

TRINITY

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Scaling tests of a new algorithm for DFT hybrid-functional calculations on Trinity Haswell

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Alliance for Computing at Extreme Scale

Objective and Approach

Objective: Develop a highly scalable implementation of Density-Functional-Theory (DFT) with hybrid functionals (combining density- and orbital-dependent electron exchange) that can be used in Sandia *Radiation-Effects* and *High-Energy-Density-Physics* Mission Areas

Approach:

- Used Sandia's Socorro DFT code [1] as a development platform
- Implemented a Compact Representation (CR) [2] of the orbital-dependent exchange operator, which is constructed from derivatives of the exchange energy with respect to the orbitals...

$$\frac{\delta E_x}{\delta \psi_{n_1 \vec{k}_1}^*(\vec{r}_1)} = f_{n_1 \vec{k}_1} \sum_{\vec{k}_2} \sum_{n_2} \left(-\frac{\Omega}{2} e^2 f_{n_2 \vec{k}_2} \psi_{n_2 \vec{k}_2}(\vec{r}_1) \int_{\Omega} \frac{\psi_{n_2 \vec{k}_2}^*(\vec{r}_2) \psi_{n_1 \vec{k}_1}(\vec{r}_2)}{|\vec{r}_1 - \vec{r}_2|} d\vec{r}_2 \right)$$

- Developed a new algorithm that allows use of integer multiples (> 1) of $N_{\text{orbitals}} \times N_{\text{k-points}}$ MPI processes when constructing the CR, and multiple threads for each MPI process
- Tested and used the new algorithm under *Open Science 1* and *ATCC 1-3*

[1] dft.sandia.gov/socorro

[2] Duchemin and Gygi, *Comput. Phys. Commun.* **181**, 855 (2010)

A Simple Example of the New Algorithm

5 orbitals and 10 MPI processes

Distribution of the LHS (row, R#) orbitals

MPI Process Number	Stage		
	0	1	2
0			
1	R1		
2	R2		
3	R3		
4	R4		
5	R5		
6			
7			
8			
9			

MPI Process Number	Stage		
	0	1	2
0	R1		
1	R2		
2	R3		
3	R4		
4	R5		
5			
6			
7			
8			
9			

Distribution of the RHS (column, C#) orbitals

MPI Process Number	Stage		
	0	1	2
0	R1		
1	R2		
2	R3		
3	R4		
4	R5		
5	R1		
6	R2		
7	R3		
8	R4		
9	R5		

MPI Process Number	Stage		
	0	1	2
0	R1		
1	R2		
2	R3		
3	R4		
4	R5		
5	R1		
6	R2		
7	R3		
8	R4		
9	R5		

Accumulation of the derivatives wrt the row orbitals (DR#)

MPI Process Number	Stage		
	0	1	2
0	R1 C1		
1	R2 C2		
2	R3 C3		
3	R4 C4		
4	R5 C5		
5	R1 C1 DR1		
6	R2 C2 DR2		
7	R3 C3 DR3		
8	R4 C4 DR4		
9	R5 C5 DR5		

MPI Process Number	Stage		
	0	1	2
0	R1 C3 DR1		
1	R2 C4 DR2		
2	R3 C5 DR3		
3	R4 C1 DR4		
4	R5 C2 DR5		
5	R1 C2 DR1		
6	R2 C3 DR2		
7	R3 C4 DR3		
8	R4 C5 DR4		
9	R5 C1 DR5		

Collection of the derivative contributions

MPI Process Number	Stage		
	0	1	2
0		DR1	
1		DR2	
2		DR3	
3		DR4	
4		DR5	
5		DR1	
6		DR2	
7		DR3	
8		DR4	
9		DR5	

Scaling Tests

Overview We show scaling results for materials of interest in Sandia *Radiation-Effects* and *High-Energy-Density-Physics* Mission Areas. Each timing is from a self-consistent calculation for bulk material. Two timings are given: (1) walltime for the construction of the CR exchange operator (*Exchange-Operator*) and (2) walltime for everything else (*non-Exchange-Operator*).

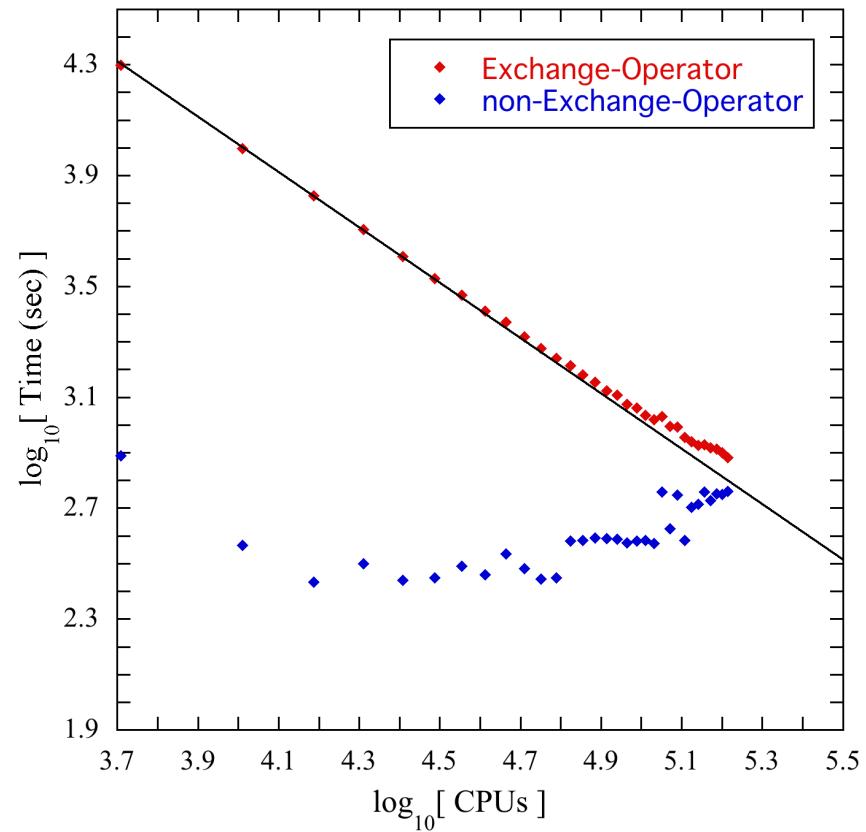
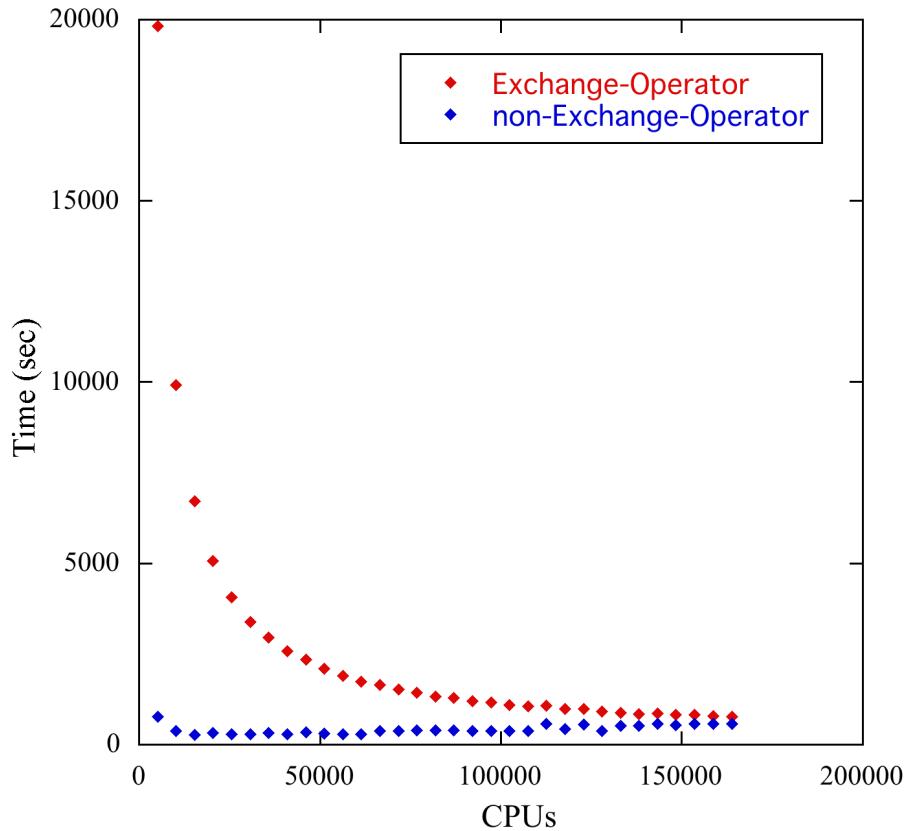
GaAs 216-atom cell: We show timings from runs using 8 k-points, 640 orbitals, a plane-wave cutoff of 40 Ryd to expand the orbitals, a PBE(23) functional [3] and **up to 286,820 CPUs**.

Gold: We show timings from runs in a 256-atom cell using 1 k-point, 2304 orbitals, a plane-wave cutoff of 50 Ryd to expand the orbitals, the HSE functional [4], and **up to 73,720 CPUs**.

GaAs 512-atom cell: We show timings from runs using 8 k-points, 1280 orbitals, a plane-wave cutoff of 40 Ryd to expand the orbitals, a PBE(23) functional and **up to 286,820 CPUs**.

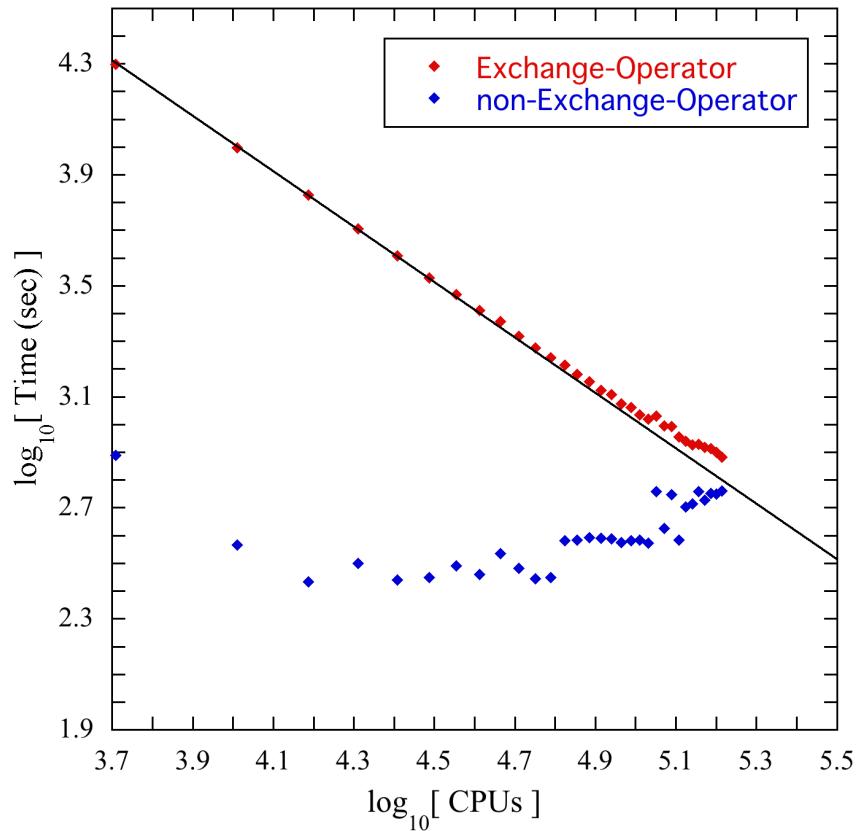
- [3] J. Chem. Phys. **110**, 1029 (1999); Phys. Rev. Lett. **77**, 3865 (1996)
- [4] J. Chem. Phys. **118**, 8207 (2003)

Timings for GaAs in a 216-atom cell w/o threads:

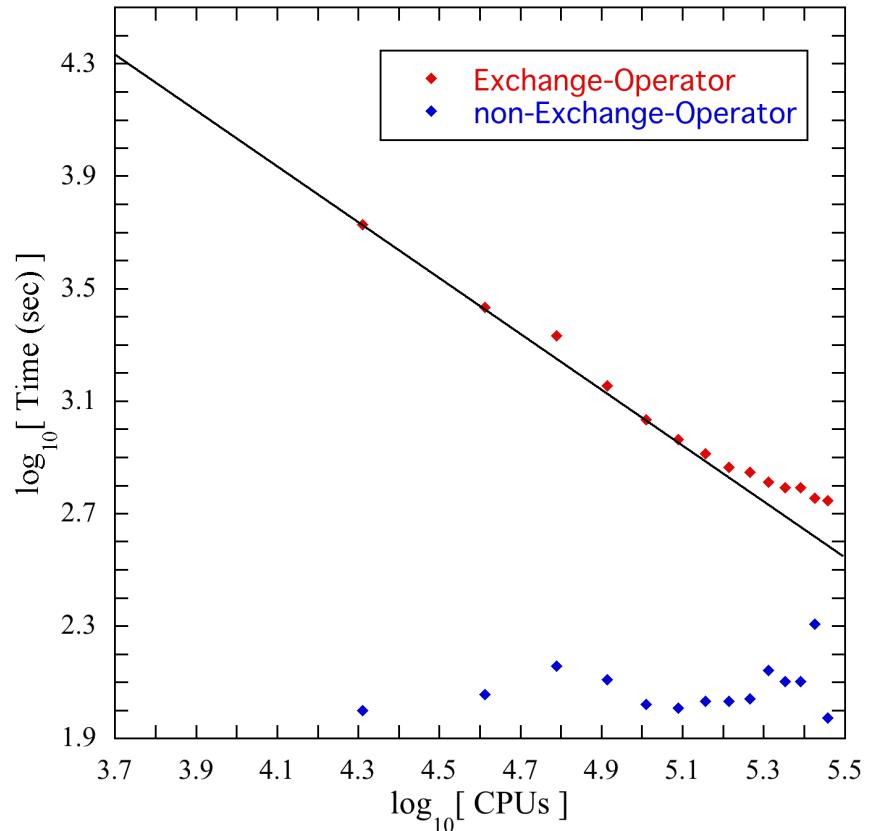


The line in the log/log plot gives the slope one should find with perfect scaling - hereafter we only show log/log plots in order to clearly reveal the scaling

Timings for GaAs in a 216-atom cell w/ and w/o threads:

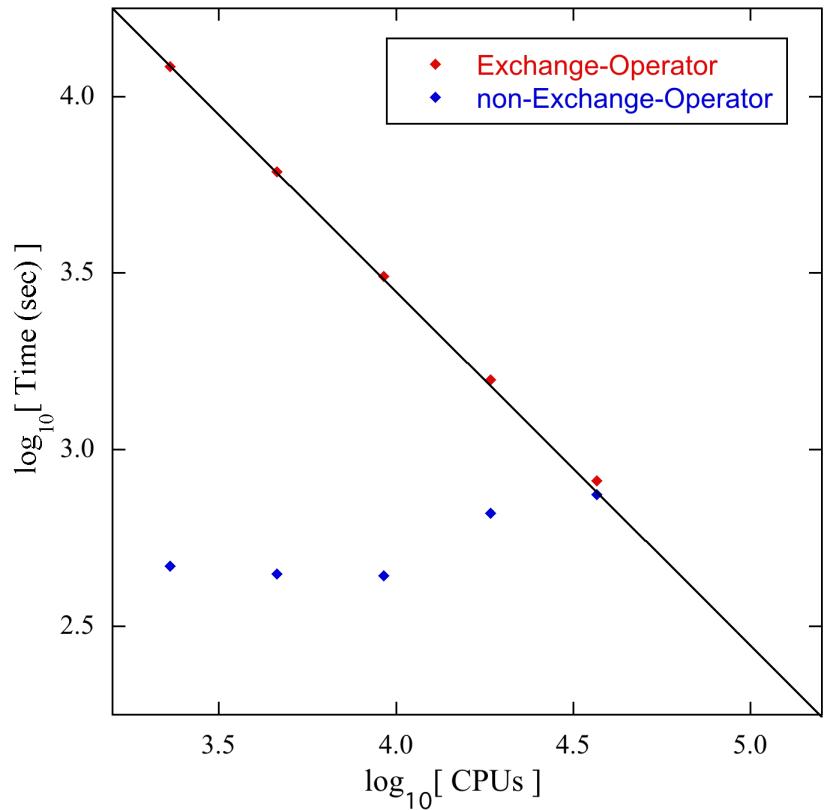


No threads

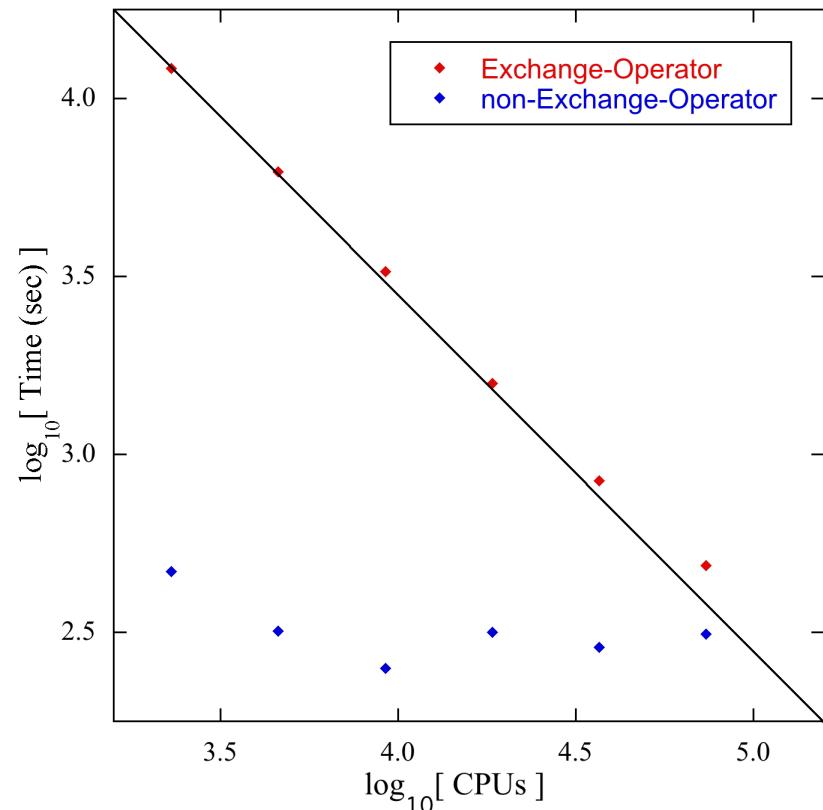


4 threads per MPI process:
The scaling range is extended and
non-Exchange-Operator times are reduced

Timings for gold with w/ and w/o threads:

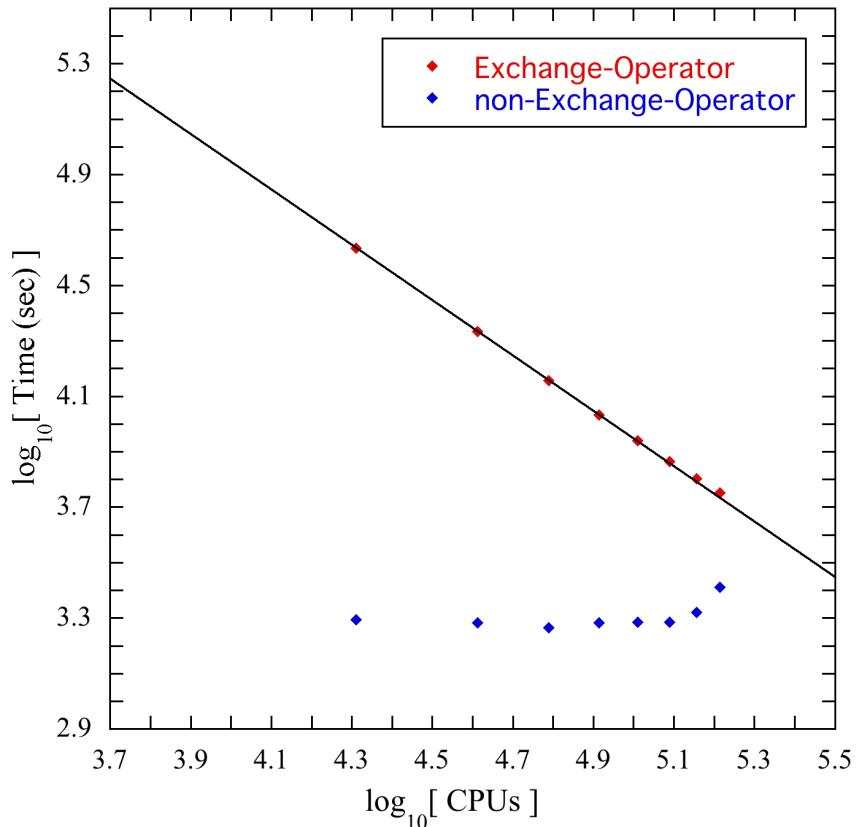


No threads

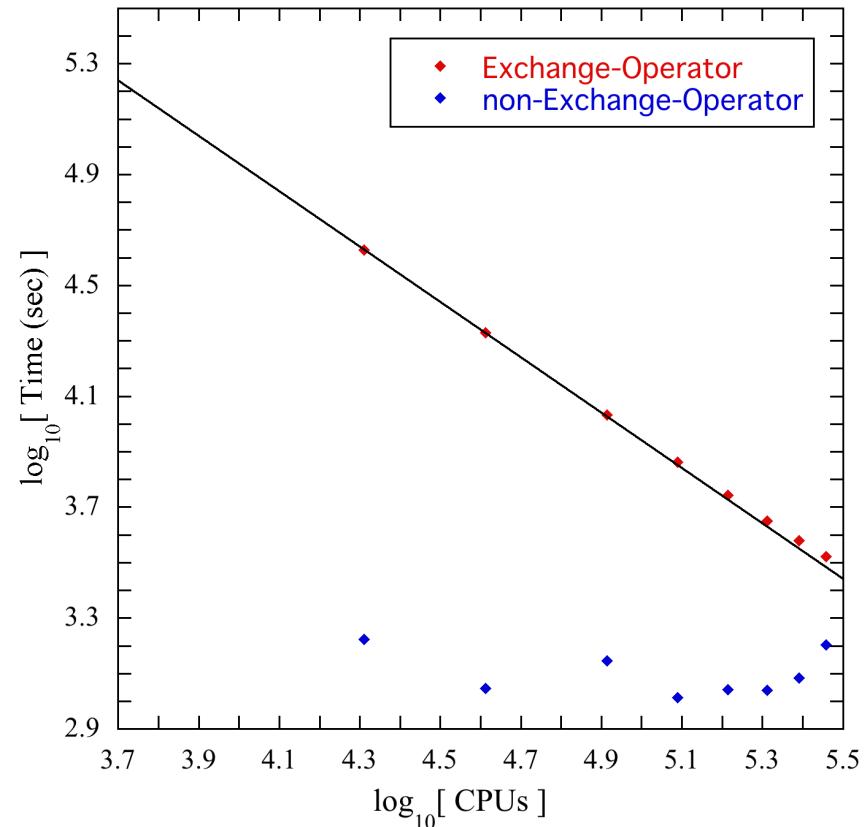


Multiple threads per MPI process"
Scaling is extended and
non-Exchange-Operator times are reduced

Timings for GaAs in a 512-atom cell w/ threads:



2 threads per MPI process



4 threads per MPI process:
Scaling runs limited by machine size

Our Assessment of Trinity

Hardware: We find the Trinity (Haswell) hardware to be fast and reliable, and have used Trinity to study migration processes of a point defect in GaAs

User Support:

- With the help of Mike Davis and Mahesh Rajan we were able to quickly get Socorro running on Trinity with excellent performance
- We requested and were given Dedicated Application Time for some of our early scaling tests
- With the help of Joel Stevenson we easily made the transition from Moab to Slurm
- In every aspect, the level of user support we received was excellent

Overall: We find Trinity to be ready for production work in the Sandia Mission Areas noted in the introduction

Future Needs: We expect that we could efficiently use a Trinity-type machine several times larger than Trinity for anticipated work in the *Radiation-Effects* Mission Area

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