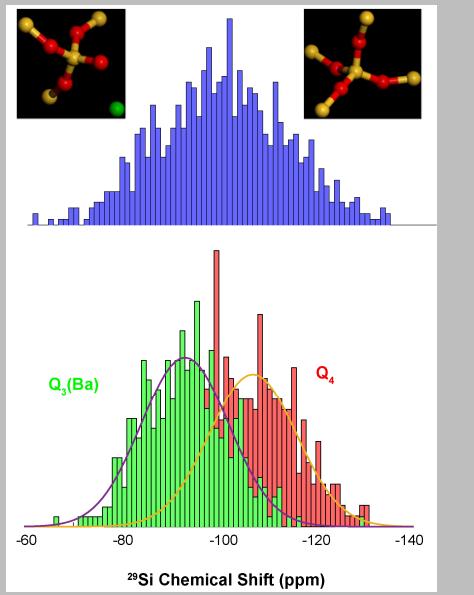


# Connecting NMR Spectroscopy Results and MD Simulations of Barium-Silicate Glasses



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and Blake A. Hammann

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Glass and Optical Materials Division Meeting

Madison WI

May 24th, 2016



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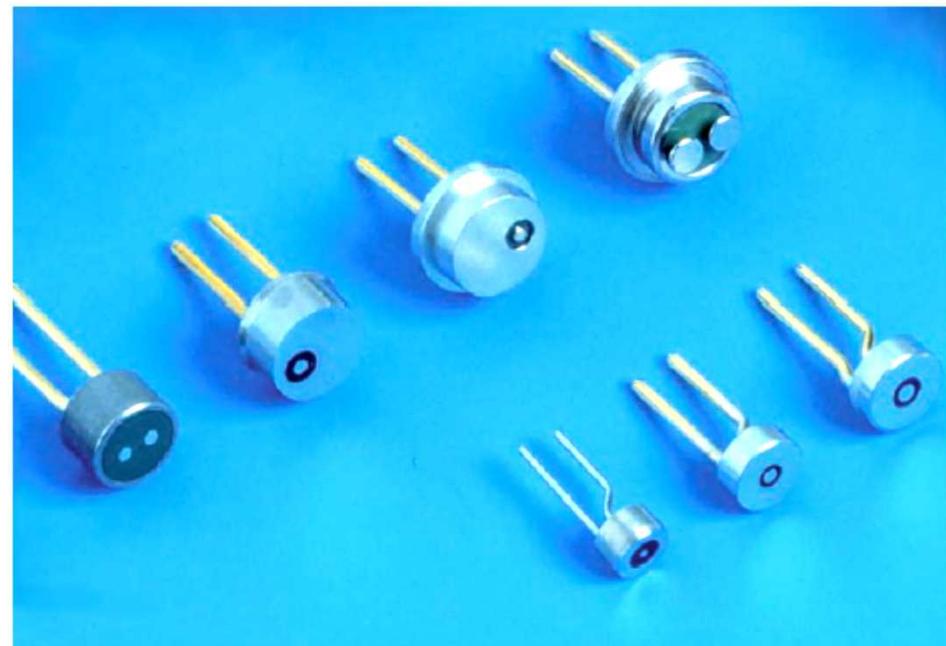
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# Glass is Used to Bond/Join Materials

## Sandia's Interest

### Glass-Bonding/Joining Applications

- **Glass-Bonded Composites**
  - Glass bonded alumina
  - Low temperature co-fired ceramic (LTCC) electronic packaging
- **Seals**
  - Hermetic glass to metal (Gtm) seals
    - Air bag motors
    - Medical implants
    - Microelectronics
  - Energy Conversion
    - Solid oxide fuel cells (SOFCs)
    - Concentrated solar



# Filled Glass Composite (FGCs)

## Glass Processability with Properties of a Ceramic

### Glass

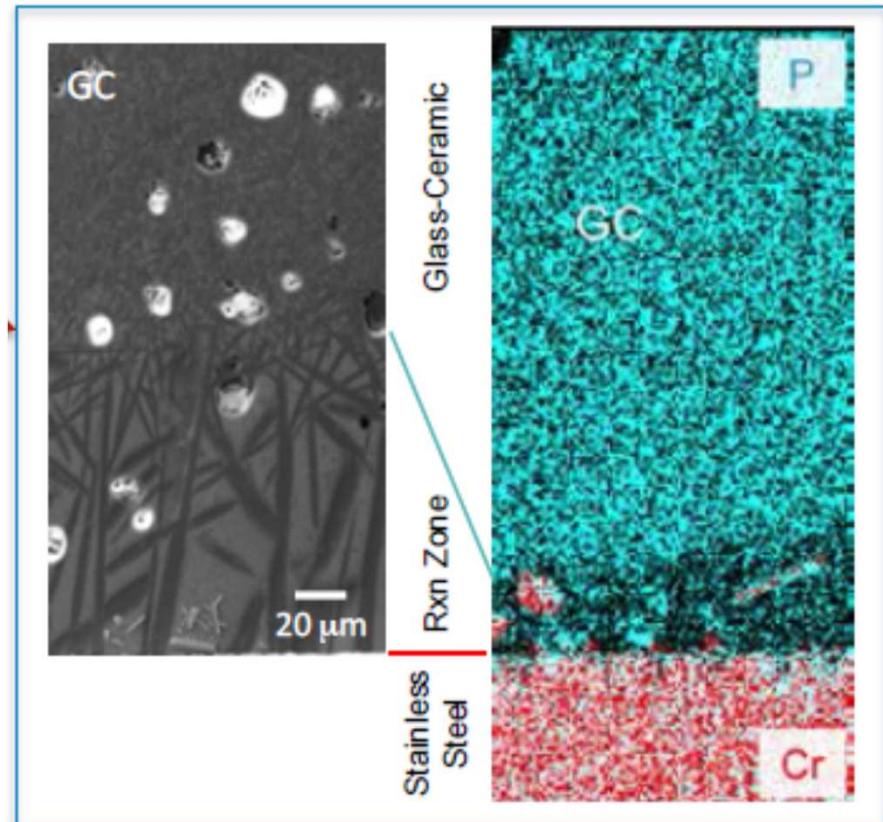
- Processability
- Materials Compatibility
- Low/Fixed CTE
- Low Toughness/Crack Tolerance

### Glass-Ceramic (GC)

- Toughness/Crack Tolerance
- High/Tunable CTE
- Process Sensitivity
- Reactivity/Instability

### Filled Glass Composite (FGC)

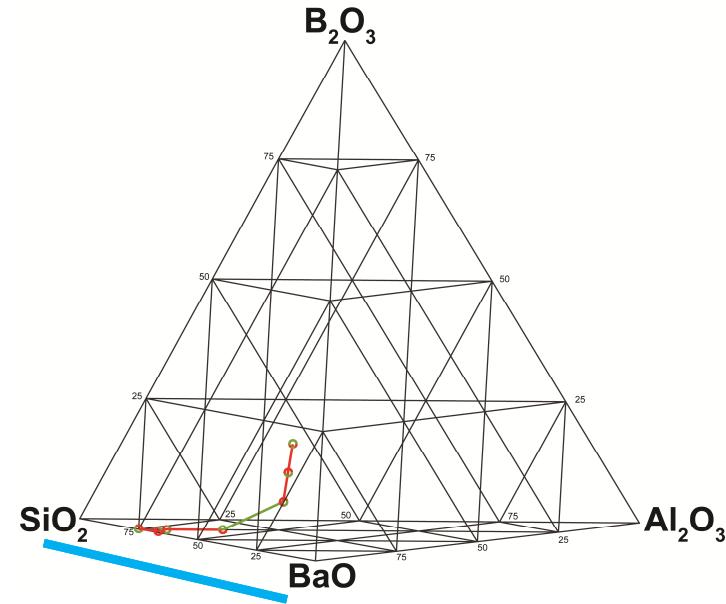
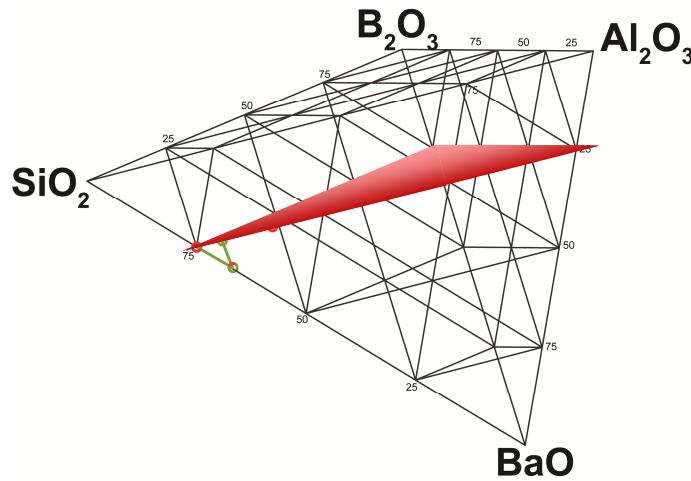
- Process Robustness
- Toughness/Crack Tolerance
- Low to High/Tunable CTE
- Chemical/Structural Stability



### *Related Sandia Presentations*

Kevin Strong May 24<sup>th</sup> 11 AM: "Characterizing and Predicting Stress and Structural Relaxation in Glass"

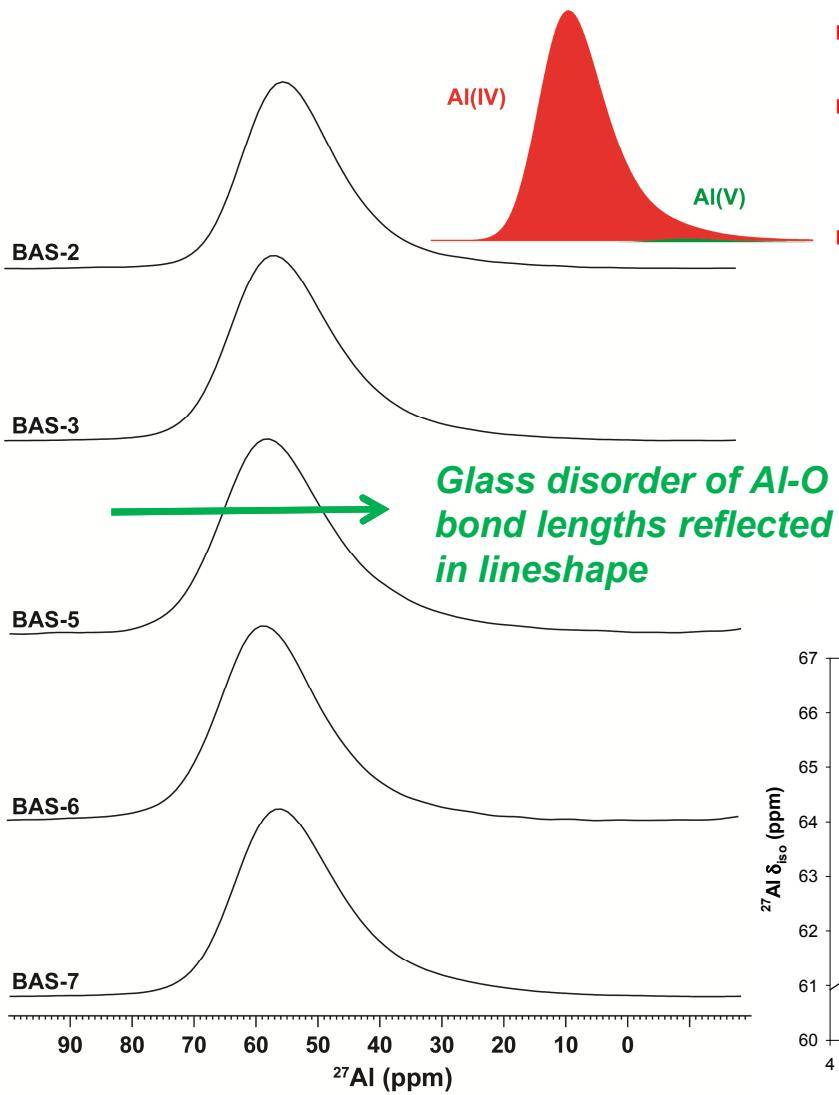
# Characterization and Modeling of Chemistry-Structure-Property Relationships



Initial Studies on Simple Boron-Aluminum Modified Barium-Silica Glass  
 $x\text{BaO}-y\text{Al}_2\text{O}_3-z\text{B}_2\text{O}_3-(100-x-y-z)\text{SiO}_2$

Sample	BaO	SiO <sub>2</sub>	Al <sub>2</sub> O <sub>3</sub>	B <sub>2</sub> O <sub>3</sub>
BAS-1	25.0	75.0	0.0	0.0
BAS-8	33.3	66.7	0.0	0.0
BAS-3	25.0	60.0	15.0	0.0
BAS-5	25.0	46.0	23.0	6.0
BAS-6	25.0	42.0	21.0	12.0
BAS-7	25.0	38.0	19.0	18.0

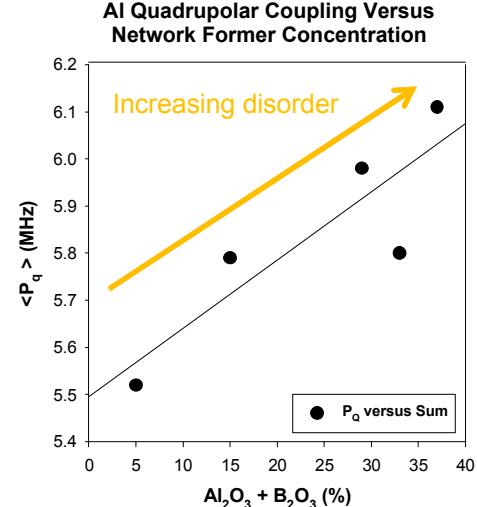
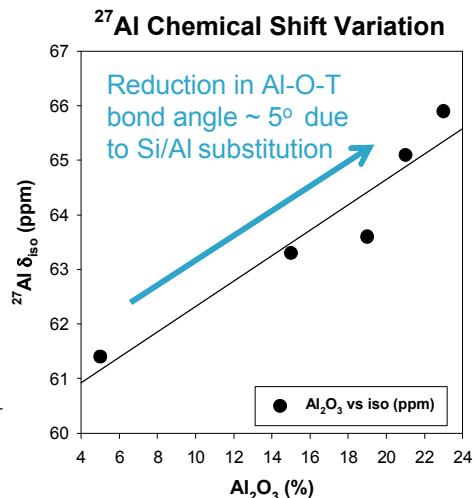
# Characterization – $^{27}\text{Al}$ MAS NMR



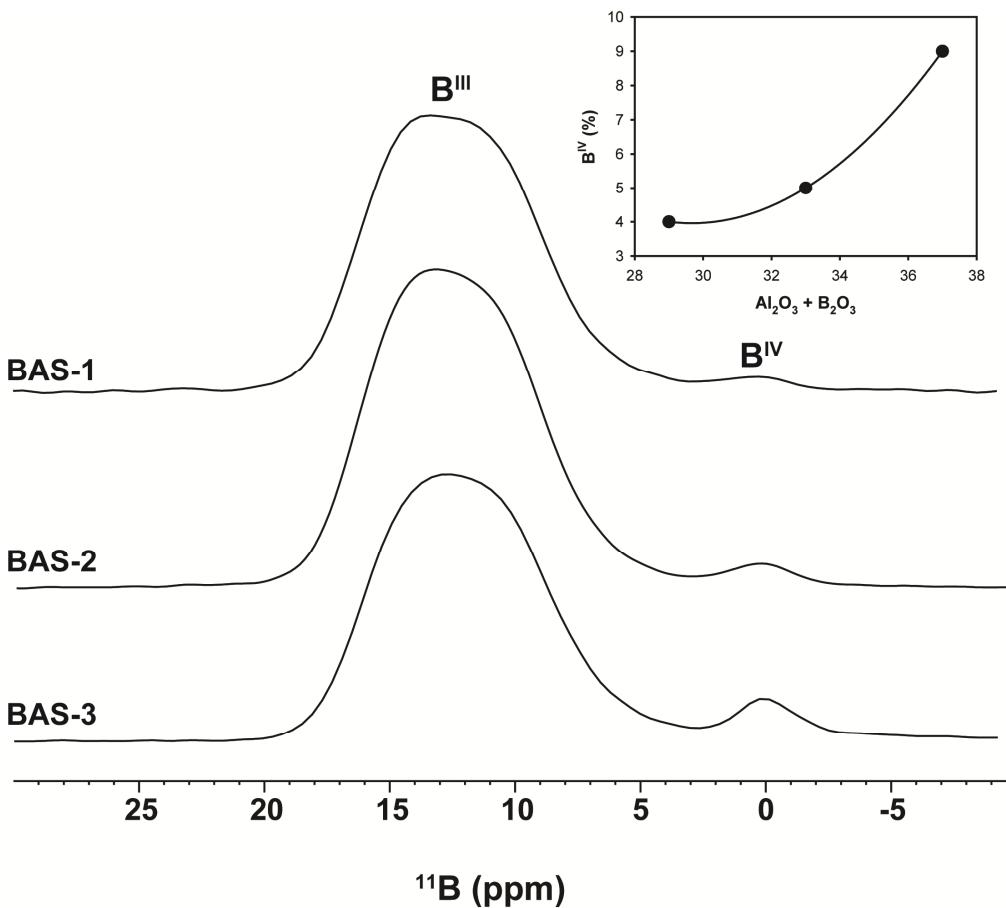
- Predominantly  $\text{Al}^{\text{IV}}$  coordination (> 98%).
- Distribution of local environments reflected in  $^{27}\text{Al}$  EFG tensor.
- No significant change in local coordination with variation in modifier and network former concentration.

## Czjzek Probability Distribution Function

$$P_Q(v_Q, \eta) = \frac{1}{\sqrt{2\pi}\sigma^5} v_Q^4 \eta \left(1 - \frac{\eta^2}{9}\right) \exp\left[-\frac{v_Q^2 \left(1 + \frac{\eta^2}{3}\right)}{2\sigma^2}\right]$$

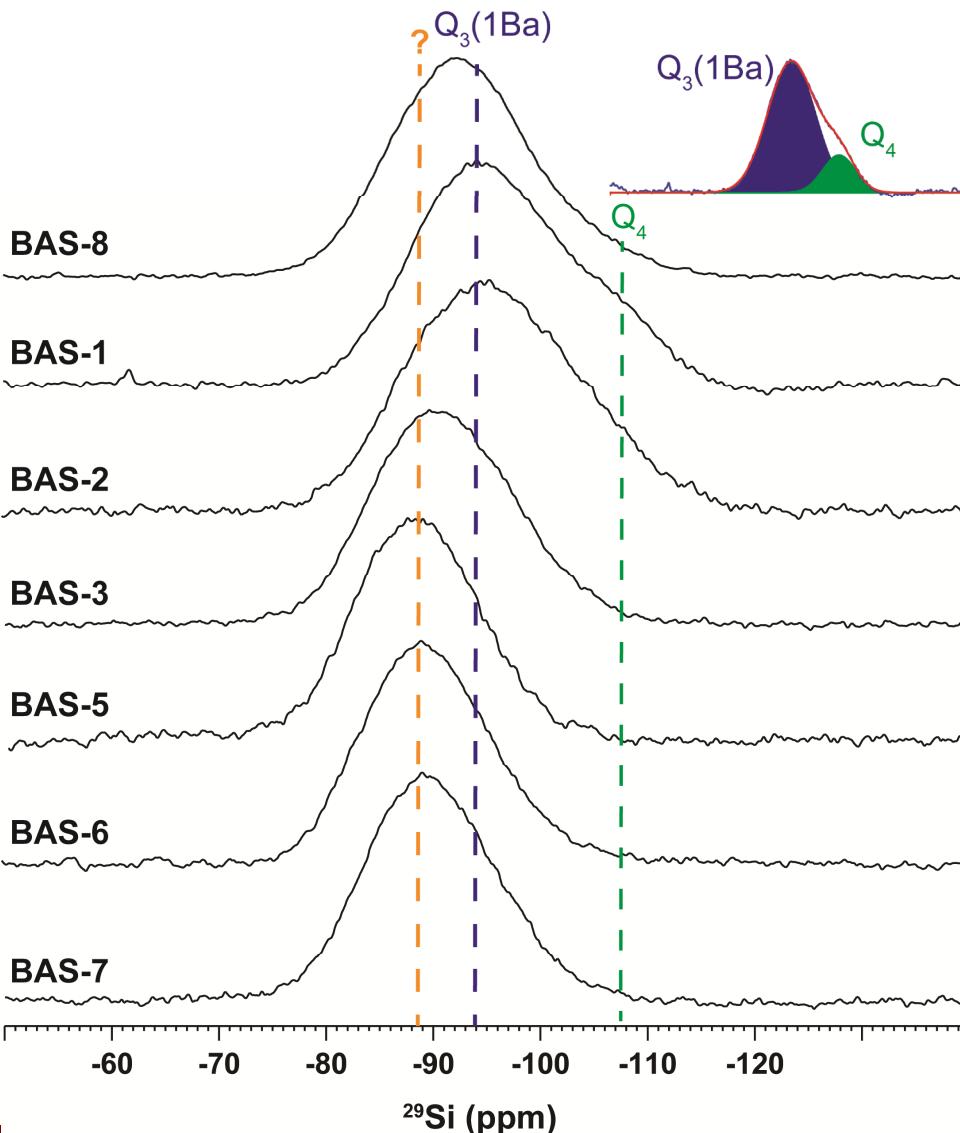


# Characterization – $^{11}\text{B}$ MAS NMR



- Trigonal  $\text{B}^{\text{III}}$  coordination (> 90%).
- Slight increase of  $\text{B}^{\text{IV}}$  with increasing  $\text{B}_2\text{O}_3$  concentration.
- No significant change in local coordination with variation in modifier and network former concentration.

# Characterization – $^{29}\text{Si}$ MAS MMR

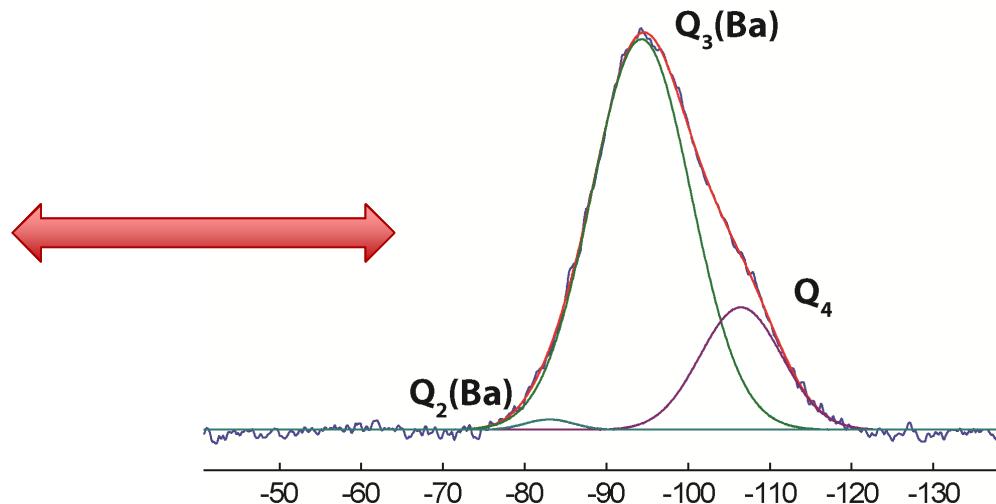
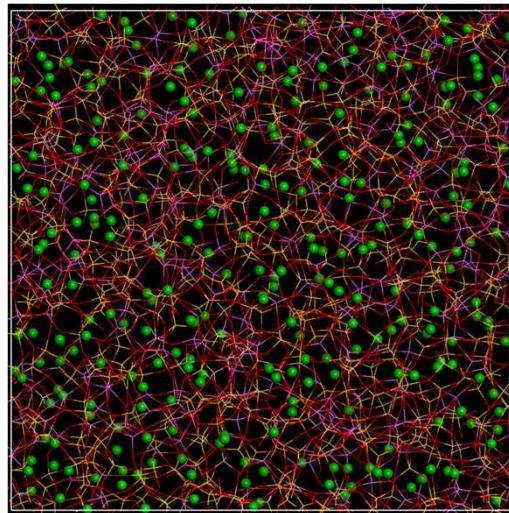


- Changes in the local  $\text{SiO}_4$  coordination with different  $\text{Q}_n$  speciation.
- Not well resolved and a gradual shift in  $\delta_{\text{Si}}$  with increasing  $\text{Al}_2\text{O}_3 + \text{B}_2\text{O}_3$  concentrations.
- Al and B in 2<sup>nd</sup> coordination sphere producing a chemical shift change.
- Low resolution seen in other Ba and Ca silicate glasses.

***Motivation for to incorporate results from MD simulation to understand and extract some of these trends.***

# Connecting MD Simulations and NMR

BAS-3

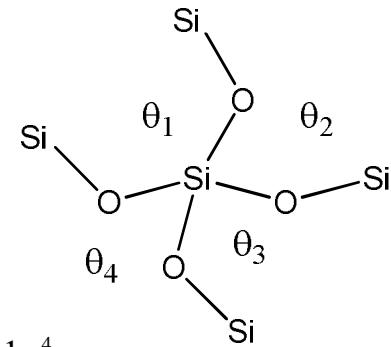


- Goal is to calculate NMR parameters from MD simulations.
- Experimental test of MD simulations.
- Allows assignment of NMR results for different nuclei.
- Can ask question about *specific* next nearest neighbor interaction (Al-O-B, Al-O-Si).
- Explore unique conditions and predict NMR (experimental changes?).
- Possibility to provide feedback for development of force-fields. [1]

[1] Gambuzzi *et al.* *Geochimica Cosmochimica Acta* (2014) 125, 170-185. Combined CASTEP feedback for MD simulations of Ca-SiO<sub>2</sub>-Al<sub>2</sub>O<sub>3</sub> glasses.

# Approaches: Empirical NMR Correlations

- Prediction of chemical shifts based on local structural parameters: bond lengths, bond order, bond angles, coordination number (CN).
- Original correlation developed from crystalline model compounds.
- Example include  $^{17}\text{O}$ ,  $^{23}\text{Na}$ ,  $^{29}\text{Si}$ ,  $^{27}\text{Al}$  NMR chemical shift calculations.
- $^{29}\text{Si}$  NMR correlations well developed (many different examples), and used to extract Bond Angle Distributions (BAD) in amorphous  $\text{SiO}_2$ .
- Many not expandable to different cation, CN, or  $Q_n$ !
- Require development of multiple correlations!
- **How do you treat the impact of low concentration species?**
- **Is it possible to develop a more empirical relationship?**



$$\delta(^{29}\text{Si}) = \frac{1}{4} \sum_{n=1}^4 F_{ac}(\theta_n)$$

$$F_{ac}(\theta) = -93.12 + 8.66 \cos \theta - 22.27 \cos 2\theta$$

Mauri et al. (2000) Phys. Rev. B, 62, R4786

$$\delta_{TMS} = \frac{1}{4} \sum_{n=1}^4 F_{b_n}(\theta_n), \text{ with } F_{b_n=B}(\theta) \text{ or } F_{b_n=Si}(\theta)$$

$$F_B(\theta) = -42.63 - 24.81 \cos \theta - 18.20 \cos 2\theta$$

$$F_{Si}(\theta) = -31.21 - 10.05 \cos \theta - 11.52 \cos 2\theta$$

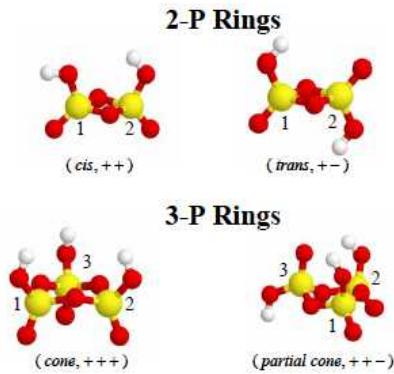
Soleilhavoup et al. (2010) Mag. Res. Chem., 48, S159-S170

$$s_i = \left( \exp \left[ (r_0 - r_i) / 0.37 \right] \right)$$

$$\Omega = \sum_{i=1}^N \left[ s_i \left( 1 - 3 \cos^2 \theta_i \right) / 3R_i^3 \right] \log D_i$$

$$\delta(^{29}\text{Si}) = 701.6\Omega - 45.7$$

# Approaches: Quantum Calculations - Clusters



T. M. Alam "Ab Initio Calculations of  $^{31}\text{P}$  NMR Chemical Shielding Anisotropy Tensors in Phosphates: Variations Due to Ring Formation", Int. J. Mol. Sci., 3, 888-906 (2002).

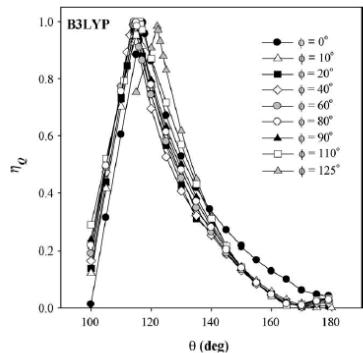
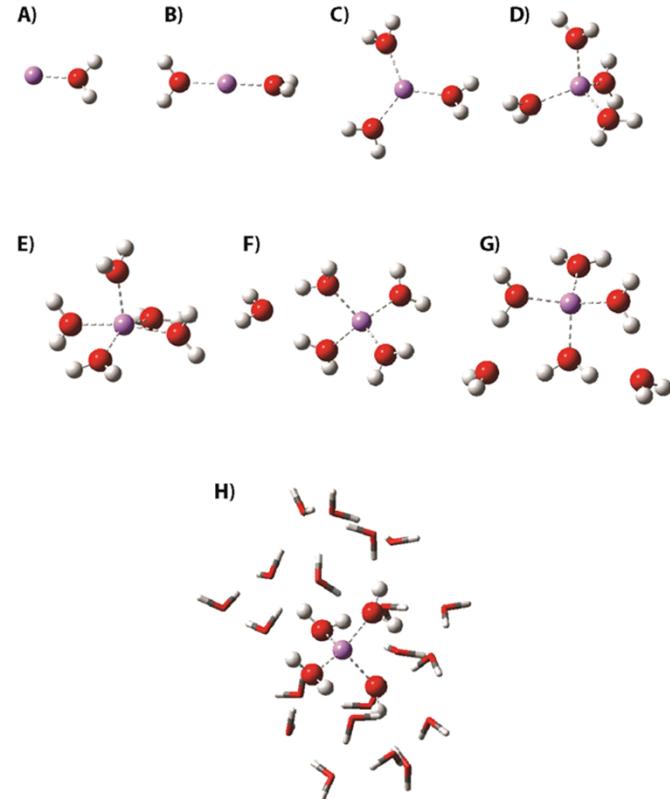


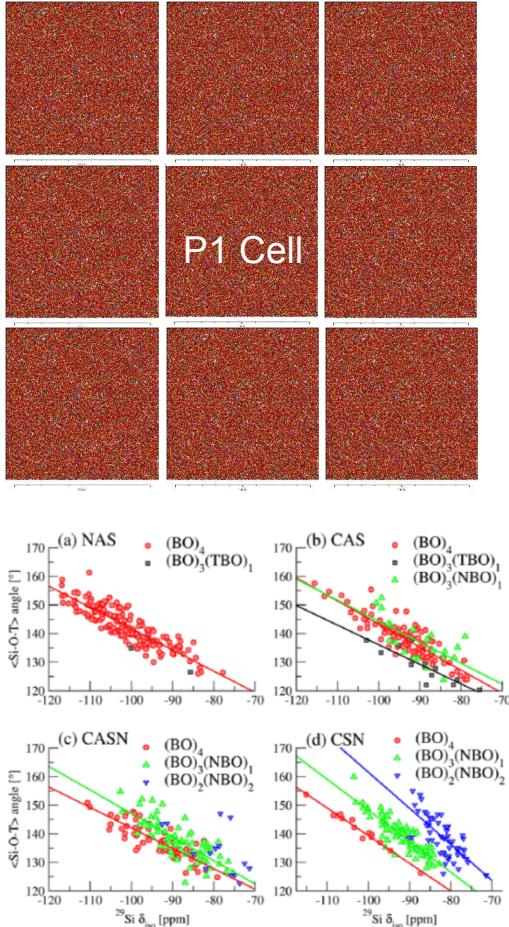
Fig. 3. Variation of the  $^{17}\text{O}$  EFG  $\eta_Q$  as a function of the P–O<sub>Q</sub>–P bond angle ( $\theta$ ) for the bridging oxygen in the  $\text{H}_3\text{P}_2\text{O}_7$  cluster are shown. The calculated values for different  $\phi$  configurations are shown for the B3LYP level of theory (See Fig. 1 for definition of the angles).

T. M. Alam and J. M. Segall, "Structural Perturbations on the Bridging Oxygen  $^{17}\text{O}$  NMR EFG Parameters in Ultraphosphates: An Ab Initio Study", J. Molecular Structure, 674, 167-175 (2004).



T. M. Alam, D. Hart, S. L. B. Rempe, "Computing the  $^7\text{Li}$  NMR Chemical Shielding of Hydrated  $\text{Li}^+$  using Cluster Calculations and Time-Averaged Configurations from *ab initio* Molecular Dynamics Simulations", *Physical Chemistry Chemical Physics*, 13, 13629-13637, (2011).

# Approaches: GIPAW Calculations - Periodic

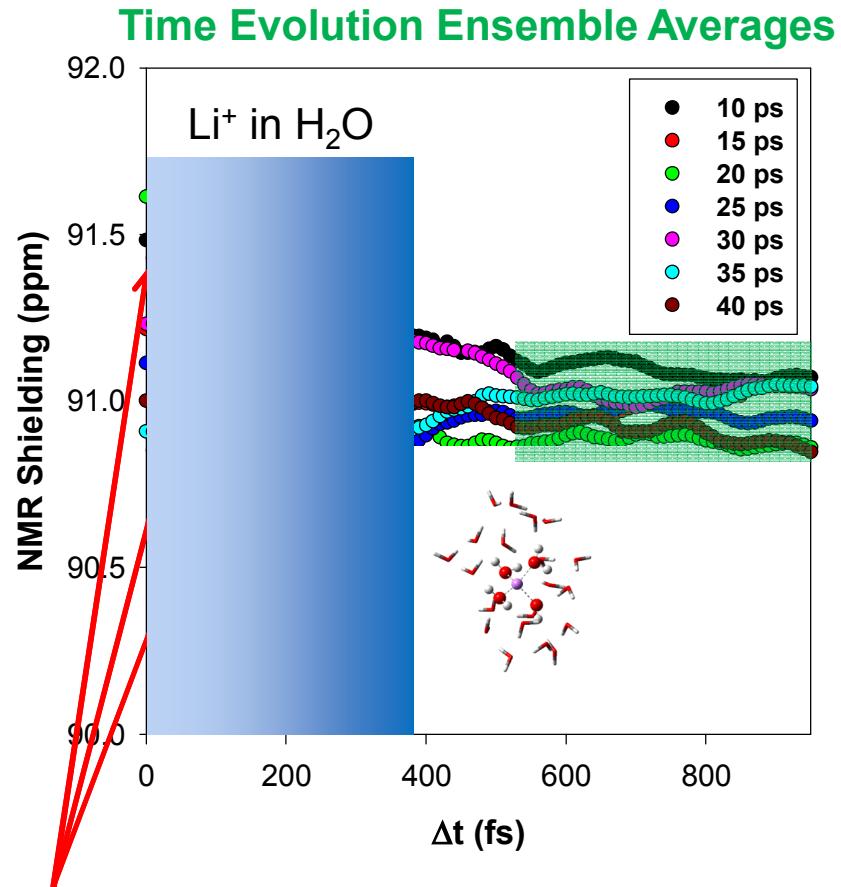


- **GIPAW** (Gauge Including Projector Augmented Wave) method allows direct calculation of NMR tensors in periodic systems. Really developed for crystalline materials – but can be extended to include primitive P1 cells like MD simulations.
- ***State of the art for NMR of glass simulations!*** No need for model systems, no needs for cluster extractions – direct quantum level calculations of ALL nuclei.
- Most commonly Implemented in CASTEP program (\$\$, UK).
- Computational expensive – as MD cell size (**limited**) increases calculation becomes very time consuming (impacts on averaging).
- More recent examples in glass use smaller P1 cells and develop empirical relationships....**future direction!**

# Issues: Extraction of Average Chemical Shifts from MD

- Time and ensemble averaging over the configurations obtained during MD simulations can provide a more accurate result in calculation of the NMR chemical shift.
- Typically, need to average the NMR shielding over an “appropriate” time scale (auto correlation time) for the NMR observable.
- This time scale is NOT known *a priori*.
- NMR time scale is NOT the same as the decay time for the energy auto correlation function.
- May require thousands of calculations to simply determine the appropriate NMR time scale.
- Long term fluctuations may not be captured in a simple auto correlation averaging. This may not be an issue for small molecules, but could represent an issue for large complexes or surface adsorption.

T. M. Alam, D. Hart, S. L. B. Rempe, "Computing the  ${}^7\text{Li}$  NMR Chemical Shielding of Hydrated  $\text{Li}^+$  using Cluster Calculations and Time-Averaged Configurations from *ab initio* Molecular Dynamics Simulations", *Physical Chemistry Chemical Physics*, **13**, 13629-13637, (2011).



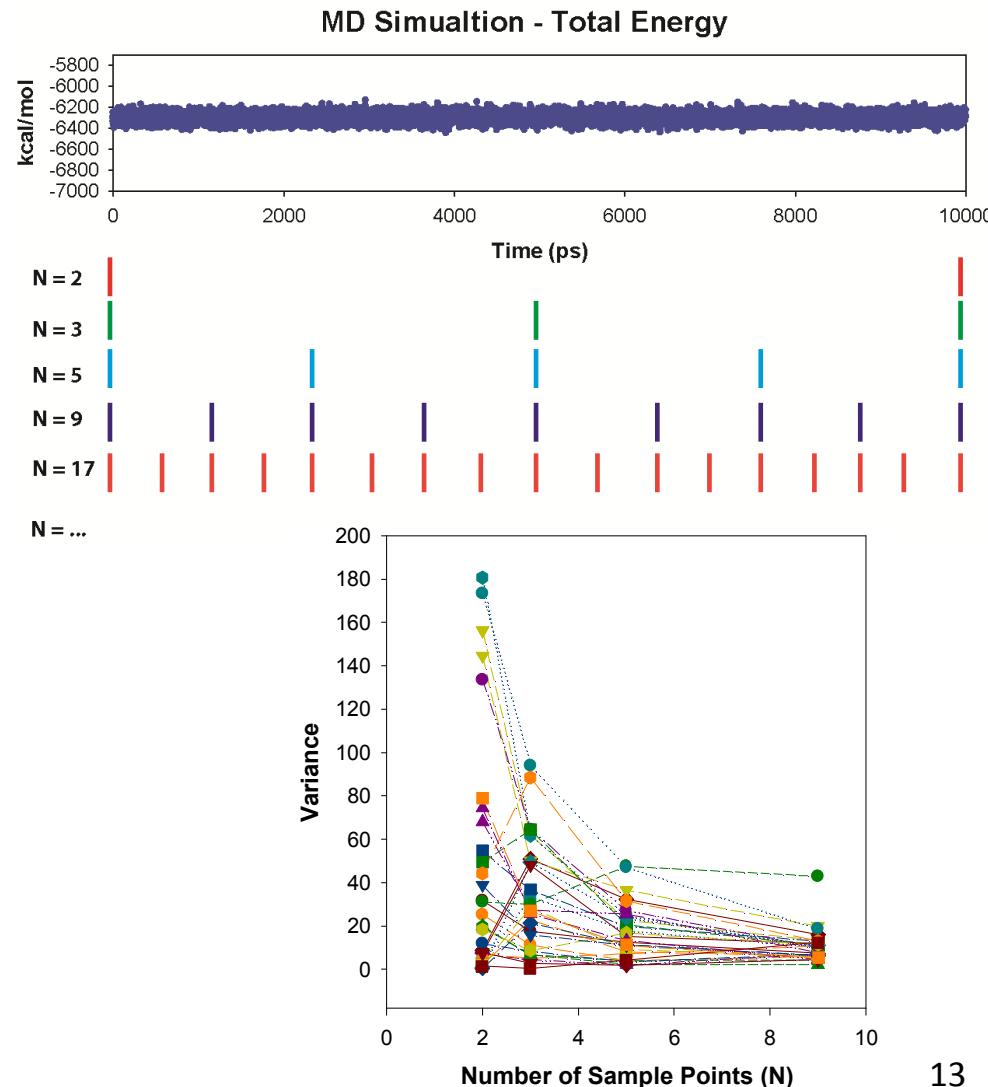
Even the **ensemble** averages (64 Li) vary on starting time slice!

Time period to approach local average chemical shift.

Finally converge on a similar NMR chemical shift.

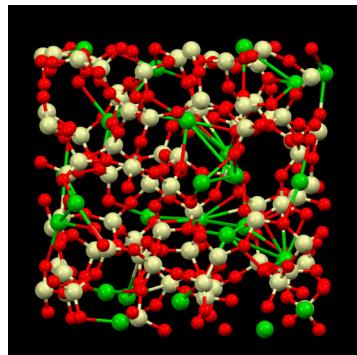
# A Solution: Extraction of Chemical Shifts from MD Simulations

- Implemented a “**halving**” sampling method to improve the speed and performance of the time and ensemble averaging of the NMR calculations.
- By monitoring the variation of the standard deviation it is possible to determine when enough sampling points have been averaged.
- Sample over the entire time series, incorporates longer term fluctuations.
- Continue to develop this interface to improve the speed and compatibility with MD simulations from different sources.
- **Still requires calculation from multiple time slices to obtain a representative chemical shift prediction.**
- **Need to consider computational speed limitations!**



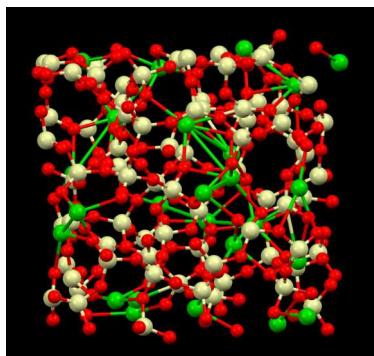
# Issues: Calculation Time and Statistics

275 atoms



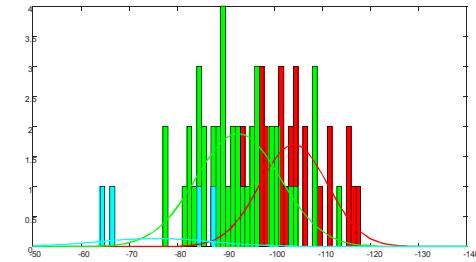
MD Snap Shot  
(Energy Relaxed)

Plane Wave  
Periodic  
Structure Calculation  
→  
~ 1 week  
calculation



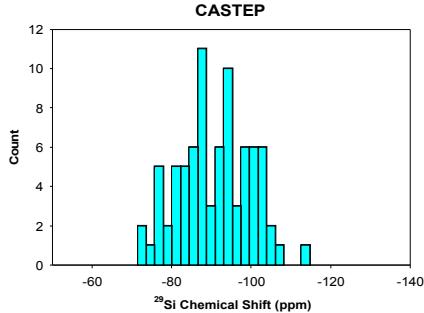
Geometry Relaxed

Empirical  
NMR Shielding  
Calculation  
(~ 1 s)  
→

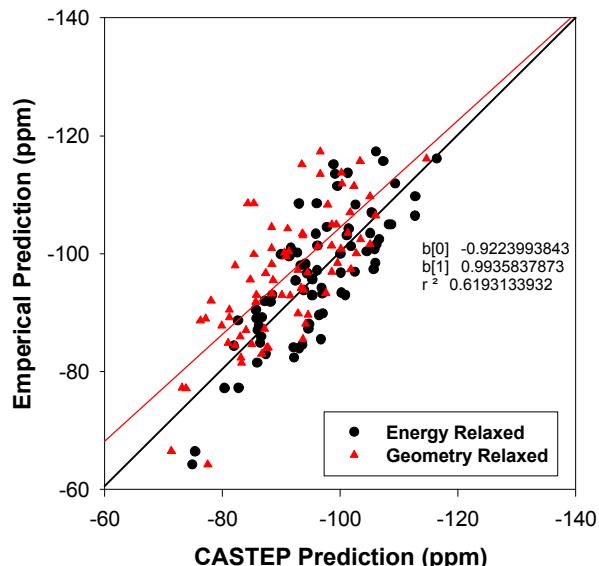


GIPAW CASTEP  
NMR Shielding  
Calculation  
(~ 1 day)

75 Si atoms

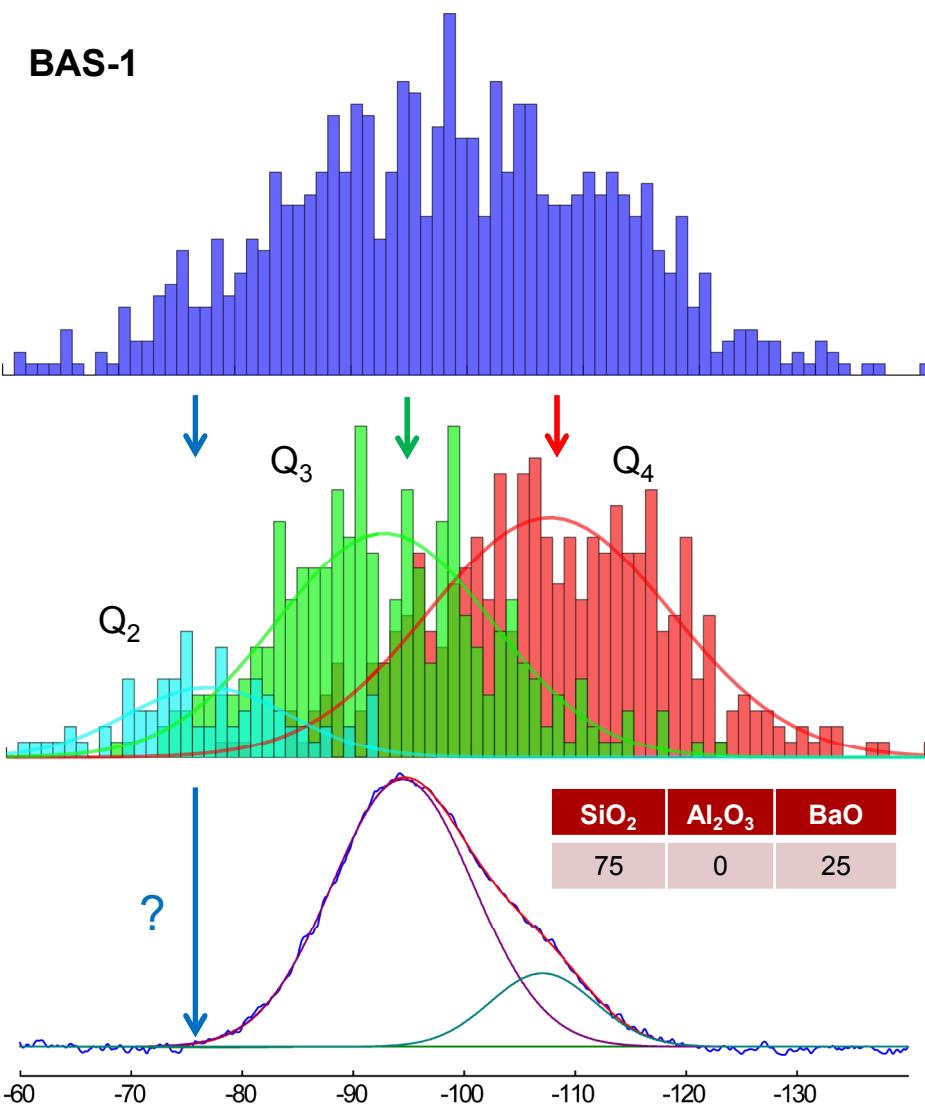


Prediction Correlations



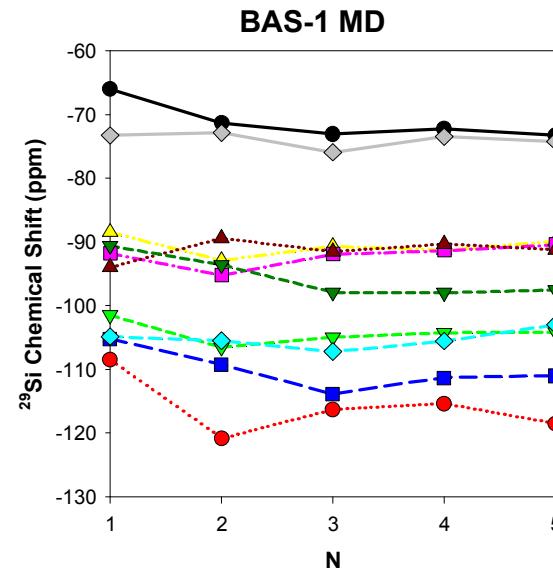
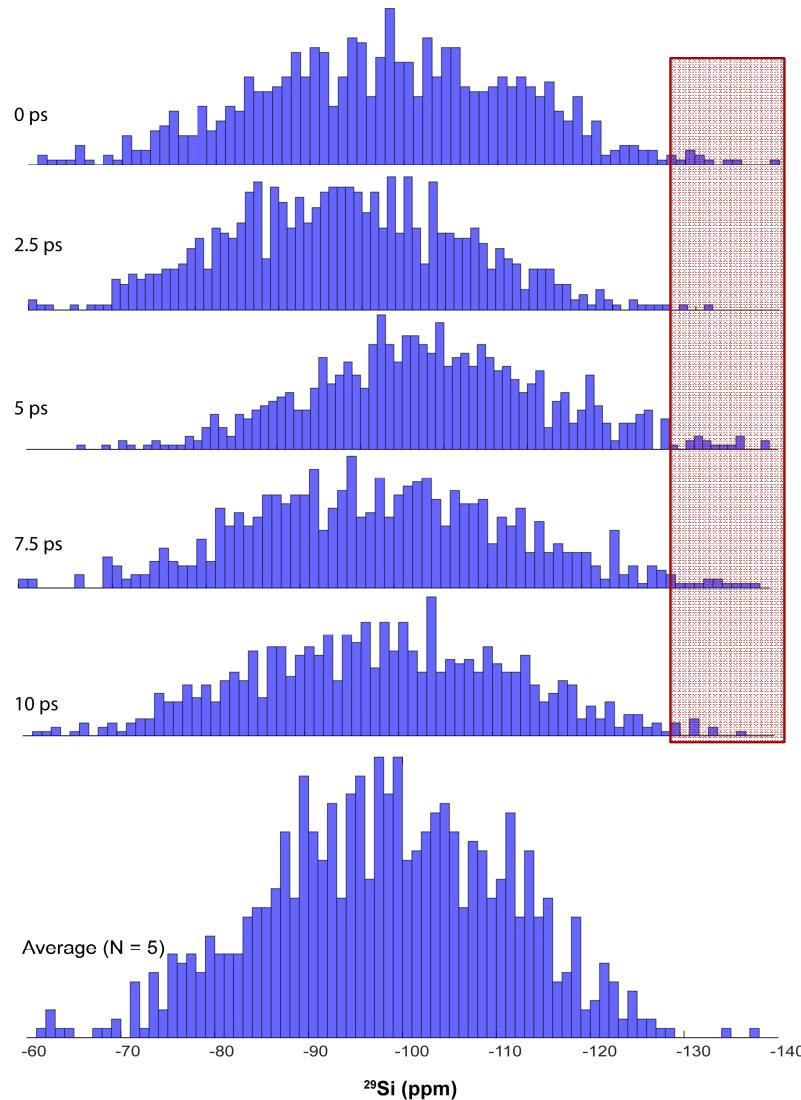
- Larger size MD snap shot computationally demanding. If scales as  $\sim N^2$  a 3000 atom calculation would require 119 days for NMR calculation and 119 weeks for geometry relaxed calculation!
- **Larger size is required for improved statistics.**
- What can be modified in empirical relationship to improve correlation?
- Sampling scheme for MD would also improve statistics.

# $^{29}\text{Si}$ NMR Shift Calculations: Empirical



- Veryfast! (~1s for 3000 atoms).
- The mean chemical shift for each  $Q_n$  species is correctly predicted.
- Allows for more reliable deconvolution for non-standard compositions.
- The MD simulation over estimates  $Q_2$  concentration, which is essentially not observed in the experimental NMR.
- MD simulation appears to predict a larger distribution on  $Q_n$  resonances than observed experimentally.
- (Ongoing) Useful in understanding and deconvolute the  $^{29}\text{Si}$  chemical shifts with  $^{27}\text{Al}$  and  $^{11}\text{B}$  added (not clearly resolved in the  $^{29}\text{Si}$  NMR line shape).

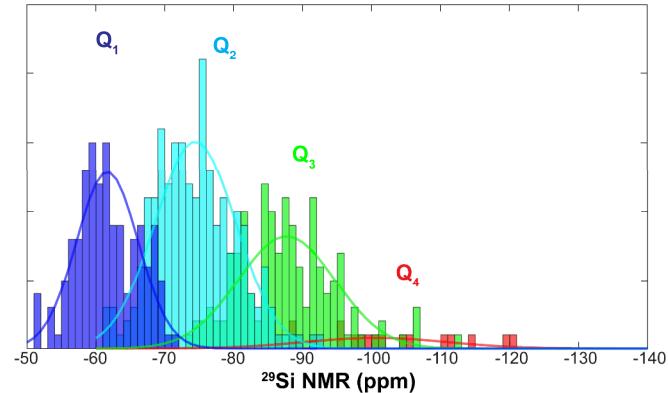
# Averaging Over MD Time Series



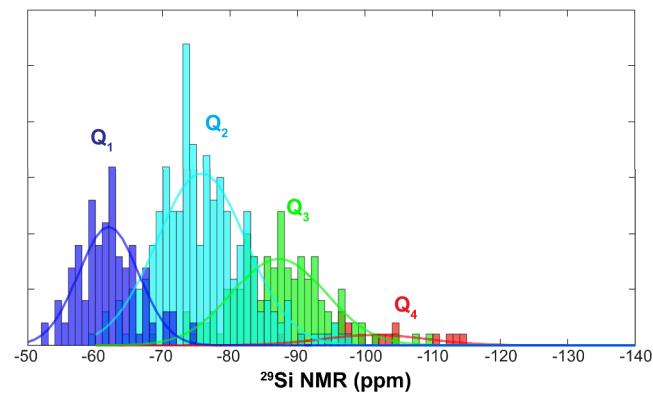
- Time averaging removes chemical shift of strained geometries.
- Slight reduction in distribution width for each  $Q_n$  species. Needs more averaging?
- Speed of empirical calculation actually allows for larger averaging set. Could be done over entire time series. (Future effort).

# Variation with Cation Compositions

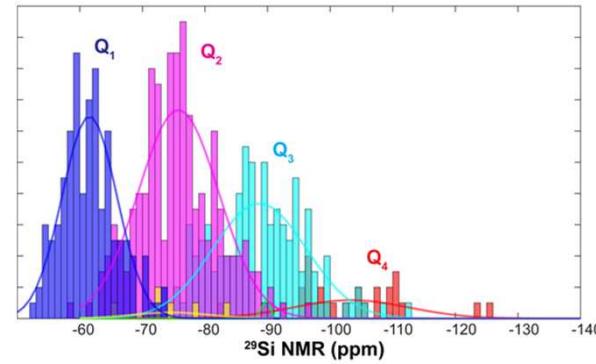
Final\_trz04  
3190 Atoms Unit Cell



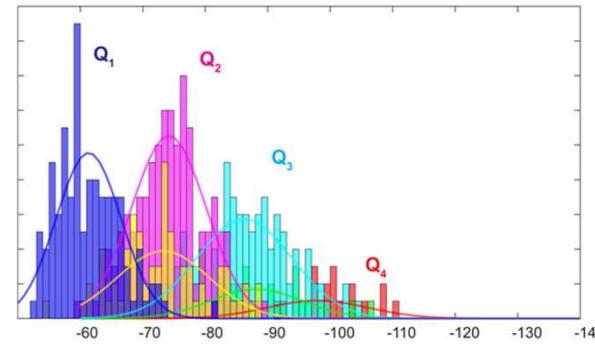
Final\_trz06  
3190 Atoms Unit Cell



Final\_PC1  
3190 Atoms Unit Cell

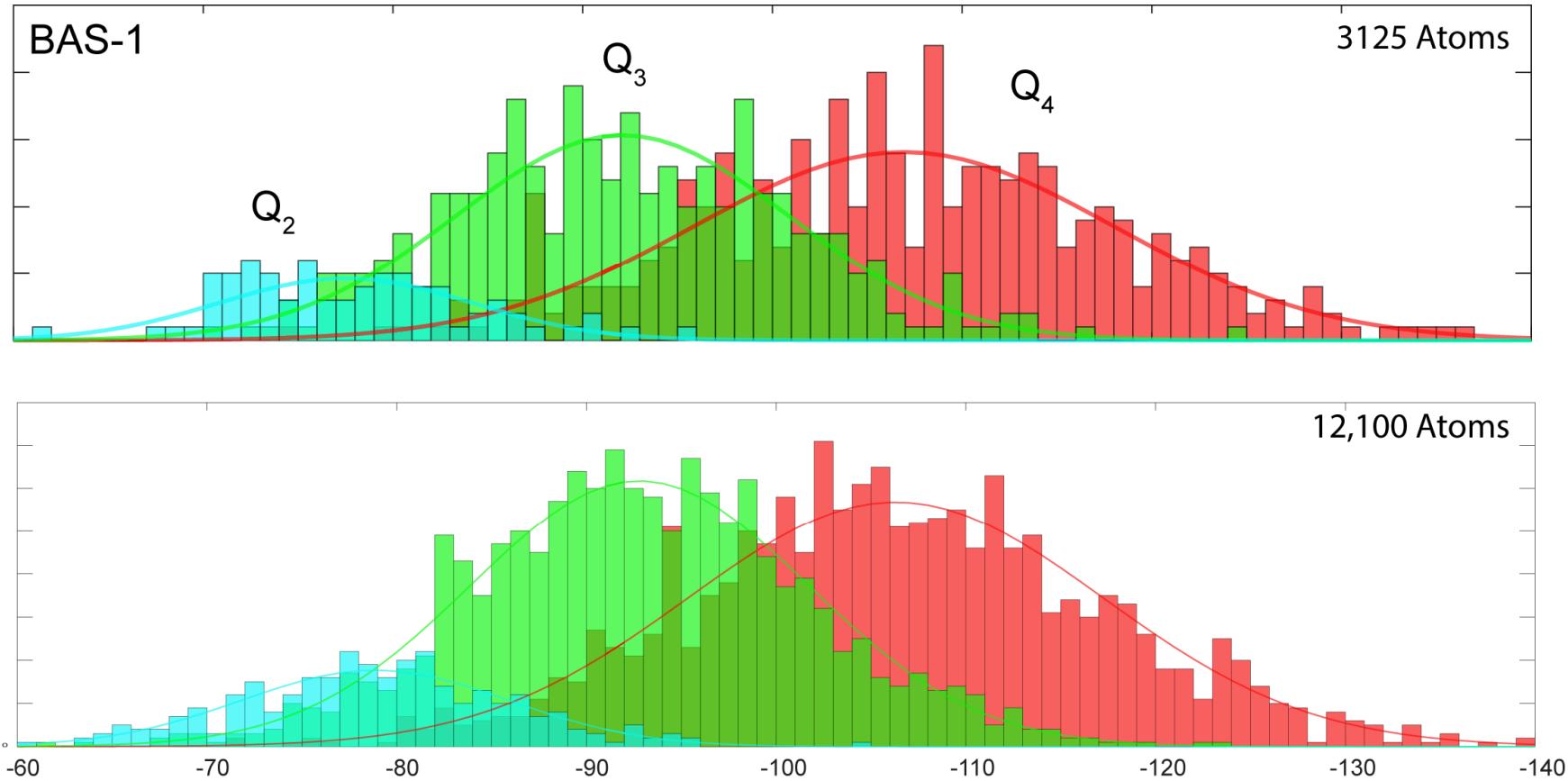


Final\_PC2  
2970 Atoms Unit Cell

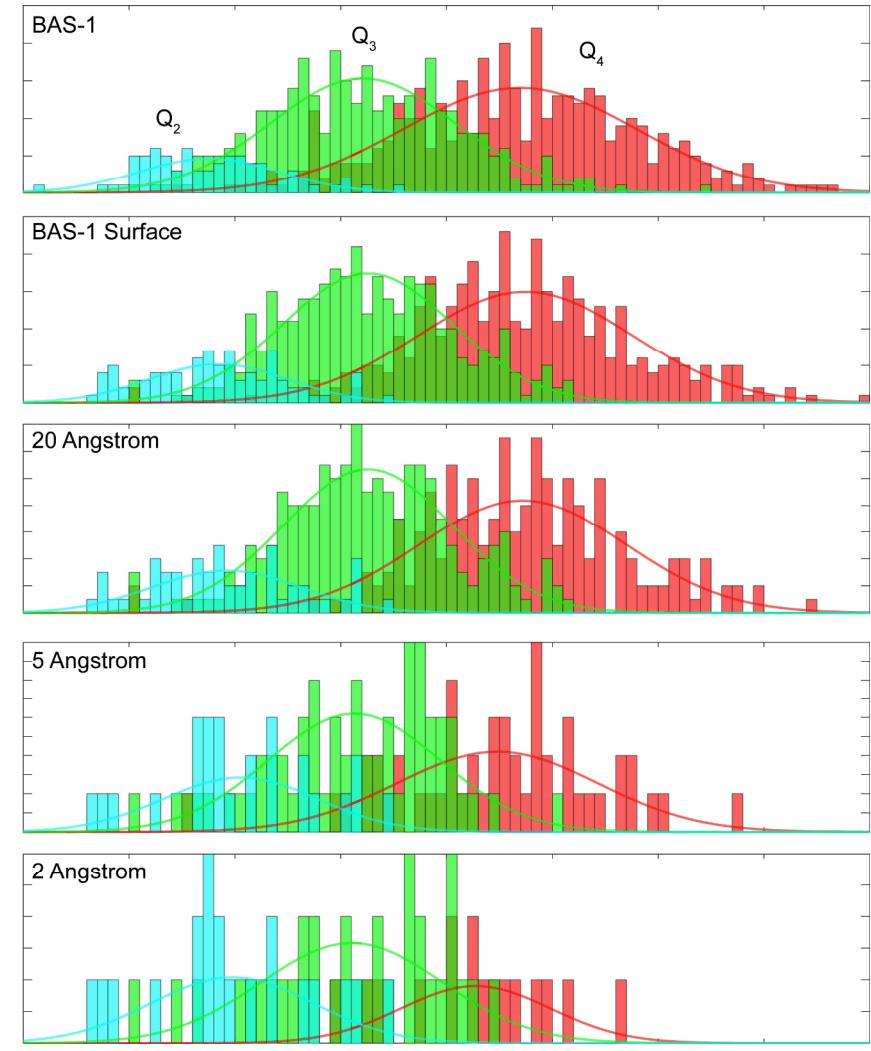
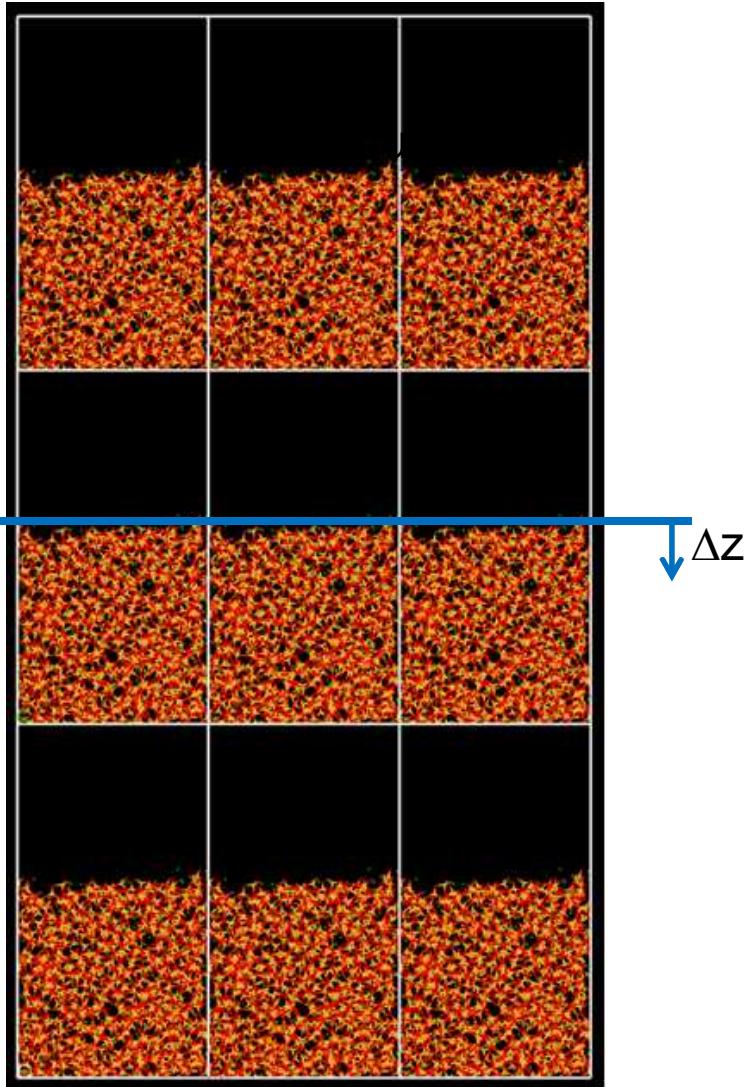


	SiO <sub>2</sub>	Al <sub>2</sub> O <sub>3</sub>	BaO	CaO	B <sub>2</sub> O <sub>3</sub>	Na <sub>2</sub> O	K <sub>2</sub> O
BAS-1	75	0	25	0	0	0	0
PC1	50	0	10	0	0	40	0
PC2	50	0	30	0	0	20	0
TRZ04	50		10			10	30
TRZ06	50		10			30	10

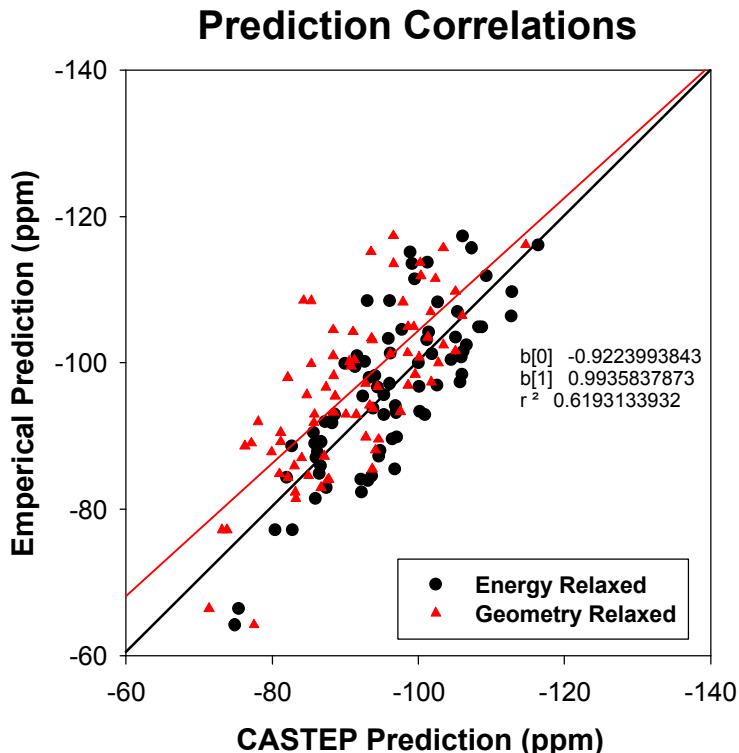
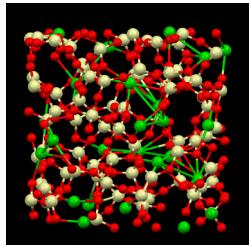
# How Large Can We Go?



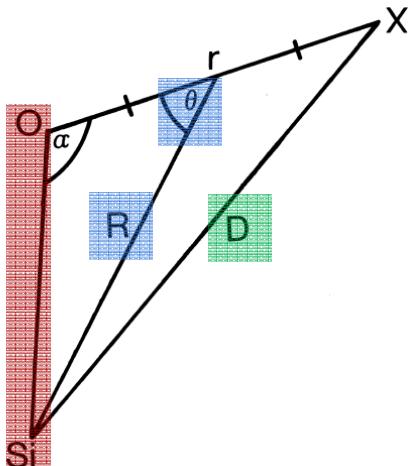
# Simulation of Vacuum Surface



# Empirical Correlations



- Larger size MD snap shot computationally demanding. If scales as  $\sim N^2$  a 3000 atom calculation would require 119 days for NMR calculation and 119 weeks for geometry relaxed calculation!
- Larger size is required for improved statistics.
- What can be modified in these empirical relationships to improve correlation?



$$s_i = \left( \exp \left[ (r_0 - r_i) / 0.37 \right] \right)$$

$$\Omega = \sum_{i=1}^N \left[ s_i \left( 1 - 3 \cos^2 \theta_i \right) / 3R_i^3 \right] \log D_i$$

$$\delta(^{29}\text{Si}) = 701.6\Omega - 45.7$$

# Conclusions and Future Efforts

- Have developed code for the empirical calculation of  $^{29}\text{Si}$  NMR chemical shifts from MD simulation structures.
- Allowed for improved NMR assignments, and identification of unique signatures.
- Reveals some discrepancies between MD predicted structures and experimental NMR results.
- Demonstrated equivalence with GIPAW plane wave periodic calculations.
- Have been able to address very generalized compositions and larger sizes!
- Continue improvements of empirical relationships based on GIPAW simulations.

# Acknowledgements

**Blake Hammann (Washington University St. Louis) - CASTEP**



**Todd Zeitler (Sandia) – All things MD**



**Kevin Ewsuk (Sandia) – Program Lead**

*Thanks for your attention.....*

*Project funding through Sandia LDRD*