



Dynamics and Ion Transport in Ionomers

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Polymer Physics GRC

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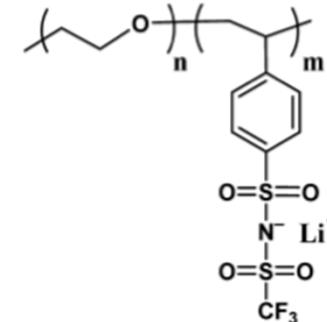
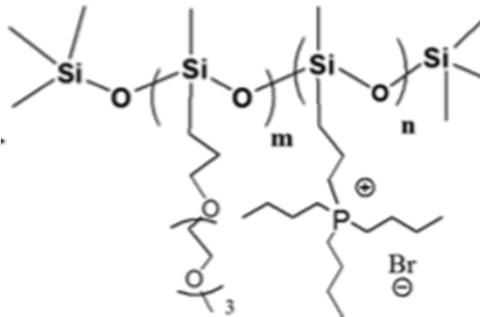
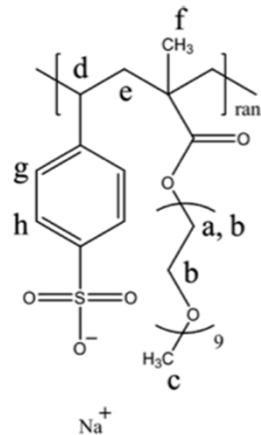
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Ionomer Melts as Single-Ion Conductors



why single-ion?

- high transference number

transference number
 t^+ = fraction of current carried by cation

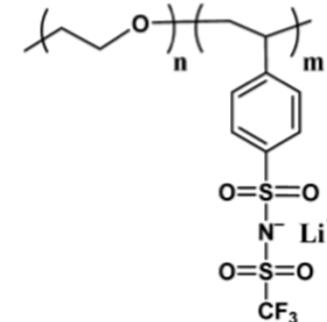
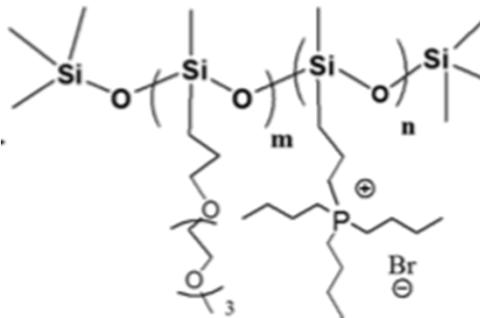
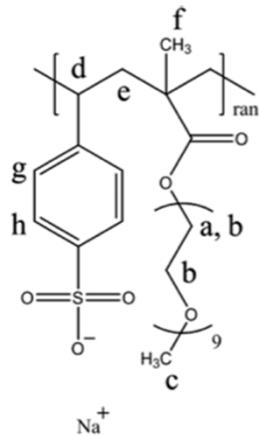
$$t^+ = \frac{\mu_+}{\mu_+ + \mu_-}$$

Wang, J.-H. H. et al. *Macromolecules* **48**, 7273–7285 (2015).

Liang, S. et al. *Macromolecules* **47**, 4428–4437 (2014).

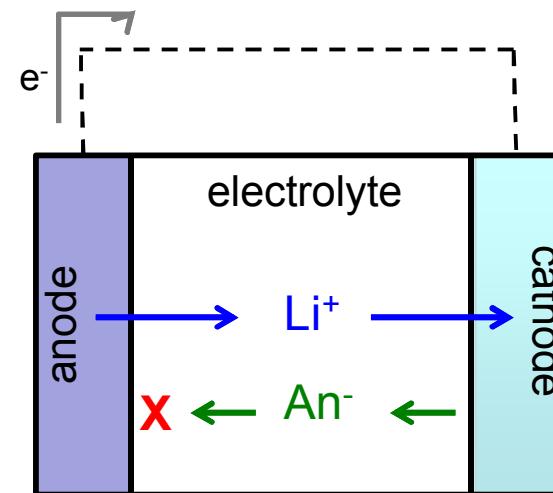
Rojas, A. A. et al. *Macromolecules* **48**, 6589–6595 (2015).

Ionomer Melts as Single-Ion Conductors



why single-ion?

- high transference number
- no concentration gradients



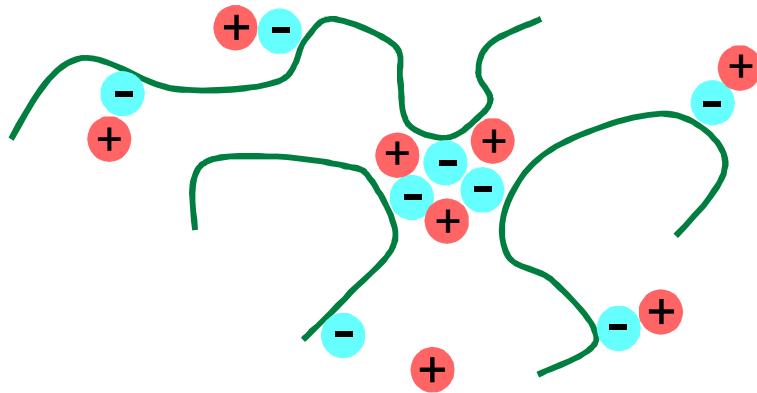
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Rojas, A. A. et al. *Macromolecules* **48**, 6589–6595 (2015).

Ionic Aggregates in Ionomers

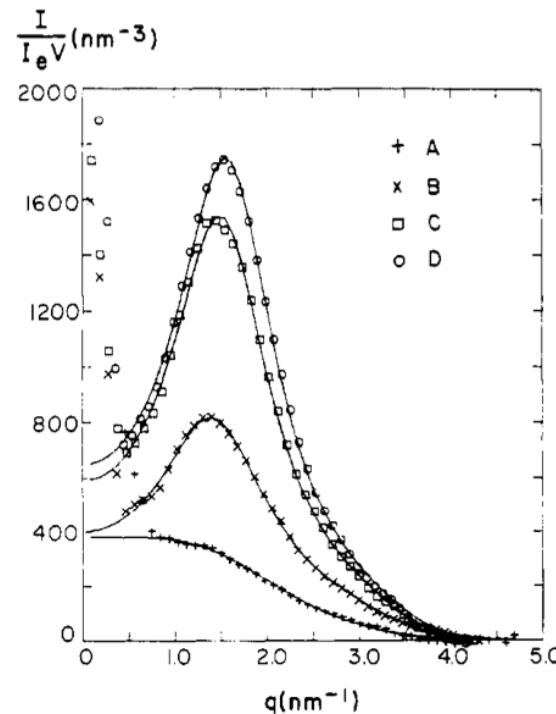
Coulombic forces favor aggregates
polymer entropy limits size



nm-scale ionic aggregates

“ionomer peak”

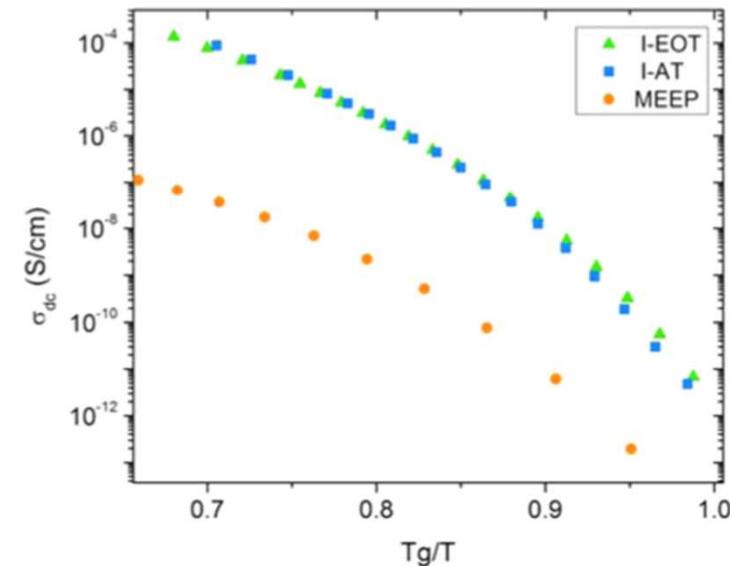
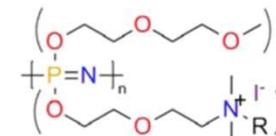
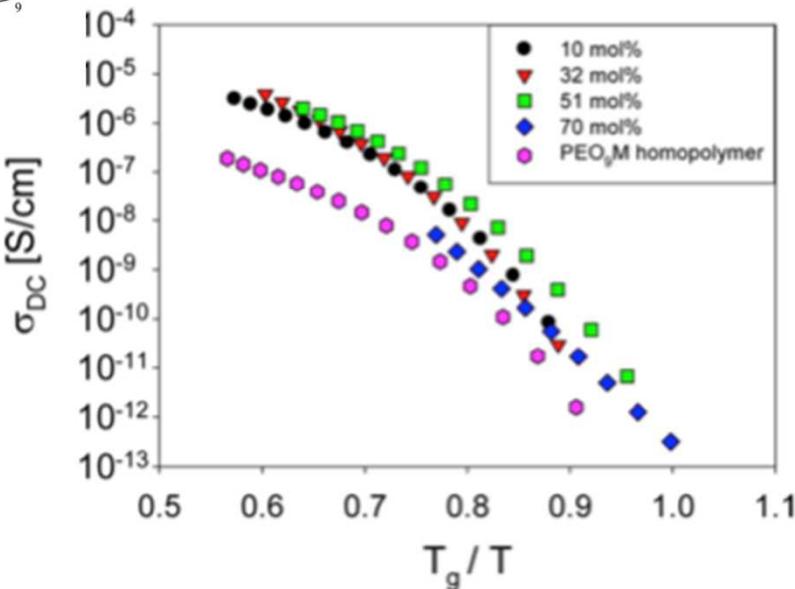
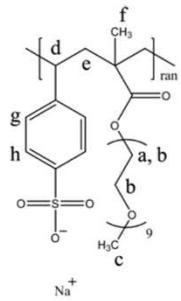
- ubiquitous
- low wavevector peak in scattering
- from inter-aggregate scattering



Yarusso & Cooper, Macromolecules, 1983

Ionic Conductivity in Ionomers

low due to low ϵ , slow polymer motion, ionic aggregates



Wang, J.-H. H. et al. *Macromolecules* **48**, 7273–7285 (2015)

Bartels, J. et al. *Macromolecules* **48**, 111–118 (2015)

need $\sigma_{DC} > 10^{-4}$ - 10^{-3} S/cm for applications

How do we improve conductivity?

ceramics can be superionic conductors

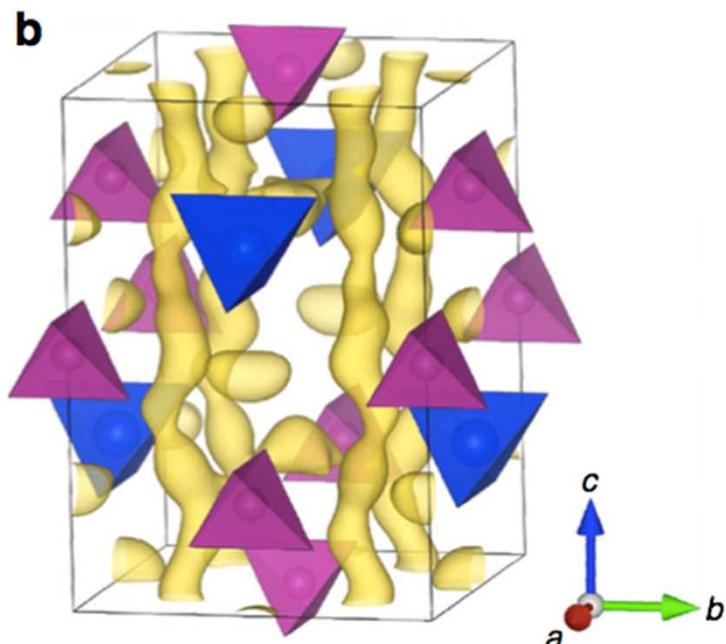
$$f = \frac{D_{charge}}{D_{self}} \quad \text{with } f > 1$$

example: $\text{Na}_{10}\text{SnP}_2\text{S}_{12}$

0.4 mS/cm at room temperature

$f \approx 1.8$

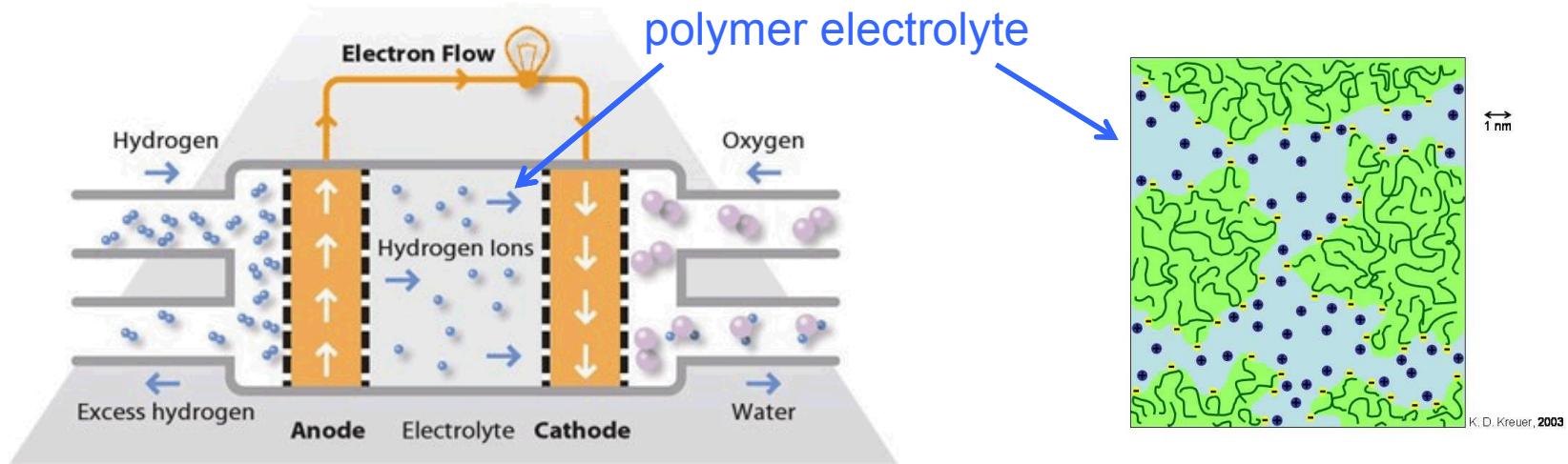
$\text{Na}_{10}\text{SnP}_2\text{S}_{12}$



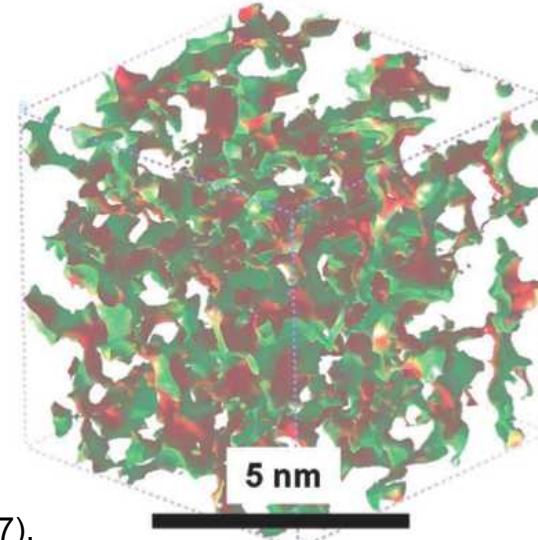
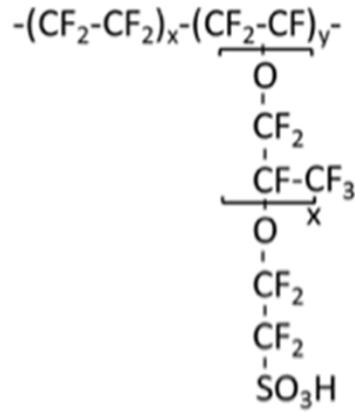
Richards, W. D. et al. *Nature Communications* 7, 1–8 (2016).

design percolated morphologies?

Hydrated ionomers



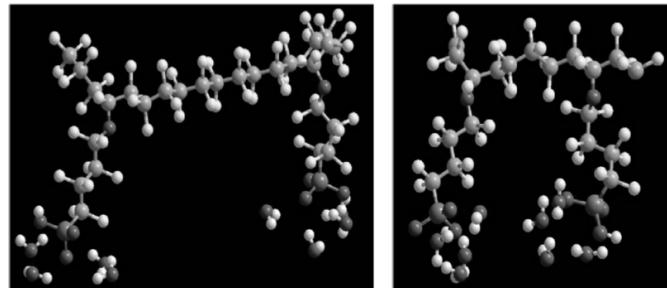
Nafion



Elliott, J. A. & Paddison, S. J. *Phys Chem Chem Phys* **9**, 2602 (2007).

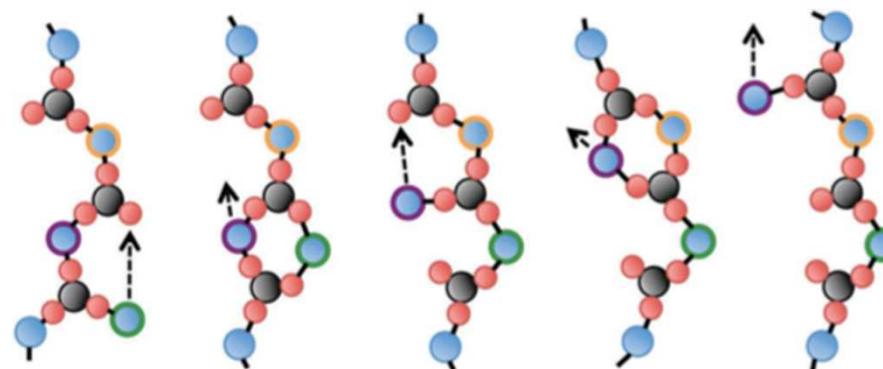
Ion Transport in Percolated Clusters

hydrated: form percolated water/ionic clusters
close sulfonic acid groups important?



Maalouf, M. et al. *International Journal of Hydrogen Energy* **39**, 2795–2800 (2014).

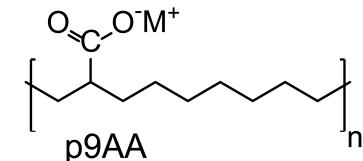
melt: ionic aggregates can help ions move collectively



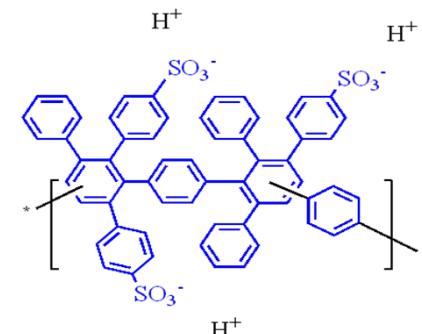
Lu, K., Maranas, J. K. & Milner, S. T. *Soft Matter*. *Soft Matter* **12**, 3943–3954 (2016).

Rest of the Talk

- melts of precise poly(ethylene-co-acrylic acid) (pAA)
 - atomistic simulations
 - morphology and comparison to X-ray
 - dynamics and comparison to QENS
 - coarse-grained simulations

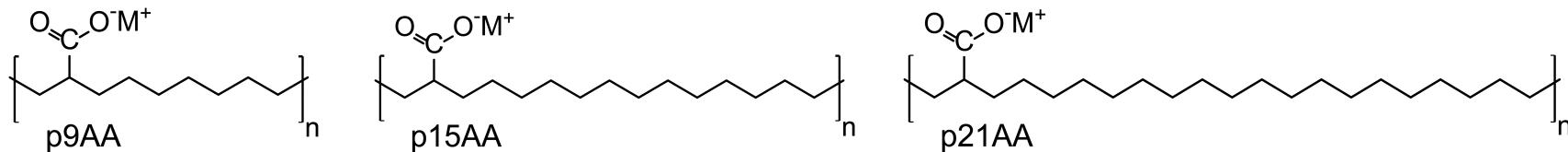


- hydrated, sulfonated Diels-Alder polyphenylenes (SDAPP)
 - atomistic simulations



Model Materials: Precise Ionomers

PE backbone with **precisely** spaced carboxylic acid functional groups

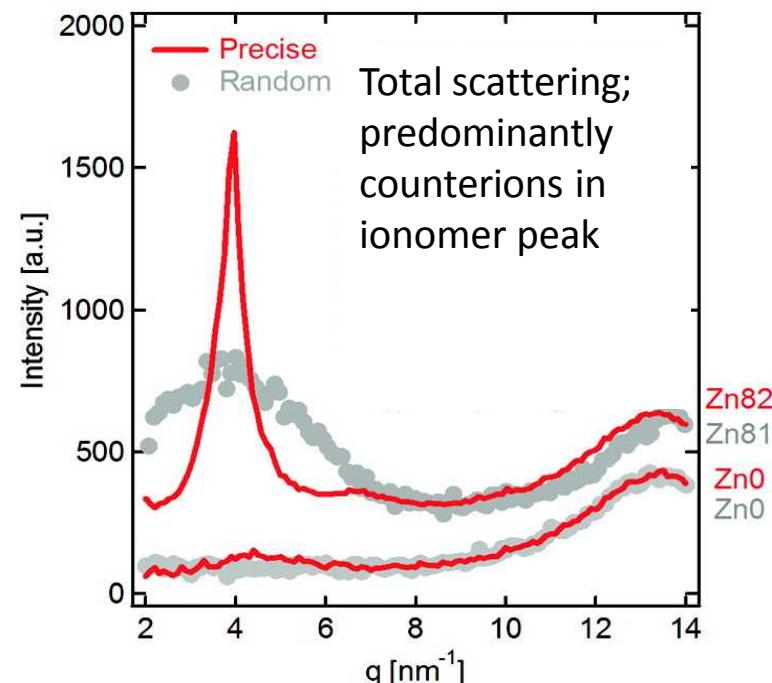


p9AA — 43% Li

Precise spacer length (p9, p15, p21)

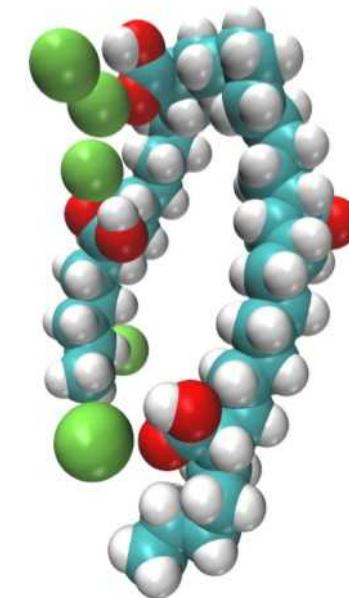
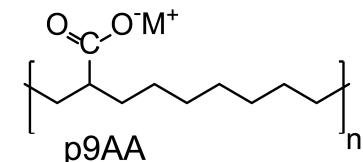
Neutralization level

Counterion type (Li^+ , Na^+ , Cs^+ , Zn^{2+})



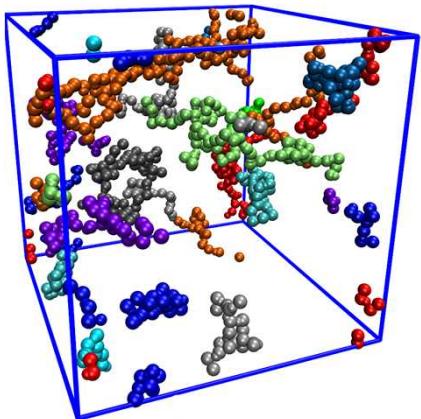
Atomistic MD Simulations

- Variations in:
 - cation type: M^+ = Li^+ , Na^+ , Cs^+ , Zn^{2+}
 - neutralization level = % COO^-M^+ vs $COOH$
 - spacing length: p9, p15, p21
- All atom OPLS-AA force-field
- 80-200 polymers, $n = 4$ repeat units (4 acid groups)
 - $\sim 64 \text{ \AA}$ box, total of $\sim 25,000$ atoms
- NVT ensemble, **150°C \rightarrow well above T_g**
- 30 ns (400 ns in one case)
- LAMMPS



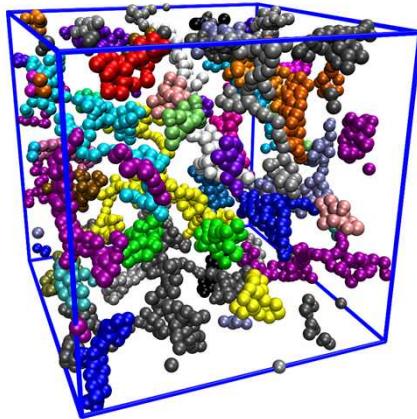
Morphology: Li-neutralized pAA

p9AA-10%Li



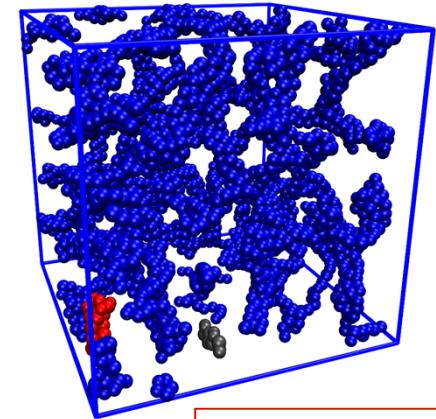
TYPE II (stringy)

p9AA-43%Li



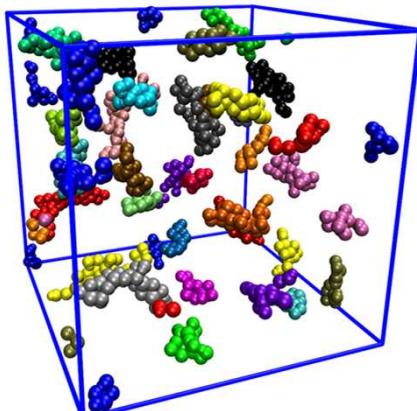
TYPE II (stringy)

p9AA-100%Li



TYPE III
(fully percolated)

p21AA-43%Li

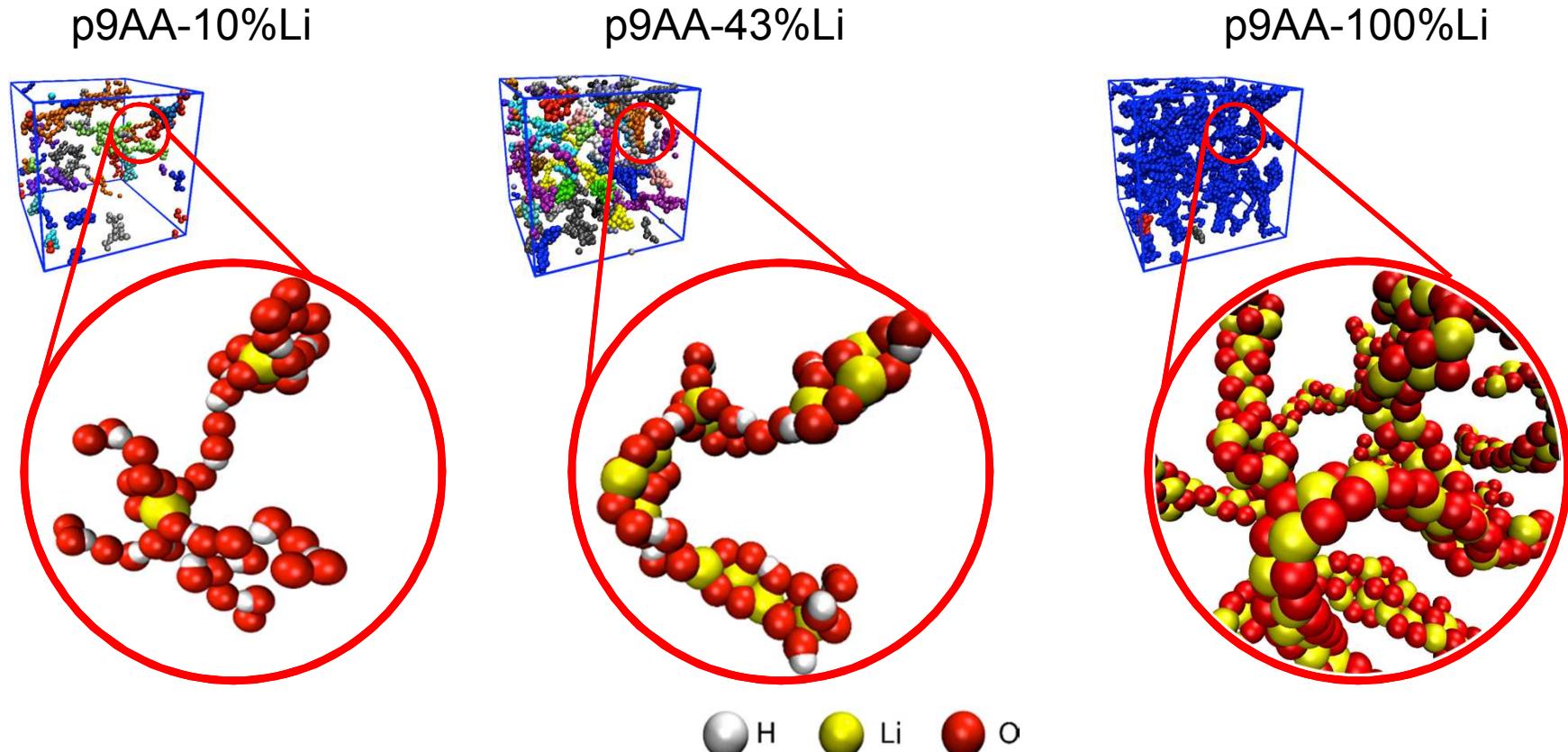


TYPE I
(compact, isolated)

coloring by cluster

Bolintineanu et al, *ACS Macro Lett*, 2013

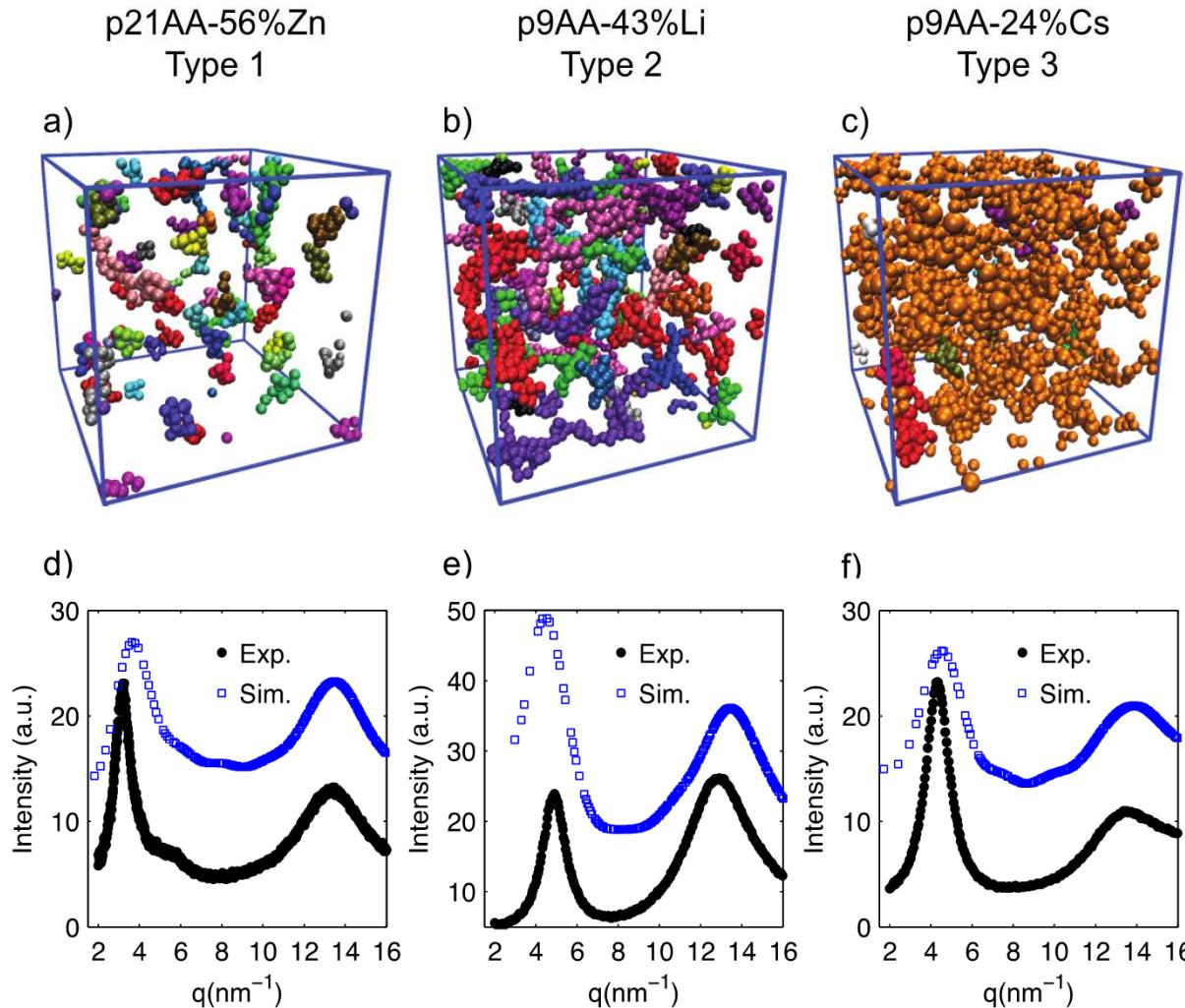
Closer look at aggregates



Two mechanisms of aggregate formation:

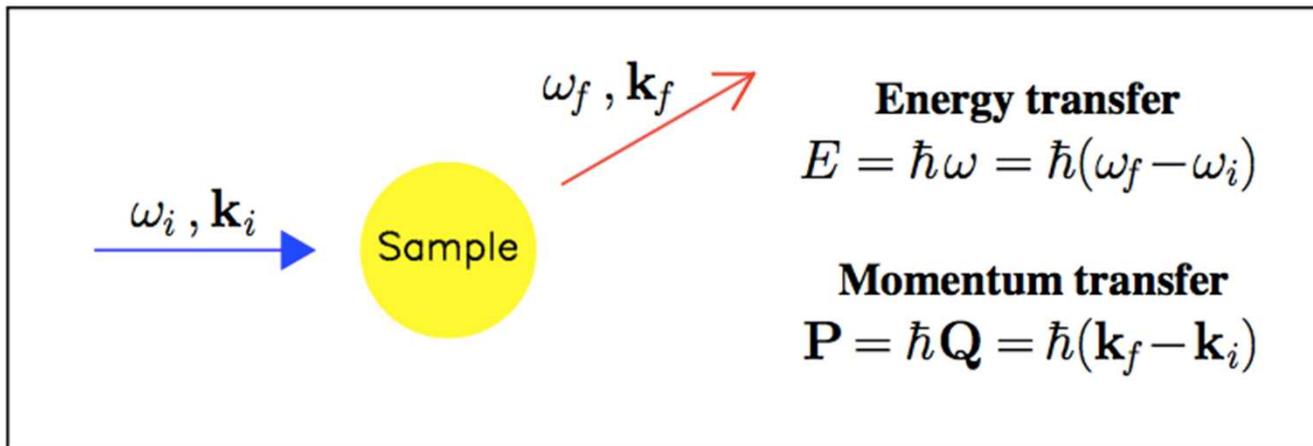
1. Counterion-oxygen association → dominant at **moderate to high** neutralization
2. Hydrogen-bonded networks → dominant at **low** neutralization

Comparison to X-ray Scattering



Buitrago, C. F. et al. *Macromolecules* **48**, 1210–1220 (2015).

Quasi-Elastic Neutron Scattering



incoherent, inelastic: sensitive to self-motion of hydrogens
scattering intensity proportional to $I(Q, \omega)$

$$S(Q, t) = \frac{\int I_{exp}(Q, \omega) e^{i\omega t} d\omega}{\int R(Q, \omega) e^{i\omega t} d\omega}$$

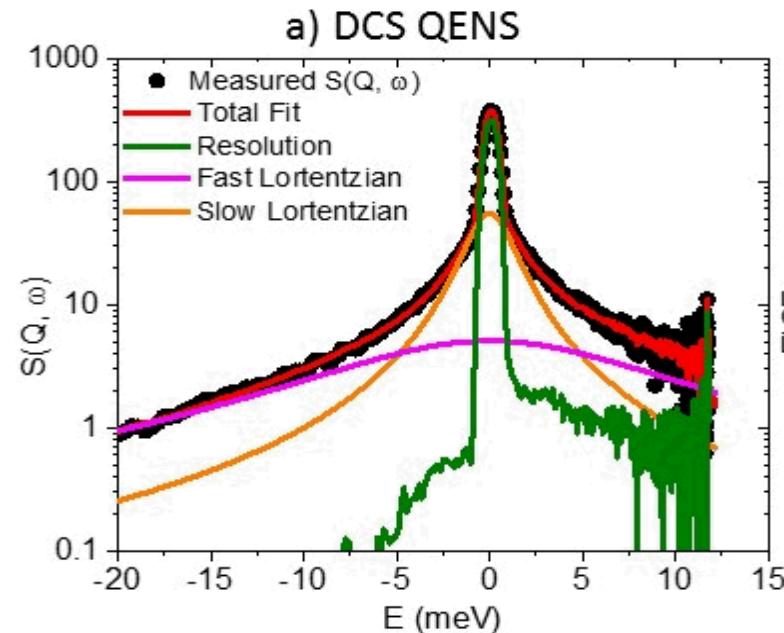
$G(r, t)$: probability that atom is at r at time t , given it was at 0 at time $t=0$

$$S(Q, t) = \int G(r, t) \frac{r \sin(Qr)}{Q} dr$$

Dynamics: QENS and MD

QENS

DCS instrument at NIST



MD simulations

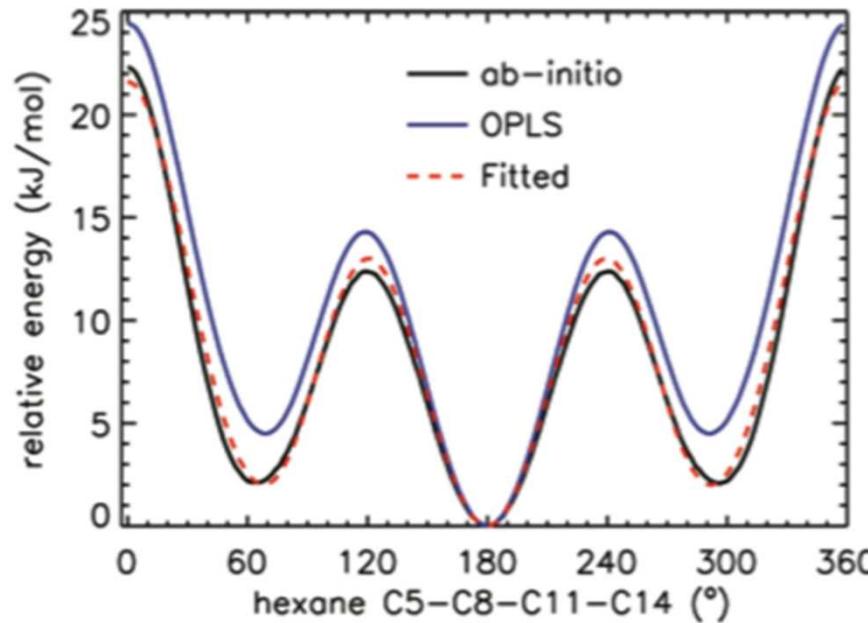
new simulations: all chains similar length (≈ 84 carbons/backbone)

calculate self-part of van Hove correlation function $G_s(r,t)$ for hydrogens
exclude chain ends

Force Field

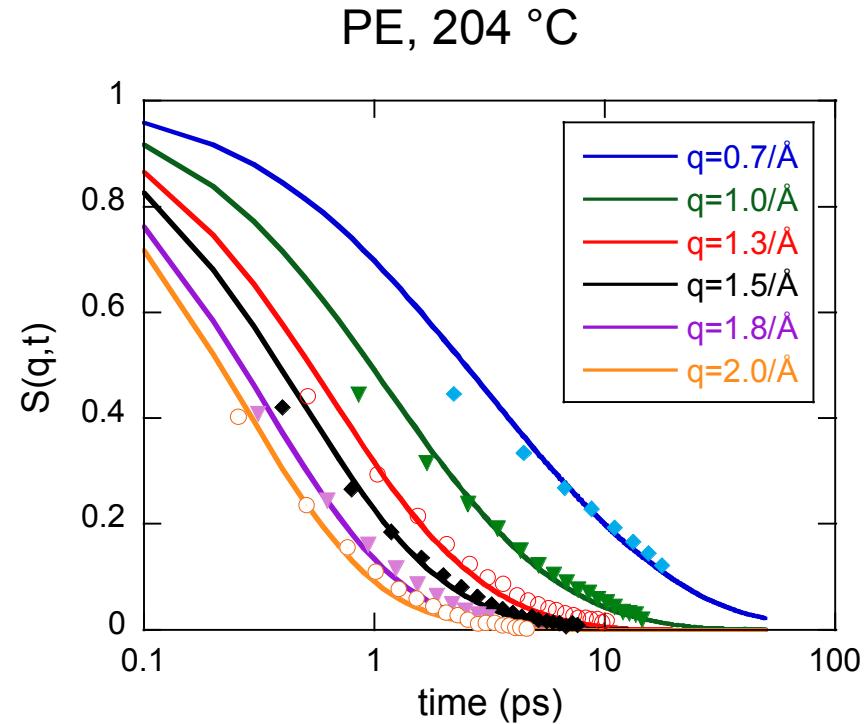
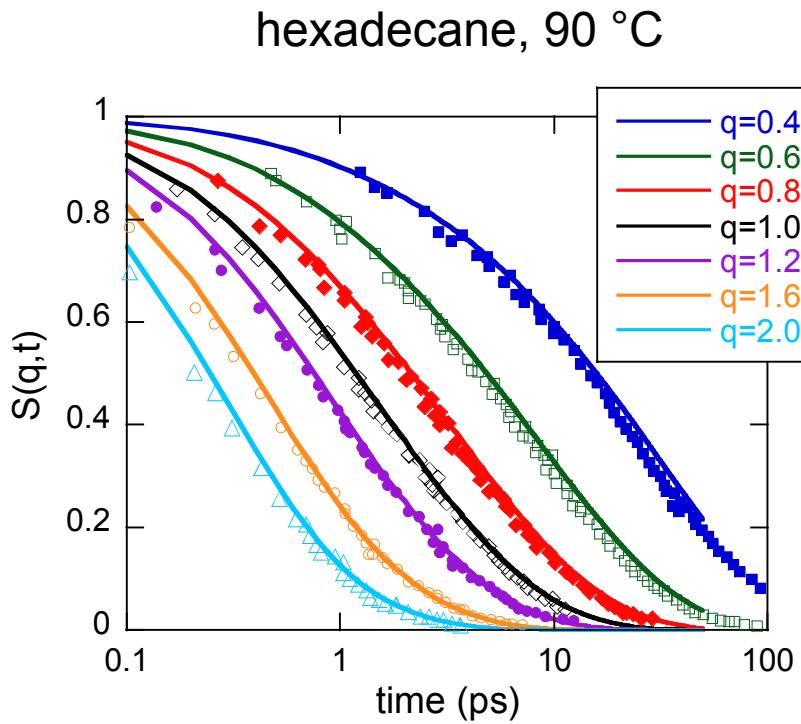
OPLS-AA: PE crystallizes at 150° C! ($T_m \approx 130$ °C)

L-OPLS: newly parameterized for long hydrocarbons



- correct gel-to-liquid transition temp in pentadecane
- improved viscosity, diffusion coefficients

Test of L-OPLS Force Field

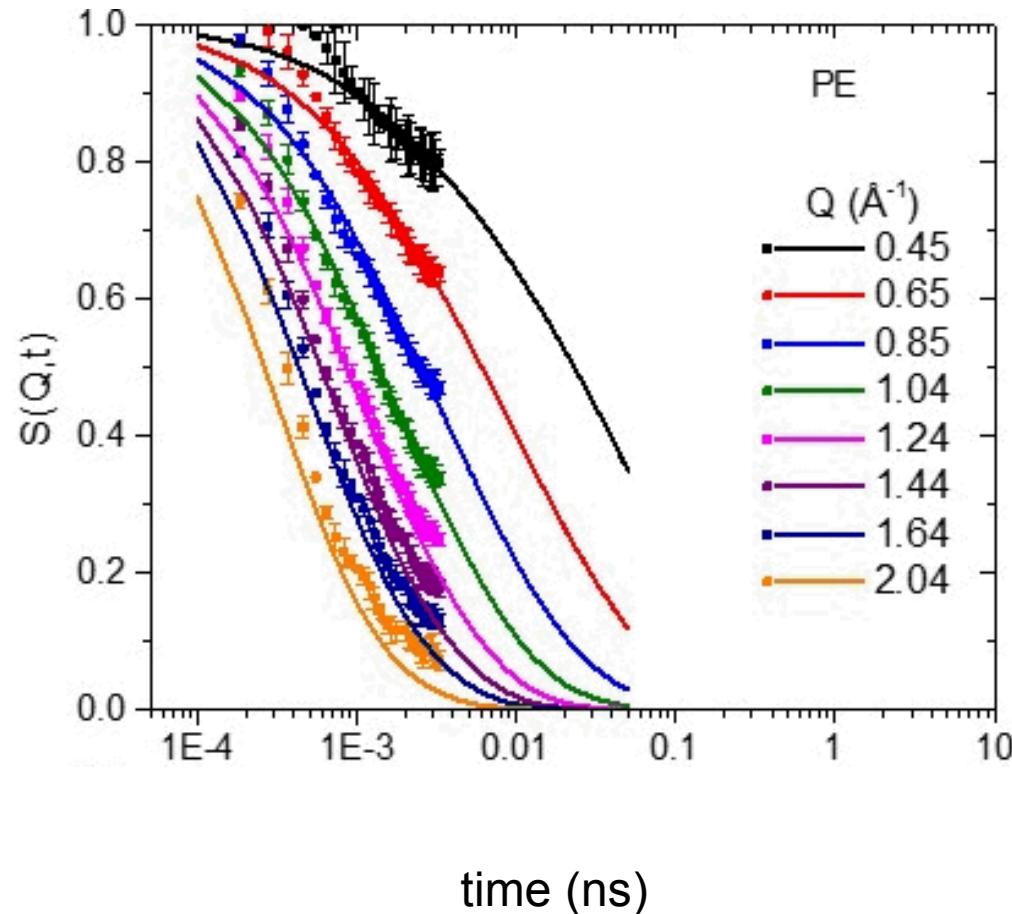


Morhenn, H., Busch, S. & Unruh, T. *J Phys-Condens Mat* **24**, 375108 (2012).

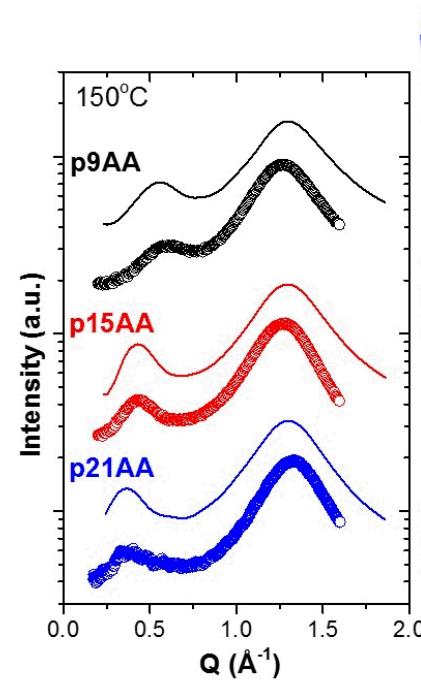
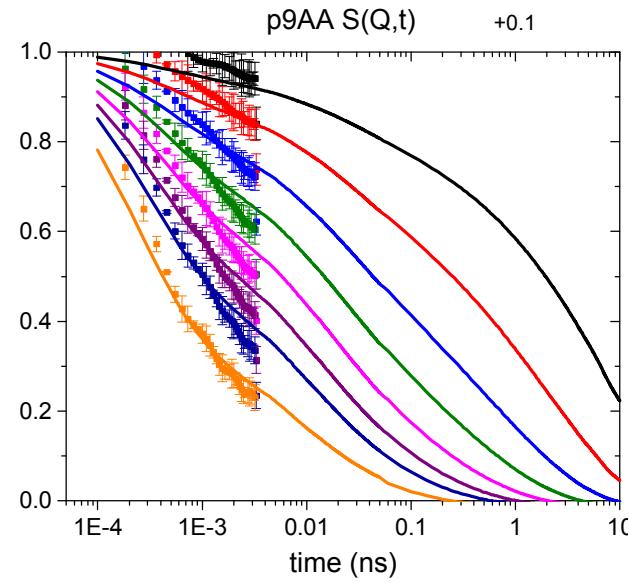
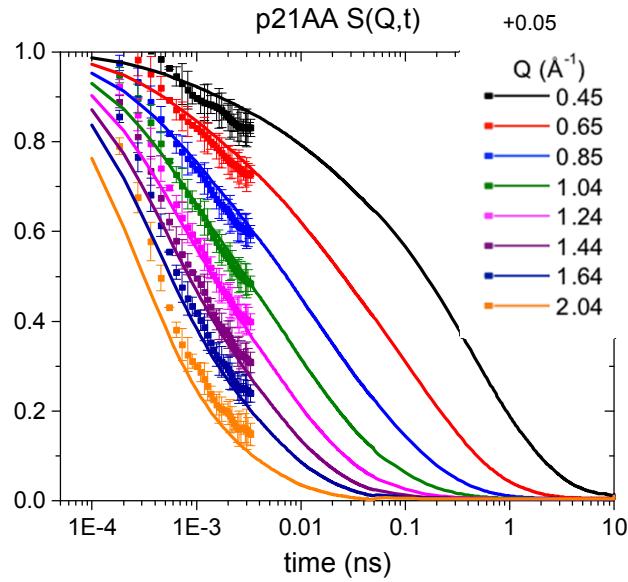
Arbe, A. & Colmenero, J. *Phys Rev E* **80**, (2009).

Our data: PE

ADMET PE, $M_n = 44.9$ kg/mol
 MD simulations, 84 C's, 1.2 kg/mol



Acid Copolymers



excellent agreement between QENS and MD

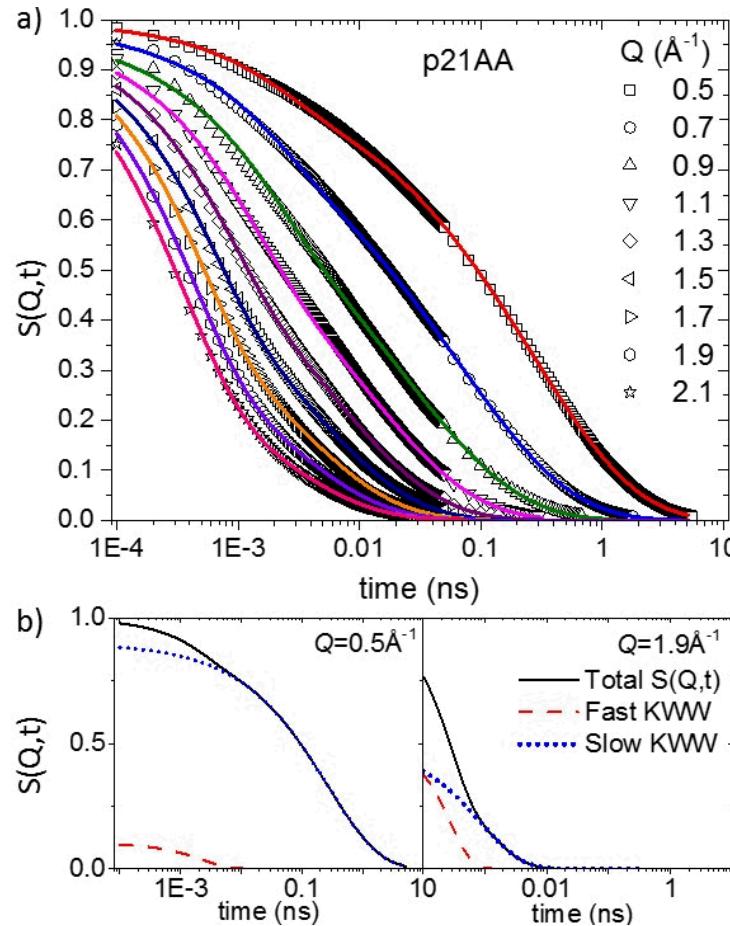
relevant length scales:

amorphous halo: $Q \approx 1.35 \text{\AA}^{-1}$

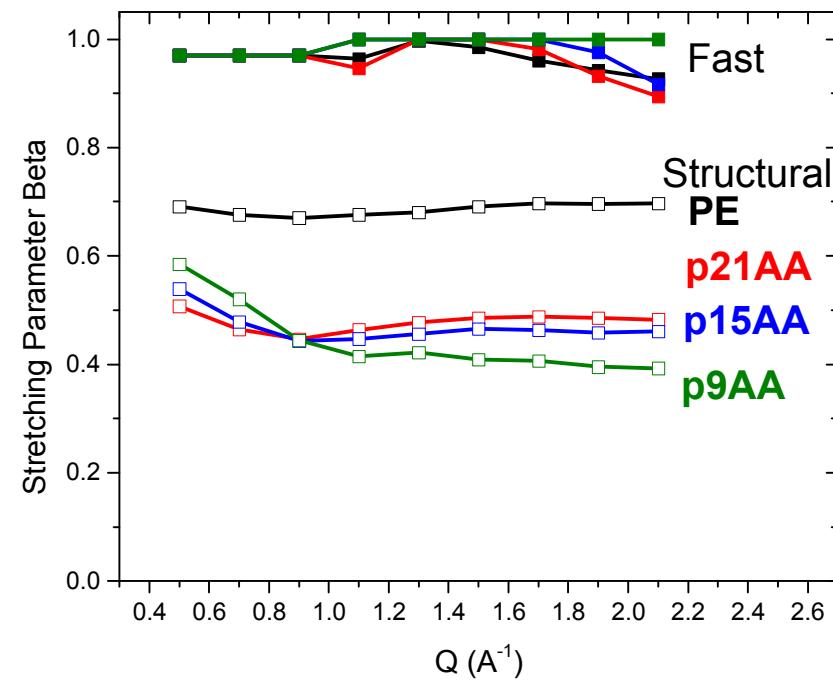
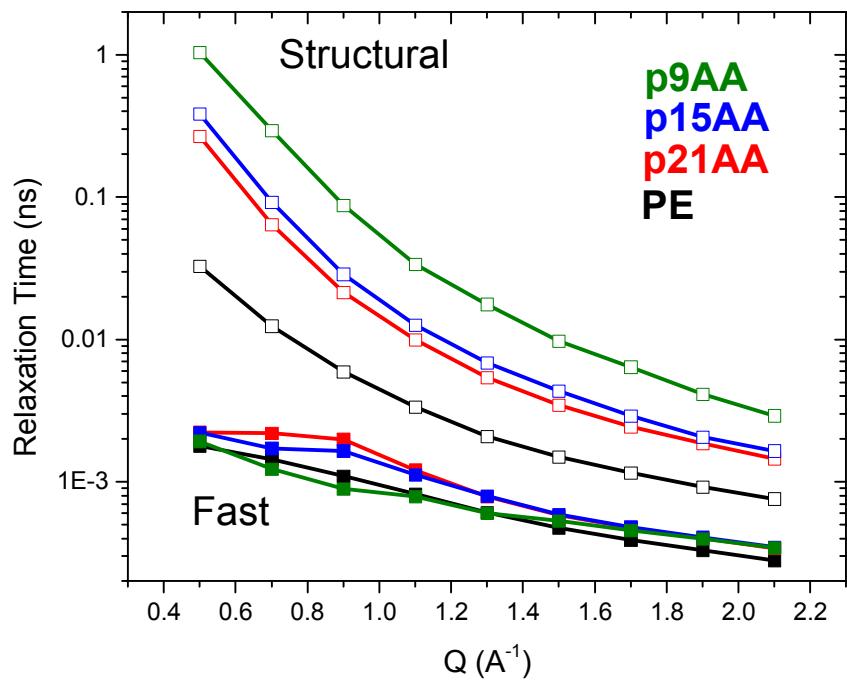
ionomer peak: $Q \approx 0.3 – 0.6 \text{\AA}^{-1}$

Fit $S(Q,t)$ to Two KWW Functions

$$S(Q,t) = \phi_{slow} e^{-\left(\frac{t}{\tau_{slow}}\right)^{\beta_{slow}}} + (1 - \phi_{slow}) e^{-\left(\frac{t}{\tau_{fast}}\right)^{\beta_{fast}}}$$

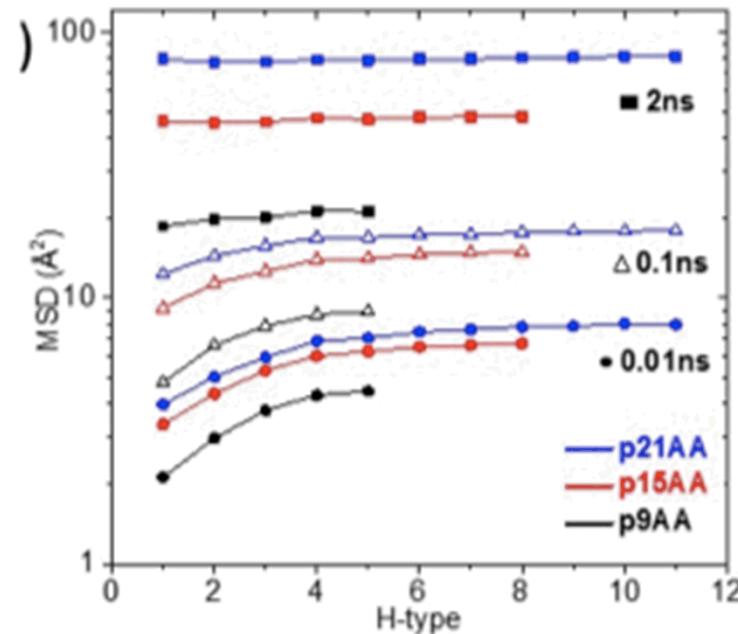
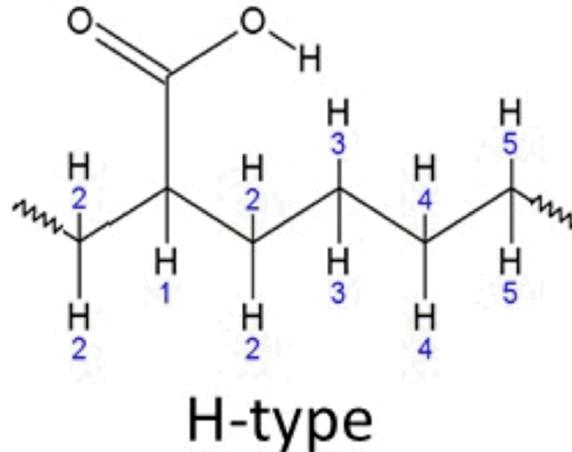


Dynamics from KWW



fast process: β -process, local motions
slow process: structural (segmental) motion

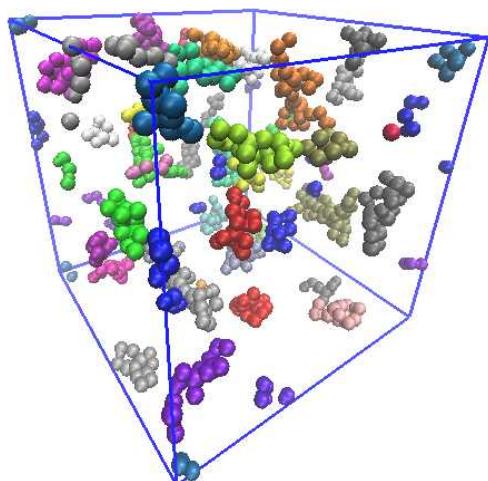
Local Dynamics



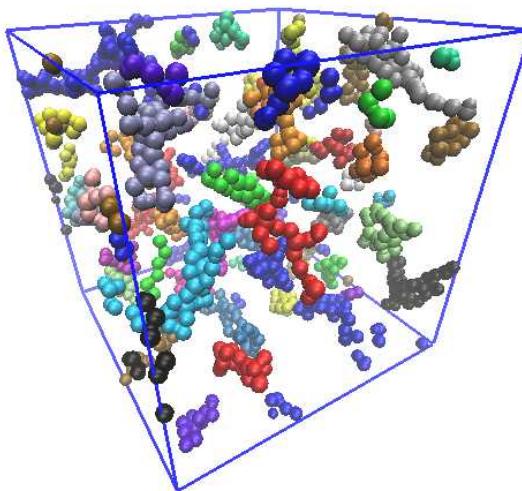
short times: H1 motion much slower than middle of chain
 long times: aggregates rearrange, all H motion similar

Li ionomers: L-OPLS

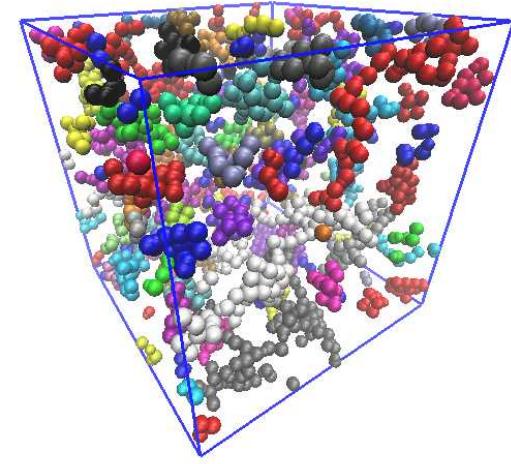
p21-37%Li



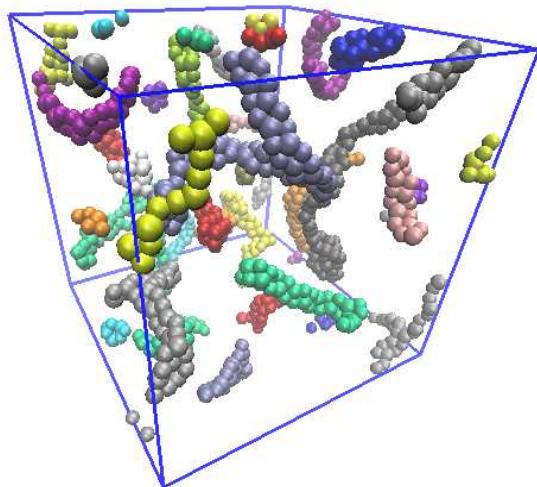
p15-38%Li



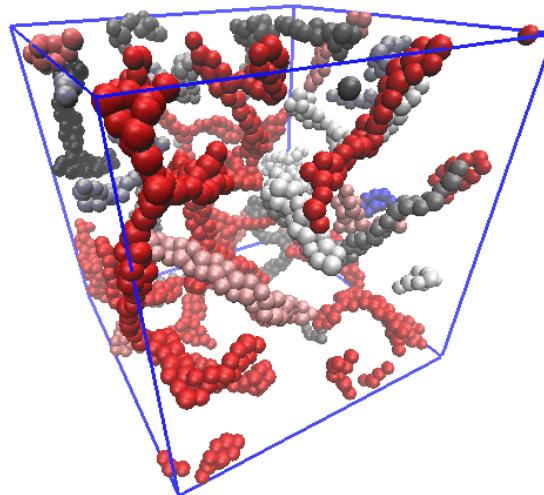
p9-20%Li



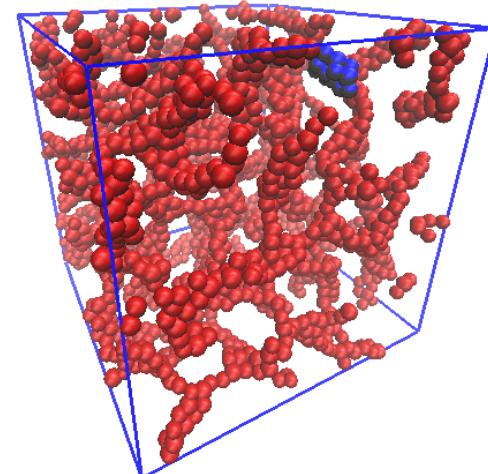
p21-100%Li



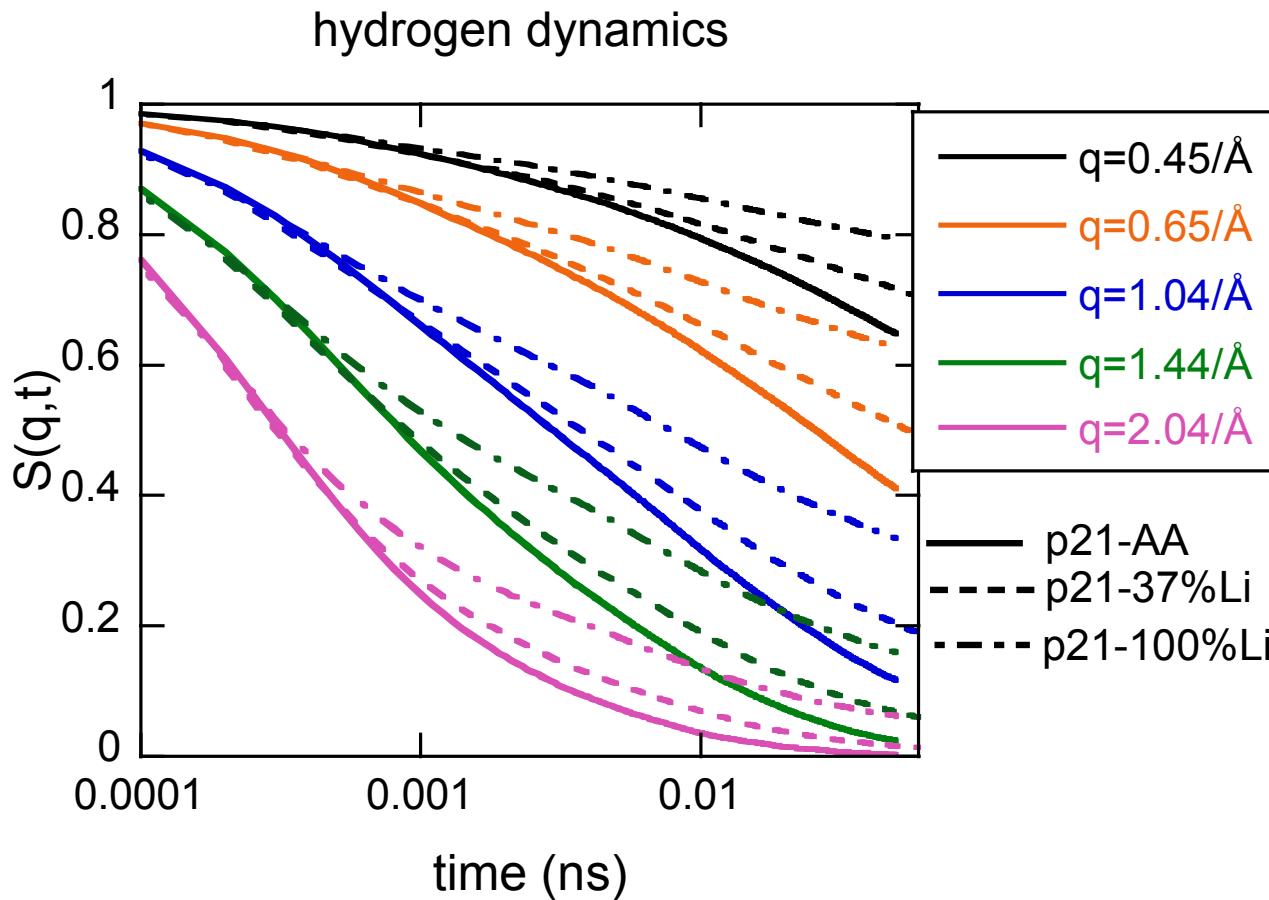
p15-100%Li



p9-100%Li



Early-time dynamics in p21-x%Li



ionic aggregates further slow polymer motion

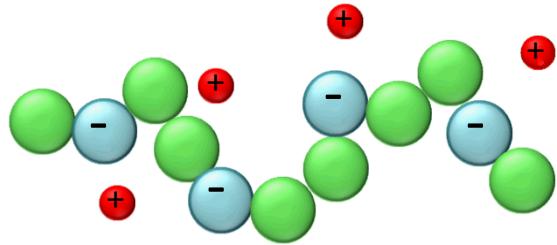
Longer times with MD

ion dynamics require longer simulations

- compare to QENS
- look at ion transport mechanisms

for better statistics at long times: coarse-grained simulations

Ions in the polymer backbone:
“ionenes”

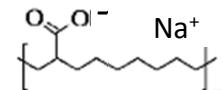
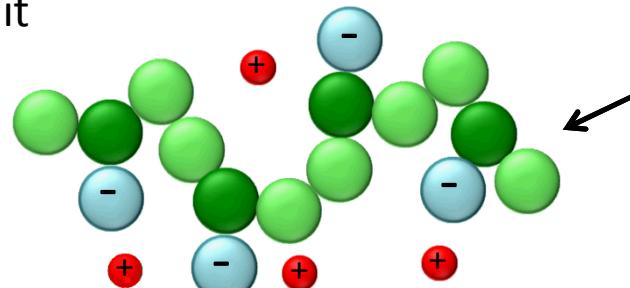


$N_{bb} = 3, 5, 7, 9 (11)$
800 polymers
100% neutralization

Ions pendant to the backbone:
“pendants”

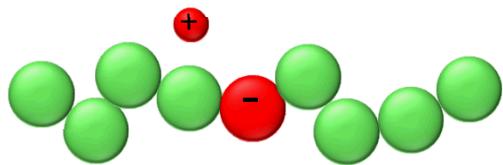
backbone beads
per repeat unit

$$N_{bb} = 3$$



bulk dielectric constant = 4
counterion size = $\frac{1}{2}\sigma$
Bjerrum length = 35.7σ

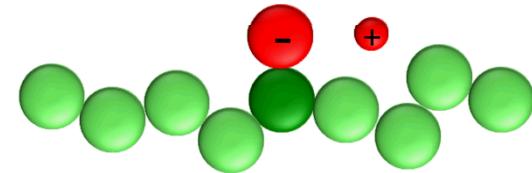
Aggregate Morphology: Architecture Matters



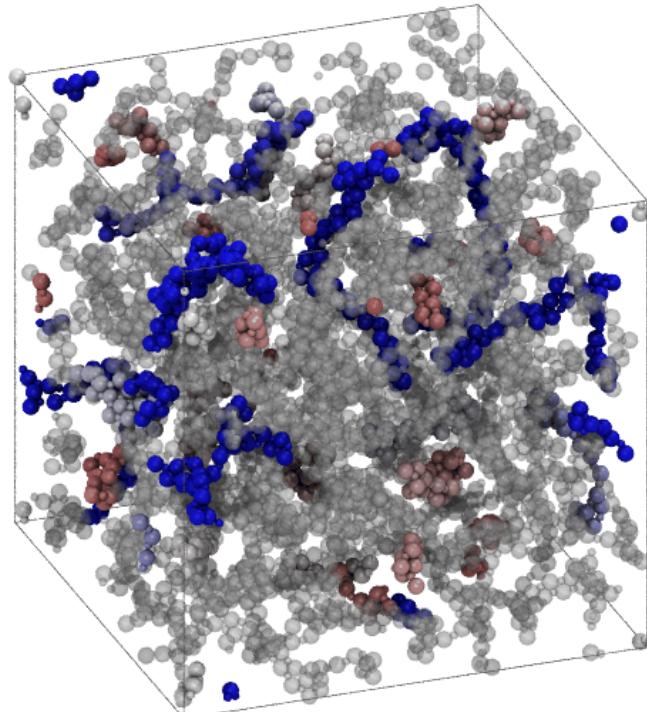
Ionenes: percolated

$$N_{bb} = 9$$

$$\epsilon_r = 4$$

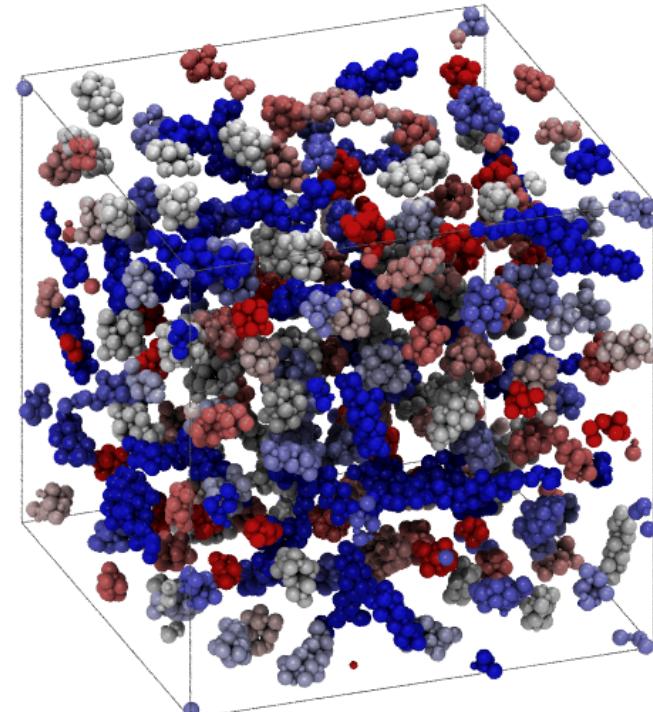


Pendants: not percolated



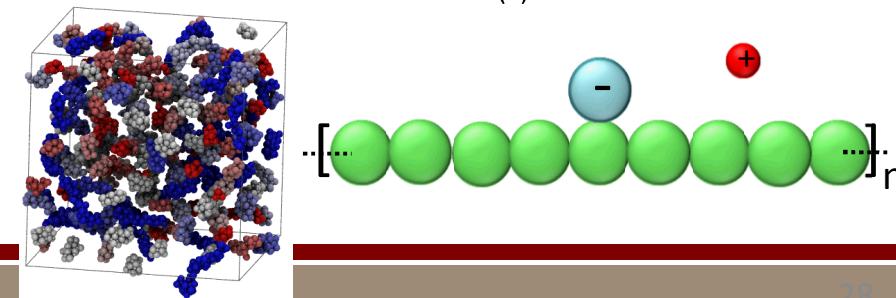
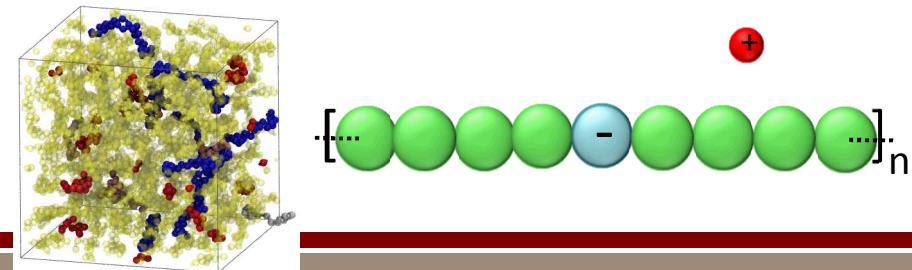
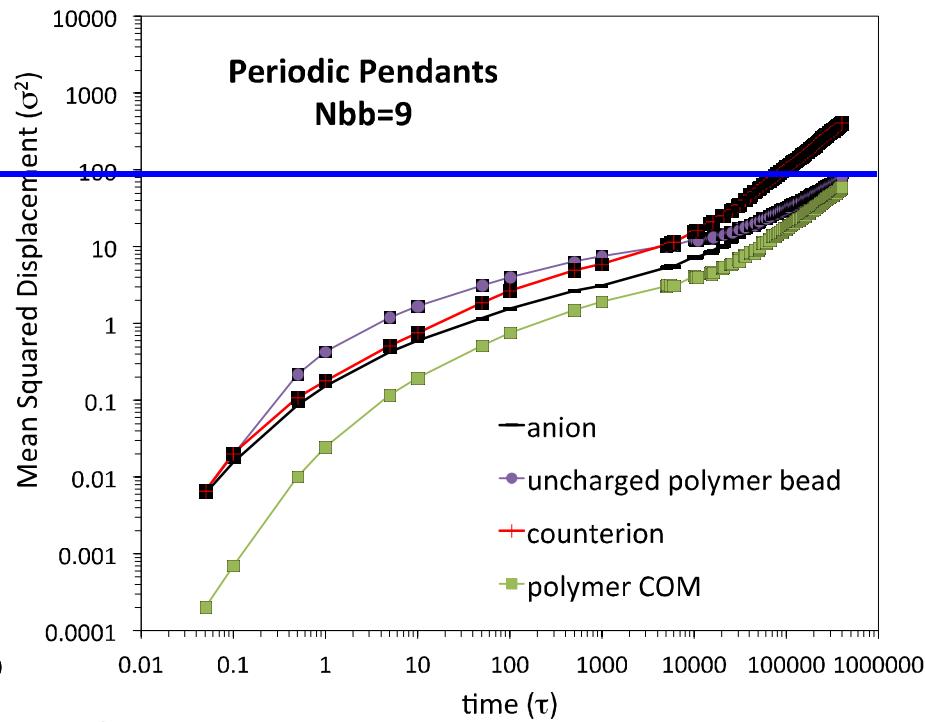
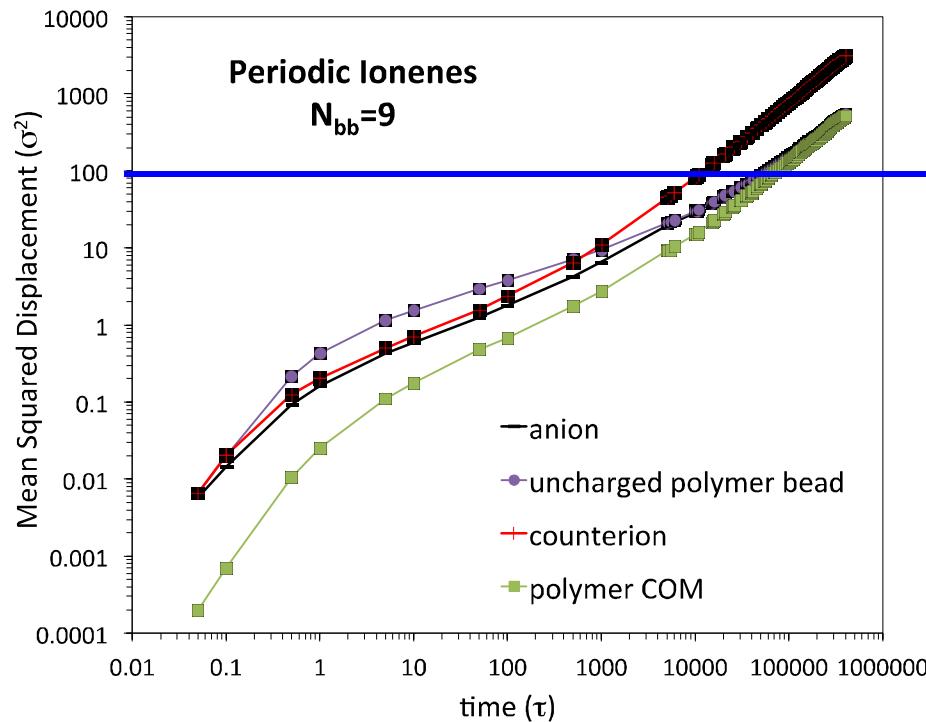
Small clusters  Large clusters

Only charged beads shown



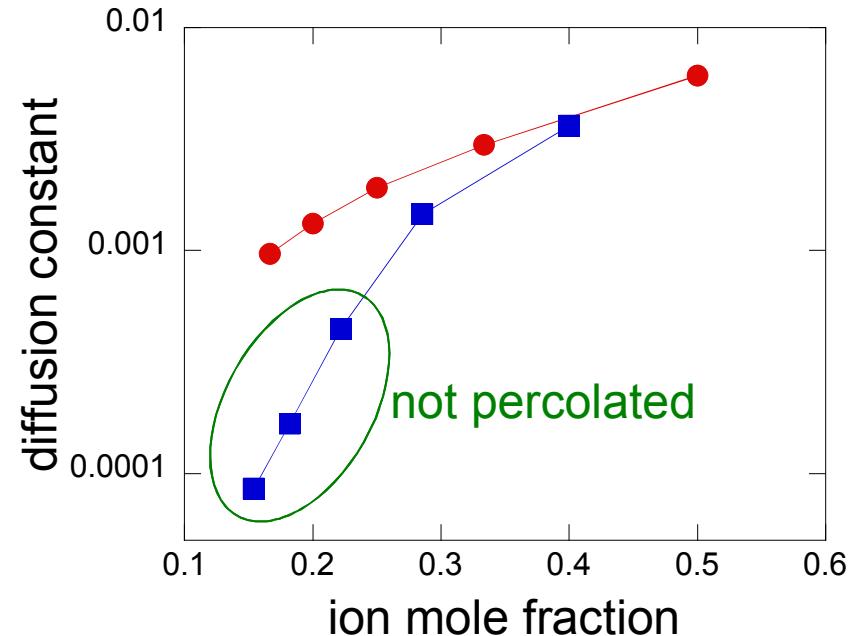
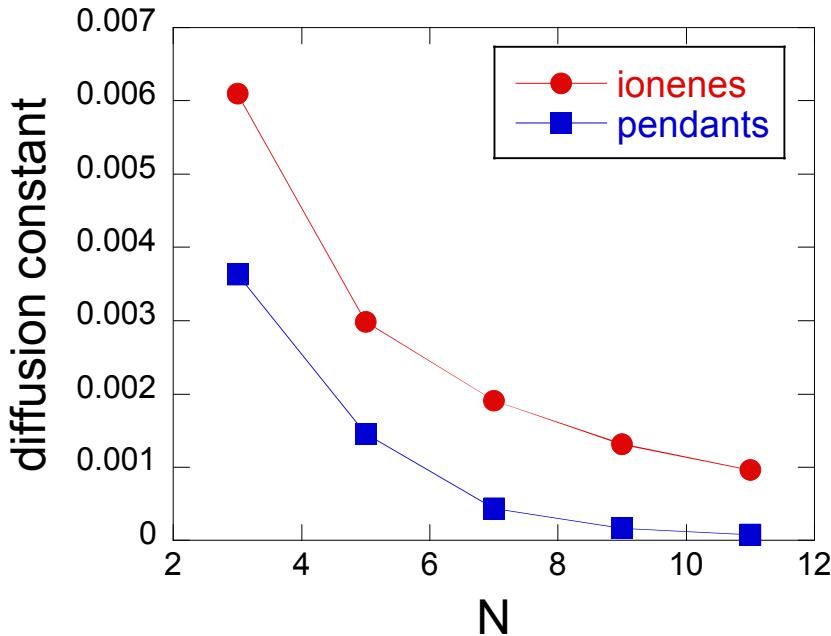
Mean Squared Displacements

- Ionenes, pendants similar at short times
 - Pendants slower but qualitatively similar at long times



Counterion Diffusion Constants

$$\langle \mathbf{r}^2(t) \rangle = 6Dt$$



- Ionenes have faster diffusion than pendants
- Percolated systems have faster diffusion

MSDs in an External E Field

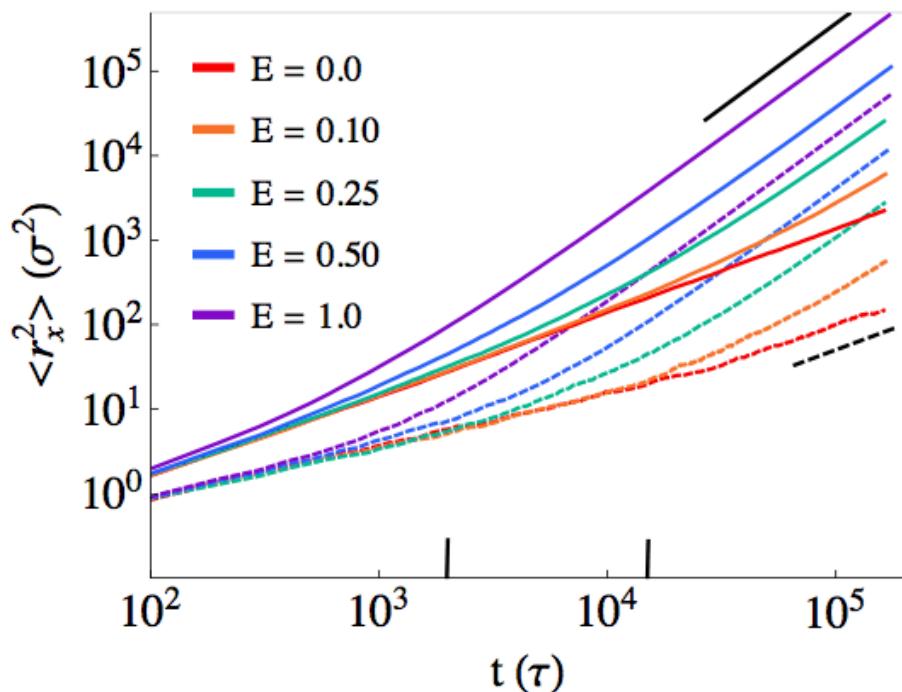
diffusion

$$\langle r_x^2 \rangle \sim D t$$

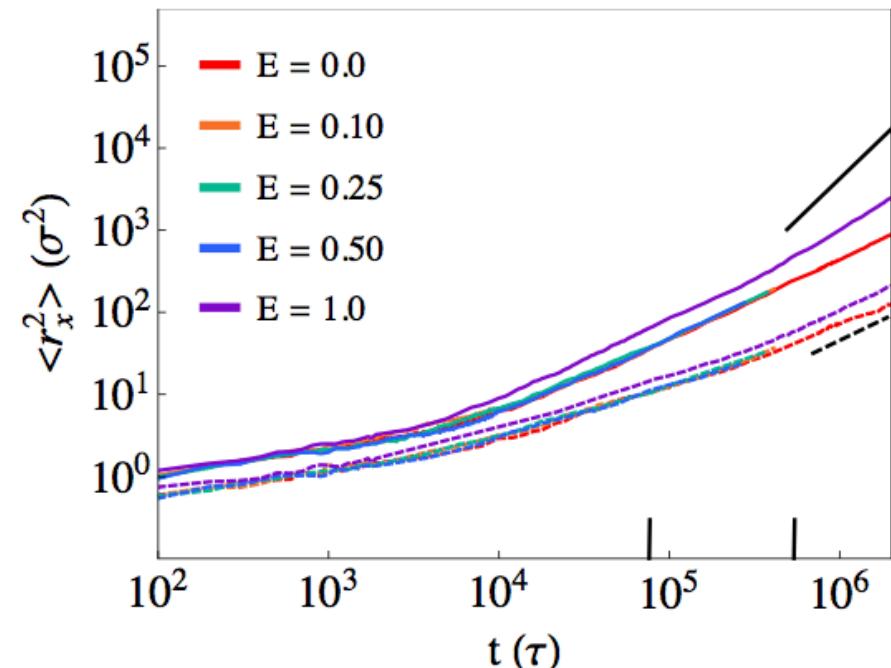
drift in the E field

$$\langle r_x(t)^2 \rangle_E - \langle r_x(t)^2 \rangle_0 = \langle v_x^2 \rangle t^2$$

ionene N = 3



pendant N = 9

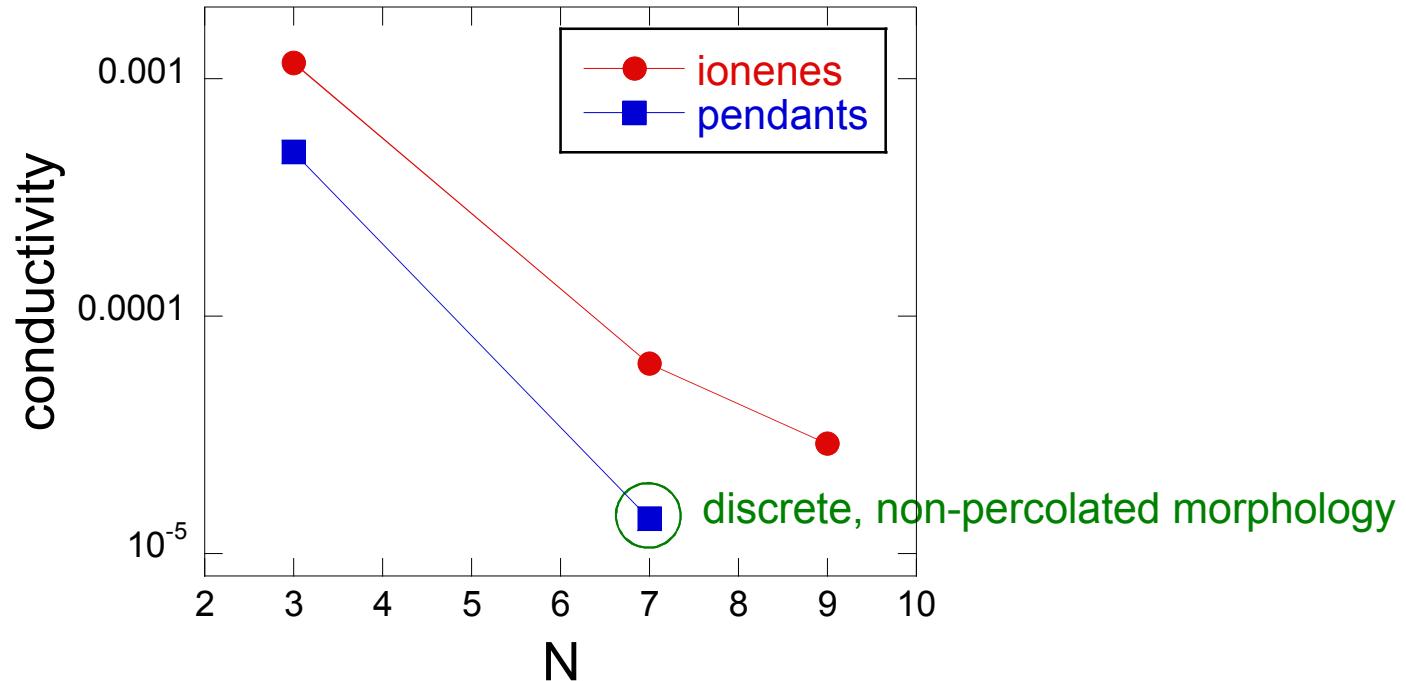


dashed = anion, solid = cation

Conductivity

$$\mu_i = \langle v_{x,i} \rangle / E$$

$$\lambda = \rho e(\mu_+ - \mu_-)$$



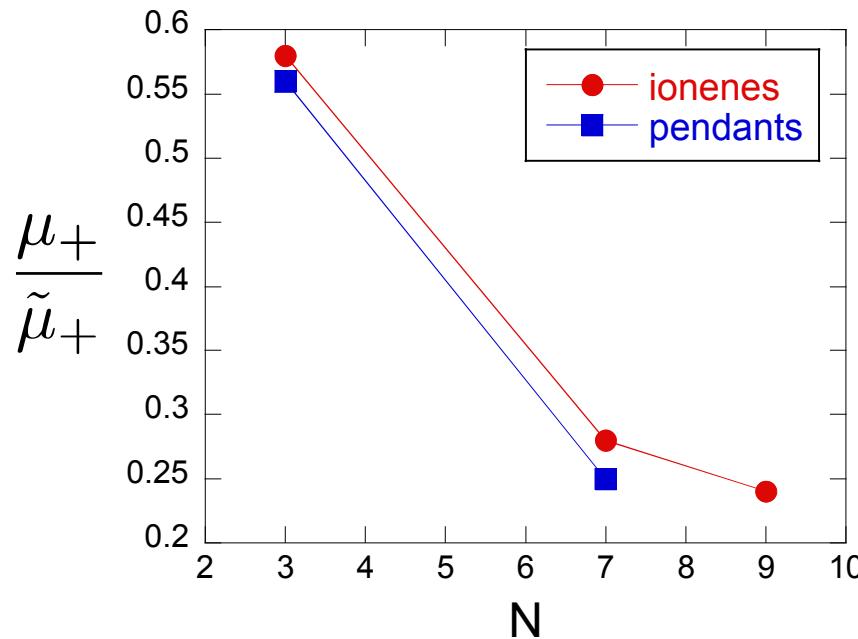
- conductivity decreases with decreasing ion concentration
- lowest for non-percolated aggregate morphology

Ion motion is correlated

from non-equilibrium simulation in field: $\mu_i = \langle v_{x,i} \rangle / E$

from equilibrium Einstein relation

$$\tilde{\mu}_i = zeD_i/kT$$

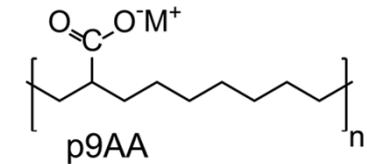


f factor < 1

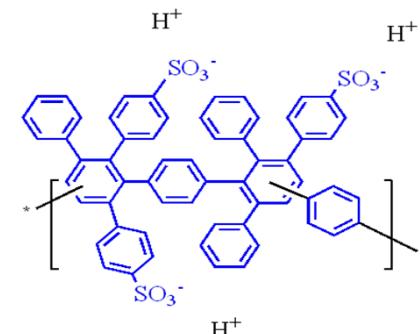
ionic aggregates slow conduction

Rest of the Talk

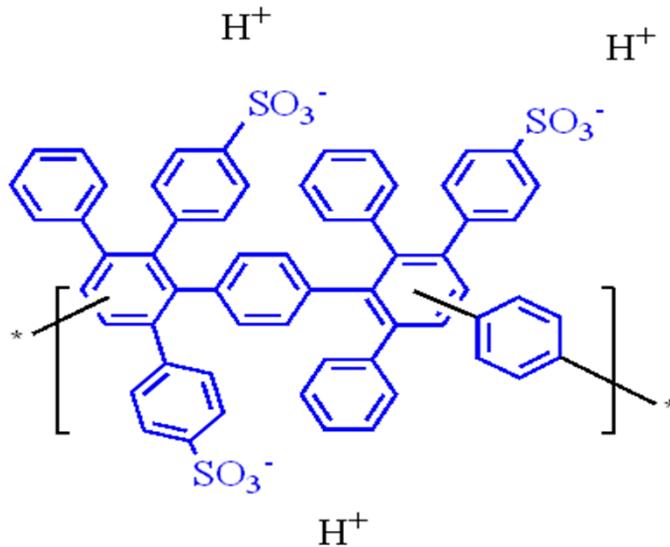
- melts of precise poly(ethylene-co-acrylic acid) (pAA)
 - atomistic simulations
 - morphology and comparison to X-ray
 - dynamics and comparison to QENS
 - coarse-grained simulations



- hydrated, sulfonated Diels-Alder polyphenylenes (SDAPP)
 - atomistic simulations

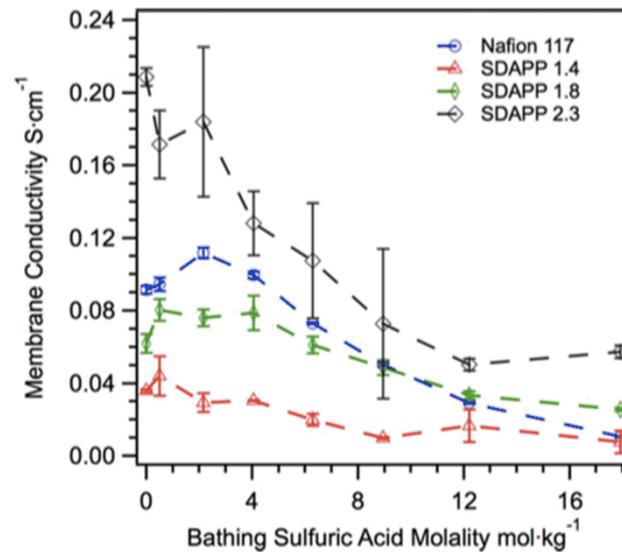
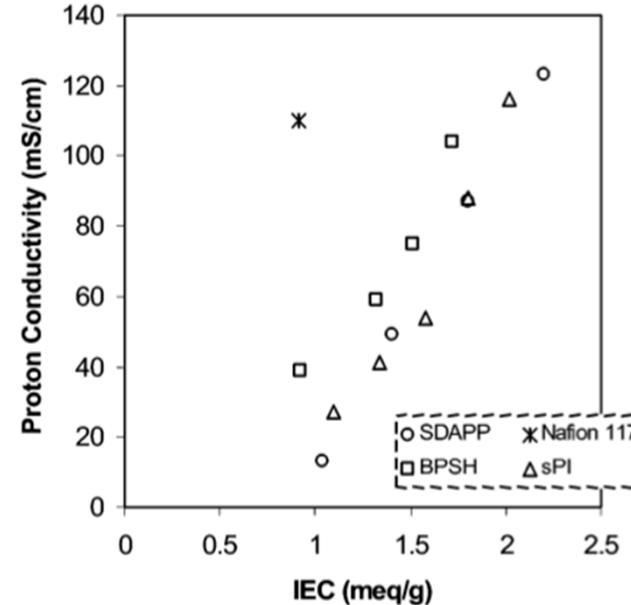


SDAPP Membranes

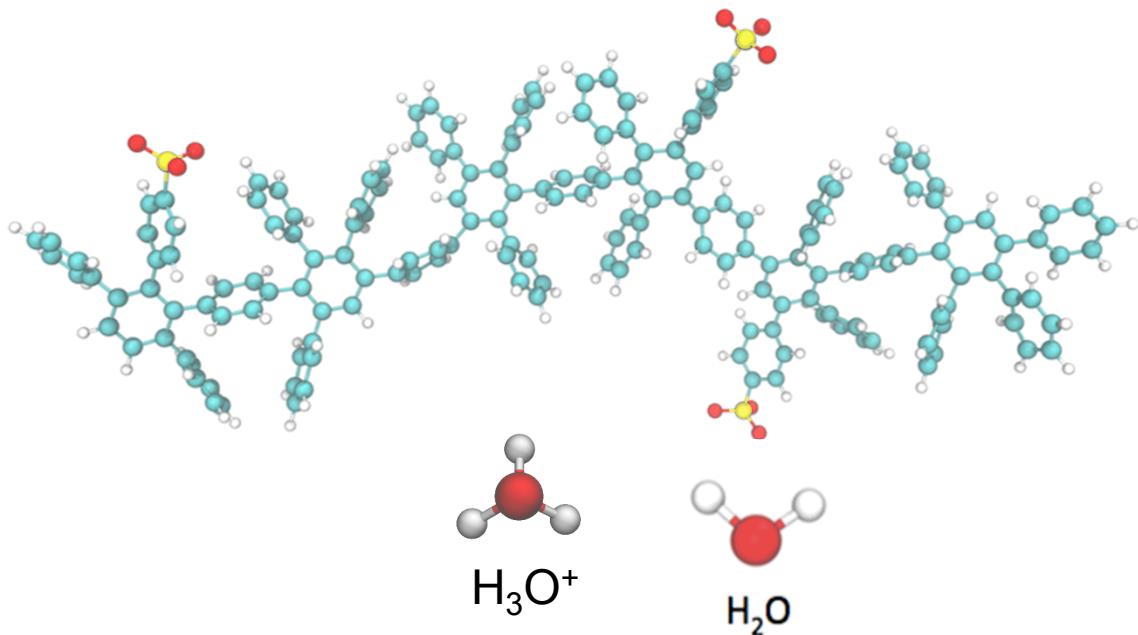


- high T_g
- high modulus
- high thermomechanical stability
- high conductivity

Fujimoto, C., Hickner, M., Cornelius, C. & Loy, D.
Macromolecules **38**, 5010–5016 (2005); Tang, Z. *et al.*, *J Electrochem Soc* **161**, A1860–A1868 (2014).



SDAPP Simulations

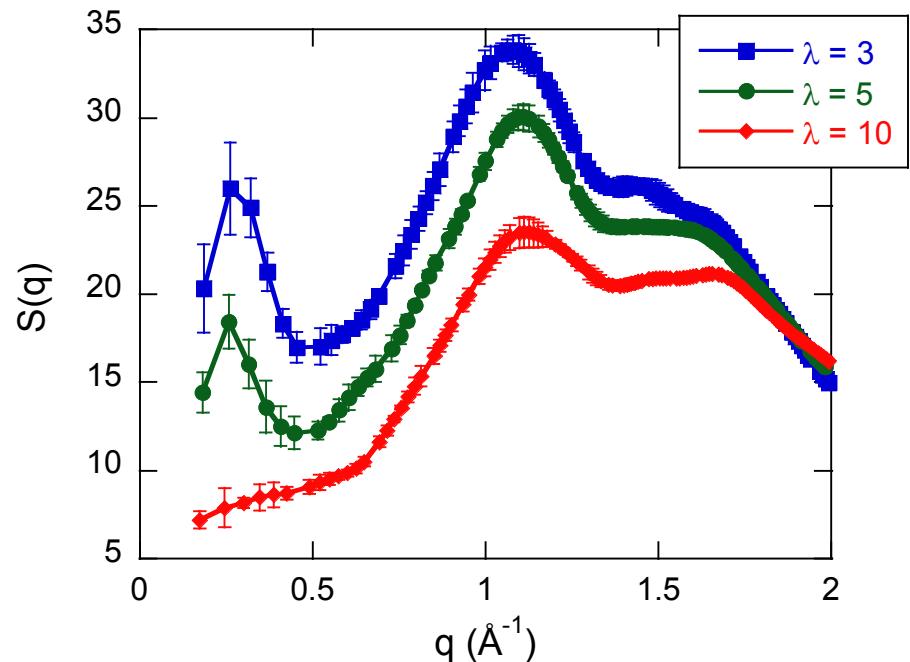
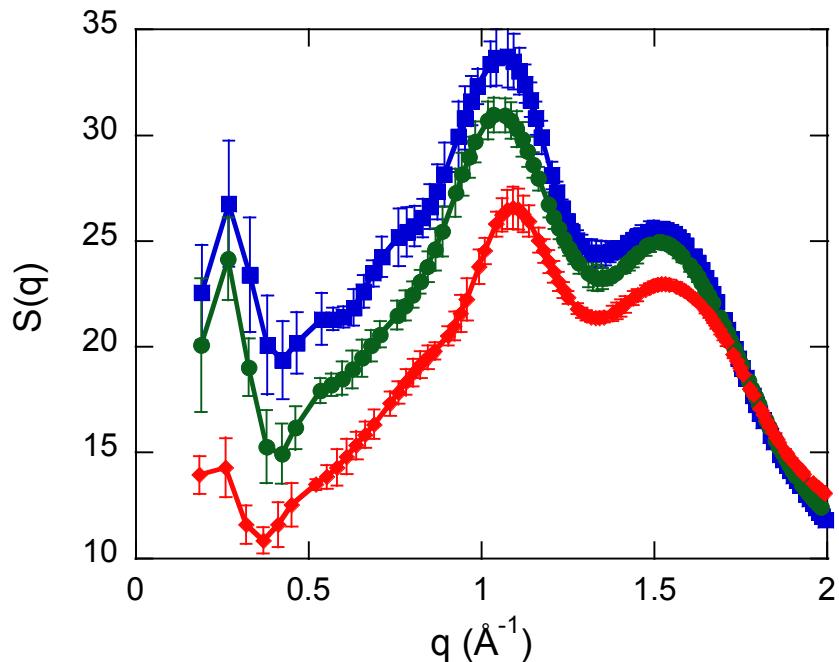


70 chains
3 monomers/chain

sulfonic acids/monomer = $S = 1, 2, 4$
waters/sulfonic acid = $\lambda = 3, 5, 10$

OPLS-AA, improvements for aromatics
TIP4P/2005 water model

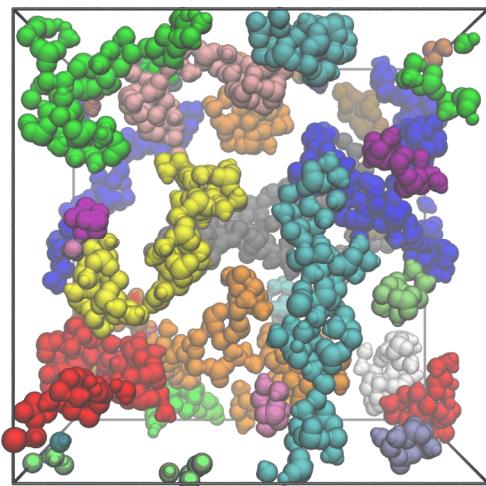
Static Structure Factors



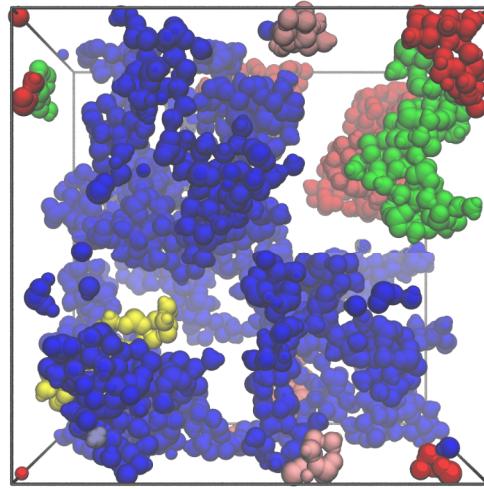
show an ionomer peak at low q
intensity decreases as add water

Cluster Morphologies

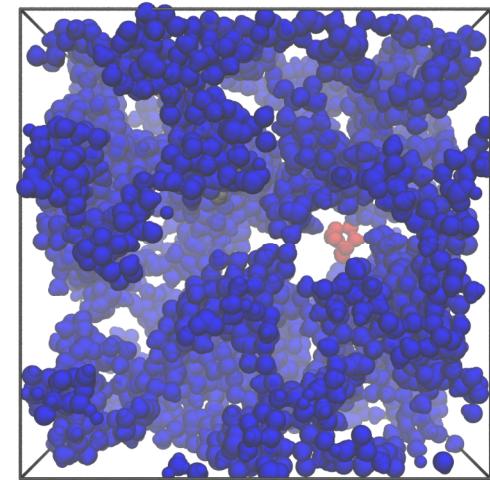
$S = 1$



$\lambda = 3$



$\lambda = 5$



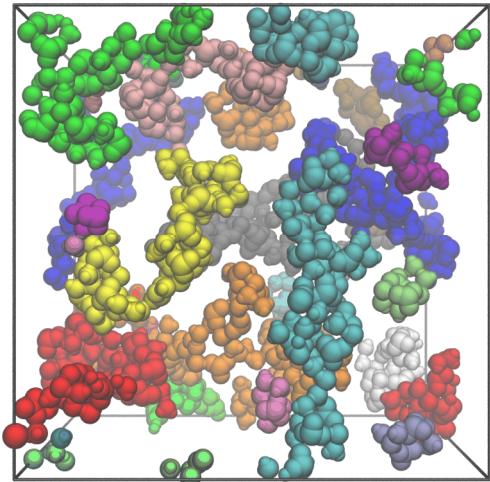
$\lambda = 10$



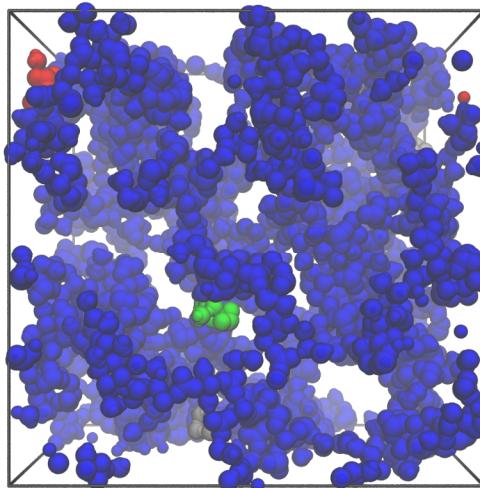
increasing water

Cluster Morphologies

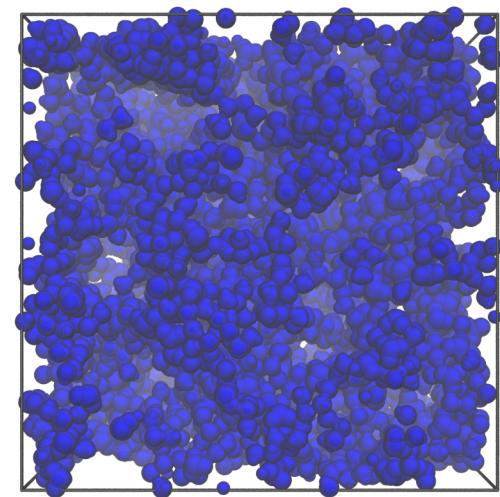
$\lambda = 3$



$S = 1$



$S = 2$



$S = 4$



increasing sulfonation level

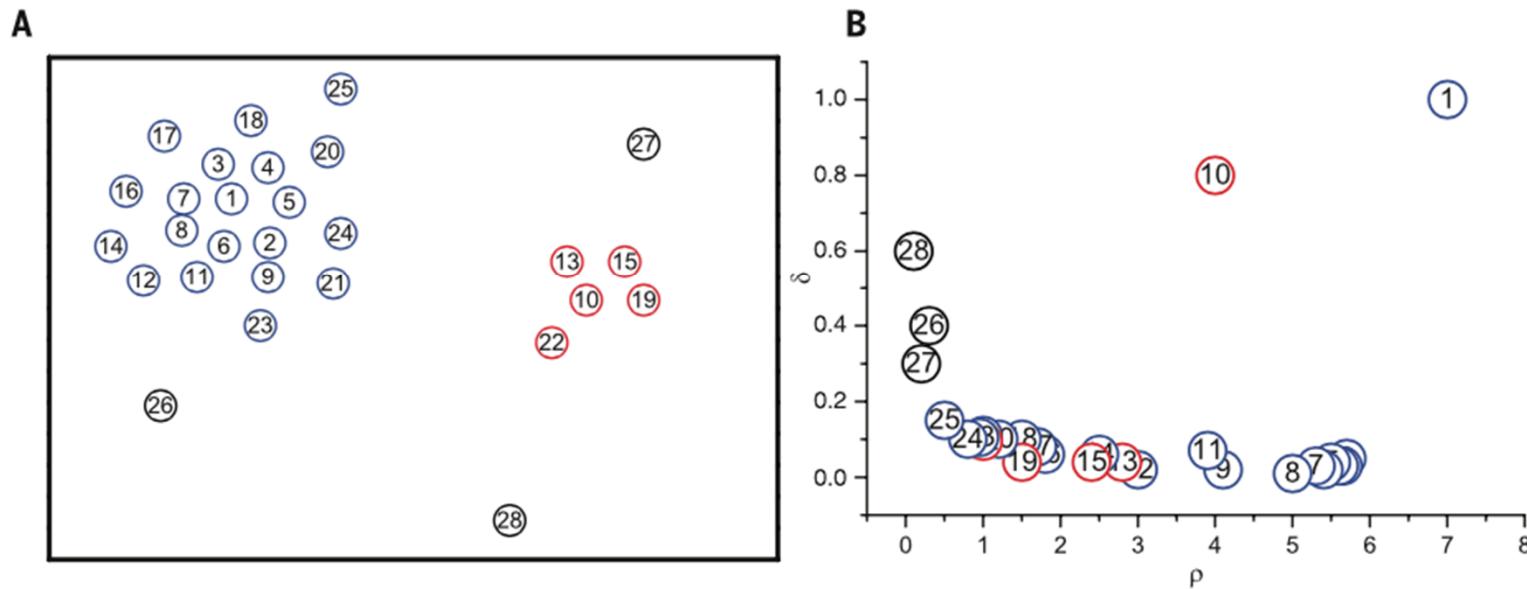
How do we better characterize percolated morphologies?

New Clustering Algorithm

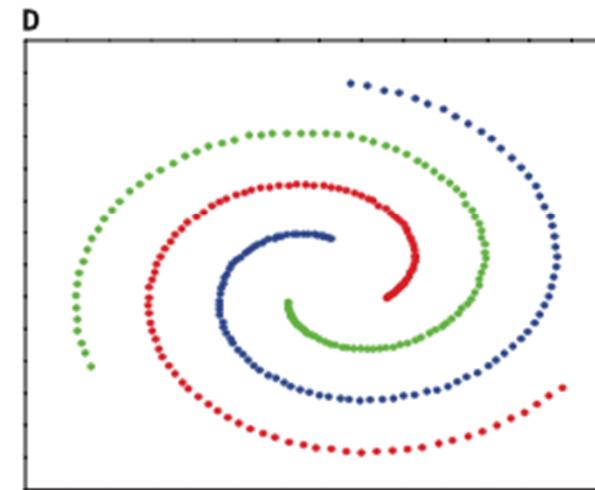
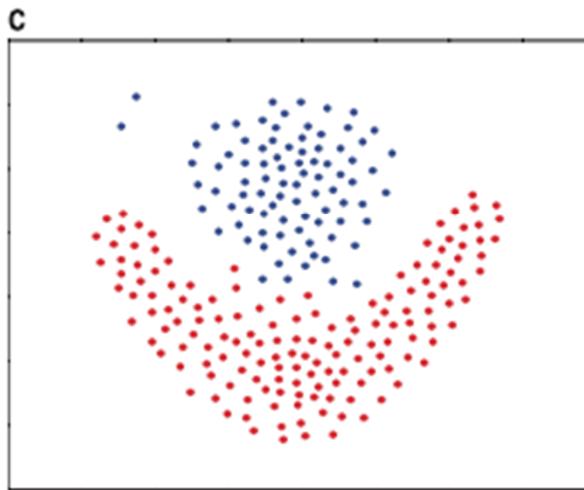
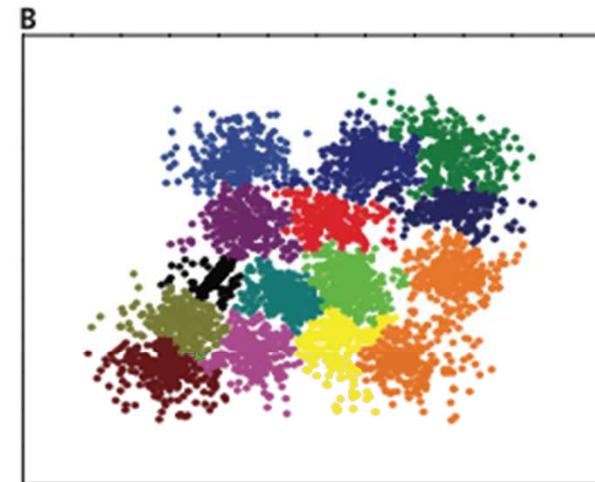
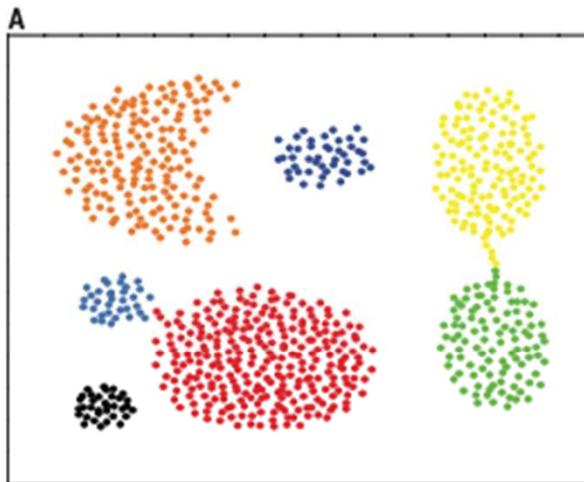
A. Rodriguez and A Laio, *Science* 344, 1492 (2014)

base on density as well as distance:

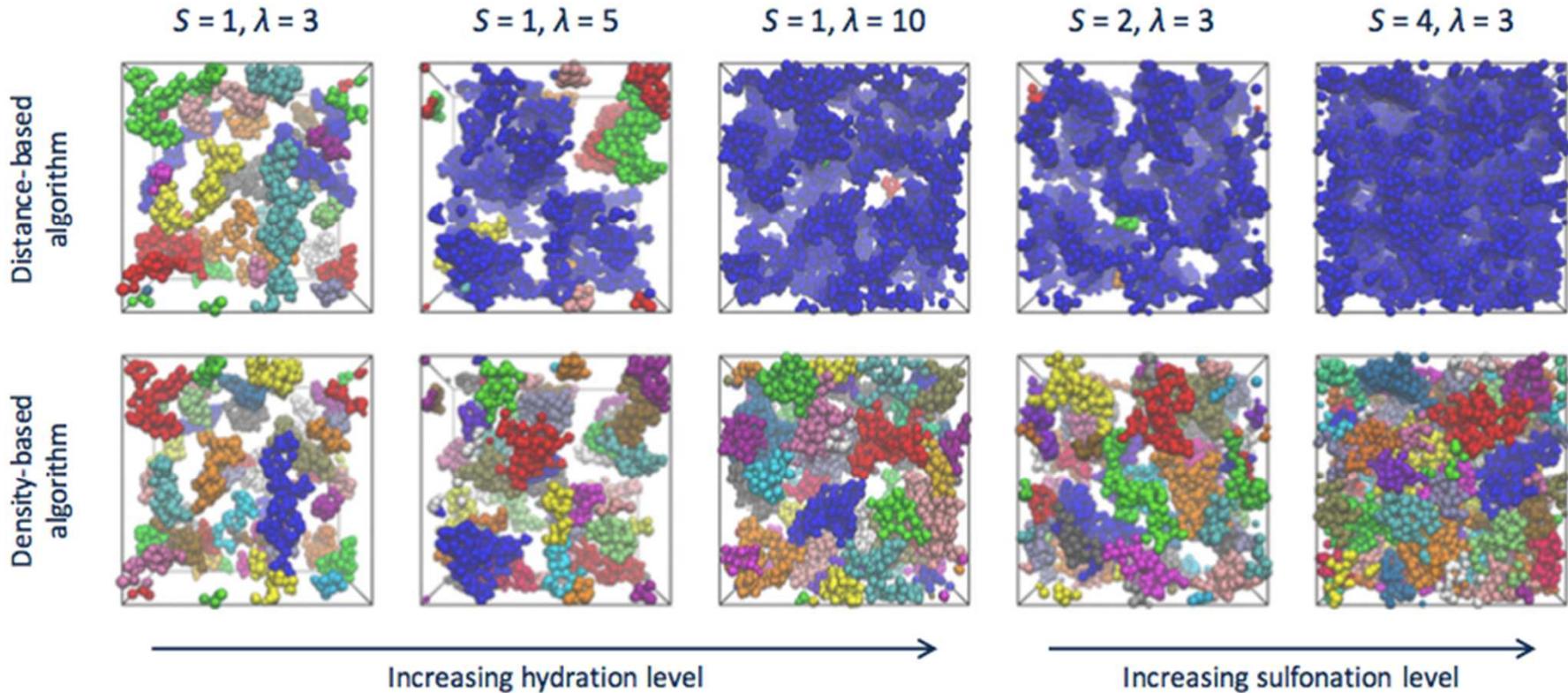
1. compute two quantities for every atom of interest:
 1. ρ : number of other atoms closer than cutoff
 2. δ : distance from the closest atom with a higher density ρ
2. define cluster centers as atoms with high ρ and high δ
3. outliers have low ρ and high δ
4. remaining atoms go in the same cluster as their nearest neighbor with higher ρ



Examples of Density-Based Clusters



SDAPP Clusters

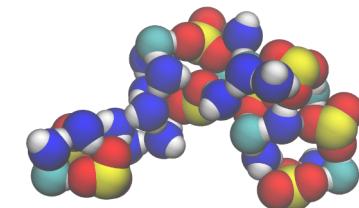
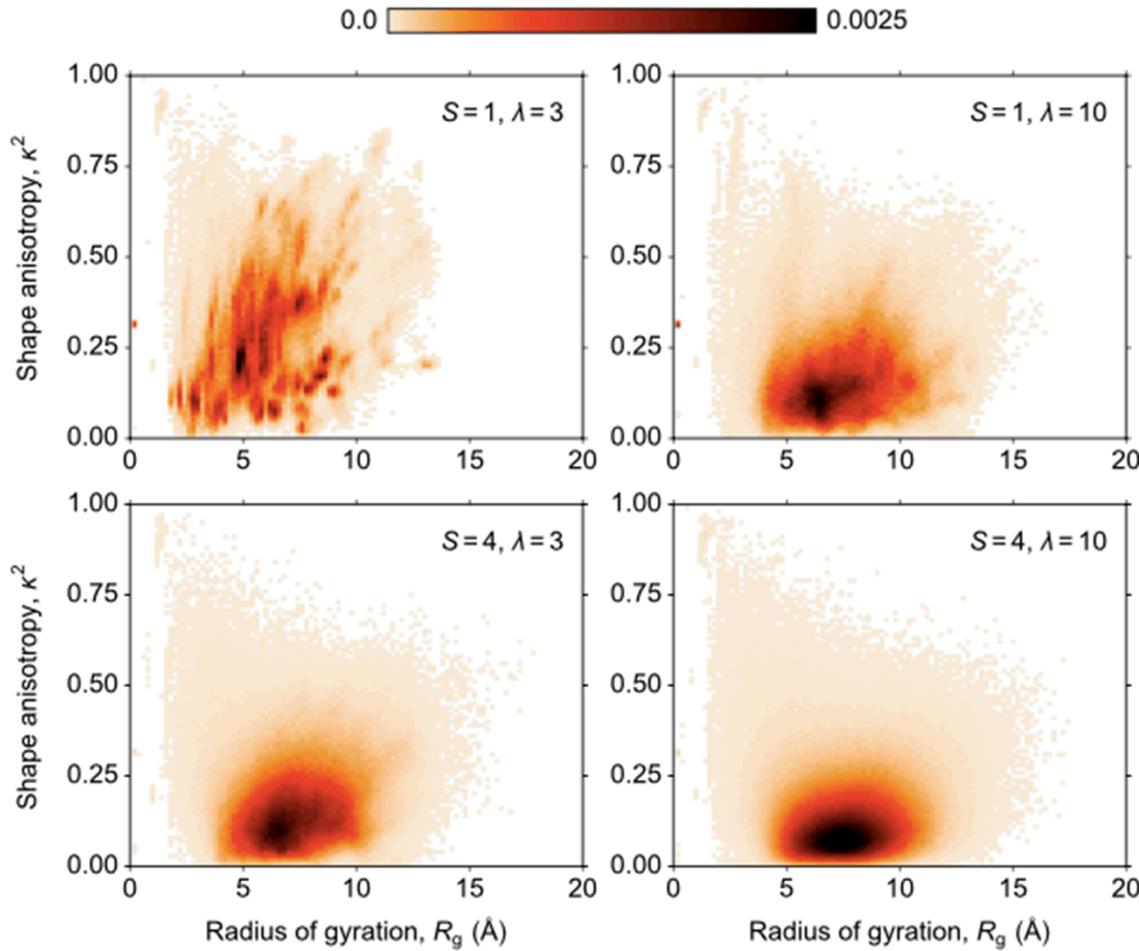


density-based algorithm resolves differences in percolated systems

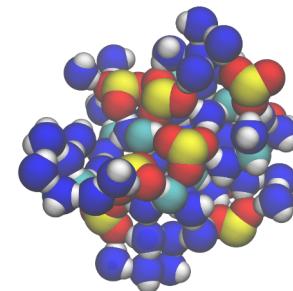
Cluster Size and Shape

radius of gyration $R_g^2 = \lambda_1 + \lambda_2 + \lambda_3$

anisotropy $\kappa^2 = 1 - 3(\lambda_1\lambda_2 + \lambda_1\lambda_3 + \lambda_2\lambda_3)/R_g^4$



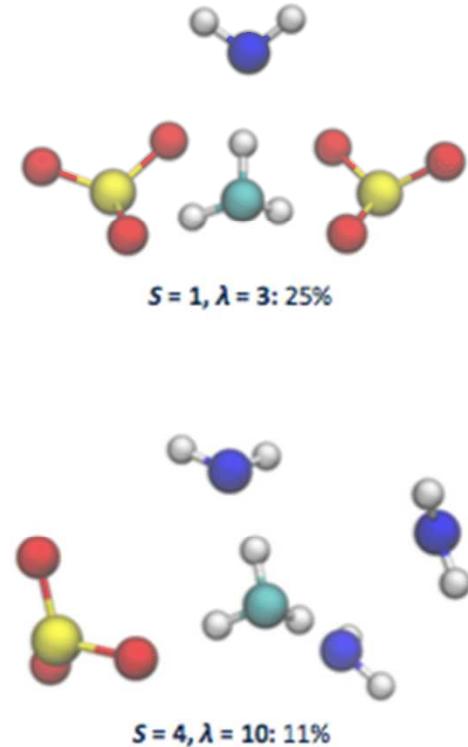
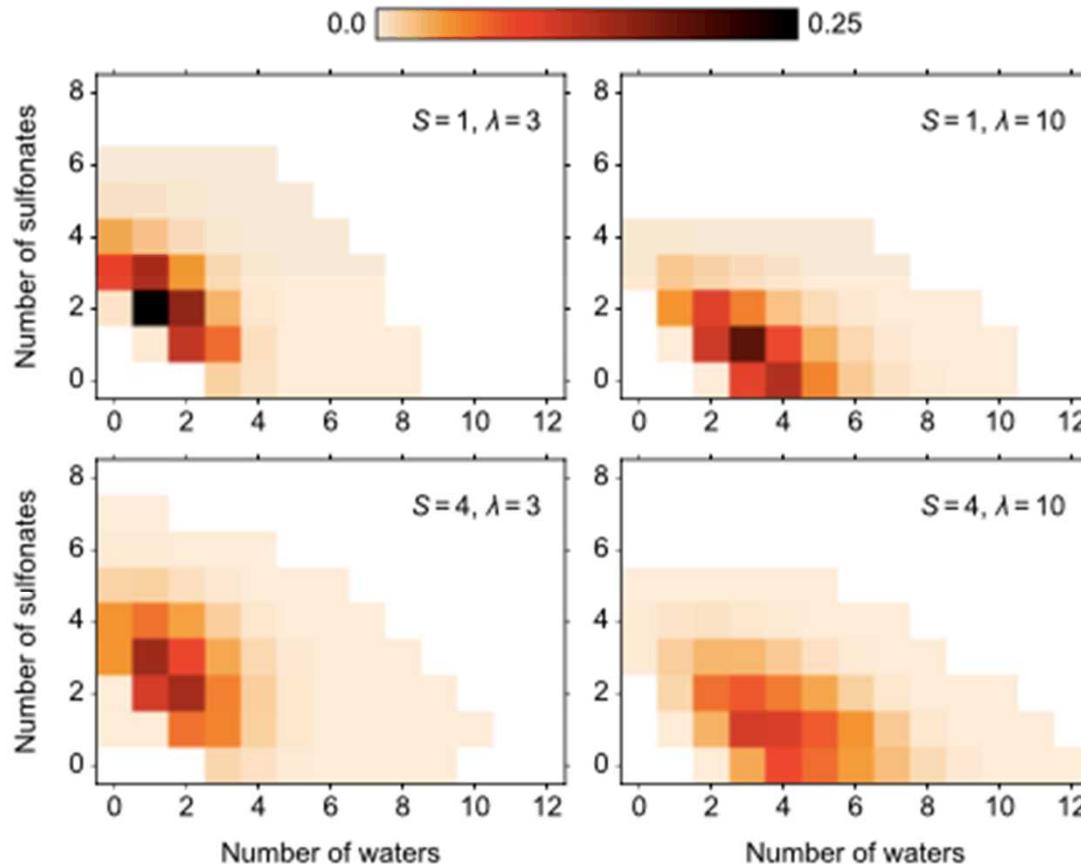
$S = 1, \lambda = 3, \kappa^2 = 0.4$



$S = 4, \lambda = 10, \kappa^2 = 0.05$

Hydronium Coordination

probability of H_3O^+ near SO_3^- and H_2O



H_3O^+ more loosely bound with more water, percolated clusters

Conclusions

- MD simulation can reveal ionic aggregate morphologies
 - good agreement with X-ray scattering
- MD in agreement with QENS for acid copolymers
 - chain dynamics are heterogeneous
 - slowed by acid aggregates
 - even slower with ionic aggregates
- MD for SDAPP
 - increasing water, sulfonation leads to percolated clusters
 - density-based algorithm for more information on percolated clusters

Future work: continued correlation of dynamics with morphology

Acknowledgments



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Karen Winey



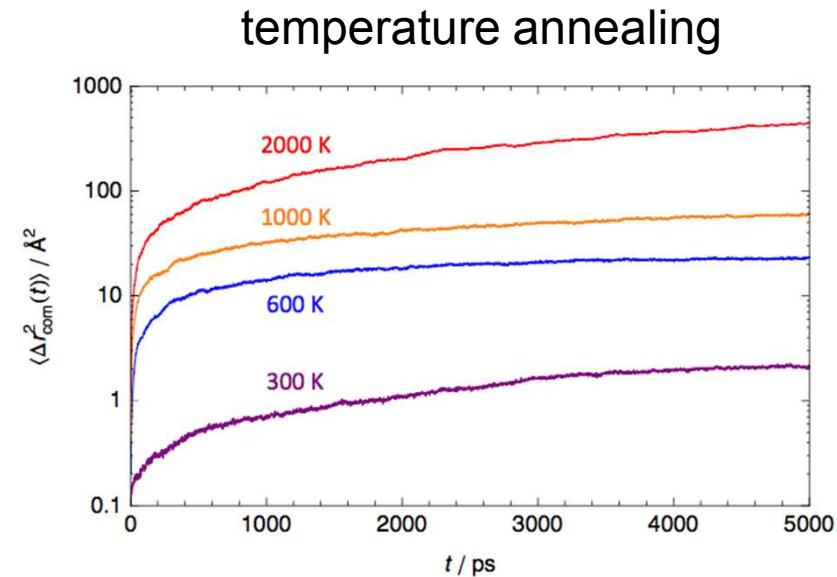
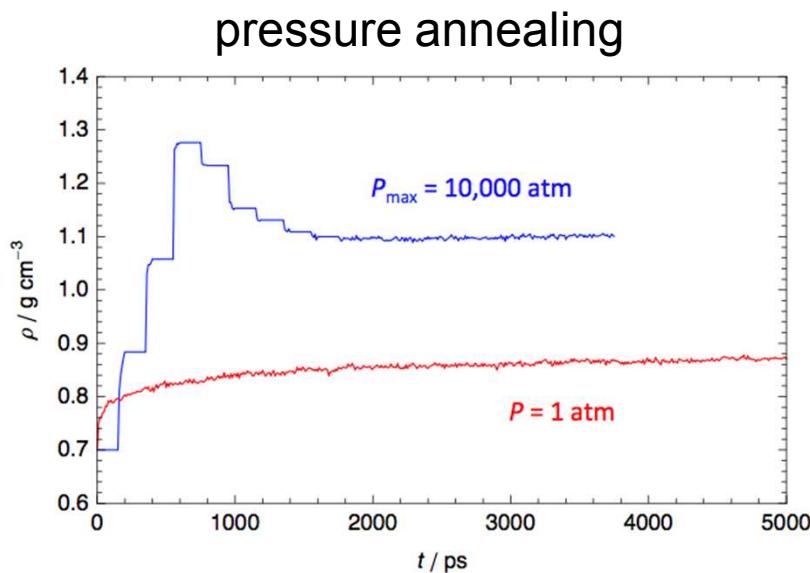
NIST

Jacob Tarver
Madhu Tyagi
Christopher Soles



Building and Equilibrating

Monte Carlo simulation
5 boxes with different initial conditions/system

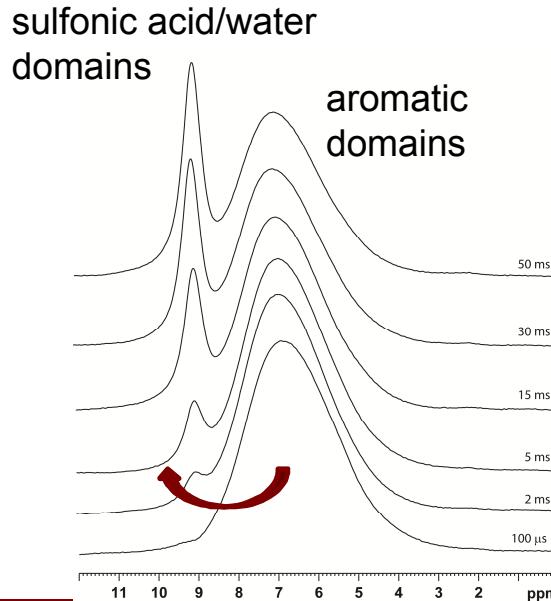


final densities match experiment: ≈ 1.2 g/cm³

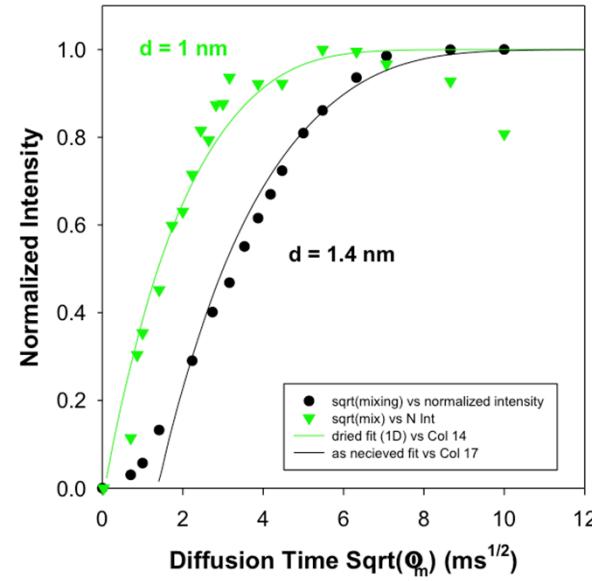
Cluster Size from NMR

spin diffusion experiments can measure domain sizes

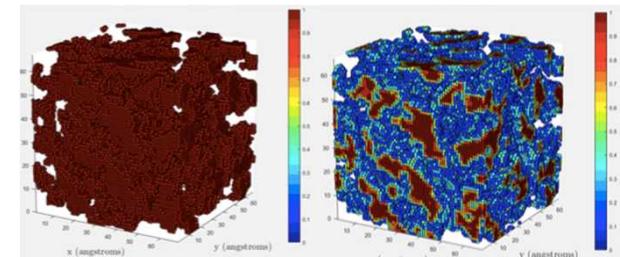
- magnetize one kind of proton
- watch the magnetization diffuse to other protons as a function of time
- fit the data to extract a distance = domain size
 - *new:* use MD morphology (acids, waters) as input
 - calculate expected spin diffusion
 - compare to measured spin diffusion by NMR



magnetization in acid/water domains



magnetization with
MD morphology

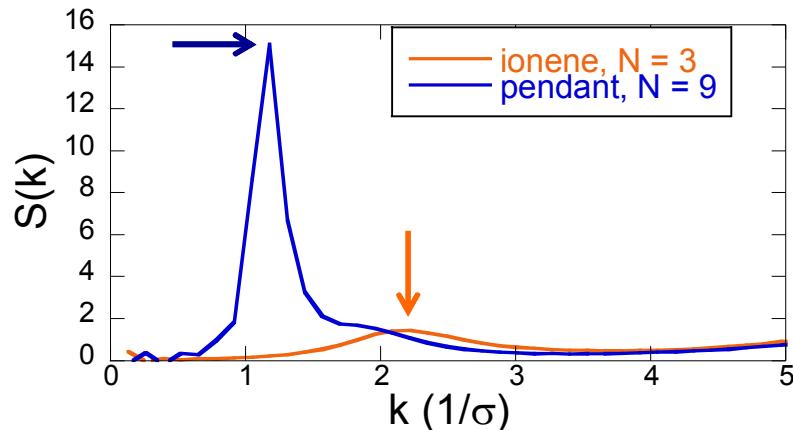


Time-dependent Structure Factors

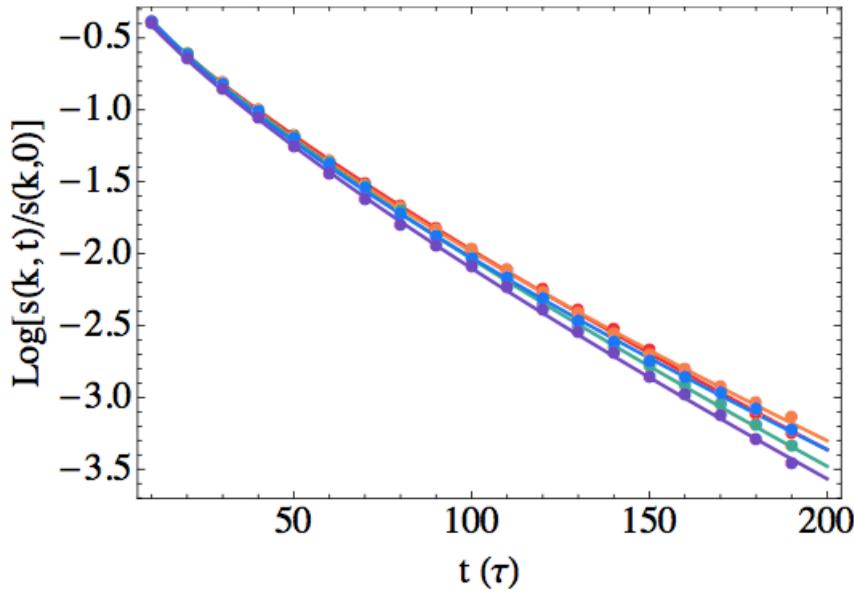
decay of counterion-counterion scattering peak

$$S(k, t)/S(k, 0) = \exp[(-t/\tau)^\beta]$$

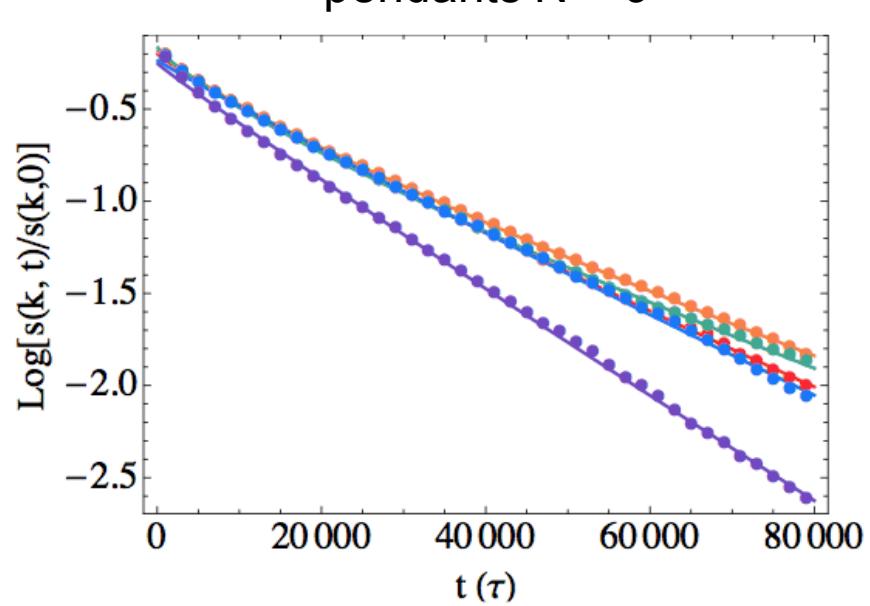
$$0.66 < \beta < 0.96$$



ionenes $N = 3$



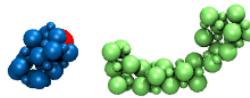
pendants $N = 9$



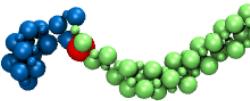
Ion Trajectories: CG MD

periodic pendants $N_{bb}=9$

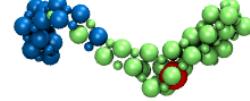
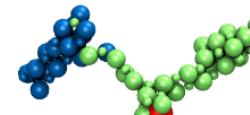
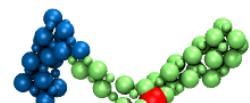
2 separate clusters
Follow one **counterion**



Clusters have collided



Ion has moved to other cluster.
NEVER separated from a cluster.

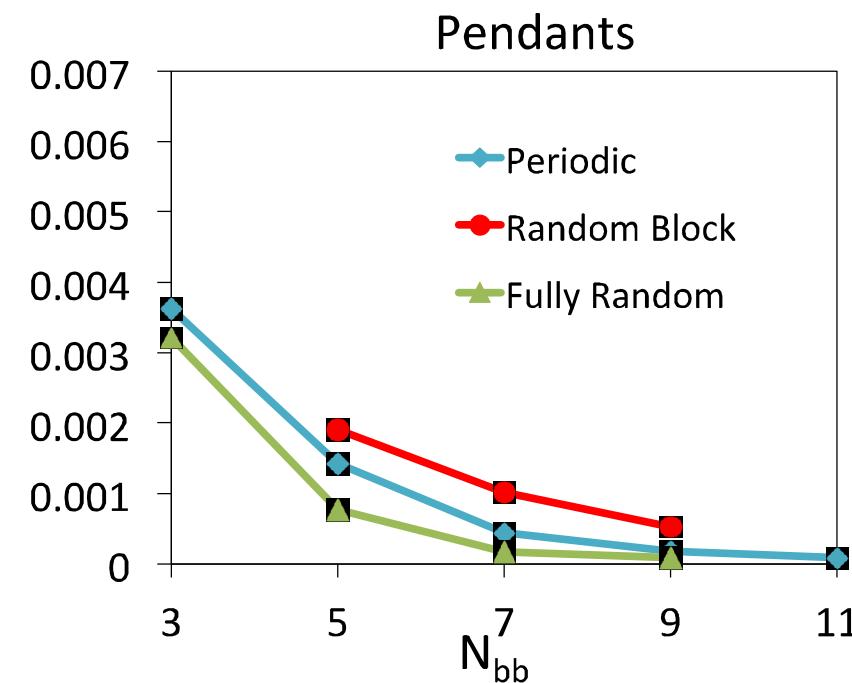
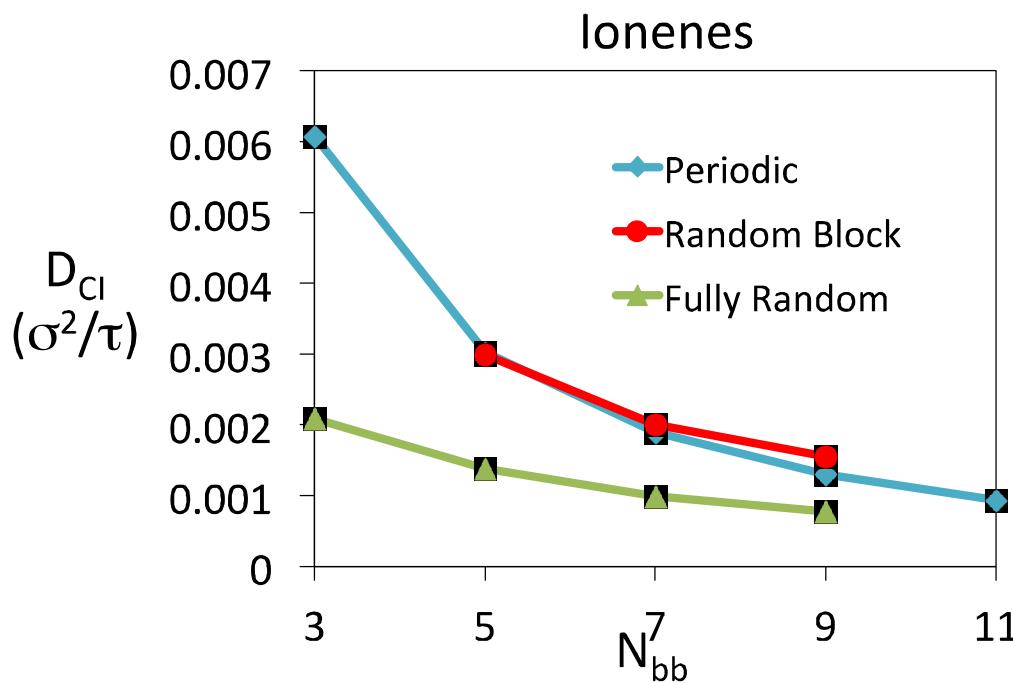


Clusters reform with ion moved

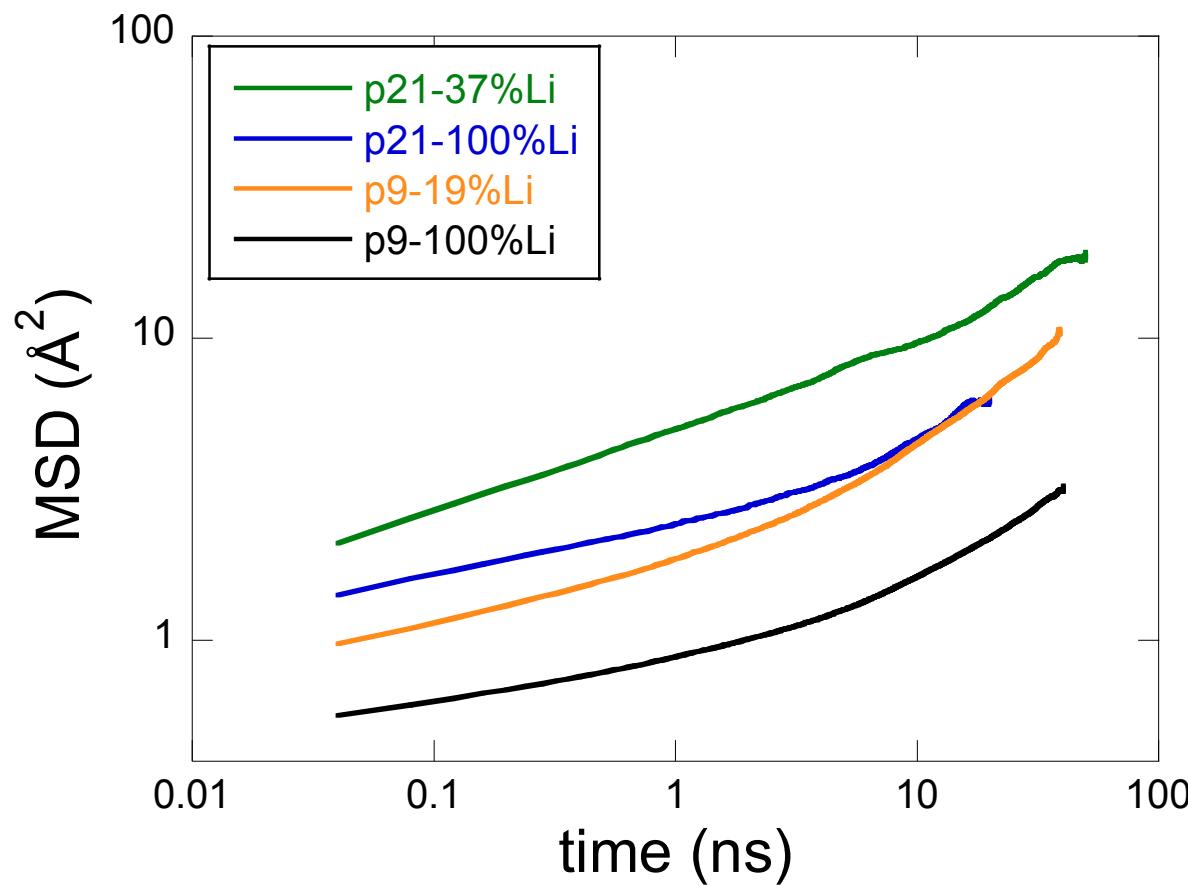
ions move by cluster
rearrangement/collision

Counterion Diffusion Constants

- Ionenes conduct better than pendants
- Greater concentration of ions increases diffusion
- Blocky random copolymerization increases diffusion

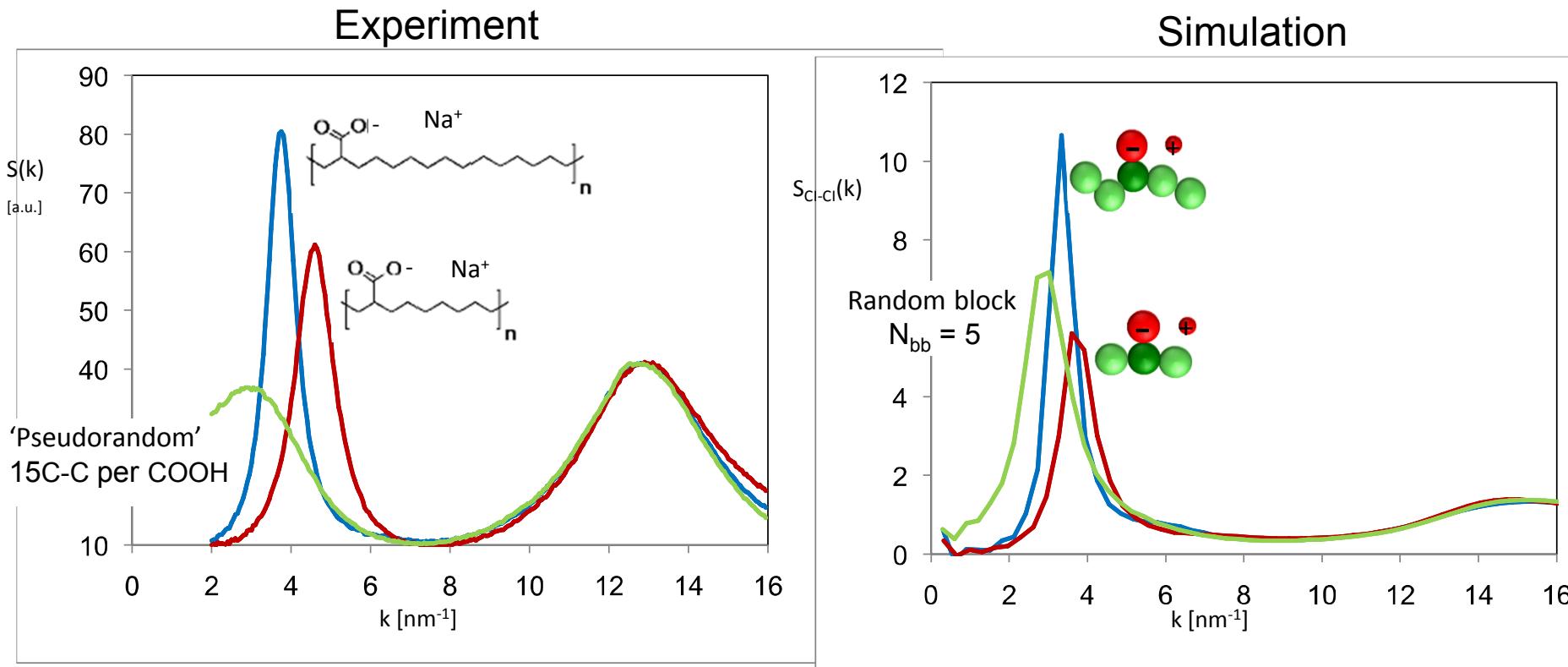


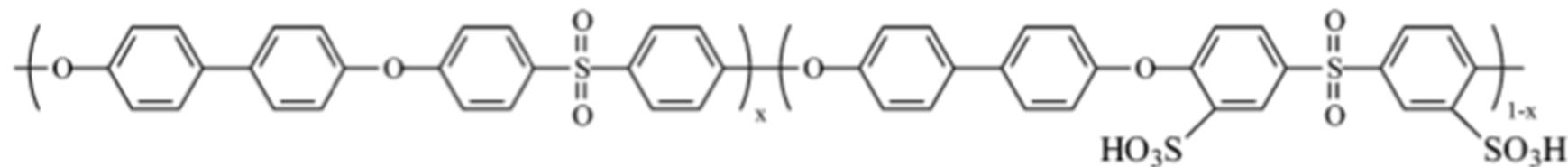
Li MSDs



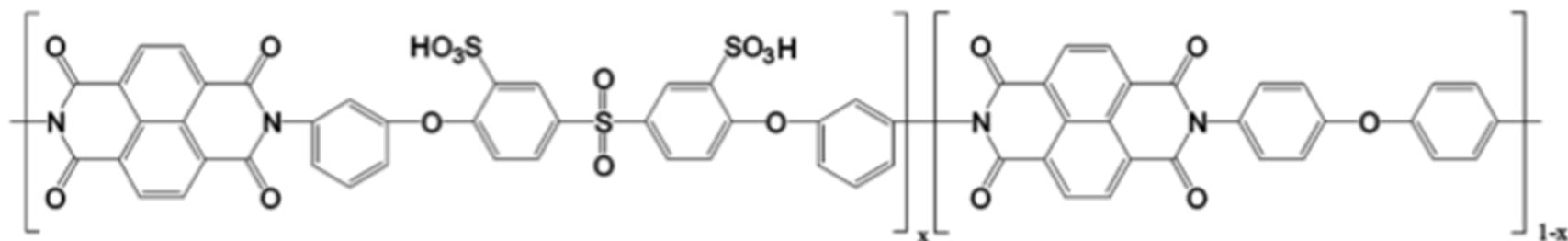
CG MD: Comparison to X-ray Scattering

- Experimental/Simulation Agreement
 - Peak location similar
 - Increasing spacing moves peak to left
 - Random spacing moves and broadens peak





BPSH



SPI

Fujimoto, C., Hickner, M., Cornelius, C. & Loy, D.
Macromolecules **38**, 5010–5016 (2005)