

# Outdoor Test and Analysis Methods for Generating Coefficients for the Sandia Array Performance Model

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## Model Basics

Short Circuit Current is central to the model

$$I_{sc} = I_{sc0} f_1(AM) \left[ \frac{G_{poa}}{G_0} \right] [1 + \hat{\alpha}_{Isc} [T_c - T_0]]$$

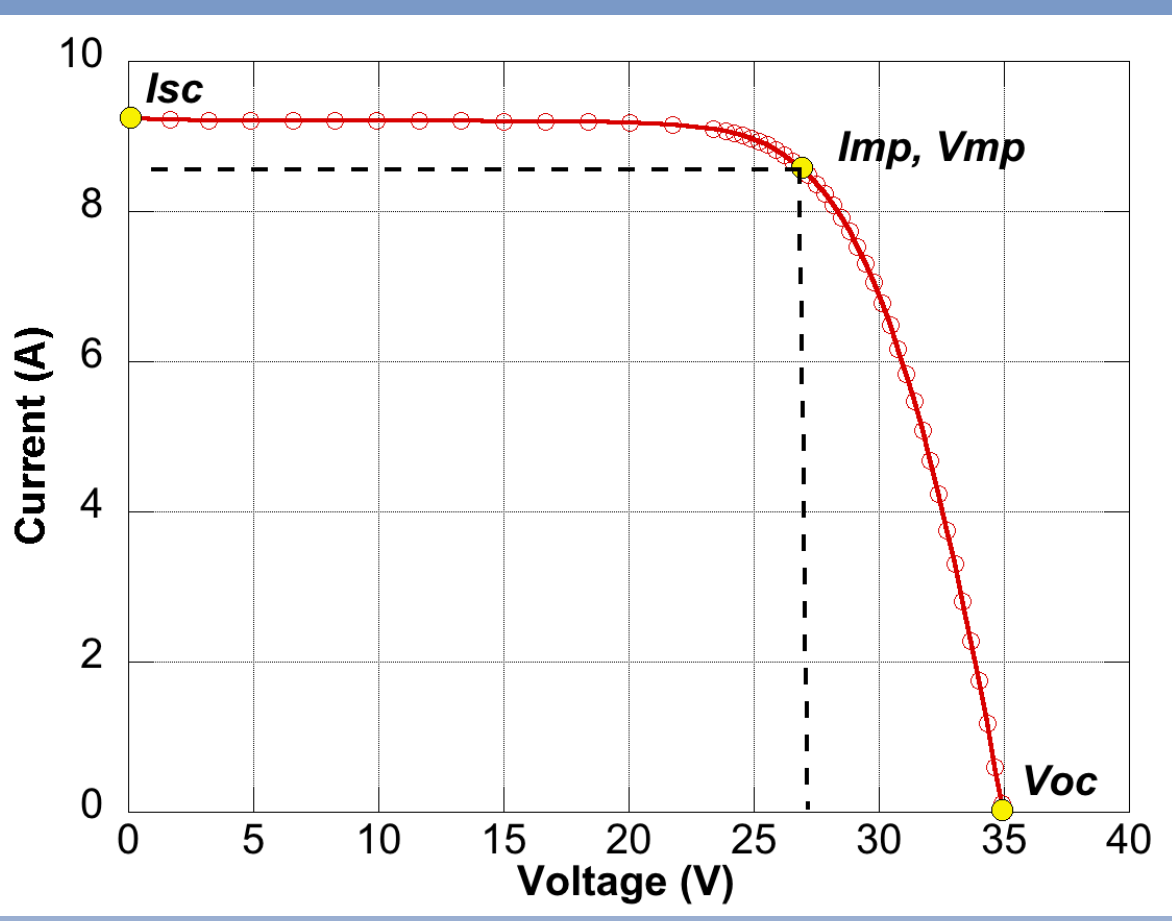
$$f_1(AM) = a_0 + a_1(AM) + a_2(AM)^2 + a_3(AM)^3 + a_4(AM)^4$$

$$E_e = \frac{I_{sc}}{I_{sc0} [1 + \hat{\alpha}_{Isc} [T_c - T_0]]}$$

Temperature Models

$$T_m = T_a + G_{POA} e^{a+bW}$$

$$T_c = T_m + \frac{G_{POA}}{G_0} \Delta T$$



Remaining primary functions dependent on  $E_e$ , not  $G_{poa}$

$$V_{oc} = V_{oc0} + N_s \delta(T_c) \ln(E_e) + \beta_{voc} [T_c - T_0]$$

$$I_{mp} = I_{mp0} [C_0 E_e + C_1 E_e^2] [1 + \hat{\alpha}_{I_{mp}} [T_c - T_0]]$$

$$V_{mp} = V_{mp0} + C_2 N_s \delta(T_c) \ln(E_e) + C_3 N_s [\delta(T_c) \ln(E_e)]^2 + \beta_{vmp} [T_c - T_0]$$

$$\delta(T_c) = \frac{nk[T_c + 273.15]}{q}$$

## Equipment

- Azimuth-Elevation solar tracker capable of AOI range between 0° and 90°.
- AOI-corrected pyranometer measuring global POA irradiance ( $G_{POA}$ ), mounted in the module test plane
- Pyranometer measuring the diffuse POA irradiance ( $G_{diff}$ ), mounted in the module test plane
- Pyrheliometer measuring DNI ( $G_{DNI}$ ), mounted on separate weather tracker
- Short circuit current and module temperature measurement
- Wind speed, ambient air temperature, barometric pressure
- Mitsubishi PV-UE125MF5N 36-Cell Polycrystalline Module (~2008)



## Test Conditions

Parameter	Required	Preferred
<i>Clear Sky Conditions</i>		
GNI	800 - 1050 W/m <sup>2</sup>	600 - 1200 W/m <sup>2</sup>
DNI/GNI	> 0.85	> 0.90
Air Mass	1.5 - 5.0	1.0 - 7.0
Wind Speed	0 - 4 m/s	0 - 10 m/s
Min. Test duration	600 minutes/2 days	1200 minutes/3 days
<i>Cloudy or All-Sky Conditions</i>		
GNI	200 - 400 W/m <sup>2</sup>	100 - 500 W/m <sup>2</sup>
DNI/GNI*	0 - 0.85 (< 0.05)	
Min. Test duration	200 minutes/1 day	1200 minutes/3 days
<i>Thermal and AOI Measurements</i>		
GNI	800 - 1200 W/m <sup>2</sup>	950 - 1050 W/m <sup>2</sup>
Variation in GNI	± 2.5%	± 0.5%
DNI/GNI	> 0.85	> 0.90
Air Mass	1 - 2	1.4 - 1.6
Wind Speed	< 4 m/s	< 2 m/s
Ambient Temperature	> 0°C	> 10°C

\* a range of conditions are preferred, however the bulk of the measurements should occur at DNI/GNI < 0.05

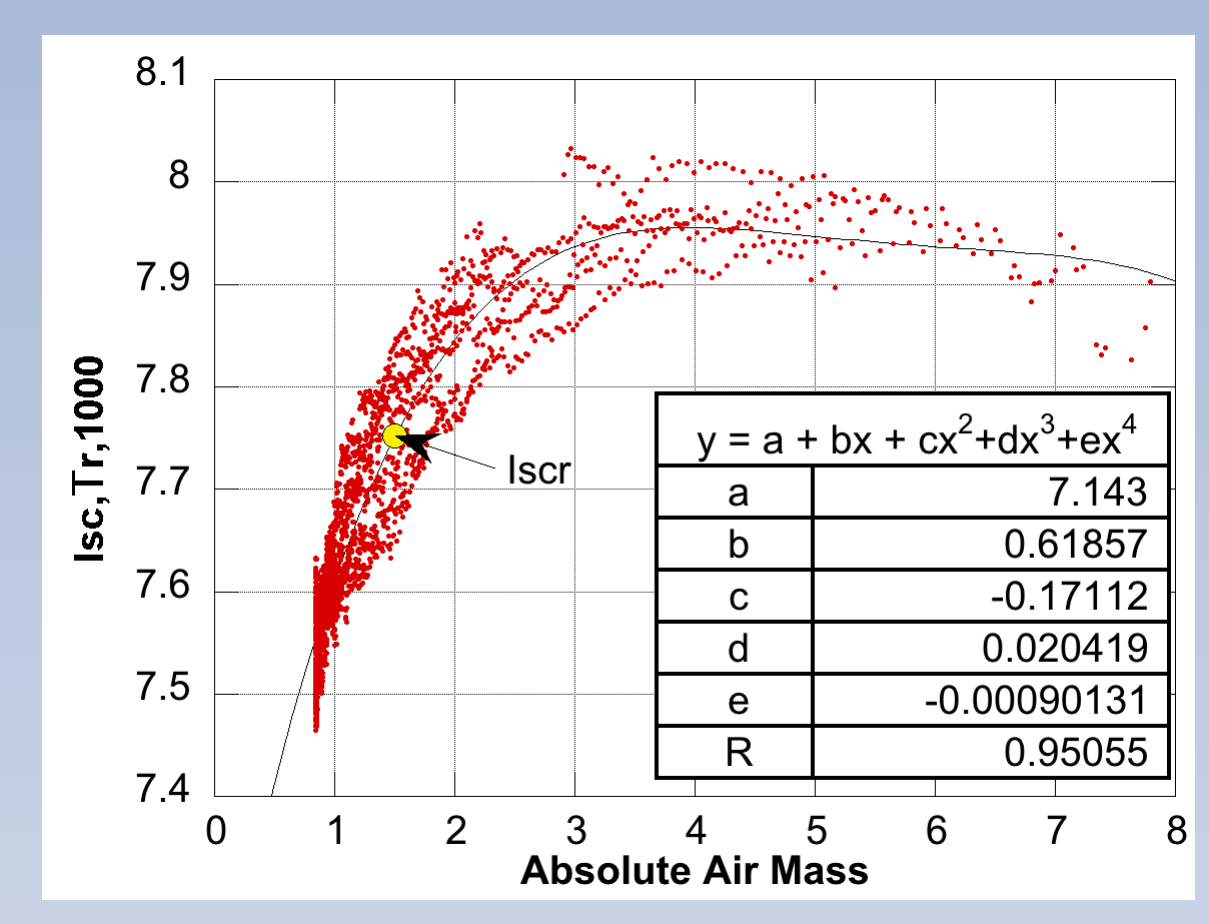
## Abstract

The Sandia Array Performance Model (SAPM), a semi-empirical model for predicting PV system power, has been in use for more than a decade. While several studies have presented laboratory intercomparisons of measurements and analysis, detailed procedures for determining model coefficients have never been published. Independent test laboratories must develop in-house procedures to determine SAPM coefficients, which contributes to uncertainty in the resulting models. In response to requests from industry, Sandia has formally documented the measurement and analysis methods as a supplement to the original model description.

## Example Analysis

- Thermal Test to measure temperature coefficients (not shown)
- Clear Sky Conditions are used to calibrate  $I_{sc0}$  and Air Mass function
- Calibrated  $I_{sc0}$  used to determine  $E_e$  as input to remaining functions
- All-Sky Conditions (Clear + Cloudy) are used to calibrate remaining primary functions
- Angle of incidence test to determine reflection losses (not shown)

### Short Circuit Current at STC and Air Mass Function



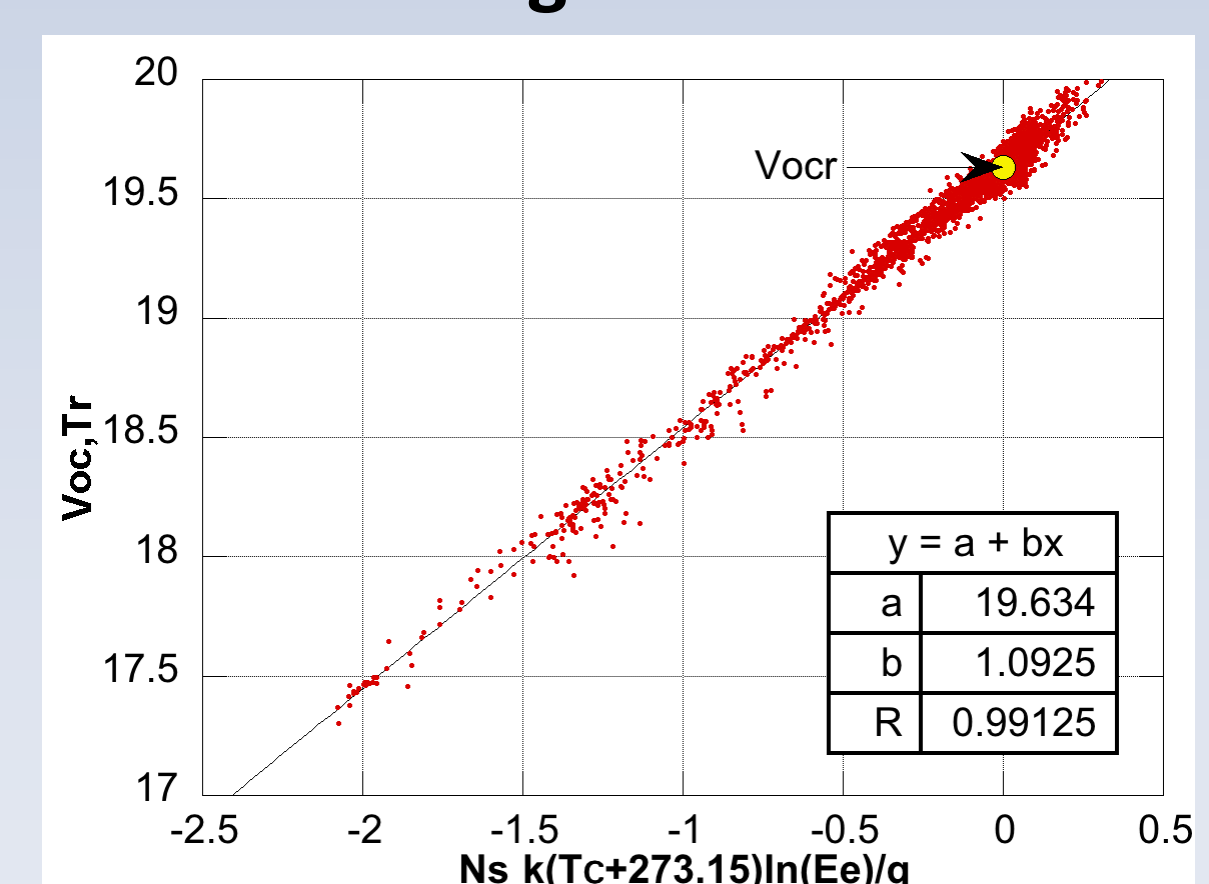
$$I_{sc,Tr,1000} = \frac{I_{sc}}{[1 + \hat{\alpha}_{Isc} [T_c - T_r]]} \left[ \frac{G_0}{G_{poa}} \right]$$

$$\bar{f}_1(AM) = y \quad I_{sc,r} = \bar{f}_1(AM = 1.5)$$

$$f_1(AM) = \frac{\bar{f}_1(AM)}{I_{sc,r}}$$

$$I_{sc0} = \frac{I_{sc,r}}{[1 + \hat{\alpha}_{Isc} [T_r - T_0]]}$$

### Open Circuit Voltage at STC and diode factor



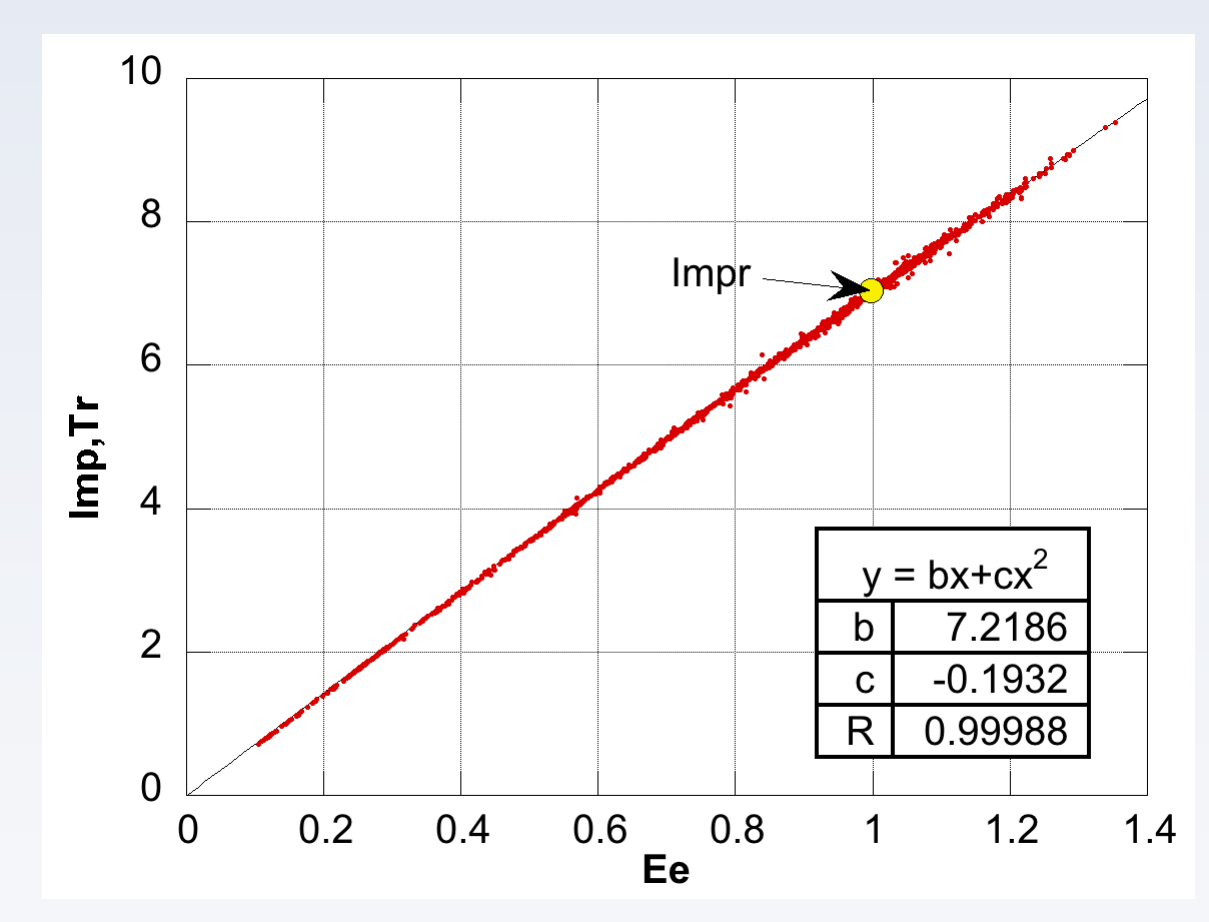
$$V_{oc,Tr} = V_{oc} - \beta_{voc} [T_c - T_r]$$

$$\frac{N_s k [T_c + 273.15] \ln(E_e)}{q}$$

$$V_{oc,r} = a \quad n = b$$

$$V_{oc0} = V_{oc,r} - \beta_{voc} [T_r - T_0]$$

### MPP Current at STC and "C" Coefficients



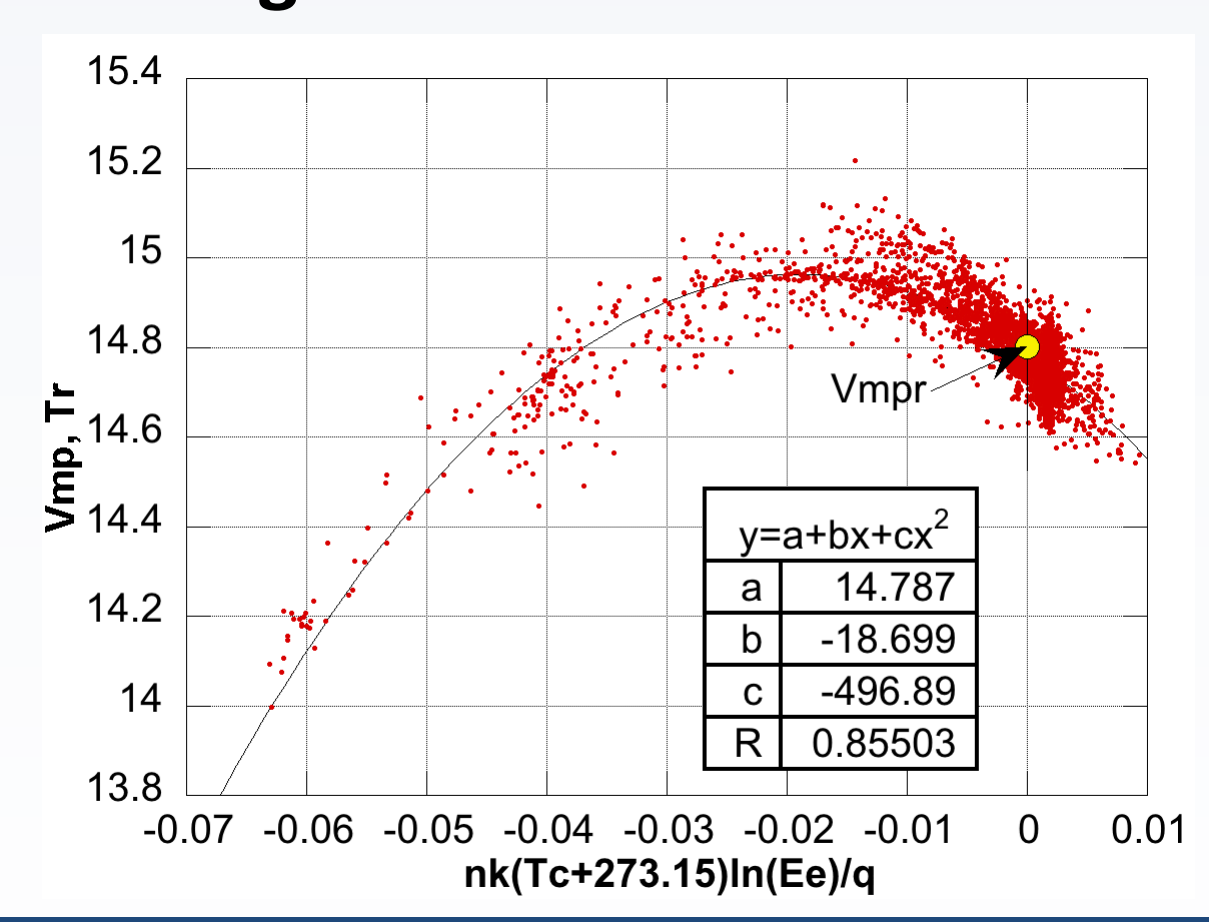
$$I_{mp,Tr} = \frac{I_{mp}}{[1 + \hat{\alpha}_{I_{mp}} [T_c - T_r]]}$$

$$I_{mp,r} = b + c$$

$$C_0 = \frac{b}{I_{mp,r}} \quad C_1 = \frac{c}{I_{mp,r}}$$

$$I_{mp0} = \frac{I_{mp,r}}{[1 + \hat{\alpha}_{I_{mp}} [T_r - T_0]]}$$

### MPP Voltage at STC and "C" Coefficients



$$V_{mp,Tr} = V_{mp} - \beta_{vmp} [T_c - T_r]$$

$$\frac{nk [T_c + 273.15] \ln(E_e)}{q}$$

$$V_{mp,r} = a \quad C_2 = \frac{b}{N_s} \quad C_3 = \frac{c}{N_s}$$

$$V_{mp0} = V_{mp,r} - \beta_{vmp} [T_r - T_0]$$

Symbol	Definition
$I_{sc}$	Short circuit current (A)
$V_{oc}$	Open Circuit Voltage (V)
$I_{mp}$	Current at maximum power (A)
$V_{mp}$	Voltage at maximum power (V)
$T_m$	Module back surface temperature, (°C)
$T_a$	Ambient temperature (°C)
$W$	Wind speed, (m/s)
$G_{poa}$	Broadband irradiance in plane of the array (W/m <sup>2</sup> ), typically a pyranometer
$G_0$	Reference irradiance, 1000 W/m <sup>2</sup>
$AM$	Pressure adjusted air mass
$\theta$	Incident angle between the module and the sun
$T_c$	Cell temperature (°C)
$\Delta T$	Temp. difference between cell and the module back surface at 1000 W/m <sup>2</sup> , typically 3°C
$T_0, T_r$	Ref temperatures, typically 25°C and 50°C
$\alpha_{Isc}, \alpha_{I_{mp}}$	Temperature coefficients for $I_{sc}$ and $I_{mp}$ (1/°C)
$\beta_{voc}, \beta_{vmp}$	Temperature coefficients for $V_{oc}$ and $V_{mp}$ (V/°C)
$I_{sc0}, I_{sc,r}$	Ref. short-circuit current at $T_0, T_r$ (A)
$V_{oc0}, V_{oc,r}$	Ref. open Circuit Voltage at $T_0, T_r$ (V)
$I_{mp0}, I_{mp,r}$	Ref. current at maximum power at $T_0, T_r$ (A)
$V_{mp0}, V_{mp,r}$	Ref. voltage at maximum power at $T_0, T_r$ (V)
$f_1(AM)$	Polynomial relating AM to $I_{sc}$
$f_2(\theta)$	Polynomial relating reflection losses to $I_{sc}$
$n$	Diode ideality factor (dimensionless)
$C_x$	Coefficients relating $E_e$ to $I_{mp}$ and $V_{mp}$
$a, b$	Coefficients relating $T_a$ and $W$ to $T_m$
$E_e$	Effective Irradiance (dimensionless)
$G_{diff}$	Diffuse component of irradiance (W/m <sup>2</sup> ),
$G_b$	Beam component of irradiance (W/m <sup>2</sup> )
$N_s$	Number of series-connected cells in a module cell-string
$k$	Boltzmann's constant, $1.38066 \times 10^{-23}$ (J/K)
$q$	Elementary charge, $1.60218 \times 10^{-19}$ (Coulomb)

## Summary

- In response to request by industry, Sandia has formally documented the measurement and analysis procedures to determine SAPM coefficients
- The procedure - along with example data sets - will be released at <https://pvpmc.sandia.gov>
- Coefficients generated using this procedure can be used with PV\_LIB or SAM
- An example analysis is shown here for the primary SAPM equations
- Full analysis including temperature coefficients and AOI response is presented in the procedure

