

**Sandia
National
Laboratories**

Development of Machine Learning Models for Turbulent Wall Pressure Fluctuations

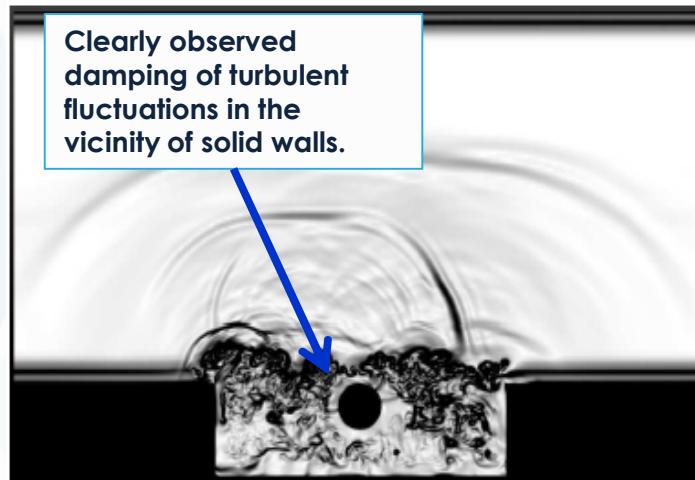
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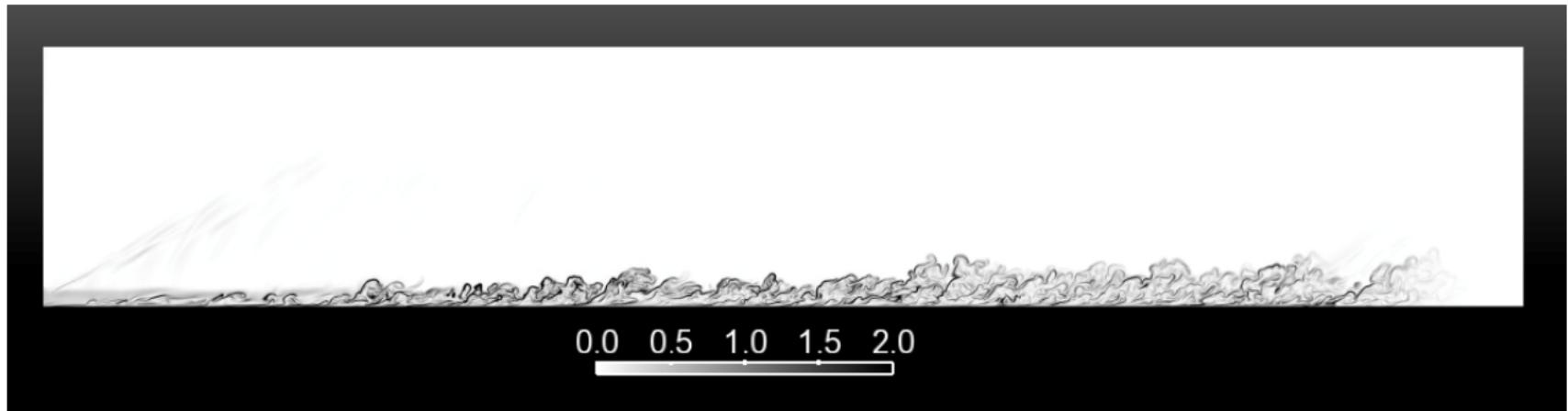
Motivation

- For fluid-structure interaction (FSI) applications, must be able to predict the pressure loading on a surface due to a turbulent flow
- Many turbulence simulations use wall-functions or simplified models near the wall due to the computational expense of resolving wall flows
- These near wall models often result in inaccurate pressure power spectra distributions



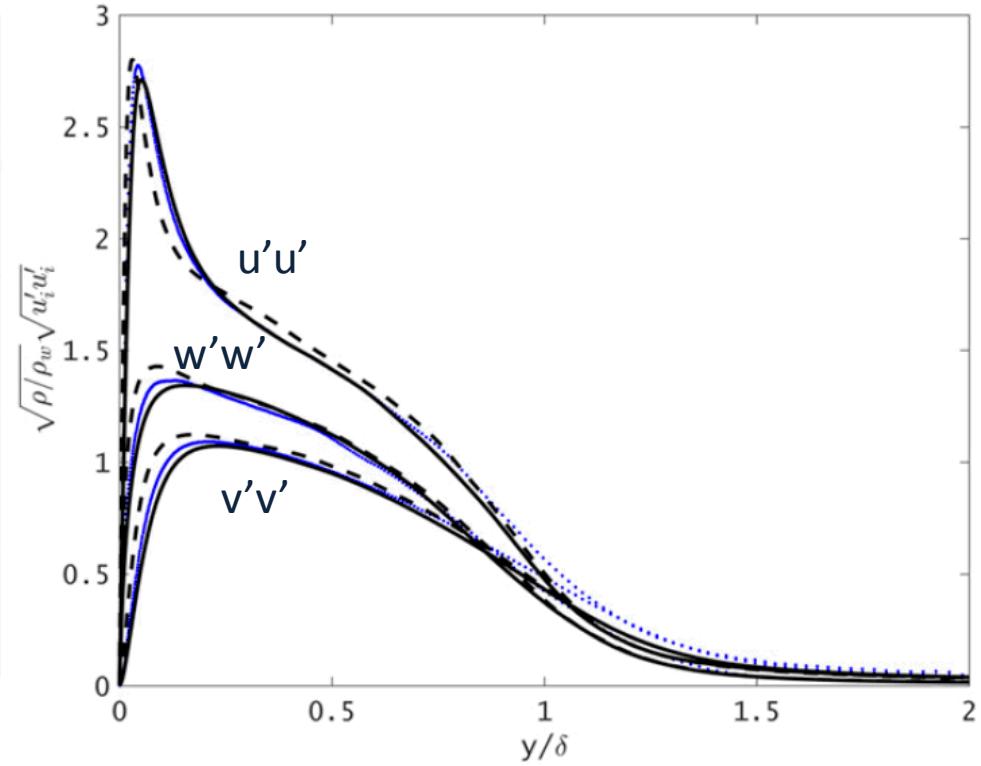
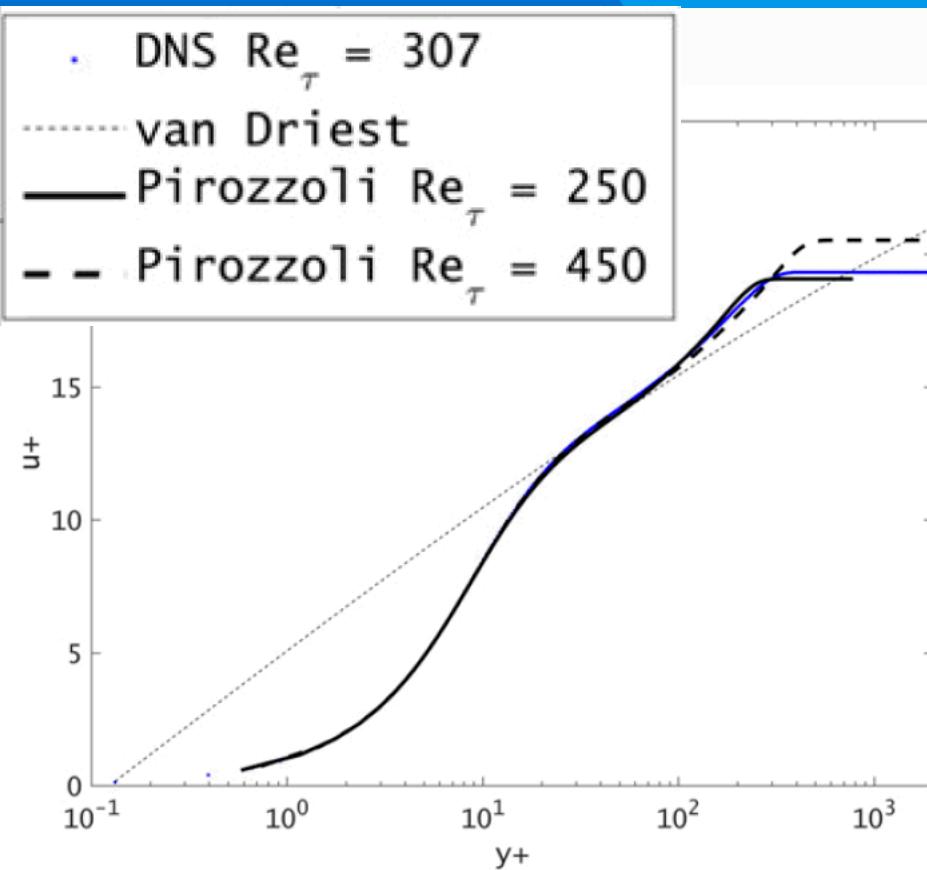
- We want to use a high fidelity Direct Numerical Simulation data set to investigate how machine learning can be used to come up with an improved near wall model for pressure fluctuations

DNS Data Set



- Mach 2.0 compressible flat plate turbulent boundary layer
- Low-dissipation 5th order upwind biased flux-reconstruction scheme
- Fourth order explicit Runge Kutta time integration
- 100.7 M mesh cells
 - Near wall resolution: $\Delta x^+ < 5$, $\Delta y^+ < 0.2$, $\Delta z^+ < 4$
- $1075 < Re_\theta < 1310$
- Run for $> 1200\tau$ (where $\tau = \delta_0 / U_\infty$)

DNS Validation



- Our DNS: $Re_\tau = 302$
- Good agreement of mean velocity and Reynolds stress profiles with Pirozzoli et al. at $Re_\tau = 250, 450$

What is Machine Learning?

- Data-driven algorithms to discern patterns and make predictions on big, high-dimensional data
- Linear regression, support vector machines, neural networks

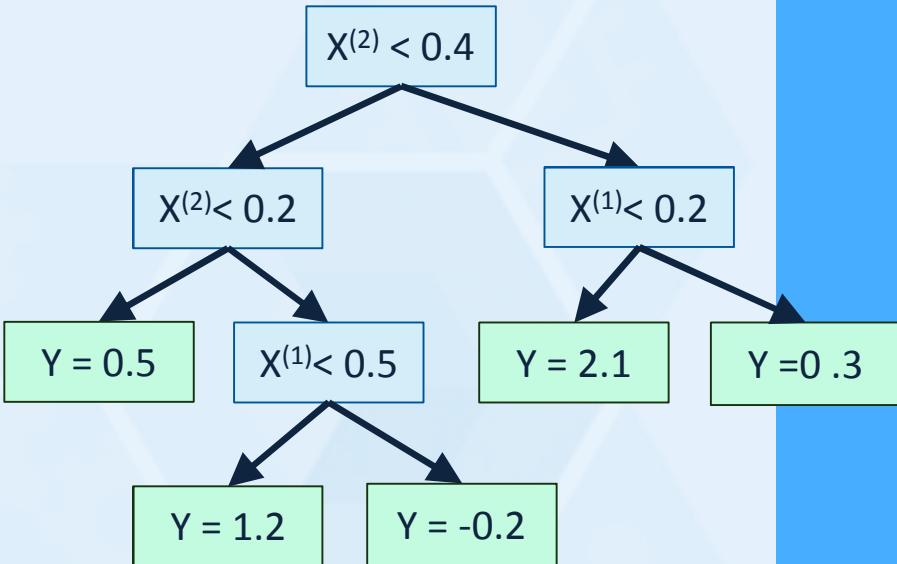
The collage illustrates the use of machine learning in three different contexts:

- News Feed (Left):** A screenshot of a news website showing a "Inspired by your Wish List" section. It displays a list of top-shared articles (MOST EMAILED) and a recommendation for an "amazonPrime Original audio series". The articles include titles like "Powerful Blast Manhattan; Se", "Ahmad Khan J Manhattan and", "Manhattan Bo F.B.I. Question", "Chelsea Bombing: What We Know and Don't Know", and "DOCTOR'S WORLD How Healthy Is Hillary Clinton? Doctors Weigh In".
- Audiobook Recommendation (Middle):** A screenshot of an Amazon Prime interface showing a "Who Gets What — and Why" audiobook by Alvin E. Roth. It also shows a "PHISHING FOR PHOOLS" book by George A. Akerlof and Robert J. Shiller.
- Music Streaming (Right):** A screenshot of the Pandora music streaming interface. It shows a "Classical" radio station playing "We all love" by Ennio Morricone. The interface includes a "Create Station" button, a progress bar (0:12), and a sidebar listing various radio stations.

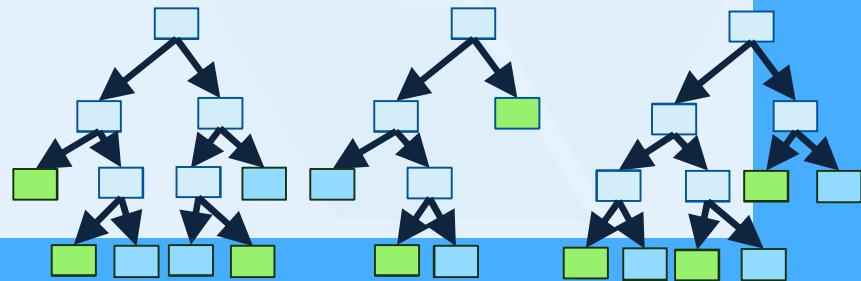
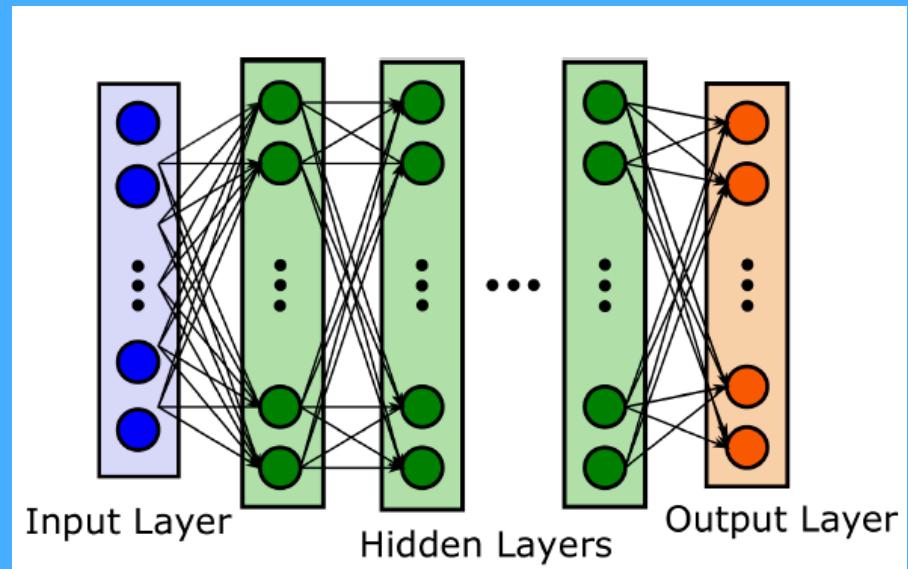
Machine Learning Algorithms



Random Forest



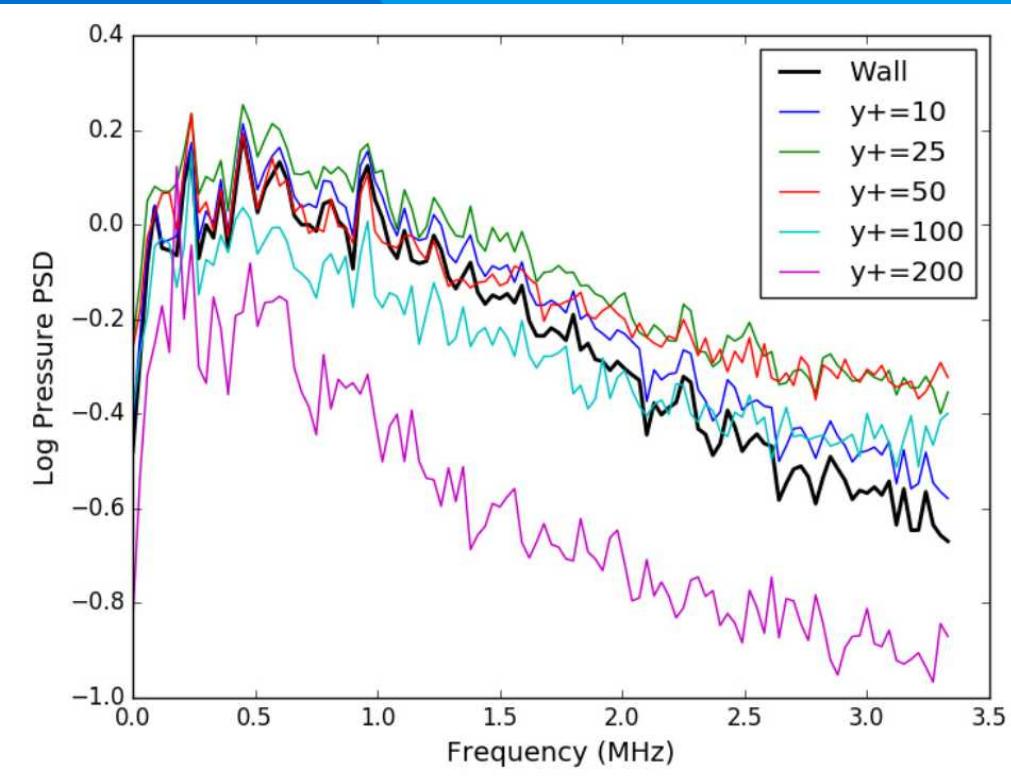
Neural Network



$$y = f(w^T x)$$

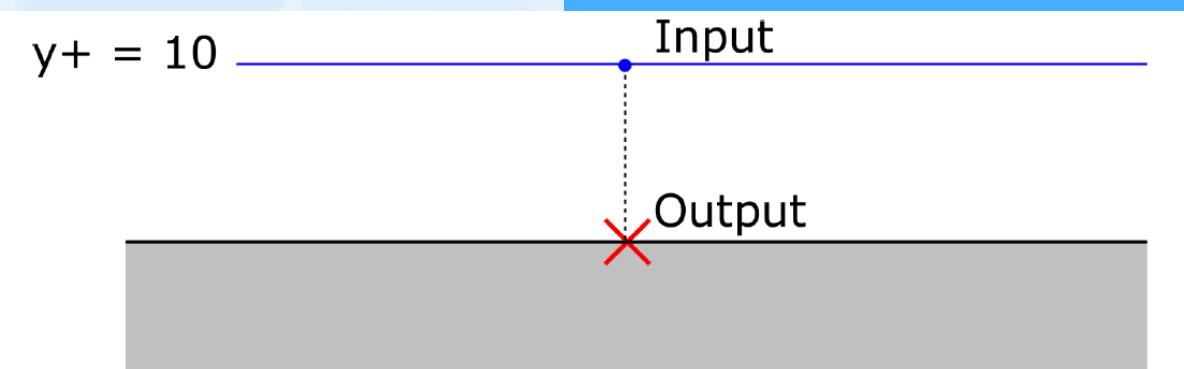


Machine Learning Framework



Given Pressure PSD at a point above the wall, can we predict the Wall Pressure PSD?

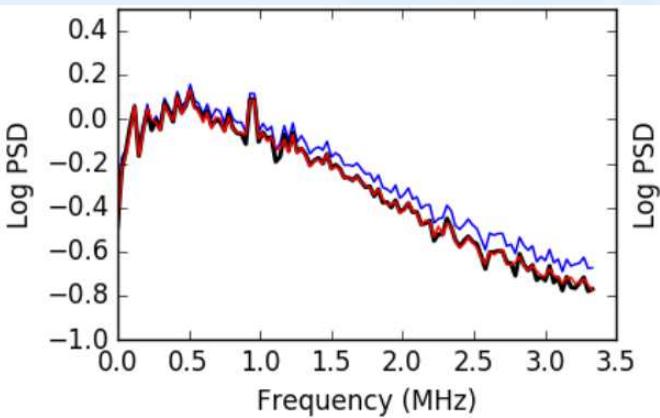
Split data sequentially into training and test set



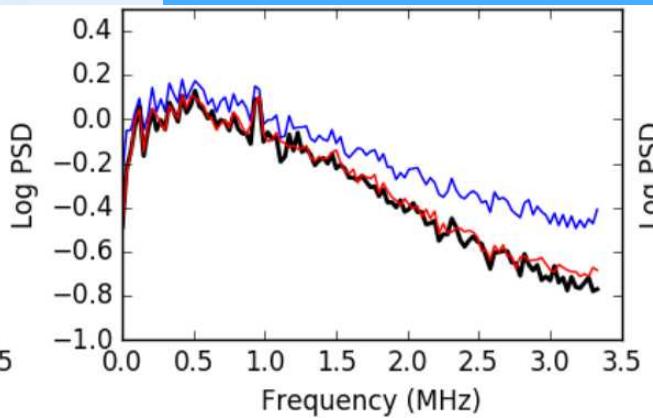
Random Forest Predictions



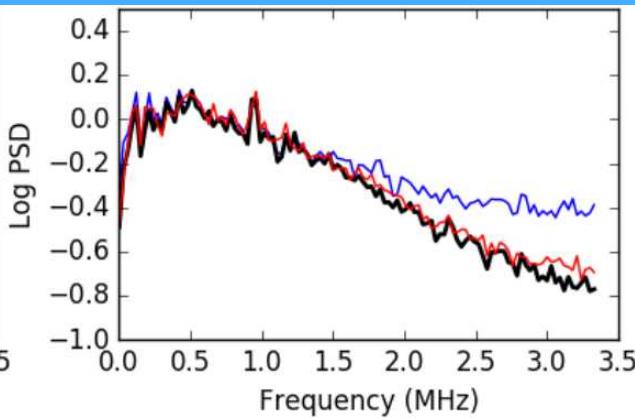
$y^+ = 10$



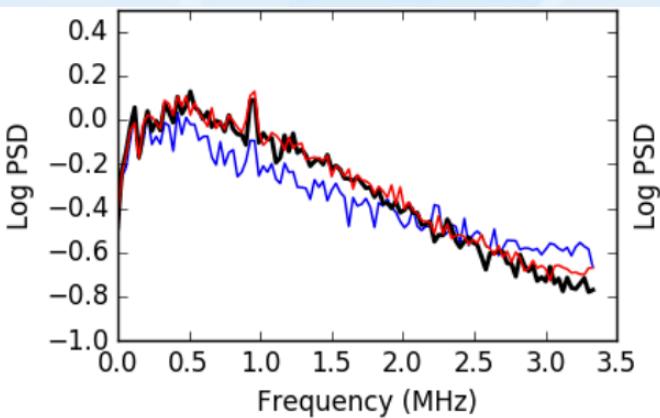
$y^+ = 25$



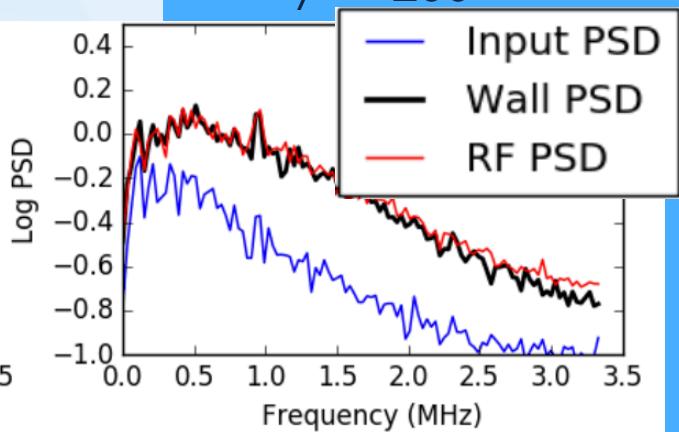
$y^+ = 50$



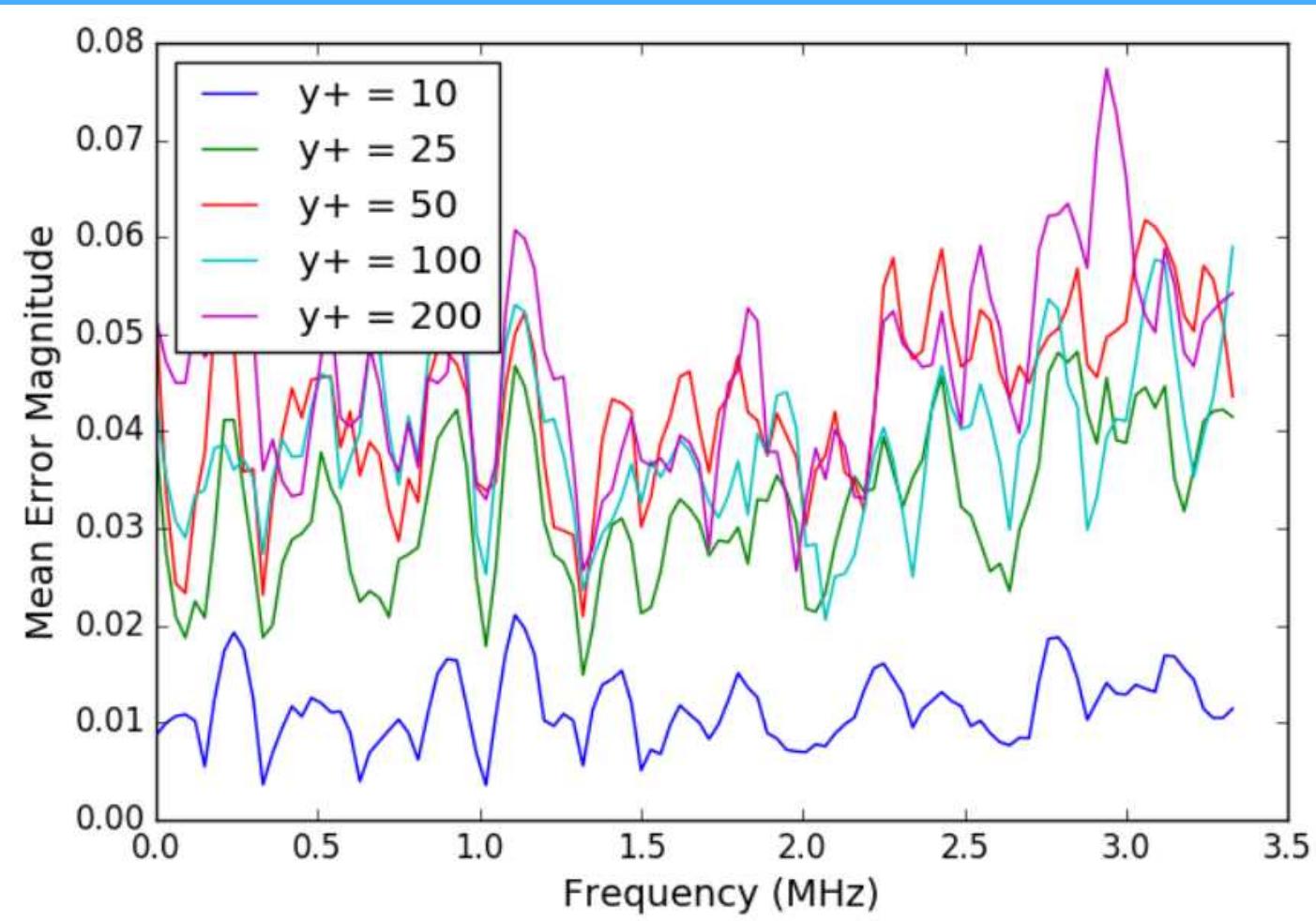
$y^+ = 100$



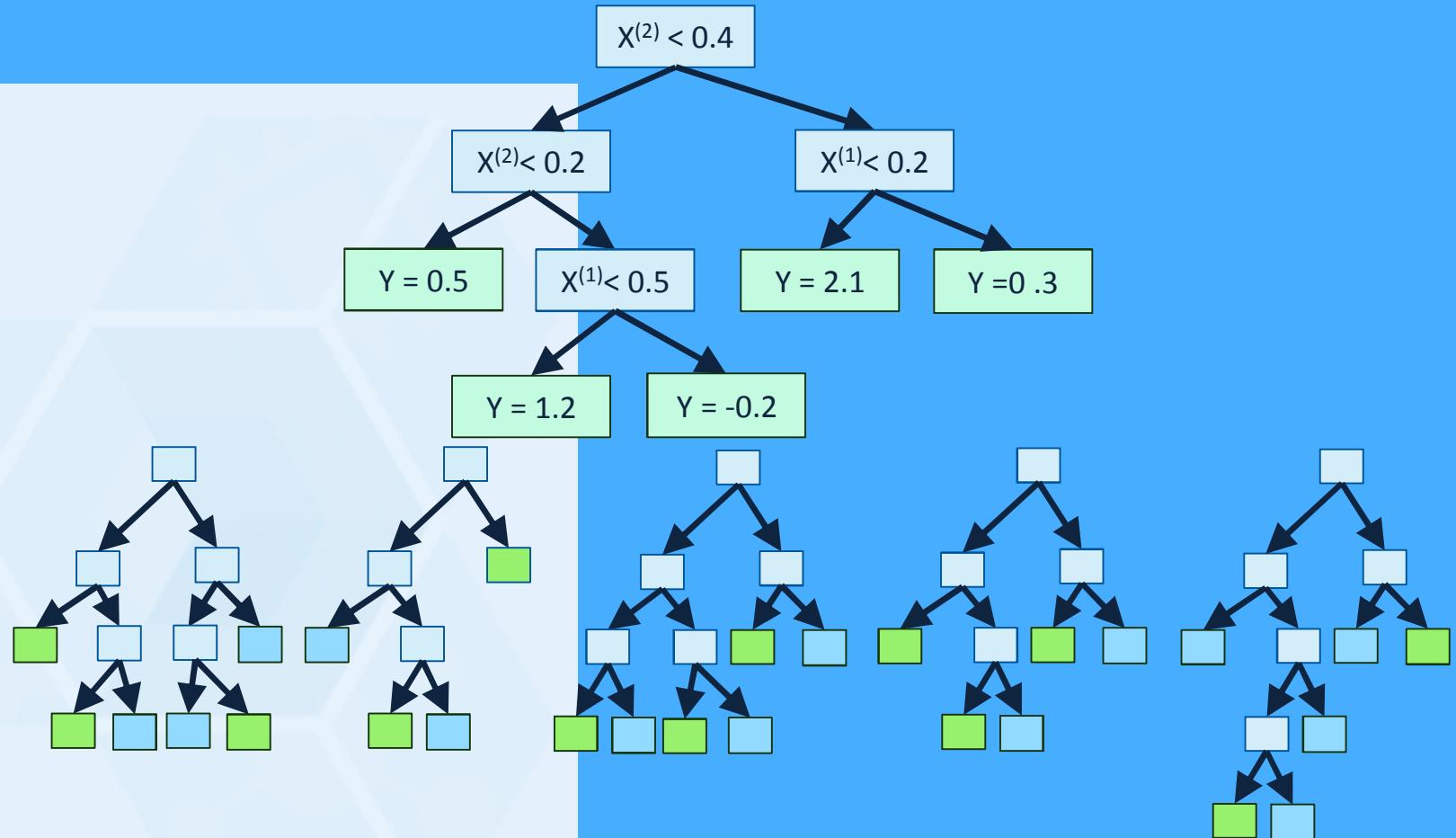
$y^+ = 200$



Frequency-Dependence of Random Forest Accuracy



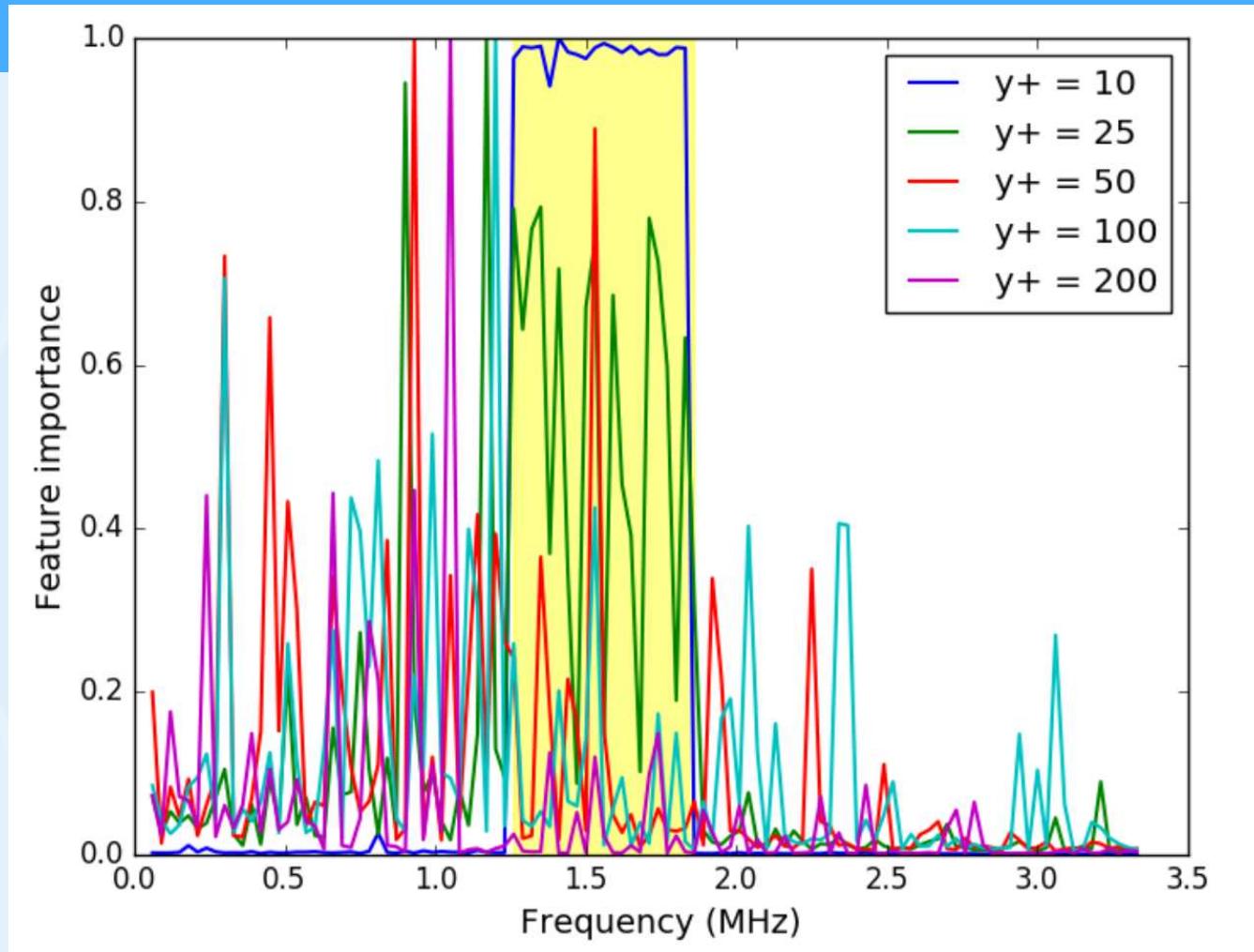
Random Forest Feature Importance



- Each split in decision tree is based on greedily maximizing the reduction in variance
- Feature importance is based on how often each feature is used in a split and the aggregated reduction in variance over those splits



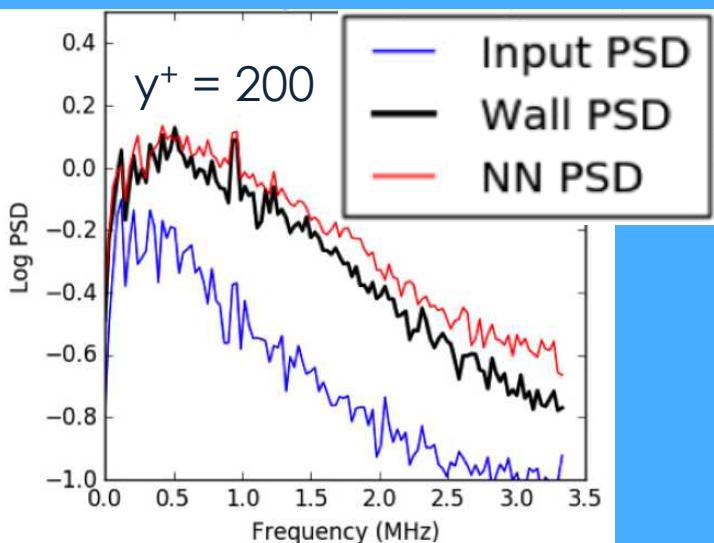
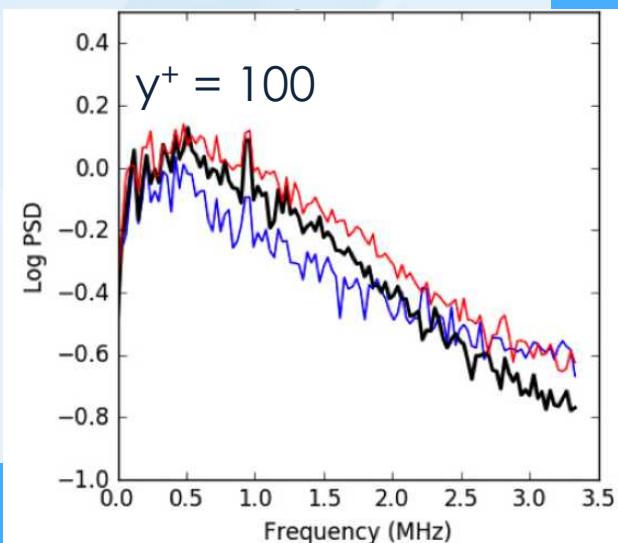
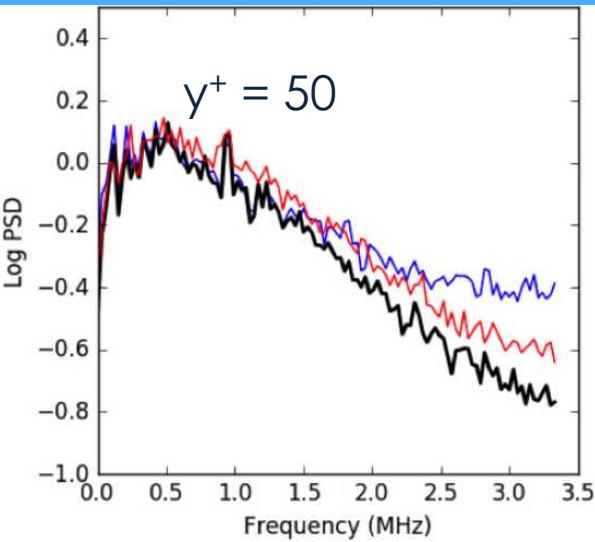
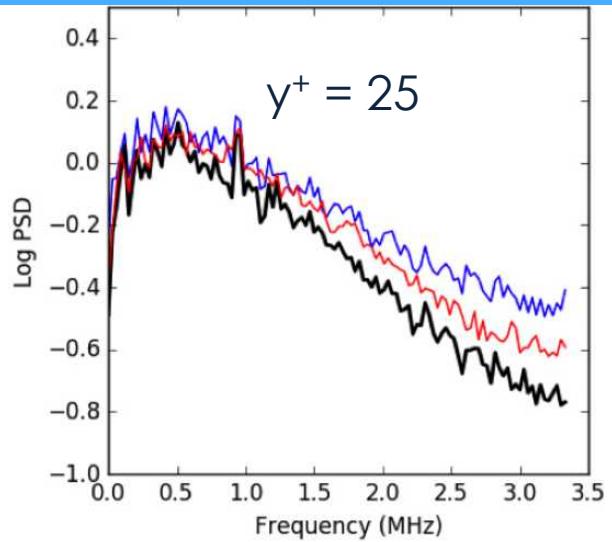
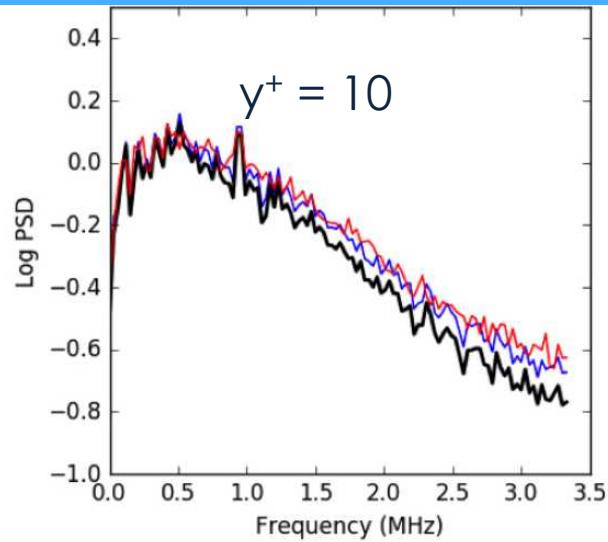
Random Forest Feature Importance



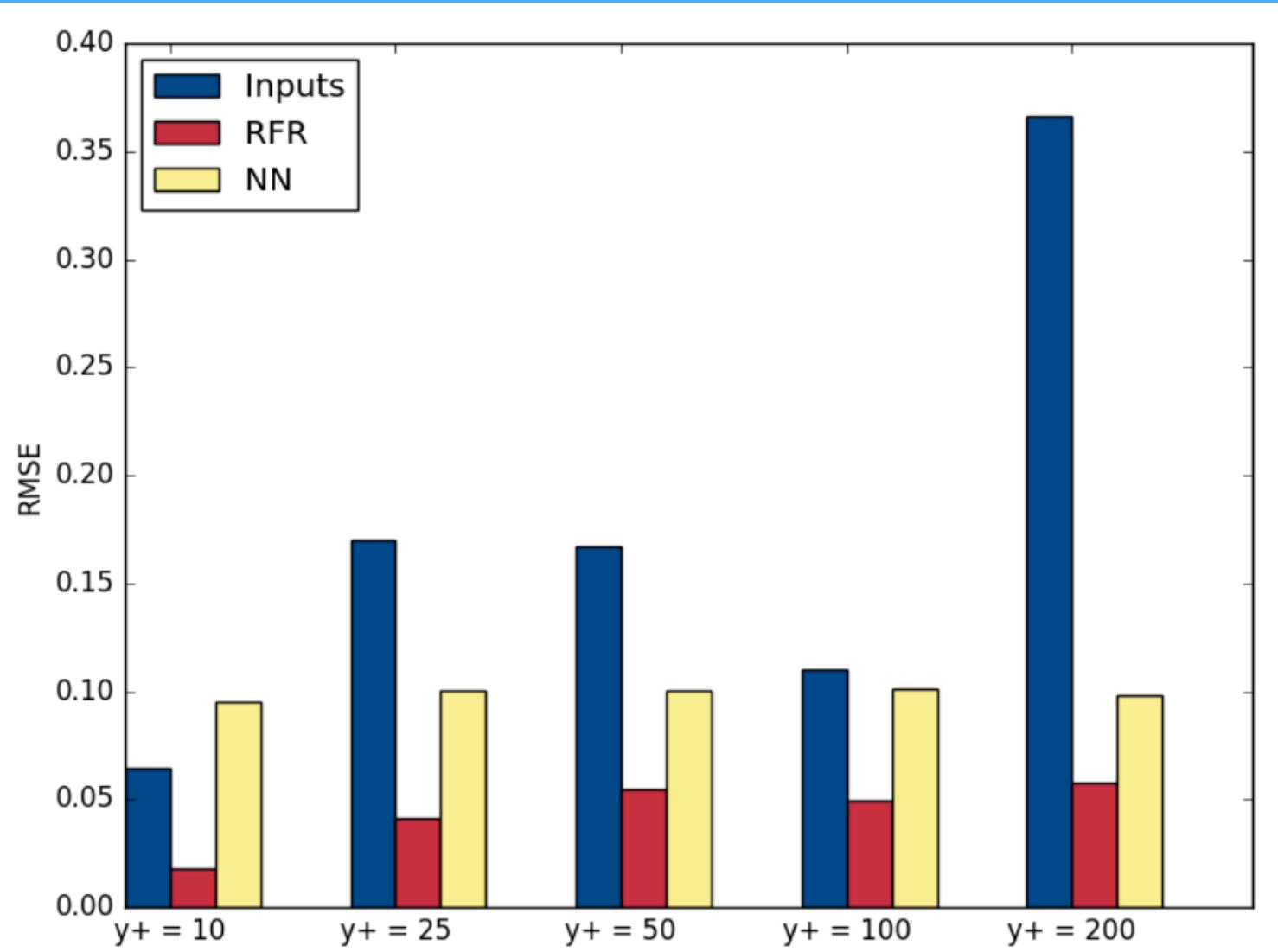
file:///Users/jling/WebstormProjects/FeatureImportance/FeatureImportance_v3.html



Neural Network Predictions



Machine Learning Performance



Conclusions



- Performed and validated a DNS of a compressible flat plate boundary layer
- Developed machine learning framework to predict wall pressure PSD given pressure PSD (or other inputs) above the wall
- Evaluated two different ML algorithms
 - Random Forest provided better performance than simple multi-layer perceptron neural network
- Evaluated machine learning performance using input data at different wall distances
 - Data out to $y^+ = 100$ allows accurate reconstruction of wall pressure PSD
 - Higher frequencies are harder to predict using information farther from the wall
 - These results suggest that it should be possible to create a data-driven wall model for the pressure PSD

Next Steps



- Train and validate across wider range of Mach numbers, different flow configurations
- Given WMLES data, try to predict DNS wall pressure PSD
- Evaluate more complex neural network architectures to see if improved neural network performance is achieved

Questions?

