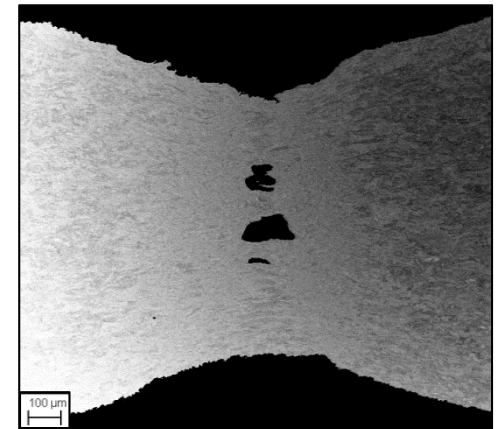
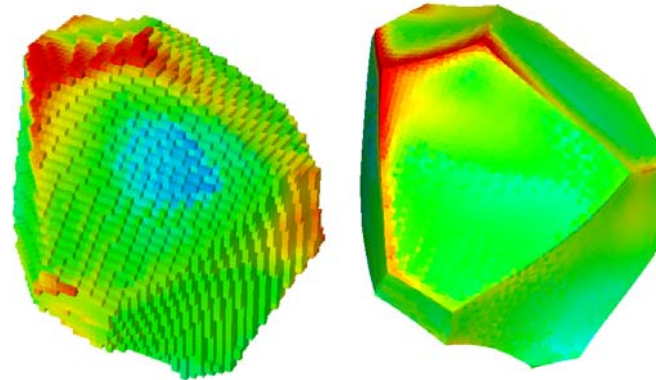
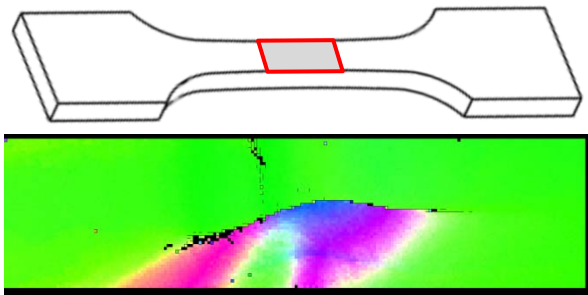


*Exceptional service in the national interest*



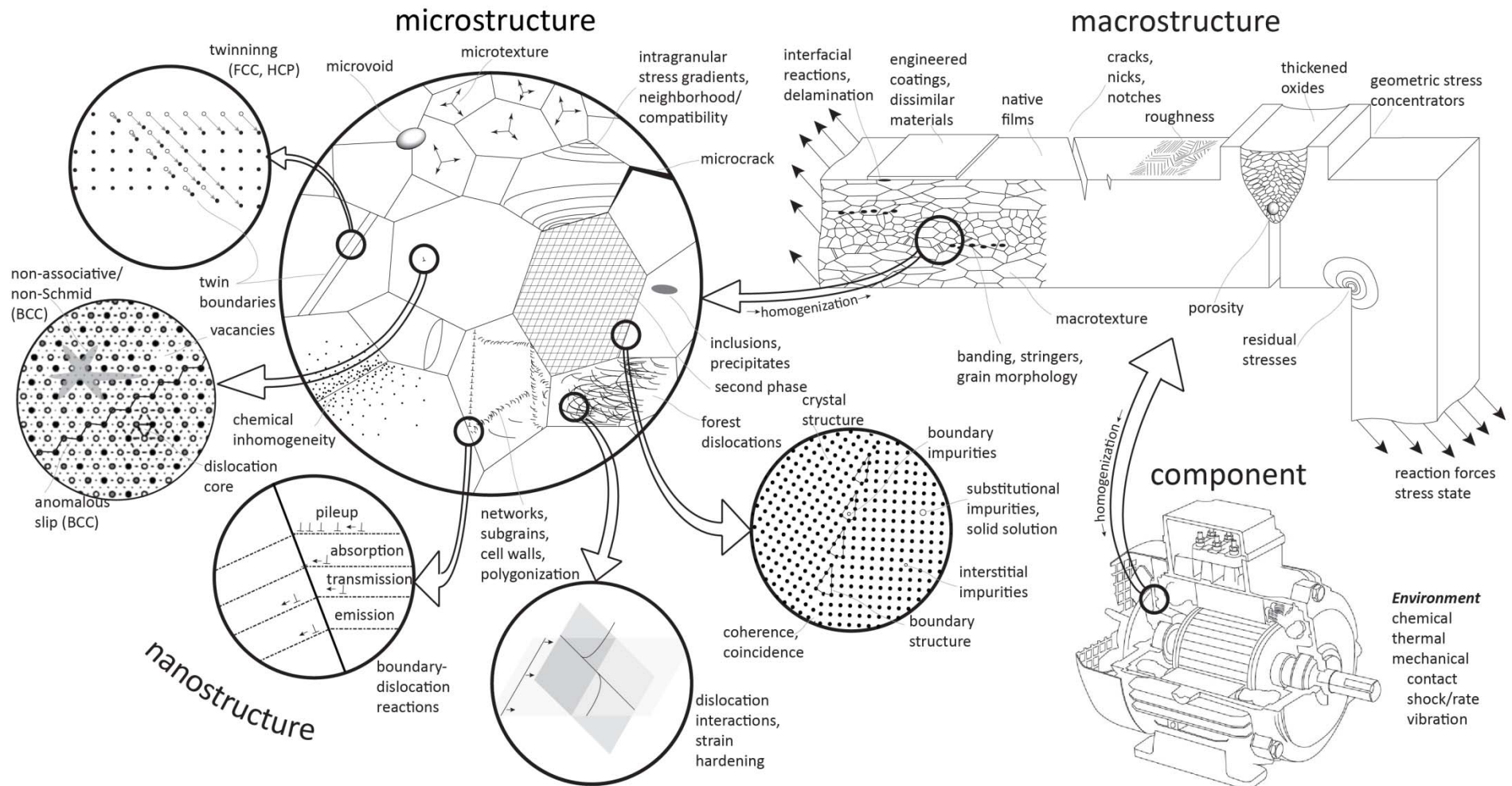
Sandia  
National  
Laboratories



## Quantifying Grain-Scale Deformation for Direct Comparison to Crystal Plasticity Predictions

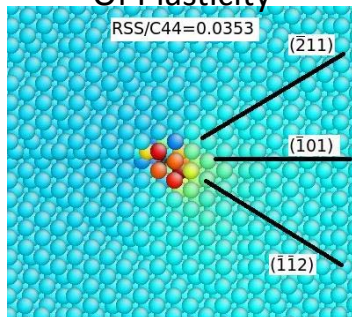
**Brad L. Boyce; Hojun Lim; Jay D. Carroll; Thomas E. Buchheit; Corbett C. Battaile**  
**Sandia National Laboratories**

# Introduction: Material and length-scale roadmap for deformation and failure of structural metals

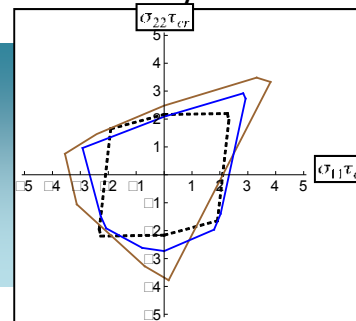


# Developing an experimentally validated model for grain-scale deformation (crystal plasticity)

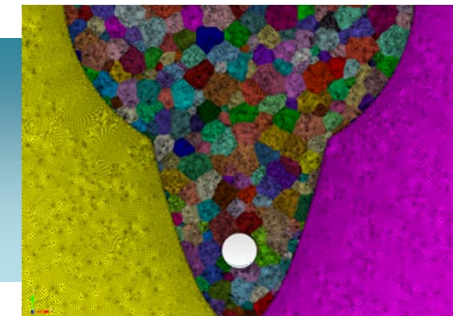
Atomic Mechanisms  
Of Plasticity



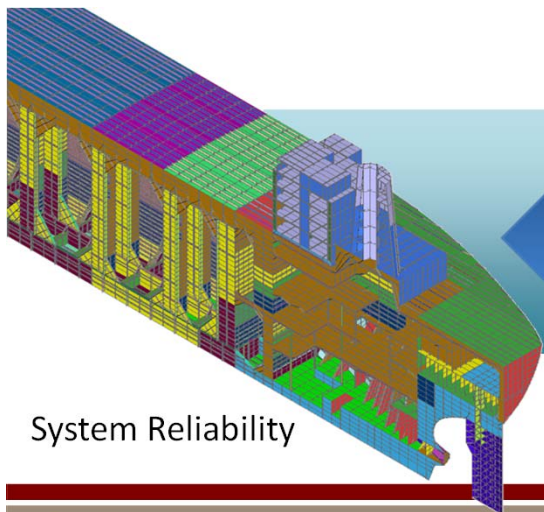
Single-Crystal  
Plasticity Models



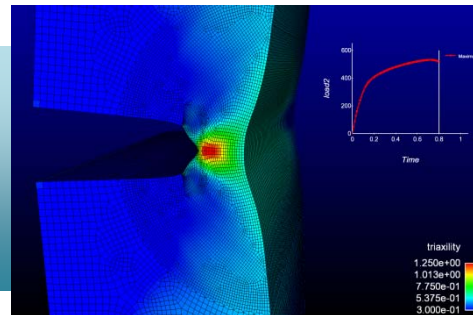
Polycrystalline  
Deformation Response



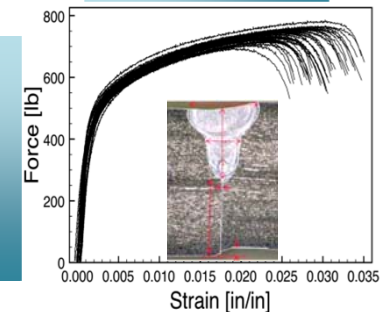
Goal: Provide a science-based foundation for design, analysis, and qualification capabilities that links mesoscopic/microscopic inhomogeneity to property variability.



System Reliability



Reduced Order Modeling  
For Efficient Stochastic Computations

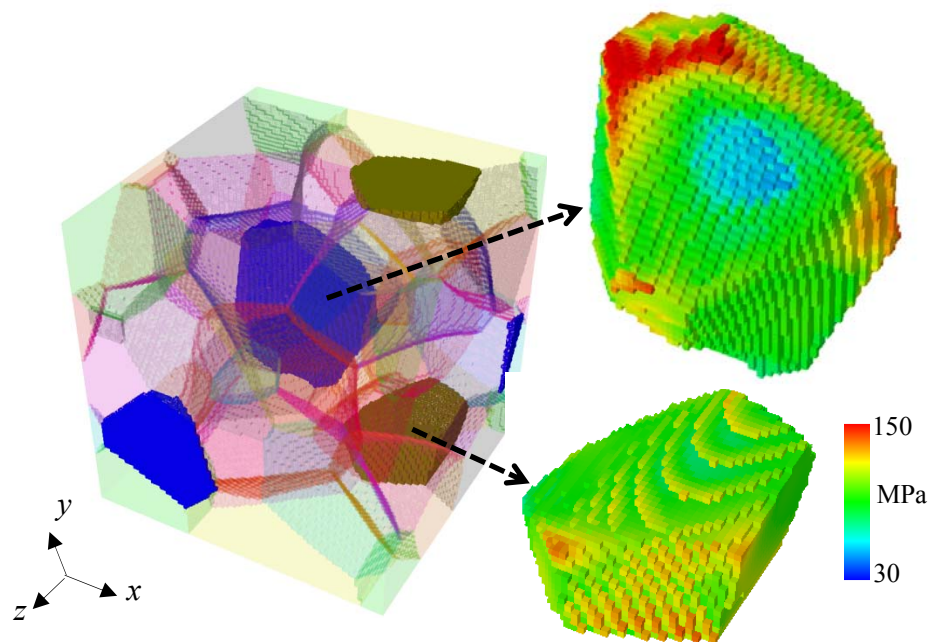


Stochastic Outcomes  
From Different Configurations

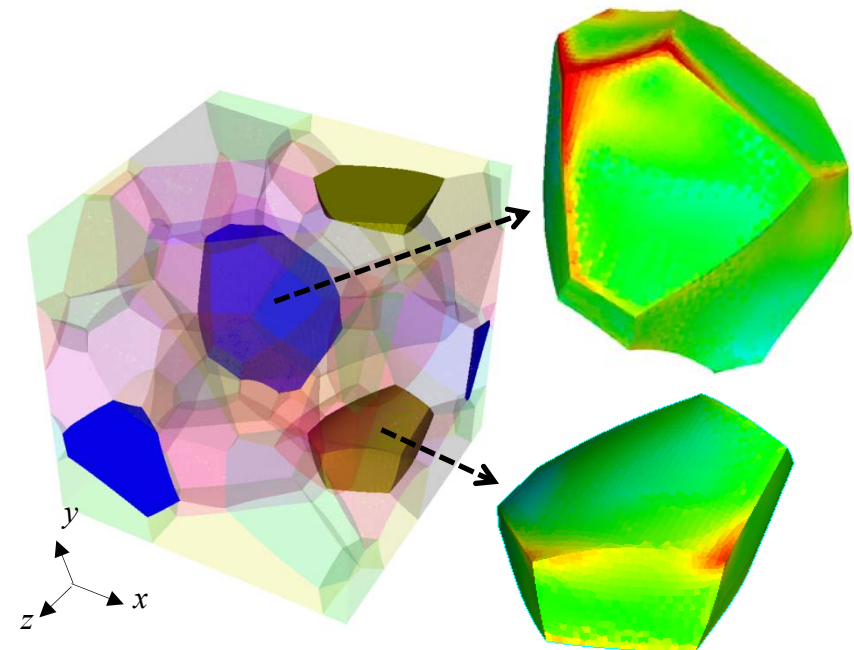


# Recent Sandia advances in Polycrystal Plasticity: Phase-Field generated microstructure & smooth meshing

Voxelated FE mesh



Conformal FE mesh

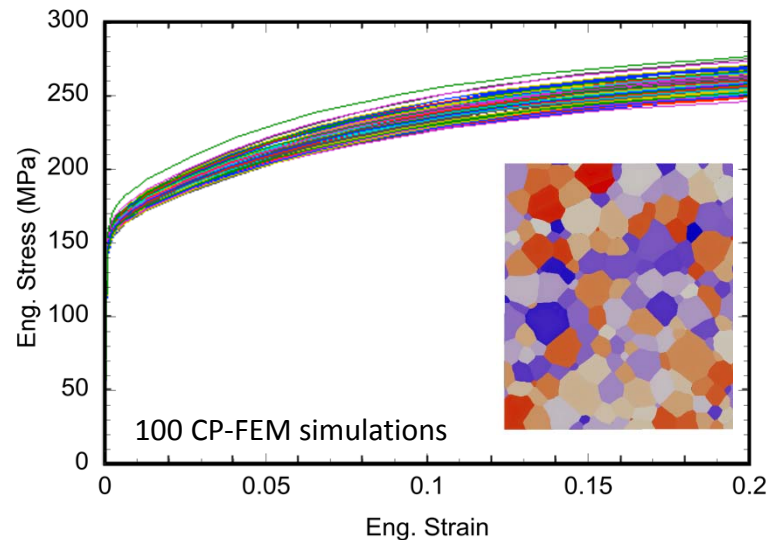
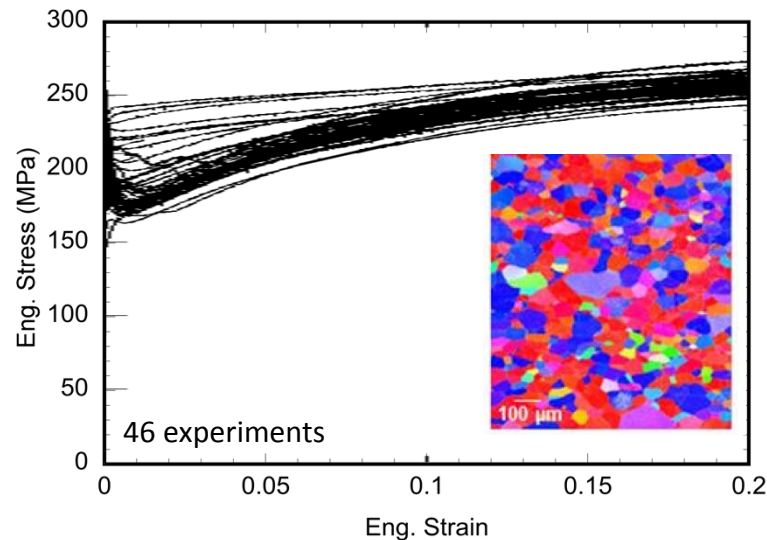


Von Mises stress contours at 10% deformation

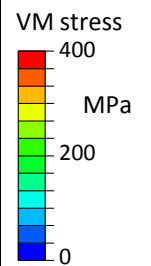
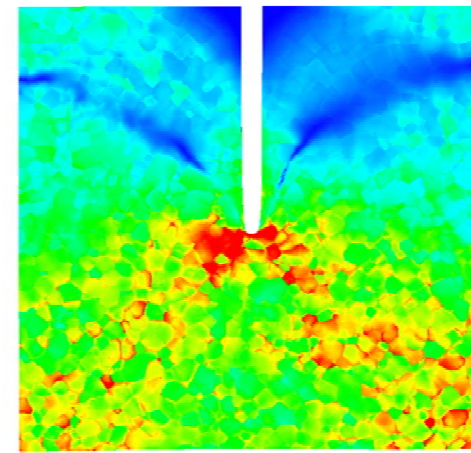
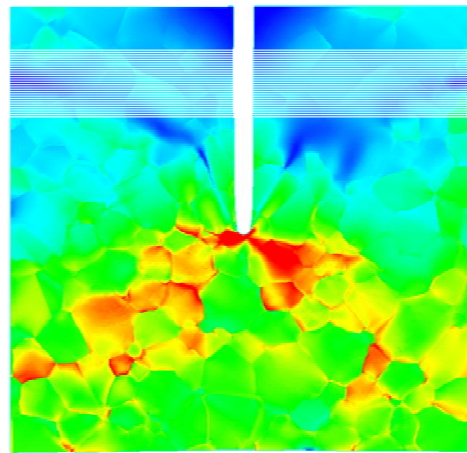
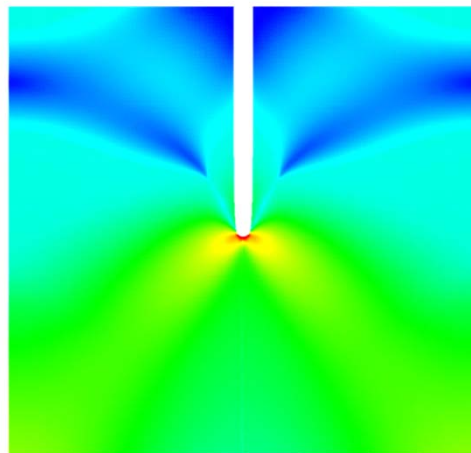
ABSTRACT	SYMPOSIUM	SESSION	WHEN	WHERE
<p><u>Developing Physically-based Three Dimensional Microstructures: Bridging Phase Field and Crystal Plasticity Models</u></p> <p>Hojun Lim<sup>1</sup>; Fadi Abdeljawad<sup>1</sup>; Steven J. Owen<sup>1</sup>; Byron W. Hanks<sup>1</sup>; Corbett C. Battaile<sup>1</sup>; <sup>1</sup>Sandia National Laboratories</p>	<p>Computational Materials Discovery and Optimization: From 2D to Bulk Materials</p>	<p>Microstructure and Mechanical Properties</p>	<p>Thursday 11:10 AM - 11:30 AM</p>	<p>Music City Center 207D</p>



# Predicting Stochastic Behavior of Polycrystals



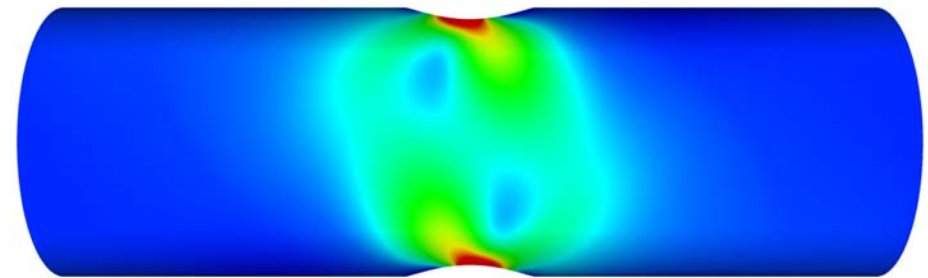
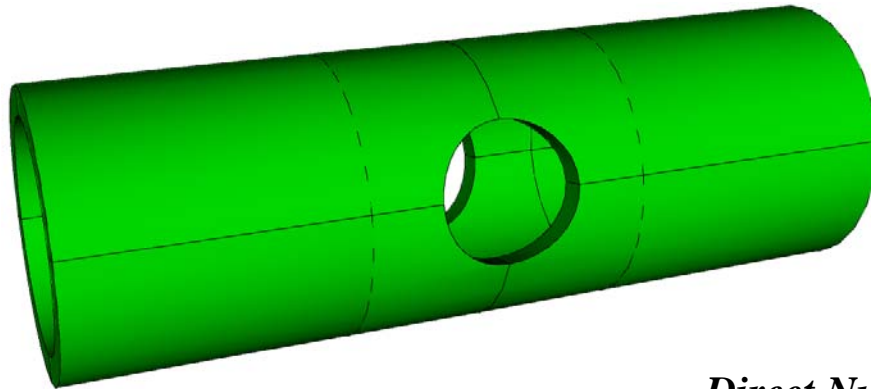
Grain-scale variability in macroscale response



VM stress fields after 3% deformation

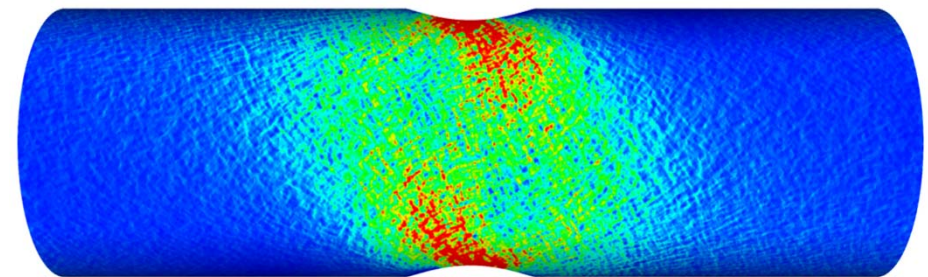
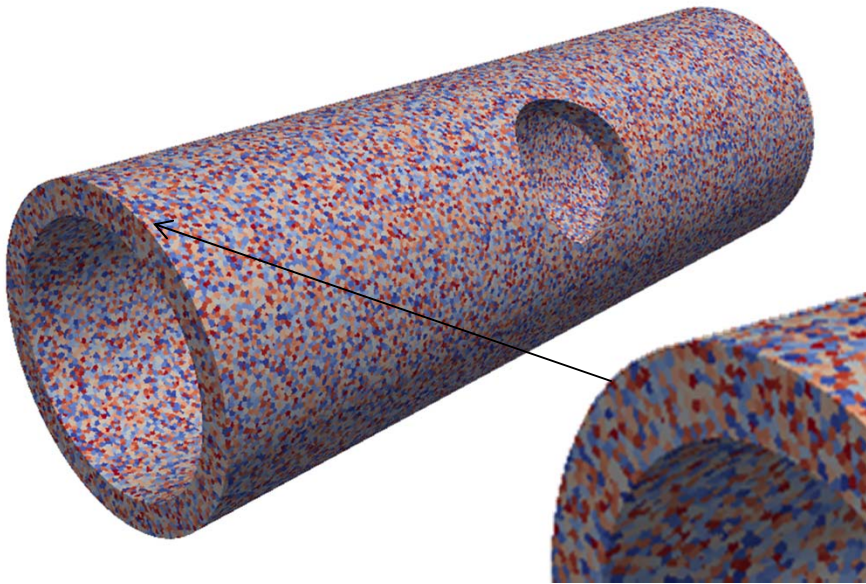
# On the horizon: System-scale simulations with explicit microstructural representations.

## *Homogenization*



8K elements

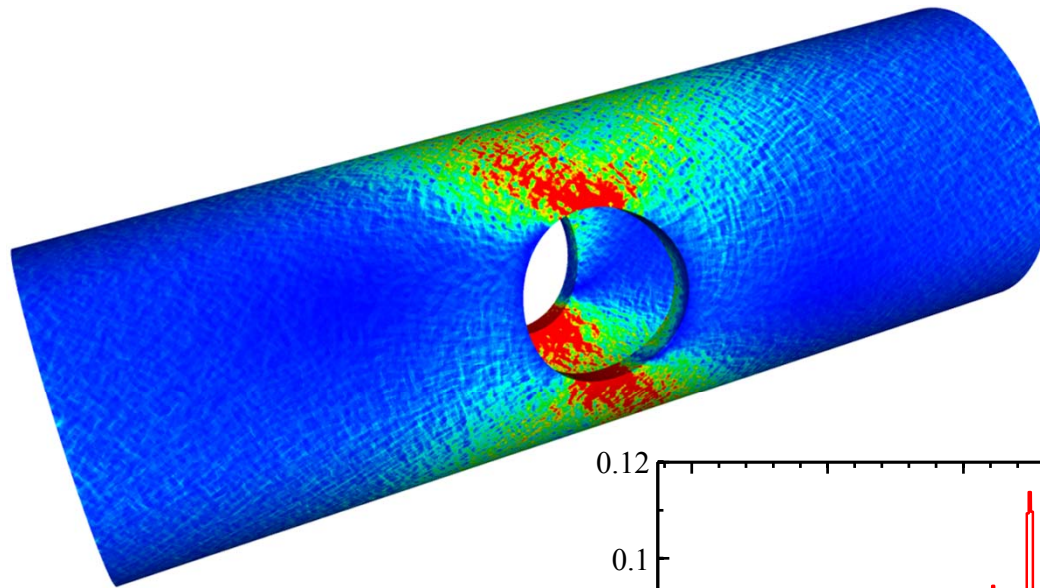
## *Direct Numerical Simulation*



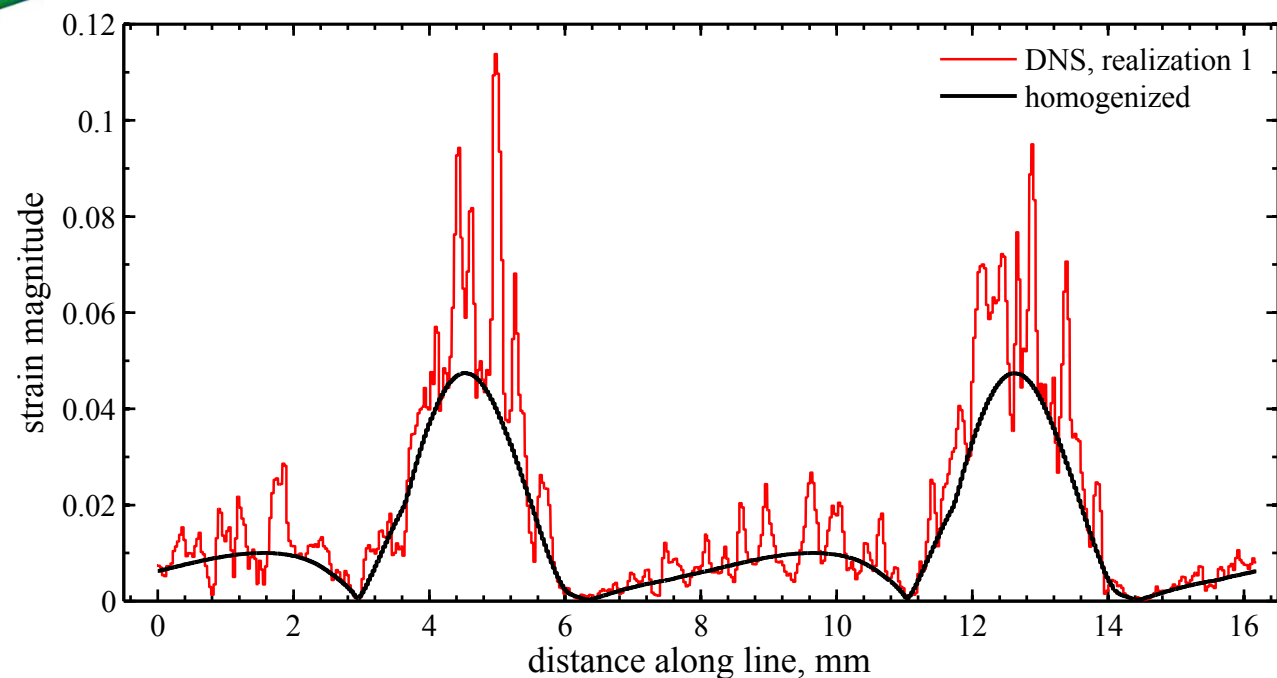
35M elements, 350K grains  
2400 processors (Chama)

effective\_log\_strain  
0.020  
0.015  
0.010  
0.005  
0.000

# On the horizon: System-scale simulations with explicit microstructural representations.



effective\_log\_strain  
0.020  
0.015  
0.010  
0.005  
0.000





## Polycrystal plasticity employs finite element method to discretize crystallographic slip at the crystallographic-level.

Slip rate:  $\dot{\gamma}^\alpha = \dot{\gamma}_0^\alpha \left( \frac{\tau^\alpha}{g^\alpha} \right)^{1/m}$  (Hutchinson, 1976)      24  $\langle 111 \rangle \{110\}$  slip systems

Slip resistance:  $g^\alpha = \max(\tau_{\text{cr}}^\alpha - \tau_{\text{ns}}^\alpha, 0) + \tau_{\text{obs}}^\alpha$  (Weinberger, 2012)

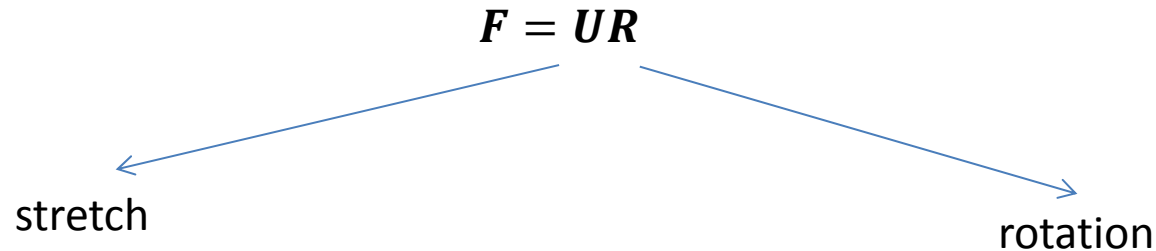
$\xrightarrow{\hspace{1.5cm}}$  Lattice friction       $\xrightarrow{\hspace{1.5cm}}$  Obstacle stress

Obstacle stress:  $\tau_{\text{obs}}^\alpha = \alpha \mu b \sqrt{\sum_{\beta=1}^{NS} \rho^\beta}$  (Taylor, 1934)

$$\rho^\alpha = \left( \kappa_1 \sqrt{\sum_{\beta=1}^{NS} \rho^\beta} - \kappa_2 \rho^\alpha \right) \cdot |\dot{\gamma}^\alpha| \quad (\text{Kocks, 1976})$$

# Options for Experimental Validation at Grain-Scale

Deformation gradient can be decomposed into a product of stretch and rotation



Analagously, experimentally we measure shape change and rotation

Digital Image Correlation  
Surface Profilometry  
Synchrotron X-ray microdiffraction

Electron Backscatter Diffraction  
Precession Electron Diffraction  
Synchrotron X-ray microdiffraction

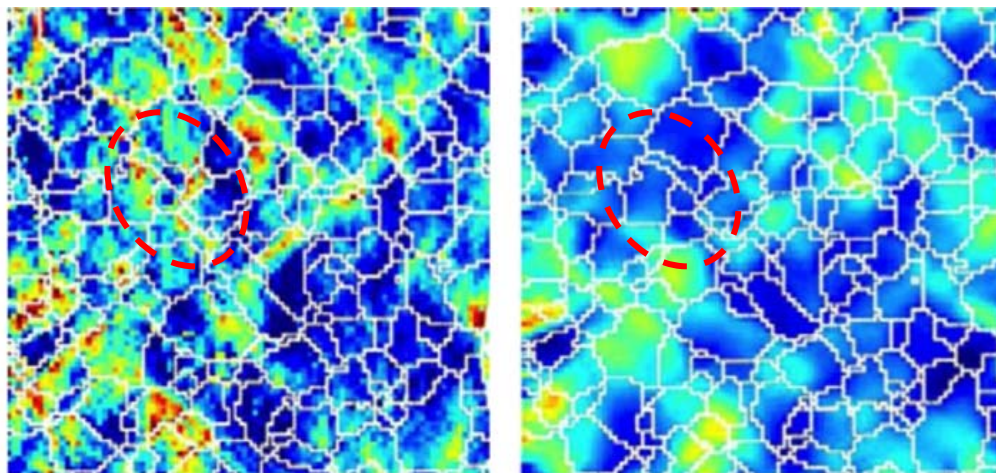
# Quantifying Shape Change



# Previous Work on Sim.- Exp. Comparison

**“Quantitative comparisons between the model and experiments”**

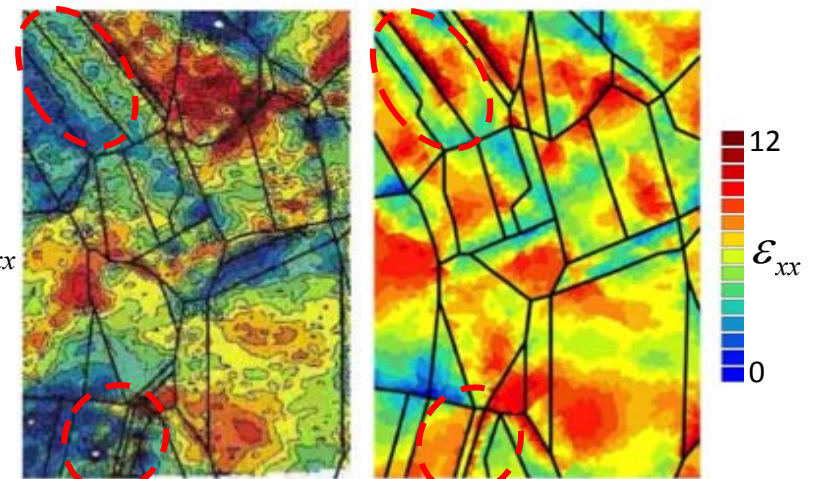
Zr 702 polycrystal (Heripre et al, 2007)  
(2.5 % strain)



Experiment

Simulation

OFHC Cu polycrystal (Musienko et al, 2007)  
(5 % strain)

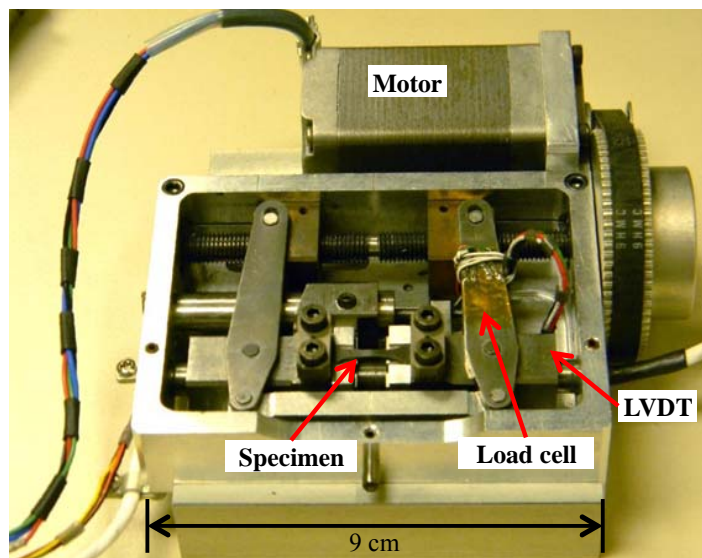


Experiment

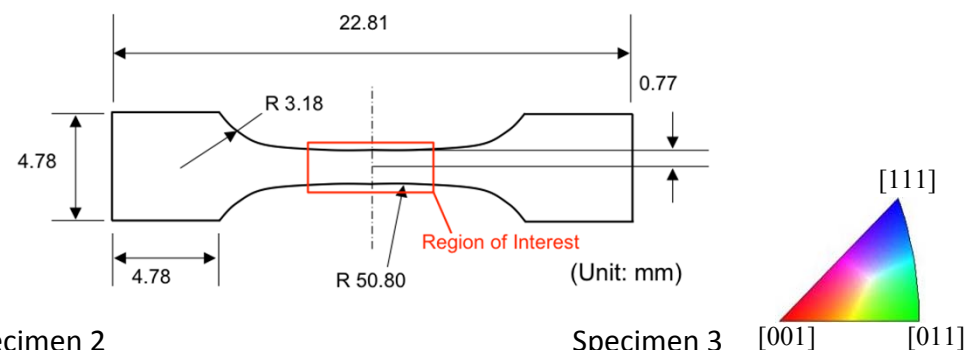
Simulation

**Limited success has been achieved in modeling polycrystal deformation behavior due to unknown subsurface grains**

# Experimental Setup



- Tantalum oligocrystals with mostly columnar 2D grain structure eliminate unknown subsurface grain morphology.
- In-situ* load frame developed at Sandia
- HR-DIC (surface strain fields) and EBSD (crystal orientations) measurements at load inside SEM



Specimen 1



1mm

15 grains  
(1,426,650 elements)

Specimen 2



18 grains  
(1,664,150 elements)

Specimen 3

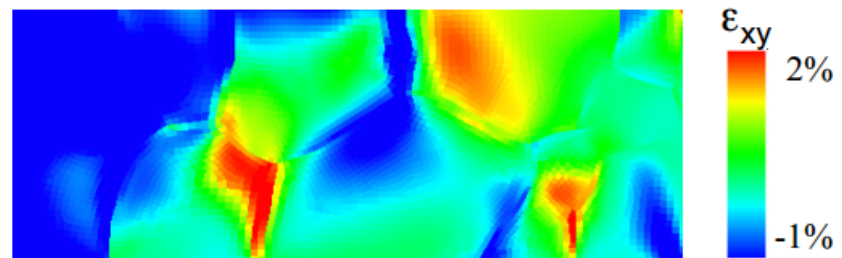
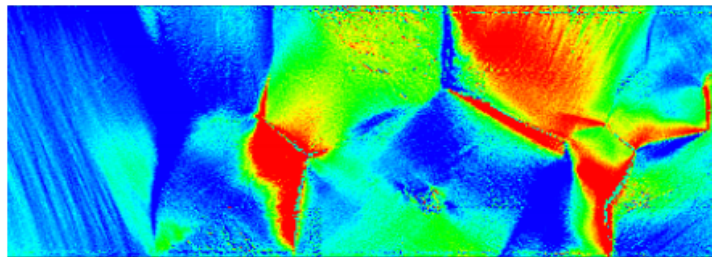
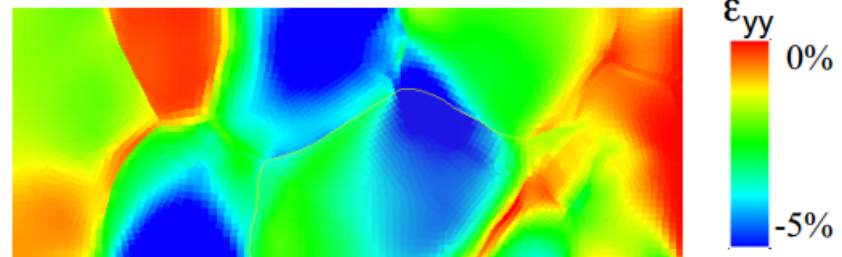
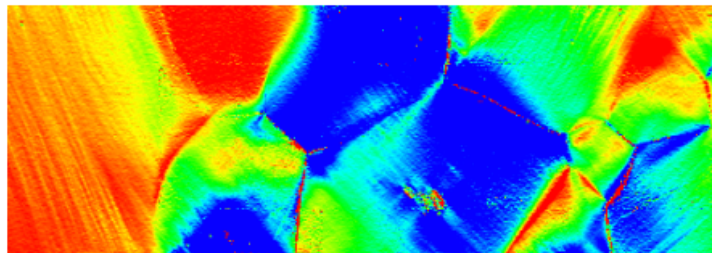
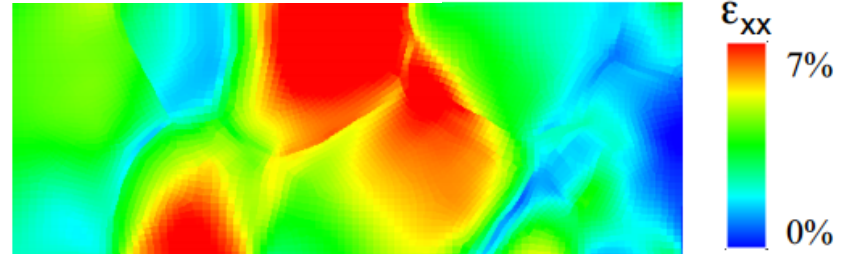
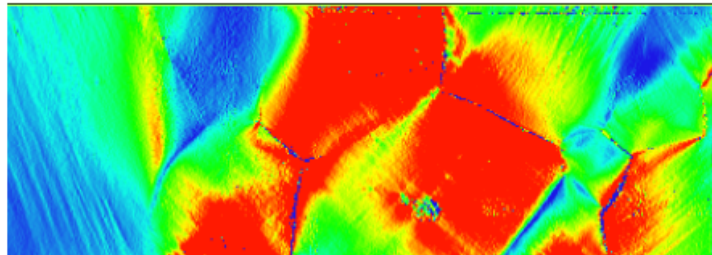
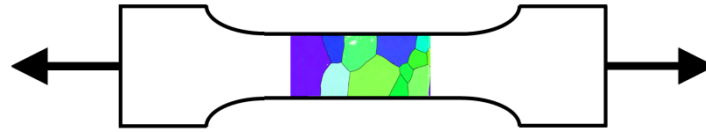


12 grains  
(2,140,020 elements)

RD  
TD



# Side-by-side qualitative comparison



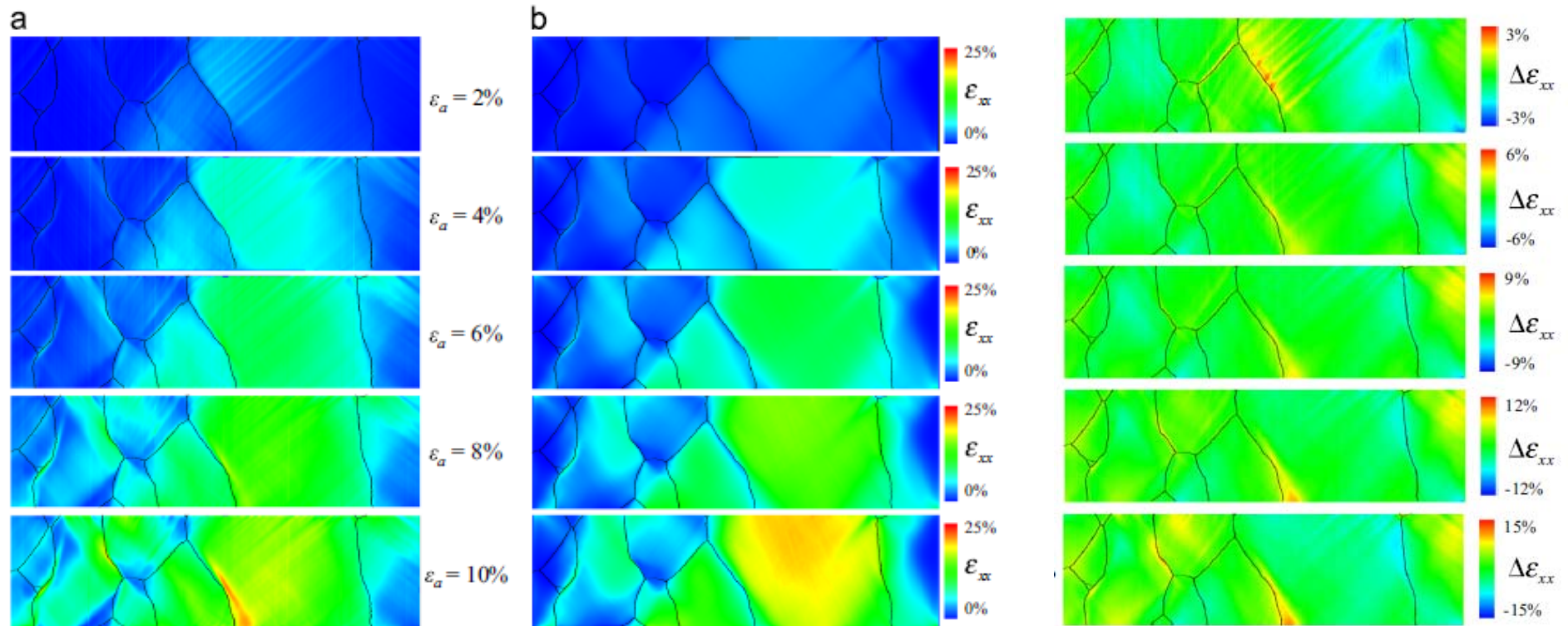
Experimental measurement of strains within individual grains using SEM Digital Image Correlation

2D slice of a 3D simulation of strain inhomogeneity based on crystal plasticity finite element modeling.



# A Quantitative Model-Experiment Difference Map

$$\epsilon_{xx}^{DIC} - \epsilon_{xx}^{CPFEM} = \Delta\epsilon_{xx}$$

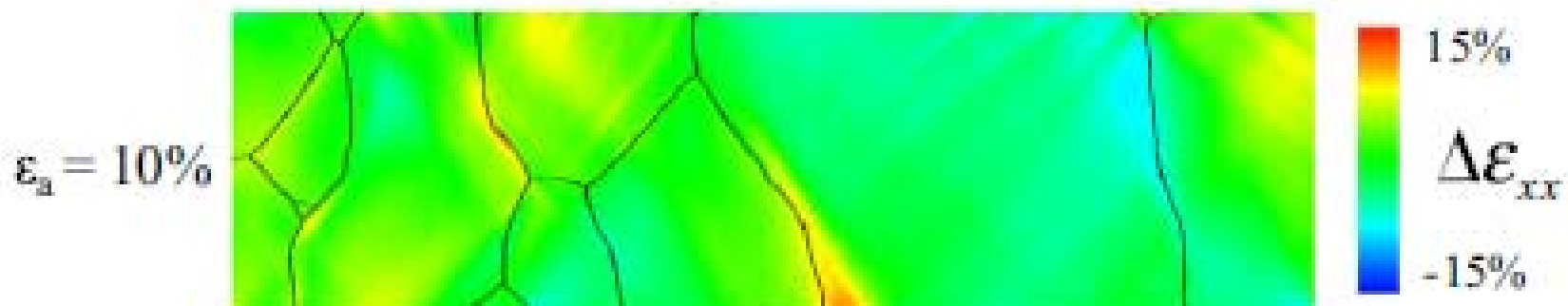


## The advantage of quantitative difference mapping:

$$\Delta \epsilon^{avg} = \sqrt{\frac{1}{N} \sum_{i=1}^N (\epsilon_i^{DIC} - \epsilon_i^{sim})^2}.$$

- A rational RMS goodness-of-fit metric to compare and discriminate effectiveness and locate deficiencies.

Deviation	Applied strain ( $\epsilon_a$ )				
	2%	4%	6%	8%	10%
$\Delta \epsilon_{xx}^{avg}$	0.0073	0.0102	0.0143	0.0215	0.0344
$\Delta \epsilon_{yy}^{avg}$	0.0059	0.0097	0.0116	0.0142	0.0180
$\Delta \epsilon_{xy}^{avg}$	0.0031	0.0071	0.0104	0.0136	0.0159



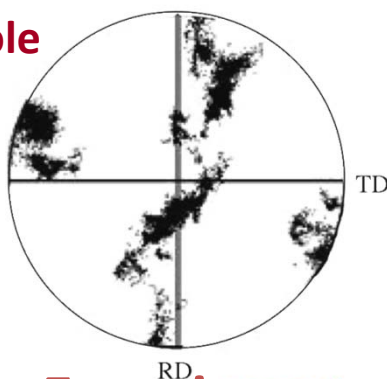
# Quantifying Rotation Change



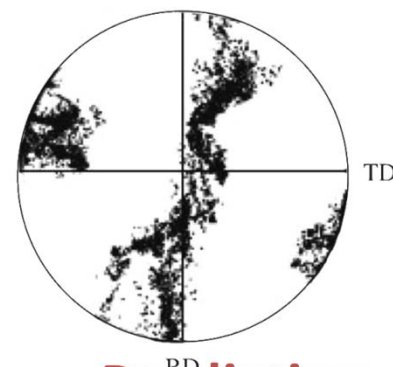
# Global vs Local Rotation Measurements

Global  
Texture  
Evolution

(100) X-ray Pole  
Figures



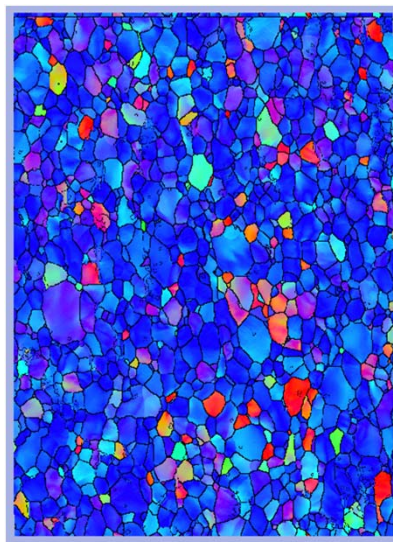
Experiment



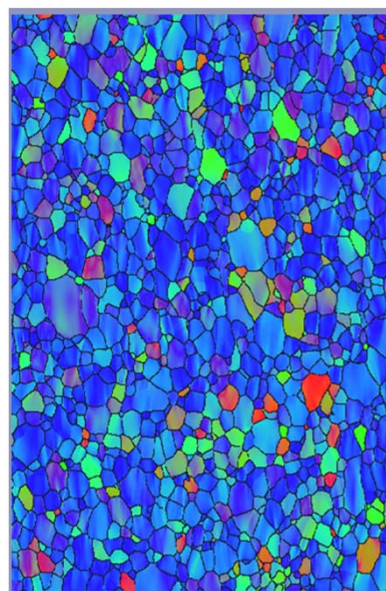
Prediction

S.R. Kalidindi, A. Bhattacharyya, and R.D. Doherty, *Proc. Roy. Soc. Lond. A* **460** (2004) 1-22.

Local Crystal  
Orientation

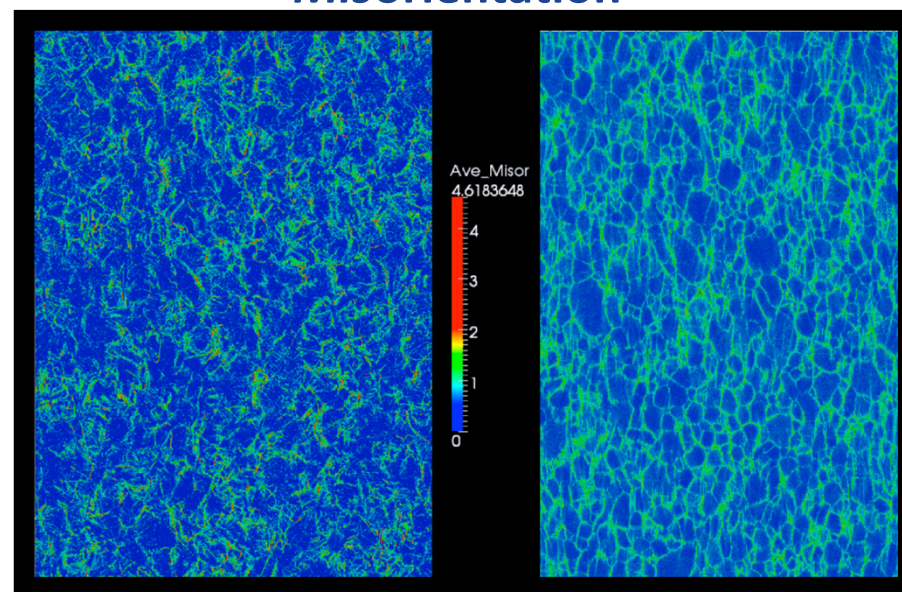


Experiment



Simulation

Misorientation

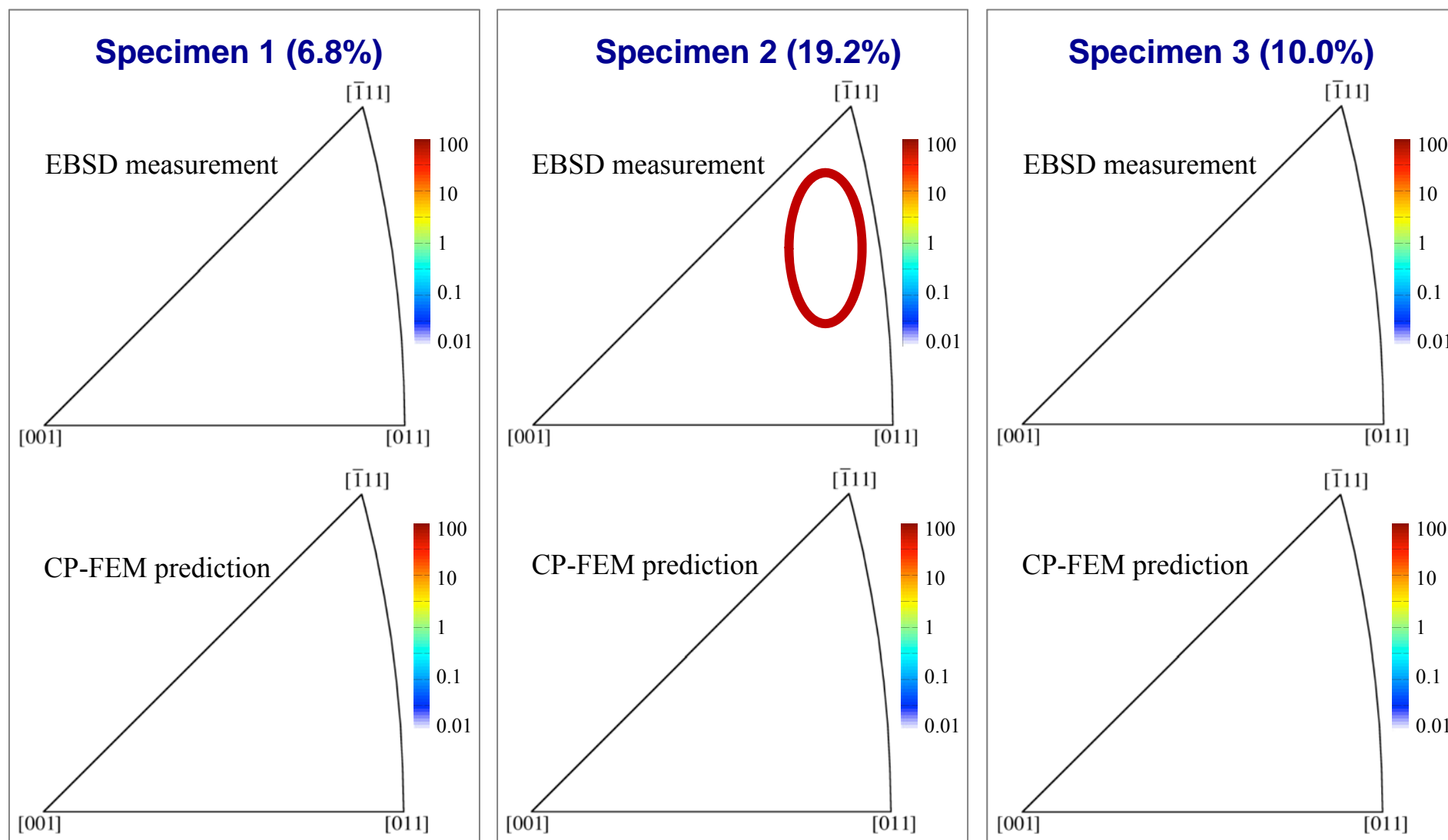


Experiment

Simulation

Courtesy of A.D. Rollett

# Texture Predictions



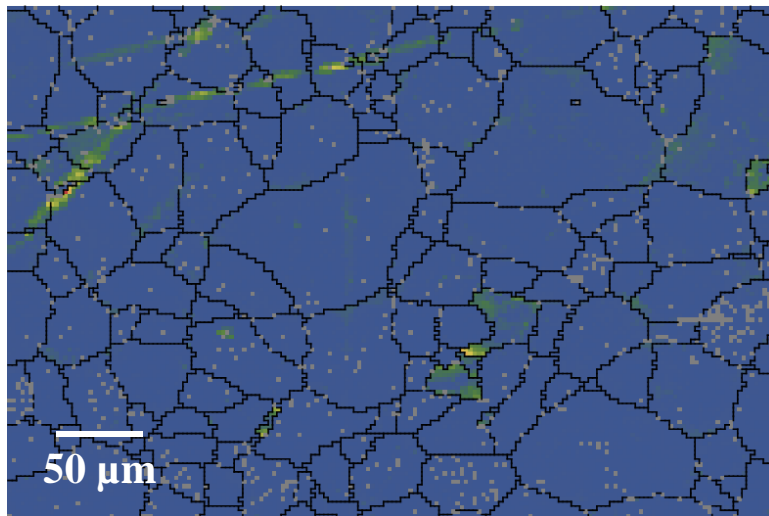
IPF contour plots indicate very good agreement between model and experiment.

# Reference Orientation Deviation Map (ROD)

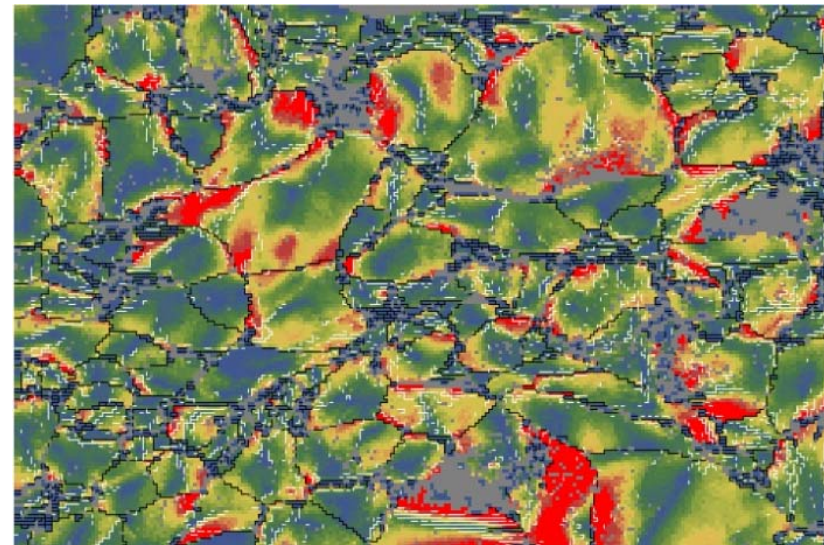
reference pixels to a specific orientation in a grain

Misorientation between all pixels in a grain and the grain's **current average orientation**

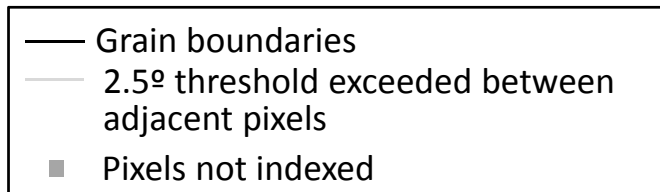
***Original Configuration***



***Deformed Configuration***  
~22% Strain (4<sup>th</sup> strain step)



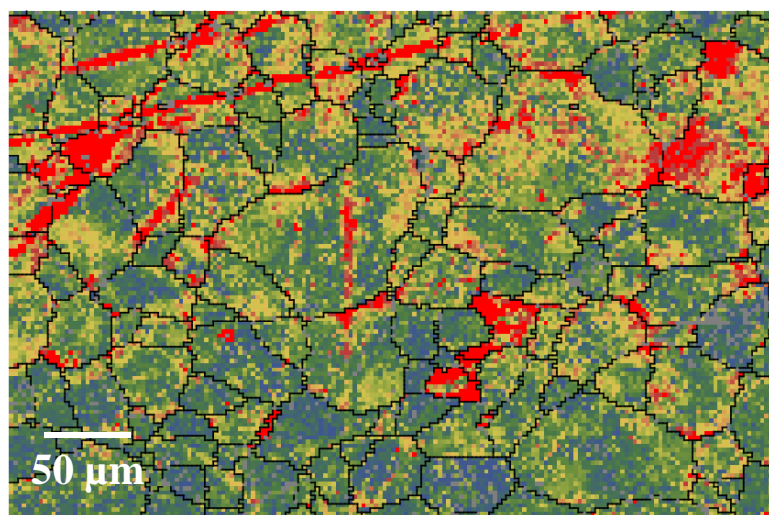
- Conventional approach –does not require a correlation between maps
- deformation history not captured



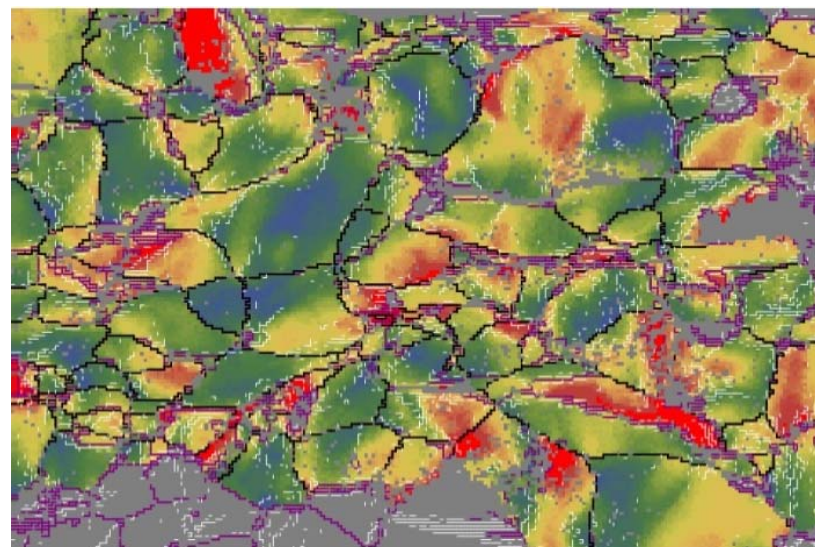


# A new type of ROD map, referencing to the average orientation of *originally defined grains*

*Original Configuration*



*Deformed Configuration*  
~22% Strain (4<sup>th</sup> strain step)



- Must track grain ID during deformation to allow orientation relative to original
- Requires ability to perform in-situ EBSD measurements during deformation
- Easily compared to a CPFEM model

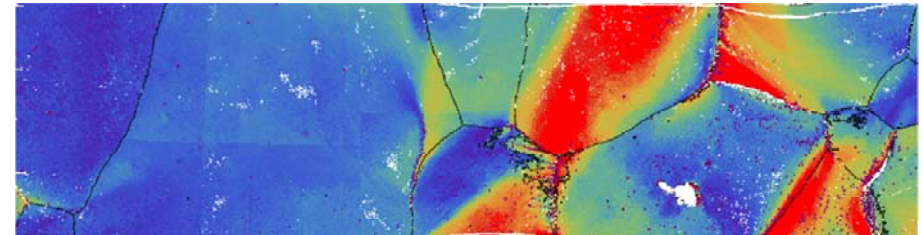
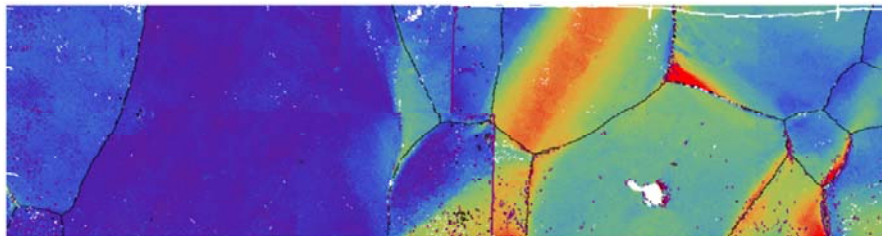
- Boundaries of originally defined grains
- Boundaries of new grains
- 2.5° threshold exceeded between adjacent pixels
- Pixels not correlated or indexed

# Comparison of pixel misorientation *relative to original average grain orientation*

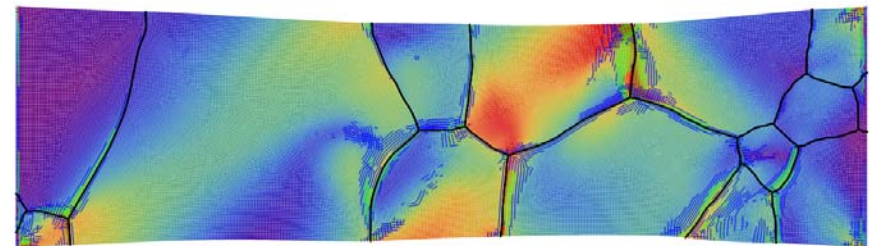
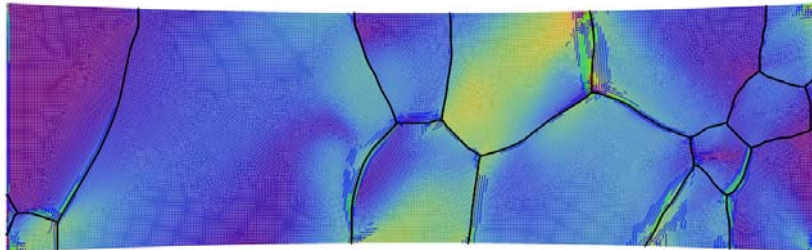
4.2% Strain

6.8% Strain

*Experiments (EBSD Maps)*



*CPFEM Simulations*



— 2.5°  
— 1.0°  
— 0.5°

Minimum misorientation angle  
relative to the undeformed grain orientation



# Grain boundary transmissivity

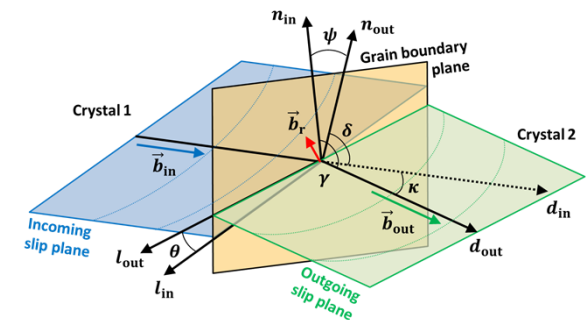
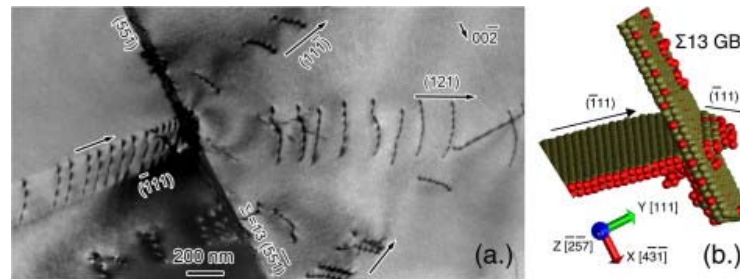
# There are many models for grain boundary slip transmissibility

## How does slip transfer across GBs? Dependence on GB type?

### ○ Explicit MD examination

- Sangid-Ezaz-Sehitoglu-Robertson, Acta Mater. 2011

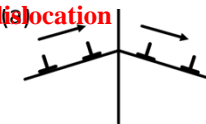
(3 boundaries)



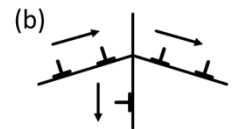
### ○ Geometrical criteria:

- ***N factor*** from Livingston-Chalmers, Acta Metall. (1957)
- ***SWC factor*** from Shen-Wagoner-Clark, Acta Metall. (1988)
- ***LRB factor*** from Lee-Robertson-Birnbaum, Scripta Metall. (1989)
- ***m' factor*** from Luster -Morris, Metal. Mat. Trans. A (1995)
- ***The residual Burgers vector***, Metal. Trans. (1970)
- ***The  $\lambda$  function*** from Werner and Prantl, Acta Metall. (1990)

GB  
transparent to  
dislocation

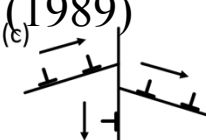


GB

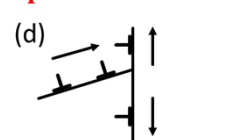


GB

Impenetrable GB



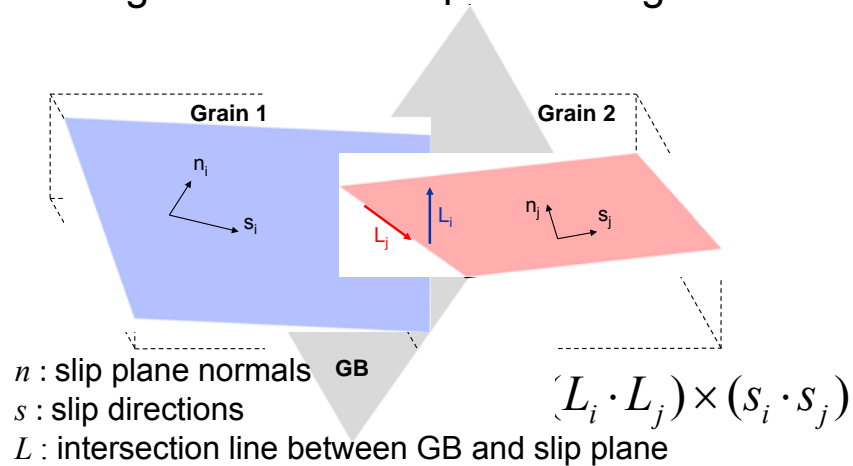
GB



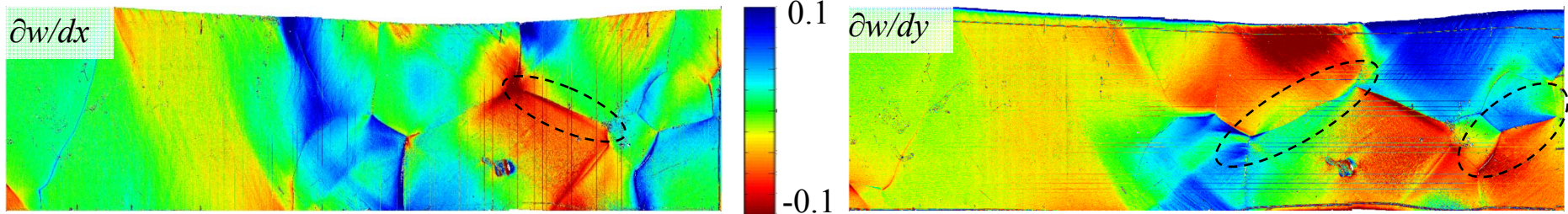
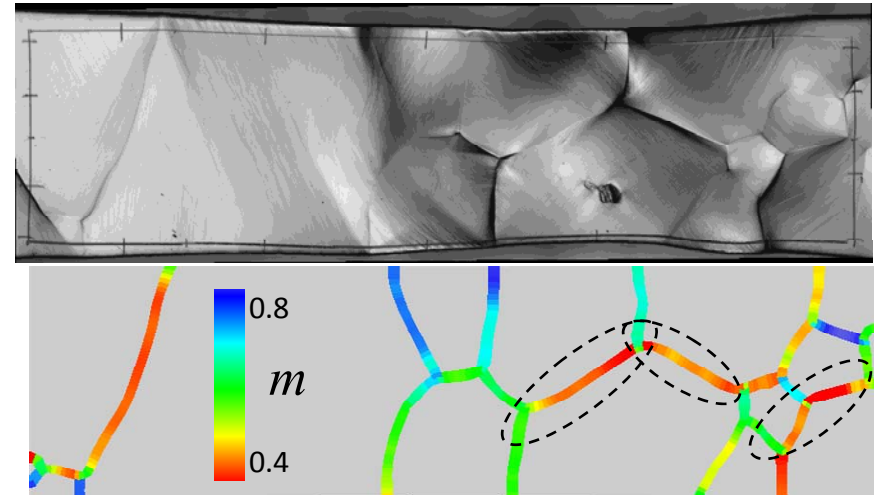
GB

# Surface profile for interpreting grain boundary transmissivity

Grain boundary slip transmissivity provides an estimate for how resistant a grain boundary is to allowing dislocations to pass through.



Deformed surface (10%)



Profilometry Measurements

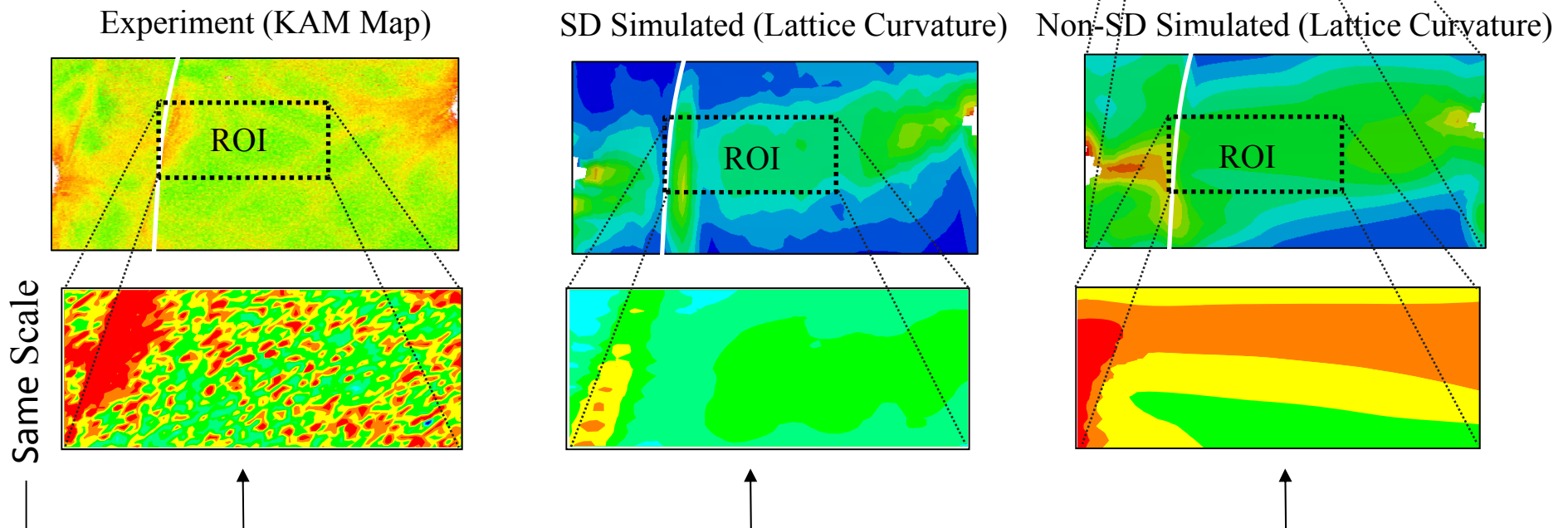
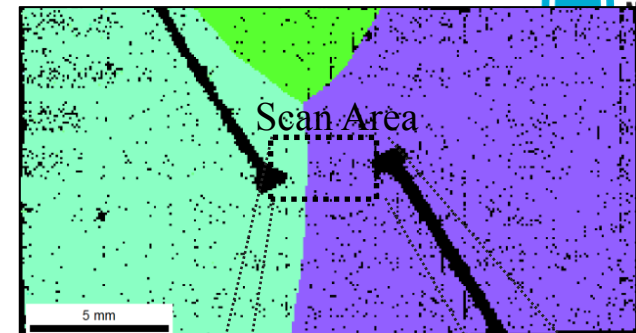
1 mm

Our transmissivity-based model for boundary – dislocation interactions provides qualitative agreement with measurements of slip band formation and surface profilometry.

Fullwood/Wagoner/Homer Collaboration:  
Quantitatively validate transmissability laws at  
individual boundaries

## Ta Bicrystal – Lattice Curvature

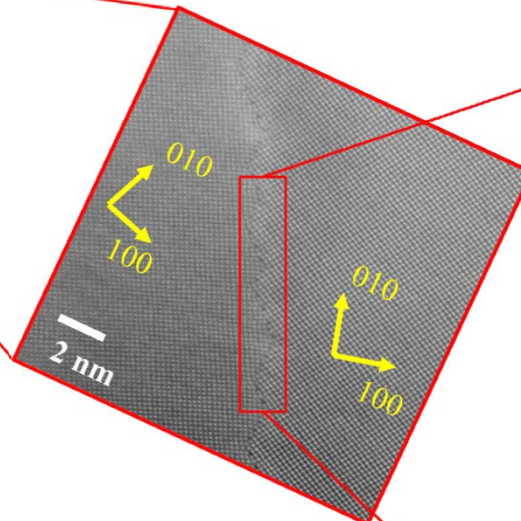
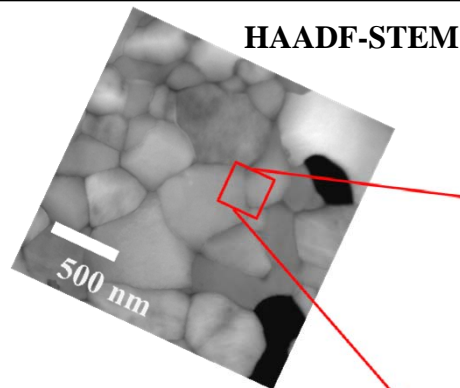
\* 0.1 mm Plastic Extension in Mini Instron



ROI Lattice Curvature (rad/mm)	Experiment	SD Model	Non-SD
Average	1.20	0.91	1.98
Maximum	2.15	1.33	2.56

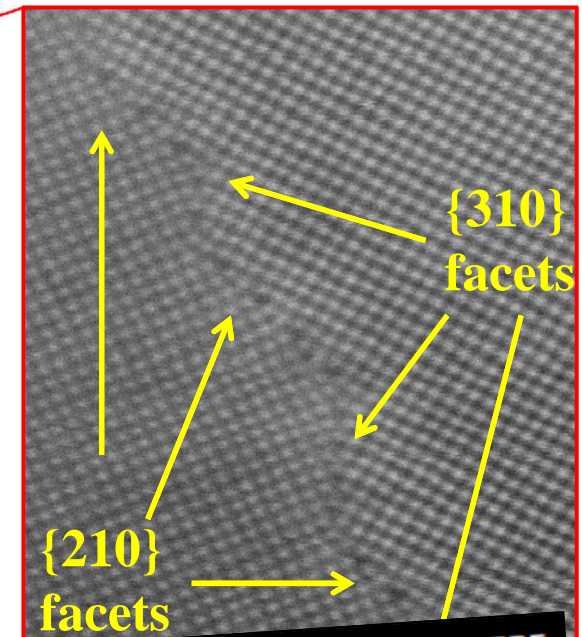


# Grain boundaries are not always as simple as ‘just’ 5 degrees of freedom!!!



HAADF-STEM  $\Sigma 5$   
<001> GB in Fe

Inclination from {310}:  $26.3^\circ$



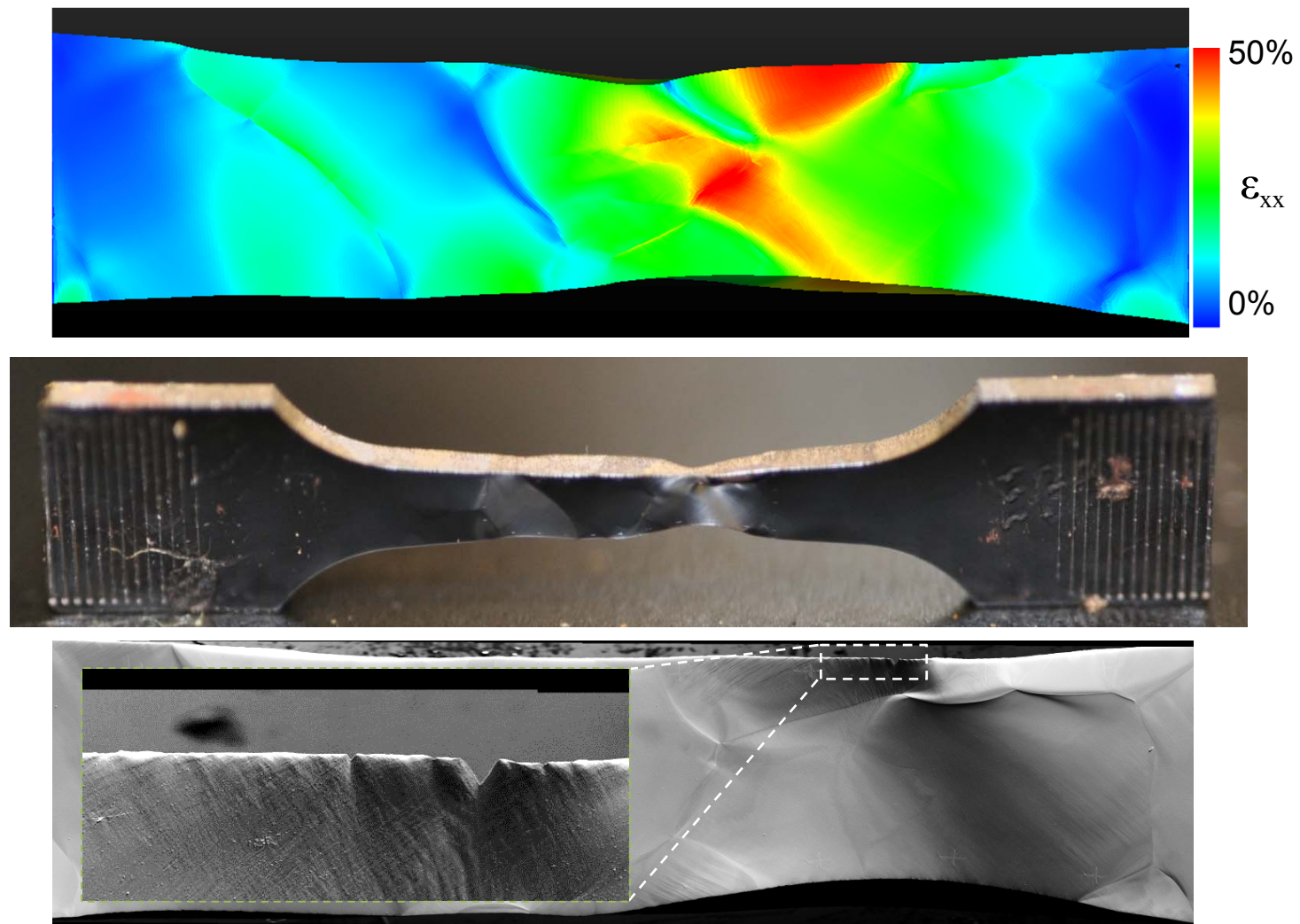
## Observations

- Thermal faceting into “hill-and-valley” morphology
- Boundary is faceted on {210} and {310} inclinations

ABSTRACT	SYMPOSIUM	SESSION	WHEN	WHERE
<p><b>Experimental Observations and Modeling of Interfacial Defects at an Asymmetric <math>\Sigma=5</math> Grain Boundary in Fe</b></p> <p>Douglas L. Medlin<sup>1</sup>; K. Hattar<sup>1</sup>; J. A. Zimmerman<sup>1</sup>; F. Abdeljawad<sup>1</sup>; S. M. Foiles<sup>1</sup>; <sup>1</sup>Sandia National Labs</p>	<p>Interface-driven Phenomena in Solids: Thermodynamics, Kinetics and Chemistry</p>	<p>Structure-Property Relations</p>	<p>Tuesday 9:30 AM - 9:50 AM</p>	<p>Music City Center 108</p>

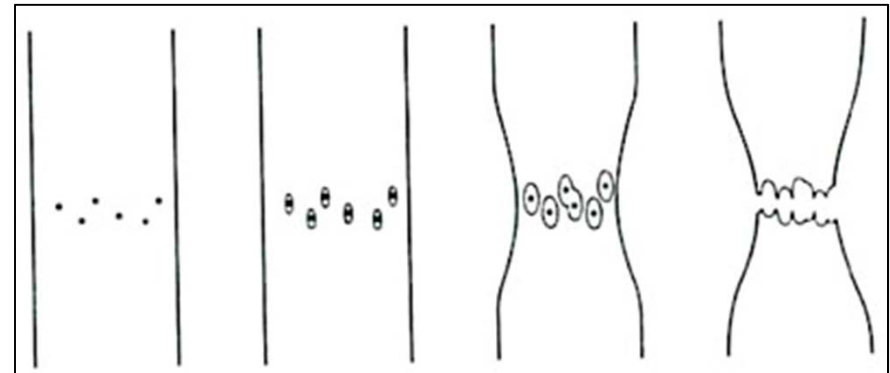
# **Void Behavior and Damage**

The crystal plasticity model predicts localized hot spots in strain at the same location where cracking is observed...

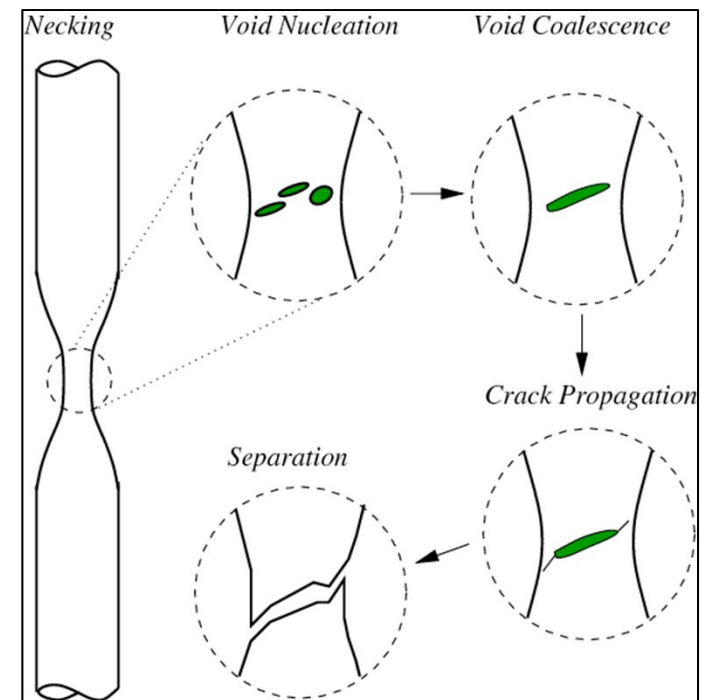


# Background: Ductile Fracture

- Initiation of voids through decohesion at second-phase particles or inclusions
- Voids continue to grow in response to high stresses
- Eventual coalescence of voids, leading to failure

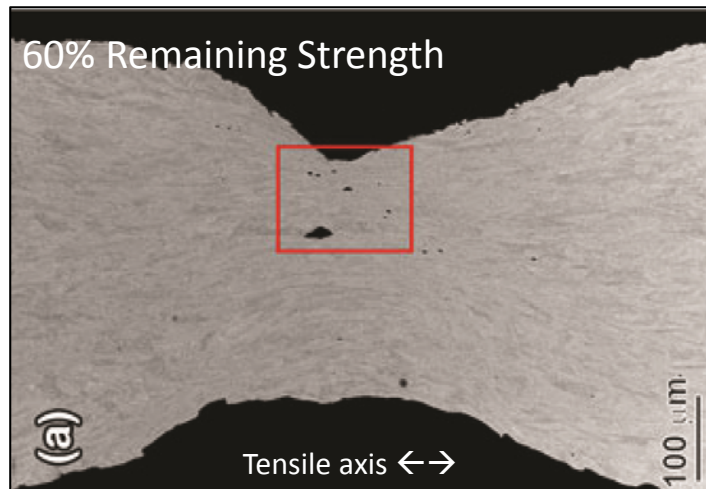


How do voids initiate in pure metals?

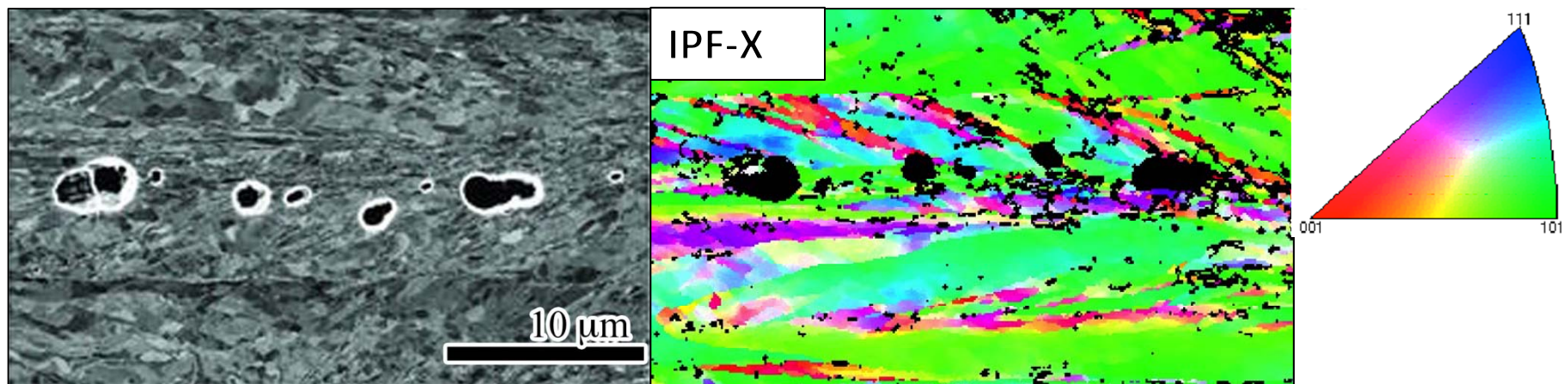




# Void Formation in 99.9%Ta



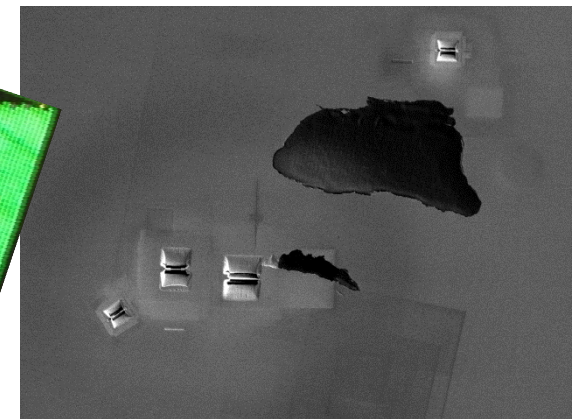
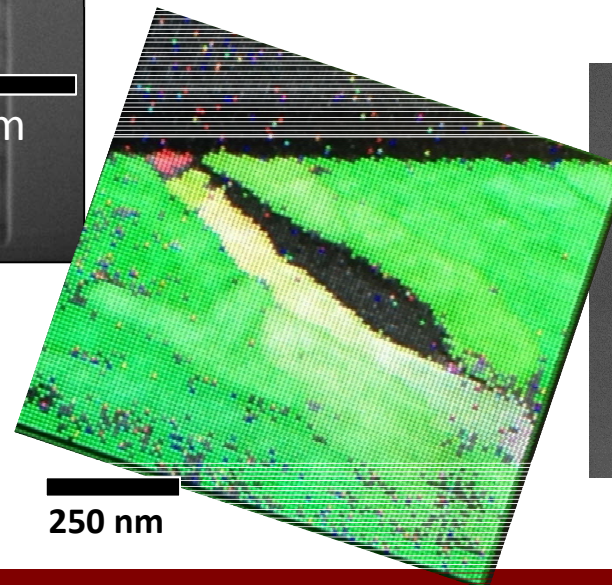
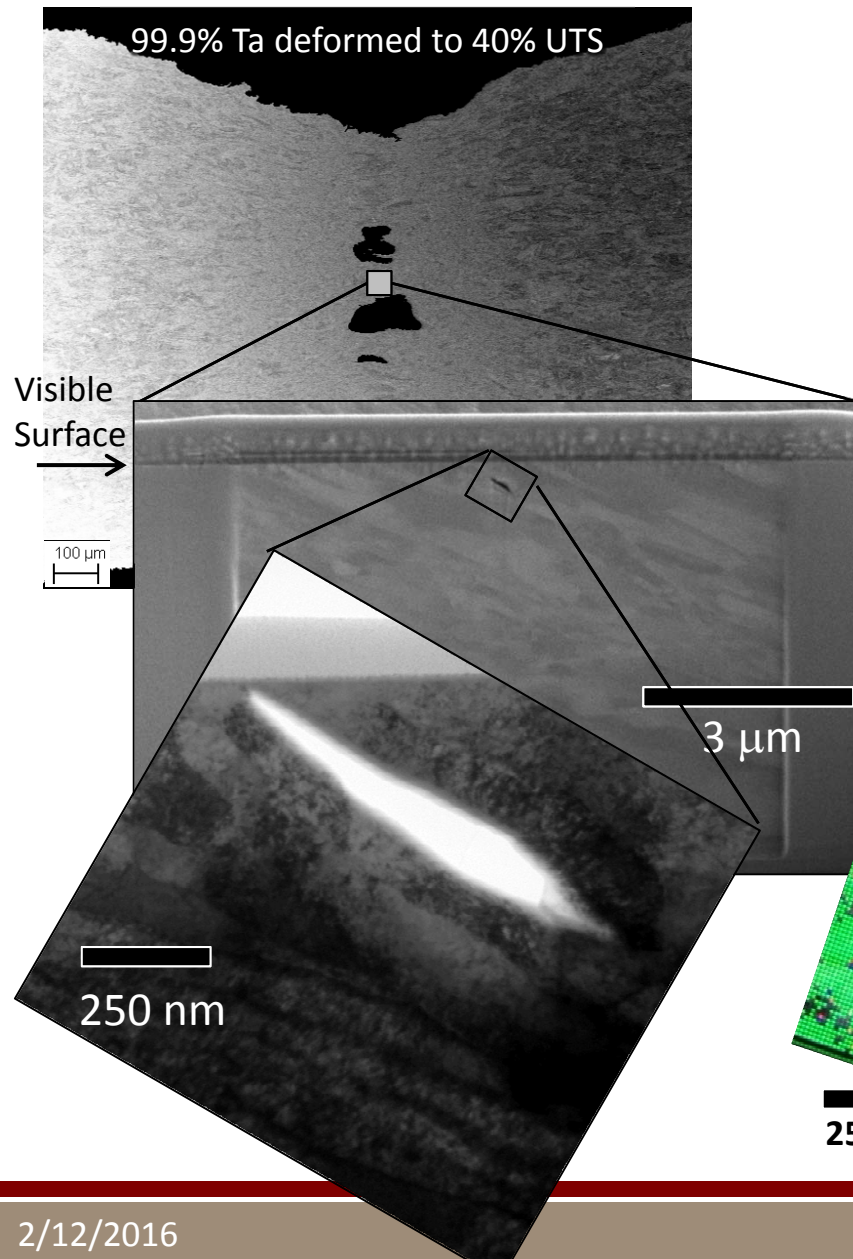
- Arrays of voids aligned along tensile axis
- EBSD shows elongated, inclined  $[001]$  subgrains associated with each void
- Alternating regions of  $[122]$  indicates high angle GBs



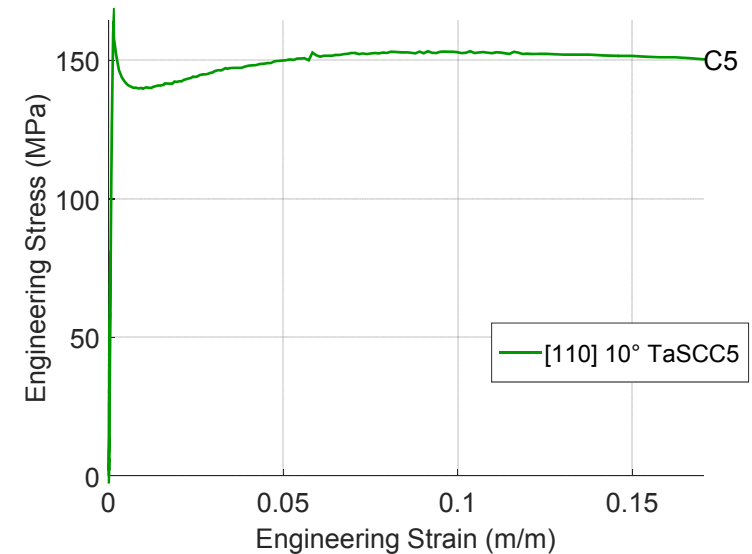
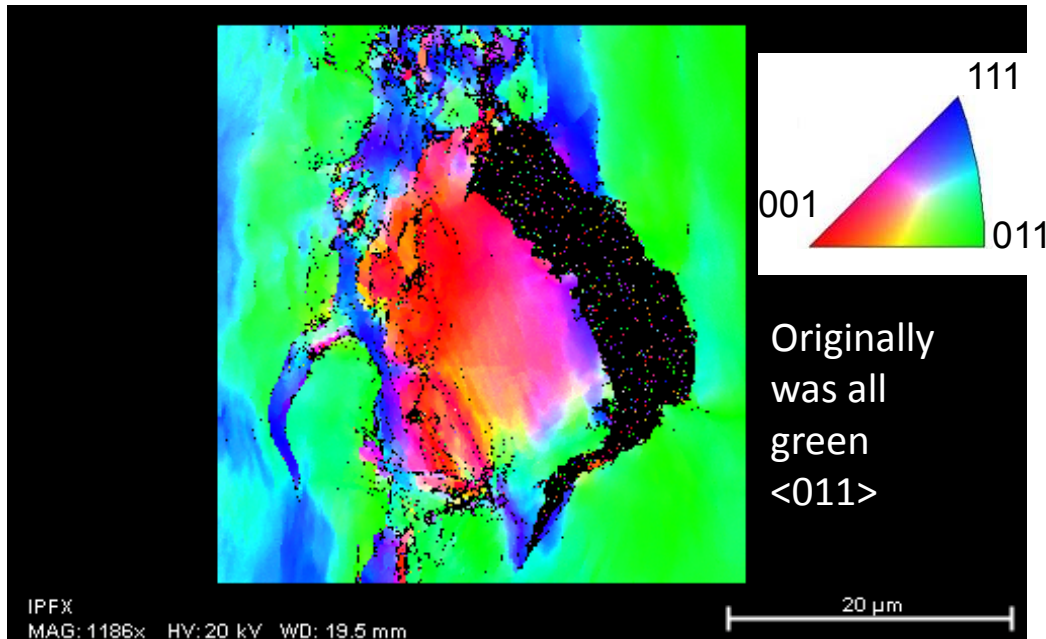
Ta failure is void-driven, with deformation-induced microstructural changes and stress state controlling the initiation/growth of voids

# Nanoscale Analysis of Void Initiation

- Focused Ion Beam (FIB) used to locate subsurface, deformation-induced voids in interrupted tensile bar.
- Preliminary TEM shows void shape aligned with angle of sub-boundaries
- Transmission Kikuchi Diffraction (TKD) to determine crystallographic orientation near void.
- Orientations are consistent with EBSD analysis showing void nucleation along high angle misorientation boundaries



# Probing relationships between void formation and crystallographic orientation



- Investigated a void formed during tensile testing of a Ta single crystal <011>. Imaging at the specimen midplane.
- Crystallographic rotations near a void in single crystal specimens improve our understanding of void formation in polycrystals.
- Void formation is associated with developing <001> and <111> crystallographic orientations.
- We are investigating whether substructure leads to these crystallographic rotations which leads to voids or whether the formation of voids causes the crystallographic rotations.



- Grain-scale validation of crystal-plasticity models is still largely qualitative
- Both distortion and rotation can be mapped relative to the original undeformed configuration
- With an ability to map back to the original undeformed configuration, it is possible to begin to assess quantitative difference metrics.
- These new statistical metrics may help identify and address gaps in CP-FEM theory:
  - Grain boundary slip transmissibility
  - Void nucleation and growth