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## A Constitutive Model for Jointed Rock Mass With Two Intersecting Sets of Joints

E. P. Chen

Prepared by  
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Albuquerque, New Mexico 87185 and Livermore, California 94550  
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# A Constitutive Model for Jointed Rock Mass with Two Intersecting Sets of Joints

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## Abstract

A constitutive model that describes the response of a jointed rock mass under applied loads has been developed in this investigation following similar procedures used previously by the author for two orthogonal joint sets. However, the present model is more general than the orthogonal joint set model because the joint sets can intersect at arbitrary angles. The mechanical behavior of the intact rock is considered elastic while the joint closure and slip response are nonlinear in nature. By using the constitutive model, the field equations have been reduced to a fourth-order algebraic equation for the solution of stresses; this equation is given explicitly in the text. Example problems have been solved to show how the rock mass responds to loads, and the effects of joint sets intersecting at nonorthogonal angles have been investigated and presented.

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## 1. Introduction

This investigation involves the development of a general two-dimensional continuum model to describe jointed rock mass. Chen (1986,1989) recently developed a model for the analysis of rock mass containing two orthogonal joint sets. Development of the orthogonal joint set model followed the general formulation of Morland (1974) and the special single joint set implementation of Morland's model by Thomas (1982). Although the orthogonal joint set model has proven useful for analyzing field-scale problems (see Costin and Chen; 1988a, 1988b), it remains restrictive in terms of the general field conditions. In this paper, the orthogonal joint set model has been extended to a more general model where the orthogonality restriction has been relaxed. Fundamental approaches remain the same for both models. However, as the general model becomes capable of treating physically more complicated problems, it becomes mathematically more complex. This complexity provides the potential to study more completely the interaction of various parameters representing the characteristics of jointed rock mass behavior. The equation governing the solution of the problem has been given, and example problems have been solved. The behavior of the rock mass predicted by the orthogonal joint set model has been compared to the general model.

This model has been developed to aid in characterizing the site of the repository at Yucca Mountain, Nevada, for the potential geologic disposal of radioactive waste. Disposal of high-level nuclear waste is currently being considered by the Yucca Mountain Project, administered by the Nevada Operations Office of the U. S. Department of Energy.

## 2. Constitutive Model Formulation and Solution

As has been mentioned previously, the procedure for developing the general model is the same as that given in Chen (1986,1989) for the orthogonal joint set model. The arrangement of a representative element of a jointed rock mass is shown in Figure 1. In this figure, two joint sets with joint spacings  $\delta_1$  and  $\delta_2$  are inclined against each other with an included angle  $\theta$ . The joints in a given set are assumed to be regularly spaced and parallel. In the plane of the joints, the orientation of the joint sets is characterized by the angles  $\theta_1$  and  $\theta_2$  with respect to a reference Cartesian coordinate  $xyz$  system, as shown in Figure 2. The plane of the joints are in the  $xy$ -plane. Also given in Figure 2 are the in-plane normals  $n_1$  and  $n_2$  and the out-of-plane normals  $t_1$  and  $t_2$  to the sets of joints. Note that the directions  $z$ ,  $t_1$ , and  $t_2$  coincide. Following the work of Morland (1974), a continuous displacement field can be defined that represents the average response of the joints. While this displacement field cannot give the individual responses of the joints, it captures the gross responses of all joints in an average sense. Based on the continuous displacement fields for the joints, a strain partitioning equation can be written for the rock mass in which the total strain is equal to the sum of the strains of the intact rock and the joints. The constitutive behavior for the intact rock is considered elastic. For a single joint, normal closure is assumed to be nonlinear elastic and to follow the empirical behavior given by Goodman (1976):

$$T_{nn} = -A \left( \frac{u^d}{u_{max}^d - u^d} \right) \quad (1)$$

where  $T_{nn}$  and  $u^d$ , the normal stress component and the corresponding displacement across the joint, are positive in tension. The constant  $A$  is referred to as the half-closure stress and  $u_{max}^d$  is the maximum amount of closure that can be sustained by the joint (see Figure 3 for definitions of these quantities). The joint is allowed to carry tension to expedite the numerical computations. Because the allowable tension is relatively small (maximum tension carried by the joint will not exceed the magnitude of the half-closure stress even for very large opening displacements), the gain in computation speed seems to outweigh this minor physical discrepancy. The joint slip behavior is defined by a bilinear shear stress-slip displacement response, shown in Figure 4. The onset of nonlinearity is governed by the Mohr-Columb criterion as

$$|\tau_p| = C_0 - \mu T_{nn} \quad (2)$$

in which  $C_0$  and  $\mu$  are, respectively, the cohesion and the coefficient of Coulomb friction.

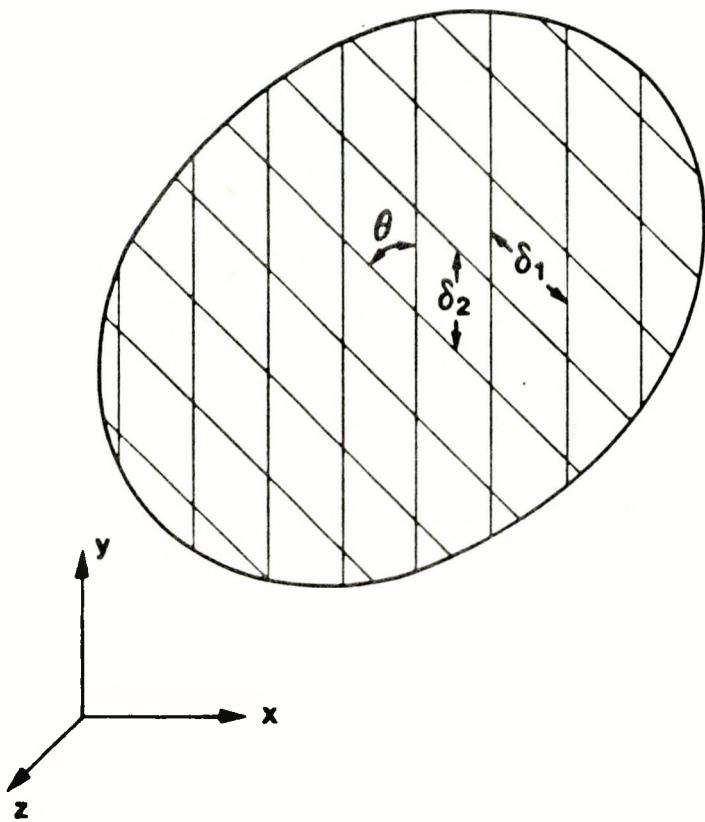


Figure 1. Geometry of Jointed Rock Mass

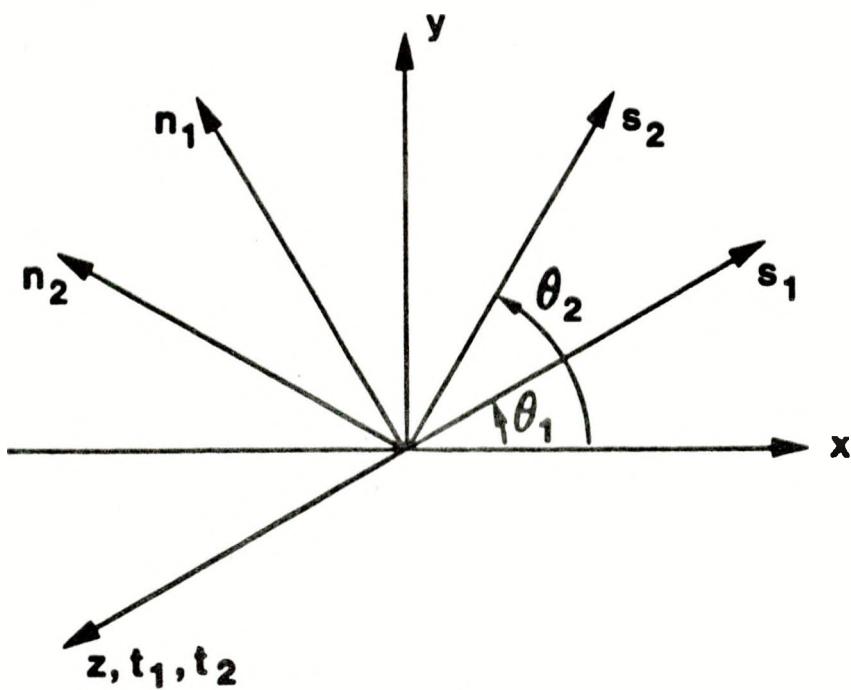


Figure 2. Joint Orientation Definitions

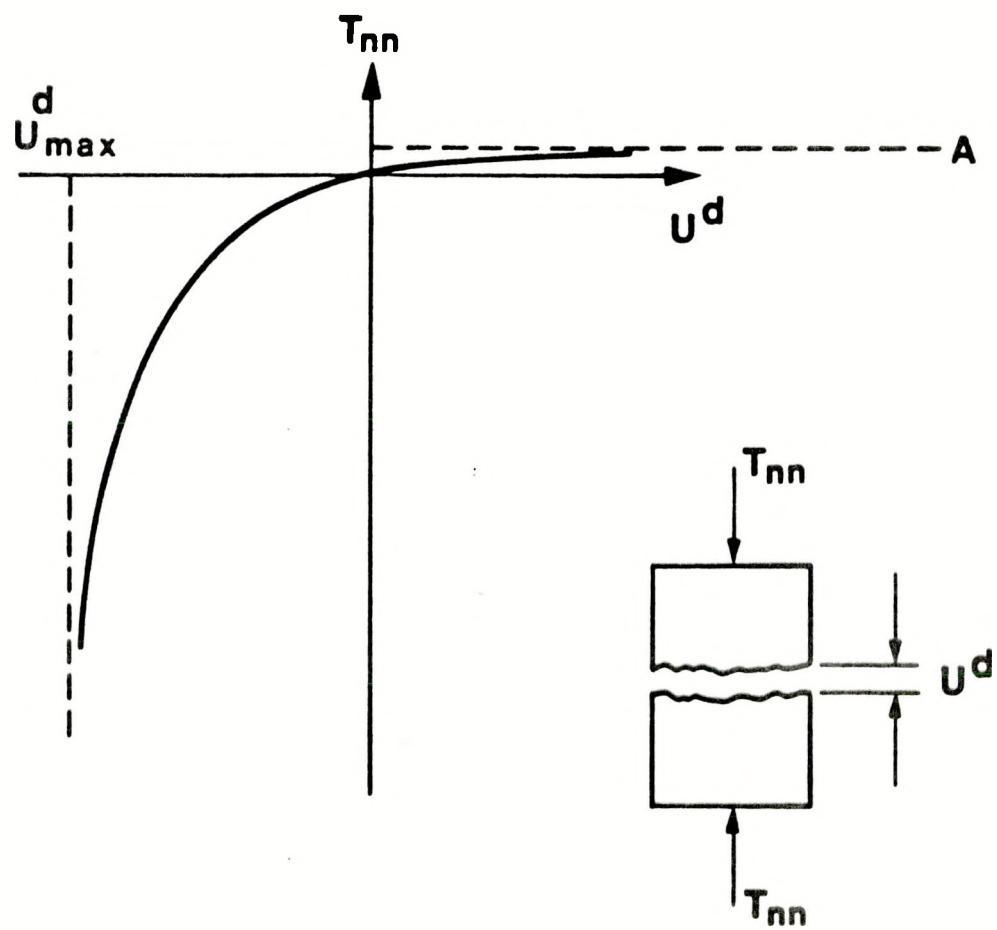


Figure 3. Nonlinear Normal Joint Closure Behavior

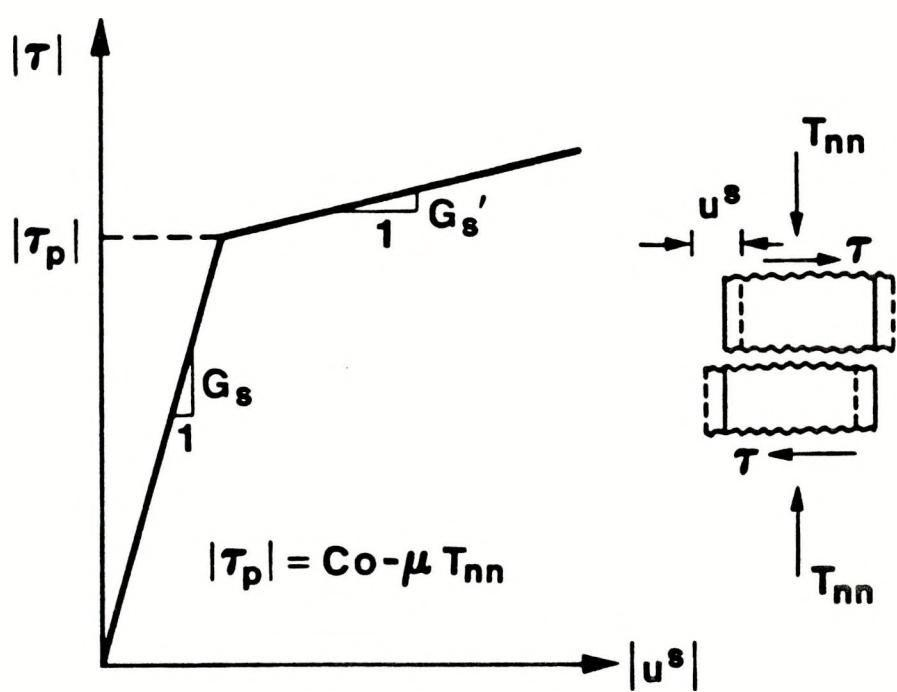


Figure 4. Nonlinear Shear Behavior of Joints

Because the problem is nonlinear in nature, incremental procedures are used to obtain solutions. The strain partitioning relationships and the above constitutive models for the intact rock and joints can be combined to establish a set of rate equations for calculating stress increments in terms of strain increments. This procedure is the same as that given by Chen (1986, 1989) for orthogonal joint sets. In Chen (1986, 1989), the problem was reduced to the solution of a fourth-order algebraic equation. In the present general case, it has been found that the problem can also be reduced to the solution of a fourth-order algebraic equation. However, the solution for the general case is more complicated because without orthogonality, coupling occurs between the normal and shear stress components. Moreover, the coefficients in the equation become more complex because an additional parameter, the included angle between the two joint sets, also appears.

In the remainder of this section, the algebraic expressions necessary for numerical implementation of the present model are presented. Note that the resulting fourth-order equation can be solved by the same procedure as given in Chen (1989). Let the bulk modulus and the shear modulus of the intact rock be  $K$  and  $G$ , respectively. For joint set  $i$ ,  $i=1,2$ , the half-closure stress is  $A_i$ , the maximum closure is  $(u_{max}^d)_i$ , and the slopes of the bilinear shear stress-slip displacement curve are  $G_{ei}$  and  $G'_{ei}$ , respectively, for the initial and the hardening part. Without going into details, the fourth-order algebraic equation to calculate the normal stress for joint set 1 at time step  $t+1$  advancing from time step  $t$  is derived as [for detailed derivation procedure, references are made to the work of Chen (1986, 1989)]:

$$a_1 T_n^4 + a_2 T_n^3 + a_3 T_n^2 + a_4 T_n + a_5 = 0 \quad (3)$$

in which  $T_n = A_1 - T_{n,n_1}^{t+1}$  and the coefficients are

$$a_1 = \frac{4GS^2(1 - \alpha_6 + \alpha_5) + 2S^2\alpha_5\alpha_6\alpha_8 + \alpha_1\alpha_7}{2S^2\alpha_5(2GC + \alpha_6\alpha_8) + \alpha_3\alpha_7} \quad (4)$$

$$a_2 = \gamma_{10} - b_1\gamma_{11}, \quad a_3 = (2G\beta_2 - \gamma_{10} \text{ gamma}_{11})b_3 - a_1b_2 - (b_4 - b_5 + b_6) \quad (5)$$

$$a_4 = (b_4 - b_5 + b_6)b_3\gamma_{11} - b_2\gamma_{10}, \quad a_5 = b_2(b_4 - b_5 + b_6). \quad (6)$$

In the above equations, the following contractions have been made:

$$\alpha_1 = K + 4G/3, \quad \alpha_2 = K - 2G/3, \quad \alpha_3 = K - 2G(1/3 - \cos^2\theta) \quad (7)$$

$$\alpha_4 = K - 2G(1/3 - \sin^2\theta), \quad \alpha_5 = \frac{G}{\delta_2 G_{s2}}, \quad \alpha_6 = 1 + \frac{G}{\delta_1 G_{s1}} \quad (8)$$

$$\alpha_7 = \alpha_5 C^2 + \alpha_6, \quad \alpha_8 = 2(K + G/3), \quad \alpha_9 = \alpha_1\alpha_4 - \alpha_2\alpha_3 \quad (9)$$

$$S = \sin\theta\cos\theta, \quad C = \cos^2\theta - \sin^2\theta, \quad \beta_i = -A_i(u_{max}^d)_i/\delta_i, \quad i = 1, 2 \quad (10)$$

$$b_1 = -\frac{4GS^2(1 - \alpha_6 + \alpha_5) + 2S^2\alpha_5\alpha_6\alpha_8 + \alpha_1\alpha_7}{2G(4S^2\alpha_5\alpha_6 + \alpha_7)} \quad (11)$$

$$b_2 = \frac{\beta_1\{2S^2\alpha_5\alpha_6(\alpha_1 + \alpha_2) + \alpha_1\alpha_7\}}{4S^2\alpha_5\alpha_6 + \alpha_7}, \quad b_3 = -\frac{2S^2\alpha_5(2GC + \alpha_6\alpha_8) + \alpha_3\alpha_7}{2G(4S^2\alpha_5\alpha_6 + \alpha_7)} \quad (12)$$

$$b_4 = \frac{\beta_1 \sin^2 \theta (\alpha_1\alpha_4 - \alpha_2\alpha_3)(\alpha_6 - \alpha_5C)}{2S^2\alpha_5(2GC + \alpha_6\alpha_8) + \alpha_3\alpha_7} \quad (13)$$

$$b_5 = \frac{4G\beta_1 S^2\alpha_5C(\alpha_1 + \alpha_2)\sin^2 \theta}{2S^2\alpha_5(2GC + \alpha_6\alpha_8) + \alpha_3\alpha_7}, \quad b_6 = \frac{4G\beta_1 S^2\{\alpha_1 + 2S^2\alpha_5(\alpha_1 + \alpha_2)\}}{2S^2\alpha_5(2GC + \alpha_6\alpha_8) + \alpha_3\alpha_7} \quad (14)$$

$$p_1 = \frac{\alpha_4\alpha_7 - 2S^2\alpha_5(2GC - \alpha_6\alpha_8)}{2S^2\alpha_5(2GC + \alpha_6\alpha_8) + \alpha_3\alpha_7}, \quad p_3 = \frac{2G(1 + \alpha_5)}{2S^2\alpha_5(2GC + \alpha_6\alpha_8) + \alpha_3\alpha_7} \quad (15)$$

$$p_2 = \frac{\beta_1\{\alpha_7(\alpha_1\alpha_4 - \alpha_2\alpha_3) - 4\alpha_5GCS^2(\alpha_1 + \alpha_2)\}}{2S^2\alpha_5(2GC + \alpha_6\alpha_8) + \alpha_3\alpha_7} \quad (16)$$

$$p_4 = \frac{\beta_1\{2G(\alpha_1 + 2S^2\alpha_5(\alpha_1 + \alpha_2)) - \alpha_5C(\alpha_1\alpha_4 - \alpha_2\alpha_3)\}}{2S^2\alpha_5(2GC + \alpha_6\alpha_8) + \alpha_3\alpha_7} \quad (17)$$

$$\gamma_0 = (\alpha_4 - \alpha_2C)\Delta\epsilon_{n_1n_1} - (\alpha_3 + \alpha_2C)\Delta\epsilon_{s_1s_1} - \alpha_2C\Delta\epsilon_{t_1t_1} \quad (18)$$

$$\gamma_1 = \alpha_1S\Delta\epsilon_{n_1n_1} + \alpha_2S(\Delta\epsilon_{s_1s_1} + \Delta\epsilon_{t_1t_1}) - \alpha_3\Delta\epsilon_{n_1s_1} \quad (19)$$

$$\gamma_2 = \alpha_1S\Delta\epsilon_{s_1s_1} + \alpha_2S(\Delta\epsilon_{n_1n_1} + \Delta\epsilon_{t_1t_1}) - \alpha_4\Delta\epsilon_{n_1s_1} \quad (20)$$

$$\gamma_3 = -\frac{2G\{2S\alpha_5C(\gamma_1 + \gamma_2) + \alpha_7\gamma_0\}}{2S^2\alpha_5(2GC + \alpha_6\alpha_8) + \alpha_3\alpha_7} \quad (21)$$

$$\gamma_4 = -\frac{2G\{S\alpha_5(2S(\gamma_1 + \gamma_2) + C\gamma_0) + \gamma_1\}}{2S^2\alpha_5(2GC + \alpha_6\alpha_8) + \alpha_3\alpha_7} \quad (22)$$

$$\gamma_5 = -\{2G\Delta\epsilon_{n_1s_1} + \alpha_5CS\gamma_3 - (\alpha_6 + \alpha_5C^2)\gamma_4\}/S \quad (23)$$

$$\gamma_6 = \gamma_5 + \frac{2G\beta_2}{A_2 - T_{n_2n_2}^t} - \frac{T_{n_1n_1}^t}{b_3} - \frac{b_2}{b_3(A_1 - T_{n_1n_1}^t)} \quad (24)$$

$$\gamma_7 = \gamma_3 - p_1T_{n_1n_1}^t + T_{s_1s_1}^t - \frac{p_2}{A_1 - T_{n_1n_1}^t} \quad (25)$$

$$\gamma_8 = \gamma_4 + Sp_3T_{n_1n_1}^t + T_{n_1s_1}^t + \frac{Sp_4}{A_1 - T_{n_1n_1}^t} \quad (26)$$

$$\gamma_9 = \gamma_7 \sin^2 \theta - 2S\gamma_8, \quad \gamma_{10} = A_2 - \gamma_9 - \frac{b_1A_1}{b_3}, \quad \gamma_{11} = \gamma_6 + \frac{A_1}{b_3}. \quad (27)$$

Because the strain increments  $\Delta\epsilon_{ij}$  and the stresses at the beginning of the load step  $T_{ij}^t$  are known,  $T_{n_1n_1}^{t+1}$  can be obtained from Equation (3). The other stress components associated with joint set 1 can be found from

$$T_{s_1s_1}^{t+1} = p_1T_{n_1n_1}^{t+1} + \gamma_7 + \frac{p_2}{A_1 - T_{n_1n_1}^{t+1}} \quad (28)$$

$$T_{n_1 s_1}^{t+1} = S p_3 T_{n_1 n_1}^{t-1} + \gamma_k + \frac{S p_4}{A_1 - T_{n_1 n_1}^{t-1}} \quad (29)$$

$$T_{t_1 t_1}^{t+1} = T_{t_1 t_1}^t - \Delta T_{t_1 t_1} \quad (30)$$

where the stress increment is given by

$$\Delta T_{t_1 t_1} = \frac{6 K G}{\alpha_8} \Delta \epsilon_{t_1 t_1} + \frac{\alpha_2}{\alpha_k} (\Delta T_{n_1 n_1} - \Delta T_{s_1 s_1}) . \quad (31)$$

Stress components in the Cartesian coordinate  $xyz$  system and in the second joint set  $n_2 s_2 t_2$  reference frame can easily be determined from the above stresses through the stress transformation equations. There remains the question of determining the shear stress when the stress level exceeds the onset of nonlinearity as governed by the Coulomb criterion. When this happens, the shear stress increment is calculated from the strain partitioning equation where an analytical expression can be derived. In this manner, it is ensured that the strain partitioning equation is satisfied and that the calculated shear stress and slip displacement follow the material property curve. Again, the solution procedures are similar to those for the orthogonal joint sets model in Chen (1986, 1989). A driver program has been written for the constitutive model, based on the above equations. This program calculates stress increments when strain increments are given and will be used to solve example problems to demonstrate some of the interesting features of the model.

### 3. Example Problems

Several example problems are solved here to demonstrate the model. The following rock properties, taken from the work of Thomas (1982), are used in all examples:

#### Intact Rock

$$K = 4.59 \text{ GPa}, G = 2.76 \text{ GPa}$$

#### Joint Properties

$$A_n = 6.89 \text{ MPa}, (u_{max}^d)_n = -0.00762 \text{ cm}$$

$$(G_s)_n = 0.27 \text{ GPa/cm}, (G'_s)_n = 2.71 \text{ MPa/cm}$$

$$\mu_n = 0.7, (C_0)_n = 1.72 \text{ MPa}, \delta_n = 1.27 \text{ cm}$$

For convenience, both joint sets are assumed to have the same properties. The geometry of the example problems is that in Figure 5. An infinite rock mass is to be strained in the Cartesian coordinate  $xy$ -plane. One joint set has a fixed horizontal direction while the direction of the other joint set varies depending on the parameter  $\theta$ . Initial stress states can also be imposed on the rock mass.

In the first example, the rock mass is loaded by uniaxial compression along the  $y$ -direction. Boundary conditions are applied such that the value for  $\epsilon_y$  is varied linearly from 0.0 to -0.005 for the time history of the problem. The rock is constrained such that all other strain components ( $\epsilon_x, \epsilon_z, \epsilon_{xy}$ ) are zero during the entire loading process. An initial stress state of  $\sigma_x = \sigma_y = \sigma_z = -1.38 \text{ MPa}$  and  $\tau_{xy} = 0.0$  is assumed to prevail in the rock mass. Results have been obtained for  $\theta = 30^\circ, 60^\circ$ , and  $90^\circ$ . The effect of the angle  $\theta$  can be seen in a plot of the variation of the normal stress on the joint against the applied strain for joint sets 1 and 2 (Figures 6 and 7). From Figure 6 it is seen that the magnitude of the normal stress increases as angle  $\theta$  increases. This is because, as  $\theta$  increases, more load is shifted from the second joint set to the horizontal first joint set simply from the geometric configuration. For the same reason, the magnitude of the normal stress on joint set 2 should decrease with respect to increasing angle  $\theta$ . This is the result shown in Figure 7. Note that the stress state in the coordinate  $xy$ -plane is the same as that for the first joint set because of the geometry selected for the example problems.

The second example involves the pure shear loading on the rock mass. The shear strain  $\epsilon_{xy}$  is increased linearly from 0 to 0.01 over the time history of the problem while

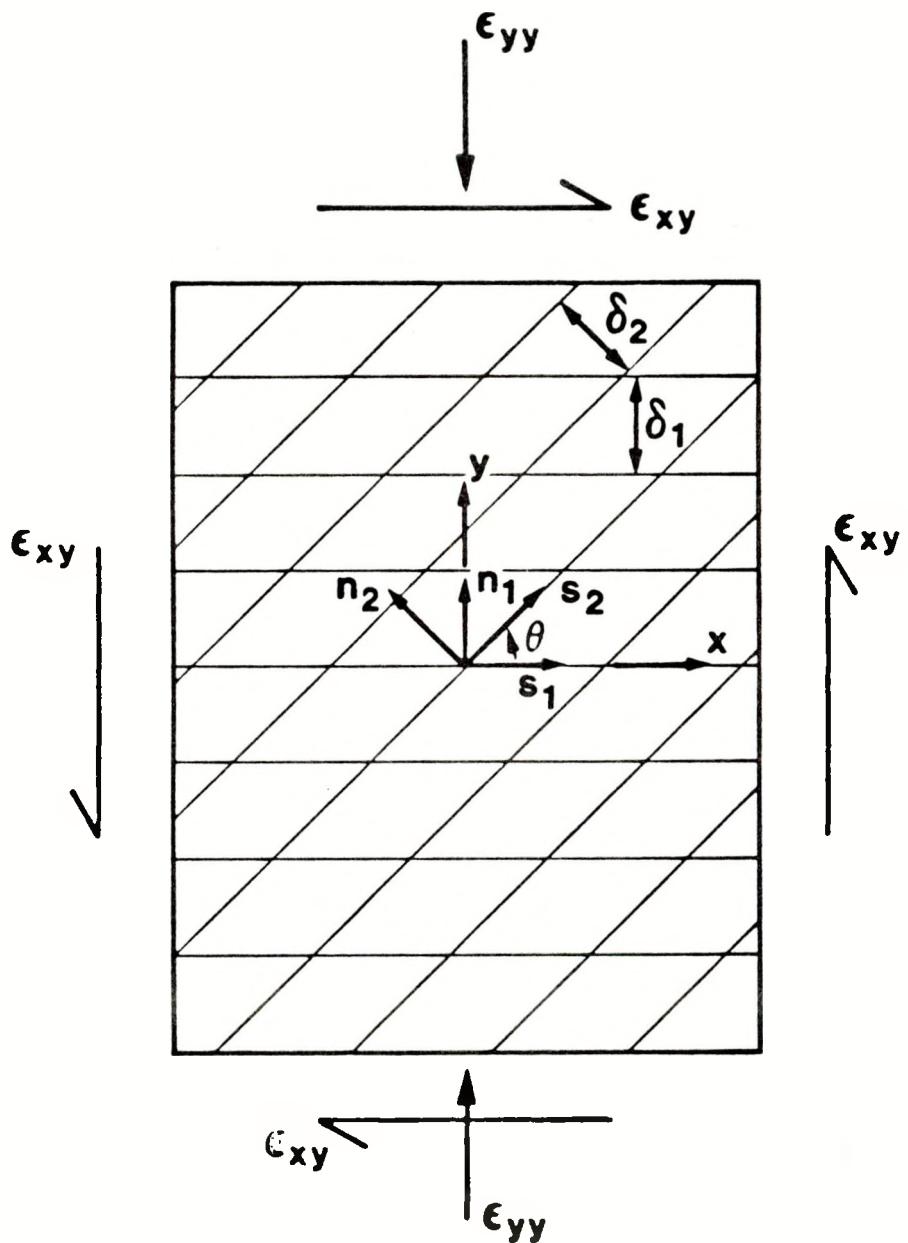


Figure 5. Example Problem Geometry

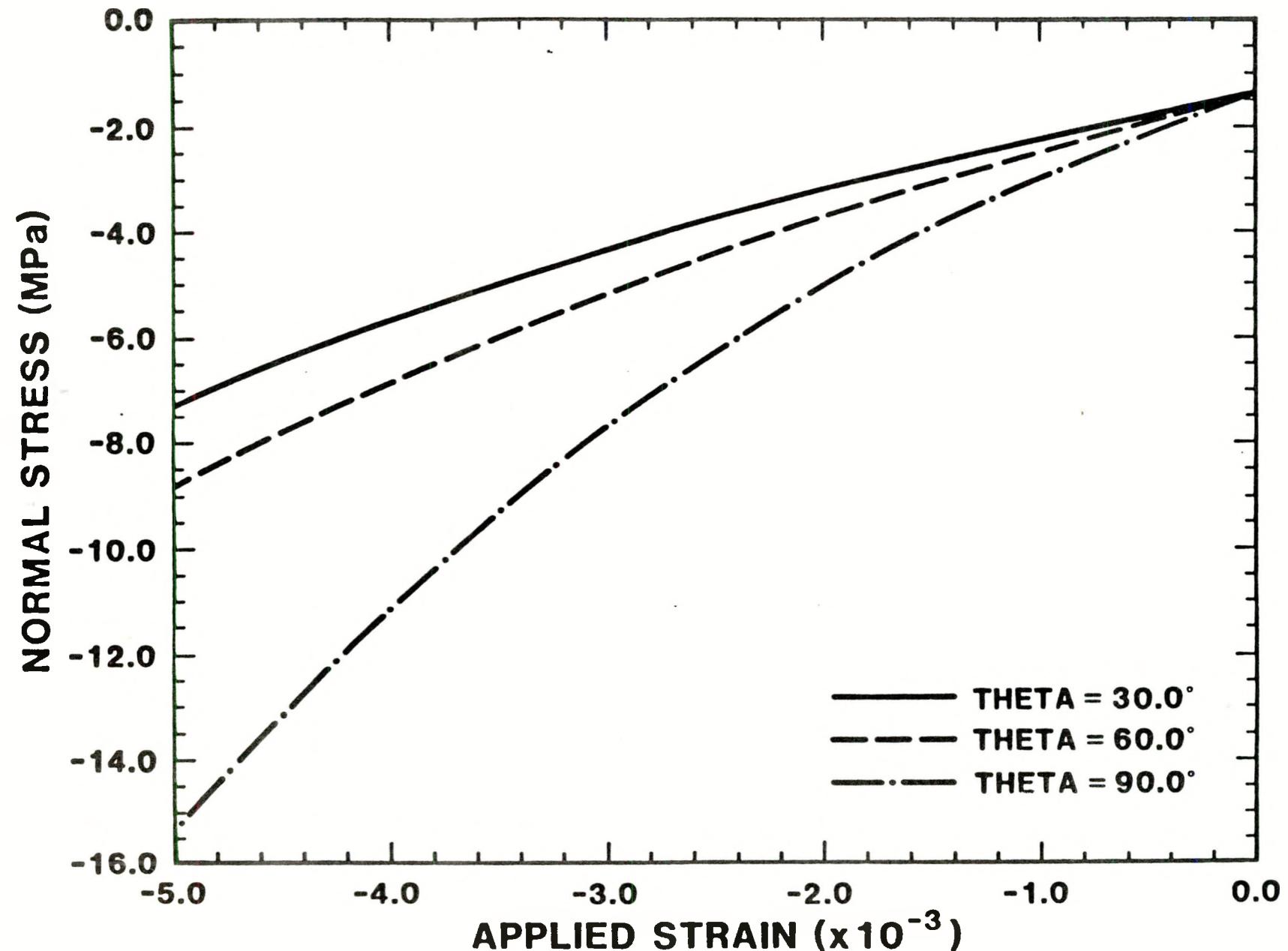


Figure 6. Stress-Strain Behavior for Joint Set 1, Example 1

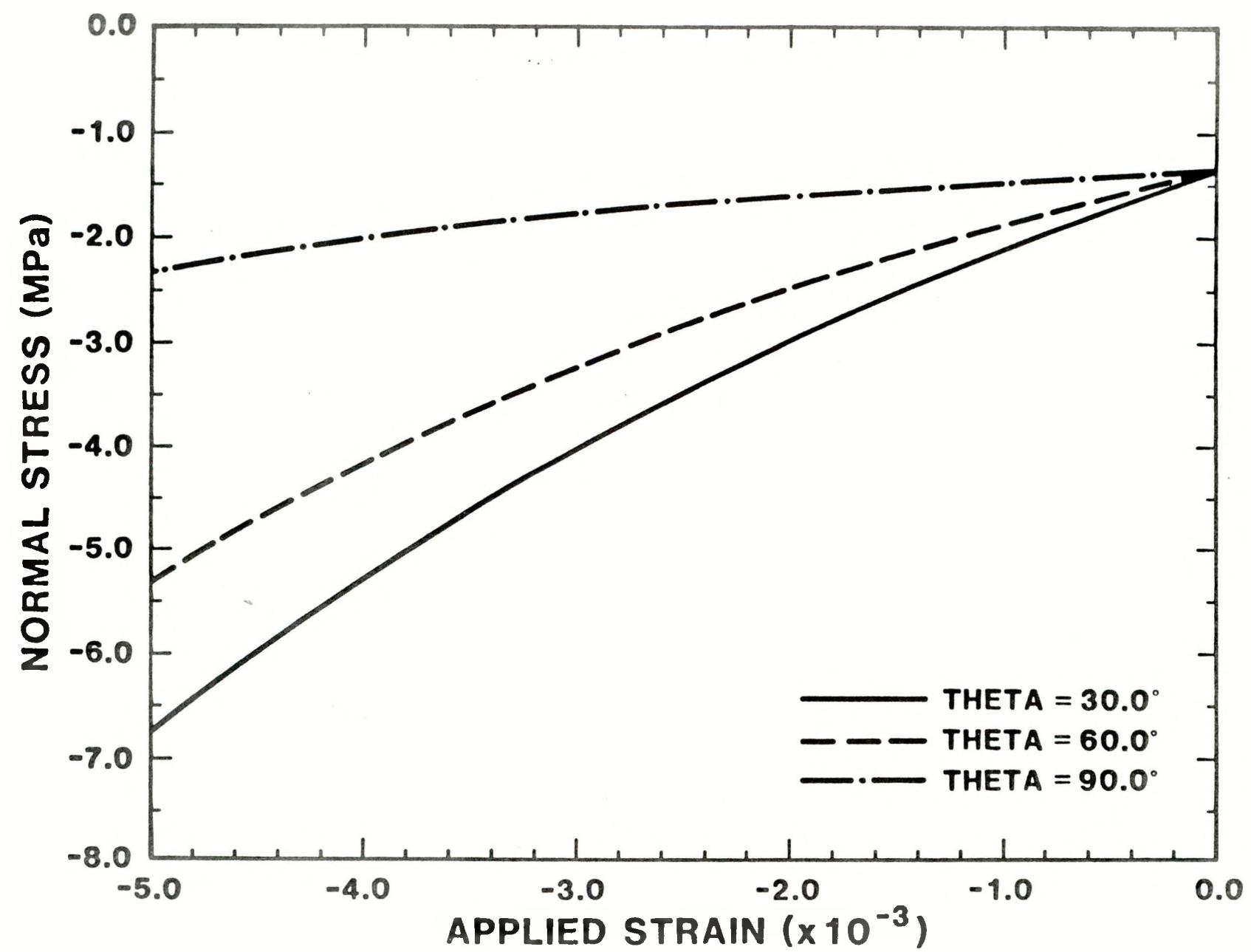


Figure 7. Stress-Strain Behavior for Joint Set 2, Example 1

all the normal strains are constrained to be zero throughout the shearing process. An initial stress state of  $\sigma_x = \sigma_z = -1.38$  MPa and  $\sigma_y = -3.45$  MPa is imposed on the system. Again, the results for  $\theta$  equals  $30^\circ$ ,  $60^\circ$  and  $90^\circ$  have been calculated. Figure 8 shows the variations of the shear stress as a function of the applied shear strain for the first (horizontal) joint set. The curves are initially linear up to some applied strain level and then begin to deviate from linearity. The trend indicates that shear stress increases as the angle  $\theta$  increases. The shear stress versus applied shear strain plots for the second joint set are shown in Figure 9. Because of the imposed initial stress state, the initial shear stresses for joint sets oriented at  $\theta$  equal to  $30^\circ$  and  $60^\circ$  are nonzero. The magnitudes of these initial shear stresses can be calculated from a simple Mohr's circle analysis. The bilinear behaviors of the curves are similar to those for the first joint set. However, with respect to angle  $\theta$ , no obvious trend for the shear stresses is observed. All curves in Figures 8 and 9 exhibit nonlinear behavior. However, in some cases, the observed nonlinearity is due to the interaction of the joints rather than the occurrence of slip nonlinearity. For the first joint set, the shear stress versus joint slip curves are plotted in Figure 10. For  $\theta$  equal to  $30^\circ$  and  $60^\circ$ , slip nonlinearities have occurred. For  $\theta$  equal to  $90^\circ$ , the shear-slip curve remains linear. The opposite is true for joint set 2, as shown in Figure 11. The complex behaviors observed in these figures are the results of the interplays among the imposed initial stress state, the applied shear strain, and the interactions between the two joint sets.

Another way to comprehend the complexities is to examine the loading paths for the two joint sets under the applied shear strain. For  $\theta$  equal to  $30^\circ$ , plots of the shear stress magnitude versus normal stress magnitude are given in Figure 12. The solid curve in Figure 12 represents the Mohr-Coulomb criterion in the stress space. For the first joint set, because of its horizontal orientation, its initial state at point A consists of a normal stress value of 3.45 MPa and zero shear stress. The initial state at A' of the second joint set has both nonzero normal and shear stresses resulting from its  $30^\circ$  orientation. Between points A and B and points A' and B, which correspond to the increase in shear strain from zero, the shear stress for joint set 1 increases while the normal stress decreases. This decrease in normal stress for joint set 1 is due to the interaction between the joint sets because the second joint set takes on more normal stress and less shear stress. The onset of slip nonlinearity for the first joint set occurs at point B and the loading path from B to the end of the applied strain point C follows closely the Mohr-Coulomb criterion. The small deviation is due to the shear hardening as shown in Figure 4. For the second joint set, the stress path reverses its course from B' to C' as a result of the nonlinearity of joint set 1. However, it is clearly seen that the combination of the applied stresses on the second joint set has been below the Mohr-Coulomb criterion throughout the loading process and, consequently, no slip for the second joint set has occurred. Loading path plots for  $\theta$  equal to  $60^\circ$  and  $90^\circ$  are shown, respectively, in Figures 13 and 14. The

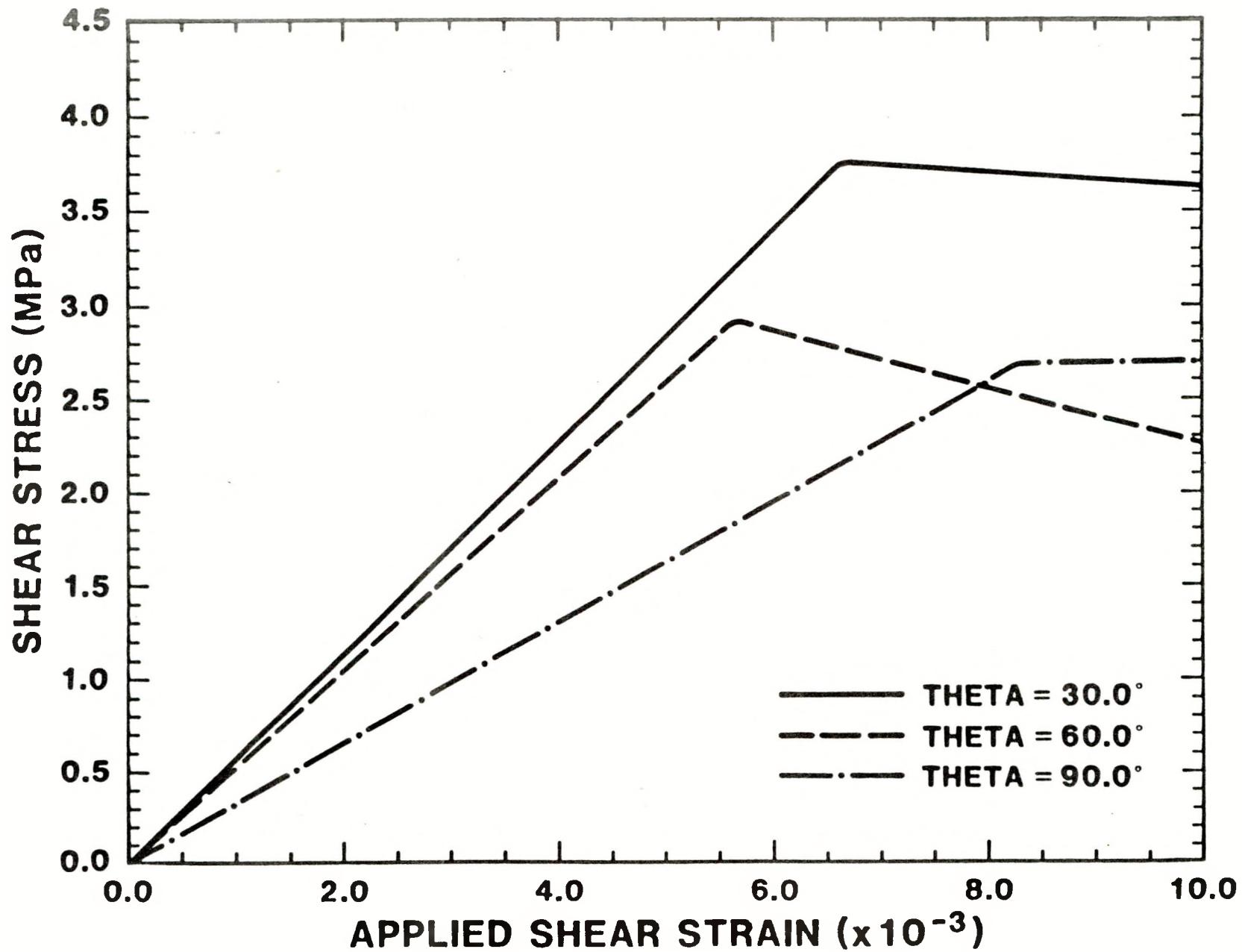


Figure 8. Stress-Strain Behavior for Joint Set 1, Example 2

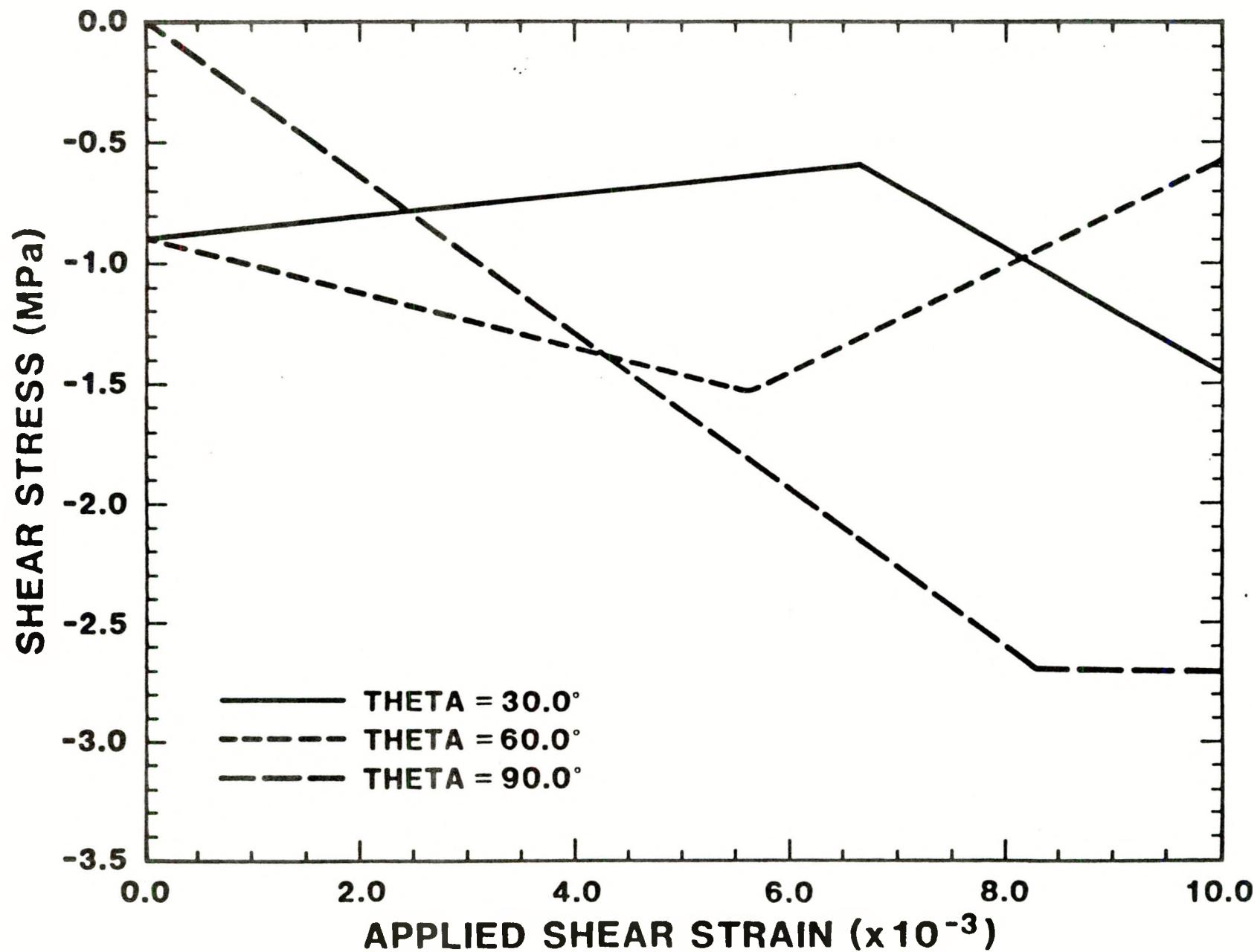


Figure 9. Stress-Strain Behavior for Joint Set 2, Example 2

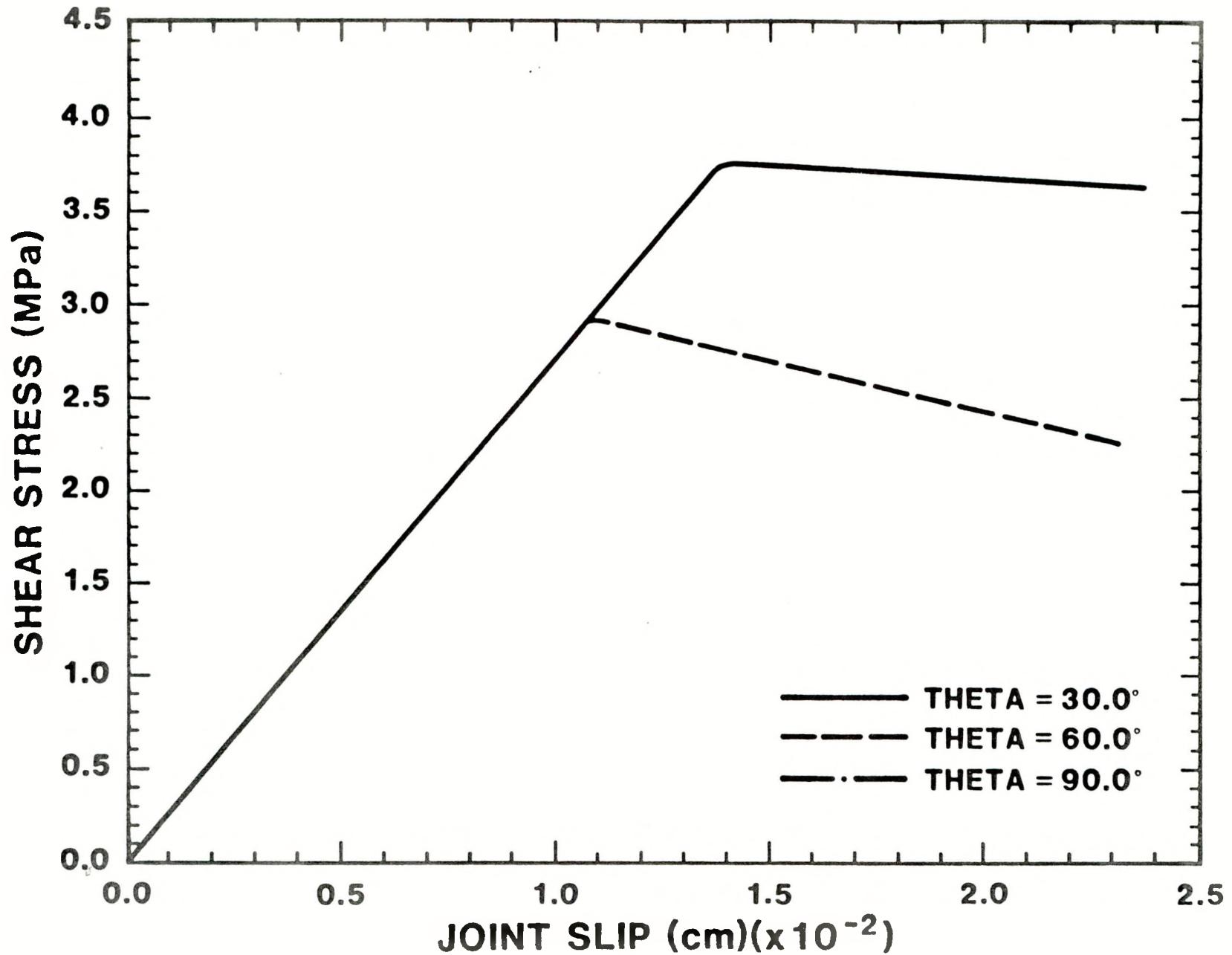


Figure 10. Stress-Slip Behavior for Joint Set 1, Example 2

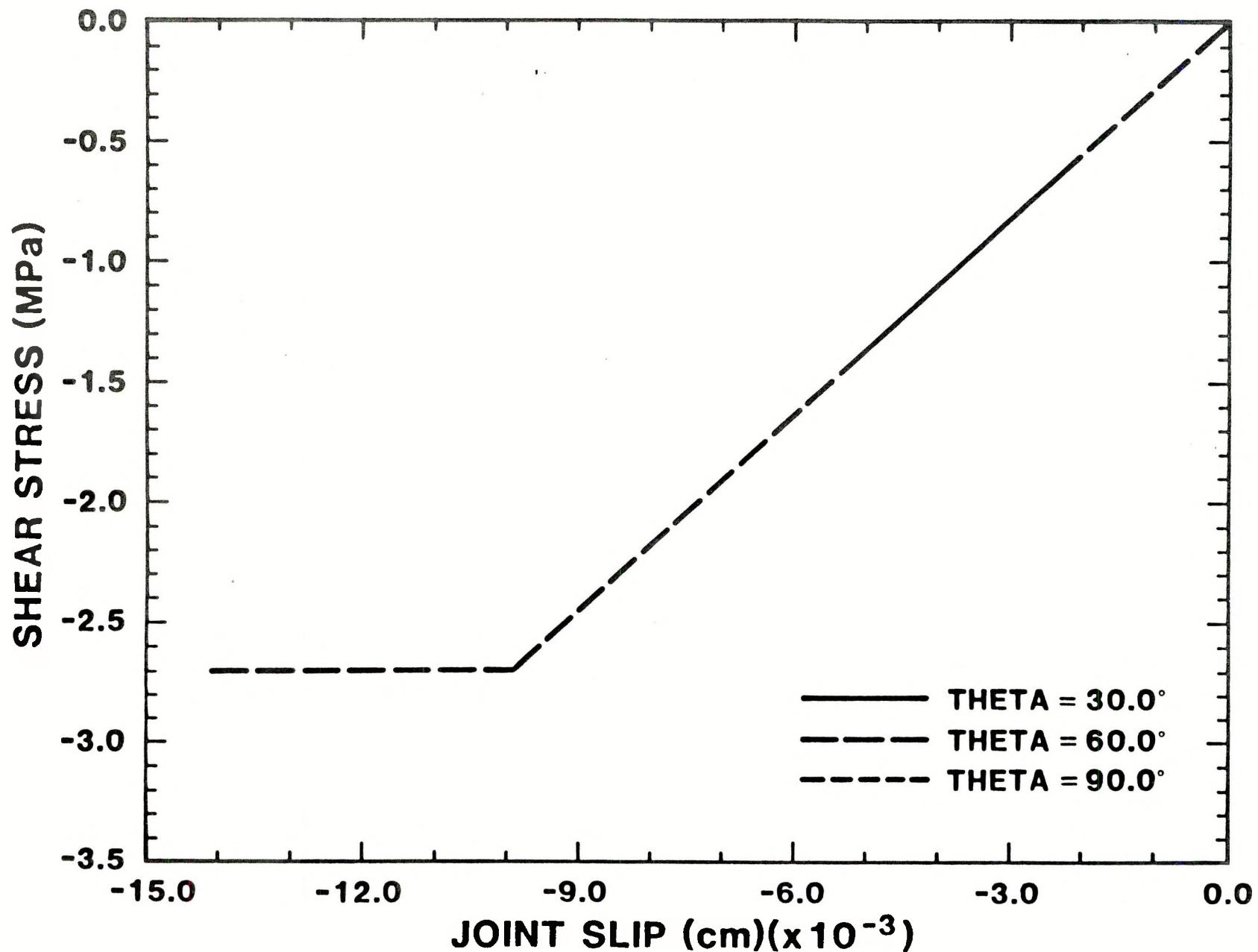


Figure 11. Stress-Slip Behavior for Joint Set 2, Example 2

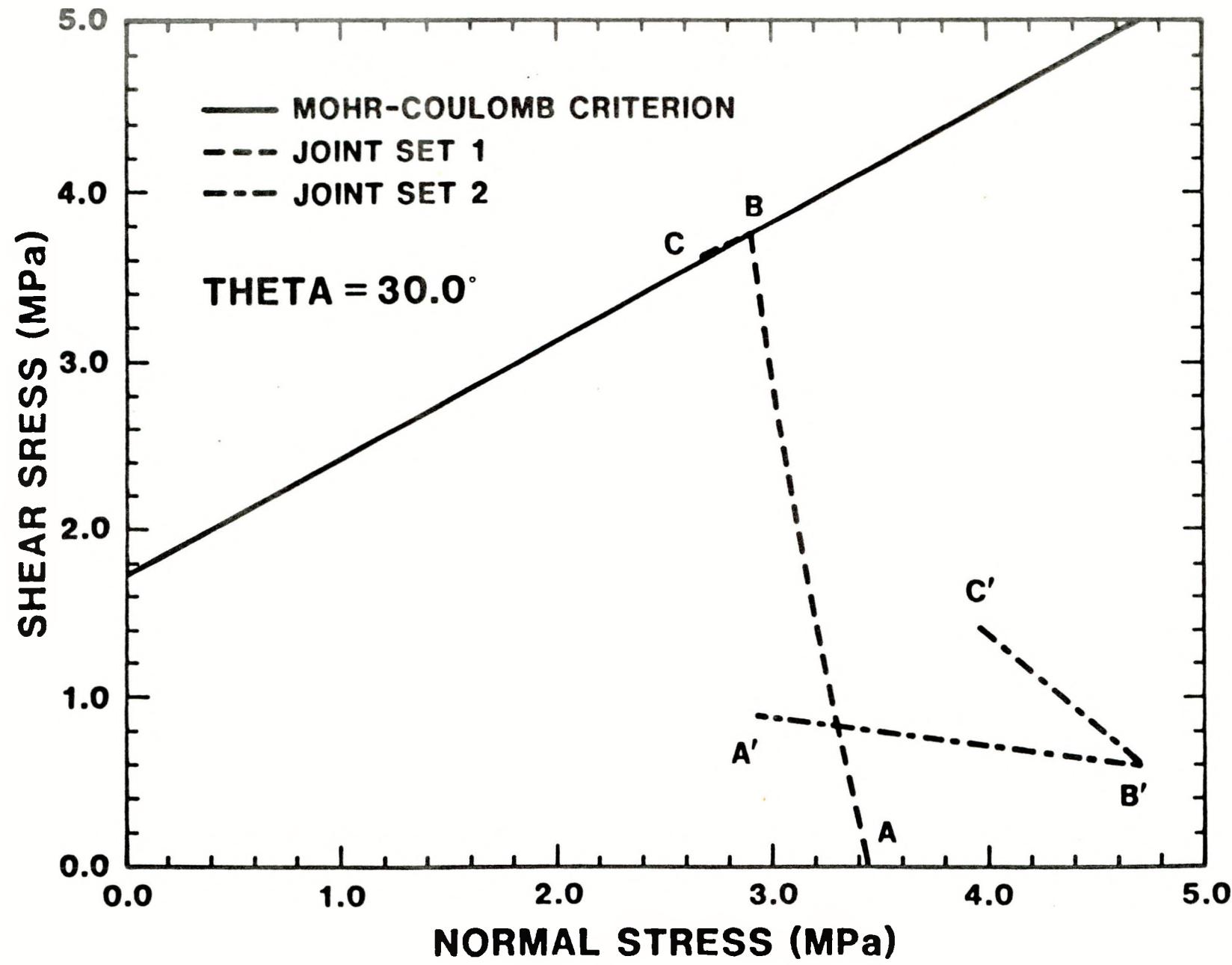


Figure 12. Load Path in Stress Space,  $\theta = 30^\circ$

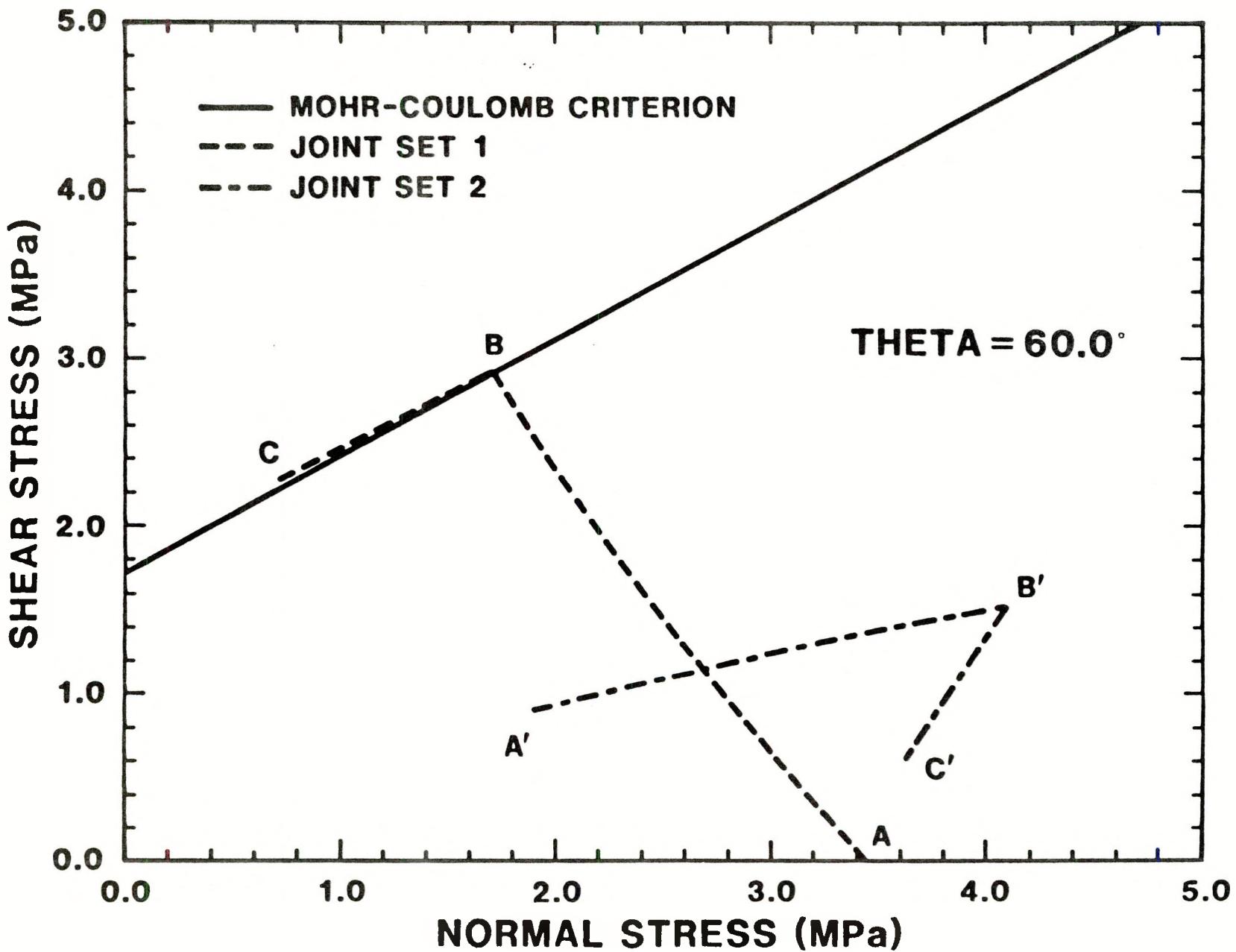


Figure 13. Load Path in Stress Space,  $\theta = 60^\circ$

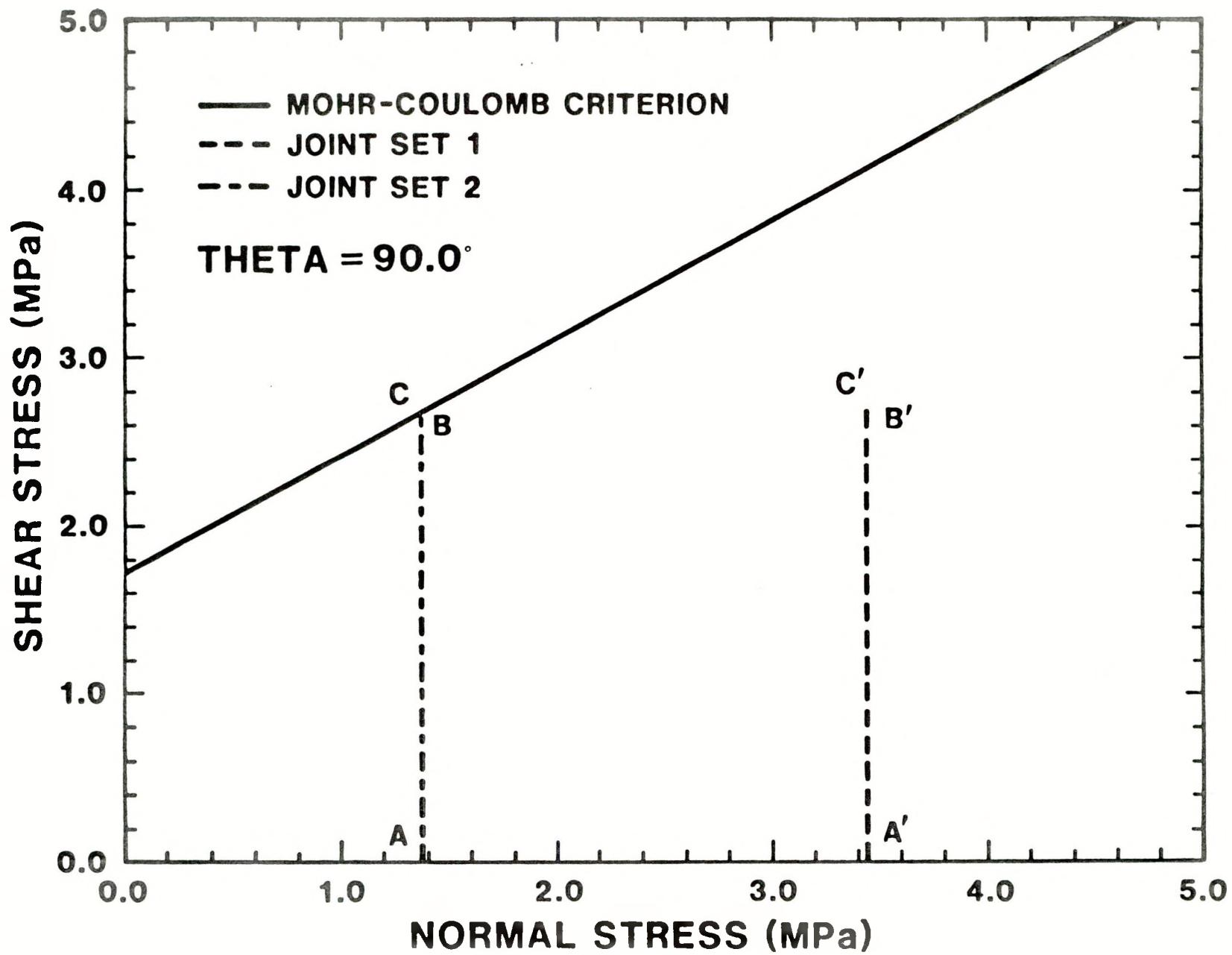


Figure 14. Load Path in Stress Space,  $\theta = 90^\circ$

behavior for  $\theta$  equals  $60^\circ$  is similar to that for  $\theta$  equals  $30^\circ$  in which the first joint set has reached slip nonlinearity while the second joint set remains in the linear range. Because the joint sets are mutually orthogonal, the normal stresses on both joint sets do not change during the straining process for the  $\theta$  equal  $90^\circ$  case. Because the second joint set has a lower normal stress, it reaches slip nonlinearity before the same can be accomplished by the first joint set. After the onset of slip nonlinearity (points B and B'), equilibrium dictates that shear stresses for the two joint sets must be equal. Therefore, throughout the shear straining process, joint set 1 remains in the linear range.

It is interesting to note from Figure 10 that beyond the points of initiation of slip nonlinearity, the shear stresses decrease with increasing joint-slip displacement. This is due to the effect of changing normal stresses. Although no normal strain is applied to the rock mass, the normal stress on the joint sets varies during the entire loading process because of the nonorthogonal joint orientation. As the magnitude of the normal stress decreases, the shear stress magnitude governing the onset of slip nonlinearity calculated from the Mohr-Coulomb criterion decreases. Hence, the softening of the shear stress-slip displacement curve is observed. For  $\theta$  equal to  $60^\circ$ , this effect of the changing normal stress on the shear curve is shown in Figure 15.

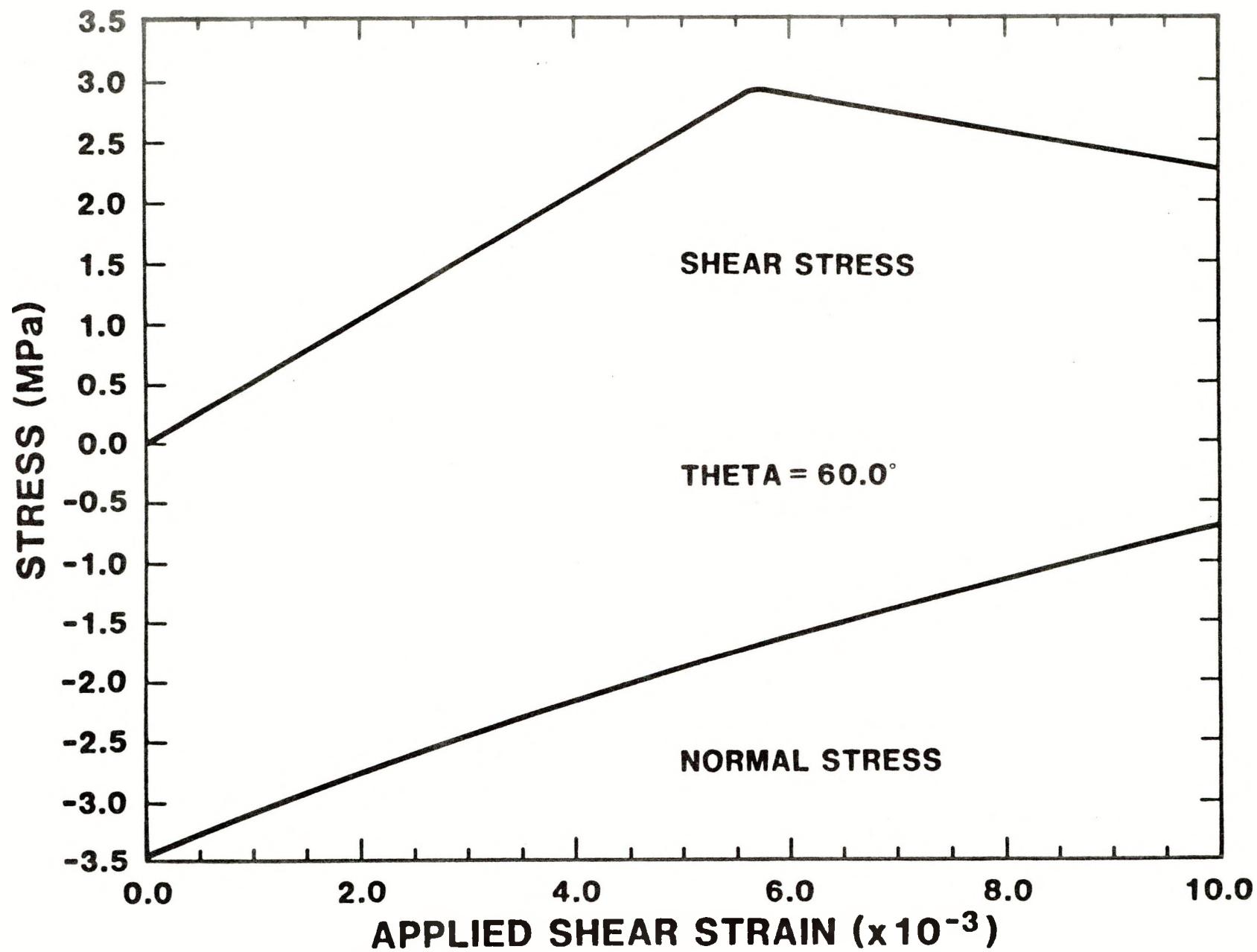


Figure 15. Stress-Strain Behavior for Joint Set 1,  $\theta = 60^\circ$

#### 4. Summary

A general constitutive model that describes the response of jointed rock mass with nonorthogonal sets of joints has been developed. Rate equations that govern the solution process have been presented, and a driver program for the constitutive model has been written and used to solve example problems. Results from these examples show complex interactions resulting from the nonorthogonal orientation of the joint sets.

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