

# Uncertainty Quantification, Verification, and Validation of a Thermal Simulation Tool for Molten Salt Batteries

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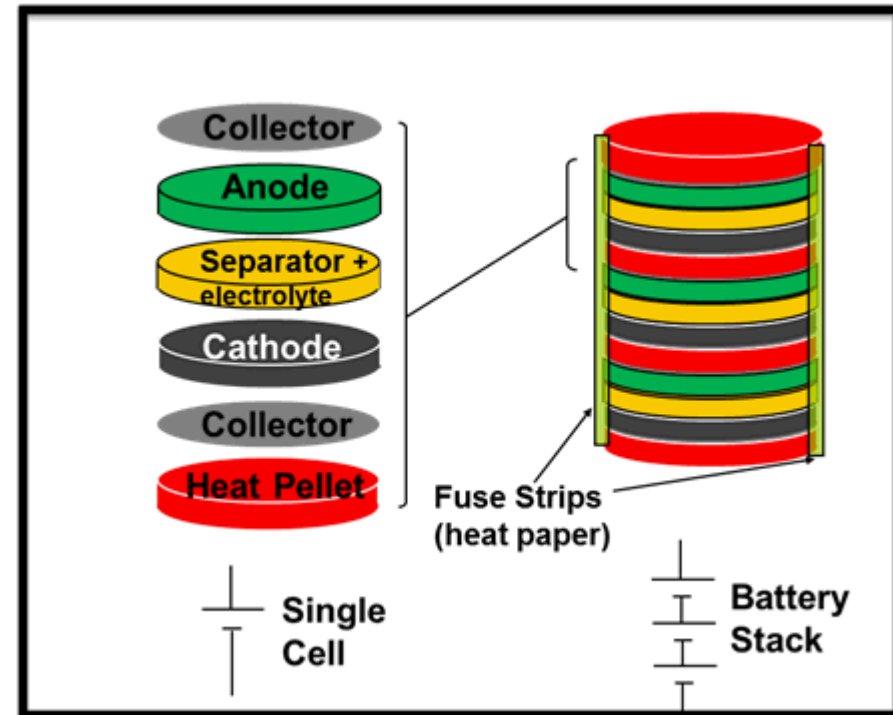


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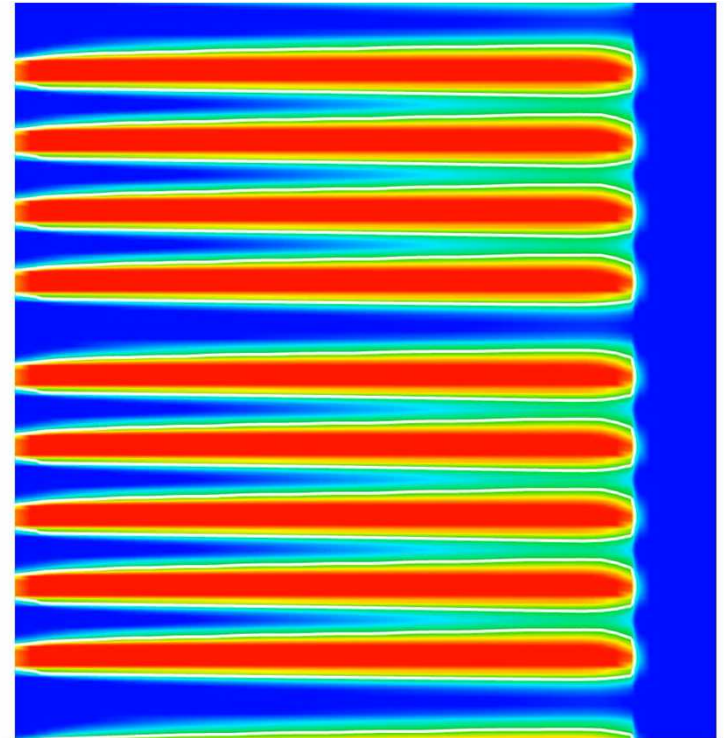
- Molten salt batteries are power sources that provide
  - Long shelf life
  - High voltage output
  - High current capacity
  - High power density
- Heat pellet burn releases large amounts of heat energy
- Solid electrolyte in separator melts and flows into porous electrodes, forming an electrochemical circuit and delivering power



- Thermal management is critical for design of molten salt batteries
  - Heat generation and transport is the dominant process driving electrochemical performance
- Computational models widely used to aid design process
- TABS solves unsteady heat equation on 2D axisymmetric computational domain, using Sierra/Aria (FEM)

$$\rho c_p \frac{\partial T}{\partial t} = \nabla \cdot \kappa \nabla T + S_E$$

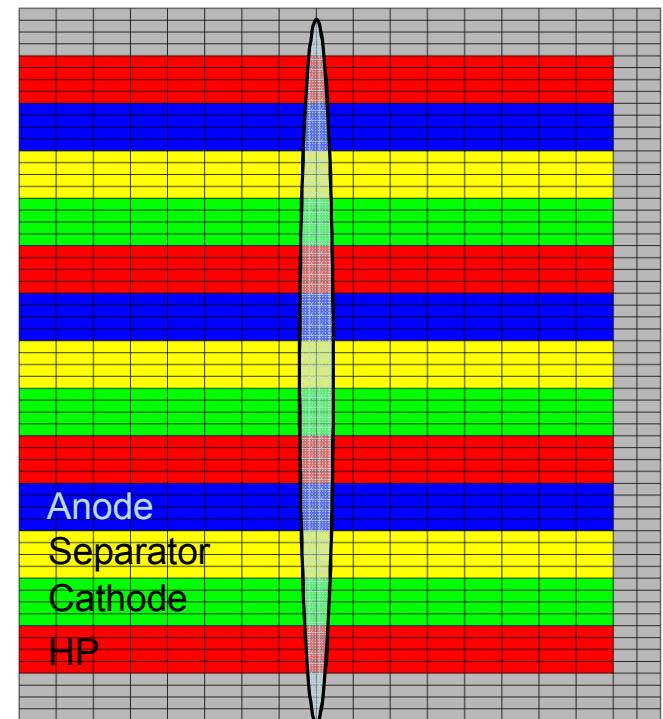
- Material properties are temperature dependent and have uncertainty
- Major energy source in  $S_E$  is burning of heat pellets. Burn front is tracked using a level-set method



Simulated battery activation

- Uncertainty Quantification: Determining the relationship between uncertain model inputs and probabilistic outputs
  - Yields more realistic simulation results and model validation
  - Allows design engineers to make informed decisions when specifying material property and manufacturing tolerances
- Verification: Ensuring models are being solved correctly
- Validation: Evaluating the models for accuracy by comparing simulations to experiments

- Rise Time: Time between heat pellet ignition and delivery of useful electric power
- Lifetime: Time between heat pellet ignition and termination of useful power
- A translation between electrochemical power and temperature is made:
  - Melted electrolyte in separator region corresponds to activated battery
- QOIs
  - Battery rise time
    - **Rise Time Min:** Any point in separator region is above electrolyte melt temperature ( $T_{melt}$ )
    - **Rise Time Mid:** Any column in separator is above  $T_{melt}$
    - **Rise Time Max:** Entire separator is above  $T_{melt}$
  - Battery lifetime
    - Inverse of three rise time metrics
  - Anode maximum temperature
  - Cathode maximum temperature



Rise Time Mid / Lifetime Mid  
2D Axisymmetric Simplified Geometry

# Uncertainty Quantification (UQ)

- Each simulation parameter has nominal value and uncertainty range (shown in table)
- Uniform distribution assumed
- Latin Hypercube sampling used to run 500 unique thermal discharge simulations; QOIs calculated (Dakota toolkit)
- Collection of inputs and outputs used in a polynomial chaos UQ study
- Result is collection of uncertainty ranges and global sensitivity metrics for each output QOI w.r.t. each input parameter

Parameter	Lower Bound	Upper Bound
HP $c_p$	60%	140%
Separator $c_p$	60%	140%
Cathode $c_p$	60%	140%
Anode $c_p$	60%	140%
HP $\kappa$	10%	190%
Separator $\kappa$	10%	190%
Cathode $\kappa$	10%	190%
Anode $\kappa$	10%	190%
Insulation $\kappa$	10%	500%
HP Density ( $\rho$ )	97%	103%
HP Mass	99.5%	100.5%
HP Burn Speed	80%	100%
HP Heat Output	99%	101%
Ambient Temp	99.6%	100.4%
Emissivity ( $\epsilon$ )	0	1

- Two types of batteries presented: long life and short life

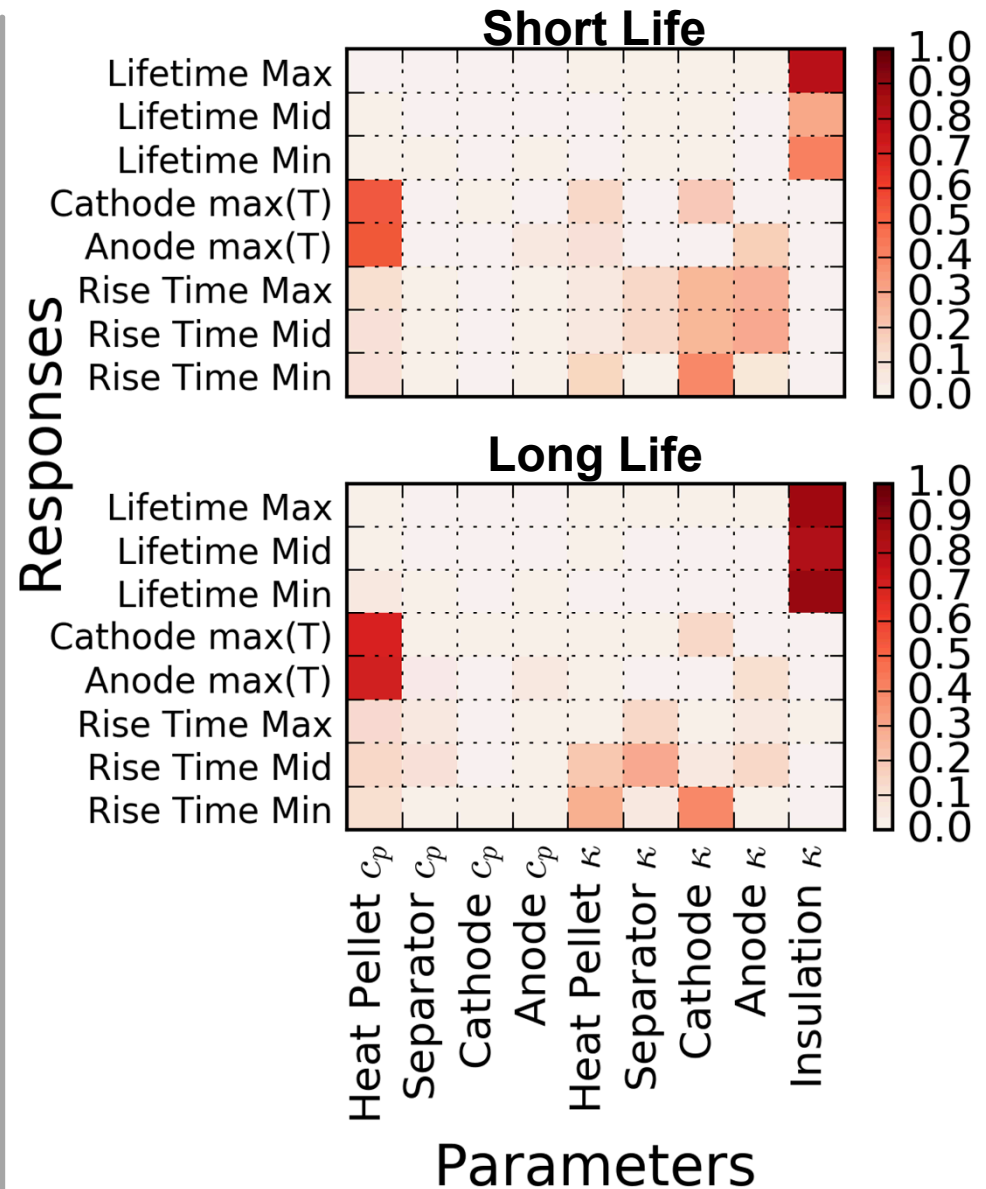
QOI	Short Life	Long Life
<i>Lifetime Max</i>	44%	32%
<i>Lifetime Mid</i>	62%	30%
<i>Lifetime Min</i>	76%	54%
Cathode max(T)	12%	10%
Anode max(T)	12%	9%
<i>Rise Time Max</i>	35%	130%
<i>Rise Time Mid</i>	47%	53%
<i>Rise Time Min</i>	59%	64%

- Maximum standard deviation ( $\sigma$ ) observed is 130% of the mean
- Maximum temperature QOIs show significantly smaller  $\sigma$ , indicating lower sensitivity to input uncertainties



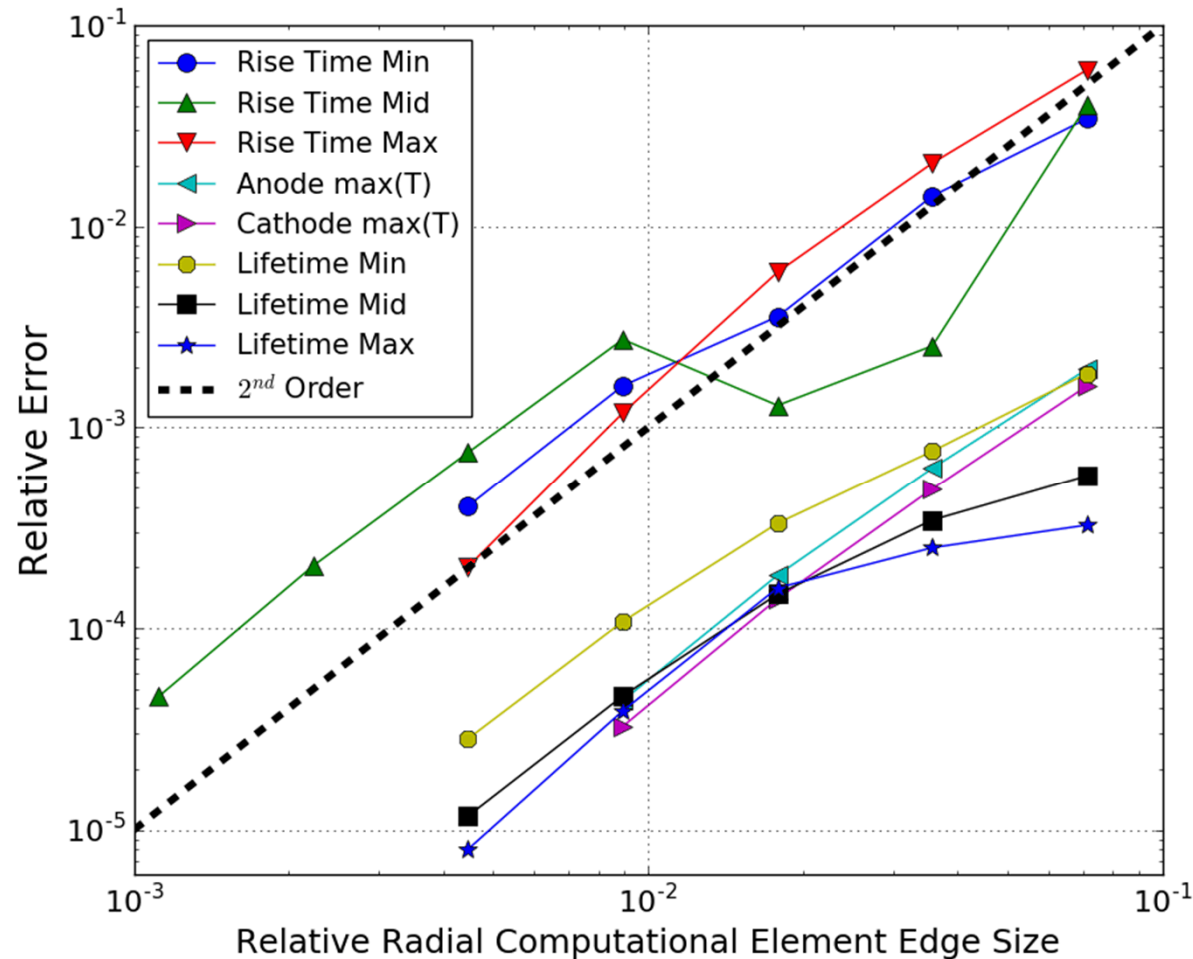
# Results: Sensitivity Index

- Sensitivity Index: Fraction of QOI uncertainty that results due to uncertainty in each input variable
  - Main effect sensitivity index shown here (no input variable interaction effects plotted)
- Darker red corresponds to larger effect of input uncertainty on output uncertainty
- Lifetime uncertainty mostly due to insulation  $\kappa$
- Max temperatures largely depend on heat pellet  $c_p$  as well as electrode material  $\kappa$
- Emissivity had large input range, but low sensitivity index

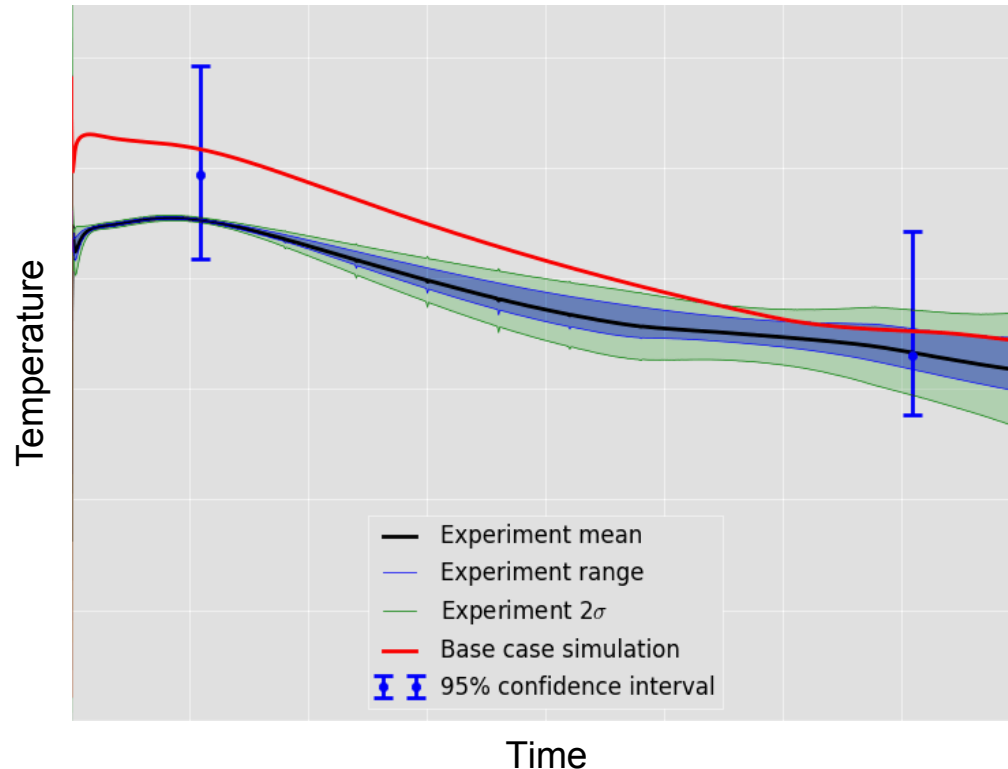


# Verification and Validation (V&V)

- Focus here on spatial discretization (mesh refinement) effects on QOIs
- Richardson Extrapolation used to determine relative error and calculate order of convergence
- All QOIs approach 2<sup>nd</sup> order convergence
- Rise time QOIs show largest relative errors (3-8% on coarsest mesh)
- Less than 1% error for other QOIs



- Three replications of instrumented battery (each with 15 thermocouples) activated to gather model validation temperature data
- Example validation plot for one thermocouple location:



- Experimental values fall within confidence interval range
- Working to improve nominal simulation accuracy and decreasing confidence interval

- Assessing effects of input uncertainties
  - Provides valuable information for battery design
  - Motivates experiments to reduce specific uncertainties
- DAKOTA toolkit allows for automated UQ and sensitivity studies
- Demonstrated efforts to both verify and validate our thermal model
  
- Ongoing/Future Work
  - Narrow uncertainty ranges with in-depth literature review and experiments
  - Incorporating electrochemistry and mechanics in addition to thermal
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Thank You