

# Yield Surface Effects on Stability and Failure

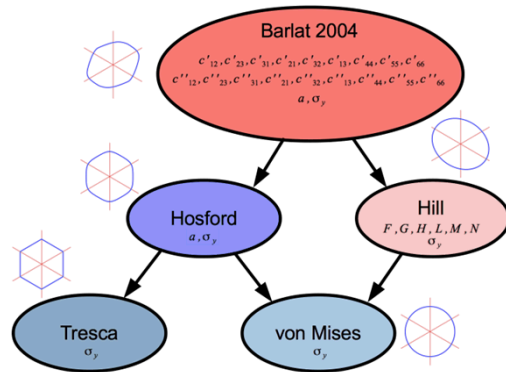
William M. Scherzinger  
Sandia National Laboratories  
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# Plasticity Model Hierarchy

## Plasticity Model Hierarchy



von Mises :

$$\phi(\sigma) = \sqrt{\frac{1}{2}[(\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2 + (\sigma_1 - \sigma_2)^2]}$$

Hosford :

$$\phi(\sigma) = \left\{ \frac{1}{2} [|\sigma_2 - \sigma_3|^a + |\sigma_3 - \sigma_1|^a + |\sigma_1 - \sigma_2|^a] \right\}^{1/a}$$

Hill :

$$\phi(\sigma) = \sqrt{F(\hat{\sigma}_{22} - \hat{\sigma}_{33})^2 + G(\hat{\sigma}_{33} - \hat{\sigma}_{11})^2 + H(\hat{\sigma}_{11} - \hat{\sigma}_{22})^2 + 2L\hat{\sigma}_{23}^2 + 2M\hat{\sigma}_{31}^2 + 2N\hat{\sigma}_{12}^2}$$

Barlat :

$$\phi(\sigma) = \left\{ \frac{1}{4} [ |s'_1 - s''_1|^a + |s'_1 - s''_2|^a + |s'_1 - s''_3|^a \right. \\ + |s'_2 - s''_1|^a + |s'_2 - s''_2|^a + |s'_2 - s''_3|^a \\ \left. + |s'_3 - s''_1|^a + |s'_3 - s''_2|^a + |s'_3 - s''_3|^a ] \right\}^{1/a}$$

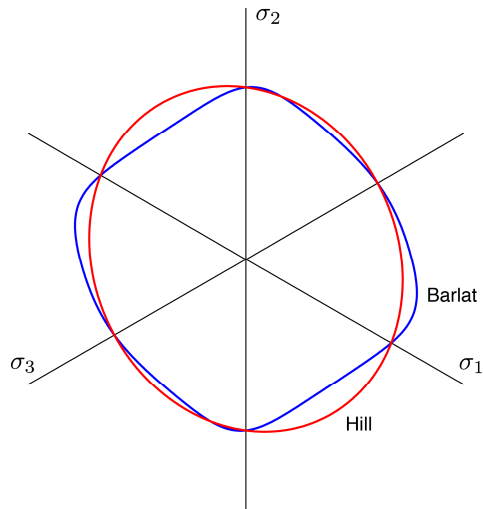
$s' = L' : \sigma$   
 $s'' = L'' : \sigma$

Model represents material behavior

- How well?
- Compared to other models?

What do we expect?

# Internal Pressurization of a Cylinder



Example of two anisotropic models that give the same yield stresses

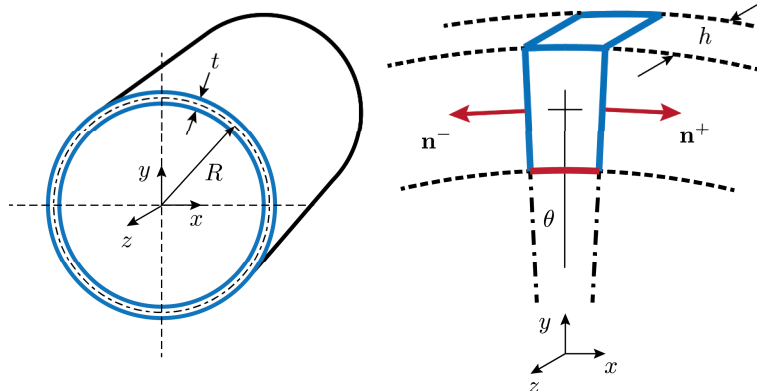
What results do they give?

We expect a maximum pressure

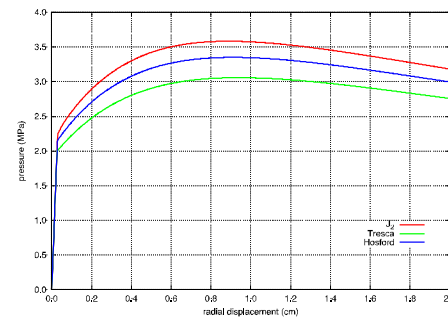
How different are our models?

We will consider parameterizations based on uniaxial stress

Internal pressurization of a cylinder



Isotropic



Anisotropic

