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# CONFIRMATION using a Fast-neutron Imaging Detector with Anti-image NULL-positive Time Encoding (CONFIDANTE)

Peter Marleau

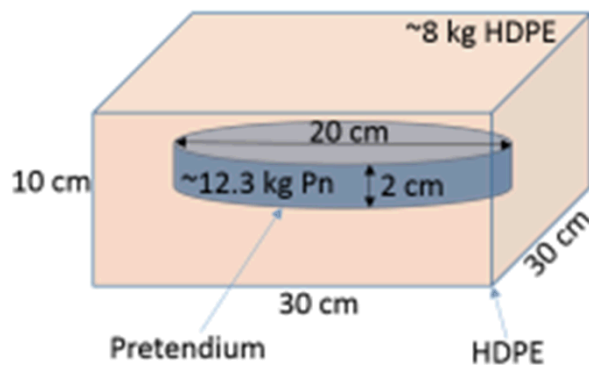
Rebecca Krentz-Wee (NSSC graduate student)

# Outline

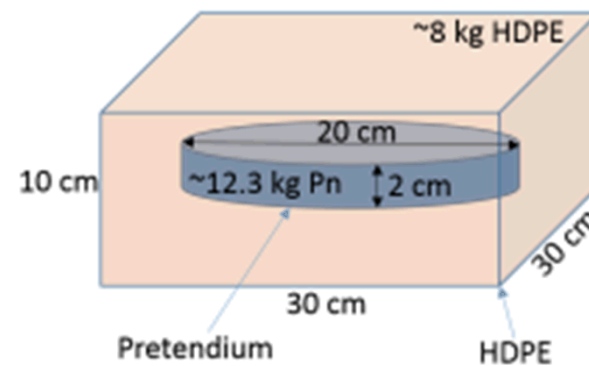
- Workshop on Techniques for Information Protection of Imaging Information
- Challenge problem
- Template-based CONOPS
- Zero Knowledge – what does it buy you?
- Comparison Measurements – a new CONOPS?
- Two-dimensional time-encoded imaging
- CONFirmation using a Fast-neutron Imaging Detector with Anti-image NULL-positive Time Encoding (CONFIDANTE)
- Preliminary results!

# Challenge problem

- The inspecting party has or had access to measure item T, which is known to be a valid type 1 treaty accountable TAI through some other mechanism.
- In the course of an inspection, the host presents item X and declares it as a type 1 TAI
- Item X should pass the verification measurement if it is a type 1 TAI, and fail if it is significantly different.



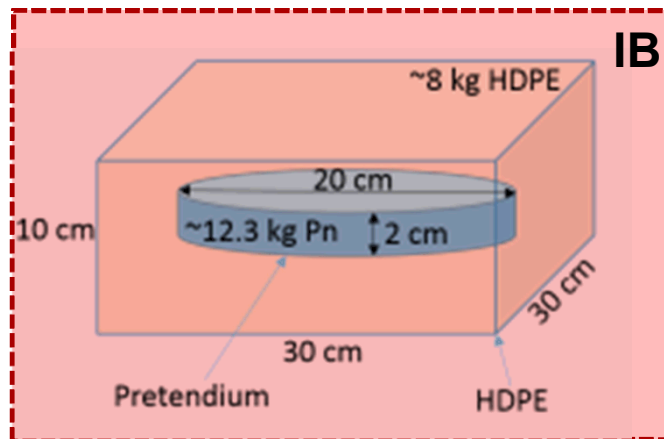
**Object T = valid  
type 1 TAI**



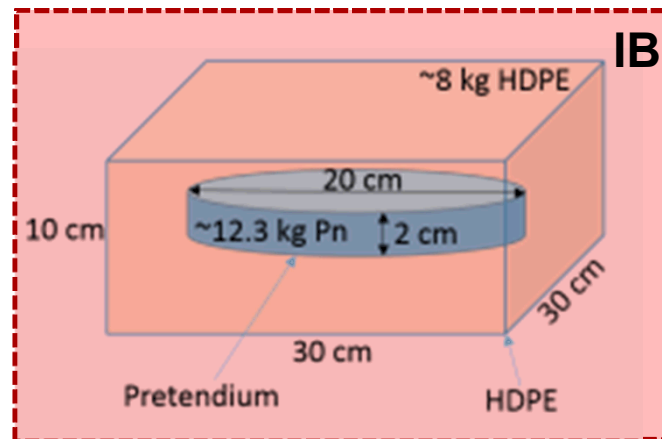
**Object X = ?**

# Challenge problem

- The host must be confident that the inspector has not learned the diameter  $d$  of the pretendium in item X, or any type 1 TAI



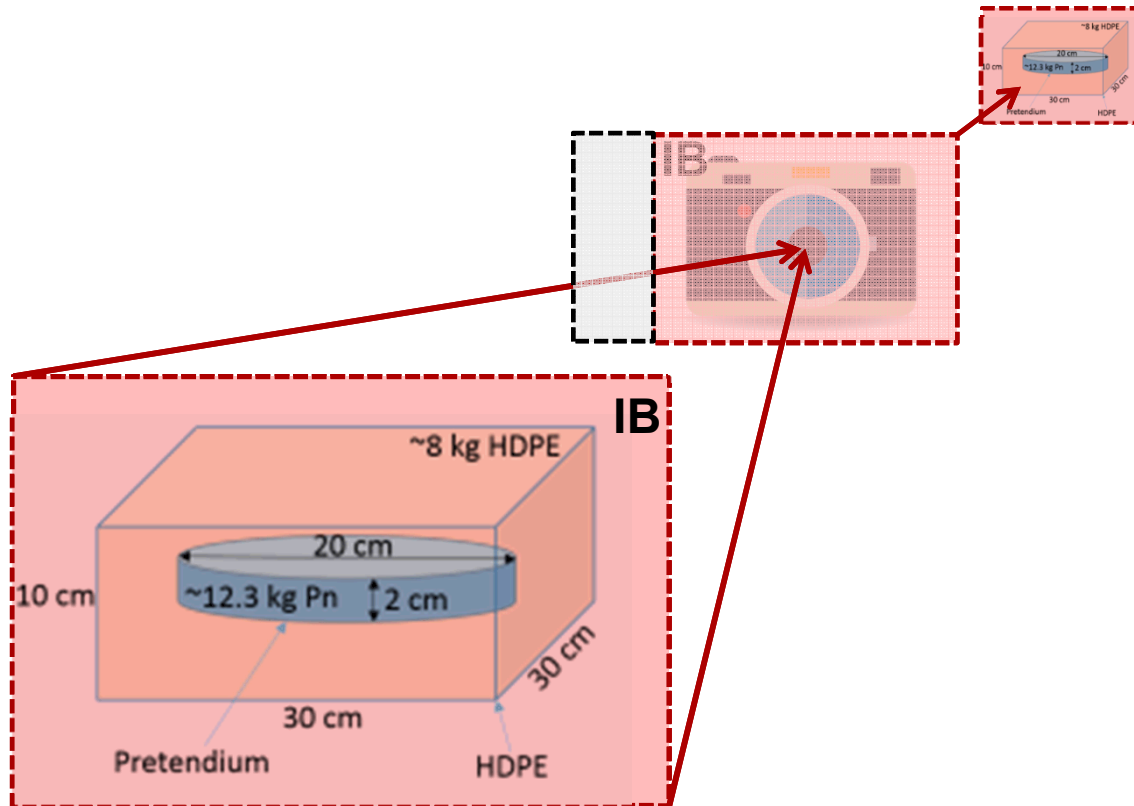
**Object T = valid  
type 1 TAI**



**Object X = ?**

# Templates - generation

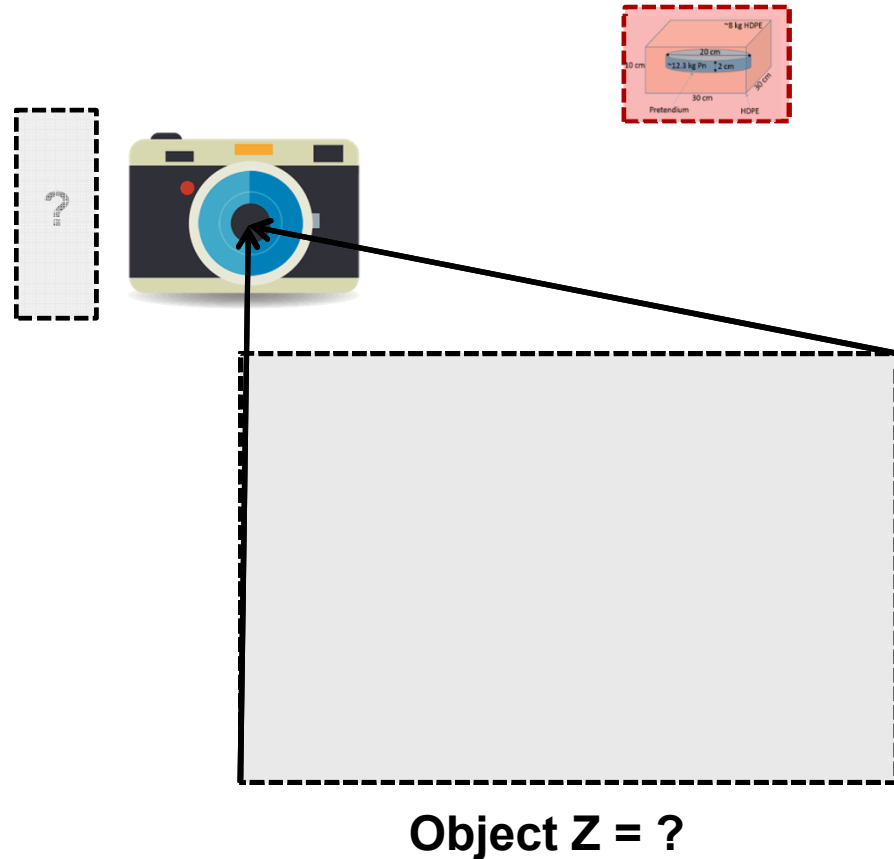
- We could generate a template behind an information barrier (IB) ...



**Object T = valid  
type 1 TAI**

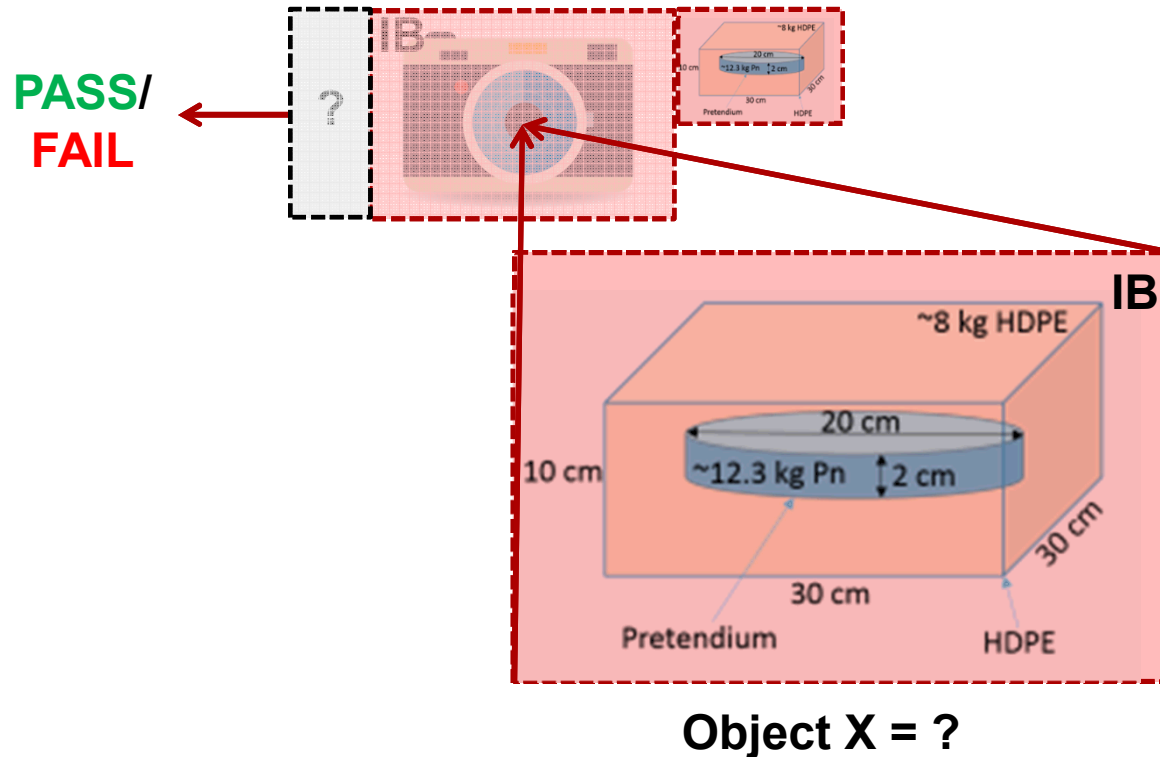
# Templates - authentication

- Sequester sensitive information
- Authenticate equipment ...



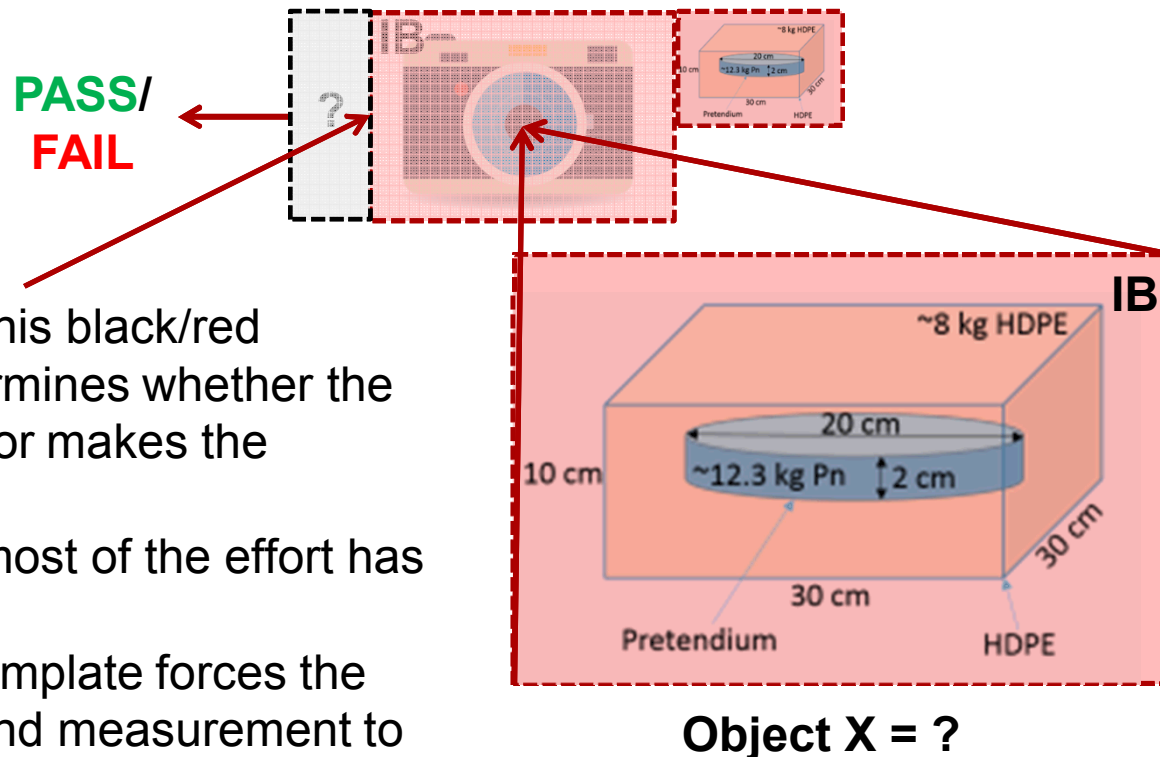
# Templates - comparison

- Make comparison measurement...



# Templates – who measures?

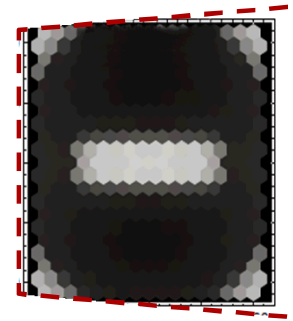
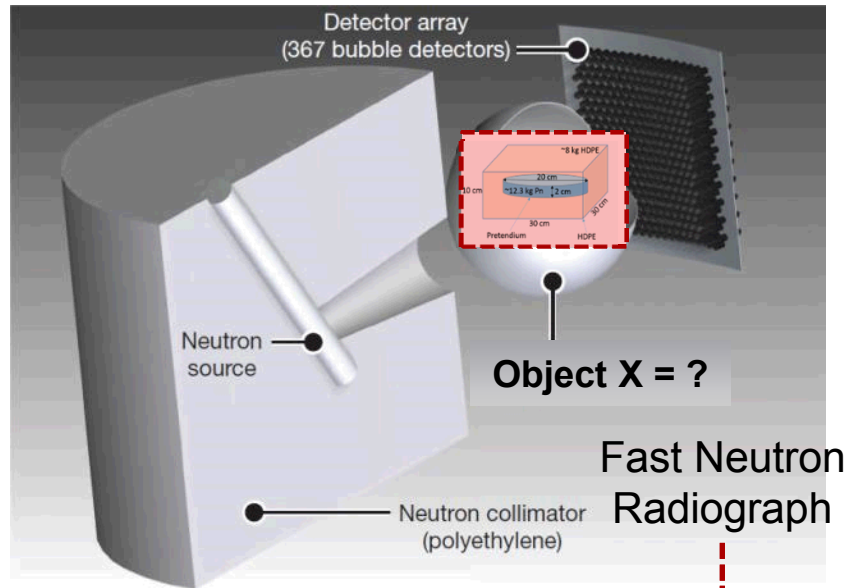
- Who makes the measurement? Is the measurement itself authenticatable?



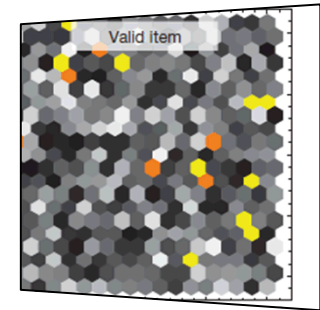
- The nature of this black/red boundary determines whether the host or inspector makes the measurement.
- This is where most of the effort has gone.
- At worst, the template forces the entire device and measurement to be behind an IB.



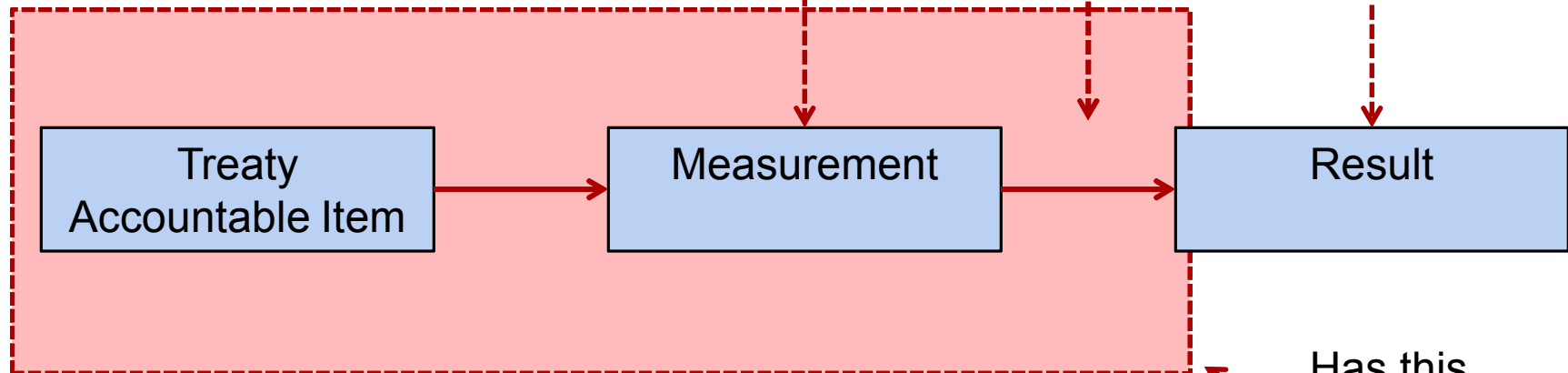
# ZKP – Princeton edition



Analog bubble detectors with preloaded complement "template"



Flat featured image (NULL) is a true positive.

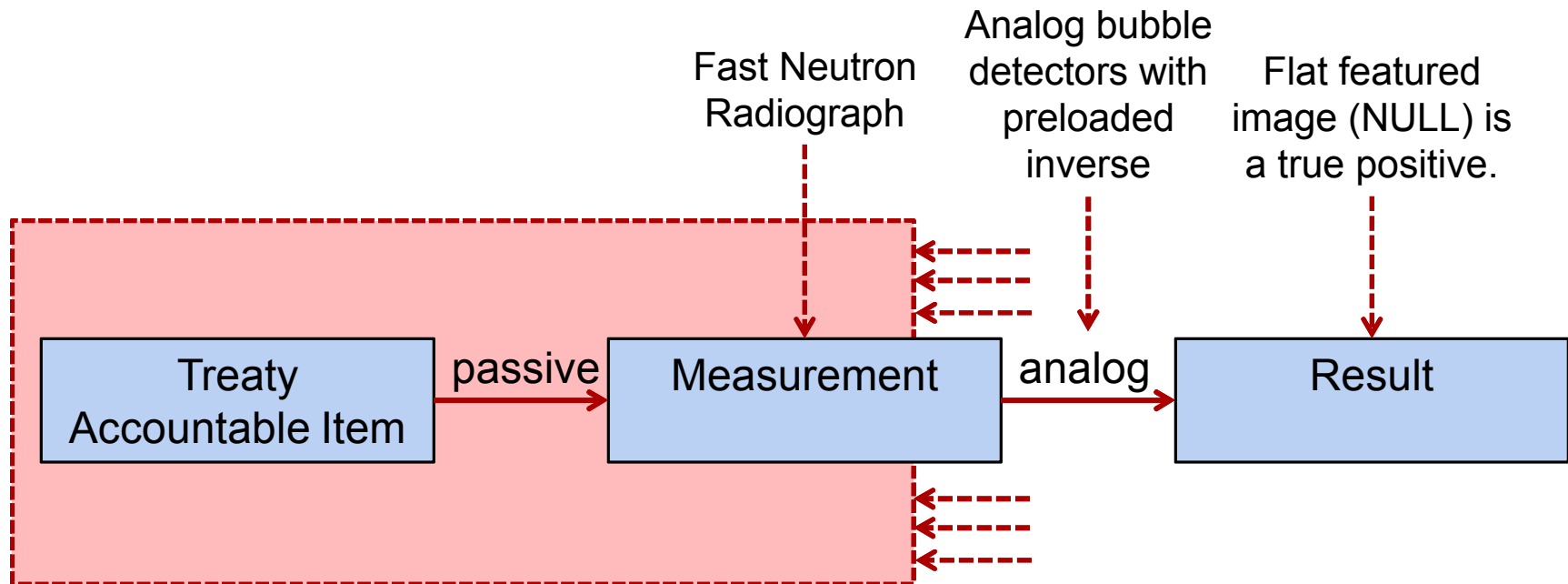


Has this boundary moved?

# ZKP – authentication measures

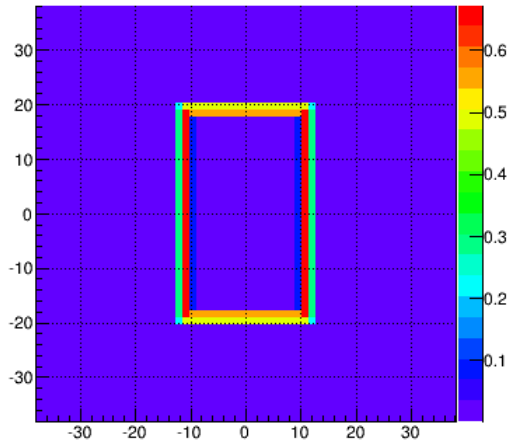
## Research Questions

- Can we share the rates in a subset (up to all) of the detector pixel counts with spatial information removed before/during/after the measurement?
- **What sensitive information is at risk?**

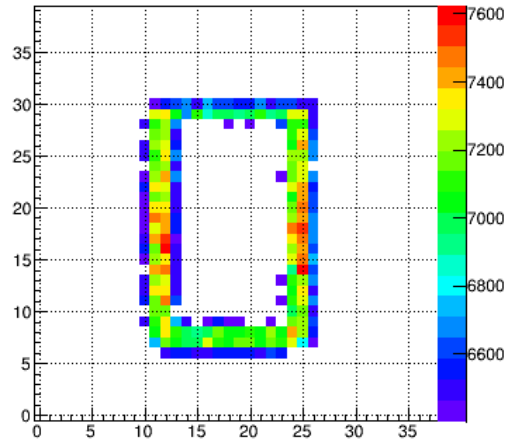


# Test case - Simulated Rectangular Source (1e7 counts)

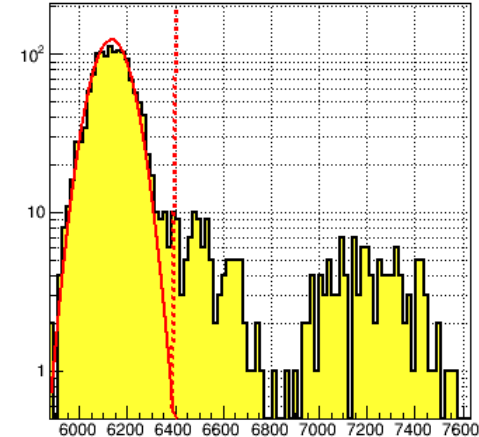
Input distribution



Projected Image



Pixel Count Distribution

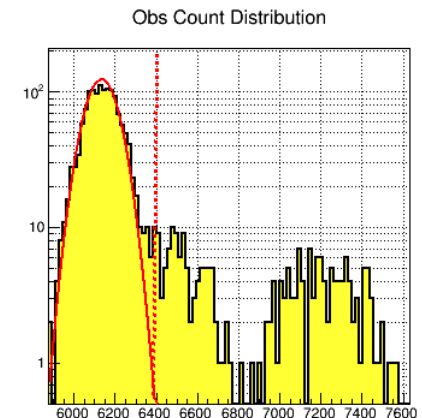
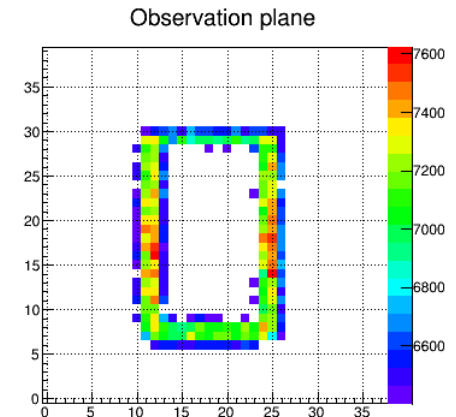


- A passive pinhole imager test case was simulated.
- A Gaussian with sigma equal to its mean is shown - the background counts seem to match statistical fluctuations in the pixel count distribution.
- It can be seen that all counts to the right of 6400 ( $\sim 3.4$  sigma) originate from a pixel within the rectangular source.
- $8.57e6$  counts represented in Gaussian.  $1.43e6$  counts in source.

# Rectangular Source Counts

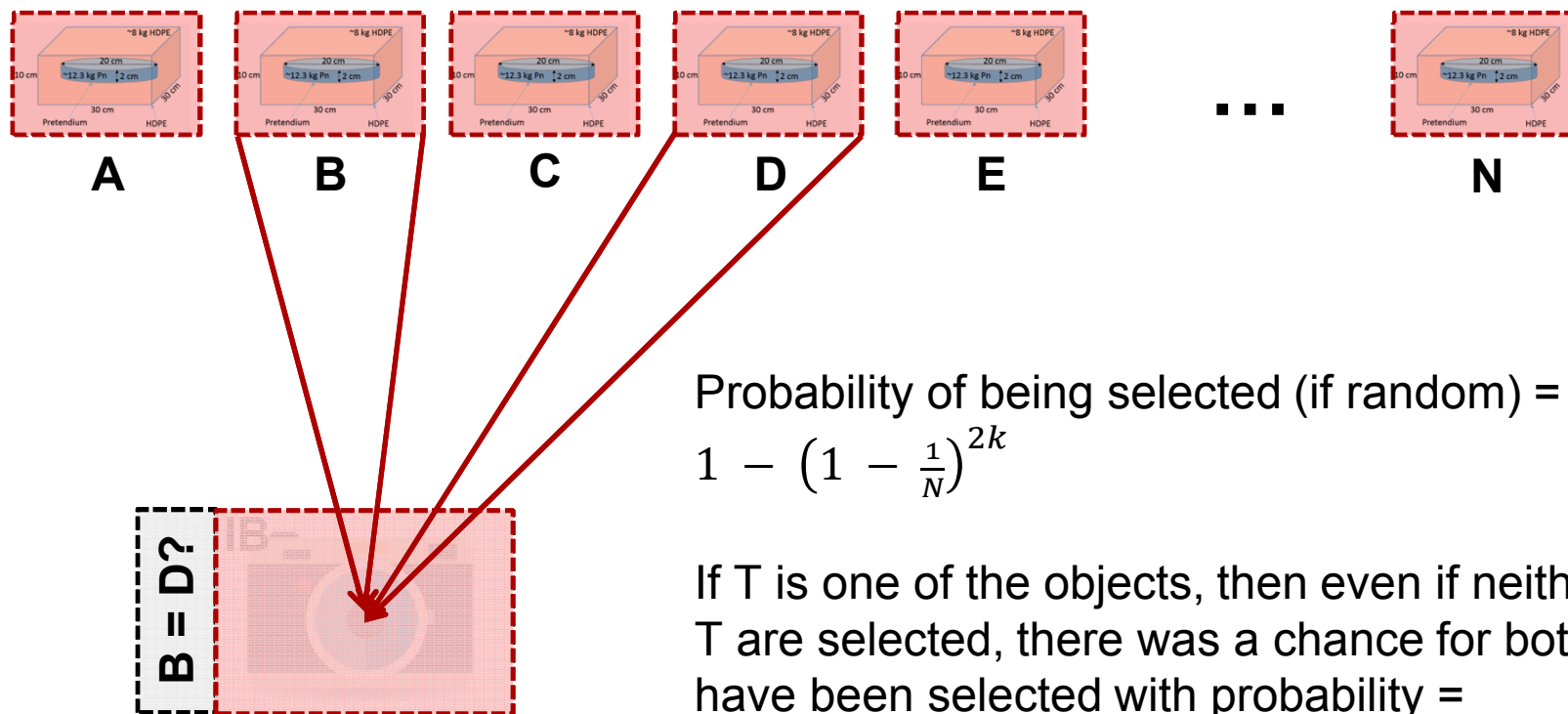
- $8.57\text{e}6$  counts represented in Gaussian.
- $1.43\text{e}6$  counts in source.
- The mask is not opaque, so the source is also the primary contribution to the “background” counts.
- Knowledge of mask opacity and mean counts therefore provides **source activity**.
- There are 230 pixels to the right of the threshold. Therefore these excess source counts are distributed across an object of this **total angular size**.
- What else can we learn? What can the shape of the distribution tell us? Have we gone far enough?

→ *Classified Study*



# ZKP – CONOPS and Inspector choice

- The ZKP CONOPS offers an interesting way to gain confidence.
- Presented with N objects and k comparison measurements will be made.



Probability of being selected (if random) =  
 $1 - \left(1 - \frac{1}{N}\right)^{2k}$

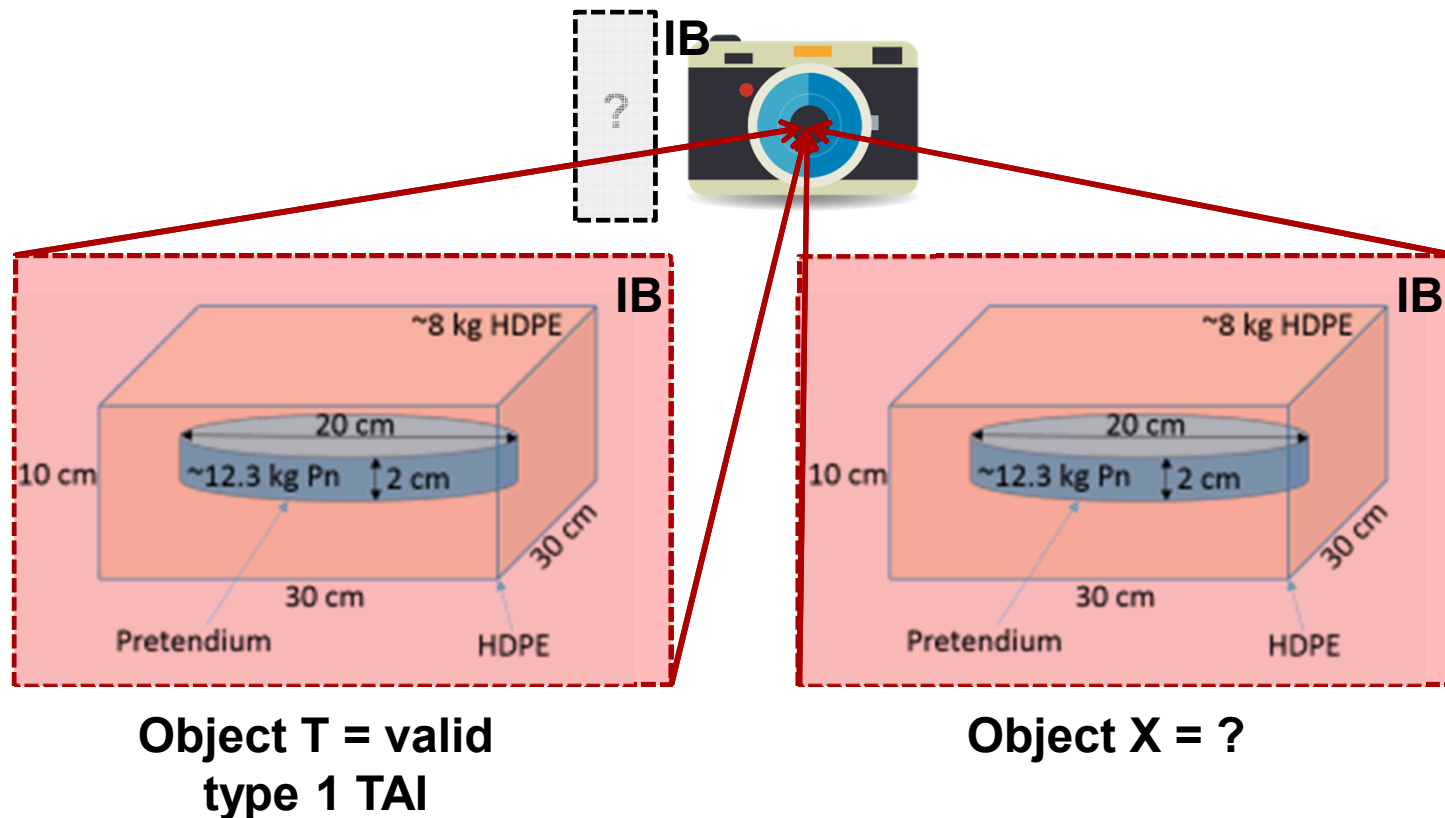
If T is one of the objects, then even if neither X nor T are selected, there was a chance for both to have been selected with probability =

$$\left(1 - \left(1 - \frac{1}{N}\right)^{2k}\right)^2$$

providing some degree of confidence

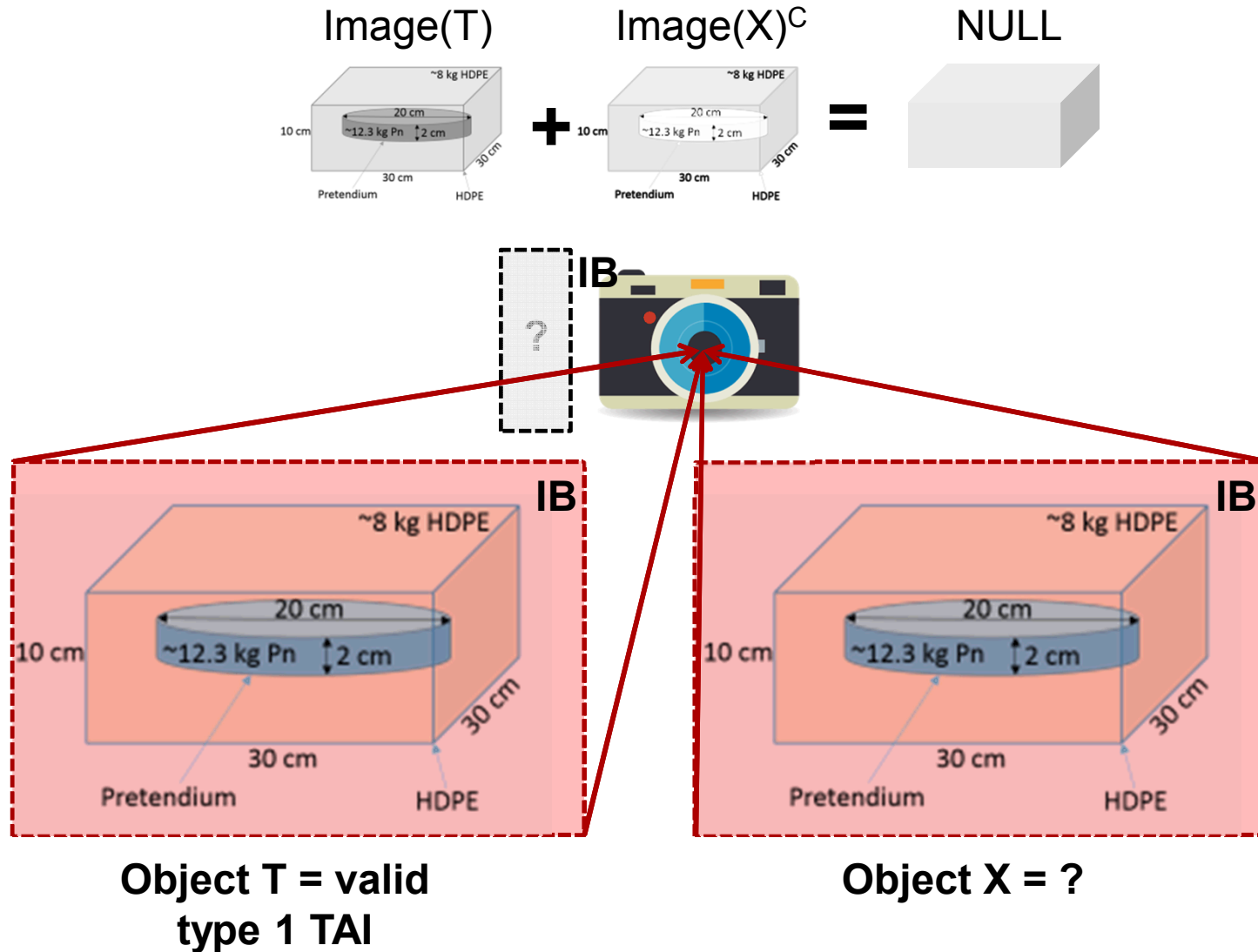
# Zero Knowledge comparison measurement?

- Is there a physical implementation of the confirmation measurement that the inspector can watch and authenticate?
- **It would be great if we could get a physical NULL as an indication of positive confirmation at all times, even during the measurement.**



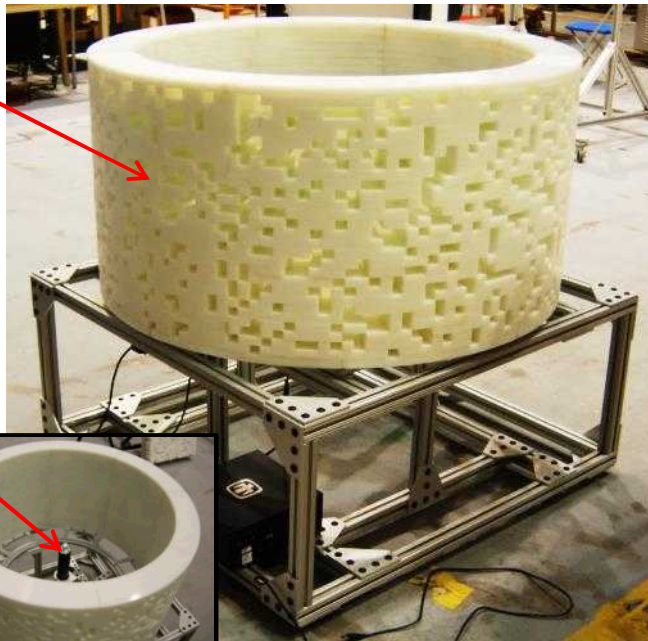
# Proposal – complementary comparison

- What we need is to turn one image into its complement ***at all times***.

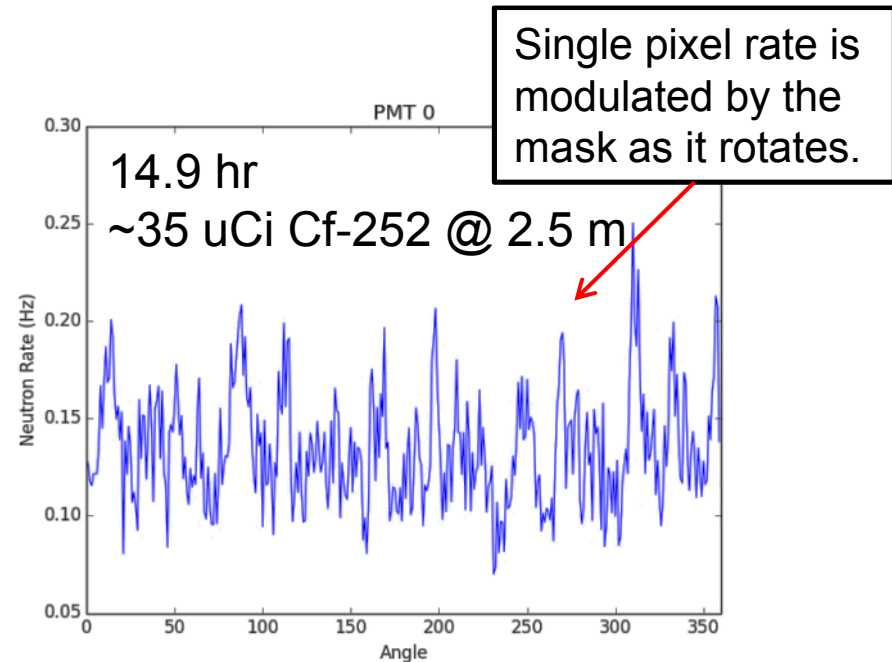


# 2D Time-encoded Imaging (TEI)

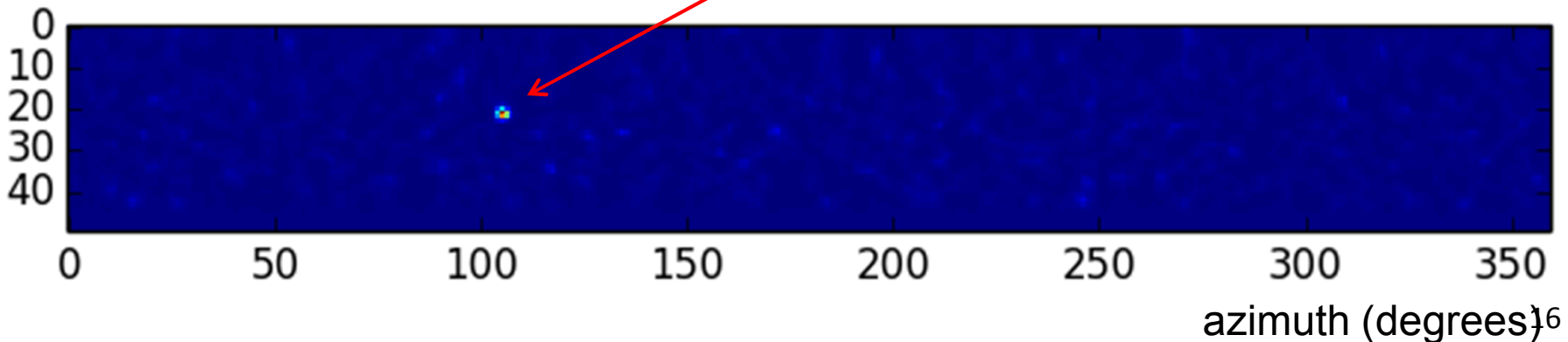
2-d  
coded  
mask



Single  
1"D x 1"  
LS pixel



Arb. Bin idx in [-1 m, 1 m]

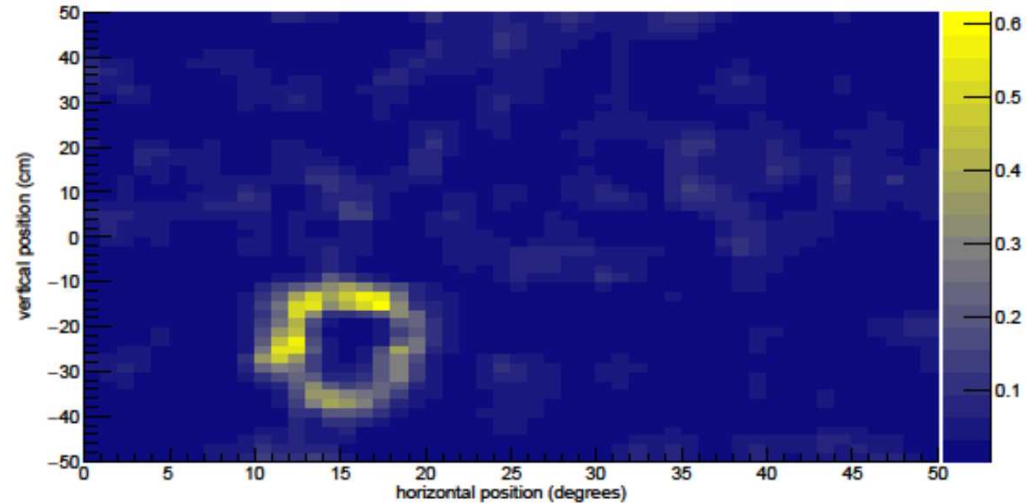




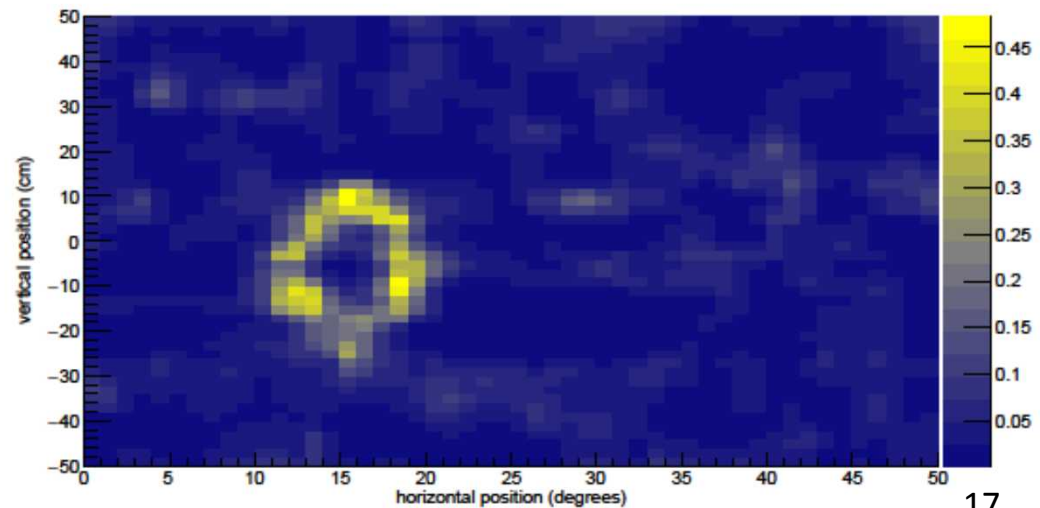
# TEI-2D imaging – extended sources

A single  $1.4 \times 10^5$  n/s  $^{252}\text{Cf}$  source move through an extended pattern at 2 m.

72 hours  
(100 mlem iterations)

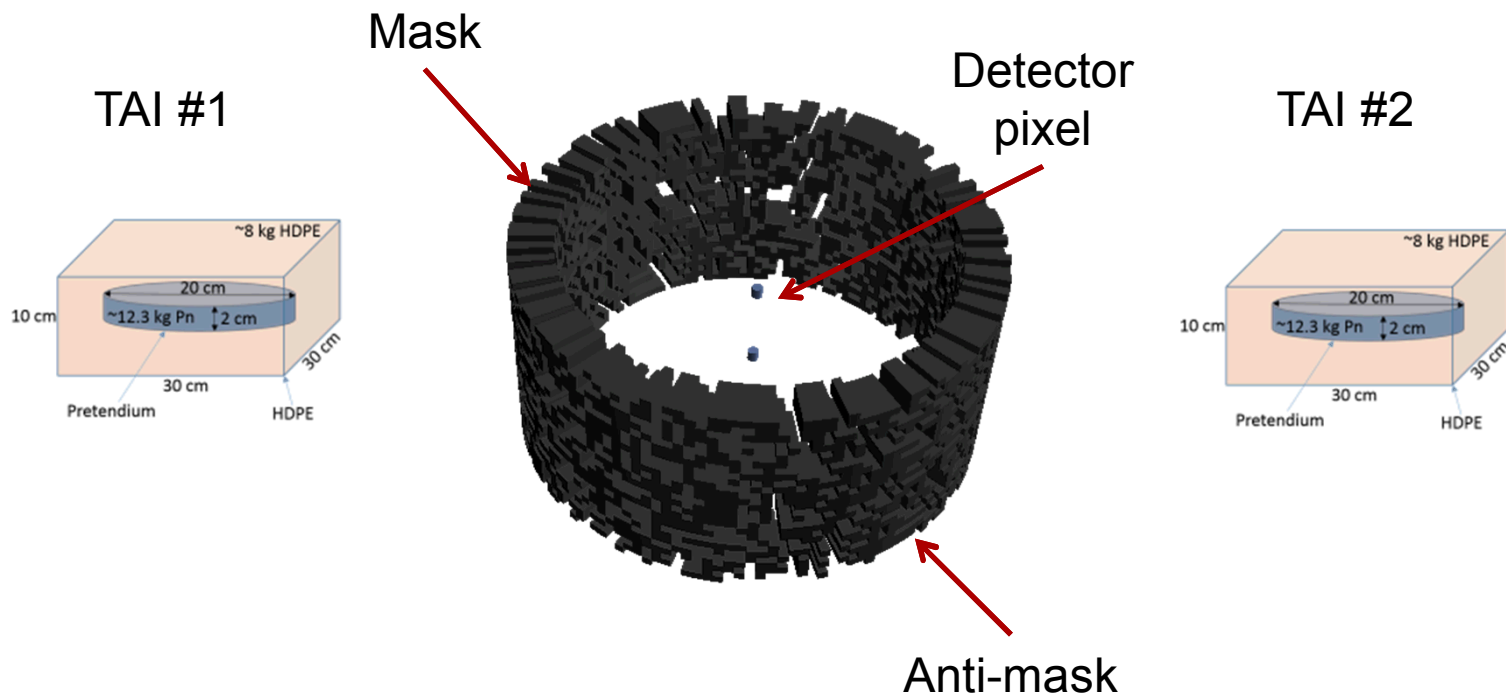


94 hours  
(100 mlem iterations)

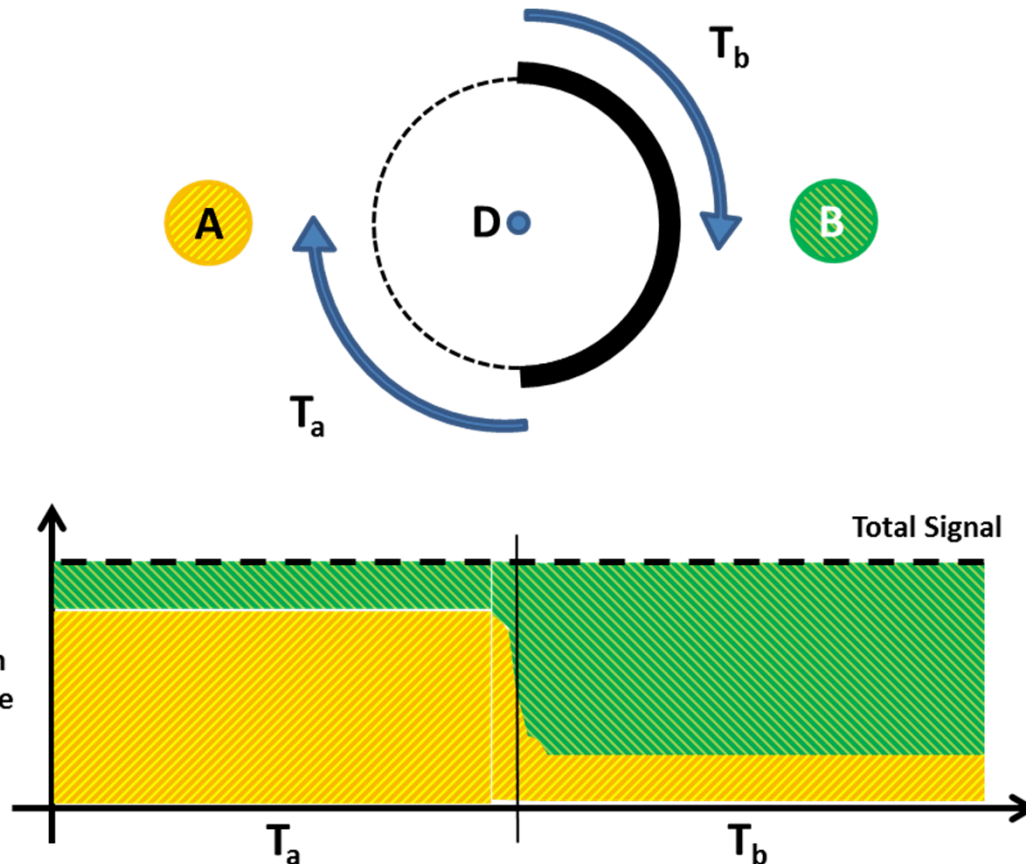


# Here's where the magic happens ...

If the mask is designed such that one side is the anti-mask of the other,  
then **TAI #2 projects the anti-image of TAI #1 at all times**  
**if and only if they are identical!**

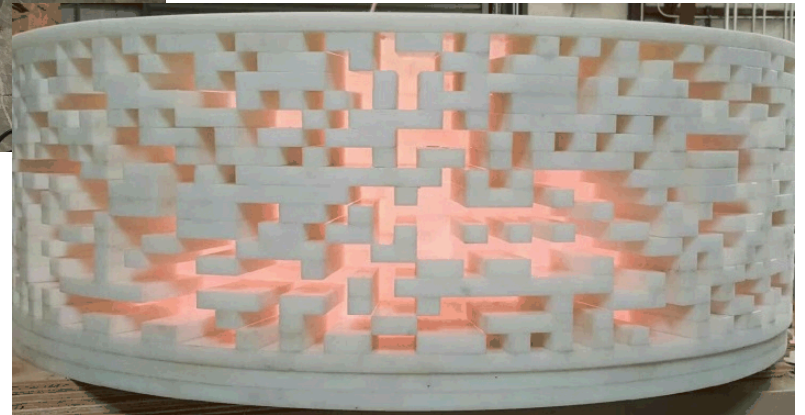


# A very simple example



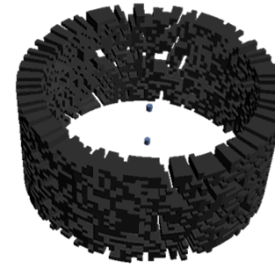
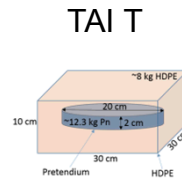
- For example, take a very simple mask: half mask, half aperture.
- The fraction of total count rate coming from  $A$  and  $B$  is unknown at any given angle.
- In this example, the location (and shape) of the boundary between regions is not revealed.

# We've made one!

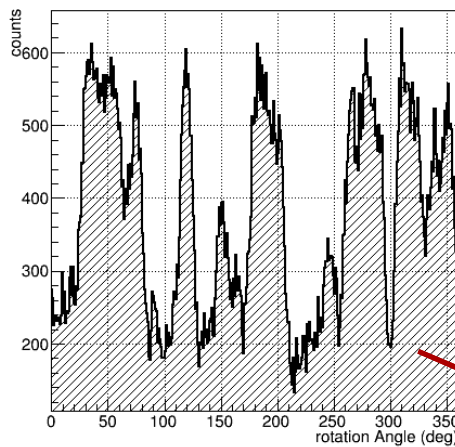


# Modeling results - Single type 1 TAI (2.5e5 counts)

Measurement of single TAI demonstrates that the instrument is sensitive to the 2D distribution of material.

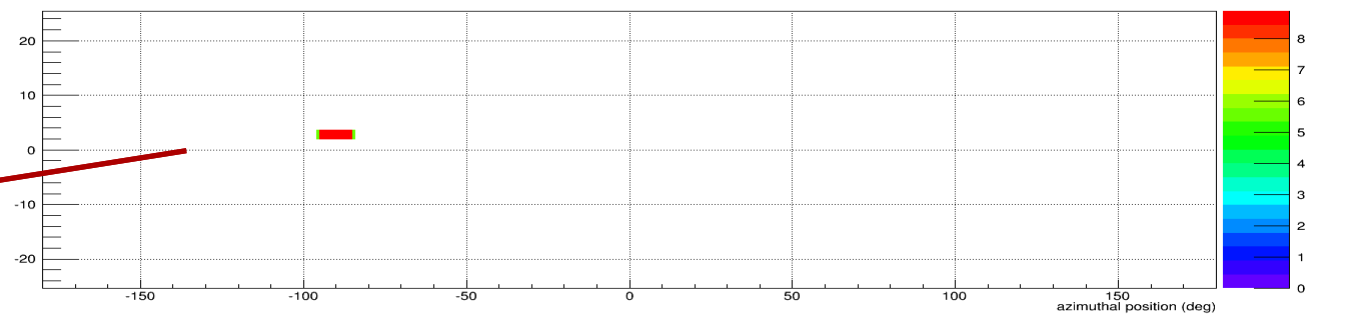


Pixel Counts

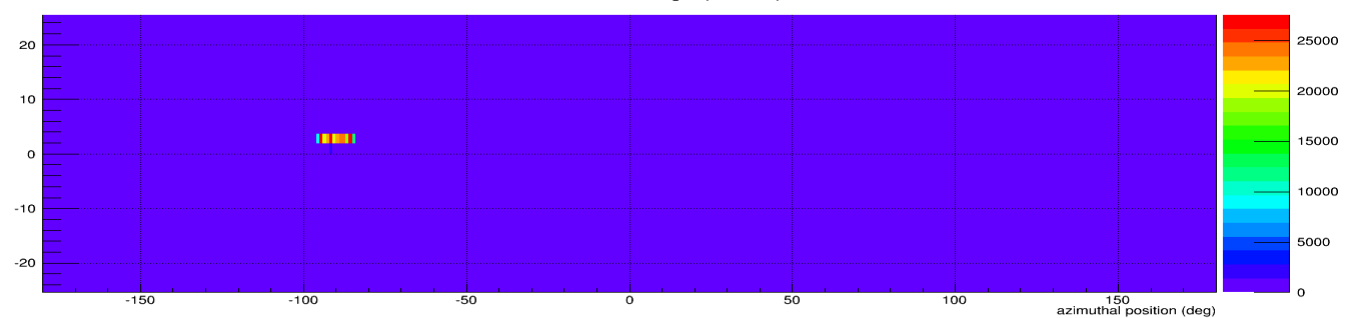


vertical position (cm)

Iso-Background plus Source



Reconstructed Image (MLEM)



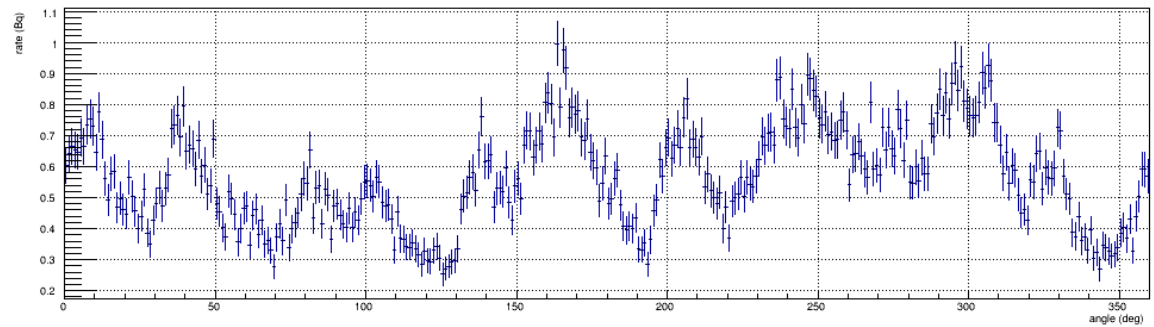


# Preliminary results – Single point source

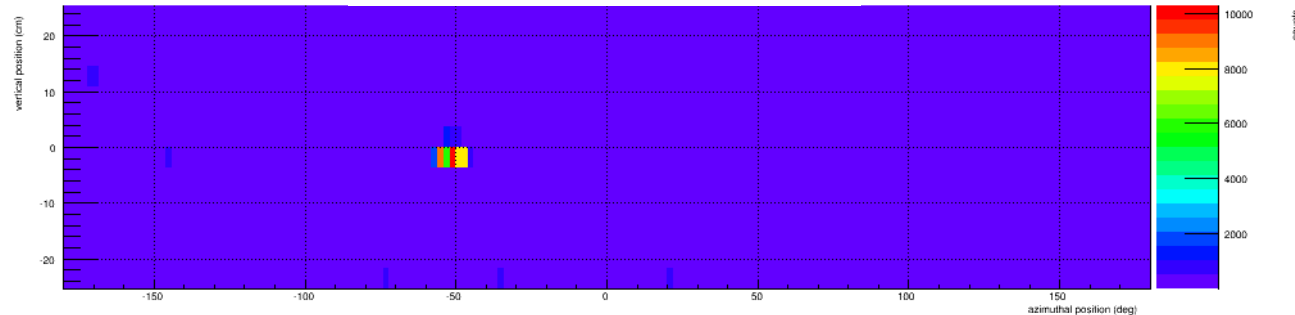
Measurement of a  
single point source



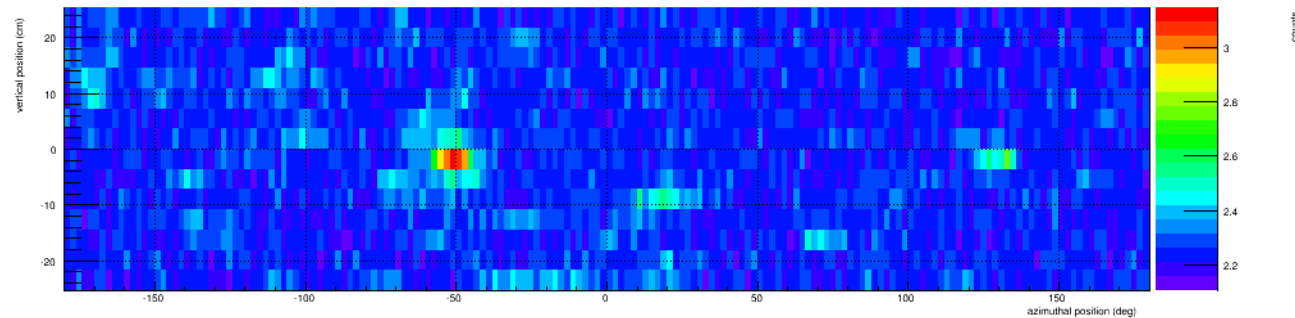
Neutron Rate



MLEM Reconstruction



Relative Variance

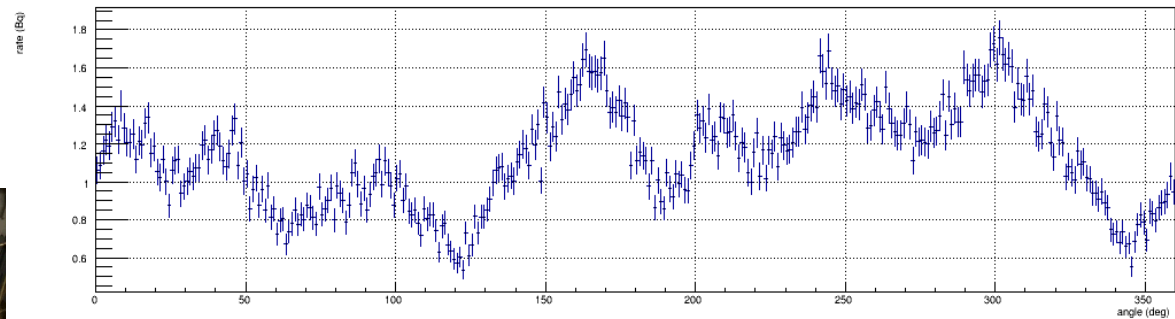


# Preliminary results – Single point source pair

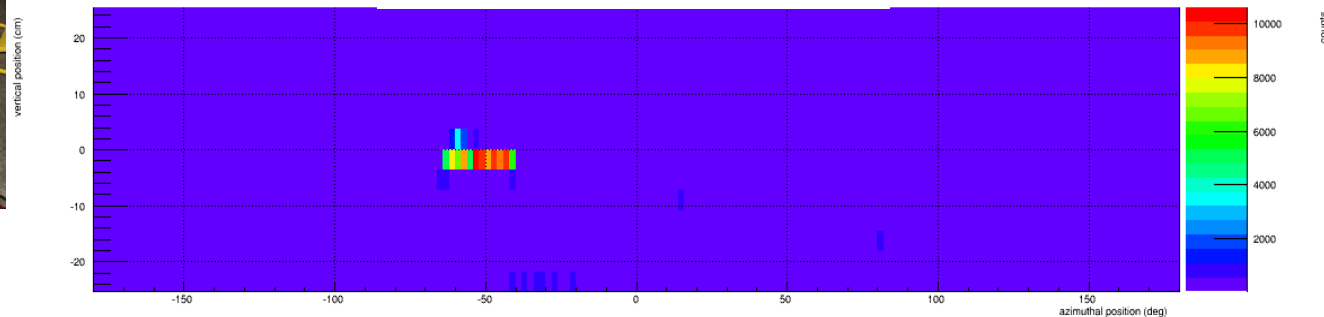
Measurement of a  
two point sources  
separated by 19 cm



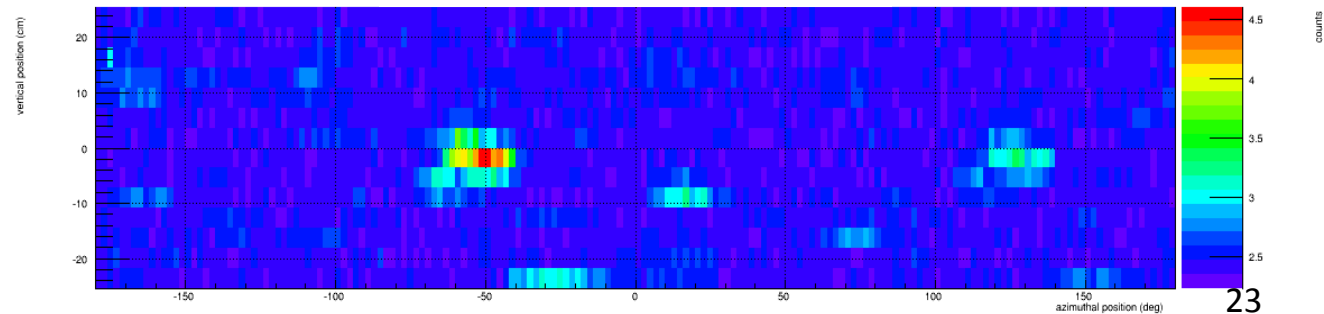
## Neutron Rate



## MLEM Reconstruction

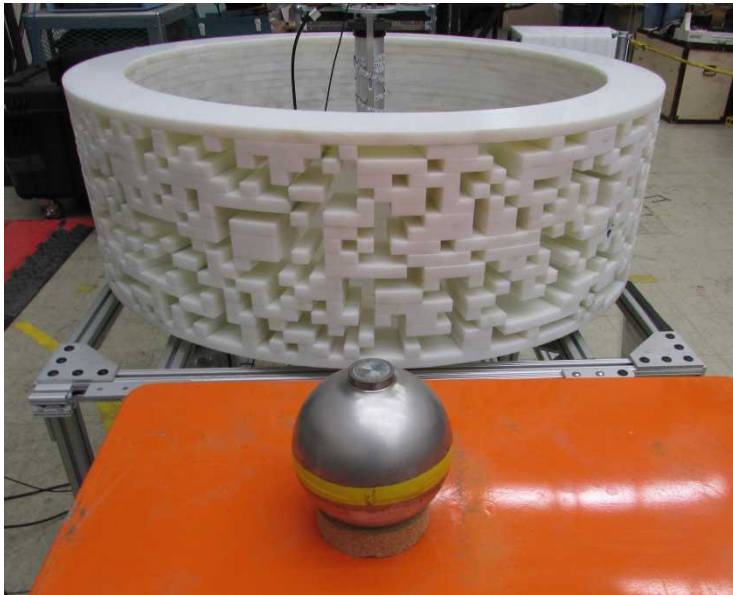


## Relative Variance

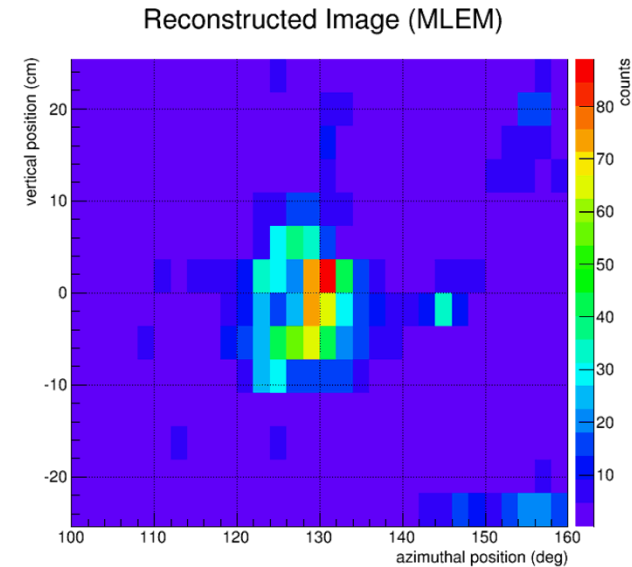


# Preliminary results – LLNL's w/g PU Hemis

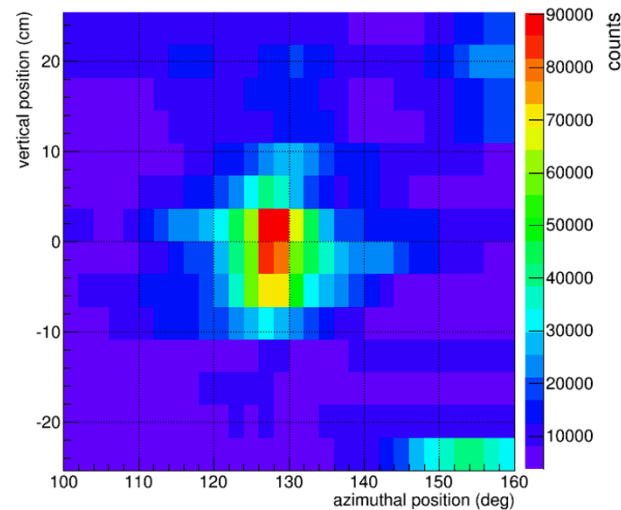
Measurement of a  
weapons-grade  
Plutonium Oxide  
Sphere at LLNL.



Neutron Image



Reconstructed Image (MLEM)

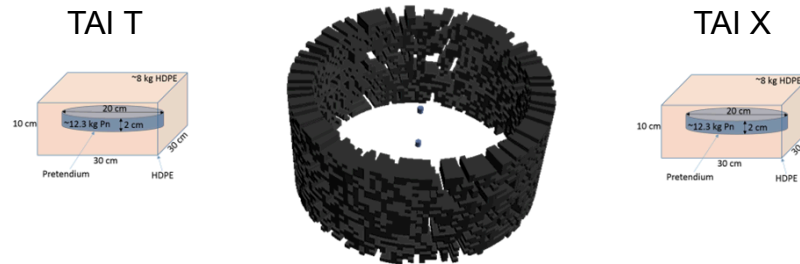


Gamma-ray Image

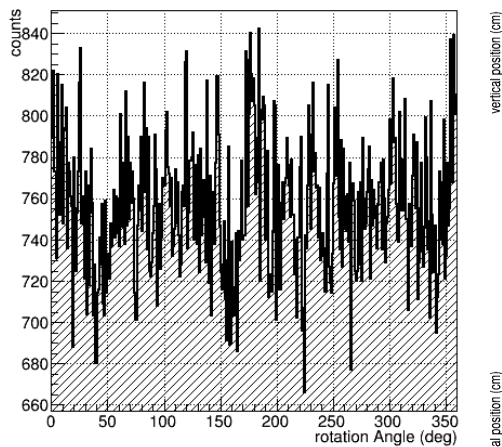


# Modeling results – T vs. X (5e5 counts)

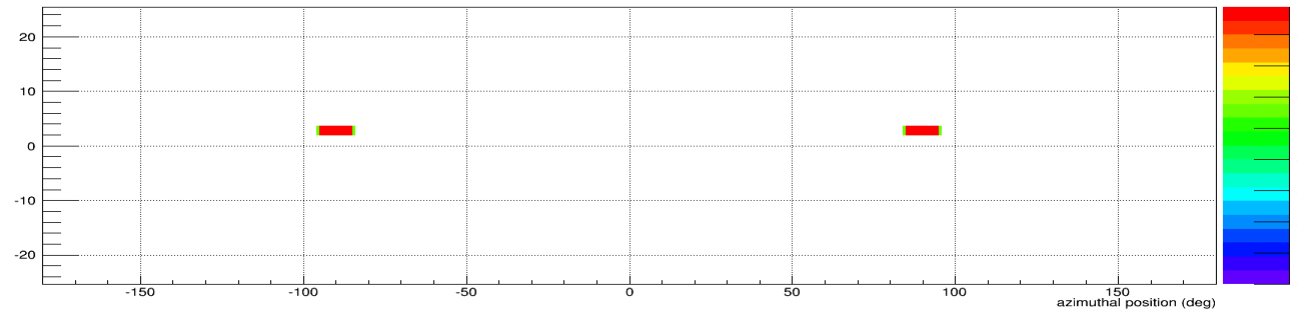
True “null”-positive  
confirmation comparison  
measurement between  
two type 1 TAIs.



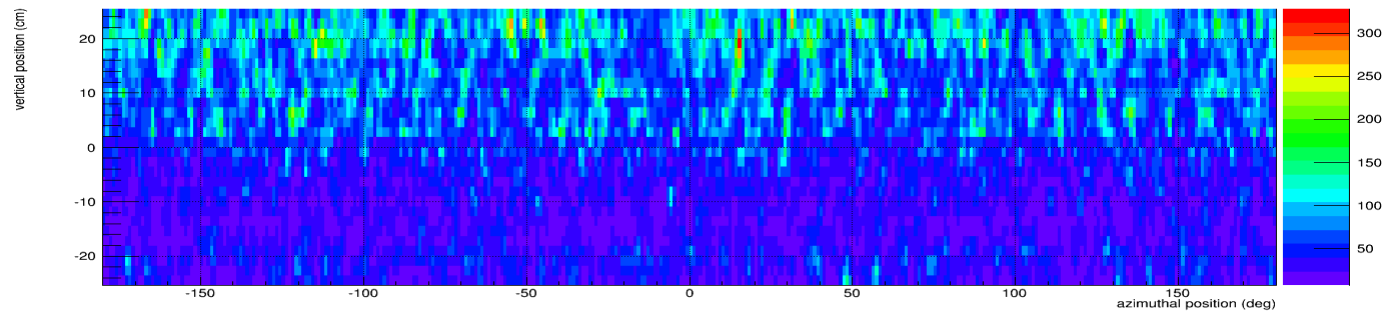
Pixel Counts



Iso-Background plus Source



Reconstructed Image (MLEM)

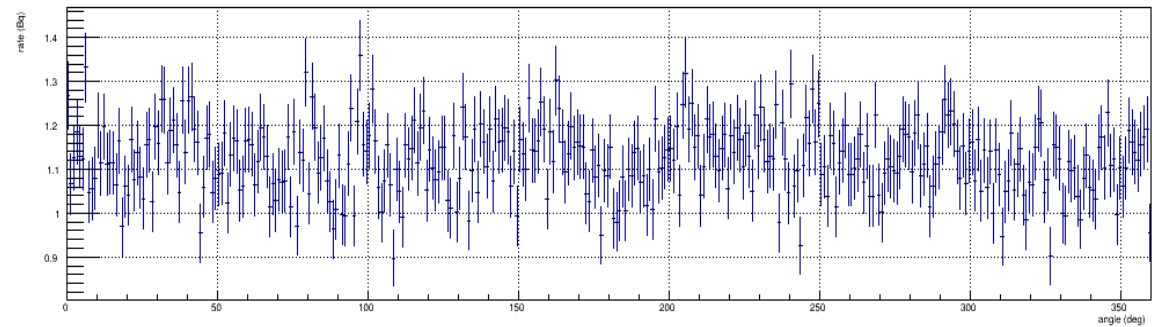


# Preliminary results – Two point sources 180 degrees apart

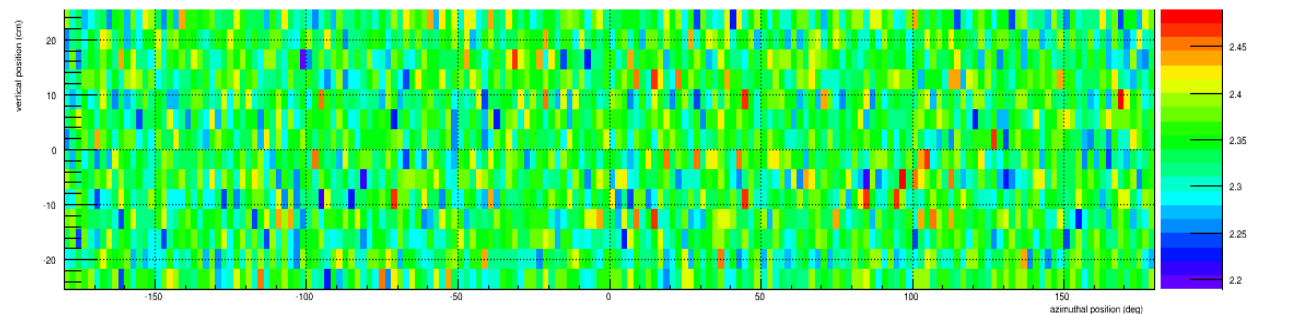
Measurement of two  
point sources 180  
degrees apart



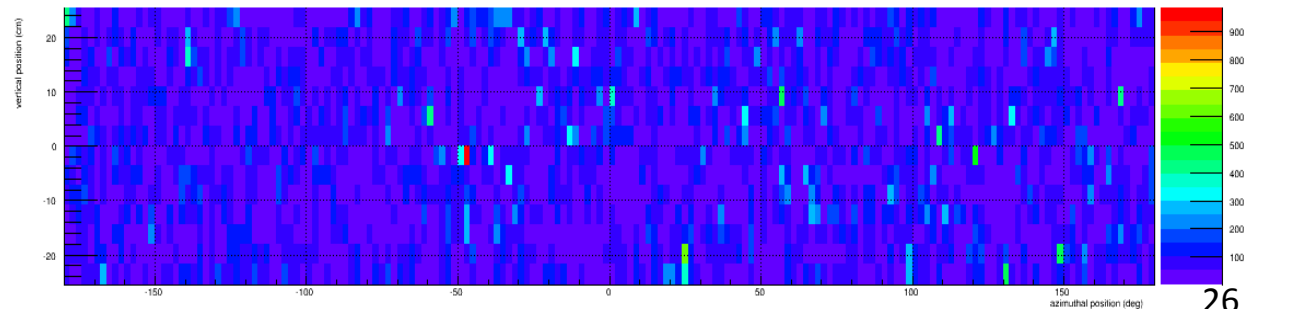
## Neutron Rate



## MLEM Reconstruction



## Relative Variance

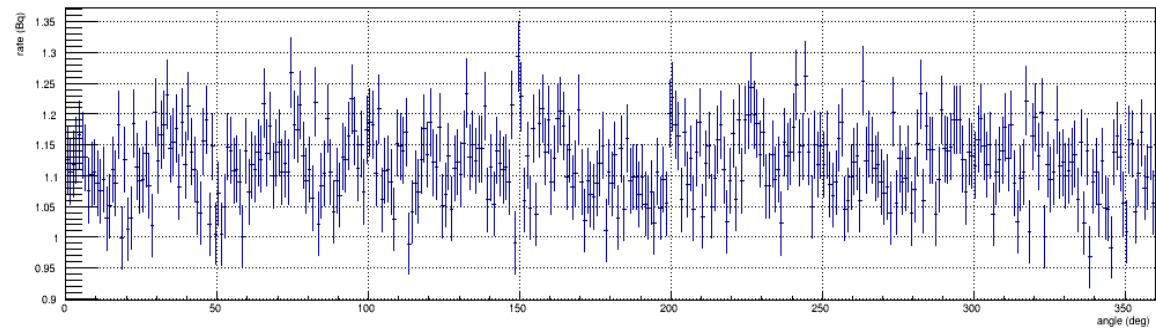


# Preliminary results – Two point source pairs

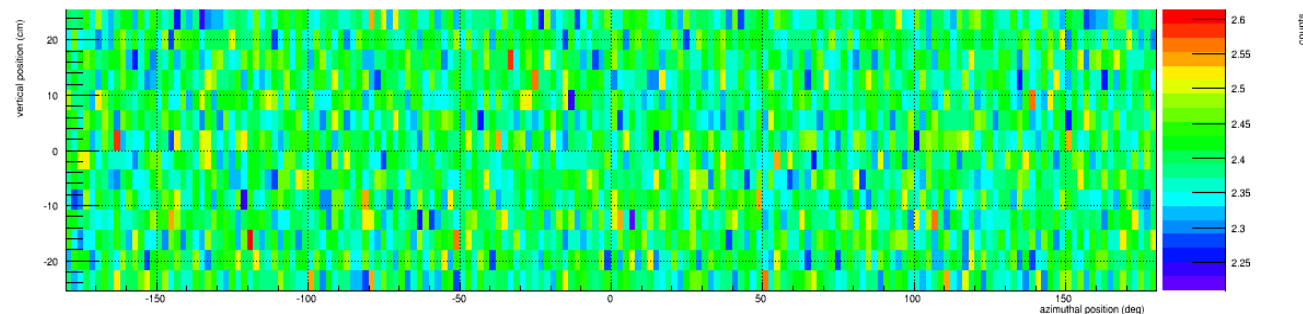
Measurement of two  
point source pairs  
separated by 19 cm  
180 degrees apart



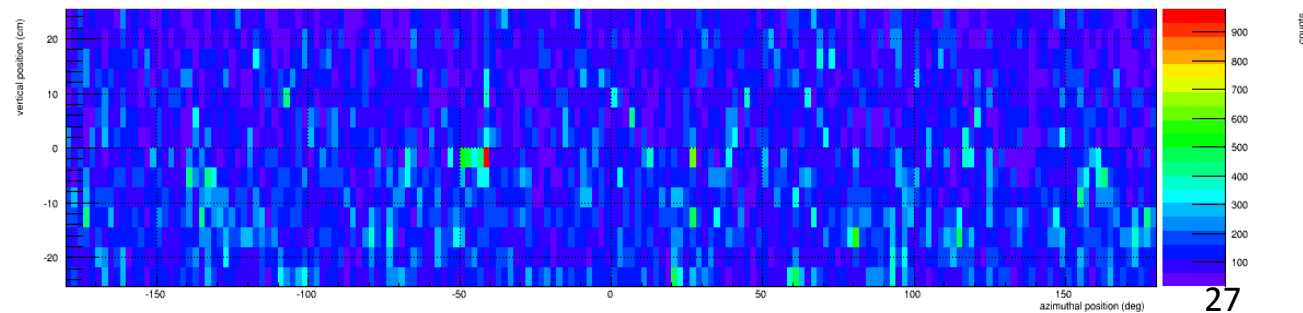
## Neutron Rate



## MLEM Reconstruction



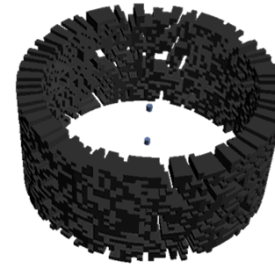
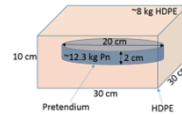
## Relative Variance



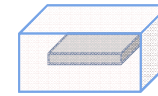
# Modeling results – T vs. F (5e5 counts)

True non-null-negative  
confirmation comparison  
measurement between  
objects T and F.

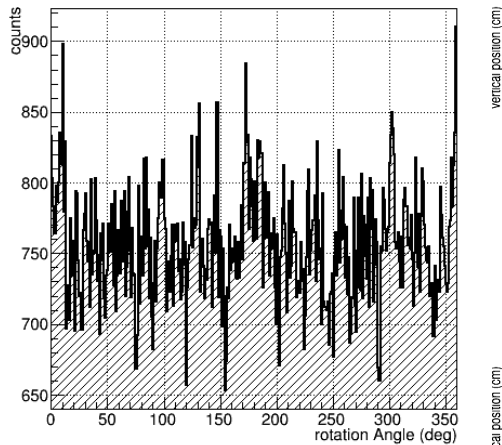
TAI T



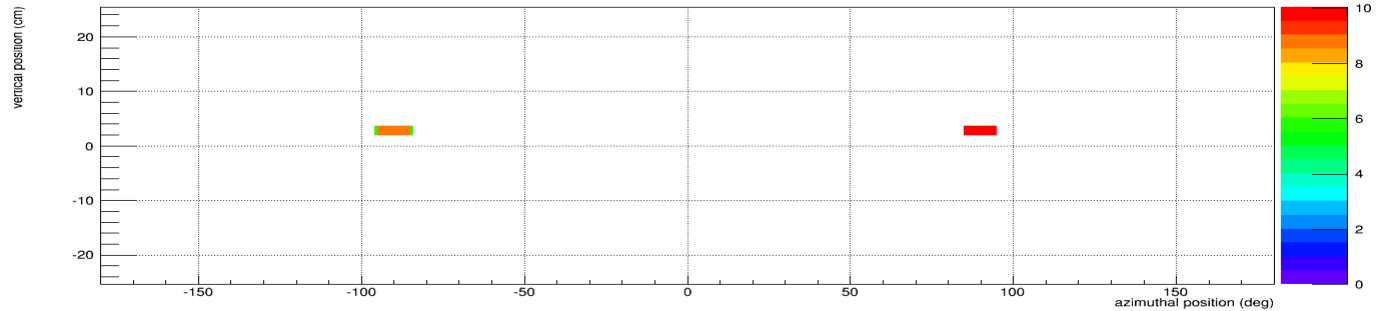
TAI F



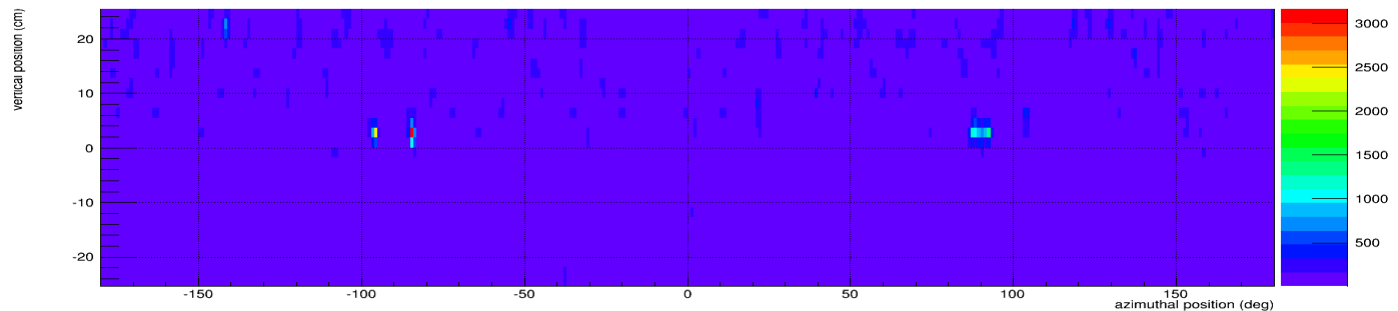
Pixel Counts



Iso-Background plus Source



Reconstructed Image (MLEM)

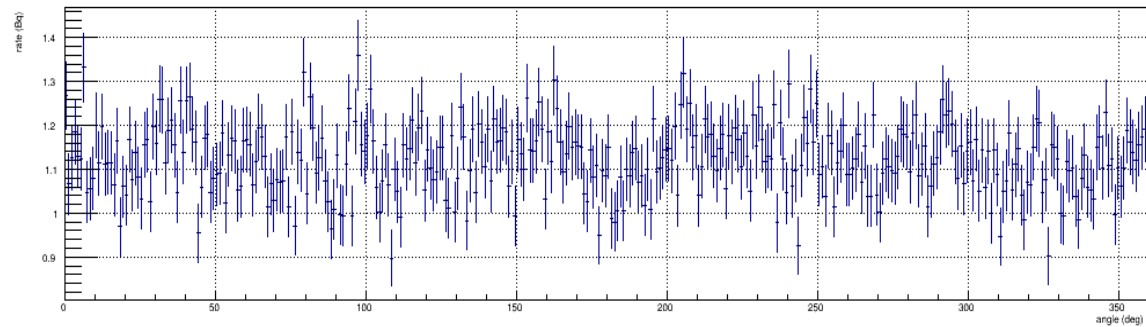


# Preliminary results – Two point sources (2.5 degrees apart)

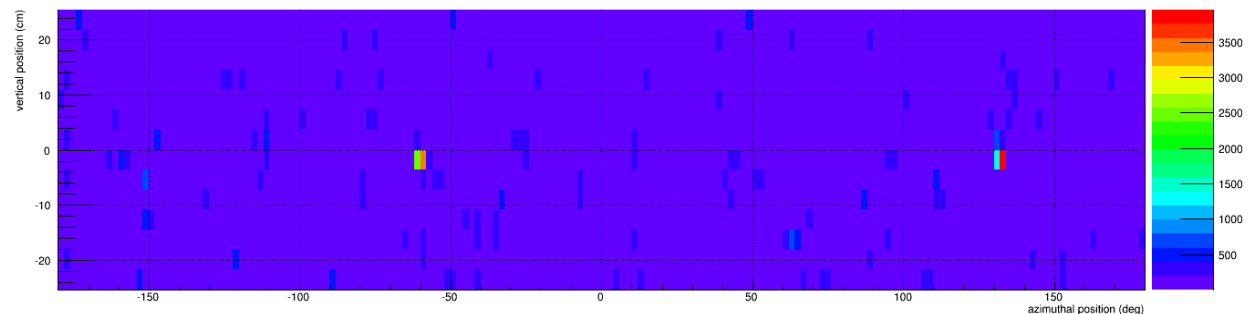
Measurement of two  
point sources 182.5  
degrees apart



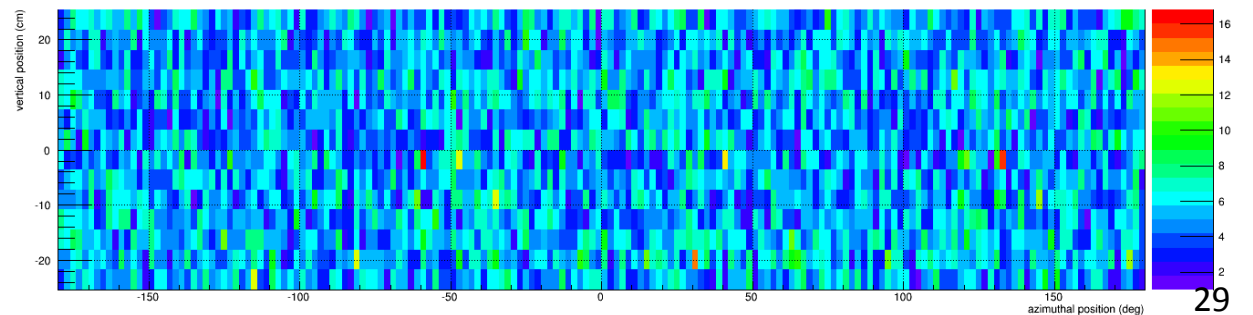
## Neutron Rate



## MLEM Reconstruction

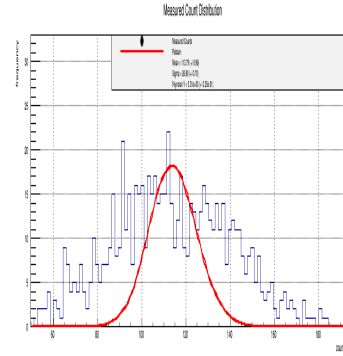
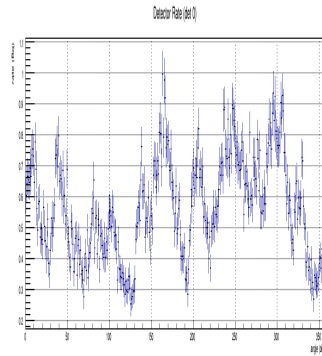


## Relative Variance



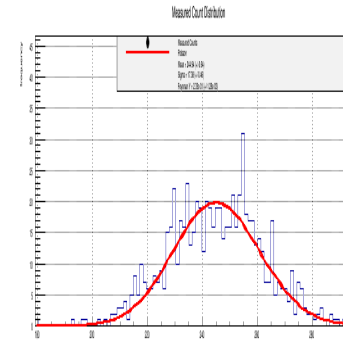
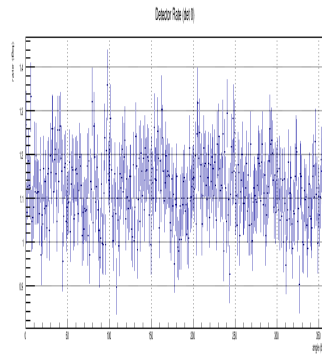
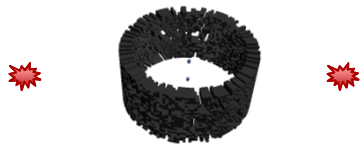
# Single Test Statistic – Feynman Y (preliminary)

## Single Point Source



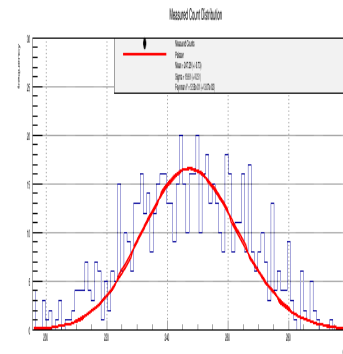
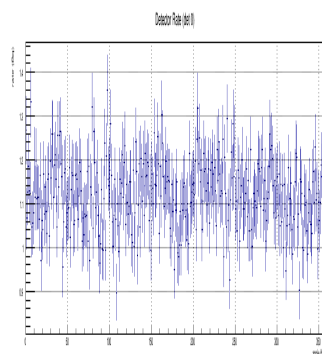
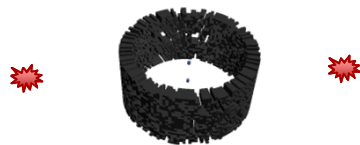
$$\begin{aligned} \text{Feynman Y} &= \left( \frac{\text{variance}}{\text{mean}} - 1 \right) \\ &= 5.3 (+/-0.3) \\ &\rightarrow \text{Far from Poisson} \end{aligned}$$

## Two Point Sources (aligned)



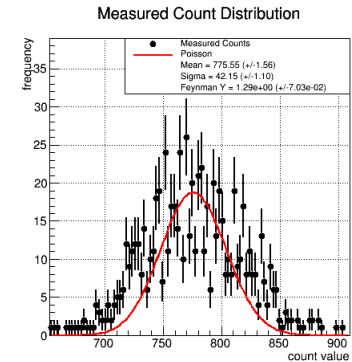
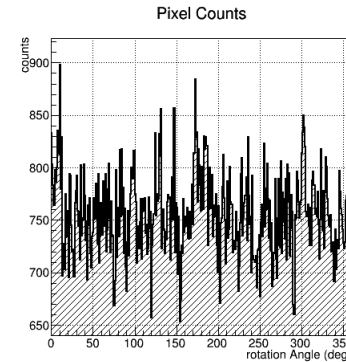
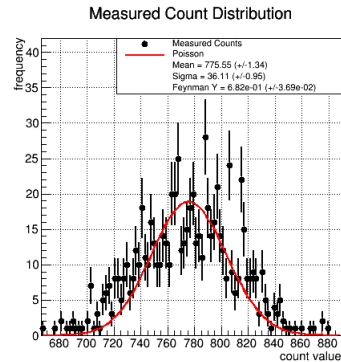
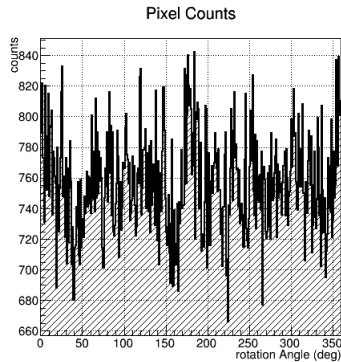
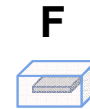
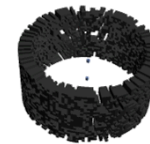
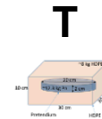
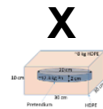
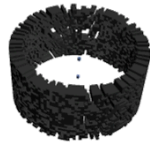
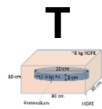
$$\begin{aligned} \text{Feynman Y} &= \left( \frac{\text{variance}}{\text{mean}} - 1 \right) \\ &= 0.23 (+/-0.01) \\ &\rightarrow \text{Fairly Poisson} \end{aligned}$$

## Two Point Sources (misaligned)

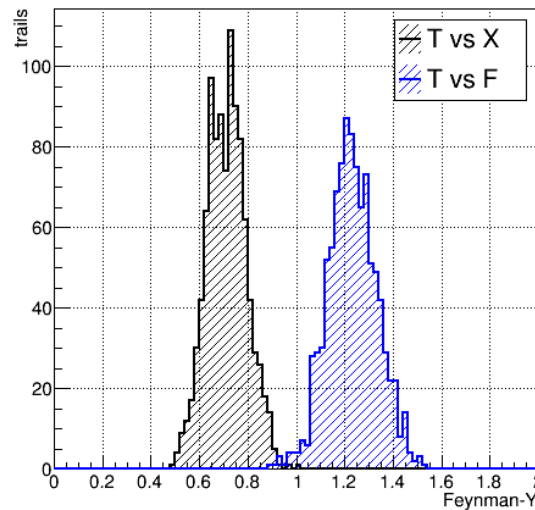


$$\begin{aligned} \text{Feynman Y} &= \left( \frac{\text{variance}}{\text{mean}} - 1 \right) \\ &= 0.56 (+/-0.03) \\ &\rightarrow \text{Less Poisson} \end{aligned}$$

# Feynman Y Test Statistic – 1000 trials of 5e5 counts



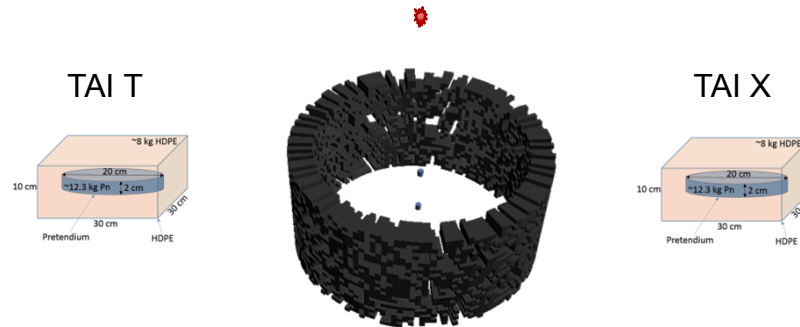
Distribution of Feynman-Y Test Statistics



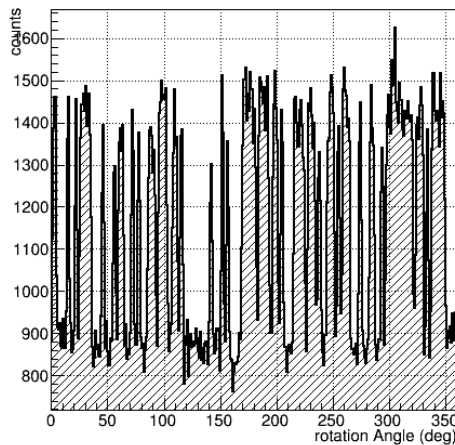


# Modeling results – T vs. X plus point source (8e5 counts)

If (and only if) the TAIs are identical, only the third source is visible!

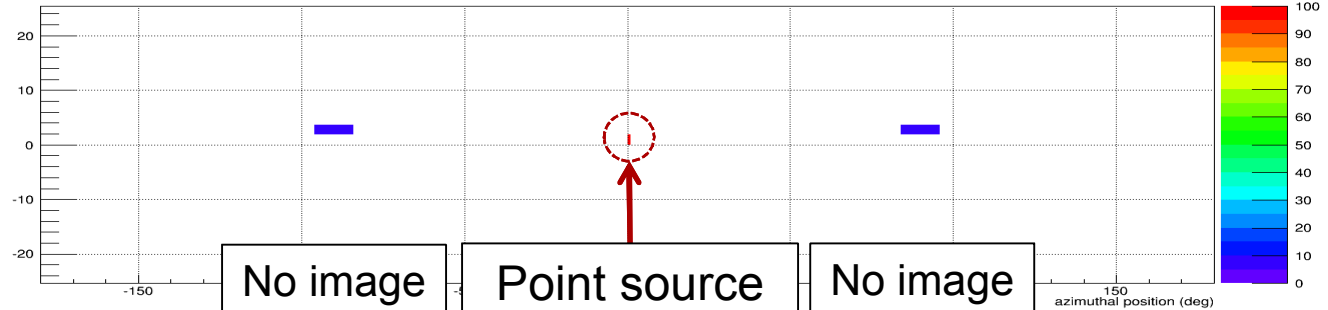


Pixel Counts

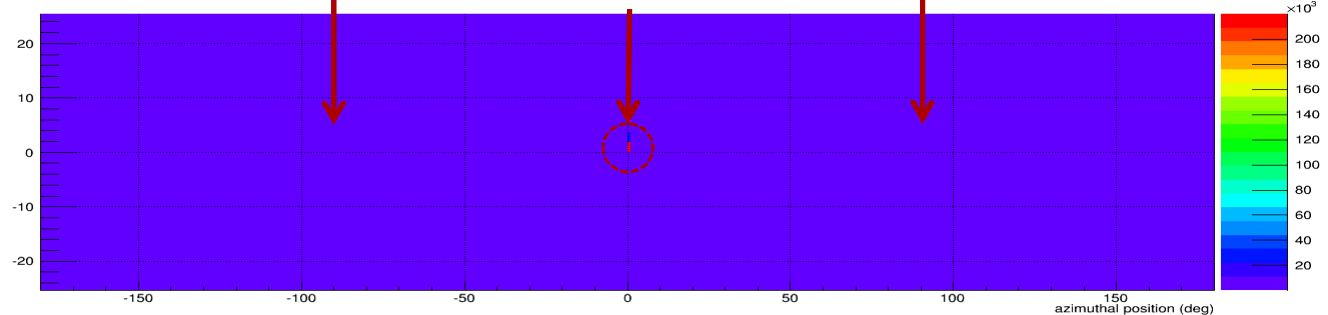


vertical position (cm)

Iso-Background plus Source



MLEM Reconstruction





# Conclusions

A properly designed two-dimensional time-encoded imager can:

1. Confirm that two objects are identical in a single measurement with NULL (constant rate) indicating a positive result.
2. Because a NULL (constant rate) is present at all times, the inspecting party might be allowed full access to the measurement and data.
3. The Feynman-Y test statistic can be updated to further protect against sensitive information loss.
4. Can image any third inspector provided object during the confirmation measurement without revealing the first two objects as an authentication measure.

# Extra Slides

# Certification vs. Authentication:

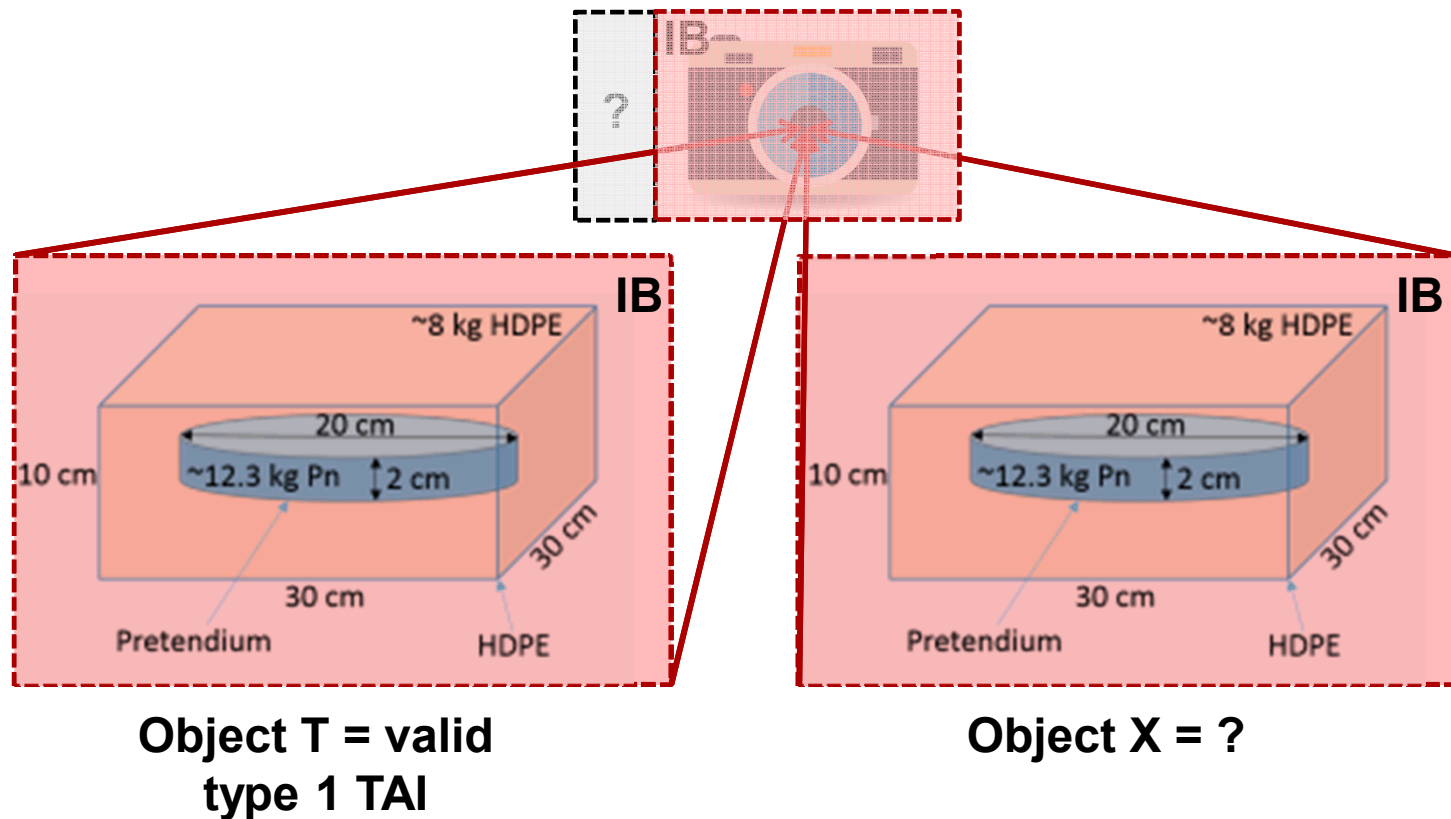
## It's not just for hardware

**Certification** – the process by which a host party gains confidence that sensitive information regarding an entity or facility remains secure.

**Authentication** - the process by which a monitoring party gains confidence that reported characteristics of an entity reflect the true state of that entity

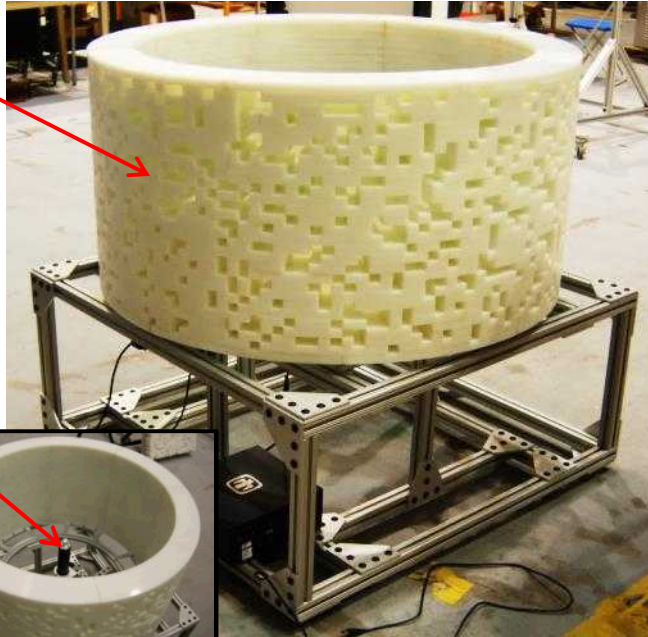
# Proposal – comparison measurements

- Can we compare two objects directly without generating a template?
- If one object is T, then X is confirmed as a type 1 TAI.
- If neither object is T, then they are confirmed to be identical, but not T.
- If multiple object comparisons are confirmed and even one is T, then all objects are confirmed as type 1 TAIs.

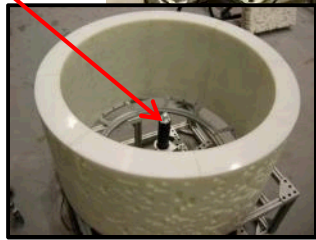


# 2D TEI – confirmation measurements?

2-d  
coded  
mask



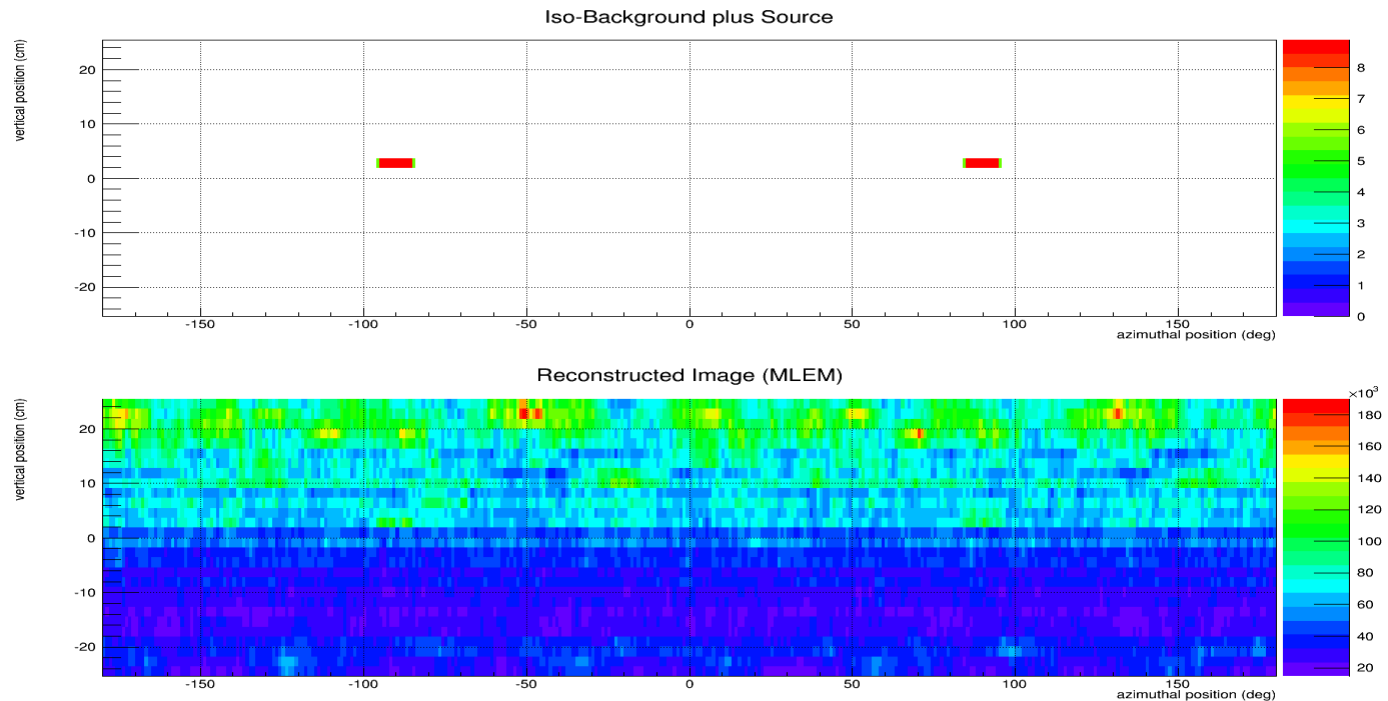
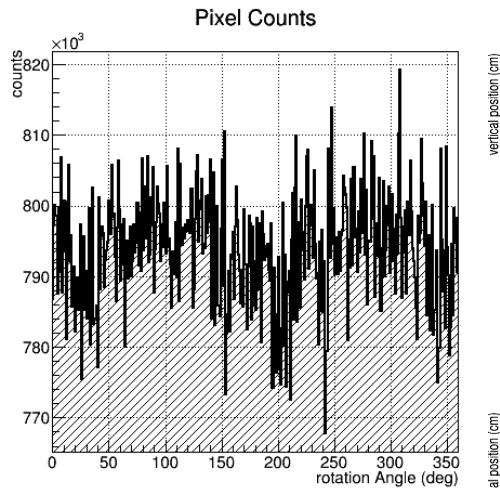
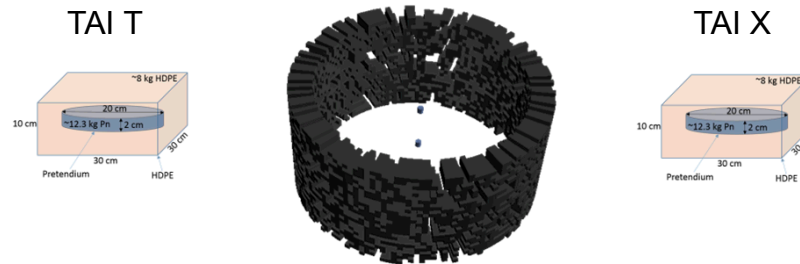
Single  
1"D x 1"  
LS pixel



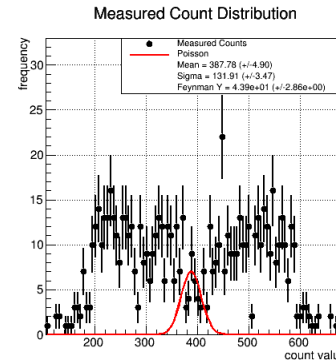
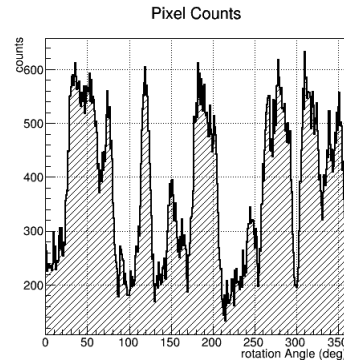
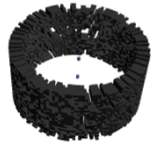
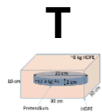
- **TEI is simple**
  1. Only one instrumented channel.
  2. Minimal calibration issues
    - a) Information encoded in the relative rate of a single detector.
    - b) Absolute gain doesn't matter.
    - c) Gain can drift over time.
  3. Potential real-time analysis
    - a) Single data stream.
    - b) Events can be processed one at a time and update a test statistic.
- **Can we design a TEI confirmation system such that the detection rates can be monitored by an inspector without putting sensitive information at risk?**

# Modeling results – T vs. X (1000 trials of 5e5 counts)

Even after summing 1000 trials worth of data, there isn't much evidence that sensitive information is present. **This must be made more rigorous.**



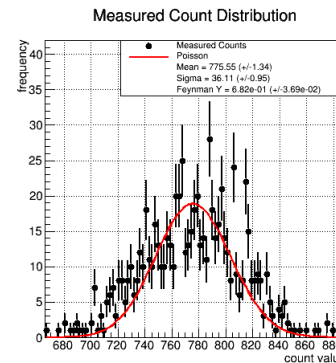
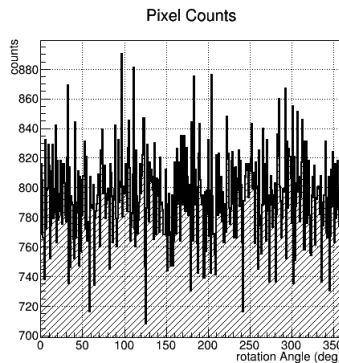
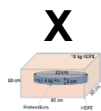
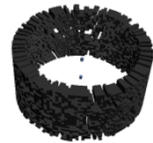
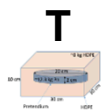
# Single Test Statistic – Feynman Y (modeling)



$$\text{Feynman Y} = \left( \frac{\text{variance}}{\text{mean}} - 1 \right)$$

$$= 86.8 (+/-5.7)$$

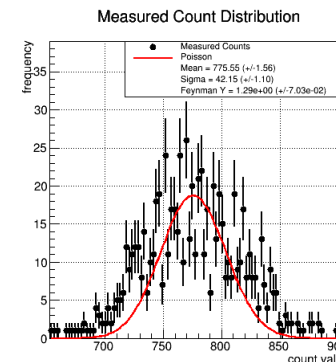
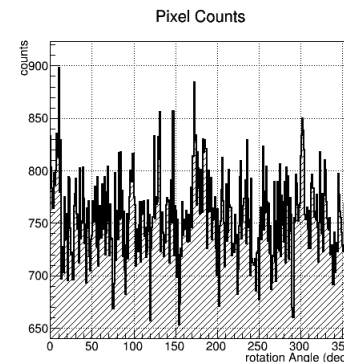
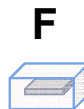
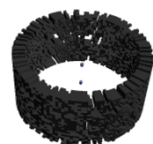
→ Far from Poisson



$$\text{Feynman Y} = \left( \frac{\text{variance}}{\text{mean}} - 1 \right)$$

$$= 0.68 (+/-0.04)$$

→ Fairly Poisson



$$\text{Feynman Y} = \left( \frac{\text{variance}}{\text{mean}} - 1 \right)$$

$$= 1.3 (+/-0.07)$$

→ Less Poisson