

# Maximizing Revenue from Electrical Energy Storage in MISO Energy & Frequency Regulation Markets

Tu A. Nguyen, Raymond H. Byrne and Ricky J. Concepcion  
 Sandia National Laboratories, Albuquerque, NM 87185  
 Email: tunguy@sandia.gov, rhbyrne@sandia.gov, rconcep@sandia.gov.

**Abstract**—FERC Order 755 requires RTO/ISOs to compensate the frequency regulation resources based on the actual regulation service provided. Based on this rule, a resource is compensated by a performance-based payment including a capacity payment which accounts for its provided regulation capacity and a performance payment which reflects the quantity and accuracy of its regulation service. The RTO/ISOs have been implementing different market rules to comply with FERC Order 755. This paper focuses on the MISO's implementation and presents the calculations to maximize the potential revenue of electrical energy storage (EES) from participation in arbitrage and frequency regulation in day-ahead market using linear programming. A case study was conducted for the Indianapolis Power & Light's 20MW/20MWh EES at Harding Street Generation Station based on MISO historical data from 2014 and 2015. The results showed the maximum revenue was primarily produced by frequency regulation.

**Index Terms**—FERC Order 755, frequency regulation market, energy arbitrage, electrical energy storage, capacity payment, performance-based payment, optimization, linear programming.

## I. INTRODUCTION

In the recent years, with the improvement in energy storage and power electronics technologies and the changes in the electricity marketplace, there has been a growing opportunity for grid-scale energy storage to provide services to the grid [1]. The cost-effective deployment of current electrical energy storage (EES) technologies depends on two main factors: 1) Policy and regulation that enable energy storage to resolve grid problems; 2) How energy storage might provide value in the current electricity markets [2].

In 2007 the Federal Energy Regulatory Commission (FERC) issued Order 890 to ensure the fair and equitable participation of non-generation resources in the markets [3]. To comply with this rule, the ISOs enhanced their market tariffs to allow demand response as well as energy storage resources to bid in their energy and ancillary services markets. Under these market rules, energy storage could generate revenue streams from energy arbitrage and participation in frequency regulation market. Arbitrage is the practice of buying energy during times of low demand when energy price is low and selling energy during times of peak demand when energy price is high. Frequency regulation service involves the increase (regulation up) or reduction (regulation down) of active power generation to the power grid to maintain the system frequency. It is

important to note that revenue from energy arbitrage and regulation services are only two among the benefits of EES. A complete review of EES revenue benefits is presented in [1].

In 2011 FERC issued Order 755 [4] which requires RTO/ISOs to compensate the frequency regulation resources based on the actual regulation service provided. Based on this rule, a resource is compensated by a performance-based payment including a capacity payment which accounts for its provided regulation capacity and a performance payment which reflects the quantity and accuracy of its regulation service. The RTO/ISOs have been implementing different changes to their market rules to comply with FERC Order 755. These changes involve the modifications in the market clearing processes and the introductions of performance tests and performance-based payments.

This paper focuses on the MISO's implementation and presents the calculations to maximize the potential revenue of electrical energy storage from participation in arbitrage and arbitrage combined with frequency regulation in MISO day-ahead market. The approach requires historical data of day-ahead energy and reserve market prices. In this approach, the revenue maximizations are formulated as linear programming problems in which the constraints are based on the energy storage model presented in [5]. The results provide the maximum revenue in the best-case scenario (with perfect knowledge of price data) that can be used to score other trading strategies. This approach is only valid for scenarios where the size of the storage is such that it does not impact market prices. For large systems that might impact the market, a production cost modeling approach must be implemented.

A similar approach has been used in the previous studies to investigate maximum revenue of an EES in CAISO [6], ERCOT [7] and PJM [8]. This paper extends the approach to include two-part performance-based payment as implemented in MISO. A case study was conducted for the Indianapolis Power & Light's 20MW/20MWh EES at Harding Street Generation Station based on MISO historical data from 2014 and 2015.

## II. MISO PERFORMANCE-BASED COMPENSATION

In order to comply with FERC Order 755 [4], in December 2012 MISO began performance-based compensation for frequency regulation services [9]. MISO enhanced its market

rules to provide two-part regulation payment to frequency regulation resources. Specifically, under MISO's market rules a regulation resource is required to submit a two-part regulation offer which include two components [10]:

- 1) Regulation capacity offer  $O_t^{\text{RegC}} [\$/\text{MWh}]$  represents the opportunity cost to hold capacity in reserve for frequency regulation.
- 2) Regulation mileage offer  $O_t^{\text{RegM}} [\$/\text{MW}]$  reflects the cost of movement to follow AGC regulation signals

The combined offer  $O_t^{\text{Reg}} [\$/\text{MWh}]$  which is used in market clearing process is specified as follows:

$$O_t^{\text{Reg}} = O_t^{\text{RegC}} + \alpha O_t^{\text{RegM}} \quad (1)$$

in which  $\alpha$  is the mileage-to-capacity ratio. Based on historical data, MISO uses an average market-wide value  $\alpha = 0.6/5\text{min}$  (or  $7.2/h$ ) [9]. The combined offer  $O_t^{\text{Reg}} [\$/\text{MWh}]$  is the total cost for a resource to reserve 1MWh of capacity and to move  $\alpha\text{MW}$  of mileage in an hour.

After the market (day-ahead or real-time) is cleared, MISO uses the regulation market clearing price  $\text{MCP}_t^{\text{Reg}} [\$/\text{MWh}]$  to pay a resource for its cleared regulation capacity  $q_t^{\text{Reg}} [\text{MWh}]$ . This payment of  $q_t^{\text{Reg}} \text{MCP}_t^{\text{Reg}} [\$]$  covers the capacity payment for  $q_t^{\text{Reg}} [\text{MWh}]$  of capacity reserve and the mileage payment for  $\alpha q_t^{\text{Reg}} [\text{MW}]$  during hour  $t$ .

In order to evaluate a resource's performance, the following quantities are defined for each 5-min interval  $i$  based on MISO's AGC stepped set point  $s$  and the resource's actual response  $q$  at each 4-second step:

- Instructed mileage [MW]:

$$q_i^{\text{insM}} = \sum_{k=1}^N |s_k - s_{k-1}| \quad (2)$$

in which  $N = 75$  is the number of stepped signals in 5-min interval.

- Desired mileage [MW]:

$$q_i^{\text{desM}} = \sum_{k=1}^N |s_k - q_{k-1}| \quad (3)$$

- Target mileage [MW]:

$$q_i^{\text{tagM}} = \min\{q_i^{\text{insM}}, q_i^{\text{desM}}\} \quad (4)$$

- Actual mileage [MW]:

$$q_i^{\text{actM}} = \sum_{k=1}^N (|s_{k-1} - q_{k-1}| - |s_{k-1} - q_k|) \quad (5)$$

- Performance test for interval  $i$ :

$$\eta_i = \frac{q_i^{\text{actM}}}{q_i^{\text{desM}}} \begin{cases} \geq 0.7 & \text{Pass} \\ < 0.7 & \text{Fail} \end{cases} \quad (6)$$

- Performance test for hour  $t$ :

$$\eta_t = \begin{cases} 0 \text{ (Fail)} & \eta_i < 0.7 \text{ for 4 consecutive intervals} \\ 1 \text{ (Pass)} & \text{otherwise} \end{cases} \quad (7)$$

The regulation compensation is then adjusted based on the resource's actual performance. MISO uses the regulation mileage market clearing price  $\text{MCP}_t^{\text{MIL}} [\$/\text{MW}]$ , which is the highest mileage offer from all resources [10], to pay (or charge) the resource for its additional (or undeployed) mileage. The adjustment at interval  $i$  to the regulation compensation of hour  $t$  are calculated as follows:

- Payment for additional mileage when  $q_i^{\text{tagM}} \geq \frac{\alpha}{12} q_t^{\text{Reg}}$ :
$$A_t^i = \begin{cases} \left( q_i^{\text{tagM}} - \frac{\alpha}{12} q_t^{\text{Reg}} \right) \text{MCP}_t^{\text{MIL}} & \text{if } \eta_i \geq 0.7 \\ \eta_i \left( q_i^{\text{tagM}} - \frac{\alpha}{12} q_t^{\text{Reg}} \right) \text{MCP}_t^{\text{MIL}} & \text{if } \eta_i < 0.7 \end{cases} \quad (8)$$
- Charge for undeployed mileage when  $q_i^{\text{tagM}} < \frac{\alpha}{12} q_t^{\text{Reg}}$ :

$$U_t^i = \left( \frac{\alpha}{12} q_t^{\text{Reg}} - q_i^{\text{tagM}} \right) \text{MCP}_t^{\text{MIL}} \quad (9)$$

The total regulation compensation of hour  $t$  after adjustment is specified as:

$$R_t^{\Sigma} = \eta_t \left[ q_t^{\text{Reg}} \text{MCP}_t^{\text{Reg}} + \sum_{i=1}^M (A_t^i - U_t^i + W_t^i) \right] \quad (10)$$

in which  $W_t^i$  is the make-whole payment from MISO to compensate for the total profit loss in interval  $i$  due to the fact that the undeployed mileage is charged back at the mileage market clearing price  $\text{MCP}_t^{\text{MIL}}$  which is higher than the mileage offer  $O_t^{\text{RegM}}$  of the resource; and  $M = 12$  is the number of intervals in an hour.

Based on historical data of 2013, the followings have been observed by MISO [9]:

- The resources fail the hourly performance test by 23% of the time on a monthly average basis. This means the probability for the resources to receive their regulation credit is 77%.
- The payment for extra mileage and the charge for undeployed mileage on monthly average basis are very close to each other by updating the deployment ratio (or mileage-to-capacity ratio  $\alpha$ ) every month.
- The make-whole payment for undeployed mileage is a small percentage (approximately 3%) of the monthly regulation revenue.

It is important to note that the performance of a regulation resource is highly coupled with its ramp rate. An EES with high ramp rate such as flywheel or battery system might pass the performance test more frequently than 77% of the time. However, in this paper 77% is used as the conservative performance test pass-rate which can be applied to any EES technologies without knowing their ramp rates. Therefore, the monthly regulation compensation can be approximated as:

$$\sum_{t=1}^T R_t^{\Sigma} = 0.77 \times 1.03 \sum_{t=1}^T (q_t^{\text{Reg}} \text{MCP}_t^{\text{Reg}}) \quad (11)$$

### III. ELECTRICAL ENERGY STORAGE (EES) MODEL

An EES system is generally characterized by the following parameters:

TABLE I  
STORAGE PARAMETERS

Symbol	Storage Parameter
$\tau$	Time period length (e.g., one hour)
$T$	Number of time periods in the optimization
$\bar{q}^D$	Maximum energy sold in a single period (MWh)
$\bar{q}^R$	Maximum energy bought in a single period (MWh)
$\bar{S}$	Maximum energy capacity (MWh)
$\gamma_s$	Storage efficiency over one period (%)
$\gamma_c$	Conversion efficiency (%)

- 1) Power Rating [MW]: The maximum power that the EES can charge or discharge.
- 2) Energy Capacity [J or MWh]: The amount of energy that the EES can store.
- 3) Efficiency [%]: Efficiency can be broken into two components: conversion efficiency,  $\gamma_c$ , and storage efficiency,  $\gamma_s$ . The conversion efficiency represents the conversion losses encountered when energy is stored during charge and released during discharge. The storage efficiency describes the time-based losses in the EES system.
- 4) Ramp Rate [MW/min]: The ramp rate describes how quickly the EES can change its power level.

In this paper, the quantity of energy charged and discharged during each time period are analyzed. For arbitrage, the EES will maintain a constant output power over each time period. For regulation, it is assumed that the EES is capable of tracking the regulation signal at high ramp rate (i.e., the ramping time is negligible). If the ramp rate is slow compared to the time period, this approximation does not hold and a model that incorporates ramp rate must be employed.

The parameters involved in storage system constraints are shown in Table I. Thus, the maximum quantity that can be sold/discharged and bought/recharged in a single period are specified as follows:

$$\bar{q}^D = (\text{Maximum discharge power level}) \times \tau \quad (12)$$

$$\bar{q}^R = (\text{Maximum recharge power level}) \times \tau \quad (13)$$

For the EES that provides only energy arbitrage, there are two decision variables in the optimization: the energy sold (discharged)  $q_t^D$  and the energy purchased (recharged)  $q_t^R$  at time  $t$ , which are assumed to be non-negative. They are subjected to the following constraints :

$$0 \leq q_t^R \leq \bar{q}^R, \forall t \in T \quad (14)$$

$$0 \leq q_t^D \leq \bar{q}^D, \forall t \in T \quad (15)$$

In this case, the state of charge (SOC)  $S_t$  at any time  $t$  is given by:

$$S_t = \gamma_s S_{t-1} + \gamma_c q_t^R - q_t^D \quad \forall t \in T \quad (16)$$

which states that the SOC at time  $t$  is the SOC at time  $t-1$  adjusted for storage plus any net charging (adjusted for conversion losses) minus the quantity discharged during  $t$ .

For the EES that is participating in energy arbitrage and frequency regulation market, an additional decision variable must be added to capture the quantity allocated to the regulation reserve,  $q_t^{\text{REG}}$ , which is assumed to be non-negative. This allocation to regulation reduces the maximum potential quantities allocated to arbitrage subjected to the charge/discharge constraints:

$$0 \leq q_t^R + q_t^{\text{REG}} \leq \bar{q}^R, \forall t \in T \quad (17)$$

$$0 \leq q_t^D + q_t^{\text{REG}} \leq \bar{q}^D, \forall t \in T \quad (18)$$

In regulation market, there is no guarantee that the capacity reserved will actually deployed. Therefore, it is useful to define the RegUp efficiency  $\gamma_t^{\text{RU}}$  and the RegDown efficiency  $\gamma_t^{\text{RD}}$  as the fraction of the reserve capacity which is actually deployed for RegUp/RegDown at time  $t$ . Thus, the SOC at time  $t$  of an EES participating in arbitrage and regulation is given by:

$$S_t = \gamma_s S_{t-1} + \gamma_c q_t^R - q_t^D + \gamma_c \gamma_t^{\text{RD}} q_t^{\text{REG}} - \gamma_t^{\text{RU}} q_t^{\text{REG}}, \forall t \in T \quad (19)$$

In both cases, the SOC must be within its physical limits as described in the following constraint:

$$0 \leq S_t \leq \bar{S}, \forall t \in T \quad (20)$$

#### IV. MAXIMIZING EES REVENUE

In this paper, the problem of maximizing revenue from an EES is formulated as an LP optimization problem [11]. The objectives are to maximize the potential revenue of an EES in two different scenarios including arbitrage and arbitrage combined with participation in the regulation market. The constraints are enforced using the aforementioned EES model.

Specifically, the optimizations are formulated as follows where all the variables and parameters are defined in Table. II:

- Arbitrage:

$$\text{Max} \sum_{t=1}^T [(P_t - C_d) q_t^D - (P_t + C_r) q_t^R] e^{-rt} \quad (21)$$

s.t. (14), (15) and (20).

- Arbitrage and regulation:

$$\text{Max} \sum_{t=1}^T [(P_t - C_d) q_t^D - (P_t + C_r) q_t^R + 0.77 \times 1.03 q_t^{\text{REG}} \text{MCP}_t^{\text{REG}}] e^{-rt} \quad (22)$$

s.t. (17), (18) and (20).

In many areas, the net energy for regulation is settled at the real-time price. This provides an additional arbitrage opportunity between the day ahead price and the real-time price. For this analysis, the price  $P_t$  was assumed to represents both. While this does not reflect the actual settlement process, it keeps the optimization from incorporating any arbitrage between the day ahead and the real-time market.

TABLE II  
NOMENCLATURES

Symbol	Description
$P_t$	LMP for energy at time $t$ [\$/MWh]
$C_d$	Cost for discharging [\$/MWh]
$C_r$	Cost for recharging [\$/MWh]
$q_t^D$	Energy discharged at time $t$ [MWh]
$q_t^R$	Energy charged at time $t$ [MWh]
$q_t^{\text{REG}}$	Regulation capacity at time $t$ [MWh]
$\text{MCP}_t^{\text{REG}}$	Regulation market clearing price at time $t$ [MWh]
$e^{-rt}$	Discounting term (time value of money)

## V. A CASE STUDY

In this section, the maximum revenue for arbitrage and frequency regulation of the EES system located at Harding Street Generation Station of Indianapolis Power & Light is evaluated. The Harding Street EES is a 20MW/MWh Li-ion battery energy storage system (BESS) which mainly focuses on primary frequency response, however, it can also provide other ancillary services such as energy arbitrage or frequency regulation [12].

The optimizations as formulated in (21) and (22) were solved on monthly basis with the following inputs:

- MISO historical price data of 2014 and 2015 [13] were used.
- Hourly day-ahead prices for node IPL.16STOU606 were used.
- Both RegUp and RegDown efficiencies are assumed to be 25%:  $\gamma_t^{\text{RU}} = \gamma_t^{\text{RD}} = 0.25$ .
- The system's efficiencies are approximated as:  $\gamma_s = 1$  and  $\gamma_c = 0.85$ .
- The discharging and recharging cost were neglected:  $C_d = C_r = 0$ .
- The discount rate was neglected:  $r = 0$ .
- The SOC is maintained at 50% at the end of each day.

The monthly revenue of 2014 and 2015 in both scenarios using perfect knowledge are shown in Figure 1. The revenue from arbitrage combined with regulation service is shown much higher than from arbitrage only. Optimal results for arbitrage combined with regulation are shown in Table III in which  $\%q^R$ ,  $\%q^D$  and  $\%q^{\text{REG}}$  respectively represent the time (percentage) each month for recharging, discharging and regulation; and  $R^{\text{arb}}$ ,  $R^{\text{reg}}$  and  $R^{\text{tot}}$  are arbitrage, regulation and total revenue. The optimal policy in this case is to participate in regulation market the majority of the time while maintaining the SOC by arbitrage. Therefore, the majority of monthly revenue is from frequency regulation. The revenue from arbitrage is low and in many cases is negative due to the purchased energy to compensate for the losses while participating in frequency regulation. The regulation revenue is decreasing from 2014 to 2015 as a result of the decrease in

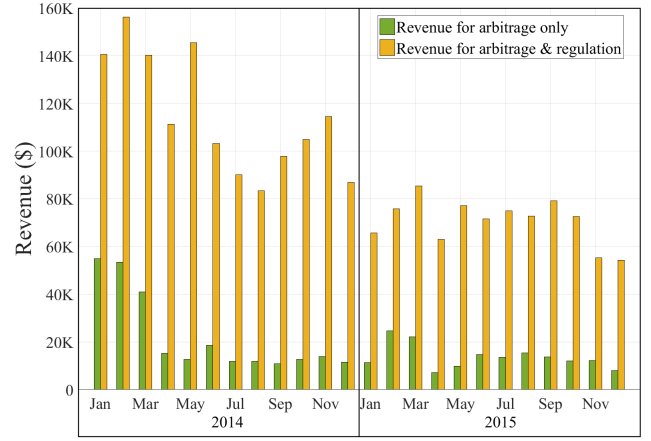


Fig. 1. Optimization Results

TABLE III  
ARBITRAGE AND REGULATION OPTIMIZATION RESULTS 2014-2015

Month	$\%q^R$	$\%q^D$	$\%q^{\text{REG}}$	$R^{\text{arb}}$	$R^{\text{reg}}$	$R^{\text{tot}}$
01/14	34.01	5.65	96.77	\$14.99K	\$125.64K	\$140.63K
02/14	37.20	6.55	96.88	\$17.24K	\$138.99K	\$156.23K
03/14	30.78	4.03	98.66	\$4.62K	\$135.58K	\$140.20K
04/14	18.75	2.08	99.86	-\$13.31K	\$124.56K	\$111.24K
05/14	16.13	1.34	100.0	-\$14.76K	\$160.14K	\$145.37K
06/14	26.39	3.47	99.86	-\$4.53K	\$107.82K	\$103.29K
07/14	21.77	1.88	100.0	-\$10.34K	\$100.41K	\$90.07K
08/14	22.31	2.82	100.0	-\$10.30K	\$93.72K	\$83.42K
09/14	19.03	1.11	100.0	-\$11.37K	\$109.12K	\$97.75K
10/14	14.78	1.34	100.0	-\$13.45K	\$118.31K	\$104.85K
11/14	14.44	0.42	100.0	-\$16.19K	\$130.69K	\$114.49K
12/14	21.77	2.42	99.73	-\$11.06K	\$97.92K	\$86.86K
<b>Total</b>				<b>-\$68.51K</b>	<b>\$1,442.96K</b>	<b>\$1,374.45K</b>
01/15	21.64	2.55	99.46	-\$10.38K	\$76.03K	\$65.65K
02/15	34.67	4.91	98.21	\$1.34K	\$74.47K	\$75.81K
03/15	33.47	3.90	98.12	-\$0.58K	\$86.02K	\$85.43K
04/15	17.92	2.08	100.0	-\$11.8K	\$74.89K	\$63.08K
05/15	23.39	2.55	100.0	-\$9.58K	\$86.79K	\$77.21K
06/15	31.94	3.19	100.0	-\$4.33K	\$76.00K	\$71.66K
07/15	29.30	2.42	100.0	-\$6.31K	\$81.31K	\$74.99K
08/15	37.37	3.49	100.0	-\$3.75K	\$76.47K	\$72.72K
09/15	29.31	2.36	100.0	-\$5.82K	\$84.91K	\$79.08K
10/15	20.97	2.69	99.87	-\$8.50K	\$81.01K	\$72.51K
11/15	28.19	3.47	99.72	-\$7.16K	\$62.48K	\$55.31K
12/15	18.82	2.15	99.73	-\$8.88K	\$63.19K	\$54.30K
<b>Total</b>				<b>-\$75.79K</b>	<b>\$923.62K</b>	<b>\$847.82K</b>

energy price which reduces the opportunity cost for holding capacity reserve.

Without perfect knowledge of the prices,  $D - 1$  forecast method was used. In other words, price data of the prior day were used to determine trading policy for the current day. The results are as follows:

- Arbitrage only: the annual revenues were approximately 93.2% of 2014's and 95.9% of 2015's optimal revenues which were calculated with perfect knowledge.

- Arbitrage combined with regulation: the annual revenues were approximately 82.3% of 2014's and 86.5% of 2015's optimal revenues which were calculated with perfect knowledge. In the latter case, the errors in both energy and reserve market price create larger deviations from the optimal results.

## VI. CONCLUSIONS

In this paper, MISO's market rules for performance-based regulation payment have been reviewed. A linear programming approach has been used to estimate the potential revenues of an EES system in two cases: arbitrage only and arbitrage combined with frequency regulation. The approach was extended to include MISO's performance-based regulation payment. With perfect knowledge of the price data, the approach finds the upper bounds for the potential revenues which can be used for evaluating other trading strategies. A case study was conducted for the Indianapolis Power & Light's 20MW/20MWh EES at Harding Street Generation Station based on MISO historical data from 2014 and 2015. The results showed the revenues were much higher when participating in regulation market. The optimal policy in this case is to participate in regulation market the majority of the time while maintaining the SOC by arbitrage. Without perfect knowledge of the prices,  $D - 1$  trading policy can capture as much as 95.9% of the arbitrage-only optimal revenue and 86.5% of the arbitrage-regulation optimal revenue. Future work would consider the uncertainties of the forecast data as well as include a more sophisticated model that distinguishes different energy storage technologies in the approach.

## ACKNOWLEDGEMENT

The authors would like to thank Dr. Imre Gyuk and his colleagues at the Energy Storage Program at the U.S Department of Energy for funding this research. Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energys National Nuclear Security Administration under contract DE-AC04-94AL85000.

## REFERENCES

- [1] J. Eyer and G. Corey, "Energy storage for the electricity grid: Benefits and market potential assessment guide," Sandia National Laboratories, Albuquerque, NM, Tech. Rep. SAND2010-0815, Feb 2010.
- [2] J. Rittershausen and M. McDonagh, "Moving energy storage from concept to reality: Southern california edison approach to evaluating energy storage," Southern California Edison, Rosemead, CA, 2011.
- [3] "Final Rule Order No. 890: Preventing undue discrimination and preference in transmission service," Federal Energy Regulatory Commission, Feb 2007.
- [4] "Final Rule Order No. 755: Frequency regulation compensation in organized wholesale power markets," Federal Energy Regulatory Commission, October 2011.
- [5] A. Akhil, G. Huff, A. B. Currier, B. C. Kaun, D. M. Rastler, S. B. Chen, A. L. Cotter, D. T. Bradshaw, and W. D. Gauntlett, "DOE/EPRI 2013 electricity storage handbook in collaboration with nreca," Sandia National Laboratories, Tech. Rep. SAND2013-5131, Jul 2013.
- [6] R. H. Byrne and C. A. Silva-Monroy, "Estimating the maximum potential revenue for grid connected electricity storage: Arbitrage and the regulation market," Sandia National Laboratories, Albuquerque, NM, SAND2012-3863, resreport, 2012.
- [7] R. H. Byrne and C. A. Silva-Monroy, "Potential revenue from electrical energy storage in ERCOT: The impact of location and recent trends," in *2015 IEEE Power Energy Society General Meeting*, July 2015, pp. –.
- [8] R. H. Byrne, R. J. Conception, and C. A. Silva-Monroy, "Estimating potential revenue from electrical energy storage in PJM," in *2016 IEEE Power Energy Society General Meeting*, July 2016, pp. –.
- [9] K. E. Benn. (2014) Midcontinent independent system operator, inc. informational report docket no. er12-1664. [Online]. Available: <https://goo.gl/AV7E6U>
- [10] Y. Chen, R. Leonard, M. Keyser, and J. Gardner, "Development of performance-based two-part regulating reserve compensation on MISO energy and ancillary service market," *IEEE Transactions on Power Systems*, vol. 30, no. 1, pp. 142–155, Jan 2015.
- [11] E. P. Chong and S. Zak, *An introduction to Optimization*. John Wiley & Sons Inc., 2001.
- [12] DOE global energy storage database - iPL Advancing energy storage array. [Online]. Available: <http://www.energystorageexchange.org/projects/1774>
- [13] MISO-market reports. [Online]. Available: <https://goo.gl/rmm6l9>