



## ABSTRACT

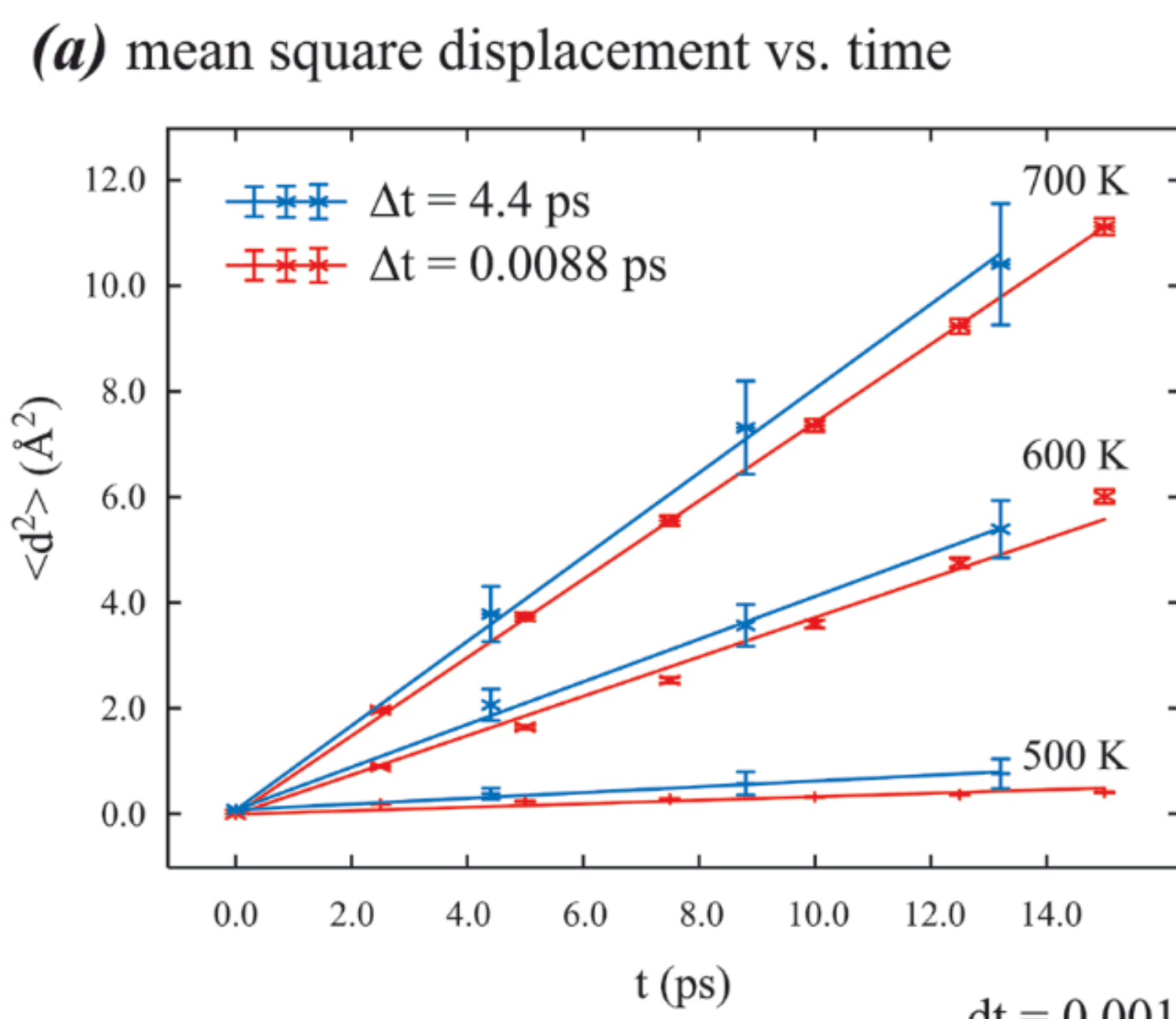
Hydrogen diffusion rates are important for hydrogen storage applications. In atomistic simulations, diffusion energy barriers are usually calculated for each atomic jump path using a nudged elastic band method. Practical materials often involve thousands of atomic jump paths not known a priori. It is also unclear how thousands of energy barriers relate to an overall diffusion behavior seen in experiments. Here we demonstrate that the overall diffusion energy barrier and pre-exponential factor can be accurately determined from Arrhenius equation constructed through molecular dynamics simulations of mean square diffusion distances at different temperatures. This progress will enable complex diffusion problems to be readily and reliably studied in the future. Preliminary application of this method has already begun to elucidate the experimental hydrogen diffusion data in aluminum and palladium.

### Method

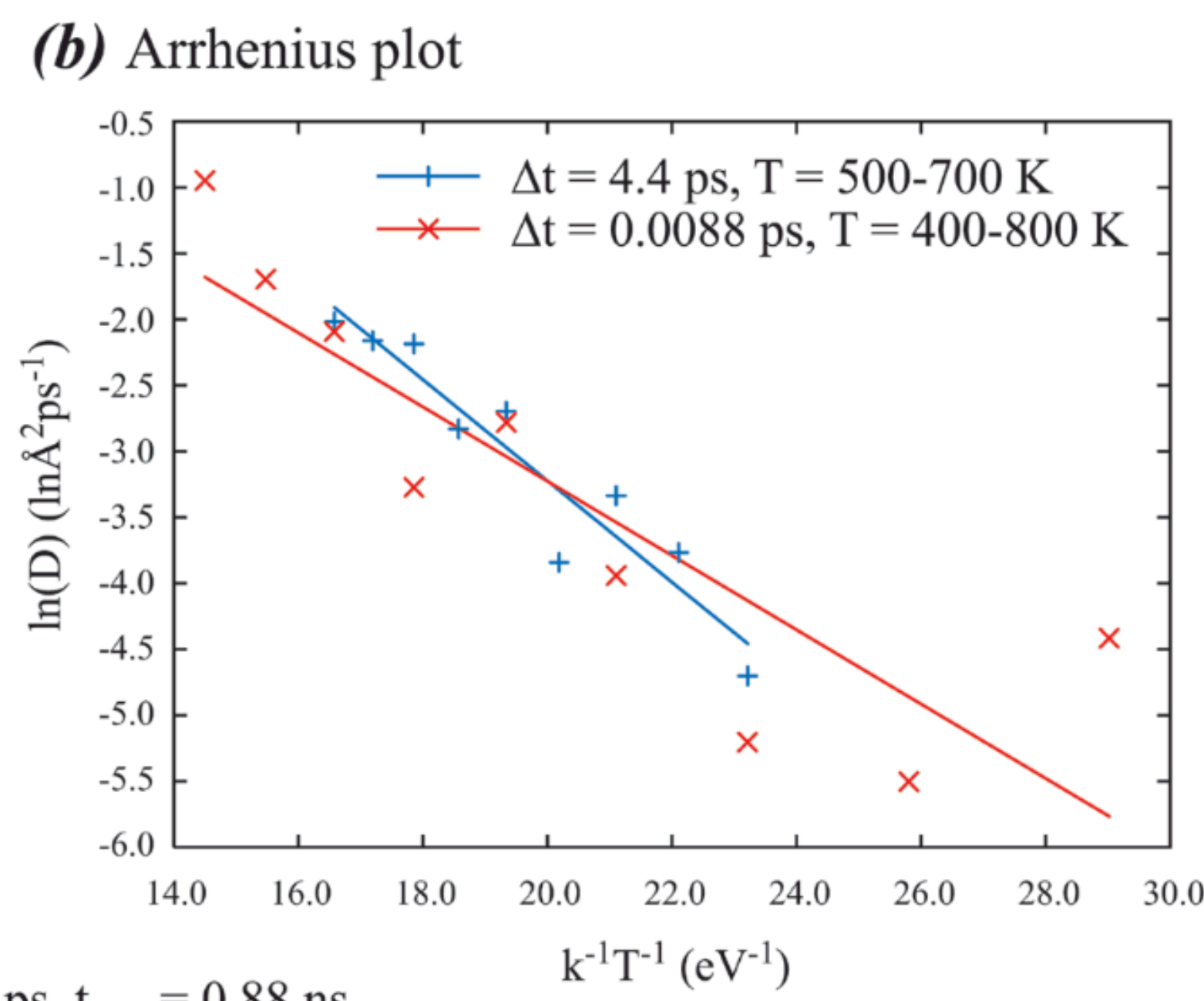
1. Molecular dynamics simulations are performed for 0.88 ns;
2. Hydrogen positions are recorded every 0.0088 ps;
3. Recorded positions are used to calculate mean square displacement;
4. Mean square displacement is converted to diffusivity;
5. Diffusivities at different temperatures are fitted to Arrhenius equation;
6. Arrhenius equation gives diffusion barrier and pre-exponential factor.

### Initial Calculation of Hydrogen Diffusion in Aluminum

#### Mean Square Displacement



#### Arrhenius Plots

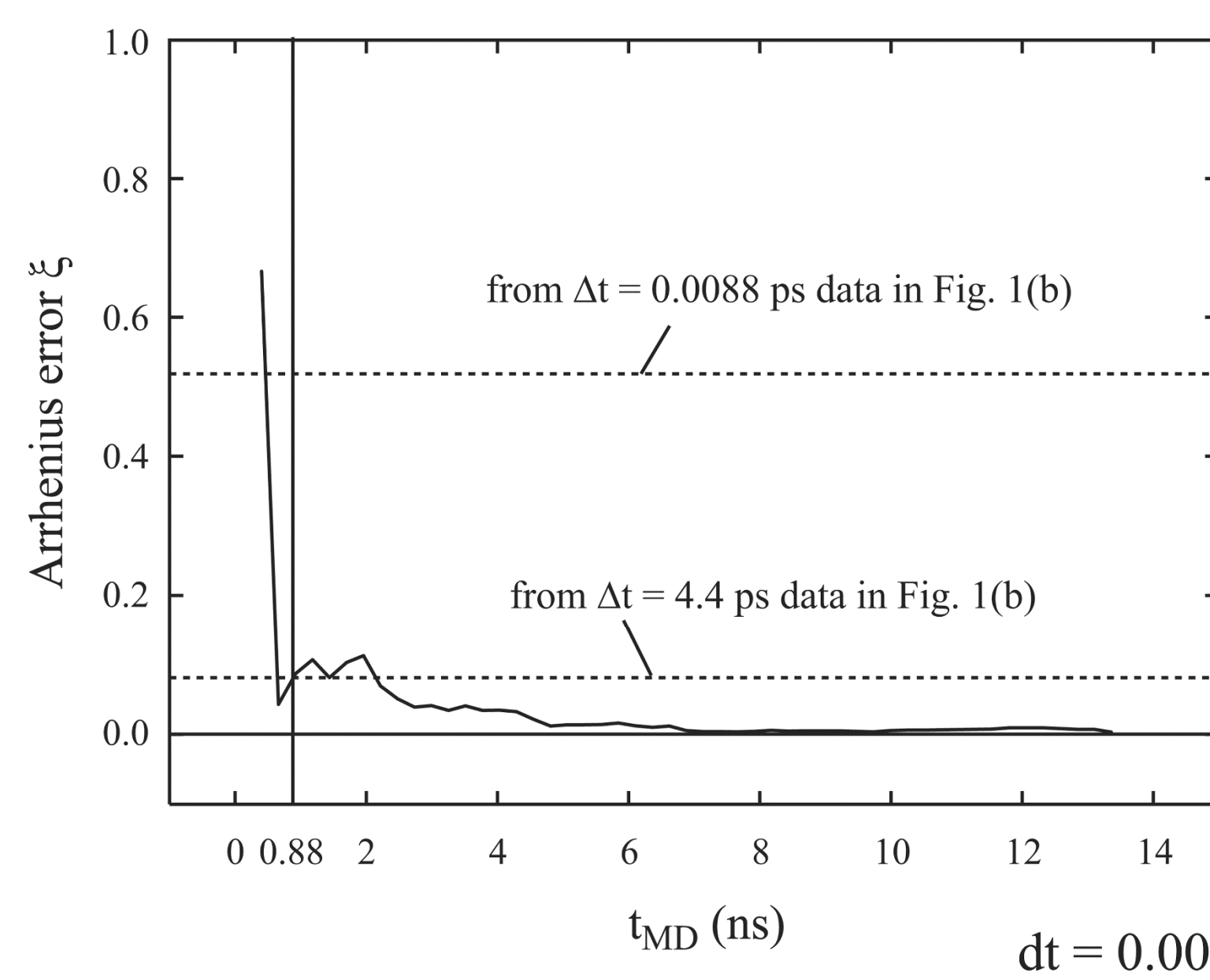


Statistical errors are too large for the results to be useful.

### Error Reduction

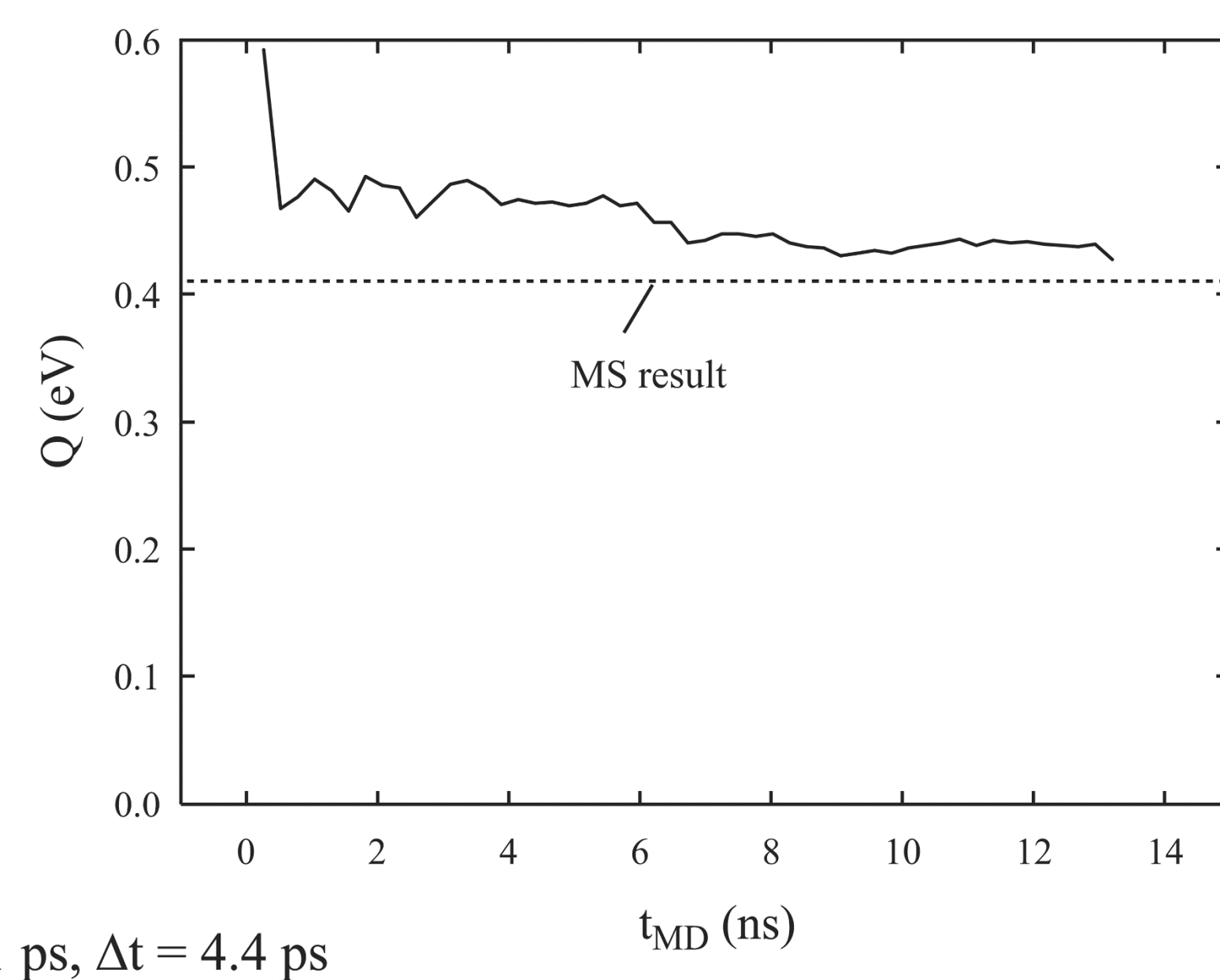
#### Error vs. Simulation time

(a) error of Arrhenius fit



#### Convergence of Diffusion Barrier

(b) activation energy Q

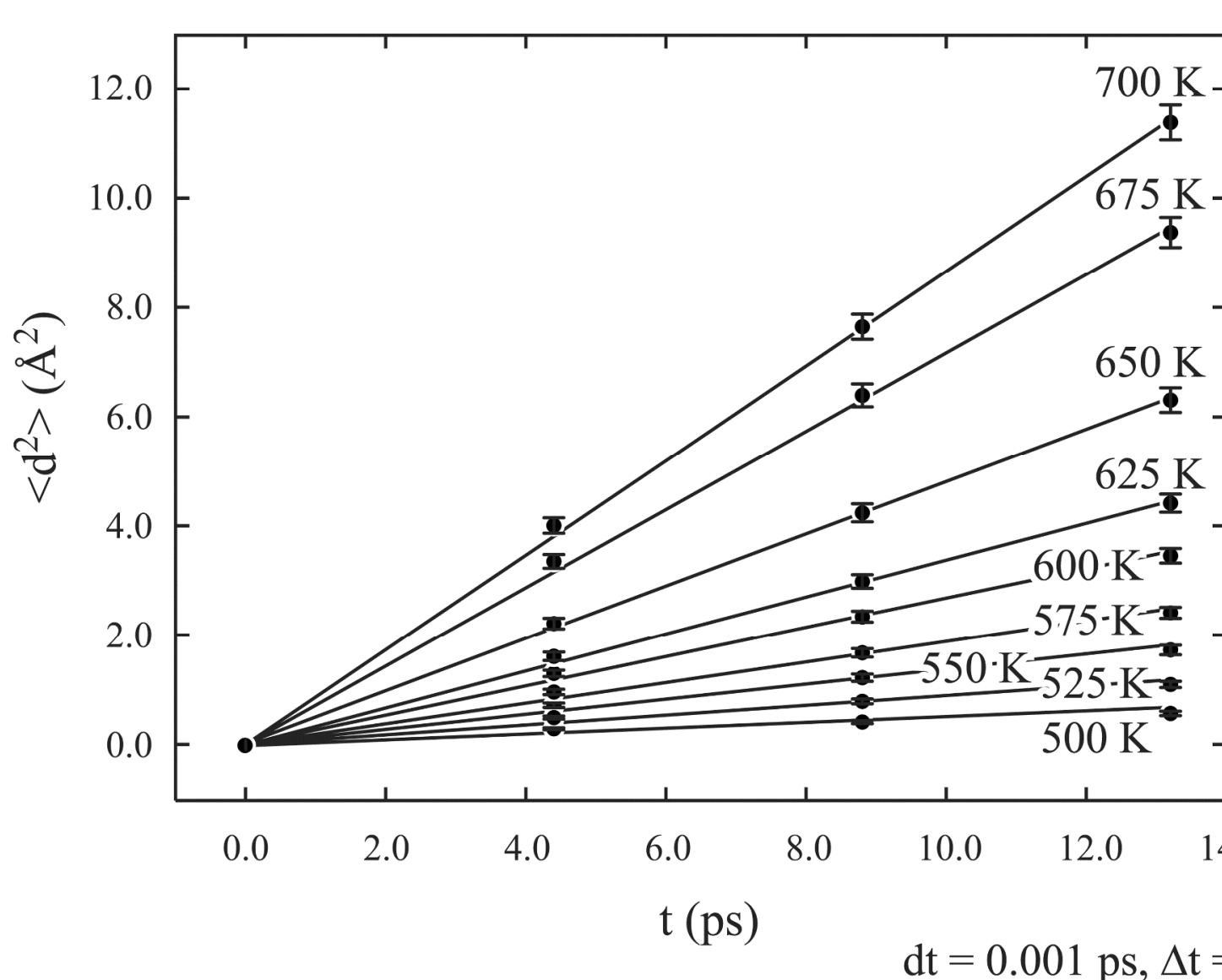


When simulation time is increased to 10 ns or above, error becomes negligible, and highly converged diffusion barrier can be achieved.

### Converged Calculation of Hydrogen Diffusion in Aluminum

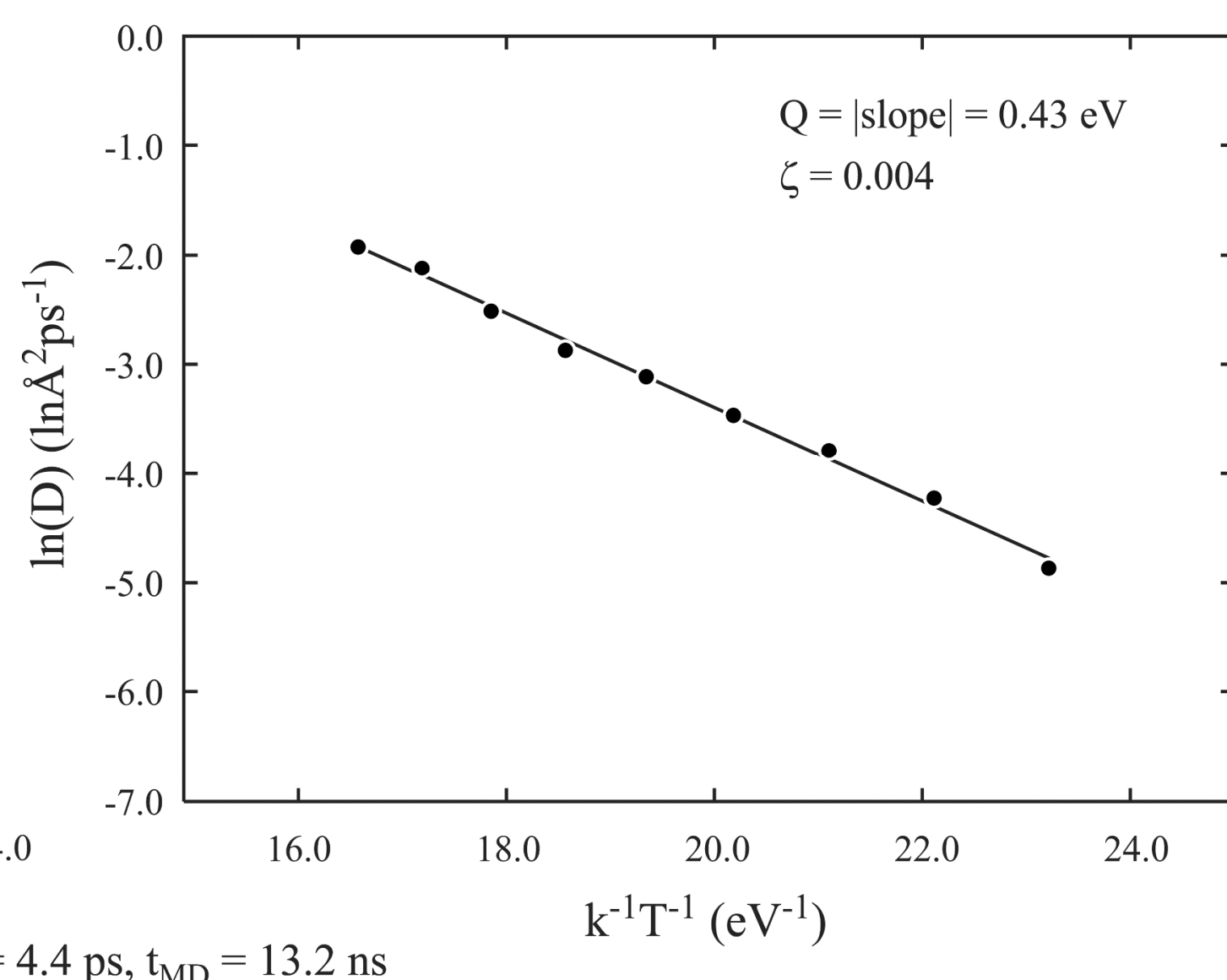
#### Mean Square Displacement

(a) mean square displacement vs. time



#### Arrhenius Plots

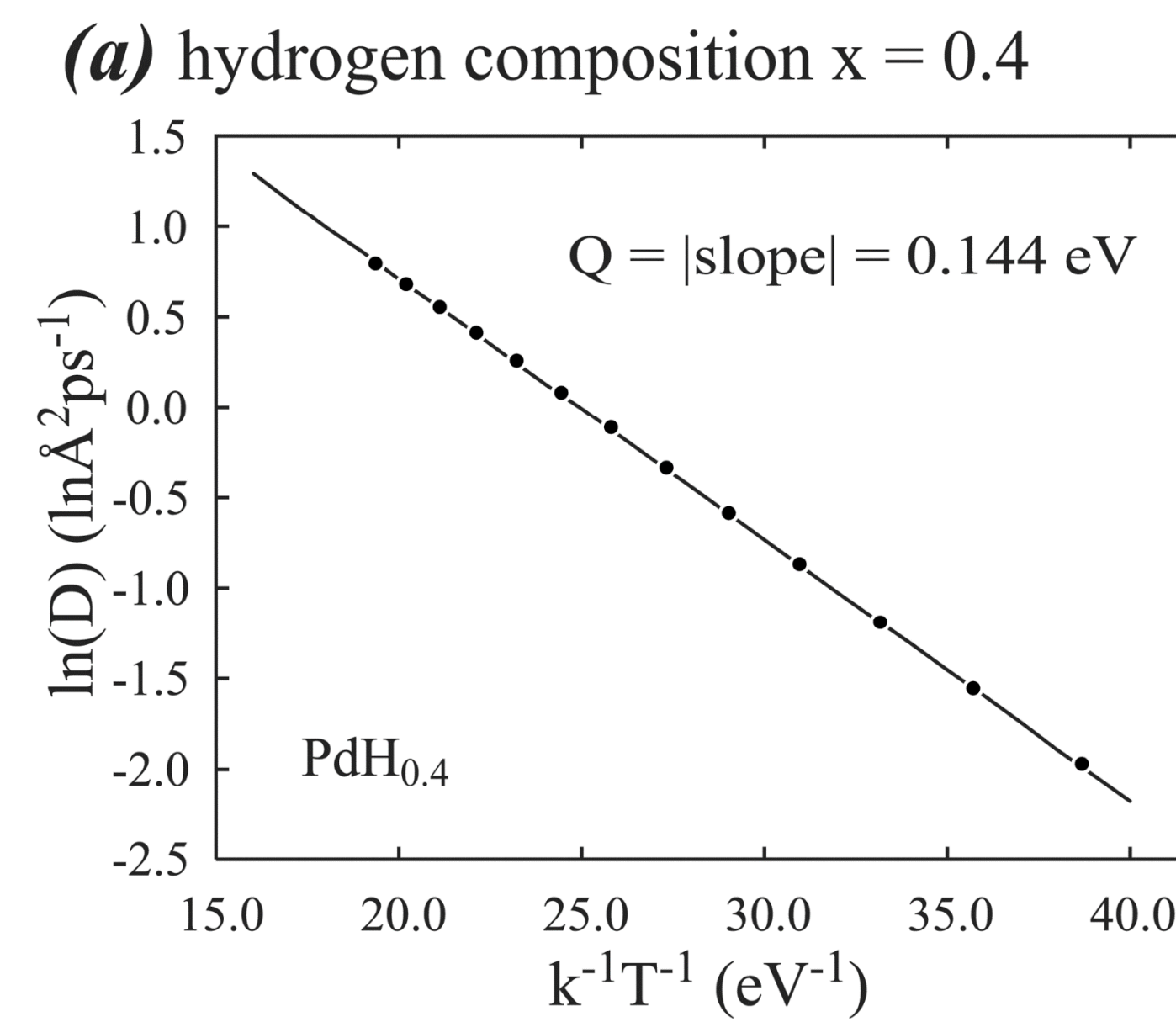
(b) Arrhenius plot



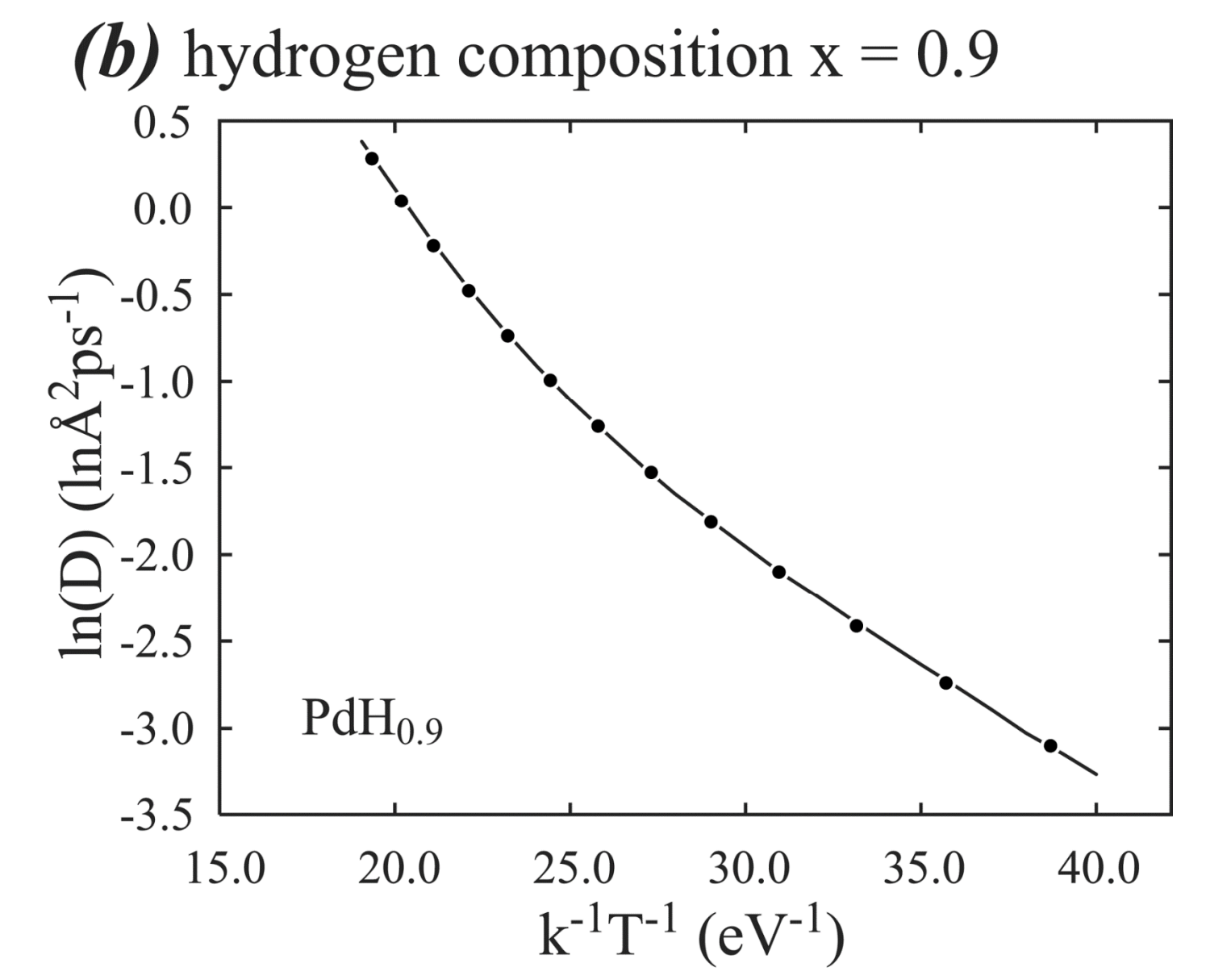
Highly converged molecular dynamics simulations convincingly indicate that the energy barrier for a single hydrogen atom diffusion in bulk aluminum is 0.43 eV.

### Converged Calculation of Hydrogen Diffusion in Palladium

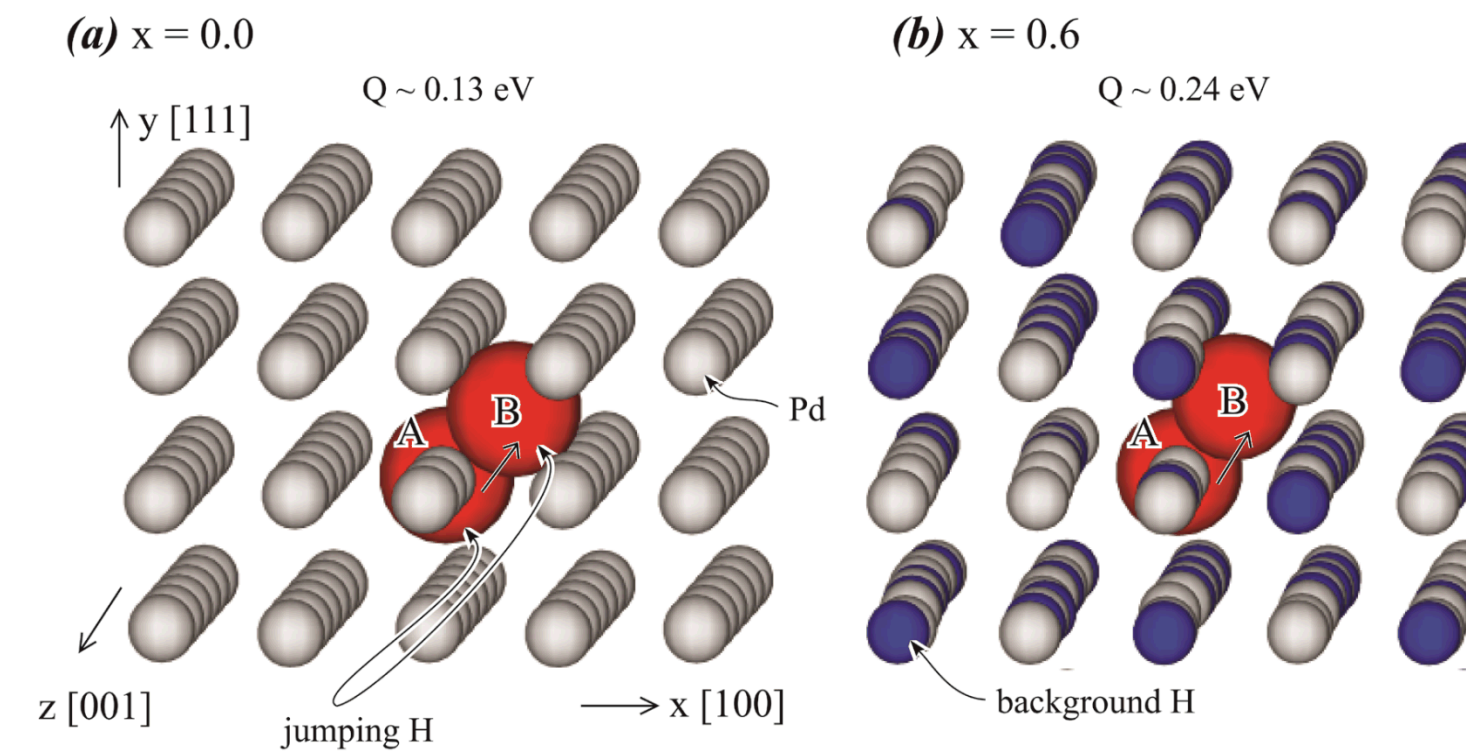
#### Arrhenius Plot at x = 0.4



#### Arrhenius Plot at x = 0.9



#### Two-Mechanism Model



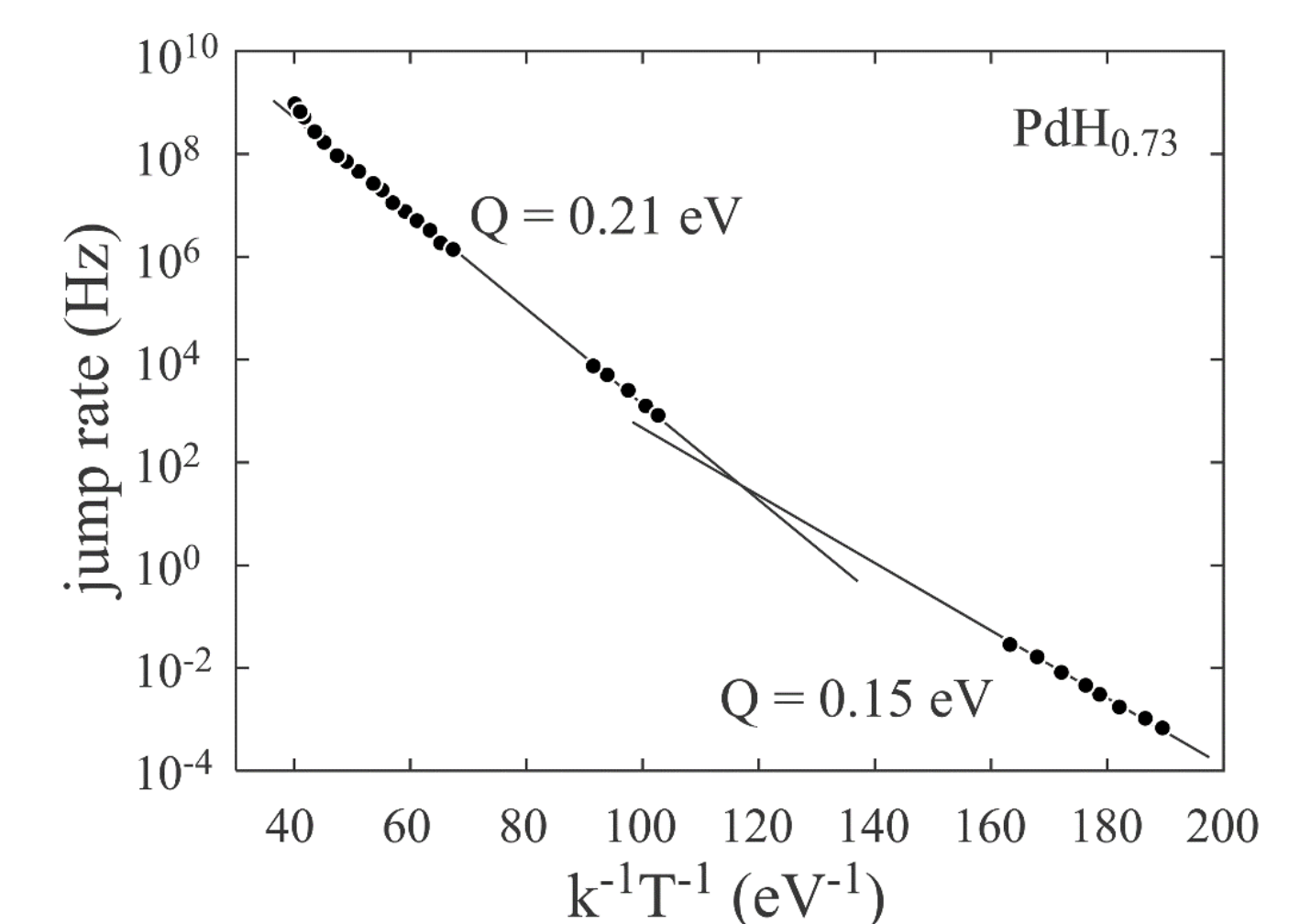
Highly converged molecular dynamics simulations convincingly predict that the Arrhenius plot is linear at low compositions and non-linear at high compositions.

### Experimental Comparisons

#### H-in-Al Measurements<sup>1</sup>

feature explored	feature metric	$D_0$ (Å²/ps)	Q (eV)	literature
grain size	> 25 mm	$9.530 \times 10^2$	0.46	Ichimura et al <sup>13,14</sup>
	15 mm	$4.580 \times 10^2$	0.38	
	4 mm	$1.520 \times 10^3$	0.55	
	2 mm	$2.110 \times 10^4$	0.69	
	3 mm	$1.540 \times 10^5$	0.84	
	3 mm	$4.220 \times 10^6$	1.11	
Al purity	99.999 %	$1.900 \times 10^3$	0.41	Papp et al <sup>15,16</sup>
	99.999 % + oxides (water-treated)	$1.100 \times 10^5$	0.74	
	99.8 %	$2.510 \times 10^6$	0.93	
unexplored	-----	$1.100 \times 10^3$	0.42	Eichenauer et al <sup>17,18</sup>
	-----	$2.100 \times 10^3$	0.47	
unexplored	-----	$1.101 \times 10^3$	0.49	Outlaw et al <sup>19</sup>
unexplored	-----	$2.000 \times 10^2$	0.52	Matsuo et al <sup>20</sup>
unexplored	-----	$9.200 \times 10^3$	0.57	Ishikawa et al <sup>21</sup>
unexplored	-----	$6.100 \times 10^3$	0.57	Saitoh et al <sup>22</sup>
unexplored	-----	$2.600 \times 10^3$	0.61	Hashimoto et al <sup>23</sup>
unexplored	-----	$1.300 \times 10^5$	0.69	Csanady et al <sup>24</sup>
unexplored	-----	$1.750 \times 10^0$	0.17	Young et al <sup>25</sup>
unexplored	-----	$1.200 \times 10^9$	1.45	Ransley et al <sup>26</sup>

#### H-in-Pd Measurements<sup>2</sup>



For PdH<sub>x</sub>, experiments validated the non-linear Arrhenius plots at high compositions.

For aluminum, experiments validated that the hydrogen diffusion energy barrier is around 0.41-0.47 when the material is single crystalline and pure. The high barriers are associated with high pre-exponential factors, suggesting the possibility of trapping. Simulations begin to elucidate the inconsistent experimental data, especially the low barrier (0.17 eV) measured by Young et al.

1: X. W. Zhou, F. El. Gabaly, V. Stavila, and M. D. Allendorf, J. Phys. Chem. C, 120, 7500 (2016).

2: R. R. Arons, H. G. Bohn, and H. Lutgemier, Solid State Comm., 14, 1203 (1974).

### Acknowledgements

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### Conclusions

Robust molecular dynamics simulation methods allow confident determination of the overall diffusion energy barrier and pre-exponential factor from Arrhenius equation. Preliminary work has begun to elucidate the experimental data measured for aluminum and palladium.