

Investigation of partitionless growth of ϵ -Al₆₀Sm₁₁ phase in Al-10at.% Sm liquid

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Abstract

Recent experiments on devitrification of Al₉₀Sm₁₀ amorphous alloys revealed an unusual polymorphic transformation to a complex cubic crystal structure called the ϵ -Al₆₀Sm₁₁ phase. Molecular dynamics simulations of the growth of the stoichiometric ϵ -phase seed in contact with an undercooled Al-10at.% Sm liquid are performed to elucidate the microscopic process of transformation. The as-grown crystal and undercooled liquid possess similar local order around Al atoms whereas a rigid network defined by the Sm sub-lattice develops during the growth. Using a template-cluster alignment method, we define an order parameter to characterize the structural evolution in the system. Estimates of the attachment rate is $R_a = 8.70 \times 10^{-4} \text{ \AA}^{-2} n_S^{-1}$ and detachment rate is $R_d = 3.83 \times 10^{-4} \text{ \AA}^{-2} n_S^{-1}$ at the interface between ϵ -Al₆₀Sm₁₁ and Al-10at.% Sm liquid at 800 K.

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1. Introduction

Amorphous alloys can display a complicated devitrification behavior during heating [1,2]. Phase and morphological selection is dependent on complex relationships between thermodynamic and kinetic factors, such as relative differences in free energy between competing phase, local chemical partitioning and epitaxial growth [3]. One approach is to search for relevant order parameters which describe this transformation, paving the way for a phase-field description which can enable detailed realistic simulations of the devitrification process. While thermodynamic measurements provide energetics of the phase transformation and *in situ* XRD studies can provide more detailed phase information [4], details of local atomic order during the transformation is challenging[5]. In this situation, atomistic simulation becomes a valuable tool to provide insight into the detailed atom-level processes[6].

The Al-Sm binary alloy is a prototype of marginal glass-forming system which exhibits the widest glass-forming composition range in the Al-RE (RE for rare earth element) series [7,8]. It has been shown that the devitrification of the Al-Sm alloys within the glass formation composition range is a complicated process [9–12]. For the melt-spun ribbon sample of the Al₉₀Sm₁₀ amorphous alloy, it shows a multi-step devitrification pathway from the glass state transforming to various metastable crystalline phases[11]. After holding the as-quenched Al₉₀Sm₁₀ glass at 457 K for 10 minutes, crystal grains appear and continue to grow rapidly until the sample totally transforms into a single crystal phase in ~1 hour[13]. A recent study using the genetic algorithm (GA) and Rietveld refinement solved the crystal structure of the first phase that appears in this complicated process: the ϵ -Al₆₀Sm₁₁ phase [12]. It has a complex structure containing around 140 atoms in the unit cell. X-ray data and theoretical simulations both provide evidence that the experimentally grown crystal structure has further structural complexity in the form of abundant point defects [12].

Although it is difficult to directly simulate the growth of the ϵ -Al₆₀Sm₁₁ phase in the Al₉₀Sm₁₀ glass due to the limitation of the short timescales ($\leq \mu\text{s}$) in current molecular dynamics (MD) simulations, it is possible to extract information about the growth process in the undercooled liquid state using accelerated MD at an elevated temperature. The stoichiometric ϵ -Al₆₀Sm₁₁ with a surface termination (100) was placed in contact with the undercooled liquid of Al-10at.% Sm. The atomic cluster alignment method [14], which quantifies the structural deviation between an as-extracted cluster and the template motif, is employed to reveal the behavior of the local structural order during the growth. The interface velocity during growth can be derived from alignment analysis. By tracing the atomic motion, the dynamic pathway from the undercooled liquid to crystal is revealed. Frequent atom attachment and detachment are found at the solid-liquid interface. The estimated attachment and detachment rates are consistent with the interface velocity in our simulation.

2. Molecular dynamics simulations

The initial structure in the simulation is constructed by combining the stoichiometric ϵ -Al₆₀Sm₁₁ and the undercooled Al-10at.% Sm liquid. A supercell of the ϵ -Al₆₀Sm₁₁ containing 3834 atoms is placed at the left part of the simulation box. The Al-10at.% Sm liquid, containing 3840 atoms, is quenched from 2000K to 800K and annealed at 800K for 3 ns to get equilibrium. Then the liquid sample is placed at the right part of the simulation box adjacent to the (100) crystal plane of the ϵ -Al₆₀Sm₁₁. The periodic boundary condition is applied in all three directions of the simulation box. All the simulations are performed with Nose-Hoover thermostats. During the simulation, we allow the length of the box in the direction perpendicular to the interface to change, resulting in constant area, constant normal pressure: NP_xAT ensemble, with x being the perpendicular direction. The Verlet algorithm is used to integrate Newton's equation of motion,

using a time step of 3 *fs*. The sample is annealed at 800 K for 285 *ns* that the Al-10at.% Sm undercooled liquid fully completes the transformation to the crystal structure. The simulations are performed with the Large-scale Atomic/Molecular Massively Parallel Simulator (LAMMPS) [15] using a semi-empirical Finnis-Sinclair (FS) potential for Al-Sm system [16].

Figure 1(a) shows the projected snapshots at the initial, medium and final time of the simulation, respectively. The total simulation time is 285 ns. One can see the growth of the ϵ phase into the liquid. The mean square displacement is plotted as a function of time in Fig. 1(b). Both Al and Sm atoms' diffusion slow dramatically, indicating that the crystalline phase has consumed the liquid.

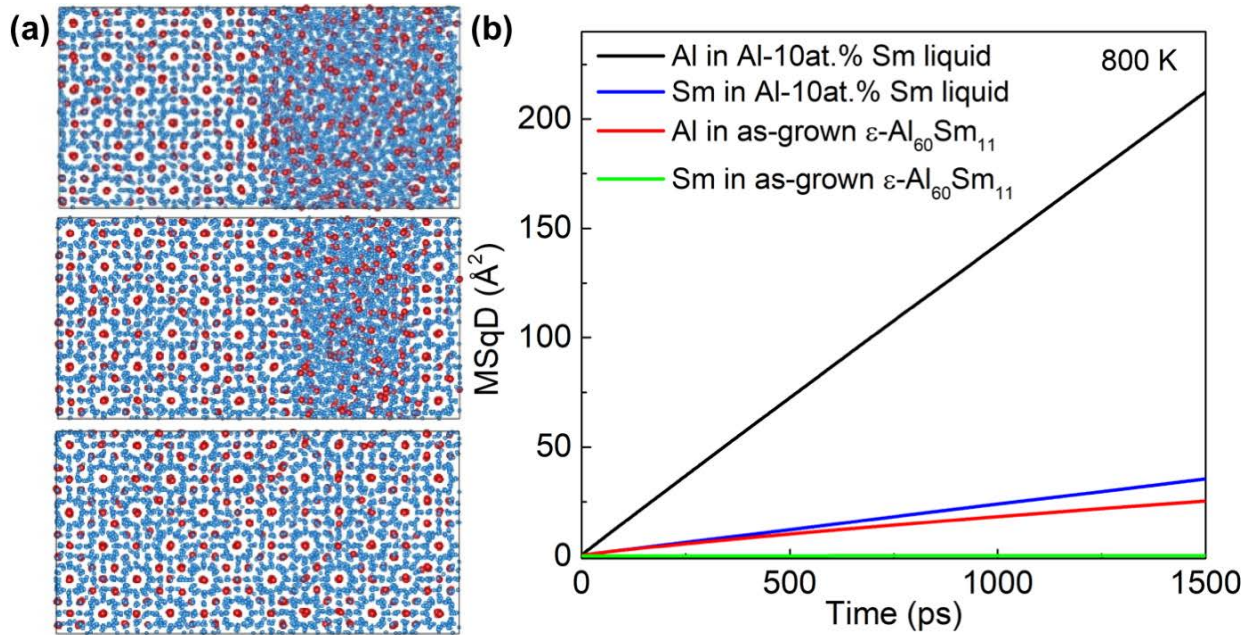


Fig. 1 (a) The projected snapshots of the initial, medium and final configurations during simulation. The blue ball stands for Al atoms and red for Sm atoms. (b) The mean square displacement for Al and Sm atoms in initial liquid and the as-grown structure.

3. Results and discussions

3.1 Pair correlation function and bond angle distribution

In Fig. 2(a)-(c), the pair correlation function (PCF) are plotted for the Al-10at.% Sm undercooled

liquid and the as-grown $\epsilon\text{-Al}_{60}\text{Sm}_{11}$ structure. Compared to the liquid state, the PCF peaks of the as-grown structure are sharper and narrower, indicating strong crystalline order. However, the peaks in Al-Al and Al-Sm PCFs of the liquid and as-grown $\epsilon\text{-Al}_{60}\text{Sm}_{11}$ show interesting coincidences in Fig. 2(a) and (b). Since the nearest neighbor atoms for both Al and Sm atoms are dominated by the Al atoms at the 10 at.% Sm composition, such coincidence suggests that the local atomic arrangements of Al atoms are similar in the undercooled liquid and the crystal. In Fig. 2(c), the first peak of liquid Sm-Sm PCF at 3.9 Å dramatically decreases after the crystallization, while a new peak emerges at 4.6 Å, indicating the development of a Sm-Sm network during the crystallization [17].

In addition to the PCFs, we performed bond angle analysis as shown in Fig. 2(d)-(f). In Fig. 2(d), the Al-Al-Al bond angle distribution in the liquid sample exhibits strong peaks at around 60° and 110° as well as a shoulder peak at 160°, which is similar to that of pure Al liquid [18]. After the liquid crystallizes, these angular distributions simply sharpen, indicating the Al packing is unaffected during the crystallization. In Fig. 2(e), the peaks of Al-Sm-Al bond angle distributions also narrow and sharpen during crystallization. However, in Fig. 2(f), the Sm-Sm-Sm bond angle distribution changes dramatically, with two sharp peaks emerging at 90° and 125°. Similar to the change of the Sm-Sm PCF in Fig. 2(c), the change in Sm-Sm-Sm bond angle distribution also indicates that the Sm-Sm packing undergoes dramatic reconstructed during crystallization.

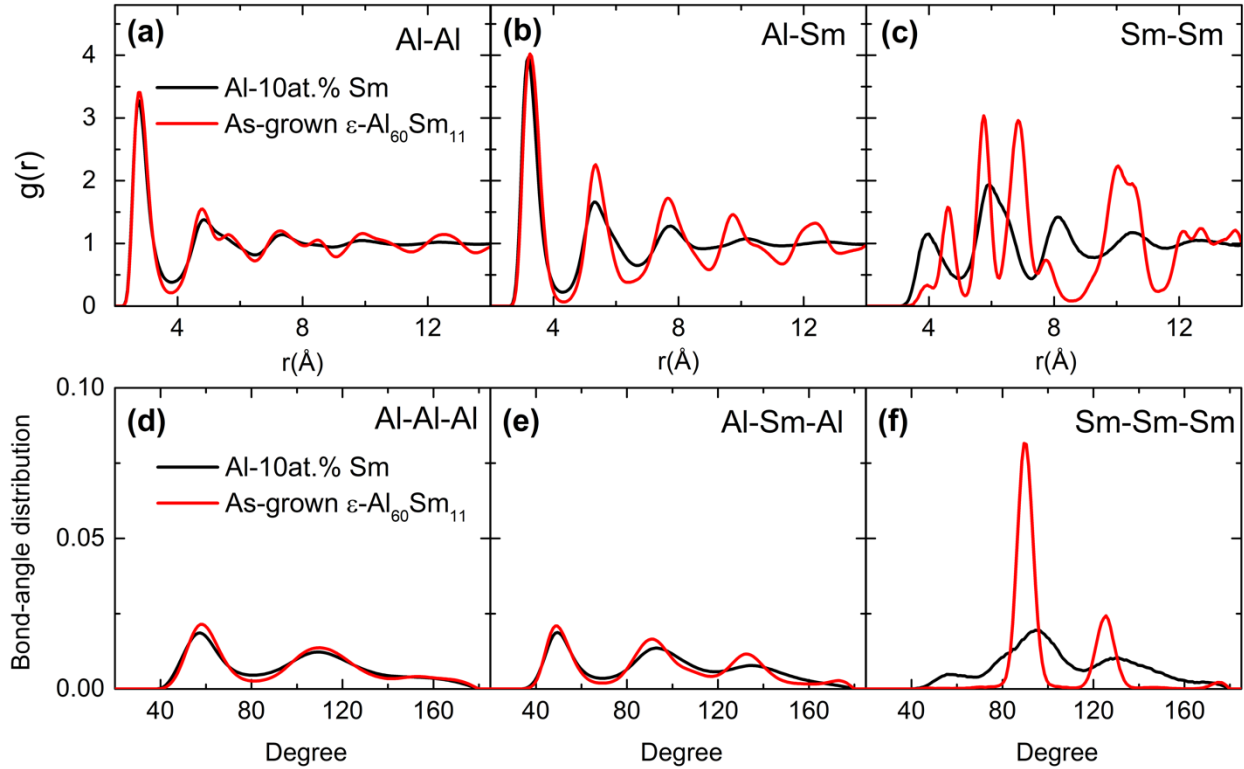


Fig. 2 The PCFs and bond angle distributions in the undercooled Al-10at.% Sm liquid and as-grown $\epsilon\text{-Al}_{60}\text{Sm}_{11}$ phase. (a) Al–Al PCF; (b) Al–Sm PCF; (c) Sm–Sm PCF; (d) Al–Al–Al angle distribution; (e) Al–Sm–Al angle distribution; (f) Sm–Sm–Sm angle distribution. The bond length cutoffs are chosen to be 3.8 \AA for the Al–Al pair, 4.2 \AA for the Al–Sm pair and 5.2 \AA for the Sm–Sm pair according to the PCFs.

3.2 Alignment analysis of atomic clusters

A comprehensive picture of the structural order requires not only bond length and bond angle distributions, but also an explicit identification of the local packing motif. While lacking long-range translational symmetry, the undercooled metallic liquids and glasses have clear elements of short- and medium-range order [6,19–25]. Many studies have led to the conclusion that the solute-centered atomic clusters are representative structural elements and fundamental building block in metallic structures [6,20,26]. Therefore, we investigate the transformation of local order around the solute Sm atoms and its relationship to the crystallization process. A close inspection

can find two types of Sm centered clusters in the ϵ -Al₆₀Sm₁₁, namely, 3661 and 16661 motifs [12] as shown in Fig. 3(a) and (b), respectively. Figure 3(c) shows the arrangement of two motifs in the crystal structure. The 3661 motif is also found to be dominant in the Al-10at.% Sm liquid and glass[27,28]. To understand how these motifs evolve during the crystallization, we employ the alignment analysis[27] for Sm-centered clusters, using 3661 and 16661 motifs as templates following the individual template-cluster alignment procedure described in Ref.[14]. The alignment score, describing how an as-extracted cluster deviates from the perfect template, is defined as

$$f = \min_{\alpha} \sqrt{\frac{1}{N} \sum_{i=1}^N \frac{(\mathbf{r}_{ci} - \alpha \mathbf{r}_{ti})^2}{(\alpha \mathbf{r}_{ti})^2}} \quad (1)$$

where N is the number of the neighbor atoms in the templates; \mathbf{r}_{ci} and \mathbf{r}_{ti} are the atomic coordinates in the aligned clusters and template, respectively; and α is the optimal scaling coefficient of the bond length in the template. A smaller alignment score represents less deviation of the cluster from the template. Each as-extracted cluster from the sample is aligned to both 3661 and 16661 templates, respectively. Figure 3(d) and (e) show the distribution of alignment scores f_{3661} and f_{16661} for Sm-centered clusters extracted from the liquid and the as-grown crystal.

In Fig. 3(d), the score distribution of liquid clusters shows a single peak at (0.19,0.24) in the f_{3661} - f_{16661} plane. Both f_{3661} and f_{16661} values at the peak position are relatively high, indicating an overall disordered state. On the other hand, f_{3661} is still significantly smaller than f_{16661} at the peak position, showing that the undercooled liquid has a more pronounced 3661-type order. This is consistent with our previous analysis [27]. In the as-grown crystal, the clusters are clearly separated into two groups centered at (0.17,0.10) and (0.12,0.24) in Fig. 3(e). These two groups correspond to 3661 and 16661 type clusters, respectively. Using a cut-off value $f_c = 0.15$ shown

as the dash line in the figure, clusters with scores below 0.15 can be divided into 3661 and 16661 types. In the Fig. 4(f), we plot the populations of each type of clusters as a function of the simulation time. In the initial liquid, while there is no 16661-type clusters, ~10% Sm centered clusters of the growing part has already formed 3661-type motif, indicating pre-existing 3661-type clusters in the liquid. During the growth process, the number of disordered clusters (alignment scores > 0.15) decreases while 3661-type and 16661-type clusters increases. The curves of 3661 and 16661 populations are almost parallel, indicating the two types of local orders are formed in parallel during the growth. The crystallization ends at 225 ns resulting in plateaus on all three curves. During the crystallization process, we can monitor the growth of the crystal by the increase in population of 3661 and 16661 clusters. Knowing the density of these clusters in the crystal, we can convert the slope of time-dependent population increase to interface velocity by $v = \frac{|k|}{2\rho A}$, where k is the slope of the linear fitting in Fig. 3(f), ρ is the Sm density in $\epsilon\text{-Al}_{60}\text{Sm}_{11}$ phase and A is the area of cross section normal to the growth direction. The factor 2 accounts for two interfaces of the crystal slab. We obtained a value of 0.081 \AA/ns for the interface velocity in our simulation.

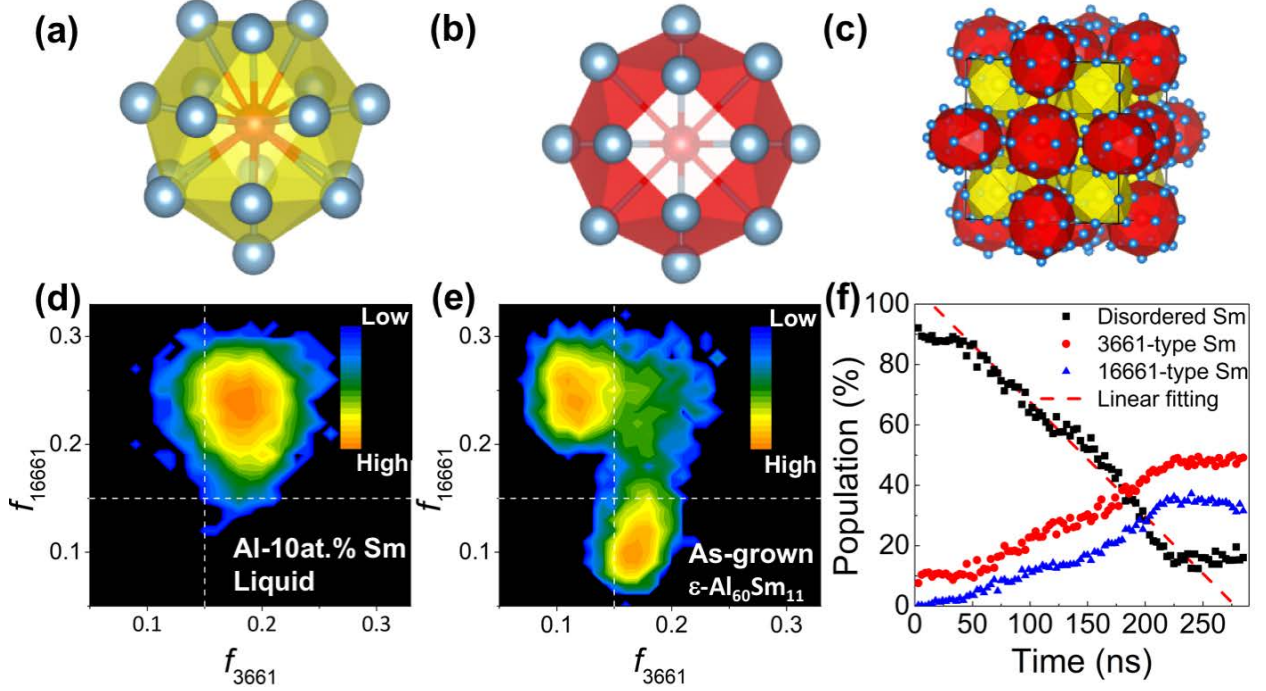


Fig. 3 (a) 3661-type cluster. (b) 16661-type cluster. Red ball stands for Sm and blue for Al. (c) The arrangement of 3661-type clusters (yellow) and 16661-type clusters (red) in the ϵ -Al₆₀Sm₁₁ structure. (d) and (e) The (f_{3661}, f_{16661}) score distribution of the Sm clusters from the liquid and as-grown ϵ -Al₆₀Sm₁₁ structure, respectively. The dash line indicates 0.15 as the threshold to classify the different types of clusters. (f) The population of 3661-type, 16661-type and disordered clusters as a function of simulation time. The linear fitting is used to estimate the interface velocity.

3.3 Dynamical characteristics during the crystallization

In addition to understanding of structural transformation from the localized SRO of liquid structure to the long-range crystalline order, the dynamical characteristics is also important to understand the transformation pathway. In Fig. 4, we trace the trajectory of a Sm atom when it attaches to the solid from the liquid. When the Sm atom is in the disordered liquid state, it diffuses continuously and the atomic trajectory shows “random walk”-like characters. When the atom approaches the ϵ -Al₆₀Sm₁₁ phase, the diffusion becomes more localized with occasional jumps at the solid-liquid interface. Eventually, the atom becomes solid-like and only vibrates at the crystalline site.

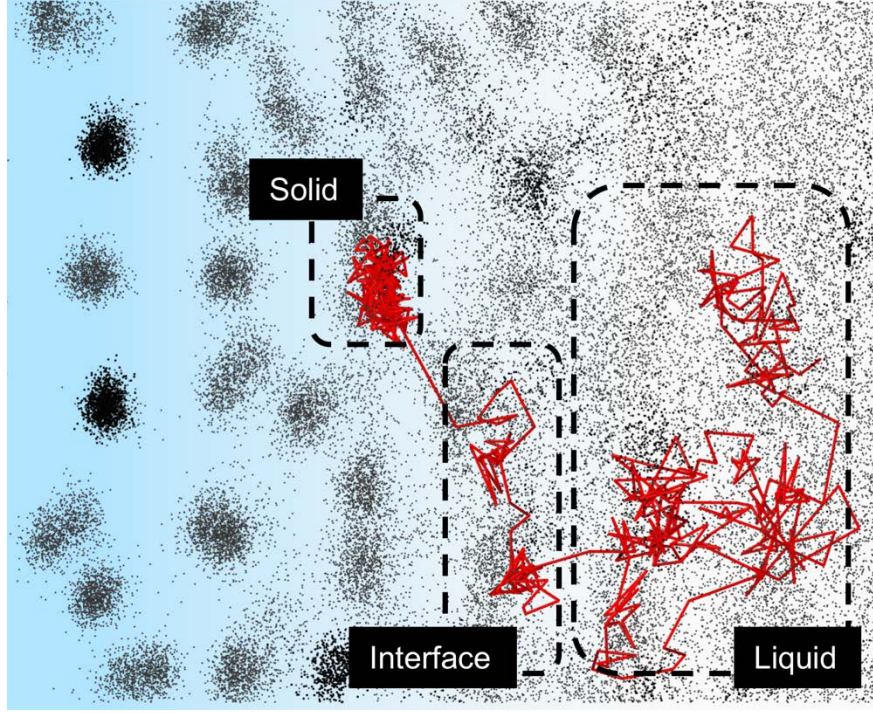


Fig. 4 A projected trajectory of a Sm atom transiting from liquid to solid during the ϵ -Al₆₀Sm₁₁ growth. The atom positions at contiguous time steps are connected. The dots on the background are the surrounding atoms in the whole trajectory.

Based on the different atom motion in solid and liquid, we employ a dynamical order parameter $\delta = |\vec{r}(t) - \vec{r}(t - \Delta t)|$ to calculate the displacement that an atom moves within a time interval Δt . Based on this parameter, the attachment and detachment transition between liquid and solid can be well identified with a threshold δ_c [30]. Here, a larger sample with 61,344 atoms is simulated for better statistical analysis. The threshold is chosen as $\delta_c = 1.2 \text{ \AA}$ with $\Delta t = 1.5 \text{ ns}$ for Sm atoms according to the dynamical parameter distributions of two phases in Fig. 5(a). The time and position of the attachment and detachment events are plotted in Fig. 5(b). Therefore, the attachment rate R_a and detachment rate R_d , which is defined as the number of attached/detached atoms in unit time at unit area, can be obtained by averaging all the events during the simulation. Here, we obtained $R_a = 8.70 \times 10^{-4} \text{ \AA}^{-2} \text{ ns}^{-1}$ and $R_d = 3.83 \times 10^{-4} \text{ \AA}^{-2} \text{ ns}^{-1}$. Based on the

attachment/detachment rate, one can also derive the interface velocity with $v = \frac{|R_a - R_d|}{\rho}$, where ρ is the Sm density in the ϵ -Al₆₀Sm₁₁ phase. The interface velocity based on the dynamical parameter is 0.095 Å/ns, which is consistent with the interface velocity determined by the structural analysis previously.

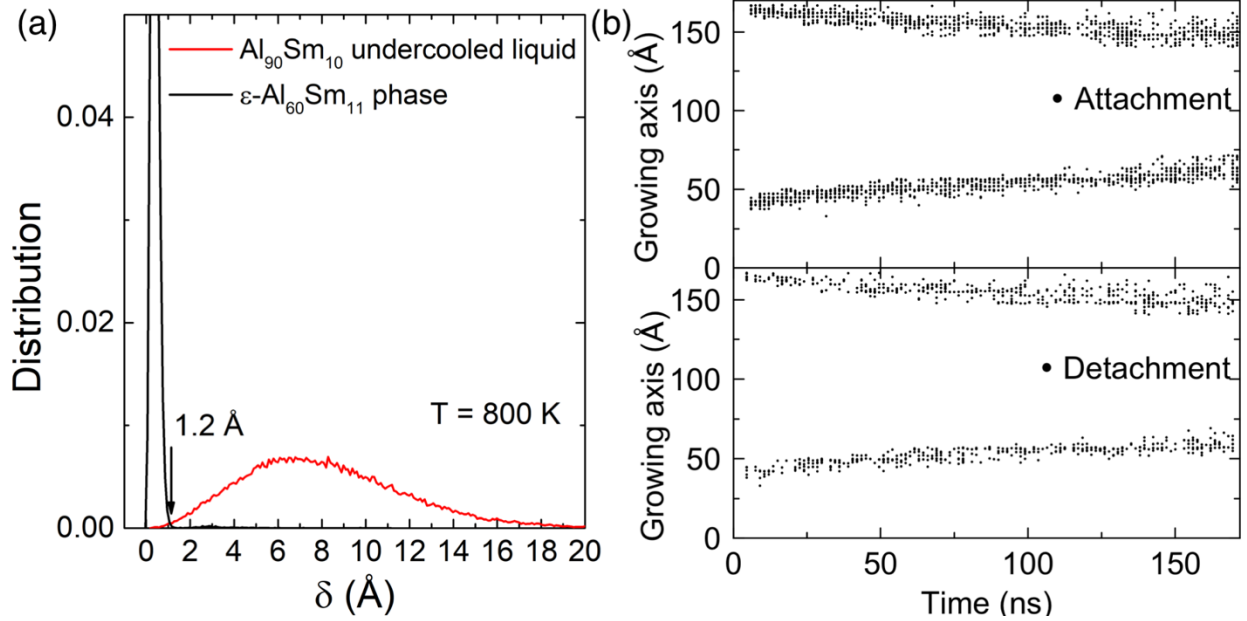


Fig. 5 (a) The distribution of dynamical order parameter δ in the Al-10at.% Sm undercooled liquid and ϵ -Al₆₀Sm₁₁ at 800 K. The threshold for labelling an atom either as liquid or as solid is chosen as 1.2 Å which is the crosspoint of the two curves. (b) The time and coordinates of the attachment and detachment events. Only the coordinates at the growing axis are plotted.

Conclusion

In summary, using the MD simulations we investigate structural and dynamical evolutions in the polymorphic transformation from the Al-10at.% Sm undercooled liquid to the crystalline ϵ -Al₆₀Sm₁₁ phase. The analysis of the PCF and bond angle distribution illustrates similar local atomic arrangements around Al atoms but dramatically different Sm-Sm networking between the liquid and the as-grown crystal structures. A common Sm-centered cluster motif is revealed as a structural precursor in the undercooled liquid. By using the alignment score as the order

parameter, we characterized the order development during the crystallization. Moreover, we identified the atomic transformation pathway and obtained atomic attachment/detachment rates based on atomic motions. The interface velocity is derived consistently by both structural and dynamical order parameters. These results pave the way to a phase-field description for detailed realistic simulations of the devitrification process.

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