



**(invited)**

# **The DC Response Of Electrically Conducting Fractures Excited By A Grounded Current Source**

**Chester J Weiss<sup>1</sup>, David F Aldridge<sup>1</sup>, Hunter A Knox<sup>1</sup>, Kimberly A  
Schramm<sup>1</sup> and Lewis C Bartel<sup>2</sup>**

*<sup>1</sup>Sandia National Laboratories*

*<sup>2</sup>CARBO Ceramics Inc.*

## Problem Statement and Approach

- Given an induced fracture system in a horizontal well with elevated electrical conductivity, what can be said about the fractures from surface measurements of DC potential differences?
- Forward model the Earth/borehole/fracture system with unstructured finite elements conformal to conductivity boundaries
  - compute the prefrack, postfrack and pre-post DC potential differences
  - parametric analysis of fracture conductivity effect
  - quantify topographic effects
  - linear inversion synthetic responses for simple fracture mapping

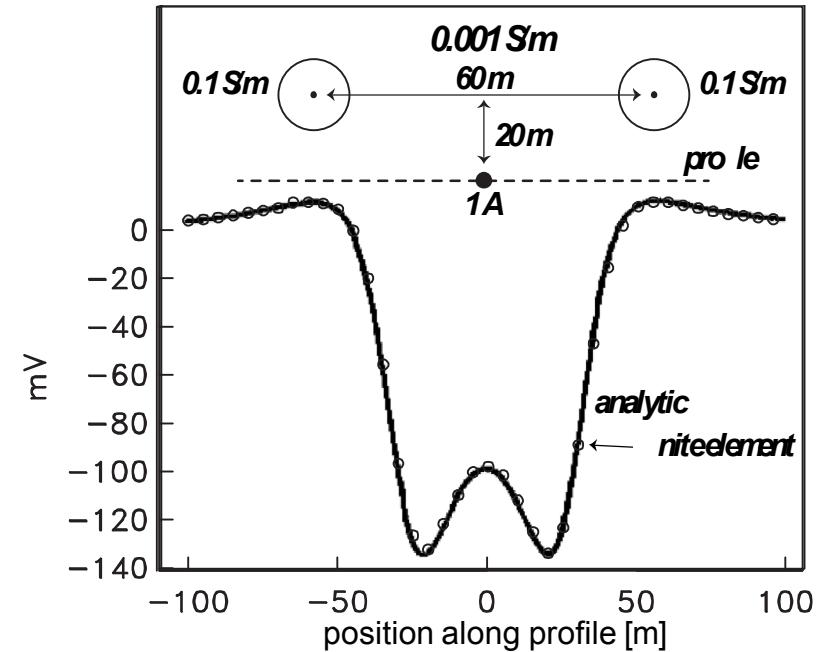
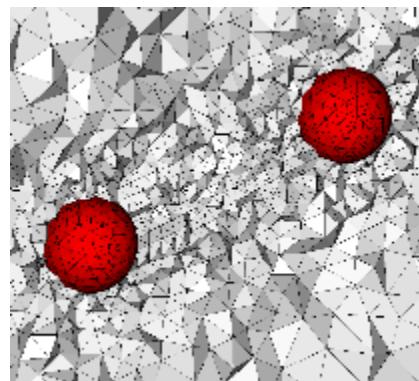
# Finite element forward solver: Benchmark test

Solve for electric scalar potential  $\Phi$  over an arbitrary conductivity model  $\sigma$  excited by a source current  $\mathbf{J}_s$ :

$$-\nabla \cdot (\sigma \nabla \Phi) = \nabla \cdot \mathbf{J}_s$$

Homogeneous Dirichlet BC on mesh bottom and sides, Neumann BC on mesh top to simulate air/Earth interface.

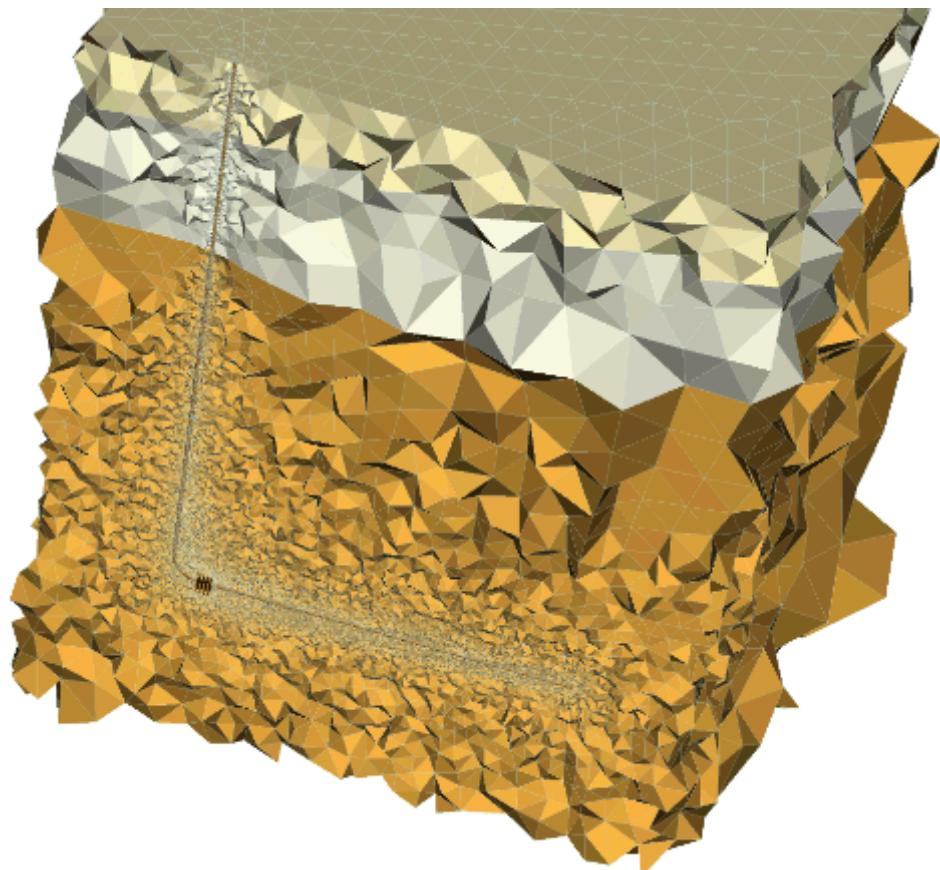
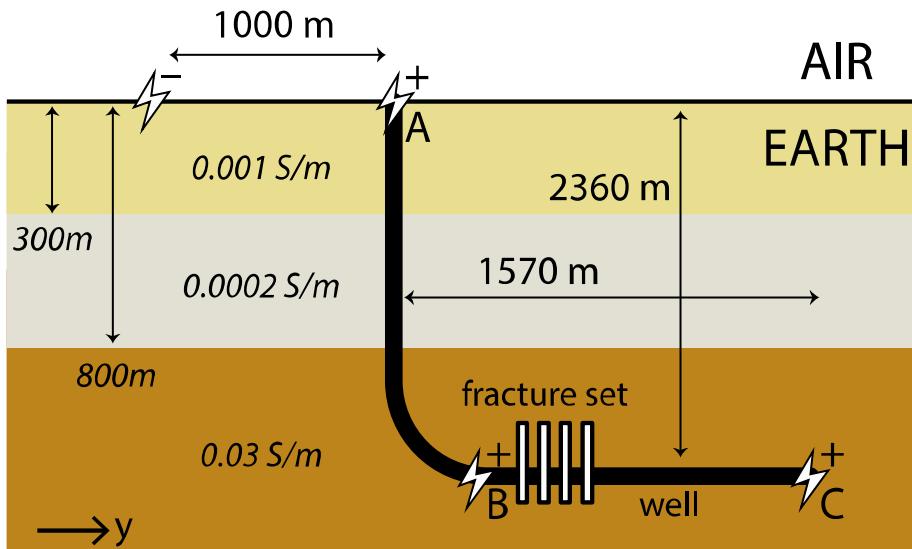
*(right)* finite element mesh for benchmark comparison against analytic solution of 2 spheres in a wholespace (Aldridge and Oldenburg, Geophysical Prospecting, 1989)



*(above)* comparison of finite element and analytic solutions of scattered electric potential for an offset point source

# Earth model of exploration scenario

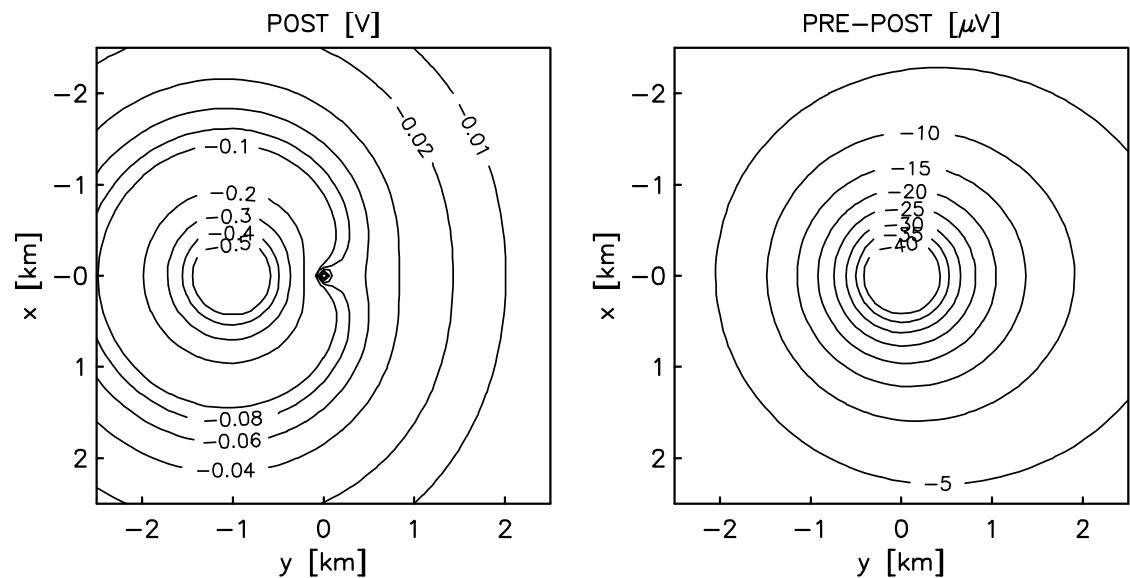
*Idealized (below) and discretized (right) Earth model for finite element analysis (FEA). Electrode location indicated by symbols, with 3 possible contact points (A-C) of the +ve electrode with steel well casing.*



# DC potential on the ground over the well head

**(left)** Plan view of electric potential (in Volts) at Earth's surface ( $z = 0$  m) over the well head ( $x = y = 0$  m) where the Earth model is energized by  $+1$  A current source at the well head (case A) and a  $-1$  A sink at  $y = 1000$  m.

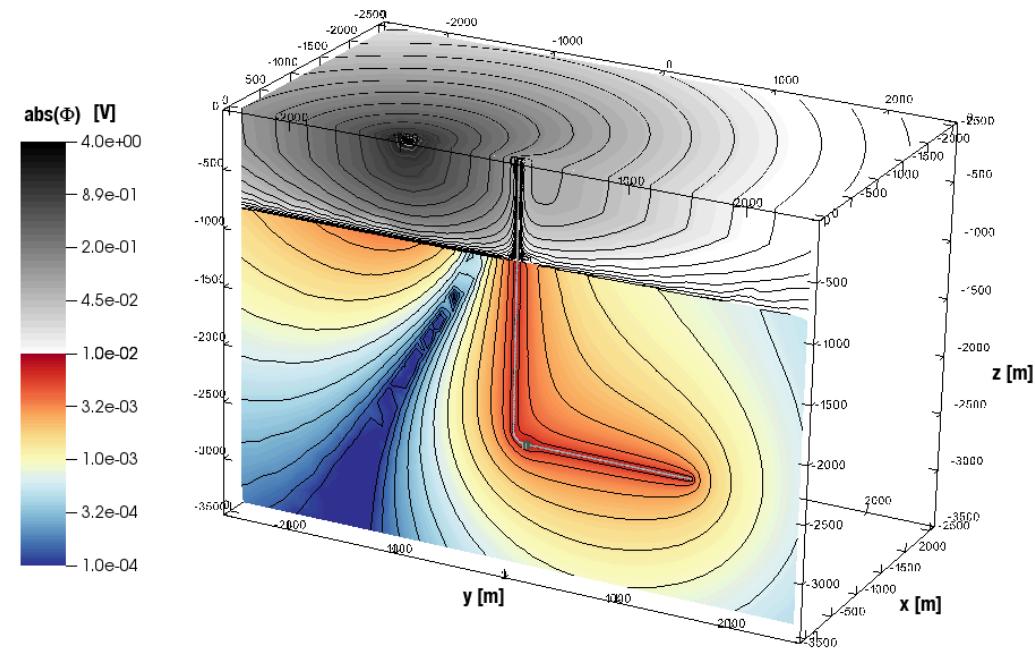
**(right)** Potential difference (in microvolts) at  $z = 0$  m computed by subtracting the response of the Earth model with a set of  $10$  S/m fractures from one where the fractures are absent, thus simulating a time-lapse scenario for detection of electrically enhanced fractures.



# How do the ground-based measurements arise?

Oblique view of the magnitude of electric potential for case A (+'ve electrode at the well head) along two intersecting surfaces: a vertical slice at  $x = 0$  m through the well track and fracture set; and, a horizontal slice at  $z = 0$  m along the air/Earth interface.

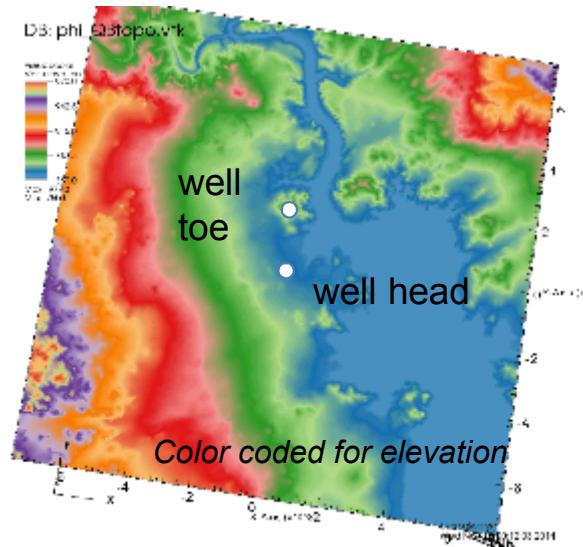
Intersecting the slices are the well track and fractures. Note the local perturbation near the well heel due to the fractures, as well as the dominance of the  $-1$  A current source on the potentials at  $z = 0$ .



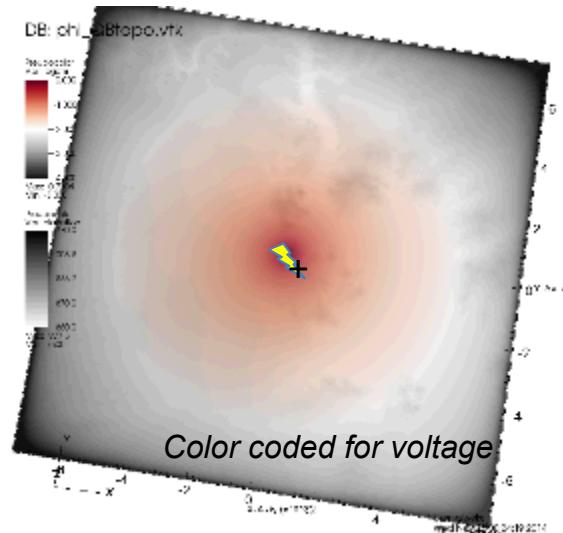
Generally small amplitudes of the potential in the region below  $z = -800$  m are consistent with its relatively high  $0.03$  S/m conductivity – in contrast to the low ( $< 0.001$  S/m) conductivity in the region above  $z = -800$  m.

# Topography effect: 3D-1D residual

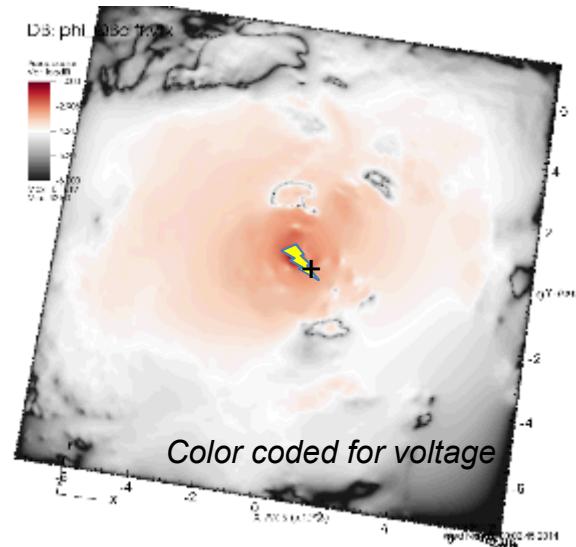
Topography: 860m to 970m elevation



3D DC FEA calculation w/ topo



topo – flat FEA residual



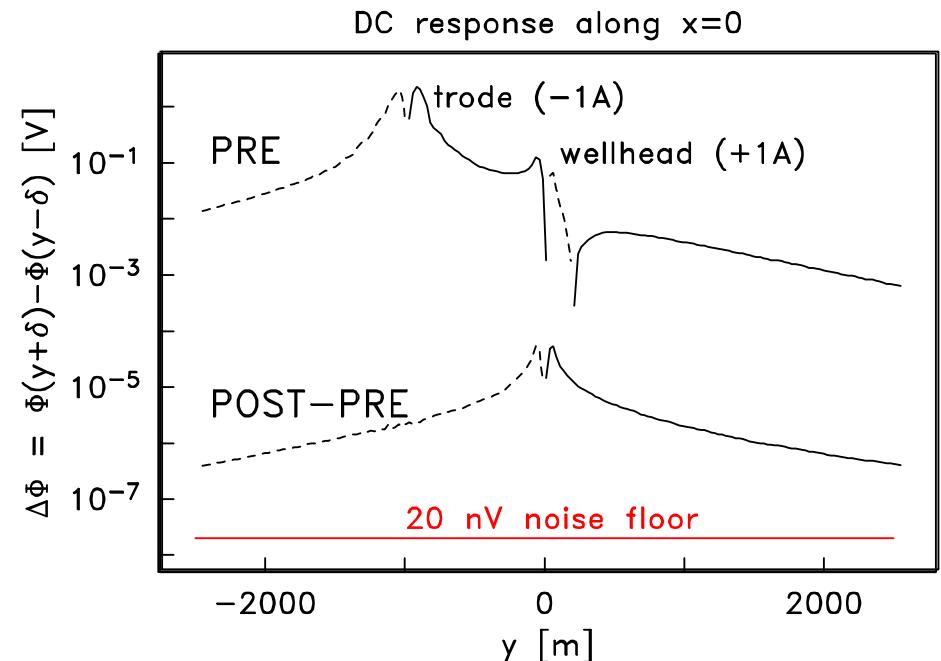
~1% change in voltage due to topography

**This relative magnitude is comparable to the change expected from electrically conductive fracture set.**

# Predicted data for inline measurement array

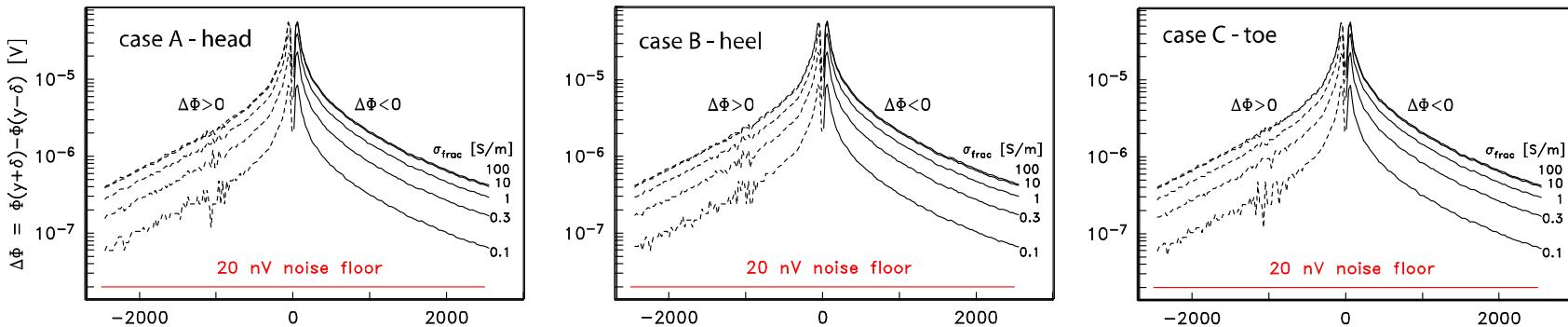
**(top curve)** Potential difference along line  $x = 0$  directly through the well head and over the horizontal section of the well, in the absence of conducting fractures for 1 A source located at the well head (case A) and  $-1$  A source at  $y = -1000$  m. Dashed lines indicate negative values; solid lines, positive.

**(bottom curve)** Scattered potential differences arising from a  $10$  S/m fracture set near the heel of the well bore.



Potential differences computed using  $100$  m electrode separation,  $\delta = 50$  m. For reference, also shown is the  $20$  nV noise floor for the 32-bit ZEN receiver from Zonge Engineering (<http://zonge.com/instruments-home/systems/distributed-em-systems/>).

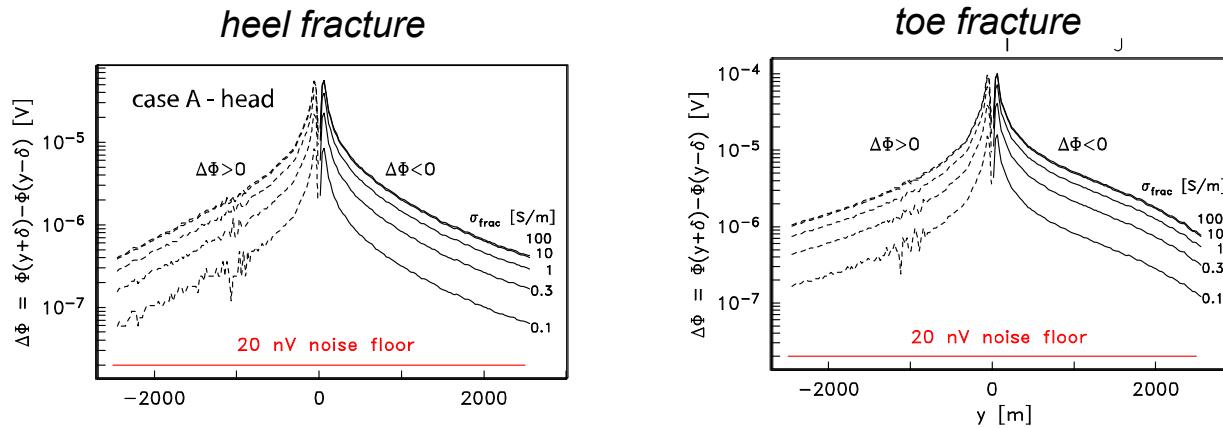
# Effect of source location and fracture conductivity



Inline scattered potential differences ( $\delta = 50$  m) as a function of fracture conductivity over the range 0.1–100 S/m for a  $-1$  A source at  $y = -1000$  m and  $+1$  A source located at either the well head, heel, or toe (cases A-C). Dashed lines indicate negative values; solid lines, positive.

Note that location of the  $+1$  A source has minimal effect on scattered potential differences, and that fracture response is saturated for conductivities greater than  $\sim 10$  S/m.

# Effect of fracture location



Inline scattered potential differences ( $\delta = 50 \text{ m}$ ) as a function of fracture conductivity over the range 0.1–100 S/m for a  $-1 \text{ A}$  source at  $y = -1000 \text{ m}$  and  $+1 \text{ A}$  source, fractures located at either the well heel (**left**), or toe (**right**). Dashed lines indicate negative values; solid lines, positive.

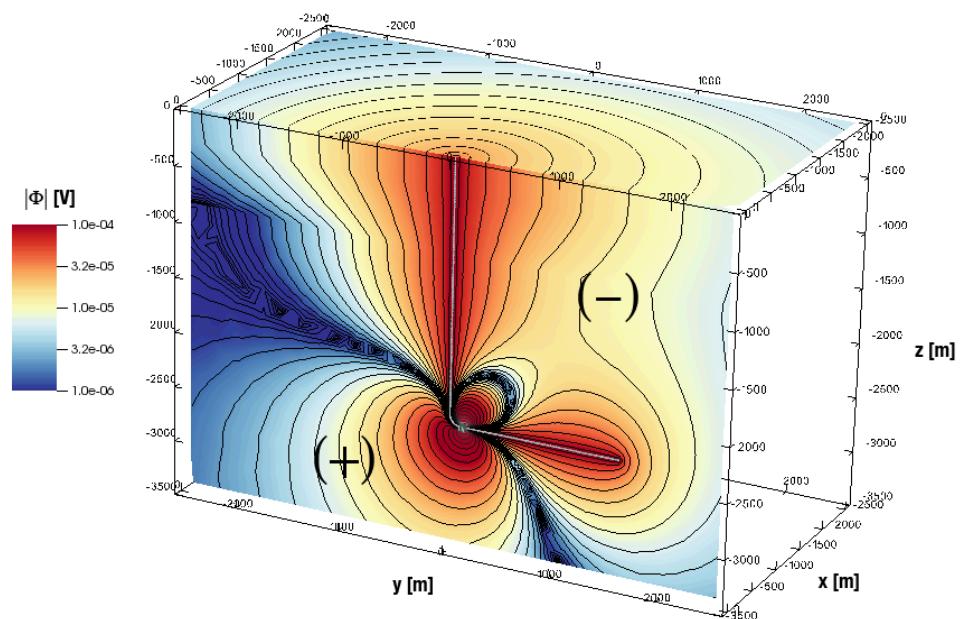
Note the pronounced left/right asymmetry of the toe-fracture result, and that fracture response remains saturated for conductivities greater than  $\sim 10 \text{ S/m}$ .

# Motivation for empirical LQS inversion

Oblique view of the magnitude of POST–PRE scattered electric potential for case A along two intersecting surfaces: a vertical slice through the well track and fracture set at  $x = 0$  m; and, a horizontal slice along the air/Earth interface  
 $z = 0$  m.

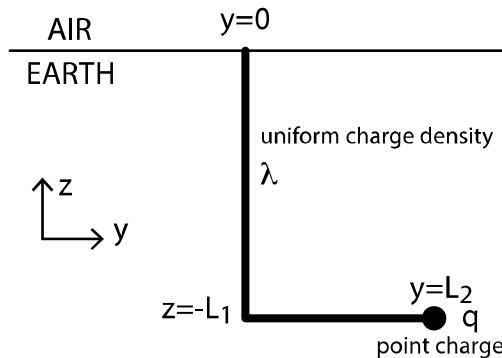
Region where  $\Phi > 0$  is denoted by (+) whereas the region  $\Phi < 0$  is denoted by (–). Superimposed on the slices are the well bore and fractures.

Observe that this POST–PRE difference data arises primarily from a combination of sources – one due to the conductivity perturbation at the fractures, and the other, a change in the relative potential of the borehole casing due to current leakage at the fracture.

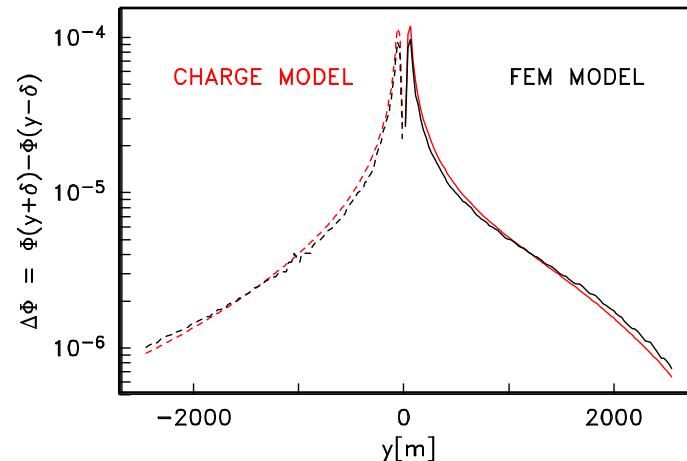


**Empirical LQS inversion:** invert time-lapse surface data for linear charge density ( $\lambda$ ) on the well casing; point charge  $q$  at the fracture, and position  $s$  of the fracture.

# LQS inversion: eyeball minimization of the misfit norm

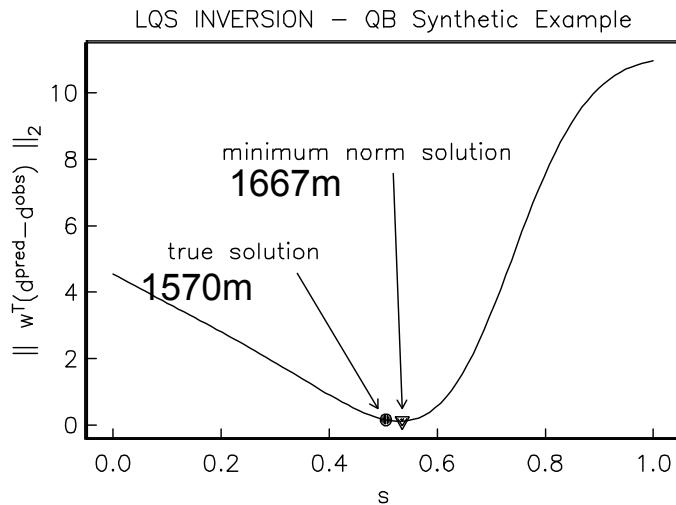


**(left)** problem setup for LQS inversion of toe-fracture data with known fracture location,  $s$ . Inversion is linear in charge magnitudes  $\lambda$  and  $q$ .

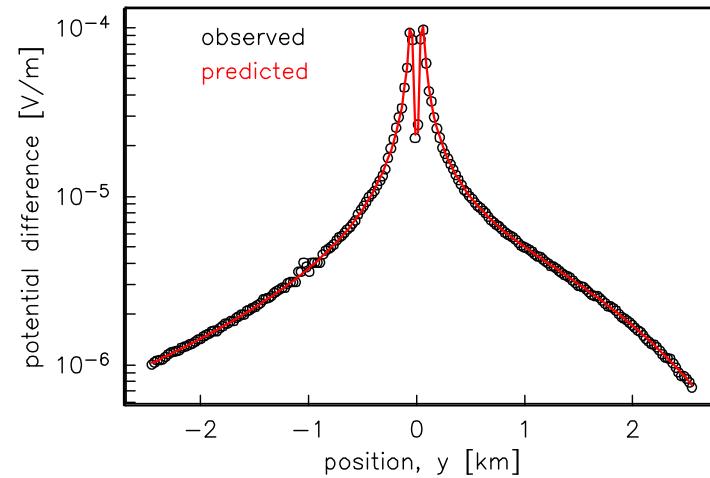


**(right)** eyeball-minimized data misfit of time lapse inline potential differences.  $\lambda = 5.6\text{E-}15$  C/m,  $q = 1.7\text{E-}11$  C.

# LQS Inversion: minimize the L2 norm

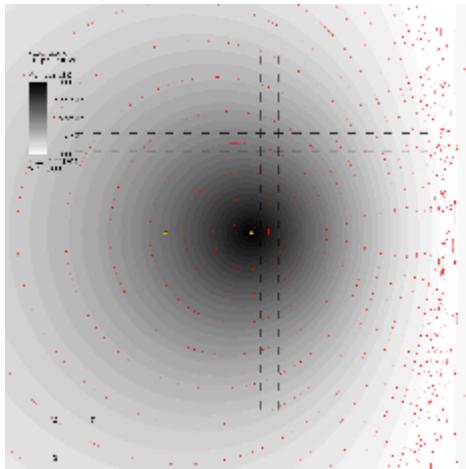


**(left)** Line search on  $s$  for minimum L2 misfit.  
At each candidate location,  $s$ , the linear inverse  
problem for  $(\lambda, q)$  is solved.

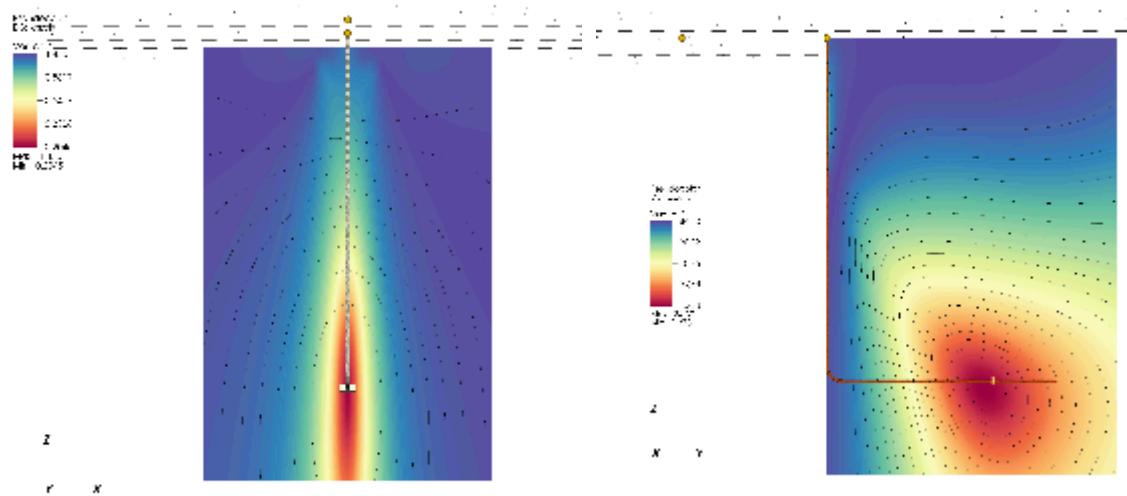


**(right)** L2-minimized data misfit of time lapse inline  
potential differences.  $\lambda = 5.1\text{E-}15 \text{ C/m}$ ,  $q = 1.8\text{E-}11 \text{ C}$ .

# LQS inversion: 2D array of 2-component data



**(above)** Broaden the array to a *massive* 20x20 grid of 2-component measurements on a 4x4 km area. Time-lapse potentials in grey scale with red contours. Stations indicated by + signs. Well head and ground point indicated by yellow dots.



Color scaled L2 norm values of optimal  $(\lambda, q)$  pairs for candidate 's' points in a plane orthogonal to the horizontal section of the well bore and through the fracture set (**left**), and in a plane containing the entire well bore (**right**).

# LQS Inversion: 3D fracture location

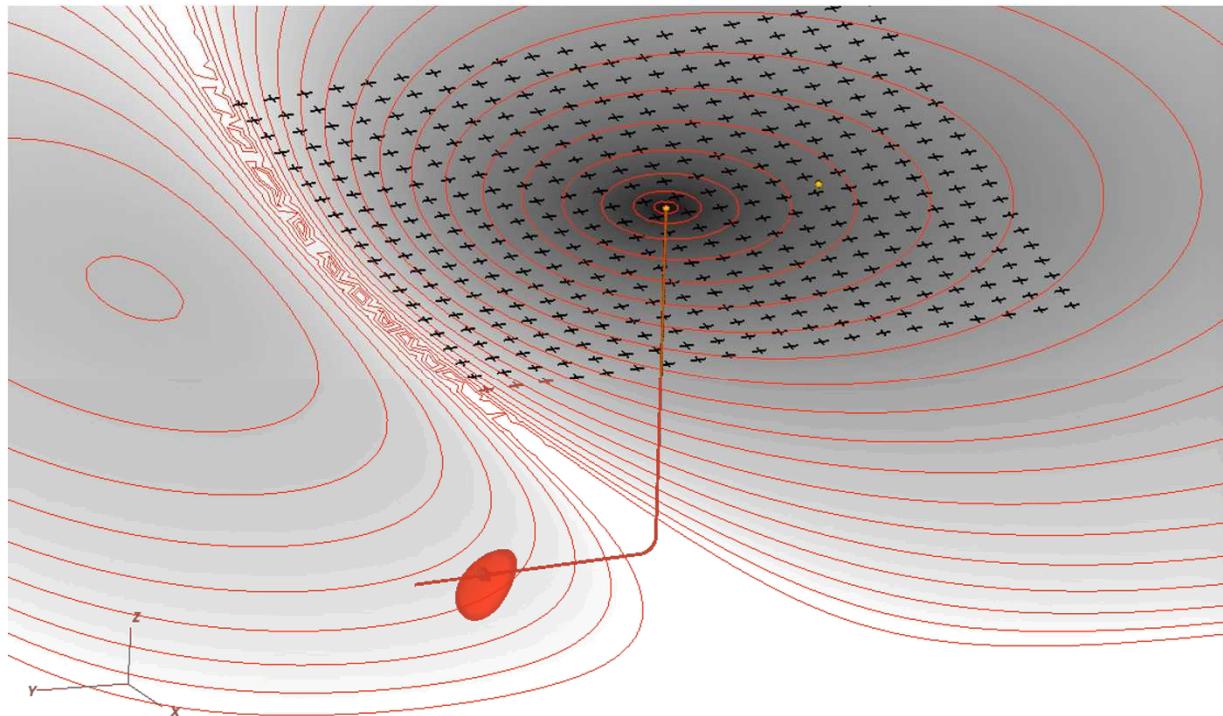
Inversion of synthetic data taken from a massive 20x20 grid of 2-component measurements on a 4x4 km area. Time-lapse potentials in grey scale with red contours.

Stations indicated by + signs. Well head and ground point indicated by yellow dots.

Red isosurface surrounding the fractures is taken at  $\chi^2=2$ , a value where its width is similar to that of the fractures.

$$\chi^2 = \sum_{i=1}^N \left( \frac{d_i^{obs} - d_i^{pred}}{d_i^{obs}} \right)^2$$

Note the strong differences in vertical and lateral resolution!



# Conclusions

- Assuming electrical continuity of the well casing, DC fracture response is generally independent of source contact point.
- DC response of the fracture set saturates for conductivities greater than 10 S/m in the scenarios tested here. Further investigation is required to quantify such thresholds in other geologic settings.
- Topographic effects introduce signals comparable in magnitude to those of the fractures.
- Time-lapse DC response of the fractures is reasonably approximated by a simple 3-parameter charge model and easily invertible.



# Acknowledgements / Thank You / Questions

VSR6

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## Slide 17

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**VSR6** I recommend getting rid of this first acknowledgment statement.

Vigil, Steven R, 10/7/2016