

iDICS

INTERNATIONAL  
DIGITAL IMAGE CORRELATION  
SOCIETY

# The story of DIC Uncertainty Quantification, thus far...

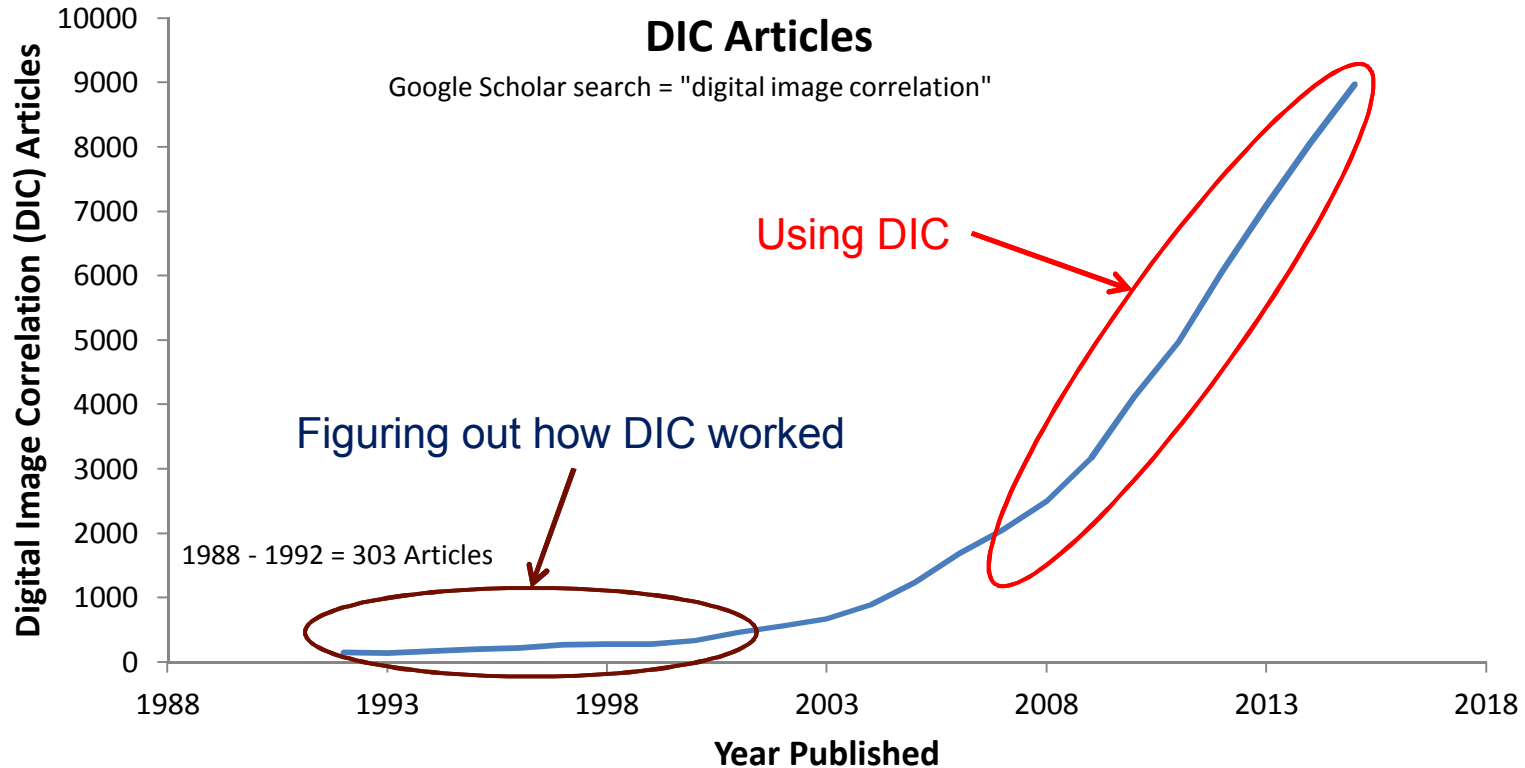


Layer up on layer of  
complication that makes you  
want to cry

Phillip L. Reu

London 2017

# DIC has changed the way we do experimental mechanics.



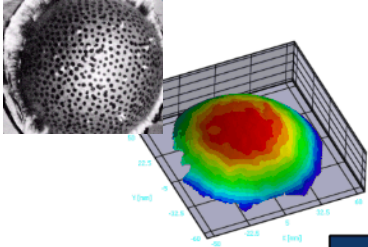
Digital Image Correlation publishing.xlsx (OneNote)

## “DIC Uncertainty” Quantification Publications

- Almost no publications before 2005
- 2005 to 2017 there are 30 publications
- I started pushing the issue for the 2009 SEM in Albuquerque where we had the first session.

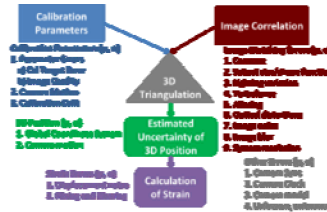
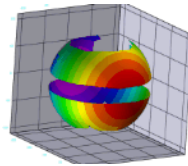
# Digital Image Correlation – Phil and Sandia

Displacement, velocity and strain

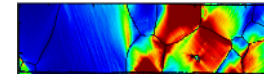


Stereo-DIC Uncertainty Quantification  
From colors to metrology.

360° coverage



Grain Scale strain



DIC for Material Properties

- Quantified Uncertainty
- More parameters per test
- Parameter interaction
- High-throughput
- Model validation



2005

2007

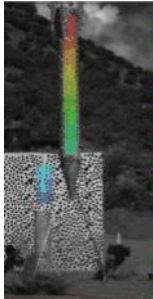
2009

2011

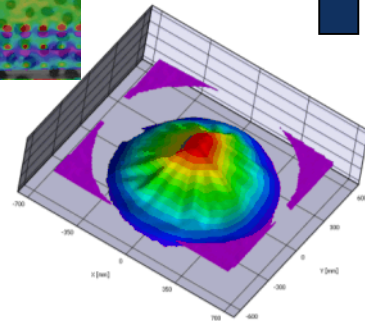
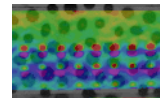
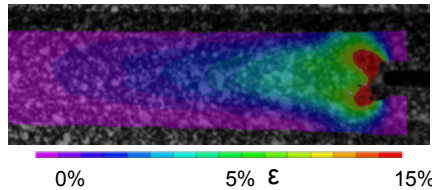
2013

2015

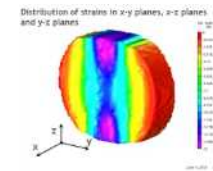
Introduction of DIC to Sandia



Crack-tip and Fracture Strain



Explosive Panel Deformation



Volumetric DIC

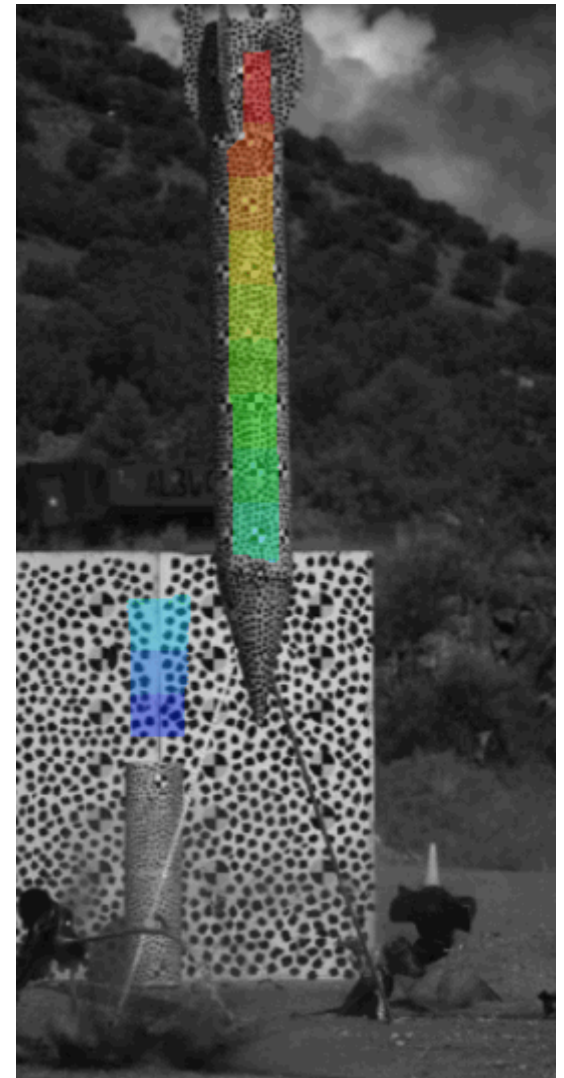
**Sandia's growing use of quantitative image based measurements.**

# Sandia required “NIST traceable” measurements with UQ



- Complicated experimental setup and environments
- Understand the error sources (bottom-up)
- Must quantify uncertainty
  - 0.125% Field-of-View (or full-range)
  - 1.9 pixel error

Reu, P.L., *Experimental Mechanics*, 2013. **53(9): p. 1661-1680.**



# There is an important difference between the definition of “error” and “uncertainty”.

## *Error*

- Difference between the measured value and the “true” value (often unknown).
- Sometimes described as bias (persistent) and random (volatile).

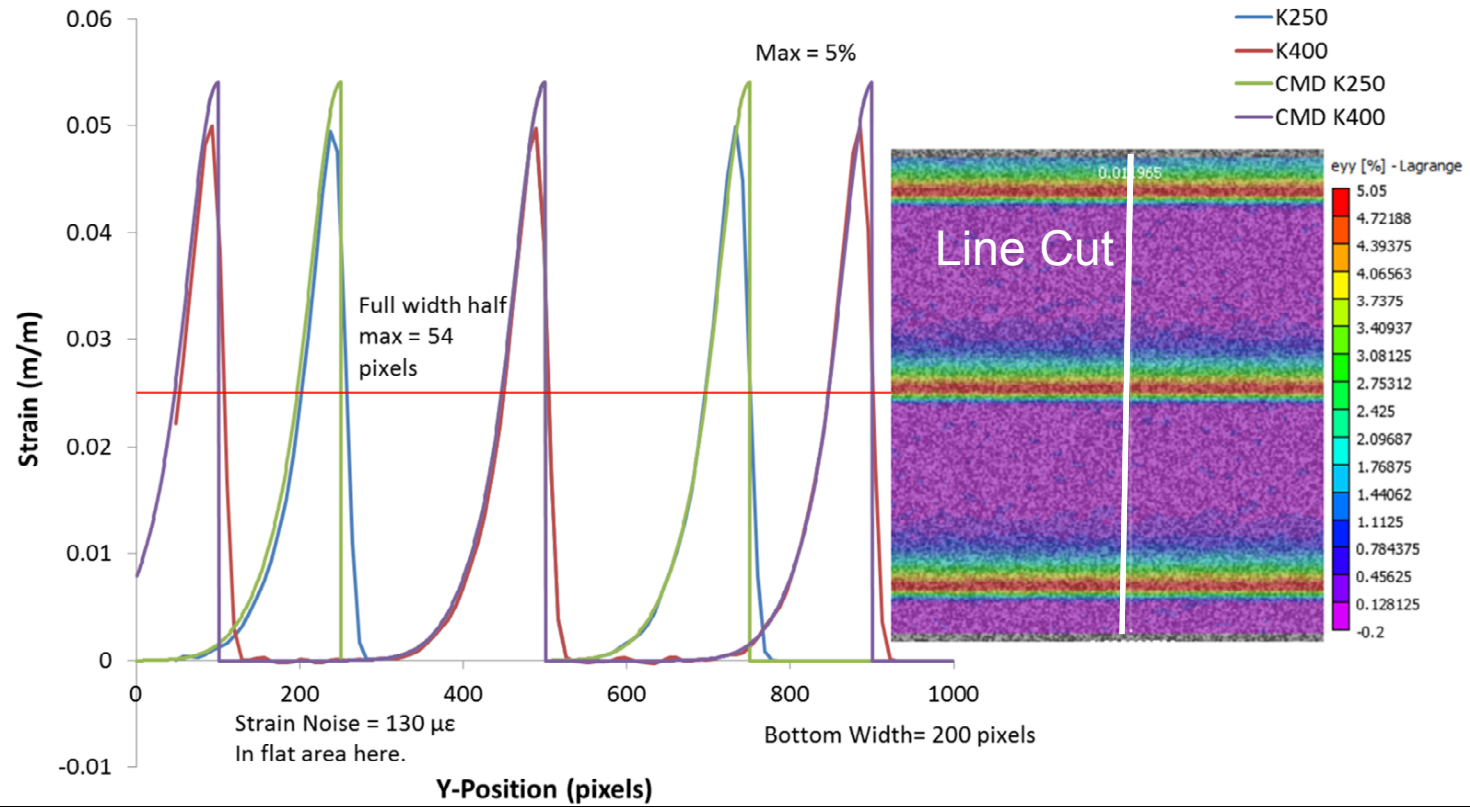
## *Uncertainty<sup>†</sup>*

- “Is the doubt that exists about the result of any measurement”.
- Determined using standard methods: Type A and Type B.
- Expressed using an interval, standard uncertainty, and a confidence level.
- Standard uncertainty ( $u$ ) is the standard deviation ( $s$ ) divided by square root of number of samples ( $N$ ).
- Traceability is assumed.

**A measurement to be useful must have an associated uncertainty!**

# Error: Difference between a known and measured value.

Simulated or synthetic images provide a “known” displacement field



## Advantages/Problems with simulated or synthetic images

- You know the answer
- Verifies the DIC code
- Investigates numerical issues
- Errors in synthetic image creation.
- **What errors have I missed?**

# DIC UQ literature is very thin, particularly for stereo-DIC.

## *Verification*

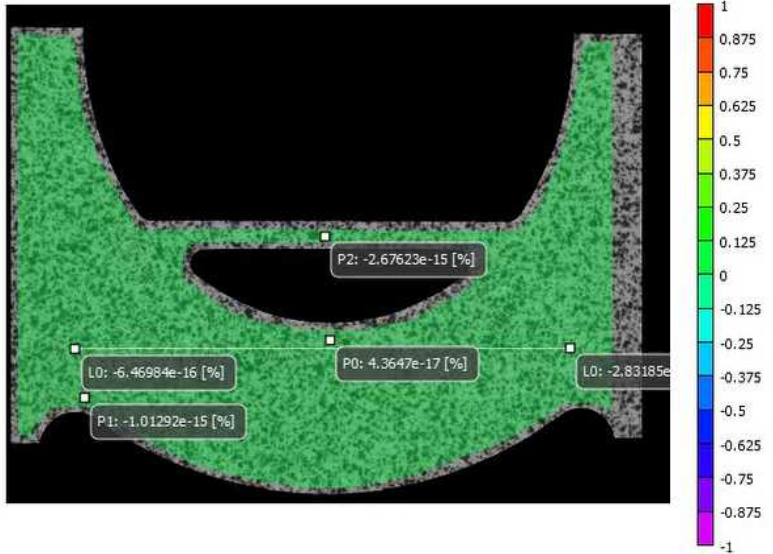
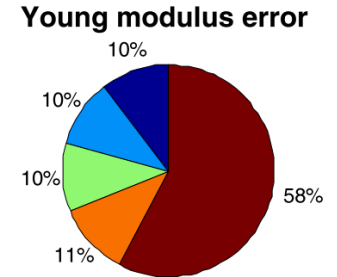
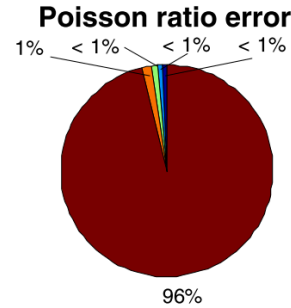
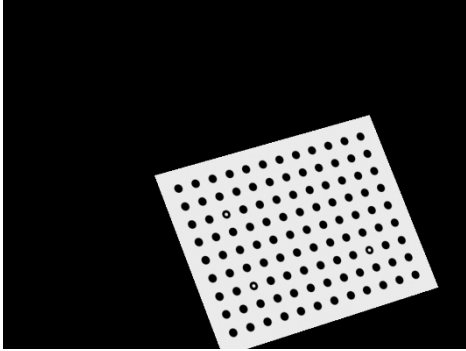
- Are we solving the equations correctly (optical flow)?
  - Do we converge to the correct answer?
  - Is the software written correctly?
  - Comparison with **synthetic** images.
- 90% of the published papers  
(and nearly all 2D!)**

## *Validation*

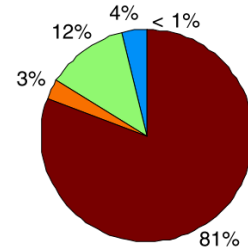
- Are the measurements an accurate representation of the real world?
- Comparisons with a 2<sup>nd</sup> measurement.
- Credibility and uncertainty quantification.

**Small number of comparison papers**

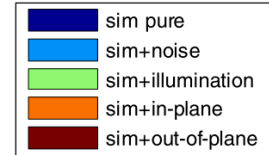
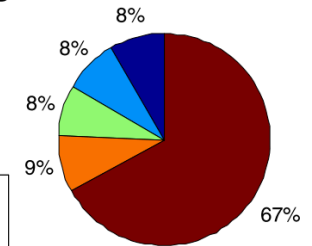
# A simulation approach may be useful in quantifying errors.



**Poisson ratio standard deviation**



**Young modulus standard deviation**



Examples of problem with leaving off different error sources in the simulation<sup>‡</sup>.

Ruben Balcaen, EM to be published.

# *Top-down versus bottom-up* uncertainty quantification approach<sup>†</sup>.

## *Top-Down Evaluation*

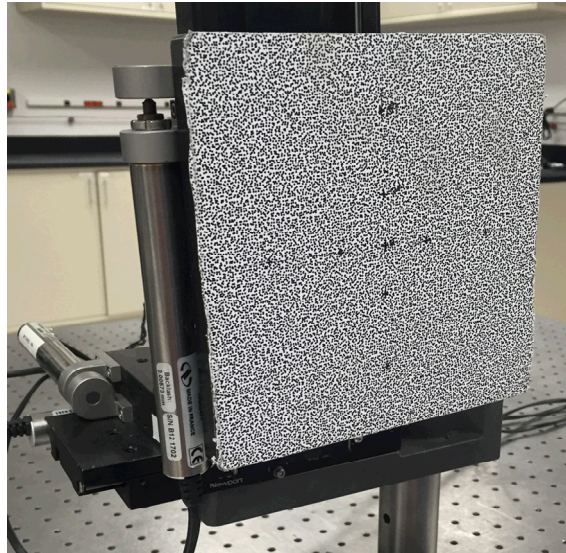
- Does not require study of contributing sources
- Inter-laboratory studies
- Comparisons with a standard
  - Displacement tests
  - Strain gages
  - Shape measurements

## *Bottom-Up Evaluation*

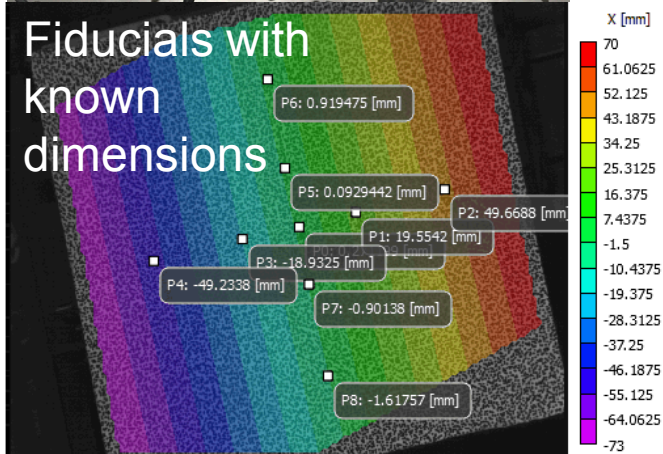
- Complete enumeration of all relevant sources of uncertainty.
- Description of their interplay and UQ influence.
- Characterization of contributions to uncertainty

# Top-Down evaluation attempts to quantify all the error sources “experimentally”

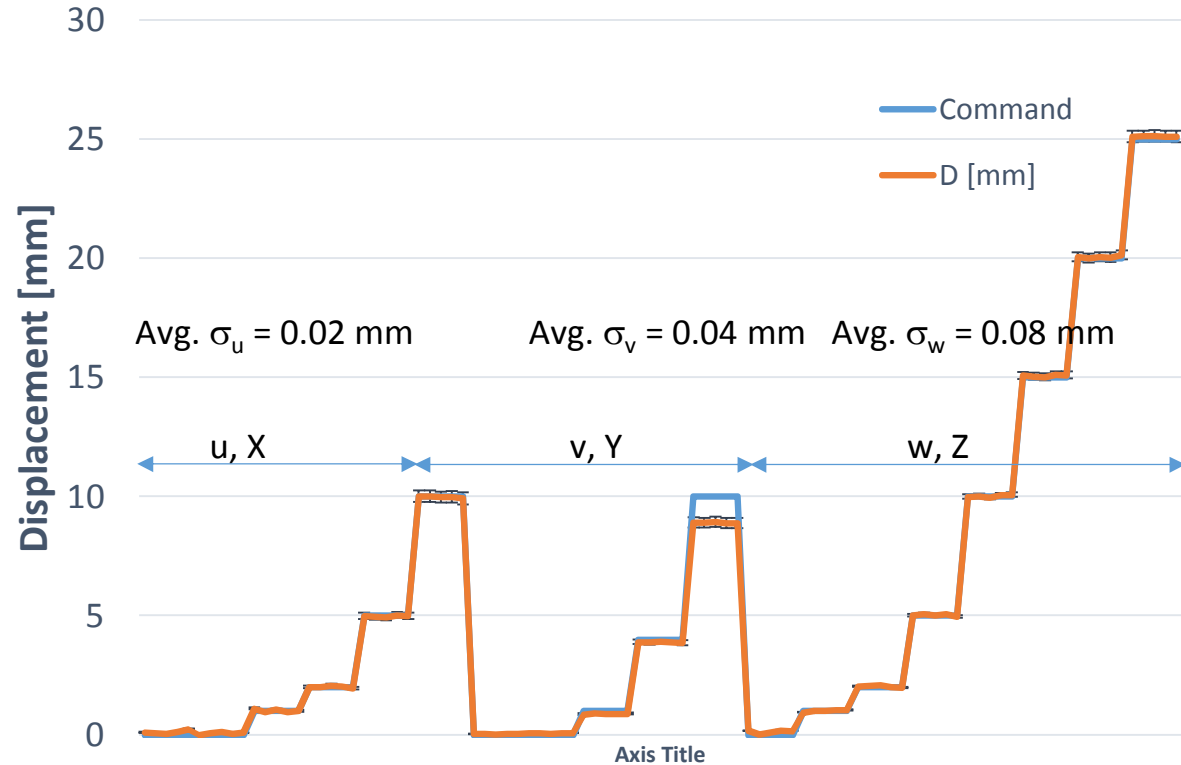
X, Y, Z Translation Stage



Fiducials with known dimensions



Translation Test



Bottom-up Methods: Compare DIC results to

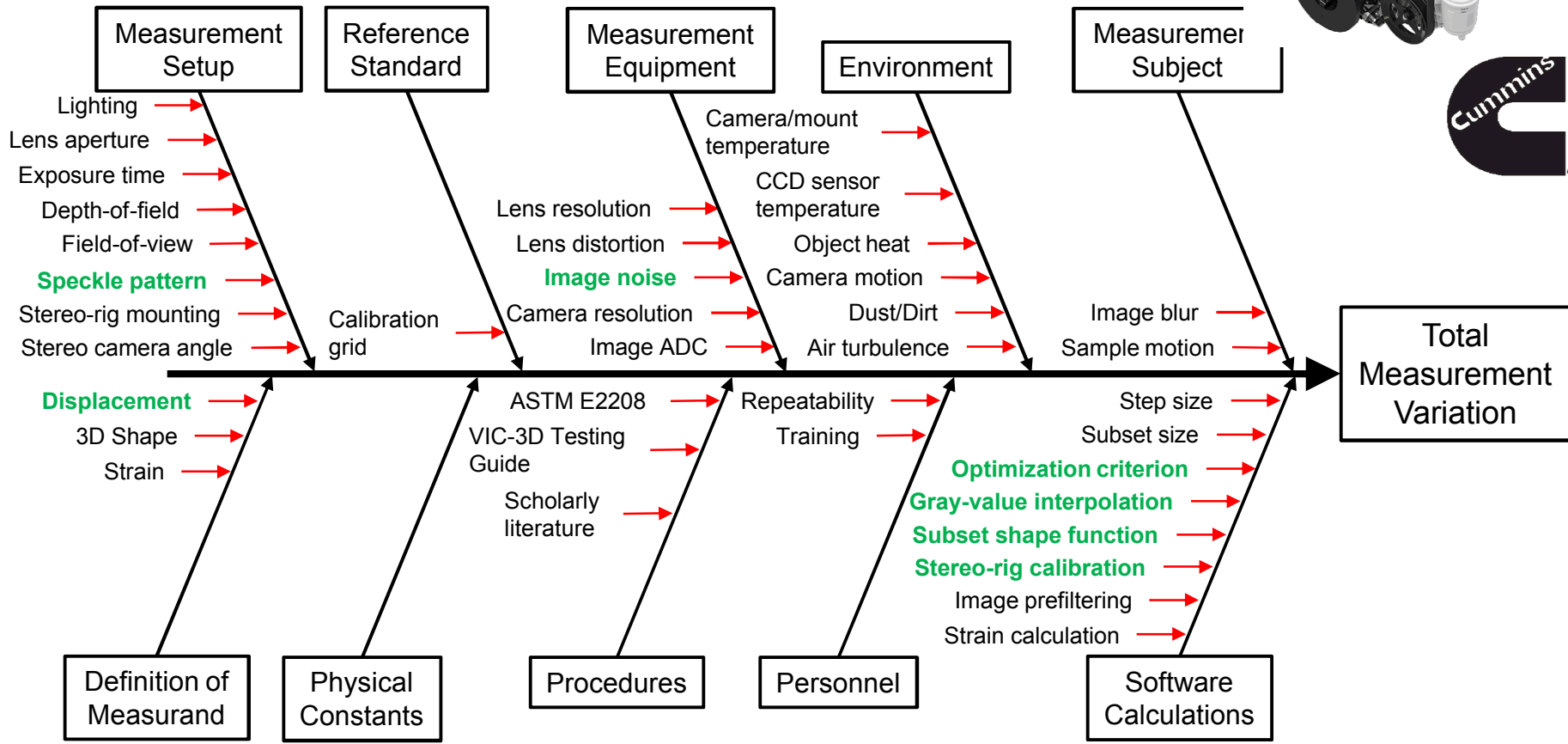
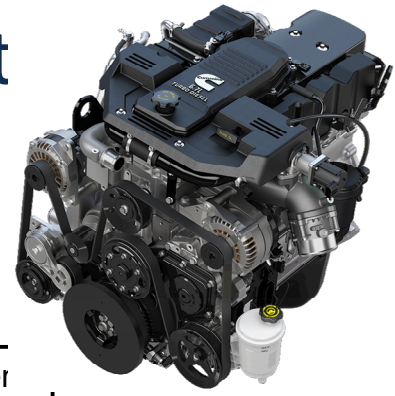
- Known shape measurements
- Known fiducial locations
- Known translations

# Bottom-up: Comprehensive list of errors

$$D = \sqrt{U^2 + V^2 + W^2}$$

2D Error Source	Type	Assessment Method/Comments	D  ≈ mm	D  ≈ pixels
Lens distortion	B	Previous calibration 100-mm Lens Not motion	<0.001	0.009
Camera motion	A,B	Stationary pattern – See later in slides	<0.02	0.18
Sample motion	B	Fixed target on table	0	0
Turbulence	A,B	This presentation for 50 C heat source	0.01 – 0.07	0.09 – 0.6
Image blur	B	Stationary	0	0
Resolution	B	Adequate pixel size	0	0
Image noise	A	Noise floor (5 frames at start of experiment)	0.001	0.009
Speckle contrast	A	Contrast ≈ 160 counts (Included in noise floor)	Noise floor	
Speckle size	B	Direct measure of speckle size ( $\mu=6.9$ ; $\sigma=1.2$ pixels)	Noise floor	
Aliasing	A,B	Noise floor (not aliased)	Noise floor	
Interpolant	B	Synthetic and experimental image studies for optimum	0.0001	0.0009
Minimization	B	DIC parameter study, synthetic and exp. image studies	0.0001	0.0009
Shape function	B	DIC parameter study, synthetic and exp. image studies	0	
Subset size	B	DIC parameter study, synthetic and exp. image studies	Noise floor	
Filtering	B	DIC parameter study		
Strain calculation	B	DIC parameter study		
Coord. system	B	Other means		

# The fundamental problem of DIC-UQ is that there are many variables to consider.

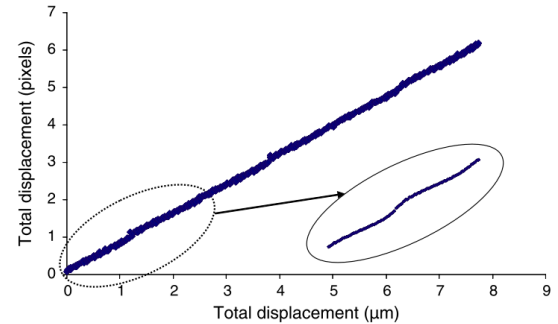


Jordan E. Kelleher, Paul J. Gloeckner, An Applications-Oriented Measurement System Analysis of 3D Digital Image Correlation, 2016 SEM Annual Conference & Exposition on Experimental & Applied Mechanics

# There were few (or no) experimental validations of the bias and noise error.

## Experimental validation is very hard!

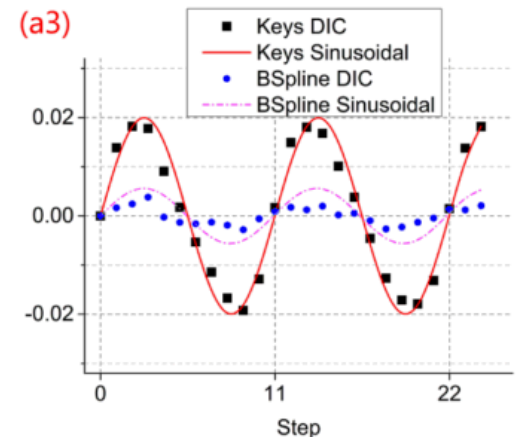
- Constant velocity test (leaves lots of questions)
- Super-resolution (next slides – still questions)
- Really expensive stages.
- Out-of-plane motion



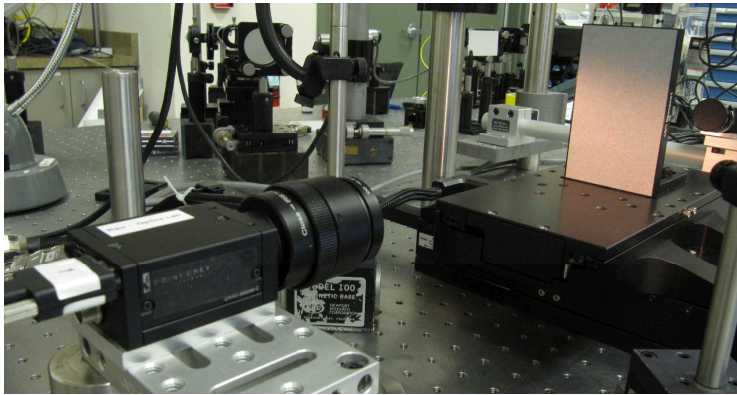
**Figure 8:** Measured horizontal image-based translation as a function of time. Measurements obtained using 2D digital image correlation with Point Grey camera images and a  $209 \times 209$  subset

Wang YQ, Sutton MA, Bruck HA, Schreier HW (2009). *Strain* 45 (2):160-178.

Su, Y., et al. (2015). *Optics Express* **23(15): 19242-19260.**



# In-plane translation test with high-precision stage.

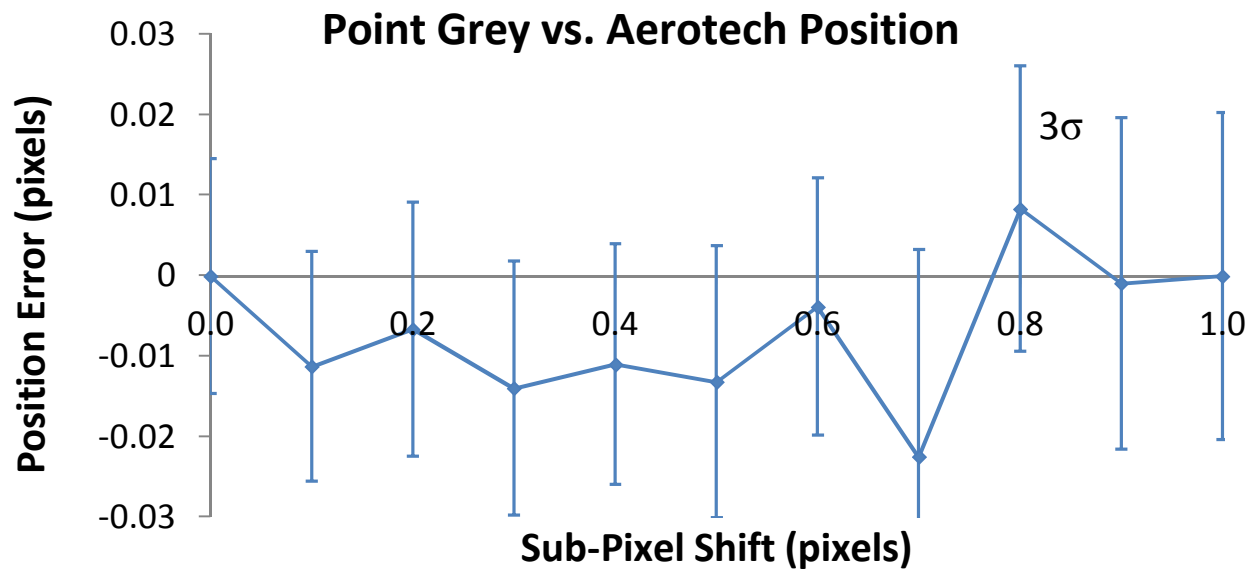


## Aerotech ultra-precision x-y stage

- $\pm 1$  nm encoder resolution (0.000 03 pixels)
- $\pm 21$  nm ( $3\sigma$ ) position stability (0.000 7 pixels)
- $\pm 75$  nm bi-directional repeatability (0.002 5)
- $\pm 300$  nm accuracy (0.01 pixels)

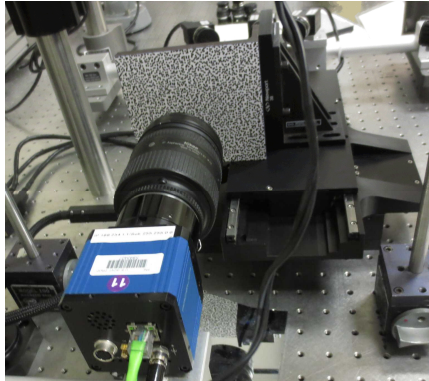
## Point Grey 5 MPixel cameras

- $29 \mu\text{m}/\text{pixel}$  or  $29\ 000 \text{ nm}/\text{pixel}$
- Stage error max. 6 nm or 0.000 2 pixels
- Pixel noise  $\approx 2.3$  counts ( $1\sigma$ ) 0.9%

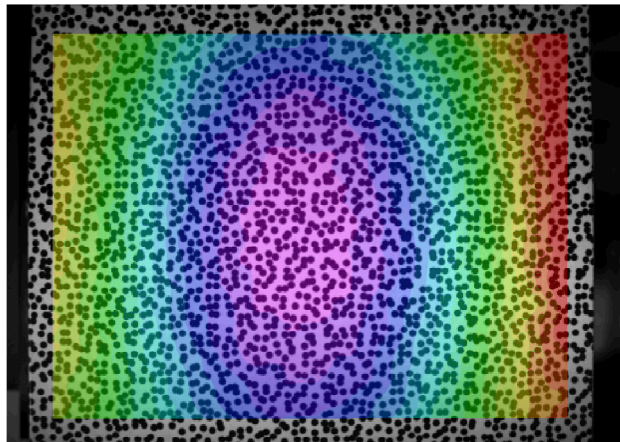
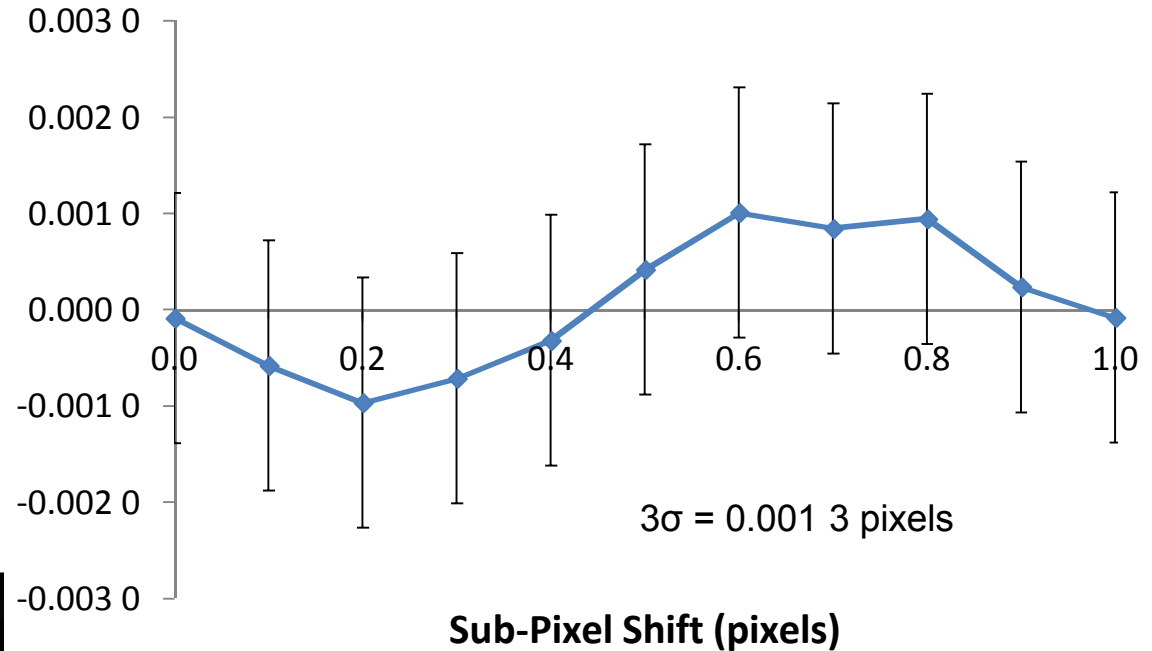


**Variance errors dominate bias errors!**

# An experimental demonstration of the interpolation bias error using in-plane translation.



Position Error (pixels)

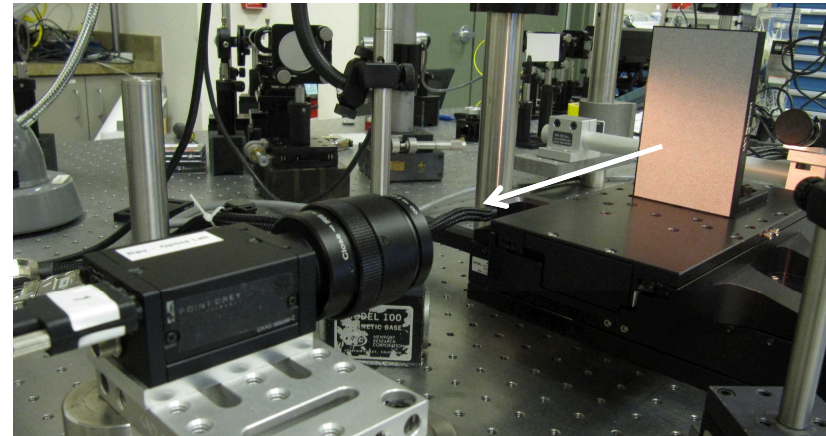
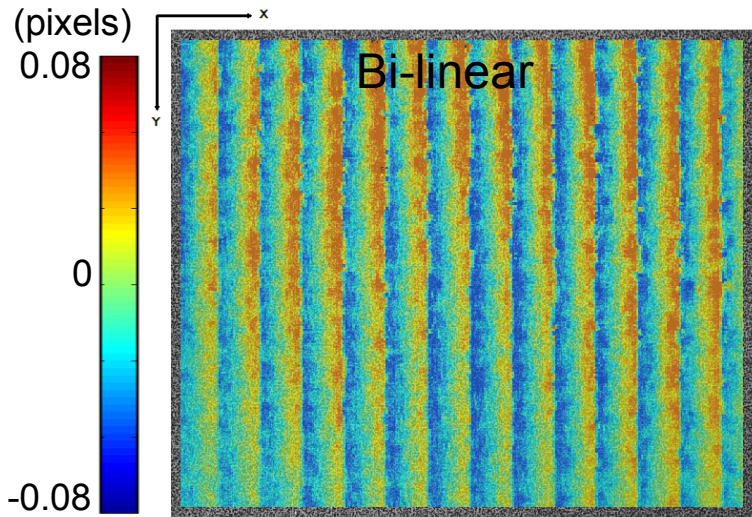


## Prosilica 14-MPixel (binned x10)

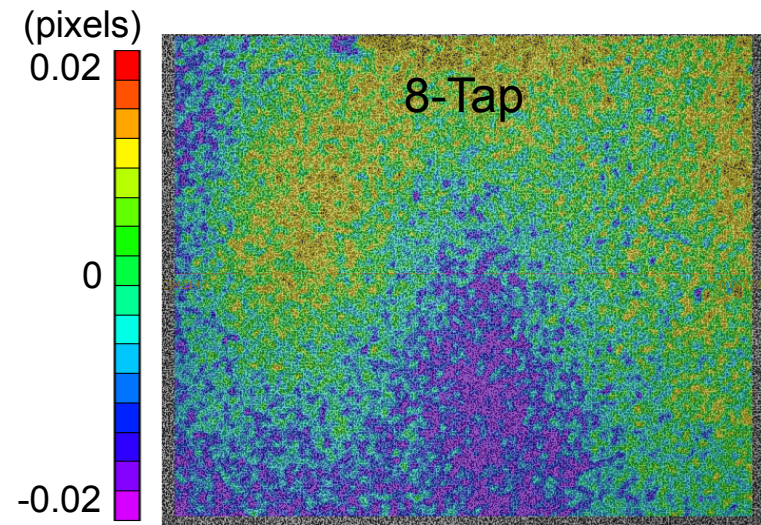
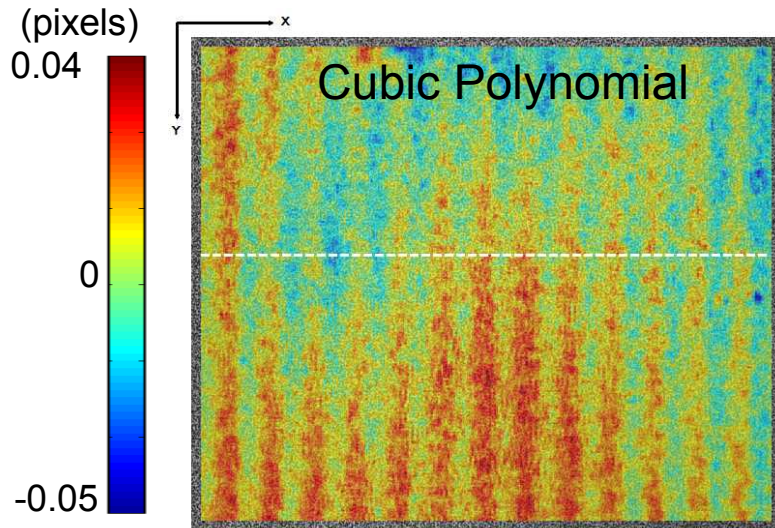
- 335  $\mu\text{m}/\text{pixel}$  or 335 000 nm/pixel
- Stage error max. 6 nm or 4e-6 pixels
- Pixel noise  $\approx$  0.26 counts ( $1\sigma$ ) 0.1%

**At this point – The lens distortion started to contribute.**

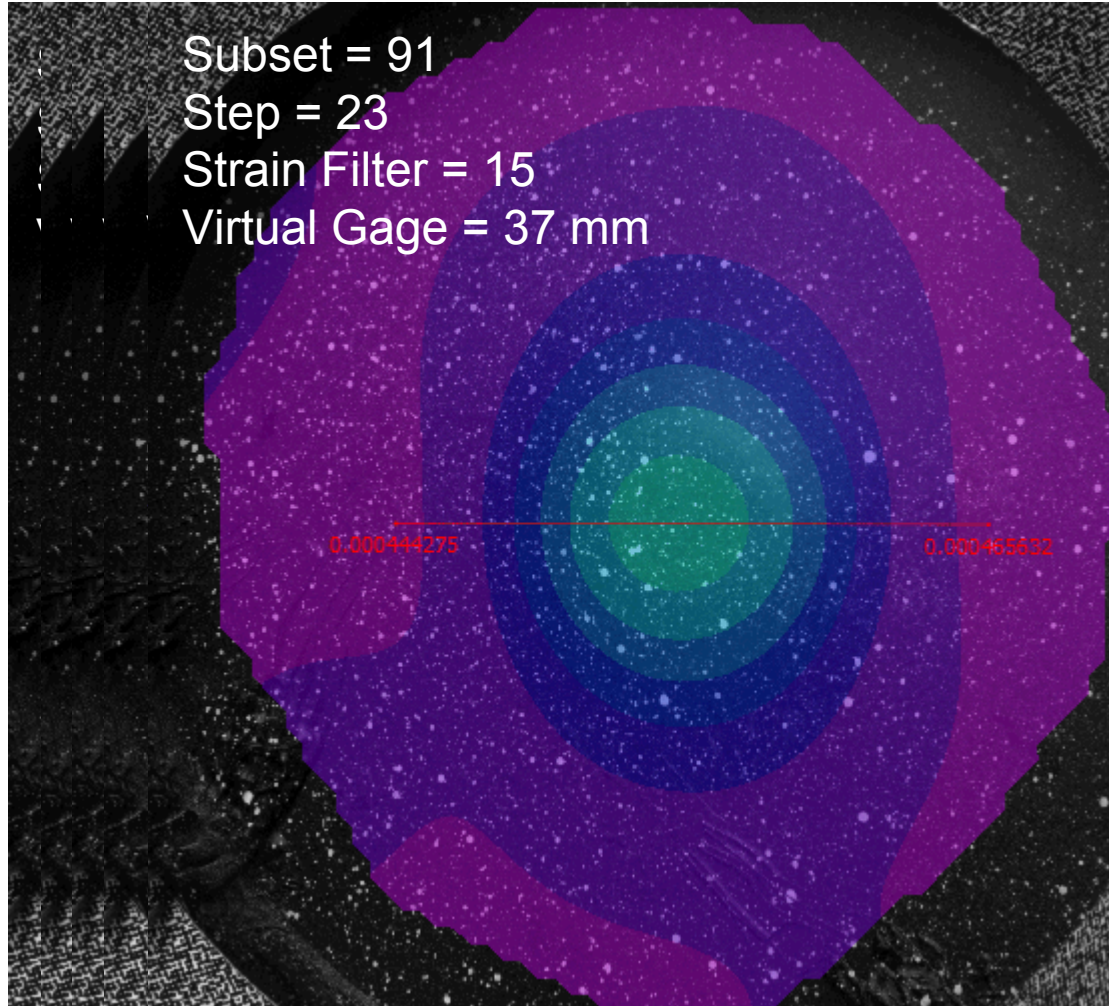
# The bias error is much easier to find with out-of-plane motion.



**This simulates a biaxial strain, but uniaxial would cause the same issues!**



# The user is a weak link in the system. Training!



exx [1] - Lagrange



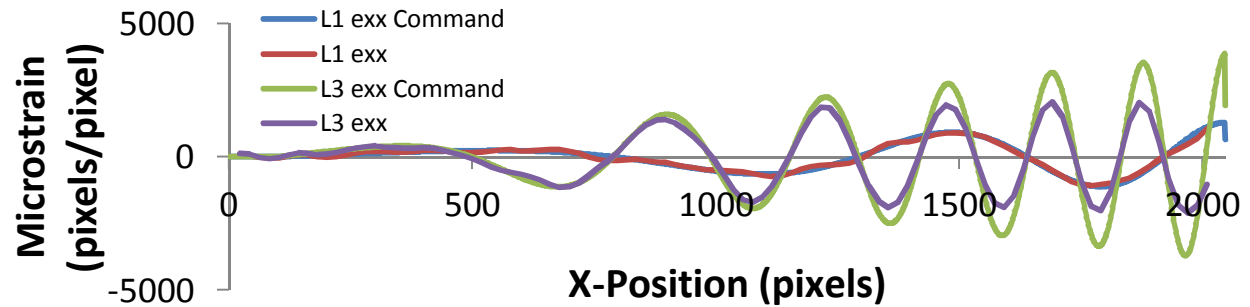
## Virtual strain gage size study

- Varying processing parameters and studying the results!

# The DIC community needs, training, standardization and guidelines.

- Publication requirements to provide important DIC information.
- A real definition of spatial resolution is needed.
- Improved training beyond vendor provided – and agnostic of DIC software.
- A society dedicated to training and DIC standards.

Strain	
Smoothing technique	Local polynomial - affine
VSG	10 data points, 8.5 mm
Spatial resolution	111 pixels, 9.4 mm
Resolution	$2.3 \cdot 10^{-4}$



THE ART AND APPLICATION OF DIC

**Calibration: Stereo Calibration**

by Phillip Reu

*Developments, Applications and Tutorials in Experimental Mechanics Techniques*

**EXPERIMENTAL TECHNIQUES**

**DIC course**  
Metrology beyond colors



**iDICS** INTERNATIONAL  
DIGITAL IMAGE CORRELATION  
SOCIETY

[www.idics.org](http://www.idics.org)



## Annual International DIC Society Conference November 6 – 9, 2017 in Barcelona Spain

<http://idics.org>

### iDICS Board

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Daniel Turner

Wei-Chung Wang

### General Call

The International Digital Image Correlation Society (iDICS) is inviting your participation in its annual conference in Barcelona Spain. We welcome you to join this society aimed at inspiring their members to continually improve their application and development of image correlation methods. The board invites you to join in presenting, organizing sessions, and participating in the active committees to help guide DIC into the future.

### Active Committees

- Applications (Chair: Dave Dawicke)
- University Education (Chair: Mark Pankow)
- Training & Certification (Chair: Tim Schmidt)
- Standards & Best Practices (Chair: Mark Iadicola)

### Monday Courses (November 6)

- To be determined

### Mission: Extend – Improve – Train

Extending the Frontiers: Training the next Generation:  
Standardizing for Industry: Improving our Practice

### Important Dates

Abstract due July, 2017

Early Registration until Sept. 1