyzed for chemical composition as a process control measure to confirm the appropriate melter feed was prepared. The composition and associated predicted properties from analyses of waste in the CRV, the measured mass of each GFC, and the volume of waste transferred from the CRV to the MFPV will be used to produce and generate data for glass production records.

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<sup>1</sup> Reporting of radionuclide concentrations will be based on measurement of radionuclide concentrations in the waste+heel samples.

### 3.0 Glass Constraints and Property Models

Estimates of maximum WOL were determined in this study by numerically optimizing glass compositions for each waste composition while simultaneously satisfying a number of property and composition constraints, the process/composition constraints described in Section 3.1 for HLW and Section 3.2 for LAW. The melter feed should be both processable and yield an adequate product, i.e., the resultant glass should have properties within acceptable ranges. Properties of the target glass are predicted using glass-composition property models; which are valid over fixed composition ranges defined by model validity constraints. The models and constraint sets used in this study are those described by Vienna (2016) and are briefly described in the following subsections.

#### 3.1 HLW Constraints and Property Models

Table 1 summarizes the HLW glass property/composition constraints used in glass optimization with bulleted descriptions and explanations for each constraint below the table. Also reported are glass component concentration limits (Table 2) for model validity, chromium tolerance, and phosphate tolerance.

| Property/Composition Constraint                                   | Limit                                                                                   |
|-------------------------------------------------------------------|-----------------------------------------------------------------------------------------|
| PCT Responses                                                     | $\ln[\text{PCT-B, Na, Li, g/m}^2] \leq 1.386^{(a)}$                                     |
| Nepheline                                                         | $p \leq 0.3$ (probability)                                                              |
| Spinel                                                            | $T_{2\%} \leq 950^\circ\text{C}$                                                        |
| Zirconium-containing phases                                       | $T_L\text{-Zr} \leq 1050^\circ\text{C}$<br>if $g_{\text{ZrO}_2} > 0.04$ (mass fraction) |
| Viscosity at $1150^\circ\text{C}$                                 | $0.693 \leq \ln(\eta_{1150}, \text{Pa}\cdot\text{s}) \leq 2.079^{(b)}$                  |
| P <sub>2</sub> O <sub>5</sub> and CaO concentrations              | $w_{\text{P}_2\text{O}_5} \times w_{\text{CaO}} \leq 6.5$ (wt%) <sup>2</sup>            |
| Salt, SO <sub>3</sub> concentration                               | $w_{\text{SO}_3} \leq w_{\text{SO}_3}^{\text{Limit}}$ (wt%)                             |
| Eskolaite formation                                               | $g_{\text{Cr}_2\text{O}_3} \leq 0.03$ (mass fraction)                                   |
| B <sub>2</sub> O <sub>3</sub> and SiO <sub>2</sub> concentrations | $g_{\text{SiO}_2} + g_{\text{B}_2\text{O}_3} \geq 0.32$ (mass fraction)                 |

(a) This corresponds to PCT-B, -Na, -Li  $\leq 4$  g/m<sup>2</sup>.

(b) This corresponds to  $2 \leq \eta_{1150} \leq 8$  Pa·s.

1. The normalized PCT responses of boron, sodium, and lithium of HLW glasses must be below those of the Defense Waste Processing Facility Environmental Assessment (DWPF-EA) glass (Jantzen et al. 1993) with sufficient confidence (DOE 1996). The WTP Wasteform Qualification Report uses a 95% confidence level (Nelson 2010). A conservative value of 4 g/m<sup>2</sup> was used in this study. Although this value is conservative (48% to 60% of the limit) it has previously been shown to not be impactful on WOL.

2. The formation of nepheline on slow-cooled glass has been previously shown to strongly impact the chemical durability of glass and the ability to predict PCT responses (Kim et al. 1995). A predicted probability of 30% nepheline precipitation by the current submixture model (Vienna et al. 2017) was found to represent roughly 95% confidence that nepheline would not form in waste glasses as described in detail in (Vienna et al. 2016).
3. The accumulation of spinel in the melter may disrupt processing and/or reduce melter life (Matyas et al. 2012). Vienna et al. (2016) used an ad-hoc yet conservative limit of 2 vol% spinel at equilibrium with the melt at 950°C.
4. Some waste types, rich in  $ZrO_2$  (> 4 wt%), are prone to precipitation of zirconia containing phases which may disrupt processing and/or reduce melter life (Crum et al. 1997). A  $T_L$  limit of 1050°C is used in this study. The model reported in (Vienna et al. 2016) for  $T_L$ -Zr was modified slightly to avoid a jump in predicted response at  $g_{ZrO_2} = 0.04$  as described at the end of this subsection.
5. The viscosity of glass melts must be maintained near 5 Pa·s for smooth processing. The  $2 < \eta_{1150} < 8$  limit was used for this study.
6. Glasses high in phosphate may form non-durable secondary phases, increase corrosivity of metal melter components, and form difficult to melt phases in the melter cold-cap. An ad-hoc constraint of calcium oxide times phosphorous oxide < 6.5 wt%<sup>2</sup> was developed to avoid the many deleterious effects of high phosphate glasses (Vienna 2008).
7. Sulfate salt accumulation in the melter may increase melter materials corrosion and increase volatility (Vienna et al. 2014). A sulfate solubility model was used to avoid compositions prone to salt accumulation in HLW melter feeds.
8. Some waste types, rich in  $Cr_2O_3$  (> 3 wt%) are prone to eskolaite precipitation and/or molten chromate salt accumulation. An ad-hoc 3 wt% constraint was used to avoid those compositions.
9. Glasses low in the two primary solvents or glass formers –  $SiO_2$  and  $B_2O_3$  – may not make a processable glass. An ad-hoc limit of 32 wt% of combined formers was used, based on preliminary test data.

The models used to predict these properties are generally of the form:

$$t(P) = \sum_{i=1}^q a_i g_i + \text{Selected} \left\{ \sum_{i=1}^q a_{ii} g_i^2 + \sum_{i=1}^{q-1} \sum_{j=i+1}^q a_{ij} g_i g_j \right\} \quad (1)$$

where,  $t(P)$  is the transformed property,  $a_i$  are the  $i^{\text{th}}$  component coefficient,  $a_{ii}$  are the  $i^{\text{th}}$  cross  $i^{\text{th}}$  and  $i^{\text{th}}$  cross  $j^{\text{th}}$  component interaction coefficients, and  $g_i$  and  $g_j$  are the mass fractions of component  $i$  and  $j$ . Exceptions to this model form are: 1) PCT models which also contain  $g_{Al_2O_3}^3$ , and  $g_{Al_2O_3}^4$  terms and 2) nepheline formation probability which is a polynomial of normalized component concentrations. Model details and coefficients are given by Vienna et al. (2016). In addition to the property constraints, the model validity constraints for glass component concentrations, shown in Table 2 are used.

Table 2. HLW Glass Component Concentration Constraints, in Mass Fractions

| Component                      | Min    | Max    |
|--------------------------------|--------|--------|
| Al <sub>2</sub> O <sub>3</sub> | 0.0190 | 0.3000 |
| B <sub>2</sub> O <sub>3</sub>  | 0.0400 | 0.2200 |
| Bi <sub>2</sub> O <sub>3</sub> | 0      | 0.0700 |
| CaO                            | 0      | 0.1000 |
| CdO                            | 0      | 0.0150 |
| Cr <sub>2</sub> O <sub>3</sub> | 0      | 0.0300 |
| F                              | 0      | 0.0250 |
| Fe <sub>2</sub> O <sub>3</sub> | 0      | 0.2000 |
| K <sub>2</sub> O               | 0      | 0.0600 |
| Li <sub>2</sub> O              | 0      | 0.0600 |
| MgO                            | 0      | 0.0600 |
| MnO                            | 0      | 0.0800 |
| Na <sub>2</sub> O              | 0.0410 | 0.2400 |
| NiO                            | 0      | 0.0300 |
| P <sub>2</sub> O <sub>5</sub>  | 0      | 0.0450 |
| SiO <sub>2</sub>               | 0.2200 | 0.5300 |
| SrO                            | 0      | 0.1010 |
| ThO <sub>2</sub>               | 0      | 0.0600 |
| TiO <sub>2</sub>               | 0      | 0.0500 |
| UO <sub>3</sub>                | 0      | 0.0630 |
| ZnO                            | 0      | 0.0400 |
| ZrO <sub>2</sub>               | 0      | 0.1350 |

Application of the constraints and models from Vienna et al. 2016 resulted in significant challenges to converge on optimal solutions using standard optimization routines (e.g., Microsoft Excel™ solver, Frontline Analytical Solver, the solver built-in to Gensym G2). Two changes were implemented in calculations described in this report to improve stability and enable optimal solutions using standard optimization routines.

1. The model reported in (Vienna et al. 2016) for T<sub>L</sub>-Zr was modified slightly to avoid a jump in predicted response at  $g_{ZrO_2} = 0.04$ . A sigmoidal function that approaches 0 at  $g_{ZrO_2} < 0.04$  and

approaches predicted T<sub>L</sub>-Zr at  $g_{ZrO_2} > 0.04$  was added:  $T_L - Zr = \frac{\sum T_i g_i}{1 + e^{-1000(g_{ZrO_2} - 0.039)}}$ . This

addition has no practical implications to meeting the constraint while allowing for successful numerical optimization of glass compositions near  $g_{ZrO_2} = 0.04$ .

2. Additives used were limited to silica, borax, sodium carbonate, lithium carbonate, zincite, wollastonite, V<sub>2</sub>O<sub>5</sub>, kyanite, and hematite. Compared to the recommended additives of: Al<sub>2</sub>O<sub>3</sub>, B<sub>2</sub>O<sub>3</sub>, CaO, Li<sub>2</sub>O, MgO, Na<sub>2</sub>O, SiO<sub>2</sub>, V<sub>2</sub>O<sub>5</sub>, ZnO, and ZrO<sub>2</sub>. Effectively, MgO and ZrO<sub>2</sub> were excluded.

### 3.2 LAW Constraints and Property Models

Table 3 summarizes the LAW glass property/composition constraints used in glass optimization. A set of waste loading rules were used during some of the calculations as an ad-hoc method of limiting loading of waste in glass (Muller et al. 2010). Whether the loading rules were applied or not, each waste glass met a set of property constraints: sulfate solubility; baddeleyite ( $\text{ZrO}_2$ ) and cassiterite ( $\text{SnO}_2$ ) precipitation; durability including alkali to  $\text{ZrO}_2 + \text{CaO} + \text{SnO}_2$  ratio, PCT response, and vapor hydration test (VHT) response;  $\eta_{1150}$ ; and refractory corrosion. A description and explanation of each of the property constraints are itemized below Table 3. In Table 4 glass component concentration constraints are identified.

Table 3. Summary of LAW Melt and Glass Constraints

| Waste Loading Rules                                    | Limit                                                                                                                                                 |
|--------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------|
| Alkali content                                         | $w_{\text{Na}_2\text{O}} + 0.66w_{\text{K}_2\text{O}} \leq 24 \text{ wt}\%$                                                                           |
| Alkali and sulfur content                              | $w_{\text{Na}_2\text{O}} + 0.66w_{\text{K}_2\text{O}} \leq 33.94 - 11.69w_{\text{SO}_3}, \text{ wt}\%$                                                |
| Sulfur content                                         | $w_{\text{SO}_3} \leq 1.5 \text{ wt}\%$                                                                                                               |
| Halide content                                         | $g_{\text{SO}_3} \leq 0.01825 - 0.4936 \times (1.761g_{\text{Cl}} + 2.971g_{\text{Cr}_2\text{O}_3} - 0.1608g_{\text{P}_2\text{O}_5})$                 |
| Property                                               | Limit                                                                                                                                                 |
| Salt, $\text{SO}_3$ concentration                      | $w_{\text{SO}_3} \leq w_{\text{SO}_3}^{\text{Limit}}$                                                                                                 |
| Combined zirconia, tin, and alumina constraint         | $g_{\text{ZrO}_2} + g_{\text{SnO}_2} + g_{\text{Al}_2\text{O}_3} \leq 0.17$                                                                           |
| Alkali minus sum of zirconia, tin, and lime constraint | $g_{\text{Na}_2\text{O}} + 0.66g_{\text{K}_2\text{O}} + 2.07g_{\text{Li}_2\text{O}} - g_{\text{ZrO}_2} - g_{\text{SnO}_2} - g_{\text{CaO}} \leq 0.15$ |
| PCT response                                           | $\ln[\text{PCT } NL, \text{ g/L}] \leq 1.386$                                                                                                         |
| VHT response                                           | $\ln[\text{VHT } D, \mu\text{m}] \leq 6.116$                                                                                                          |
| Viscosity at 1150°C                                    | $0.693 \leq \ln[\eta_{1150}, \text{ Pa}\cdot\text{s}] \leq 2.079$                                                                                     |
| K-3 neck corrosion at 1208°C                           | $\ln[k_{1208}, \text{ in}] \leq -3.2189$                                                                                                              |

1. Sulfate salt accumulation in the melter may increase melter materials corrosion and increase volatility (Vienna et al. 2014). A sulfate solubility model was used to avoid compositions prone to salt accumulation in LAW melter feeds.
2. Some glass formulations, rich in combined  $\text{ZrO}_2$ ,  $\text{SnO}_2$ , and  $\text{Al}_2\text{O}_3$  are prone to precipitation of baddeleyite ( $\text{ZrO}_2$ ) or cassiterite ( $\text{SnO}_2$ ) which may disrupt processing and/or reduce melter life. An ad-hoc empirical rule constraining the combine concentrations of those oxides reduces the likelihood of their precipitation.
3. LAW glasses are particularly prone to relatively poor chemical durability due to high alkali content. Above some threshold in alkali content the durability test responses of glasses become very high and change in a non-linear fashion.  $\text{ZrO}_2$ ,  $\text{SnO}_2$ , and  $\text{CaO}$  generally increase the alkali concentration where the durability becomes highly non-linear. An empirical, ad-hoc, concentration constraint is used to 1) help reduce the likelihood of non-durable glasses and 2) improve the ability of PCT and VHT models to better predict responses.
4. The normalized PCT responses of boron, sodium, and silicon of LAW glasses must be below 4 g/L (DOE 2000).
5. The VHT response of LAW glasses must be below 50 g/m<sup>2</sup>/d (DOE 2000).
6. The viscosity of glass melts must be maintained near 5 Pa·s for smooth processing. The  $2 < \eta_{1150} < 8$  limit was used for this study.

7. Glasses rich in alkali are prone to excessive refractory corrosion. K-3 corrosion > 0.04 inches per year at the melt line was suggested as an appropriate limit to avoid excessive corrosion (Muller et al. 2015).

The models used to predict these properties are generally of the form shown in Eqn 1. Model details and coefficients are given by Vienna et al. (2016). In addition to the property constraints, the model validity constraints for glass components are used (Table 4).

Table 4. LAW Glass Component Concentration Constraints, in Mass Fractions

| Component                      | Min    | Max    |
|--------------------------------|--------|--------|
| Al <sub>2</sub> O <sub>3</sub> | 0.0553 | 0.1370 |
| B <sub>2</sub> O <sub>3</sub>  | 0.0600 | 0.1370 |
| CaO                            | 0      | 0.1060 |
| Cl                             | 0      | 0.0117 |
| Cr <sub>2</sub> O <sub>3</sub> | 0      | 0.0100 |
| Fe <sub>2</sub> O <sub>3</sub> | 0      | 0.0997 |
| K <sub>2</sub> O               | 0      | 0.0589 |
| Li <sub>2</sub> O              | 0      | 0.0503 |
| MgO                            | 0      | 0.0350 |
| Na <sub>2</sub> O              | 0.0248 | 0.2600 |
| P <sub>2</sub> O <sub>5</sub>  | 0      | 0.0340 |
| SiO <sub>2</sub>               | 0.2983 | 0.5020 |
| SnO <sub>2</sub>               | 0      | 0.0501 |
| TiO <sub>2</sub>               | 0      | 0.0341 |
| V <sub>2</sub> O <sub>5</sub>  | 0      | 0.0401 |
| ZnO                            | 0      | 0.0540 |
| ZrO <sub>2</sub>               | 0      | 0.0675 |

## 4.0 Uncertainty Estimates

As stated earlier, glass compositions are optimized for each waste to maximize WOL while simultaneously satisfying a number of property and composition constraints. Both glass composition and glass property predictions are uncertain and in practical applications variation in estimated glass composition, along with uncertainties in glass property predictions, are combined to ensure that the final glass will meet constraints with sufficient confidence. Figure 2 shows a schematic diagram of the glass formulation method applied to Hanford HLW. The ternary diagram on the left is meant to represent the multidimensional composition region made up by a particular waste batch at the top of the diagram; the concentrations of each of the ten potential glass forming additives are expressed across the bottom. The property constraints (calculated using glass property models) limit the portion of composition region within which glass can be formulated as shown by the solid black lines for different properties. Model prediction uncertainties further narrow the composition space within which glass can be formulated as shown by the dotted black lines. A glass can be formulated anywhere within the region defined by the property limits with associated uncertainties. The composition of the glass isn't precisely known. So, various sources of composition uncertainties must be accounted for as shown by the tan circle. The final glass formulation region is the region surrounded by the dotted lines (representing property limits with prediction uncertainty) that an uncertain composition (represented by the tan circle and defined in schematic on right side of Figure 2) can fit.

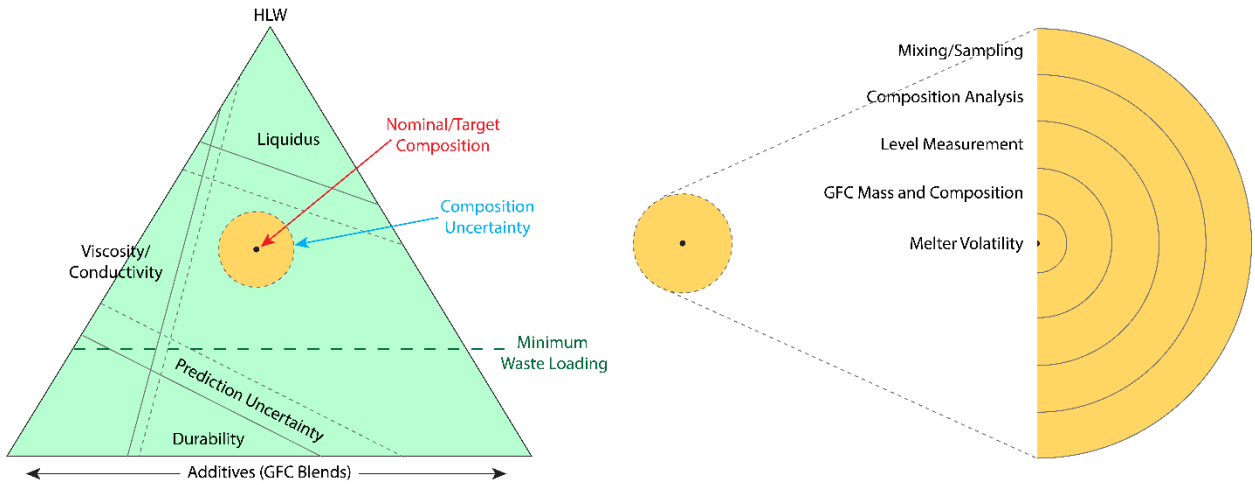


Figure 2. Schematic Representation of the Hanford HLW Glass Processing Envelope, from Vienna (2014).

The constraints used thus expressed as lower- and upper- combined confidence intervals:

$$L_{\alpha}^L \leq t(P_{\alpha}) - U_{\alpha}^{pred} - U_{\alpha}^{comp} \text{ and } L_{\alpha}^U \geq t(P_{\alpha}) + U_{\alpha}^{pred} + U_{\alpha}^{comp} \quad (2)$$

where  $L_{\alpha}^L$  and  $L_{\alpha}^U$  are the lower and upper limits on transformed property  $\alpha$  [ $t(P_{\alpha})$ ],  $U_{\alpha}^{Pred}$  is the uncertainty in prediction of  $t(P_{\alpha})$ , and  $U_{\alpha}^{Comp}$  is the expression of composition uncertainty expressed in units of  $t(P_{\alpha})$ . The values of uncertainty scale with the level of confidence obtained. The following subsection describes the calculation of these uncertainty values.

## 4.1 Model Prediction Uncertainties

Most of the property models used in this study are of the form of partial quadratic models of a transformed property (Eqn 1). Prediction uncertainty can be expressed as a confidence interval (CI) as in Eqn 3 or a simultaneous confidence interval (SCI), Eqn 4:

$$U_{CI}^{pred} = t_{1-\alpha(n-p)} \sqrt{s^2 \mathbf{x}^T (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{x}} \quad (3)$$

$$U_{SCI}^{pred} = \sqrt{ps^2 F_{1-\alpha(p, n-p)} \mathbf{x}^T (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{x}} \quad (4)$$

where:

- n = number of data in the model
- s = root mean squared error (RMSE) of model
- F = 1- $\alpha$  quantile of an F-distribution
- t = 1- $\alpha$  quantile of a t-distribution
- $\alpha$  = the confidence level
- p = number of model parameters (terms)
- $\mathbf{x}$  = glass composition vector represented in model terms
- $\mathbf{X}$  = matrix of glass compositions used in fitting the model

Generally SCI's are used when you need a given confidence that all batches will meet the limit while CI's are used when you need confidence that the single batch will meet the limit. The variance covariance matrix ( $\mathbf{\Omega}$ ), tables listed in Table 5 and 0, combines the terms of these equations into a single matrix:

$$\mathbf{\Omega} = s^2 (\mathbf{X}^T \mathbf{X})^{-1} \quad (5)$$

Table 5 lists the property models used in formulation optimization and the uncertainty expressions assumed along with the Appendix A table for each associated variance covariance matrix.

Table 5. Summary of Predicted Properties and Associated Uncertainty Expressions

| Property, units                                                                    | $t(P)$             | Confidence     | $\Omega$                 |
|------------------------------------------------------------------------------------|--------------------|----------------|--------------------------|
| HLW PCT normalized boron release, g/m <sup>2</sup>                                 | $\ln(r_B)$         | 95% SCI        | Table A.1                |
| HLW PCT normalized sodium release, g/m <sup>2</sup>                                | $\ln(r_{Na})$      | 95% SCI        | Table A.2                |
| HLW PCT normalized lithium release, g/m <sup>2</sup>                               | $\ln(r_{Li})$      | 95% SCI        | Table A.3                |
| HLW $T_L$ of Zr containing phases, °C                                              | $T_L$              | 90% CI         | Table A.4                |
| HLW $T_{2\%}$ of spinel, °C                                                        | $T_{2\%}$          | 90% CI         | Table A.5                |
| HLW nepheline probability, distance above the cutoff in $SiO_2+x B_2O_3$ direction | Norm mass fract    | 95% boot-strap | boot-strap trials in A.6 |
| HLW viscosity at 1150°C, Pa·s                                                      | $\ln(\eta_{1150})$ | 90% CI         | Table A.7                |
| HLW sulfate solubility, wt%                                                        | $w_{SO_3}$         | 90% CI         | Table A.8                |
| LAW PCT normalized concentration, g/L                                              | $\ln(NC)$          | 90% SCI        | Table A.9                |
| LAW VHT alteration depth, $\mu m$                                                  | $\ln(d)$           | 90% SCI        | Table A.10               |
| LAW K-3 neck corrosion, in                                                         | $\ln(k)$           | 90% CI         | Table A.11               |
| LAW sulfate solubility, wt%                                                        | $w_{SO_3}$         | 90% CI         | Table A.12               |
| LAW viscosity at 1150°C, Pa·s                                                      | $\ln(\eta_{1150})$ | 90% CI         | Table A.13               |

One key exception to the typical uncertainty quantification method is the nepheline probability model. The mathematical form of this model is different than Eqn (1):

$$P = -\frac{bC + 2bB - \sqrt{3}C}{2(A + B + C)} - \frac{c(2B + C)^2}{4(A + B + C)^2} - a \quad (6)$$

where A, B, C are normalized weighted combinations of component concentrations in the glass (Vienna et al. 2017). A boot strapping method was used to estimate the uncertainty in this models prediction. This boot strapping method, described in detail in (Vienna et al. 2016), was aimed at obtaining a 95% confidence in model predictions.

## 4.2 Process/Composition Uncertainties

The glass composition is estimated using a mass balance for each MFPV batch (see MFPV in Figure 1) and will be defined in Subsections 4.2.1 and 4.2.2. As shown in the right half of Figure 2 there are several uncertainty parameters which impact this mass balance. Due to the non-linear nature of the mass balance equation, there is not an analytical solution to the uncertainty value. Therefore, a Monte-Carlo approach was taken to estimate compositions uncertainties (Kim and Vienna 2012; Vienna and Kim 2014). Monte Carlo simulations are a class of computational methods that rely on repeated random sampling to model the probability of different outcomes in processes that cannot easily be predicted due to the presence of uncertain variables. Monte Carlo methods use probability distribution for modelling random variables. Different types of probability distributions are used to describe the uncertain variable, such as normal, triangular, and PERT. Then many iterations, or simulations, are run using numerical computations that will generate different outcomes (compositions and predicted properties in this case) and their probability of occurrence. In other words, the Monte Carlo method provides a probabilistic estimate of the uncertainty in glass composition and associated predicted properties. Although a very similar approach is taken to define the composition uncertainties in LAW and HLW glasses, the details of the mass balance equation require slightly different treatment.

#### 4.2.1 HLW Process/Composition Uncertainties

The HLW mass balance is given by:

$$g_i = \frac{\left[ c_i^{HLW} V^{HLW} f_i + \sum_{k=1}^{n^{GFCs}} g_{ik}^{oxide} M_k^{GFCin} \right] v_i}{\sum_{i=1}^{noxides} \left[ c_i^{HLW} V^{HLW} f_i + \sum_{k=1}^{n^{GFCs}} g_{ik}^{oxide} M_k^{GFCin} \right] v_i} \quad (7)$$

where:

- $g_i$  = mass fraction of  $i^{th}$  oxide in glass (g/g)
- $c_i^{HLW}$  = Concentration of the  $i^{th}$  component measured in samples from the MFPV prior to addition of GFCs (g/mL)
- $V^{HLW}$  = Volume of waste in the HLW MFPV batch (L)
- $f_i$  = A conversion factor from element mg to oxide kg (kg/mg)
- $g_{ik}^{oxide}$  = Mass fraction of the  $i^{th}$  oxide in the  $k^{th}$  GFC (g/g)
- $M_k^{GFCin}$  = Mass of the  $k^{th}$  GFC in the MFPV batch (kg)
- $n^{GFCs}$  = Number of GFC's added to the MFPV batch
- $v_i$  = Fraction of  $i^{th}$  oxide retained in the glass (g/g)

The values:  $c_i^{HLW}$ ,  $V^{HLW}$ ,  $g_{ik}^{oxide}$ ,  $M_k^{GFCin}$ , and  $v_i$  are each uncertain and each is given a probability distribution. The uncertainty on waste component concentration is estimated as a normal distribution centered on the average measured values (in this study the nominal value for the waste composition) and a standard deviation ( $s_i^{cHLW}$ ) is given by:

$$s_i^{cHLW} = \frac{\sqrt{\left( c_i^{HLW} RSD_i^{Analysis} \right)^2 + \left( c_i^{HLW} RSD_i^{mix/samp} \right)^2}}{\sqrt{n^{samps}}} \quad (8)$$

where  $RSD_i^{Analysis}$  and  $RSD_i^{mix/samp}$  are the relative standard deviations for analysis of analyte  $i$  and mixing and sampling, and  $n^{samps}$  is the number of MFPV samples analyzed for analyte  $i$ . The analytical RSD's were derived from Dodd and Kaiser (2006) and are listed in Appendix B. The mixing and sampling RSD is 3.58% based on (Piepel et al. 2013).

Specific components and their levels of uncertainty are described below which are necessary for the computation of Eqn 7:

The MFPV volume will be obtained from the radar level measurement before and after waste addition. The standard deviation ( $s^V$ ) for waste volume is calculated from error propagation of two volume measurements as described in Appendix J of Vienna and Kim (2014). A normal probability distribution is assumed centered on the nominal volume with an  $s^V$  of 125 L.

The composition of GFC's are uncertain with near normal distributions of major components and skewed distributions of impurity concentrations (centered near zero with long positive tails). A PERT (or Beta) distribution was used to estimate the probability distribution of all GFC compositions (see Appendix L of Vienna and Kim 2014). Appendix C lists the minimum, maximum, and most likely concentration of components in each GFC (based on values reported in Table A-4 of Vienna and Kim 2014).

The mass of each GFC is determined by measurements of multiple (3) load cells on each weigh hopper in the Glass Former Storage Facility. A normal probability distribution centered on the nominal weight with a standard deviation ( $s^{GFCM}$ ) of 0.260 kg was used based on the results reported in Appendix K of Vienna and Kim 2014.

The natural log of melter decontamination factor –  $\ln \left[ \frac{1}{1-v_i} \right]$  was found to be near normal in distribution (Nelson 2013). However to avoid the non-physical option of greater  $v_i > 1$ , a PERT distribution in  $\ln \left[ \frac{1}{1-v_i} \right]$  with minimum, maximum, and most likely values are reported in Appendix D, based on the values reported by Nelson (2013).

The mass balance equation with parameter probability distributions was used in a Monte Carlo routine to generate 10,000 realizations of the target glass composition. The Microsoft Excel™ add-in RiskAmp™, version 4.90, was used to perform the calculations. For each glass composition realization, each of the properties and composition constraints listed in Section 3.1 were calculated. The half-width of each property distribution for the associated confidence level listed in Table 5 (95% confidence for PCT and nepheline formation, 90% confidence for all other properties) was as  $U_{\alpha}^{Comp}$ .

$$U_{comp}^{prop} = Q_{CL\%}^{prop} - Q_{50\%}^{prop} \text{ or } Q_{50\%}^{prop} - Q_{100-CL\%}^{prop} \quad (9)$$

where  $U_{comp}^{prop}$  = composition uncertainty for “prop”, i.e., uncertainty in predicted “prop” due to glass composition uncertainty (in property model units)  
 $Q_{CL\%}^{prop}$  = CL% [=100(1- $\alpha$ )] percentile of the distribution of 10,000 property values  
 $Q_{50\%}^{prop}$  = median predicted property value or CL% = 50% percentile of the distribution of 10,000 property values

Figure 3 shows an example of the probability distribution calculated by this method.

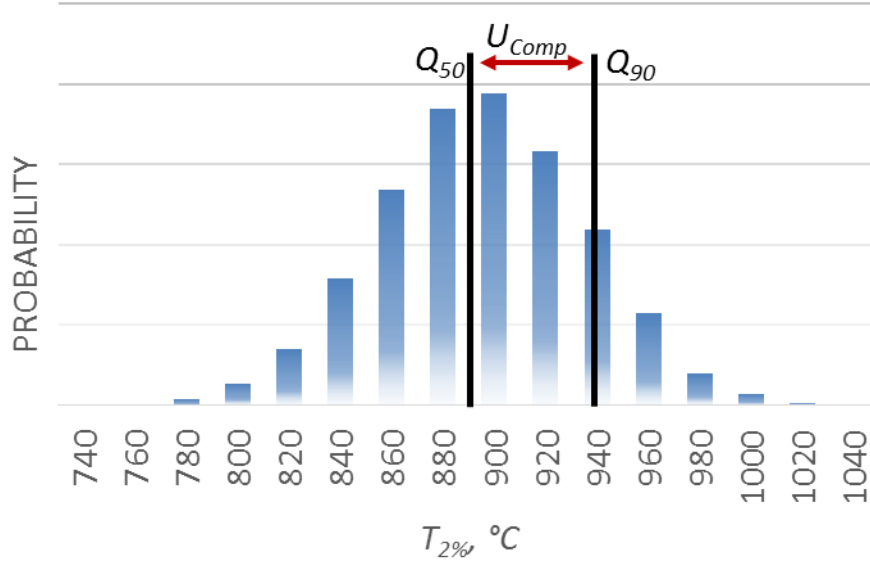


Figure 3. Example Histogram of Predicted  $T_{2\%}$  Values from a 10,000 Run Monte Carlo Calculation.

This process mimic's nearly exactly the Step 2 calculation used in Vienna and Kim 2014. The primary difference being the inclusion of MFPV heel (melter feed) was included in their calculation, but, not included in this study. This had the effect of slightly decreasing the calculated uncertainty in  $c_i^{HLW}$  in this study compared to that shown previously. To adjust for the decrease, the assumed number of MFPV samples was decreased. The initial calculations were performed with four MFPV samples (the nominal for plant operation). Calculations were then repeated assuming a single MFPV sample. The real impact of uncertainty is expected to lie between these two estimates. The values for both are reported in Section 6.4. Comparisons are drawn based on the average of the results from 1 and 4 samples.

#### 4.2.2 LAW Process/Composition Uncertainties

The process for estimating  $U_{\alpha}^{Comp}$  for LAW glass compositions follows very nearly the same as that for HLW (described in Section 4.2.1) with a few differences. The mass balance for each batch depends on volume and composition of waste in the CRV which is transferred to the MFPV instead of analysis of waste in the MFPV (see Figure 1). The LAW mass balance is given by:

$$g_i = \frac{\left[ c_i^{LAW} V^{LAW} f_i + \sum_{k=1}^{n^{GFCs}} g_{ik}^{oxide} M_k^{GFCin} \right] v_i}{\sum_{i=1}^{noxides} \left[ c_i^{LAW} V^{LAW} f_i + \sum_{k=1}^{n^{GFCs}} g_{ik}^{oxide} M_k^{GFCin} \right] v_i} \quad (10)$$

where:

- $g_i$  = mass fraction of  $i^{th}$  oxide in glass (g/g)
- $c_i^{LAW}$  = Concentration of the  $i^{th}$  component measured in samples from the CRV prior to transfer to the MFPV (g/mL)
- $V^{LAW}$  = Volume of LAW transferred in a batch to the MFPV (L)

$$\begin{aligned}
 f_i &= \text{A conversion factor from element mg to oxide kg (kg/mg)} \\
 g_{ik}^{oxide} &= \text{Mass fraction of the } i^{\text{th}} \text{ oxide in the } k^{\text{th}} \text{ GFC (g/g)} \\
 M_k^{GFCinMFPV} &= \text{Mass of the } k^{\text{th}} \text{ GFC in the MFPV batch (kg)} \\
 n^{GFCs} &= \text{Number of GFC's added to the MFPV batch} \\
 v_i &= \text{Fraction of } i^{\text{th}} \text{ oxide retained in the glass (g/g)}
 \end{aligned}$$

The values:  $c_i^{LAW}$ ,  $V^{LAW}$ ,  $g_{ik}^{oxide}$ ,  $M_k^{GFCinMFPV}$ , and  $v_i$  are each uncertain and each is given a probability distribution. The uncertainty on waste component concentration is estimated as a normal distribution centered on the average measured values (in this study the nominal value for the waste composition) and a standard deviation ( $s_i^{cLAW}$ ) is given by:

$$s_i^{cLAW} = \frac{\sqrt{(c_i^{LAW} RSD_i^{Analysis})^2 + (c_i^{LAW} RSD_i^{mix/samp})^2}}{\sqrt{n^{samps}}} \quad (11)$$

where  $RSD_i^{Analysis}$  and  $RSD_i^{mix/samp}$  are the relative standard deviations for analysis of analyte  $i$  and mixing and sampling, and  $n^{samps}$  is the number of CRV samples analyzed for analyte  $i$ . The analytical RSD's were derived from Dodd and Kaiser (2005) and are listed in Appendix B. The mixing and sampling RSD is 1.47% based on Petkus (2012). The  $n^{samps}$  for LAW is 3 per the sampling and analysis plan (Arakali and Johnson 2013).

Specific components and their levels of uncertainty are described below which are necessary for the computation of Eqn 10:

The LAW volume transferred from the CRV to the MFPV will be obtained from the radar level measurement before and after waste transfer from each vessel. The standard deviation ( $s^V$ ) for waste volume is calculated from error propagation of four volume measurements as described in Appendix D of Kim and Vienna (2012). A normal probability distribution is assumed centered on the nominal volume with an  $s^V$  of 447.2 L.

The composition of GFC's are uncertain with near normal distributions of major components and skewed distributions of impurity concentrations (centered near zero with long positive tails). A PERT (or Beta) distribution was used to estimate the probability distribution of all GFC compositions. Appendix C lists the minimum, maximum, and most likely concentration of components in each GFC (based on values reported in Table A-4 of Kim and Vienna 2012).

The mass of each GFC is determined by measurements of multiple (3) load cells on each weigh hopper in the Glass Former Storage Facility. A normal probability distribution centered on the nominal weight with a standard deviation ( $s^{GFCM}$ ) of 0.1039 kg for major components (>41.6 kg per batch) and 0.0520 kg for minor components (<41.6 kg per batch) was used based on the results reported in Appendix E of Kim and Vienna 2012.

The natural log of melter decontamination factor –  $\ln \left[ \frac{1}{1 - v_i} \right]$  was found to be near normal in distribution (Petkus and Vienna 2012). However to avoid the non-physical option of greater  $v_i > 1$ , a PERT distribution in  $\ln \left[ \frac{1}{1 - v_i} \right]$  with minimum, maximum, and most likely values reported in Appendix D, based on the values reported by Petkus and Vienna (2012).

The mass balance equation with parameter probability distributions was used in a Monte Carlo routine to generate 10,000 realizations of the target glass composition. The Microsoft Excel™ add-in RiskAmp™, version 4.90, was used to perform the calculations. For each glass composition realization, each of the properties and composition limits listed in Section 3.2 were calculated. The half-width of each property distribution for the associated confidence level (shown in Table 5) was as  $U_{\alpha}^{Comp}$ . This process is exactly the Step 1 calculation used in Kim and Vienna 2012.

### 4.3 Estimation of Individual Uncertainty Impacts on Glass

The impact of individual sources of uncertainty were estimated by systematically removing individual and combined sources of uncertainty and repeating the glass optimization to determine the resulting WOL and associated glass mass. The first three cases to be evaluated were:

- 1) no uncertainties
- 2) prediction uncertainties only (no composition/process uncertainties)
- 3) prediction plus composition/process uncertainties.

Then the prediction uncertainties for individual properties were removed one-at-a-time (e.g.,  $U_{T_{2\%}}^{Pred} = 0$ ,  $U_{VHT}^{Pred} = 0$ ,  $U_{nepheline}^{Pred} = 0$ , ...) until most of the glass mass increase caused by application of prediction uncertainties only was accounted for.

## 5.0 Waste Feeds

The waste feed estimate used for this study is from the *River Protection Project System Plan* revision 8 (SP8) (DOE 2017) which is required to estimate the impacts of the glass property models and constraints and associated uncertainties on glass to be produced at Hanford<sup>1</sup>. The base line case (Case #1) waste feed batches were used in this study. According to this case, 4008 batches of HLW are to be delivered from PT to HLW while 28,458 batches of LAW are planned to be delivered to supplemental LAW vitrification facilities, initially from a combined input of LAWPS (roughly 10 years) then from PT. Internal recycles of off gas scrub solution from ETF (first 10 years roughly) and LAWPS are included in the LAW feed estimates. The major component concentrations in waste are shown vs batch number in Figure 4 and Figure 5 for HLW and LAW, respectively.

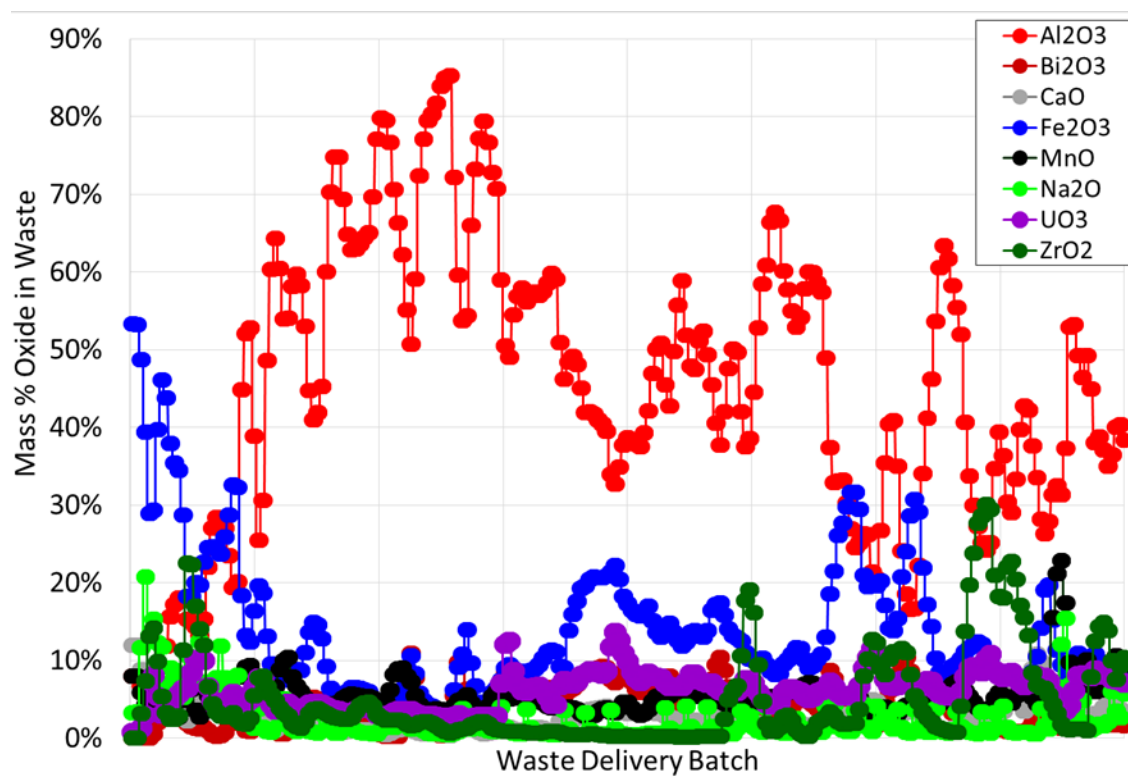


Figure 4. Plot of Major HLW Component Concentrations vs Batch Number (~4000 batches)

<sup>1</sup> The SP8 case 1 represents one of the current River Protection Project baseline flowsheets. The previous baseline flowsheet was documented in revision 6 of that report (SP6) case 1.

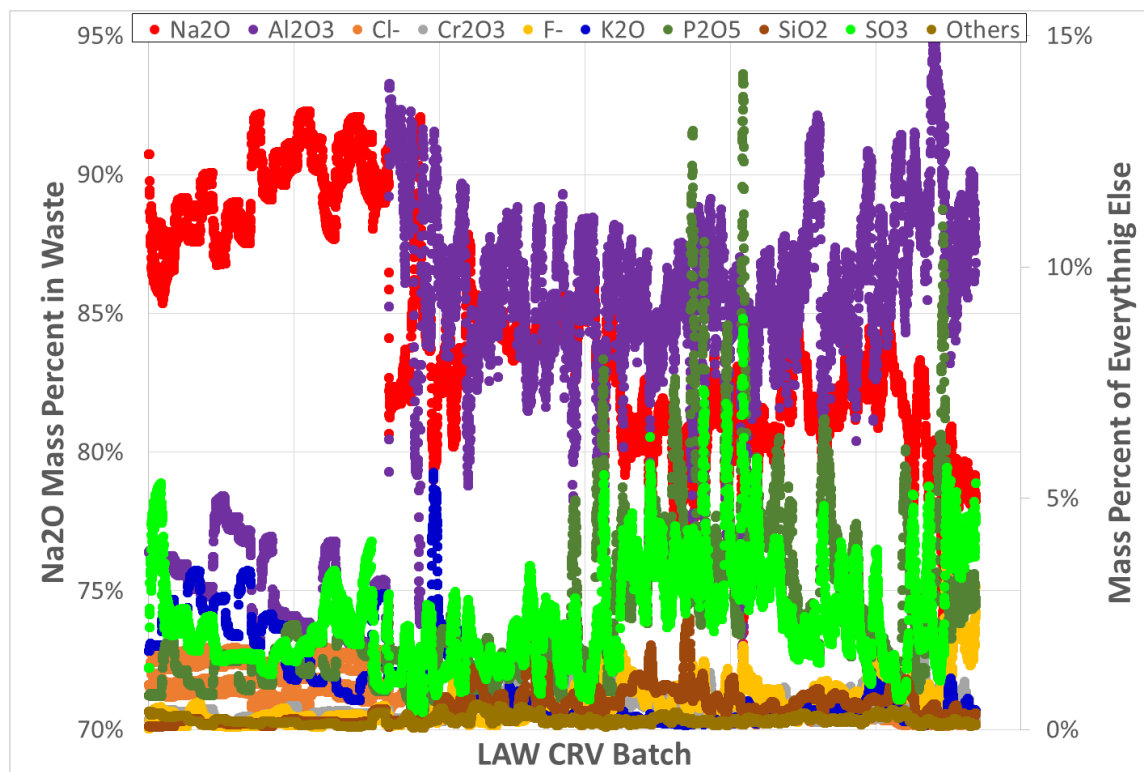


Figure 5. Plot of Major LAW Component Concentrations vs Batch Number (~28,500)

As the number of batches for both HLW and LAW exceed the amount that could be practically used in the calculations performed in this study, cluster analysis was used to group wastes of like composition into clusters. The mass weighted average composition of each cluster was then used to estimate the WOL (and associated glass mass) represented by each cluster. Hierarchical clustering was performed using JMP® statistical software (version 13.2.1, SAS Institute, Inc., Cary, NC).

For HLW waste batches clustering was performed on the mass fractions of the following 12 waste components:  $\text{Al}_2\text{O}_3$ ,  $\text{Bi}_2\text{O}_3$ ,  $\text{Cr}_2\text{O}_3$ ,  $\text{Fe}_2\text{O}_3$ ,  $\text{MnO}$ ,  $\text{Na}_2\text{O}$ ,  $\text{NiO}$ ,  $\text{P}_2\text{O}_5$ ,  $\text{SO}_3$ ,  $\text{ThO}_2$ ,  $\text{UO}_3$ , and  $\text{ZrO}_2$ . The number of clusters was varied from 15 to 50 and the resulting mean composition distance<sup>2</sup> was calculated (shown in Figure 6). Several plateaus around clusters 15, 18, 24, 30 and 34 are apparent in this analysis. Analyses of parallel plots of clusters at each of the plateaus suggested that 30 clusters would represent a good balance between few enough clusters for practical calculation and sufficient number of clusters to well represent the waste. The parallel plots for the 30 HLW cluster case is shown in Figure 7.

<sup>2</sup> Mean distance between each glass composition and the cluster center point.

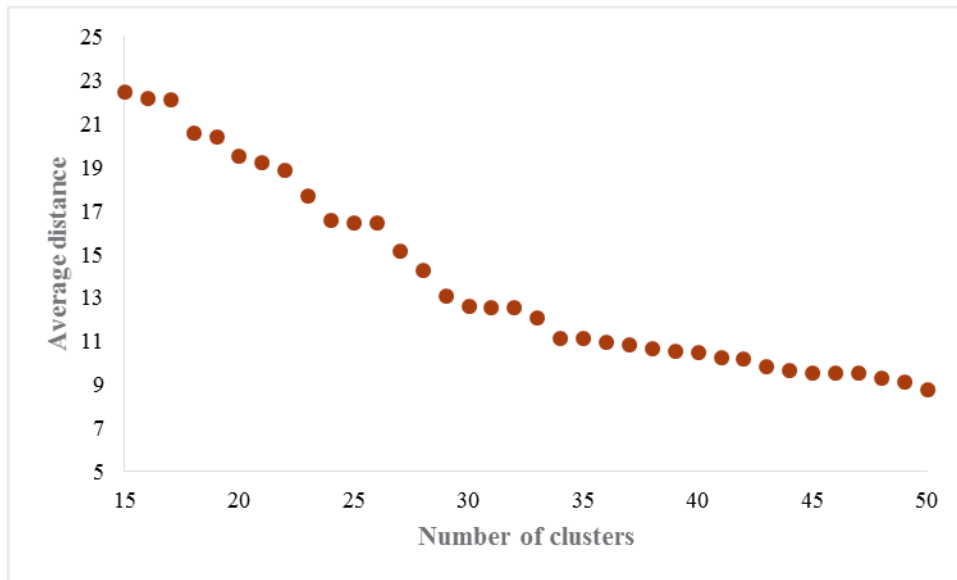
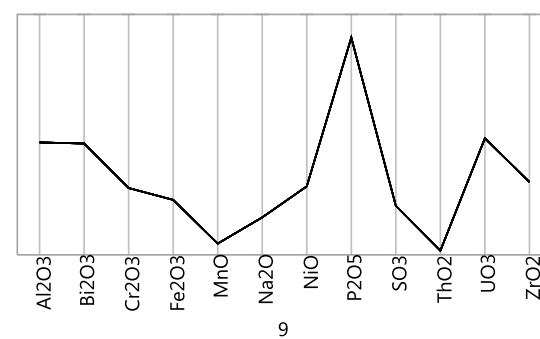
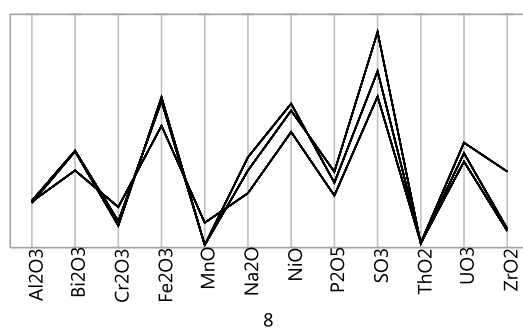
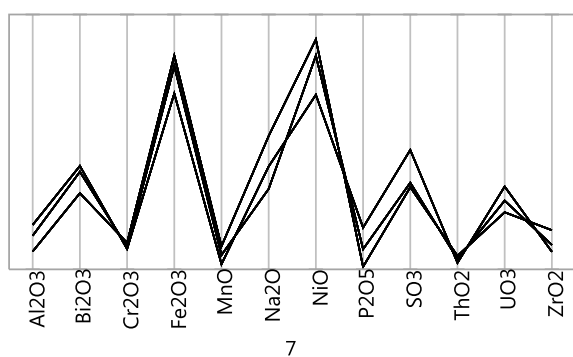
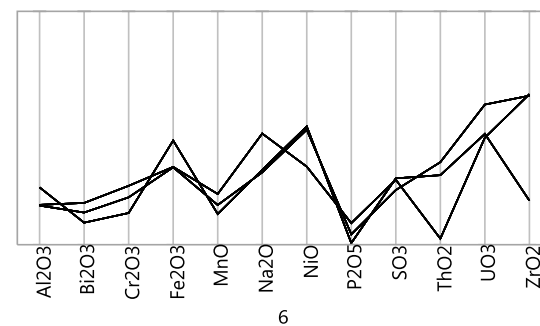
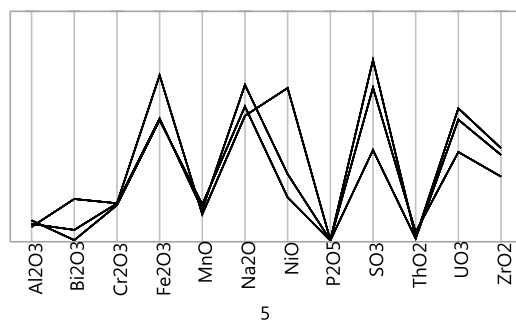
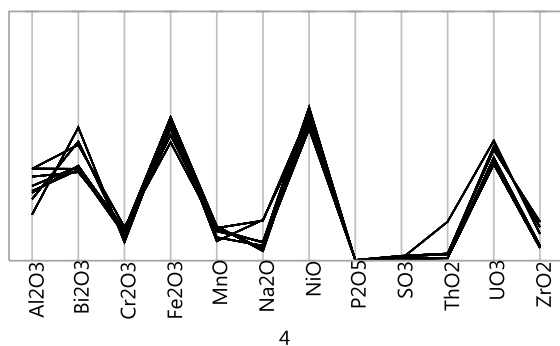
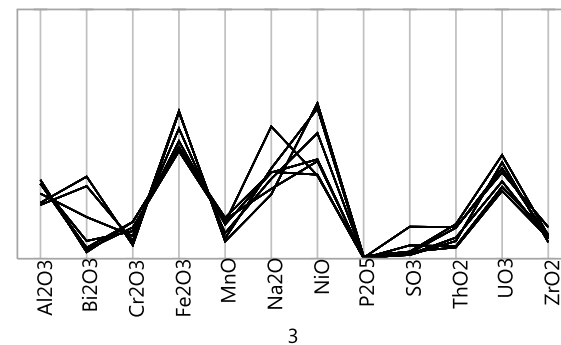
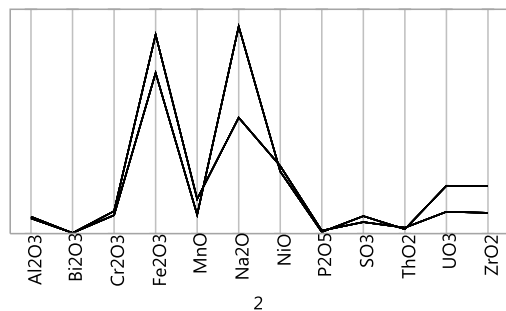
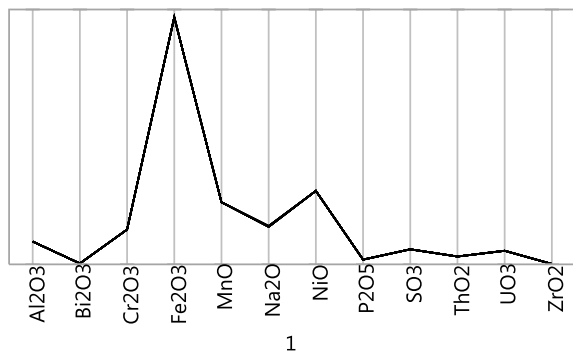
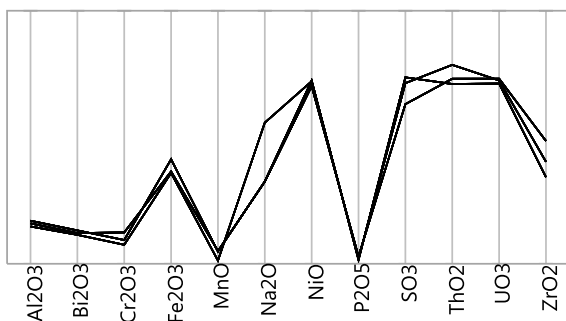
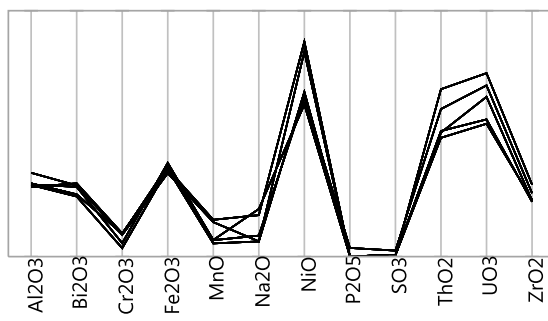


Figure 6. Average Distance versus Number of HLW Clusters from Hierarchical Cluster Analysis.

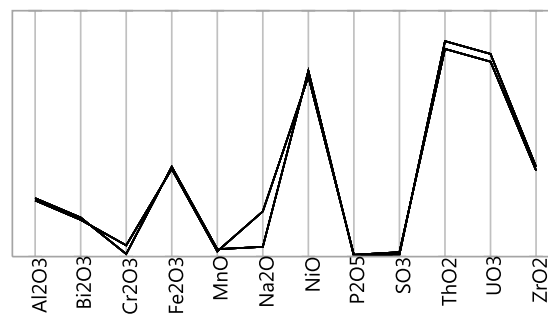




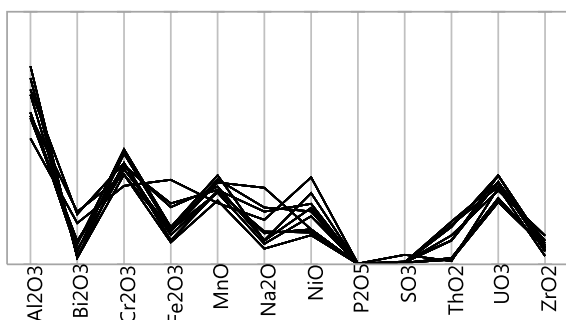
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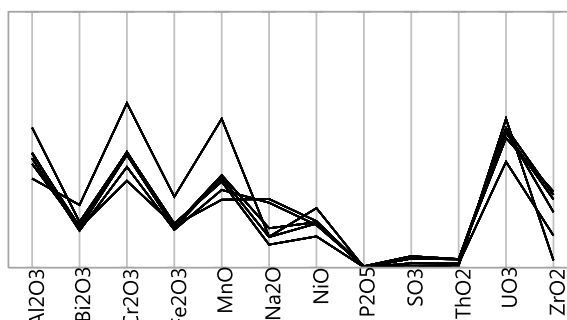
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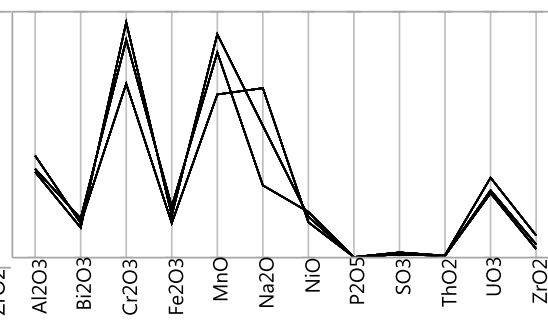
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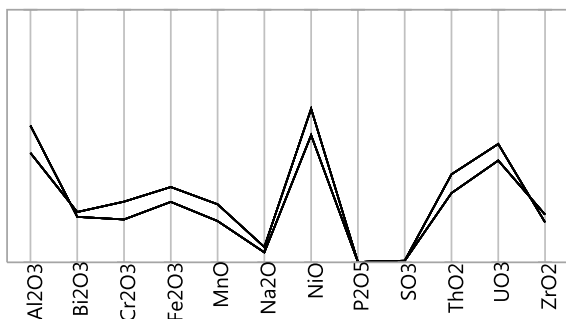
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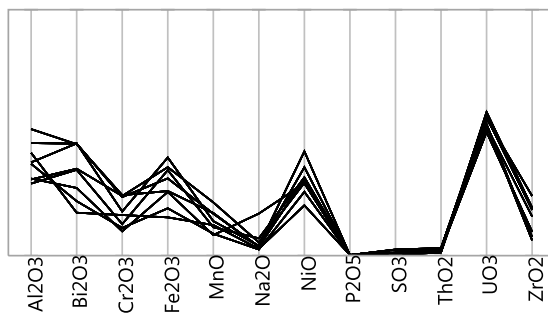
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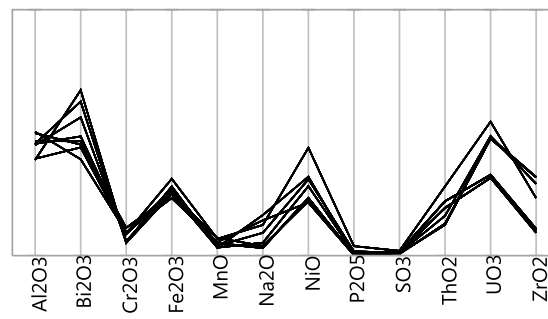
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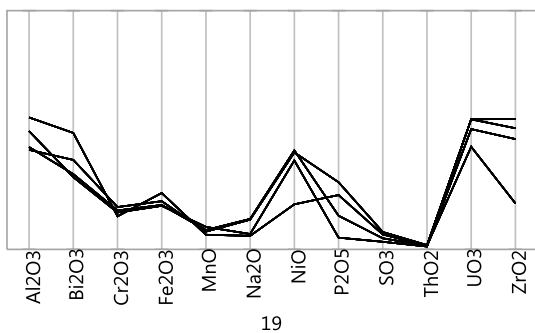
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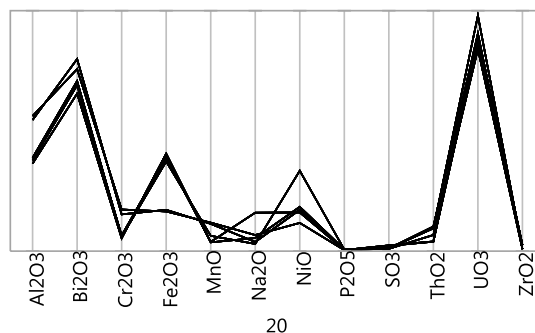
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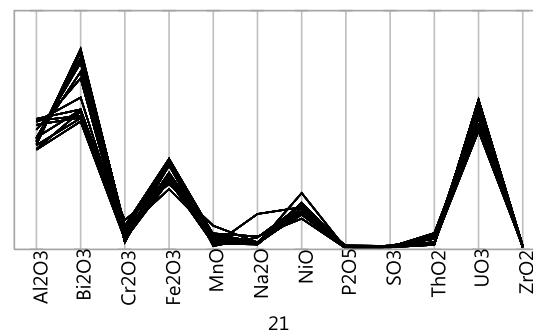
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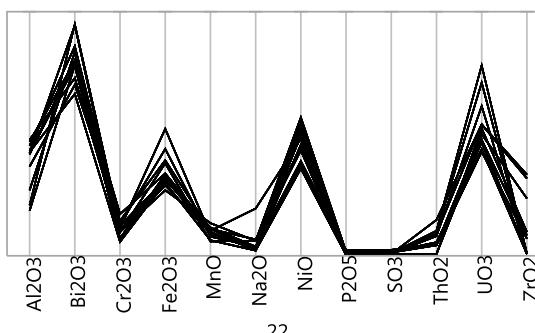
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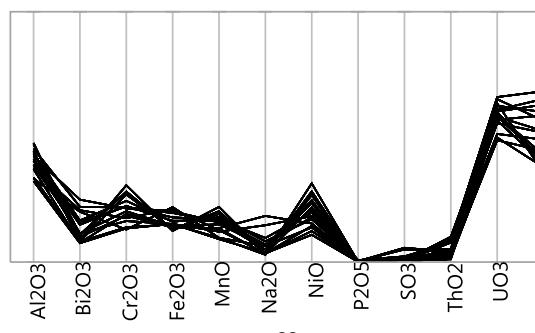
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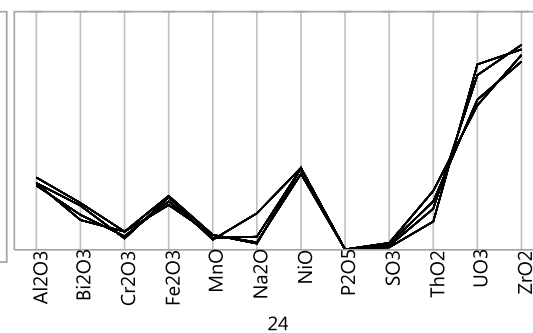
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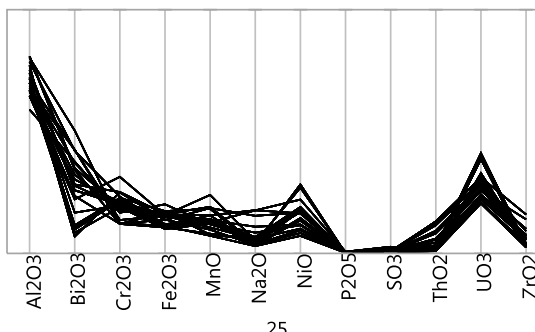
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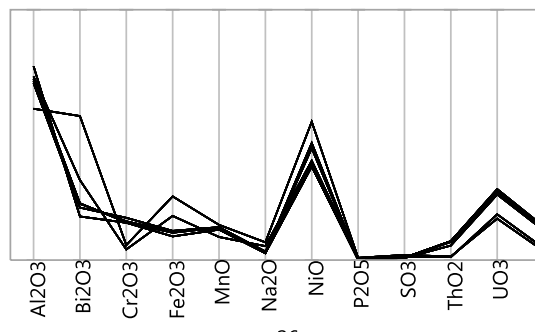
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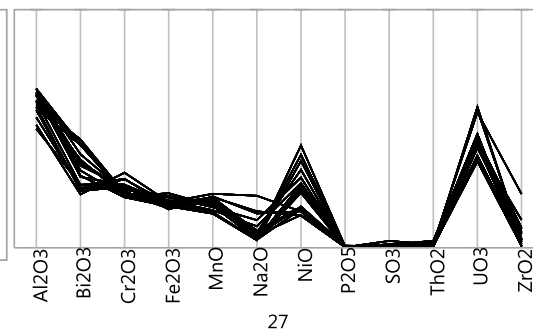
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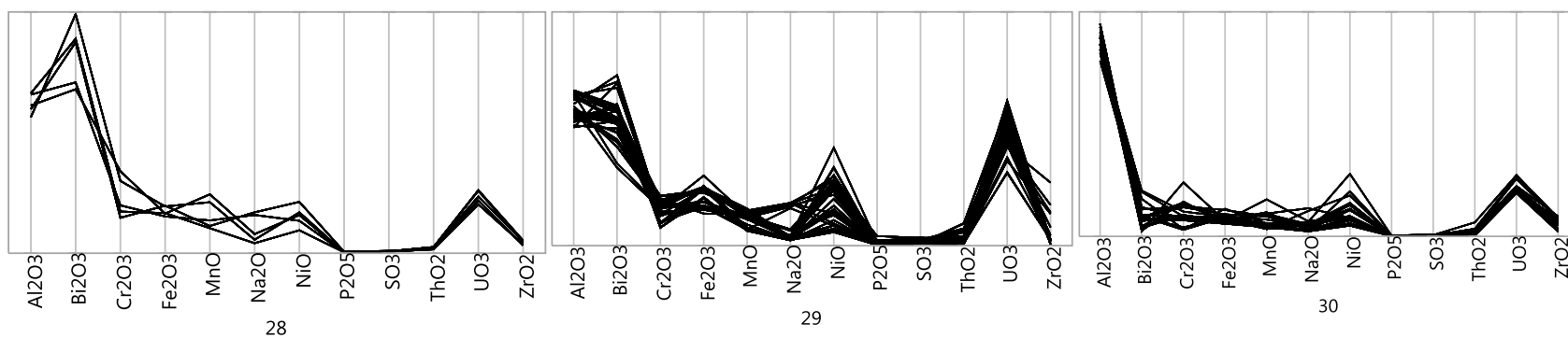


Figure 7. Parallel Plots of 30 HLW Composition Clusters

For LAW waste batches clustering was performed on the mass fractions of the following 8 waste components:  $\text{Al}_2\text{O}_3$ ,  $\text{Cl}^-$ ,  $\text{Cr}_2\text{O}_3$ ,  $\text{F}^-$ ,  $\text{K}_2\text{O}$ ,  $\text{Na}_2\text{O}$ ,  $\text{P}_2\text{O}_5$ , and  $\text{SO}_3$ . The number of clusters was varied from 15 to 50 and the resulting mean composition distance<sup>1</sup> was calculated (shown in Figure 8). Several plateaus around clusters 25, 36, 42 and 47 are apparent in this analysis. Analyses of parallel plots of clusters at each of the plateaus suggested that 36 clusters would represent a good balance between few enough clusters for practical calculation and sufficient number of clusters to well represent the waste. The parallel plots for the 36 LAW cluster case is shown in Figure 9.

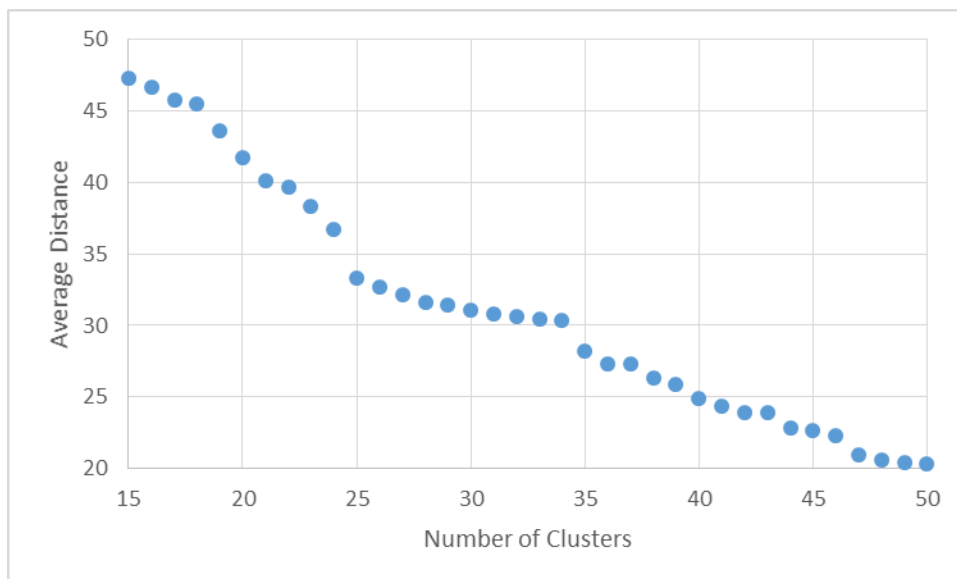
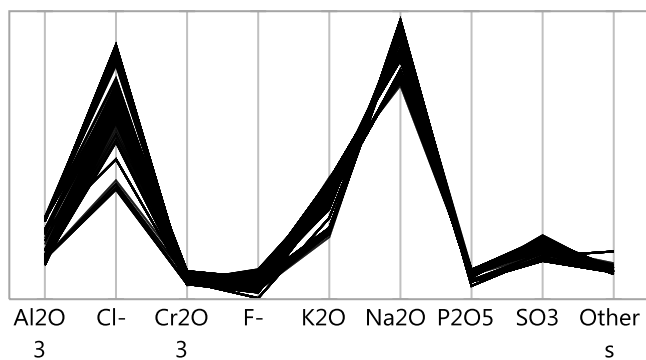


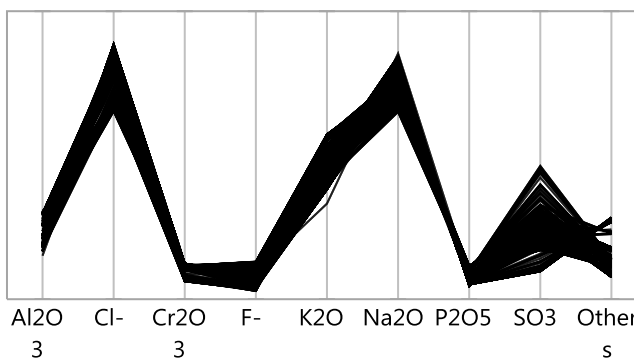
Figure 8. Average Distance versus Number of LAW Clusters from Hierarchical Cluster Analysis.

Attachment 1 lists the batch compositions and cluster number assignment for each batch of HLW and LAW feed. Also listed are the masses (of calcined oxide) and average composition of each cluster.

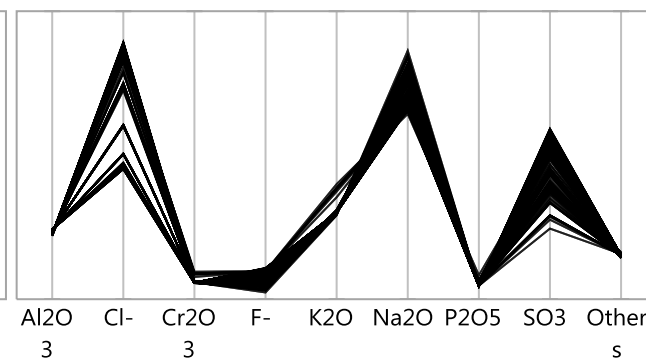
<sup>1</sup> Mean distance between each glass composition in the cluster to the cluster center point.



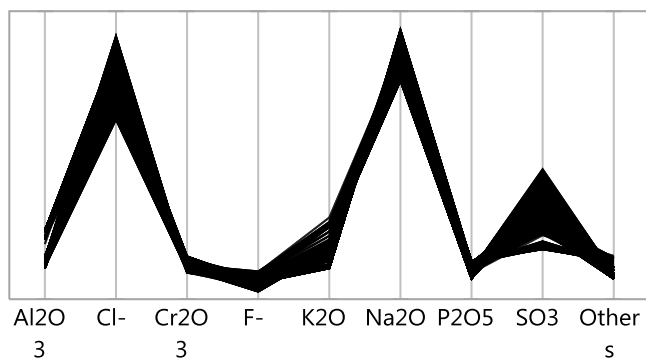
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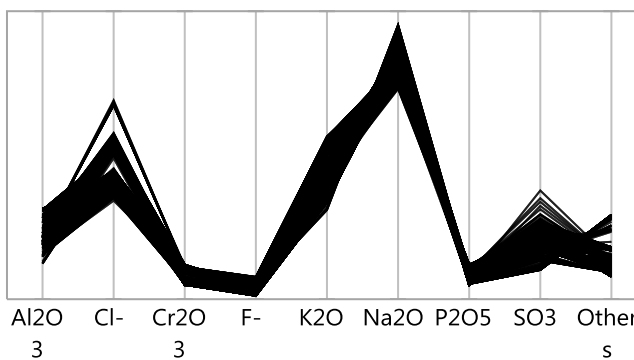
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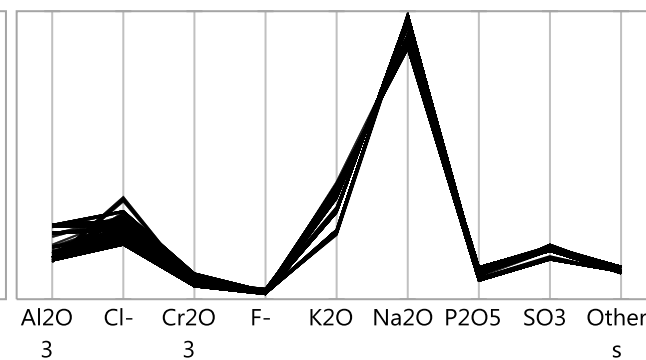
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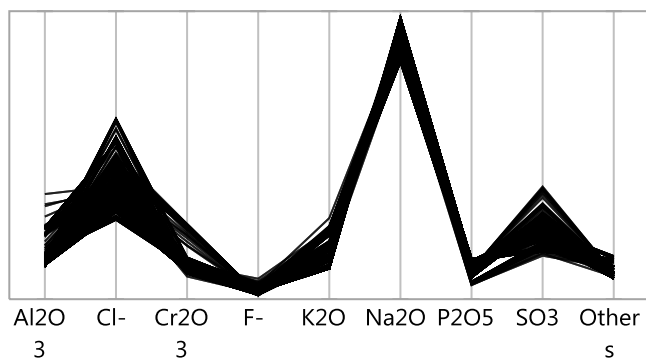
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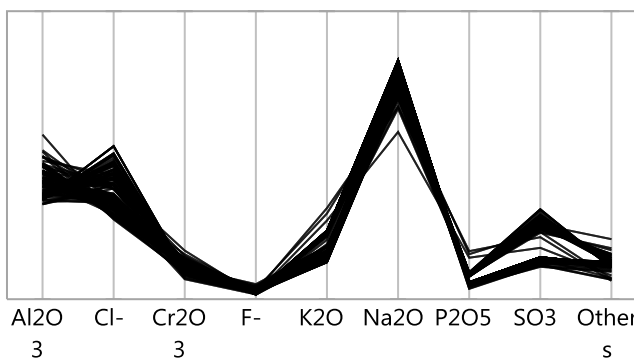
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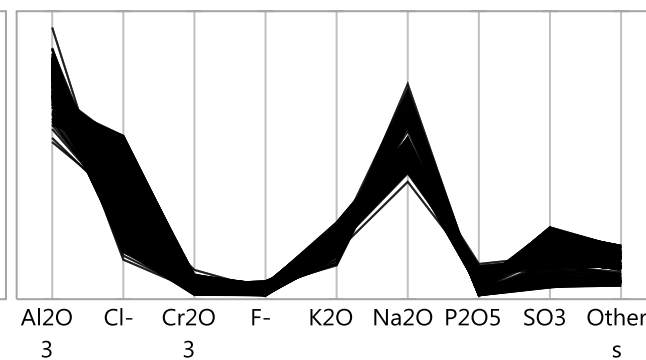
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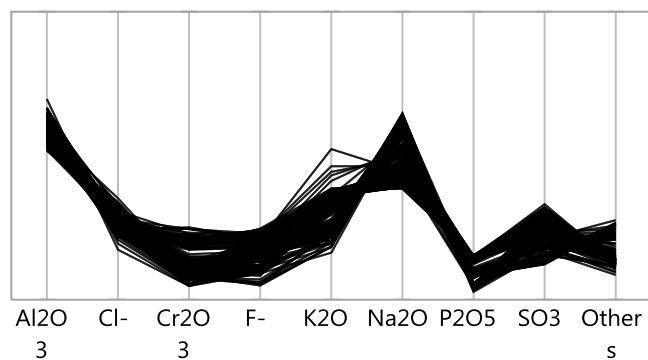
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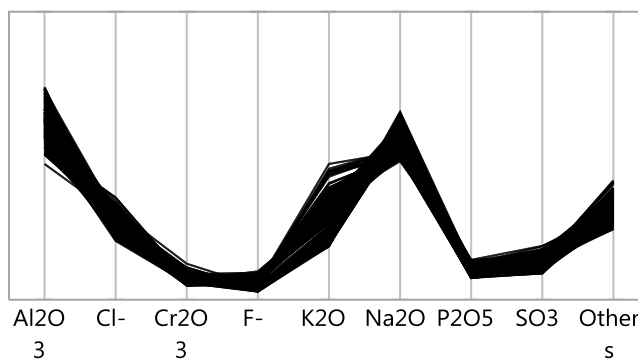
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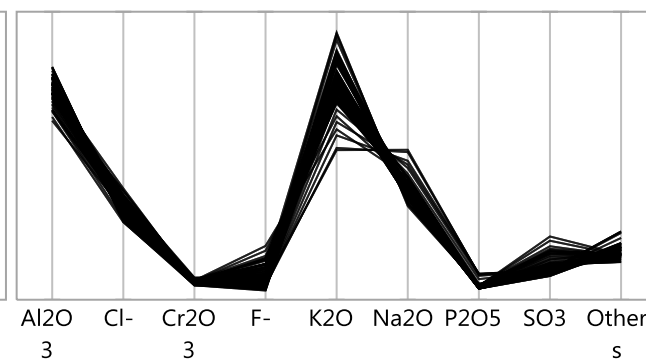
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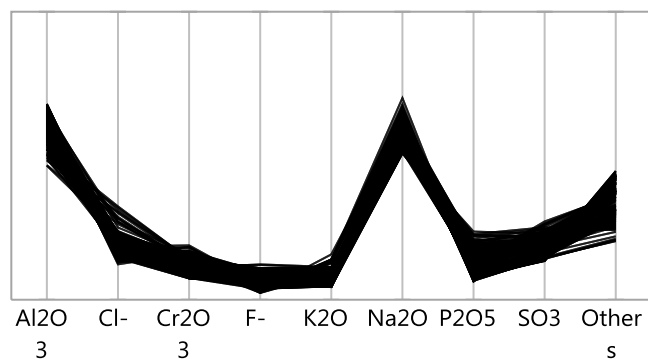
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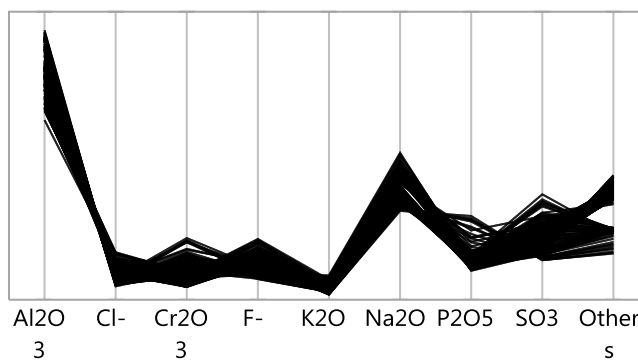
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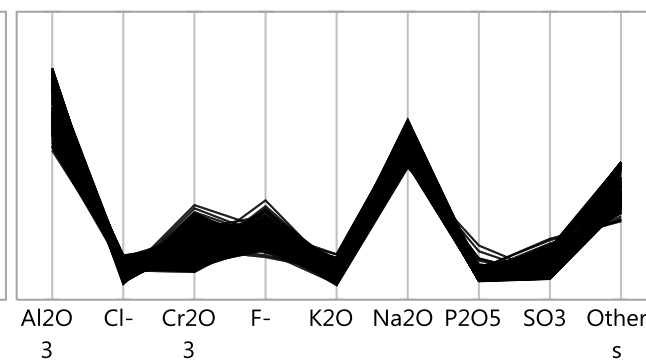
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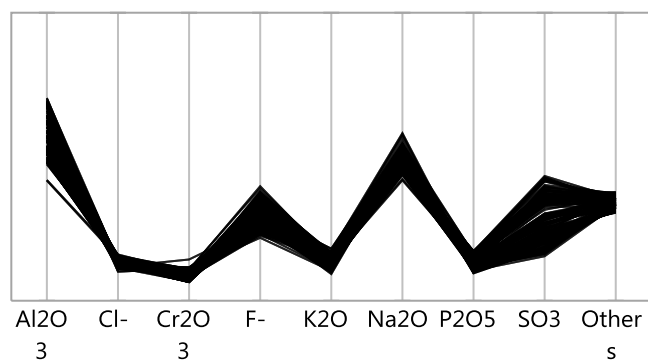
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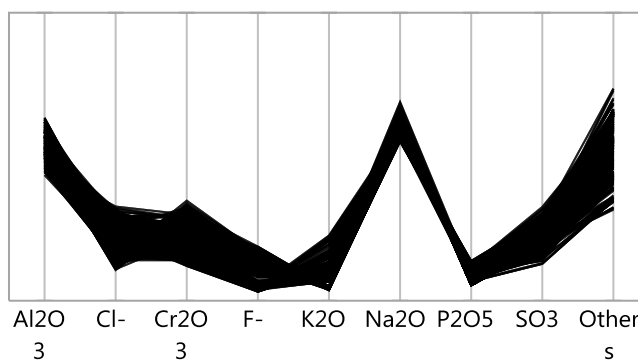
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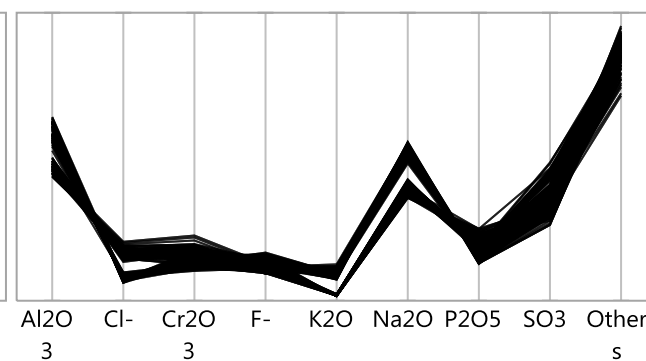
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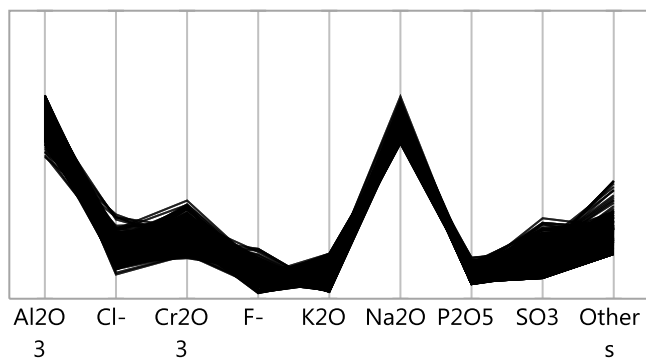
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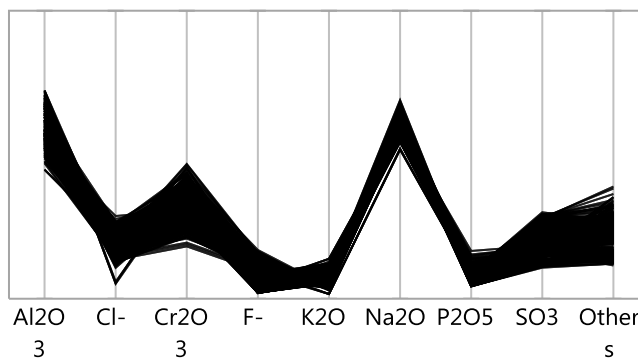
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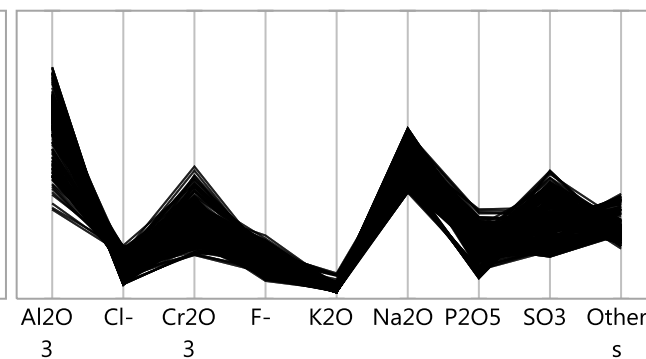
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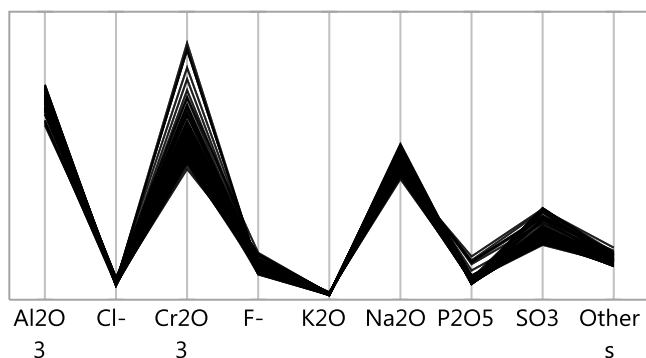
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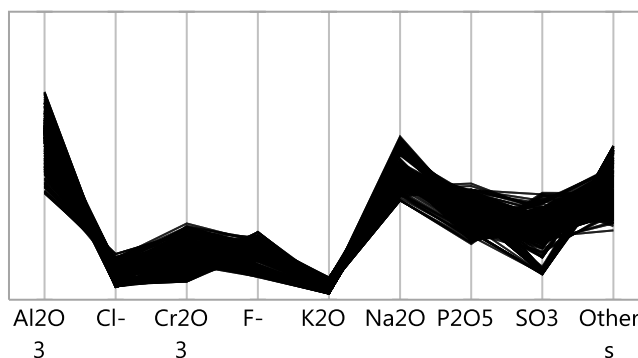
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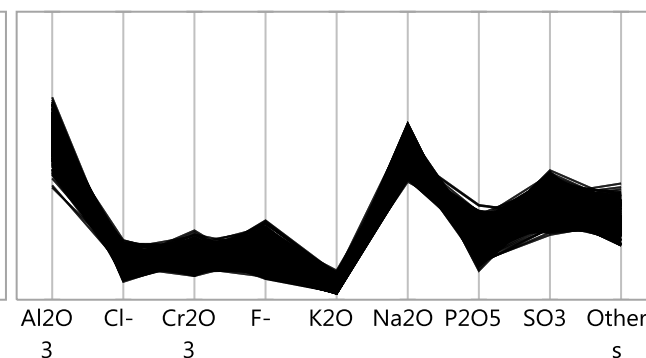
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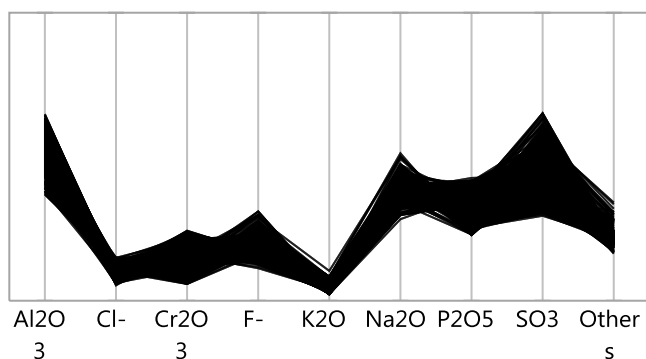
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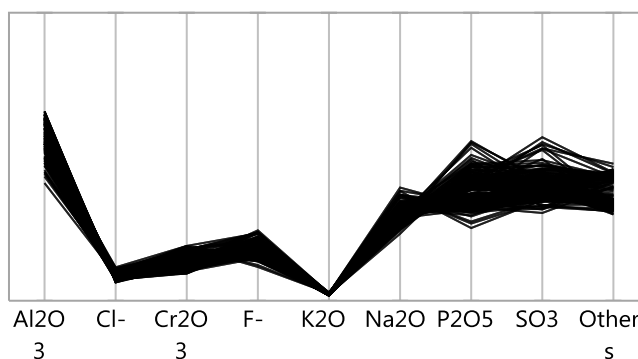
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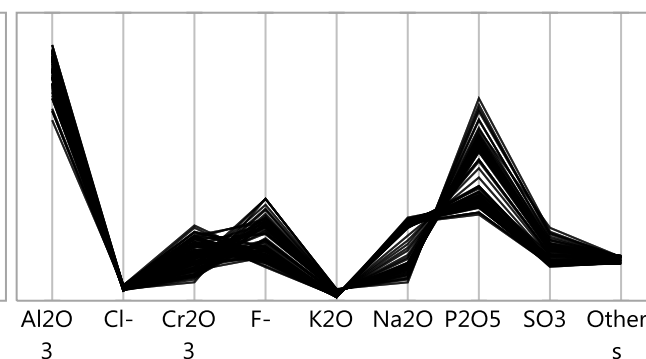
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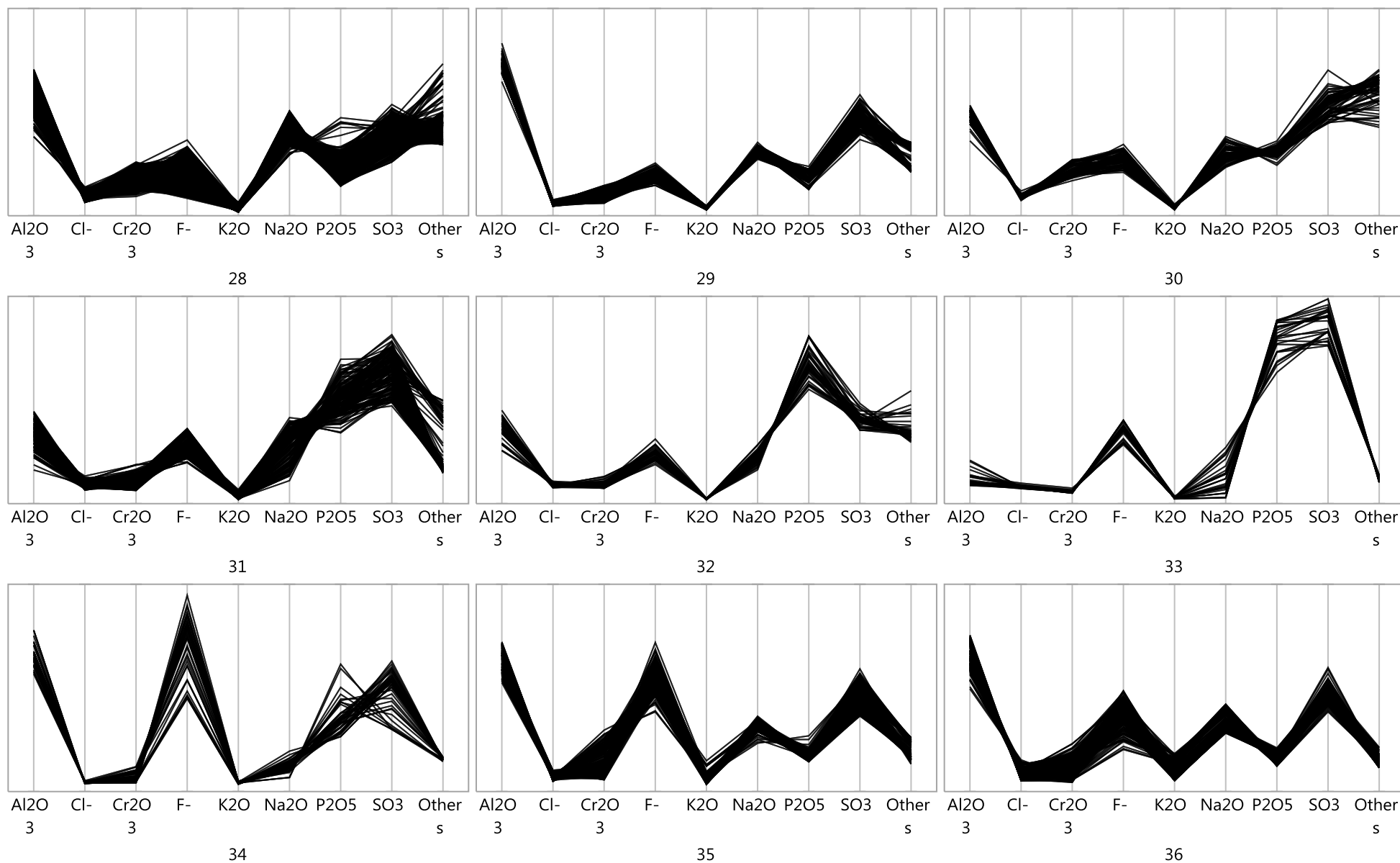


Figure 9. Parallel Coordinate Plots for 36 LAW Clusters.

## 6.0 HLW Calculation Results and Discussion

A series of calculations were performed to maximize the WOL for each HLW composition while simultaneously satisfying all of the HLW constraints listed in Section 3.1. If one of the property/composition constraints (Table 1) limits the WOL, the additive composition is adjusted to increase the loading until one or more additional constraints are met. Therefore, the WOL is limited by more than one constraint, unless a single component concentration constraint, typically, a model validity constraint (Table 2) for waste components (e.g.,  $\text{Fe}_2\text{O}_3$ ,  $\text{MnO}$ , or  $\text{Al}_2\text{O}_3$ ) is encountered. Some glasses with WOL limited by property/composition constraints may also be limited by a model validity constraint (Table 2) for additive components (e.g.,  $\text{B}_2\text{O}_3$ ,  $\text{Na}_2\text{O}$ , or  $\text{Li}_2\text{O}$ ).

Calculations were performed without any uncertainties for the 30 HLW feed composition clusters and described in Section 6.1. The impact of prediction uncertainties are discussed in Sections 6.2 and 6.3. Finally, the impacts of various composition/process uncertainties are discussed in Sections 6.4 and 6.5.

### 6.1 No Uncertainties

The maximum WOL for each of the 30 waste clusters was determined and reported in Table 6. Using the constraints and models reported by Vienna et al. (2016), 23,360 MT of HLW glass would be produced (7735 canisters, assuming 3.02 MT of glass per canister). The glass is most limited by viscosity,  $T_2\%$ , and nepheline with a lower fraction limited by single component (Al, Fe and Mn) constraints (12 wt%) (Figure 10). For comparison, 100% of the *River Protection Project System Plan* revision 6 wastes were limited by single component constraints using the WTP baseline models and constraints (Certa et al. 2011).

Table 6. Waste Mass, Maximum WOL, Glass Mass, and Limiting Factors for each of 30 HLW Clusters with No Uncertainties

| Cluster | Waste oxides, kg | WOL, wt% | Glass, MT | Limits(a)  |
|---------|------------------|----------|-----------|------------|
| 1       | 102,015          | 37.4     | 272.5     | Max Fe     |
| 2       | 93,314           | 45.1     | 206.8     | Max Fe     |
| 3       | 304,764          | 49.6     | 614.5     | T2,Vis,NP  |
| 4       | 340,138          | 45.0     | 756.1     | T2,Vis,NP  |
| 5       | 118,988          | 52.1     | 228.2     | T2,Vis,B   |
| 6       | 130,884          | 49.6     | 263.7     | T2,Vis,NP  |
| 7       | 129,640          | 44.7     | 290.1     | T2,Vis,Na  |
| 8       | 135,350          | 49.1     | 275.6     | T2,Vis,NP  |
| 9       | 40,217           | 42.8     | 94.0      | TZr,Vis,NP |
| 10      | 137,773          | 54.1     | 254.7     | T2,Vis,NP  |
| 11      | 229,181          | 49.3     | 464.7     | T2,Vis,NP  |
| 12      | 96,641           | 52.0     | 185.7     | T2,Vis,NP  |
| 13      | 414,412          | 42.4     | 977.3     | T2,Vis,B   |
| 14      | 226,581          | 48.3     | 469.5     | T2,Vis     |

| Cluster | Waste oxides, kg | WOL, wt% | Glass, MT | Limits(a)    |
|---------|------------------|----------|-----------|--------------|
| 15      | 102,370          | 39.0     | 262.4     | Max Mn       |
| 16      | 89,071           | 43.9     | 203.1     | T2,Visc,B    |
| 17      | 334,869          | 50.8     | 659.1     | T2,Vis       |
| 18      | 376,435          | 50.5     | 746.1     | T2,Vis       |
| 19      | 178,911          | 40.1     | 446.5     | TZr,Vis,NP,B |
| 20      | 228,853          | 48.8     | 469.3     | T2,Vis       |
| 21      | 710,511          | 47.7     | 1,489.9   | T2,Vis,B     |
| 22      | 546,626          | 47.6     | 1,148.9   | T2,Vis,NP    |
| 23      | 709,324          | 42.3     | 1,677.2   | TZr,Vis,NP   |
| 24      | 196,576          | 42.0     | 467.9     | T2,Vis,NP    |
| 25      | 979,245          | 43.5     | 2,251.2   | T2,NP,B      |
| 26      | 276,233          | 41.8     | 660.3     | T2,Vis       |
| 27      | 784,370          | 43.7     | 1,793.9   | T2,Vis,B     |
| 28      | 220,037          | 44.2     | 497.3     | T2,Vis,B     |
| 29      | 1,388,456        | 46.0     | 3,020.4   | T2,Vis       |
| 30      | 841,474          | 38.0     | 2,213.7   | Max Al       |
| Sum(b)  | 10,463,259       | 44.8     | 23,360    |              |

(a) limiting factors include: Max Fe ( $g_{Fe_2O_3} = 20\text{wt}\%$ ), T2 ( $T_{2\%} = 950^\circ\text{C}$ ), Vis ( $\eta_{1150} = 2 \text{ or } 8 \text{ Pa}\cdot\text{s}$ ), NP (nepheline probability = 30%), TZr ( $T_L\text{-Zr} = 1050^\circ\text{C}$ ), Max Mn ( $g_{MnO} = 8 \text{ wt}\%$ ), Max Al ( $g_{Al_2O_3} = 30 \text{ wt}\%$ ). B (model validity,  $g_{B_2O_3} = 4 - 22 \text{ wt}\%$ ), Na (model validity,  $g_{Na_2O} = 4.1 - 24 \text{ wt}\%$ ).  
(b) sum for waste oxide mass and glass mass, weighted average for WOL.

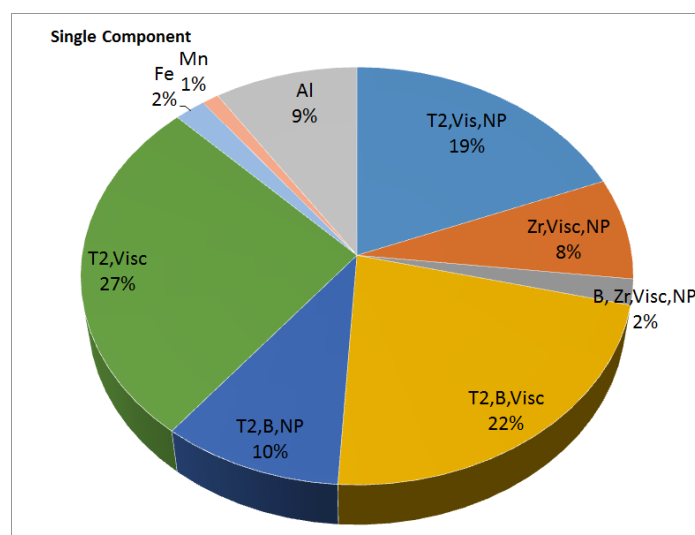


Figure 10. Waste Loading Limiting Factors (Glass Mass Basis) for HLW Glasses.

## 6.2 Prediction Uncertainties Only

The waste estimates were performed using the prediction uncertainties (as described in Section 4.1). The results are summarized in Table 7. The total glass mass produced is 23,963 MT, 2.58 relative percent higher than the case without any uncertainties. Generally, the waste loading limiting factors were the same as in the no uncertainty case. Exceptions include:

- Clusters 9 was limited by TZr, viscosity and nepheline with no uncertainty, with prediction uncertainties there are limitations by TZr, viscosity, nepheline and boron;
- Clusters 14, 18, 20 and 29 were limited by T2 and viscosity without uncertainty, with prediction uncertainties there are limitations by T2, viscosity and boron;
- Clusters 13 and 27 were limited by T2, boron and viscosity with no uncertainty, with prediction uncertainties there are limitations by T2 and viscosity only;
- Cluster 17 was limited by T2 and viscosity without uncertainty, is limited by T2, viscosity and nepheline with prediction uncertainties;
- Cluster 26 was limited by T2 and viscosity with no uncertainty, is limited by T2, viscosity and nepheline with prediction uncertainties.

Table 7. Waste Mass, Maximum WOL, Glass Mass, and Limiting Factors for 30 HLW Clusters with Prediction Uncertainties

| Cluster | Waste oxides, kg | WOL, wt% | Glass, MT | Limits(a)    |
|---------|------------------|----------|-----------|--------------|
| 1       | 102,015          | 37.4     | 272.5     | Max Fe       |
| 2       | 93,314           | 45.1     | 206.8     | Max Fe       |
| 3       | 304,764          | 48.6     | 626.9     | T2,Vis,NP    |
| 4       | 340,138          | 44.1     | 770.7     | T2,Vis,NP    |
| 5       | 118,988          | 51.0     | 233.2     | T2,Vis,B     |
| 6       | 130,884          | 48.4     | 270.3     | T2,Vis,NP    |
| 7       | 129,640          | 43.7     | 296.8     | T2,Vis,Na    |
| 8       | 135,350          | 48.2     | 280.5     | T2,Vis,NP    |
| 9       | 40,217           | 40.7     | 98.9      | TZr,Vis,NP,B |
| 10      | 137,773          | 52.9     | 260.6     | T2,Vis,NP    |
| 11      | 229,181          | 48.2     | 475.7     | T2,Vis,NP    |
| 12      | 96,641           | 51.0     | 189.5     | T2,Vis,NP    |
| 13      | 414,412          | 41.3     | 1,003.8   | T2,Vis       |
| 14      | 226,581          | 46.9     | 483.2     | T2,Vis,B     |
| 15      | 102,370          | 39.0     | 262.4     | Max Mn       |
| 16      | 89,071           | 42.7     | 208.6     | T2,Visc,B    |
| 17      | 334,869          | 49.8     | 672.8     | T2,Vis,NP    |
| 18      | 376,435          | 49.3     | 763.8     | T2,Vis,B     |
| 19      | 178,911          | 37.6     | 475.3     | TZr,Vis,NP,B |
| 20      | 228,853          | 47.7     | 480.0     | T2,Vis,B     |
| 21      | 710,511          | 46.6     | 1,525.9   | T2,Vis,B     |
| 22      | 546,626          | 46.4     | 1,177.7   | T2,Vis,NP    |
| 23      | 709,324          | 39.8     | 1,783.8   | TZr,Vis,NP   |

| Cluster                                                                                                                                                                                                                                                                                                                                                                                                                                                          | Waste oxides, kg | WOL, wt% | Glass, MT | Limits(a) |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------|----------|-----------|-----------|
| 24                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 196,576          | 40.2     | 489.4     | T2,Vis,NP |
| 25                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 979,245          | 42.3     | 2,314.5   | T2,NP,B   |
| 26                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 276,233          | 40.7     | 679.2     | T2,Vis,NP |
| 27                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 784,370          | 42.7     | 1,838.5   | T2,Vis    |
| 28                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 220,037          | 43.0     | 511.5     | T2,Vis,B  |
| 29                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 1,388,456        | 44.8     | 3,096.6   | T2,Vis,B  |
| 30                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 841,474          | 38.0     | 2,213.8   | Max Al    |
| Sum(b)                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 10,463,259       | 43.7     | 23,963.2  |           |
| (a) limiting factors include: Max Fe ( $g_{Fe_2O_3} = 20\text{wt}\%$ ), T2 ( $T_{2\%} = 950^\circ\text{C}$ ), Vis ( $\eta_{1150} = 2 \text{ or } 8 \text{ Pa}\cdot\text{s}$ ), NP (nepheline probability = 30%), TZr ( $T_{L-Zr} = 1050^\circ\text{C}$ ), Max Mn ( $g_{MnO} = 8 \text{ wt}\%$ ), Max Al ( $g_{Al_2O_3} = 30 \text{ wt}\%$ ). B (model validity, $g_{B_2O_3} = 4 - 22 \text{ wt}\%$ ), Na (model validity, $g_{Na_2O} = 4.1 - 24 \text{ wt}\%$ ). |                  |          |           |           |
| (b) sum for waste oxide mass and glass mass, weighted average for WOL.                                                                                                                                                                                                                                                                                                                                                                                           |                  |          |           |           |

### 6.3 Evaluation of Individual Property Prediction Uncertainties

With a roughly 2.58 relative percent increase in predicted HLW glass mass due to the application of prediction uncertainties, a study was performed to determine which prediction uncertainties had the most significant impact on glass mass. Table 8 shows the glass masses resulting from excluding individual prediction uncertainties one-at-a-time while all other prediction uncertainties were applied. Excluding the  $T_{2\%}$  prediction uncertainties had the strongest effect with RPD of -1.67% followed by -0.36% for  $T_{L-Zr}$ , -0.30% for nepheline, and -0.13% for viscosity.

Table 8. HLW Glass Masses Generated by Individually Excluding Prediction Uncertainties for Various Properties

| Cluster | No Uncertainties | Prediction Uncertainties all properties | Prediction Uncertainties No $\eta$ | Prediction Uncertainties No $T_{2\%}$ | Prediction Uncertainties No NP | Prediction Uncertainties No $T_{L-Zr}$ |
|---------|------------------|-----------------------------------------|------------------------------------|---------------------------------------|--------------------------------|----------------------------------------|
| 1       | 272.5            | 272.5                                   | 272.5                              | 272.5                                 | 272.5                          | 272.5                                  |
| 2       | 206.8            | 206.8                                   | 206.8                              | 206.8                                 | 206.8                          | 206.8                                  |
| 3       | 614.5            | 626.9                                   | 625.9                              | 617.1                                 | 625.2                          | 626.9                                  |
| 4       | 756.1            | 770.7                                   | 769.5                              | 759.4                                 | 768.7                          | 770.7                                  |
| 5       | 228.2            | 233.2                                   | 232.4                              | 229.1                                 | 233.2                          | 233.2                                  |
| 6       | 263.7            | 270.3                                   | 269.8                              | 265.1                                 | 269.2                          | 270.3                                  |
| 7       | 290.1            | 296.8                                   | 296.2                              | 290.7                                 | 296.8                          | 296.8                                  |
| 8       | 275.6            | 280.5                                   | 280.0                              | 277.2                                 | 279.4                          | 280.5                                  |
| 9       | 94.0             | 98.9                                    | 98.8                               | 98.9                                  | 97.2                           | 96.0                                   |
| 10      | 254.7            | 260.6                                   | 260.0                              | 256.3                                 | 259.4                          | 260.6                                  |
| 11      | 464.7            | 475.7                                   | 474.7                              | 466.0                                 | 474.6                          | 475.7                                  |
| 12      | 185.7            | 189.5                                   | 189.1                              | 186.3                                 | 189.0                          | 189.5                                  |
| 13      | 977.3            | 1,003.8                                 | 1,002.4                            | 978.8                                 | 1,003.8                        | 1,003.8                                |
| 14      | 469.5            | 483.2                                   | 482.4                              | 470.1                                 | 483.2                          | 483.2                                  |

| Cluster | No<br>Uncertainties | Prediction<br>Uncertainties<br>all properties | Prediction<br>Uncertainties<br>No $\eta$ | Prediction<br>Uncertainties<br>No T <sub>2</sub> % | Prediction<br>Uncertainties<br>No NP | Prediction<br>Uncertainties<br>No T <sub>L</sub> -Zr |
|---------|---------------------|-----------------------------------------------|------------------------------------------|----------------------------------------------------|--------------------------------------|------------------------------------------------------|
| 15      | 262.4               | 262.4                                         | 262.4                                    | 262.4                                              | 262.4                                | 262.4                                                |
| 16      | 203.1               | 208.6                                         | 208.3                                    | 203.4                                              | 208.6                                | 208.6                                                |
| 17      | 659.1               | 672.8                                         | 672.0                                    | 659.7                                              | 672.7                                | 672.7                                                |
| 18      | 746.1               | 763.8                                         | 762.8                                    | 746.9                                              | 763.8                                | 763.8                                                |
| 19      | 446.5               | 475.3                                         | 474.5                                    | 475.3                                              | 463.5                                | 458.1                                                |
| 20      | 469.3               | 480.0                                         | 479.1                                    | 469.9                                              | 480.0                                | 480.0                                                |
| 21      | 1,489.9             | 1,525.9                                       | 1,523.7                                  | 1,492.2                                            | 1,525.9                              | 1,525.9                                              |
| 22      | 1,148.9             | 1,177.7                                       | 1,175.8                                  | 1,150.3                                            | 1,177.1                              | 1,177.7                                              |
| 23      | 1,677.2             | 1,783.8                                       | 1,777.4                                  | 1,783.8                                            | 1,746.0                              | 1,716.8                                              |
| 24      | 467.9               | 489.4                                         | 488.6                                    | 484.1                                              | 488.0                                | 489.4                                                |
| 25      | 2,251.2             | 2,314.5                                       | 2,314.5                                  | 2,264.0                                            | 2,303.8                              | 2,314.5                                              |
| 26      | 660.3               | 679.2                                         | 678.8                                    | 663.2                                              | 679.1                                | 679.2                                                |
| 27      | 1,793.9             | 1,838.5                                       | 1,836.0                                  | 1,796.7                                            | 1,838.5                              | 1,838.5                                              |
| 28      | 497.3               | 511.5                                         | 510.9                                    | 498.1                                              | 511.5                                | 511.5                                                |
| 29      | 3,020.4             | 3,096.6                                       | 3,092.3                                  | 3,025.1                                            | 3,096.6                              | 3,096.6                                              |
| 30      | 2,213.7             | 2,213.8                                       | 2,213.8                                  | 2,213.7                                            | 2,213.8                              | 2,213.8                                              |
| Sum     | 23,360              | 23,963                                        | 23,931                                   | 23,563                                             | 23,890                               | 23,876                                               |

## 6.4 Prediction and Composition/Process Uncertainties

The HLW waste estimates were performed using both prediction uncertainties (as described in Section 4.1) and composition/process uncertainties (as described in Section 4.2.1). The results are summarized in Table 9. The total glass masses produced are 24,703 MT and 24,359 MT for combined uncertainties if one or four MFPV samples are analyzed, respectively. The average glass mass (used for comparisons later in the report) is 24,531 MT. The average is 5.01 relative percent higher than the no uncertainty case and therefore composition uncertainties account for 2.43 relative percent increase in glass mass (the remaining 2.58% from prediction uncertainties). Generally, the waste loading limiting factors were the same as in the no uncertainty case. Exceptions include:

- Cluster 9 limited by TZr, viscosity and nepheline with no uncertainty and limited by TZr, viscosity, nepheline and boron with prediction and composition uncertainties;
- Cluster 13 limited by T2, boron and viscosity with no uncertainty and limited only by T2 and viscosity with prediction and composition/process uncertainties;
- Cluster 17 limited by T2 and viscosity with no uncertainty and limited by T2, viscosity and nepheline with prediction and composition/process uncertainties;
- Cluster 18 limited by T2 and viscosity with no uncertainty and limited by T2, viscosity and boron with prediction and composition/process uncertainties;
- Cluster 25 limited by T2, boron and nepheline with no uncertainty and limited by the same properties with 4 MFPV samplings with prediction and composition/process uncertainties and by T2, viscosity and nepheline with one sampling with prediction and composition/process uncertainties.

Table 9. Glass Mass and Limiting Factors for 30 HLW Clusters with Prediction and Composition/Process Uncertainties

| Cluster | Waste oxides, kg | One MFPV Sample |           | Four MFPV Samples |           | Limits(a)                                   |
|---------|------------------|-----------------|-----------|-------------------|-----------|---------------------------------------------|
|         |                  | WOL, wt%        | Glass, MT | WOL, wt%          | Glass, MT |                                             |
| 1       | 102,015          | 37.4            | 272.6     | 37.4              | 272.5     | Max Fe                                      |
| 2       | 93,314           | 45.1            | 206.9     | 45.1              | 206.9     | Max Fe                                      |
| 3       | 304,764          | 47.1            | 647.0     | 47.8              | 637.9     | T2,Vis,NP                                   |
| 4       | 340,138          | 42.8            | 795.3     | 43.4              | 783.8     | T2,Vis,NP                                   |
| 5       | 118,988          | 49.1            | 242.2     | 50.0              | 237.9     | T2,Vis,B                                    |
| 6       | 130,884          | 47.1            | 278.0     | 47.7              | 274.4     | T2,Vis,NP                                   |
| 7       | 129,640          | 41.9            | 309.3     | 42.7              | 303.3     | T2,Vis,Na                                   |
| 8       | 135,350          | 46.7            | 289.6     | 47.4              | 285.4     | T2,Vis,NP                                   |
| 9       | 40,217           | 39.2            | 102.5     | 39.8              | 101.1     | TZr,Vis,NP,B                                |
| 10      | 137,773          | 51.4            | 268.0     | 52.1              | 264.5     | T2,Vis,NP                                   |
| 11      | 229,181          | 46.8            | 489.5     | 47.4              | 483.1     | T2,Vis,NP                                   |
| 12      | 96,641           | 49.6            | 194.7     | 50.2              | 192.3     | T2,Vis,NP                                   |
| 13      | 414,412          | 39.8            | 1,040.6   | 40.5              | 1,023.7   | T2,Vis                                      |
| 14      | 226,581          | 45.4            | 499.6     | 46.1              | 492.0     | T2,Vis,B                                    |
| 15      | 102,370          | 39.0            | 262.6     | 39.0              | 262.5     | Max Mn                                      |
| 16      | 89,071           | 41.3            | 215.6     | 41.9              | 212.4     | T2,Visc,B                                   |
| 17      | 334,869          | 48.3            | 693.5     | 49.0              | 683.8     | T2,Vis,NP                                   |
| 18      | 376,435          | 47.8            | 788.3     | 48.4              | 777.0     | T2,Vis,B                                    |
| 19      | 178,911          | 36.2            | 493.8     | 36.8              | 485.8     | TZr,Vis,NP,B                                |
| 20      | 228,853          | 46.1            | 496.3     | 46.8              | 488.7     | T2,Vis                                      |
| 21      | 710,511          | 45.0            | 1,578.6   | 45.7              | 1,554.2   | T2,Vis,B                                    |
| 22      | 546,626          | 45.0            | 1,215.6   | 45.6              | 1,198.4   | T2,Vis,NP                                   |
| 23      | 709,324          | 38.2            | 1,857.3   | 38.9              | 1,823.4   | TZr,Vis,NP                                  |
| 24      | 196,576          | 38.9            | 505.7     | 39.5              | 498.0     | T2,Vis,NP                                   |
| 25      | 979,245          | 40.9            | 2,393.3   | 41.6              | 2,355.6   | T2,Vis,NP (1 sample)<br>T2,NP,B (4 samples) |
| 26      | 276,233          | 39.2            | 704.9     | 39.9              | 692.9     | T2,Vis                                      |
| 27      | 784,370          | 41.2            | 1,905.7   | 41.8              | 1,875.3   | T2,Vis,B                                    |
| 28      | 220,037          | 41.5            | 530.0     | 42.2              | 521.6     | T2,Vis,B                                    |
| 29      | 1,388,456        | 43.2            | 3,211.8   | 44.0              | 3,156.3   | T2,Vis,B                                    |
| 30      | 841,474          | 38.0            | 2,214.0   | 38.0              | 2,213.9   | Max Al                                      |
| Sum     | 10,463,259       | 42.4            | 24,702.8  | 43.0              | 24,358.6  |                                             |

(a) limiting factors include: Max Fe ( $g_{Fe_2O_3} = 20\text{wt}\%$ ), T2 ( $T_{2\%} = 950^\circ\text{C}$ ), Vis ( $\eta_{1150} = 2$  or  $8 \text{ Pa}\cdot\text{s}$ ), NP (nepheline probability = 30%), TZr ( $T_{L-Zr} = 1050^\circ\text{C}$ ), Max Mn ( $g_{MnO} = 8 \text{ wt}\%$ ), Max Al ( $g_{Al_2O_3} = 30 \text{ wt}\%$ ). B (model validity,  $g_{B_2O_3} = 4 - 22 \text{ wt}\%$ ), Na (model validity,  $g_{Na_2O} = 4.1 - 24 \text{ wt}\%$ ).

## 6.5 Evaluation of Individual Sources of Composition/Process Uncertainty

With a roughly 2.43 relative percent increase in predicted HLW glass mass due to the application of composition/process uncertainties, a study was performed to determine which components of composition uncertainties had the most significant impact on glass mass. Table 10 shows the glass masses resulting from excluding individual composition uncertainties, one-at-a-time, while all other composition uncertainty components were applied. Excluding the analytical uncertainties had the strongest effect by decreasing the total glass mass by 1.31% followed by 0.1% for mixing and sampling uncertainty. The individual effects of remaining four composition uncertainty components were not calculated for all clusters because their effects calculated for selected clusters were negligible, all less than 0.1%.

Table 10. HLW Glass Masses Generated by Individually Excluding Prediction Uncertainties for Various Properties, kg

| Cluster | No uncertainties | Prediction uncertainties for all properties | Full Prediction & Composition Uncertainties(a) | Prediction & Composition Uncertainties without Analytical Uncertainty(a) | Prediction & Composition Uncertainties without Mixing and Sampling Uncertainty(a) |
|---------|------------------|---------------------------------------------|------------------------------------------------|--------------------------------------------------------------------------|-----------------------------------------------------------------------------------|
| 1       | 272.5            | 272.5                                       | 272.6                                          | 272.6                                                                    | 272.6                                                                             |
| 2       | 206.8            | 206.8                                       | 206.9                                          | 206.9                                                                    | 206.9                                                                             |
| 3       | 614.5            | 626.9                                       | 642.4                                          | 634.4                                                                    | 641.6                                                                             |
| 4       | 756.1            | 770.7                                       | 789.5                                          | 779.6                                                                    | 788.1                                                                             |
| 5       | 228.2            | 233.2                                       | 240.1                                          | 236.3                                                                    | 239.7                                                                             |
| 6       | 263.7            | 270.3                                       | 276.2                                          | 273.5                                                                    | 275.7                                                                             |
| 7       | 290.1            | 296.8                                       | 306.3                                          | 300.5                                                                    | 306.0                                                                             |
| 8       | 275.6            | 280.5                                       | 287.5                                          | 283.8                                                                    | 286.9                                                                             |
| 9       | 94.0             | 98.9                                        | 101.8                                          | 100.7                                                                    | 101.5                                                                             |
| 10      | 254.7            | 260.6                                       | 266.3                                          | 263.8                                                                    | 265.6                                                                             |
| 11      | 464.7            | 475.7                                       | 486.3                                          | 481.1                                                                    | 485.6                                                                             |
| 12      | 185.7            | 189.5                                       | 193.5                                          | 191.8                                                                    | 193.2                                                                             |
| 13      | 977.3            | 1,003.8                                     | 1,032.1                                        | 1,015.3                                                                  | 1,031.6                                                                           |
| 14      | 469.5            | 483.2                                       | 495.8                                          | 489.1                                                                    | 495.1                                                                             |
| 15      | 262.4            | 262.4                                       | 262.5                                          | 262.6                                                                    | 262.6                                                                             |
| 16      | 203.1            | 208.6                                       | 214.0                                          | 211.1                                                                    | 213.7                                                                             |
| 17      | 659.1            | 672.8                                       | 688.6                                          | 680.3                                                                    | 687.8                                                                             |
| 18      | 746.1            | 763.8                                       | 782.6                                          | 772.1                                                                    | 782.0                                                                             |
| 19      | 446.5            | 475.3                                       | 489.8                                          | 481.8                                                                    | 489.2                                                                             |
| 20      | 469.3            | 480.0                                       | 492.5                                          | 485.3                                                                    | 492.2                                                                             |
| 21      | 1,489.9          | 1,525.9                                     | 1,566.4                                        | 1,542.5                                                                  | 1,565.1                                                                           |
| 22      | 1,148.9          | 1,177.7                                     | 1,207.0                                        | 1,190.8                                                                  | 1,205.9                                                                           |
| 23      | 1,677.2          | 1,783.8                                     | 1,840.3                                        | 1,809.9                                                                  | 1,838.9                                                                           |

| Cluster                                                                                        | No<br>uncertainties | Prediction<br>uncertainties<br>for all<br>properties | Full Prediction<br>& Composition<br>Uncertainties(a) | Prediction &<br>Composition<br>Uncertainties<br>without<br>Analytical<br>Uncertainty(a) | Prediction &<br>Composition<br>Uncertainties<br>without Mixing<br>and Sampling<br>Uncertainty(a) |
|------------------------------------------------------------------------------------------------|---------------------|------------------------------------------------------|------------------------------------------------------|-----------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------|
| 24                                                                                             | 467.9               | 489.4                                                | 501.9                                                | 494.5                                                                                   | 501.3                                                                                            |
| 25                                                                                             | 2,251.2             | 2,314.5                                              | 2,374.4                                              | 2,338.5                                                                                 | 2,371.7                                                                                          |
| 26                                                                                             | 660.3               | 679.2                                                | 698.9                                                | 687.0                                                                                   | 698.3                                                                                            |
| 27                                                                                             | 1,793.9             | 1,838.5                                              | 1,890.5                                              | 1,859.5                                                                                 | 1,888.5                                                                                          |
| 28                                                                                             | 497.3               | 511.5                                                | 525.8                                                | 517.3                                                                                   | 525.2                                                                                            |
| 29                                                                                             | 3,020.4             | 3,096.6                                              | 3,184.1                                              | 3,132.6                                                                                 | 3,180.2                                                                                          |
| 30                                                                                             | 2,213.7             | 2,213.8                                              | 2,214.0                                              | 2,214.0                                                                                 | 2,214.0                                                                                          |
| Sum                                                                                            | 23,360              | 23,963                                               | 24,531                                               | 24,209                                                                                  | 24,507                                                                                           |
| (a) Glass Mass reported are the average of the masses produced with one and four MFPV samples. |                     |                                                      |                                                      |                                                                                         |                                                                                                  |

## 7.0 LAW Calculation Results and Discussion

Calculations were performed using the 36 LAW feed composition clusters. Initially, calculations were performed using the waste loading line rules with and without uncertainties (Section 7.1). Then the calculations were performed without the waste loading line rules (Section 7.2). The impact of various prediction uncertainties are discussed in Section 7.2.3. Finally, the impacts of various composition/process uncertainties are discussed in Section 7.2.5.

### 7.1 LAW Glass Mass with Waste Loading ('Line') Rules

A series of waste loading line rules were developed in Vienna et al. (2016) to simply estimate the likely WOL of LAW glass during production without recourse to a detailed set of constraints, property models, and uncertainty descriptions. These rules are primarily used to constrain total alkali and  $\text{SO}_3$  in glass as shown in Figure 11. In addition to the three blue lines in this figure (new proposed waste loading rules), there is also a combined chlorine, chromium, and phosphorous rule with equations listed in Table 3. The initial question to answer is if the loadings estimated by the line rules can be obtained by glasses for estimated Hanford wastes while still meeting all the property constraints with sufficient confidence. This subsection aims to answer that question.

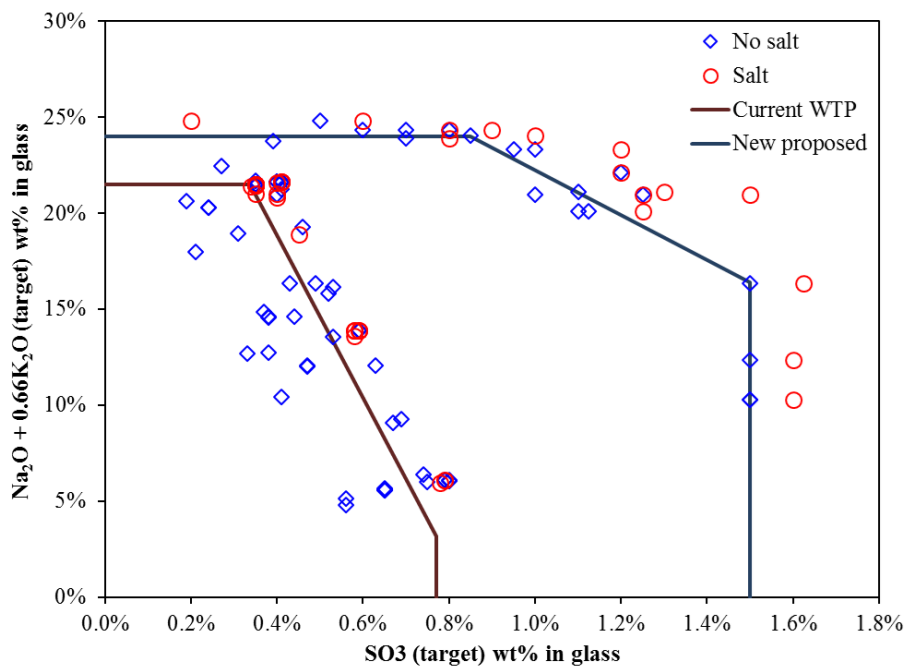


Figure 11. Comparison of the WTP Baseline and Proposed New Waste Loading Line Rules for Normalized Alkali and Sulfur Content. (Vienna et al. (2016)).

The maximum WOL for each of the 36 waste clusters was determined and reported in Table 11. Using the constraints and models reported by Vienna et al. (2016), 282,350 MT of LAW glass would be produced (51,243 containers, assuming 5.51 MT of glass per container). The glass is more limited by the alkali constraint (68%) than by the alkali plus sulfur constraint (32%), sometimes including halide constraints (28%) – see Figure 12.

Table 11. Waste Mass, Maximum WOL, Glass Mass, and Limiting Factors for each of 36 LAW Clusters with Line Rules

| Cluster | Waste oxides, MT | No Uncertainty |           | Pred + Comp Uncertainty |           | Limits(a)       |
|---------|------------------|----------------|-----------|-------------------------|-----------|-----------------|
|         |                  | WOL, wt%       | Glass, MT | WOL, wt%                | Glass, MT |                 |
| 1       | 2,295            | 26.2           | 8,749     | 26.2                    | 8,751     | NaK             |
| 2       | 2,334            | 26.5           | 8,806     | 26.5                    | 8,813     | NaK             |
| 3       | 1,244            | 26.9           | 4,632     | 26.5                    | 4,690     | NaK+H           |
| 4       | 2,257            | 26.9           | 8,399     | 26.8                    | 8,408     | NaK+H           |
| 5       | 484              | 23.4           | 2,067     | 23.4                    | 2,067     | NaKS+H          |
| 6       | 2,021            | 26.9           | 7,525     | 26.8                    | 7,531     | NaK             |
| 7       | 492              | 27.4           | 1,798     | 27.4                    | 1,800     | NaK             |
| 8       | 3,669            | 26.1           | 14,083    | 26.0                    | 14,093    | NaK             |
| 9       | 1,920            | 26.5           | 7,258     | 26.4                    | 7,282     | NaK+H           |
| 10      | 5,375            | 28.4           | 18,924    | 28.4                    | 18,930    | NaK             |
| 11      | 5,812            | 28.2           | 20,636    | 28.1                    | 20,650    | NaK             |
| 12      | 4,898            | 28.3           | 17,286    | 28.3                    | 17,295    | NaK             |
| 13      | 2,345            | 28.6           | 8,205     | 28.6                    | 8,214     | NaK             |
| 14      | 1,025            | 28.9           | 3,548     | 28.9                    | 3,551     | NaK             |
| 15      | 4,719            | 28.7           | 16,417    | 28.7                    | 16,420    | NaKS            |
| 16      | 2,450            | 28.6           | 8,552     | 28.6                    | 8,558     | NaK             |
| 17      | 3,775            | 29.0           | 13,033    | 28.9                    | 13,043    | NaK             |
| 18      | 1,085            | 29.1           | 3,723     | 29.1                    | 3,725     | NaK             |
| 19      | 2,643            | 29.1           | 9,080     | 29.1                    | 9,082     | NaK             |
| 20      | 2,253            | 29.8           | 7,566     | 29.8                    | 7,572     | NaK             |
| 21      | 558              | 29.0           | 1,927     | 28.9                    | 1,927     | NaK             |
| 22      | 2,398            | 29.0           | 8,275     | 29.0                    | 8,276     | NaKS            |
| 23      | 2,584            | 27.6           | 9,376     | 27.6                    | 9,376     | NaKS+H          |
| 24      | 4,992            | 29.6           | 16,893    | 29.5                    | 16,908    | NaK             |
| 25      | 4,622            | 27.1           | 17,051    | 27.1                    | 17,052    | NaKS+H          |
| 26      | 1,547            | 27.3           | 5,661     | 27.3                    | 5,661     | NaKS+H          |
| 27      | 1,481            | 26.2           | 5,649     | 26.2                    | 5,649     | NaKS+H          |
| 28      | 681              | 28.5           | 2,392     | 28.5                    | 2,392     | NaKS            |
| 29      | 1,536            | 26.5           | 5,796     | 26.5                    | 5,797     | NaKS+H          |
| 30      | 2,214            | 26.4           | 8,390     | 26.4                    | 8,391     | NaKS+H          |
| 31      | 463              | 30.9           | 1,497     | 30.9                    | 1,498     | NaK             |
| 32      | 404              | 32.0           | 1,261     | 31.8                    | 1,271     | NaK             |
| 33      | 358              | 26.6           | 1,346     | 26.6                    | 1,346     | NaKS+H          |
| 34      | 500              | 23.9           | 2,091     | 23.9                    | 2,091     | NaKS+H          |
| 35      | 919              | 24.0           | 3,836     | 24.0                    | 3,836     | NaKS            |
| 36      | 112              | 18.1           | 619       | 18.1                    | 619       | SO <sub>3</sub> |
| Sum(b)  | 78,465           | 27.8           | 282,350   | 27.8                    | 282,562   |                 |

| Cluster                                                                                                                                                                                                                                                                                                                                                | Waste oxides, MT | No Uncertainty WOL, wt% | Glass, MT | Pred + Comp Uncertainty WOL, wt% | Glass, MT | Limits(a) |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------|-------------------------|-----------|----------------------------------|-----------|-----------|
| (a) NaK = Na <sub>2</sub> O+K <sub>2</sub> O Line Rule, NaKS = Na <sub>2</sub> O+K <sub>2</sub> O+SO <sub>3</sub> Line Rule, SO <sub>3</sub> = SO <sub>3</sub> Line Rule, +H includes also Halide Line Rule. The limits reported in this table are applicable to both uncertainty cases: No Uncertainty and Prediction plus Composition Uncertainties. |                  |                         |           |                                  |           |           |
| (b) Sum for waste oxide and glass masses, weighted average for WOL                                                                                                                                                                                                                                                                                     |                  |                         |           |                                  |           |           |

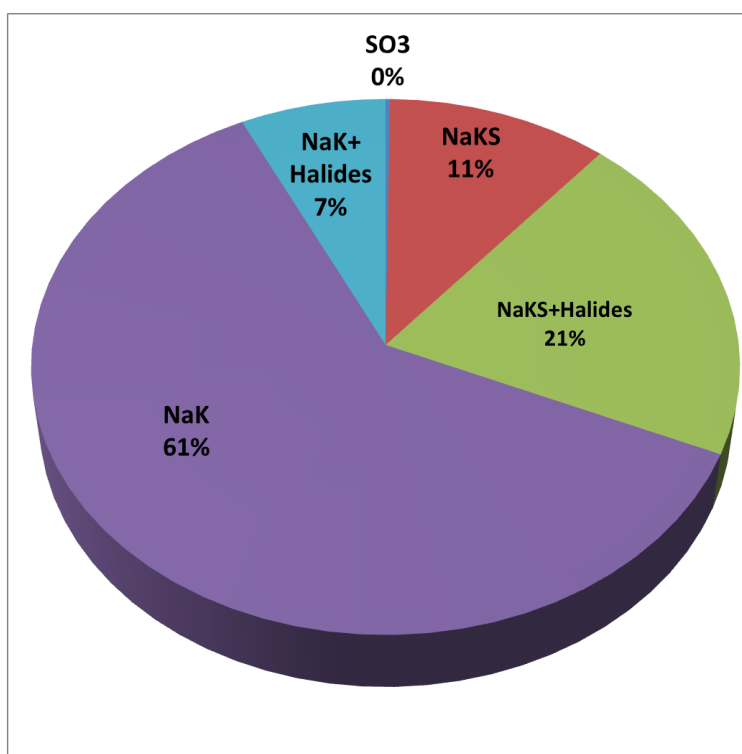


Figure 12. Distribution of LAW Glass Mass Limited by Various Line Rules.

The total glass mass increases only slightly when prediction and composition/process uncertainties are applied – no more than 1.25 relative percent increase for any individual cluster with an average of 0.08% relative difference as a weighted average across all clusters. Therefore, the application of waste loading line rules do serve the initial purpose.

## 7.2 LAW Glass Mass without Waste Loading ('Line') Rules

The waste loading line rules were found in Section 7.1 to be sufficiently conservative to account for various uncertainties in LAW WOL. The next related question to answer is “how conservative are the line rules?” The following sub-sections seeks to answer that question. A series of calculations were performed to maximize the WOL for each LAW composition while simultaneously satisfying all of the LAW constraints listed in Section 3.2. If one of the property/composition constraints (Table 3) limits the WOL, the additive composition is adjusted to increase the loading until one or more additional constraints are met. Therefore, the WOL is limited by more than one constraint. Unlike HLW glasses there are no LAW glasses limited by single component concentration constraints but all LAW glasses were also limited by one or more model validity constraints (Table 4).

## 7.2.1 No Uncertainties

Reported in Table 12 are the maximum WOL for each of the 36 waste clusters which was determined with the line rules suppressed. These calculations resulted in an estimate of 252,490 MT of LAW glass to be produced (45,824 containers, assuming 5.51 MT of glass per container). This is 10.58 relative percent lower than the estimates made when line rules are applied. The glass is most limited by K-3 corrosion, viscosity and Alkali + Zr + Sn +Ca (58%) (Figure 13).

Table 12. Waste Mass, Maximum WOL, Glass Mass, and Limiting Factors for each of 36 LAW Clusters with No Uncertainties and No Line Rules

| Cluster | Waste oxides, MT | WOL, wt% | Glass, MT | Limits(a)                                         |
|---------|------------------|----------|-----------|---------------------------------------------------|
| 1       | 2,295            | 28.9     | 7,946     | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)                 |
| 2       | 2,334            | 29.3     | 7,973     | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)                 |
| 3       | 1,244            | 29.4     | 4,238     | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca),wSO3            |
| 4       | 2,257            | 29.7     | 7,597     | Al,B,Na,Zr,K3,Visc,(Zr+Sn+Al),(Alk+Zr+Sn+Ca),wSO3 |
| 5       | 484              | 27.9     | 1,734     | V,VHT,K3,Visc,wSO3,(Zr+Sn+Al)                     |
| 6       | 2,021            | 29.6     | 6,838     | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)                 |
| 7       | 492              | 29.9     | 1,649     | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)                 |
| 8       | 3,669            | 28.5     | 12,893    | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)                 |
| 9       | 1,920            | 28.8     | 6,656     | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca),wSO3            |
| 10      | 5,375            | 31.0     | 17,362    | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)                 |
| 11      | 5,812            | 30.6     | 18,972    | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)                 |
| 12      | 4,898            | 30.8     | 15,906    | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)                 |
| 13      | 2,345            | 31.1     | 7,553     | Al,B,Na,Ti,Zr,K3,Visc,(Alk+Zr+Sn+Ca),wSO3         |
| 14      | 1,025            | 31.3     | 3,270     | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)                 |
| 15      | 4,719            | 31.6     | 14,919    | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca),wSO3            |
| 16      | 2,450            | 31.5     | 7,782     | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)                 |
| 17      | 3,775            | 31.5     | 11,989    | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)                 |
| 18      | 1,085            | 31.5     | 3,439     | B,Cr,Zr,K3,Visc,(Zr+Sn+Al),(Alk+Zr+Sn+Ca)         |
| 19      | 2,643            | 31.7     | 8,324     | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)                 |
| 20      | 2,253            | 32.3     | 6,972     | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)                 |
| 21      | 558              | 32.5     | 1,715     | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)                 |
| 22      | 2,398            | 32.2     | 7,452     | Al,B,Na,Zr,K3,wSO3,(Alk+Zr+Sn+Ca)                 |
| 23      | 2,584            | 32.4     | 7,988     | Al,B,Na,Zr,K3,wSO3,(Alk+Zr+Sn+Ca)                 |
| 24      | 4,992            | 32.1     | 15,567    | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)                 |
| 25      | 4,622            | 32.2     | 14,353    | Al,B,Na,Zr,K3,wSO3,(Alk+Zr+Sn+Ca)                 |
| 26      | 1,547            | 32.5     | 4,763     | Al,B,Na,Zr,K3,wSO3,(Alk+Zr+Sn+Ca)                 |
| 27      | 1,481            | 33.2     | 4,461     | B,Na,V,Zr,VHT,K3,wSO3                             |
| 28      | 681              | 33.0     | 2,062     | Al,B,Na,Zr,K3,wSO3,(Alk+Zr+Sn+Ca)                 |
| 29      | 1,536            | 32.9     | 4,676     | Cr,V,Zr,VHT,K3,wSO3,(Zr+Sn+Al)                    |
| 30      | 2,214            | 32.7     | 6,774     | Cr,V,Zr,VHT,K3,wSO3,(Zr+Sn+Al)                    |

| Cluster                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | Waste oxides, MT | WOL, wt% | Glass, MT | Limits(a)                           |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------|----------|-----------|-------------------------------------|
| 31                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | 463              | 33.5     | 1,381     | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)   |
| 32                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | 404              | 34.8     | 1,162     | Al,B,Na,Zr,K3,Visc,(Alk+Zr+Sn+Ca)   |
| 33                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | 358              | 33.8     | 1,058     | Si,V,VHT,K3,Visc,wSO3,(Zr+Sn+Al)    |
| 34                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | 500              | 30.5     | 1,640     | Al,B,V,Zr,PCT,VHT,K3,Visc,wSO3      |
| 35                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | 919              | 30.9     | 2,977     | Al,Ca,V,VHT,K3,Visc,wSO3            |
| 36                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | 112              | 25.0     | 449       | Al,B,P,PCT,Visc,wSO3,(Alk-Zr-Sn-Ca) |
| Sum(b)                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | 78,465           | 31.1     | 252,490   |                                     |
| <p>(a) Limiting factors include: Al, B, Ca, Cr, Na, P, Si, Ti, V, and Zr represent model validity constraints for correspond oxide components given in Table 4. (Alk-Zr-Sn-Ca) =</p> $g_{Na_2O} + 0.66g_{K_2O} + 2.07g_{Li_2O} - g_{ZrO_2} - g_{SnO_2} - g_{CaO} \leq 0.15$ <p>K3 = K-3 neck corrosion at 1208°C <math>\ln[k_{1208}, \text{in}] \leq -3.2189</math>, PCT = <math>\ln[\text{PCT } NL, \text{ g/L}] \leq 1.386</math>, VHT = <math>\ln[\text{VHT } D, \mu\text{m}] \leq 6.116</math>, Visc = <math>0.693 \leq \ln [\eta_{1150}, \text{ Pa}\cdot\text{s}] \leq 2.079</math>, wSO3 = SO<sub>3</sub> salt concentration <math>w_{SO_3} \leq w_{SO_3}^{Limit}</math>, (Zr+Sn+Al) = <math>g_{ZrO_2} + g_{SnO_2} + g_{Al_2O_3} \leq 0.17</math>.</p> <p>(b) Sum for waste oxide and glass masses, weighted average for WOL</p> |                  |          |           |                                     |

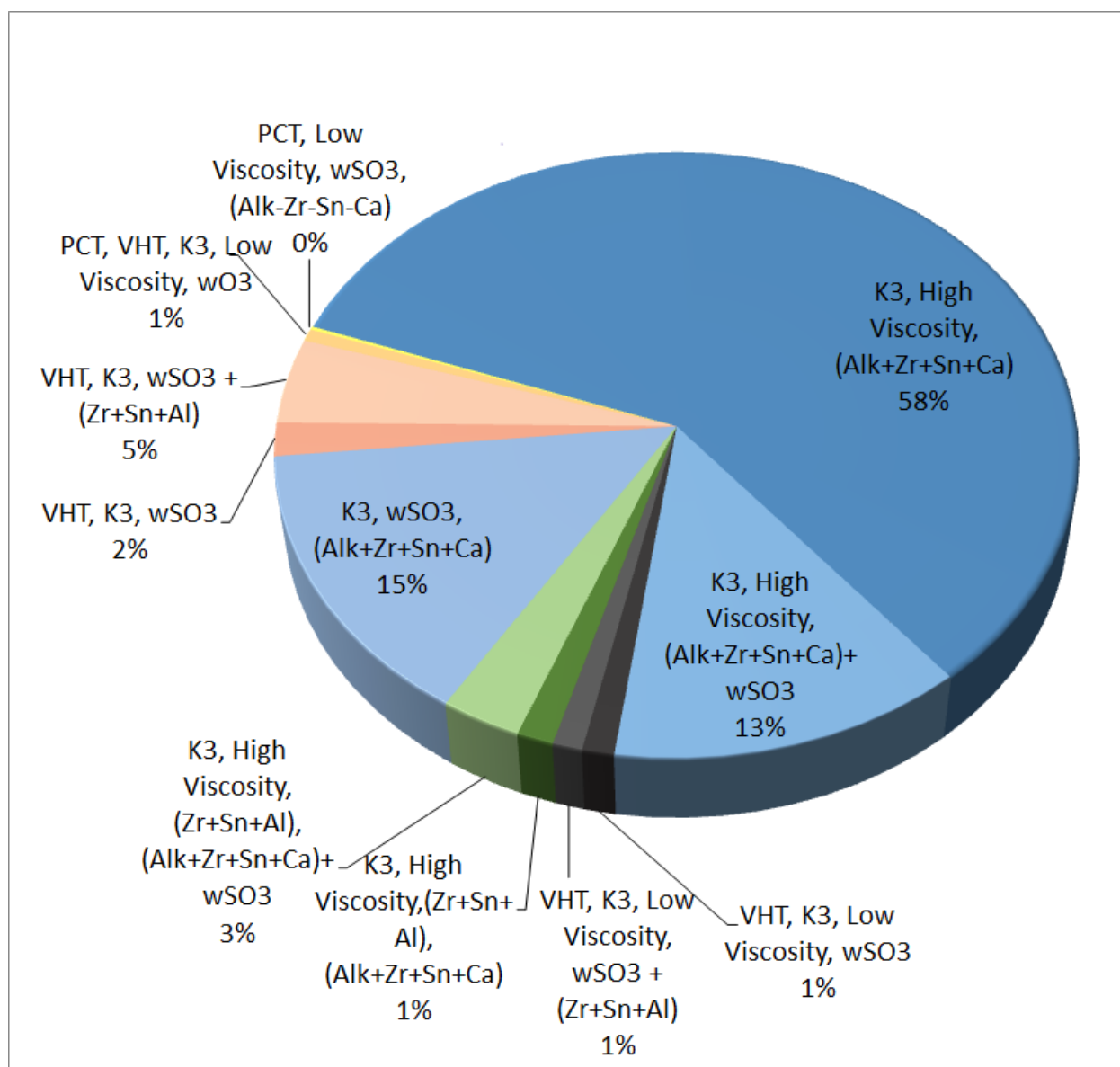


Figure 13. Waste Loading Limiting Factors for LAW Glasses without Line Rules.

## 7.2.2 Prediction Uncertainties Only

The waste estimates were performed using the prediction uncertainties (as described in Section 4.1) and without the waste loading line rules. The results are summarized in Table 13. The total glass mass produced is 255,833 MT, 1.32 relative percent higher than the case without any uncertainties. The waste loading limiting factors are reported in Table 13.

Table 13. Waste Mass, Maximum WOL, Glass Mass, and Limiting Factors for 36 LAW Clusters with Prediction Uncertainties without Line Rules

| Cluster | Waste oxides, kg | WOL, wt% | Glass, MT | Limits(a)                            |
|---------|------------------|----------|-----------|--------------------------------------|
| 1       | 2,295            | 28.8     | 7,959     | Al,B,Cr,Zr,VHT,K3,Visc,(Zr+Sn+Al)    |
| 2       | 2,334            | 29.0     | 8,050     | Al,B,Cr,Zr,VHT,K3,Visc,(Zr+Sn+Al)    |
| 3       | 1,244            | 28.9     | 4,304     | B,Cr,Zr,VHT,K3,Visc,wSO3,(Zr+Sn+Al)  |
| 4       | 2,257            | 29.2     | 7,741     | B,Cr,Zr,VHT,K3,Visc,(Zr+Sn+Al)       |
| 5       | 484              | 26.5     | 1,825     | V,VHT,K3,wSO3                        |
| 6       | 2,021            | 29.5     | 6,862     | Al,B,Cr,Zr,VHT,K3,Visc,(Zr+Sn+Al)    |
| 7       | 492              | 29.9     | 1,649     | Al,B,Cr,Na,Zr,VHT,K3,Visc,(Zr+Sn+Al) |
| 8       | 3,669            | 28.4     | 12,896    | Al,B,Na,Zr,VHT,K3,Visc,(Zr+Sn+Al)    |
| 9       | 1,920            | 28.7     | 6,695     | B,Cr,Zr,VHT,K3,Visc,(Zr+Sn+Al)       |
| 10      | 5,375            | 31.0     | 17,365    | Al,B,Na,Zr,VHT,K3,Visc,(Zr+Sn+Al)    |
| 11      | 5,812            | 30.6     | 18,974    | Al,B,Na,Zr,VHT,K3,Visc,(Zr+Sn+Al)    |
| 12      | 4,898            | 30.8     | 15,907    | Al,B,Na,Zr,VHT,K3,Visc,(Zr+Sn+Al)    |
| 13      | 2,345            | 31.0     | 7,567     | B,Cr,Zr,VHT,K3,Visc,(Zr+Sn+Al)       |
| 14      | 1,025            | 31.3     | 3,271     | Al,B,Cr,Na,Zr,VHT,K3,Visc,(Zr+Sn+Al) |
| 15      | 4,719            | 31.3     | 15,068    | B,Cr,Zr,VHT,K3,Visc,wSO3,(Zr+Sn+Al)  |
| 16      | 2,450            | 31.5     | 7,787     | Al,B,Cr,Zr,VHT,K3,Visc,(Zr+Sn+Al)    |
| 17      | 3,775            | 31.5     | 11,992    | Al,B,Na,Zr,VHT,K3,Visc,(Zr+Sn+Al)    |
| 18      | 1,085            | 31.5     | 3,444     | B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al)     |
| 19      | 2,643            | 31.7     | 8,326     | Al,B,Na,Zr,VHT,K3,Visc,(Zr+Sn+Al)    |
| 20      | 2,253            | 32.3     | 6,974     | Al,B,Na,Zr,VHT,K3,Visc,(Zr+Sn+Al)    |
| 21      | 558              | 31.8     | 1,756     | Al,B,Cr,Zr,VHT,K3,Visc,(Zr+Sn+Al)    |
| 22      | 2,398            | 31.8     | 7,547     | B,Cr,Zr,VHT,K3,wSO3,(Zr+Sn+Al)       |
| 23      | 2,584            | 31.5     | 8,213     | B,Cr,V,Zr,VHT,K3,wSO3,(Zr+Sn+Al)     |
| 24      | 4,992            | 32.1     | 15,573    | Al,B,Cr,Na,Zr,VHT,K3,Visc,(Zr+Sn+Al) |
| 25      | 4,622            | 31.2     | 14,819    | B,V,Zr,VHT,K3,wSO3                   |
| 26      | 1,547            | 31.5     | 4,909     | B,V,Zr,VHT,K3,wSO3                   |
| 27      | 1,481            | 30.9     | 4,793     | V,VHT,K3,wSO3                        |
| 28      | 681              | 32.4     | 2,103     | B,Cr,V,Zr,VHT,K3,wSO3,(Zr+Sn+Al)     |
| 29      | 1,536            | 30.7     | 5,010     | Al,V,VHT,K3,wSO3                     |
| 30      | 2,214            | 30.7     | 7,215     | V,VHT,K3,wSO3                        |
| 31      | 463              | 33.5     | 1,382     | Al,B,Na,Zr,VHT,K3,Visc,(Zr+Sn+Al)    |
| 32      | 404              | 34.7     | 1,165     | Al,B,Cr,Zr,VHT,K3,Visc,(Zr+Sn+Al)    |
| 33      | 358              | 31.4     | 1,141     | V,VHT,K3,wSO3                        |
| 34      | 500              | 28.3     | 1,767     | V,VHT,K3,wSO3                        |
| 35      | 919              | 28.4     | 3,237     | V,VHT,K3,wSO3                        |
| 36      | 112              | 20.5     | 547       | Al,B,Ca,V,VHT,Visc,wSO3              |
| Sum(b)  | 78,465           | 30.7     | 255,833   |                                      |

| Cluster                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | Waste oxides, kg | WOL, wt% | Glass, MT | Limits(a) |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------|----------|-----------|-----------|
| (a) Limiting factors include: Al, B, Ca, Cr, Na, P, Si, V, and Zr represent model validity constraints for correspond oxide components given in Table 4. (Alk-Zr-Sn-Ca) = $g_{Na_2O} + 0.66g_{K_2O} + 2.07g_{Li_2O} - g_{ZrO_2} - g_{SnO_2} - g_{CaO} \leq 0.15$ , K3 = K-3 neck corrosion at 1208°C $\ln[k_{1208, in}] \leq -3.2189$ , PCT = $\ln[PCT\ NL, g/L] \leq 1.386$ , VHT = $\ln[VHT\ D, \mu m] \leq 6.116$ , Visc = $0.693 \leq \ln[\eta_{1150}, Pa \cdot s] \leq 2.079$ , wSO <sub>3</sub> = SO <sub>3</sub> salt concentration $w_{SO_3} \leq w_{SO_3}^{Limit}$ , (Zr+Sn+Al) = $g_{ZrO_2} + g_{SnO_2} + g_{Al_2O_3} \leq 0.17$ .<br>(b) Sum for waste oxide and glass masses, weighted average for WOL |                  |          |           |           |

### 7.2.3 Evaluation of Individual Property Prediction Uncertainties

An analysis was performed to determine the role of prediction uncertainties for individual properties on the amount of glass produced. Table 14 summarizes the glass masses resulting from systematic elimination of prediction uncertainties for different properties. The most influential property was VHT with -0.81% (RPD after removing prediction uncertainty for VHT) followed by K3 -0.61%, wSO<sub>3</sub> -0.28%, and least influential was viscosity with -0.03%. Analysis was not performed for PCT because PCT was not a limiting property for any cluster when prediction uncertainties were applied as shown in Table 13.

Table 14. LAW Glass Mass (MT) for Various Different Property Prediction Uncertainty Cases

| Cluster | No uncertainties | Prediction uncertainties for all properties | Prediction uncertainties for all but VHT | Prediction uncertainties for all but K3 | Prediction uncertainties for all but wSO <sub>3</sub> | Prediction uncertainties for all but Viscosity |
|---------|------------------|---------------------------------------------|------------------------------------------|-----------------------------------------|-------------------------------------------------------|------------------------------------------------|
| 1       | 7,946            | 7,959                                       | 7,946                                    | 7,947                                   | 7,959                                                 | 7,955                                          |
| 2       | 7,973            | 8,050                                       | 7,974                                    | 7,999                                   | 8,050                                                 | 8,045                                          |
| 3       | 4,238            | 4,304                                       | 4,240                                    | 4,257                                   | 4,297                                                 | 4,304                                          |
| 4       | 7,597            | 7,741                                       | 7,599                                    | 7,680                                   | 7,741                                                 | 7,734                                          |
| 5       | 1,734            | 1,825                                       | 1,803                                    | 1,783                                   | 1,805                                                 | 1,825                                          |
| 6       | 6,838            | 6,862                                       | 6,838                                    | 6,839                                   | 6,862                                                 | 6,858                                          |
| 7       | 1,649            | 1,649                                       | 1,649                                    | 1,649                                   | 1,649                                                 | 1,649                                          |
| 8       | 12,893           | 12,896                                      | 12,894                                   | 12,894                                  | 12,896                                                | 12,896                                         |
| 9       | 6,656            | 6,695                                       | 6,658                                    | 6,658                                   | 6,695                                                 | 6,688                                          |
| 10      | 17,362           | 17,365                                      | 17,362                                   | 17,362                                  | 17,365                                                | 17,365                                         |
| 11      | 18,972           | 18,974                                      | 18,972                                   | 18,972                                  | 18,974                                                | 18,974                                         |
| 12      | 15,906           | 15,907                                      | 15,906                                   | 15,906                                  | 15,907                                                | 15,906                                         |
| 13      | 7,553            | 7,567                                       | 7,555                                    | 7,555                                   | 7,567                                                 | 7,560                                          |
| 14      | 3,270            | 3,271                                       | 3,270                                    | 3,270                                   | 3,271                                                 | 3,271                                          |
| 15      | 14,919           | 15,068                                      | 14,925                                   | 14,925                                  | 15,044                                                | 15,068                                         |
| 16      | 7,782            | 7,787                                       | 7,783                                    | 7,783                                   | 7,787                                                 | 7,785                                          |
| 17      | 11,989           | 11,992                                      | 11,990                                   | 11,990                                  | 11,992                                                | 11,991                                         |
| 18      | 3,439            | 3,444                                       | 3,439                                    | 3,441                                   | 3,444                                                 | 3,442                                          |
| 19      | 8,324            | 8,326                                       | 8,325                                    | 8,325                                   | 8,326                                                 | 8,325                                          |

|     |         |         |         |         |         |         |
|-----|---------|---------|---------|---------|---------|---------|
| 20  | 6,972   | 6,974   | 6,973   | 6,973   | 6,974   | 6,974   |
| 21  | 1,715   | 1,756   | 1,716   | 1,747   | 1,756   | 1,755   |
| 22  | 7,452   | 7,547   | 7,456   | 7,465   | 7,533   | 7,547   |
| 23  | 7,988   | 8,213   | 8,015   | 8,089   | 8,167   | 8,213   |
| 24  | 15,567  | 15,573  | 15,570  | 15,569  | 15,573  | 15,572  |
| 25  | 14,353  | 14,819  | 14,433  | 14,582  | 14,709  | 14,819  |
| 26  | 4,763   | 4,909   | 4,771   | 4,833   | 4,877   | 4,909   |
| 27  | 4,461   | 4,793   | 4,684   | 4,690   | 4,708   | 4,793   |
| 28  | 2,062   | 2,103   | 2,063   | 2,074   | 2,097   | 2,103   |
| 29  | 4,676   | 5,010   | 4,891   | 4,876   | 4,911   | 4,978   |
| 30  | 6,774   | 7,215   | 7,086   | 7,070   | 7,118   | 7,215   |
| 31  | 1,381   | 1,382   | 1,382   | 1,381   | 1,382   | 1,382   |
| 32  | 1,162   | 1,165   | 1,162   | 1,162   | 1,165   | 1,164   |
| 33  | 1,058   | 1,141   | 1,117   | 1,113   | 1,120   | 1,141   |
| 34  | 1,640   | 1,767   | 1,719   | 1,721   | 1,730   | 1,767   |
| 35  | 2,977   | 3,237   | 3,130   | 3,143   | 3,150   | 3,237   |
| 36  | 449     | 547     | 462     | 547     | 512     | 547     |
| Sum | 252,490 | 255,833 | 253,760 | 254,268 | 255,112 | 255,757 |

## 7.2.4 Prediction and Composition/Process Uncertainties

The waste estimates were performed using both prediction uncertainties (as described in Section 4.1) and composition/process uncertainties (as described in Section 4.2). The results are summarized in Table 15. The total glass masses produced is 275,359 MT for combined uncertainties, 9.06 relative percent higher than the no uncertainty case and therefore composition uncertainties account for 7.73 relative percent additional increase in glass mass (the remaining 1.32% from prediction uncertainties). The glass mass is 2.48 relative percent below that estimated with the line rules. The waste loading limiting factors are reported in Table 15.

Table 15. Waste Mass, Maximum WOL, Glass Mass, and Limiting Factors for 36 LAW Clusters with Prediction and Composition/Process Uncertainties without Line Rules

| Cluster | Waste oxides,<br>MT | WOL,<br>wt% | Glass,<br>MT | Limits                              |
|---------|---------------------|-------------|--------------|-------------------------------------|
| 1       | 2,295               | 26.4        | 8,683        | Al,B,Cr, Zr,VHT, K3,Visc,(Zr+Sn+Al) |
| 2       | 2,334               | 26.9        | 8,688        | Al,B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al) |
| 3       | 1,244               | 26.6        | 4,668        | B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al)    |
| 4       | 2,257               | 27.0        | 8,372        | Al,B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al) |
| 5       | 484                 | 24.9        | 1,944        | V,VHT,K3,wSO3                       |
| 6       | 2,021               | 27.3        | 7,411        | Al,B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al) |
| 7       | 492                 | 27.6        | 1,781        | Al,B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al) |
| 8       | 3,669               | 26.5        | 13,859       | Al,B,Cr,Zr,VHT,K3,Visc,(Zr+Sn+Al)   |
| 9       | 1,920               | 26.5        | 7,257        | B,CrV,Zr,VHT,K3,Visc,(Zr+Sn+Al)     |

| Cluster                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | Waste oxides,<br>MT | WOL,<br>wt% | Glass,<br>MT | Limits                                |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------|-------------|--------------|---------------------------------------|
| 10                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 5,375               | 28.8        | 18,660       | Al,B,CrV,Zr,VHT,K3,Visc,(Zr+Sn+Al)    |
| 11                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 5,812               | 28.6        | 20,356       | Al,B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al)   |
| 12                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 4,898               | 28.8        | 16,981       | Al,B,Cr,Zr,VHT,K3,Visc,(Zr+Sn+Al)     |
| 13                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 2,345               | 28.5        | 8,225        | Al,B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al)   |
| 14                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 1,025               | 29.0        | 3,536        | Al,B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al)   |
| 15                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 4,719               | 28.9        | 16,326       | B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al)      |
| 16                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 2,450               | 28.8        | 8,513        | Al,B,Cr,Zr,VHT,K3,Visc,(Zr+Sn+Al)     |
| 17                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 3,775               | 29.2        | 12,919       | Al,B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al)   |
| 18                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 1,085               | 29.4        | 3,689        | Al,B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al)   |
| 19                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 2,643               | 29.7        | 8,907        | Al,B,Cr,Zr,VHT,K3,Visc,(Zr+Sn+Al)     |
| 20                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 2,253               | 30.1        | 7,491        | Al,B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al)   |
| 21                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 558                 | 29.2        | 1,911        | Al,B,Cr,Zr,VHT,K3,Visc,(Zr+Sn+Al)     |
| 22                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 2,398               | 29.4        | 8,165        | B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al)      |
| 23                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 2,584               | 29.3        | 8,821        | Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al),wSO3   |
| 24                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 4,992               | 29.7        | 16,833       | Al,B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al)   |
| 25                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 4,622               | 29.1        | 15,865       | Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al),wSO3   |
| 26                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 1,547               | 29.4        | 5,259        | B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al),wSO3 |
| 27                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 1,481               | 28.9        | 5,115        | V,VHT,K3,wSO3                         |
| 28                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 681                 | 30.1        | 2,257        | B,Cr,V,Zr,VHT,K3,Visc,(Zr+Sn+Al),wSO3 |
| 29                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 1,536               | 28.7        | 5,355        | Al,V,VHT,K3,Visc,wSO3                 |
| 30                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 2,214               | 28.7        | 7,711        | V,VHT,K3,wSO3                         |
| 31                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 463                 | 31.5        | 1,466        | Al,B,Cr,Zr,VHT,K3,Visc,(Zr+Sn+Al)     |
| 32                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 404                 | 32.2        | 1,254        | Al,B,Cr,Zr,VHT,K3,Visc,(Zr+Sn+Al)     |
| 33                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 358                 | 29.5        | 1,216        | V,VHT,K3,wSO3                         |
| 34                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 500                 | 26.6        | 1,875        | V,VHT,K3,wSO3                         |
| 35                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 919                 | 26.8        | 3,426        | V,VHT,K3,wSO3                         |
| 36                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 112                 | 20.0        | 561          | Al,B,Ca,V,VHT,Visc,wSO3               |
| Sum(b)                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | 78,465              | 28.5        | 275,359      |                                       |
| (a) Limiting factors include: Al, B, Ca, Cr, Na, P, Si, V, and Zr represent model validity constraints for correspond oxide components given in Table 4. (Alk-Zr-Sn-Ca) = $g_{Na_2O} + 0.66g_{K_2O} + 2.07g_{Li_2O} - g_{ZrO_2} - g_{SnO_2} - g_{CaO} \leq 0.15$ , K3 = K-3 neck corrosion at 1208°C $\ln[k_{1208}, \text{in}] \leq -3.2189$ , PCT = $\ln[\text{PCT NL, g/L}] \leq 1.386$ , VHT = $\ln[\text{VHT D, } \mu\text{m}] \leq 6.116$ , Visc = $0.693 \leq \ln[\eta_{1150}, \text{Pa}\cdot\text{s}] \leq 2.079$ , wSO3 = SO <sub>3</sub> salt concentration $w_{SO_3} \leq w_{SO_3}^{Limit}$ , (Zr+Sn+Al) = $g_{ZrO_2} + g_{SnO_2} + g_{Al_2O_3} \leq 0.17$ .<br>(b) Sum for waste oxide and glass masses, weighted average for WOL |                     |             |              |                                       |

## 7.2.5 Evaluation of Individual Sources of Composition/Process Uncertainty

An analysis was performed to determine the role of individual sources of composition uncertainties on the amount of glass produced. Table 16 summarizes the glass masses resulting from systematic elimination of sources of composition uncertainties. Excluding the analytical uncertainties had the strongest effect by

decreasing the total glass mass by 3.19% followed by 1.62% for volume transfer uncertainty. The individual effects of remaining four composition uncertainty components were not calculated for all clusters because their effects calculated for selected clusters were negligible.

Table 16. LAW Glass Mass (MT) for Full Prediction and Composition Uncertainty Compared to Cases with Analytical and Mixing and Sampling Uncertainties Removed

| Cluster | No uncertainties | Prediction uncertainties for all properties | Full Prediction & Composition Uncertainties | Prediction & Composition Uncertainties without Analytical Uncertainty | Prediction & Composition Uncertainties without Volume Transfer Uncertainty |
|---------|------------------|---------------------------------------------|---------------------------------------------|-----------------------------------------------------------------------|----------------------------------------------------------------------------|
| 1       | 7,946            | 7,959                                       | 8,683                                       | 8,312                                                                 | 8,540                                                                      |
| 2       | 7,973            | 8,050                                       | 8,688                                       | 8,423                                                                 | 8,554                                                                      |
| 3       | 4,238            | 4,304                                       | 4,668                                       | 4,503                                                                 | 4,576                                                                      |
| 4       | 7,597            | 7,741                                       | 8,372                                       | 8,104                                                                 | 8,229                                                                      |
| 5       | 1,734            | 1,825                                       | 1,944                                       | 1,892                                                                 | 1,922                                                                      |
| 6       | 6,838            | 6,862                                       | 7,411                                       | 7,174                                                                 | 7,289                                                                      |
| 7       | 1,649            | 1,649                                       | 1,781                                       | 1,725                                                                 | 1,750                                                                      |
| 8       | 12,893           | 12,896                                      | 13,859                                      | 13,422                                                                | 13,643                                                                     |
| 9       | 6,656            | 6,695                                       | 7,257                                       | 7,023                                                                 | 7,128                                                                      |
| 10      | 17,362           | 17,365                                      | 18,660                                      | 18,086                                                                | 18,344                                                                     |
| 11      | 18,972           | 18,974                                      | 20,356                                      | 19,715                                                                | 20,035                                                                     |
| 12      | 15,906           | 15,907                                      | 16,981                                      | 16,432                                                                | 16,685                                                                     |
| 13      | 7,553            | 7,567                                       | 8,225                                       | 7,947                                                                 | 8,056                                                                      |
| 14      | 3,270            | 3,271                                       | 3,536                                       | 3,423                                                                 | 3,472                                                                      |
| 15      | 14,919           | 15,068                                      | 16,326                                      | 15,775                                                                | 16,021                                                                     |
| 16      | 7,782            | 7,787                                       | 8,513                                       | 8,209                                                                 | 8,355                                                                      |
| 17      | 11,989           | 11,992                                      | 12,919                                      | 12,474                                                                | 12,681                                                                     |
| 18      | 3,439            | 3,444                                       | 3,689                                       | 3,575                                                                 | 3,636                                                                      |
| 19      | 8,324            | 8,326                                       | 8,907                                       | 8,628                                                                 | 8,751                                                                      |
| 20      | 6,972            | 6,974                                       | 7,491                                       | 7,256                                                                 | 7,381                                                                      |
| 21      | 1,715            | 1,756                                       | 1,911                                       | 1,835                                                                 | 1,878                                                                      |
| 22      | 7,452            | 7,547                                       | 8,165                                       | 7,890                                                                 | 8,023                                                                      |
| 23      | 7,988            | 8,213                                       | 8,821                                       | 8,546                                                                 | 8,684                                                                      |
| 24      | 15,567           | 15,573                                      | 16,833                                      | 16,275                                                                | 16,568                                                                     |
| 25      | 14,353           | 14,819                                      | 15,865                                      | 15,415                                                                | 15,660                                                                     |
| 26      | 4,763            | 4,909                                       | 5,259                                       | 5,102                                                                 | 5,180                                                                      |
| 27      | 4,461            | 4,793                                       | 5,115                                       | 4,967                                                                 | 5,058                                                                      |
| 28      | 2,062            | 2,103                                       | 2,257                                       | 2,187                                                                 | 2,220                                                                      |
| 29      | 4,676            | 5,010                                       | 5,355                                       | 5,200                                                                 | 5,287                                                                      |
| 30      | 6,774            | 7,215                                       | 7,711                                       | 7,491                                                                 | 7,613                                                                      |
| 31      | 1,381            | 1,382                                       | 1,466                                       | 1,424                                                                 | 1,448                                                                      |

| Cluster | No uncertainties | Prediction uncertainties for all properties | Full Prediction & Composition Uncertainties | Prediction & Composition Uncertainties without Analytical Uncertainty | Prediction & Composition Uncertainties without Volume Transfer Uncertainty |
|---------|------------------|---------------------------------------------|---------------------------------------------|-----------------------------------------------------------------------|----------------------------------------------------------------------------|
| 32      | 1,162            | 1,165                                       | 1,254                                       | 1,215                                                                 | 1,234                                                                      |
| 33      | 1,058            | 1,141                                       | 1,216                                       | 1,182                                                                 | 1,202                                                                      |
| 34      | 1,640            | 1,767                                       | 1,875                                       | 1,832                                                                 | 1,855                                                                      |
| 35      | 2,977            | 3,237                                       | 3,426                                       | 3,350                                                                 | 3,388                                                                      |
| 36      | 449              | 547                                         | 561                                         | 557                                                                   | 558                                                                        |
| Sum     | 252,490          | 255,833                                     | 275,359                                     | 266,566                                                               | 270,903                                                                    |

## 7.2.6 Without VHT Constraint

As most of the glasses were limited by the VHT constraint a calculation was performed to evaluate the impacts of the VHT constraint on glass mass. For full prediction and composition/process uncertainties, 275,359 MT of LAW glass is estimated. Table 17 summarizes the calculations made on LAW glasses. Removing only the VHT constraint (while keeping all other constraints with both prediction and composition uncertainties) results in an estimated 260,281 MT of LAW glass— a 5.48 relative percent reduction in glass mass. This reduction in mass translates to roughly 3 years of operation assuming 30 MT/d at 70% total online efficiency (TOE). As the correlation between VHT response and glass source-term in IDF is tenuous at best, there appears to be a significant schedule and cost driver to reevaluate this contract constraint.

Table 17. Glass Mass (MT) Projected for the Full Mission for Each of the 12 Evaluated Cases

| Case                                     | Line Rules | Prediction Uncertainties | Composition Uncertainties | Full Mission, MT |
|------------------------------------------|------------|--------------------------|---------------------------|------------------|
| 1                                        | Y          | None                     | None                      | 282,350          |
| 2                                        | Y          | All                      | All                       | 282,562          |
| 3                                        | N          | None                     | None                      | 252,490          |
| 4                                        | N          | All                      | None                      | 255,833          |
| 5                                        | N          | All but VHT              | None                      | 253,760          |
| 6                                        | N          | All but K3               | None                      | 254,268          |
| 7                                        | N          | All but $w_{SO_3}$       | None                      | 255,112          |
| 8                                        | N          | All but $\eta$           | None                      | 255,757          |
| 9                                        | N          | All                      | All                       | 275,359          |
| 10                                       | N          | All                      | All but analytical        | 266,566          |
| 11                                       | N          | All                      | All but volume transfer   | 270,903          |
| 12(a)                                    | N          | All but VHT              | All but VHT               | 260,281          |
| (a) Case 12 excludes VHT as a constraint |            |                          |                           |                  |

## 7.2.7 Evaluation of Glass Mass for Initial Phase of LAW Processing

In the first roughly 10 years of processing, the LAW vitrification facility will be fed by the LAWPS with recycles coming from the EMF. This waste is distinct in composition as seen in Figure 5 with the very high sodium content compared to all other wastes. Estimates of the uncertainty impacts for these specific clusters are useful to evaluating processing during the initial stages of plant operation. They also give an indication of the impacts of the PT process on LAW performance by difference. Evaluation of the waste feeds identified eight clusters (1-6, 8, and 9) to make up this initial time period. Table 18 summarizes the results of the 12 cases evaluated and described in Sections 7.1 and 7.2 for the full mission and also for the eight clusters of waste to be processed in the initial phase of deployment (roughly 10 years of processing). Results from the initial phase shows the same general trend as the full mission. That is the relative differences in glass masses between cases are generally the same for the initial phase and for the full mission.

Table 18. Glass Mass (MT) Projected for the Initial Phase of Processing and Full Mission for Each of the 12 Evaluated Cases

| Case                                     | Line Rules | Prediction Uncertainties  | Composition Uncertainties | Initial Phase, MT | Full Mission, MT |
|------------------------------------------|------------|---------------------------|---------------------------|-------------------|------------------|
| 1                                        | Y          | None                      | None                      | 61,520            | 282,350          |
| 2                                        | Y          | All                       | All                       | 61,633            | 282,562          |
| 3                                        | N          | None                      | None                      | 55,875            | 252,490          |
| 4                                        | N          | All                       | None                      | 56,332            | 255,833          |
| 5                                        | N          | All but VHT               | None                      | 55,953            | 253,760          |
| 6                                        | N          | All but K3                | None                      | 56,057            | 254,268          |
| 7                                        | N          | All but $w_{\text{SO}_3}$ | None                      | 56,306            | 255,112          |
| 8                                        | N          | All but $\eta$            | None                      | 56,304            | 255,757          |
| 9                                        | N          | All                       | All                       | 60,882            | 275,359          |
| 10                                       | N          | All                       | All but analytical        | 58,854            | 266,566          |
| 11                                       | N          | All                       | All but volume transfer   | 59,880            | 270,903          |
| 12(a)                                    | N          | All but VHT               | All but VHT               | 58,014            | 260,281          |
| (a) Case 12 excludes VHT as a constraint |            |                           |                           |                   |                  |

## 8.0 Summary and Conclusions

Analyses were performed to evaluate the impacts of using the advanced glass models, constraints (Vienna et al. 2016), and uncertainty descriptions on projected Hanford glass mass. Waste feed vectors supporting the SP8 (DOE 2017) were used as a basis for Hanford LAW and HLW compositions to be vitrified. The large number of waste batches (4008 for HLW and 28,458 for LAW) would not allow detailed calculations for each individual batch. Cluster analysis was performed to group the 4008 HLW batches into 30 clusters and the 28,458 LAW batches into 36 clusters, each of like composition. The maximum allowable WOL was estimated for each cluster while simultaneously satisfying all applicable glass property and composition constraints with sufficient confidence. Different components of prediction and composition/process uncertainties were systematically excluded in the calculations to evaluate their impacts on glass mass. The results of these calculations are described in the subsections below for HLW and LAW.

### 8.1 High-Level Waste

Applying the advanced glass models and constraints to the SP8 estimate of Hanford HLW generated 23,360 MT of HLW glass (7,735 canisters, assuming 3.02 MT of glass per canister) without use of uncertainty estimates. The WOL of glass is most limited by viscosity,  $T_{2\%}$ , and nepheline with a small fraction limited by single component (Al, Fe and Mn) constraints (12 wt%) as shown in Figure 14. Accounting for prediction and composition/process uncertainties resulted in 5.01 relative percent increase in estimated glass mass: 24,531 MT (8,123 canisters). Roughly equal impacts were found for prediction uncertainties (2.58 RPD) and composition/process uncertainties (2.43 RPD). The prediction uncertainties with the largest impact are:  $T_{2\%}$  >  $T_L$ -Zr > nepheline > viscosity. The composition/process uncertainties with the largest impact are: analytical > mixing and sampling > all others.

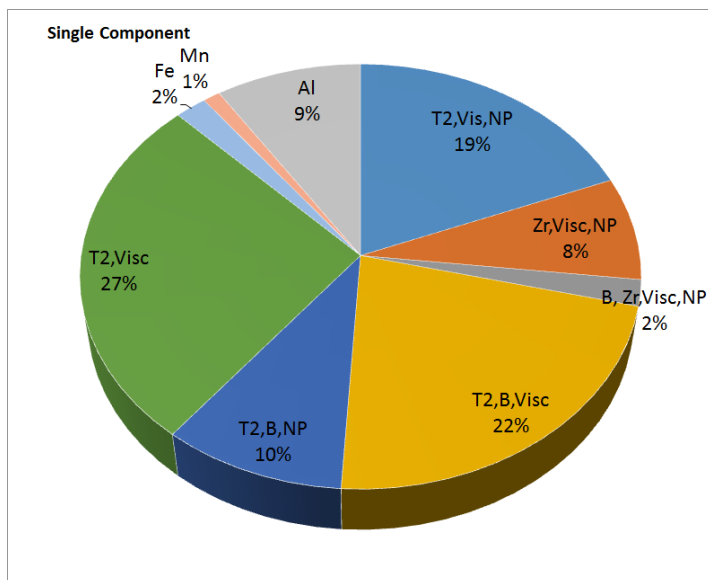


Figure 14. Waste Loading Limiting Factors (Glass Mass Basis) for HLW Glasses.

## 8.2 Low-Activity Waste

Applying the advanced glass models and constraints reported by Vienna et al. (2016) to the SP8 estimate of Hanford LAW generated 282,350 MT of LAW glass (51,243 containers, assuming 5.51 MT of glass container) without use of uncertainty estimates. The WOL of glass for all wastes were determined by the waste loading line rules (Figure 11). The glass is more limited by the alkali constraint (68%) than by the alkali plus sulfur constraint (32%), sometimes including halide constraints (28%). Accounting for prediction and composition/process uncertainties resulted in 0.08 relative percent increase in estimated glass mass: 282,562 MT (51,282 containers). The line rules were developed to simply estimate the likely WOL of LAW glass during production without recourse to a detailed set of constraints, property models, and uncertainty descriptions. The result that glass mass did not increase after application of all applicable uncertainties shows that the line rules successfully limited the loading as intended. However, they may be too conservative and unnecessarily limit WOL. Calculations were therefore performed without the line rules to determine the maximum WOL both with and without applicable uncertainties.

Table 19 summarizes the LAW glass mass estimates for a series of cases with different sources of uncertainty accounted for (see Section 7.0 for detailed explanation of each case). Without application of line rules the glass mass decreases by 10.6 relative percent (252,490 MT) for the case with no uncertainties. Addition of prediction uncertainties increases glass mass by 1.32 relative percent and the addition of composition/process uncertainties increase glass mass by an additional 7.73 relative percent (9.06 relative percent increase combined). The glass mass estimate without line rules (275,359 MT) was 2.55 relative percent lower than that with the line rules (282,562 MT), after accounting for all applicable uncertainties. These comparisons are shown in Table 20.

Table 19. LAW Glass Mass Estimates for Cases Including Various Uncertainty Terms

| Case                                      | Line Rules | Prediction Uncertainties | Composition Uncertainties | Glass Mass, MT | Containers |
|-------------------------------------------|------------|--------------------------|---------------------------|----------------|------------|
| 1                                         | Y          | None                     | None                      | 282,350        | 51,243     |
| 2                                         | Y          | All                      | All                       | 282,562        | 51,282     |
| 3                                         | N          | None                     | None                      | 252,490        | 45,824     |
| 4                                         | N          | All                      | None                      | 255,833        | 46,431     |
| 5                                         | N          | All but VHT              | None                      | 253,760        | 40,054     |
| 6                                         | N          | All but K3               | None                      | 254,268        | 46,147     |
| 7                                         | N          | All but $w_{SO_3}$       | None                      | 255,112        | 46,300     |
| 8                                         | N          | All but $\eta$           | None                      | 255,757        | 46,417     |
| 9                                         | N          | All                      | All                       | 275,359        | 49,974     |
| 10                                        | N          | All                      | All but analytical        | 266,566        | 48,379     |
| 11                                        | N          | All                      | All but volume transfer   | 270,903        | 49,166     |
| 12(a)                                     | N          | All but VHT              | All but VHT               | 260,281        | 47,238     |
| (a) Case 12 excludes VHT as a constraint. |            |                          |                           |                |            |

Table 20. Summary of Impacts of Line Rules and Uncertainties on LAW Glass Mass and Containers (a)

|                                                                                                                                                      | No Uncertainty | Property Prediction<br>Uncertainties Only | Property Prediction +<br>Composition Uncertainties |
|------------------------------------------------------------------------------------------------------------------------------------------------------|----------------|-------------------------------------------|----------------------------------------------------|
| <b>With Line Rules ON</b>                                                                                                                            |                |                                           |                                                    |
| <b>Mass (MTG)</b>                                                                                                                                    | 282,350        | 282,358                                   | 282,562                                            |
| <b>Containers</b>                                                                                                                                    | 51,243         | 51,245                                    | 51,282                                             |
| <b>RPD</b>                                                                                                                                           |                | (0%)                                      | (+0.1%)                                            |
| <b>With Line Rules OFF</b>                                                                                                                           |                |                                           |                                                    |
| <b>Mass (MTG)</b>                                                                                                                                    | 252,490        | 255,833                                   | 275,359                                            |
| <b>Containers</b>                                                                                                                                    | 45,824         | 46,431                                    | 49,974                                             |
| <b>RPD</b>                                                                                                                                           | [-11%]         | (+1%)[-9%]                                | (+9%)[-3%]                                         |
| (a) change in parentheses is relative to no uncertainty cases (e.g., left), change in square brackets is relative to the line rules cases (e.g., up) |                |                                           |                                                    |

## 9.0 References

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## Appendix A

**Table A.1. Variance covariance matrix for HLW PCT-B**

| Term                                           | Al <sub>2</sub> O <sub>3</sub> | B <sub>2</sub> O <sub>3</sub> | Fe <sub>2</sub> O <sub>3</sub> | Li <sub>2</sub> O | MgO    | Na <sub>2</sub> O | SiO <sub>2</sub> | TiO <sub>2</sub> | ZnO     | ZrO <sub>2</sub> | CaO    | P <sub>2</sub> O <sub>5</sub> | SO <sub>3</sub> | UO <sub>3</sub> | Others  | (Al <sub>2</sub> O <sub>3</sub> ) <sup>2</sup> | (Al <sub>2</sub> O <sub>3</sub> ) <sup>3</sup> | (Al <sub>2</sub> O <sub>3</sub> ) <sup>4</sup> |
|------------------------------------------------|--------------------------------|-------------------------------|--------------------------------|-------------------|--------|-------------------|------------------|------------------|---------|------------------|--------|-------------------------------|-----------------|-----------------|---------|------------------------------------------------|------------------------------------------------|------------------------------------------------|
| Al <sub>2</sub> O <sub>3</sub>                 | 9.203                          | -0.113                        | -0.284                         | -0.111            | -0.095 | -0.270            | -0.245           | -0.174           | -1.459  | 0.364            | -0.009 | -0.497                        | -0.834          | -0.409          | -0.258  | -109.681                                       | 460.920                                        | -632.078                                       |
| B <sub>2</sub> O <sub>3</sub>                  | -0.113                         | 0.132                         | 0.005                          | 0.016             | -0.049 | 0.008             | -0.019           | 0.015            | -0.033  | -0.055           | -0.006 | -0.108                        | 0.197           | 0.091           | -0.012  | 1.371                                          | -8.118                                         | 13.665                                         |
| Fe <sub>2</sub> O <sub>3</sub>                 | -0.284                         | 0.005                         | 0.119                          | -0.027            | -0.042 | -0.015            | -0.001           | -0.090           | -0.040  | 0.042            | -0.004 | -0.023                        | 0.212           | -0.037          | -0.027  | 3.232                                          | -12.304                                        | 15.482                                         |
| Li <sub>2</sub> O                              | -0.111                         | 0.016                         | -0.027                         | 0.795             | -0.024 | 0.080             | -0.077           | 0.010            | 0.156   | -0.045           | 0.106  | 0.126                         | -0.404          | -0.163          | 0.017   | 1.058                                          | -6.552                                         | 10.638                                         |
| MgO                                            | -0.095                         | -0.049                        | -0.042                         | -0.024            | 2.374  | -0.022            | -0.026           | 0.417            | 0.809   | 0.110            | -0.101 | -0.458                        | 0.708           | 0.155           | -0.075  | 1.953                                          | -6.123                                         | 4.062                                          |
| Na <sub>2</sub> O                              | -0.270                         | 0.008                         | -0.015                         | 0.080             | -0.022 | 0.124             | -0.022           | 0.007            | 0.033   | -0.036           | 0.000  | 0.040                         | -0.027          | -0.018          | 0.035   | 2.539                                          | -10.287                                        | 14.174                                         |
| SiO <sub>2</sub>                               | -0.245                         | -0.019                        | -0.001                         | -0.077            | -0.026 | -0.022            | 0.030            | -0.016           | 0.041   | -0.012           | -0.018 | 0.053                         | 0.049           | -0.004          | -0.006  | 2.853                                          | -11.185                                        | 14.607                                         |
| TiO <sub>2</sub>                               | -0.174                         | 0.015                         | -0.090                         | 0.010             | 0.417  | 0.007             | -0.016           | 1.949            | 0.632   | 0.072            | 0.035  | 0.014                         | -0.618          | 0.353           | -0.106  | 3.160                                          | -14.728                                        | 20.597                                         |
| ZnO                                            | -1.459                         | -0.033                        | -0.040                         | 0.156             | 0.809  | 0.033             | 0.041            | 0.632            | 6.980   | -0.617           | 0.180  | 0.366                         | 1.840           | 0.270           | -0.316  | 15.841                                         | -60.122                                        | 75.188                                         |
| ZrO <sub>2</sub>                               | 0.364                          | -0.055                        | 0.042                          | -0.045            | 0.110  | -0.036            | -0.012           | 0.072            | -0.617  | 0.610            | -0.048 | -0.200                        | -0.229          | 0.059           | -0.085  | -3.575                                         | 15.532                                         | -22.673                                        |
| CaO                                            | -0.009                         | -0.006                        | -0.004                         | 0.106             | -0.101 | 0.000             | -0.018           | 0.035            | 0.180   | -0.048           | 0.537  | -0.110                        | -0.210          | 0.051           | 0.021   | -0.461                                         | 3.032                                          | -5.895                                         |
| P <sub>2</sub> O <sub>5</sub>                  | -0.497                         | -0.108                        | -0.023                         | 0.126             | -0.458 | 0.040             | 0.053            | 0.014            | 0.366   | -0.200           | -0.110 | 5.066                         | 0.574           | -0.010          | -0.296  | 5.550                                          | -30.000                                        | 50.390                                         |
| SO <sub>3</sub>                                | -0.834                         | 0.197                         | 0.212                          | -0.404            | 0.708  | -0.027            | 0.049            | -0.618           | 1.840   | -0.229           | -0.210 | 0.574                         | 44.957          | -0.577          | -0.762  | -13.251                                        | 111.718                                        | -205.065                                       |
| UO <sub>3</sub>                                | -0.409                         | 0.091                         | -0.037                         | -0.163            | 0.155  | -0.018            | -0.004           | 0.353            | 0.270   | 0.059            | 0.051  | -0.010                        | -0.577          | 0.959           | -0.012  | 5.056                                          | -20.777                                        | 27.378                                         |
| Others                                         | -0.258                         | -0.012                        | -0.027                         | 0.017             | -0.075 | 0.035             | -0.006           | -0.106           | -0.316  | -0.085           | 0.021  | -0.296                        | -0.762          | -0.012          | 0.274   | 3.041                                          | -12.885                                        | 17.967                                         |
| (Al <sub>2</sub> O <sub>3</sub> ) <sup>2</sup> | -109.681                       | 1.371                         | 3.232                          | 1.058             | 1.953  | 2.539             | 2.853            | 3.160            | 15.841  | -3.575           | -0.461 | 5.550                         | -13.251         | 5.056           | 3.041   | 1379.785                                       | -6022.753                                      | 8487.915                                       |
| (Al <sub>2</sub> O <sub>3</sub> ) <sup>3</sup> | 460.920                        | -8.118                        | -12.304                        | -6.552            | -6.123 | -10.287           | -11.185          | -14.728          | -60.122 | 15.532           | 3.032  | -30.000                       | 111.718         | -20.777         | -12.885 | -6022.753                                      | 27206.367                                      | -39386.450                                     |
| (Al <sub>2</sub> O <sub>3</sub> ) <sup>4</sup> | -632.078                       | 13.665                        | 15.482                         | 10.638            | 4.062  | 14.174            | 14.607           | 20.597           | 75.188  | -22.673          | -5.895 | 50.390                        | -205.065        | 27.378          | 17.967  | 8487.915                                       | -39386.450                                     | 58302.720                                      |

**Table A.2. Variance covariance matrix for HLW PCT-Na**

| Term                                           | Al <sub>2</sub> O <sub>3</sub> | B <sub>2</sub> O <sub>3</sub> | Fe <sub>2</sub> O <sub>3</sub> | Li <sub>2</sub> O | MgO    | Na <sub>2</sub> O | SiO <sub>2</sub> | TiO <sub>2</sub> | ZnO     | ZrO <sub>2</sub> | CaO    | P <sub>2</sub> O <sub>5</sub> | SO <sub>3</sub> | UO <sub>3</sub> | Others  | (Al <sub>2</sub> O <sub>3</sub> ) <sup>2</sup> | (Al <sub>2</sub> O <sub>3</sub> ) <sup>3</sup> | (Al <sub>2</sub> O <sub>3</sub> ) <sup>4</sup> |
|------------------------------------------------|--------------------------------|-------------------------------|--------------------------------|-------------------|--------|-------------------|------------------|------------------|---------|------------------|--------|-------------------------------|-----------------|-----------------|---------|------------------------------------------------|------------------------------------------------|------------------------------------------------|
| Al <sub>2</sub> O <sub>3</sub>                 | 7.049                          | -0.088                        | -0.219                         | -0.093            | -0.081 | -0.213            | -0.184           | -0.136           | -1.134  | 0.291            | -0.009 | -0.380                        | -0.667          | -0.315          | -0.203  | -83.939                                        | 352.587                                        | -483.369                                       |
| B <sub>2</sub> O <sub>3</sub>                  | -0.088                         | 0.100                         | 0.004                          | 0.013             | -0.037 | 0.006             | -0.015           | 0.011            | -0.024  | -0.043           | -0.004 | -0.082                        | 0.151           | 0.070           | -0.009  | 1.061                                          | -6.249                                         | 10.492                                         |
| Fe <sub>2</sub> O <sub>3</sub>                 | -0.219                         | 0.004                         | 0.091                          | -0.020            | -0.032 | -0.011            | -0.001           | -0.068           | -0.029  | 0.031            | -0.003 | -0.017                        | 0.164           | -0.028          | -0.020  | 2.489                                          | -9.473                                         | 11.921                                         |
| Li <sub>2</sub> O                              | -0.093                         | 0.013                         | -0.020                         | 0.608             | -0.016 | 0.063             | -0.059           | 0.008            | 0.124   | -0.038           | 0.082  | 0.096                         | -0.301          | -0.123          | 0.014   | 0.894                                          | -5.324                                         | 8.525                                          |
| MgO                                            | -0.081                         | -0.037                        | -0.032                         | -0.016            | 1.811  | -0.015            | -0.020           | 0.319            | 0.622   | 0.081            | -0.076 | -0.348                        | 0.546           | 0.119           | -0.055  | 1.569                                          | -4.971                                         | 3.482                                          |
| Na <sub>2</sub> O                              | -0.213                         | 0.006                         | -0.011                         | 0.063             | -0.015 | 0.095             | -0.017           | 0.006            | 0.029   | -0.030           | 0.001  | 0.031                         | -0.015          | -0.013          | 0.028   | 2.001                                          | -8.088                                         | 11.117                                         |
| SiO <sub>2</sub>                               | -0.184                         | -0.015                        | -0.001                         | -0.059            | -0.020 | -0.017            | 0.023            | -0.013           | 0.030   | -0.009           | -0.014 | 0.040                         | 0.036           | -0.003          | -0.005  | 2.152                                          | -8.440                                         | 11.027                                         |
| TiO <sub>2</sub>                               | -0.136                         | 0.011                         | -0.068                         | 0.008             | 0.319  | 0.006             | -0.013           | 1.485            | 0.484   | 0.054            | 0.027  | 0.011                         | -0.468          | 0.269           | -0.080  | 2.440                                          | -11.343                                        | 15.846                                         |
| ZnO                                            | -1.134                         | -0.024                        | -0.029                         | 0.124             | 0.622  | 0.029             | 0.030            | 0.484            | 5.332   | -0.479           | 0.139  | 0.280                         | 1.421           | 0.207           | -0.237  | 12.293                                         | -46.653                                        | 58.353                                         |
| ZrO <sub>2</sub>                               | 0.291                          | -0.043                        | 0.031                          | -0.038            | 0.081  | -0.030            | -0.009           | 0.054            | -0.479  | 0.470            | -0.037 | -0.153                        | -0.186          | 0.044           | -0.067  | -2.862                                         | 12.358                                         | -17.937                                        |
| CaO                                            | -0.009                         | -0.004                        | -0.003                         | 0.082             | -0.076 | 0.001             | -0.014           | 0.027            | 0.139   | -0.037           | 0.410  | -0.084                        | -0.158          | 0.039           | 0.017   | -0.331                                         | 2.236                                          | -4.400                                         |
| P <sub>2</sub> O <sub>5</sub>                  | -0.380                         | -0.082                        | -0.017                         | 0.096             | -0.348 | 0.031             | 0.040            | 0.011            | 0.280   | -0.153           | -0.084 | 3.860                         | 0.439           | -0.007          | -0.225  | 4.244                                          | -22.916                                        | 38.467                                         |
| SO <sub>3</sub>                                | -0.667                         | 0.151                         | 0.164                          | -0.301            | 0.546  | -0.015            | 0.036            | -0.468           | 1.421   | -0.186           | -0.158 | 0.439                         | 34.282          | -0.437          | -0.575  | -9.785                                         | 83.944                                         | -154.758                                       |
| UO <sub>3</sub>                                | -0.315                         | 0.070                         | -0.028                         | -0.123            | 0.119  | -0.013            | -0.003           | 0.269            | 0.207   | 0.044            | 0.039  | -0.007                        | -0.437          | 0.731           | -0.009  | 3.885                                          | -15.956                                        | 21.019                                         |
| Others                                         | -0.203                         | -0.009                        | -0.020                         | 0.014             | -0.055 | 0.028             | -0.005           | -0.080           | -0.237  | -0.067           | 0.017  | -0.225                        | -0.575          | -0.009          | 0.210   | 2.382                                          | -10.062                                        | 13.999                                         |
| (Al <sub>2</sub> O <sub>3</sub> ) <sup>2</sup> | -83.939                        | 1.061                         | 2.489                          | 0.894             | 1.569  | 2.001             | 2.152            | 2.440            | 12.293  | -2.862           | -0.331 | 4.244                         | -9.785          | 3.885           | 2.382   | 1054.954                                       | -4602.750                                      | 6484.726                                       |
| (Al <sub>2</sub> O <sub>3</sub> ) <sup>3</sup> | 352.587                        | -6.249                        | -9.473                         | -5.324            | -4.971 | -8.088            | -8.440           | -11.343          | -46.653 | 12.358           | 2.236  | -22.916                       | 83.944          | -15.956         | -10.062 | -4602.750                                      | 20781.754                                      | -30076.171                                     |
| (Al <sub>2</sub> O <sub>3</sub> ) <sup>4</sup> | -483.369                       | 10.492                        | 11.921                         | 8.525             | 3.482  | 11.117            | 11.027           | 15.846           | 58.353  | -17.937          | -4.400 | 38.467                        | -154.758        | 21.019          | 13.999  | 6484.726                                       | -30076.171                                     | 44506.919                                      |

**Table A.3. Variance covariance matrix for HLW PCT-Li**

| Term                                           | Al <sub>2</sub> O <sub>3</sub> | B <sub>2</sub> O <sub>3</sub> | Fe <sub>2</sub> O <sub>3</sub> | Li <sub>2</sub> O | MgO    | Na <sub>2</sub> O | SiO <sub>2</sub> | TiO <sub>2</sub> | ZnO     | ZrO <sub>2</sub> | CaO    | P <sub>2</sub> O <sub>5</sub> | SO <sub>3</sub> | UO <sub>3</sub> | Others | (Al <sub>2</sub> O <sub>3</sub> ) <sup>2</sup> | (Al <sub>2</sub> O <sub>3</sub> ) <sup>3</sup> | (Al <sub>2</sub> O <sub>3</sub> ) <sup>4</sup> |
|------------------------------------------------|--------------------------------|-------------------------------|--------------------------------|-------------------|--------|-------------------|------------------|------------------|---------|------------------|--------|-------------------------------|-----------------|-----------------|--------|------------------------------------------------|------------------------------------------------|------------------------------------------------|
| Al <sub>2</sub> O <sub>3</sub>                 | 7.098                          | -0.077                        | -0.232                         | -0.078            | -0.072 | -0.196            | -0.191           | -0.112           | -0.986  | 0.262            | 0.057  | -0.385                        | -0.453          | -0.299          | -0.200 | -85.124                                        | 358.041                                        | -490.306                                       |
| B <sub>2</sub> O <sub>3</sub>                  | -0.077                         | 0.111                         | 0.008                          | 0.030             | -0.043 | 0.004             | -0.019           | 0.011            | -0.044  | -0.041           | -0.010 | -0.104                        | 0.154           | 0.075           | -0.008 | 0.941                                          | -5.976                                         | 10.366                                         |
| Fe <sub>2</sub> O <sub>3</sub>                 | -0.232                         | 0.008                         | 0.102                          | -0.001            | -0.042 | -0.017            | -0.003           | -0.075           | -0.075  | 0.038            | -0.018 | -0.026                        | 0.178           | -0.029          | -0.019 | 2.613                                          | -9.830                                         | 12.218                                         |
| Li <sub>2</sub> O                              | -0.078                         | 0.030                         | -0.001                         | 0.874             | -0.029 | 0.040             | -0.083           | 0.032            | 0.096   | -0.021           | 0.024  | 0.162                         | -0.202          | -0.124          | 0.017  | 0.413                                          | -3.920                                         | 7.535                                          |
| MgO                                            | -0.072                         | -0.043                        | -0.042                         | -0.029            | 2.023  | -0.018            | -0.022           | 0.390            | 0.961   | 0.092            | -0.063 | -0.261                        | 0.980           | 0.149           | -0.078 | 1.308                                          | -2.761                                         | -1.029                                         |
| Na <sub>2</sub> O                              | -0.196                         | 0.004                         | -0.017                         | 0.040             | -0.018 | 0.102             | -0.016           | 0.003            | 0.021   | -0.030           | -0.001 | 0.021                         | -0.054          | -0.014          | 0.030  | 1.853                                          | -7.594                                         | 10.564                                         |
| SiO <sub>2</sub>                               | -0.191                         | -0.019                        | -0.003                         | -0.083            | -0.022 | -0.016            | 0.026            | -0.015           | 0.034   | -0.011           | -0.009 | 0.042                         | 0.014           | -0.006          | -0.006 | 2.283                                          | -8.965                                         | 11.674                                         |
| TiO <sub>2</sub>                               | -0.112                         | 0.011                         | -0.075                         | 0.032             | 0.390  | 0.003             | -0.015           | 1.476            | 0.646   | 0.055            | 0.037  | 0.035                         | -0.319          | 0.274           | -0.090 | 2.084                                          | -9.719                                         | 13.435                                         |
| ZnO                                            | -0.986                         | -0.044                        | -0.075                         | 0.096             | 0.961  | 0.021             | 0.034            | 0.646            | 6.503   | -0.490           | 0.231  | 0.352                         | 2.519           | 0.222           | -0.344 | 10.202                                         | -36.838                                        | 43.623                                         |
| ZrO <sub>2</sub>                               | 0.262                          | -0.041                        | 0.038                          | -0.021            | 0.092  | -0.030            | -0.011           | 0.055            | -0.490  | 0.463            | -0.037 | -0.156                        | -0.170          | 0.046           | -0.060 | -2.584                                         | 11.485                                         | -17.096                                        |
| CaO                                            | 0.057                          | -0.010                        | -0.018                         | 0.024             | -0.063 | -0.001            | -0.009           | 0.037            | 0.231   | -0.037           | 0.497  | -0.114                        | -0.135          | 0.043           | 0.008  | -1.017                                         | 5.007                                          | -8.235                                         |
| P <sub>2</sub> O <sub>5</sub>                  | -0.385                         | -0.104                        | -0.026                         | 0.162             | -0.261 | 0.021             | 0.042            | 0.035            | 0.352   | -0.156           | -0.114 | 4.173                         | 0.424           | -0.023          | -0.248 | 4.536                                          | -25.465                                        | 43.392                                         |
| SO <sub>3</sub>                                | -0.453                         | 0.154                         | 0.178                          | -0.202            | 0.980  | -0.054            | 0.014            | -0.319           | 2.519   | -0.170           | -0.135 | 0.424                         | 35.222          | -0.409          | -0.646 | -13.188                                        | 101.530                                        | -182.219                                       |
| UO <sub>3</sub>                                | -0.299                         | 0.075                         | -0.029                         | -0.124            | 0.149  | -0.014            | -0.006           | 0.274            | 0.222   | 0.046            | 0.043  | -0.023                        | -0.409          | 0.727           | -0.006 | 3.705                                          | -15.159                                        | 19.809                                         |
| Others                                         | -0.200                         | -0.008                        | -0.019                         | 0.017             | -0.078 | 0.030             | -0.006           | -0.090           | -0.344  | -0.060           | 0.008  | -0.248                        | -0.646          | -0.006          | 0.220  | 2.347                                          | -9.831                                         | 13.595                                         |
| (Al <sub>2</sub> O <sub>3</sub> ) <sup>2</sup> | -85.124                        | 0.941                         | 2.613                          | 0.413             | 1.308  | 1.853             | 2.283            | 2.084            | 10.202  | -2.584           | -1.017 | 4.536                         | -13.188         | 3.705           | 2.347  | 1077.438                                       | -4706.340                                      | 6621.798                                       |
| (Al <sub>2</sub> O <sub>3</sub> ) <sup>3</sup> | 358.041                        | -5.976                        | -9.830                         | -3.920            | -2.761 | -7.594            | -8.965           | -9.719           | -36.838 | 11.485           | 5.007  | -25.465                       | 101.530         | -15.159         | -9.831 | -4706.340                                      | 21282.228                                      | -30765.789                                     |
| (Al <sub>2</sub> O <sub>3</sub> ) <sup>4</sup> | -490.306                       | 10.366                        | 12.218                         | 7.535             | -1.029 | 10.564            | 11.674           | 13.435           | 43.623  | -17.096          | -8.235 | 43.392                        | -182.219        | 19.809          | 13.595 | 6621.798                                       | -30765.789                                     | 45480.242                                      |

**Table A.4. Variance covariance matrix for HLW TL-ZR**

| Term                           | Al <sub>2</sub> O <sub>3</sub> | B <sub>2</sub> O <sub>3</sub> | Ln <sub>2</sub> O <sub>3</sub> | Li <sub>2</sub> O | Na <sub>2</sub> O | SrO         | ZrO <sub>2</sub> | Others    |
|--------------------------------|--------------------------------|-------------------------------|--------------------------------|-------------------|-------------------|-------------|------------------|-----------|
| Al <sub>2</sub> O <sub>3</sub> | 36866.261                      | -5799.889                     | 44567.343                      | -26798.297        | -13555.884        | -36355.717  | 17890.969        | -363.724  |
| B <sub>2</sub> O <sub>3</sub>  | -5799.889                      | 9277.831                      | -19508.584                     | 2450.367          | 7865.096          | -23166.554  | -6514.831        | -1173.851 |
| Ln <sub>2</sub> O <sub>3</sub> | 44567.343                      | -19508.584                    | 224350.880                     | -29383.636        | -26904.436        | 60874.755   | 42864.823        | -3878.191 |
| Li <sub>2</sub> O              | -26798.297                     | 2450.367                      | -29383.636                     | 58010.595         | 16883.040         | 102908.803  | -32737.169       | -369.637  |
| Na <sub>2</sub> O              | -13555.884                     | 7865.096                      | -26904.436                     | 16883.040         | 26584.493         | 6667.999    | -16736.785       | -2897.094 |
| SrO                            | -36355.717                     | -23166.554                    | 60874.755                      | 102908.803        | 6667.999          | 2095713.065 | -9353.337        | -7281.736 |
| ZrO <sub>2</sub>               | 17890.969                      | -6514.831                     | 42864.823                      | -32737.169        | -16736.785        | -9353.337   | 33140.190        | -1150.326 |
| Others                         | -363.724                       | -1173.851                     | -3878.191                      | -369.637          | -2897.094         | -7281.736   | -1150.326        | 1042.873  |

**Table A.5. Variance covariance matrix for HLW T<sub>2</sub>%**

| Term                                              | Al <sub>2</sub> O <sub>3</sub> | B <sub>2</sub> O <sub>3</sub> | Bi <sub>2</sub> O <sub>3</sub> | Cr <sub>2</sub> O <sub>3</sub> | Fe <sub>2</sub> O <sub>3</sub> | Li <sub>2</sub> O | MgO        | MnO        | Na <sub>2</sub> O | NiO        | RuO <sub>2</sub> | TiO <sub>2</sub> | ZnO        | ZrO <sub>2</sub> | Others    | Al <sub>2</sub> O <sub>3</sub> ·Na <sub>2</sub> O | ZrO <sub>2</sub> ·ZrO <sub>2</sub> |
|---------------------------------------------------|--------------------------------|-------------------------------|--------------------------------|--------------------------------|--------------------------------|-------------------|------------|------------|-------------------|------------|------------------|------------------|------------|------------------|-----------|---------------------------------------------------|------------------------------------|
| Al <sub>2</sub> O <sub>3</sub>                    | 60368.27                       | -20613.59                     | -471.59                        | -23232.87                      | -1230.25                       | -12900.76         | -17615.06  | -204.61    | 36511.73          | -9544.46   | -152196.86       | -448.53          | 20084.23   | -856.41          | -4149.22  | -483655.12                                        | 10144.14                           |
| B <sub>2</sub> O <sub>3</sub>                     | -20613.59                      | 17698.99                      | -7410.85                       | -5673.46                       | -2503.15                       | 1129.30           | 6542.99    | 1347.34    | -7189.48          | 5935.64    | 4225.23          | -4439.65         | -12233.95  | -1505.35         | 44.57     | 126396.11                                         | -3891.75                           |
| Bi <sub>2</sub> O <sub>3</sub>                    | -471.59                        | -7410.85                      | 137578.42                      | -100575.                       | 6775.61                        | 13326.02          | 20528.15   | 4547.47    | -341.88           | -121900.33 | 755885.62        | -33339.67        | -9171.17   | 43686.68         | -1746.88  | 2400.97                                           | -438059.42                         |
| Cr <sub>2</sub> O <sub>3</sub>                    | -23232.87                      | -5673.46                      | -100575.                       | 1110498.                       | 23719.73                       | 2226.62           | 61216.95   | 27819.63   | -30185.42         | 113575.30  | 2145584.22       | -19596.99        | -7085.39   | 45860.52         | -10272.6  | 215702.76                                         | -407432.93                         |
| Fe <sub>2</sub> O <sub>3</sub>                    | -1230.25                       | -2503.15                      | 6775.61                        | 23719.73                       | 15769.82                       | -67.11            | 2428.91    | 1385.40    | -10125.87         | 8409.86    | 424971.63        | 17292.47         | 8193.02    | -13350.45        | -2301.69  | 50472.07                                          | 245738.97                          |
| Li <sub>2</sub> O                                 | -12900.76                      | 1129.30                       | 13326.02                       | 2226.62                        | -67.11                         | 90102.51          | 943.42     | 1429.88    | 6553.71           | -28967.94  | 668307.09        | -14329.94        | -17417.53  | 1761.70          | -5875.61  | 48601.46                                          | -293698.81                         |
| MgO                                               | -17615.06                      | 6542.99                       | 20528.15                       | 61216.95                       | 2428.91                        | 943.42            | 709299.15  | 15238.16   | -18771.81         | 30201.64   | 1037656.03       | -51944.64        | -32226.03  | 27544.73         | -3902.98  | 144349.77                                         | -268439.89                         |
| MnO                                               | -204.61                        | 1347.34                       | 4547.47                        | 27819.63                       | 1385.40                        | 1429.88           | 15238.16   | 52050.05   | -6824.52          | 34792.05   | -58522.84        | -19271.56        | -9937.39   | 29839.57         | -3535.55  | 41911.02                                          | -350375.98                         |
| Na <sub>2</sub> O                                 | 36511.73                       | -7189.48                      | -341.88                        | -30185.42                      | -10125.9                       | 6553.71           | -18771.81  | -6824.52   | 47547.00          | -59350.78  | -219485.71       | -12973.24        | -816.62    | -10690.73        | -3839.11  | -415621.73                                        | -22616.55                          |
| NiO                                               | -9544.46                       | 5935.64                       | -121900.                       | 113575.30                      | 8409.86                        | -28967.94         | 30201.64   | 34792.05   | -59350.78         | 1014828.   | 570369.89        | -105785.9        | 72690.31   | -117909.88       | -3607.64  | 251148.47                                         | 1298993.8                          |
| RuO <sub>2</sub>                                  | -152196.9                      | 4225.23                       | 755885.6                       | 2145584.                       | 424971.6                       | 668307.09         | 1037656.   | -58522.84  | -219485.7         | 570369.89  | 170952473.       | 97577.52         | -2409503.8 | -1442569.        | -206156.6 | 2370858.3                                         | 15238190.5                         |
| TiO <sub>2</sub>                                  | -448.53                        | -4439.65                      | -33339.67                      | -19596.99                      | 17292.47                       | -14329.94         | -51944.64  | -19271.56  | -12973.24         | -105785.88 | 97577.52         | 789035.44        | -22957.88  | -38504.21        | 901.17    | 49773.71                                          | 899957.55                          |
| ZnO                                               | 20084.23                       | -12233.95                     | -9171.17                       | -7085.39                       | 8193.02                        | -17417.53         | -32226.03  | -9937.39   | -816.62           | 72690.31   | -2409503.78      | -22957.88        | 239519.88  | 39765.05         | -5114.86  | -39076.91                                         | -409132.58                         |
| ZrO <sub>2</sub>                                  | -856.41                        | -1505.35                      | 43686.68                       | 45860.52                       | -13350.45                      | 1761.70           | 27544.73   | 29839.57   | -10690.73         | -117909.88 | -1442569.11      | -38504.21        | 39765.05   | 408969.47        | -4828.46  | 68236.47                                          | -5266742.6                         |
| Others                                            | -4149.22                       | 44.57                         | -1746.88                       | -10272.59                      | -2301.69                       | -5875.61          | -3902.98   | -3535.55   | -3839.11          | -3607.64   | -206156.57       | 901.17           | -5114.86   | -4828.46         | 2700.45   | 33479.29                                          | 59822.84                           |
| Al <sub>2</sub> O <sub>3</sub> ·Na <sub>2</sub> O | -483655.12                     | 126396.11                     | 2400.97                        | 215702.76                      | 50472.1                        | 48601.46          | 144349.77  | 41911.02   | -415621.7         | 251148.47  | 2370858.38       | 49773.71         | -39076.91  | 68236.47         | 33479.29  | 4784519.66                                        | 166795.91                          |
| ZrO <sub>2</sub> ·ZrO <sub>2</sub>                | 10144.14                       | -3891.75                      | -438059.42                     | -407432.93                     | 245739                         | -293698.81        | -268439.89 | -350375.98 | -22616.55         | 1298993.79 | 15238190.47      | 899957.55        | -409132.6  | -5266742.63      | 59822.84  | 166795.91                                         | 77191014.                          |

**Table A.6. Variance covariance matrix for HLW Nepheline**

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.732                                       | 0.804                          | 0.294            | -64.085   | 498.338   | -102.179  | -522.382  |
| 1.654                                       | 0.974                          | 0.255            | -69.306   | 523.697   | -102.02   | -554.696  |
| 1.815                                       | 0.982                          | 0.245            | -69.82    | 504.258   | -93.033   | -530.758  |
| 2.012                                       | 0.607                          | 0.286            | -77.127   | 560.992   | -107.989  | -575.491  |
| 1.778                                       | 0.942                          | 0.333            | -71.162   | 556.967   | -114.326  | -586.02   |
| 1.807                                       | 0.593                          | 0.274            | -80.132   | 582.966   | -109.369  | -607.526  |
| 1.828                                       | 0.715                          | 0.282            | -66.338   | 496.473   | -98.574   | -514.944  |
| 1.705                                       | 0.899                          | 0.322            | -71.346   | 544.912   | -109.32   | -572.611  |
| 1.643                                       | 0.544                          | 0.264            | -34.3     | 395.61    | -106.811  | -425.436  |
| 1.672                                       | 1.03                           | 0.277            | -65.45    | 553.441   | -119.95   | -594.517  |
| 1.855                                       | 0.539                          | 0.344            | -93.729   | 631.804   | -109.069  | -649.925  |
| 1.65                                        | 0.637                          | 0.267            | -83.695   | 628.311   | -126.212  | -651.855  |
| 1.618                                       | 0.963                          | 0.278            | -50.874   | 408.029   | -85.916   | -431.775  |
| 1.794                                       | 0.705                          | 0.29             | -87.186   | 580.708   | -98.442   | -599.056  |
| 1.773                                       | 0.785                          | 0.378            | -73.586   | 556.052   | -109.311  | -584.665  |
| 1.686                                       | 0.782                          | 0.316            | -49.509   | 432.382   | -98.655   | -457.659  |
| 1.682                                       | 0.796                          | 0.223            | -52.026   | 496.116   | -122.697  | -522.931  |
| 1.777                                       | 0.916                          | 0.324            | -58.455   | 473.791   | -100.744  | -499.552  |
| 1.811                                       | 0.565                          | 0.28             | -62.782   | 478.354   | -97.063   | -493.649  |
| 1.662                                       | 1.019                          | 0.379            | -71.464   | 518.407   | -94.556   | -552.83   |
| 1.678                                       | 0.727                          | 0.317            | -65.711   | 497.053   | -96.891   | -523.932  |
| 1.784                                       | 0.831                          | 0.318            | -54.455   | 424.272   | -86.466   | -446.519  |
| 1.727                                       | 0.586                          | 0.225            | -80.038   | 590.794   | -115.386  | -610.845  |
| 1.586                                       | 0.784                          | 0.28             | -46.716   | 432.276   | -104.302  | -457.404  |
| 1.598                                       | 0.74                           | 0.264            | -57.88    | 499.073   | -114.652  | -524.028  |
| 1.554                                       | 1.114                          | 0.253            | -67.02    | 503.589   | -96.995   | -537.395  |
| 1.724                                       | 1.03                           | 0.313            | -75.168   | 554.308   | -105.611  | -586.15   |
| 1.576                                       | 0.914                          | 0.232            | -72.091   | 542.545   | -105.792  | -574.014  |
| 1.564                                       | 0.341                          | 0.308            | -85.379   | 629.37    | -125.156  | -646.389  |
| 1.633                                       | 0.723                          | 0.283            | -55.518   | 459.021   | -101.074  | -481.858  |
| 1.823                                       | 0.684                          | 0.23             | -111.343  | 684.572   | -100.41   | -703.098  |
| 1.692                                       | 0.868                          | 0.235            | -38.334   | 369.373   | -90.123   | -393.991  |
| 1.683                                       | 0.649                          | 0.206            | -63.333   | 504.042   | -108.752  | -519.71   |
| 1.98                                        | 0.922                          | 0.281            | -80.279   | 610.007   | -122.045  | -634.75   |
| 1.55                                        | 0.569                          | 0.27             | -44.1     | 439.951   | -110.373  | -468.211  |
| 1.658                                       | 0.869                          | 0.364            | -53.355   | 445.142   | -96.213   | -474.346  |
| 1.777                                       | 1.029                          | 0.394            | -82.927   | 595.326   | -106.748  | -632.852  |
| 1.659                                       | 1.037                          | 0.309            | -74.691   | 555.91    | -108.841  | -585.366  |
| 1.648                                       | 0.827                          | 0.37             | -65.326   | 509.463   | -103.505  | -539.408  |
| 1.717                                       | 0.941                          | 0.343            | -81.852   | 644.707   | -131.087  | -684.996  |
| 1.781                                       | 0.726                          | 0.279            | -43.645   | 405.697   | -97.124   | -427.978  |
| 1.61                                        | 0.83                           | 0.271            | -42.94    | 390.691   | -91.639   | -416.281  |
| 1.914                                       | 0.842                          | 0.286            | -49.111   | 395.753   | -83.562   | -415.137  |
| 1.644                                       | 0.776                          | 0.368            | -85.899   | 640.656   | -123.517  | -674.423  |
| 1.773                                       | 0.623                          | 0.231            | -53.73    | 438.293   | -94.616   | -457.759  |
| 1.772                                       | 0.707                          | 0.218            | -63.175   | 502.164   | -108.146  | -519.584  |
| 1.829                                       | 0.743                          | 0.341            | -67.748   | 497.377   | -94.081   | -521.316  |
| 1.857                                       | 0.799                          | 0.308            | -68.2     | 506.522   | -99.81    | -525.283  |
| 1.457                                       | 0.467                          | 0.249            | -17.905   | 379.496   | -128.116  | -415.328  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.796                                       | 0.811                          | 0.301            | -74.886   | 579.531   | -118.729  | -604.633  |
| 1.671                                       | 0.866                          | 0.26             | -58.668   | 481.495   | -101.501  | -512.106  |
| 1.736                                       | 0.976                          | 0.332            | -94.13    | 614.253   | -99.672   | -641.666  |
| 1.508                                       | 1.197                          | 0.221            | -78.467   | 583.29    | -112.8    | -619.686  |
| 1.746                                       | 1.151                          | 0.323            | -69.031   | 520.581   | -101.346  | -552.495  |
| 1.68                                        | 0.671                          | 0.258            | -55.552   | 433.197   | -89.947   | -451.495  |
| 1.574                                       | 0.683                          | 0.346            | -53.415   | 516.512   | -125.909  | -553.772  |
| 1.706                                       | 0.648                          | 0.197            | -58.025   | 468.677   | -103.366  | -483.504  |
| 1.763                                       | 0.767                          | 0.225            | -64.086   | 484.678   | -97.498   | -503.891  |
| 1.809                                       | 0.619                          | 0.236            | -65.693   | 513.159   | -107.04   | -530.324  |
| 1.887                                       | 0.757                          | 0.308            | -73.255   | 561.868   | -113.53   | -584.984  |
| 1.51                                        | 1.077                          | 0.255            | -77.196   | 608.643   | -124.729  | -649.542  |
| 1.66                                        | 0.875                          | 0.199            | -70.053   | 539.402   | -109.061  | -566.184  |
| 1.535                                       | 0.979                          | 0.237            | -54.018   | 434.202   | -94.107   | -457.697  |
| 1.729                                       | 0.745                          | 0.25             | -69.171   | 552.435   | -118.968  | -574.837  |
| 1.746                                       | 0.988                          | 0.263            | -57.687   | 473.168   | -101.861  | -500.892  |
| 1.711                                       | 0.736                          | 0.263            | -61.984   | 495.079   | -105.753  | -514.925  |
| 1.619                                       | 0.978                          | 0.278            | -79.411   | 601.83    | -118.726  | -636.697  |
| 1.649                                       | 0.597                          | 0.249            | -63.405   | 479.704   | -94.752   | -500.59   |
| 1.575                                       | 0.898                          | 0.192            | -59.337   | 486.45    | -105.298  | -512.822  |
| 1.681                                       | 0.863                          | 0.221            | -49.311   | 406.185   | -89.523   | -424.074  |
| 1.772                                       | 0.939                          | 0.38             | -33.256   | 408.445   | -112.888  | -446.064  |
| 1.64                                        | 0.613                          | 0.224            | -65.29    | 515.795   | -110.236  | -533.837  |
| 1.865                                       | 0.974                          | 0.332            | -80.414   | 612.099   | -122.405  | -641.065  |
| 1.814                                       | 0.721                          | 0.293            | -60.775   | 461.552   | -93.25    | -478.786  |
| 1.812                                       | 0.979                          | 0.366            | -61.145   | 480.306   | -96.681   | -510.683  |
| 1.795                                       | 0.658                          | 0.29             | -65.013   | 517.043   | -110.437  | -536.032  |
| 1.757                                       | 1.019                          | 0.328            | -81.555   | 621.4     | -123.422  | -656.274  |
| 1.806                                       | 1.076                          | 0.417            | -72.92    | 574.923   | -117.574  | -611.834  |
| 1.785                                       | 0.73                           | 0.254            | -67.465   | 538.582   | -114.03   | -562.416  |
| 1.932                                       | 0.791                          | 0.252            | -95.495   | 616.342   | -99.732   | -633.065  |
| 1.528                                       | 1.094                          | 0.233            | -61.142   | 541.303   | -123.453  | -583.155  |
| 1.696                                       | 0.813                          | 0.311            | -61.192   | 499.353   | -107.116  | -526.826  |
| 1.795                                       | 0.939                          | 0.357            | -60.73    | 457.462   | -89.613   | -482.421  |
| 1.698                                       | 0.768                          | 0.323            | -47.005   | 403.206   | -87.956   | -431.622  |
| 1.807                                       | 0.745                          | 0.243            | -69.383   | 544.932   | -115.717  | -562.926  |
| 1.547                                       | 0.758                          | 0.331            | -66.127   | 497.1     | -98.248   | -523.547  |
| 1.748                                       | 0.963                          | 0.232            | -81.239   | 620.363   | -125.731  | -648.265  |
| 1.656                                       | 0.496                          | 0.191            | -70.123   | 543.481   | -113.332  | -560.143  |
| 1.85                                        | 0.614                          | 0.318            | -58.022   | 477.286   | -104.352  | -496.386  |
| 1.853                                       | 0.891                          | 0.28             | -75.279   | 569.419   | -115.722  | -590.443  |
| 1.708                                       | 0.662                          | 0.368            | -59.414   | 491.152   | -105.468  | -519.082  |
| 1.678                                       | 0.596                          | 0.153            | -39.379   | 373.084   | -93.491   | -387.228  |
| 1.696                                       | 0.751                          | 0.29             | -73.708   | 578.795   | -120.691  | -605.324  |
| 1.475                                       | 0.732                          | 0.191            | -54.132   | 404.681   | -78.65    | -426.761  |
| 1.673                                       | 0.675                          | 0.251            | -54.113   | 448.129   | -98.311   | -468.955  |
| 1.804                                       | 0.835                          | 0.332            | -80.99    | 577.556   | -107.722  | -600.856  |
| 1.768                                       | 0.618                          | 0.233            | -92.581   | 611.565   | -103.542  | -626.845  |
| 1.764                                       | 0.499                          | 0.414            | -57.429   | 473.656   | -102.412  | -496.134  |
| 1.867                                       | 0.92                           | 0.329            | -64.17    | 506.547   | -104.075  | -534.172  |
| 1.749                                       | 0.887                          | 0.303            | -66.519   | 496.663   | -95.557   | -524.241  |
| 1.63                                        | 0.953                          | 0.197            | -64.118   | 505.728   | -106.338  | -530.679  |
| 1.779                                       | 0.706                          | 0.319            | -65.395   | 524.824   | -110.347  | -550.809  |
| 1.664                                       | 0.877                          | 0.368            | -73.841   | 597.995   | -125.401  | -636.265  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.54                                        | 0.659                          | 0.208            | -28.071   | 375.405   | -109.848  | -404.739  |
| 1.681                                       | 1.313                          | 0.299            | -105.006  | 719.667   | -122.765  | -764.89   |
| 1.78                                        | 0.739                          | 0.317            | -77.36    | 554.817   | -102.486  | -578.999  |
| 1.886                                       | 0.793                          | 0.33             | -81.45    | 554.373   | -96.476   | -574.174  |
| 1.437                                       | 1.139                          | 0.274            | -81.141   | 602.272   | -112.379  | -649      |
| 2.008                                       | 0.674                          | 0.252            | -79.259   | 547.907   | -99.329   | -559.744  |
| 1.711                                       | 0.723                          | 0.398            | -74.453   | 564.885   | -110.727  | -595.514  |
| 1.778                                       | 0.931                          | 0.291            | -65.447   | 521.998   | -110.856  | -546.636  |
| 1.627                                       | 1.001                          | 0.325            | -63.676   | 498.372   | -100.173  | -531.715  |
| 1.736                                       | 0.944                          | 0.362            | -80.694   | 582.035   | -106.9    | -614.684  |
| 1.728                                       | 0.67                           | 0.182            | -57.508   | 448.954   | -95.813   | -461.706  |
| 1.92                                        | 0.793                          | 0.276            | -70.939   | 531.751   | -103.876  | -554.952  |
| 1.624                                       | 0.882                          | 0.263            | -66.598   | 515.916   | -105.591  | -543.118  |
| 1.922                                       | 0.808                          | 0.326            | -63.837   | 532.372   | -117.394  | -555.903  |
| 1.798                                       | 0.618                          | 0.215            | -66.54    | 518.555   | -109.402  | -533.445  |
| 1.758                                       | 0.646                          | 0.277            | -63.348   | 474.016   | -95.105   | -489.598  |
| 1.801                                       | 0.714                          | 0.352            | -61.002   | 486.152   | -101.381  | -510.646  |
| 1.912                                       | 0.584                          | 0.227            | -83.07    | 577.52    | -106.164  | -588.441  |
| 1.859                                       | 0.743                          | 0.3              | -89.136   | 581.563   | -97.841   | -594.436  |
| 1.925                                       | 0.661                          | 0.282            | -78.394   | 557.477   | -103.086  | -576.479  |
| 1.712                                       | 0.657                          | 0.342            | -75.131   | 551.73    | -105.473  | -575.715  |
| 1.75                                        | 0.689                          | 0.267            | -58.937   | 463.073   | -96.297   | -483.775  |
| 1.754                                       | 0.898                          | 0.317            | -78.091   | 567.98    | -107.528  | -594.33   |
| 1.735                                       | 0.674                          | 0.275            | -63.785   | 499.75    | -102.95   | -522.582  |
| 1.747                                       | 0.92                           | 0.257            | -81.471   | 555.874   | -95.291   | -581.333  |
| 1.761                                       | 0.792                          | 0.317            | -58.626   | 480.875   | -103.805  | -506.122  |
| 1.762                                       | 0.865                          | 0.226            | -69.927   | 526.122   | -101.99   | -554.407  |
| 1.741                                       | 0.712                          | 0.247            | -73.316   | 554.38    | -112.141  | -574.384  |
| 1.812                                       | 0.791                          | 0.293            | -76.893   | 561.171   | -107.452  | -584.34   |
| 1.852                                       | 0.827                          | 0.367            | -47.787   | 418.646   | -96.303   | -441.796  |
| 1.729                                       | 0.649                          | 0.177            | -63.633   | 469.665   | -92.177   | -486.248  |
| 1.648                                       | 0.788                          | 0.363            | -69.957   | 534.682   | -107.619  | -562.239  |
| 1.731                                       | 0.671                          | 0.249            | -65.744   | 487.587   | -95.784   | -506.117  |
| 1.637                                       | 1.009                          | 0.282            | -46.497   | 412.023   | -94.498   | -440.417  |
| 1.698                                       | 0.653                          | 0.278            | -81.623   | 617.066   | -124.411  | -641.779  |
| 1.63                                        | 1.081                          | 0.204            | -105.875  | 698.113   | -114.613  | -731.753  |
| 1.888                                       | 1.03                           | 0.479            | -130.558  | 787.698   | -107.32   | -825.078  |
| 1.788                                       | 0.991                          | 0.319            | -59.042   | 484.777   | -104.699  | -511.921  |
| 1.629                                       | 0.745                          | 0.245            | -67.485   | 530.403   | -111.503  | -552.985  |
| 1.848                                       | 0.867                          | 0.354            | -55.493   | 453.401   | -96.324   | -478.658  |
| 1.714                                       | 0.756                          | 0.272            | -75.508   | 536.986   | -97.744   | -561.781  |
| 1.933                                       | 0.811                          | 0.364            | -75.974   | 557.205   | -106.902  | -579.818  |
| 1.805                                       | 1.011                          | 0.326            | -84.97    | 609.537   | -112.564  | -640.513  |
| 1.81                                        | 0.711                          | 0.302            | -62.116   | 498.829   | -105.068  | -522.325  |
| 1.606                                       | 0.698                          | 0.235            | -64.237   | 510       | -109.74   | -530.368  |
| 1.682                                       | 0.696                          | 0.249            | -65.672   | 508.714   | -103.126  | -533.323  |
| 1.587                                       | 0.888                          | 0.268            | -64.301   | 527.276   | -114.508  | -557.713  |
| 1.696                                       | 0.873                          | 0.362            | -43.647   | 424.347   | -102.893  | -457.667  |
| 1.785                                       | 0.589                          | 0.186            | -61.326   | 477.683   | -98.965   | -494.265  |
| 1.806                                       | 0.98                           | 0.379            | -82.145   | 632.689   | -128.184  | -664.268  |
| 1.758                                       | 0.904                          | 0.346            | -60.843   | 481.992   | -100.827  | -506.472  |
| 1.622                                       | 0.786                          | 0.305            | -76.583   | 597.806   | -124.626  | -625.849  |
| 1.607                                       | 0.862                          | 0.233            | -71.369   | 537.596   | -106.293  | -564.76   |
| 1.761                                       | 0.909                          | 0.226            | -80.239   | 596.473   | -119.822  | -616.945  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.615                                       | 0.661                          | 0.187            | -51.542   | 421.997   | -90.498   | -443.962  |
| 1.568                                       | 0.776                          | 0.274            | -60.361   | 490.547   | -105.899  | -516.283  |
| 1.577                                       | 0.861                          | 0.298            | -56.992   | 487.714   | -110.108  | -516.238  |
| 1.838                                       | 0.709                          | 0.278            | -69.332   | 516.48    | -100.919  | -537.274  |
| 1.86                                        | 0.656                          | 0.309            | -71.026   | 495.611   | -89.676   | -512.437  |
| 1.755                                       | 0.537                          | 0.323            | -103.895  | 641.663   | -97.544   | -655.118  |
| 1.718                                       | 0.985                          | 0.403            | -79.741   | 594.522   | -113.984  | -630.591  |
| 1.92                                        | 0.837                          | 0.341            | -66.983   | 524.129   | -107.488  | -549.109  |
| 1.559                                       | 0.479                          | 0.286            | -57.114   | 470.676   | -102.369  | -494.182  |
| 1.755                                       | 0.88                           | 0.308            | -78.639   | 576.96    | -111.222  | -602.148  |
| 1.521                                       | 0.966                          | 0.181            | -65.069   | 520.346   | -109.275  | -552.774  |
| 1.629                                       | 1.001                          | 0.293            | -73.846   | 558.725   | -111.257  | -589.672  |
| 1.741                                       | 0.85                           | 0.3              | -61.661   | 500.34    | -107.884  | -523.777  |
| 1.641                                       | 1.079                          | 0.311            | -84.487   | 607.231   | -110.924  | -644.217  |
| 1.608                                       | 0.714                          | 0.204            | -68.376   | 518.288   | -104.672  | -539.979  |
| 1.779                                       | 0.583                          | 0.293            | -71.812   | 520.2     | -98.369   | -538.31   |
| 1.644                                       | 0.994                          | 0.272            | -71.565   | 570.244   | -119.37   | -605.356  |
| 1.885                                       | 0.915                          | 0.298            | -59.814   | 444.201   | -86.861   | -462.479  |
| 1.871                                       | 0.929                          | 0.289            | -92.764   | 659.397   | -122.838  | -684.407  |
| 1.758                                       | 0.599                          | 0.204            | -57.185   | 458.355   | -96.726   | -478.202  |
| 1.873                                       | 0.675                          | 0.362            | -85.589   | 596.783   | -107.916  | -616.987  |
| 1.637                                       | 0.891                          | 0.266            | -60.731   | 478.913   | -97.854   | -508.009  |
| 1.737                                       | 0.656                          | 0.316            | -70.534   | 548.695   | -115.095  | -568.814  |
| 1.825                                       | 0.832                          | 0.273            | -80.756   | 590.078   | -113.51   | -612.233  |
| 1.768                                       | 0.767                          | 0.39             | -64.069   | 512.981   | -105.575  | -544.699  |
| 1.672                                       | 1.169                          | 0.243            | -90.443   | 657.199   | -121.2    | -698.826  |
| 1.737                                       | 0.92                           | 0.368            | -77.612   | 610.596   | -122.815  | -652.384  |
| 1.51                                        | 0.865                          | 0.226            | -71.628   | 531.636   | -104.28   | -558.783  |
| 1.737                                       | 0.78                           | 0.326            | -64.997   | 518.756   | -108.006  | -547.614  |
| 1.592                                       | 0.763                          | 0.243            | -56.1     | 471.261   | -106.449  | -493.688  |
| 1.751                                       | 0.785                          | 0.237            | -49.339   | 424.915   | -96.086   | -446.937  |
| 1.641                                       | 0.72                           | 0.395            | -50.532   | 451.817   | -102.637  | -483.896  |
| 1.555                                       | 0.75                           | 0.305            | -65.418   | 508.281   | -104.139  | -535.244  |
| 1.585                                       | 0.518                          | 0.248            | -65.376   | 490.388   | -97.32    | -510.14   |
| 1.701                                       | 0.967                          | 0.334            | -49.77    | 446.073   | -102.218  | -478.807  |
| 1.777                                       | 0.739                          | 0.289            | -53.413   | 482.439   | -114.58   | -506.073  |
| 1.57                                        | 0.824                          | 0.315            | -56.579   | 479.589   | -107.818  | -505.916  |
| 1.644                                       | 1.058                          | 0.365            | -89.868   | 684.573   | -136.662  | -724.284  |
| 1.734                                       | 0.713                          | 0.288            | -67.918   | 532.562   | -111.971  | -553.561  |
| 1.959                                       | 0.788                          | 0.419            | -104.635  | 648.296   | -95.33    | -670.653  |
| 1.563                                       | 0.548                          | 0.18             | -72.705   | 549.914   | -113.261  | -566.424  |
| 1.576                                       | 0.797                          | 0.278            | -80.082   | 605.017   | -119.361  | -637.621  |
| 1.6                                         | 0.878                          | 0.294            | -51.674   | 457.674   | -103.351  | -492.202  |
| 1.905                                       | 0.562                          | 0.241            | -71.741   | 541.322   | -109.739  | -554.702  |
| 1.686                                       | 0.687                          | 0.262            | -71.595   | 540.872   | -108.791  | -562.321  |
| 1.691                                       | 1.005                          | 0.266            | -66.992   | 561.859   | -125.613  | -591.127  |
| 1.678                                       | 0.783                          | 0.263            | -57.331   | 484.157   | -108.016  | -508.864  |
| 1.77                                        | 0.923                          | 0.318            | -81.913   | 641.91    | -132.463  | -674.973  |
| 1.652                                       | 0.942                          | 0.276            | -68.53    | 537.478   | -110.156  | -568.453  |
| 1.689                                       | 0.858                          | 0.236            | -61.028   | 489.127   | -103.033  | -516.279  |
| 1.827                                       | 0.813                          | 0.288            | -74.32    | 588.045   | -122.174  | -616.056  |
| 1.775                                       | 0.838                          | 0.275            | -60.565   | 487.202   | -103.39   | -510.689  |
| 1.546                                       | 1.125                          | 0.308            | -75.823   | 606.304   | -123.699  | -653.715  |
| 1.601                                       | 1.29                           | 0.31             | -73.521   | 542.43    | -99.475   | -587.439  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.652                                       | 0.878                          | 0.246            | -60.717   | 469.319   | -96.015   | -492.053  |
| 1.753                                       | 0.911                          | 0.348            | -62.865   | 480.48    | -95.752   | -506.643  |
| 1.736                                       | 0.976                          | 0.363            | -78.08    | 598.829   | -119.356  | -633.626  |
| 1.783                                       | 0.789                          | 0.318            | -62.691   | 500.769   | -105.419  | -525.805  |
| 1.874                                       | 0.77                           | 0.331            | -95.292   | 653.491   | -116.707  | -673.78   |
| 1.743                                       | 0.949                          | 0.359            | -74.833   | 582.909   | -119.016  | -615.645  |
| 1.742                                       | 0.697                          | 0.299            | -50.237   | 412.898   | -89.934   | -432.167  |
| 1.813                                       | 0.874                          | 0.316            | -66.269   | 498.455   | -99.6     | -518.967  |
| 1.64                                        | 0.789                          | 0.274            | -59.213   | 516.604   | -116.217  | -551.728  |
| 1.665                                       | 0.745                          | 0.303            | -65.656   | 523.554   | -112.162  | -547.404  |
| 1.769                                       | 0.836                          | 0.372            | -75.146   | 562.53    | -107.808  | -594.752  |
| 1.821                                       | 0.663                          | 0.45             | -69.491   | 518.096   | -98.799   | -545.086  |
| 1.571                                       | 0.838                          | 0.282            | -57.822   | 480.873   | -104.091  | -511.774  |
| 1.595                                       | 0.756                          | 0.346            | -55.306   | 498.151   | -116.013  | -530.216  |
| 1.822                                       | 0.951                          | 0.377            | -55.288   | 448.514   | -95.137   | -475.215  |
| 1.854                                       | 0.799                          | 0.284            | -70.502   | 552.694   | -114.39   | -576.391  |
| 1.894                                       | 1.107                          | 0.413            | -79       | 602.374   | -116.947  | -642.209  |
| 1.809                                       | 0.813                          | 0.274            | -62.067   | 492.108   | -103.379  | -513.374  |
| 1.596                                       | 1.121                          | 0.274            | -71.095   | 544.347   | -107.679  | -580.704  |
| 1.578                                       | 0.881                          | 0.241            | -71.968   | 551.404   | -109.2    | -584.211  |
| 1.636                                       | 0.909                          | 0.241            | -78.798   | 581.901   | -111.45   | -612.386  |
| 1.791                                       | 0.822                          | 0.314            | -70.811   | 537.916   | -107.146  | -563.358  |
| 1.696                                       | 0.753                          | 0.348            | -66.375   | 519.162   | -107.787  | -543.089  |
| 1.706                                       | 0.866                          | 0.347            | -47.053   | 393.152   | -86.672   | -415.433  |
| 1.768                                       | 0.802                          | 0.214            | -61.05    | 499.815   | -107.407  | -525.025  |
| 1.714                                       | 0.745                          | 0.257            | -81.237   | 566.895   | -103.339  | -586.899  |
| 1.646                                       | 0.799                          | 0.239            | -61.001   | 473.578   | -98.023   | -494.392  |
| 1.725                                       | 0.514                          | 0.315            | -70.963   | 540.284   | -110.381  | -558.432  |
| 1.807                                       | 0.751                          | 0.344            | -78.934   | 554.249   | -100.916  | -575.871  |
| 1.908                                       | 0.705                          | 0.318            | -64.969   | 495.337   | -99.097   | -514.451  |
| 1.916                                       | 0.942                          | 0.347            | -74.295   | 560.363   | -111.297  | -585.732  |
| 1.668                                       | 0.804                          | 0.341            | -79.221   | 561.089   | -101.408  | -589.167  |
| 1.551                                       | 1.267                          | 0.375            | -73.759   | 541.299   | -100.721  | -581.463  |
| 1.816                                       | 0.784                          | 0.305            | -57.98    | 443.18    | -89.486   | -462.108  |
| 1.831                                       | 1.195                          | 0.285            | -71.269   | 523.264   | -99.253   | -552.101  |
| 1.837                                       | 0.738                          | 0.255            | -71.44    | 538.995   | -108.607  | -558.056  |
| 1.774                                       | 0.782                          | 0.398            | -73.381   | 570       | -116.62   | -598.616  |
| 1.677                                       | 0.928                          | 0.35             | -67.344   | 531.918   | -110.748  | -561.591  |
| 1.771                                       | 0.911                          | 0.4              | -64.902   | 507.291   | -102.746  | -537.041  |
| 1.886                                       | 0.76                           | 0.326            | -50.543   | 428.889   | -95.983   | -448.942  |
| 1.905                                       | 0.892                          | 0.309            | -82.437   | 579.914   | -106.333  | -600.585  |
| 1.702                                       | 0.661                          | 0.311            | -64.758   | 516.166   | -110.031  | -537.585  |
| 1.708                                       | 0.66                           | 0.263            | -45.298   | 478.62    | -126.182  | -505.87   |
| 1.666                                       | 0.787                          | 0.355            | -70.449   | 501.876   | -91.891   | -527.052  |
| 1.646                                       | 0.543                          | 0.278            | -38.688   | 361.926   | -87.264   | -381.852  |
| 1.565                                       | 1.114                          | 0.287            | -62.56    | 484.419   | -97.234   | -516.037  |
| 1.683                                       | 0.823                          | 0.277            | -67.446   | 490.33    | -92.508   | -513.206  |
| 1.807                                       | 0.948                          | 0.306            | -67.455   | 534.214   | -112.069  | -560.266  |
| 1.926                                       | 0.829                          | 0.289            | -67.985   | 535.077   | -110.609  | -559.287  |
| 1.711                                       | 0.775                          | 0.317            | -60.592   | 481.112   | -101.222  | -503.472  |
| 1.536                                       | 0.629                          | 0.29             | -44.357   | 412.816   | -98.335   | -440.015  |
| 1.559                                       | 0.97                           | 0.214            | -80.347   | 603.875   | -118.492  | -637.307  |
| 1.807                                       | 0.712                          | 0.323            | -75.053   | 583.369   | -119.399  | -609.034  |
| 1.706                                       | 0.88                           | 0.325            | -60.516   | 483.651   | -99.681   | -513.68   |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.624                                       | 0.826                          | 0.27             | -62.412   | 477.909   | -96.721   | -500.913  |
| 1.78                                        | 0.881                          | 0.249            | -60.791   | 495.797   | -106.774  | -520.719  |
| 1.608                                       | 0.753                          | 0.283            | -90.02    | 684.118   | -137.716  | -716.351  |
| 1.654                                       | 0.508                          | 0.26             | -63.533   | 505.724   | -109.928  | -521.698  |
| 1.853                                       | 1.036                          | 0.462            | -83.351   | 557.823   | -93.378   | -585.112  |
| 1.785                                       | 0.824                          | 0.259            | -65.228   | 531.854   | -115.273  | -556.584  |
| 1.648                                       | 0.54                           | 0.245            | -79.444   | 574.812   | -110.708  | -593.264  |
| 1.389                                       | 1.219                          | 0.322            | -67.799   | 549.64    | -110.325  | -604.459  |
| 1.727                                       | 0.949                          | 0.346            | -56.458   | 448.553   | -93.51    | -473.944  |
| 1.546                                       | 0.703                          | 0.201            | -62.98    | 492.314   | -100.533  | -519.122  |
| 1.831                                       | 0.763                          | 0.301            | -74.851   | 534.195   | -98.721   | -555.697  |
| 1.683                                       | 0.763                          | 0.244            | -55.898   | 457.981   | -99.403   | -479.963  |
| 1.82                                        | 0.822                          | 0.217            | -53.68    | 438.47    | -94.636   | -459.013  |
| 1.638                                       | 0.758                          | 0.321            | -38.987   | 370.285   | -90.213   | -393.161  |
| 1.535                                       | 0.781                          | 0.256            | -48.118   | 422.937   | -96.877   | -449.827  |
| 1.543                                       | 1.177                          | 0.287            | -79.313   | 611.401   | -120.022  | -658.062  |
| 1.476                                       | 1.117                          | 0.309            | -65.485   | 494.793   | -95.091   | -532.458  |
| 1.669                                       | 0.881                          | 0.192            | -69.115   | 524.672   | -103.191  | -552.796  |
| 1.651                                       | 0.808                          | 0.21             | -82.914   | 623.659   | -124.522  | -650.221  |
| 1.771                                       | 0.802                          | 0.238            | -80.052   | 542.921   | -96.868   | -557.042  |
| 1.697                                       | 1.017                          | 0.291            | -59.666   | 470.6     | -97.03    | -497.767  |
| 1.579                                       | 0.497                          | 0.261            | -48.111   | 428.161   | -99.779   | -451.226  |
| 1.781                                       | 0.786                          | 0.313            | -72.153   | 532.78    | -103.384  | -554.722  |
| 1.674                                       | 0.959                          | 0.259            | -77.348   | 558.083   | -104.656  | -585.486  |
| 1.708                                       | 0.811                          | 0.365            | -97.919   | 636.362   | -102.057  | -663.623  |
| 1.883                                       | 0.974                          | 0.299            | -90.313   | 615.69    | -103.763  | -647.809  |
| 1.727                                       | 0.831                          | 0.339            | -61.65    | 495.671   | -106.082  | -520.934  |
| 1.624                                       | 0.868                          | 0.32             | -71.949   | 590.391   | -129.562  | -621.051  |
| 1.635                                       | 0.642                          | 0.255            | -60.488   | 505.083   | -112.246  | -527.773  |
| 1.696                                       | 0.814                          | 0.202            | -60.301   | 467.34    | -97.398   | -486.792  |
| 1.949                                       | 0.788                          | 0.324            | -68.462   | 516.147   | -102.311  | -536.827  |
| 1.658                                       | 0.846                          | 0.299            | -68.522   | 535.017   | -111.22   | -560.691  |
| 1.76                                        | 0.803                          | 0.391            | -67.628   | 507.745   | -98.513   | -535.422  |
| 1.762                                       | 0.721                          | 0.255            | -64.051   | 462.143   | -88.333   | -477.861  |
| 1.591                                       | 0.699                          | 0.317            | -58.596   | 475.28    | -100.208  | -503.922  |
| 1.74                                        | 0.956                          | 0.228            | -57.078   | 449.23    | -93.195   | -471.539  |
| 1.697                                       | 0.94                           | 0.369            | -74.207   | 600.467   | -127.529  | -636.898  |
| 1.763                                       | 0.62                           | 0.299            | -58.247   | 457.569   | -95.299   | -476.517  |
| 1.848                                       | 0.675                          | 0.325            | -74.545   | 538.018   | -99.619   | -561.801  |
| 1.756                                       | 0.996                          | 0.359            | -72.922   | 530.223   | -101.004  | -555.562  |
| 1.686                                       | 0.795                          | 0.306            | -75.621   | 572.522   | -115.135  | -597.584  |
| 1.762                                       | 0.776                          | 0.197            | -79.405   | 588.025   | -114.855  | -610.63   |
| 1.757                                       | 0.765                          | 0.28             | -56.495   | 478.082   | -107.506  | -500.873  |
| 1.443                                       | 0.625                          | 0.23             | -34.438   | 373.923   | -100.377  | -398.262  |
| 1.854                                       | 0.668                          | 0.318            | -108.606  | 679.496   | -104.837  | -696.743  |
| 1.897                                       | 0.912                          | 0.354            | -92.581   | 601.054   | -96.977   | -624.164  |
| 1.821                                       | 0.905                          | 0.258            | -96.189   | 649.948   | -110.285  | -677.327  |
| 1.831                                       | 0.84                           | 0.343            | -75.435   | 572.512   | -113.469  | -601.416  |
| 1.85                                        | 0.553                          | 0.222            | -87.509   | 612.63    | -112.48   | -628.829  |
| 1.715                                       | 0.848                          | 0.326            | -62.118   | 483.011   | -100.168  | -505.875  |
| 1.624                                       | 0.723                          | 0.31             | -76.859   | 571.504   | -111.416  | -598.966  |
| 1.78                                        | 0.789                          | 0.267            | -56.816   | 449.406   | -94.26    | -469.463  |
| 1.81                                        | 0.609                          | 0.226            | -64.422   | 526.606   | -115.076  | -545.544  |
| 1.525                                       | 1.055                          | 0.301            | -76.342   | 563.24    | -106.099  | -600.498  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.719                                       | 1.02                           | 0.375            | -65.957   | 516.992   | -103.888  | -553.789  |
| 1.76                                        | 0.604                          | 0.342            | -64.182   | 529.047   | -114.851  | -554.118  |
| 1.754                                       | 1.011                          | 0.188            | -88.366   | 628.009   | -114.221  | -660.484  |
| 1.733                                       | 0.883                          | 0.258            | -64.964   | 611.597   | -148.107  | -649.798  |
| 1.615                                       | 0.787                          | 0.252            | -66.174   | 528.733   | -112.523  | -555.093  |
| 1.658                                       | 0.959                          | 0.378            | -74.346   | 573.799   | -115.686  | -607.467  |
| 1.77                                        | 0.943                          | 0.306            | -41.55    | 340.628   | -70.919   | -363.919  |
| 1.831                                       | 0.752                          | 0.262            | -73.246   | 551.863   | -112.493  | -568.558  |
| 1.798                                       | 0.855                          | 0.336            | -69.867   | 537.823   | -108.976  | -563.932  |
| 1.653                                       | 0.488                          | 0.318            | -67.524   | 525.318   | -108.687  | -546.558  |
| 1.674                                       | 0.658                          | 0.28             | -70.63    | 543.783   | -110.648  | -567.735  |
| 1.878                                       | 0.696                          | 0.319            | -106.174  | 634.958   | -91.574   | -645.461  |
| 1.822                                       | 0.924                          | 0.304            | -69.008   | 546.605   | -115.008  | -572.009  |
| 1.969                                       | 0.464                          | 0.206            | -51.479   | 423.463   | -93.025   | -435.275  |
| 1.695                                       | 0.65                           | 0.265            | -75.906   | 557.884   | -107.147  | -580.848  |
| 1.622                                       | 0.835                          | 0.28             | -62.129   | 518.413   | -113.808  | -547.821  |
| 1.868                                       | 0.851                          | 0.187            | -68.856   | 538.026   | -113.774  | -554.656  |
| 1.976                                       | 0.549                          | 0.321            | -62.287   | 524.05    | -115.627  | -545.99   |
| 1.87                                        | 0.905                          | 0.194            | -49.526   | 417.429   | -94.659   | -434.837  |
| 1.748                                       | 0.789                          | 0.286            | -71.711   | 537.331   | -106.311  | -560.184  |
| 1.91                                        | 0.767                          | 0.343            | -85.671   | 563.643   | -94.51    | -579.57   |
| 1.735                                       | 0.864                          | 0.34             | -55.96    | 429.263   | -84.911   | -453.689  |
| 1.644                                       | 0.756                          | 0.274            | -67.949   | 507.308   | -97.677   | -534.447  |
| 1.776                                       | 0.751                          | 0.285            | -70.294   | 533.213   | -105.179  | -558.857  |
| 1.78                                        | 0.842                          | 0.31             | -73.324   | 576.912   | -120.351  | -603.474  |
| 1.885                                       | 0.738                          | 0.354            | -76.359   | 566.818   | -108.537  | -593.529  |
| 1.647                                       | 0.667                          | 0.141            | -70.14    | 519.971   | -102.73   | -538.938  |
| 1.554                                       | 0.683                          | 0.23             | -88.437   | 618.713   | -112.445  | -643.539  |
| 1.666                                       | 0.759                          | 0.266            | -48.313   | 450.734   | -107.41   | -478.734  |
| 1.7                                         | 0.967                          | 0.253            | -83.177   | 562.263   | -96.171   | -588.233  |
| 1.61                                        | 0.596                          | 0.295            | -73.121   | 550.368   | -109.813  | -572.724  |
| 1.659                                       | 0.688                          | 0.299            | -66.734   | 502.331   | -99.176   | -524.749  |
| 1.838                                       | 0.818                          | 0.39             | -60.864   | 452.817   | -85.774   | -478.664  |
| 1.655                                       | 0.899                          | 0.288            | -66.73    | 533.596   | -111.92   | -564.721  |
| 1.714                                       | 0.735                          | 0.255            | -56.908   | 478.969   | -107.108  | -501.304  |
| 1.649                                       | 0.806                          | 0.377            | -86.206   | 590.305   | -103.575  | -615.408  |
| 1.753                                       | 0.572                          | 0.248            | -70.99    | 527.569   | -105.086  | -543.278  |
| 1.549                                       | 0.457                          | 0.278            | -51.56    | 449.429   | -102.364  | -473.213  |
| 1.757                                       | 0.544                          | 0.237            | -68.254   | 504.626   | -99.813   | -519.042  |
| 1.837                                       | 0.703                          | 0.252            | -44.959   | 430.226   | -106.415  | -451.033  |
| 1.786                                       | 0.612                          | 0.257            | -71.039   | 491.114   | -89.584   | -503.434  |
| 1.817                                       | 0.826                          | 0.363            | -122.013  | 752.966   | -114.992  | -771.024  |
| 2.026                                       | 0.782                          | 0.323            | -81.993   | 583.389   | -106.499  | -605.23   |
| 1.655                                       | 1.075                          | 0.332            | -107.491  | 690.773   | -107.466  | -725.592  |
| 1.589                                       | 0.925                          | 0.231            | -80.531   | 598.45    | -115.956  | -630.279  |
| 1.72                                        | 0.955                          | 0.33             | -69.293   | 538.618   | -108.926  | -569.186  |
| 1.746                                       | 0.999                          | 0.367            | -73.187   | 556.246   | -109.476  | -587.828  |
| 1.557                                       | 0.749                          | 0.281            | -50.645   | 462.363   | -110.718  | -489.431  |
| 1.629                                       | 1.047                          | 0.34             | -74.339   | 523.83    | -93.03    | -555.531  |
| 1.868                                       | 1.007                          | 0.294            | -70.186   | 518.638   | -99.133   | -545.289  |
| 1.89                                        | 0.844                          | 0.362            | -58.566   | 479.098   | -101.509  | -507.61   |
| 1.592                                       | 0.756                          | 0.242            | -51.519   | 423.82    | -92.254   | -445.55   |
| 2.033                                       | 0.651                          | 0.118            | -71.118   | 520.112   | -103.047  | -529.013  |
| 1.837                                       | 0.953                          | 0.225            | -57.238   | 445.066   | -91.154   | -466.273  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.649                                       | 0.777                          | 0.146            | -90.74    | 686.958   | -139.203  | -713.759  |
| 1.859                                       | 0.832                          | 0.36             | -79.97    | 601.16    | -118.07   | -629.464  |
| 1.611                                       | 0.717                          | 0.183            | -48.504   | 448.247   | -108.448  | -470.309  |
| 1.669                                       | 0.751                          | 0.29             | -58.921   | 481.227   | -103.801  | -505.983  |
| 1.901                                       | 0.865                          | 0.322            | -88.108   | 656.922   | -126.724  | -689.284  |
| 1.726                                       | 0.692                          | 0.218            | -73.443   | 529.679   | -100.59   | -548.638  |
| 1.668                                       | 0.643                          | 0.311            | -41.599   | 399.086   | -97.206   | -423.948  |
| 1.79                                        | 0.755                          | 0.319            | -71.423   | 541.965   | -108.32   | -565.519  |
| 1.847                                       | 0.879                          | 0.349            | -61.008   | 509.677   | -112.482  | -535.537  |
| 1.675                                       | 0.77                           | 0.249            | -62.693   | 477.882   | -95.36    | -500.982  |
| 1.64                                        | 0.755                          | 0.265            | -61.511   | 471.85    | -97.69    | -489.81   |
| 1.658                                       | 0.88                           | 0.271            | -63.039   | 495.189   | -103.564  | -518.779  |
| 1.811                                       | 0.739                          | 0.212            | -62.444   | 487.363   | -101.122  | -505.402  |
| 1.786                                       | 0.953                          | 0.359            | -75.805   | 606.489   | -127.852  | -639.893  |
| 1.757                                       | 0.914                          | 0.242            | -70.774   | 531.407   | -105.328  | -555.865  |
| 1.744                                       | 0.686                          | 0.375            | -84.733   | 604.42    | -110.991  | -631.378  |
| 1.728                                       | 0.639                          | 0.249            | -70.284   | 539.46    | -108.305  | -563.169  |
| 1.538                                       | 1.109                          | 0.212            | -74.957   | 548.256   | -102.646  | -583.538  |
| 1.74                                        | 0.719                          | 0.245            | -59.551   | 473.477   | -100.826  | -492.571  |
| 1.489                                       | 1.315                          | 0.311            | -88.015   | 596.741   | -98       | -640.77   |
| 1.751                                       | 0.711                          | 0.315            | -54.393   | 440.868   | -94.344   | -461.336  |
| 1.587                                       | 0.826                          | 0.26             | -52.99    | 439.104   | -95.089   | -466.36   |
| 1.564                                       | 0.63                           | 0.231            | -45.711   | 440.771   | -109.515  | -465.286  |
| 1.722                                       | 0.758                          | 0.309            | -67.225   | 571.327   | -128.266  | -599.935  |
| 1.739                                       | 0.751                          | 0.199            | -73.453   | 538.934   | -105.417  | -557.547  |
| 1.715                                       | 0.895                          | 0.322            | -81.328   | 607.805   | -118.631  | -638.448  |
| 1.64                                        | 0.856                          | 0.25             | -67.438   | 508.171   | -100.046  | -534.522  |
| 1.902                                       | 0.565                          | 0.244            | -77.365   | 541.38    | -100.589  | -552.373  |
| 1.808                                       | 0.871                          | 0.321            | -56.487   | 466.793   | -100.144  | -494.271  |
| 1.637                                       | 0.99                           | 0.256            | -65.46    | 513.869   | -104.194  | -546.815  |
| 1.627                                       | 0.628                          | 0.291            | -49.06    | 433.377   | -100.069  | -457.228  |
| 1.562                                       | 0.716                          | 0.302            | -70.917   | 539.671   | -107.648  | -567.065  |
| 1.734                                       | 0.574                          | 0.182            | -67.918   | 520.894   | -106.299  | -539.391  |
| 1.661                                       | 0.746                          | 0.253            | -61.565   | 492.624   | -106.427  | -513.735  |
| 1.651                                       | 0.715                          | 0.268            | -44.9     | 449.265   | -112.412  | -479.771  |
| 1.501                                       | 0.839                          | 0.297            | -52.294   | 458.27    | -103.256  | -491.663  |
| 1.65                                        | 0.807                          | 0.32             | -61.485   | 475.62    | -94.007   | -505.489  |
| 1.613                                       | 0.274                          | 0.206            | -65.983   | 522.961   | -112.1    | -535.95   |
| 1.778                                       | 0.878                          | 0.352            | -67.496   | 546.591   | -118.552  | -571.836  |
| 1.66                                        | 1.078                          | 0.287            | -87.542   | 621.319   | -112.072  | -656.847  |
| 1.671                                       | 0.817                          | 0.316            | -76.988   | 537.469   | -95.024   | -564.34   |
| 1.902                                       | 0.748                          | 0.282            | -63.238   | 512.904   | -112.032  | -530.082  |
| 1.696                                       | 0.898                          | 0.373            | -71.926   | 561.709   | -114.751  | -594.362  |
| 1.685                                       | 0.72                           | 0.286            | -70.616   | 511.166   | -94.892   | -537.273  |
| 1.735                                       | 0.531                          | 0.253            | -71.291   | 541.129   | -110.35   | -557.878  |
| 1.674                                       | 0.568                          | 0.184            | -59.116   | 458.372   | -96.672   | -470.741  |
| 1.583                                       | 0.934                          | 0.333            | -73.295   | 558.674   | -110.901  | -591.942  |
| 1.718                                       | 0.759                          | 0.25             | -44.155   | 414.346   | -100.242  | -437.673  |
| 2.033                                       | 0.794                          | 0.279            | -126.842  | 781.414   | -120.237  | -791.785  |
| 1.832                                       | 0.795                          | 0.351            | -70.334   | 495.339   | -90.265   | -515.454  |
| 1.681                                       | 0.627                          | 0.251            | -55.448   | 426.115   | -86.606   | -444.638  |
| 2.043                                       | 0.705                          | 0.299            | -122.497  | 761.809   | -118.824  | -773.049  |
| 1.571                                       | 0.853                          | 0.269            | -63.956   | 504.852   | -105.537  | -533.28   |
| 1.665                                       | 0.555                          | 0.272            | -77.209   | 555.787   | -106.455  | -572.736  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.72                                        | 0.937                          | 0.257            | -43.851   | 385.008   | -89.338   | -407.418  |
| 1.634                                       | 1.003                          | 0.185            | -127.288  | 851.812   | -143.866  | -890.744  |
| 1.872                                       | 0.83                           | 0.306            | -61.232   | 463.453   | -94.34    | -480.138  |
| 1.713                                       | 0.678                          | 0.243            | -54.098   | 461.849   | -102.887  | -485.342  |
| 1.88                                        | 0.547                          | 0.264            | -61.879   | 506.621   | -109.947  | -526.264  |
| 1.937                                       | 0.776                          | 0.306            | -65.119   | 478.505   | -91.213   | -498.518  |
| 1.739                                       | 0.638                          | 0.32             | -89.657   | 666.732   | -131.849  | -690.996  |
| 1.77                                        | 0.9                            | 0.353            | -66.977   | 539.283   | -112.909  | -570.313  |
| 1.839                                       | 0.886                          | 0.364            | -70.37    | 516.026   | -97.289   | -542.264  |
| 1.719                                       | 0.764                          | 0.303            | -69.111   | 537.214   | -108.682  | -565.111  |
| 1.747                                       | 0.989                          | 0.316            | -72.662   | 534.863   | -102.612  | -562.25   |
| 1.664                                       | 0.614                          | 0.247            | -63.799   | 480.302   | -96.78    | -496.732  |
| 1.701                                       | 0.548                          | 0.191            | -51.068   | 398.686   | -84.469   | -410.643  |
| 1.692                                       | 0.946                          | 0.294            | -63.264   | 500.366   | -105.015  | -526.227  |
| 1.698                                       | 0.79                           | 0.257            | -70.278   | 550.843   | -115.446  | -574.073  |
| 1.475                                       | 0.951                          | 0.19             | -80.475   | 613.578   | -123.135  | -648.495  |
| 1.749                                       | 0.651                          | 0.335            | -46.374   | 402.498   | -91.628   | -423.572  |
| 1.654                                       | 1.16                           | 0.284            | -68.76    | 549.669   | -115.356  | -584.783  |
| 1.661                                       | 0.657                          | 0.22             | -40.554   | 416.247   | -107.138  | -440.846  |
| 1.756                                       | 0.719                          | 0.279            | -58.426   | 474.029   | -102.118  | -495.272  |
| 1.668                                       | 0.722                          | 0.323            | -68.004   | 509.648   | -98.693   | -536.608  |
| 1.626                                       | 0.772                          | 0.284            | -49.723   | 417.957   | -92.167   | -441.982  |
| 1.743                                       | 0.839                          | 0.281            | -47.666   | 489.364   | -127.31   | -518.542  |
| 1.568                                       | 0.719                          | 0.205            | -72.774   | 561.673   | -112.874  | -591.61   |
| 1.669                                       | 0.971                          | 0.216            | -84.279   | 570.114   | -96.721   | -597.614  |
| 1.771                                       | 0.865                          | 0.317            | -54.512   | 441.045   | -93.175   | -465.948  |
| 1.805                                       | 0.84                           | 0.301            | -100.768  | 693.977   | -122.709  | -721.006  |
| 1.696                                       | 1.103                          | 0.341            | -166.685  | 987.162   | -129.973  | -1032.924 |
| 1.805                                       | 0.458                          | 0.208            | -61.297   | 516.26    | -115.683  | -533.919  |
| 1.678                                       | 1.096                          | 0.385            | -93.102   | 615.735   | -97.51    | -654.605  |
| 1.803                                       | 1.135                          | 0.31             | -69.474   | 508.605   | -95.952   | -537.209  |
| 1.71                                        | 0.711                          | 0.266            | -75.252   | 557.212   | -109.253  | -579.298  |
| 1.74                                        | 0.858                          | 0.317            | -52.268   | 454.175   | -103.679  | -479.73   |
| 1.765                                       | 0.786                          | 0.253            | -67.742   | 510.237   | -101.012  | -532.429  |
| 1.681                                       | 0.799                          | 0.304            | -57.646   | 441.841   | -87.84    | -465.017  |
| 1.485                                       | 1.023                          | 0.233            | -67.567   | 530.477   | -107.516  | -567.049  |
| 1.633                                       | 0.849                          | 0.32             | -56.864   | 498.42    | -112.734  | -532.114  |
| 1.677                                       | 0.599                          | 0.24             | -64.986   | 493.878   | -99.931   | -512.767  |
| 1.69                                        | 0.843                          | 0.302            | -68.771   | 530.338   | -108.114  | -556.582  |
| 1.702                                       | 0.818                          | 0.259            | -50.816   | 437.875   | -99.107   | -462.574  |
| 1.637                                       | 0.635                          | 0.241            | -51.24    | 419.811   | -89.713   | -442.754  |
| 1.528                                       | 0.92                           | 0.332            | -57.848   | 507.8     | -114.47   | -545.695  |
| 1.747                                       | 0.715                          | 0.177            | -64.119   | 484.892   | -98.239   | -500.938  |
| 1.676                                       | 0.532                          | 0.304            | -62.548   | 498.999   | -107.309  | -516.709  |
| 1.791                                       | 0.635                          | 0.288            | -89.875   | 576.965   | -93.694   | -590.97   |
| 1.728                                       | 0.831                          | 0.315            | -59.24    | 494.122   | -108.211  | -521.005  |
| 1.689                                       | 1.102                          | 0.411            | -72.275   | 571.952   | -117.016  | -610.753  |
| 1.917                                       | 0.717                          | 0.313            | -84.585   | 601.336   | -113.724  | -617.414  |
| 1.578                                       | 0.715                          | 0.248            | -58.122   | 508.227   | -118.607  | -533.289  |
| 1.697                                       | 0.972                          | 0.295            | -76.234   | 612.285   | -128.334  | -648.727  |
| 1.791                                       | 0.868                          | 0.293            | -62.606   | 476.017   | -94.788   | -499.142  |
| 1.884                                       | 0.934                          | 0.367            | -88.298   | 646.044   | -124.868  | -671.994  |
| 1.582                                       | 0.651                          | 0.196            | -41.871   | 437.575   | -114.675  | -462.715  |
| 1.985                                       | 0.414                          | 0.146            | -82.409   | 577.852   | -108.419  | -583.786  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.686                                       | 0.949                          | 0.304            | -57.693   | 461.789   | -96.999   | -489.092  |
| 1.626                                       | 0.778                          | 0.352            | -96.604   | 687.774   | -125.95   | -721.375  |
| 1.833                                       | 0.866                          | 0.352            | -76.111   | 584.273   | -116.388  | -615.649  |
| 1.494                                       | 1.062                          | 0.361            | -48.261   | 425.249   | -95.317   | -461.693  |
| 1.706                                       | 0.542                          | 0.213            | -59       | 472.359   | -102.353  | -487.398  |
| 1.566                                       | 0.964                          | 0.181            | -76.575   | 562.03    | -108.506  | -588.742  |
| 1.731                                       | 0.799                          | 0.407            | -85.644   | 673.397   | -137.353  | -713.495  |
| 1.723                                       | 0.796                          | 0.333            | -42.309   | 383.134   | -90.984   | -403.83   |
| 1.613                                       | 1.094                          | 0.277            | -68.215   | 519.33    | -101.086  | -555.998  |
| 1.572                                       | 0.982                          | 0.208            | -62.692   | 485.147   | -98.842   | -512.423  |
| 1.764                                       | 0.658                          | 0.307            | -101.536  | 697.408   | -125.598  | -718.004  |
| 1.74                                        | 0.63                           | 0.259            | -70.405   | 538.064   | -108.826  | -559.137  |
| 1.442                                       | 0.825                          | 0.269            | -63.518   | 504.184   | -104.325  | -536.837  |
| 1.886                                       | 0.789                          | 0.255            | -90.828   | 640.891   | -117.547  | -663.541  |
| 1.886                                       | 1.096                          | 0.408            | -92.013   | 624.767   | -106.437  | -655.788  |
| 1.745                                       | 0.63                           | 0.282            | -75.551   | 550.561   | -106.881  | -567.621  |
| 1.769                                       | 0.697                          | 0.305            | -77.311   | 549.478   | -103.048  | -567.304  |
| 1.664                                       | 0.752                          | 0.213            | -64.583   | 530.601   | -117.757  | -552.38   |
| 1.763                                       | 0.709                          | 0.21             | -68.748   | 521.292   | -106.781  | -536.579  |
| 1.876                                       | 0.928                          | 0.377            | -79.163   | 593.728   | -113.842  | -627.988  |
| 1.692                                       | 0.793                          | 0.331            | -65.246   | 499.605   | -101.232  | -522.672  |
| 1.739                                       | 0.886                          | 0.277            | -76.837   | 571.863   | -112.226  | -595.635  |
| 1.747                                       | 0.965                          | 0.373            | -76.752   | 597.399   | -121.227  | -630.533  |
| 1.531                                       | 0.964                          | 0.295            | -63.356   | 489.939   | -98.06    | -522.437  |
| 1.555                                       | 0.691                          | 0.261            | -69.632   | 512.219   | -99.378   | -534.193  |
| 1.864                                       | 0.844                          | 0.237            | -61.249   | 451.658   | -86.19    | -472.51   |
| 1.621                                       | 0.402                          | 0.295            | -67.798   | 503.782   | -96.391   | -527.265  |
| 1.66                                        | 1.038                          | 0.349            | -71.867   | 543.789   | -101.459  | -587.527  |
| 1.834                                       | 0.793                          | 0.286            | -48.871   | 433.94    | -99       | -458.757  |
| 1.842                                       | 0.89                           | 0.338            | -124.048  | 776.6     | -120.681  | -798.073  |
| 1.788                                       | 0.627                          | 0.266            | -76.269   | 569.092   | -113.031  | -587.683  |
| 1.652                                       | 0.764                          | 0.326            | -54.872   | 452.237   | -99.499   | -473.732  |
| 1.943                                       | 0.624                          | 0.25             | -58.617   | 461.338   | -96.388   | -477.503  |
| 1.732                                       | 0.468                          | 0.332            | -69.086   | 516.053   | -103.842  | -530.855  |
| 1.712                                       | 0.787                          | 0.338            | -53.498   | 436.861   | -93.79    | -460.367  |
| 1.897                                       | 0.883                          | 0.314            | -80.952   | 555.171   | -98.133   | -574.529  |
| 1.821                                       | 0.809                          | 0.353            | -57.773   | 469.138   | -98.29    | -496.514  |
| 1.793                                       | 0.814                          | 0.288            | -63.245   | 483.413   | -95.759   | -507.99   |
| 1.833                                       | 0.786                          | 0.262            | -74.48    | 553.95    | -108.756  | -575.657  |
| 1.619                                       | 0.885                          | 0.245            | -61.305   | 490.341   | -103.539  | -517.113  |
| 1.4                                         | 0.821                          | 0.235            | -45.08    | 415.514   | -98.001   | -447.168  |
| 1.812                                       | 0.84                           | 0.364            | -76.263   | 563.813   | -109.005  | -589.929  |
| 1.601                                       | 0.561                          | 0.279            | -36.564   | 390.87    | -101.595  | -417.243  |
| 1.642                                       | 0.934                          | 0.259            | -75.603   | 547.738   | -105.112  | -570.259  |
| 1.743                                       | 0.755                          | 0.335            | -65.859   | 497.042   | -99.568   | -517.96   |
| 1.69                                        | 0.624                          | 0.253            | -67.721   | 511.694   | -102.228  | -531.814  |
| 1.631                                       | 0.707                          | 0.271            | -69.957   | 518.698   | -101.208  | -541      |
| 1.561                                       | 0.611                          | 0.313            | -60.442   | 491.718   | -105.477  | -517.997  |
| 1.58                                        | 0.718                          | 0.341            | -62.782   | 501.238   | -103.803  | -531.53   |
| 1.861                                       | 0.566                          | 0.281            | -65.747   | 525.982   | -111.14   | -547.244  |
| 1.805                                       | 0.717                          | 0.248            | -54.632   | 417.342   | -85.462   | -432.425  |
| 1.633                                       | 0.989                          | 0.22             | -61.251   | 481.275   | -99.417   | -508.392  |
| 1.675                                       | 0.868                          | 0.302            | -53.384   | 444.477   | -97.908   | -468.183  |
| 1.627                                       | 0.745                          | 0.293            | -63.617   | 490.577   | -100.211  | -513.777  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.798                                       | 0.96                           | 0.422            | -75.28    | 555.688   | -105.74   | -586.497  |
| 1.583                                       | 0.626                          | 0.296            | -58.019   | 485.243   | -106.027  | -512.548  |
| 1.613                                       | 0.627                          | 0.234            | -67.16    | 503.576   | -100.034  | -524.642  |
| 1.707                                       | 0.889                          | 0.347            | -65.943   | 544.747   | -117.858  | -576.632  |
| 2.107                                       | 0.795                          | 0.315            | -128.221  | 754.828   | -107.402  | -760.229  |
| 1.492                                       | 0.891                          | 0.219            | -57.234   | 475.355   | -102.986  | -505.657  |
| 1.684                                       | 0.887                          | 0.303            | -60.546   | 495.345   | -106.028  | -524.97   |
| 1.731                                       | 0.868                          | 0.278            | -62.336   | 500.13    | -106.429  | -524.406  |
| 1.716                                       | 0.777                          | 0.295            | -65.102   | 513.96    | -107.767  | -537.791  |
| 1.546                                       | 0.952                          | 0.279            | -57.481   | 464.622   | -96.449   | -498.498  |
| 1.801                                       | 0.769                          | 0.296            | -72.271   | 523.038   | -99.913   | -542.774  |
| 1.577                                       | 0.718                          | 0.258            | -47.934   | 411.965   | -91.407   | -437.725  |
| 1.696                                       | 1.006                          | 0.401            | -69.59    | 546.196   | -111.41   | -581.094  |
| 1.669                                       | 0.605                          | 0.315            | -76.512   | 562.773   | -108.817  | -585.531  |
| 1.683                                       | 0.718                          | 0.231            | -58.006   | 487.783   | -110.707  | -507.228  |
| 1.526                                       | 0.951                          | 0.28             | -53.208   | 449.004   | -97.357   | -481.638  |
| 1.837                                       | 0.65                           | 0.232            | -80.906   | 579.518   | -110.081  | -596.692  |
| 1.801                                       | 0.954                          | 0.21             | -56.053   | 453.408   | -98.061   | -474.249  |
| 1.548                                       | 0.758                          | 0.24             | -50.67    | 456.184   | -106.893  | -484.921  |
| 1.651                                       | 0.764                          | 0.29             | -43.103   | 399.49    | -96.039   | -422.911  |
| 1.82                                        | 0.988                          | 0.304            | -52.687   | 460.103   | -105.282  | -486.813  |
| 1.584                                       | 0.617                          | 0.274            | -45.581   | 402.204   | -92.43    | -425.472  |
| 1.631                                       | 0.676                          | 0.251            | -76.025   | 570.53    | -114.634  | -591.313  |
| 1.692                                       | 0.799                          | 0.239            | -42.133   | 366.865   | -84.929   | -385.504  |
| 1.623                                       | 0.787                          | 0.301            | -57.452   | 451.08    | -92.853   | -475.726  |
| 1.78                                        | 0.831                          | 0.319            | -88.704   | 606.43    | -107.141  | -628.327  |
| 1.781                                       | 0.726                          | 0.349            | -77.852   | 550.314   | -99.848   | -573.639  |
| 1.486                                       | 0.955                          | 0.268            | -59.925   | 496.893   | -107.58   | -530.795  |
| 1.775                                       | 0.892                          | 0.325            | -66.43    | 500.604   | -100.956  | -520.565  |
| 1.551                                       | 0.905                          | 0.321            | -62.928   | 507.086   | -105.395  | -542.012  |
| 1.808                                       | 0.716                          | 0.297            | -65.433   | 492.815   | -97.915   | -512.739  |
| 1.469                                       | 0.613                          | 0.325            | -53.925   | 449.934   | -99.002   | -474.723  |
| 1.696                                       | 0.803                          | 0.25             | -83.044   | 577.21    | -102.025  | -604.312  |
| 1.852                                       | 0.566                          | 0.303            | -68.486   | 513.452   | -101.479  | -531.37   |
| 1.827                                       | 0.948                          | 0.269            | -54.643   | 459.37    | -102.712  | -482.015  |
| 1.828                                       | 0.66                           | 0.225            | -77.026   | 543.569   | -101.495  | -557.934  |
| 1.622                                       | 0.937                          | 0.233            | -64.808   | 511.449   | -106.701  | -539.011  |
| 1.763                                       | 0.937                          | 0.339            | -70.381   | 542.898   | -108.752  | -573.231  |
| 1.637                                       | 0.941                          | 0.257            | -58.624   | 475.814   | -101.564  | -503.341  |
| 1.81                                        | 0.935                          | 0.356            | -79.574   | 582.893   | -110.626  | -611.047  |
| 1.592                                       | 0.642                          | 0.27             | -57.236   | 519.628   | -118.831  | -557.745  |
| 1.78                                        | 0.839                          | 0.298            | -64.603   | 505.63    | -105.177  | -528.256  |
| 1.622                                       | 0.899                          | 0.263            | -55.831   | 452.385   | -98.242   | -475.193  |
| 1.658                                       | 0.762                          | 0.27             | -64.653   | 500.075   | -104.216  | -519.88   |
| 1.758                                       | 0.743                          | 0.276            | -69.064   | 527.776   | -106.661  | -549.781  |
| 1.824                                       | 0.706                          | 0.266            | -58.378   | 448.015   | -91.176   | -465.971  |
| 1.633                                       | 0.831                          | 0.184            | -87.594   | 644.918   | -121.578  | -680.736  |
| 1.371                                       | 0.748                          | 0.229            | -74.947   | 565.963   | -111.758  | -597.689  |
| 1.491                                       | 0.7                            | 0.212            | -53.851   | 427.405   | -89.08    | -450.572  |
| 1.689                                       | 0.993                          | 0.241            | -65.412   | 491.97    | -98.176   | -515.557  |
| 1.799                                       | 0.765                          | 0.388            | -80.862   | 590.338   | -110.814  | -620.403  |
| 1.571                                       | 0.737                          | 0.287            | -55.315   | 485.017   | -111.894  | -511.778  |
| 1.688                                       | 0.738                          | 0.201            | -61.813   | 482.768   | -99.649   | -504.155  |
| 1.748                                       | 0.659                          | 0.246            | -55.785   | 439.433   | -93.428   | -454.598  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.761                                       | 0.911                          | 0.329            | -67.119   | 528.378   | -109.592  | -555.269  |
| 1.771                                       | 0.838                          | 0.34             | -70.289   | 529.102   | -105.284  | -553.26   |
| 1.542                                       | 0.961                          | 0.259            | -87.437   | 630.837   | -117.969  | -665.295  |
| 1.763                                       | 0.59                           | 0.252            | -69.756   | 488.668   | -89.538   | -502.749  |
| 1.721                                       | 0.238                          | 0.242            | -94.167   | 663.477   | -122.538  | -678.64   |
| 1.684                                       | 0.914                          | 0.272            | -74.252   | 516.711   | -91.975   | -539.908  |
| 1.484                                       | 0.858                          | 0.242            | -27.83    | 366.817   | -108.195  | -397.433  |
| 1.894                                       | 0.837                          | 0.322            | -58.823   | 453.932   | -91.539   | -476.179  |
| 1.644                                       | 0.78                           | 0.189            | -56.419   | 475.476   | -106.718  | -498.97   |
| 1.624                                       | 0.965                          | 0.238            | -56.664   | 461.684   | -99.65    | -487.621  |
| 1.712                                       | 0.91                           | 0.329            | -85.324   | 618.954   | -117.006  | -648.918  |
| 1.757                                       | 0.768                          | 0.309            | -69.69    | 510.08    | -98.337   | -530.452  |
| 1.675                                       | 1.222                          | 0.422            | -58.301   | 467.115   | -97.07    | -500.359  |
| 1.878                                       | 0.778                          | 0.235            | -65.288   | 521.878   | -112.443  | -540.196  |
| 1.676                                       | 0.848                          | 0.311            | -60.176   | 479.574   | -99.862   | -506.984  |
| 1.676                                       | 0.642                          | 0.285            | -72.849   | 528.073   | -101.052  | -546.831  |
| 1.787                                       | 0.864                          | 0.275            | -63.593   | 484.192   | -97.469   | -505.693  |
| 1.796                                       | 0.584                          | 0.191            | -67.034   | 494.766   | -99.236   | -505.812  |
| 1.899                                       | 0.78                           | 0.301            | -68.397   | 523.116   | -105.825  | -543.615  |
| 1.862                                       | 0.839                          | 0.374            | -74.498   | 563.463   | -112.049  | -588.502  |
| 1.71                                        | 0.896                          | 0.325            | -67.137   | 504.086   | -99.105   | -529.445  |
| 1.633                                       | 0.853                          | 0.254            | -80.104   | 586.632   | -113.045  | -612.783  |
| 1.828                                       | 1.028                          | 0.293            | -47.827   | 419.72    | -96.213   | -444.592  |
| 1.671                                       | 0.644                          | 0.326            | -71.732   | 540.196   | -106.368  | -565.115  |
| 1.848                                       | 0.603                          | 0.34             | -49.757   | 444.432   | -103.429  | -465.898  |
| 1.883                                       | 0.655                          | 0.296            | -59.415   | 470.936   | -101.03   | -486.032  |
| 1.901                                       | 0.848                          | 0.264            | -64.506   | 505.953   | -105.474  | -526.019  |
| 1.843                                       | 0.783                          | 0.339            | -78.646   | 607.908   | -122.144  | -638.024  |
| 1.826                                       | 0.865                          | 0.285            | -80.222   | 586.795   | -113.146  | -609.666  |
| 1.843                                       | 0.87                           | 0.322            | -62.589   | 486.372   | -98.003   | -512.793  |
| 1.669                                       | 0.706                          | 0.19             | -69.427   | 540.772   | -113.388  | -560.442  |
| 1.715                                       | 0.706                          | 0.216            | -69.967   | 521.229   | -104.049  | -538.549  |
| 1.535                                       | 0.659                          | 0.311            | -88.813   | 580.97    | -96.62    | -600.798  |
| 1.819                                       | 0.614                          | 0.288            | -70.1     | 536.952   | -111.25   | -552.835  |
| 1.578                                       | 0.861                          | 0.218            | -60.06    | 466.733   | -96.279   | -489.788  |
| 1.912                                       | 0.696                          | 0.323            | -84.078   | 602.416   | -111.108  | -627.439  |
| 1.674                                       | 0.877                          | 0.283            | -42.123   | 429.523   | -110.878  | -456.234  |
| 1.691                                       | 0.552                          | 0.311            | -73.236   | 533.422   | -102.204  | -553.687  |
| 1.465                                       | 0.933                          | 0.241            | -67.792   | 531.442   | -107.898  | -566.951  |
| 1.682                                       | 0.573                          | 0.336            | -54.155   | 443.754   | -94.412   | -468.533  |
| 1.614                                       | 0.884                          | 0.294            | -64.947   | 544.416   | -120.41   | -576.306  |
| 1.836                                       | 0.942                          | 0.367            | -79.244   | 571.009   | -107.217  | -596.931  |
| 1.826                                       | 0.736                          | 0.363            | -68.6     | 540.404   | -110.884  | -568.808  |
| 1.841                                       | 0.831                          | 0.329            | -51.314   | 443.411   | -98.49    | -469.943  |
| 1.852                                       | 0.999                          | 0.339            | -73.112   | 505.244   | -88.004   | -530.988  |
| 1.614                                       | 0.586                          | 0.206            | -67.862   | 527.683   | -108.935  | -548.736  |
| 1.925                                       | 0.91                           | 0.257            | -72.76    | 525.85    | -100.116  | -545.171  |
| 1.709                                       | 0.968                          | 0.211            | -63.984   | 480.044   | -94.588   | -503.193  |
| 1.443                                       | 0.931                          | 0.215            | -71.531   | 544.506   | -104.688  | -584.934  |
| 1.549                                       | 1.021                          | 0.359            | -55.776   | 440.317   | -88.789   | -473.272  |
| 1.674                                       | 0.724                          | 0.324            | -49.987   | 441.635   | -101.27   | -467.478  |
| 1.588                                       | 0.704                          | 0.227            | -64.264   | 534.057   | -117.773  | -561.652  |
| 1.709                                       | 0.949                          | 0.355            | -54.156   | 436.581   | -92.069   | -463.936  |
| 1.726                                       | 0.818                          | 0.314            | -76.796   | 564.19    | -108.82   | -588.448  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.711                                       | 0.904                          | 0.286            | -91.076   | 624.105   | -107.633  | -655.298  |
| 1.875                                       | 0.755                          | 0.327            | -80.189   | 595.651   | -116.014  | -618.651  |
| 1.649                                       | 0.779                          | 0.203            | -45.442   | 419.508   | -99.968   | -444.758  |
| 1.69                                        | 1.054                          | 0.357            | -58.7     | 474.999   | -99.962   | -506.242  |
| 1.764                                       | 0.746                          | 0.246            | -78.773   | 556.816   | -102.141  | -577.379  |
| 1.928                                       | 0.751                          | 0.346            | -59.636   | 489.179   | -104.295  | -514.176  |
| 1.803                                       | 0.578                          | 0.247            | -67.174   | 523.06    | -111.756  | -535.171  |
| 1.678                                       | 1.041                          | 0.335            | -61.696   | 491.709   | -100.279  | -526.707  |
| 1.656                                       | 0.818                          | 0.276            | -71.609   | 509.431   | -93.571   | -532.79   |
| 1.655                                       | 0.835                          | 0.246            | -60.687   | 452.36    | -88.846   | -474.246  |
| 1.828                                       | 0.824                          | 0.309            | -62.569   | 479.761   | -96.181   | -502.565  |
| 1.804                                       | 0.749                          | 0.279            | -58.296   | 456.655   | -94.878   | -476.136  |
| 1.985                                       | 0.766                          | 0.372            | -133.63   | 787.828   | -105.659  | -809.594  |
| 1.562                                       | 0.874                          | 0.286            | -45.344   | 419.694   | -99.248   | -450.138  |
| 1.814                                       | 0.755                          | 0.358            | -79.183   | 576.245   | -107.662  | -603.756  |
| 1.482                                       | 0.486                          | 0.28             | -79.549   | 576.287   | -110.602  | -597.688  |
| 1.749                                       | 1.002                          | 0.249            | -100.689  | 620.757   | -89.282   | -648.132  |
| 1.725                                       | 0.924                          | 0.306            | -70.058   | 531.415   | -106.219  | -558.204  |
| 1.788                                       | 0.795                          | 0.307            | -64.878   | 490.493   | -96.083   | -515.188  |
| 1.793                                       | 0.819                          | 0.298            | -62.027   | 516.845   | -112.598  | -545.491  |
| 1.634                                       | 0.808                          | 0.317            | -44.501   | 421.546   | -101.501  | -450.788  |
| 1.746                                       | 0.728                          | 0.292            | -70.343   | 556.178   | -115.549  | -583.296  |
| 1.639                                       | 0.708                          | 0.234            | -64.061   | 516.49    | -109.066  | -542.814  |
| 1.597                                       | 0.688                          | 0.214            | -82.887   | 619.091   | -123.273  | -643.052  |
| 1.612                                       | 0.613                          | 0.268            | -60.222   | 480.769   | -99.723   | -506.69   |
| 1.69                                        | 0.847                          | 0.238            | -80.567   | 611.432   | -123.002  | -637.467  |
| 1.738                                       | 0.687                          | 0.191            | -89.38    | 625.431   | -113.605  | -647.675  |
| 1.797                                       | 0.991                          | 0.259            | -68.388   | 530.281   | -107.761  | -558.201  |
| 1.695                                       | 0.952                          | 0.255            | -71.795   | 549.595   | -108.417  | -583.27   |
| 1.658                                       | 0.715                          | 0.314            | -65.527   | 491.55    | -95.094   | -518.278  |
| 1.825                                       | 0.868                          | 0.316            | -55.558   | 502.708   | -119.254  | -529.114  |
| 2                                           | 0.629                          | 0.145            | -60.857   | 435.819   | -84.273   | -441.543  |
| 1.737                                       | 0.977                          | 0.321            | -66.044   | 521.773   | -107.492  | -552.509  |
| 1.442                                       | 0.824                          | 0.229            | -72.759   | 533.191   | -101.983  | -561.54   |
| 1.769                                       | 1.026                          | 0.374            | -77.564   | 553.664   | -101.414  | -583.444  |
| 1.838                                       | 0.864                          | 0.348            | -55.233   | 468.651   | -105.653  | -491.493  |
| 1.795                                       | 0.894                          | 0.315            | -51.192   | 431.576   | -95.156   | -454.115  |
| 1.853                                       | 0.893                          | 0.378            | -84.284   | 586.764   | -106.289  | -609.431  |
| 1.826                                       | 0.786                          | 0.244            | -64.061   | 478.862   | -95.888   | -494.003  |
| 1.769                                       | 0.795                          | 0.307            | -66.652   | 525.945   | -108.755  | -553.409  |
| 1.812                                       | 0.807                          | 0.325            | -78.27    | 573.227   | -110.186  | -596.351  |
| 1.726                                       | 0.74                           | 0.27             | -59.778   | 455.226   | -91.971   | -473.449  |
| 1.727                                       | 1.088                          | 0.448            | -87.362   | 635.215   | -116.481  | -677.422  |
| 1.723                                       | 0.882                          | 0.296            | -65.582   | 497.223   | -97.372   | -525.579  |
| 1.782                                       | 0.789                          | 0.398            | -66.631   | 518.204   | -104.373  | -546.524  |
| 1.931                                       | 0.591                          | 0.351            | -76.166   | 556.087   | -107.816  | -571.897  |
| 1.723                                       | 0.924                          | 0.283            | -63.486   | 505.391   | -105.834  | -533.094  |
| 1.83                                        | 0.642                          | 0.327            | -82.604   | 604.81    | -116.983  | -625.459  |
| 1.78                                        | 0.747                          | 0.274            | -64.013   | 499.895   | -104.602  | -519.754  |
| 1.527                                       | 0.896                          | 0.301            | -65.786   | 536.118   | -114.525  | -569.808  |
| 1.409                                       | 1.315                          | 0.275            | -66.035   | 533.35    | -109.544  | -582.234  |
| 1.558                                       | 1.275                          | 0.355            | -69.92    | 526.524   | -100.827  | -567.008  |
| 1.668                                       | 0.831                          | 0.256            | -79.244   | 595.099   | -115.53   | -626.717  |
| 1.705                                       | 0.852                          | 0.326            | -58.066   | 471.353   | -100.119  | -498.266  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.895                                       | 1.033                          | 0.364            | -55.453   | 446.031   | -92.866   | -472.955  |
| 1.929                                       | 0.626                          | 0.407            | -61.472   | 494.148   | -104.148  | -516.233  |
| 1.513                                       | 0.557                          | 0.323            | -74.904   | 555.225   | -107.64   | -580.849  |
| 1.516                                       | 0.9                            | 0.241            | -54.972   | 480.174   | -111.259  | -507.364  |
| 1.744                                       | 0.789                          | 0.295            | -59.232   | 483.305   | -102.237  | -510.419  |
| 1.724                                       | 0.925                          | 0.296            | -51.266   | 440.625   | -97.753   | -469.575  |
| 1.738                                       | 0.509                          | 0.3              | -48.319   | 438.329   | -102.527  | -460.495  |
| 1.653                                       | 0.631                          | 0.246            | -65.866   | 561.107   | -126.226  | -588.392  |
| 1.617                                       | 1.201                          | 0.284            | -79.932   | 605.387   | -117.426  | -648.329  |
| 1.617                                       | 0.696                          | 0.269            | -74.246   | 546.237   | -106.998  | -567.995  |
| 1.724                                       | 0.839                          | 0.209            | -83.799   | 631.526   | -126.333  | -658.363  |
| 1.672                                       | 0.593                          | 0.275            | -68.333   | 523.669   | -105.702  | -546.54   |
| 1.834                                       | 0.956                          | 0.305            | -60.31    | 475.253   | -96.883   | -503.412  |
| 1.743                                       | 0.795                          | 0.307            | -64.565   | 518.998   | -110.636  | -543.367  |
| 1.582                                       | 0.793                          | 0.159            | -71.235   | 560.301   | -119.679  | -581.852  |
| 1.768                                       | 0.626                          | 0.292            | -71.965   | 542.078   | -108.665  | -561.756  |
| 1.999                                       | 0.729                          | 0.314            | -52.079   | 414.328   | -87.13    | -430.084  |
| 1.557                                       | 0.844                          | 0.145            | -64.904   | 510.402   | -107.637  | -533.47   |
| 1.717                                       | 0.633                          | 0.23             | -51.382   | 453.529   | -105.399  | -474.609  |
| 1.56                                        | 1.12                           | 0.261            | -87.154   | 644.539   | -122.991  | -685.644  |
| 1.828                                       | 0.833                          | 0.252            | -62.163   | 460.789   | -89.669   | -481.347  |
| 1.606                                       | 0.67                           | 0.263            | -46.576   | 394.881   | -88.389   | -415.465  |
| 1.56                                        | 0.871                          | 0.312            | -69.208   | 534.64    | -108.071  | -565.907  |
| 1.668                                       | 0.687                          | 0.254            | -57.432   | 460.553   | -96.348   | -485.437  |
| 1.784                                       | 1.061                          | 0.349            | -53.52    | 443.822   | -96.039   | -471.509  |
| 1.369                                       | 1.042                          | 0.267            | -50.85    | 461.649   | -106.061  | -503.821  |
| 1.718                                       | 0.769                          | 0.288            | -54.947   | 457.062   | -101.518  | -477.783  |
| 1.633                                       | 0.55                           | 0.318            | -63.455   | 544.758   | -122.307  | -573.43   |
| 1.805                                       | 0.825                          | 0.315            | -90.92    | 598.495   | -97.844   | -622.238  |
| 1.74                                        | 0.666                          | 0.299            | -66.458   | 488.028   | -93.177   | -510.468  |
| 1.665                                       | 1.007                          | 0.292            | -70.085   | 546.879   | -111.733  | -577.919  |
| 1.618                                       | 0.601                          | 0.274            | -64.644   | 482.968   | -94.854   | -504.181  |
| 1.66                                        | 0.949                          | 0.266            | -72.033   | 558.973   | -113.475  | -590.811  |
| 1.812                                       | 0.909                          | 0.446            | -58.314   | 477.438   | -99.429   | -511.377  |
| 1.641                                       | 0.817                          | 0.319            | -64.725   | 494.799   | -99.165   | -520.521  |
| 1.849                                       | 0.842                          | 0.24             | -76.744   | 570.19    | -111.62   | -592.604  |
| 1.733                                       | 0.903                          | 0.268            | -63.173   | 487.833   | -97.879   | -515.663  |
| 1.836                                       | 1.072                          | 0.368            | -69.555   | 504.06    | -93.388   | -532.087  |
| 1.658                                       | 0.948                          | 0.412            | -60.37    | 461.221   | -90.381   | -491.134  |
| 1.787                                       | 0.826                          | 0.348            | -79.976   | 590.08    | -111.986  | -620.052  |
| 1.708                                       | 0.857                          | 0.418            | -59.059   | 470.036   | -96.894   | -498.752  |
| 1.762                                       | 0.617                          | 0.261            | -43.412   | 423.616   | -107.38   | -443.262  |
| 1.662                                       | 0.761                          | 0.313            | -51.265   | 426.268   | -93.798   | -449.024  |
| 1.481                                       | 0.85                           | 0.261            | -71.099   | 527.45    | -102.048  | -556.154  |
| 1.847                                       | 0.687                          | 0.27             | -77.422   | 572.94    | -112.027  | -592.552  |
| 1.656                                       | 0.659                          | 0.309            | -58.041   | 485.764   | -109.935  | -505.372  |
| 1.786                                       | 0.864                          | 0.305            | -62.272   | 478.724   | -94.711   | -505.81   |
| 1.73                                        | 0.535                          | 0.248            | -82.445   | 604.301   | -118.074  | -622.315  |
| 1.671                                       | 0.948                          | 0.245            | -85.299   | 620.813   | -116.408  | -654.833  |
| 1.72                                        | 0.673                          | 0.261            | -65.131   | 522.69    | -112.846  | -543.532  |
| 1.838                                       | 0.794                          | 0.342            | -75.915   | 564.724   | -110.246  | -588.953  |
| 1.644                                       | 0.676                          | 0.226            | -64.374   | 510.285   | -107.999  | -531.871  |
| 1.876                                       | 0.822                          | 0.264            | -57.948   | 463.846   | -99.971   | -481.292  |
| 1.656                                       | 0.555                          | 0.304            | -59.777   | 470.796   | -98.051   | -491.968  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.725                                       | 0.782                          | 0.246            | -45.231   | 423.031   | -102.948  | -446.049  |
| 1.624                                       | 0.671                          | 0.275            | -66.218   | 529.604   | -111.805  | -555.276  |
| 1.579                                       | 0.757                          | 0.239            | -59.054   | 455.563   | -92.316   | -479.897  |
| 1.626                                       | 0.913                          | 0.291            | -42.772   | 425.816   | -108      | -453.389  |
| 1.65                                        | 0.88                           | 0.341            | -53.205   | 483.849   | -111.342  | -519.593  |
| 1.87                                        | 0.777                          | 0.371            | -61.964   | 471.193   | -92.482   | -494.945  |
| 1.827                                       | 0.618                          | 0.267            | -83.288   | 613.706   | -119.943  | -634.28   |
| 1.726                                       | 0.933                          | 0.284            | -62.764   | 504.275   | -107.36   | -531.114  |
| 1.644                                       | 0.95                           | 0.346            | -72.895   | 537.494   | -101.42   | -570.394  |
| 1.84                                        | 0.865                          | 0.341            | -63.78    | 500.144   | -102.589  | -524.677  |
| 1.43                                        | 0.7                            | 0.212            | -47.643   | 445.948   | -108.633  | -473.337  |
| 1.739                                       | 0.728                          | 0.189            | -60.504   | 466.433   | -95.637   | -484.695  |
| 1.761                                       | 0.702                          | 0.321            | -71.333   | 562.1     | -117.63   | -586.992  |
| 1.809                                       | 0.927                          | 0.326            | -75.663   | 556.882   | -105.974  | -584.554  |
| 1.796                                       | 0.838                          | 0.28             | -63.411   | 516.207   | -112.092  | -538.411  |
| 1.811                                       | 0.867                          | 0.278            | -58.655   | 482.68    | -103.919  | -508.836  |
| 1.682                                       | 0.742                          | 0.325            | -59.153   | 471.833   | -99.465   | -496.222  |
| 1.731                                       | 0.98                           | 0.337            | -61.053   | 487.572   | -102.905  | -514.917  |
| 1.822                                       | 0.872                          | 0.303            | -62.868   | 499.632   | -103.023  | -527.303  |
| 1.675                                       | 0.998                          | 0.319            | -89.134   | 608.076   | -105.236  | -638.33   |
| 1.922                                       | 0.532                          | 0.308            | -70.968   | 545.356   | -112.409  | -561.34   |
| 1.643                                       | 0.912                          | 0.298            | -71.77    | 538.546   | -109.606  | -558.901  |
| 1.693                                       | 0.902                          | 0.268            | -63.321   | 501.138   | -104.027  | -528.861  |
| 1.832                                       | 0.639                          | 0.267            | -87.409   | 630.718   | -120.514  | -649.545  |
| 1.655                                       | 0.7                            | 0.246            | -63.884   | 510.228   | -108.512  | -532.335  |
| 1.873                                       | 0.83                           | 0.358            | -67.521   | 523.851   | -107.186  | -547.856  |
| 1.841                                       | 0.638                          | 0.264            | -70.272   | 523.743   | -104.396  | -539.505  |
| 1.819                                       | 0.55                           | 0.189            | -72.947   | 523.209   | -102.464  | -531.011  |
| 1.746                                       | 1.005                          | 0.338            | -62.364   | 488.201   | -98.983   | -519.268  |
| 1.776                                       | 0.861                          | 0.279            | -90.007   | 607.921   | -105.851  | -628.902  |
| 2.004                                       | 0.878                          | 0.429            | -95.244   | 678.659   | -124.28   | -708.459  |
| 1.773                                       | 0.791                          | 0.316            | -82.706   | 586.121   | -107.684  | -610.422  |
| 1.64                                        | 0.873                          | 0.287            | -72.45    | 555.233   | -113.011  | -581.775  |
| 1.651                                       | 0.829                          | 0.26             | -55.235   | 457.75    | -100.142  | -483.168  |
| 1.895                                       | 1.035                          | 0.317            | -97.598   | 634.229   | -101.649  | -660.783  |
| 1.647                                       | 0.613                          | 0.266            | -63.102   | 516.052   | -113.001  | -537.672  |
| 1.613                                       | 0.587                          | 0.28             | -64.343   | 496.621   | -100.227  | -520.562  |
| 1.709                                       | 1.093                          | 0.373            | -70.477   | 542.855   | -108.467  | -576.735  |
| 1.69                                        | 0.966                          | 0.319            | -68.968   | 556.718   | -118.353  | -588.921  |
| 1.846                                       | 0.779                          | 0.34             | -57.253   | 460.024   | -96.348   | -485.17   |
| 1.749                                       | 0.523                          | 0.241            | -49.587   | 404.011   | -89.458   | -416.209  |
| 1.797                                       | 0.881                          | 0.364            | -64.664   | 502.736   | -101.177  | -532.124  |
| 1.598                                       | 0.911                          | 0.269            | -79.66    | 567.803   | -101.813  | -602.562  |
| 1.724                                       | 0.788                          | 0.327            | -68.682   | 516.302   | -102.919  | -538.158  |
| 1.777                                       | 0.59                           | 0.321            | -67.391   | 534.475   | -111.93   | -556.923  |
| 1.841                                       | 0.78                           | 0.297            | -61.789   | 472.646   | -95.004   | -494.225  |
| 1.813                                       | 0.98                           | 0.337            | -71.188   | 529.414   | -101.009  | -560.803  |
| 1.771                                       | 0.827                          | 0.323            | -57.456   | 480.359   | -105.587  | -506.276  |
| 1.741                                       | 0.663                          | 0.261            | -66.795   | 508.397   | -103.424  | -526.57   |
| 1.664                                       | 0.934                          | 0.384            | -78.726   | 593.937   | -117.317  | -626.396  |
| 1.713                                       | 1.012                          | 0.392            | -68.482   | 521.364   | -102.424  | -553.504  |
| 1.54                                        | 0.508                          | 0.277            | -67.157   | 506.919   | -102.496  | -526.967  |
| 1.682                                       | 1.024                          | 0.33             | -66.93    | 503.264   | -97.093   | -535.559  |
| 1.734                                       | 0.865                          | 0.257            | -51.682   | 420.539   | -90.048   | -442.59   |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.714                                       | 0.449                          | 0.272            | -70.082   | 536.567   | -109.053  | -555.333  |
| 1.661                                       | 0.711                          | 0.248            | -58.999   | 498.315   | -113.172  | -518.568  |
| 1.847                                       | 1.21                           | 0.3              | -82.023   | 641.086   | -129.585  | -682.273  |
| 1.817                                       | 0.946                          | 0.209            | -45.838   | 407.373   | -93.703   | -431.596  |
| 1.958                                       | 0.635                          | 0.352            | -80.914   | 567.021   | -103.643  | -584.162  |
| 1.695                                       | 0.64                           | 0.259            | -56.99    | 442.37    | -91.927   | -458.486  |
| 1.908                                       | 0.874                          | 0.31             | -78.282   | 560.793   | -104.073  | -582.626  |
| 1.774                                       | 0.612                          | 0.158            | -57.328   | 479.601   | -107.784  | -496.432  |
| 1.844                                       | 0.855                          | 0.333            | -69.583   | 536.55    | -108.804  | -561.92   |
| 1.575                                       | 0.794                          | 0.134            | -67.311   | 521.637   | -106.952  | -546.332  |
| 1.867                                       | 0.652                          | 0.284            | -58.663   | 438.614   | -84.851   | -457.401  |
| 1.659                                       | 0.896                          | 0.327            | -60.446   | 501.591   | -108.179  | -534.321  |
| 1.516                                       | 0.987                          | 0.347            | -67       | 520.995   | -104.773  | -556.011  |
| 1.84                                        | 0.472                          | 0.202            | -93.927   | 615.636   | -104.829  | -624.121  |
| 1.696                                       | 1.085                          | 0.32             | -58.104   | 465.644   | -97.677   | -495.454  |
| 1.654                                       | 0.488                          | 0.279            | -65.045   | 515.463   | -110.036  | -532.46   |
| 1.805                                       | 0.721                          | 0.16             | -56.32    | 449.885   | -96.156   | -465.831  |
| 1.733                                       | 0.678                          | 0.297            | -63.324   | 485.035   | -98.438   | -506.103  |
| 1.632                                       | 0.764                          | 0.36             | -62.049   | 519.403   | -111.943  | -554.166  |
| 1.577                                       | 0.639                          | 0.253            | -91.018   | 682.331   | -136.638  | -710.047  |
| 1.465                                       | 0.83                           | 0.271            | -63.683   | 503.58    | -100.817  | -539.648  |
| 1.529                                       | 1.19                           | 0.269            | -50.357   | 465.617   | -108.957  | -506.121  |
| 1.914                                       | 0.732                          | 0.273            | -47.031   | 448.746   | -110.608  | -470.351  |
| 1.666                                       | 0.576                          | 0.258            | -79.362   | 604.5     | -123.477  | -626.229  |
| 1.736                                       | 0.819                          | 0.289            | -73.035   | 564.956   | -116.584  | -589.554  |
| 1.637                                       | 0.529                          | 0.27             | -70.108   | 527.752   | -105.2    | -548.063  |
| 1.862                                       | 1.041                          | 0.349            | -65.662   | 507.085   | -101.381  | -535.192  |
| 1.649                                       | 0.692                          | 0.313            | -49.841   | 461.623   | -108.423  | -492.726  |
| 1.932                                       | 0.77                           | 0.356            | -59.646   | 480.219   | -98.537   | -508.224  |
| 1.622                                       | 0.944                          | 0.267            | -64.909   | 505.015   | -100.674  | -538.396  |
| 1.615                                       | 0.719                          | 0.288            | -66.415   | 515.112   | -104.542  | -541.679  |
| 1.617                                       | 0.979                          | 0.375            | -64.811   | 507.605   | -103.931  | -538.758  |
| 1.699                                       | 0.735                          | 0.247            | -69.623   | 544.908   | -114.217  | -567.565  |
| 2.104                                       | 0.439                          | 0.24             | -151.17   | 889.793   | -125.588  | -891.761  |
| 1.639                                       | 0.762                          | 0.28             | -39.218   | 426.095   | -111.312  | -459.087  |
| 1.59                                        | 0.961                          | 0.29             | -69.066   | 529.301   | -105.571  | -561.092  |
| 1.833                                       | 0.954                          | 0.216            | -62.241   | 471.518   | -95.622   | -489.073  |
| 1.781                                       | 1.137                          | 0.317            | -71.811   | 519.247   | -94.379   | -552.2    |
| 1.708                                       | 0.982                          | 0.205            | -77.298   | 575.28    | -112.87   | -601.852  |
| 1.762                                       | 0.934                          | 0.317            | -51.586   | 460.347   | -104.914  | -491.861  |
| 1.785                                       | 0.849                          | 0.372            | -59.746   | 478.448   | -99.472   | -507.32   |
| 1.612                                       | 0.676                          | 0.331            | -107.854  | 716.736   | -122.623  | -739.941  |
| 1.699                                       | 0.83                           | 0.301            | -74.757   | 584.432   | -119.679  | -615.363  |
| 1.952                                       | 0.671                          | 0.259            | -67.925   | 529.312   | -107.349  | -551.22   |
| 1.902                                       | 0.765                          | 0.351            | -66.852   | 508.896   | -101.693  | -531.02   |
| 1.725                                       | 0.962                          | 0.32             | -59.44    | 475.323   | -99.347   | -503.434  |
| 1.736                                       | 0.692                          | 0.202            | -54.802   | 451.465   | -99.653   | -469.193  |
| 1.872                                       | 0.607                          | 0.281            | -61.778   | 478.498   | -98.121   | -496.61   |
| 1.744                                       | 0.512                          | 0.216            | -64.033   | 484.129   | -98.495   | -498.008  |
| 1.783                                       | 0.837                          | 0.285            | -80.91    | 551.404   | -97.013   | -570.433  |
| 1.669                                       | 0.835                          | 0.263            | -58.438   | 489.824   | -107.552  | -518.89   |
| 1.784                                       | 1.182                          | 0.379            | -78.105   | 583.012   | -112.129  | -619.832  |
| 1.671                                       | 1.085                          | 0.332            | -69.176   | 532.288   | -107.48   | -563.224  |
| 1.876                                       | 0.63                           | 0.278            | -63.631   | 457.704   | -85.365   | -475.123  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.838                                       | 0.799                          | 0.335            | -66.893   | 524.879   | -109.716  | -547.403  |
| 1.696                                       | 0.936                          | 0.383            | -68.257   | 521.586   | -105.035  | -549.523  |
| 1.619                                       | 0.951                          | 0.304            | -48.225   | 427.621   | -98.784   | -455.558  |
| 1.729                                       | 0.95                           | 0.362            | -74.076   | 540.712   | -99.479   | -574.686  |
| 1.692                                       | 0.778                          | 0.24             | -62.975   | 487.425   | -101.826  | -504.965  |
| 1.506                                       | 0.652                          | 0.317            | -51.449   | 438.667   | -98.367   | -464.798  |
| 1.743                                       | 0.817                          | 0.355            | -70.429   | 553.384   | -112.29   | -585.64   |
| 1.627                                       | 0.656                          | 0.271            | -46.353   | 437.417   | -104.647  | -465.111  |
| 1.794                                       | 0.567                          | 0.139            | -67.431   | 482.743   | -92.561   | -493.185  |
| 1.499                                       | 1.072                          | 0.243            | -67.398   | 559.918   | -118.626  | -605.982  |
| 1.789                                       | 0.561                          | 0.232            | -77.521   | 563.454   | -108.035  | -580.386  |
| 1.711                                       | 0.972                          | 0.363            | -74.233   | 518.882   | -91.553   | -547.987  |
| 1.606                                       | 1.239                          | 0.326            | -88.765   | 680.924   | -135.898  | -727.409  |
| 1.777                                       | 0.773                          | 0.282            | -45.548   | 395.328   | -91.399   | -413.7    |
| 1.496                                       | 1.071                          | 0.225            | -76.264   | 582.644   | -115.531  | -621.088  |
| 1.802                                       | 0.778                          | 0.425            | -79.579   | 599.456   | -115.447  | -634.123  |
| 1.814                                       | 0.501                          | 0.265            | -76.591   | 561.548   | -107.989  | -580.566  |
| 1.881                                       | 0.672                          | 0.217            | -63.466   | 517.17    | -112.342  | -535.795  |
| 1.62                                        | 0.921                          | 0.317            | -58.408   | 466.304   | -96.791   | -496.304  |
| 1.741                                       | 0.884                          | 0.301            | -70.637   | 557.11    | -115.754  | -585.472  |
| 1.701                                       | 0.937                          | 0.213            | -65.817   | 502.028   | -100.355  | -526.869  |
| 1.503                                       | 0.932                          | 0.234            | -67.287   | 554.504   | -119.452  | -590.93   |
| 1.765                                       | 0.933                          | 0.313            | -54.444   | 449.028   | -94.817   | -479.528  |
| 1.688                                       | 0.705                          | 0.28             | -71.254   | 539.537   | -109.465  | -559.498  |
| 1.816                                       | 0.882                          | 0.408            | -67.138   | 513.834   | -102.771  | -542.048  |
| 1.97                                        | 0.691                          | 0.289            | -86.521   | 614.048   | -114.923  | -630.999  |
| 1.766                                       | 0.564                          | 0.267            | -83.142   | 588.99    | -111.146  | -603.409  |
| 1.556                                       | 0.837                          | 0.301            | -57.131   | 463.659   | -99.736   | -489.736  |
| 1.684                                       | 0.723                          | 0.297            | -52.834   | 453.487   | -99.519   | -482.059  |
| 1.717                                       | 0.886                          | 0.251            | -59.963   | 462.743   | -94.409   | -486.139  |
| 1.865                                       | 0.865                          | 0.345            | -66.643   | 513.267   | -103.407  | -538.401  |
| 1.632                                       | 1.154                          | 0.321            | -86.908   | 630.515   | -115.449  | -673.047  |
| 1.529                                       | 0.539                          | 0.333            | -13.277   | 296.041   | -100.86   | -326.287  |
| 1.742                                       | 0.969                          | 0.303            | -35.516   | 402.953   | -109.259  | -434.525  |
| 1.506                                       | 0.909                          | 0.277            | -70.877   | 557.043   | -113.681  | -594.293  |
| 1.811                                       | 0.937                          | 0.399            | -87.134   | 602.441   | -105.678  | -630.999  |
| 1.67                                        | 0.783                          | 0.342            | -68.241   | 500.711   | -94.414   | -527.657  |
| 1.564                                       | 0.837                          | 0.194            | -58.584   | 471.365   | -100.611  | -495.581  |
| 1.894                                       | 0.914                          | 0.352            | -94.826   | 618.648   | -98.565   | -645.646  |
| 1.932                                       | 0.832                          | 0.335            | -70.788   | 534.283   | -105.178  | -557.443  |
| 1.62                                        | 1.21                           | 0.34             | -82.045   | 588.823   | -104.891  | -633.514  |
| 1.851                                       | 0.907                          | 0.263            | -67.693   | 526.626   | -110.092  | -548.044  |
| 1.768                                       | 0.747                          | 0.358            | -71.283   | 631.456   | -147.941  | -662.479  |
| 1.806                                       | 0.729                          | 0.319            | -57.919   | 457.047   | -96.46    | -476.414  |
| 1.602                                       | 0.599                          | 0.195            | -62.829   | 501.582   | -106.862  | -523.442  |
| 1.777                                       | 0.947                          | 0.354            | -66.027   | 516.235   | -108.372  | -539.016  |
| 1.662                                       | 0.678                          | 0.304            | -73.247   | 550.673   | -109.917  | -572.7    |
| 1.727                                       | 0.975                          | 0.342            | -81.317   | 572.97    | -104.607  | -599.372  |
| 1.78                                        | 0.722                          | 0.31             | -75.679   | 564.292   | -111.319  | -587.311  |
| 1.707                                       | 0.902                          | 0.381            | -81.694   | 614.48    | -118.615  | -652.61   |
| 1.966                                       | 0.941                          | 0.403            | -74.415   | 547.14    | -104.078  | -573.261  |
| 1.626                                       | 0.89                           | 0.352            | -63.735   | 534.352   | -117.125  | -568.891  |
| 1.757                                       | 0.735                          | 0.231            | -54.2     | 434.636   | -92.767   | -453.226  |
| 1.652                                       | 0.597                          | 0.326            | -70.779   | 562.077   | -119.816  | -584.452  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.939                                       | 0.855                          | 0.383            | -93.217   | 629.685   | -107.3    | -655.047  |
| 1.782                                       | 0.754                          | 0.294            | -75.294   | 574.602   | -116.32   | -598.187  |
| 1.66                                        | 0.558                          | 0.206            | -59.559   | 445.586   | -88.574   | -461.905  |
| 1.435                                       | 0.608                          | 0.282            | -66.261   | 504.554   | -102.12   | -528.174  |
| 1.616                                       | 0.823                          | 0.284            | -62.407   | 506.725   | -110.725  | -531.965  |
| 1.799                                       | 0.917                          | 0.418            | -70.752   | 501.23    | -89.945   | -528.132  |
| 1.644                                       | 0.827                          | 0.27             | -64.374   | 502.082   | -101.809  | -530.916  |
| 1.843                                       | 1.004                          | 0.232            | -67.225   | 488.466   | -92.922   | -509.528  |
| 2.029                                       | 0.685                          | 0.269            | -92.499   | 581.049   | -89.995   | -593.718  |
| 1.741                                       | 0.946                          | 0.271            | -69.25    | 522.447   | -101.703  | -552.512  |
| 1.813                                       | 0.766                          | 0.284            | -50.676   | 405.813   | -84.486   | -427.635  |
| 1.587                                       | 1.04                           | 0.211            | -68.912   | 554.977   | -116.153  | -591.474  |
| 1.764                                       | 0.692                          | 0.157            | -63.105   | 517.495   | -116.351  | -531.065  |
| 1.609                                       | 0.892                          | 0.165            | -80.177   | 617.82    | -124.001  | -652.34   |
| 1.775                                       | 0.751                          | 0.322            | -74.827   | 562.83    | -110.267  | -590.074  |
| 1.751                                       | 0.465                          | 0.191            | -60.664   | 448.772   | -88.501   | -462.109  |
| 1.712                                       | 0.724                          | 0.303            | -49.643   | 424.778   | -94.312   | -449.162  |
| 1.718                                       | 0.622                          | 0.327            | -80.541   | 588.543   | -112.277  | -613.14   |
| 1.75                                        | 1.012                          | 0.349            | -50.602   | 408.626   | -86.708   | -432.501  |
| 1.862                                       | 1.121                          | 0.435            | -86.044   | 616.195   | -113.956  | -648.211  |
| 1.62                                        | 1.039                          | 0.278            | -71.5     | 546.976   | -108.683  | -581.338  |
| 1.704                                       | 0.868                          | 0.324            | -70.791   | 519.747   | -100.348  | -543.637  |
| 1.59                                        | 0.589                          | 0.231            | -55.043   | 463.736   | -102.929  | -486.67   |
| 1.603                                       | 0.679                          | 0.319            | -44.92    | 393.227   | -90.378   | -415.463  |
| 1.751                                       | 0.905                          | 0.315            | -75.927   | 570.188   | -112.227  | -598.176  |
| 1.431                                       | 1.167                          | 0.316            | -60.256   | 509.614   | -109.995  | -554.492  |
| 1.852                                       | 0.823                          | 0.259            | -46.853   | 460.823   | -116.395  | -485.295  |
| 1.602                                       | 0.687                          | 0.335            | -80.177   | 613.674   | -125.041  | -641.551  |
| 1.713                                       | 0.774                          | 0.183            | -60.23    | 483.685   | -103.657  | -505.206  |
| 1.805                                       | 0.747                          | 0.3              | -77.745   | 555.155   | -102.438  | -578.524  |
| 1.766                                       | 0.752                          | 0.311            | -75.887   | 597.794   | -123.619  | -627.692  |
| 1.764                                       | 0.693                          | 0.295            | -52.135   | 450.127   | -102.003  | -472.548  |
| 1.77                                        | 0.595                          | 0.271            | -69.91    | 520.971   | -101.479  | -541.907  |
| 1.634                                       | 1.016                          | 0.327            | -40.203   | 404.374   | -101.403  | -436.071  |
| 1.7                                         | 1.285                          | 0.29             | -102.127  | 707.877   | -121.671  | -753.827  |
| 1.419                                       | 0.929                          | 0.244            | -66.423   | 502.944   | -97.303   | -538.091  |
| 1.34                                        | 0.591                          | 0.19             | -44.512   | 434.776   | -109.3    | -462.64   |
| 1.531                                       | 0.742                          | 0.246            | -75.905   | 552.909   | -105.668  | -578.206  |
| 1.662                                       | 0.903                          | 0.278            | -61.514   | 477.686   | -95.795   | -507.318  |
| 1.726                                       | 1.027                          | 0.33             | -59.393   | 480.169   | -101.134  | -510.105  |
| 1.708                                       | 0.599                          | 0.266            | -67.127   | 517.362   | -105.829  | -538.183  |
| 1.53                                        | 0.608                          | 0.182            | -42.722   | 411.479   | -102.215  | -434.318  |
| 1.792                                       | 0.675                          | 0.235            | -76.301   | 570.189   | -113.774  | -588.019  |
| 1.597                                       | 0.853                          | 0.257            | -63.481   | 572.34    | -135.118  | -607.729  |
| 1.693                                       | 0.949                          | 0.297            | -64.05    | 517.081   | -111.432  | -543.395  |
| 1.731                                       | 0.786                          | 0.249            | -54.161   | 440.954   | -94.592   | -463.549  |
| 1.752                                       | 0.586                          | 0.214            | -67.919   | 508.417   | -100.161  | -528.079  |
| 1.805                                       | 0.84                           | 0.3              | -70.588   | 541.575   | -109.634  | -565.174  |
| 1.623                                       | 0.685                          | 0.243            | -87.813   | 641.731   | -122.431  | -669.39   |
| 1.614                                       | 0.747                          | 0.327            | -71.701   | 564.468   | -118.826  | -591.154  |
| 1.87                                        | 0.972                          | 0.35             | -75.317   | 568.847   | -111.666  | -598.207  |
| 1.726                                       | 0.782                          | 0.301            | -65.817   | 506.316   | -103.917  | -527.862  |
| 1.958                                       | 0.865                          | 0.455            | -120.295  | 698.589   | -90.516   | -718.77   |
| 1.566                                       | 0.826                          | 0.282            | -75.061   | 575.791   | -117.562  | -603.598  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.664                                       | 0.773                          | 0.292            | -58.216   | 447.422   | -89.648   | -470.918  |
| 1.754                                       | 0.645                          | 0.238            | -72.834   | 534.597   | -102.745  | -554.565  |
| 1.719                                       | 0.785                          | 0.301            | -87.062   | 578.015   | -98.32    | -596.973  |
| 1.818                                       | 0.89                           | 0.334            | -68.223   | 517.553   | -104.351  | -540.261  |
| 1.67                                        | 1.054                          | 0.355            | -90.528   | 630.506   | -108.927  | -671.307  |
| 1.707                                       | 0.732                          | 0.344            | -68.688   | 501.621   | -95.944   | -523.738  |
| 1.84                                        | 0.561                          | 0.289            | -79.727   | 610.965   | -125.589  | -629.213  |
| 1.494                                       | 0.775                          | 0.296            | -67.476   | 520.242   | -106.167  | -547.624  |
| 1.912                                       | 0.82                           | 0.338            | -124.245  | 740.068   | -103.757  | -757.923  |
| 1.889                                       | 0.652                          | 0.334            | -62.028   | 508.475   | -108.493  | -533.47   |
| 1.721                                       | 1.035                          | 0.347            | -53.489   | 472.746   | -109.157  | -503.89   |
| 1.76                                        | 0.955                          | 0.36             | -72.493   | 511.938   | -91.548   | -539.288  |
| 1.587                                       | 0.846                          | 0.237            | -40.069   | 423.519   | -112.894  | -449.823  |
| 1.689                                       | 0.991                          | 0.328            | -76.531   | 577.92    | -113.346  | -610.965  |
| 1.717                                       | 1.15                           | 0.406            | -66.394   | 504.12    | -98.331   | -538.519  |
| 1.956                                       | 0.712                          | 0.261            | -58.858   | 443.65    | -89.013   | -458.607  |
| 1.754                                       | 0.688                          | 0.321            | -65.951   | 517.075   | -106.296  | -541.679  |
| 1.581                                       | 0.813                          | 0.195            | -56.585   | 471.703   | -102.278  | -500.198  |
| 1.779                                       | 0.869                          | 0.242            | -61.227   | 498.42    | -108.147  | -520.733  |
| 1.516                                       | 1.07                           | 0.277            | -62.385   | 488.661   | -97.337   | -525.809  |
| 1.725                                       | 0.833                          | 0.334            | -60.858   | 476.264   | -95.989   | -505.138  |
| 1.796                                       | 0.902                          | 0.37             | -68.07    | 481.735   | -87.118   | -505.992  |
| 1.779                                       | 0.663                          | 0.248            | -37.235   | 413.783   | -111.826  | -439.274  |
| 1.703                                       | 0.73                           | 0.273            | -77.294   | 585.16    | -118.128  | -608.864  |
| 1.742                                       | 0.883                          | 0.259            | -62.081   | 500.828   | -106.83   | -525.777  |
| 1.779                                       | 0.749                          | 0.383            | -69.861   | 508.936   | -95.305   | -534.288  |
| 1.631                                       | 0.883                          | 0.241            | -64.783   | 507.425   | -106.461  | -531.376  |
| 1.715                                       | 0.685                          | 0.186            | -67.887   | 514.86    | -104.194  | -533.126  |
| 1.776                                       | 0.774                          | 0.282            | -70.62    | 510.57    | -97.952   | -529.089  |
| 1.753                                       | 0.739                          | 0.218            | -66.116   | 511.914   | -106.321  | -531.379  |
| 1.675                                       | 0.819                          | 0.328            | -48.806   | 408.06    | -90.081   | -430.409  |
| 1.651                                       | 1.095                          | 0.382            | -64.86    | 521.719   | -109.24   | -555.795  |
| 1.407                                       | 0.628                          | 0.154            | -74.18    | 559.015   | -110.704  | -585.791  |
| 1.904                                       | 0.586                          | 0.265            | -63.539   | 485.712   | -99.126   | -500.255  |
| 1.664                                       | 0.862                          | 0.342            | -54.685   | 466.771   | -103.633  | -497.734  |
| 1.659                                       | 0.813                          | 0.29             | -84.647   | 618.531   | -114.361  | -654.021  |
| 1.515                                       | 1.135                          | 0.197            | -62.131   | 504.269   | -109.586  | -533.928  |
| 1.693                                       | 0.688                          | 0.212            | -53.23    | 398.281   | -78.489   | -414.845  |
| 1.53                                        | 0.777                          | 0.217            | -51.727   | 422.592   | -91.207   | -445.891  |
| 1.773                                       | 1.039                          | 0.343            | -67.03    | 528.015   | -109.341  | -557.288  |
| 1.815                                       | 0.659                          | 0.218            | -68.066   | 534.19    | -110.119  | -556.256  |
| 1.722                                       | 0.805                          | 0.331            | -71.044   | 533.867   | -106.515  | -557.577  |
| 1.722                                       | 0.813                          | 0.33             | -62.199   | 486.656   | -101.341  | -510.184  |
| 1.743                                       | 0.801                          | 0.25             | -55.227   | 452.253   | -99.662   | -470.721  |
| 1.799                                       | 0.774                          | 0.344            | -57.792   | 471.066   | -102.703  | -492.001  |
| 1.793                                       | 0.785                          | 0.28             | -62.829   | 499.984   | -104.909  | -524.152  |
| 1.98                                        | 0.886                          | 0.312            | -85.907   | 625.662   | -117.945  | -651.823  |
| 1.471                                       | 0.711                          | 0.279            | -78.808   | 595.583   | -120.639  | -622.269  |
| 1.788                                       | 0.947                          | 0.206            | -104.296  | 773.793   | -151.709  | -806.361  |
| 1.53                                        | 0.876                          | 0.336            | -60.789   | 492.963   | -103.379  | -526.483  |
| 1.663                                       | 0.704                          | 0.271            | -59.299   | 486.752   | -107.54   | -507.818  |
| 1.901                                       | 0.709                          | 0.297            | -73.394   | 566.739   | -117.738  | -585.265  |
| 1.566                                       | 0.798                          | 0.267            | -62.12    | 488.259   | -100.581  | -516.367  |
| 1.792                                       | 0.728                          | 0.296            | -58.726   | 485.561   | -105.121  | -509.724  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.69                                        | 0.588                          | 0.255            | -76.511   | 593.558   | -122.841  | -616.7    |
| 1.59                                        | 0.89                           | 0.237            | -75.184   | 571.916   | -114.432  | -601.952  |
| 1.777                                       | 0.717                          | 0.294            | -62.987   | 490.425   | -100.785  | -512.51   |
| 1.933                                       | 0.92                           | 0.29             | -86.296   | 578.074   | -96.163   | -602.992  |
| 1.764                                       | 0.782                          | 0.329            | -69.849   | 564.726   | -121.469  | -590.327  |
| 1.564                                       | 1.031                          | 0.232            | -87.594   | 656.043   | -127.073  | -694.621  |
| 1.708                                       | 0.688                          | 0.22             | -56.113   | 465.359   | -103.402  | -485.609  |
| 1.865                                       | 0.933                          | 0.304            | -69.425   | 523.521   | -102.475  | -550.966  |
| 1.585                                       | 0.913                          | 0.28             | -62.1     | 486.705   | -101.588  | -511.677  |
| 1.755                                       | 0.836                          | 0.299            | -74.132   | 580.495   | -119.218  | -610.252  |
| 1.695                                       | 0.749                          | 0.306            | -62.661   | 497.724   | -103.853  | -523.946  |
| 1.745                                       | 0.867                          | 0.346            | -66.326   | 513.926   | -104.641  | -541.044  |
| 1.704                                       | 0.803                          | 0.322            | -76.113   | 561.797   | -109.974  | -584.777  |
| 1.712                                       | 0.929                          | 0.355            | -54.925   | 448.014   | -93.461   | -479.067  |
| 1.924                                       | 0.775                          | 0.298            | -66.448   | 537.23    | -115.373  | -559.914  |
| 1.671                                       | 0.649                          | 0.262            | -86.727   | 546.167   | -85.746   | -560.42   |
| 1.816                                       | 0.874                          | 0.29             | -60.43    | 503.396   | -111.299  | -527.669  |
| 1.808                                       | 0.775                          | 0.347            | -56.873   | 447.293   | -92.411   | -468.49   |
| 1.56                                        | 0.933                          | 0.309            | -66.2     | 543.929   | -118.079  | -576.366  |
| 1.752                                       | 0.584                          | 0.315            | -78.166   | 570.084   | -109.202  | -591.767  |
| 1.61                                        | 0.666                          | 0.238            | -67.073   | 526.239   | -110.474  | -549.009  |
| 1.837                                       | 0.726                          | 0.194            | -48.836   | 428.289   | -99.558   | -445.614  |
| 1.653                                       | 0.803                          | 0.272            | -65.369   | 488.373   | -93.16    | -517.214  |
| 1.758                                       | 0.93                           | 0.3              | -72.113   | 542.816   | -105.251  | -572.647  |
| 1.806                                       | 0.64                           | 0.187            | -69.407   | 515.101   | -103.732  | -527.343  |
| 1.661                                       | 0.813                          | 0.328            | -110.6    | 723.986   | -121.162  | -747.948  |
| 1.438                                       | 0.929                          | 0.287            | -68.861   | 514.094   | -98.044   | -549.04   |
| 1.722                                       | 1.102                          | 0.292            | -76.661   | 560.626   | -105.123  | -593.443  |
| 1.711                                       | 1.198                          | 0.278            | -72.632   | 563.244   | -114.404  | -597.101  |
| 1.724                                       | 0.718                          | 0.279            | -50.752   | 434.402   | -98.895   | -454.521  |
| 1.743                                       | 0.923                          | 0.36             | -65.513   | 487.191   | -95.882   | -510.034  |
| 1.625                                       | 1.042                          | 0.357            | -68.319   | 511.568   | -98.106   | -545.884  |
| 1.633                                       | 1.018                          | 0.323            | -63.25    | 491.215   | -101.344  | -518.347  |
| 1.698                                       | 0.769                          | 0.305            | -56.153   | 477.812   | -109.396  | -498.527  |
| 1.762                                       | 0.88                           | 0.325            | -67.832   | 497.628   | -96.347   | -518.694  |
| 1.962                                       | 0.722                          | 0.306            | -88.752   | 626.065   | -116.624  | -642.039  |
| 1.671                                       | 0.691                          | 0.111            | -60.077   | 464.933   | -95.948   | -483.478  |
| 1.752                                       | 0.825                          | 0.268            | -51.663   | 419.672   | -89.506   | -441.98   |
| 1.718                                       | 0.99                           | 0.438            | -73.72    | 550.029   | -105.063  | -584.802  |
| 1.905                                       | 0.563                          | 0.292            | -68.221   | 539.898   | -115.519  | -554.297  |
| 1.741                                       | 0.72                           | 0.313            | -76.756   | 547.295   | -100.947  | -570.255  |
| 1.58                                        | 0.722                          | 0.273            | -64.014   | 505.145   | -105.86   | -529.044  |
| 1.81                                        | 0.921                          | 0.284            | -71.591   | 533.253   | -101.863  | -563.578  |
| 1.656                                       | 0.578                          | 0.329            | -65.155   | 498.818   | -101.629  | -518.979  |
| 1.689                                       | 0.573                          | 0.318            | -72.064   | 544.123   | -107.713  | -567.468  |
| 1.59                                        | 0.72                           | 0.273            | -64.289   | 517.367   | -109.038  | -545.677  |
| 1.934                                       | 0.876                          | 0.305            | -51.873   | 417.86    | -88.522   | -438.142  |
| 1.624                                       | 0.788                          | 0.308            | -78.798   | 562.56    | -103.835  | -590.097  |
| 1.68                                        | 1.008                          | 0.366            | -77.165   | 595.543   | -118.786  | -633.62   |
| 1.718                                       | 0.69                           | 0.243            | -54.025   | 432.639   | -91.169   | -453.682  |
| 1.642                                       | 0.798                          | 0.251            | -71.802   | 544.923   | -108.83   | -570.557  |
| 1.613                                       | 0.815                          | 0.34             | -66.17    | 548.983   | -117.258  | -585.192  |
| 1.732                                       | 0.777                          | 0.3              | -44.571   | 374.38    | -81.713   | -396.721  |
| 1.576                                       | 0.916                          | 0.246            | -52.39    | 455.688   | -104.826  | -482.25   |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.414                                       | 1.238                          | 0.371            | -65.486   | 499.707   | -95.459   | -544.315  |
| 1.966                                       | 0.803                          | 0.225            | -157.524  | 873.567   | -101.894  | -891.673  |
| 1.773                                       | 0.862                          | 0.317            | -65.181   | 527.235   | -111.4    | -556.364  |
| 1.676                                       | 0.706                          | 0.305            | -60.767   | 500.151   | -109.978  | -522.85   |
| 1.876                                       | 0.952                          | 0.305            | -82.646   | 617.543   | -121.154  | -645.112  |
| 1.668                                       | 0.706                          | 0.195            | -62.779   | 495.564   | -102.777  | -518.667  |
| 1.852                                       | 0.752                          | 0.358            | -76.384   | 579.127   | -115.084  | -605.323  |
| 1.598                                       | 0.66                           | 0.233            | -63.345   | 507.995   | -110.447  | -527.466  |
| 1.707                                       | 0.545                          | 0.291            | -65.087   | 501.806   | -102.413  | -522.35   |
| 1.901                                       | 0.732                          | 0.262            | -90.307   | 595.755   | -101.785  | -609.116  |
| 1.712                                       | 0.696                          | 0.322            | -55.798   | 460.605   | -98.43    | -487.419  |
| 1.768                                       | 0.753                          | 0.257            | -61.293   | 474.774   | -96.938   | -495.534  |
| 1.838                                       | 0.903                          | 0.405            | -64.857   | 516.986   | -105.729  | -549.962  |
| 1.596                                       | 0.705                          | 0.233            | -42.036   | 380.139   | -89.221   | -402.707  |
| 1.716                                       | 1.008                          | 0.297            | -59.417   | 500.599   | -109.418  | -533.946  |
| 1.705                                       | 0.949                          | 0.284            | -63.808   | 481.635   | -93.869   | -509.328  |
| 1.737                                       | 0.724                          | 0.282            | -76.334   | 575.746   | -114.955  | -600.268  |
| 1.671                                       | 0.781                          | 0.253            | -58.675   | 476.367   | -102.13   | -500.601  |
| 1.773                                       | 0.895                          | 0.44             | -59.744   | 474.857   | -97.29    | -505.314  |
| 1.627                                       | 1.033                          | 0.224            | -66.987   | 521.306   | -105.434  | -553.511  |
| 1.887                                       | 0.85                           | 0.334            | -60.855   | 484.556   | -101.432  | -507.672  |
| 1.742                                       | 0.86                           | 0.268            | -57.922   | 483.501   | -106.25   | -509.786  |
| 1.813                                       | 0.743                          | 0.28             | -81.556   | 613.04    | -123.506  | -632.792  |
| 1.714                                       | 0.711                          | 0.313            | -107.318  | 760.265   | -139.261  | -791.616  |
| 1.74                                        | 0.748                          | 0.252            | -45.647   | 472.579   | -122.493  | -500.624  |
| 1.657                                       | 0.733                          | 0.248            | -64.367   | 507.51    | -106.846  | -529.406  |
| 1.695                                       | 0.99                           | 0.356            | -60.406   | 476.865   | -97.639   | -506.311  |
| 1.84                                        | 0.656                          | 0.366            | -88.914   | 624.461   | -112.574  | -649.267  |
| 1.682                                       | 0.95                           | 0.166            | -71.486   | 529.79    | -105.186  | -551.475  |
| 1.788                                       | 0.901                          | 0.318            | -62.525   | 509.936   | -109.48   | -537.396  |
| 1.584                                       | 0.843                          | 0.209            | -51.136   | 435.893   | -99.084   | -458.066  |
| 1.724                                       | 0.775                          | 0.376            | -67.785   | 537.813   | -111.906  | -566.945  |
| 1.821                                       | 0.934                          | 0.313            | -65.916   | 486.452   | -93.136   | -510.659  |
| 1.546                                       | 0.684                          | 0.227            | -59.092   | 462.103   | -96.56    | -482.63   |
| 1.65                                        | 0.792                          | 0.265            | -62.148   | 485.19    | -99.488   | -510.676  |
| 1.649                                       | 1.064                          | 0.308            | -90.762   | 623.572   | -108.247  | -656.764  |
| 1.756                                       | 0.846                          | 0.363            | -69.979   | 527.516   | -102.724  | -555.978  |
| 1.709                                       | 0.865                          | 0.278            | -66.512   | 539.318   | -116.778  | -563.556  |
| 1.751                                       | 1.058                          | 0.329            | -79.587   | 575.342   | -106.116  | -608.779  |
| 1.593                                       | 0.629                          | 0.255            | -71.502   | 541.108   | -107.516  | -565.589  |
| 1.629                                       | 0.853                          | 0.332            | -77.632   | 574.867   | -110.459  | -606.349  |
| 1.749                                       | 0.689                          | 0.244            | -66.474   | 497.019   | -98.458   | -516.124  |
| 1.744                                       | 0.703                          | 0.297            | -59.855   | 516.827   | -117.033  | -542.805  |
| 1.707                                       | 0.758                          | 0.238            | -69.812   | 494.621   | -90.836   | -514.612  |
| 1.689                                       | 0.847                          | 0.333            | -52.994   | 436.384   | -93.81    | -462.979  |
| 1.575                                       | 0.922                          | 0.233            | -70.701   | 524.502   | -101.07   | -553.424  |
| 1.659                                       | 0.818                          | 0.222            | -73.782   | 559.256   | -111.997  | -585.272  |
| 1.632                                       | 0.839                          | 0.289            | -73.491   | 589.689   | -125.67   | -621.047  |
| 1.717                                       | 0.803                          | 0.299            | -68.622   | 545.363   | -112.176  | -576.4    |
| 1.682                                       | 0.801                          | 0.385            | -61.279   | 514.879   | -113.604  | -545.15   |
| 1.866                                       | 0.613                          | 0.348            | -72.013   | 538.89    | -107.519  | -555.871  |
| 1.3                                         | 1.004                          | 0.306            | -63.184   | 532.645   | -112.562  | -583.069  |
| 1.666                                       | 0.75                           | 0.299            | -64.043   | 523.707   | -115.213  | -547.091  |
| 1.595                                       | 1.083                          | 0.324            | -63.842   | 484.639   | -94.832   | -517.695  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.663                                       | 0.795                          | 0.252            | -62.917   | 489.973   | -100.933  | -513.453  |
| 1.469                                       | 0.643                          | 0.361            | -50.415   | 437.717   | -99.082   | -466.292  |
| 1.677                                       | 0.936                          | 0.264            | -90.831   | 705.986   | -148.23   | -736.443  |
| 1.677                                       | 0.752                          | 0.418            | -61.139   | 445.573   | -83.931   | -468.534  |
| 1.798                                       | 0.876                          | 0.283            | -62.503   | 478.572   | -96.681   | -500.898  |
| 1.617                                       | 0.65                           | 0.279            | -65.773   | 477.994   | -90.321   | -498.837  |
| 1.751                                       | 1.017                          | 0.337            | -66.34    | 510.904   | -103.643  | -538.591  |
| 1.742                                       | 0.846                          | 0.31             | -55.292   | 444.767   | -95.334   | -466.339  |
| 1.821                                       | 0.744                          | 0.331            | -52.272   | 437.727   | -95.045   | -462.245  |
| 1.673                                       | 0.818                          | 0.257            | -80.519   | 603.988   | -119.207  | -632.555  |
| 1.478                                       | 0.689                          | 0.24             | -61.63    | 520.849   | -115.417  | -551.434  |
| 1.661                                       | 0.769                          | 0.304            | -67.192   | 542.07    | -113.397  | -574.215  |
| 1.787                                       | 0.853                          | 0.203            | -67.482   | 492.999   | -95.141   | -512.152  |
| 1.819                                       | 1.042                          | 0.31             | -74.999   | 556.263   | -109.196  | -580.328  |
| 1.618                                       | 0.923                          | 0.355            | -71.207   | 548.575   | -112.461  | -576.479  |
| 1.731                                       | 0.682                          | 0.367            | -68.789   | 532.772   | -109.179  | -556.118  |
| 1.735                                       | 0.91                           | 0.322            | -65.237   | 507.318   | -102.474  | -537.051  |
| 1.844                                       | 0.695                          | 0.244            | -54.224   | 434.146   | -93.152   | -449.981  |
| 1.723                                       | 0.644                          | 0.252            | -49.735   | 407.14    | -87.967   | -426.271  |
| 1.525                                       | 0.733                          | 0.27             | -54.716   | 424.953   | -89.429   | -442.982  |
| 1.549                                       | 0.668                          | 0.303            | -61.65    | 499.446   | -106.779  | -527.642  |
| 1.815                                       | 0.774                          | 0.276            | -77.151   | 597.503   | -121.761  | -623.589  |
| 1.76                                        | 0.883                          | 0.379            | -63.568   | 482.753   | -95.557   | -507.635  |
| 1.818                                       | 0.909                          | 0.285            | -69.824   | 517.797   | -101.452  | -540.012  |
| 1.635                                       | 0.804                          | 0.273            | -50.487   | 427.008   | -94.805   | -451.325  |
| 1.577                                       | 0.887                          | 0.305            | -44.331   | 410.909   | -97.41    | -440.684  |
| 1.59                                        | 1.015                          | 0.274            | -58.136   | 480.429   | -103.586  | -511.54   |
| 1.784                                       | 0.698                          | 0.243            | -62.223   | 525.267   | -116.754  | -549.786  |
| 1.767                                       | 0.919                          | 0.319            | -67.38    | 510.906   | -100.907  | -537.28   |
| 1.772                                       | 1.035                          | 0.356            | -76.602   | 584.115   | -116.414  | -614.94   |
| 1.707                                       | 0.673                          | 0.284            | -95.154   | 647.433   | -115.976  | -664.944  |
| 1.68                                        | 0.923                          | 0.318            | -64.062   | 505.976   | -103.705  | -536.318  |
| 1.648                                       | 0.995                          | 0.312            | -80.346   | 596.257   | -113.657  | -631.412  |
| 1.63                                        | 0.985                          | 0.271            | -55.553   | 450.337   | -96.178   | -477.081  |
| 1.646                                       | 0.766                          | 0.329            | -79.434   | 583.401   | -110.432  | -613.406  |
| 1.532                                       | 0.995                          | 0.275            | -61.935   | 498.906   | -104.472  | -532.325  |
| 1.782                                       | 1.099                          | 0.374            | -117.457  | 738.824   | -111.28   | -773.74   |
| 1.733                                       | 0.83                           | 0.292            | -74       | 549.44    | -106.934  | -574.517  |
| 1.874                                       | 0.825                          | 0.353            | -75.76    | 562.083   | -108.133  | -588.171  |
| 1.901                                       | 0.735                          | 0.357            | -77.523   | 556.657   | -103.994  | -577.71   |
| 1.758                                       | 0.737                          | 0.209            | -56.894   | 474.701   | -104.721  | -496.385  |
| 1.66                                        | 0.604                          | 0.294            | -61.333   | 495.457   | -106.681  | -516.117  |
| 1.561                                       | 0.653                          | 0.212            | -36.69    | 397.468   | -107.647  | -420.283  |
| 1.688                                       | 0.579                          | 0.194            | -73.626   | 545.401   | -108.167  | -562.25   |
| 1.806                                       | 0.598                          | 0.298            | -103.016  | 689.33    | -118.525  | -708.65   |
| 1.722                                       | 0.699                          | 0.239            | -55.53    | 457.506   | -99.33    | -478.934  |
| 1.54                                        | 0.808                          | 0.27             | -56.642   | 453.553   | -96.01    | -478.474  |
| 1.662                                       | 0.671                          | 0.302            | -77.725   | 557.791   | -105.616  | -578.302  |
| 1.643                                       | 0.809                          | 0.303            | -43.331   | 420.434   | -103.571  | -448.167  |
| 1.691                                       | 0.822                          | 0.41             | -56.265   | 458.869   | -96.677   | -489.268  |
| 1.455                                       | 0.942                          | 0.257            | -63.249   | 542.155   | -122.821  | -576.452  |
| 1.588                                       | 0.697                          | 0.257            | -53.86    | 433.359   | -93.767   | -451.903  |
| 1.734                                       | 0.758                          | 0.306            | -73.423   | 548.451   | -107.118  | -573.493  |
| 1.803                                       | 0.77                           | 0.252            | -65.734   | 499.69    | -101.224  | -518.378  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.717                                       | 0.659                          | 0.244            | -68.526   | 532.71    | -110.545  | -553.592  |
| 1.777                                       | 0.894                          | 0.378            | -89.02    | 628.295   | -114.271  | -656.022  |
| 1.681                                       | 0.793                          | 0.384            | -71.892   | 541.411   | -104.791  | -573.436  |
| 1.955                                       | 1.002                          | 0.323            | -76.659   | 545.155   | -98.135   | -572.039  |
| 1.591                                       | 0.72                           | 0.185            | -51.955   | 405.088   | -83.945   | -424.24   |
| 1.874                                       | 0.623                          | 0.201            | -80.031   | 567.89    | -106.927  | -581.748  |
| 1.659                                       | 0.55                           | 0.224            | -89.133   | 635.352   | -120.816  | -653.128  |
| 1.904                                       | 0.687                          | 0.335            | -82.612   | 597.039   | -114.38   | -616.355  |
| 1.849                                       | 0.806                          | 0.271            | -88.283   | 630.913   | -119.84   | -649.835  |
| 1.673                                       | 0.79                           | 0.285            | -72.081   | 543.605   | -109.116  | -566.724  |
| 1.56                                        | 0.938                          | 0.261            | -83.578   | 652.29    | -133.825  | -689.925  |
| 1.763                                       | 0.802                          | 0.349            | -75.81    | 554.096   | -106.526  | -577.495  |
| 1.532                                       | 0.788                          | 0.341            | -53.829   | 438.777   | -92.769   | -467.722  |
| 1.841                                       | 0.802                          | 0.379            | -56.807   | 496.525   | -110.717  | -528.414  |
| 1.726                                       | 0.779                          | 0.301            | -96.565   | 709.471   | -135.945  | -740.923  |
| 1.75                                        | 0.717                          | 0.288            | -84.542   | 582.079   | -103.855  | -602.02   |
| 1.555                                       | 0.803                          | 0.189            | -65.154   | 490.597   | -98.491   | -512.964  |
| 1.863                                       | 0.75                           | 0.217            | -50.952   | 421.897   | -93.724   | -437.118  |
| 1.718                                       | 1.001                          | 0.295            | -76.024   | 580.233   | -115.536  | -612.163  |
| 1.858                                       | 0.57                           | 0.176            | -62.411   | 464.24    | -92.584   | -476.325  |
| 1.619                                       | 1.055                          | 0.306            | -76.298   | 591.087   | -119.464  | -628.302  |
| 1.77                                        | 0.782                          | 0.359            | -56.766   | 455.436   | -95.672   | -479.703  |
| 1.508                                       | 0.595                          | 0.241            | -42.529   | 437.854   | -110.636  | -470.215  |
| 1.78                                        | 1.013                          | 0.326            | -75.413   | 595.988   | -122.741  | -631.56   |
| 1.708                                       | 0.783                          | 0.309            | -66.692   | 505.432   | -100.338  | -529.21   |
| 1.798                                       | 0.781                          | 0.328            | -63.924   | 483.915   | -97.729   | -502.513  |
| 1.798                                       | 1.096                          | 0.441            | -83.46    | 601.356   | -106.525  | -643.926  |
| 2.023                                       | 0.729                          | 0.236            | -120.046  | 700.843   | -95.569   | -710.227  |
| 1.553                                       | 0.652                          | 0.201            | -77.04    | 548.219   | -102.706  | -568.42   |
| 1.662                                       | 0.902                          | 0.363            | -71.171   | 505.174   | -90.049   | -535.821  |
| 1.837                                       | 0.718                          | 0.238            | -96.201   | 635.77    | -106.868  | -653.282  |
| 1.594                                       | 1.017                          | 0.372            | -80.963   | 562.616   | -96.747   | -598.266  |
| 1.658                                       | 0.849                          | 0.274            | -54.446   | 480.716   | -110.135  | -510.349  |
| 1.752                                       | 0.892                          | 0.213            | -76.896   | 585.645   | -117.744  | -612.447  |
| 1.757                                       | 0.628                          | 0.231            | -76.484   | 547.913   | -104.95   | -562.892  |
| 1.748                                       | 0.964                          | 0.354            | -56.141   | 456.824   | -97.46    | -483.616  |
| 1.781                                       | 0.85                           | 0.301            | -78.197   | 603.748   | -121.378  | -635.292  |
| 1.946                                       | 0.611                          | 0.228            | -73.04    | 486.433   | -84.856   | -494.504  |
| 1.694                                       | 1.084                          | 0.348            | -69.263   | 544.596   | -109.996  | -582.14   |
| 1.761                                       | 0.799                          | 0.233            | -80.493   | 615.554   | -124.788  | -641.158  |
| 1.833                                       | 0.751                          | 0.291            | -78.923   | 581.663   | -113.039  | -603.714  |
| 1.736                                       | 0.783                          | 0.338            | -62.607   | 494.022   | -101.025  | -522.227  |
| 1.95                                        | 1.109                          | 0.358            | -75.473   | 579.811   | -117.691  | -609.89   |
| 1.757                                       | 0.7                            | 0.234            | -70.54    | 564.555   | -120.901  | -585.618  |
| 1.768                                       | 0.896                          | 0.324            | -75.267   | 552.189   | -103.626  | -582.319  |
| 1.673                                       | 0.969                          | 0.296            | -53.313   | 430.696   | -92.214   | -455.226  |
| 1.599                                       | 0.836                          | 0.146            | -74.132   | 568.473   | -117.309  | -591.676  |
| 1.939                                       | 1.173                          | 0.403            | -90.267   | 632.555   | -109.978  | -670.051  |
| 1.586                                       | 0.892                          | 0.297            | -56.85    | 450.99    | -94.294   | -476.399  |
| 1.853                                       | 1.022                          | 0.378            | -84.522   | 608.027   | -113.267  | -637.605  |
| 1.515                                       | 0.758                          | 0.311            | -50.914   | 418.09    | -90.45    | -442.62   |
| 1.723                                       | 0.844                          | 0.4              | -59.745   | 488.11    | -101.266  | -522.516  |
| 1.803                                       | 0.633                          | 0.289            | -60.409   | 457.899   | -90.938   | -477.09   |
| 1.5                                         | 0.978                          | 0.174            | -75.97    | 600.078   | -123.33   | -639.052  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.741                                       | 0.567                          | 0.321            | -42.837   | 449.671   | -116.343  | -476.914  |
| 1.856                                       | 1.182                          | 0.341            | -63.333   | 465.72    | -88.147   | -492.225  |
| 1.636                                       | 0.899                          | 0.285            | -50.916   | 411.593   | -86.852   | -437.115  |
| 1.424                                       | 0.535                          | 0.226            | -59.993   | 431.277   | -80.577   | -450.905  |
| 1.892                                       | 0.803                          | 0.374            | -47       | 390.995   | -85.143   | -411.556  |
| 1.919                                       | 0.946                          | 0.35             | -64.48    | 485.29    | -95.305   | -508.493  |
| 1.737                                       | 0.628                          | 0.254            | -67.951   | 508.488   | -102.019  | -525.499  |
| 1.674                                       | 0.76                           | 0.304            | -50.509   | 454.037   | -105.262  | -483.078  |
| 1.87                                        | 0.849                          | 0.31             | -56.336   | 486.866   | -111.536  | -510.219  |
| 1.672                                       | 0.718                          | 0.369            | -87.207   | 619.661   | -113.427  | -648.265  |
| 1.622                                       | 1.069                          | 0.224            | -62.64    | 479.923   | -97.393   | -506.775  |
| 1.871                                       | 0.596                          | 0.305            | -66.615   | 527.678   | -110.341  | -548.526  |
| 1.563                                       | 1.037                          | 0.271            | -63.811   | 536.815   | -116.629  | -576.337  |
| 1.756                                       | 0.819                          | 0.319            | -57.032   | 449.301   | -93.634   | -471.086  |
| 1.764                                       | 0.675                          | 0.187            | -50.423   | 407.923   | -86.621   | -426.369  |
| 1.756                                       | 0.819                          | 0.323            | -65.467   | 504.406   | -99.65    | -533.44   |
| 1.686                                       | 0.717                          | 0.269            | -69.871   | 513.026   | -100.452  | -530.776  |
| 1.791                                       | 0.808                          | 0.342            | -64.535   | 507.501   | -103.141  | -536.59   |
| 1.838                                       | 0.693                          | 0.316            | -84.142   | 564.338   | -98.565   | -578.214  |
| 1.685                                       | 0.983                          | 0.376            | -51.882   | 429.756   | -91.401   | -460.531  |
| 1.82                                        | 0.823                          | 0.234            | -66.637   | 540.627   | -118.02   | -561.999  |
| 1.627                                       | 1.218                          | 0.35             | -69.385   | 517.97    | -97.351   | -557.335  |
| 1.733                                       | 0.671                          | 0.305            | -59.326   | 446.414   | -87.196   | -466.801  |
| 1.775                                       | 0.681                          | 0.289            | -66.311   | 518.242   | -107.53   | -539.381  |
| 1.74                                        | 1.065                          | 0.375            | -61.097   | 487.972   | -100.626  | -521.032  |
| 1.992                                       | 0.58                           | 0.349            | -76.365   | 588.149   | -118.97   | -609.193  |
| 1.562                                       | 0.866                          | 0.249            | -88.244   | 666.439   | -132.395  | -700.727  |
| 1.698                                       | 1.126                          | 0.293            | -57.124   | 477.813   | -103.274  | -512.326  |
| 1.738                                       | 0.863                          | 0.251            | -71.487   | 545.662   | -108.186  | -574.236  |
| 1.78                                        | 0.994                          | 0.411            | -79.336   | 581.072   | -109.993  | -612.372  |
| 1.46                                        | 0.624                          | 0.284            | -41.508   | 411.59    | -101.858  | -442.52   |
| 1.593                                       | 0.545                          | 0.279            | -57.266   | 451.474   | -95.391   | -469.775  |
| 1.642                                       | 0.83                           | 0.305            | -61.25    | 489.637   | -102.879  | -517.456  |
| 1.812                                       | 0.923                          | 0.233            | -56.593   | 452.21    | -97.536   | -470.512  |
| 1.621                                       | 0.803                          | 0.3              | -63.948   | 520.67    | -112.219  | -548.016  |
| 1.671                                       | 0.581                          | 0.348            | -84.085   | 594.762   | -108.956  | -618.809  |
| 1.656                                       | 0.964                          | 0.304            | -66.324   | 545.967   | -119.103  | -577.195  |
| 1.857                                       | 0.866                          | 0.311            | -63.801   | 502.525   | -102.664  | -529.877  |
| 1.703                                       | 0.81                           | 0.372            | -76.231   | 570.446   | -108.966  | -603.635  |
| 1.541                                       | 0.596                          | 0.211            | -52.136   | 432.482   | -95.194   | -452.756  |
| 1.819                                       | 0.987                          | 0.321            | -59.106   | 461.012   | -94.592   | -485.912  |
| 1.576                                       | 0.729                          | 0.275            | -67.523   | 514.522   | -102.715  | -540.431  |
| 1.608                                       | 1.162                          | 0.293            | -96.262   | 669.029   | -114.29   | -715.182  |
| 1.755                                       | 0.762                          | 0.272            | -62.829   | 513.054   | -110.835  | -537.068  |
| 1.619                                       | 1.054                          | 0.279            | -84.131   | 596.179   | -107.356  | -631.284  |
| 1.608                                       | 0.761                          | 0.24             | -61.583   | 489.4     | -105.702  | -508.102  |
| 1.848                                       | 0.908                          | 0.32             | -68.578   | 520.831   | -103.477  | -545.893  |
| 1.606                                       | 0.908                          | 0.314            | -79.352   | 561.128   | -99.374   | -595.091  |
| 1.603                                       | 0.817                          | 0.202            | -77.217   | 584.156   | -114.58   | -615.705  |
| 1.736                                       | 0.719                          | 0.275            | -86.725   | 656.339   | -131.603  | -683.849  |
| 1.564                                       | 1.051                          | 0.26             | -52.34    | 447.966   | -100.392  | -478.305  |
| 1.66                                        | 0.869                          | 0.311            | -52.648   | 430.531   | -91.778   | -457.396  |
| 1.761                                       | 0.745                          | 0.239            | -74       | 542.089   | -103.216  | -565.202  |
| 1.69                                        | 0.706                          | 0.304            | -97.167   | 726.761   | -141.322  | -759.359  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.65                                        | 1.192                          | 0.317            | -77.24    | 531.461   | -89.362   | -567.706  |
| 1.854                                       | 0.691                          | 0.277            | -57.202   | 441.581   | -89.868   | -460.262  |
| 1.568                                       | 0.947                          | 0.258            | -67.329   | 510.134   | -100.653  | -540.631  |
| 1.735                                       | 0.962                          | 0.347            | -88.183   | 635.518   | -118.482  | -666.689  |
| 1.822                                       | 0.925                          | 0.321            | -63.093   | 476.811   | -93.279   | -502.241  |
| 1.671                                       | 0.922                          | 0.29             | -60.002   | 474.105   | -97.909   | -501.574  |
| 1.79                                        | 0.936                          | 0.359            | -81.391   | 596.261   | -112.527  | -627.662  |
| 1.573                                       | 0.775                          | 0.319            | -50.132   | 421.624   | -91.535   | -450.245  |
| 1.618                                       | 0.828                          | 0.317            | -79.194   | 573.291   | -108.377  | -600.115  |
| 1.683                                       | 0.922                          | 0.249            | -60.434   | 451.949   | -88.029   | -475.587  |
| 1.821                                       | 0.751                          | 0.289            | -85.204   | 641.378   | -127.85   | -666.56   |
| 1.795                                       | 0.93                           | 0.242            | -66.77    | 521.824   | -110.821  | -541.118  |
| 1.843                                       | 0.575                          | 0.214            | -70.278   | 526.99    | -105.744  | -541.444  |
| 1.734                                       | 0.974                          | 0.32             | -73.065   | 536.302   | -101.769  | -565.736  |
| 1.84                                        | 0.847                          | 0.352            | -78.569   | 577.408   | -109.034  | -607.389  |
| 1.503                                       | 1.008                          | 0.231            | -73.687   | 576.146   | -117.685  | -613.205  |
| 1.709                                       | 0.7                            | 0.263            | -72.908   | 576.748   | -122.058  | -600.504  |
| 1.739                                       | 0.775                          | 0.292            | -78.292   | 594.128   | -118.569  | -622.272  |
| 1.754                                       | 0.86                           | 0.358            | -59.528   | 482.073   | -101.167  | -510.381  |
| 1.579                                       | 0.834                          | 0.344            | -56.852   | 487.392   | -108.882  | -519.089  |
| 1.721                                       | 0.492                          | 0.26             | -68.523   | 483.74    | -89.533   | -498.068  |
| 1.835                                       | 0.633                          | 0.244            | -56.208   | 460.825   | -102.909  | -474.177  |
| 1.765                                       | 0.838                          | 0.282            | -74.61    | 543.02    | -101.647  | -569.428  |
| 1.827                                       | 0.679                          | 0.296            | -72.536   | 533.79    | -103.647  | -552.829  |
| 1.656                                       | 0.698                          | 0.276            | -68.937   | 521.555   | -102.645  | -548.741  |
| 1.772                                       | 0.745                          | 0.265            | -65.116   | 529.565   | -113.696  | -554.579  |
| 1.564                                       | 0.918                          | 0.227            | -86.045   | 613.633   | -112.43   | -646.436  |
| 1.699                                       | 0.68                           | 0.253            | -87.35    | 614.449   | -111.706  | -638.318  |
| 1.757                                       | 0.748                          | 0.288            | -63.539   | 490.265   | -98.926   | -514.081  |
| 1.773                                       | 0.901                          | 0.337            | -60.536   | 485.278   | -102.64   | -510.686  |
| 1.495                                       | 1.084                          | 0.298            | -52.022   | 456.349   | -102.049  | -494.97   |
| 1.732                                       | 0.978                          | 0.342            | -53.024   | 442.944   | -95.416   | -472.858  |
| 1.578                                       | 0.72                           | 0.312            | -49.816   | 477.127   | -114.824  | -512.271  |
| 1.797                                       | 0.68                           | 0.286            | -63.863   | 510.653   | -108.204  | -532.343  |
| 1.84                                        | 0.944                          | 0.41             | -75.102   | 569.869   | -113.755  | -597.956  |
| 1.967                                       | 0.849                          | 0.291            | -63.742   | 477.954   | -94.145   | -496.539  |
| 1.737                                       | 1.153                          | 0.281            | -79.416   | 589.185   | -111.031  | -627.706  |
| 1.702                                       | 0.716                          | 0.295            | -100.354  | 665.489   | -112.593  | -688.473  |
| 1.843                                       | 0.817                          | 0.308            | -70.486   | 531.909   | -106.097  | -554.351  |
| 1.753                                       | 1.035                          | 0.365            | -106.573  | 654.416   | -94.193   | -683.14   |
| 1.65                                        | 0.827                          | 0.257            | -60.477   | 510.186   | -113.892  | -535.623  |
| 1.754                                       | 0.927                          | 0.342            | -90.017   | 710.39    | -147.473  | -748.75   |
| 1.722                                       | 1.021                          | 0.26             | -69.081   | 516.712   | -99.797   | -545.278  |
| 1.865                                       | 1.105                          | 0.407            | -86.768   | 643.166   | -121.952  | -681.906  |
| 1.867                                       | 0.881                          | 0.333            | -60.312   | 489.741   | -103.119  | -517.949  |
| 1.717                                       | 0.881                          | 0.331            | -72.028   | 567.777   | -115.883  | -602.161  |
| 1.45                                        | 0.836                          | 0.259            | -68.904   | 540.017   | -112.287  | -569.21   |
| 1.797                                       | 0.559                          | 0.303            | -91.303   | 675.024   | -133.048  | -694.391  |
| 1.753                                       | 0.661                          | 0.292            | -68.319   | 531.686   | -109.365  | -555.154  |
| 1.589                                       | 0.896                          | 0.393            | -90.336   | 665.037   | -123.666  | -708.636  |
| 1.739                                       | 0.637                          | 0.326            | -64.471   | 523.649   | -113.886  | -544.041  |
| 1.796                                       | 0.64                           | 0.251            | -74.379   | 600.936   | -131.59   | -620.239  |
| 1.691                                       | 0.968                          | 0.308            | -101.28   | 697.023   | -119.187  | -735.912  |
| 1.814                                       | 0.765                          | 0.322            | -76.021   | 607.67    | -128.811  | -635.225  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.666                                       | 0.986                          | 0.286            | -80.48    | 624.361   | -127.093  | -660.344  |
| 1.609                                       | 0.984                          | 0.339            | -68.041   | 515.971   | -100.609  | -548.61   |
| 1.721                                       | 0.663                          | 0.232            | -64.251   | 492.42    | -100.548  | -511.151  |
| 1.552                                       | 0.935                          | 0.26             | -63.285   | 509.218   | -107.136  | -540.897  |
| 1.693                                       | 0.686                          | 0.307            | -61.439   | 514.166   | -113.539  | -540.056  |
| 1.724                                       | 0.907                          | 0.361            | -77.149   | 509.831   | -81.481   | -537.564  |
| 1.657                                       | 0.995                          | 0.208            | -67.95    | 513.732   | -101.761  | -540.725  |
| 1.662                                       | 0.762                          | 0.308            | -66.623   | 524.118   | -107.497  | -552.969  |
| 1.661                                       | 0.538                          | 0.305            | -85.036   | 639.512   | -126.942  | -663.835  |
| 1.772                                       | 0.742                          | 0.342            | -61.756   | 486.049   | -101.177  | -508.194  |
| 1.57                                        | 1.097                          | 0.25             | -59.642   | 472.605   | -98.143   | -502.559  |
| 1.787                                       | 0.719                          | 0.29             | -68.798   | 528.897   | -108.431  | -549.497  |
| 1.623                                       | 0.736                          | 0.309            | -49.173   | 430.46    | -97.654   | -457.089  |
| 1.745                                       | 0.677                          | 0.204            | -72.9     | 578.268   | -124.848  | -596.664  |
| 1.744                                       | 0.87                           | 0.438            | -55.011   | 478.561   | -106.683  | -513.032  |
| 1.71                                        | 0.818                          | 0.26             | -73.781   | 595.324   | -127.396  | -623.404  |
| 1.636                                       | 0.767                          | 0.29             | -92.154   | 625.808   | -107.199  | -653.378  |
| 1.749                                       | 0.851                          | 0.352            | -59.106   | 482.099   | -103.308  | -508.849  |
| 1.791                                       | 0.908                          | 0.355            | -64.369   | 543.681   | -119.303  | -576.884  |
| 1.577                                       | 0.893                          | 0.246            | -39.768   | 385.228   | -94.239   | -413.96   |
| 1.58                                        | 0.584                          | 0.219            | -53.007   | 422.345   | -91.44    | -437.777  |
| 1.585                                       | 0.882                          | 0.231            | -65.46    | 495.141   | -96.492   | -524.782  |
| 1.727                                       | 0.879                          | 0.301            | -70.562   | 551.379   | -114.379  | -578.313  |
| 1.714                                       | 0.907                          | 0.288            | -66.304   | 532.267   | -114.456  | -557.811  |
| 1.666                                       | 0.993                          | 0.338            | -64.055   | 527.095   | -111.843  | -564.593  |
| 1.75                                        | 0.623                          | 0.266            | -64.153   | 511.34    | -110.38   | -528.593  |
| 1.645                                       | 1.151                          | 0.279            | -74.156   | 567.998   | -111.259  | -607.753  |
| 1.804                                       | 0.883                          | 0.308            | -73.702   | 567.675   | -112.632  | -600.497  |
| 1.701                                       | 0.613                          | 0.322            | -82.393   | 591.4     | -111.385  | -612.888  |
| 1.65                                        | 0.722                          | 0.282            | -61.721   | 500.264   | -105.424  | -527.29   |
| 1.655                                       | 0.682                          | 0.289            | -49.426   | 424.843   | -96.333   | -446.727  |
| 1.794                                       | 0.81                           | 0.352            | -69.847   | 526.397   | -101.621  | -555.372  |
| 1.715                                       | 0.618                          | 0.244            | -57.281   | 484.082   | -108.034  | -506.354  |
| 1.698                                       | 0.849                          | 0.287            | -91.982   | 630.207   | -111.258  | -655.034  |
| 1.595                                       | 0.661                          | 0.237            | -66.689   | 517.932   | -106.395  | -541.988  |
| 1.806                                       | 0.686                          | 0.193            | -75.312   | 591.271   | -128.013  | -604.231  |
| 1.697                                       | 0.683                          | 0.306            | -75.235   | 572.265   | -115.859  | -595.35   |
| 1.623                                       | 0.682                          | 0.343            | -79.032   | 587.37    | -113.275  | -616.963  |
| 1.698                                       | 0.81                           | 0.28             | -58.178   | 469.455   | -98.011   | -497.435  |
| 1.602                                       | 1.202                          | 0.199            | -103.152  | 690.892   | -117.482  | -724.973  |
| 1.691                                       | 0.832                          | 0.236            | -68.916   | 522.891   | -104.637  | -547.268  |
| 1.784                                       | 0.754                          | 0.345            | -55.583   | 463.407   | -102.015  | -486.641  |
| 1.585                                       | 0.893                          | 0.289            | -61.976   | 498.949   | -105.784  | -527.247  |
| 1.733                                       | 0.774                          | 0.281            | -53.462   | 454.265   | -101.114  | -479.498  |
| 1.702                                       | 1.041                          | 0.352            | -70.569   | 559.179   | -116.037  | -592.954  |
| 1.603                                       | 0.658                          | 0.255            | -68.888   | 508.926   | -98.566   | -530.528  |
| 1.69                                        | 0.706                          | 0.235            | -59.353   | 483.869   | -104.718  | -506.175  |
| 1.784                                       | 0.762                          | 0.28             | -63.181   | 499.655   | -104.069  | -523.069  |
| 1.591                                       | 0.98                           | 0.315            | -54.899   | 470.667   | -104.458  | -503.08   |
| 1.692                                       | 0.909                          | 0.208            | -52.793   | 420.447   | -87.121   | -444.626  |
| 1.747                                       | 0.989                          | 0.313            | -53.465   | 421.3     | -86.051   | -447.52   |
| 1.812                                       | 0.699                          | 0.253            | -63.484   | 469.888   | -91.722   | -487.305  |
| 1.634                                       | 1.02                           | 0.22             | -57.946   | 473.757   | -102.682  | -500.003  |
| 1.786                                       | 0.769                          | 0.317            | -61.882   | 487.721   | -101.694  | -510.709  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.95                                        | 0.726                          | 0.274            | -67.309   | 509.054   | -103.128  | -523.621  |
| 1.679                                       | 0.697                          | 0.364            | -68.255   | 505.655   | -97.793   | -529.897  |
| 1.823                                       | 0.679                          | 0.239            | -72.281   | 525.49    | -102.383  | -540.263  |
| 1.797                                       | 0.601                          | 0.256            | -72.423   | 528.316   | -101.001  | -547.332  |
| 1.794                                       | 0.777                          | 0.278            | -55.975   | 444.125   | -93.23    | -464.317  |
| 1.704                                       | 0.874                          | 0.213            | -75.077   | 562.18    | -109.983  | -589.36   |
| 1.885                                       | 0.858                          | 0.327            | -70.291   | 537.745   | -107.833  | -561.682  |
| 1.537                                       | 0.987                          | 0.211            | -61.458   | 502.67    | -106.009  | -538.747  |
| 1.924                                       | 0.616                          | 0.304            | -60.571   | 465.889   | -93.363   | -484.706  |
| 1.738                                       | 0.77                           | 0.367            | -44.609   | 414.775   | -98.283   | -442.837  |
| 1.755                                       | 0.668                          | 0.276            | -74.233   | 544.939   | -105.838  | -564.022  |
| 1.719                                       | 0.761                          | 0.289            | -55.91    | 450.07    | -94.851   | -473.084  |
| 1.751                                       | 0.788                          | 0.298            | -68.956   | 523.83    | -104.93   | -546.681  |
| 1.751                                       | 0.678                          | 0.292            | -68.535   | 544.385   | -114.579  | -568.795  |
| 1.867                                       | 0.535                          | 0.355            | -60.024   | 474.14    | -99.477   | -491.107  |
| 1.714                                       | 0.834                          | 0.35             | -62.933   | 522.494   | -114.099  | -551.231  |
| 1.802                                       | 0.965                          | 0.332            | -59.326   | 474.238   | -98.726   | -502.03   |
| 1.538                                       | 0.745                          | 0.317            | -57.852   | 493.326   | -108.882  | -527.018  |
| 1.741                                       | 0.715                          | 0.254            | -76.169   | 573.066   | -113.644  | -596.479  |
| 1.58                                        | 0.862                          | 0.245            | -67.272   | 505.449   | -97.351   | -536.572  |
| 1.825                                       | 0.8                            | 0.27             | -61.492   | 496.334   | -106.127  | -518.566  |
| 1.699                                       | 0.751                          | 0.274            | -57.917   | 462.008   | -98.735   | -480.754  |
| 1.764                                       | 0.887                          | 0.389            | -78.077   | 595.379   | -117.934  | -628.622  |
| 1.755                                       | 0.756                          | 0.266            | -75.109   | 558.652   | -110.194  | -579.91   |
| 1.601                                       | 0.709                          | 0.283            | -50.417   | 411.965   | -89.061   | -433.41   |
| 1.639                                       | 0.872                          | 0.325            | -59.782   | 480.795   | -101.877  | -508.804  |
| 1.926                                       | 0.889                          | 0.326            | -74.375   | 557.083   | -109.52   | -580.631  |
| 1.831                                       | 0.877                          | 0.326            | -73.724   | 545.336   | -105.597  | -570.024  |
| 1.674                                       | 1.001                          | 0.294            | -66.467   | 520.256   | -106.049  | -552.861  |
| 1.778                                       | 0.667                          | 0.292            | -72.819   | 550.775   | -110.201  | -571.699  |
| 1.75                                        | 0.884                          | 0.302            | -61.721   | 492.551   | -104.741  | -515.928  |
| 1.918                                       | 0.88                           | 0.3              | -64.095   | 481.591   | -94.604   | -503.165  |
| 1.522                                       | 0.636                          | 0.219            | -54.653   | 469.291   | -106.851  | -492.377  |
| 1.469                                       | 0.867                          | 0.189            | -54.683   | 450.87    | -98.325   | -477.852  |
| 1.689                                       | 0.872                          | 0.274            | -86.173   | 575.435   | -98.211   | -596.907  |
| 1.748                                       | 0.696                          | 0.132            | -70.093   | 508.407   | -98.275   | -524.645  |
| 1.709                                       | 0.98                           | 0.315            | -57.483   | 453.63    | -93.021   | -481.91   |
| 1.657                                       | 0.653                          | 0.232            | -76.204   | 557.243   | -106.196  | -582.009  |
| 1.711                                       | 0.928                          | 0.202            | -61.412   | 462.326   | -92.198   | -483.819  |
| 1.799                                       | 0.656                          | 0.37             | -56.59    | 454.09    | -94.411   | -477.771  |
| 1.737                                       | 0.859                          | 0.331            | -76.937   | 600.491   | -125.311  | -628.026  |
| 1.852                                       | 0.638                          | 0.25             | -55.791   | 430.767   | -89.528   | -444.314  |
| 1.817                                       | 0.992                          | 0.188            | -61.157   | 489.485   | -105.093  | -510.722  |
| 1.687                                       | 0.69                           | 0.272            | -53.555   | 450.389   | -98.981   | -473.909  |
| 1.643                                       | 0.982                          | 0.25             | -65.27    | 542.886   | -118.264  | -576.671  |
| 1.791                                       | 0.81                           | 0.289            | -64.878   | 537.2     | -120.198  | -558.03   |
| 1.747                                       | 0.94                           | 0.365            | -74.203   | 591.166   | -123.959  | -623.902  |
| 1.662                                       | 0.857                          | 0.29             | -104.803  | 663.897   | -102.215  | -690.18   |
| 1.58                                        | 0.872                          | 0.288            | -48.903   | 461.158   | -112.235  | -490.956  |
| 1.62                                        | 0.921                          | 0.272            | -77.46    | 586.619   | -114.986  | -621.213  |
| 1.581                                       | 0.94                           | 0.282            | -32.978   | 364.579   | -96.88    | -394.616  |
| 1.725                                       | 0.766                          | 0.304            | -68.396   | 525.274   | -107.035  | -548.33   |
| 1.68                                        | 0.73                           | 0.293            | -56.6     | 469.482   | -102.582  | -493.887  |
| 1.714                                       | 0.733                          | 0.221            | -36.987   | 363.484   | -91.679   | -383.54   |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.716                                       | 0.552                          | 0.268            | -61.321   | 493.292   | -107.23   | -510.175  |
| 1.672                                       | 0.882                          | 0.377            | -63.365   | 530.325   | -115.962  | -562.79   |
| 1.906                                       | 0.727                          | 0.287            | -51.87    | 431.689   | -94.902   | -449.841  |
| 1.601                                       | 0.791                          | 0.3              | -49.311   | 402.308   | -86.845   | -424.55   |
| 1.635                                       | 0.786                          | 0.291            | -50.657   | 422.621   | -93.657   | -444.337  |
| 1.678                                       | 0.597                          | 0.311            | -66.219   | 526.229   | -110.411  | -550.356  |
| 1.708                                       | 0.803                          | 0.347            | -39.329   | 447.729   | -120.126  | -483.515  |
| 1.759                                       | 0.577                          | 0.261            | -68.877   | 511.398   | -103.471  | -523.704  |
| 1.682                                       | 0.8                            | 0.29             | -55.862   | 432.846   | -88.343   | -454.464  |
| 1.689                                       | 0.945                          | 0.302            | -58.347   | 481.208   | -105.308  | -507.114  |
| 1.466                                       | 0.877                          | 0.295            | -24.268   | 321.077   | -94.083   | -350.758  |
| 1.725                                       | 0.725                          | 0.365            | -63.951   | 492.949   | -99.437   | -517.702  |
| 1.723                                       | 0.518                          | 0.207            | -56.362   | 465.36    | -104.142  | -479.318  |
| 1.618                                       | 0.749                          | 0.261            | -77.053   | 596.588   | -121.897  | -625.73   |
| 1.57                                        | 0.787                          | 0.272            | -62.108   | 513.173   | -112.745  | -539.286  |
| 1.772                                       | 0.456                          | 0.21             | -107.598  | 699.072   | -117.653  | -708.871  |
| 1.644                                       | 0.871                          | 0.229            | -59.808   | 498.612   | -107.727  | -530.606  |
| 1.792                                       | 0.647                          | 0.282            | -75.087   | 580.447   | -117.736  | -605.135  |
| 1.777                                       | 0.737                          | 0.215            | -61.699   | 487.735   | -102.778  | -507.001  |
| 1.687                                       | 0.744                          | 0.25             | -56.355   | 466.746   | -102.596  | -489.325  |
| 1.854                                       | 0.728                          | 0.284            | -78.073   | 536.47    | -90.947   | -563.127  |
| 1.824                                       | 0.873                          | 0.299            | -80.395   | 608.908   | -119.266  | -640.913  |
| 1.777                                       | 0.953                          | 0.369            | -73.913   | 541.066   | -102.459  | -569.01   |
| 1.743                                       | 0.858                          | 0.337            | -61.061   | 493.343   | -105.699  | -517.998  |
| 1.688                                       | 0.954                          | 0.258            | -91.188   | 623.482   | -108.994  | -650.428  |
| 1.474                                       | 0.815                          | 0.193            | -72.454   | 560.656   | -114.663  | -589.679  |
| 1.892                                       | 0.785                          | 0.312            | -79.337   | 581.245   | -109.483  | -608.973  |
| 1.712                                       | 0.967                          | 0.345            | -69.426   | 559.19    | -119.431  | -589.915  |
| 1.609                                       | 1.026                          | 0.312            | -84.834   | 638.474   | -123.831  | -679.039  |
| 1.68                                        | 0.73                           | 0.266            | -60.973   | 484.934   | -102.799  | -507.291  |
| 1.742                                       | 0.878                          | 0.273            | -67.963   | 514.709   | -101.463  | -540.753  |
| 1.607                                       | 0.747                          | 0.144            | -51.867   | 438.539   | -97.002   | -461.791  |
| 1.701                                       | 0.962                          | 0.255            | -89.149   | 620.12    | -109.285  | -650.993  |
| 1.709                                       | 0.79                           | 0.324            | -81.767   | 599.358   | -115.554  | -625.326  |
| 1.752                                       | 0.794                          | 0.364            | -55.957   | 432.424   | -87.077   | -455.898  |
| 1.48                                        | 1.173                          | 0.368            | -49.801   | 455.827   | -101.962  | -505.049  |
| 1.493                                       | 0.801                          | 0.253            | -68.52    | 517.976   | -99.78    | -551.774  |
| 1.816                                       | 0.895                          | 0.236            | -52.253   | 450.066   | -102.347  | -472.815  |
| 1.847                                       | 0.805                          | 0.355            | -68.769   | 542.913   | -112.541  | -570.328  |
| 1.771                                       | 0.934                          | 0.209            | -108.624  | 679.722   | -104.183  | -701.947  |
| 1.713                                       | 0.694                          | 0.222            | -61.241   | 495.498   | -106.643  | -515.731  |
| 1.593                                       | 0.908                          | 0.21             | -53.88    | 504.01    | -119.872  | -540.435  |
| 1.745                                       | 1.188                          | 0.304            | -66.886   | 515.526   | -104.73   | -544.95   |
| 1.785                                       | 0.981                          | 0.399            | -90.325   | 658       | -124.135  | -692.812  |
| 1.829                                       | 0.835                          | 0.379            | -60.133   | 476.676   | -96.264   | -506.542  |
| 1.836                                       | 0.608                          | 0.174            | -72.997   | 486.913   | -84.961   | -496.024  |
| 1.726                                       | 0.902                          | 0.259            | -66.256   | 510.142   | -104.28   | -533.815  |
| 1.782                                       | 0.888                          | 0.389            | -79.081   | 592.413   | -115.289  | -623.022  |
| 1.696                                       | 0.84                           | 0.318            | -53.685   | 420.057   | -85.842   | -443.861  |
| 1.653                                       | 0.85                           | 0.274            | -46.816   | 445.024   | -109.129  | -472.113  |
| 1.663                                       | 0.69                           | 0.264            | -51.479   | 429.182   | -94.972   | -449.766  |
| 1.8                                         | 0.726                          | 0.296            | -49.391   | 426.614   | -95.015   | -452.21   |
| 1.694                                       | 0.897                          | 0.302            | -56.228   | 468.088   | -103.332  | -494.067  |
| 1.663                                       | 1.022                          | 0.356            | -42.404   | 387.372   | -90.873   | -415.95   |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.59                                        | 0.634                          | 0.282            | -28.879   | 360.709   | -103.041  | -387.975  |
| 1.615                                       | 0.528                          | 0.256            | -69.713   | 544.875   | -113.114  | -567.271  |
| 1.744                                       | 0.587                          | 0.26             | -55.492   | 423.616   | -85.292   | -440.464  |
| 1.873                                       | 0.539                          | 0.27             | -85.69    | 552.216   | -89.887   | -564.706  |
| 1.797                                       | 0.654                          | 0.388            | -83.96    | 574.778   | -99.477   | -598.534  |
| 1.797                                       | 0.849                          | 0.28             | -73.121   | 559.412   | -113.524  | -582.413  |
| 1.712                                       | 0.923                          | 0.206            | -99.109   | 623.339   | -95.229   | -646.106  |
| 1.666                                       | 1.039                          | 0.256            | -79.507   | 592.19    | -112.725  | -629.492  |
| 1.831                                       | 1.046                          | 0.29             | -63.433   | 500.193   | -104.635  | -523.886  |
| 1.574                                       | 1.056                          | 0.177            | -71.969   | 545.209   | -108.446  | -575.498  |
| 1.767                                       | 0.908                          | 0.189            | -82.072   | 574.774   | -104.405  | -596.809  |
| 2.016                                       | 0.585                          | 0.399            | -88.443   | 598.227   | -105.575  | -610.423  |
| 1.947                                       | 0.846                          | 0.272            | -62.214   | 478.93    | -98.87    | -494.984  |
| 1.791                                       | 0.672                          | 0.285            | -68.288   | 531.356   | -110.981  | -550.525  |
| 2.05                                        | 0.666                          | 0.306            | -55.236   | 431.928   | -89.812   | -446.562  |
| 1.638                                       | 0.957                          | 0.288            | -62.423   | 488.534   | -101.145  | -515.4    |
| 1.777                                       | 0.707                          | 0.307            | -41.262   | 391.036   | -94.737   | -414.146  |
| 1.575                                       | 0.579                          | 0.313            | -69.287   | 506.355   | -95.016   | -531.136  |
| 1.87                                        | 0.748                          | 0.376            | -54.797   | 439.393   | -92.713   | -459.972  |
| 1.683                                       | 0.558                          | 0.236            | -62.747   | 495.902   | -105.451  | -513.816  |
| 1.365                                       | 0.843                          | 0.24             | -62.201   | 547.684   | -124.446  | -589.414  |
| 1.788                                       | 0.563                          | 0.293            | -77.717   | 576.998   | -113.84   | -596.28   |
| 1.717                                       | 0.858                          | 0.29             | -52.376   | 439.127   | -96.535   | -464.214  |
| 1.663                                       | 0.7                            | 0.305            | -62.978   | 497.614   | -105.125  | -518.634  |
| 1.877                                       | 0.847                          | 0.334            | -149.775  | 826.249   | -94.712   | -846.709  |
| 1.681                                       | 0.832                          | 0.131            | -65.249   | 540.81    | -121.976  | -561.185  |
| 1.749                                       | 0.65                           | 0.317            | -51.259   | 423.131   | -91.993   | -443.373  |
| 1.812                                       | 1.263                          | 0.263            | -87.203   | 622.035   | -113.464  | -656.116  |
| 1.766                                       | 0.916                          | 0.262            | -57.179   | 483.032   | -108.046  | -508.504  |
| 1.772                                       | 0.75                           | 0.347            | -68.412   | 513.712   | -101.47   | -536.378  |
| 1.552                                       | 0.768                          | 0.289            | -51.51    | 464.014   | -109.572  | -491.12   |
| 1.611                                       | 0.958                          | 0.261            | -55.44    | 454.558   | -99.354   | -479.502  |
| 1.783                                       | 0.608                          | 0.271            | -52.884   | 458.564   | -105.445  | -477.482  |
| 1.515                                       | 0.671                          | 0.201            | -57.913   | 444.365   | -87.133   | -471.621  |
| 1.782                                       | 0.93                           | 0.325            | -54.976   | 462.505   | -101.757  | -489.698  |
| 1.703                                       | 0.972                          | 0.335            | -69.035   | 526.426   | -104.464  | -556.882  |
| 1.844                                       | 0.735                          | 0.22             | -72.133   | 556.912   | -112.957  | -579.334  |
| 1.655                                       | 0.834                          | 0.302            | -77.436   | 549.225   | -97.109   | -582.23   |
| 1.603                                       | 0.67                           | 0.226            | -69.9     | 522.463   | -100.474  | -549.557  |
| 1.396                                       | 0.992                          | 0.227            | -62.08    | 473.508   | -93.748   | -505.069  |
| 1.734                                       | 0.799                          | 0.289            | -42.788   | 402.695   | -98.152   | -425.63   |
| 1.817                                       | 0.519                          | 0.211            | -62.124   | 471.515   | -95.768   | -485.379  |
| 1.504                                       | 1.424                          | 0.324            | -69.716   | 519.844   | -96.318   | -566.155  |
| 1.738                                       | 0.582                          | 0.281            | -72.268   | 502.333   | -92.18    | -517.207  |
| 1.729                                       | 0.542                          | 0.288            | -55.377   | 449.344   | -95.294   | -470.471  |
| 1.47                                        | 0.608                          | 0.3              | -54.021   | 443.037   | -96.738   | -466.564  |
| 1.766                                       | 0.698                          | 0.273            | -66.92    | 500.056   | -98.294   | -520.64   |
| 1.587                                       | 0.66                           | 0.294            | -85.512   | 660.771   | -135.456  | -690.056  |
| 1.643                                       | 0.807                          | 0.363            | -69.078   | 548.572   | -115.46   | -578.465  |
| 1.945                                       | 0.661                          | 0.325            | -63.645   | 492.61    | -101.734  | -509.157  |
| 2.024                                       | 0.809                          | 0.335            | -115.571  | 719.76    | -107.118  | -742.019  |
| 1.61                                        | 0.924                          | 0.319            | -59.42    | 465.435   | -94.542   | -494.109  |
| 1.672                                       | 0.627                          | 0.3              | -67.387   | 518.098   | -105.009  | -540.833  |
| 1.842                                       | 0.852                          | 0.215            | -83.074   | 610.414   | -119.328  | -631.414  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.68                                        | 0.906                          | 0.357            | -69.311   | 548.71    | -114.007  | -579.716  |
| 1.811                                       | 0.747                          | 0.304            | -66.375   | 503.917   | -101.077  | -524.472  |
| 1.675                                       | 0.619                          | 0.224            | -71.454   | 552.714   | -114.709  | -572.315  |
| 1.852                                       | 0.894                          | 0.403            | -109.635  | 671.837   | -95.512   | -698.671  |
| 1.708                                       | 0.643                          | 0.234            | -78.307   | 572.408   | -113.663  | -587.866  |
| 1.856                                       | 0.635                          | 0.324            | -66.299   | 479.154   | -91.014   | -495.026  |
| 1.77                                        | 1.024                          | 0.305            | -69.675   | 521.678   | -103.474  | -546.409  |
| 1.951                                       | 0.729                          | 0.349            | -71.454   | 526.278   | -101.114  | -546.782  |
| 1.615                                       | 0.808                          | 0.246            | -72.549   | 573.387   | -120.036  | -602.928  |
| 1.867                                       | 0.879                          | 0.352            | -76.543   | 592.737   | -119.157  | -623.851  |
| 1.75                                        | 0.616                          | 0.283            | -45.974   | 407.187   | -93.916   | -427.324  |
| 1.834                                       | 0.649                          | 0.315            | -92.865   | 631.829   | -115.799  | -642.87   |
| 1.729                                       | 0.798                          | 0.258            | -64.376   | 491.954   | -98.65    | -516.315  |
| 1.649                                       | 0.837                          | 0.249            | -39.819   | 400.286   | -100.649  | -428.293  |
| 1.909                                       | 1.084                          | 0.243            | -67.973   | 526.592   | -107.034  | -555.112  |
| 1.77                                        | 0.929                          | 0.404            | -79.706   | 627.925   | -128.855  | -664.09   |
| 1.745                                       | 0.674                          | 0.291            | -49.668   | 425.33    | -95.779   | -447.472  |
| 1.737                                       | 0.722                          | 0.355            | -73.896   | 494.677   | -82.593   | -516.651  |
| 1.552                                       | 1.236                          | 0.301            | -83.604   | 607.162   | -109.928  | -653.809  |
| 1.803                                       | 0.557                          | 0.332            | -81.057   | 601.453   | -115.874  | -626.659  |
| 1.843                                       | 0.979                          | 0.318            | -72.934   | 572.311   | -116.082  | -606.344  |
| 1.691                                       | 0.743                          | 0.283            | -48.658   | 422.512   | -98.347   | -441.727  |
| 1.669                                       | 0.752                          | 0.304            | -58.875   | 494.459   | -108.172  | -522.743  |
| 1.745                                       | 0.662                          | 0.266            | -42.841   | 433.15    | -109.917  | -459.376  |
| 1.675                                       | 0.854                          | 0.155            | -92.823   | 704.097   | -142.365  | -731.993  |
| 1.753                                       | 0.783                          | 0.312            | -63.736   | 530.12    | -116.685  | -556.91   |
| 1.679                                       | 0.808                          | 0.353            | -84.569   | 594.307   | -106.474  | -623.321  |
| 1.66                                        | 0.987                          | 0.323            | -77.151   | 610.675   | -127.684  | -645.087  |
| 1.661                                       | 0.714                          | 0.269            | -75.538   | 562.497   | -109.474  | -588.518  |
| 1.968                                       | 0.641                          | 0.33             | -74.942   | 534.839   | -101.146  | -549.772  |
| 1.691                                       | 0.484                          | 0.295            | -50.727   | 431.329   | -97.187   | -450.321  |
| 1.682                                       | 0.95                           | 0.275            | -69.735   | 557.169   | -116.763  | -588.354  |
| 1.716                                       | 0.969                          | 0.31             | -71.801   | 557.578   | -112.772  | -589.472  |
| 1.724                                       | 0.748                          | 0.199            | -69.38    | 550.39    | -116.166  | -572.88   |
| 1.506                                       | 1.174                          | 0.245            | -68.45    | 538.261   | -109.845  | -576.823  |
| 1.664                                       | 0.743                          | 0.285            | -91.378   | 645.022   | -118.891  | -669.862  |
| 1.629                                       | 0.618                          | 0.346            | -79.568   | 587.531   | -112.609  | -615.167  |
| 1.683                                       | 0.878                          | 0.304            | -59.897   | 489.128   | -105.008  | -517.193  |
| 1.871                                       | 1.063                          | 0.393            | -87.156   | 589.665   | -98.324   | -621.651  |
| 1.589                                       | 1.018                          | 0.253            | -56.743   | 461.701   | -96.635   | -494.569  |
| 1.749                                       | 0.8                            | 0.321            | -64.588   | 517.875   | -112.293  | -538.834  |
| 1.855                                       | 0.634                          | 0.204            | -82.484   | 576.922   | -106.686  | -590.719  |
| 1.762                                       | 0.837                          | 0.303            | -62.702   | 477.93    | -97.162   | -497.753  |
| 1.586                                       | 0.776                          | 0.347            | -81.056   | 605.907   | -117.989  | -638.079  |
| 1.806                                       | 0.746                          | 0.247            | -59.086   | 472.843   | -100.962  | -491.599  |
| 1.669                                       | 0.718                          | 0.286            | -23.583   | 365.066   | -113.391  | -395.367  |
| 1.623                                       | 0.684                          | 0.314            | -58.505   | 503.577   | -112.748  | -533.876  |
| 1.697                                       | 1.112                          | 0.313            | -101.35   | 631.5     | -93.071   | -661.23   |
| 1.848                                       | 0.762                          | 0.336            | -71.289   | 530.313   | -101.845  | -556.056  |
| 1.816                                       | 0.826                          | 0.248            | -64.462   | 494.77    | -100.383  | -516.061  |
| 1.485                                       | 1.024                          | 0.308            | -69.806   | 522.979   | -99.971   | -559.89   |
| 1.918                                       | 0.856                          | 0.341            | -84.458   | 608.907   | -113.438  | -635.664  |
| 1.809                                       | 0.698                          | 0.279            | -61.057   | 485.729   | -102.217  | -507.253  |
| 1.366                                       | 0.509                          | 0.316            | -57.142   | 530.396   | -126.357  | -567.271  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.689                                       | 0.699                          | 0.317            | -59.175   | 468.582   | -97.776   | -490.94   |
| 1.795                                       | 0.948                          | 0.281            | -75.464   | 556.09    | -106.097  | -584.835  |
| 1.751                                       | 0.894                          | 0.295            | -62.306   | 538.681   | -124.033  | -565.618  |
| 1.591                                       | 0.934                          | 0.275            | -80.98    | 580.392   | -104.33   | -617.765  |
| 1.632                                       | 0.625                          | 0.299            | -66.882   | 542.029   | -118.787  | -564.042  |
| 1.615                                       | 0.735                          | 0.297            | -72.726   | 544.852   | -106.787  | -571.87   |
| 1.851                                       | 0.8                            | 0.348            | -73.351   | 540.168   | -103.678  | -563.719  |
| 1.972                                       | 0.696                          | 0.343            | -68.213   | 503.361   | -97.622   | -521.874  |
| 1.633                                       | 0.516                          | 0.187            | -58.249   | 450.578   | -94.252   | -464.227  |
| 1.861                                       | 0.705                          | 0.364            | -66.393   | 504.543   | -97.627   | -532.268  |
| 1.597                                       | 0.781                          | 0.238            | -71.801   | 556.714   | -114.473  | -582.945  |
| 1.537                                       | 0.809                          | 0.221            | -76.413   | 573.929   | -114.266  | -601.311  |
| 1.829                                       | 0.871                          | 0.348            | -74.587   | 537.034   | -98.534   | -564.414  |
| 1.654                                       | 0.949                          | 0.271            | -54.079   | 485.075   | -111.059  | -520.82   |
| 1.807                                       | 0.664                          | 0.261            | -68.35    | 500.701   | -96.482   | -519.164  |
| 1.715                                       | 1.058                          | 0.337            | -91.147   | 663.563   | -124.532  | -701.382  |
| 1.733                                       | 0.957                          | 0.316            | -70.815   | 568.604   | -118.57   | -602.842  |
| 1.798                                       | 0.994                          | 0.224            | -53.478   | 435.67    | -94.878   | -455.828  |
| 1.639                                       | 0.699                          | 0.271            | -41.121   | 418.298   | -105.395  | -448.7    |
| 2.017                                       | 0.729                          | 0.31             | -110.255  | 694.518   | -106.955  | -712.79   |
| 1.695                                       | 1.109                          | 0.274            | -58.747   | 471.56    | -99.293   | -500.811  |
| 1.621                                       | 0.748                          | 0.296            | -68.476   | 533.473   | -111.355  | -556.909  |
| 1.812                                       | 0.828                          | 0.344            | -61.484   | 511.477   | -112.121  | -537.841  |
| 1.705                                       | 0.89                           | 0.267            | -64.027   | 500.696   | -104.975  | -522.401  |
| 1.594                                       | 0.768                          | 0.312            | -71.572   | 567.408   | -118.831  | -597.653  |
| 1.584                                       | 0.567                          | 0.187            | -50.729   | 439.01    | -101.168  | -457.965  |
| 1.77                                        | 0.654                          | 0.294            | -51.533   | 408.777   | -86.063   | -425.814  |
| 1.821                                       | 0.933                          | 0.341            | -61.767   | 487.769   | -101.42   | -512.827  |
| 1.722                                       | 0.746                          | 0.269            | -71.308   | 545.878   | -110.732  | -569.03   |
| 1.633                                       | 1.033                          | 0.263            | -75.956   | 545.652   | -98.331   | -580.984  |
| 1.839                                       | 0.531                          | 0.323            | -66.742   | 503.758   | -99.182   | -524.261  |
| 1.676                                       | 0.802                          | 0.273            | -58.603   | 496.24    | -111.68   | -520.854  |
| 1.778                                       | 0.905                          | 0.346            | -73.653   | 500.3     | -86.864   | -521.47   |
| 1.699                                       | 0.829                          | 0.295            | -64.108   | 504.492   | -106.715  | -526.272  |
| 1.644                                       | 0.818                          | 0.353            | -52.534   | 424.398   | -88.03    | -452.816  |
| 1.658                                       | 0.72                           | 0.253            | -53.513   | 439.788   | -95.558   | -461.336  |
| 1.727                                       | 0.873                          | 0.212            | -55.503   | 470.763   | -104.018  | -496.294  |
| 1.635                                       | 1.003                          | 0.309            | -65.805   | 583.428   | -132.191  | -628.742  |
| 1.939                                       | 0.628                          | 0.324            | -67.741   | 520.229   | -104.177  | -542.132  |
| 1.769                                       | 0.882                          | 0.308            | -60.358   | 460.187   | -91.62    | -484.269  |
| 1.76                                        | 0.93                           | 0.347            | -76.93    | 557.23    | -103.108  | -588.092  |
| 1.514                                       | 1.072                          | 0.206            | -58.644   | 459.363   | -94.425   | -488.607  |
| 1.623                                       | 1.087                          | 0.331            | -61.934   | 493.124   | -100.781  | -529.711  |
| 1.782                                       | 0.861                          | 0.237            | -64.981   | 493.417   | -102.257  | -508.647  |
| 1.771                                       | 0.772                          | 0.278            | -56.935   | 455.527   | -97.453   | -474.86   |
| 1.48                                        | 0.716                          | 0.267            | -65.453   | 509.212   | -105.582  | -534.085  |
| 1.714                                       | 0.812                          | 0.276            | -79.169   | 593.761   | -117.374  | -619.885  |
| 1.675                                       | 0.86                           | 0.361            | -64.568   | 509.822   | -104.303  | -539.907  |
| 1.577                                       | 0.576                          | 0.29             | -82.231   | 589.359   | -110.154  | -614.281  |
| 1.794                                       | 1.018                          | 0.337            | -78.342   | 574.954   | -107.255  | -608.234  |
| 1.661                                       | 0.811                          | 0.266            | -45.369   | 464.892   | -121.052  | -491.989  |
| 1.568                                       | 0.678                          | 0.286            | -67.832   | 532.862   | -112.778  | -555.758  |
| 1.734                                       | 0.584                          | 0.321            | -84.769   | 583.651   | -106.195  | -598.477  |
| 1.853                                       | 0.961                          | 0.299            | -69.05    | 524.735   | -104.574  | -550.494  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.57                                        | 0.647                          | 0.206            | -50.532   | 428.27    | -97.79    | -446.233  |
| 1.751                                       | 0.82                           | 0.235            | -69.865   | 499.512   | -93.664   | -518.846  |
| 1.661                                       | 0.579                          | 0.234            | -55.599   | 474.674   | -107.458  | -495.732  |
| 1.884                                       | 0.371                          | 0.298            | -77.175   | 525.088   | -94.088   | -533.489  |
| 1.599                                       | 0.783                          | 0.212            | -70.316   | 501.215   | -93.132   | -523.269  |
| 1.847                                       | 0.533                          | 0.242            | -83.169   | 613.432   | -120.707  | -629.696  |
| 1.676                                       | 0.552                          | 0.339            | -96.027   | 648.34    | -113.479  | -667.343  |
| 1.556                                       | 0.669                          | 0.298            | -80.751   | 624.613   | -127.155  | -656.341  |
| 1.68                                        | 0.956                          | 0.279            | -52.647   | 430.999   | -92.488   | -457.506  |
| 1.765                                       | 1.02                           | 0.332            | -67.289   | 480.96    | -88.368   | -506.099  |
| 1.715                                       | 0.565                          | 0.269            | -72.22    | 547.978   | -109.043  | -570.184  |
| 1.452                                       | 0.958                          | 0.262            | -80.138   | 570.334   | -101.874  | -608.458  |
| 1.812                                       | 0.597                          | 0.358            | -60.537   | 471.101   | -96.133   | -492.899  |
| 1.811                                       | 0.939                          | 0.384            | -89.585   | 670.454   | -129.966  | -708.366  |
| 1.85                                        | 0.691                          | 0.241            | -88.087   | 605.878   | -109.887  | -619.424  |
| 1.793                                       | 0.881                          | 0.281            | -66.951   | 515.673   | -104.376  | -539.714  |
| 1.6                                         | 1.173                          | 0.266            | -94.84    | 737.95    | -146.949  | -791.402  |
| 1.72                                        | 0.826                          | 0.279            | -64.126   | 482.913   | -92.856   | -509.795  |
| 1.791                                       | 0.949                          | 0.345            | -71.885   | 498.602   | -88.076   | -521.686  |
| 1.545                                       | 0.969                          | 0.239            | -61.085   | 474.942   | -96.689   | -502.975  |
| 1.56                                        | 0.708                          | 0.201            | -75.034   | 567.195   | -114.642  | -591.018  |
| 1.759                                       | 0.88                           | 0.374            | -89.394   | 639.043   | -119.542  | -666.235  |
| 1.686                                       | 0.619                          | 0.335            | -71.372   | 519.981   | -99.394   | -541.687  |
| 1.515                                       | 0.727                          | 0.198            | -57.273   | 530.824   | -127.346  | -564.002  |
| 1.724                                       | 1.026                          | 0.351            | -65.206   | 539.676   | -115.423  | -575.453  |
| 1.863                                       | 0.717                          | 0.257            | -75.294   | 541.602   | -102.948  | -558.068  |
| 1.708                                       | 0.956                          | 0.24             | -47.14    | 397.771   | -87.845   | -421.894  |
| 1.828                                       | 1.036                          | 0.21             | -55.096   | 456.127   | -99.9     | -480.288  |
| 1.576                                       | 0.85                           | 0.292            | -67.839   | 523.848   | -106.405  | -551.625  |
| 1.81                                        | 0.75                           | 0.297            | -66.952   | 476.878   | -88.454   | -496.021  |
| 1.688                                       | 0.836                          | 0.31             | -74.99    | 580.272   | -119.74   | -607.519  |
| 1.872                                       | 0.644                          | 0.312            | -56.849   | 468.748   | -103.318  | -486.794  |
| 1.69                                        | 0.824                          | 0.348            | -74.36    | 568.028   | -115.183  | -594.748  |
| 1.788                                       | 1.006                          | 0.437            | -61.228   | 499.531   | -106.016  | -532.035  |
| 1.735                                       | 0.985                          | 0.335            | -70.565   | 548.099   | -111.025  | -579.871  |
| 1.669                                       | 0.628                          | 0.183            | -56.199   | 437.629   | -92.103   | -451.875  |
| 1.514                                       | 0.897                          | 0.247            | -87.558   | 667.693   | -133.435  | -705.663  |
| 1.583                                       | 0.902                          | 0.298            | -44.072   | 400.35    | -94.025   | -428.618  |
| 1.685                                       | 0.836                          | 0.331            | -71.447   | 538.436   | -105.713  | -566.341  |
| 1.918                                       | 0.968                          | 0.355            | -71.965   | 548.054   | -108.691  | -576.451  |
| 1.675                                       | 0.939                          | 0.238            | -55.728   | 462.683   | -103.087  | -485.037  |
| 1.636                                       | 0.9                            | 0.373            | -52.616   | 414.496   | -83.844   | -441.897  |
| 1.569                                       | 0.659                          | 0.298            | -55.979   | 429.707   | -87.218   | -451.121  |
| 1.777                                       | 0.842                          | 0.437            | -82.835   | 632.005   | -126.557  | -663.676  |
| 1.765                                       | 0.838                          | 0.247            | -56.569   | 459.131   | -98.716   | -482.015  |
| 1.579                                       | 0.957                          | 0.227            | -75.63    | 568.74    | -113.994  | -596.716  |
| 1.784                                       | 0.87                           | 0.297            | -82.068   | 625.83    | -125.666  | -654.394  |
| 1.986                                       | 0.829                          | 0.33             | -129.762  | 810.247   | -126.386  | -825.687  |
| 1.726                                       | 1.001                          | 0.301            | -56.447   | 463.441   | -101.057  | -489.262  |
| 1.528                                       | 1.105                          | 0.355            | -80.728   | 597.223   | -114.628  | -634.724  |
| 2.003                                       | 0.71                           | 0.24             | -78.722   | 546.903   | -100.933  | -557.506  |
| 1.695                                       | 0.811                          | 0.224            | -48.236   | 422.392   | -96.507   | -446.499  |
| 1.635                                       | 0.701                          | 0.231            | -35.253   | 398.673   | -107.439  | -427.542  |
| 1.869                                       | 0.682                          | 0.308            | -64.71    | 515.502   | -108.618  | -536.268  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.729                                       | 0.862                          | 0.268            | -58.357   | 468.151   | -98.91    | -492.377  |
| 1.734                                       | 0.632                          | 0.259            | -70.948   | 550.923   | -113.671  | -573.256  |
| 1.646                                       | 1.063                          | 0.272            | -78.494   | 610.112   | -121.685  | -652.245  |
| 1.758                                       | 1.032                          | 0.387            | -59.337   | 494.409   | -103.828  | -533.255  |
| 1.713                                       | 0.764                          | 0.204            | -58.714   | 474.321   | -101.676  | -496.465  |
| 1.868                                       | 0.626                          | 0.257            | -63.709   | 469.195   | -91.166   | -484.726  |
| 1.642                                       | 1.151                          | 0.288            | -70.646   | 526.339   | -100.978  | -560.861  |
| 1.862                                       | 0.83                           | 0.313            | -57.869   | 462.384   | -96.461   | -487.365  |
| 1.843                                       | 0.886                          | 0.305            | -63.196   | 510.055   | -108.212  | -535.665  |
| 1.601                                       | 0.981                          | 0.312            | -65.005   | 542.076   | -117.923  | -577.536  |
| 1.783                                       | 0.821                          | 0.35             | -79.534   | 608.808   | -121.934  | -638.34   |
| 1.776                                       | 0.903                          | 0.357            | -61.613   | 489.845   | -102.405  | -517.351  |
| 1.828                                       | 0.874                          | 0.315            | -106.456  | 695.178   | -115.411  | -716.932  |
| 1.729                                       | 0.907                          | 0.324            | -48.729   | 459.936   | -111.182  | -490.345  |
| 1.783                                       | 0.914                          | 0.296            | -66.727   | 503.755   | -99.47    | -528.954  |
| 1.756                                       | 0.81                           | 0.282            | -84.932   | 643.017   | -127.467  | -673.368  |
| 1.923                                       | 1.045                          | 0.327            | -64.48    | 493.94    | -98.971   | -519.88   |
| 1.68                                        | 0.668                          | 0.229            | -67.809   | 544.771   | -118.361  | -565.333  |
| 1.794                                       | 1.114                          | 0.355            | -65.2     | 497.868   | -99.282   | -526.921  |
| 1.845                                       | 0                              | 0.243            | -71.104   | 492.271   | -91.137   | -495.521  |
| 1.844                                       | 0.728                          | 0.297            | -72.966   | 518.343   | -94.944   | -539.847  |
| 1.603                                       | 1.193                          | 0.278            | -88.042   | 649.159   | -123.55   | -689.235  |
| 1.682                                       | 0.647                          | 0.316            | -56.179   | 460.208   | -100.815  | -480.259  |
| 1.858                                       | 0.81                           | 0.34             | -48.721   | 399.866   | -86.647   | -418.959  |
| 1.71                                        | 0.589                          | 0.301            | -67.131   | 534.214   | -112.313  | -557.139  |
| 1.808                                       | 0.917                          | 0.339            | -51.123   | 473.626   | -111.499  | -506.823  |
| 1.762                                       | 0.991                          | 0.335            | -60.025   | 513.135   | -113.066  | -547.256  |
| 1.693                                       | 0.591                          | 0.229            | -67.795   | 534.264   | -111.851  | -556.178  |
| 1.376                                       | 1.076                          | 0.26             | -82.809   | 679.003   | -144.093  | -731.986  |
| 1.794                                       | 0.644                          | 0.313            | -65.046   | 523.861   | -110.815  | -548.185  |
| 1.746                                       | 0.355                          | 0.24             | -93.902   | 611.056   | -102.989  | -619.135  |
| 1.896                                       | 0.861                          | 0.312            | -54.856   | 473.518   | -107.202  | -497.168  |
| 1.815                                       | 0.79                           | 0.296            | -68.714   | 523.668   | -104.858  | -546.355  |
| 1.615                                       | 0.577                          | 0.208            | -71.179   | 555.783   | -115.13   | -579.036  |
| 1.748                                       | 0.91                           | 0.294            | -64.19    | 501.557   | -103.202  | -527.965  |
| 1.685                                       | 0.579                          | 0.315            | -88.203   | 685.525   | -141.541  | -715.746  |
| 1.718                                       | 0.872                          | 0.339            | -85.904   | 576.5     | -98.764   | -598.178  |
| 1.638                                       | 0.795                          | 0.291            | -60.463   | 441.779   | -84.461   | -462.248  |
| 1.721                                       | 0.71                           | 0.238            | -58.95    | 480.033   | -105.996  | -496.87   |
| 1.712                                       | 0.681                          | 0.252            | -69.709   | 522.456   | -103.389  | -544.232  |
| 1.601                                       | 0.891                          | 0.238            | -58.67    | 475.367   | -100.624  | -504.157  |
| 1.721                                       | 0.788                          | 0.245            | -59.281   | 487.588   | -106.622  | -511.67   |
| 1.711                                       | 0.849                          | 0.271            | -76.312   | 545.247   | -101.881  | -567.943  |
| 1.846                                       | 0.869                          | 0.234            | -74.511   | 575.633   | -118.85   | -598.601  |
| 1.512                                       | 0.77                           | 0.249            | -60.257   | 510.282   | -115.244  | -536.693  |
| 1.595                                       | 0.824                          | 0.27             | -43.251   | 419.624   | -104.071  | -447.293  |
| 1.559                                       | 0.476                          | 0.262            | -78.123   | 570.709   | -107.646  | -596.531  |
| 1.911                                       | 0.578                          | 0.298            | -57.477   | 456.675   | -96.903   | -472.531  |
| 1.804                                       | 0.511                          | 0.245            | -76.908   | 554.285   | -105.667  | -568.82   |
| 1.656                                       | 0.981                          | 0.378            | -74.028   | 519.935   | -91.227   | -552.465  |
| 1.776                                       | 0.749                          | 0.271            | -65.978   | 506.708   | -104.172  | -526.236  |
| 1.73                                        | 0.645                          | 0.263            | -55.237   | 422.271   | -85.776   | -439.136  |
| 1.79                                        | 0.917                          | 0.315            | -59.992   | 479.821   | -98.999   | -509.918  |
| 1.793                                       | 0.772                          | 0.314            | -81.069   | 591.755   | -113.8    | -614.949  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.739                                       | 0.797                          | 0.211            | -62.844   | 496.896   | -106.328  | -515.638  |
| 1.818                                       | 1.115                          | 0.316            | -59.546   | 446.39    | -85.132   | -474.558  |
| 1.664                                       | 1.074                          | 0.226            | -116.388  | 767.598   | -126.6    | -802.583  |
| 1.732                                       | 0.906                          | 0.312            | -61.625   | 492.153   | -102.426  | -520.897  |
| 1.774                                       | 0.756                          | 0.29             | -72.243   | 546.466   | -107.496  | -572.396  |
| 1.762                                       | 0.891                          | 0.35             | -64.48    | 482.285   | -93.745   | -508.124  |
| 1.608                                       | 0.72                           | 0.307            | -38.117   | 420.094   | -109.743  | -456.246  |
| 1.727                                       | 0.815                          | 0.286            | -61.145   | 477.868   | -99.098   | -499.939  |
| 1.678                                       | 0.941                          | 0.346            | -60.989   | 481.945   | -99.535   | -510.366  |
| 1.811                                       | 0.903                          | 0.255            | -62.279   | 465.361   | -90.805   | -486.279  |
| 1.655                                       | 0.978                          | 0.249            | -71.075   | 530.994   | -104.546  | -557.34   |
| 1.673                                       | 0.925                          | 0.204            | -41.698   | 396.086   | -98.714   | -417.32   |
| 1.878                                       | 0.936                          | 0.357            | -77.624   | 586.975   | -113.293  | -622.228  |
| 1.999                                       | 0.738                          | 0.365            | -68.222   | 503.266   | -95.779   | -525.092  |
| 1.836                                       | 0.765                          | 0.298            | -75.348   | 566.309   | -113.665  | -587.167  |
| 1.637                                       | 0.812                          | 0.249            | -74.02    | 590.559   | -123.926  | -622.583  |
| 1.795                                       | 0.92                           | 0.429            | -70.589   | 540.782   | -107.183  | -572.048  |
| 1.859                                       | 0.684                          | 0.312            | -70.898   | 555.619   | -113.912  | -580.438  |
| 1.575                                       | 0.7                            | 0.27             | -54.99    | 446.939   | -97.57    | -466.732  |
| 1.714                                       | 0.844                          | 0.318            | -75.165   | 570.949   | -115.443  | -596.586  |
| 1.753                                       | 0.877                          | 0.329            | -80.303   | 629.851   | -129.684  | -663.031  |
| 1.692                                       | 0.77                           | 0.277            | -65.615   | 513.181   | -106.533  | -536.715  |
| 1.682                                       | 0.793                          | 0.237            | -56.714   | 525.936   | -124.918  | -558.881  |
| 1.566                                       | 0.73                           | 0.219            | -60.233   | 476.396   | -100.683  | -498.051  |
| 1.709                                       | 0.925                          | 0.394            | -80.965   | 576.607   | -106.059  | -605.356  |
| 1.815                                       | 0.931                          | 0.354            | -59.668   | 471.398   | -98.032   | -496.082  |
| 1.586                                       | 0.896                          | 0.284            | -53.496   | 437.803   | -94.56    | -463.172  |
| 1.611                                       | 0.749                          | 0.297            | -52.82    | 440.391   | -95.511   | -466.55   |
| 1.811                                       | 0.528                          | 0.239            | -50.493   | 424.892   | -94.206   | -442.714  |
| 1.846                                       | 0.709                          | 0.333            | -77.787   | 543.556   | -97.523   | -563.828  |
| 1.717                                       | 0.755                          | 0.344            | -58.06    | 463.619   | -96.329   | -490.368  |
| 1.718                                       | 0.629                          | 0.312            | -62.327   | 511.403   | -109.283  | -538.099  |
| 1.717                                       | 0.752                          | 0.332            | -71.833   | 538.771   | -105.715  | -562.718  |
| 1.59                                        | 0.858                          | 0.382            | -73.488   | 547.87    | -104.136  | -582.535  |
| 1.633                                       | 0.649                          | 0.259            | -71.75    | 552.381   | -112.973  | -575.916  |
| 1.68                                        | 0.921                          | 0.321            | -49.52    | 404.106   | -86.286   | -427.996  |
| 1.558                                       | 0.814                          | 0.339            | -67.795   | 522.305   | -106.552  | -550.049  |
| 1.654                                       | 0.854                          | 0.298            | -62.557   | 466.023   | -89.994   | -490.713  |
| 1.61                                        | 0.724                          | 0.188            | -73.965   | 557.007   | -112.606  | -577.986  |
| 1.496                                       | 1.081                          | 0.252            | -55.368   | 475.317   | -106.285  | -509.205  |
| 1.709                                       | 0.679                          | 0.242            | -79.155   | 555.806   | -102.845  | -573.893  |
| 1.578                                       | 0.647                          | 0.333            | -108.214  | 784.767   | -148.942  | -820.044  |
| 1.591                                       | 0.749                          | 0.207            | -64.796   | 498.834   | -100.831  | -522.739  |
| 1.626                                       | 0.9                            | 0.203            | -86.242   | 642.615   | -125.843  | -673.965  |
| 1.894                                       | 0.826                          | 0.347            | -93.915   | 641.704   | -113.617  | -662.793  |
| 1.515                                       | 0.961                          | 0.249            | -50.651   | 428.348   | -93.768   | -459.055  |
| 1.581                                       | 0.846                          | 0.299            | -60.847   | 488.81    | -100.982  | -520.946  |
| 1.696                                       | 0.974                          | 0.301            | -76.685   | 570.191   | -110.069  | -602.158  |
| 1.772                                       | 0.862                          | 0.265            | -66.911   | 512.554   | -105.14   | -533.848  |
| 1.695                                       | 1.052                          | 0.328            | -75.126   | 571.857   | -111.117  | -609.983  |
| 1.688                                       | 0.542                          | 0.272            | -65.931   | 509.652   | -105.846  | -526.866  |
| 1.781                                       | 0.607                          | 0.273            | -72.288   | 541.386   | -106.182  | -563.982  |
| 1.448                                       | 1.035                          | 0.3              | -82.181   | 590.329   | -106.958  | -630.585  |
| 1.737                                       | 0.793                          | 0.285            | -74.924   | 544.18    | -102.733  | -568.633  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.858                                       | 0.583                          | 0.284            | -47.356   | 435.694   | -102.507  | -459.195  |
| 1.633                                       | 0.978                          | 0.183            | -63.392   | 505.482   | -106.694  | -532.149  |
| 1.552                                       | 0.743                          | 0.183            | -62.237   | 493.696   | -105.38   | -513.816  |
| 1.597                                       | 0.952                          | 0.236            | -66.931   | 511.525   | -101.957  | -541.091  |
| 1.904                                       | 0.871                          | 0.343            | -88.158   | 604.513   | -104.979  | -630.511  |
| 1.979                                       | 0.921                          | 0.443            | -118.378  | 718.233   | -99.994   | -747.144  |
| 1.685                                       | 0.78                           | 0.351            | -63.325   | 530.473   | -115.489  | -562.516  |
| 1.817                                       | 1.22                           | 0.315            | -71.517   | 552.869   | -110.883  | -587.595  |
| 2.051                                       | 0.758                          | 0.308            | -71.405   | 503.924   | -92.58    | -520.391  |
| 1.785                                       | 0.785                          | 0.27             | -55.351   | 491.071   | -115.331  | -513.734  |
| 1.67                                        | 0.693                          | 0.301            | -99.78    | 651.408   | -110.107  | -666.885  |
| 1.791                                       | 0.895                          | 0.317            | -61.373   | 501.818   | -107.05   | -530.734  |
| 1.76                                        | 0.73                           | 0.273            | -60.767   | 482.256   | -100.739  | -504.741  |
| 1.762                                       | 0.496                          | 0.259            | -70.589   | 526.2     | -103.975  | -543.586  |
| 1.644                                       | 0.956                          | 0.211            | -67.94    | 528.002   | -106.72   | -558.748  |
| 1.765                                       | 0.736                          | 0.316            | -69.138   | 528.135   | -106.253  | -551.093  |
| 1.664                                       | 0.602                          | 0.252            | -76       | 586.232   | -121.21   | -607.087  |
| 1.768                                       | 0.765                          | 0.297            | -61.85    | 467.239   | -93.841   | -485.616  |
| 1.952                                       | 0.551                          | 0.302            | -46.172   | 391.426   | -88.945   | -403.863  |
| 1.872                                       | 0.708                          | 0.291            | -88.959   | 681.501   | -140.005  | -705.003  |
| 1.88                                        | 1.022                          | 0.32             | -79.103   | 546.972   | -95.866   | -572.017  |
| 1.796                                       | 0.861                          | 0.382            | -67.08    | 522.525   | -105.834  | -551.717  |
| 1.65                                        | 0.76                           | 0.243            | -63.079   | 495.102   | -103.608  | -516.551  |
| 1.706                                       | 0.866                          | 0.353            | -78.213   | 572.883   | -107.735  | -604.157  |
| 1.761                                       | 0.847                          | 0.323            | -80.425   | 587.994   | -111.958  | -615.483  |
| 1.675                                       | 0.929                          | 0.352            | -79.767   | 613.197   | -121.566  | -651.764  |
| 1.624                                       | 0.868                          | 0.233            | -53.59    | 442.132   | -96.536   | -465.717  |
| 1.557                                       | 0.893                          | 0.217            | -71.343   | 567.169   | -120.73   | -594.799  |
| 1.885                                       | 0.972                          | 0.34             | -64.27    | 486.314   | -96.323   | -510.048  |
| 1.744                                       | 0.67                           | 0.328            | -65.908   | 498.236   | -98.278   | -521.04   |
| 1.767                                       | 1.009                          | 0.37             | -64.848   | 481.975   | -91.048   | -512.709  |
| 1.92                                        | 1.069                          | 0.425            | -111.661  | 717.112   | -108.804  | -755.375  |
| 1.667                                       | 0.767                          | 0.158            | -36.104   | 351.4     | -89.058   | -369.137  |
| 1.73                                        | 0.881                          | 0.374            | -74.748   | 570.087   | -112.389  | -602.167  |
| 1.772                                       | 0.623                          | 0.317            | -69.883   | 508.221   | -96.248   | -528.175  |
| 1.725                                       | 1.007                          | 0.294            | -60.826   | 466.016   | -94.863   | -489.338  |
| 1.596                                       | 0.805                          | 0.275            | -39.079   | 363.864   | -86.329   | -389.506  |
| 1.678                                       | 0.939                          | 0.235            | -34.315   | 381.484   | -101.545  | -412.022  |
| 1.807                                       | 0.696                          | 0.263            | -77.063   | 533.646   | -97.578   | -548.495  |
| 1.73                                        | 0.852                          | 0.332            | -68.206   | 528.642   | -106.647  | -557.586  |
| 1.769                                       | 1.025                          | 0.329            | -53.32    | 471.725   | -109.54   | -499.991  |
| 1.858                                       | 0.925                          | 0.294            | -84.424   | 568.884   | -97.972   | -589.04   |
| 1.677                                       | 0.935                          | 0.229            | -89.746   | 648.965   | -121.245  | -681.235  |
| 1.849                                       | 0.826                          | 0.28             | -79.796   | 583.994   | -112.747  | -604.265  |
| 1.792                                       | 0.965                          | 0.445            | -94.065   | 619.634   | -99.053   | -651.941  |
| 1.721                                       | 0.922                          | 0.274            | -59.386   | 479.257   | -101.379  | -506.505  |
| 1.632                                       | 1.014                          | 0.292            | -48.801   | 411.919   | -92.09    | -436.715  |
| 1.737                                       | 0.773                          | 0.296            | -75.522   | 542.492   | -102.27   | -564.644  |
| 1.616                                       | 0.883                          | 0.272            | -61.127   | 469.311   | -93.987   | -496.378  |
| 1.822                                       | 1.041                          | 0.308            | -69.393   | 533.194   | -105.104  | -564.9    |
| 1.479                                       | 0.817                          | 0.219            | -62.092   | 483.301   | -100.374  | -506.511  |
| 1.806                                       | 0.718                          | 0.303            | -62.203   | 474.667   | -96.036   | -493.789  |
| 1.784                                       | 0.779                          | 0.362            | -71.462   | 522.15    | -98.826   | -546.878  |
| 1.562                                       | 0.766                          | 0.203            | -53.356   | 464.217   | -106.895  | -488.878  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.726                                       | 0.799                          | 0.274            | -73.727   | 554.425   | -111.26   | -576.333  |
| 1.739                                       | 0.763                          | 0.292            | -93.133   | 679.783   | -129.769  | -708.986  |
| 1.541                                       | 0.72                           | 0.279            | -83.443   | 586.194   | -104.122  | -616.531  |
| 1.702                                       | 1.022                          | 0.306            | -57.534   | 457.922   | -95.672   | -484.745  |
| 1.833                                       | 0.861                          | 0.284            | -75.274   | 544.203   | -102.806  | -567.53   |
| 1.617                                       | 0.963                          | 0.266            | -75.061   | 570.031   | -111.995  | -603.468  |
| 1.618                                       | 0.577                          | 0.214            | -64.964   | 501.083   | -102.32   | -521.666  |
| 1.849                                       | 0.706                          | 0.222            | -52.867   | 426.976   | -91.807   | -443.449  |
| 1.688                                       | 0.739                          | 0.294            | -64.964   | 472.252   | -90.071   | -491.517  |
| 1.657                                       | 0.874                          | 0.32             | -36.092   | 389.775   | -102.506  | -420.006  |
| 1.665                                       | 0.892                          | 0.296            | -39.896   | 410.95    | -105.868  | -439.911  |
| 1.717                                       | 0.965                          | 0.287            | -59.55    | 470.408   | -98.857   | -494.455  |
| 1.72                                        | 0.883                          | 0.313            | -87.856   | 585.609   | -99.902   | -607.524  |
| 1.503                                       | 0.772                          | 0.148            | -62.39    | 494.672   | -102.334  | -522.539  |
| 1.896                                       | 0.706                          | 0.275            | -106.41   | 657.591   | -100.61   | -668.759  |
| 1.846                                       | 0.647                          | 0.278            | -65.073   | 529.699   | -113.775  | -553.283  |
| 1.748                                       | 0.892                          | 0.312            | -65.608   | 496.529   | -97.313   | -522.807  |
| 1.795                                       | 0.796                          | 0.299            | -77.849   | 552.106   | -102.425  | -573.281  |
| 1.757                                       | 0.707                          | 0.302            | -60.474   | 469.074   | -96.394   | -489.888  |
| 1.597                                       | 1.027                          | 0.296            | -132.587  | 784.583   | -105.496  | -817.523  |
| 1.835                                       | 0.673                          | 0.326            | -78.531   | 596.119   | -118.45   | -622.625  |
| 1.756                                       | 0.679                          | 0.308            | -81.27    | 568.485   | -103.234  | -589.478  |
| 1.719                                       | 1.059                          | 0.249            | -92.957   | 677.905   | -124.047  | -721.771  |
| 1.634                                       | 0.728                          | 0.333            | -47.225   | 441.376   | -105.906  | -469.106  |
| 1.743                                       | 0.769                          | 0.254            | -63.899   | 500.44    | -104.498  | -520.998  |
| 1.639                                       | 0.929                          | 0.301            | -47.633   | 431.032   | -100.798  | -459.551  |
| 1.654                                       | 1.035                          | 0.145            | -58.989   | 465.017   | -94.629   | -494.7    |
| 1.856                                       | 0.625                          | 0.289            | -105.997  | 702.138   | -120.293  | -717.518  |
| 1.685                                       | 0.845                          | 0.312            | -64.621   | 502.331   | -103.381  | -527.795  |
| 1.811                                       | 0.817                          | 0.302            | -90.892   | 656.491   | -124.971  | -680.264  |
| 1.477                                       | 0.859                          | 0.226            | -42.336   | 395.763   | -96.513   | -420.96   |
| 1.853                                       | 0.624                          | 0.266            | -67.712   | 517.936   | -106.396  | -532.497  |
| 1.657                                       | 0.907                          | 0.321            | -71.474   | 528.25    | -100.202  | -559.027  |
| 1.488                                       | 0.545                          | 0.244            | -58.963   | 505.969   | -116.185  | -529.303  |
| 1.587                                       | 0.837                          | 0.258            | -74.176   | 580.669   | -120.007  | -611.14   |
| 1.791                                       | 0.702                          | 0.307            | -69.439   | 535.322   | -109.631  | -556.681  |
| 1.722                                       | 0.925                          | 0.378            | -64.712   | 509.305   | -103.655  | -541.55   |
| 1.579                                       | 0.776                          | 0.271            | -67.275   | 559.171   | -122.415  | -590.585  |
| 1.552                                       | 1.14                           | 0.301            | -64.134   | 513.069   | -105.819  | -551.247  |
| 1.757                                       | 0.789                          | 0.278            | -61.35    | 494.69    | -106.16   | -517.148  |
| 1.779                                       | 0.869                          | 0.335            | -60.281   | 481.872   | -101.502  | -507.331  |
| 1.826                                       | 0.886                          | 0.35             | -92.624   | 702.649   | -139.222  | -738.138  |
| 1.788                                       | 0.73                           | 0.278            | -57.504   | 463.453   | -98.111   | -484.9    |
| 1.712                                       | 1.004                          | 0.282            | -77.238   | 572.762   | -108.254  | -606.669  |
| 1.904                                       | 0.755                          | 0.33             | -79.4     | 577.623   | -108.535  | -602.481  |
| 1.658                                       | 0.903                          | 0.395            | -74.392   | 510.689   | -86.818   | -541.557  |
| 1.643                                       | 0.701                          | 0.179            | -55.974   | 466.652   | -104.793  | -485.265  |
| 1.788                                       | 0.878                          | 0.151            | -76.225   | 581.61    | -120.977  | -600.028  |
| 1.782                                       | 0.656                          | 0.174            | -60.2     | 457.943   | -93.257   | -472.988  |
| 1.458                                       | 0.993                          | 0.177            | -75.804   | 603.153   | -126.336  | -640.309  |
| 1.575                                       | 0.949                          | 0.281            | -70.511   | 514.513   | -96.127   | -544.915  |
| 1.695                                       | 0.956                          | 0.3              | -76.336   | 606.518   | -125.905  | -641.352  |
| 1.762                                       | 0.689                          | 0.322            | -56.068   | 464.651   | -101.55   | -487.537  |
| 1.748                                       | 0.666                          | 0.344            | -70.791   | 525.015   | -100.132  | -551.404  |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.782                                       | 0.744                          | 0.332            | -74.744   | 565.462   | -113.129  | -588.916  |
| 1.883                                       | 0.779                          | 0.292            | -64.512   | 517.818   | -109.734  | -540.317  |
| 1.787                                       | 0.917                          | 0.33             | -71.413   | 571.45    | -120.209  | -601.536  |
| 1.525                                       | 0.76                           | 0.339            | -82.118   | 620.016   | -121.031  | -656.54   |
| 1.646                                       | 0.697                          | 0.267            | -71.829   | 553.753   | -113.004  | -578.678  |
| 1.882                                       | 0.634                          | 0.22             | -68.937   | 536.295   | -114.629  | -548.219  |
| 1.804                                       | 0.882                          | 0.396            | -75.565   | 586.24    | -117.239  | -621.088  |
| 1.559                                       | 0.797                          | 0.238            | -62.273   | 487.053   | -98.947   | -516.351  |
| 1.738                                       | 0.702                          | 0.228            | -57.821   | 501.95    | -117.157  | -522.408  |
| 1.466                                       | 0.989                          | 0.275            | -74.226   | 576.009   | -112.676  | -622.395  |
| 1.627                                       | 0.874                          | 0.219            | -51.793   | 437.689   | -97.925   | -461.309  |
| 1.701                                       | 0.982                          | 0.342            | -82.416   | 588.351   | -108.018  | -618.507  |
| 1.773                                       | 0.736                          | 0.31             | -61.444   | 474.18    | -96.54    | -495.49   |
| 1.778                                       | 0.577                          | 0.28             | -57.531   | 467.034   | -101.148  | -484.863  |
| 1.827                                       | 0.61                           | 0.244            | -60.848   | 484.878   | -105.398  | -498.171  |
| 1.813                                       | 1.107                          | 0.251            | -81.058   | 581.57    | -106.857  | -611.349  |
| 1.82                                        | 0.79                           | 0.241            | -70.169   | 580.81    | -129.864  | -602.111  |
| 1.903                                       | 1.012                          | 0.397            | -84.1     | 614.234   | -115.211  | -646.757  |
| 1.703                                       | 1.023                          | 0.34             | -78.101   | 579.92    | -108.404  | -618.504  |
| 1.61                                        | 0.943                          | 0.302            | -57.372   | 482.778   | -105.908  | -514.365  |
| 1.68                                        | 0.839                          | 0.234            | -61.291   | 490.002   | -104.086  | -512.83   |
| 1.64                                        | 0.47                           | 0.197            | -63.158   | 483.446   | -99.482   | -498.789  |
| 1.82                                        | 0.686                          | 0.197            | -71.075   | 554.058   | -115.314  | -572.783  |
| 1.791                                       | 0.868                          | 0.262            | -79.855   | 585.931   | -112.076  | -612.17   |
| 1.666                                       | 1.053                          | 0.359            | -80.635   | 619.588   | -123.709  | -658.935  |
| 1.587                                       | 1.151                          | 0.187            | -72.207   | 535.377   | -102.406  | -568.866  |
| 1.903                                       | 0.787                          | 0.348            | -66.836   | 513.792   | -103.153  | -536.659  |
| 1.752                                       | 0.98                           | 0.303            | -54.311   | 436.748   | -91.793   | -462.209  |
| 1.576                                       | 0.973                          | 0.348            | -60.308   | 518.362   | -115.641  | -554.074  |
| 1.796                                       | 0.815                          | 0.3              | -67.87    | 500.928   | -96.886   | -522.714  |
| 1.61                                        | 0.738                          | 0.256            | -65.107   | 523.225   | -112.137  | -547.171  |
| 1.732                                       | 0.584                          | 0.286            | -62.813   | 483.988   | -99.216   | -502.596  |
| 1.648                                       | 0.738                          | 0.279            | -64.61    | 484.799   | -96.418   | -506.246  |
| 1.948                                       | 0.733                          | 0.363            | -98.852   | 686.824   | -122.863  | -711.416  |
| 1.626                                       | 1.078                          | 0.306            | -75.673   | 557.425   | -104.642  | -594.613  |
| 1.757                                       | 0.704                          | 0.251            | -70.961   | 539.345   | -109.414  | -558.558  |
| 1.697                                       | 0.586                          | 0.284            | -69.032   | 543.85    | -113.332  | -565.949  |
| 1.801                                       | 0.591                          | 0.239            | -60.951   | 490.038   | -104.796  | -508.69   |
| 1.617                                       | 0.881                          | 0.319            | -57.773   | 443.371   | -87.299   | -472.213  |
| 1.692                                       | 0.837                          | 0.286            | -73.232   | 535.01    | -101.235  | -560.076  |
| 1.666                                       | 0.673                          | 0.186            | -85.525   | 647.295   | -130.209  | -673.399  |
| 1.483                                       | 0.974                          | 0.262            | -72.882   | 583.349   | -122.107  | -621.663  |
| 1.589                                       | 1.066                          | 0.299            | -64.499   | 513.751   | -107.497  | -546.721  |
| 1.575                                       | 0.629                          | 0.274            | -45.472   | 425.039   | -102.947  | -449.464  |
| 1.624                                       | 0.822                          | 0.184            | -71.483   | 525.797   | -102.838  | -546.887  |
| 1.788                                       | 0.962                          | 0.331            | -64.212   | 475.854   | -91.641   | -499.48   |
| 1.677                                       | 0.728                          | 0.319            | -75.616   | 578.452   | -116.599  | -605.558  |
| 1.961                                       | 0.781                          | 0.305            | -64.235   | 484.472   | -97.757   | -499.957  |
| 1.428                                       | 0.9                            | 0.253            | -54.867   | 454.798   | -98.063   | -485.775  |
| 1.86                                        | 0.754                          | 0.31             | -66.975   | 499.495   | -98.864   | -518.152  |
| 1.829                                       | 0.82                           | 0.314            | -85.103   | 644.795   | -129.672  | -671.642  |
| 1.694                                       | 1.19                           | 0.215            | -111.35   | 704.688   | -109.526  | -733.582  |
| 1.7                                         | 0.733                          | 0.275            | -67.018   | 515.65    | -106.265  | -536.088  |
| 1.704                                       | 0.695                          | 0.289            | -68.999   | 520.665   | -102.68   | -543.93   |

| $\alpha_6$ (B <sub>2</sub> O <sub>3</sub> ) | $\alpha_1$ (Li <sub>2</sub> O) | $\alpha_3$ (CaO) | $\beta_0$ | $\beta_1$ | $\beta_2$ | $\beta_3$ |
|---------------------------------------------|--------------------------------|------------------|-----------|-----------|-----------|-----------|
| 1.605                                       | 0.845                          | 0.228            | -82.187   | 592.908   | -112.185  | -618.095  |
| 1.721                                       | 0.739                          | 0.294            | -69.486   | 517.683   | -103.106  | -537.442  |
| 1.348                                       | 1.039                          | 0.295            | -80.246   | 612.241   | -117.1    | -663.644  |
| 1.588                                       | 0.669                          | 0.313            | -54.024   | 435.392   | -93.914   | -455.495  |
| 1.839                                       | 0.59                           | 0.209            | -59.081   | 466.484   | -97.404   | -483.269  |
| 1.758                                       | 0.628                          | 0.272            | -82.51    | 626.034   | -126.993  | -647.731  |
| 1.7                                         | 0.681                          | 0.294            | -53.598   | 447.47    | -96.981   | -472.766  |
| 1.567                                       | 1.033                          | 0.384            | -30.994   | 389.525   | -109.562  | -430.354  |

**Table A.7. Variance covariance matrix for HLW Viscosity**

| Term                           | Al <sub>2</sub> O <sub>3</sub> | B <sub>2</sub> O <sub>3</sub> | CaO    | Cr <sub>2</sub> O <sub>3</sub> | F      | LN <sub>2</sub> O <sub>3</sub> | Li <sub>2</sub> O | MnO    | Na <sub>2</sub> O | NiO    | P <sub>2</sub> O <sub>5</sub> | SiO <sub>2</sub> | SrO    | TiO <sub>2</sub> | UO <sub>3</sub> | ZrO <sub>2</sub> | Others |
|--------------------------------|--------------------------------|-------------------------------|--------|--------------------------------|--------|--------------------------------|-------------------|--------|-------------------|--------|-------------------------------|------------------|--------|------------------|-----------------|------------------|--------|
| Al <sub>2</sub> O <sub>3</sub> | 0.050                          | -0.029                        | -0.022 | -0.142                         | -0.082 | 0.000                          | -0.046            | -0.001 | -0.021            | 0.042  | -0.053                        | 0.005            | -0.012 | 0.075            | -0.002          | 0.026            | 0.009  |
| B <sub>2</sub> O <sub>3</sub>  | -0.029                         | 0.060                         | 0.000  | 0.052                          | -0.097 | 0.060                          | 0.012             | 0.015  | 0.005             | 0.009  | 0.001                         | -0.011           | 0.009  | -0.090           | 0.005           | -0.014           | -0.006 |
| CaO                            | -0.022                         | 0.000                         | 0.137  | -0.010                         | -0.308 | 0.006                          | 0.024             | 0.011  | 0.010             | -0.008 | 0.024                         | -0.005           | 0.010  | 0.028            | 0.006           | -0.009           | 0.000  |
| Cr <sub>2</sub> O <sub>3</sub> | -0.142                         | 0.052                         | -0.010 | 9.590                          | -3.040 | -0.019                         | 0.057             | -0.297 | -0.022            | -0.362 | -0.520                        | -0.013           | 0.060  | 1.322            | 0.032           | -0.011           | -0.006 |
| F                              | -0.082                         | -0.097                        | -0.308 | -3.040                         | 15.635 | -0.703                         | -0.093            | 0.129  | 0.003             | -0.862 | -0.483                        | 0.063            | -0.012 | -0.167           | -0.300          | -0.029           | -0.046 |
| LN <sub>2</sub> O <sub>3</sub> | 0.000                          | 0.060                         | 0.006  | -0.019                         | -0.703 | 0.613                          | 0.019             | 0.083  | 0.013             | -0.272 | 0.020                         | -0.032           | 0.027  | 0.116            | -0.027          | -0.019           | 0.013  |
| Li <sub>2</sub> O              | -0.046                         | 0.012                         | 0.024  | 0.057                          | -0.093 | 0.019                          | 0.389             | 0.013  | 0.054             | 0.018  | 0.049                         | -0.040           | -0.002 | -0.149           | 0.024           | -0.042           | 0.001  |
| MnO                            | -0.001                         | 0.015                         | 0.011  | -0.297                         | 0.129  | 0.083                          | 0.013             | 0.406  | -0.005            | -0.100 | 0.052                         | -0.008           | -0.104 | 0.045            | -0.012          | -0.016           | -0.020 |
| Na <sub>2</sub> O              | -0.021                         | 0.005                         | 0.010  | -0.022                         | 0.003  | 0.013                          | 0.054             | -0.005 | 0.057             | -0.047 | 0.010                         | -0.014           | 0.009  | -0.009           | 0.001           | -0.020           | -0.005 |
| NiO                            | 0.042                          | 0.009                         | -0.008 | -0.362                         | -0.862 | -0.272                         | 0.018             | -0.100 | -0.047            | 3.240  | -0.460                        | -0.012           | -0.003 | 0.092            | 0.100           | -0.015           | -0.013 |
| P <sub>2</sub> O <sub>5</sub>  | -0.053                         | 0.001                         | 0.024  | -0.520                         | -0.483 | 0.020                          | 0.049             | 0.052  | 0.010             | -0.460 | 1.102                         | 0.007            | 0.053  | -0.634           | 0.005           | -0.026           | -0.047 |
| SiO <sub>2</sub>               | 0.005                          | -0.011                        | -0.005 | -0.013                         | 0.063  | -0.032                         | -0.040            | -0.008 | -0.014            | -0.012 | 0.007                         | 0.012            | -0.001 | 0.027            | 0.003           | -0.002           | -0.008 |
| SrO                            | -0.012                         | 0.009                         | 0.010  | 0.060                          | -0.012 | 0.027                          | -0.002            | -0.104 | 0.009             | -0.003 | 0.053                         | -0.001           | 0.312  | 0.273            | -0.116          | -0.018           | -0.016 |
| TiO <sub>2</sub>               | 0.075                          | -0.090                        | 0.028  | 1.322                          | -0.167 | 0.116                          | -0.149            | 0.045  | -0.009            | 0.092  | -0.634                        | 0.027            | 0.273  | 11.097           | -0.072          | 0.196            | -0.228 |
| UO <sub>3</sub>                | -0.002                         | 0.005                         | 0.006  | 0.032                          | -0.300 | -0.027                         | 0.024             | -0.012 | 0.001             | 0.100  | 0.005                         | 0.003            | -0.116 | -0.072           | 0.466           | -0.050           | -0.020 |
| ZrO <sub>2</sub>               | 0.026                          | -0.014                        | -0.009 | -0.011                         | -0.029 | -0.019                         | -0.042            | -0.016 | -0.020            | -0.015 | -0.026                        | -0.002           | -0.018 | 0.196            | -0.050          | 0.132            | 0.011  |
| Others                         | 0.009                          | -0.006                        | 0.000  | -0.006                         | -0.046 | 0.013                          | 0.001             | -0.020 | -0.005            | -0.013 | -0.047                        | -0.008           | -0.016 | -0.228           | -0.020          | 0.011            | 0.037  |

**Table A.8. Variance covariance matrix for HLW Sulfate**

| Term                           | Al <sub>2</sub> O <sub>3</sub> | B <sub>2</sub> O <sub>3</sub> | CaO    | Cl       | Fe <sub>2</sub> O <sub>3</sub> | Li <sub>2</sub> O | Na <sub>2</sub> O | SiO <sub>2</sub> | V <sub>2</sub> O <sub>5</sub> | ZrO <sub>2</sub> | Others  |
|--------------------------------|--------------------------------|-------------------------------|--------|----------|--------------------------------|-------------------|-------------------|------------------|-------------------------------|------------------|---------|
| Al <sub>2</sub> O <sub>3</sub> | 0.367                          | -0.323                        | -0.118 | 2.196    | 0.130                          | -0.416            | -0.173            | 0.081            | 0.136                         | 0.119            | -0.089  |
| B <sub>2</sub> O <sub>3</sub>  | -0.323                         | 0.518                         | 0.194  | 0.850    | -0.195                         | -0.348            | -0.016            | -0.034           | 0.192                         | 0.139            | 0.073   |
| CaO                            | -0.118                         | 0.194                         | 0.636  | 10.628   | -0.002                         | -0.087            | -0.007            | -0.059           | 0.099                         | 0.065            | -0.056  |
| Cl                             | 2.196                          | 0.850                         | 10.628 | 1352.916 | -13.047                        | -10.925           | 6.204             | 1.304            | 12.125                        | 11.862           | -14.486 |
| Fe <sub>2</sub> O <sub>3</sub> | 0.130                          | -0.195                        | -0.002 | -13.047  | 0.584                          | 0.455             | -0.148            | -0.088           | 0.217                         | -0.376           | 0.166   |
| Li <sub>2</sub> O              | -0.416                         | -0.348                        | -0.087 | -10.925  | 0.455                          | 5.357             | 1.111             | -0.587           | -1.687                        | -0.949           | 0.077   |
| Na <sub>2</sub> O              | -0.173                         | -0.016                        | -0.007 | 6.204    | -0.148                         | 1.111             | 0.680             | -0.172           | -0.313                        | -0.104           | -0.162  |
| SiO <sub>2</sub>               | 0.081                          | -0.034                        | -0.059 | 1.304    | -0.088                         | -0.587            | -0.172            | 0.113            | 0.021                         | 0.072            | -0.037  |
| V <sub>2</sub> O <sub>5</sub>  | 0.136                          | 0.192                         | 0.099  | 12.125   | 0.217                          | -1.687            | -0.313            | 0.021            | 4.207                         | 0.548            | -0.066  |
| ZrO <sub>2</sub>               | 0.119                          | 0.139                         | 0.065  | 11.862   | -0.376                         | -0.949            | -0.104            | 0.072            | 0.548                         | 1.476            | -0.182  |
| Others                         | -0.089                         | 0.073                         | -0.056 | -14.486  | 0.166                          | 0.077             | -0.162            | -0.037           | -0.066                        | -0.182           | 0.312   |

**Table A.9. Variance covariance matrix for LAW PCT**

| Term                                                         | Al <sub>2</sub> O <sub>3</sub> | B <sub>2</sub> O <sub>3</sub> | CaO     | K <sub>2</sub> O | Li <sub>2</sub> O | MgO    | Na <sub>2</sub> O | P <sub>2</sub> O <sub>5</sub> | SiO <sub>2</sub> | SnO <sub>2</sub> | TiO <sub>2</sub> | ZrO <sub>2</sub> | Others | B <sub>2</sub> O <sub>3</sub> ×B <sub>2</sub> O <sub>3</sub> | K <sub>2</sub> O×K <sub>2</sub> O | Al <sub>2</sub> O <sub>3</sub> ×Li <sub>2</sub> O | CaO×Li <sub>2</sub> O | Li <sub>2</sub> O×Li <sub>2</sub> O | B <sub>2</sub> O <sub>3</sub> ×Na <sub>2</sub> O | K <sub>2</sub> O×Na <sub>2</sub> O | Li <sub>2</sub> O×Na <sub>2</sub> O | Na <sub>2</sub> O×Na <sub>2</sub> O |
|--------------------------------------------------------------|--------------------------------|-------------------------------|---------|------------------|-------------------|--------|-------------------|-------------------------------|------------------|------------------|------------------|------------------|--------|--------------------------------------------------------------|-----------------------------------|---------------------------------------------------|-----------------------|-------------------------------------|--------------------------------------------------|------------------------------------|-------------------------------------|-------------------------------------|
| Al <sub>2</sub> O <sub>3</sub>                               | 1.013                          | -1.878                        | 0.029   | -0.770           | -1.828            | 0.145  | -1.113            | 0.230                         | 0.225            | 0.230            | 0.509            | 0.126            | 0.164  | 8.083                                                        | -2.792                            | -20.321                                           | 3.973                 | 18.004                              | 1.894                                            | 6.609                              | 15.842                              | 2.058                               |
| B <sub>2</sub> O <sub>3</sub>                                | -1.878                         | 43.732                        | -1.333  | 4.584            | -16.823           | -1.918 | -2.995            | -0.700                        | -2.186           | -0.892           | -3.374           | -2.930           | -1.659 | -205.279                                                     | -8.583                            | 0.909                                             | -11.416               | 144.499                             | -29.551                                          | -32.885                            | 57.039                              | 9.398                               |
| CaO                                                          | 0.029                          | -1.333                        | 0.643   | -0.696           | -2.126            | 0.164  | -1.236            | 0.212                         | 0.195            | -0.012           | 0.584            | 0.315            | 0.166  | 5.506                                                        | 2.965                             | 5.268                                             | -11.690               | 17.528                              | 2.093                                            | 4.922                              | 12.420                              | 3.266                               |
| K <sub>2</sub> O                                             | -0.770                         | 4.584                         | -0.696  | 16.850           | 2.239             | -0.335 | 2.034             | 0.091                         | -0.361           | -0.326           | -3.111           | -0.308           | -0.801 | -23.286                                                      | -188.420                          | -5.355                                            | 5.967                 | -1.464                              | -3.366                                           | -41.545                            | -21.732                             | -5.720                              |
| Li <sub>2</sub> O                                            | -1.828                         | -16.823                       | -2.126  | 2.239            | 119.479           | -3.045 | 32.741            | -1.476                        | -3.577           | -0.853           | -2.707           | -3.586           | -2.344 | 71.149                                                       | -73.657                           | -98.258                                           | -56.501               | -868.660                            | -4.015                                           | -2.388                             | -496.237                            | -84.031                             |
| MgO                                                          | 0.145                          | -1.918                        | 0.164   | -0.335           | -3.045            | 1.551  | -1.239            | -0.006                        | 0.252            | 0.042            | -0.001           | 0.332            | 0.133  | 7.525                                                        | -2.234                            | 1.689                                             | 3.631                 | 15.484                              | 4.071                                            | 3.680                              | 15.092                              | 2.637                               |
| Na <sub>2</sub> O                                            | -1.113                         | -2.995                        | -1.236  | 2.034            | 32.741            | -1.239 | 16.396            | -1.496                        | -1.714           | -1.015           | -2.073           | -1.643           | -1.319 | 22.809                                                       | -10.069                           | -21.228                                           | -9.123                | -170.604                            | -21.903                                          | -19.918                            | -172.718                            | -41.097                             |
| P <sub>2</sub> O <sub>5</sub>                                | 0.230                          | -0.700                        | 0.212   | 0.091            | -1.476            | -0.006 | -1.496            | 4.717                         | 0.152            | -0.021           | 0.454            | 0.302            | 0.074  | 0.419                                                        | -9.639                            | -1.736                                            | 1.216                 | 9.018                               | 4.736                                            | 4.822                              | 10.324                              | 3.354                               |
| SiO <sub>2</sub>                                             | 0.225                          | -2.186                        | 0.195   | -0.361           | -3.577            | 0.252  | -1.714            | 0.152                         | 0.388            | 0.150            | 0.248            | 0.328            | 0.170  | 8.692                                                        | 2.024                             | 2.860                                             | 1.426                 | 20.205                              | 4.507                                            | 2.856                              | 18.164                              | 3.900                               |
| SnO <sub>2</sub>                                             | 0.230                          | -0.892                        | -0.012  | -0.326           | -0.853            | 0.042  | -1.015            | -0.021                        | 0.150            | 1.717            | 0.700            | 0.049            | 0.184  | 2.937                                                        | -13.892                           | -5.292                                            | 10.158                | -7.227                              | 4.190                                            | 4.932                              | 4.261                               | 1.544                               |
| TiO <sub>2</sub>                                             | 0.509                          | -3.374                        | 0.584   | -3.111           | -2.707            | -0.001 | -2.073            | 0.454                         | 0.248            | 0.700            | 4.661            | 0.853            | 0.112  | 19.031                                                       | 23.306                            | 4.040                                             | 1.856                 | 1.648                               | 1.840                                            | 12.511                             | 21.653                              | 6.343                               |
| ZrO <sub>2</sub>                                             | 0.126                          | -2.930                        | 0.315   | -0.308           | -3.586            | 0.332  | -1.643            | 0.302                         | 0.328            | 0.049            | 0.853            | 1.536            | 0.286  | 12.508                                                       | -4.379                            | 6.631                                             | -0.370                | 18.409                              | 4.996                                            | 3.730                              | 17.297                              | 3.407                               |
| Others                                                       | 0.164                          | -1.659                        | 0.166   | -0.801           | -2.344            | 0.133  | -1.319            | 0.074                         | 0.170            | 0.184            | 0.112            | 0.286            | 0.587  | 8.338                                                        | 4.200                             | 2.760                                             | 3.027                 | 6.130                               | 1.760                                            | 5.020                              | 13.772                              | 3.676                               |
| B <sub>2</sub> O <sub>3</sub> ×B <sub>2</sub> O <sub>3</sub> | 8.083                          | -205.279                      | 5.506   | -23.286          | 71.149            | 7.525  | 22.809            | 0.419                         | 8.692            | 2.937            | 19.031           | 12.508           | 8.338  | 1059.776                                                     | 133.488                           | 36.004                                            | 93.718                | -713.695                            | 31.511                                           | 137.960                            | -240.895                            | -40.476                             |
| K <sub>2</sub> O×K <sub>2</sub> O                            | -2.792                         | -8.583                        | 2.965   | -188.420         | -73.657           | -2.234 | -10.069           | -9.639                        | 2.024            | -13.892          | 23.306           | -4.379           | 4.200  | 133.488                                                      | 4116.753                          | 374.910                                           | -42.274               | 307.374                             | -69.922                                          | -131.780                           | 337.169                             | 69.399                              |
| Al <sub>2</sub> O <sub>3</sub> ×Li <sub>2</sub> O            | -20.321                        | 0.909                         | 5.268   | -5.355           | -98.258           | 1.689  | -21.228           | -1.736                        | 2.860            | -5.292           | 4.040            | 6.631            | 2.760  | 36.004                                                       | 374.910                           | 1185.957                                          | -36.162               | 78.082                              | 7.946                                            | -70.077                            | 128.766                             | 82.532                              |
| CaO×Li <sub>2</sub> O                                        | 3.973                          | -11.416                       | -11.690 | 5.967            | -56.501           | 3.631  | -9.123            | 1.216                         | 1.426            | 10.158           | 1.856            | -0.370           | 3.027  | 93.718                                                       | -42.274                           | -36.162                                           | 703.693               | -77.100                             | 11.620                                           | -24.359                            | 179.508                             | 24.134                              |
| Li <sub>2</sub> O×Li <sub>2</sub> O                          | 18.004                         | 144.499                       | 17.528  | -1.464           | -868.660          | 15.484 | -170.604          | 9.018                         | 20.205           | -7.227           | 1.648            | 18.409           | 6.130  | -713.695                                                     | 307.374                           | 78.082                                            | -77.100               | 9033.259                            | -5.957                                           | -80.419                            | 3215.376                            | 389.557                             |
| B <sub>2</sub> O <sub>3</sub> ×Na <sub>2</sub> O             | 1.894                          | -29.551                       | 2.093   | -3.366           | -4.015            | 4.071  | -21.903           | 4.736                         | 4.507            | 4.190            | 1.840            | 4.996            | 1.760  | 31.511                                                       | -69.922                           | 7.946                                             | 11.620                | -5.957                              | 174.187                                          | 55.109                             | 48.683                              | 23.286                              |
| K <sub>2</sub> O×Na <sub>2</sub> O                           | 6.609                          | -32.885                       | 4.922   | -41.545          | -2.388            | 3.680  | -19.918           | 4.822                         | 2.856            | 4.932            | 12.511           | 3.730            | 5.020  | 137.960                                                      | -131.780                          | -70.077                                           | -24.359               | -80.419                             | 55.109                                           | 318.414                            | 130.617                             | 44.618                              |
| Li <sub>2</sub> O×Na <sub>2</sub> O                          | 15.842                         | 57.039                        | 12.420  | -21.732          | -496.237          | 15.092 | -172.718          | 10.324                        | 18.164           | 4.261            | 21.653           | 17.297           | 13.772 | -240.895                                                     | 337.169                           | 128.766                                           | 179.508               | 3215.376                            | 48.683                                           | 130.617                            | 2463.752                            | 455.719                             |
| Na <sub>2</sub> O×Na <sub>2</sub> O                          | 2.058                          | 9.398                         | 3.266   | -5.720           | -84.031           | 2.637  | -41.097           | 3.354                         | 3.900            | 1.544            | 6.343            | 3.407            | 3.676  | -40.476                                                      | 69.399                            | 82.532                                            | 24.134                | 389.557                             | 23.286                                           | 44.618                             | 455.719                             | 114.386                             |

**Table A.10. Variance covariance matrix for LAW VHT**

| Term                                | Al <sub>2</sub> O <sub>3</sub> | B <sub>2</sub> O <sub>3</sub> | CaO       | Fe <sub>2</sub> O <sub>3</sub> | K <sub>2</sub> O | Li <sub>2</sub> O | Na <sub>2</sub> O | SiO <sub>2</sub> | SnO <sub>2</sub> | TiO <sub>2</sub> | ZrO <sub>2</sub> | Others  | CaO·CaO   | Li <sub>2</sub> O·Li <sub>2</sub> O | K <sub>2</sub> O·Na <sub>2</sub> O | Li <sub>2</sub> O·Na <sub>2</sub> O | CaO·SiO <sub>2</sub> | K <sub>2</sub> O·K <sub>2</sub> O | Li <sub>2</sub> O·SiO <sub>2</sub> |
|-------------------------------------|--------------------------------|-------------------------------|-----------|--------------------------------|------------------|-------------------|-------------------|------------------|------------------|------------------|------------------|---------|-----------|-------------------------------------|------------------------------------|-------------------------------------|----------------------|-----------------------------------|------------------------------------|
| Al <sub>2</sub> O <sub>3</sub>      | 12.746                         | 0.717                         | -44.230   | 5.183                          | 1.344            | -113.697          | -2.794            | -2.544           | 6.346            | 9.709            | 2.318            | 2.947   | 52.426    | 485.601                             | -17.296                            | 280.223                             | 103.449              | 90.626                            | 107.165                            |
| B <sub>2</sub> O <sub>3</sub>       | 0.717                          | 10.804                        | -40.807   | 3.351                          | -6.163           | 0.816             | 0.844             | -3.543           | 5.031            | 0.519            | 3.699            | 0.975   | 76.321    | -102.487                            | 24.771                             | -63.066                             | 81.805               | 32.649                            | 23.555                             |
| CaO                                 | -44.230                        | -40.807                       | 617.498   | -37.925                        | -29.592          | 312.852           | -24.581           | 38.237           | -43.182          | -28.746          | -12.014          | -29.643 | -795.889  | -1514.524                           | 116.451                            | -626.993                            | -1368.016            | -280.083                          | -349.151                           |
| Fe <sub>2</sub> O <sub>3</sub>      | 5.183                          | 3.351                         | -37.925   | 12.907                         | -2.946           | -60.692           | 0.104             | -3.717           | 7.813            | -7.885           | 5.458            | 3.207   | 70.259    | 157.710                             | 1.496                              | 119.081                             | 83.080               | 86.574                            | 81.063                             |
| K <sub>2</sub> O                    | 1.344                          | -6.163                        | -29.592   | -2.946                         | 414.284          | -676.601          | -3.878            | 1.107            | 6.921            | -33.011          | 10.215           | 0.378   | 3.334     | 2956.842                            | -1435.935                          | 1635.399                            | 95.804               | -2562.025                         | 694.912                            |
| Li <sub>2</sub> O                   | -113.697                       | 0.816                         | 312.852   | -60.692                        | -676.601         | 5618.445          | 66.341            | 20.844           | -95.659          | -150.804         | -131.107         | -71.612 | -1081.111 | -26761.881                          | 3310.805                           | -12174.931                          | -673.883             | 178.923                           | -6401.233                          |
| Na <sub>2</sub> O                   | -2.794                         | 0.844                         | -24.581   | 0.104                          | -3.878           | 66.341            | 10.316            | -4.120           | -2.805           | 3.097            | -6.046           | -1.016  | 47.683    | -656.006                            | 23.449                             | -246.026                            | 45.487               | 71.573                            | 34.983                             |
| SiO <sub>2</sub>                    | -2.544                         | -3.543                        | 38.237    | -3.717                         | 1.107            | 20.844            | -4.120            | 4.451            | -2.990           | -6.681           | -1.574           | -2.421  | -52.270   | 111.298                             | -23.053                            | 24.855                              | -84.717              | -5.993                            | -82.258                            |
| SnO <sub>2</sub>                    | 6.346                          | 5.031                         | -43.182   | 7.813                          | 6.921            | -95.659           | -2.805            | -2.990           | 24.829           | 10.163           | 4.776            | 2.651   | 88.206    | 203.569                             | -31.182                            | 201.058                             | 96.865               | -53.258                           | 105.113                            |
| TiO <sub>2</sub>                    | 9.709                          | 0.519                         | -28.746   | -7.885                         | -33.011          | -150.804          | 3.097             | -6.681           | 10.163           | 97.242           | 9.776            | 2.336   | 108.370   | 85.139                              | 159.999                            | 135.046                             | 60.480               | 123.403                           | 324.192                            |
| ZrO <sub>2</sub>                    | 2.318                          | 3.699                         | -12.014   | 5.458                          | 10.215           | -131.107          | -6.046            | -1.574           | 4.776            | 9.776            | 23.459           | 3.287   | 70.999    | 480.686                             | -25.555                            | 220.229                             | 19.980               | -143.365                          | 162.848                            |
| Others                              | 2.947                          | 0.975                         | -29.643   | 3.207                          | 0.378            | -71.612           | -1.016            | -2.421           | 2.651            | 2.336            | 3.287            | 9.340   | 20.976    | 376.337                             | 20.973                             | 147.949                             | 71.223               | -48.571                           | 72.778                             |
| CaO×CaO                             | 52.426                         | 76.321                        | -795.889  | 70.259                         | 3.334            | -1081.111         | 47.683            | -52.270          | 88.206           | 108.370          | 70.999           | 20.976  | 4832.705  | -6889.248                           | -160.396                           | 131.261                             | 759.346              | 1345.902                          | 3164.818                           |
| Li <sub>2</sub> O×Li <sub>2</sub> O | 485.601                        | -102.487                      | -1514.524 | 157.710                        | 2956.842         | -26761.881        | -656.006          | 111.298          | 203.569          | 85.139           | 480.686          | 376.337 | -6889.248 | 282652.050                          | -14440.190                         | 81168.356                           | 6545.537             | -7117.321                         | 7483.857                           |
| K <sub>2</sub> O×Na <sub>2</sub> O  | -17.296                        | 24.771                        | 116.451   | 1.496                          | -1435.935        | 3310.805          | 23.449            | -23.053          | -31.182          | 159.999          | -25.555          | 20.973  | -160.396  | -14440.190                          | 8228.991                           | -9463.356                           | -318.559             | -1617.293                         | -2859.521                          |
| Li <sub>2</sub> O×Na <sub>2</sub> O | 280.223                        | -63.066                       | -626.993  | 119.081                        | 1635.399         | -12174.931        | -246.026          | 24.855           | 201.058          | 135.046          | 220.229          | 147.949 | 131.261   | 81168.356                           | -9463.356                          | 40141.239                           | 1899.236             | 3175.249                          | 6950.847                           |
| CaO×SiO <sub>2</sub>                | 103.449                        | 81.805                        | -1368.016 | 83.080                         | 95.804           | -673.883          | 45.487            | -84.717          | 96.865           | 60.480           | 19.980           | 71.223  | 759.346   | 6545.537                            | -318.559                           | 1899.236                            | 3327.562             | 229.069                           | 201.205                            |
| K <sub>2</sub> O×K <sub>2</sub> O   | 90.626                         | 32.649                        | -280.083  | 86.574                         | -2562.025        | 178.923           | 71.573            | -5.993           | -53.258          | 123.403          | -143.365         | -48.571 | 1345.902  | -7117.321                           | -1617.293                          | 3175.249                            | 229.069              | 53642.927                         | -465.127                           |
| Li <sub>2</sub> O×SiO <sub>2</sub>  | 107.165                        | 23.555                        | -349.151  | 81.063                         | 694.912          | -6401.233         | 34.983            | -82.258          | 105.113          | 324.192          | 162.848          | 72.778  | 3164.818  | 7483.857                            | -2859.521                          | 6950.847                            | 201.205              | -465.127                          | 12262.160                          |

**Table A.11. Variance covariance matrix for LAW K-3 Neck Corrosion**

| Term                                            | Al <sub>2</sub> O <sub>3</sub> | B <sub>2</sub> O <sub>3</sub> | CaO    | Cr <sub>2</sub> O <sub>3</sub> | Fe <sub>2</sub> O <sub>3</sub> | K <sub>2</sub> O | Li <sub>2</sub> O | MgO       | Na <sub>2</sub> O | P <sub>2</sub> O <sub>5</sub> | SiO <sub>2</sub> | SnO <sub>2</sub> | TiO <sub>2</sub> | V <sub>2</sub> O <sub>5</sub> | ZnO      | ZrO <sub>2</sub> | Others   | MgO×MgO   | Li <sub>2</sub> O×P <sub>2</sub> O <sub>5</sub> | Na <sub>2</sub> O×P <sub>2</sub> O <sub>5</sub> | SiO <sub>2</sub> ×TiO <sub>2</sub> | Na <sub>2</sub> O×V <sub>2</sub> O <sub>5</sub> | V <sub>2</sub> O <sub>5</sub> ×ZnO | SnO <sub>2</sub> ×Others |
|-------------------------------------------------|--------------------------------|-------------------------------|--------|--------------------------------|--------------------------------|------------------|-------------------|-----------|-------------------|-------------------------------|------------------|------------------|------------------|-------------------------------|----------|------------------|----------|-----------|-------------------------------------------------|-------------------------------------------------|------------------------------------|-------------------------------------------------|------------------------------------|--------------------------|
| Al <sub>2</sub> O <sub>3</sub>                  | 1.221                          | -0.076                        | -0.082 | -0.432                         | -0.073                         | 0.075            | -1.502            | 0.440     | -0.656            | -2.757                        | 0.158            | 0.098            | -4.742           | -1.721                        | -0.812   | 0.314            | -0.210   | -19.572   | 31.342                                          | 15.318                                          | 11.589                             | -0.516                                          | 58.617                             | -13.609                  |
| B <sub>2</sub> O <sub>3</sub>                   | -0.076                         | 1.634                         | -0.467 | -1.029                         | 0.271                          | 0.002            | 1.278             | 0.725     | 0.138             | 2.296                         | -0.417           | 0.963            | -5.864           | 1.702                         | -0.572   | 0.429            | -1.142   | -30.149   | -49.941                                         | -8.486                                          | 15.447                             | -6.467                                          | 5.696                              | -10.627                  |
| CaO                                             | -0.082                         | -0.467                        | 1.236  | 1.175                          | 0.344                          | 0.196            | -1.160            | -2.311    | -0.047            | -2.030                        | 0.053            | -0.500           | 3.213            | -4.153                        | -0.378   | 0.171            | -0.488   | 72.567    | 41.805                                          | 10.578                                          | -5.992                             | 12.383                                          | 31.957                             | 61.119                   |
| Cr <sub>2</sub> O <sub>3</sub>                  | -0.432                         | -1.029                        | 1.175  | 180.761                        | -0.767                         | -0.305           | -5.593            | 9.739     | -1.802            | 69.659                        | 0.300            | -45.505          | 32.021           | -2.782                        | 0.863    | 0.079            | 5.351    | -212.958  | -1323.156                                       | -336.205                                        | -58.112                            | 58.465                                          | -1015.350                          | 2492.961                 |
| Fe <sub>2</sub> O <sub>3</sub>                  | -0.073                         | 0.271                         | 0.344  | -0.767                         | 1.186                          | -0.391           | -0.148            | -0.617    | -0.031            | 0.060                         | -0.218           | 2.578            | 0.517            | 0.472                         | 0.030    | 0.791            | -0.417   | 8.466     | -0.755                                          | -2.979                                          | -0.301                             | -1.819                                          | 33.108                             | -127.001                 |
| K <sub>2</sub> O                                | 0.075                          | 0.002                         | 0.196  | -0.305                         | -0.391                         | 2.108            | 1.849             | 1.052     | 0.259             | 4.698                         | -0.265           | -5.018           | -5.856           | -3.661                        | -0.474   | 0.220            | 0.293    | -12.704   | -71.499                                         | -23.250                                         | 15.266                             | 13.324                                          | 22.216                             | 445.272                  |
| Li <sub>2</sub> O                               | -1.502                         | 1.278                         | -1.160 | -5.593                         | -0.148                         | 1.849            | 14.460            | 5.020     | 3.130             | 47.110                        | -1.705           | 0.612            | -18.963          | -2.385                        | 0.081    | -0.687           | 0.359    | -162.457  | -816.760                                        | -215.811                                        | 48.105                             | 20.218                                          | -95.077                            | -13.422                  |
| MgO                                             | 0.440                          | 0.725                         | -2.311 | 9.739                          | -0.617                         | 1.052            | 5.020             | 86.686    | -0.888            | 4.598                         | -1.238           | 9.502            | -15.994          | -1.703                        | -4.967   | 1.202            | 5.059    | -2274.683 | -124.851                                        | -34.090                                         | 36.928                             | 11.249                                          | 40.756                             | -481.985                 |
| Na <sub>2</sub> O                               | -0.656                         | 0.138                         | -0.047 | -1.802                         | -0.031                         | 0.259            | 3.130             | -0.888    | 1.022             | 9.533                         | -0.414           | 0.784            | -4.854           | 1.612                         | 0.502    | -0.557           | -0.020   | 40.549    | -146.074                                        | -45.412                                         | 12.234                             | -2.293                                          | -47.241                            | -77.863                  |
| P <sub>2</sub> O <sub>5</sub>                   | -2.757                         | 2.296                         | -2.030 | 69.659                         | 0.060                          | 4.698            | 47.110            | 4.598     | 9.533             | 1812.446                      | -5.886           | -56.662          | -122.566         | 17.484                        | 6.576    | -1.182           | 3.621    | -679.942  | -32061.469                                      | -8471.361                                       | 313.660                            | -35.652                                         | -651.416                           | 5159.127                 |
| SiO <sub>2</sub>                                | 0.158                          | -0.417                        | 0.053  | 0.300                          | -0.218                         | -0.265           | -1.705            | -1.238    | -0.414            | -5.886                        | 0.412            | -0.497           | 6.776            | -1.564                        | -0.375   | -0.290           | 0.008    | 27.046    | 94.924                                          | 26.834                                          | -17.521                            | 3.347                                           | 27.199                             | 10.981                   |
| SnO <sub>2</sub>                                | 0.098                          | 0.963                         | -0.500 | -45.505                        | 2.578                          | -5.018           | 0.612             | 9.502     | 0.784             | -56.662                       | -0.497           | 80.005           | -0.388           | 1.492                         | -1.509   | -3.294           | 0.380    | -129.183  | 1082.934                                        | 229.969                                         | 4.599                              | -20.404                                         | 578.491                            | -6561.121                |
| TiO <sub>2</sub>                                | -4.742                         | -5.864                        | 3.213  | 32.021                         | 0.517                          | -5.856           | -18.963           | -15.994   | -4.854            | -122.566                      | 6.776            | -0.388           | 520.421          | -58.847                       | -2.967   | -11.124          | -1.491   | 599.431   | 2025.336                                        | 531.455                                         | -1283.638                          | 191.836                                         | 506.500                            | -245.139                 |
| V <sub>2</sub> O <sub>5</sub>                   | -1.721                         | 1.702                         | -4.153 | -2.782                         | 0.472                          | -3.661           | -2.385            | -1.703    | 1.612             | 17.484                        | -1.564           | 1.492            | -58.847          | 257.351                       | 18.625   | -2.686           | 3.743    | 154.743   | -318.970                                        | -64.224                                         | 131.245                            | -528.481                                        | -5083.903                          | 329.670                  |
| ZnO                                             | -0.812                         | -0.572                        | -0.378 | 0.863                          | 0.030                          | -0.474           | 0.081             | -4.967    | 0.502             | 6.576                         | -0.375           | -1.509           | -2.967           | 18.625                        | 8.062    | -0.739           | 1.908    | 84.784    | -31.510                                         | 5.454                                           | -27.096                            | -445.202                                        | 202.217                            |                          |
| ZrO <sub>2</sub>                                | 0.314                          | 0.429                         | 0.171  | 0.079                          | 0.791                          | 0.220            | -0.687            | 1.202     | -0.557            | -1.182                        | -0.290           | -3.294           | -11.124          | -2.686                        | -0.739   | 4.107            | -0.885   | -54.482   | -9.059                                          | 16.961                                          | 27.173                             | -4.968                                          | 115.730                            | 182.968                  |
| Others                                          | -0.210                         | -1.142                        | -0.488 | 5.351                          | -0.417                         | 0.293            | 0.359             | 5.059     | -0.020            | 3.621                         | 0.008            | 0.380            | -1.491           | 3.743                         | 1.908    | -0.885           | 5.645    | -107.767  | -50.172                                         | -27.485                                         | 3.880                              | -2.301                                          | -108.316                           | 9.504                    |
| MgO×MgO                                         | -19.572                        | -30.149                       | 72.567 | -212.958                       | 8.466                          | -12.704          | -162.457          | -2274.683 | 40.549            | -679.942                      | 27.046           | -129.183         | 599.431          | 154.743                       | 84.784   | -54.482          | -107.767 | 69459.709 | 12166.362                                       | 3361.524                                        | -1396.751                          | -1132.268                                       | 2754.270                           | 124.032                  |
| Li <sub>2</sub> O×P <sub>2</sub> O <sub>5</sub> | 31.342                         | -49.941                       | 41.805 | -1323.156                      | -0.755                         | -71.499          | -816.760          | -124.851  | -146.074          | -32061.469                    | 94.924           | 1082.934         | 2025.336         | -318.970                      | -31.510  | -9.059           | -50.172  | 12166.362 | 593929.474                                      | 148142.141                                      | -5190.311                          | 991.599                                         | 10515.689                          | -97200.545               |
| Na <sub>2</sub> O×P <sub>2</sub> O <sub>5</sub> | 15.318                         | -8.486                        | 10.578 | -336.205                       | -2.979                         | -23.250          | -215.811          | -34.090   | -45.412           | -8471.361                     | 26.834           | 229.969          | 531.455          | -64.224                       | -36.443  | 16.961           | -27.485  | 3361.524  | 148142.141                                      | 40472.588                                       | -1359.444                          | 93.011                                          | 2031.022                           | -21807.393               |
| SiO <sub>2</sub> ×TiO <sub>2</sub>              | 11.589                         | 15.447                        | -5.992 | -58.112                        | -0.301                         | 15.266           | 48.105            | 36.928    | 12.234            | 313.660                       | -17.521          | 4.599            | -1283.638        | 131.245                       | 5.454    | 27.173           | 3.880    | -1396.751 | -5190.311                                       | -1359.444                                       | 3192.268                           | -446.287                                        | -962.560                           | 460.891                  |
| Na <sub>2</sub> O×V <sub>2</sub> O <sub>5</sub> | -0.516                         | -6.467                        | 12.383 | 58.465                         | -1.819                         | 13.324           | 20.218            | 11.249    | -2.293            | -35.652                       | 3.347            | -20.404          | 191.836          | -528.481                      | -27.096  | -4.968           | -2.301   | -1132.268 | 991.599                                         | 93.011                                          | -446.287                           | 1902.362                                        | 4583.929                           | 1098.163                 |
| V <sub>2</sub> O <sub>5</sub> ×ZnO              | 58.617                         | 5.696                         | 31.957 | -1015.350                      | 33.108                         | 22.216           | -95.077           | 40.756    | -47.241           | -651.416                      | 27.199           | 578.491          | 506.500          | -5083.903                     | -445.202 | 115.730          | -108.316 | 2754.270  | 10515.689                                       | 2031.022                                        | -962.560                           | 4583.929                                        | 155520.756                         | -50357.458               |
| SnO <sub>2</sub> ×Others                        | -13.609                        | -10.627                       | 61.119 | 2492.961                       | -127.001                       | 445.272          | -13.422           | -481.985  | -77.863           | 5159.127                      | 10.981           | -6561.121        | -245.139         | 329.670                       | 202.217  | 182.968          | 9.504    | 124.032   | -97200.545                                      | -21807.393                                      | 460.891                            | 1098.163                                        | -50357.458                         | 615219.982               |

**Table A.12. Variance covariance matrix for LAW Sulfate**

| Term                                | Al <sub>2</sub> O <sub>3</sub> | B <sub>2</sub> O <sub>3</sub> | CaO   | Cl      | Cr <sub>2</sub> O <sub>3</sub> | K <sub>2</sub> O | Li <sub>2</sub> O | Na <sub>2</sub> O | P <sub>2</sub> O <sub>5</sub> | SiO <sub>2</sub> | SnO <sub>2</sub> | V <sub>2</sub> O <sub>5</sub> | ZrO <sub>2</sub> | Others  | Li <sub>2</sub> OxLi <sub>2</sub> O |
|-------------------------------------|--------------------------------|-------------------------------|-------|---------|--------------------------------|------------------|-------------------|-------------------|-------------------------------|------------------|------------------|-------------------------------|------------------|---------|-------------------------------------|
| Al <sub>2</sub> O <sub>3</sub>      | 0.228                          | -0.04                         | -0.05 | -0.0483 | -0.392                         | 0.021            | -0.063            | -0.0754           | 0.0049                        | 0.00593          | 0.044            | -0.0206                       | 0.02127          | 0.00042 | -1.156                              |
| B <sub>2</sub> O <sub>3</sub>       | -0.038                         | 0.165                         | -0.03 | -0.6468 | -0.225                         | -0.003           | -0.013            | 0.02625           | 0.0808                        | -0.0371          | 0.055            | 0.01019                       | 0.01786          | 0.01591 | 0.9863                              |
| CaO                                 | -0.045                         | -0.03                         | 0.17  | -0.2871 | 0.181                          | -0.037           | -0.328            | 0.00582           | 0.1068                        | -0.01581         | 0.123            | -0.0888                       | 0.04882          | 0.03159 | 4.4471                              |
| Cl                                  | -0.048                         | -0.65                         | -0.29 | 19.6498 | 6.2705                         | 0.824            | 3.6138            | -0.5416           | -1.489                        | 0.243986         | -0.26            | 1.5278                        | -0.8566          | -0.114  | -58.96                              |
| Cr <sub>2</sub> O <sub>3</sub>      | -0.392                         | -0.23                         | 0.181 | 6.27046 | 26.834                         | -0.365           | -1.181            | -0.3685           | -0.996                        | 0.231613         | -3               | -1.1946                       | -0.7319          | -0.0177 | 0.8038                              |
| K <sub>2</sub> O                    | 0.021                          | -0                            | -0.04 | 0.82383 | -0.365                         | 0.341            | 0.4523            | 0.01943           | -0.18                         | -0.02992         | -0.1             | 0.20537                       | -0.0582          | 0.03152 | -4.118                              |
| Li <sub>2</sub> O                   | -0.063                         | -0.01                         | -0.33 | 3.61376 | -1.181                         | 0.452            | 5.1086            | 0.16011           | -0.599                        | -0.11048         | 0.078            | 0.3264                        | -0.1426          | 0.14457 | -81.36                              |
| Na <sub>2</sub> O                   | -0.075                         | 0.026                         | 0.006 | -0.5416 | -0.369                         | 0.019            | 0.1601            | 0.09633           | $-9 \times 10^{-04}$          | -0.03053         | -0               | -0.0406                       | -0.0434          | 0.01919 | 0.9899                              |
| P <sub>2</sub> O <sub>5</sub>       | 0.0049                         | 0.081                         | 0.107 | -1.4887 | -0.996                         | -0.18            | -0.599            | -0.0009           | 2.7017                        | -0.03085         | 0.215            | -0.2128                       | 0.21784          | -0.0254 | 8.9113                              |
| SiO <sub>2</sub>                    | 0.0059                         | -0.04                         | -0.02 | 0.24399 | 0.2316                         | -0.03            | -0.11             | -0.0305           | -0.031                        | 0.038062         | -0.05            | -0.0134                       | -0.0591          | -0.0445 | 0.2602                              |
| SnO <sub>2</sub>                    | 0.0443                         | 0.055                         | 0.123 | -0.2615 | -2.998                         | -0.099           | 0.0777            | -0.0022           | 0.2146                        | -0.05104         | 1.279            | 0.27211                       | -0.0925          | 0.08384 | -0.689                              |
| V <sub>2</sub> O <sub>5</sub>       | -0.021                         | 0.01                          | -0.09 | 1.5278  | -1.195                         | 0.205            | 0.3264            | -0.0406           | -0.213                        | -0.01344         | 0.272            | 1.04019                       | -0.023           | 0.04337 | -2.685                              |
| ZrO <sub>2</sub>                    | 0.0213                         | 0.018                         | 0.049 | -0.8566 | -0.732                         | -0.058           | -0.143            | -0.0434           | 0.2178                        | -0.05906         | -0.09            | -0.023                        | 0.68582          | 0.07489 | 0.5904                              |
| Others                              | 0.0004                         | 0.016                         | 0.032 | -0.114  | -0.018                         | 0.032            | 0.1446            | 0.01919           | -0.025                        | -0.04455         | 0.084            | 0.04337                       | 0.07489          | 0.0931  | -1.661                              |
| Li <sub>2</sub> OxLi <sub>2</sub> O | -1.156                         | 0.986                         | 4.447 | -58.956 | 0.8038                         | -4.118           | -81.36            | 0.9899            | 8.9113                        | 0.260196         | -0.69            | -2.6847                       | 0.5904           | -1.6606 | 1623.9                              |

**Table A.13. Variance covariance matrix for LAW Viscosity**

| Term                           | Al <sub>2</sub> O <sub>3</sub> | B <sub>2</sub> O <sub>3</sub> | CaO    | Fe <sub>2</sub> O <sub>3</sub> | K <sub>2</sub> O | Li <sub>2</sub> O | MgO    | Na <sub>2</sub> O | P <sub>2</sub> O <sub>5</sub> | SiO <sub>2</sub> | SnO <sub>2</sub> | TiO <sub>2</sub> | V <sub>2</sub> O <sub>5</sub> | ZnO    | ZrO <sub>2</sub> | Others |
|--------------------------------|--------------------------------|-------------------------------|--------|--------------------------------|------------------|-------------------|--------|-------------------|-------------------------------|------------------|------------------|------------------|-------------------------------|--------|------------------|--------|
| Al <sub>2</sub> O <sub>3</sub> | 0.119                          | -0.017                        | -0.014 | 0.006                          | -0.006           | -0.083            | -0.029 | -0.041            | 0.030                         | 0.006            | 0.024            | 0.036            | 0.000                         | -0.003 | -0.017           | -0.030 |
| B <sub>2</sub> O <sub>3</sub>  | -0.017                         | 0.138                         | -0.002 | 0.013                          | 0.001            | -0.029            | -0.017 | -0.008            | -0.014                        | -0.023           | 0.044            | 0.029            | -0.023                        | -0.016 | -0.006           | -0.003 |
| CaO                            | -0.014                         | -0.002                        | 0.064  | 0.008                          | 0.012            | -0.013            | 0.019  | 0.010             | 0.019                         | -0.010           | 0.018            | 0.034            | -0.025                        | 0.001  | 0.001            | -0.033 |
| Fe <sub>2</sub> O <sub>3</sub> | 0.006                          | 0.013                         | 0.008  | 0.132                          | -0.009           | -0.010            | -0.011 | -0.002            | -0.007                        | -0.019           | 0.045            | -0.114           | 0.017                         | 0.030  | 0.020            | 0.102  |
| K <sub>2</sub> O               | -0.006                         | 0.001                         | 0.012  | -0.009                         | 0.229            | 0.075             | 0.028  | 0.017             | 0.058                         | -0.010           | -0.107           | -0.094           | -0.008                        | 0.001  | -0.054           | 0.030  |
| Li <sub>2</sub> O              | -0.083                         | -0.029                        | -0.013 | -0.010                         | 0.075            | 0.616             | -0.006 | 0.153             | 0.052                         | -0.048           | -0.152           | -0.013           | -0.162                        | -0.018 | -0.043           | -0.096 |
| MgO                            | -0.029                         | -0.017                        | 0.019  | -0.011                         | 0.028            | -0.006            | 0.568  | 0.033             | -0.049                        | -0.022           | -0.063           | -0.178           | -0.069                        | 0.009  | -0.023           | 0.043  |
| Na <sub>2</sub> O              | -0.041                         | -0.008                        | 0.010  | -0.002                         | 0.017            | 0.153             | 0.033  | 0.059             | 0.005                         | -0.017           | -0.044           | -0.017           | -0.048                        | 0.006  | -0.030           | -0.059 |
| P <sub>2</sub> O <sub>5</sub>  | 0.030                          | -0.014                        | 0.019  | -0.007                         | 0.058            | 0.052             | -0.049 | 0.005             | 1.714                         | -0.012           | -0.110           | -0.013           | -0.047                        | -0.010 | 0.072            | -0.298 |
| SiO <sub>2</sub>               | 0.006                          | -0.023                        | -0.010 | -0.019                         | -0.010           | -0.048            | -0.022 | -0.017            | -0.012                        | 0.022            | -0.002           | -0.022           | 0.019                         | -0.045 | -0.008           | -0.022 |
| SnO <sub>2</sub>               | 0.024                          | 0.044                         | 0.018  | 0.045                          | -0.107           | -0.152            | -0.063 | -0.044            | -0.110                        | -0.002           | 0.463            | 0.122            | -0.116                        | 0.043  | -0.007           | 0.007  |
| TiO <sub>2</sub>               | 0.036                          | 0.029                         | 0.034  | -0.114                         | -0.094           | -0.013            | -0.178 | -0.017            | -0.013                        | -0.022           | 0.122            | 1.025            | 0.109                         | -0.003 | 0.111            | -0.093 |
| V <sub>2</sub> O <sub>5</sub>  | 0.000                          | -0.023                        | -0.025 | 0.017                          | -0.008           | -0.162            | -0.069 | -0.048            | -0.047                        | 0.019            | -0.116           | 0.109            | 0.653                         | 0.048  | 0.059            | -0.095 |
| ZnO                            | -0.003                         | -0.016                        | 0.001  | 0.030                          | 0.001            | -0.018            | 0.009  | 0.006             | -0.010                        | -0.045           | 0.043            | -0.003           | 0.048                         | 0.567  | -0.003           | 0.051  |
| ZrO <sub>2</sub>               | -0.017                         | -0.006                        | 0.001  | 0.020                          | -0.054           | -0.043            | -0.023 | -0.030            | 0.072                         | -0.008           | -0.007           | 0.111            | 0.059                         | -0.003 | 0.295            | -0.018 |
| Others                         | -0.030                         | -0.003                        | -0.033 | 0.102                          | 0.030            | -0.096            | 0.043  | -0.059            | -0.298                        | -0.022           | 0.007            | -0.093           | -0.095                        | 0.051  | -0.018           | 1.716  |

## Appendix B

**Table B.1 Analytical HLW RSDs derived from Dodd and Kaiser (2006)**

| Comp | Analytical RSD | Comp | Analytical RSD | Comp | Analytical RSD |
|------|----------------|------|----------------|------|----------------|
| Ac   | 22.5%          | Mn   | 5.0%           | Ti   | 10.8%          |
| Ag   | 6.6%           | Mo   | 15.0%          | Tl   | 15.0%          |
| Al   | 5.0%           | Na   | 5.0%           | U    | 14.1%          |
| Am   | 22.5%          | Nb   | 25.0%          | V    | 25.0%          |
| As   | 30.0%          | Nd   | 6.6%           | W    | 20.0%          |
| B    | 15.0%          | Ni   | 5.0%           | Y    | 24.2%          |
| Ba   | 10.0%          | Np   | 22.5%          | Zn   | 9.4%           |
| Be   | 20.0%          | P    | 10.0%          | Zr   | 14.6%          |
| Bi   | 25.0%          | Pa   | 22.5%          |      |                |
| Ca   | 5.0%           | Pb   | 10.0%          |      |                |
| Cd   | 15.0%          | Pd   | 25.0%          |      |                |
| Ce   | 8.9%           | Pr   | 10.0%          |      |                |
| Cl   | 15.0%          | Pu   | 22.5%          |      |                |
| Cm   | 22.5%          | Ra   | 15.0%          |      |                |
| Co   | 15.0%          | Rb   | 30.0%          |      |                |
| Cr   | 10.0%          | Rh   | 20.0%          |      |                |
| Cs   | 30.0%          | Ru   | 45.4%          |      |                |
| Cu   | 14.8%          | S    | 15.0%          |      |                |
| Eu   | 50.0%          | Sb   | 25.0%          |      |                |
| F    | 15.0%          | Se   | 50.0%          |      |                |
| Fe   | 5.0%           | Si   | 5.0%           |      |                |
| Gd   | 15.0%          | Sm   | 15.0%          |      |                |
| Hg   | 20.0%          | Sn   | 15.0%          |      |                |
| I    | 15.0%          | Sr   | 6.5%           |      |                |
| K    | 5.0%           | Ta   | 13.2%          |      |                |
| La   | 11.0%          | Tc   | 22.5%          |      |                |
| Li   | 9.9%           | Te   | 50.0%          |      |                |
| Mg   | 13.6%          | Th   | 15.0%          |      |                |

| Rad    | Analytical<br>RSD | Rad   | Analytical<br>RSD |
|--------|-------------------|-------|-------------------|
| 59Ni   | 22.5%             | 233U  | 22.5%             |
| 60Co   | 22.5%             | 234U  | 22.5%             |
| 63Ni   | 22.5%             | 235U  | 22.5%             |
| 79Se   | 22.5%             | 236U  | 22.5%             |
| 90Sr   | 22.5%             | 237Np | 22.5%             |
| 90Y    | 22.5%             | 238Pu | 22.5%             |
| 93mNb  | 22.5%             | 238U  | 22.5%             |
| 93Zr   | 22.5%             | 239Pu | 22.5%             |
| 99Tc   | 22.5%             | 240Pu | 22.5%             |
| 106Ru  | 22.5%             | 241Am | 22.5%             |
| 113mCd | 22.5%             | 241Pu | 22.5%             |
| 125Sb  | 22.5%             | 242Cm | 22.5%             |
| 126Sn  | 22.5%             | 242Pu | 22.5%             |
| 129I   | 22.5%             | 243Am | 22.5%             |
| 134Cs  | 22.5%             | 243Cm | 22.5%             |
| 137mBa | 22.5%             | 244Cm | 22.5%             |
| 137Cs  | 22.5%             |       |                   |
| 151Sm  | 22.5%             |       |                   |
| 152Eu  | 22.5%             |       |                   |
| 154Eu  | 22.5%             |       |                   |
| 155Eu  | 22.5%             |       |                   |
| 226Ra  | 22.5%             |       |                   |
| 227Ac  | 22.5%             |       |                   |
| 228Ra  | 22.5%             |       |                   |
| 229Th  | 22.5%             |       |                   |
| 231Pa  | 22.5%             |       |                   |
| 232Th  | 22.5%             |       |                   |
| 232U   | 22.5%             |       |                   |

**Table B.2 Analytical LAW RSDs derived from Dodd and Kaiser (2005)**

| Comp | CRV<br>aRSD | Comp | CRV<br>aRSD | Comp | CRV<br>aRSD |
|------|-------------|------|-------------|------|-------------|
| Ac   | 25.0%       | Mn   | 15.0%       | Ti   | 25.0%       |
| Ag   | 20.0%       | Mo   | 10.0%       | Tl   | 25.0%       |
| Al   | 5.0%        | Na   | 10.0%       | U    | 5.0%        |
| Am   | 25.0%       | Nb   | 15.0%       | V    | 15.0%       |
| As   | 25.0%       | Nd   | 15.0%       | W    | 15.0%       |
| B    | 25.0%       | Ni   | 10.0%       | Y    | 25.0%       |
| Ba   | 15.0%       | Np   | 25.0%       | Zn   | 25.0%       |
| Be   | 25.0%       | P    | 10.0%       | Zr   | 15.0%       |
| Bi   | 15.0%       | Pa   | 25.0%       |      |             |
| Ca   | 5.0%        | Pb   | 15.0%       |      |             |
| Cd   | 10.0%       | Pd   | 15.0%       |      |             |
| Ce   | 10.0%       | Pr   | 15.0%       |      |             |
| Cl   | 10.0%       | Pu   | 25.0%       |      |             |
| Cm   | 25.0%       | Ra   | 15.0%       |      |             |
| Co   | 25.0%       | Rb   | 25.0%       |      |             |
| Cr   | 5.0%        | Rh   | 20.0%       |      |             |
| Cs   | 15.0%       | Ru   | 25.0%       |      |             |
| Cu   | 25.0%       | S    | 5.0%        |      |             |
| Eu   | 10.0%       | Sb   | 25.0%       |      |             |
| F    | 10.0%       | Se   | 25.0%       |      |             |
| Fe   | 5.0%        | Si   | 5.0%        |      |             |
| Gd   | 15.0%       | Sm   | 10.0%       |      |             |
| Hg   | 10.0%       | Sn   | 25.0%       |      |             |
| I    | 10.0%       | Sr   | 5.0%        |      |             |
| K    | 5.0%        | Ta   | 15.0%       |      |             |
| La   | 10.0%       | Tc   | 25.0%       |      |             |
| Li   | 15.0%       | Te   | 25.0%       |      |             |
| Mg   | 25.0%       | Th   | 25.0%       |      |             |

## Appendix C

**Minimum, maximum, and most likely concentration of components in each GFC  
(based on values reported in Table A-4 of Vienna and Kim 2014).**

| Min                            | Kyanite | Borax | Boric Acid | Wollastonite | Hematite | Li Carbonate | Olivine | Cr <sub>2</sub> O <sub>3</sub> (e) | Silica | Rutile | Zincite | Zircon | V <sub>2</sub> O <sub>5</sub> (b) | SnO <sub>2</sub> (d) |
|--------------------------------|---------|-------|------------|--------------|----------|--------------|---------|------------------------------------|--------|--------|---------|--------|-----------------------------------|----------------------|
| Ac <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Ag <sub>2</sub> O              | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Al <sub>2</sub> O <sub>3</sub> | 0.54    | 0     | 0          | 0.0013       | 0.0099   | 0            | 0.0003  | 0                                  | 0.0004 | 0      | 0       | 0.001  | 0                                 | 0                    |
| Am <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| As <sub>2</sub> O <sub>5</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| B <sub>2</sub> O <sub>3</sub>  | 0       | 0.369 | 0.5625     | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| BaO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| BeO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Bi <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| CaO                            | 0       | 0     | 0          | 0.4477       | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| CdO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Ce <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Cl                             | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Cm <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| CoO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Cr <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0.985                              | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Cs <sub>2</sub> O              | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| CuO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |

| Min                            | Kyanite | Borax | Boric Acid | Wollastonite | Hematite | Li Carbonate | Olivine | Cr <sub>2</sub> O <sub>3</sub> (c) | Silica | Rutile | Zincite | Zircon | V <sub>2</sub> O <sub>5</sub> (b) | SnO <sub>2</sub> (d) |
|--------------------------------|---------|-------|------------|--------------|----------|--------------|---------|------------------------------------|--------|--------|---------|--------|-----------------------------------|----------------------|
| Eu <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| F                              | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Fe <sub>2</sub> O <sub>3</sub> | 0.0042  | 0     | 0          | 0.0029       | 0.9615   | 0            | 0.0468  | 0                                  | 0.0001 | 0      | 0       | 0.0006 | 0                                 | 0                    |
| Gd <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| HgO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| I                              | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| K <sub>2</sub> O               | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| La <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Li <sub>2</sub> O              | 0       | 0     | 0          | 0            | 0        | 0.4          | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| MgO                            | 0       | 0     | 0          | 0            | 0.0001   | 0            | 0.4634  | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| MnO                            | 0       | 0     | 0          | 0.0009       | 0.0003   | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| MoO <sub>3</sub>               | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Na <sub>2</sub> O              | 0       | 0.164 | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Nb <sub>2</sub> O <sub>5</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Nd <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| NiO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0.0022  | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| NpO <sub>2</sub>               | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| P <sub>2</sub> O <sub>5</sub>  | 0       | 0     | 0          | 0            | 0.0018   | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Pa <sub>2</sub> O <sub>5</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| PbO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| PdO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Pr <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| PuO <sub>2</sub>               | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| RaO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Rb <sub>2</sub> O              | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Rh <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |

|                                | SnO <sub>2</sub> (d) | V <sub>2</sub> O <sub>5</sub> (b) | Zircon | Zincite | Rutile | Silica | Cr <sub>2</sub> O <sub>3</sub> (c) | Olivine | Li Carbonate | Hematite | Wollastonite | Boric Acid | Borax | Kyanite | Min   |
|--------------------------------|----------------------|-----------------------------------|--------|---------|--------|--------|------------------------------------|---------|--------------|----------|--------------|------------|-------|---------|-------|
| RuO <sub>2</sub>               | 0                    | 0                                 | 0      | 0       | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0     |
| SO <sub>3</sub>                | 0                    | 0                                 | 0      | 0       | 0      | 0      | 0                                  | 0       | 0            | 0.0006   | 0            | 0          | 0     | 0       | 0     |
| Sb <sub>2</sub> O <sub>3</sub> | 0                    | 0                                 | 0      | 0       | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0     |
| SeO <sub>2</sub>               | 0                    | 0                                 | 0      | 0       | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0     |
| SiO <sub>2</sub>               | 0.39                 | 0                                 | 0.32   | 0       | 0      | 0.992  | 0                                  | 0.4085  | 0            | 0.0084   | 0.48         | 0          | 0     | 0.39    | 0     |
| Sm <sub>2</sub> O <sub>3</sub> | 0                    | 0                                 | 0      | 0       | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0     |
| SnO <sub>2</sub>               | 0                    | 0                                 | 0      | 0       | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0.999 |
| SrO                            | 0                    | 0                                 | 0      | 0       | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0     |
| Ta <sub>2</sub> O <sub>5</sub> | 0                    | 0                                 | 0      | 0       | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0     |
| Tc <sub>2</sub> O <sub>7</sub> | 0                    | 0                                 | 0      | 0       | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0     |
| TeO <sub>2</sub>               | 0                    | 0                                 | 0      | 0       | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0     |
| ThO <sub>2</sub>               | 0                    | 0                                 | 0      | 0       | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0     |
| TiO <sub>2</sub>               | 0.005                | 0                                 | 0.0007 | 0       | 0.928  | 0      | 0                                  | 0       | 0            | 0        | 0.0001       | 0          | 0     | 0.005   | 0     |
| Tl <sub>2</sub> O              | 0                    | 0                                 | 0      | 0       | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0     |
| UO <sub>3</sub>                | 0                    | 0                                 | 0.0003 | 0       | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0     |
| V <sub>2</sub> O <sub>5</sub>  | 0                    | 0                                 | 0      | 0       | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0.992 |
| WO <sub>3</sub>                | 0                    | 0                                 | 0      | 0       | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0     |
| Y <sub>2</sub> O <sub>3</sub>  | 0                    | 0                                 | 0      | 0       | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0     |
| ZnO                            | 0                    | 0                                 | 0      | 0.993   | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0     |
| ZrO <sub>2</sub>               | 0                    | 0                                 | 0.65   | 0       | 0      | 0      | 0                                  | 0       | 0            | 0        | 0            | 0          | 0     | 0       | 0     |

| Max                            | Kyanite | Borax  | Boric Acid | Wollastonite | Hematite | Li Carbonate | Olivine | Cr <sub>2</sub> O <sub>3</sub> (e) | Silica | Rutile | Zincite | Zircon | V <sub>2</sub> O <sub>5</sub> © | SnO <sub>2</sub> (d) |
|--------------------------------|---------|--------|------------|--------------|----------|--------------|---------|------------------------------------|--------|--------|---------|--------|---------------------------------|----------------------|
| Ac <sub>2</sub> O <sub>3</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| Ag <sub>2</sub> O              | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| Al <sub>2</sub> O <sub>3</sub> | 0.6     | 0      | 0          | 0.0027       | 0.0201   | 0            | 0.0078  | 0                                  | 0.004  | 0.0075 | 0       | 0.004  | 0                               | 0                    |
| Am <sub>2</sub> O <sub>3</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| As <sub>2</sub> O <sub>5</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| B <sub>2</sub> O <sub>3</sub>  | 0       | 0.382  | 0.568      | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| BaO                            | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| BeO                            | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| Bi <sub>2</sub> O <sub>3</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0.00017              |
| CaO                            | 0.0004  | 0      | 0          | 0.5023       | 0.0008   | 0.022        | 0.0003  | 0                                  | 0.0002 | 0      | 0       | 0      | 0                               | 0                    |
| CdO                            | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0.0002  | 0      | 0                               | 0                    |
| Ce <sub>2</sub> O <sub>3</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| Cl                             | 0       | 0.0007 | 0          | 0            | 0        | 0.0001       | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| Cm <sub>2</sub> O <sub>3</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| CoO                            | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| Cr <sub>2</sub> O <sub>3</sub> | 0       | 0      | 0          | 0            | 0        | 0.0002       | 0.0078  | 0.991                              | 0      | 0.0075 | 0       | 0      | 0                               | 0                    |
| Cs <sub>2</sub> O              | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| CuO                            | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |

| Max                            | Kyanite | Borax  | Boric Acid | Wollastonite | Hematite | Li Carbonate | Olivine | Cr <sub>2</sub> O <sub>3</sub> (c) | Silica | Rutile | Zincite | Zircon | V <sub>2</sub> O <sub>5</sub> © | SnO <sub>2</sub> (d) |
|--------------------------------|---------|--------|------------|--------------|----------|--------------|---------|------------------------------------|--------|--------|---------|--------|---------------------------------|----------------------|
| Eu <sub>2</sub> O <sub>3</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| F                              | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| Fe <sub>2</sub> O <sub>3</sub> | 0.01    | 0.0001 | 0          | 0.0051       | 0.9785   | 0.0001       | 0.1068  | 0.0003                             | 0.0004 | 0.025  | 0.0001  | 0.0009 | 0.00057189                      | 0.00021              |
| Gd <sub>2</sub> O <sub>3</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| HgO                            | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| I                              | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| K <sub>2</sub> O               | 0.0007  | 0      | 0          | 0            | 0        | 0.0001       | 0       | 0                                  | 0.0002 | 0      | 0       | 0      | 0.00018069                      | 0                    |
| La <sub>2</sub> O <sub>3</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| Li <sub>2</sub> O              | 0       | 0      | 0          | 0            | 0        | 0.4044       | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| MgO                            | 0.0004  | 0      | 0          | 0.001        | 0.0037   | 0.0002       | 0.4934  | 0                                  | 0.0001 | 0      | 0       | 0      | 0                               | 0                    |
| MnO                            | 0       | 0      | 0          | 0.0011       | 0.0039   | 0            | 0       | 0                                  | 0      | 0      | 0.0001  | 0      | 0                               | 0                    |
| MoO <sub>3</sub>               | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| Na <sub>2</sub> O              | 0.0042  | 0.17   | 0          | 0            | 0        | 0.0011       | 0.0004  | 0                                  | 0.0002 | 0      | 0       | 0      | 0.00033699                      | 0                    |
| Nb <sub>2</sub> O <sub>5</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| Nd <sub>2</sub> O <sub>3</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| NiO                            | 0       | 0      | 0          | 0            | 0        | 0            | 0.0052  | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| NpO <sub>2</sub>               | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| P <sub>2</sub> O <sub>5</sub>  | 0       | 0      | 0          | 0            | 0.0054   | 0            | 0       | 0                                  | 0      | 0.0007 | 0       | 0      | 0                               | 0                    |
| Pa <sub>2</sub> O <sub>5</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| PbO                            | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0.0001  | 0      | 0                               | 0.00054              |
| PdO                            | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| Pr <sub>2</sub> O <sub>3</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| PuO <sub>2</sub>               | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| RaO                            | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| Rb <sub>2</sub> O              | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| Rh <sub>2</sub> O <sub>3</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |

| Max                            | Kyanite | Borax  | Boric Acid | Wollastonite | Hematite | Li Carbonate | Olivine | Cr <sub>2</sub> O <sub>3</sub> (c) | Silica | Rutile | Zincite | Zircon | V <sub>2</sub> O <sub>5</sub> © | SnO <sub>2</sub> (d) |
|--------------------------------|---------|--------|------------|--------------|----------|--------------|---------|------------------------------------|--------|--------|---------|--------|---------------------------------|----------------------|
| RuO <sub>2</sub>               | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| SO <sub>3</sub>                | 0       | 0.0005 | 0.0003     | 0            | 0.0009   | 0.0004       | 0       | 0                                  | 0      | 0.0007 | 0       | 0      | 0                               | 0                    |
| Sb <sub>2</sub> O <sub>3</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0.00018              |
| SeO <sub>2</sub>               | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| SiO <sub>2</sub>               | 0.42    | 0      | 0          | 0.53         | 0.0186   | 0            | 0.4385  | 0                                  | 0.999  | 0.025  | 0       | 0.325  | 0.00021393                      | 0                    |
| Sm <sub>2</sub> O <sub>3</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| SnO <sub>2</sub>               | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0.9999               |
| SrO                            | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| Ta <sub>2</sub> O <sub>5</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| Tc <sub>2</sub> O <sub>7</sub> | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| TeO <sub>2</sub>               | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| ThO <sub>2</sub>               | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| TiO <sub>2</sub>               | 0.016   | 0      | 0          | 0.0003       | 0        | 0            | 0       | 0                                  | 0.0005 | 0.936  | 0       | 0.0014 | 0                               | 0                    |
| Tl <sub>2</sub> O              | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| UO <sub>3</sub>                | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0.0008 | 0                               | 0                    |
| V <sub>2</sub> O <sub>5</sub>  | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0.0075 | 0       | 0      | 0.996                           | 0                    |
| WO <sub>3</sub>                | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| Y <sub>2</sub> O <sub>3</sub>  | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                               | 0                    |
| ZnO                            | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0.9999  | 0      | 0                               | 0                    |
| ZrO <sub>2</sub>               | 0       | 0      | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0.025  | 0       | 0.67   | 0                               | 0                    |

| Most likely                    | Kyanite | Borax | Boric Acid | Wollastonite | Hematite | Li Carbonate | Olivine | Cr <sub>2</sub> O <sub>3</sub> (c) | Silica | Rutile | Zincite | Zircon | V <sub>2</sub> O <sub>5</sub> (a) | SnO <sub>2</sub> (d) |
|--------------------------------|---------|-------|------------|--------------|----------|--------------|---------|------------------------------------|--------|--------|---------|--------|-----------------------------------|----------------------|
| Ac <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Ag <sub>2</sub> O              | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Al <sub>2</sub> O <sub>3</sub> | 0.5703  | 0     | 0          | 0.002        | 0.015    | 0            | 0.0019  | 0                                  | 0.0014 | 0.005  | 0       | 0.0025 | 0                                 | 0                    |
| Am <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| As <sub>2</sub> O <sub>5</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| B <sub>2</sub> O <sub>3</sub>  | 0       | 0.375 | 0.5652     | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| BaO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| BeO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Bi <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| CaO                            | 0.0003  | 0     | 0          | 0.475        | 0.0004   | 0            | 0.0002  | 0                                  | 0.0001 | 0      | 0       | 0      | 0                                 | 0                    |
| CdO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0.0001  | 0      | 0                                 | 0                    |
| Ce <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Cl                             | 0       | 0     | 0          | 0            | 0        | 0.0001       | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Cm <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| CoO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Cr <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0.0001       | 0.0013  | 0.991                              | 0      | 0.0016 | 0       | 0      | 0                                 | 0                    |
| Cs <sub>2</sub> O              | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| CuO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |

| Most likely                    | Kyanite | Borax | Boric Acid | Wollastonite | Hematite | Li Carbonate | Olivine | Cr <sub>2</sub> O <sub>3</sub> (e) | Silica | Rutile | Zincite | Zircon | V <sub>2</sub> O <sub>5</sub> (a) | SnO <sub>2</sub> (d) |
|--------------------------------|---------|-------|------------|--------------|----------|--------------|---------|------------------------------------|--------|--------|---------|--------|-----------------------------------|----------------------|
| Eu <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| F                              | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Fe <sub>2</sub> O <sub>3</sub> | 0.0078  | 0     | 0          | 0.004        | 0.97     | 0            | 0.0768  | 0                                  | 0.0002 | 0.007  | 0       | 0.0008 | 0                                 | 0                    |
| Gd <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| HgO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| I                              | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| K <sub>2</sub> O               | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| La <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Li <sub>2</sub> O              | 0       | 0     | 0          | 0            | 0        | 0.402        | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| MgO                            | 0.0001  | 0     | 0          | 0.001        | 0.001    | 0.0001       | 0.4801  | 0                                  | 0.0001 | 0      | 0       | 0      | 0                                 | 0                    |
| MnO                            | 0       | 0     | 0          | 0.001        | 0.0012   | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| MoO <sub>3</sub>               | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Na <sub>2</sub> O              | 0.0042  | 0.167 | 0          | 0            | 0        | 0.0008       | 0.0003  | 0                                  | 0.0002 | 0      | 0       | 0      | 0                                 | 0                    |
| Nb <sub>2</sub> O <sub>5</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Nd <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| NiO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0.0037  | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| NpO <sub>2</sub>               | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| P <sub>2</sub> O <sub>5</sub>  | 0       | 0     | 0          | 0            | 0.0027   | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Pa <sub>2</sub> O <sub>5</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| PbO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| PdO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Pr <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| PuO <sub>2</sub>               | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| RaO                            | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Rb <sub>2</sub> O              | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Rh <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0            | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |

| Most likely                    | Kyanite | Borax | Boric Acid | Wollastonite | Hematite | Carbonate<br>Li | Olivine | Cr <sub>2</sub> O <sub>3</sub> (c) | Silica | Rutile | Zincite | Zircon | V <sub>2</sub> O <sub>5</sub> (a) | SnO <sub>2</sub> (d) |
|--------------------------------|---------|-------|------------|--------------|----------|-----------------|---------|------------------------------------|--------|--------|---------|--------|-----------------------------------|----------------------|
| RuO <sub>2</sub>               | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| SO <sub>3</sub>                | 0       | 0     | 0          | 0            | 0.0007   | 0.0003          | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Sb <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| SeO <sub>2</sub>               | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| SiO <sub>2</sub>               | 0.4067  | 0     | 0          | 0.51         | 0.0135   | 0               | 0.4252  | 0                                  | 0.997  | 0.022  | 0       | 0.3225 | 0                                 | 0                    |
| Sm <sub>2</sub> O <sub>3</sub> | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| SnO <sub>2</sub>               | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0.99945              |
| SrO                            | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Ta <sub>2</sub> O <sub>5</sub> | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Tc <sub>2</sub> O <sub>7</sub> | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| TeO <sub>2</sub>               | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| ThO <sub>2</sub>               | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| TiO <sub>2</sub>               | 0.0079  | 0     | 0          | 0.0002       | 0        | 0               | 0       | 0                                  | 0.0001 | 0.932  | 0       | 0.001  | 0                                 | 0                    |
| Tl <sub>2</sub> O              | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| UO <sub>3</sub>                | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0      | 0       | 0.0004 | 0                                 | 0                    |
| V <sub>2</sub> O <sub>5</sub>  | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0.0045 | 0       | 0      | 0.994                             | 0                    |
| WO <sub>3</sub>                | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| Y <sub>2</sub> O <sub>3</sub>  | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0      | 0       | 0      | 0                                 | 0                    |
| ZnO                            | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0      | 0.999   | 0      | 0                                 | 0                    |
| ZrO <sub>2</sub>               | 0       | 0     | 0          | 0            | 0        | 0               | 0       | 0                                  | 0      | 0.019  | 0       | 0.66   | 0                                 | 0                    |

## Appendix D

Minimum, maximum, and most likely PERT distribution in  $\ln \left[ \frac{1}{1 - \nu_i} \right]$  with minimum, based on the values reported by Nelson (2013).

| Comp                           | ln(DF), Min | ln(DF),<br>Most likely | ln(DF), Max |  | Comp                           | ln(DF), Min | ln(DF),<br>Most likely | ln(DF), Max |  | Comp                          | ln(DF), Min | ln(DF),<br>Most likely | ln(DF), Max |
|--------------------------------|-------------|------------------------|-------------|--|--------------------------------|-------------|------------------------|-------------|--|-------------------------------|-------------|------------------------|-------------|
| Ac <sub>2</sub> O <sub>3</sub> | 2.9601      | 6.8772                 | 11.1239     |  | MoO <sub>3</sub>               | 1.8563      | 4.194                  | 6.4944      |  | UO <sub>3</sub>               | 2.9601      | 6.8772                 | 11.1239     |
| Ag <sub>2</sub> O              | 1.8563      | 4.194                  | 6.4944      |  | Na <sub>2</sub> O              | 3.4874      | 4.8633                 | 6.4944      |  | V <sub>2</sub> O <sub>5</sub> | 1.8563      | 4.194                  | 6.4944      |
| Al <sub>2</sub> O <sub>3</sub> | 5.0764      | 7.0814                 | 8.8901      |  | Nb <sub>2</sub> O <sub>5</sub> | 2.9601      | 6.8772                 | 11.1239     |  | WO <sub>3</sub>               | 2.9601      | 6.8772                 | 11.1239     |
| Am <sub>2</sub> O <sub>3</sub> | 1.8563      | 4.194                  | 6.4944      |  | Nd <sub>2</sub> O <sub>3</sub> | 2.9601      | 6.8772                 | 11.1239     |  | Y <sub>2</sub> O <sub>3</sub> | 2.9601      | 6.8772                 | 11.1239     |
| As <sub>2</sub> O <sub>5</sub> | 0.0945      | 1.5296                 | 4.237       |  | NiO                            | 3.9299      | 4.7875                 | 6.3835      |  | ZnO                           | 4.7353      | 6.2383                 | 7.8709      |
| B <sub>2</sub> O <sub>3</sub>  | 3.708       | 4.5886                 | 5.8519      |  | NpO <sub>2</sub>               | 2.9601      | 6.8772                 | 11.1239     |  | ZrO <sub>2</sub>              | 7.2204      | 8.7143                 | 11.1239     |
| BaO                            | 2.9601      | 6.8772                 | 11.1239     |  | P <sub>2</sub> O <sub>5</sub>  | 2.9601      | 5.1381                 | 6.7822      |  |                               |             |                        |             |
| BeO                            | 2.9601      | 6.8772                 | 11.1239     |  | Pa <sub>2</sub> O <sub>5</sub> | 2.9601      | 6.8772                 | 11.1239     |  |                               |             |                        |             |
| Bi <sub>2</sub> O <sub>3</sub> | 1.8563      | 4.194                  | 6.4944      |  | PbO                            | 3.2542      | 4.4716                 | 6.2971      |  |                               |             |                        |             |
| CaO                            | 5.2311      | 7.0825                 | 8.6034      |  | PdO                            | 2.9601      | 6.8772                 | 11.1239     |  |                               |             |                        |             |
| CdO                            | 2.9601      | 6.8772                 | 11.1239     |  | Pr <sub>2</sub> O <sub>3</sub> | 2.9601      | 6.8772                 | 11.1239     |  |                               |             |                        |             |
| Ce <sub>2</sub> O <sub>3</sub> | 2.9601      | 6.8772                 | 11.1239     |  | PuO <sub>2</sub>               | 2.9601      | 6.8772                 | 11.1239     |  |                               |             |                        |             |
| Cl                             | 0.0979      | 0.7583                 | 1.9095      |  | RaO                            | 0.0945      | 1.5296                 | 4.237       |  |                               |             |                        |             |
| Cm <sub>2</sub> O <sub>3</sub> | 2.9601      | 6.8772                 | 11.1239     |  | Rb <sub>2</sub> O              | 1.8563      | 4.194                  | 6.4944      |  |                               |             |                        |             |
| CoO                            | 2.9601      | 6.8772                 | 11.1239     |  | Rh <sub>2</sub> O <sub>3</sub> | 2.9601      | 6.8772                 | 11.1239     |  |                               |             |                        |             |
| Cr <sub>2</sub> O <sub>3</sub> | 1.8563      | 3.0681                 | 5.3033      |  | RuO <sub>2</sub>               | 1.8563      | 4.194                  | 6.4944      |  |                               |             |                        |             |
| Cs <sub>2</sub> O              | 0.47        | 2.3609                 | 4.237       |  | SO <sub>3</sub>                | 0.6308      | 1.9694                 | 3.2089      |  |                               |             |                        |             |
| CuO                            | 2.9601      | 6.8772                 | 11.1239     |  | Sb <sub>2</sub> O <sub>3</sub> | 0.0945      | 1.5296                 | 4.237       |  |                               |             |                        |             |
| Eu <sub>2</sub> O <sub>3</sub> | 2.9601      | 6.8772                 | 11.1239     |  | SeO <sub>2</sub>               | 0.0945      | 1.5296                 | 4.237       |  |                               |             |                        |             |
| F                              | 0.1179      | 1.4682                 | 2.4361      |  | SiO <sub>2</sub>               | 5.3471      | 7.5372                 | 9.7527      |  |                               |             |                        |             |
| Fe <sub>2</sub> O <sub>3</sub> | 4.9381      | 6.6712                 | 8.8984      |  | Sm <sub>2</sub> O <sub>3</sub> | 2.9601      | 6.8772                 | 11.1239     |  |                               |             |                        |             |
| Gd <sub>2</sub> O <sub>3</sub> | 2.9601      | 6.8772                 | 11.1239     |  | SnO <sub>2</sub>               | 2.9601      | 6.8772                 | 11.1239     |  |                               |             |                        |             |
| HgO                            | 0           | 0                      | 0           |  | SrO                            | 2.9601      | 6.8772                 | 11.1239     |  |                               |             |                        |             |
| I                              | 0.0945      | 0.5807                 | 2.266       |  | Ta <sub>2</sub> O <sub>5</sub> | 2.9601      | 6.8772                 | 11.1239     |  |                               |             |                        |             |
| K <sub>2</sub> O               | 2.0669      | 3.3844                 | 5.5607      |  | Tc <sub>2</sub> O <sub>7</sub> | 0.0953      | 0.47                   | 1.6094      |  |                               |             |                        |             |
| La <sub>2</sub> O <sub>3</sub> | 2.9601      | 6.8772                 | 11.1239     |  | TeO <sub>2</sub>               | 0.0945      | 1.5296                 | 4.237       |  |                               |             |                        |             |
| Li <sub>2</sub> O              | 3.4689      | 5.987                  | 7.2894      |  | ThO <sub>2</sub>               | 2.9601      | 6.8772                 | 11.1239     |  |                               |             |                        |             |
| MgO                            | 7.2464      | 8.8618                 | 11.0268     |  | TiO <sub>2</sub>               | 4.6308      | 6.1247                 | 8.074       |  |                               |             |                        |             |
| MnO                            | 2.9601      | 6.8772                 | 11.1239     |  | Tl <sub>2</sub> O              | 0.0945      | 1.5296                 | 4.237       |  |                               |             |                        |             |



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