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Comparative study of the counterflow forced ignition of the butanol isomers at atmospheric and elevated pressures

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Abstract

In support of the development of robust combustion models, the present study describes experimental and computational results on the non-premixed counterflow ignition of all four butanol isomers against heated air for pressures of 1–4 atm, pressure-weighted strain rates of 200–400 s⁻¹, and fuel molar fractions in nitrogen-diluted mixtures of 0.05–0.25. Comparison of the parametric effects of varied pressure, strain rate, and fuel loading amongst the isomers facilitates a comprehensive evaluation of the effect of varied structural isomerism on transport-affected ignition. The experimental results are simulated using isomer-specific skeletal mechanisms developed from two comprehensive butanol models available in the literature, and are used to validate and assess the performance of these models. Comparison of the experimental and computational results reveal that while both models largely capture the trends in ignition temperature as functions of pressure-weighted strain rate, fuel loading, and pressure, for all isomers both models over-predict the experimental data to an appreciable extent. In addition, neither model captures the experimentally-observed ignition temperature rankings, with both models predicting a large spread amongst *n*-/*iso*-/*sec*-butanol which does not appear in the experimental results. Sensitivity and path analyses reveal that the butene isomers play a significant role in determining the ignition temperatures of the butanol isomers in both models, with the relative branching ratios likely accounting for the ignition temperature rankings observed using each model. It is observed that the reactivity of the butene isomers varies appreciably between the two butanol models, which may account for some of the variability in predictions between the two models. Furthermore, effects of transport properties and their uncertainties on ignition temperature predictions are discussed.

Keywords: Counterflow, Ignition, Butanol isomers, Non-premixed, Skeletal mechanism

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4 **1. Introduction**
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Despite recent advances in electric vehicle technologies, their limited range, long recharge cycles, and limited at-large charging options have constrained their consumer appeal [1]. Moreover, while significant advances in terms of energy density over current lithium battery technology are conceivable, attaining such performance will require major technological breakthroughs in terms of electrode/electrolyte materials and chemistry [2]. Alternative technologies such as fuel cell vehicles can potentially address both range and recharge/refuel time issues; however such vehicles have largely been based upon hydrogen fuel cells, which would require an entirely new, world-wide fuel distribution infrastructure to be developed. As a result, there is a clear need for combustion-based near- and intermediate-term alternative transportation energy solutions that address the pressing issues of improved efficiency, reduced emissions, and lowered lifecycle carbon footprint. While both novel engine designs and alternative fuels promise to provide efficiency gains and emissions improvements, their success is predicated upon a robust understanding of the coupled effects of chemical kinetics and convective-diffusive transport, and their accurate representation in predictive reactive-flow models under engine relevant conditions.

As part of a push towards renewable fuels and reduced emissions, alcohols have emerged as a leading prospect both for near-term performance and sustainability improvements, as well as for the long-term replacement of fossil fuels in novel engine concepts. Ethanol, the most successful of these to date, currently comprises up to 10% of all gasoline purchased in the United States and has facilitated the elimination or phase-out of both tetra-ethyl lead (TEL) and methyl tert-butyl ether (MTBE) as anti-knock additives. Through its long history, ethanol has received significant research attention and has been investigated in shock tube, flame, and reactor experiments (cf. [3]). However, the fermentation process by which the majority of ethanol is

produced has been criticized for both its use of food-grade feedstocks as well as its low conversion efficiency, and second generation production from cellulosic plant waste has yet to be proven commercially viable. Partly as a result, so-called “second generation” alcohol-based alternative fuels such as butanol have recently received significant research attention. As a stand-alone alternative transportation fuel or as a fuel blend with gasoline, butanol offers several advantages over ethanol. Whereas ethanol is fully miscible with water, both *n*- and *iso*-butanol isomers exhibit limited solubility with water and are less corrosive, opening up the possibility of more efficient distribution methods through pipelines. In addition, its higher energy density allows higher blending ratios with gasoline without engine modifications, and its lower vapor pressure would greatly reduce evaporative emissions. Aside from its potential impact as a transportation fuel, chemical kinetics of butanol is scientifically interesting as it represents the smallest alcohol exhibiting all forms of structural isomerism. As a result, by comparing the behavior of the butanol isomers in well-defined combustion configurations, the impacts of molecular structural variations on combustion chemistry can be better understood and broadly applied to the modeling of alcohol-based transportation fuels.

Due to the interest from both practical and scientific points of view, an appreciable body of fundamental research has been developed for butanol isomers in recent years. Though by no means a comprehensive review, numerous fundamental studies have been conducted using a variety of experimental systems including laminar flame speeds [4–7], flame extinction [8-10], pyrolysis [11], flame structure [6,12-15], species and temperature measurements in a flow reactor [12], jet-stirred reactors (JSR) [6,16], and ignition delays in rapid compression machines (RCM) [17-19] and shock tubes [20,21]. Several of these studies have investigated the impact of isomeric variations on global combustion properties. Veloo and Egolfopoulos [7] determined

atmospheric pressure laminar flame speeds of the butanol isomers in the equivalence ratio range of 0.7–1.5, finding highly similar flame propagation rates for *n*-/*iso*-/*sec*-butanol but significantly lower flame speeds for *tert*-butanol. Gu *et al.* [4] observed laminar flame speed differences between the various isomers, finding that the isomers followed a ranking of *n*-butanol > *iso*-butanol \approx *sec*-butanol > *tert*-butanol for atmospheric pressure. Stranic *et al.* [20] investigated ignition delay times of the butanol isomers in a shock tube at 1050–1600 K, 1.5–43 atm, and equivalence ratios of 0.5 and 1.0, finding that the butanol isomers exhibited noticeably different ignition delay times, with the relative rankings changing as a function of pressure. At 1.5 atm, *n*-butanol exhibited the shortest ignition delay times, followed by *iso*- and *sec*-butanol, with *tert*-butanol exhibiting considerably longer ignition delays, whereas at 43 atm the rankings followed *n*-butanol \approx *iso*-butanol < *sec*-butanol < *tert*-butanol. In an RCM configuration Weber and Sung [17] found quite different ignition delay trends for stoichiometric mixtures at 715–910 K and 15 and 30 bar pressures. At both pressure conditions *n*-butanol exhibited significantly faster ignition delay times than other isomers, additionally finding that the ignition delay ranking followed *n*-butanol < *iso*-butanol \approx *sec*-butanol < *tert*-butanol at 15 bar, but *n*-butanol < *tert*-butanol < *sec*-butanol < *iso*-butanol at 30 bar. In addition to global combustion properties, the effect of structural isomerism on intermediate species production has been explored by several studies. McEnally *et al.* [15] conducted speciation studies on the butanol isomers in a doped methane co-flow flame at atmospheric pressure, and concluded that the dominant decomposition process was unimolecular decomposition rather than H-abstraction. Oßwald *et al.* [14] conducted a molecular beam mass spectrometry (MBMS) study of the butanol isomers in a fuel-rich low-pressure laminar premixed flame, noting significant differences amongst the butanol isomers in terms of

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4 the intermediate species pool. In particular, large disparities were observed for butene, enol, and
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6 aldehyde species in [14].
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8 From these and similar works, several detailed combustion models have recently been
9 compiled and developed that comprehensively describe the chemical kinetics of butanol isomers.
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11 The model of Frassoldati *et al.* [22] – an update of the mechanism of Grana *et al.* [13] – includes
12 all four isomers and has been validated against pyrolysis, shock tube ignition delay time, and
13 premixed and non-premixed flame structure data. The model of Merchant *et al.* [23] – including
14 all four isomers, and based upon the comprehensive model of Van Geem *et al.* [24] – has been
15 validated against pyrolysis, laminar flame speed, low-pressure premixed flame structure, and
16 shock tube ignition delay data. Additionally, the comprehensive model of Sarathy *et al.* [25] has
17 been validated against laminar flame speeds, low-pressure premixed flame structures, RCM and
18 shock tube ignition delays, and JSR species profiles.
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21 Despite the research attention that butanol isomers have garnered, there is relatively little
22 data exploring limit phenomena in convective/diffusive environments for these fuels. In fact, to
23 the authors' knowledge, the only available forced ignition data came from the stagnation-pool
24 study of Liu *et al.* [26] for *n*- and *iso*-butanol, while flame extinction data were limited to the *n*-
25 butanol studies of Veloo *et al.* [10] and Hashimoto *et al.* [9], and the *n*-, *iso*-, and *sec*-butanol
26 study of Mitsingas and Kyritsis [8]. Ignition and extinction data in convective/diffusive systems
27 are relevant to the operation of practical combustion devices, and can also offer a highly-
28 sensitive experimental platform for the validation of both chemical kinetic and transport models.
29 As such, the present work compares the impact of ambient pressure, strain rate, and fuel loading
30 on the counterflow ignition temperatures of all four butanol isomers in order to understand the
31 isomeric structural effects on diffusive ignition. The experimental results are further simulated
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4 using isomer-specific skeletal mechanisms derived from comprehensive butanol models
5 available in the literature. A comparison of experimental and simulated results is then used to
6 validate and assess the performance of these literature butanol models.
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2. Experimental and computational descriptions

2.1 Experimental apparatus

16 The details of the non-premixed counterflow ignition apparatus, including a detailed
17 experimental characterization, have been previously described by the authors [27]. Briefly, the
18 counterflow burner consists of a quartz straight-tube upper section directing heated air downward
19 against a nitrogen-diluted fuel stream emanating from a stainless steel lower section. The air and
20 fuel streams are surrounded by concentric nitrogen co-flow to isolate the test section from the
21 ambient atmosphere and improve the quality of the resulting stagnation-point flow field. The air
22 and fuel tubes have inner diameters of $D=19$ mm and the co-flow tubes have 28 mm inner
23 diameters. The air and fuel streams are separated by $L=20$ mm, resulting in an L/D ratio for all
24 experimental conditions of 1.05. Heating on the air side is accomplished using an internal helical
25 SiC heater, capable of heating the airflow to 1250–1300 K at the tube exit depending on
26 operating conditions, and an external heater that is used to reduce heat loss. The ignition
27 temperature, measured as the air-side centerline boundary temperature, is determined from a K-
28 type bare wire thermocouple with proper radiation correction. The location of the ignition event
29 is monitored using a Vision Research Phantom v710 high-speed camera acquiring visible-light
30 images at a frame rate of 3000 Hz. This frame rate is sufficient to capture the onset of ignition
31 and facilitates determining its precise location within the test section to ensure consistency
32 amongst data sets as well as ensure quasi-one-dimensional ignition behavior. For all the
33 experimental data reported herein, the onset of ignition was observed to take place near the
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4 middle of the test section and then propagate radially in a fairly one-dimensional manner. The
5 thermocouple design, details of the radiation correction, and discussion of the importance of
6 monitoring ignition location have been described previously [27].
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11 Flow control is accomplished through the use of sonic nozzles for all gases. The air stream
12 is synthesized by a 21%/79% O₂/N₂ mixture by mole, while the nitrogen-diluted fuel stream
13 varies between 5–25% fuel by mole. The flow rate of liquid fuel is controlled using a precision
14 Teledyne Isco 1000D high-pressure syringe pump, with fuel vaporization accomplished through
15 a heated spray system. The fuel vaporization system and the subsequent fuel lines are heated to
16 surface temperatures just above the boiling point of the isomer in question to prevent surface
17 condensation – for the current study, ~140 °C. For all conditions tested here, the mixture
18 temperature at the fuel boundary is maintained at ~380 K. To ensure proper vaporization, the
19 partial pressure of the fuel is maintained well below the corresponding saturation vapor pressure
20 for a given butanol isomer, calculated using the correlation from Yaw's Chemical Handbook
21 [28] at the temperature/pressure conditions within the fuel line. Furthermore, the fuel partial
22 pressure never exceeds 50% of the calculated saturation vapor pressure for all experimental
23 conditions in an effort to ensure complete vaporization. It is worth noting that the concentration
24 validation has been conducted previously [27] using *n*-butanol as a model fuel. This isomer
25 represents a “worst-case” in terms of condensation as it exhibits the lowest vapor pressures.
26 Since no condensation was observed for the *n*-butanol concentration validation, the fuel line
27 settings can be presumed adequate for all butanol isomers.
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30 As has been thoroughly described in previous work [27], both systematic and random
31 uncertainties are relevant to the analysis of the present experimental results. Systematic
32 uncertainty results from defects in a parameter model (e.g., Nusselt number for thermocouple
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radiation correction) or measuring equipment (e.g., pressure gauges) which cause system-wide deviations from true behavior. Such uncertainty results in reproducible inaccuracies that tend to impact the entire data set in a largely equivalent manner. Random error represents statistical fluctuations in measured data based upon the precision of the measurement device, and their impact can be minimized through averaging of multiple observations. These definitions are important to the present analysis because, while the total uncertainty (including both systematic and random errors) is relevant for the comparison of experimental and numerical ignition temperatures, only the random error is applicable when comparing amongst the experimental results since all data should be equally affected by systematic errors. As a result, comparisons amongst the experimental isomer ignition temperature data should be compared using the random error (± 5 K), while comparisons between experimental and numerical data are best compared using the total estimated uncertainty (systematic plus random), which ranges from 20 K for the lowest ignition temperatures to 35 K for the highest [27].

2.2 *Experimental procedure*

In the present experiments, the oxidizer boundary temperature at the onset of ignition is denoted as the ignition temperature (T_{ig}). The procedure for acquiring this temperature is as follows: 1) The internal, external, and flow system heaters are brought up to a steady-state temperature close to the ignition state, the desired gaseous mass flow rates (excepting any fuel) for a given strain rate condition are set on the flow system, and the chamber is pressurized to the desired set point. 2) Fuel is introduced through the flow system and allowed to come to steady state. 3) The high-speed camera begins acquiring data, and the air temperature is gradually raised by increasing power to the internal heater until a flame ignites. 4) The fuel supply is shut off to extinguish the flame. 5) The thermocouple solenoid is activated, rotating the thermocouple bead to the center of

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4 the air duct and the air temperature, along with the fuel-side gas temperature, is recorded. 6) The
5 images acquired from the high-speed camera are checked to verify that ignition occurs at or near
6 the longitudinal axis, and that it occurs near the middle of the test section, ± 2 mm. If ignition
7 occurs too far towards the fuel or oxidizer exits, the flow rates are adjusted to move the
8 stagnation plane in the appropriate direction while maintaining a constant global strain rate. In
9 addition, if ignition occurs at a temperature more than 10 K away from the estimated temperature
10 used to compute flow rates for a given global strain rate, the flow rates are updated and Steps 2–
11 20 are repeated. Steps 2–6 are repeated a minimum of three times once the proper flow settings
12 21 have been achieved to ensure a consistent value for T_{ig} .
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17 26 Here, the global strain rate (K) is defined based on the relation of Seshadri and Williams
18 27 [29]: $K = \frac{2V_O}{L} \left(1 + \frac{V_F \sqrt{\rho_F}}{V_O \sqrt{\rho_O}} \right)$, where V is the bulk velocity at the boundary, L is the separation
19 28 distance, ρ is the density, and the subscripts F and O represent the fuel and air boundaries,
20 29 respectively. The adequacy of this global strain rate definition to account for the effects of
21 30 varying density due to the temperature gradients inherent to counterflow ignition has been
22 31 demonstrated in [27]. Following the work of Fotache *et al.* [30], the pressure-weighted strain
23 32 rate (k'), defined as $k' = \frac{P_C}{P_{ref}} K$, is used to isolate the chemical effect of pressure variations by
24 33 keeping the spatial scalar structure (temperature and concentration profiles) approximately
25 34 constant. In the definition of k' , P_C is the chamber pressure and P_{ref} is a reference pressure,
26 35 taken throughout this work as 1 atm.
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2.3 Computational specifications

The ignition state is modeled using an in-house counterflow non-premixed ignition code based on the potential-flow formulation of Smooke *et al.* [31] and identical to that used previously [27]. As in the work of Kreutz *et al.* [32], the ignition temperature corresponds to the turning point of

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4 the lower-branch ignition response curve with respect to air boundary temperature, while the
5 current navigation of the ignition turning point is achieved using the two-point flame-controlling
6 continuation method developed by Nishioka *et al.* [33]. In this study, the H radical is chosen as
7 the controlled species due to its crucial role in governing ignition, although other key radicals are
8 equally applicable [33]. For a given strain rate, the use of the two-point H-controlling
9 continuation requires boundary conditions of the mixture compositions at both fuel and oxidizer
10 boundaries and the fuel boundary temperature (380 K in the current work), along with the H
11 concentration values at two different locations as internal boundary conditions [33]. As such, the
12 mass fluxes at the fuel and oxidizer boundaries are solved as edge values, while the air boundary
13 temperature becomes the system response [33]. By varying the H concentration values at the two
14 selected locations, continuous mapping of the ignition response curve is then obtained. It is also
15 worth noting that because of the convective/diffusive process involved in the counterflow non-
16 premixed configuration and the Arrhenius dependence of reaction rates favoring a higher
17 temperature environment, the ignition kernel is located on the air side of the stagnation surface
18 and its local stoichiometry is always very lean. This has been demonstrated in Fotache *et al.*
19 [34,35] using C₁–C₄ alkanes, for cases with fuel concentrations at the boundary ranging between
20 6% and 100%. A similar situation is also observed in the present study of butanol isomers.
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45 Similar to the procedure discussed in previous work [27], skeletal mechanisms specific to
46 each isomer are created using the Directed Relation Graph with Error Propagation (DRGEP)
47 implementation of the Mechanism Automatic Reduction Software (MARS) package of Niemeyer
48 and co-authors [36-39]. Each skeletal mechanism is reduced using constant-volume ignition
49 delays for equivalence ratios of 0.5–2, pressures of 1–40 atm, and temperatures of 1000–1800 K,
50 using the fuel, N₂, and O₂ as target species. In addition, the reduction procedure utilizes perfectly
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stirred reactor (PSR) extinction profiles for inlet temperatures of 400 and 500 K, covering the same range of pressure and equivalence ratio as the autoignition results. For both ignition delay and PSR targets, the maximum error tolerance during the reduction process is set at 10%. As mentioned in the introduction, a number of detailed kinetic mechanisms for butanol isomers have been developed in recent years, including the models of Frassoldati *et al.* [22], Merchant *et al.* [23], and Sarathy *et al.* [25], each validated for all four butanol isomers. Unfortunately, the inclusion of non-integer stoichiometric coefficients in the Frassoldati model makes it incompatible with both the current Chemkin-based ignition code and the MARS package, as well as running exceedingly slowly in CHEMKIN-PRO [40]. Hence, only the Sarathy and Merchant models are included and compared in the present study. The resulting isomer-specific skeletal mechanisms are referred to hereafter as SN, SI, SS, and ST (referring to the *n*-, *iso*-, *sec*-, and *tert*-butanol skeletal mechanisms derived from the Sarathy detailed model), and MN, MS, and MT (referring to the *n*-, *sec*-, and *tert*-butanol skeletal mechanisms derived from the Merchant detailed model). Due to some issues arising from *iso*-butanol-relevant reactions in the Merchant model, which are detailed in Section 2.4.1, the skeletal reduction cannot be conducted for *iso*-butanol, and hence “MI” is lacking here.

Validation of the skeletal mechanisms for each of the isomers is shown in Fig. 1, by plotting the computed peak mole fraction of hydrogen radical as a function of air boundary temperature (T_0) for the cases with fuel mole fraction of $X_f=0.15$ in the nitrogen-diluted fuel stream. For all isomers, the skeletal Sarathy mechanisms perform nearly identically to the detailed model at both 1 and 5 atm, with a maximum deviation of ~5 K shown by the ST mechanism at 5 atm where the skeletal mechanism under-predicts the detailed model. The skeletal Merchant mechanisms also perform quite well, with a maximum deviation of <1% for the MN mechanism at 5 atm, where

the skeletal mechanism over-predicts the detailed model. The MS mechanism over-predicts the detailed model by <5 K, while the MT mechanism exhibits turning points essentially identical to those of the detailed model. In general, the Merchant model predicts higher ignition temperatures than the Sarathy model. Additional validation of the resulting skeletal mechanisms includes the targets of ignition delay times, PSR response curves, and laminar flame speeds over a wide range of conditions. Some comparative results for *n*-butanol can be found in the Supplementary Material of [27].

Table 1 summarizes the size of each mechanism used in this study in terms of number of species and reactions, including both the detailed and skeletal mechanisms. All the skeletal mechanisms generated in this study are included in the Supplementary Material.

2.4 Modifications to combustion models

In the course of investigating the butanol isomers numerically, several important issues with the Merchant and Sarathy models have become apparent, and have necessitated modification of the mechanisms and the exclusion of certain data. Due to the significant impact of these changes and their implications on future modeling studies, these modifications are detailed in the following sections and are incorporated into the respective skeletal mechanisms.

2.4.1 Merchant model

In the course of mechanism reduction, it was discovered that the Merchant model contains several reactions in the PLOG format that contain negative pre-exponential factors. The PLOG format provides the flexibility to describe reaction rates in different pressure ranges by different Arrhenius coefficient sets. For pressures intermediate between two reaction rate descriptions, a linear interpolation for $\ln(k)$ is used to obtain the reaction rate:

$$\ln k = \ln k_i + (\ln k_{i+1} - \ln k_i) \left[\frac{\ln P - \ln P_i}{\ln P_{i+1} - \ln P_i} \right], \quad \text{Eqn. 1}$$

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4 where k is the interpolated reaction rate, k_i and k_{i+1} are the reaction rates at pressures bracketing
5 the pressure for which k is desired, and P is the pressure, with the subscripts following an
6 identical nomenclature. Since the logarithm of a negative number is undefined, the PLOG
7 interpolation cannot be evaluated for negative values of k_i 's. Such a situation arises for the *iso*-
8 butanol decomposition reaction, producing methyl radical and 2-hydroxypropyl, where the
9 formatting of this reaction as a “declared duplicate” forces interpolation using a negative reaction
10 rate. As a result, both the ignition code and the mechanism reduction code fail. It is worth noting
11 that when the same mechanism is used in CHEMKIN-PRO [40], the calculation neither fails nor
12 displays any warning messages. Given the nature of the interpolation, it is unclear what allows
13 CHEMKIN-PRO calculations to proceed.

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15 For the purposes of the present study, the above-mentioned *iso*-butanol decomposition
16 reaction is problematic in that its reaction rate cannot be evaluated. In order to facilitate as broad
17 a mechanism comparison as possible, this reaction is manually removed so that skeletal
18 mechanisms for *n*-, *sec*-, and *tert*-butanol can be obtained and used in the ignition code. This
19 methodology is deemed valid for these isomers given that the reverse of this removed reaction
20 should at most represent a minor recombination pathway in these cases. However, given that this
21 *iso*-butanol decomposition reaction defines one possible pathway for *iso*-butanol destruction, it
22 cannot be removed from the mechanism *a priori* without potentially significant impacts to the
23 fidelity of an *iso*-butanol skeletal mechanism. As a result, no computational data for *iso*-butanol
24 from the Merchant model is shown in this work.

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2.4.2 Sarathy model

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28 In the course of evaluating the impact of transport parameters on the ignition temperature of the
29 butanol isomers, it was discovered that, while the Lennard-Jones parameters for *n*-butanol were
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4 quite similar between all three models [22,23,25], the parameters for *iso*-, *sec*-, and *tert*-butanol
5 within the Sarathy model differed significantly from the parameters used in both the Frassoldati
6 and Merchant models. While nitrogen-fuel binary diffusion coefficients for *n*-butanol differed
7 between the Merchant and Sarathy models by only ~5%, the computed diffusion coefficients for
8 the other three isomers were as much as 125% larger in the Sarathy model. In fact, the stated
9 values for collision diameter were almost half that of similar C₄ species, and even smaller than
10 those of the oxygen and hydroxyl radicals. Following the procedures laid out in Sarathy *et al.*
11 [6,25] for the estimation of transport parameters, values more similar to those found in the
12 Frassoldati and Merchant models were obtained, suggesting that these parameters included in the
13 transport database of Sarathy *et al.* [25] were questionable. It is worth noting that different
14 transport parameters for the butanol isomers were included in a recent hierarchical C₁–C₅ alcohol
15 model developed by Sarathy *et al.* [41]. These values result in closer agreement with the
16 Merchant transport model (~15% larger nitrogen-fuel diffusion coefficients). However, this
17 change was not described by Sarathy *et al.* [41], and the new transport parameters do not appear
18 to coincide with the stable-species transport parameter correlation methodology stated in [25].
19 Thus, it is unclear how these parameters were derived in [41].

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22 As will be shown in detail in Section 3.2, the effect of such large discrepancies in diffusion
23 coefficients is significant. As a result, the transport parameters for the three butanol isomers – as
24 well as all related C₄ species that use identical parameters to the respective parent fuel – are
25 modified to the corresponding parameters used in the Merchant model and the resulting transport
26 database is used to compute all numerical results presented for the Sarathy model. Since the
27 transport properties are otherwise similar, this change not only modifies the transport parameters
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4 to more realistic values, but also facilitates a more direct comparison of the underlying chemistry
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6 of the two models.
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9 **3. Ignition results and discussion**
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12 *3.1 Experimental results*
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14 Figure 2 demonstrates the effect of strain rate on the ignition temperature of the four butanol
15 isomers at 1 and 3 atm for $X_f=0.15$. Only a single data point for *tert*-butanol is included at 1 atm
16 due to the difficulty in igniting this fuel under atmospheric conditions. All isomers respond
17 similarly to varied strain rate within the range of $k'=200\text{--}400\text{ s}^{-1}$, with the differences between
18 the isomers narrowing slightly as strain rate increases. However, two interesting features with
19 regards to isomer ranking are apparent. First, *tert*-butanol exhibits significantly higher ignition
20 temperatures relative to the other three isomers. This ignition temperature difference amounts to
21 43–57 K at 1 atm, and 64–83 K at 3 atm. Second, the relationship between *iso*- and *sec*-butanol
22 reverses between 1 and 3 atm. While *iso*-butanol exhibits the highest ignition temperature
23 amongst the *n/iso/sec*-butanol group at 1 atm, *sec*-butanol occupies this position at 3 atm. Similar
24 behaviors are observed when comparing the isomers in terms of the effect of fuel loading. As
25 shown in Fig. 3 for $k'=350\text{ s}^{-1}$, while all isomers exhibit highly similar behavior as a function of
26 fuel loading, the relative ranking between *iso*- and *sec*-butanol again changes between 1 and 3
27 atm and is consistent across the fuel loading range investigated. It is worth noting that while the
28 differences amongst the *n/iso/sec*-butanol group are relatively small (on the order of 5–20 K), in
29 general the noteworthy trends involve ignition temperature differences in excess of the maximum
30 random error estimated from repeated measurements at the same operating conditions ($\pm 5\text{ K}$). In
31 addition, the aforementioned trends are consistent across a wide range of strain rate and fuel
32 loading.
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4 loading conditions, suggesting that they are unlikely to be the result of experimental variability
5 and therefore merit further investigation.
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10 Figure 4 provides a clearer demonstration of the *iso*/*sec*-butanol ranking switch by plotting
11 ignition temperature as a function of pressure at $k'=350\text{ s}^{-1}$ and $X_f=0.15$. A clear crossover point
12 for these isomers exists between 2 and 2.5 atm; below this pressure *sec*-butanol is the more
13 reactive one of the pair, while above this pressure *iso*-butanol becomes more reactive.
14 Throughout the pressure range, *tert*-butanol exhibits significantly higher ignition temperatures
15 than the other three isomers. It is worth noting that similar “crossover” behavior has been
16 observed in homogenous experiments involving similar temperature ranges. The shock-tube
17 study of Stranic *et al.* [20] found that at 1.5 atm, the ignition delay times of *iso*- and *sec*-butanol
18 were quite similar, while at higher pressures *sec*-butanol exhibited noticeably longer ignition
19 delays than *iso*-butanol. In addition, in line with the results of the present study, *tert*-butanol
20 manifested significantly longer ignition delays under all pressure conditions investigated.
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3.2 Effect of transport model uncertainties in the Sarathy mechanism

37 As discussed in Section 2.4.2, the original transport data contained in the mechanism of Sarathy
38 *et al.* [25] has apparent discrepancies in the Lennard-Jones parameters for *iso*-, *sec*-, and *tert*-
39 butanol, as compared to those of Frassoldati *et al.* [22] and Merchant *et al.* [23]. The effect of
40 changing these parameters – for both the parent fuel molecules and related C₄ intermediates
41 using identical values to the respective parent fuel – to those used by Merchant *et al.* [23] is
42 exemplified in Fig. 5 for 3 atm, $k'=350\text{ s}^{-1}$ conditions. In addition to being shifted upwards by
43 55–100 K, the sensitivity of ignition temperature to fuel loading (i.e. rate of change as a function
44 of fuel loading) is also increased. Comparing the original and modified transport model results,
45 the difference between predicted ignition temperatures at $X_f=0.05$ and 0.25 is ~60–70 K for all
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4 three isomers using the original parameters, however using the modified model this difference
5 increases to 100–110 K.
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8 Comparing the numerical results to the accompanying experimental results in Fig. 5, it is
9 clear that this modification results in a greater disagreement with experimental data than the
10 original model, with the difference between experimental and numerical data rising to between
11 80–120 K, depending on the isomer and operating conditions in question. While this
12 modification could hardly be termed an “improvement” in terms of fidelity to experimental
13 results, it does serve to illustrate two important points. First, it is imperative to include non-
14 premixed validation data during combustion model development to provide more rigorous
15 validation of the transport model. The larger sensitivities of non-premixed systems to transport
16 properties can help to improve the performance of the complete combustion model in transport-
17 affected environments, a designation encompassing most practical combustion devices. Second –
18 and most relevantly for the present discussion – while transport parameters exhibit significantly
19 larger sensitivities relative to individual reactions (to be discussed in due course), the fuel
20 diffusion coefficients of the original model would have to be increased by an excessively large
21 amount to close the gap between the numerical and experimental data. Since the resulting
22 transport parameters would then be entirely unreasonable – as outlined in Section 2.4.2 –
23 alternative factors must be considered to account for the differences. This observation proves
24 valuable in the evaluation of the Sarathy and Merchant models, as modification of the fuel
25 transport parameters – within reasonable bounds – cannot account for the disparity between
26 numerical and experimental results, and thus the source of the remaining disparities must lie
27 within the chemical kinetic mechanism.
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4 *3.3 Numerical results from the Sarathy model*
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3.3 Numerical results from the Sarathy model

While the accompanying numerical results to Figs. 2 and 3 have been computed, the trends in terms of strain rate and fuel loading are highly similar amongst the various isomers within a given mechanism set, and largely capture the experimentally-observed trends. As a result, the following description and analysis will focus on the effect of varied pressure. Figure 6 shows a comparison between the experimentally obtained ignition temperatures and numerical results computed using the SN, SI, SS, and ST mechanisms for $k' = 350 \text{ s}^{-1}$, $X_f = 0.15$, and $P = 1-4 \text{ atm}$. Several interesting observations can be made from Fig. 6. First, the numerical results for all isomers over-predict the experimental results by an appreciable extent, ranging from 70 to 140 K (6–10%). While such a deviation could be considered relatively small on a percentage basis, it should be noted that the gap between numerical and experimental results is of similar magnitude to the difference between 1 and 4 atm experimental ignition temperatures. As such, the difference between numerical and experimental results should be considered significant within the context of the experimental data. Second, while the experimental ignition temperature trends for *n*/iso/sec-butanol as a function of pressure are largely well-captured by its accompanying numerical results, for *tert*-butanol the difference is more dramatic. At 1 atm the difference stands at 140 K, however at 4 atm the gap shrinks to just 70 K. Interestingly, the numerical results for the butanol isomers exhibit one of two behavior sets corresponding to the isomer types; the positional isomers (*n*- and *sec*-butanol) exhibit a highly similar rate of change as a function of pressure, while the branched chain isomers (*iso*- and *tert*-butanol) also exhibit remarkable similarity but with a slightly greater pressure sensitivity. Third, unlike the experimental data where *n*-, *iso*-, and *sec*-butanol exhibit highly similar ignition temperatures, the results from the Sarathy model predict a noticeable offset between *n*-butanol and *iso/sec*-butanol. This behavior

suggests appreciable differences in the modeled fuel breakdown chemistry, a subject that will be explored further in due course. Finally, the crossover between the *iso*- and *sec*-butanol results observed experimentally is reproduced by the numerical results, with both the crossover pressure and the difference between the two isomers at 1 and 4 atm closely matching those seen experimentally. This suggests that while overall the ignition temperatures are shifted upwards relative to the experimental data, the Sarathy model nonetheless captures some of the isomer-specific differences in terms of pressure-dependent reactions.

To begin to explore some of the above observations, a sensitivity analysis is conducted for reaction rates (by perturbing pre-exponential factors, A_i 's) and binary diffusion coefficients (by perturbing the zeroth-order coefficients of the polynomial fits for D_{jk} 's) defined as $S_{Ai} = \frac{\partial \ln T_{ig}}{\partial \ln A_i}$ and $S_{D_{jk}} = \frac{\partial \ln T_{ig}}{\partial \ln D_{jk}}$, respectively. Figures 7–10 demonstrate the ten largest reaction rate and transport sensitivity coefficients for all four butanol isomers, computed at the ignition turning points for 1 and 4 atm pressures, $k' = 350 \text{ s}^{-1}$, and $X_f = 0.15$, ranked by the sensitivity magnitude at 4 atm. Similar to the results previously discussed by the authors [27], for each isomer the sensitivity analysis of binary diffusion coefficients demonstrates significant sensitivity to the N_2 -butanol and O_2 -butanol transport rates as well as those of several important intermediates. Of particular note is the consistent importance of butene isomers ($1\text{-C}_4\text{H}_8$, $2\text{-C}_4\text{H}_8$, and $i\text{C}_4\text{H}_8$) in the transport sensitivity analysis for each of the butanol isomers. Sarathy *et al.* [25] attributed the lower experimental laminar flame speeds of *iso*- and *tert*-butanol relative to *n*-butanol to the predominance of *iso*-butene ($i\text{C}_4\text{H}_8$), and additionally noted that the branching ratios for isomerization and beta-scission of hydroxybutyl radicals warranted improvement to better predict the formation of butene isomers. Indeed, deficiencies were noted compared to both low-pressure flame speciation and JSR experiments. As a result, the persistent appearance of butene

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4 isomers in the present analysis suggests that further investigation of their role in counterflow
5 ignition merits further examination, and will be discussed in more detail in conjunction with path
6 analyses in due course.
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11 Examination of reaction rate sensitivity analyses in Figs. 7–10 demonstrates additional
12 differences associated with differing isomerism. Comparing amongst the positional isomers (*n*-
13 butanol and *sec*-butanol), noticeable correspondence is apparent in terms of the sensitive reaction
14 rates, with both isomers primarily exhibiting sensitivity to H₂/C₁ chemistry. In contrast, while the
15 branched chain isomers (*iso*-butanol and *tert*-butanol) also exhibit sensitivity to H₂/C₁ chemistry,
16 a number of reactions involved in the early stages of fuel breakdown also appear in the
17 sensitivity analysis. For *iso*-butanol, this includes the initial H-abstraction from the α and γ sites,
18 as well as subsequent H-abstraction and scission reactions from the α -hydroxybutyl radical.
19 Similarly, *tert*-butanol displays substantial sensitivity to fuel breakdown reactions through both
20 *iso*-butene and propen-2-ol (CH₂=COHCH₃) pathways. Interestingly, for both branched chain
21 isomers the fuel breakdown reactions display appreciable pressure sensitivity in contrast to the
22 positional isomers where – with the exception of hydrogen peroxide decomposition and H-
23 abstraction from the parent fuel via hydroperoxyl – most reactions display comparatively less
24 pressure sensitivity. This difference may account for the different variation of ignition
25 temperature with pressure between the positional and branched chain isomers observed in the
26 numerical results.
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29 Figures 11–14 show spatially-integrated path flux analyses at the ignition turning point for
30 the butanol isomers at $k' = 350 \text{ s}^{-1}$, $X_f = 0.15$, and atmospheric pressure. In agreement with the
31 sensitivity analysis, the butene isomers feature prominently in the initial fuel breakdown steps for
32 all butanol isomers, albeit to differing extents. The path analysis for *n*-butanol (Fig. 11) shows
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that the majority of the 1-butene produced is through β -hydroxybutyl radical decomposition, with a minor pathway to 1-butene directly from *n*-butanol. In comparison, noticeably more butenes production is apparent in the flux maps of the other isomers. Approximately 6% of *iso*-butanol (Fig. 12) is converted directly to *iso*-butene, and ~80% of the β -hydroxybutyl radical is consumed through decomposition to *iso*-butene. The *sec*-butanol analysis (Fig. 13) shows significant paths to both 1-butene and 2-butene through the β -hydroxybutyl radicals, as well as minor pathways to each directly from the parent fuel. Finally, the overwhelming majority of *tert*-butanol consumption (Fig. 14) occurs through *iso*-butene, either directly from the parent fuel or via the hydroxybutyl radical. Interestingly, the ignition temperature ranking of the isomers at 1 atm based on the Sarathy model – *n*-butanol < *iso*-butanol < *sec*-butanol < *tert*-butanol – correlates well with the relative production of butenes by each isomer. This correspondence suggests that the butene chemistry plays a significant role in prescribing the ignition temperature trends observed amongst the butanol isomers, specifically their relative ranking in terms of ignition temperature, and may account for the disparity observed between experimental and numerical results when comparing *n*-butanol with *iso/sec*-butanol. This possibility will be explored in more detail in Section 3.5.

3.4 Numerical results from the Merchant model

Figure 15 compares the numerical results derived from the MN, MS, and MT mechanisms to the experimentally obtained ignition temperatures for $k' = 350 \text{ s}^{-1}$, $X_f = 0.15$, and $P = 1-4 \text{ atm}$. As mentioned in Section 2.4.2, *iso*-butanol results are not shown due to the inability of the MARS reduction package or the ignition code to interpret the aforementioned *iso*-butanol decomposition reaction in its current PLOG form. The corresponding results using the skeletal Sarathy mechanisms are also shown in Fig. 15 for comparison. Similar to the results in the previous

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4 section, the skeletal Merchant mechanisms universally over-predict experimental ignition
5 temperatures – in this case by ~100–190 K. In addition, the MS mechanism predicts *sec*-butanol
6 ignition temperatures offset from the *n*-butanol results predicted using the MN mechanism by
7 20–40 K, with the disparity rising as pressure increases. In fact, based on the skeletal Merchant
8 mechanisms, the *sec*-butanol results are more similar in magnitude to those for *tert*-butanol, and
9 exhibit the highest ignition temperatures for pressures above ~ 2 atm. This behavior runs counter
10 to the experimental results, where *tert*-butanol consistently ignites at appreciably higher
11 temperatures than the other three isomers, which ignite at largely similar temperatures for most
12 operating conditions. Unlike the results from the skeletal Sarathy mechanisms, *sec*-butanol and
13 *n*-butanol are not predicted to exhibit similar ignition temperature variation with pressure in the
14 Merchant model, which in fact seems to capture a slight divergence in ignition temperature trend
15 observed experimentally between the two isomers at elevated pressures.
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18 Sensitivity analyses of the ten largest reaction rate and transport sensitivity coefficients for
19 *n*-, *sec*-, and *tert*-butanol isomers are shown in Figs. 16–18, respectively. The results are largely
20 similar to those obtained using the skeletal Sarathy mechanisms, with the positional isomers
21 exhibiting sensitivity to many of the same reactions and *tert*-butanol showing strong sensitivity
22 to early-stage fuel breakdown reactions. Also similar to the results of the previous section, a
23 consistent dependence upon the transport of butene isomers is observed. However, there are
24 some notable differences. The *n*-butanol results (Fig. 16) demonstrate sensitivity to H-abstraction
25 from the fuel molecule via hydroperoxyl to form β -hydroxybutyl, as compared to the SN
26 mechanism which exhibits sensitivity to abstraction at the α -carbon. In addition, the MN
27 mechanism is noticeably less sensitive to the chain-branching $H + O_2 \leftrightarrow O + OH$ reaction at 1
28 atm relative to the SN mechanism.
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With regards to *sec*-butanol (Fig. 17), while the reaction rate sensitivity results are quite similar aside from minor differences in coefficient magnitude, the MS mechanism exhibits a greater degree of sensitivity to the transport properties of both 1-butene and 2-butene. Also of interest is the presence of propen-2-ol in the transport sensitivity analysis of Fig. 17(b). As pointed out by Sarathy *et al.* [25], the allylic radical of propen-2-ol exhibits resonant stabilization characteristics and thus is expected to be relatively unreactive. Since path analysis on the MS mechanism predicts that almost a quarter of propen-2-ol is consumed to form the allylic radical at both 1 and 4 atm, the relatively large negative transport sensitivity of propen-2-ol may indicate that enhanced transport results in migration of propen-2-ol to locations where alternative pathways – e.g., tautomerization to acetone – become more prevalent, thus avoiding the less reactive allylic radical pathway.

Sensitivity results for *tert*-butanol (Fig. 18) also display significant similarities to the ST mechanism, with *iso*-butene, propen-2-ol, and acetone featuring prominently in the transport sensitivity analysis, and reactions related to *iso*-butene comprising a significant proportion of the most sensitive reaction rates. Of note in the reaction rate sensitivity analysis shown in Fig. 18(a) is the sign change in the sensitivity coefficient for the water elimination reaction from *tert*-butanol: $tC_4H_9OH \leftrightarrow iC_4H_8 + H_2O$. While at atmospheric conditions an increase in this reaction rate tends to inhibit ignition, at 4 atm this trend reverses, suggesting a significant pressure-dependent change in this important fuel breakdown reaction. This strong pressure dependence may be partially responsible for the growing disparity between the two numerical sets of *tert*-butanol results as pressure increases.

Furthermore, for the sensitive reactions related to H₂/C₁–C₂ chemistry shown in Figs. 7–10 and Figs. 16–18, their reaction rates over a temperature range relevant to the present study are

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4 compared between the Sarathy and Merchant models. This comparison shows that the reaction
5 rates of most of them are quite similar except that noticeable differences exist for the reactions of
6 $C_2H_3 + O_2 \leftrightarrow CH_2CHO + O$ and $OH + C_2H_4 \leftrightarrow C_2H_3 + H_2O$. It should be highlighted that
7 replacing the rate coefficients for these two reactions in the Sarathy model with those from the
8 Merchant model results in better agreement between the two models. However, a significant
9 disparity remains, suggesting that additional differences exist in the C₂ sub-mechanism between
10 the Sarathy and Merchant models.
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13 To investigate the isomeric differences further, path analyses at the ignition turning point for
14 *n*-, *sec*-, and *tert*-butanol using the MN, MS, and MT mechanisms are shown in Fig. 19 for 1 atm,
15 $k' = 350 \text{ s}^{-1}$, and $X_f = 0.15$. As was the case in the previous section, the butene isomers figure
16 prominently in the path analysis for each isomer, with the molar flux proceeding through butene
17 pathways roughly correlating to the trend in ignition temperature (at 1 atm), namely *n*-butanol <
18 *sec*-butanol < *tert*-butanol. However, several noteworthy differences are apparent in the path
19 analyses of *sec*-butanol (Fig. 19(b)) and *tert*-butanol (Fig. 19(c)). First, while the MS and SS
20 mechanisms predict a similar flux of parent fuel to the α -hydroxybutyl radical (27% versus
21 29.3%, respectively) as well as the same major products (propen-2-ol and methyl radical or 2-
22 butanone), the branching ratios from the α -hydroxybutyl radical are nearly reversed. Whereas the
23 MS mechanism predicts 39.4% of α -hydroxybutyl is converted to propen-2-ol and 60% to 2-
24 butanone, the SS mechanism predicts 74.8% proceeds to propen-2-ol while only 23.1% is
25 converted to 2-butanone. It is worth noting that unlike the MS mechanism, the SS mechanism
26 does not contain a pathway to propen-2-ol's allylic radical. Second, the molar flux through 1-
27 butene and 2-butene pathways is significantly larger in the MS mechanism. Nearly 55% of the
28 parent fuel in the MS mechanism is consumed through butene-related pathways – either directly
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4 from *sec*-butanol via water elimination or indirectly via the β -hydroxybutyl radicals – as
5 compared to 12% in the SS mechanism. As other pathways are largely similar between the two
6 mechanisms, the large difference in the level of butene involvement is likely responsible for the
7 differences observed between the *sec*-butanol ignition temperatures for the MS and SS
8 mechanisms.
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11 Comparing the MT mechanism path analysis results (Fig. 19(c)) to those of the ST
12 mechanism (Fig. 14), it can be seen that the MT mechanism predicts somewhat more water
13 elimination to directly form *iso*-butene while forming relatively less hydroxybutyl and almost no
14 hydroxypropyl radicals. The MT mechanism also predicts less conversion of hydroxybutyl to
15 *iso*-butene, instead favoring more production of propen-2-ol. The resulting total molar flux
16 through *iso*-butene pathways is fairly similar between the two mechanisms (~62% in the MT
17 mechanism compared to ~69% in the ST Mechanism), which likely accounts for the quite similar
18 predictions in terms of ignition temperatures at 1 atm. However, as pressure increases the
19 predicted ignition temperatures begin to diverge, with the MT mechanism predicting *tert*-butanol
20 ignition temperature ~ 20 K higher than the ST mechanism at 4 atm. This difference is attributed
21 to a significant increase in the importance of the ROOH pathway in the MT mechanism as a
22 result of a simultaneous rise in the proportion of *tert*-butanol reduced to hydroxybutyl (46% at 1
23 atm versus 68.5% at 4 atm) and a tripling of the branching ratio from hydroxybutyl to *iso*-
24 butenyl hydroperoxide (9.5% at 1 atm versus 34.8% at 4 atm), as shown in Fig. 19(c). The ST
25 mechanism shown in Fig. 14, in contrast, does not contain this pathway from hydroxybutyl, and
26 the branching ratios to *iso*-butene and propen-2-ol remain quite similar between 1 and 4 atm.
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4 *3.5 Potential areas for model improvement*
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3.5 Potential areas for model improvement

The preceding discussion has highlighted a number of important points regarding the differences between the Sarathy *et al.* [25] and Merchant *et al.* [23] models. First, the transport parameters for *iso*-/*sec*-/*tert*-butanol in the Sarathy model – despite describing unreasonably fast fuel diffusion – still cannot account for the disparity between the numerical and experimental data. Furthermore, despite utilizing identical butanol isomer transport parameters, significant differences remain between the Sarathy and Merchant models. These observations suggest that, while the transport model is unquestionably important to the accurate prediction of ignition temperatures, modifications to transport parameters can resolve neither the disparity between the numerical results and the experimental data, nor the differences observed between the Sarathy and Merchant models. This leads to the conclusion that these discrepancies must result from the chemical kinetics. Second, when the skeletal mechanisms from each model are compared, appreciable differences in the fuel breakdown pathways can be observed. For example, as has been discussed at length in previous study [27], the breakdown of *n*-butanol differs substantially between the Sarathy and Merchant models, including significant variations in the predicted branching ratios to both γ - and δ -hydroxybutyl (cf. Figs. 11 and 19(a)) as well as the presence of additional pathways involving enols/aldehydes in the Merchant model. With regards to *sec*-butanol, despite describing largely similar chemical pathways and predicting mostly similar branching ratios directly from the parent fuel, path analysis reveals that approximately 5 times more *sec*-butanol is consumed through butene pathways in the Merchant model relative to the Sarathy model. Moreover, the butene pathways themselves differ substantially. Path analysis reveals that both the branching ratios from the butene isomers as well as the subsequent breakdown pathways are dramatically different. In fact, as a proxy for estimating reactivity,

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4 additional ignition turning point calculations using butene isomers as a fuel are conducted with
5 both models, showing that 1- and 2-butene ignition occur at 88 K and 108 K higher temperatures,
6 respectively, at atmospheric pressure in the Merchant model. Combined with the increased flux
7 through butene pathways, the differing descriptions for butene breakdown likely accounts for the
8 sec-butanol ignition temperature disparity observed between the two models, and likely
9 contributes to differences observed for other isomers as well. Finally, even where substantial
10 agreement exists between the models' ignition temperature predictions – i.e. atmospheric *tert*-
11 butanol ignition (cf. Fig. 15) – the matching appears to be somewhat serendipitous. As
12 demonstrated for *tert*-butanol by Figs. 14 and 19(c), even under atmospheric conditions the
13 branching ratios from the hydroxybutyl radical differ dramatically, and the Merchant model even
14 includes an additional ROOH pathway from hydroxybutyl which is absent in the Sarathy model.
15 This ROOH pathway becomes significantly more important at elevated pressures, and likely is a
16 key factor resulting in the growing disparities between the two models as pressure increases.
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19 Taken as a whole, the above observations suggest that despite reasonably matching
20 experimental trends as functions of pressure-weighted strain rate, fuel loading, and pressure,
21 substantial uncertainties remain in the description of combustion chemistry of the butanol
22 isomers. Based upon the above analysis, it is likely that the disparities between the experimental
23 and numerical results cannot be resolved without additional specification of the nature of both
24 butanol and butene breakdown chemistry. With regards to fuel breakdown, Vasu and Sarathy
25 [42] provided minor updates to *n*-butanol unimolecular decomposition reactions based on the
26 shock tube study of Rosado-Reyes and Tsang [43], and additionally increased the rate constant
27 for H-abstraction from formaldehyde, showing slightly improved matching with the data of
28 Stranic *et al.* [20]. In a recent review of alcohol combustion chemistry, Sarathy *et al.* [41] also
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4 pointed out that significant uncertainties remain in the description of H-abstraction reactions
5 from the butanol isomers, particularly by OH and HO₂. Although site-specific OH-abstraction
6 reaction rates developed by McGillen *et al.* [44] were suggested as a possible avenue of
7 improvement, these reaction rates had yet to be implemented into a combustion model.
8 Additional uncertainties exist with regards to abstraction by HO₂, for which no experimental
9 measurements are currently available [41]. Regarding modeling of butene pathways, its sub-
10 mechanism itself is an area of current research. For example, a recent study by Schenk *et al.* [45]
11 experimentally explored the behavior of the butene isomers in a low-pressure premixed flame
12 configuration and made improvements to an existing hydrocarbon model [46] based upon their
13 results. However, a subsequent study of the ignition of butene isomers in non-premixed
14 counterflow by Zhao *et al.* [47] discovered significant discrepancies between their experimental
15 data and the model of Schenk *et al.* [45], and subsequently developed their own butene model
16 which exhibited somewhat improved performance. Taking the above into consideration, it is
17 anticipated that further study of the isomer-specific branching ratios (particularly better
18 understanding of H-abstraction reactions) and the development of comprehensive butene
19 chemistry can help to close the gap between the models, as well as resolve discrepancies between
20 the models and the experimental data. Furthermore, recognizing that the two models do not share
21 the same C₁–C₂ sub-mechanism, the foundation fuel chemistry could also play some role in the
22 disparities observed between the Sarathy and Merchant models.
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4. Conclusions

5 The present study comprehensively explores the ignition temperature trends of the four butanol
6 isomers as a function of pressure-weighted strain rate ($k' = 200\text{--}400\text{ s}^{-1}$), fuel loading ($X_f = 0.05\text{--}$
7 0.25), and pressure ($P = 1\text{--}4\text{ atm}$) in a non-premixed counterflow configuration. These trends are
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4 compared to numerical results derived from isomer-specific skeletal mechanisms developed from
5 two comprehensive butanol models available in the literature. While these mechanisms largely
6 capture the experimentally-observed trends, they universally over-predict the experimental data
7 to an appreciable extent. Additionally, for both sets of skeletal mechanisms the “ranking” of
8 isomers in terms of predicted ignition temperatures deviates significantly from the experimental
9 results. Whereas the experimental *n*-/*iso*-/*sec*-butanol results all lie in close proximity to each
10 other, the Sarathy *et al.*-based [25] and Merchant *et al.*-based [23] skeletal mechanisms predict
11 significant separation amongst these isomers. Both ST and MT mechanisms predict largely
12 similar *tert*-butanol ignition temperatures, although the disparity increases as pressure is raised
13 from atmospheric pressure to 4 atm. Detailed sensitivity and path analyses suggest that the
14 butene isomers may play a significant role in determining the relative levels of reactivity
15 between the butanol isomers, as the relative reactivity of the butanol isomers correlates well with
16 the relative amounts of parent fuel consumed through butene pathways. These trends suggest that
17 the disparities between simulated results from the different base chemical kinetic models may be
18 the result of differing butene chemistry, and that further work is necessary to better define both
19 the branching ratios of reactions leading from the parent fuel to the butene isomers and the
20 subsequent butene chemistry itself.
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Table and Figure Captions

Table 1: Number of species and reactions contained within the detailed and skeletal mechanisms used in this study.

Figure 1: Ignition turning point validation comparing the results computed from the isomer-specific skeletal mechanisms to those of the detailed Sarathy *et al.* [25] and Merchant *et al.* [23] mechanisms. Turning points for (a) *n*-butanol (b) *iso*-butanol (c) *sec*-butanol, and (d) *tert*-butanol are computed at $X_f=0.15$ for 1 atm, $k'=300\text{ s}^{-1}$ and 5 atm, $k'=500\text{ s}^{-1}$. In (b), only the results based on the Sarathy model are shown (cf. Section 2.4.1).

Figure 2: Experimental ignition temperatures for the butanol isomers at $P=1$ and 3 atm, $X_f=0.15$, as a function of pressure-weighted strain rate. Ignition temperature error bars represent the random error of $\pm 5\text{ K}$, while pressure-weighted strain rate error bars represent the total estimated uncertainty.

Figure 3: Experimental ignition temperatures for the butanol isomers at $P=1$ and 3 atm, $k'=350\text{ s}^{-1}$ as a function of fuel loading. Ignition temperature error bars represent the random error of $\pm 5\text{ K}$, while fuel loading error bars represent the total estimated uncertainty.

Figure 4: Experimental ignition temperatures for the butanol isomers at $X_f=0.15$ and $k'=350\text{ s}^{-1}$ as a function of pressure. Ignition temperature error bars represent the random error of $\pm 5\text{ K}$, while pressure error bars represent the total estimated uncertainty.

Figure 5: Demonstration of the effect of modifying the Lennard-Jones transport parameters for *iso*-/*sec*-/*tert*-butanol and C_4 intermediates related to the parent fuel breakdown in the Sarathy *et al.* [25] to the matching parameters listed in Merchant *et al.* [23]. Conditions: $P=3\text{ atm}$ and $k'=350\text{ s}^{-1}$. Experimental data are also included for reference.

Figure 6: Comparison between experimental data and numerical predictions using the SN/SI/SS/ST skeletal mechanisms as a function of pressure for $X_f=0.15$, $k'=350\text{ s}^{-1}$.

Figure 7: Normalized (a) reaction rate and (b) binary diffusion sensitivity coefficients for *n*-butanol computed at $P=1$ and 4 atm, $k'=350\text{ s}^{-1}$, $X_f=0.15$ at the ignition turning point for the SN skeletal mechanism.

Figure 8: Normalized (a) reaction rate and (b) binary diffusion sensitivity coefficients for *iso*-butanol computed at $P=1$ and 4 atm, $k'=350\text{ s}^{-1}$, $X_f=0.15$ at the ignition turning point for the SI skeletal mechanism.

Figure 9: Normalized (a) reaction rate and (b) binary diffusion sensitivity coefficients for *sec*-butanol computed at $P=1$ and 4 atm, $k'=350\text{ s}^{-1}$, $X_f=0.15$ at the ignition turning point for the SS skeletal mechanism.

Figure 10: Normalized (a) reaction rate and (b) binary diffusion sensitivity coefficients for *tert*-butanol computed at $P=1$ and 4 atm, $k'=350\text{ s}^{-1}$, $X_f=0.15$ at the ignition turning point for the ST skeletal mechanism.

Figure 11: Spatially-integrated path analysis for *n*-butanol at $P=1\text{ atm}$, $k'=350\text{ s}^{-1}$, $X_f=0.15$, evaluated at the ignition turning point using the SN skeletal mechanism.

Figure 12: Spatially-integrated path analysis for *iso*-butanol at $P=1\text{ atm}$, $k'=350\text{ s}^{-1}$, $X_f=0.15$, evaluated at the ignition turning point using the SI skeletal mechanism.

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4 Figure 13: Spatially-integrated path analysis for *sec*-butanol at $P=1$ atm, $k'=350$ s^{-1} , $X_f=0.15$,
5 evaluated at the ignition turning point using the SS skeletal mechanism.
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7 Figure 14: Spatially-integrated path analysis for *tert*-butanol at $P=1$ atm, $k'=350$ s^{-1} , $X_f=0.15$,
8 evaluated at the ignition turning point using the ST skeletal mechanism. Pathways from the
9 hydroxybutyl radical under 4 atm conditions (in bold) are also included to illustrate differences at
10 elevated pressure, as discussed in Section 3.4.
11

12 Figure 15: Comparison between experimental data and numerical predictions using the
13 MN/MS/MT skeletal mechanisms as a function of pressure for $X_f=0.15$, $k'=350$ s^{-1} . Results from
14 the SN/SS/ST skeletal mechanisms are also included for comparison purposes.
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16 Figure 16: Normalized (a) reaction rate and (b) binary diffusion sensitivity coefficients for *n*-
17 butanol computed at $P=1$ and 4 atm, $k'=350$ s^{-1} , $X_f=0.15$ at the ignition turning point for the MN
18 skeletal mechanism.
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20 Figure 17: Normalized (a) reaction rate and (b) binary diffusion sensitivity coefficients for *sec*-
21 butanol computed at $P=1$ and 4 atm, $k'=350$ s^{-1} , $X_f=0.15$ at the ignition turning point for the MS
22 skeletal mechanism.
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24 Figure 18: Normalized (a) reaction rate and (b) binary diffusion sensitivity coefficients for *tert*-
25 butanol computed at $P=1$ and 4 atm, $k'=350$ s^{-1} , $X_f=0.15$ at the ignition turning point for the MT
26 skeletal mechanism.
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28 Figure 19: Spatially-integrated path analysis at $P=1$ atm, $k'=350$ s^{-1} , $X_f=0.15$, evaluated at the
29 ignition turning point (a) for *n*-butanol using the MN skeletal mechanism, (b) for *sec*-butanol
30 using the MS skeletal mechanism, and (c) for *tert*-butanol using the MT skeletal mechanism. In
31 (c), some important pathways under 4 atm conditions (in bold) are also included to illustrate
32 differences at elevated pressure, as discussed in Section 3.4.
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<u>Mechanism</u>	<u>Number of Species</u>	<u>Number of Reactions</u>
Sarathy <i>et al.</i> (2012)	426	2335
Merchant <i>et al.</i> (2013)	372	8723
SN	126	832
SI	149	953
SS	126	929
ST	84	543
MN	102	1904
MS	108	2197
MT	117	1755

Table 1

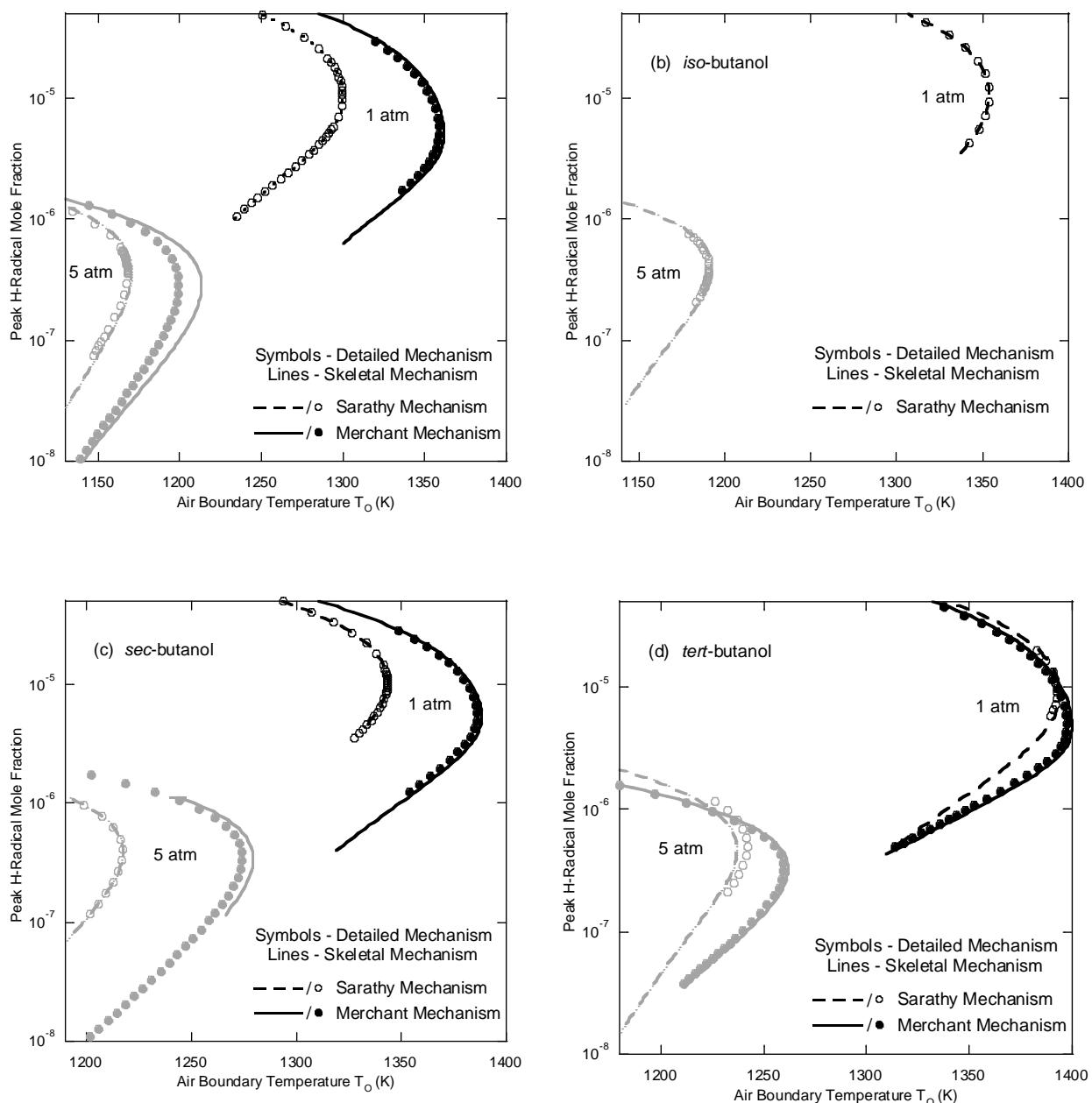


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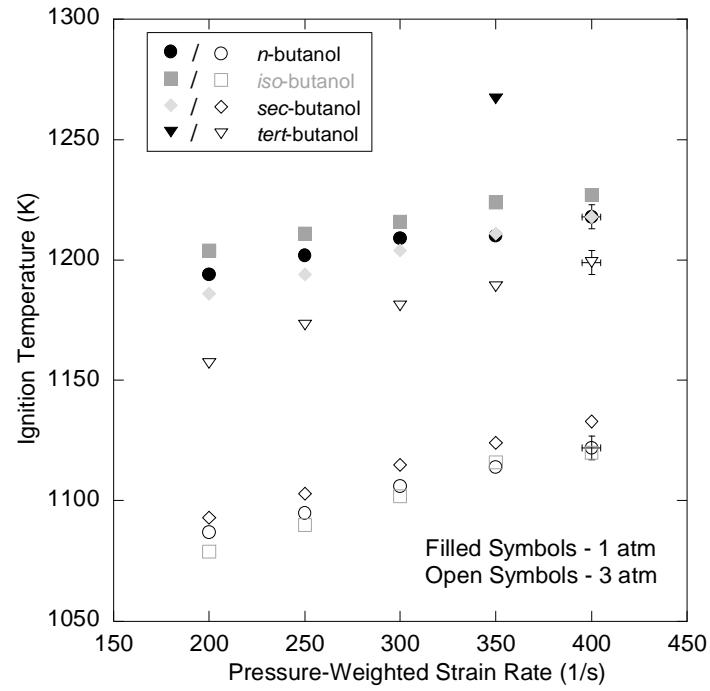


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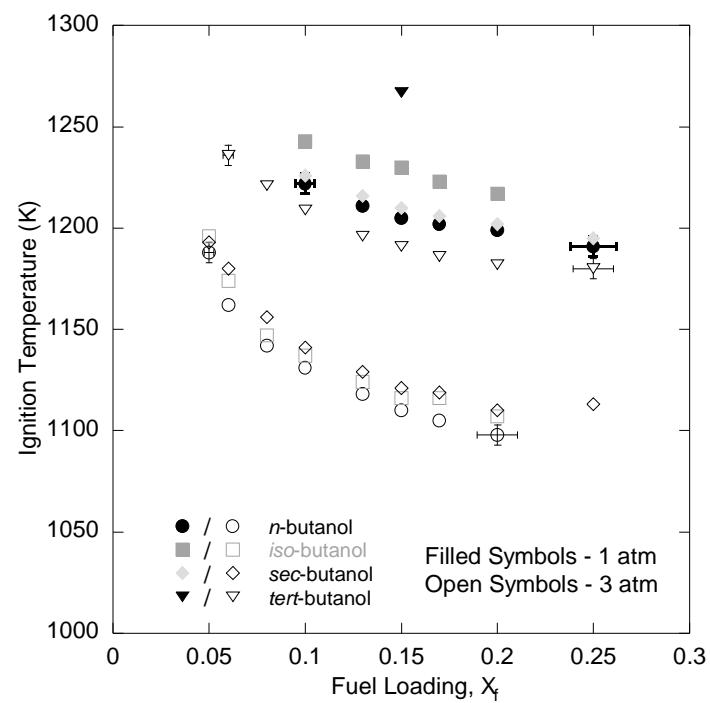


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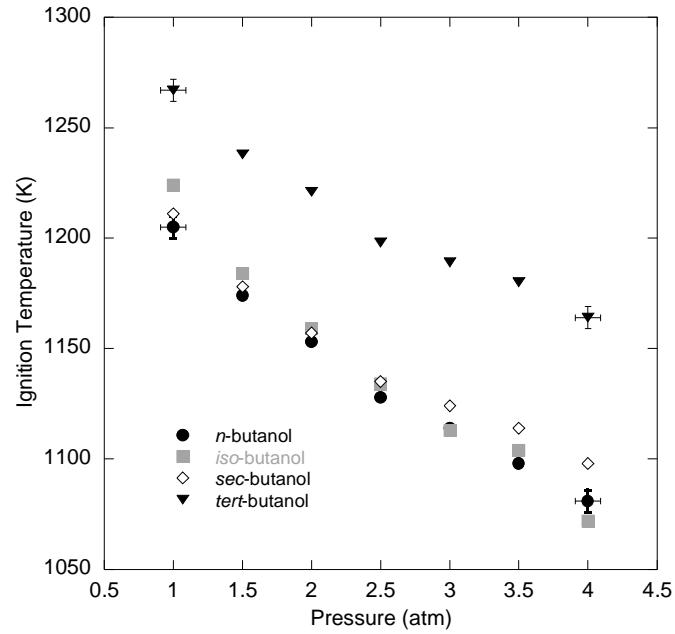


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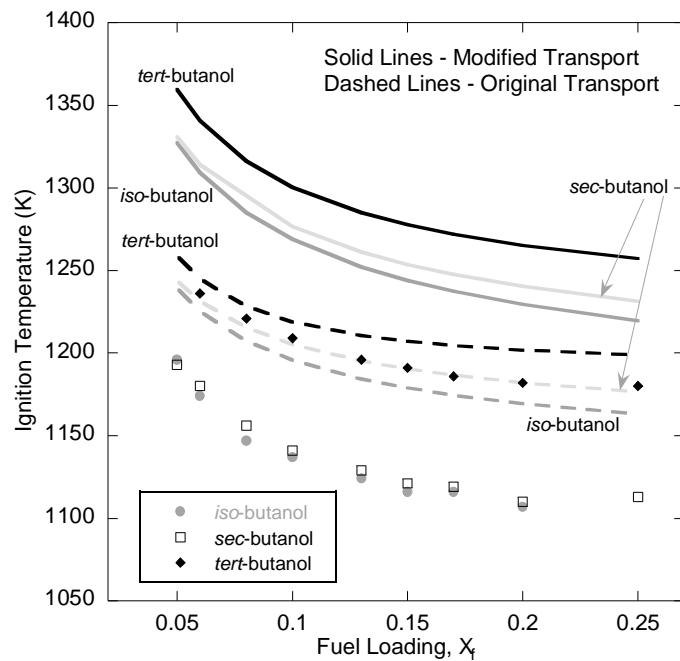


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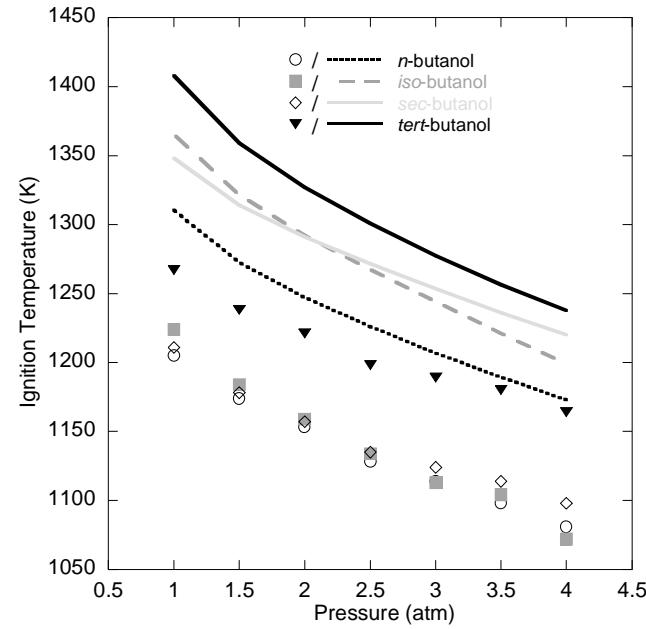


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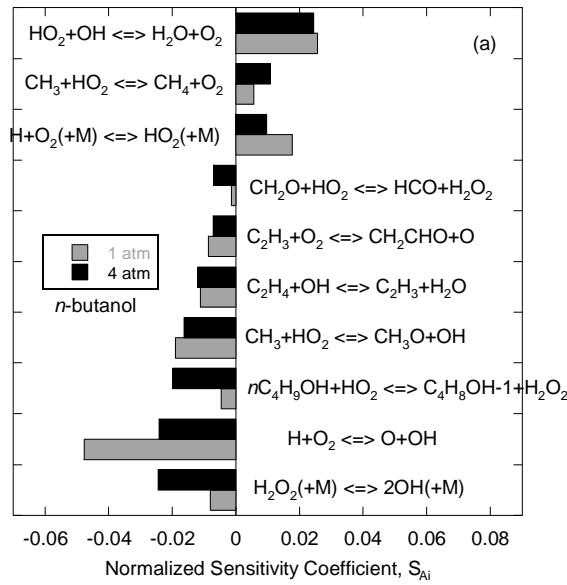


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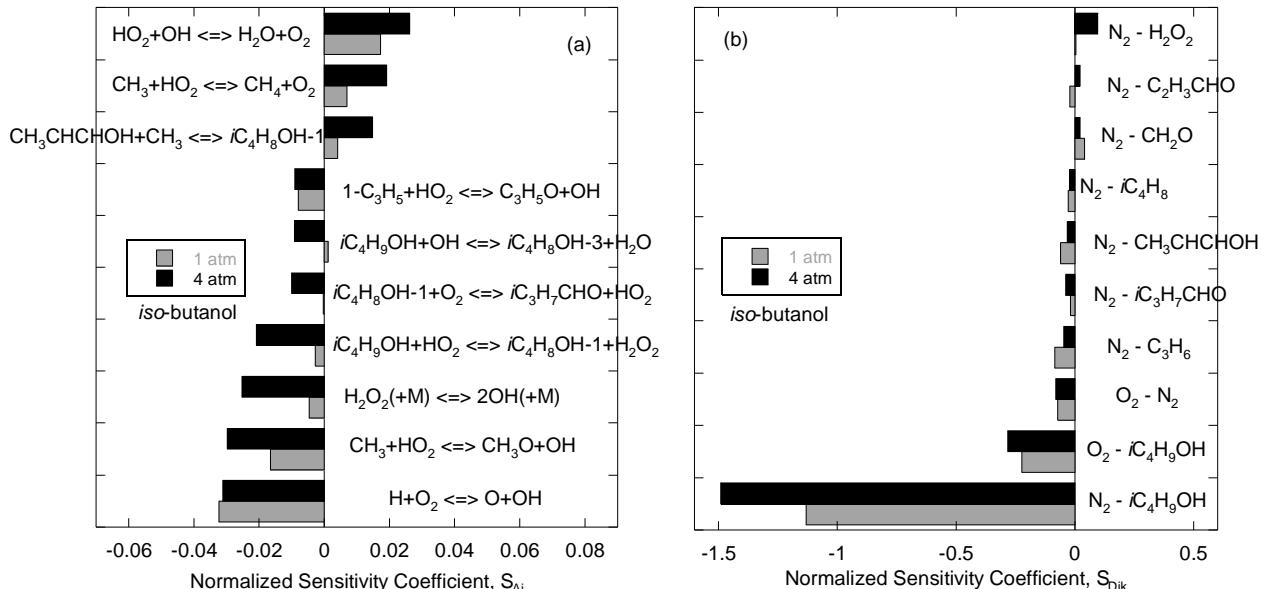


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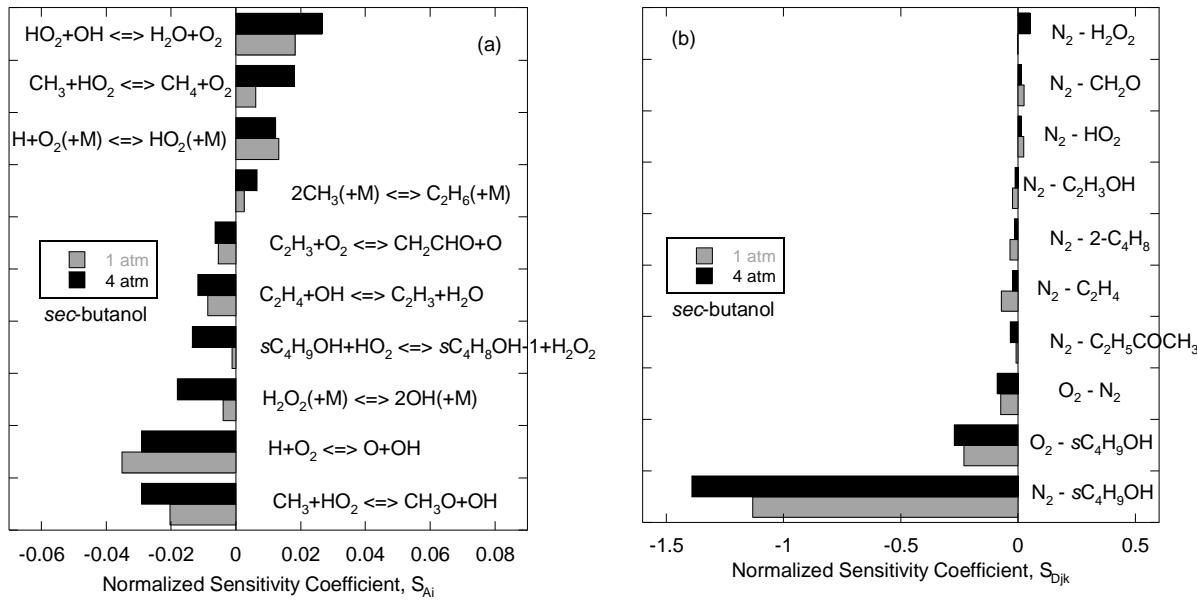


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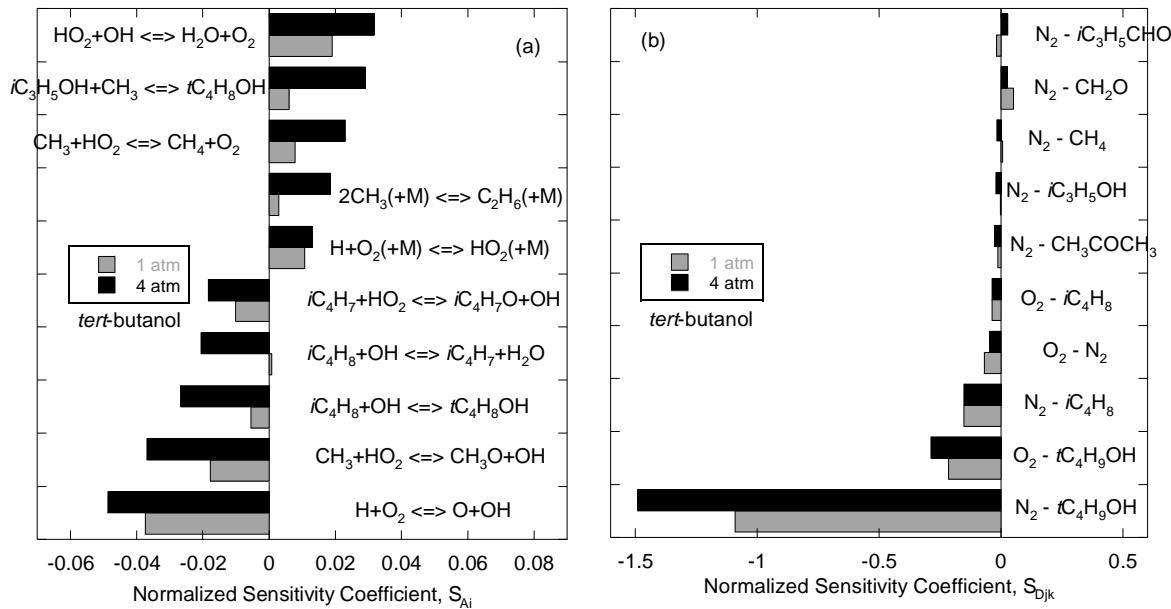
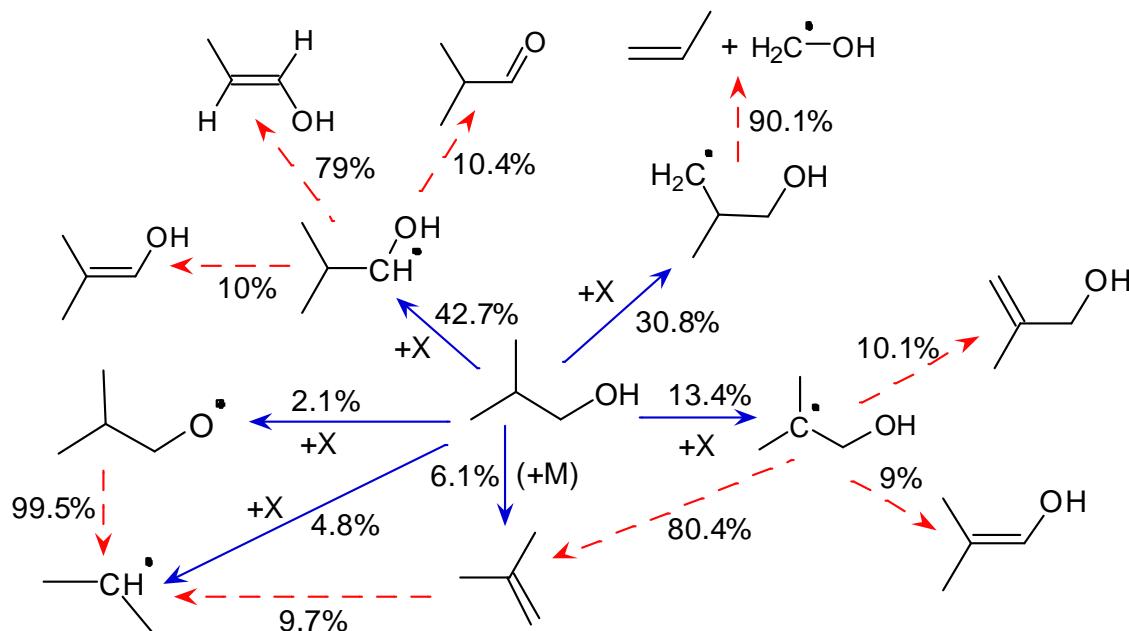
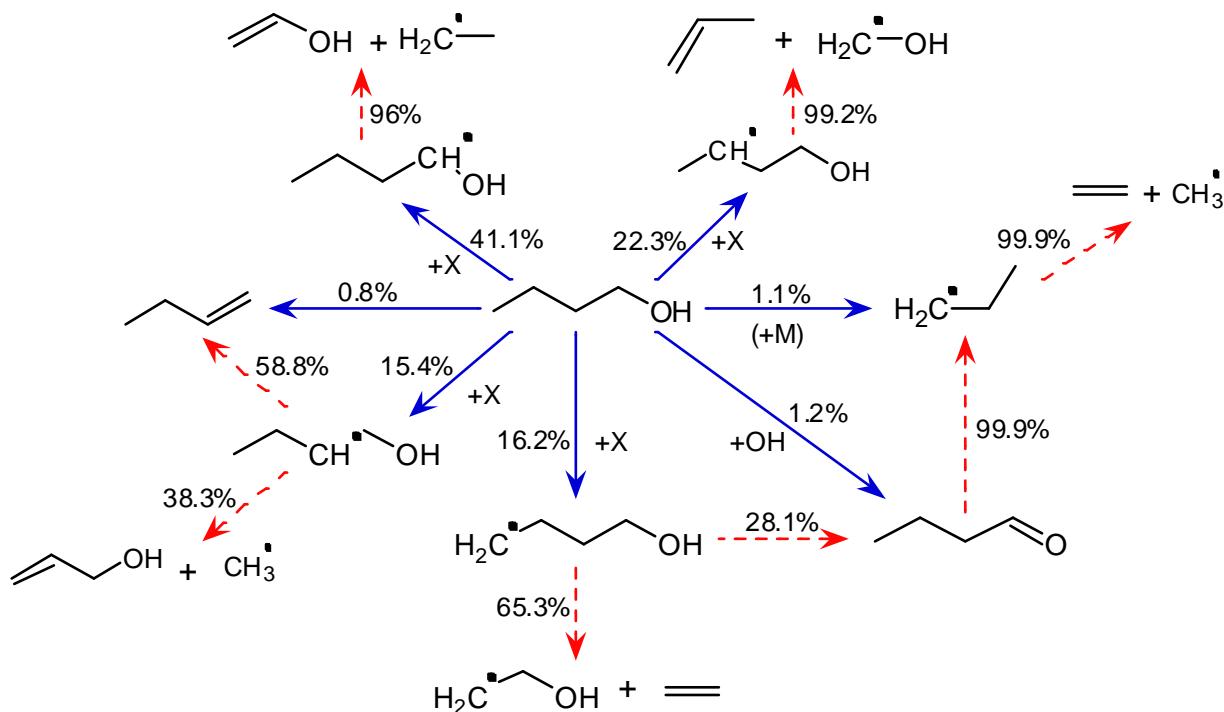


Figure 10



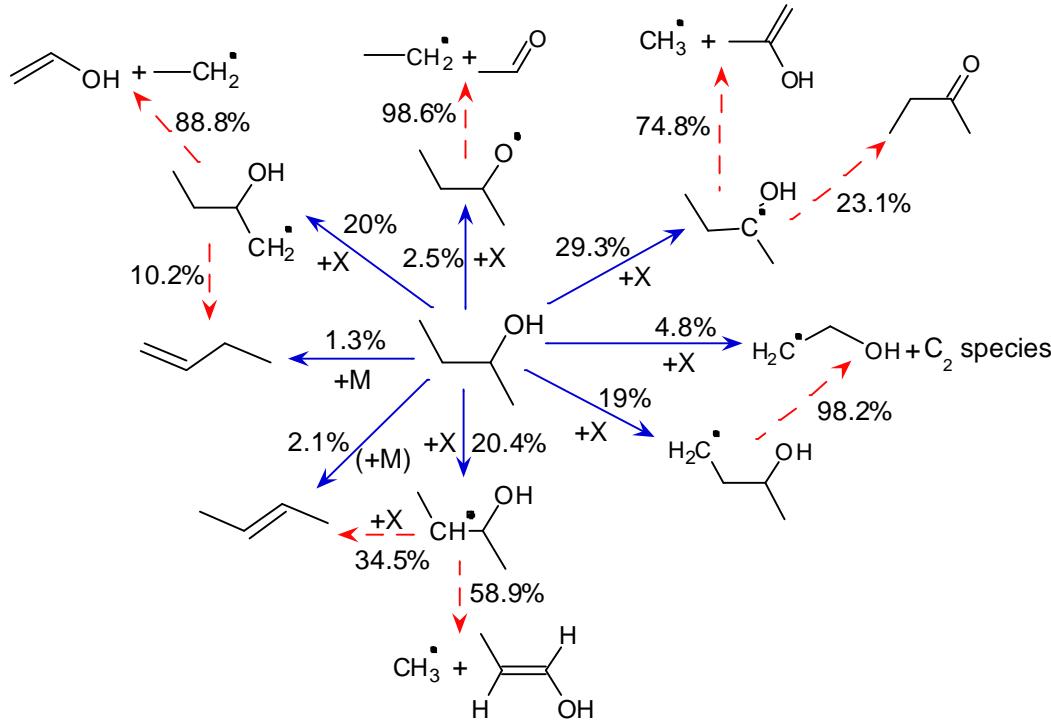


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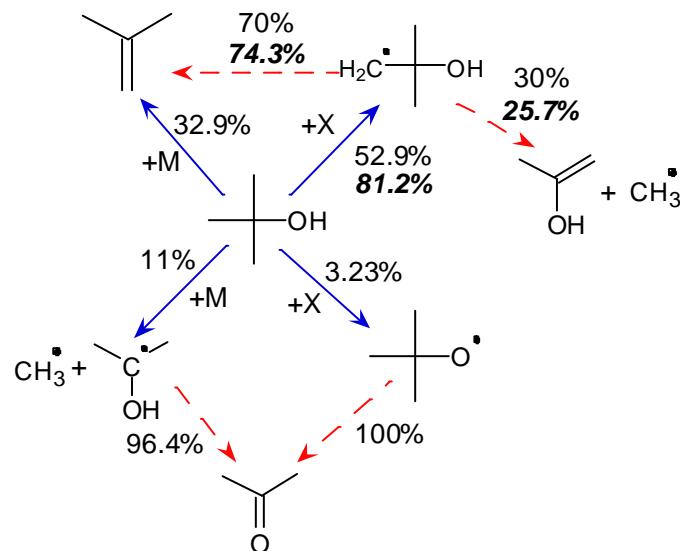


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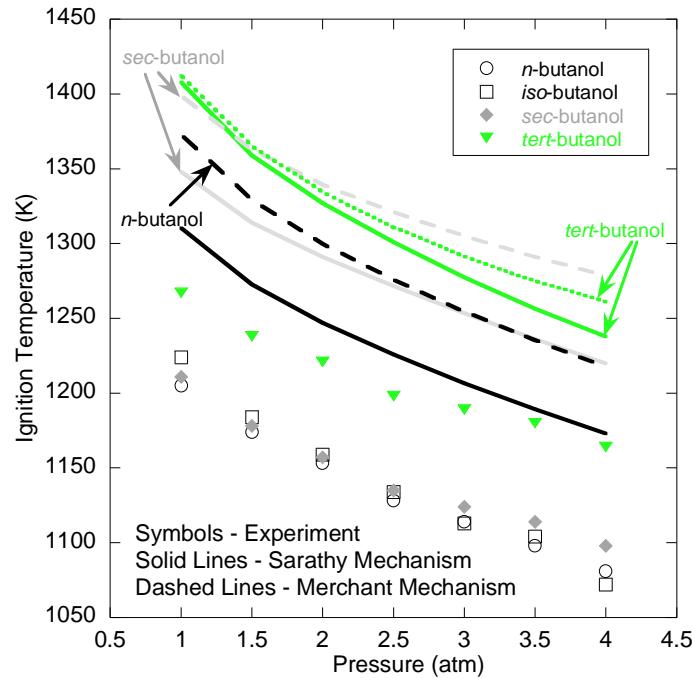


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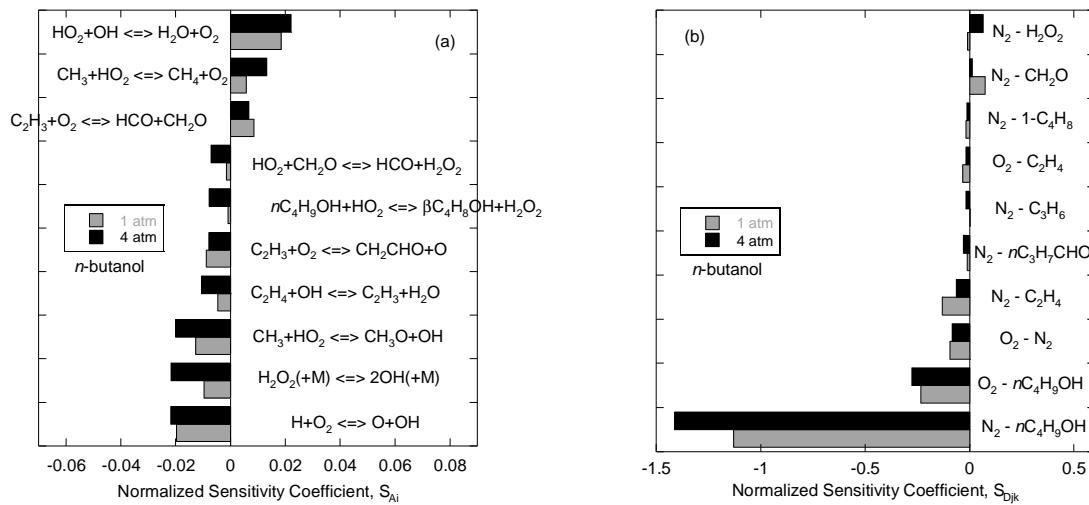


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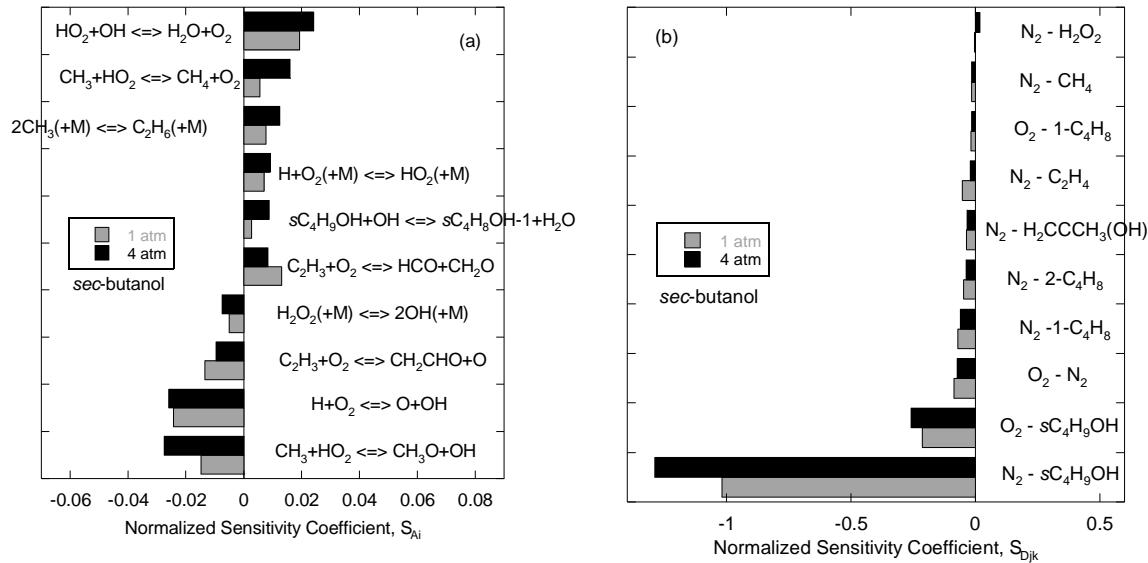


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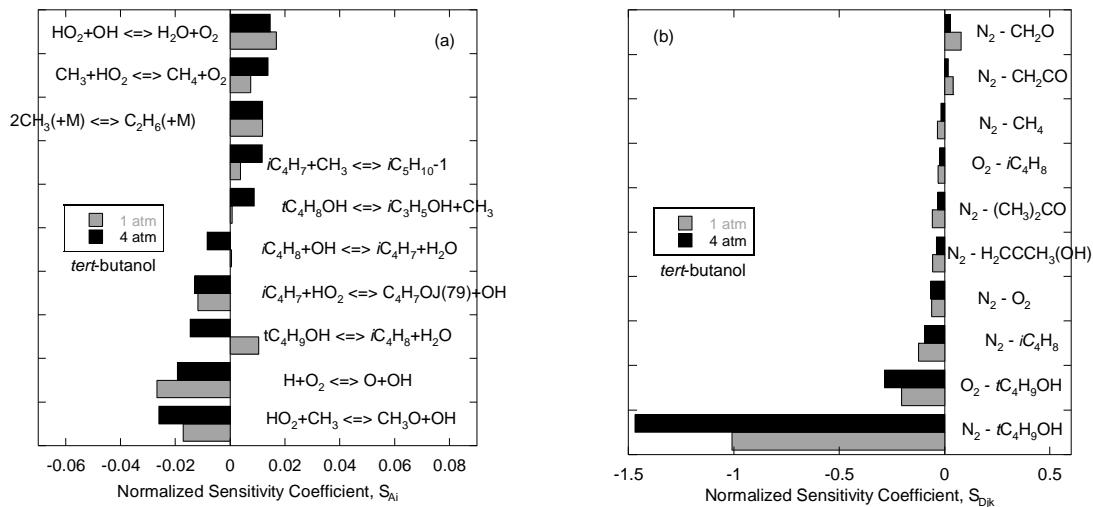


Figure 18

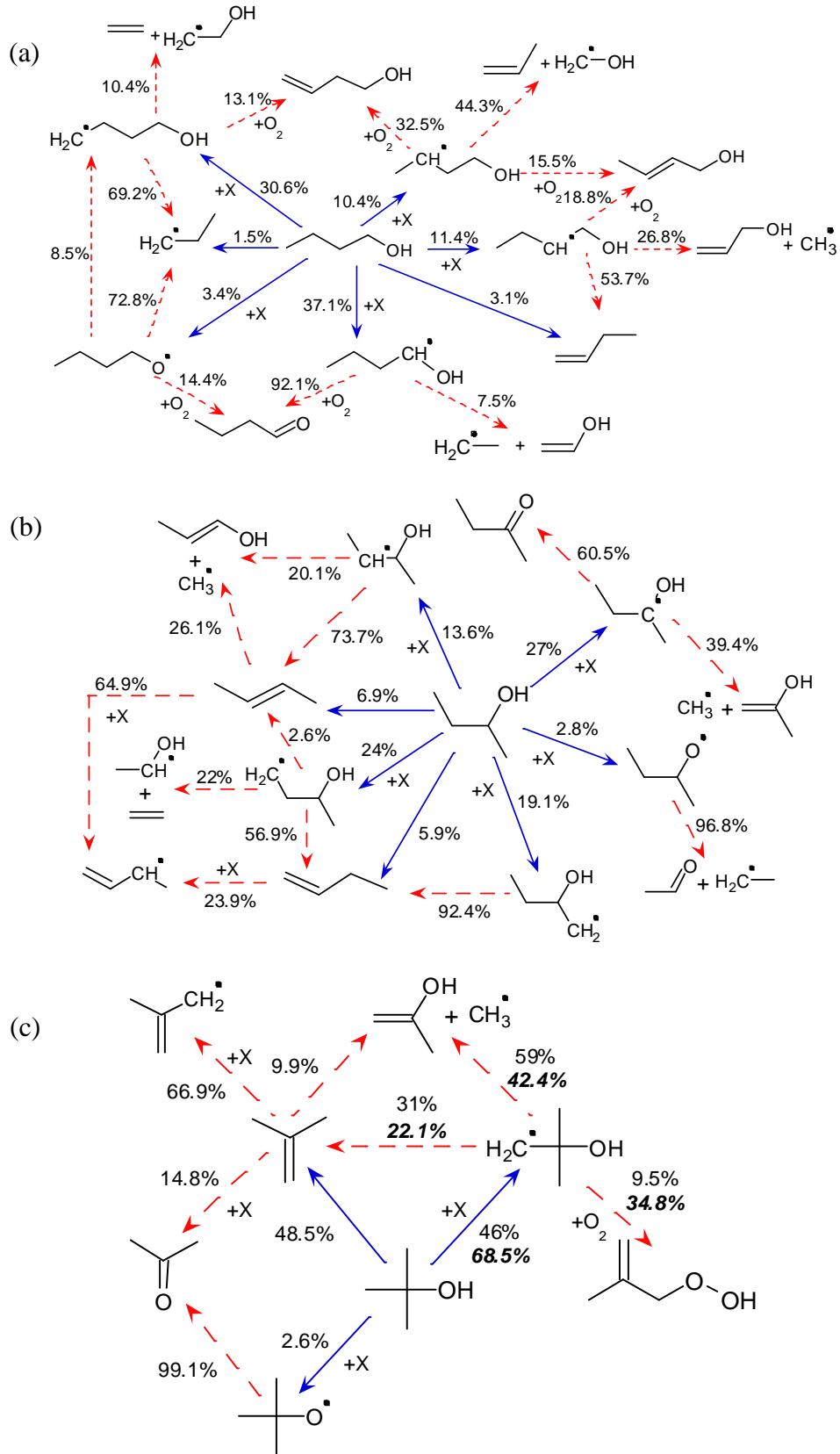


Figure 19