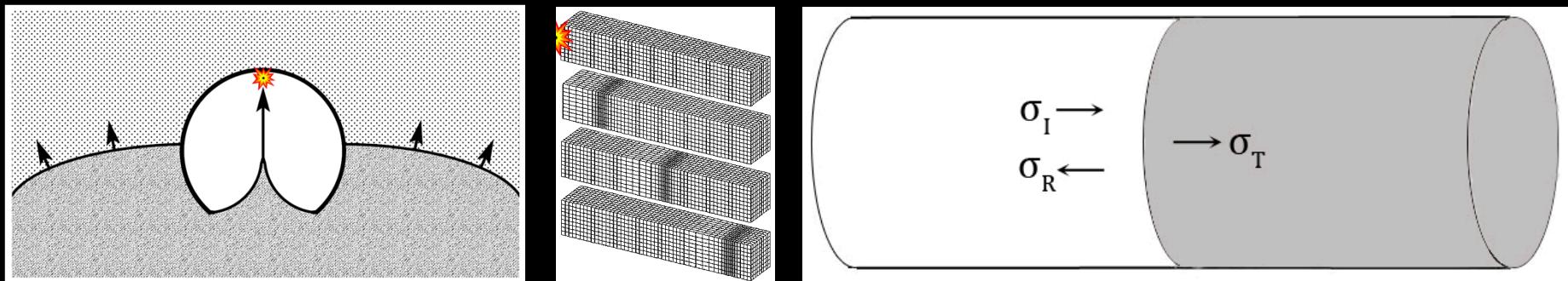


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Physics of Explosives Initiation

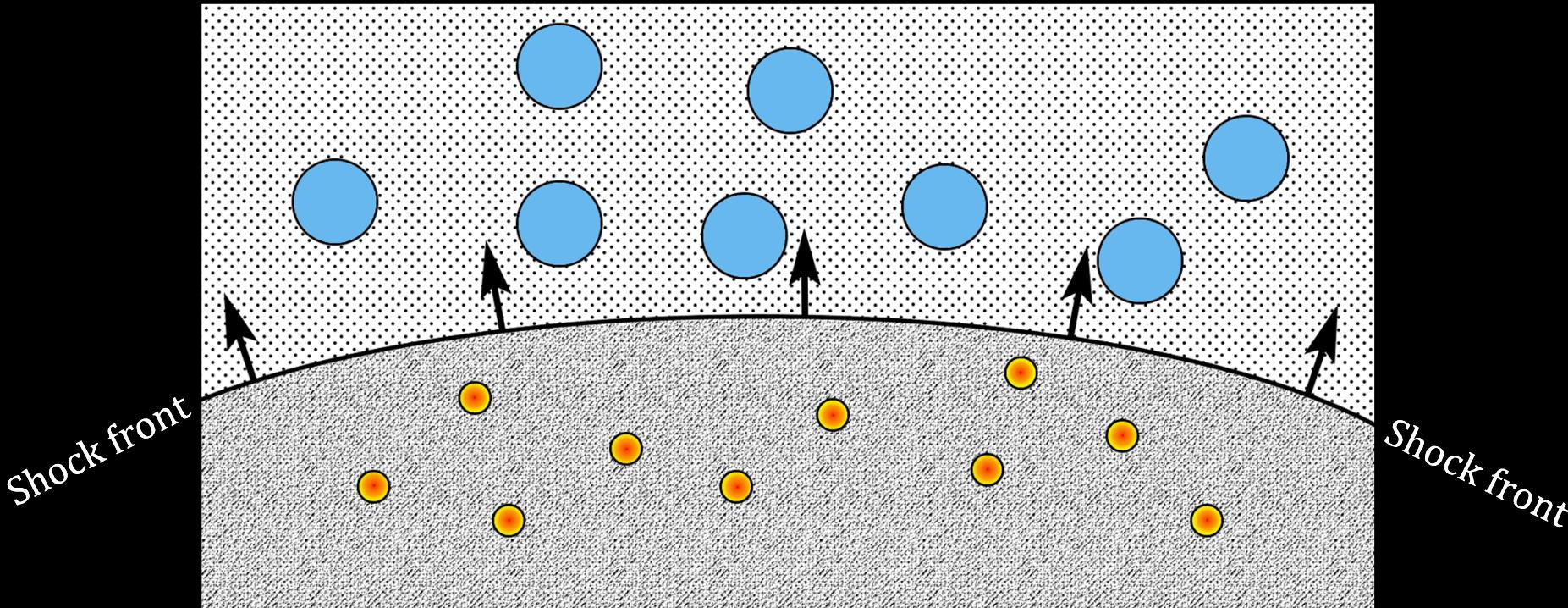
Jason J. Phillips

Energetics Characterization, Org. 2555



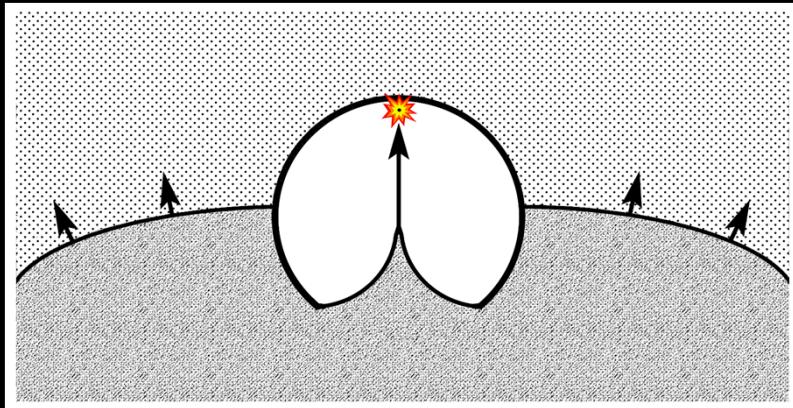
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Basic Hot Spot Theory

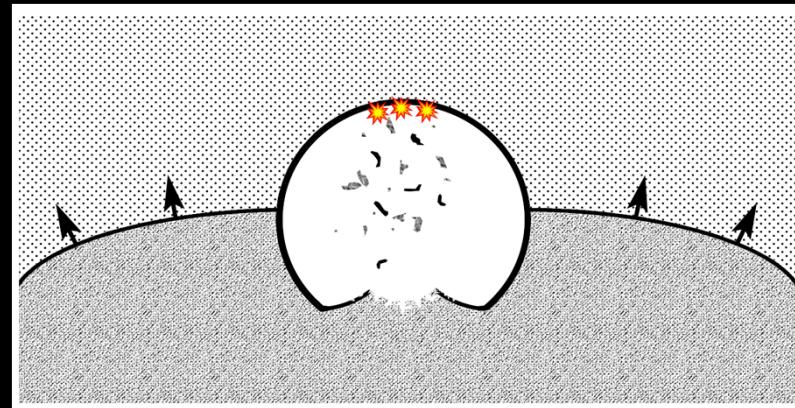


Rapid, adiabatic shock compression of gas filled pores/voids causes localized temperature spikes and decomposition of energetic material.

Hot Spot Theory – Additional Mechanisms

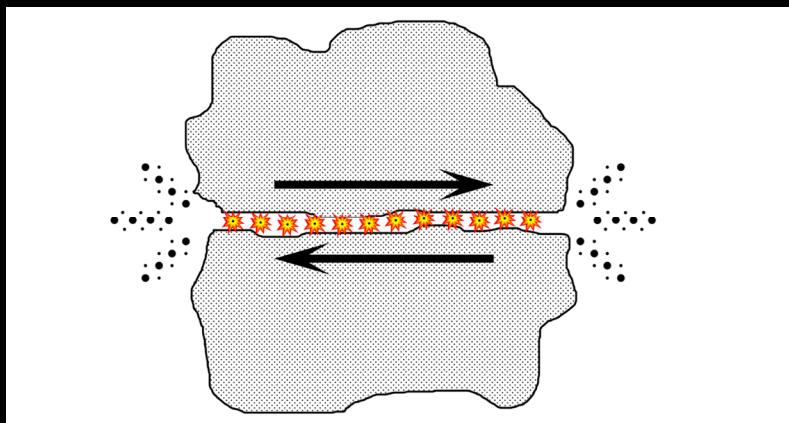


Viscous Flow/Jetting

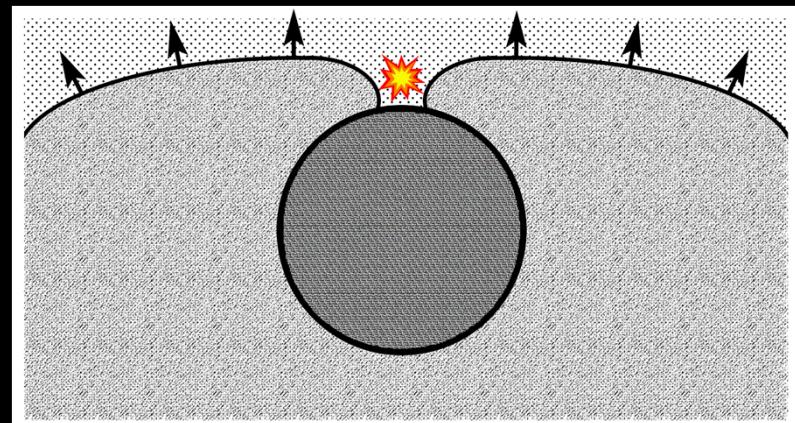


Jetting/Spallation

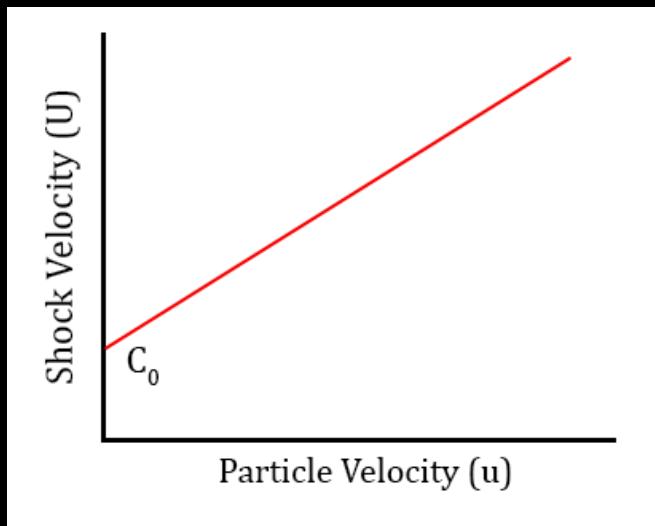
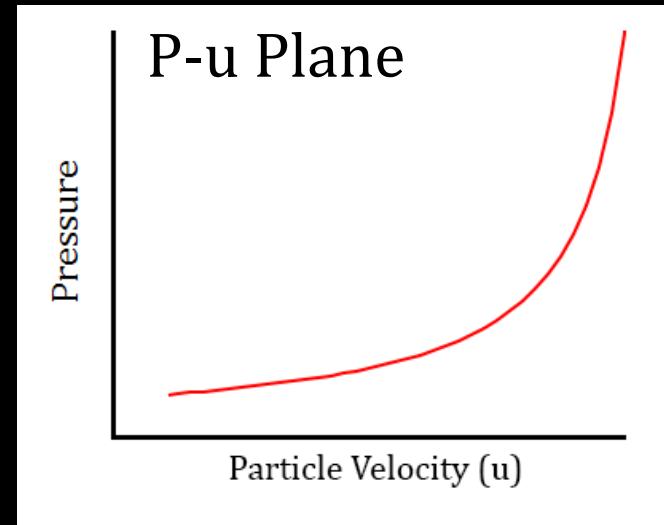
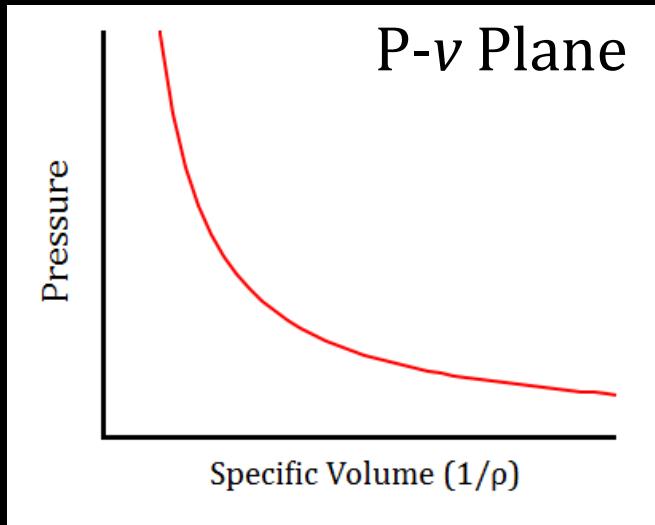
Friction



Shock Interaction

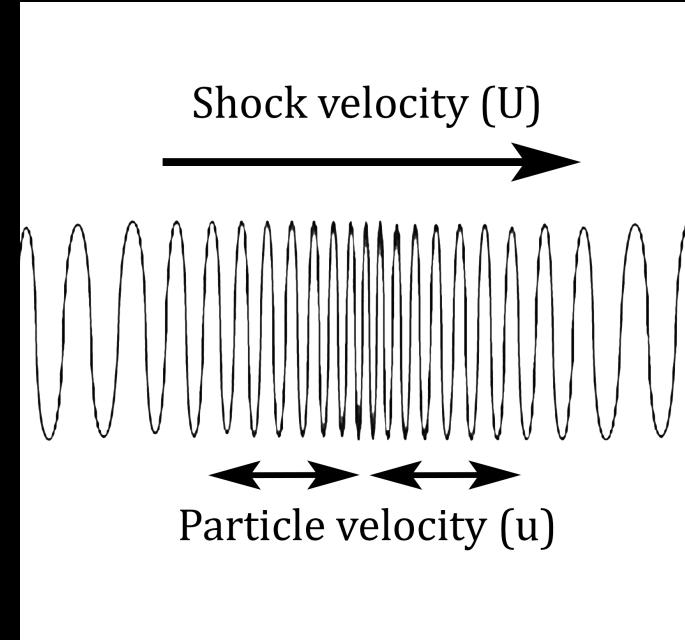
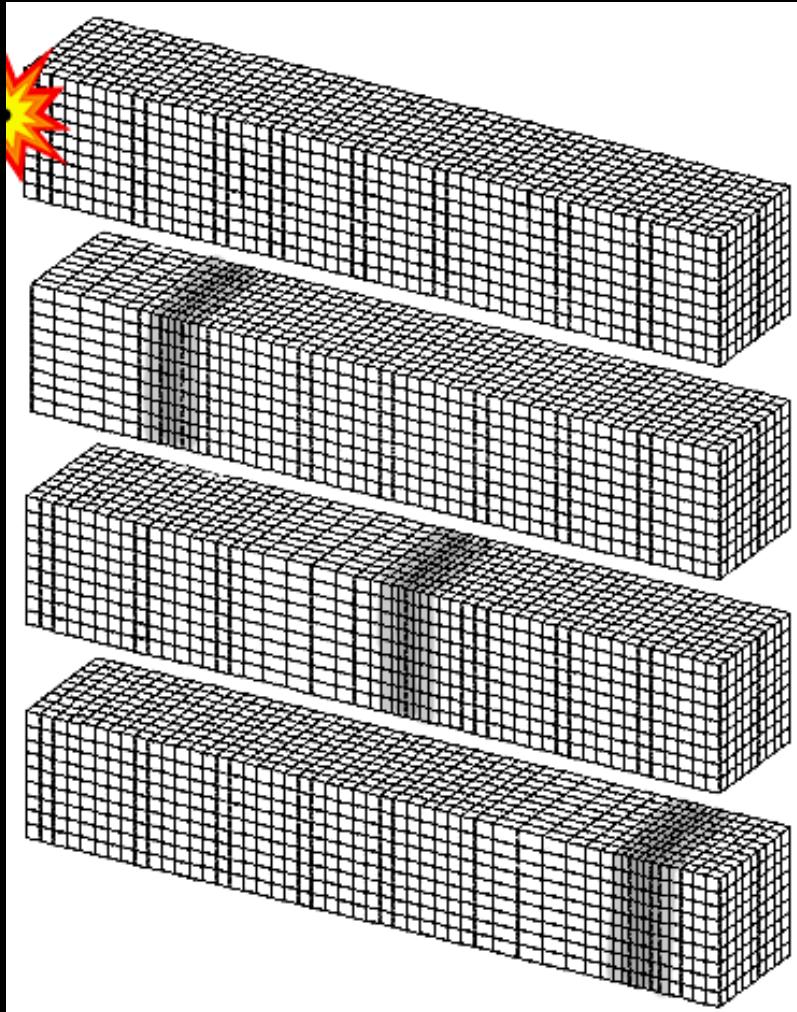


Hugoniot Overview



- 3 useful Hugoniot planes
- Y-intercept in the U-u Hugoniot plane represents the bulk sound speed (C_0).

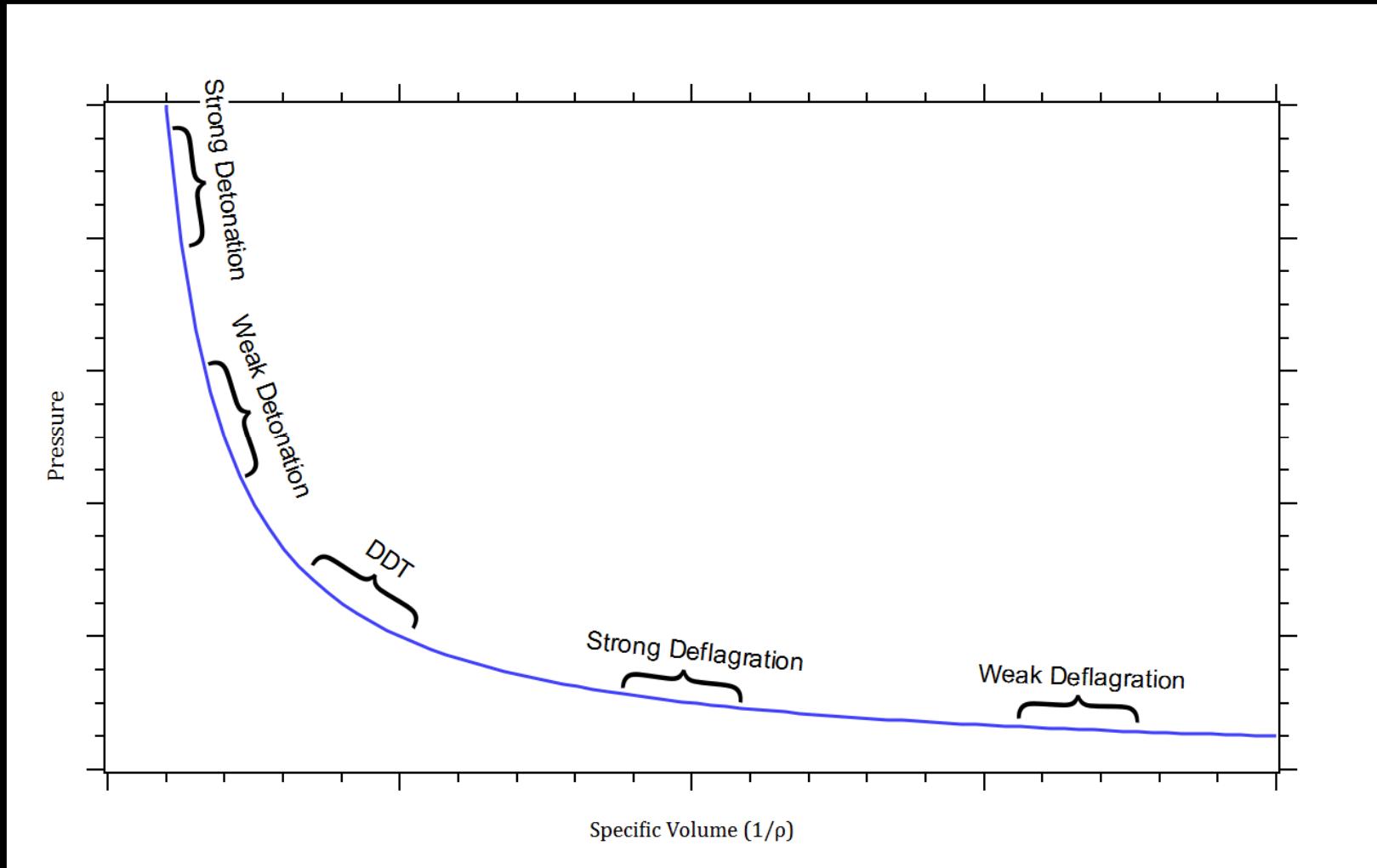
Shock vs Particle Velocity (U vs u)



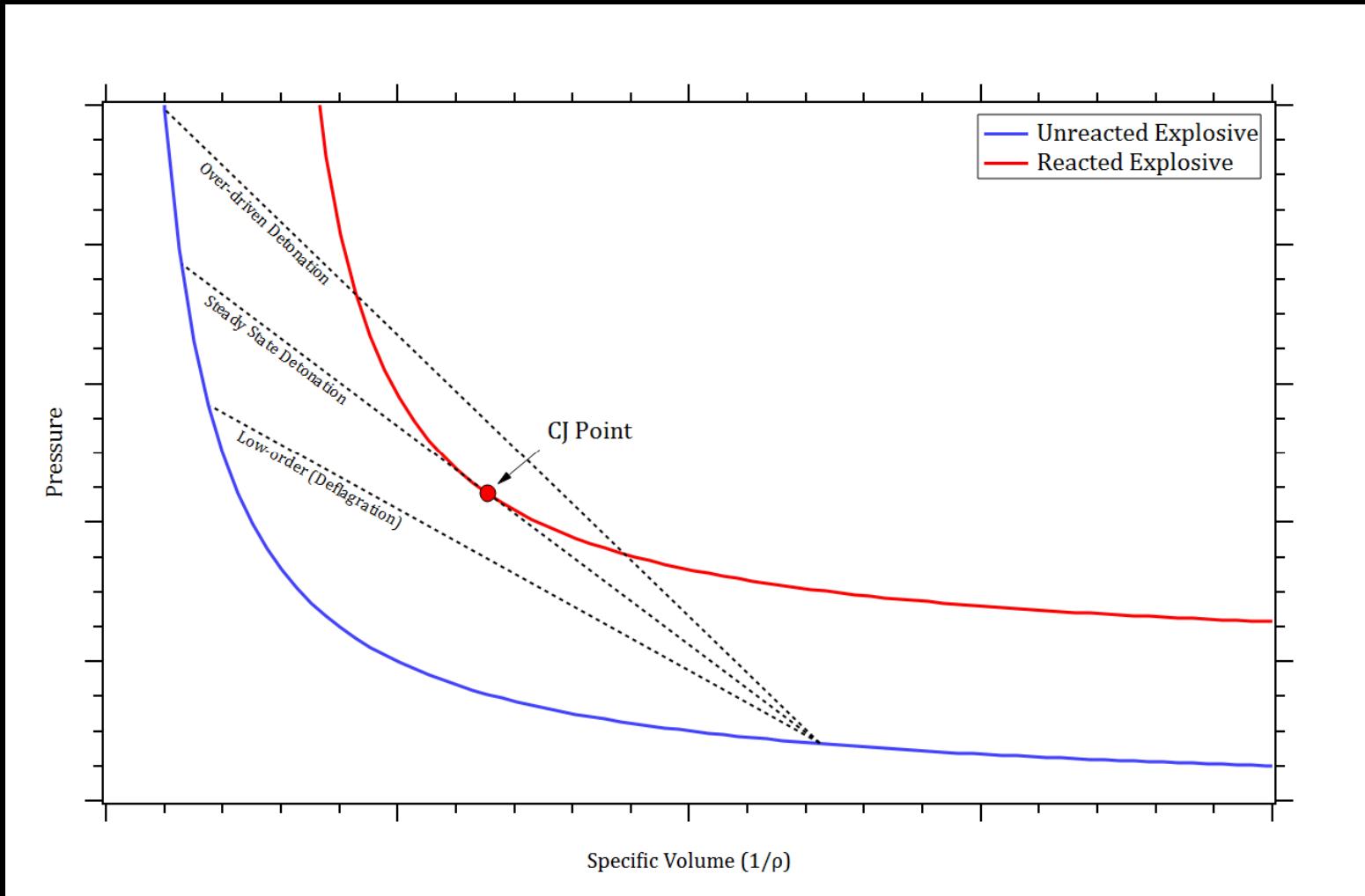
u – Refers to relative motion within the shock disturbance

U – Refers to the propagation of the disturbance through the material

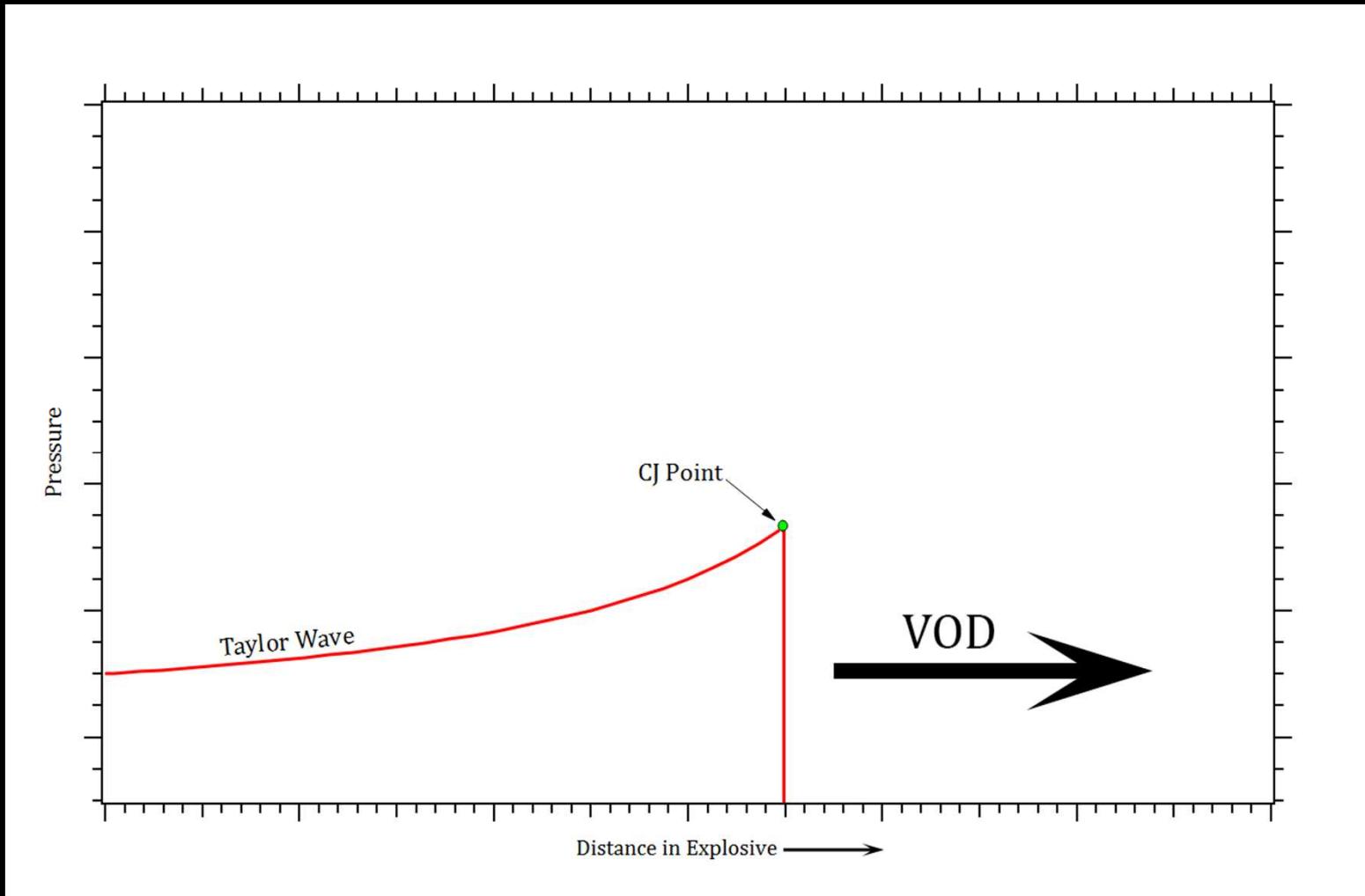
Hugoniot Overview



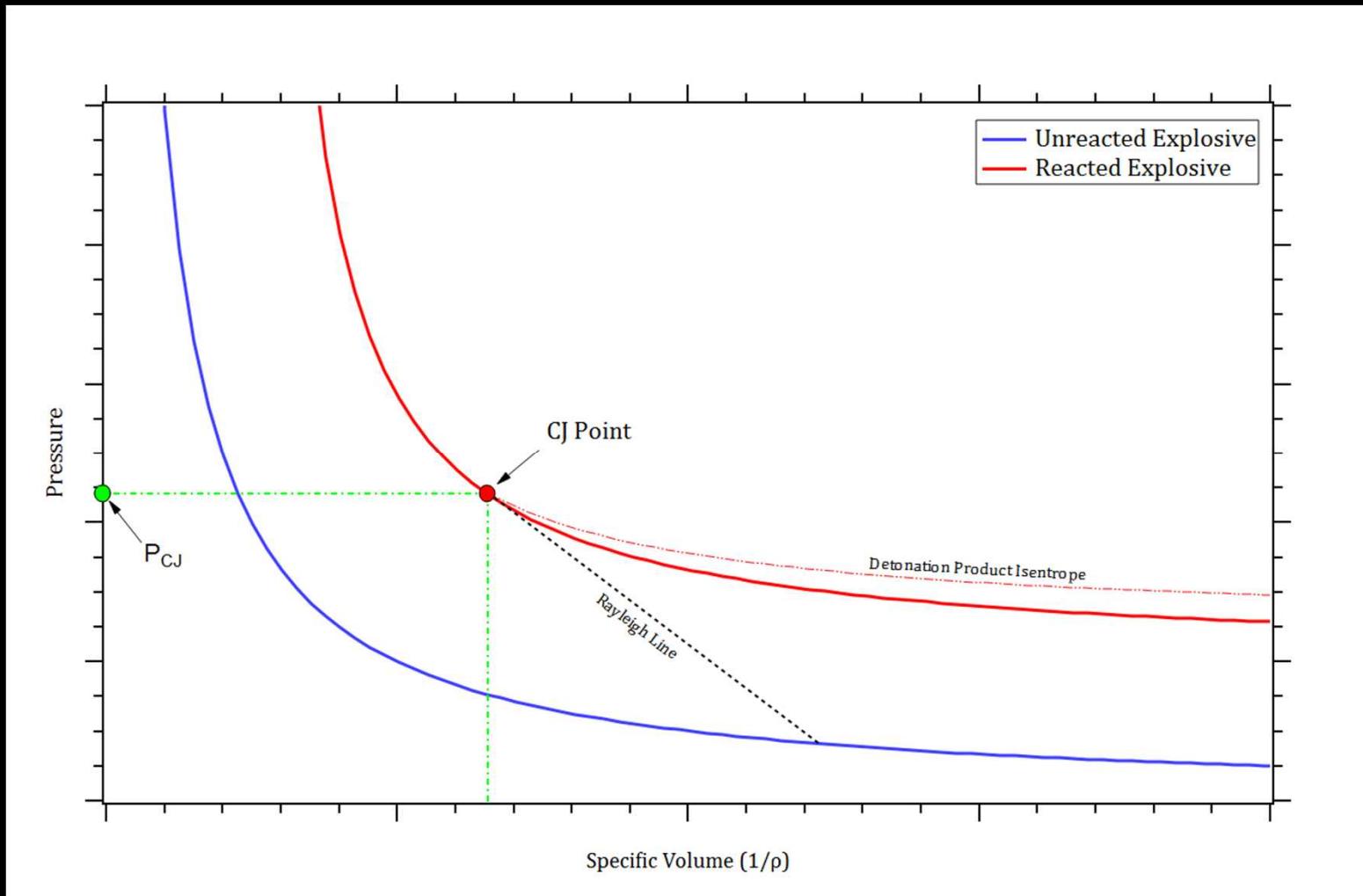
Rayleigh Line Overview



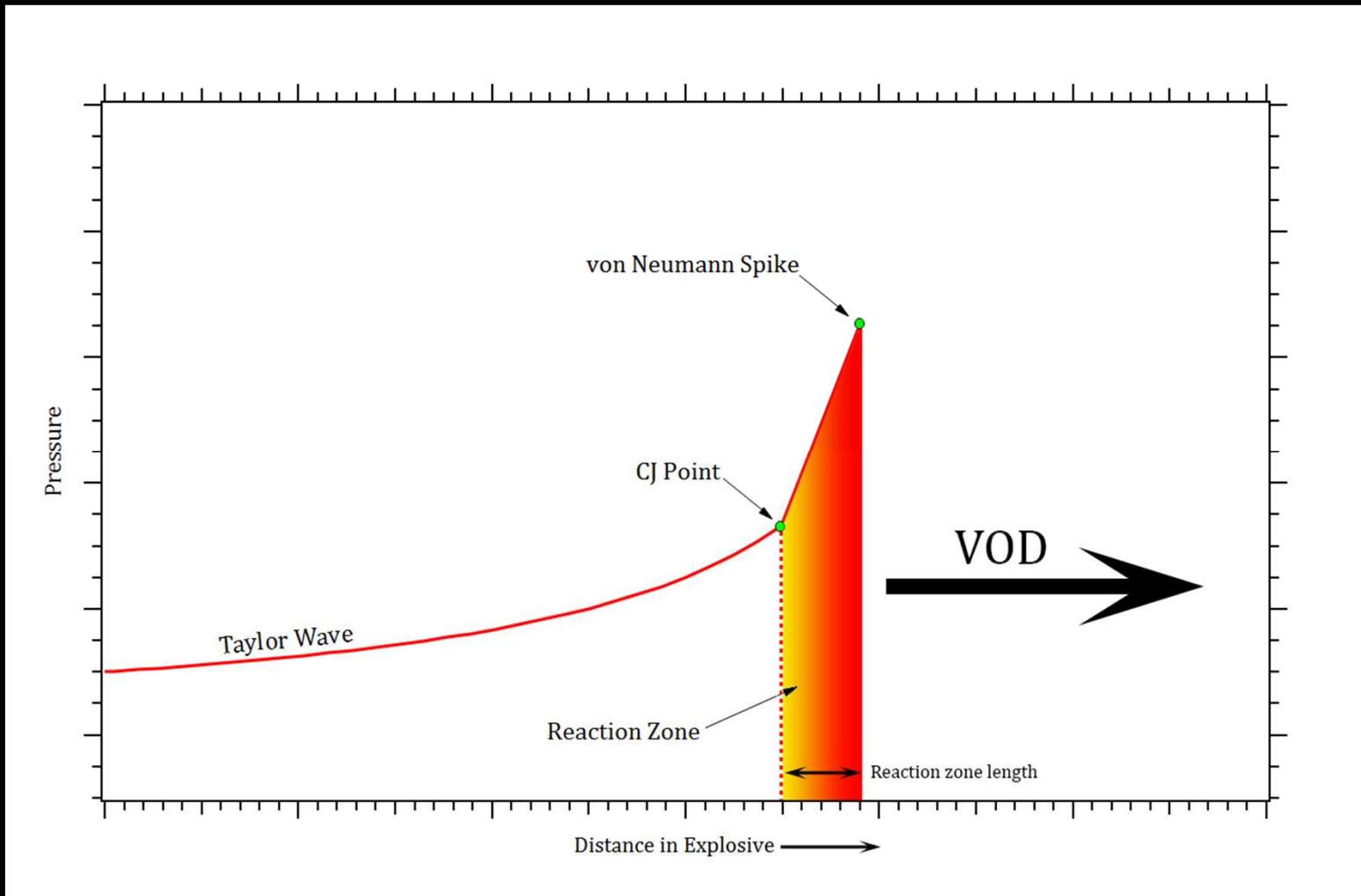
CJ Detonation Model



CJ Detonation Model

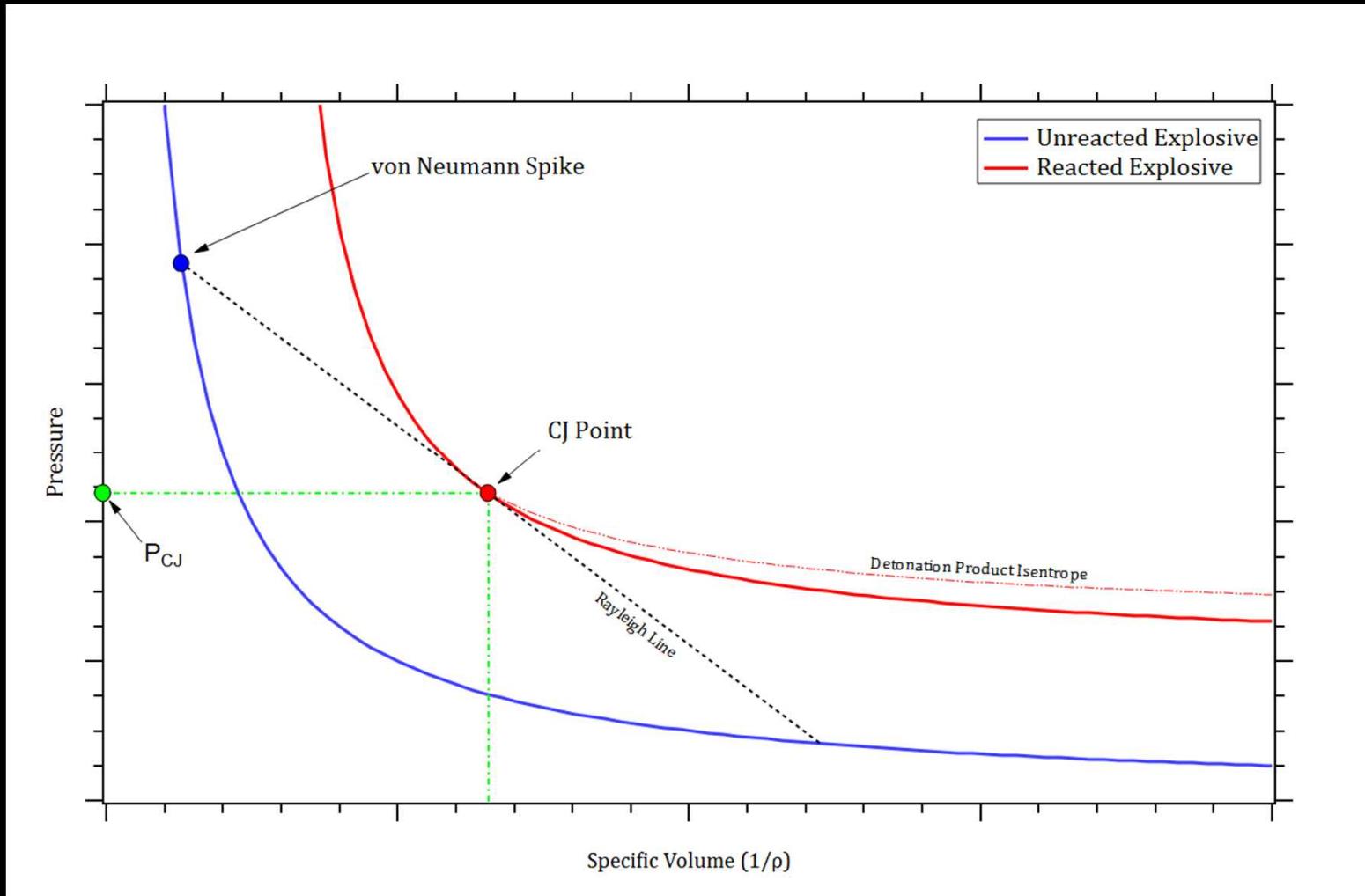


ZND* Detonation Model

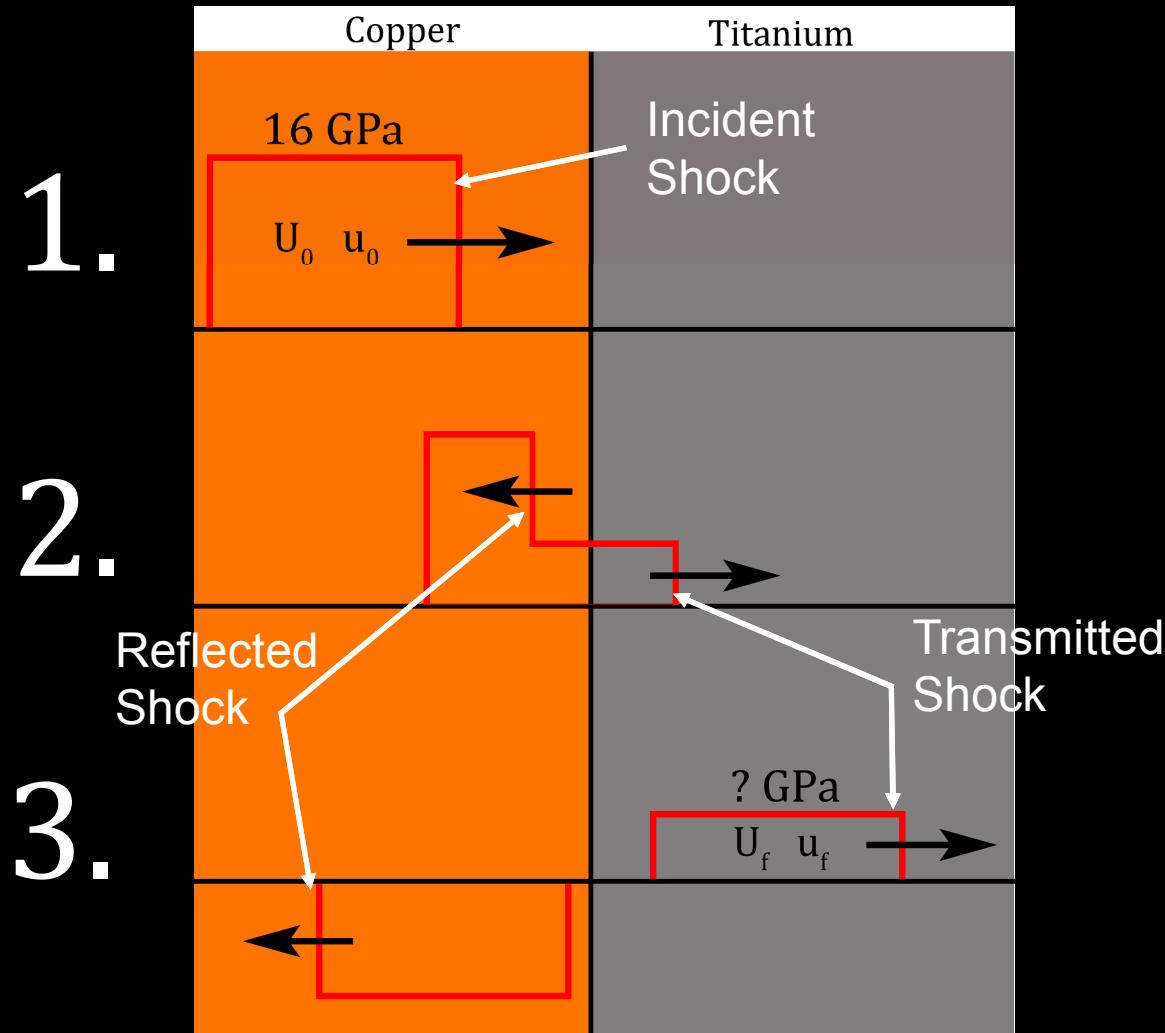


*Zel'dovich, von Neumann, Döring

ZND Detonation Model



Shock Propagation Example



Impedance (Z):

Effectively, a material's resistance to shock propagation

$$Z_{\text{Cu}} > Z_{\text{Ti}}$$

Calculated Solution

$$U = C_0 + su$$



U-u relationship (derived via empirical testing)

$$P = \rho_0 C_0 u_1 + \rho_0 s u_1^2$$



P-u relationship in a neat material

$$P = \rho_0 C_0 (u_0 - u_1) + \rho_0 s (u_0 - u_1)^2$$



P-u relationship at an interface/discontinuity

P : pressure (GPa)

U : shock velocity (km/s)

ρ_0 : density (g/cm³)

s : constant (slope value)

C_0 : bulk sound velocity (km/s)

u : particle velocity (km/s)

$$\rho_{Cu} = 8.924 \text{ g/cm}^3$$

$$C_{Cu} = 4.76 \text{ km/s}$$

$$s_{Cu} = 1.439$$

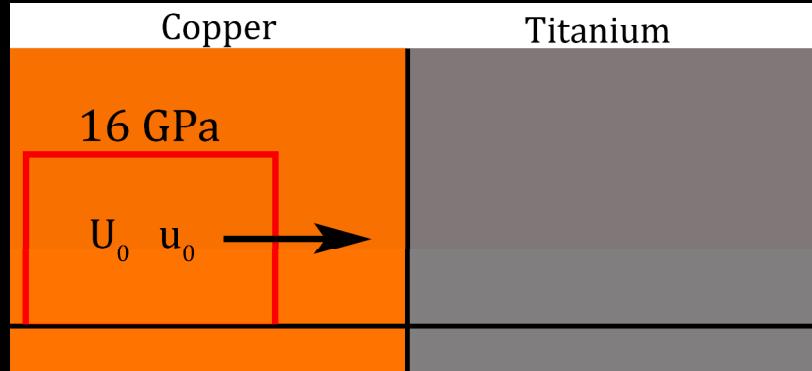
$$\rho_{Ti} = 4.527 \text{ g/cm}^3$$

$$C_{Ti} = 6.16 \text{ km/s}$$

$$s_{Ti} = 0.976$$

Calculated Solution - 1

Step 1: Calculate initial particle/shock velocity in the copper: $P_1 = 16 \text{ GPa}$



$$P_1 = \rho_{Cu} C_{Cu} u_0 + \rho_{Cu} s_{Cu} u_0^2$$
$$16 = (8.924)(4.76)u_0 + (8.924)(1.439)u_0^2$$

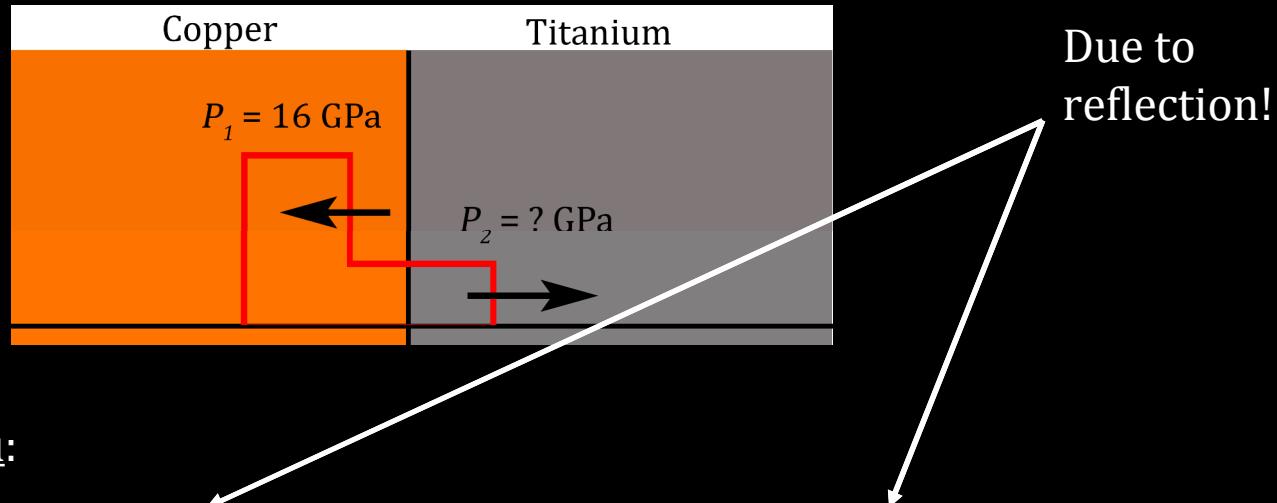
$$u_0 = 0.34 \text{ km/s}$$

$$U_0 = C_{Cu} + s_{Cu} u_0$$
$$U_0 = 4.76 + (1.439)(0.34)$$

$$U_0 = 5.25 \text{ km/s}$$

Calculated Solution - 2

Step 2: Set up the calculations for the interface



Reflected shock in Cu:

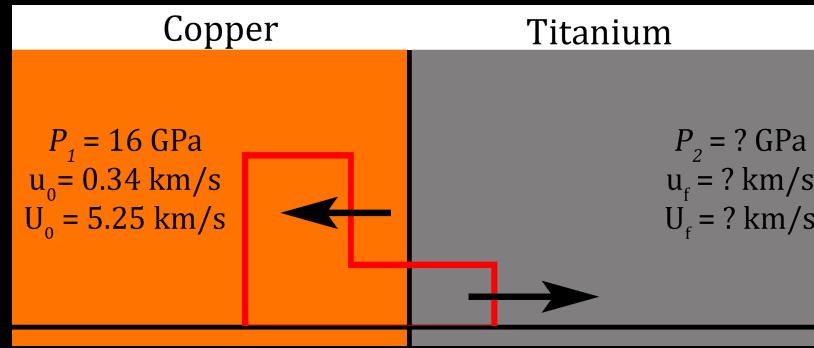
$$P_2 = (8.924)(4.76)(2 \times 0.34 - u_f) + (8.924)(1.439)(2 \times 0.34 - u_f)^2$$
$$P_2 = 32.45 - 58.91u_f + 12.84u_f^2$$

Transmitted shock in Ti:

$$P_2 = (4.527)(6.16)u_f + (4.527)(0.976)u_f^2$$
$$P_2 = 27.89u_f + 4.418u_f^2$$

Calculated Solution - 3

Step 3: Set equations equal to each other and solve



$$32.45 - 58.91u_f + 12.84u_f^2 = 27.89u_f + 4.418u_f^2$$
$$0 = 32.45 - 86.80u_f + 8.42u_f^2$$

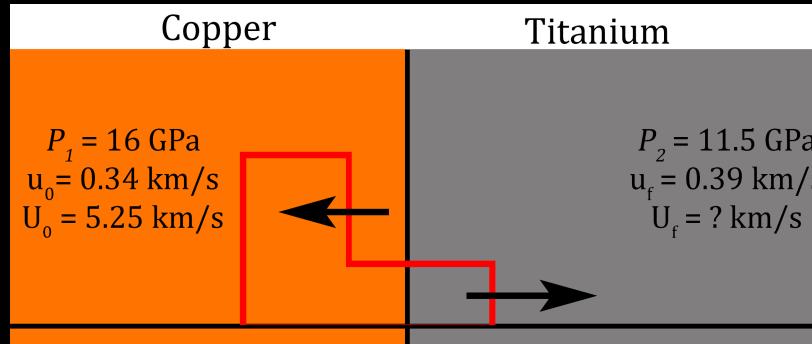
$$u_f = 0.39 \text{ km/s}$$

$$P_2 = 27.89(0.39) + 4.418(0.39)^2$$

$$P_2 = 11.5 \text{ GPa}$$

Calculated Solution - 4

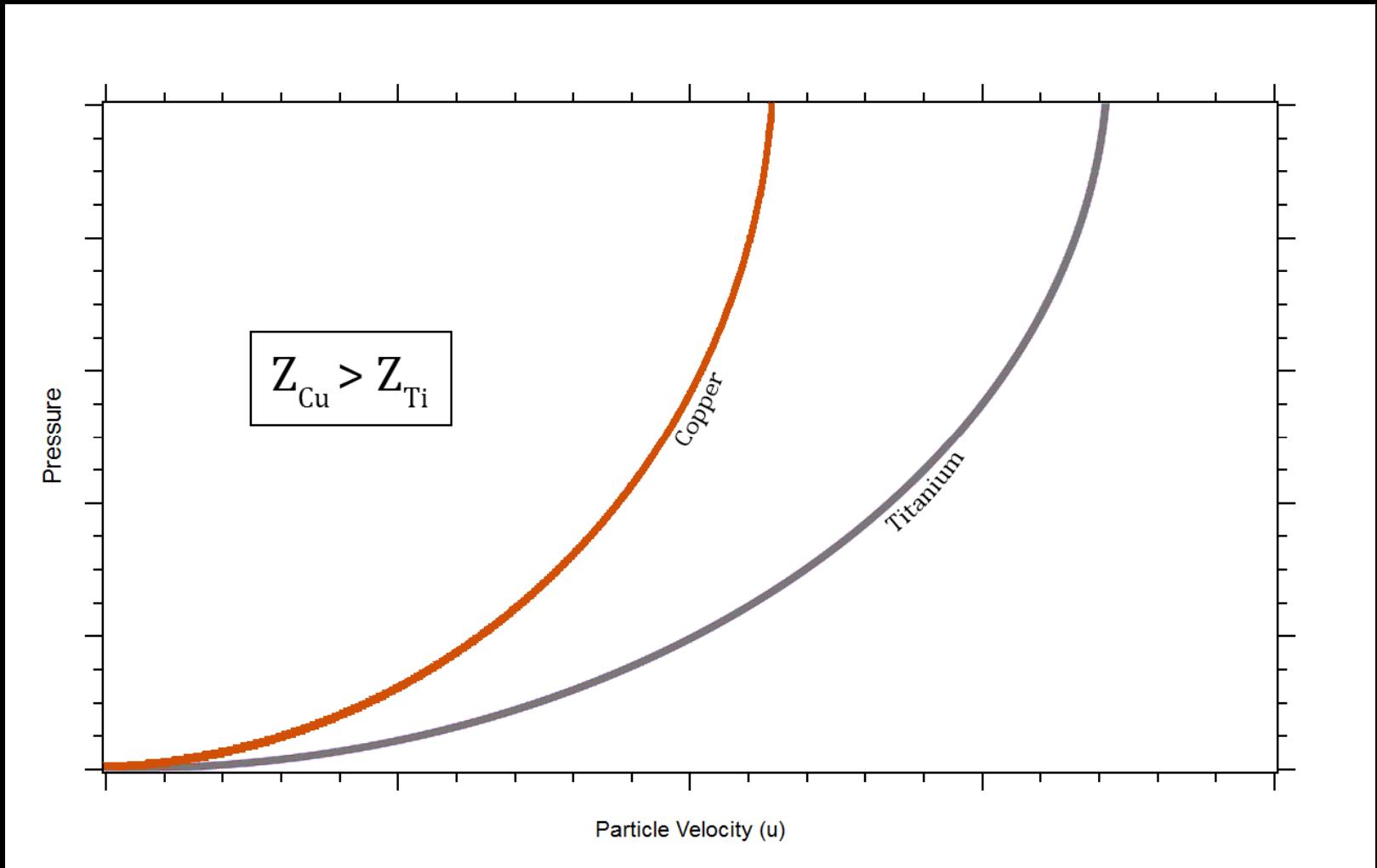
Step 4: Solve for final shock velocity



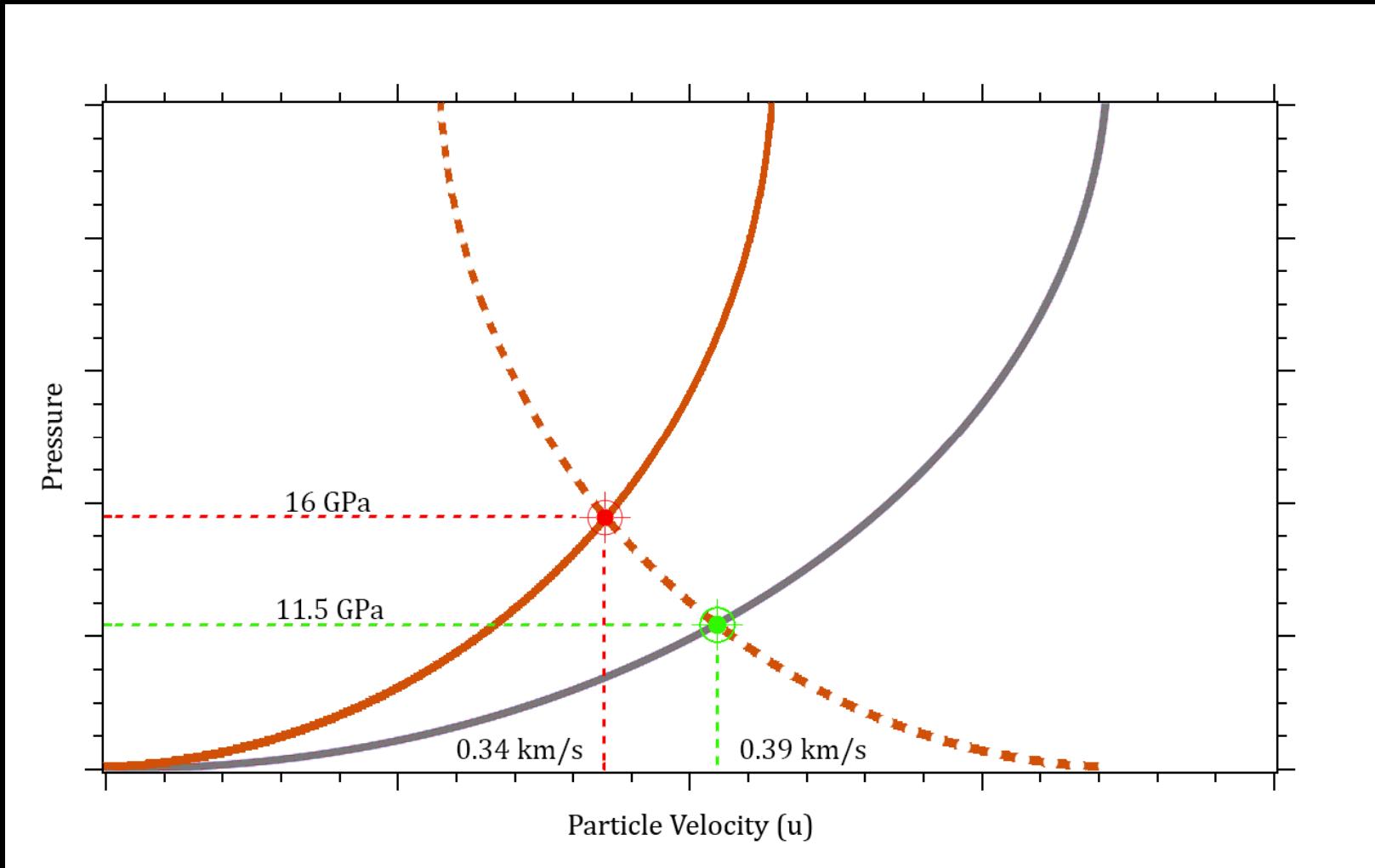
$$U_f = C_{Ti} + s_{Ti} u_f$$
$$U_f = 6.16 + (0.976)(0.39)$$

$$U_f = 6.54 \text{ km/s}$$

Graphical Solution - 1



Graphical Solution - 2



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