

# TRINITY

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## Scaling tests of a new algorithm for DFT hybrid-functional calculations on Trinity Haswell

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*Alliance for Computing at Extreme Scale*

# Objective and Approach

**Objective:** Develop a highly scalable implementation of Density-Functional-Theory (DFT) with hybrid functionals (combining density- and orbital-dependent electron exchange) that can be used in Sandia *Radiation-Effects* and *High-Energy-Density-Physics* Mission Areas

## Approach:

- Used Sandia's Socorro DFT code [1] as a development platform
- Implemented a Compact Representation (CR) [2] of the orbital-dependent exchange operator, which is constructed from derivatives of the exchange energy with respect to the orbitals...

$$\frac{\delta E_x}{\delta \psi_{n_1 \vec{k}_1}^*(\vec{r}_1)} = f_{n_1 \vec{k}_1} \sum_{\vec{k}_2} \sum_{n_2} \left( -\frac{\Omega}{2} e^2 f_{n_2 \vec{k}_2} \psi_{n_2 \vec{k}_2}(\vec{r}_1) \int_{\Omega} \frac{\psi_{n_2 \vec{k}_2}^*(\vec{r}_2) \psi_{n_1 \vec{k}_1}(\vec{r}_2)}{|\vec{r}_1 - \vec{r}_2|} d\vec{r}_2 \right)$$

- Developed a new algorithm that allows use of integer multiples ( $> 1$ ) of  $N_{\text{orbitals}} \times N_{\text{k-points}}$  MPI processes when constructing the CR, and multiple threads for each MPI process
- Tested and used the new algorithm under *Open Science 1* and *ATCC 1-3*

[1] [dft.sandia.gov/socorro](http://dft.sandia.gov/socorro)

[2] Duchemin and Gygi, Comput. Phys. Commun. **181**, 855 (2010)

# A Simple Example of the New Algorithm

## 5 orbitals and 10 MPI processes

Distribution of the LHS (row, R#) orbitals

|                    |   | Stage |    |    |
|--------------------|---|-------|----|----|
|                    |   | 0     | 1  | 2  |
| MPI Process Number | 0 |       | R1 | R1 |
|                    | 4 |       | R2 | R2 |
|                    | 5 |       | R3 | R3 |
|                    | 9 |       | R4 | R4 |
|                    |   |       | R5 | R5 |

Distribution of the RHS (column, C#) orbitals

|                    |   | Stage |       |       |       |
|--------------------|---|-------|-------|-------|-------|
|                    |   | 0     | 1     | 2     | 3     |
| MPI Process Number | 0 | R1    | R1 C1 | R1 C1 | R1 C1 |
|                    | 4 | R2    | R2 C2 | R2 C2 | R2 C2 |
|                    | 5 | R3    | R3 C3 | R3 C3 | R3 C3 |
|                    | 9 | R4    | R4 C4 | R4 C4 | R4 C4 |
|                    |   | R5    | R5 C5 | R5 C5 | R5 C5 |

Accumulation of the derivatives wrt the row orbitals (DR#)

|                    |   | Stage |           |           |           |
|--------------------|---|-------|-----------|-----------|-----------|
|                    |   | 0     | 1         | 2         | 3         |
| MPI Process Number | 0 | R1 C1 | R1 C1 DR1 | R1 C3 DR1 | R1 C5 DR1 |
|                    | 4 | R2 C2 | R2 C2 DR2 | R2 C4 DR2 | R2 C1 DR2 |
|                    | 5 | R3 C3 | R3 C3 DR3 | R3 C5 DR3 | R3 C2 DR3 |
|                    | 9 | R4 C4 | R4 C4 DR4 | R4 C1 DR4 | R4 C3 DR4 |
|                    |   | R5 C5 | R5 C5 DR5 | R5 C2 DR5 | R5 C4 DR5 |

Collection of the derivative contributions

|                    |   | Stage |     |
|--------------------|---|-------|-----|
|                    |   | 0     | 1   |
| MPI Process Number | 0 | DR1   | DR1 |
|                    | 4 | DR2   | DR2 |
|                    | 5 | DR3   | DR3 |
|                    | 9 | DR4   | DR4 |
|                    |   | DR5   | DR5 |

# Scaling Tests

**Overview** We show scaling results for materials of interest in Sandia *Radiation-Effects* and *High-Energy-Density-Physics* Mission Areas. Each timing is from a self-consistent calculation for bulk material. Two timings are given: (1) walltime for the construction of the CR exchange operator (*Exchange-Operator*) and (2) walltime for everything else (*non-Exchange-Operator*).

**GaAs 216-atom cell:** We show timings from runs using 8 k-points, 640 orbitals, a plane-wave cutoff of 40 Ryd to expand the orbitals, a PBE(23) functional [3] and **up to 286,820 CPUs**.

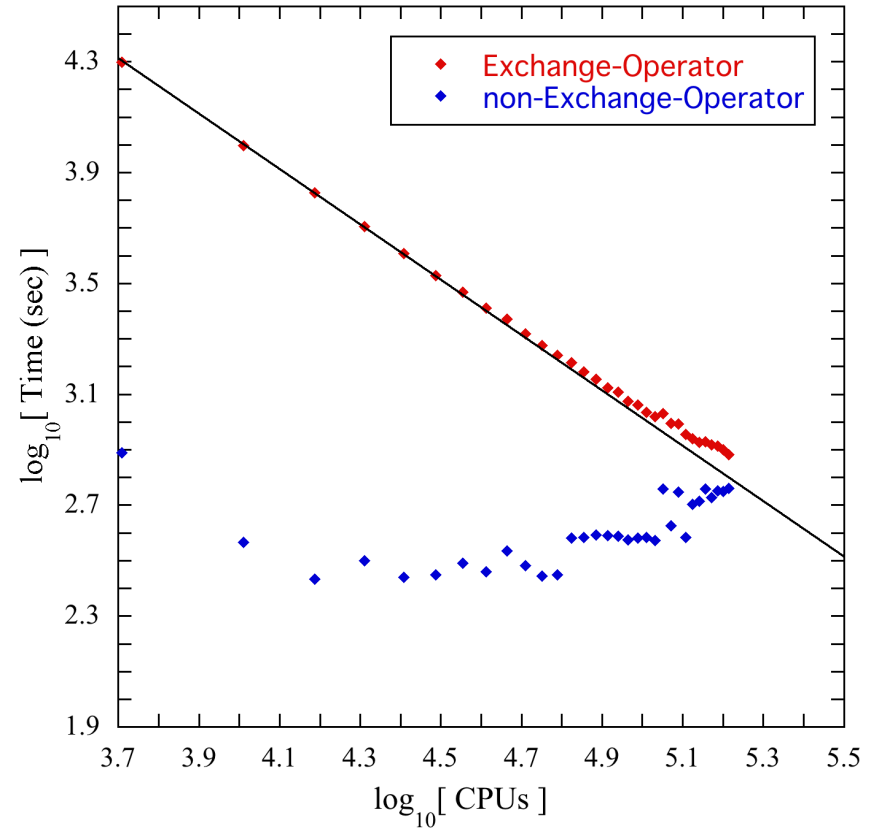
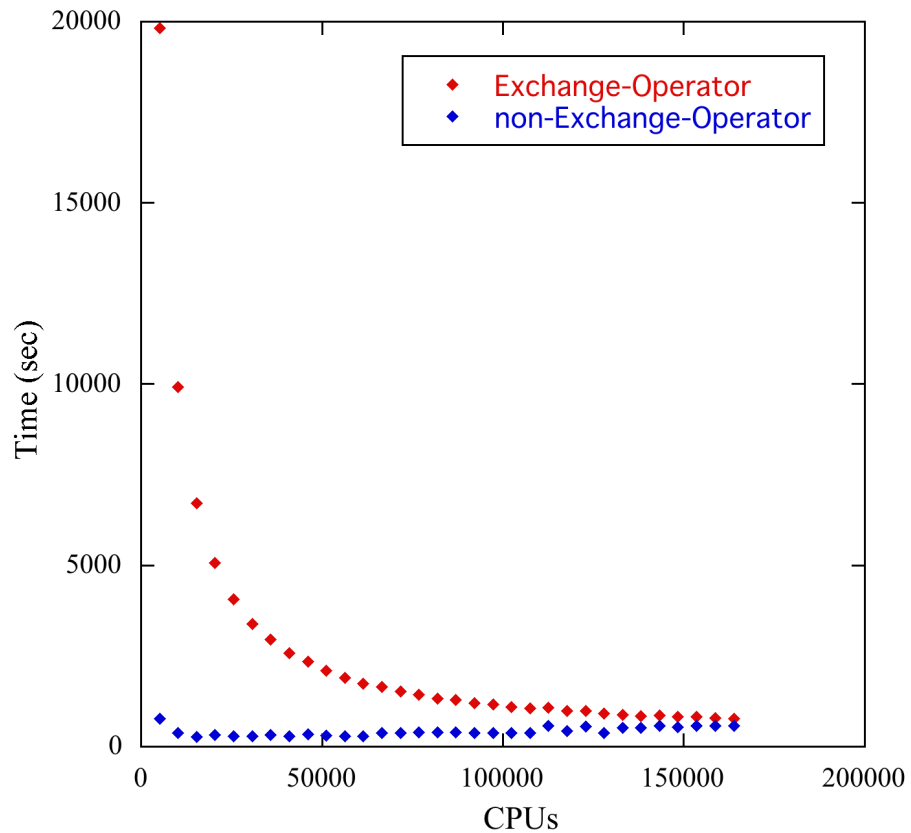
**Gold:** We show timings from runs in a 256-atom cell using 1 k-point, 2304 orbitals, a plane-wave cutoff of 50 Ryd to expand the orbitals, the HSE functional [4], and **up to 73,720 CPUs**.

**GaAs 512-atom cell:** We show timings from runs using 8 k-points, 1280 orbitals, a plane-wave cutoff of 40 Ryd to expand the orbitals, a PBE(23) functional and **up to 286,820 CPUs**.

[3] J. Chem. Phys. **110**, 1029 (1999); Phys. Rev. Lett. **77**, 3865 (1996)

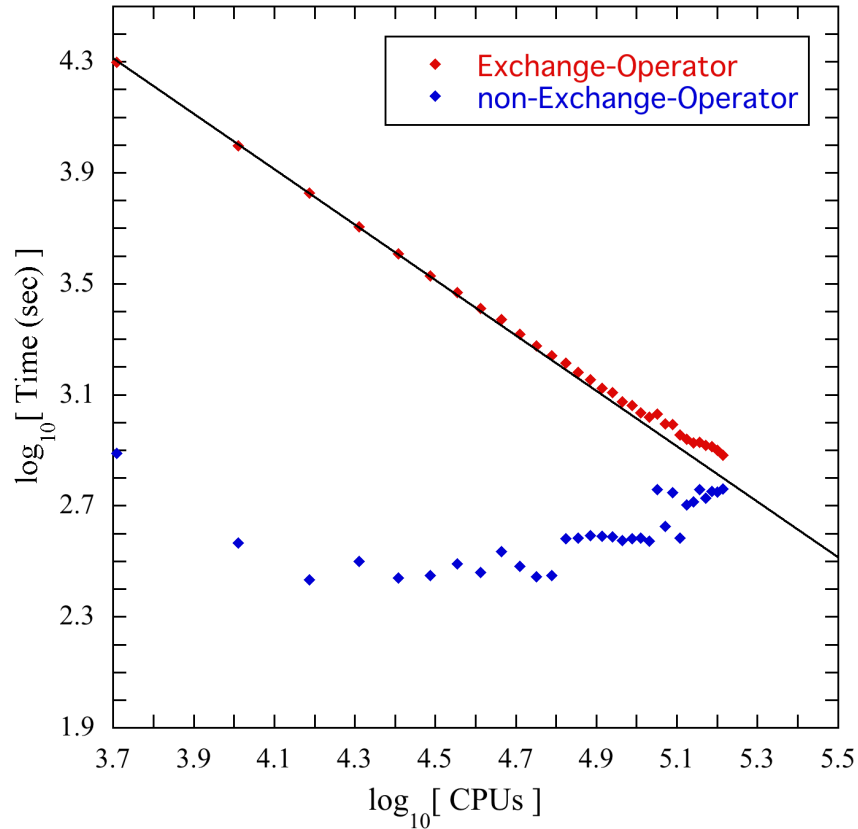
[4] J. Chem. Phys. **118**, 8207 (2003)

# Timings for GaAs in a 216-atom cell w/o threads:

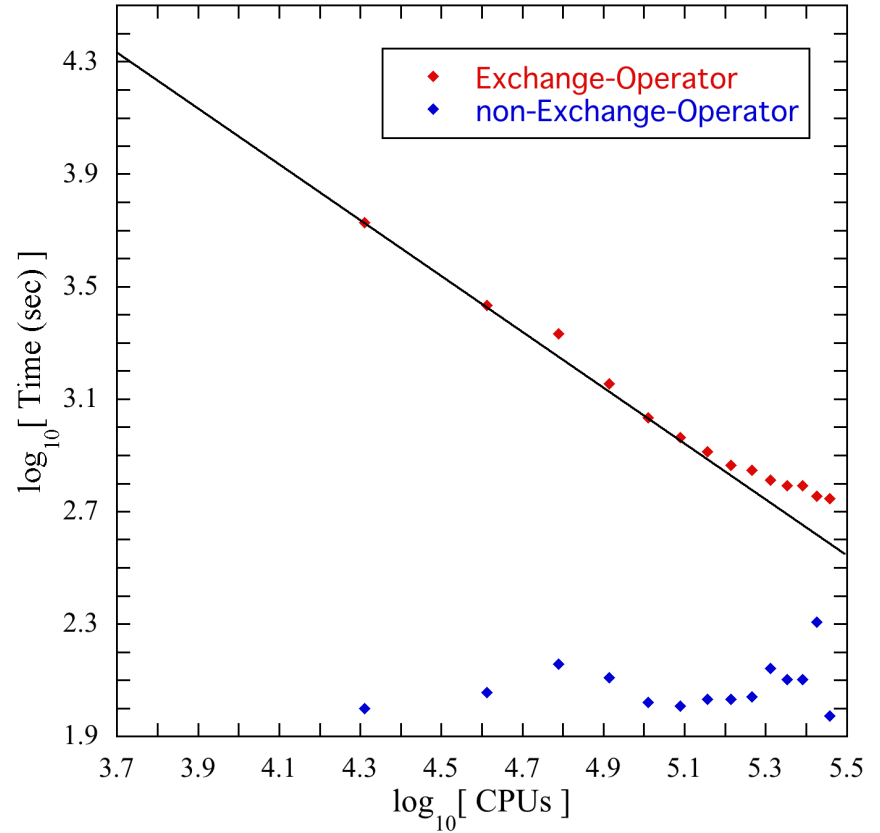


The line in the log/log plot gives the slope one should find with perfect scaling - hereafter we only show log/log plots in order to clearly reveal the scaling

# Timings for GaAs in a 216-atom cell w/ and w/o threads:

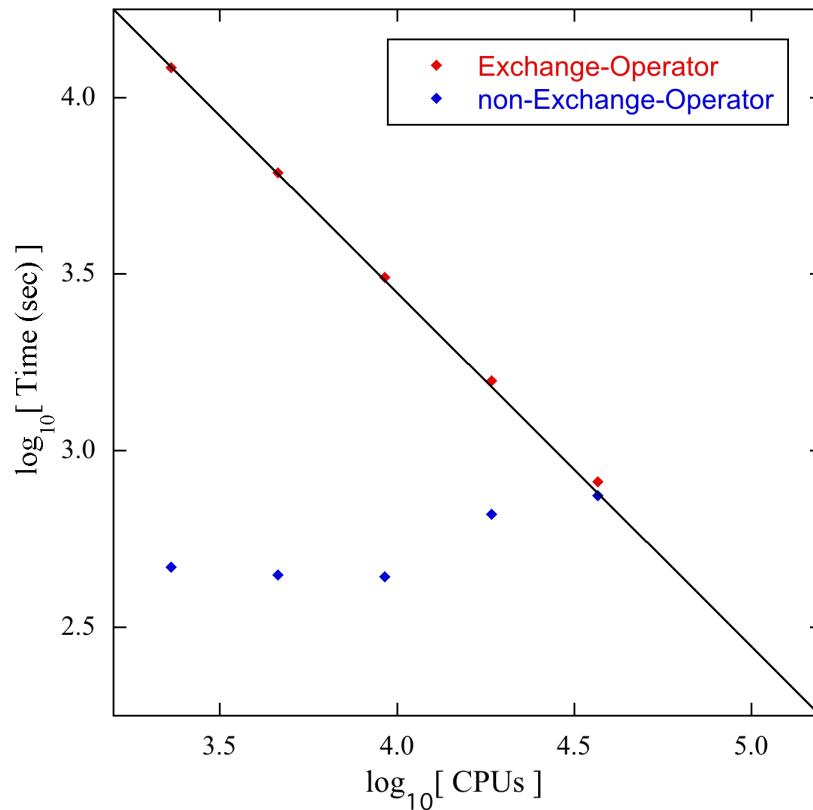


No threads

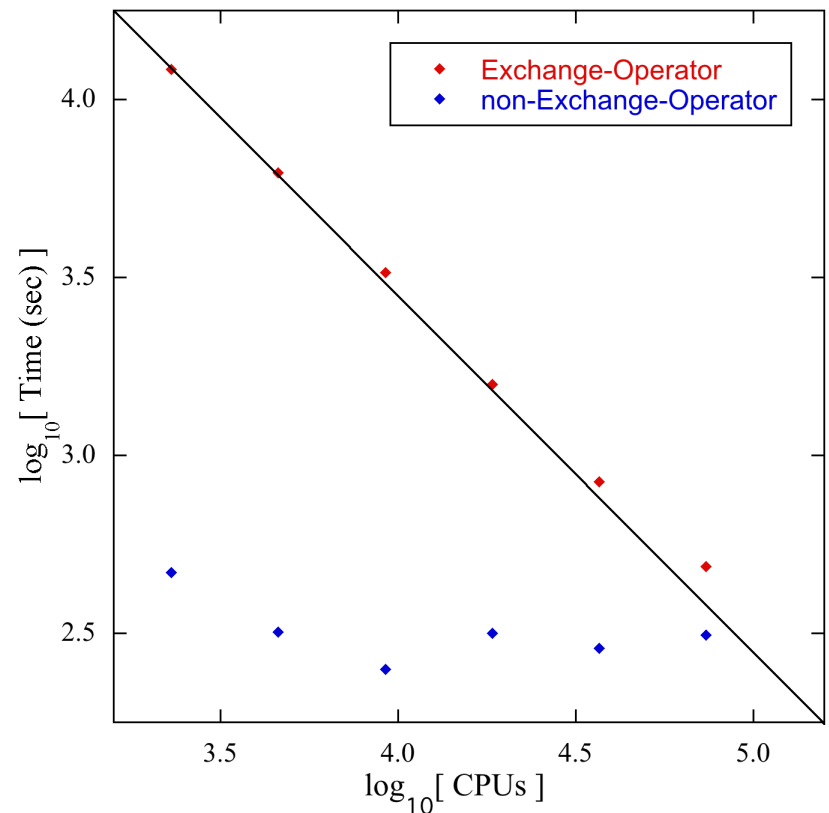


4 threads per MPI process:  
The scaling range is extended and  
non-Exchange-Operator times are reduced

# Timings for gold with w/ and w/o threads:

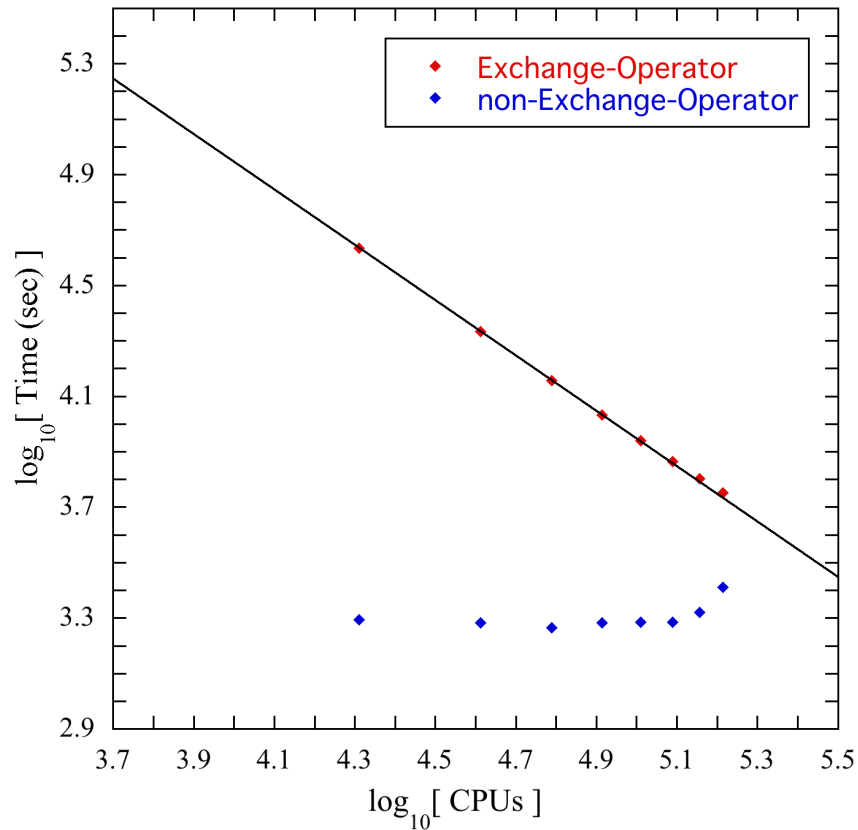


No threads

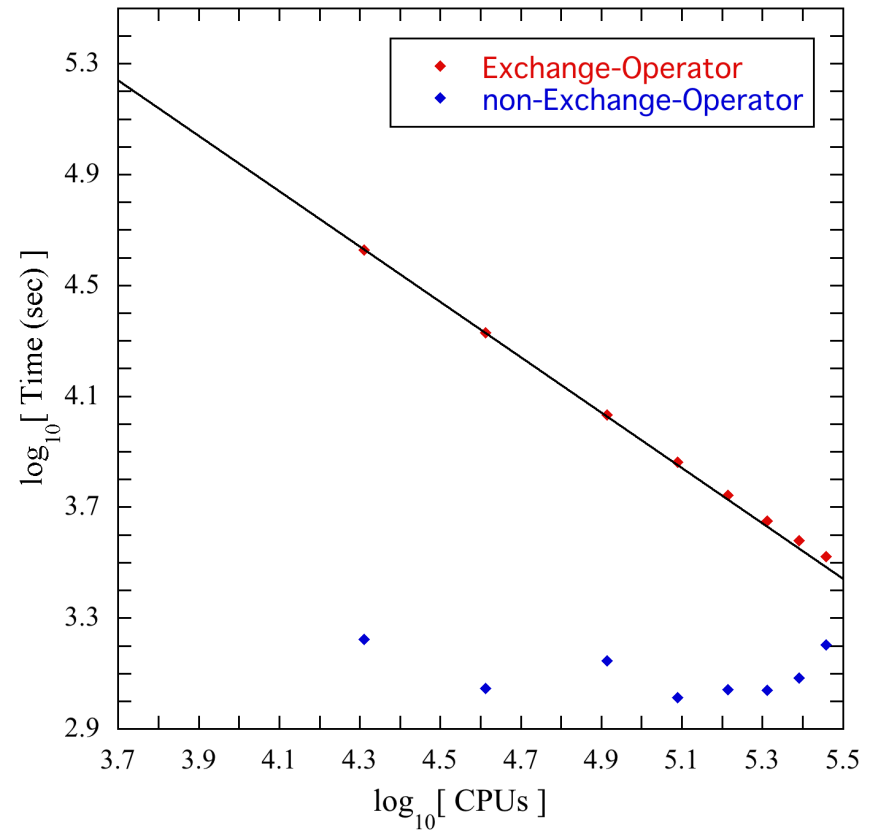


Multiple threads per MPI process"  
Scaling is extended and  
non-Exchange-Operator times are reduced

# Timings for GaAs in a 512-atom cell w/ threads:



2 threads per MPI process



4 threads per MPI process:  
Scaling runs limited by machine size

# Our Assessment of Trinity

**Hardware:** We find the Trinity (Haswell) hardware to be fast and reliable, and have used Trinity to study migration processes of a point defect in GaAs

**User Support:**

- With the help of Mike Davis and Mahesh Rajan we were able to quickly get Socorro running on Trinity with excellent performance
- We requested and were given Dedicated Application Time for some of our early scaling tests
- With the help of Joel Stevenson we easily made the transition from Moab to Slurm
- In every aspect, the level of user support we received was excellent

**Overall:** We find Trinity to be ready for production work in the Sandia Mission Areas noted in the introduction

**Future Needs:** We expect that we could efficiently use a Trinity-type machine several times larger than Trinity for anticipated work in the *Radiation-Effects* Mission Area

# Our Sincere Thanks to the High-Performance Computing Staffs at SNL and LANL, and to ASC