

# Entanglement and the Jaynes-Cummings model with Rydberg-dressed atoms

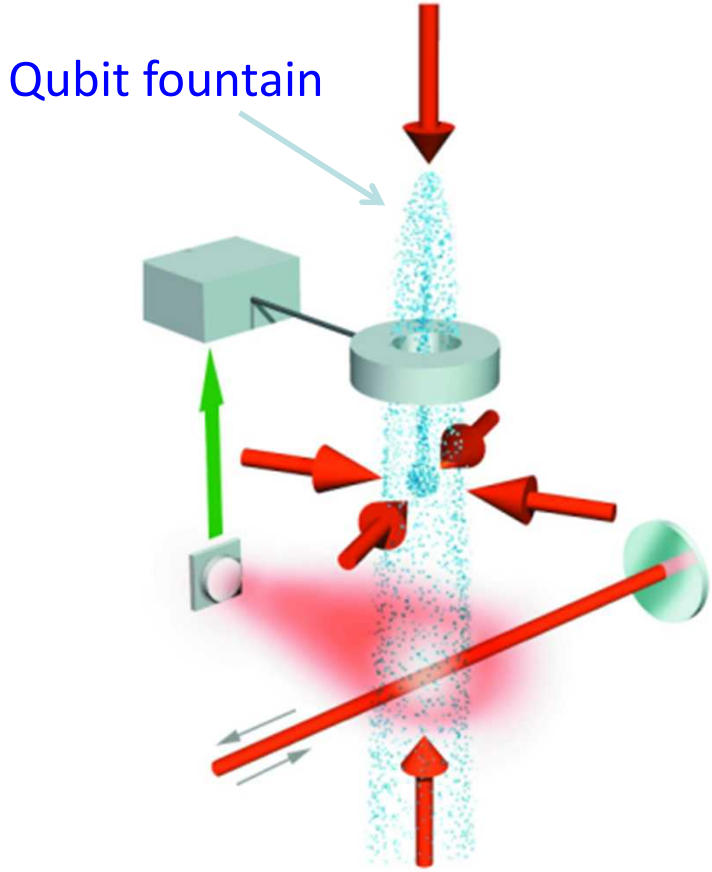
## Team members

- Yuan-Yu Jau (Sandia)
- Jongmin Lee (Sandia)
- Mike Martin (Sandia)
- Bob Keating (UNM)
- Ivan Deutsch (UNM)
- Aaron Hankin (Sandia, currently at NIST, Boulder, Colorado)

Grant Biedermann  
Albuquerque, New Mexico



# Precision metrology with Alkali atoms



Qubit fountain

Atomic fountain principle

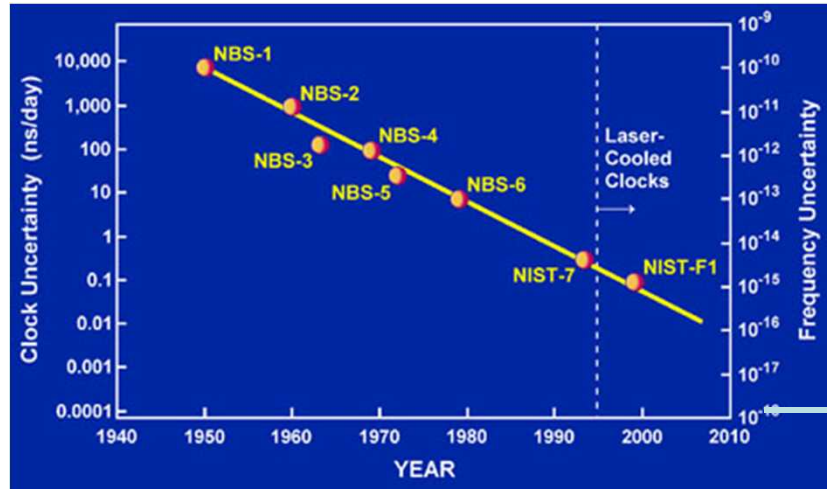
[http://smc.cnes.fr/PHARAO/GP\\_instrument.htm](http://smc.cnes.fr/PHARAO/GP_instrument.htm)

Outstanding quantum coherence in neutral atoms enables precision metrology and quantum information

- Example: atomic clocks

$$|6^2 S_{1/2}; F = 3, M_F = 0\rangle \leftrightarrow |6^2 S_{1/2}; F = 4, M_F = 0\rangle$$

$$|0\rangle \leftrightarrow |1\rangle$$

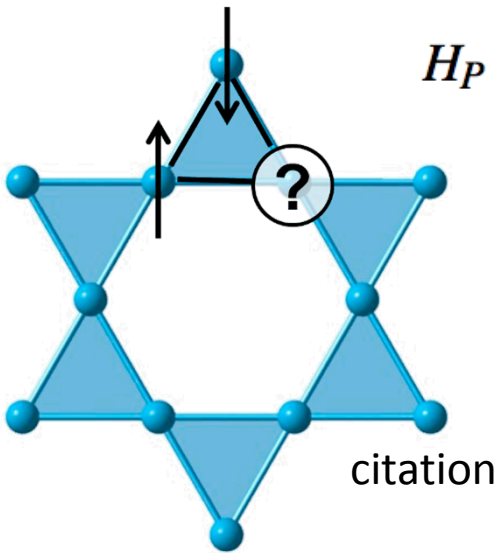
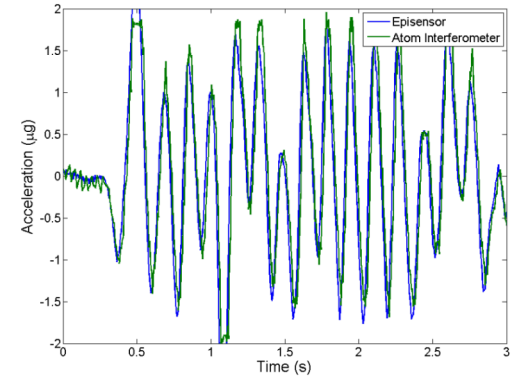
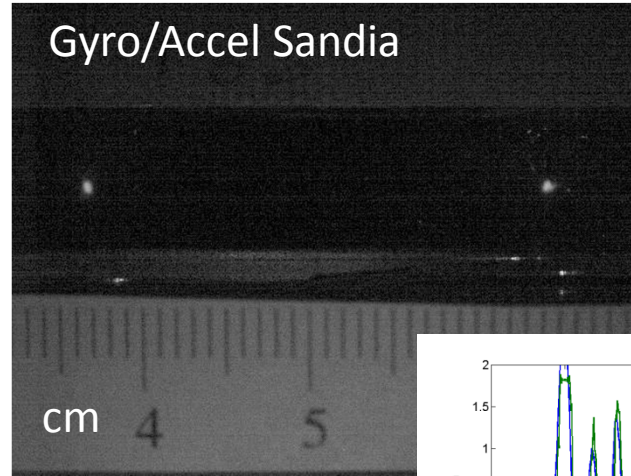


<http://www.nist.gov>

Optical clocks

# Applications

- Atom interferometer inertial sensors
- Clocks
- Magnetometers
- Quantum information
  - improved sensors
  - quantum simulation
  - quantum computation



$$H_P = \sum_{i=1}^N \tilde{h}_i \sigma_z^{(i)} + \sum_{i,j=1}^N \tilde{J}_{ij} \sigma_z^{(i)} \otimes \sigma_z^{(j)}$$

Generic Ising model  
& beyond?

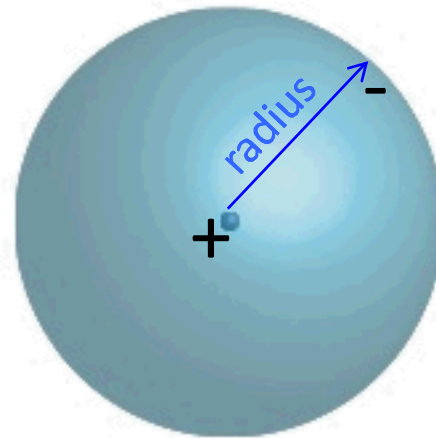
citation

Frustrated magnetism



# Interaction between *neutral* atoms

Valence electron in  
Rydberg state

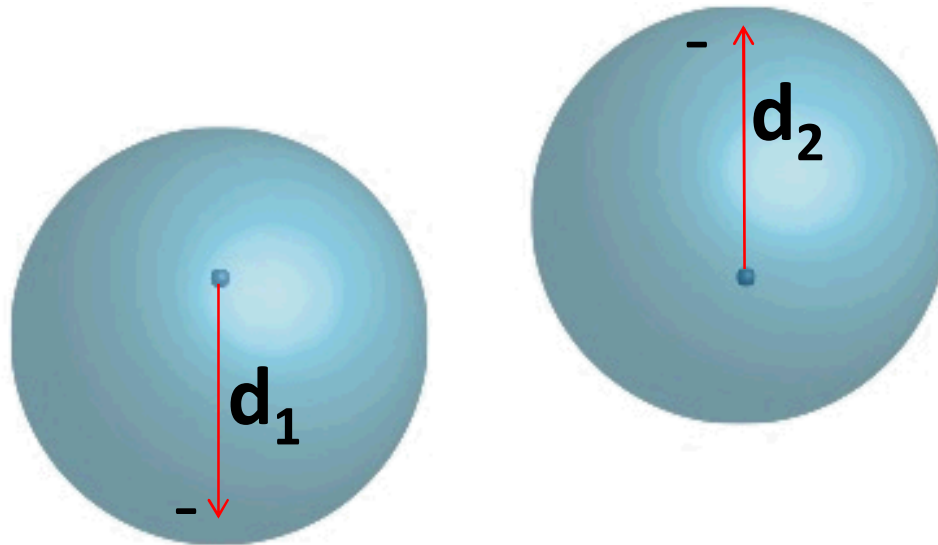


orbital radius  $\propto n^2$

*Wavefunction symmetric  
in zero electric field*

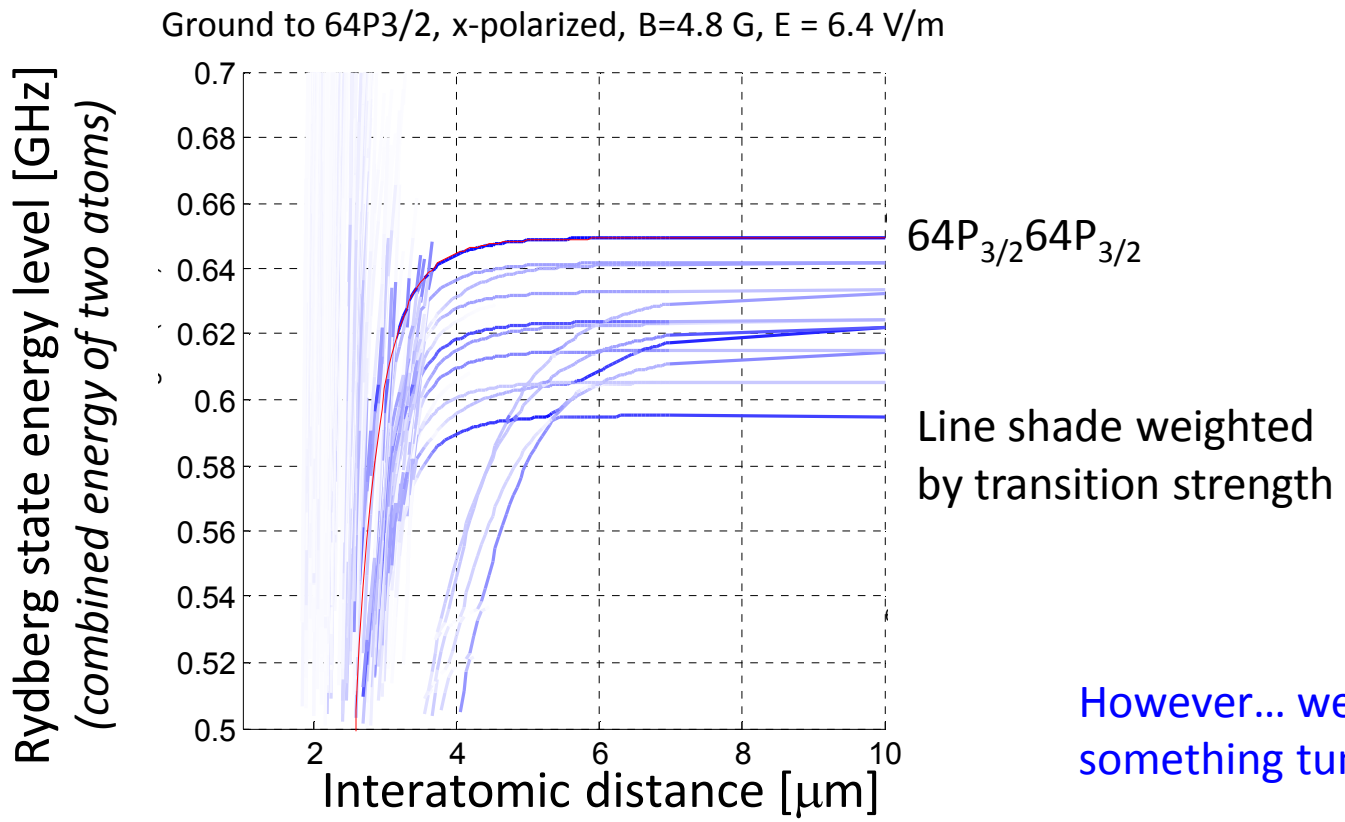
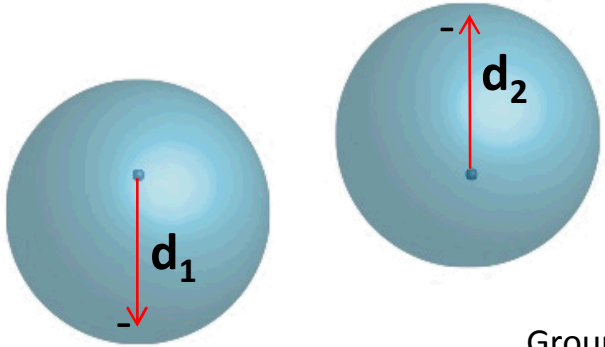
- Interaction between ground state atoms is small  $\sim 100$  Hz
- Excite valence electron to Rydberg state—nearly ionized
- Atom becomes highly polarizable—strong interactions
- Even the presence of another atom can cause a massive response  $> 10$  MHz

# Interaction between *neutral* atoms



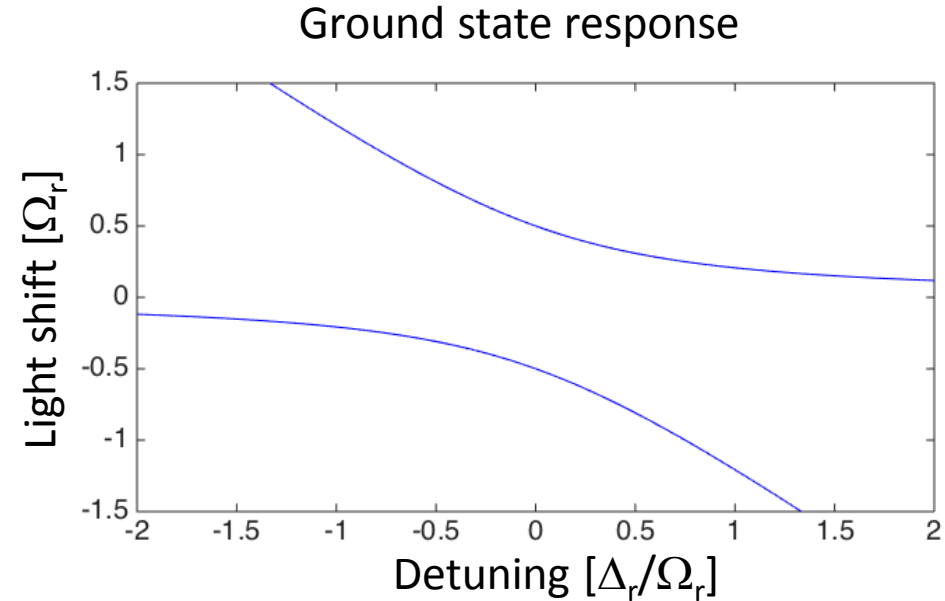
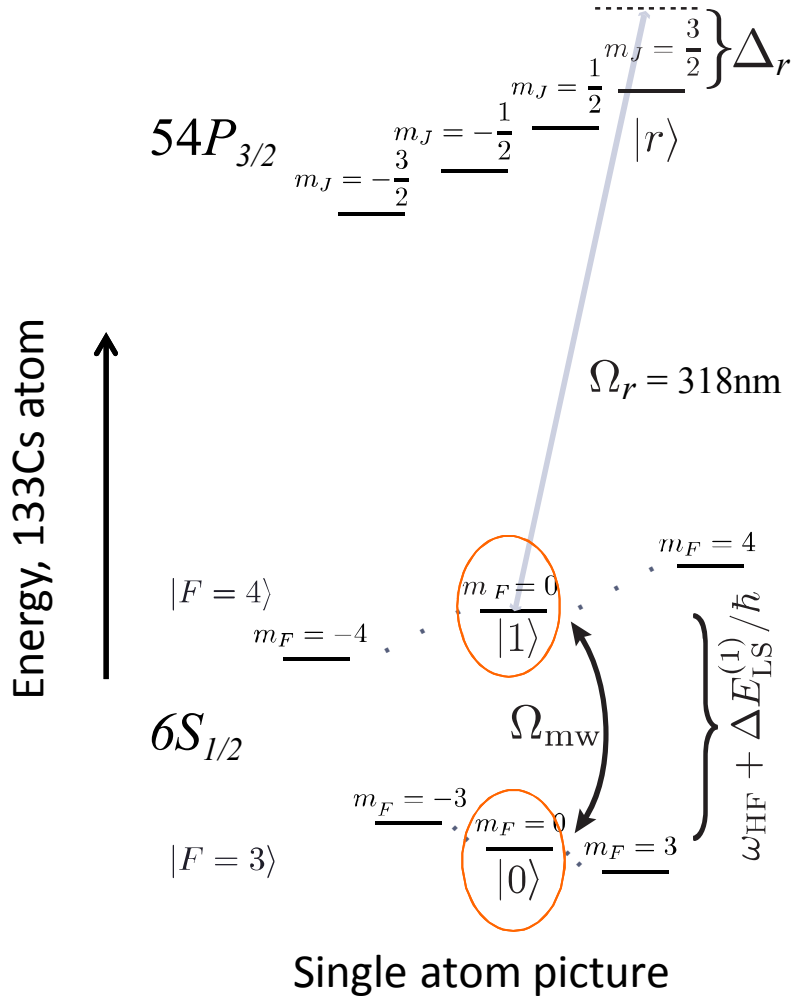
- Interaction between ground state atoms is small  $\sim 100$  Hz
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# Interaction between *neutral* atoms



However... we want something tunable

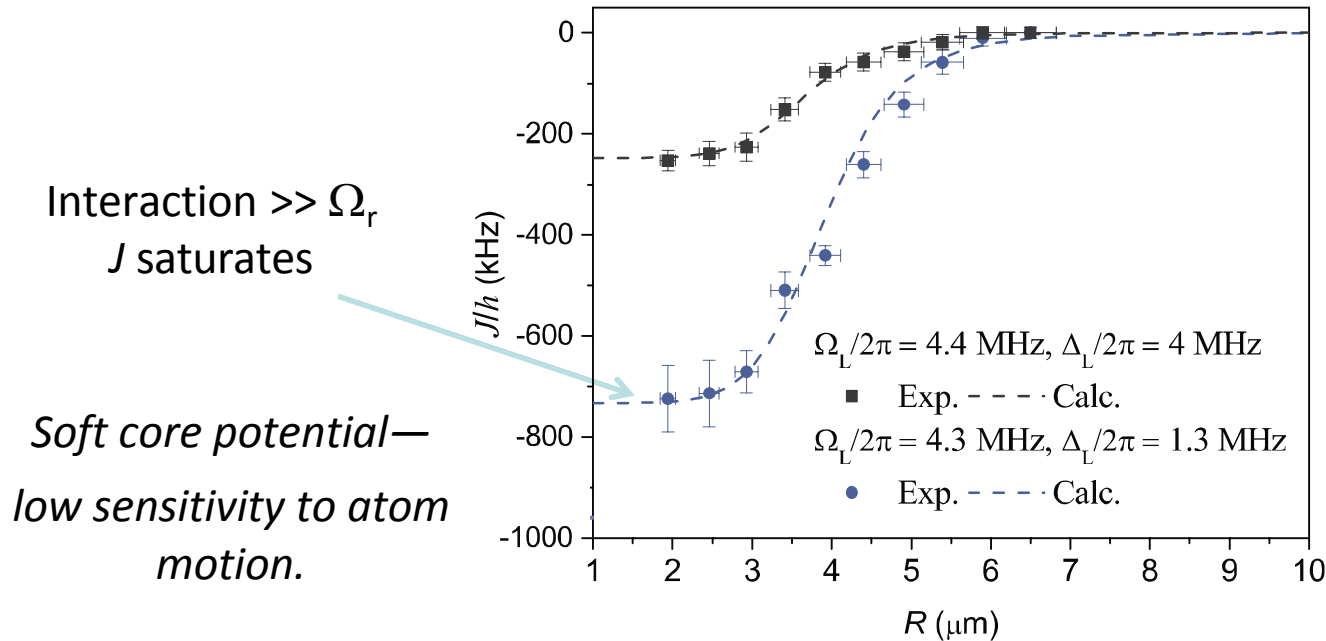
# Rydberg-dressed states



- Controllable with laser intensity and detuning—on demand
- 2 atom case—Rydberg blockade affects light shift
- Transfers blockade effect to ground state manifold

# Rydberg-dressed interaction, $J$

$J$  = change in light shift due to interaction



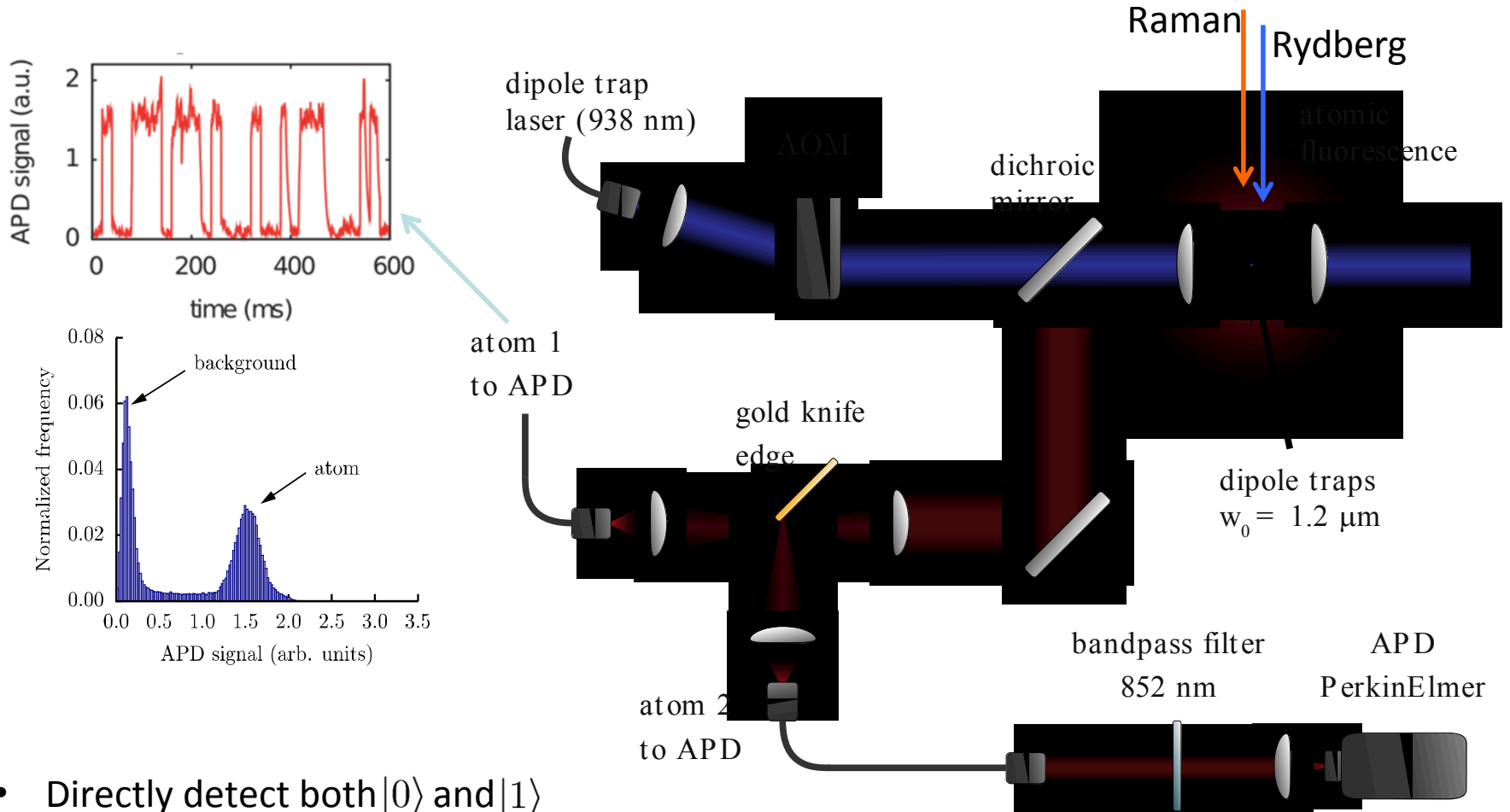
*Can be either  
attractive or  
repulsive*

Work near resonance to maximize  $J$

For  $\Delta = 0$ :  $J_{max} \approx 0.59 * \Omega$

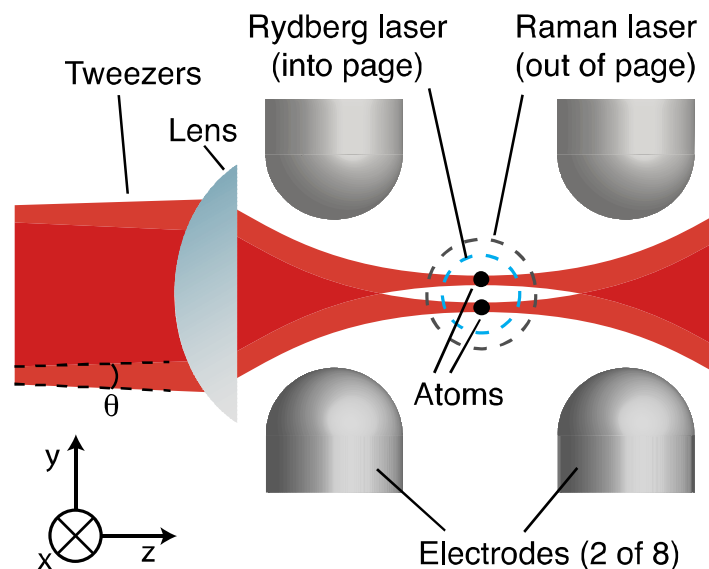
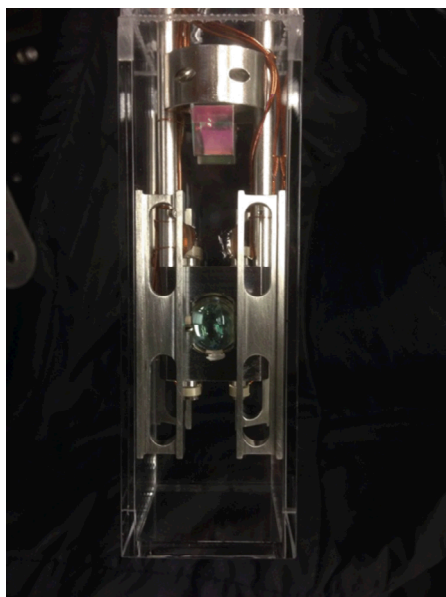
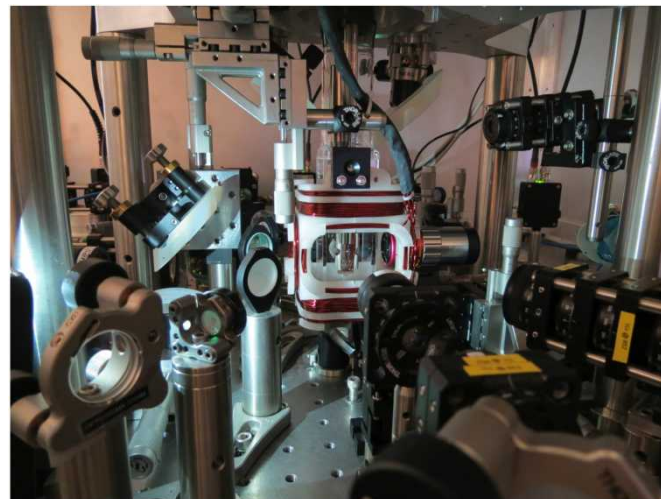
For  $\Delta = 10 \Omega$ :  $J_{max} \approx 0.0001 * \Omega$

# Single atom control of 2 atoms

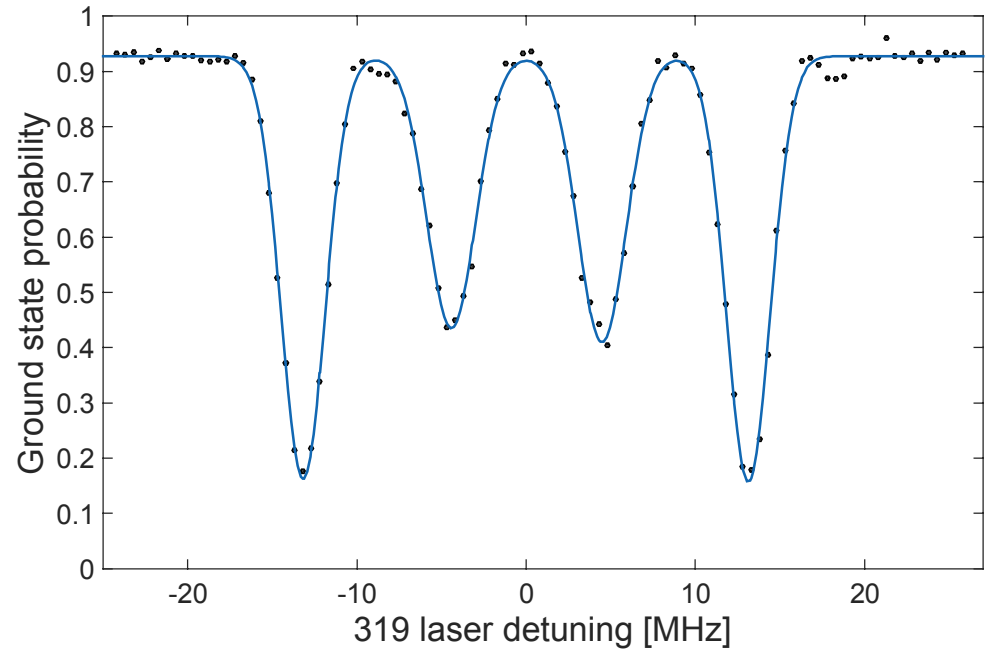
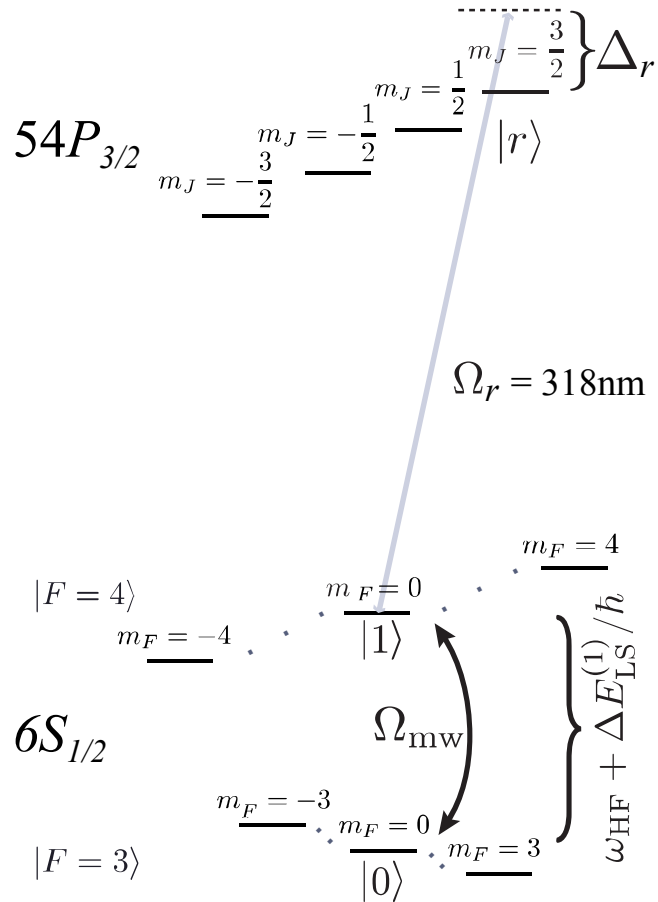


- Directly detect both  $|0\rangle$  and  $|1\rangle$
- Distinguishable from loss
- FPGA control: Reuse atoms
- Data rate  $\approx 10 \text{ s}^{-1}$  for two atoms

# Apparatus



# Rydberg state spectrum



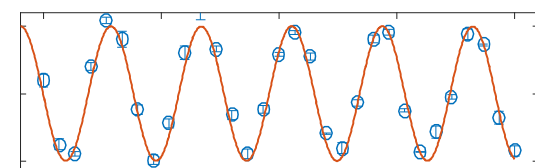
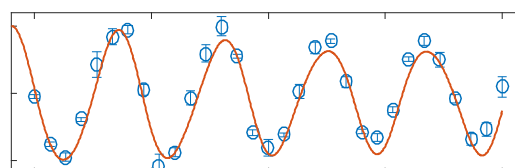
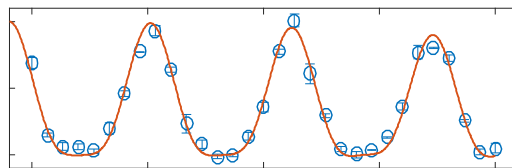
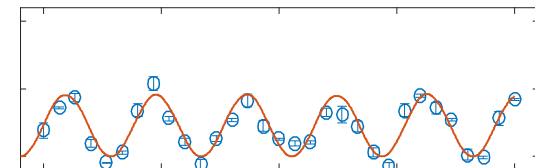
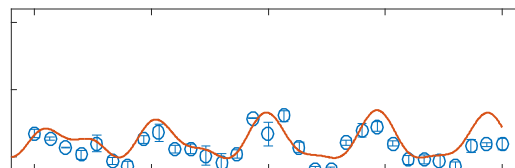
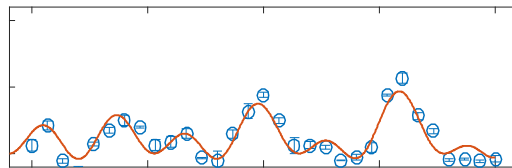
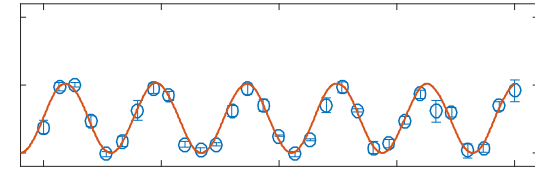
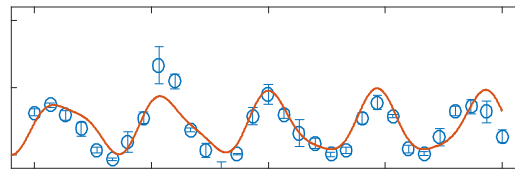
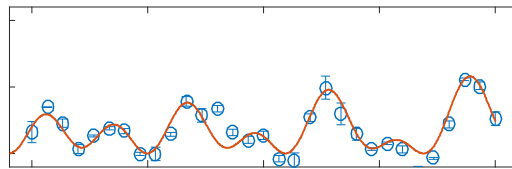
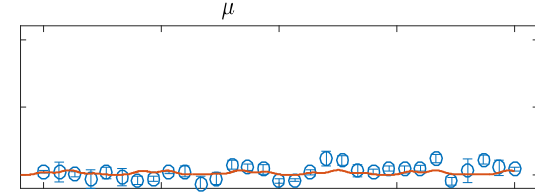
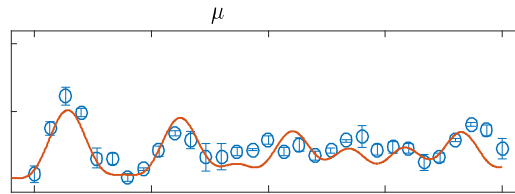
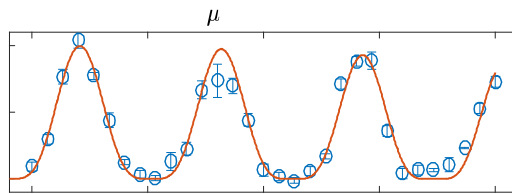
# Rydberg blockade—direct excitation

Weak ( $U_{RR} < 100$  kHz)

Intermediate ( $U_{RR} = 1.9$  MHz)

Strong ( $U_{RR} > 6$  MHz)

1- $\rightarrow$ r

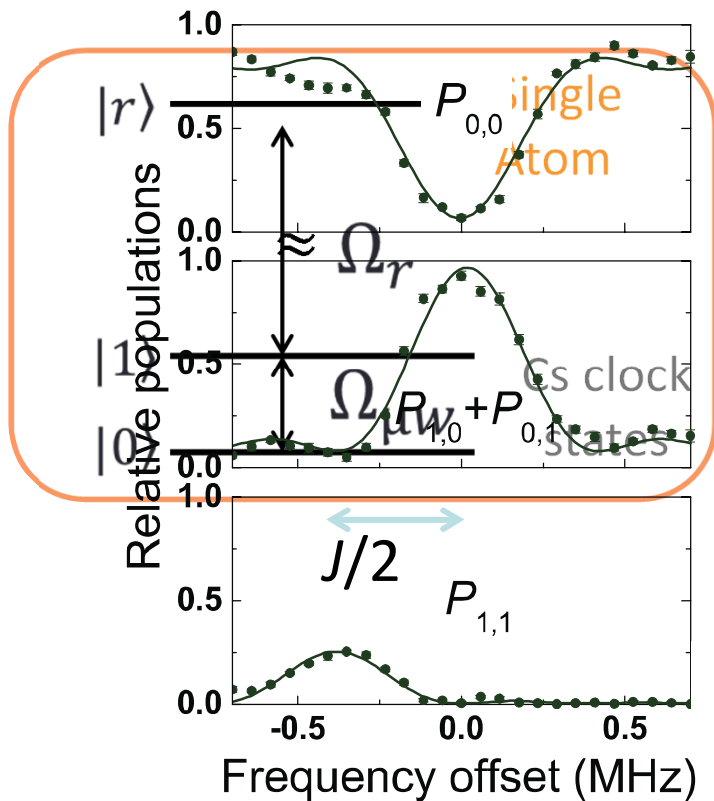


$\mu$

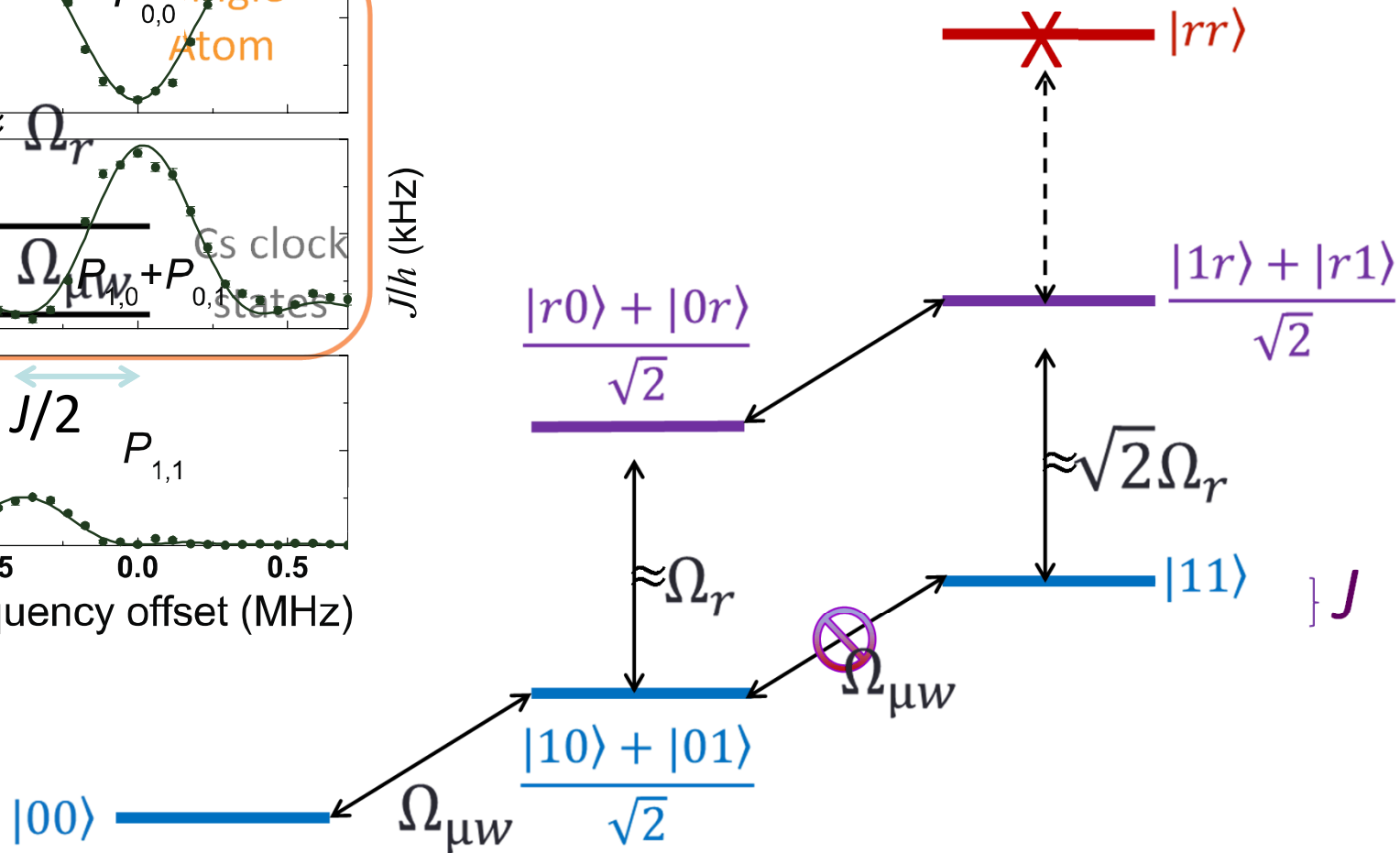
$\mu$

$\mu$

# Ground state, *Spin-flip* blockade

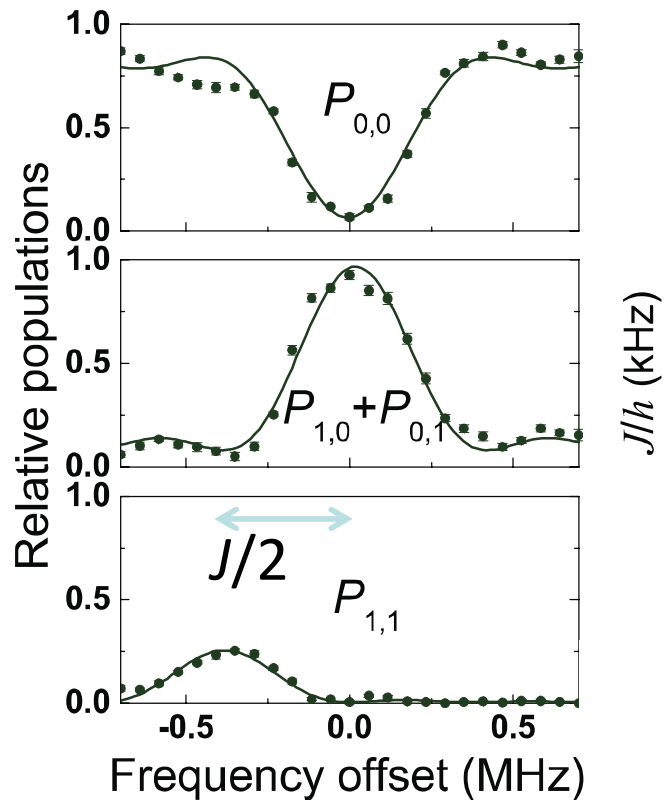


$J/h$  (kHz)

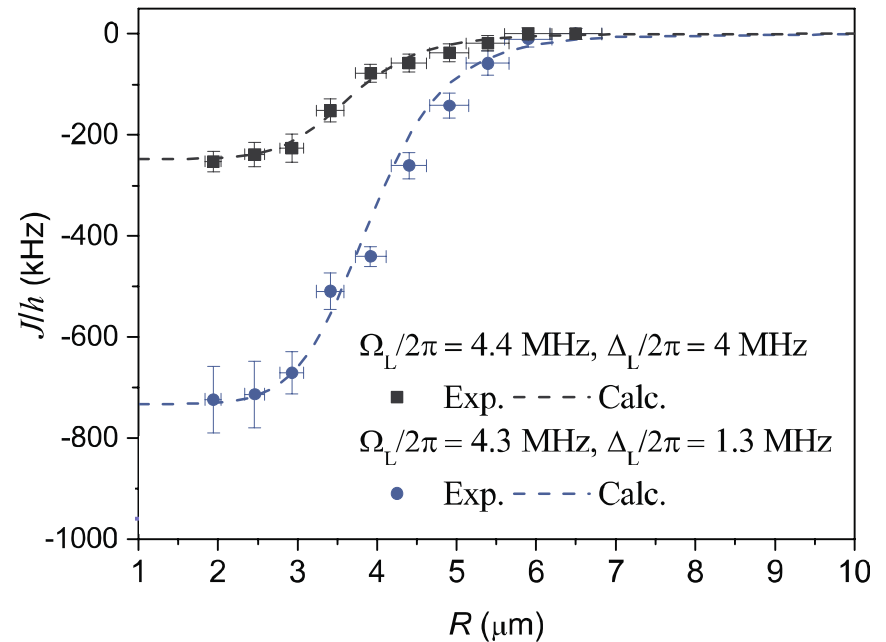


# $J$ vs. $R$

Direct measurement of two-qubit interaction strength  $J$  as a function of two-atom separation with two conditions.

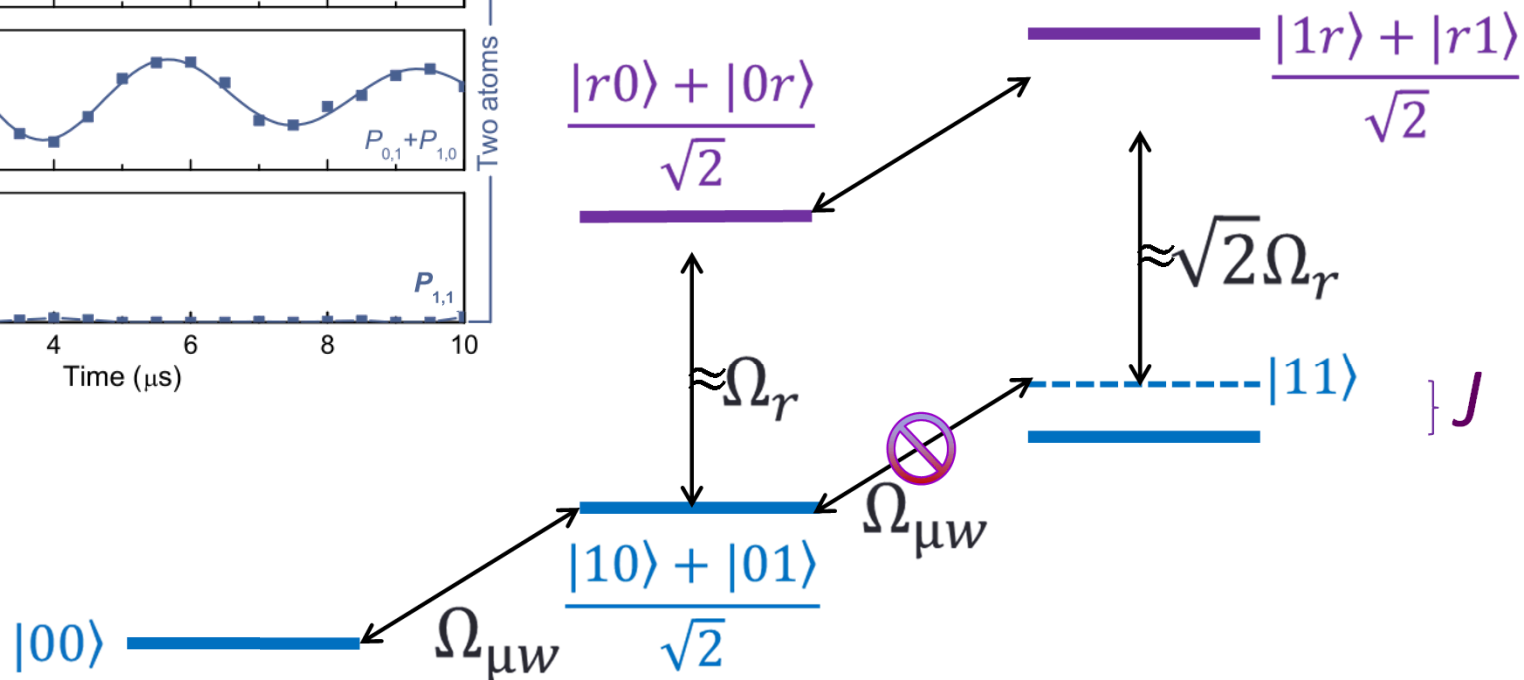
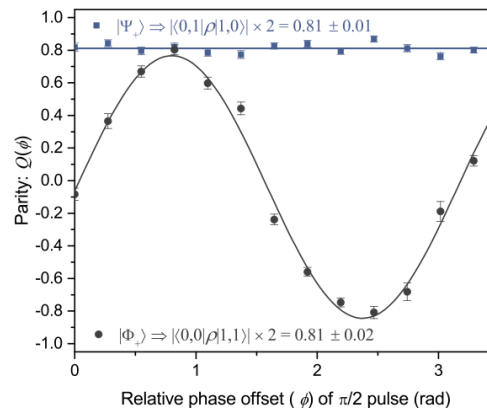
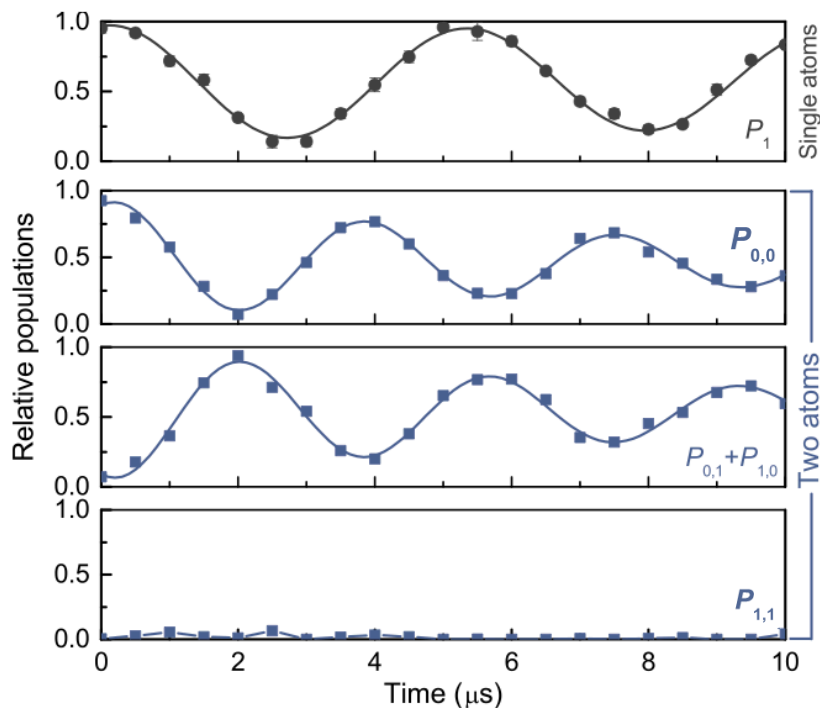


$J/h$  (kHz)



Jau, et al., Nature Phys. (2016)

# Ground state, *Spin-flip* blockade



# Extending to $N$ atoms—symmetric

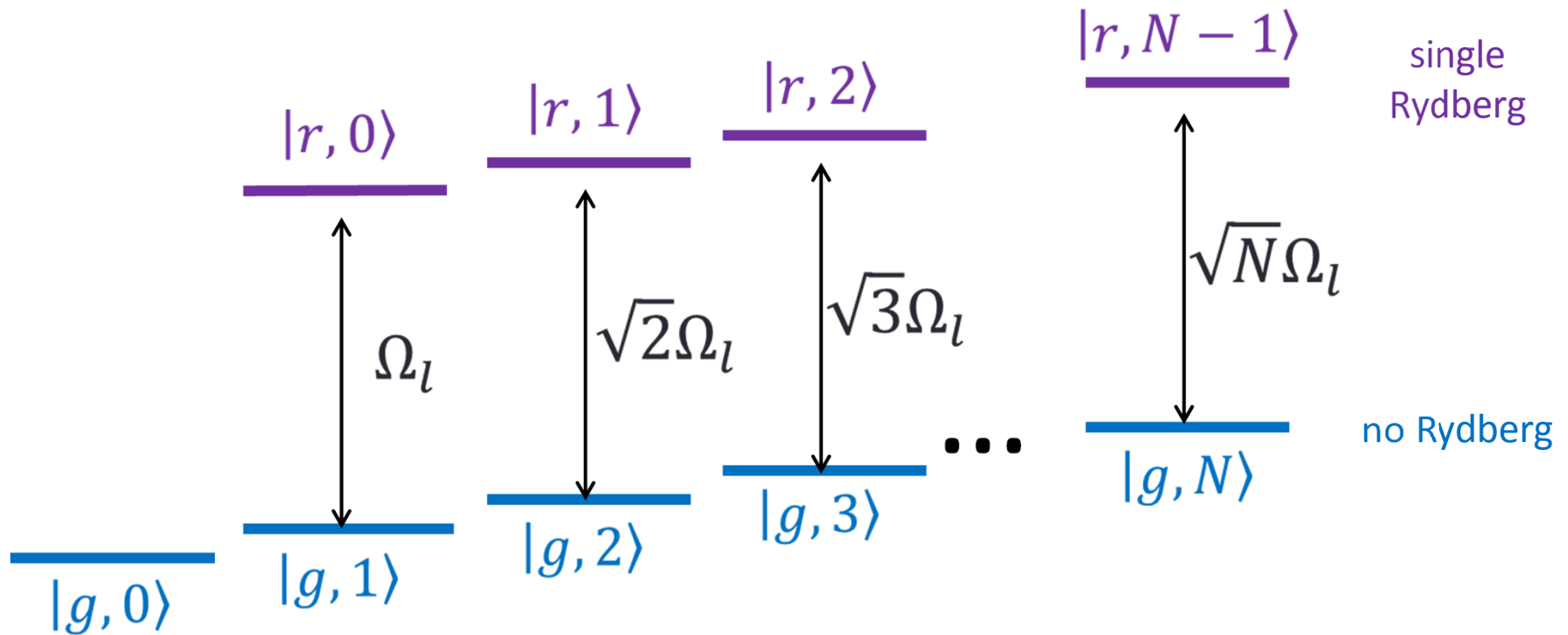
## notation

$$|g, n\rangle \equiv \text{Sym.}(|0\rangle^{\otimes N-n}|1\rangle^{\otimes n})$$

$$|r, n\rangle \equiv \text{Sym.}(|r\rangle|0\rangle^{\otimes N-n-1}|1\rangle^{\otimes n})$$

$N$  atoms

$n$  hyperfine excitations



# Extending to $N$ atoms—symmetric

## notation

$$|g, n\rangle \equiv \text{Sym.}(|0\rangle^{\otimes N-n}|1\rangle^{\otimes n})$$

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$N$  atoms

$n$  hyperfine excitations

⋮

$$\begin{array}{l} |+, 3\rangle \\ |-, 3\rangle \end{array} \left. \vphantom{\begin{array}{l} |+, 3\rangle \\ |-, 3\rangle \end{array}} \right\} \sqrt{3\Omega_r^2 + \delta_r^2}$$

$$\begin{array}{l} |+, 2\rangle \\ |-, 2\rangle \end{array} \left. \vphantom{\begin{array}{l} |+, 2\rangle \\ |-, 2\rangle \end{array}} \right\} \sqrt{2\Omega_r^2 + \delta_r^2}$$

$$\begin{array}{l} |+, 1\rangle \\ |-, 1\rangle \end{array} \left. \vphantom{\begin{array}{l} |+, 1\rangle \\ |-, 1\rangle \end{array}} \right\} \sqrt{\Omega_r^2 + \delta_r^2}$$

Dressed ground states

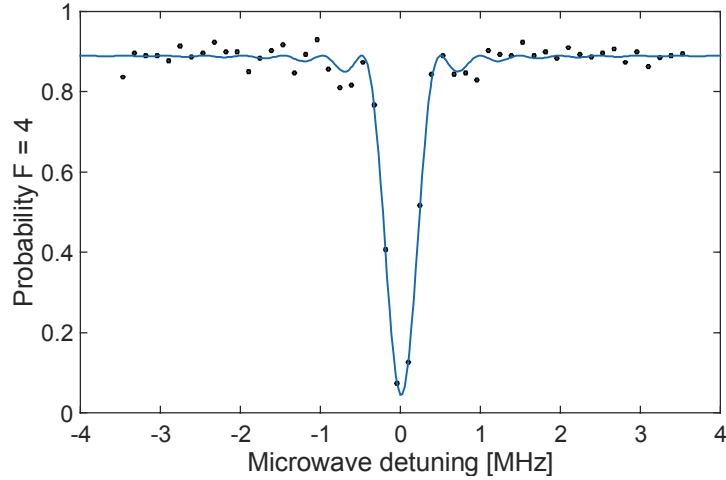
Autler-Townes splitting

$$|g, 0\rangle$$

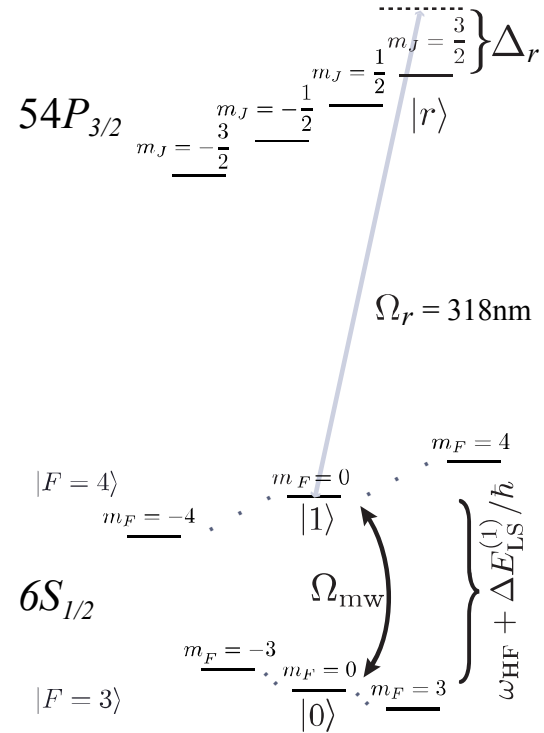
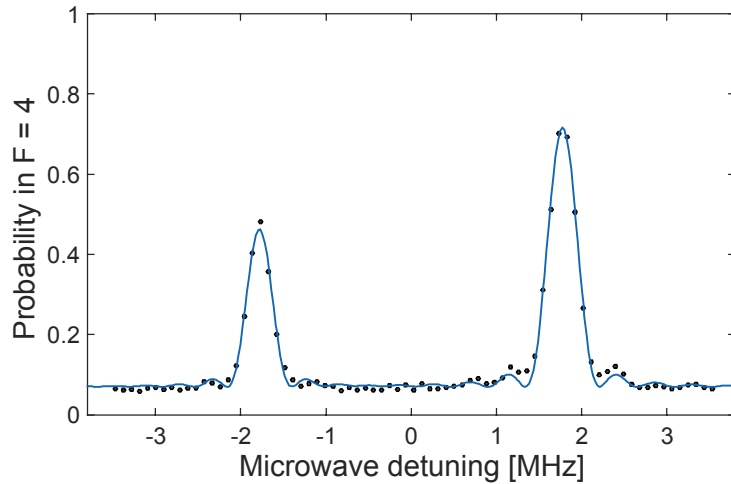
- Consider only ground states
- Isomorphic to Jaynes-Cummings model of a single atom in an optical cavity

# Rydberg-dressed states

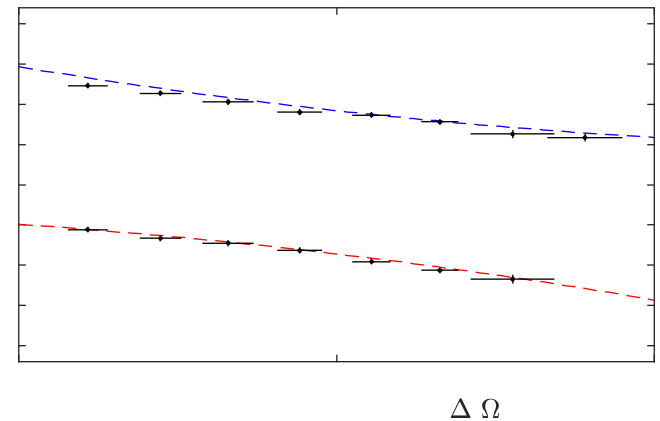
Bare atom



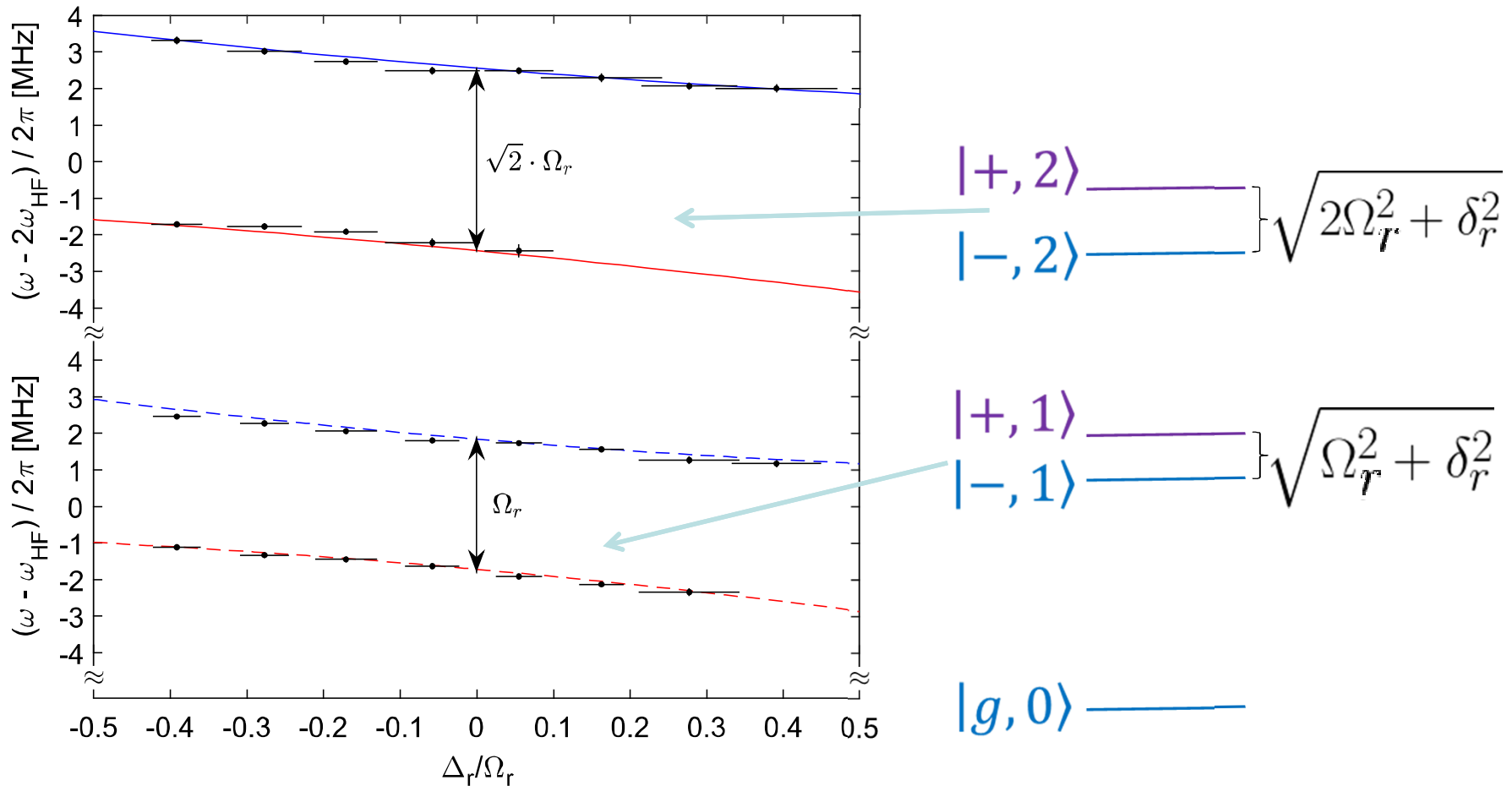
Dressed  $F=4$  state



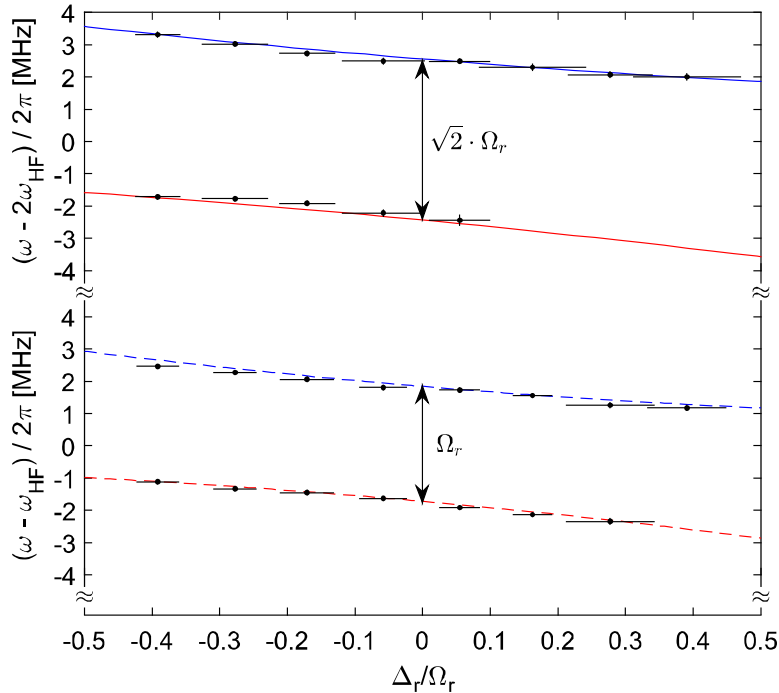
Autler-Townes splitting



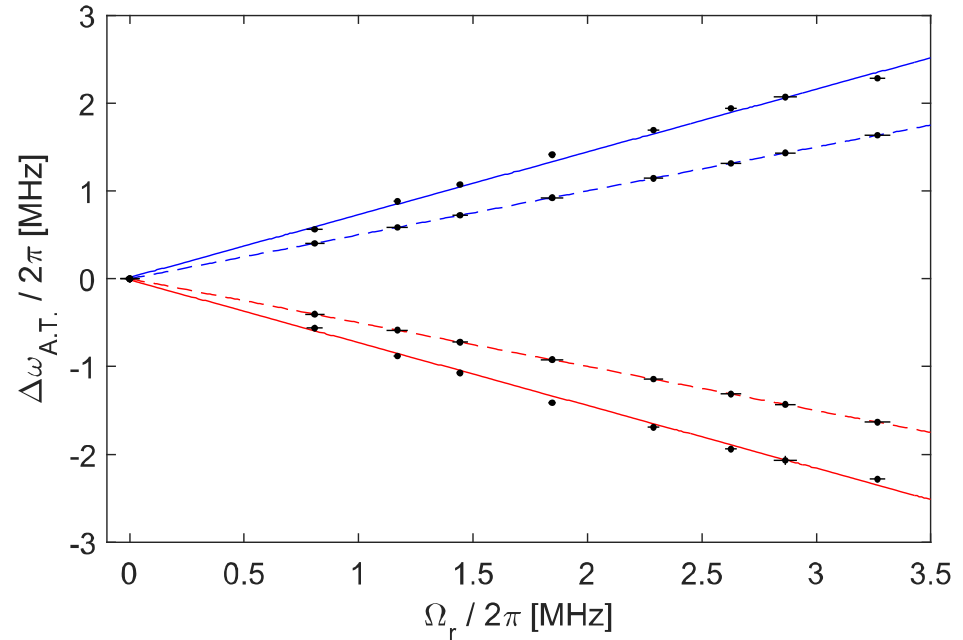
# Rydberg-dressed states under blockade



# Rydberg-dressed interactions—the big picture



$\Delta$  dependence



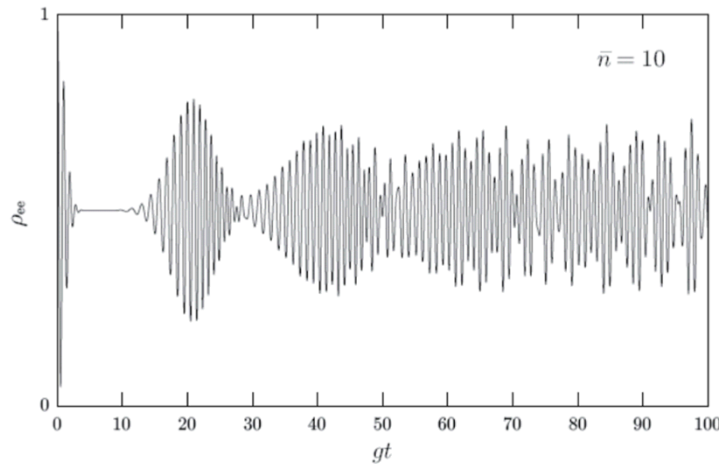
$\Omega$  dependence

- Choose sign of interaction
- Design time-dependent interaction
- Opens new doors for adiabatic approach to entanglement, Gates, and quantum simulation—Phys. Rev. A 91, 012337 (2015)

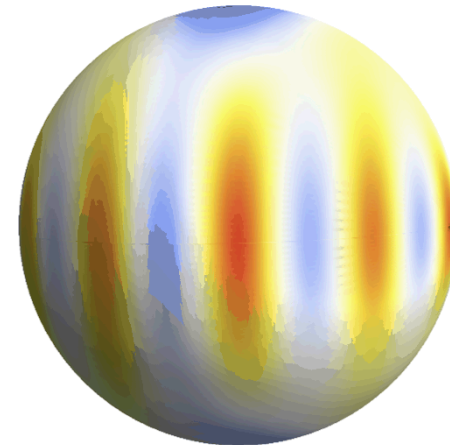


# Controlling the System

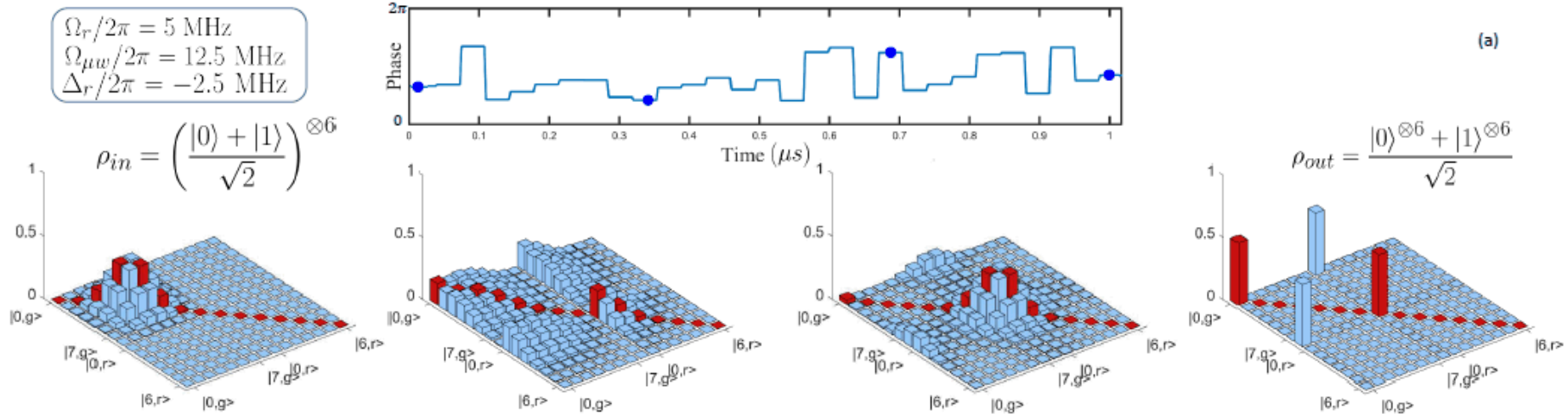
- Port over entanglement protocols from other JC platforms
  - Collective spin squeezing: Tomáš Opatrný and Klaus Mølmer. *Phys. Rev. A* **86**, 023845 (2012)
  - Collapse and revival: I. I. Beterov *et al.* *Phys. Rev. A* **90**, 043413 (2014)



from D.A. Steck, *Quantum and Atom Optics*

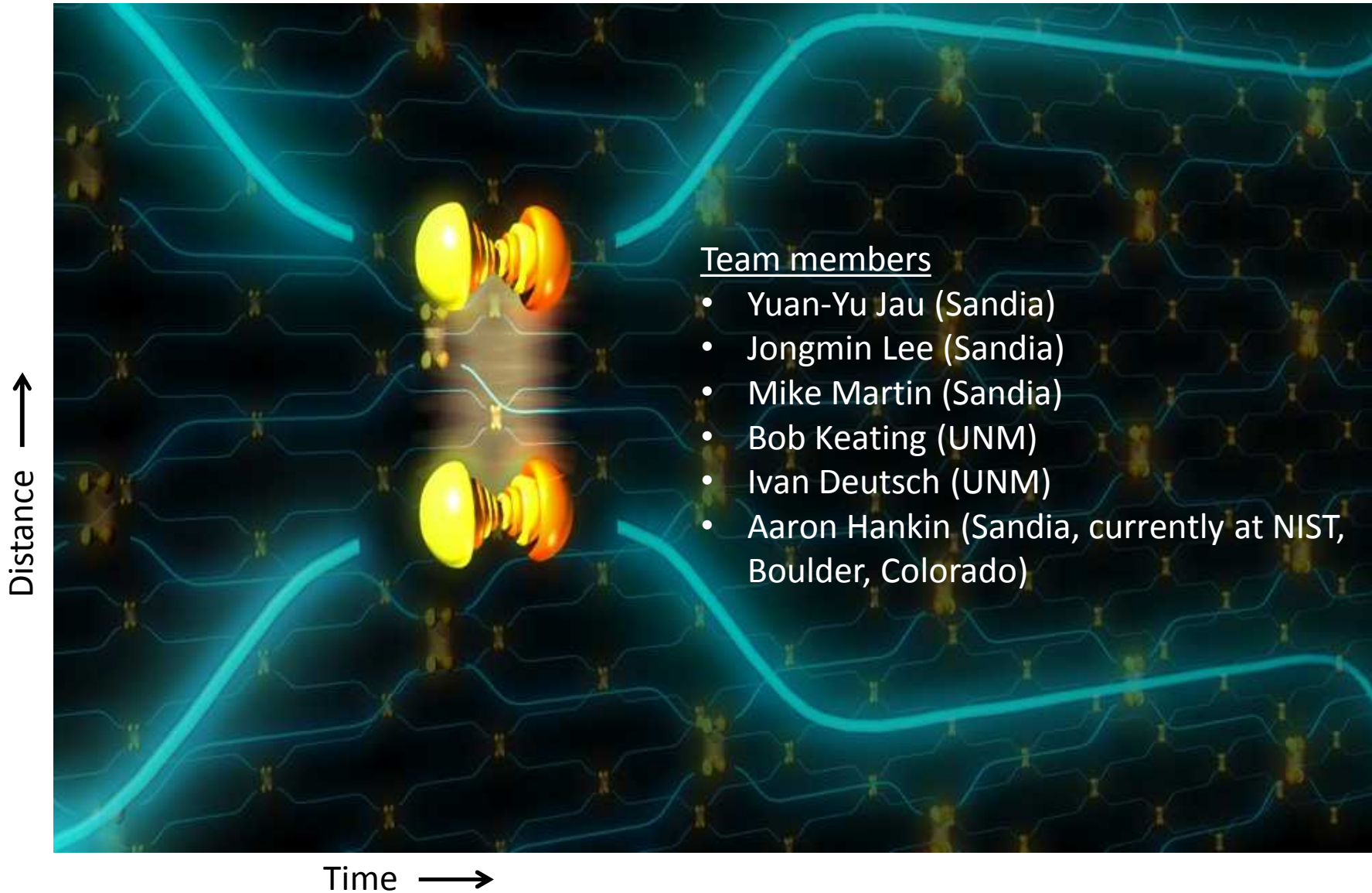


# Arbitrary control



The nonlinearity of the JCM, together with externally applied fields makes the system fully controllable on the whole Hilbert space, i.e., we can generate an arbitrary superposition state.

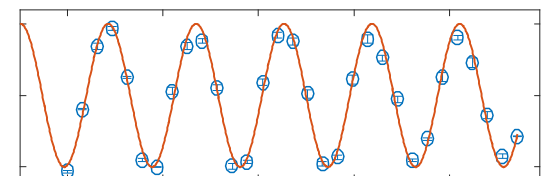
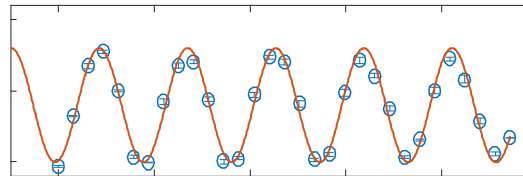
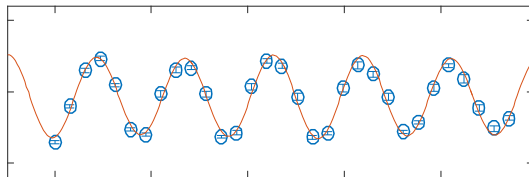
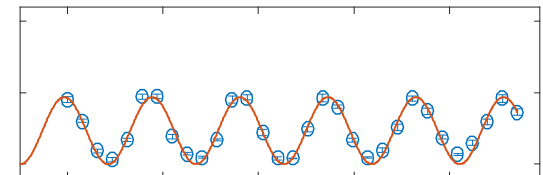
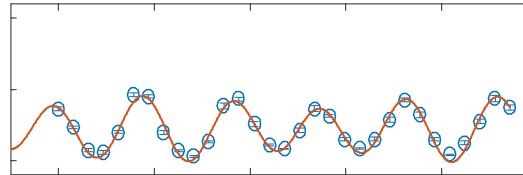
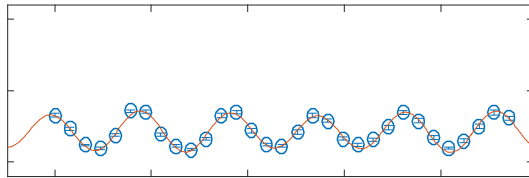
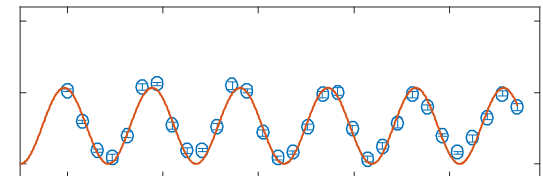
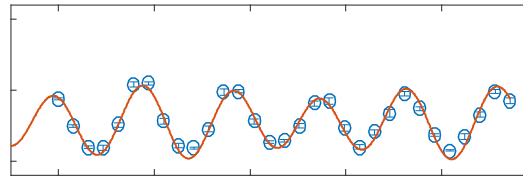
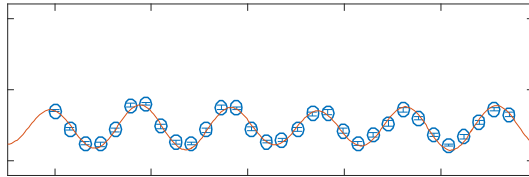
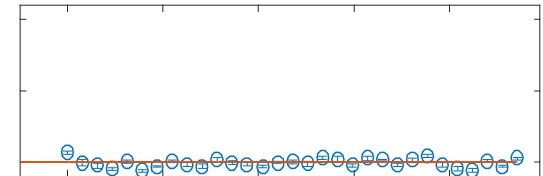
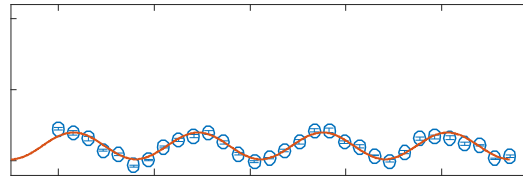
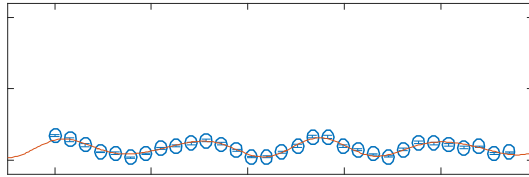
# Thank you!



Remove contributions from all non two-atom loading

Raw data and fit

Correct for state detection errors

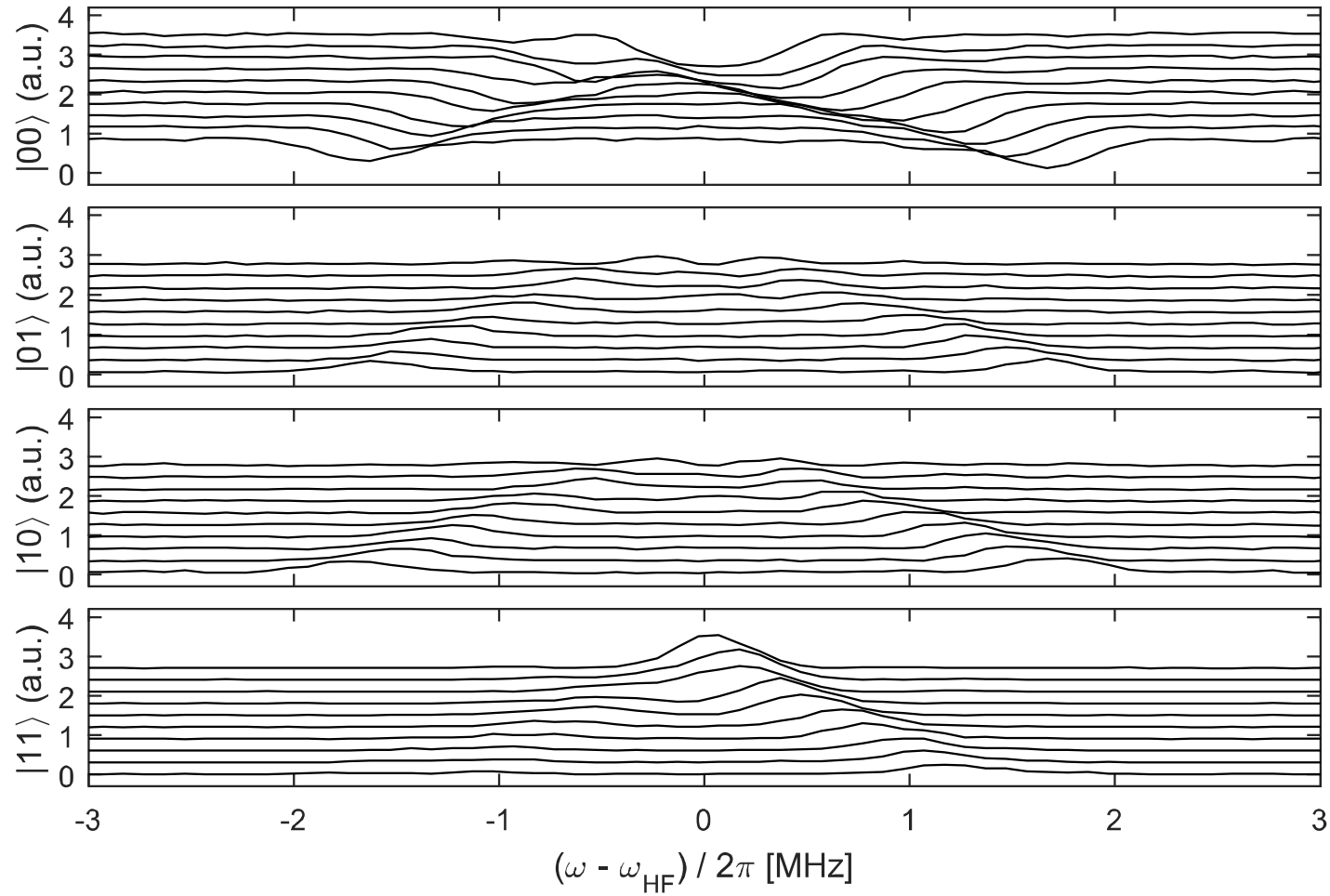


$\mu$

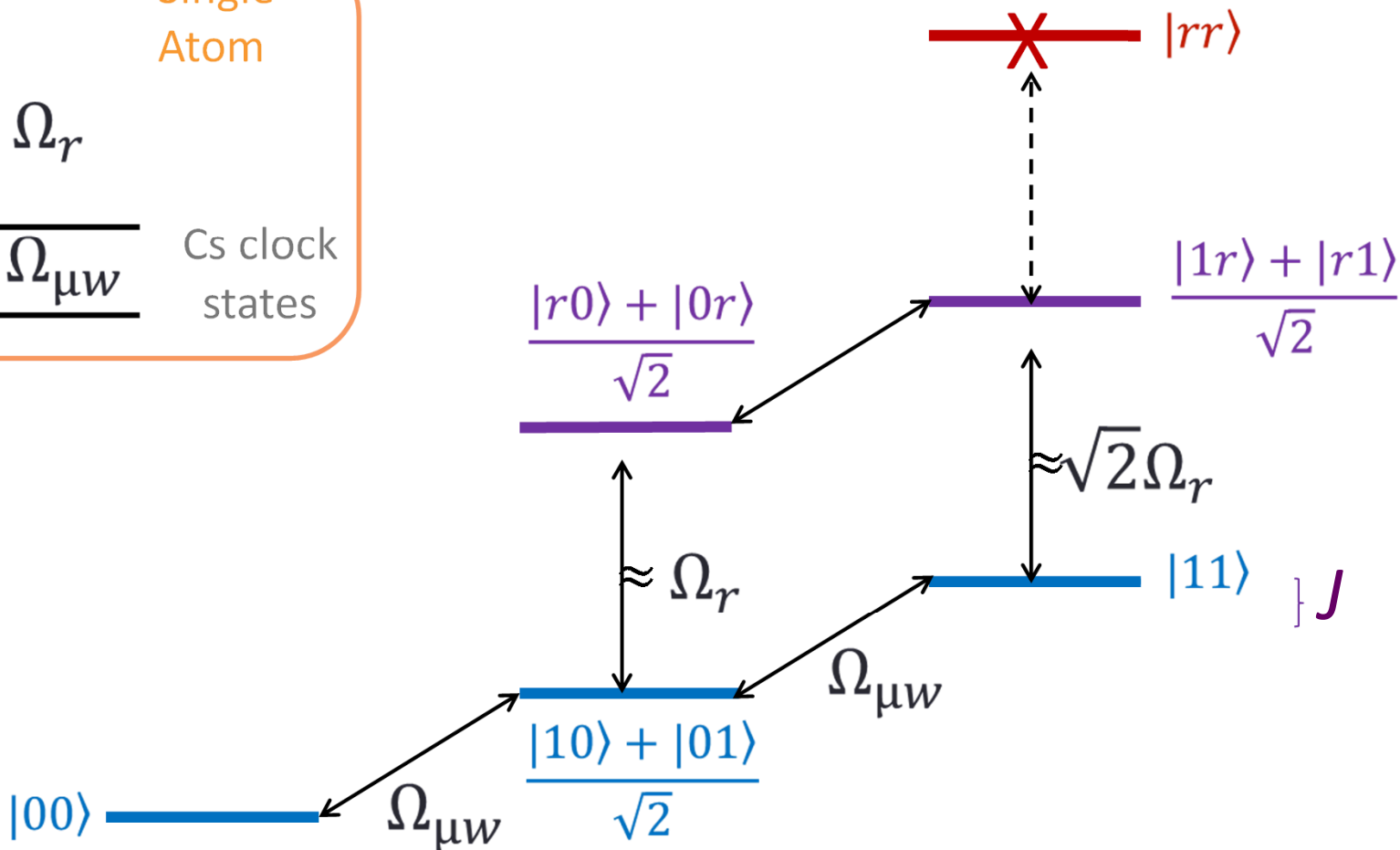
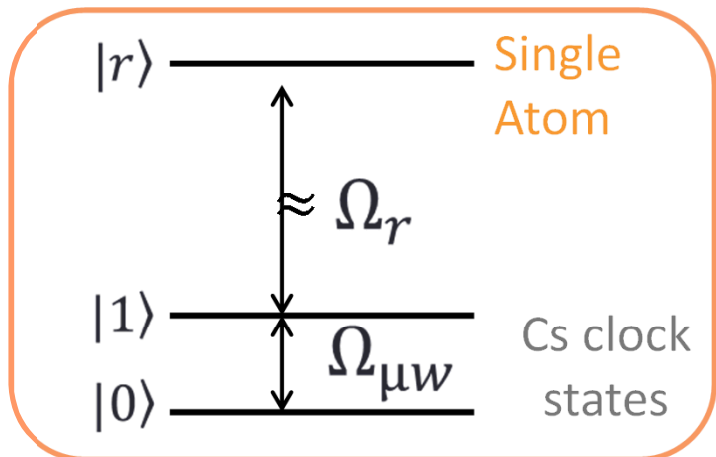
$\mu$

$\mu$

# $\sqrt{N}$ dependence



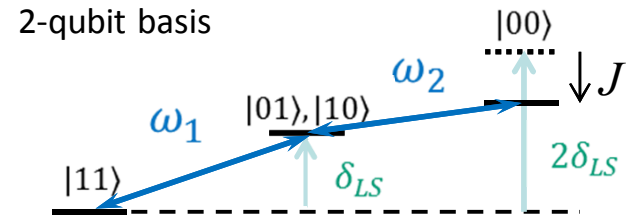
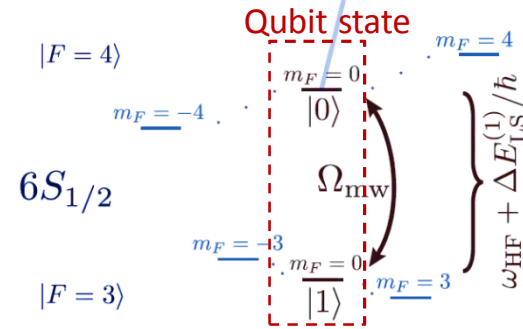
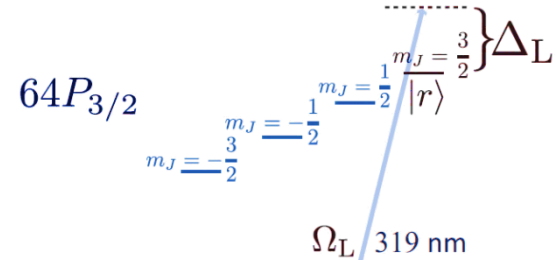
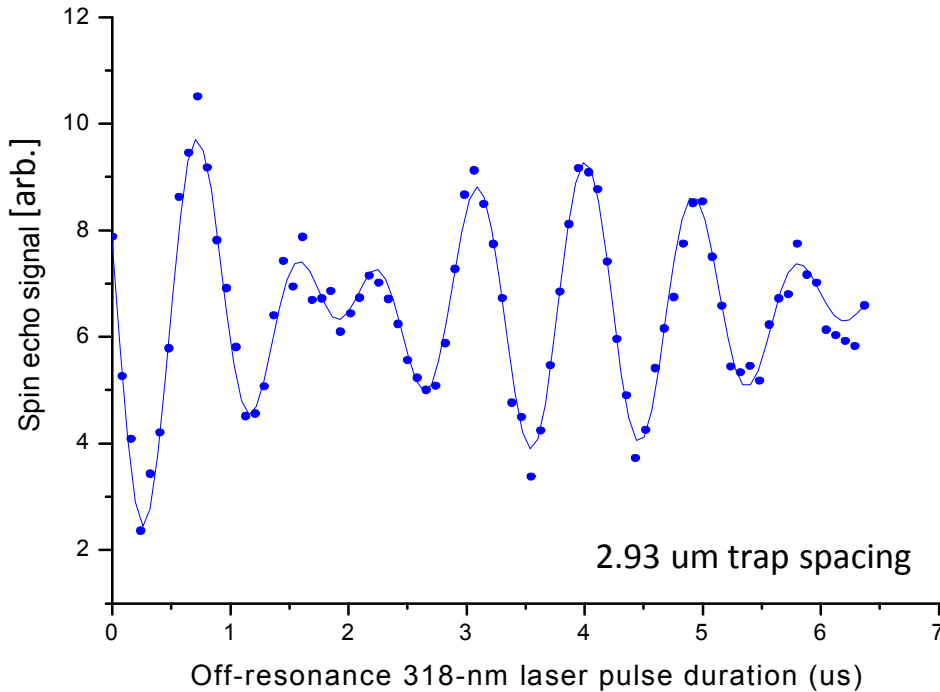
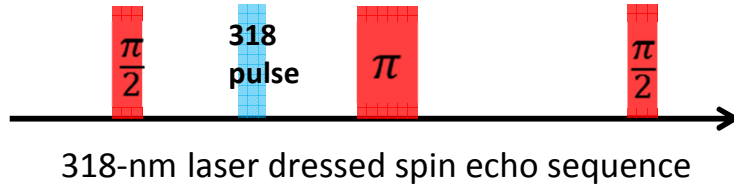
# Generating Entanglement





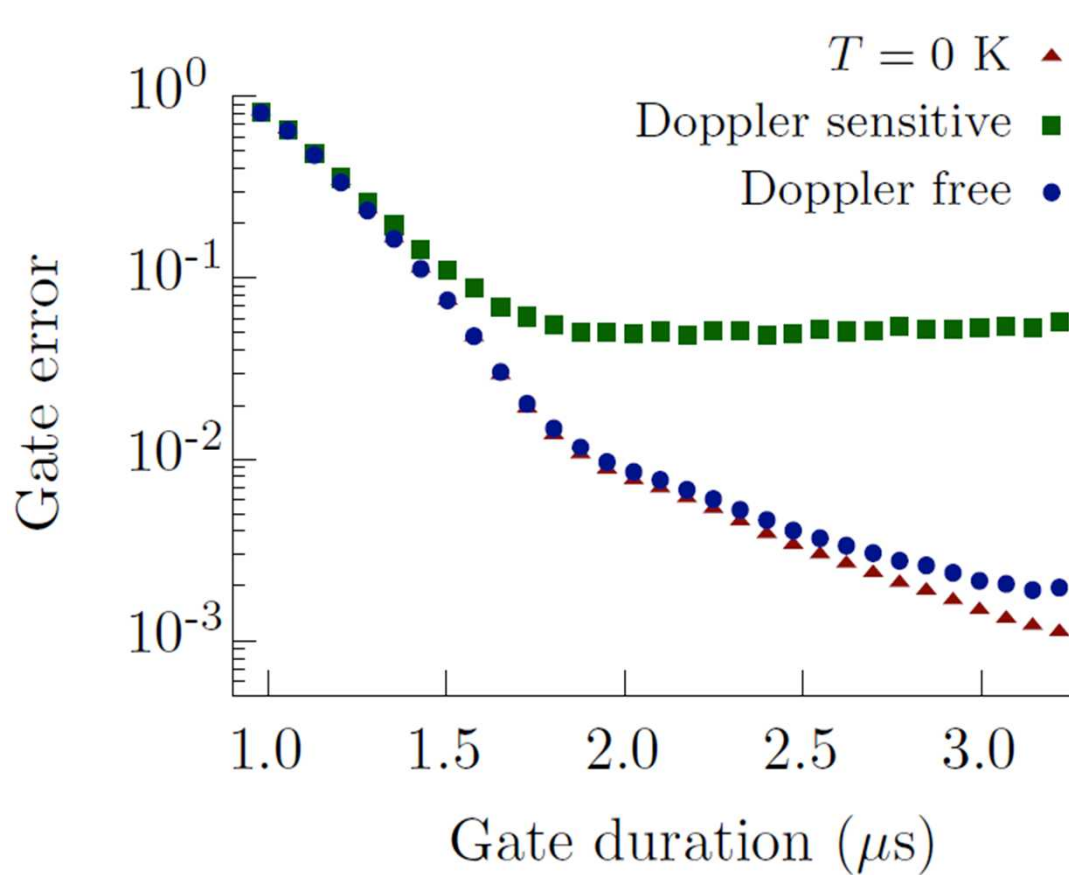
# Rydberg-dressed Ramsey dynamics

Microwave transition is via Raman laser



A frequency beat note is generated if  $\omega_1 \neq \omega_2$

# Simulated CPHASE gate fidelities



$\Omega = 0 \rightarrow 3 \text{ MHz}$   
 $\Delta/2\pi = 6 \rightarrow 0 \text{ MHz}$   
 $\Gamma = 3.7 \text{ kHz}$   
 $T = 16 \mu\text{K}$

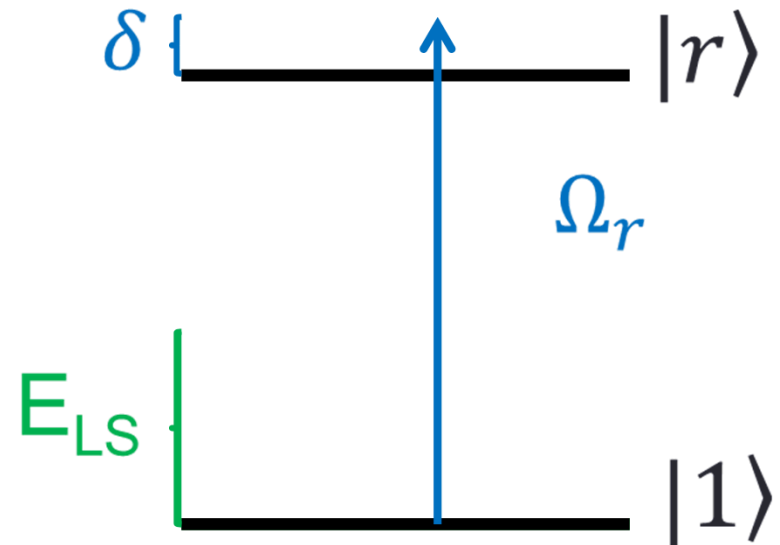
- Motional errors set a high floor on error for the single-beam scheme.
- The Doppler-free scheme is limited by the much smaller photon scattering rate.

Phys. Rev. A 91, 012337 (2015)



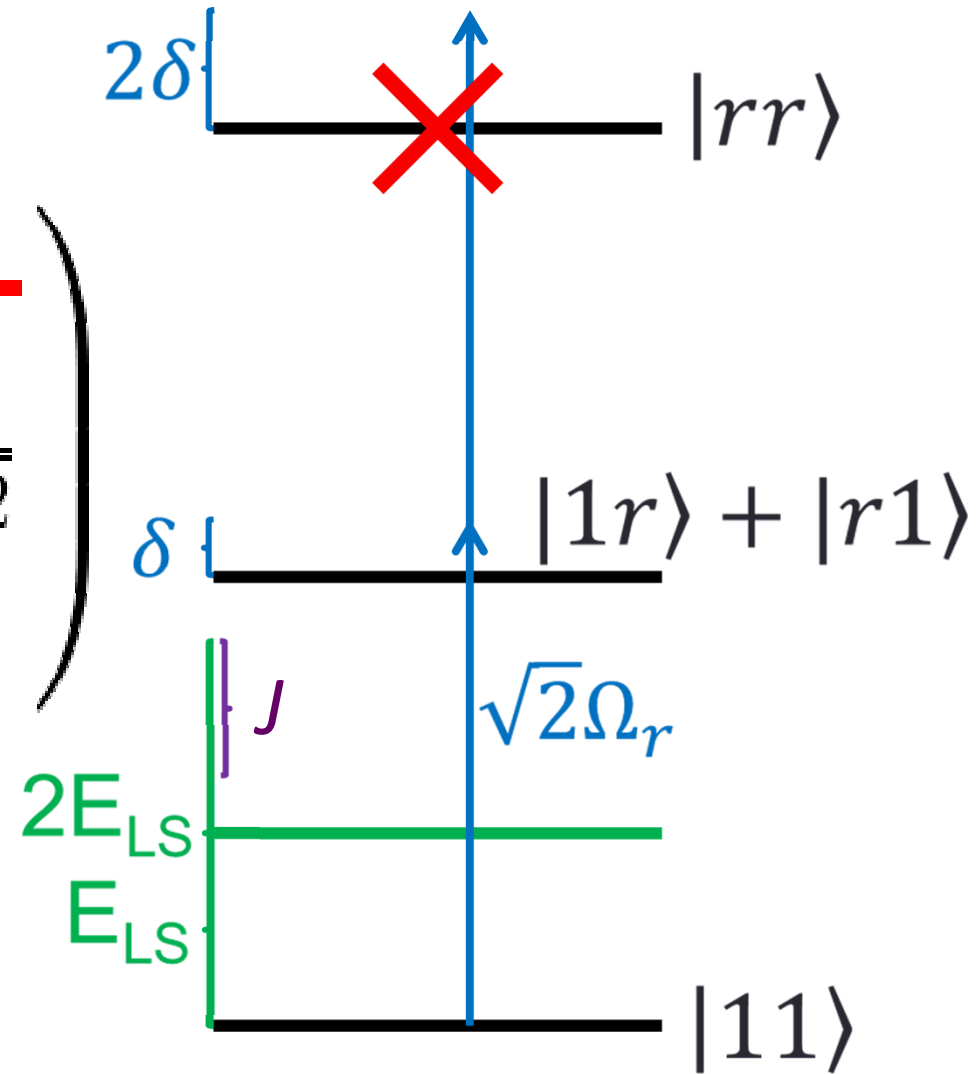
# Rydberg-dressed states

$$H^{(1)} = \begin{pmatrix} -\delta_r & \frac{\Omega_r}{2} \\ \frac{\Omega_r}{2} & 0 \end{pmatrix}$$



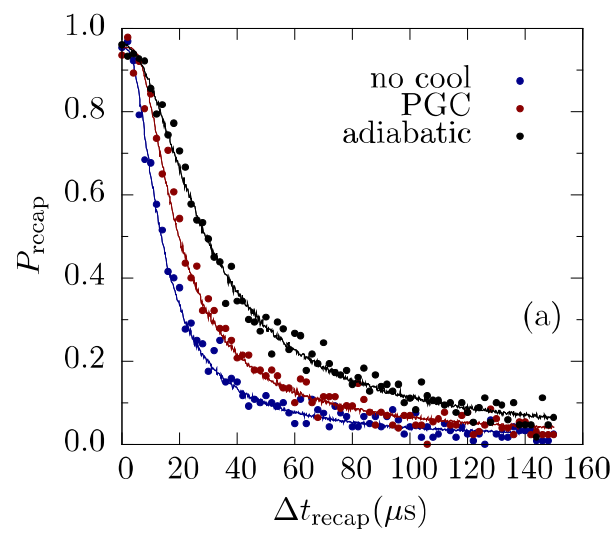
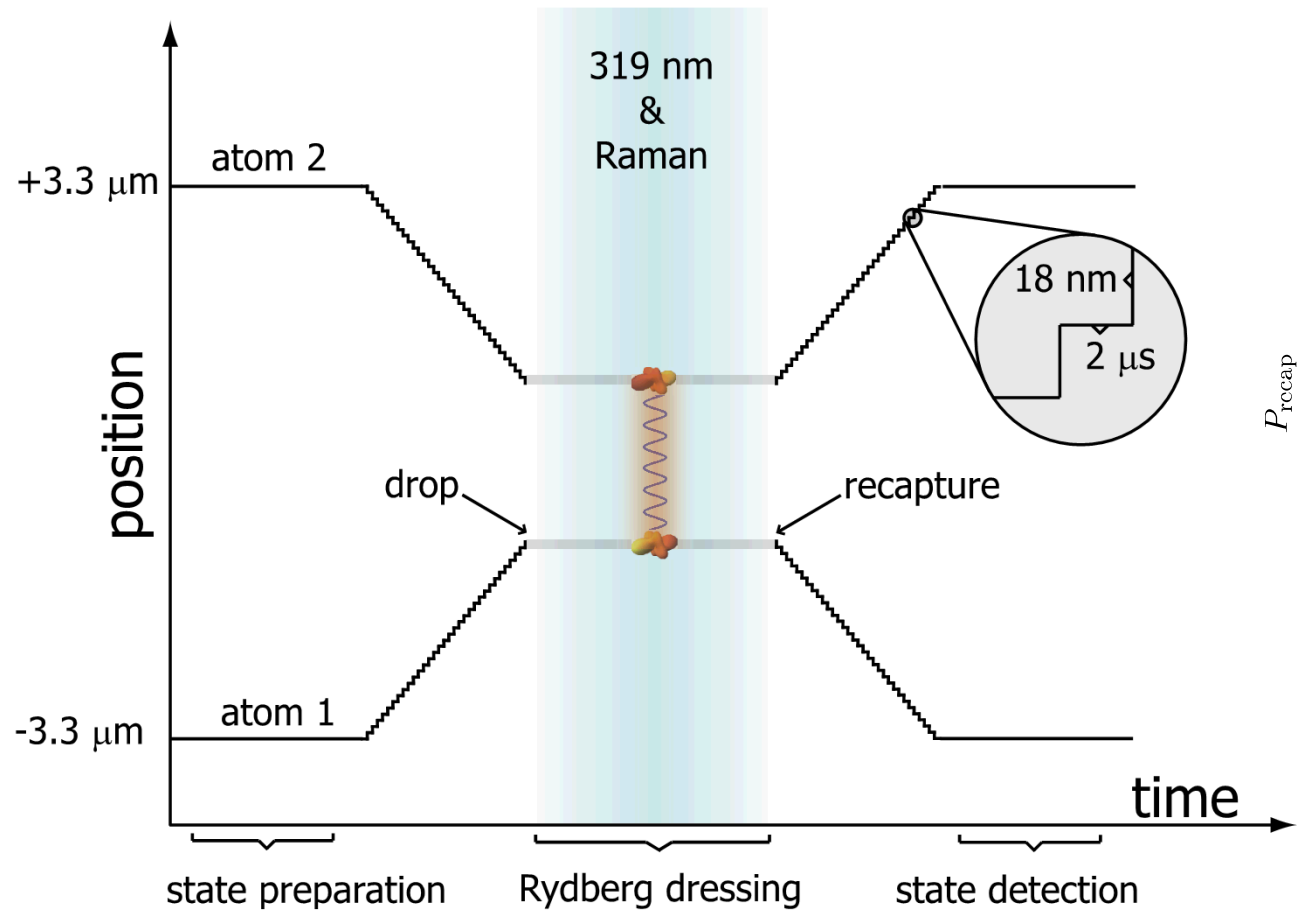
# Rydberg-dressed states

$$H^{(2)} = \begin{pmatrix} \cancel{W_{aa}} & \frac{\Omega_r}{\sqrt{2}} & 0 \\ \frac{\delta_r}{\sqrt{2}} & -\delta_r & \frac{\Omega_r}{\sqrt{2}} \\ 0 & \frac{\Omega_r}{\sqrt{2}} & 0 \end{pmatrix}$$



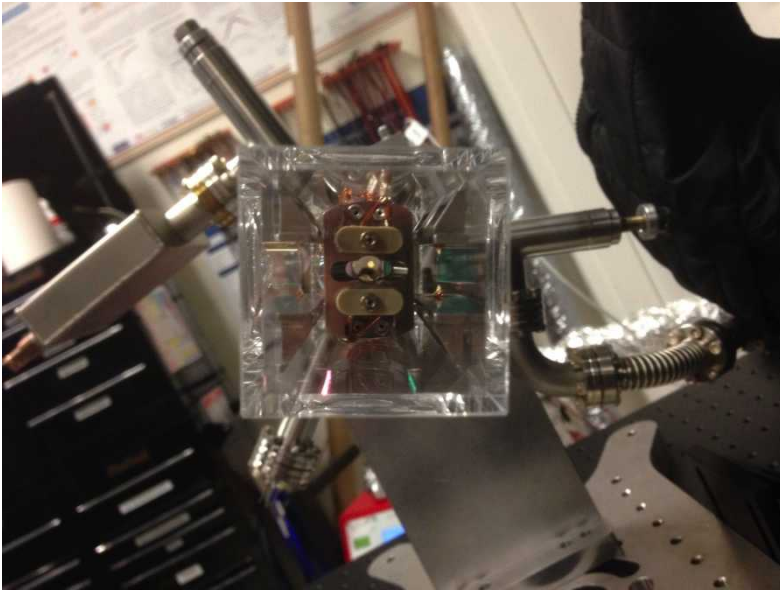
$$\kappa = E_{LS}^{(2)} - 2E_{LS}^{(1)}$$

# Dynamic atom positioning

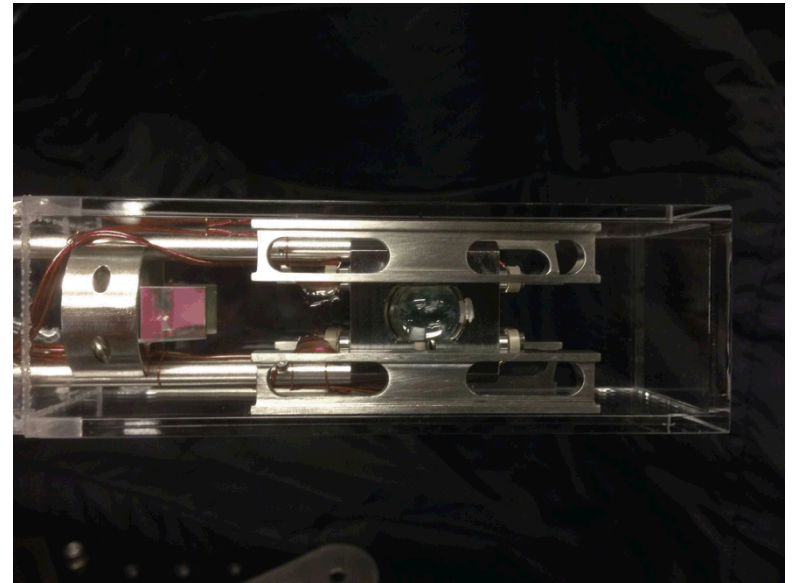


Drop and recapture

# Apparatus—new configuration



End view



Side view