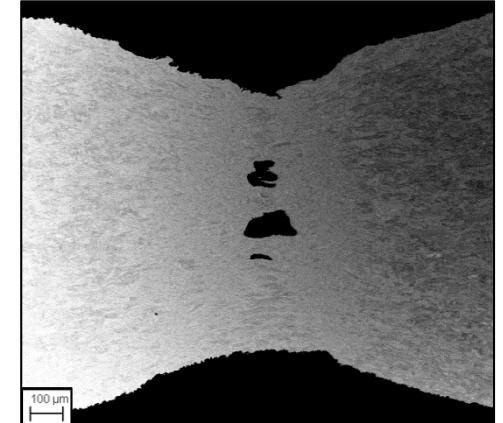
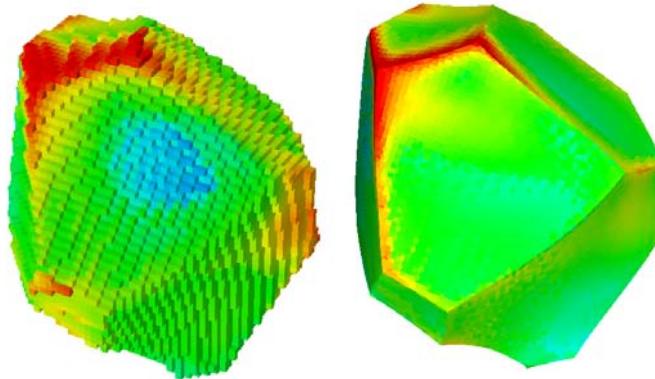
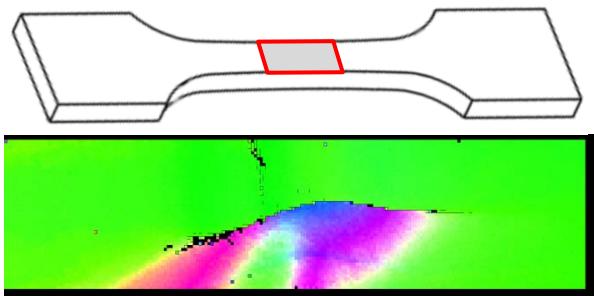


*Exceptional service in the national interest*



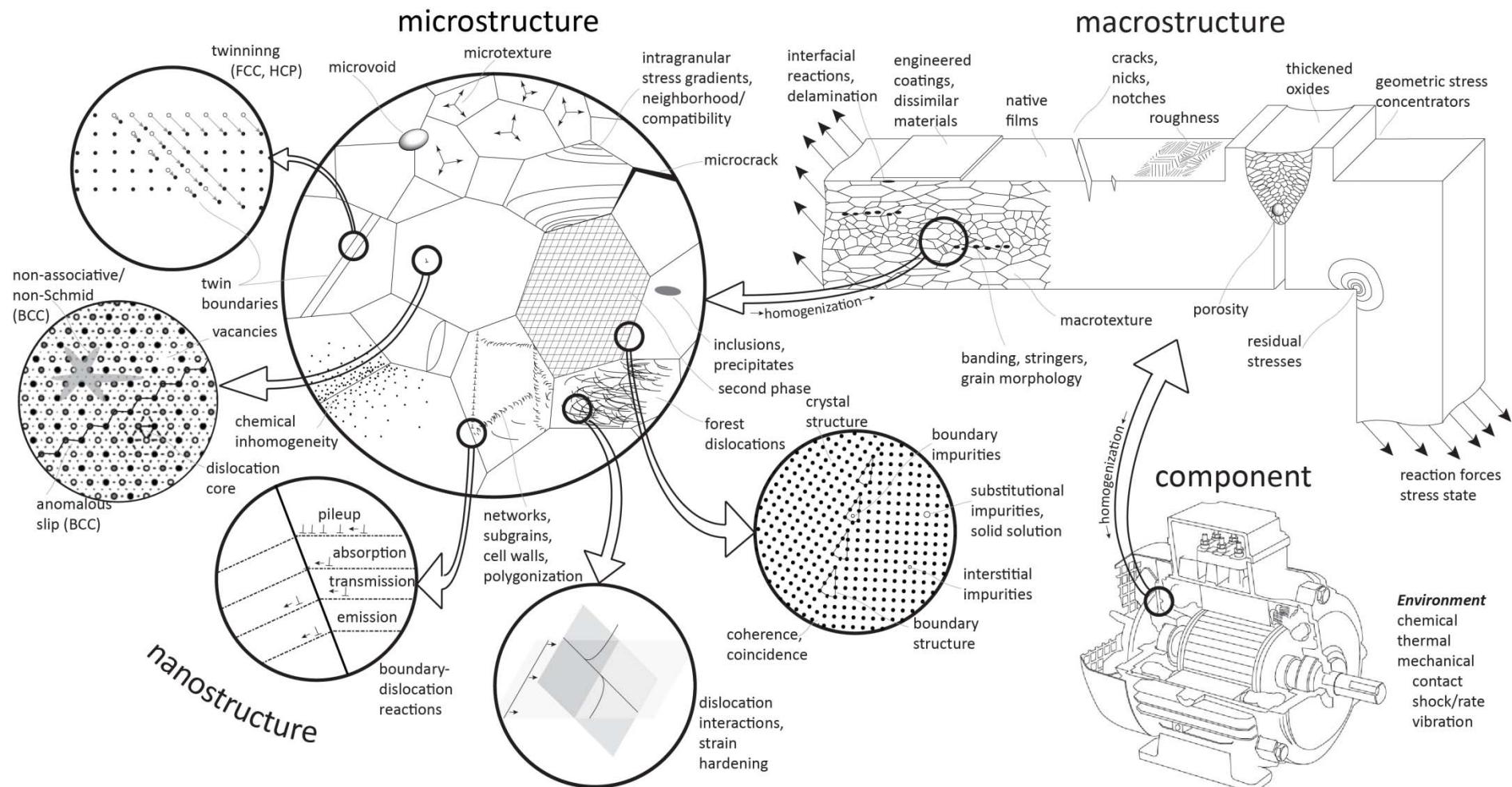
## Quantifying Grain-Scale Deformation for Direct Comparison to Crystal Plasticity Predictions

**Brad L. Boyce; Hojun Lim; Jay D. Carroll; Thomas E. Buchheit; Corbett C. Battaile**  
Sandia National Laboratories



Sandia National Laboratories is a multi-program laboratory managed and operated by Sandia Corporation, a wholly owned subsidiary of Lockheed Martin Corporation, for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000. Tracking # 397226

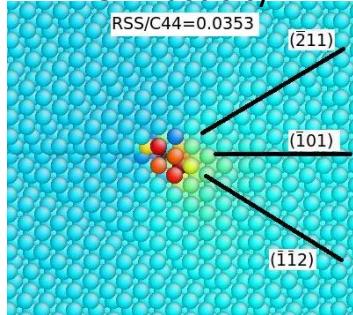
# Introduction: Material and length-scale roadmap for deformation and failure of structural metals



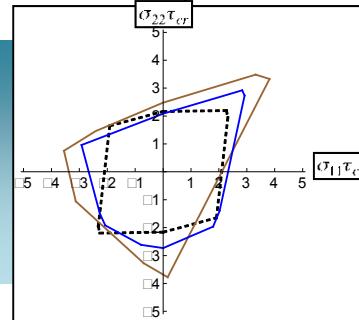
# Developing an experimentally validated model for grain-scale deformation (crystal plasticity)



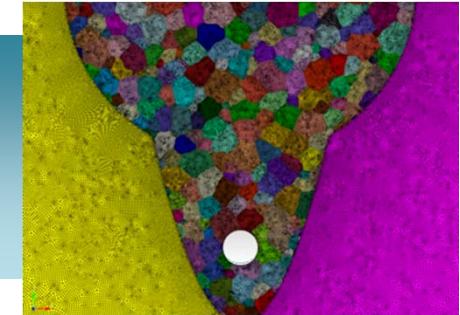
Atomic Mechanisms  
Of Plasticity



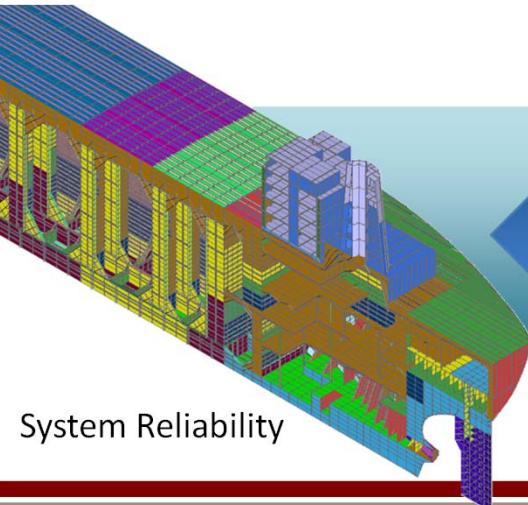
Single-Crystal  
Plasticity Models



Polycrystalline  
Deformation Response

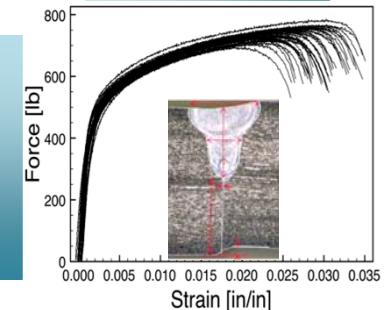
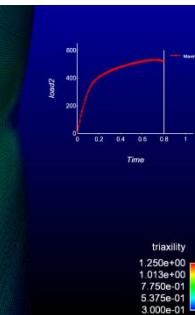


Goal: Provide a science-based foundation for design, analysis, and qualification capabilities that links mesoscopic/microscopic inhomogeneity to property variability.



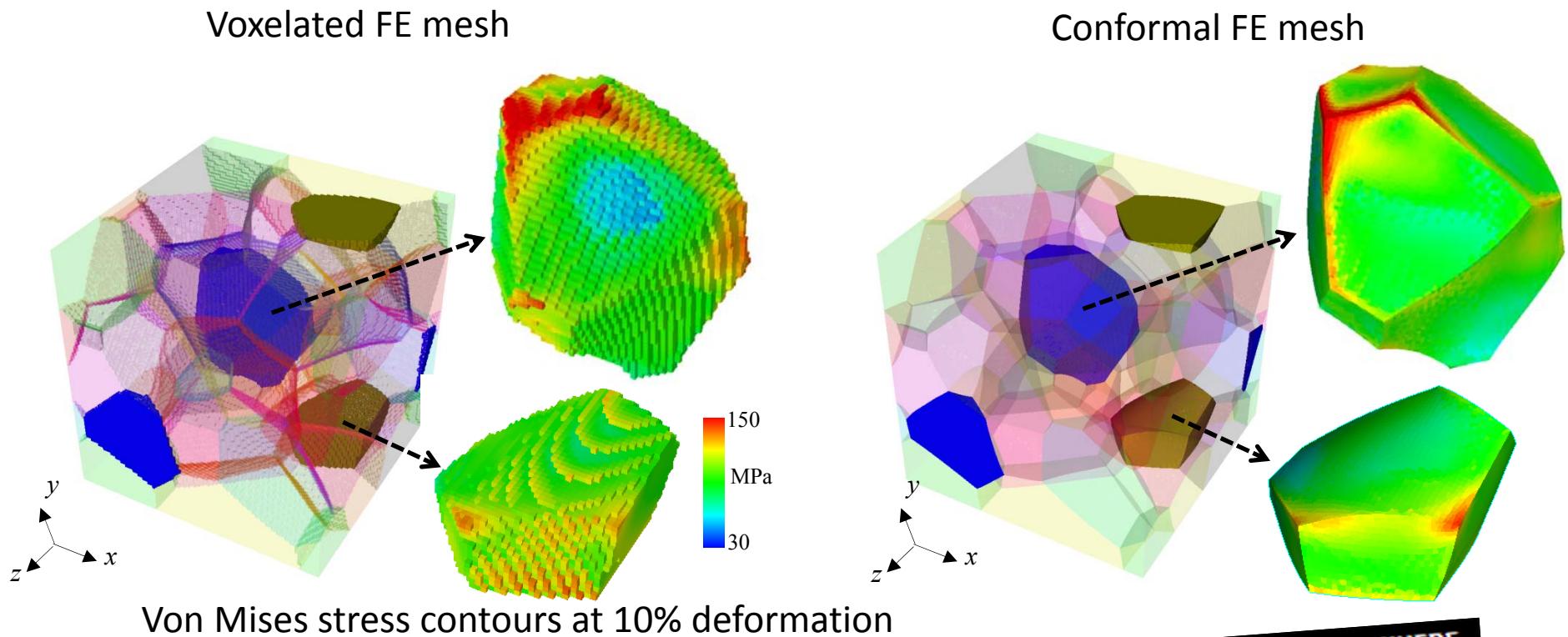
System Reliability

Reduced Order Modeling  
For Efficient Stochastic Computations



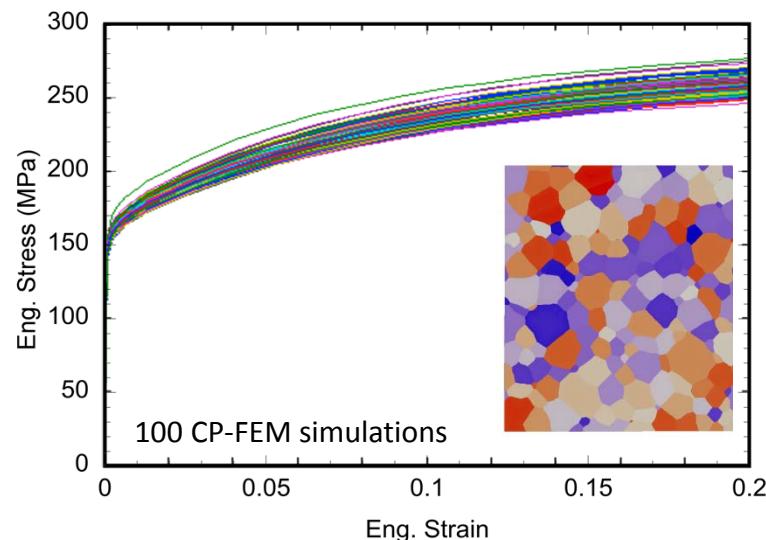
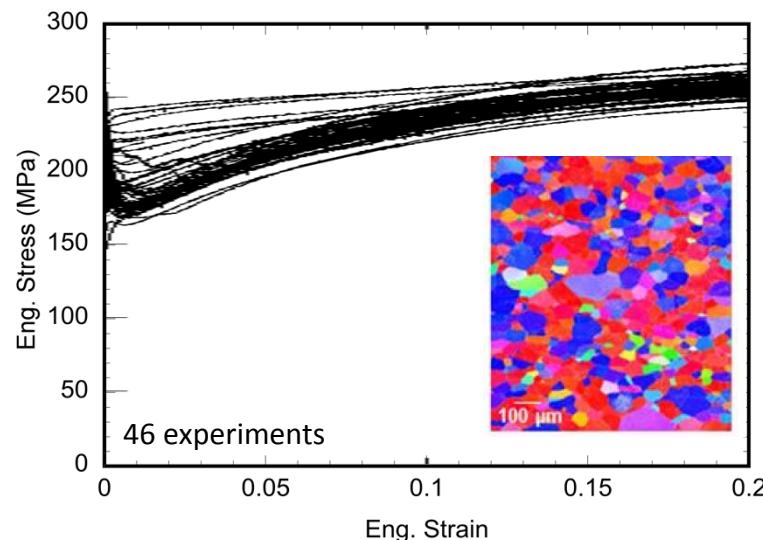
Stochastic Outcomes  
From Different Configurations

# Recent Sandia advances in Polycrystal Plasticity: Phase-Field generated microstructure & smooth meshing

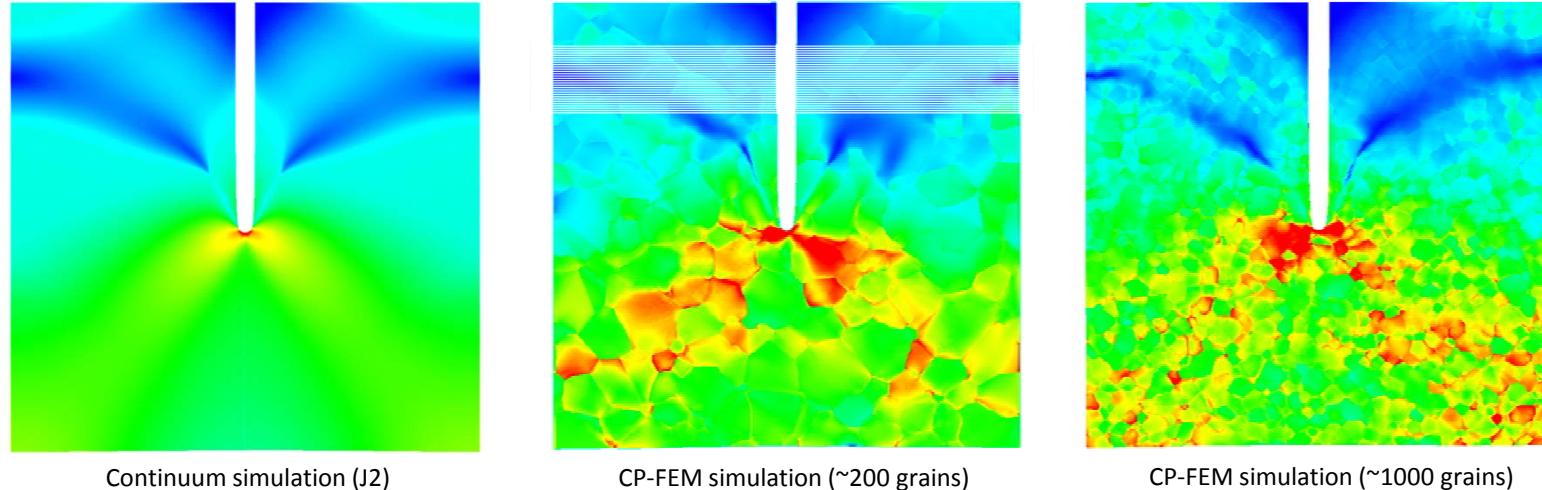


ABSTRACT	SYMPOSIUM	SESSION	WHEN	WHERE
<p><u><a href="#">Developing Physically-based Three Dimensional Microstructures: Bridging Phase Field and Crystal Plasticity Models</a></u></p> <p>Hojun Lim<sup>1</sup>; Fadi Abdeljawad<sup>1</sup>; Steven J. Owen<sup>1</sup>; Byron W. Hanks<sup>1</sup>; Corbett C. Battaile<sup>1</sup>; <sup>1</sup>Sandia National Laboratories</p>	<p>Computational Materials Discovery and Optimization: From 2D to Bulk Materials</p>	<p>Microstructure and Mechanical Properties</p>	<p>Thursday 11:10 AM - 11:30 AM</p>	<p>Music City Center 207D</p>

# Predicting Stochastic Behavior of Polycrystals

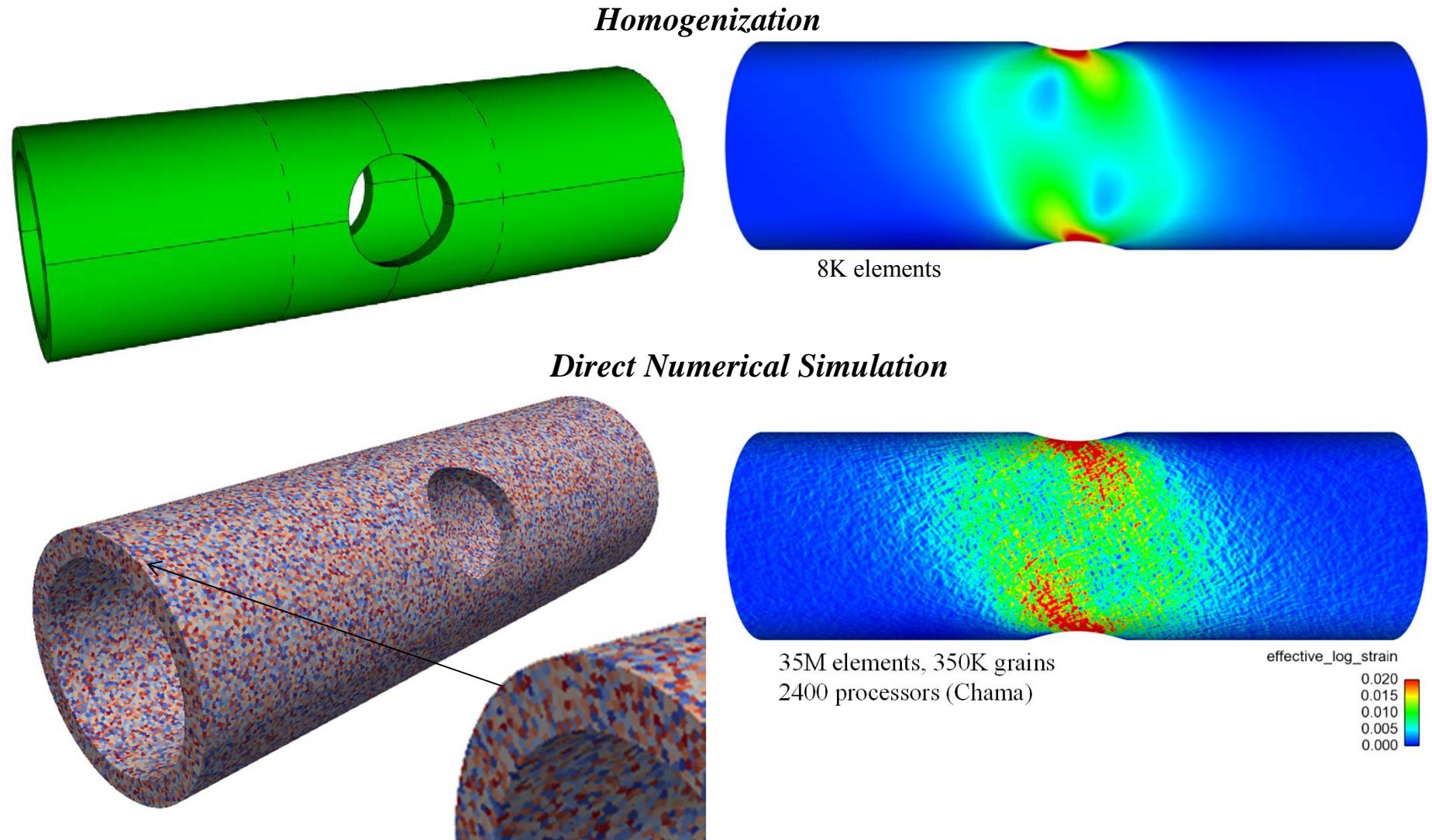


Grain-scale variability in macroscale response

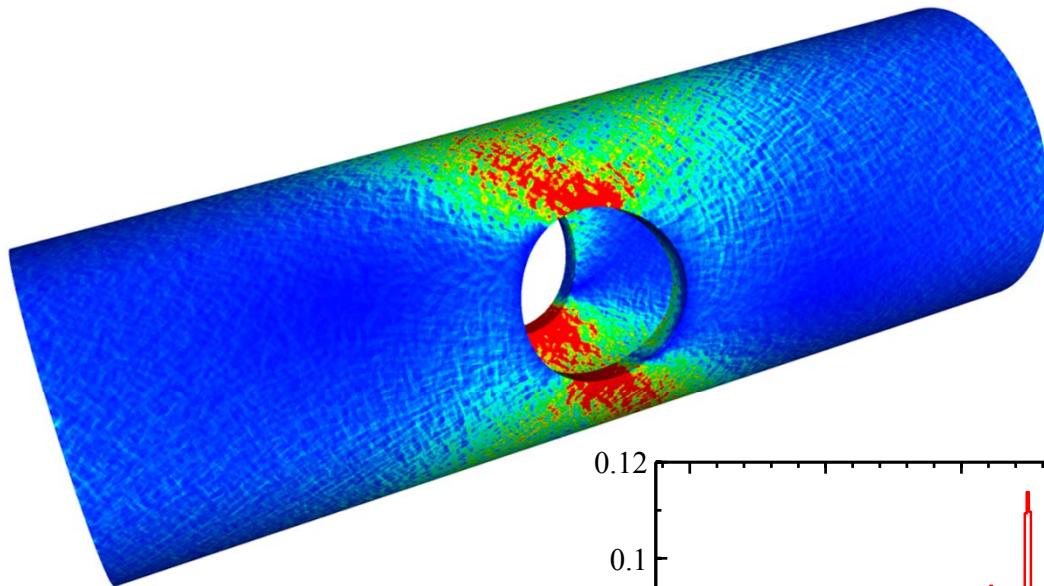


VM stress fields after 3% deformation

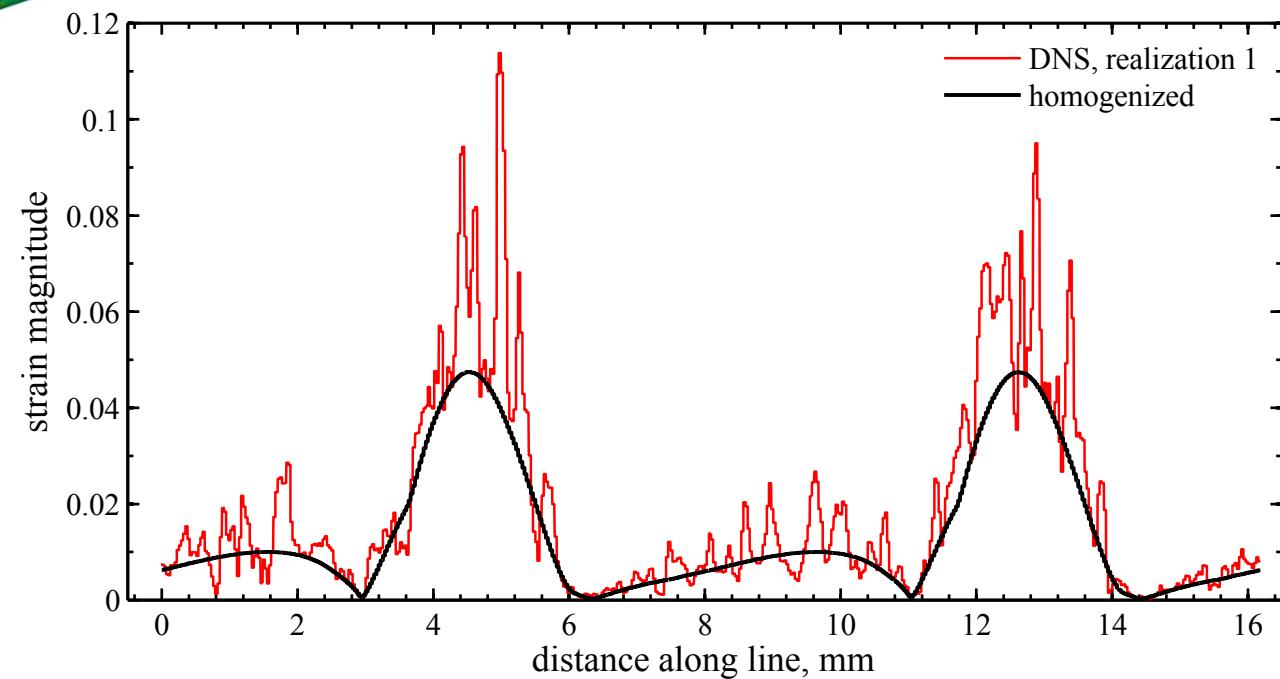
# On the horizon: System-scale simulations with explicit microstructural representations.



# On the horizon: System-scale simulations with explicit microstructural representations.



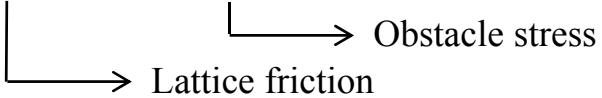
effective\_log\_strain  
0.020  
0.015  
0.010  
0.005  
0.000



## Polycrystal plasticity employs finite element method to discretize crystallographic slip at the crystallographic-level.

Slip rate:  $\dot{\gamma}^\alpha = \dot{\gamma}_0^\alpha \left( \frac{\tau^\alpha}{g^\alpha} \right)^{1/m}$  (Hutchinson, 1976) 24  $<111>\{110\}$  slip systems

Slip resistance:  $g^\alpha = \max(\tau_{\text{cr}}^\alpha - \tau_{\text{ns}}^\alpha, 0) + \tau_{\text{obs}}^\alpha$  (Weinberger, 2012)


  
 ↗ Obstacle stress  
 ↗ Lattice friction

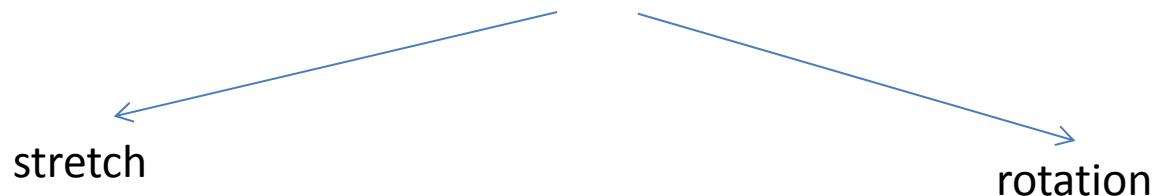
Obstacle stress:  $\tau_{\text{obs}}^\alpha = \alpha \mu b \sqrt{\sum_{\beta=1}^{NS} \rho^\beta}$  (Taylor, 1934)

$$\rho^\alpha = \left( \kappa_1 \sqrt{\sum_{\beta=1}^{NS} \rho^\beta} - \kappa_2 \rho^\alpha \right) \cdot |\gamma^\alpha| \quad (\text{Kocks, 1976})$$

# Options for Experimental Validation at Grain-Scale



Deformation gradient can be decomposed into a product of stretch and rotation

$$\mathbf{F} = \mathbf{U}\mathbf{R}$$


The diagram illustrates the decomposition of the deformation gradient  $\mathbf{F}$  into stretch and rotation components. A horizontal line segment is labeled  $\mathbf{F} = \mathbf{U}\mathbf{R}$  at its top center. A blue arrow points to the left from the center of the segment, labeled 'stretch'. Another blue arrow points to the right from the center, labeled 'rotation'.

Analogously, experimentally we measure shape change and rotation

- Digital Image Correlation
- Surface Profilometry
- Synchrotron X-ray microdiffraction

- Electron Backscatter Diffraction
- Precession Electron Diffraction
- Synchrotron X-ray microdiffraction

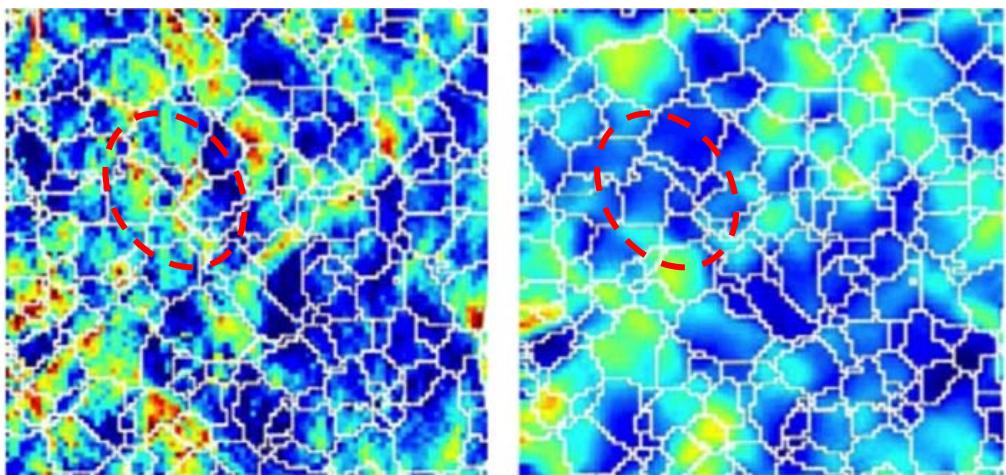
# Quantifying Shape Change

# Previous Work on Sim.- Exp. Comparison



“Quantitative comparisons between the model and experiments”

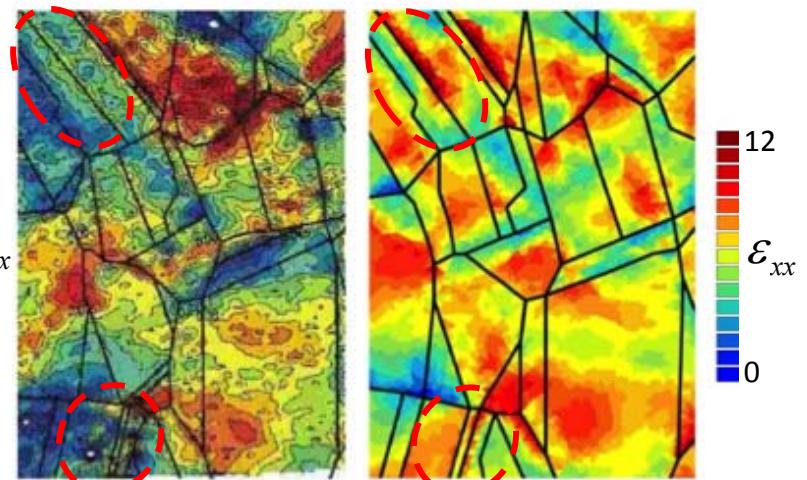
Zr 702 polycrystal (Heripre et al, 2007)  
(2.5 % strain)



Experiment

Simulation

OFHC Cu polycrystal (Musienko et al, 2007)  
(5 % strain)

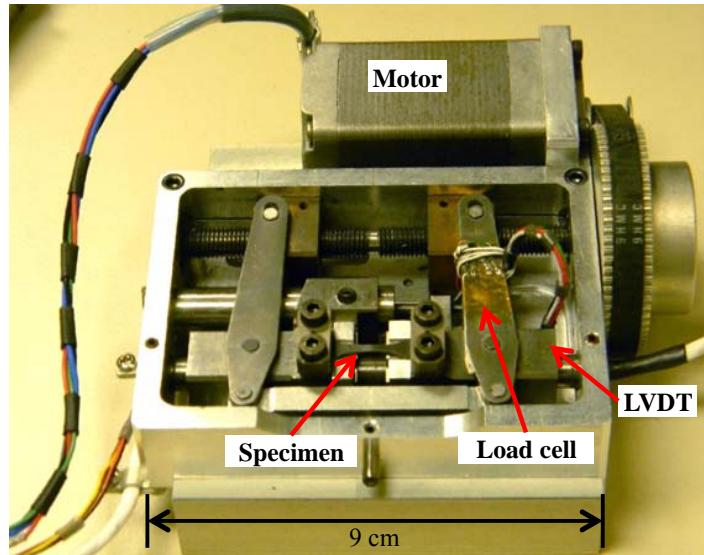


Experiment

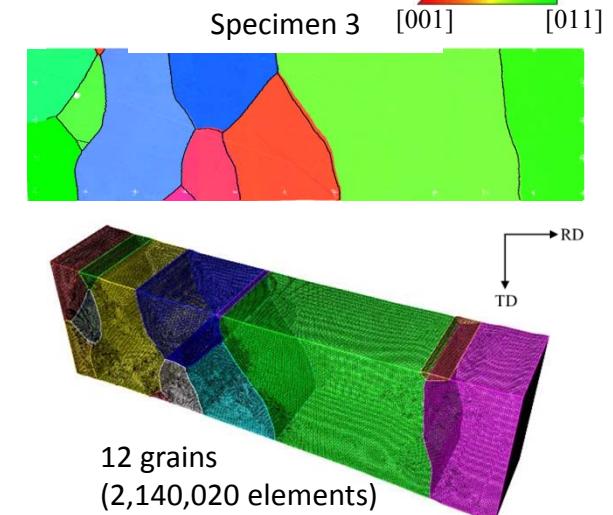
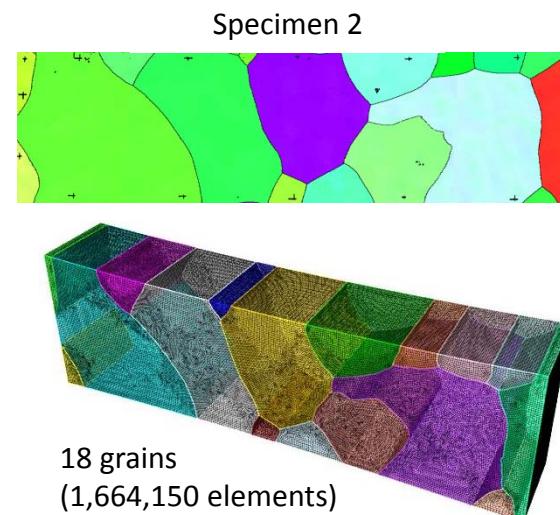
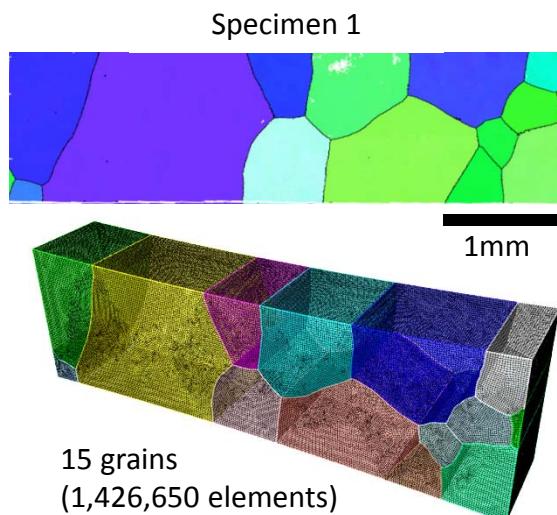
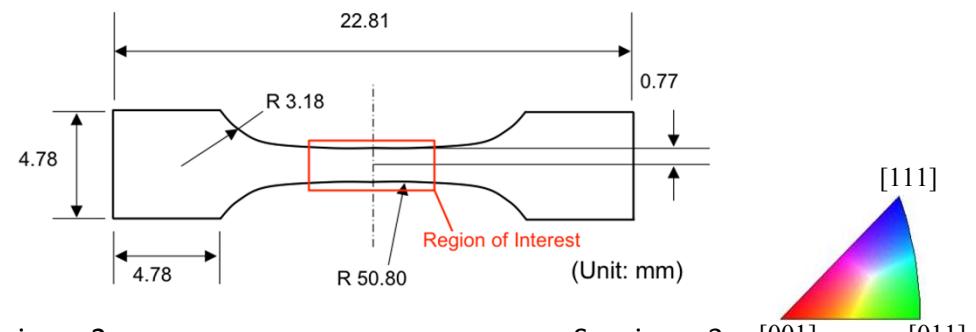
Simulation

Limited success has been achieved in modeling polycrystal deformation behavior due to unknown subsurface grains

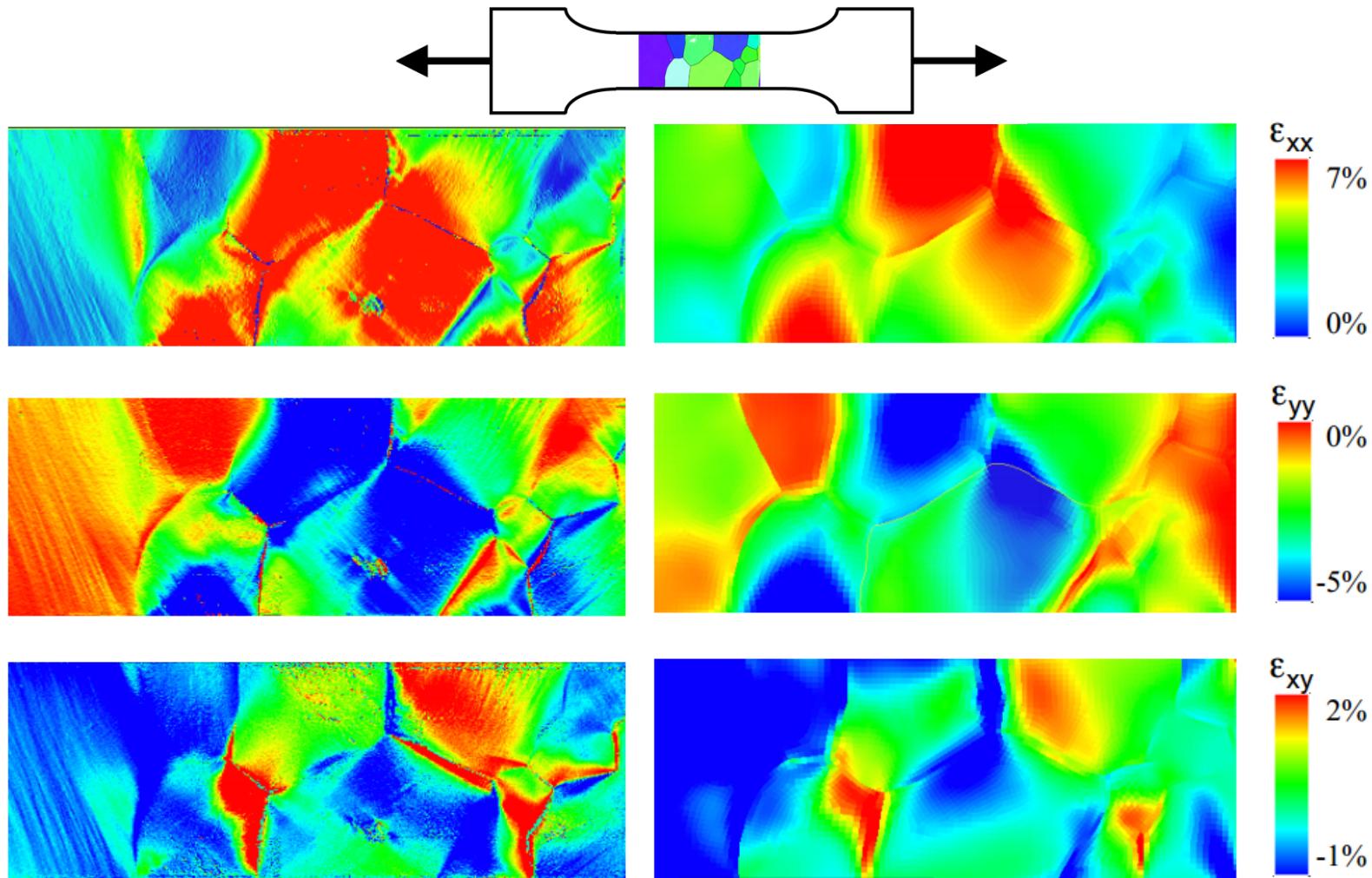
# Experimental Setup



- Tantalum oligocrystals with mostly columnar 2D grain structure eliminate unknown subsurface grain morphology.
- *In-situ* load frame developed at Sandia
- HR-DIC (surface strain fields) and EBSD (crystal orientations) measurements at load inside SEM



# Side-by-side qualitative comparison

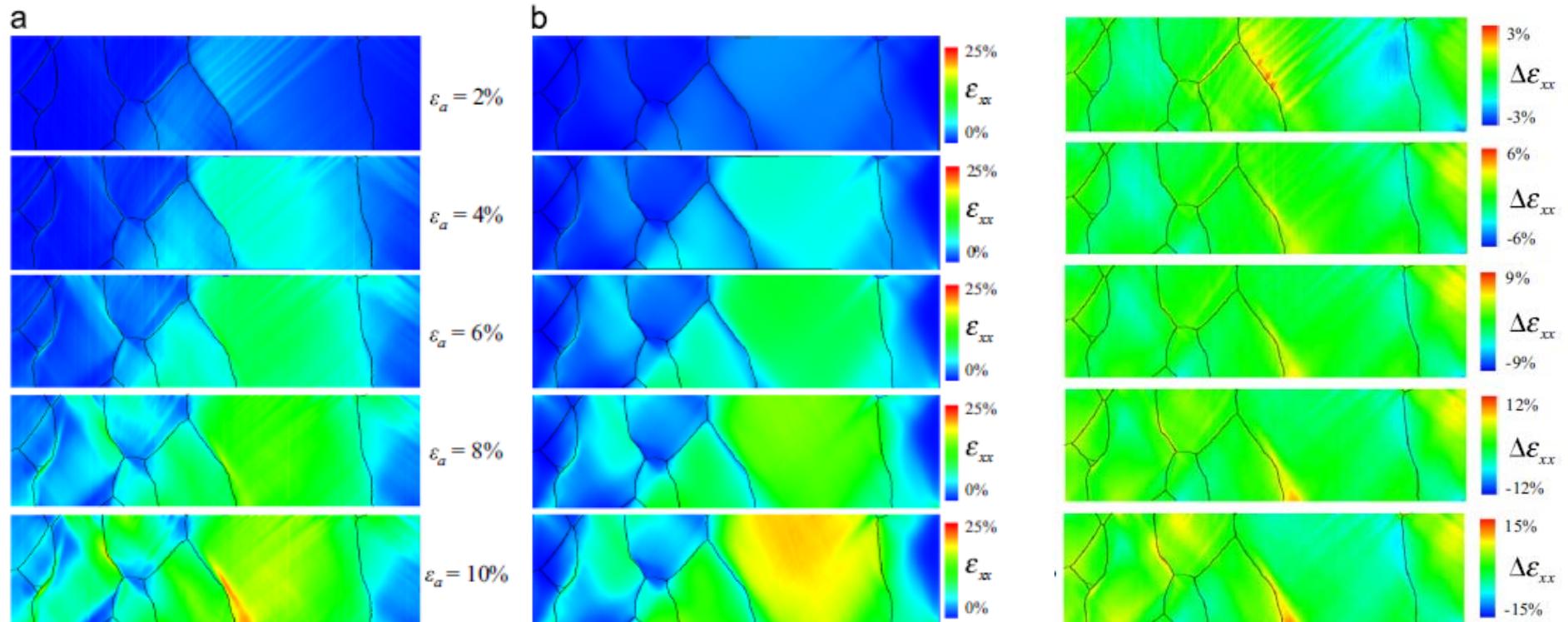


Experimental measurement of strains within individual grains using SEM Digital Image Correlation

2D slice of a 3D simulation of strain inhomogeneity based on crystal plasticity finite element modeling.

# A Quantitative Model-Experiment Difference Map

$$\varepsilon_{xx}^{DIC} - \varepsilon_{xx}^{CPFEM} = \Delta\varepsilon_{xx}$$

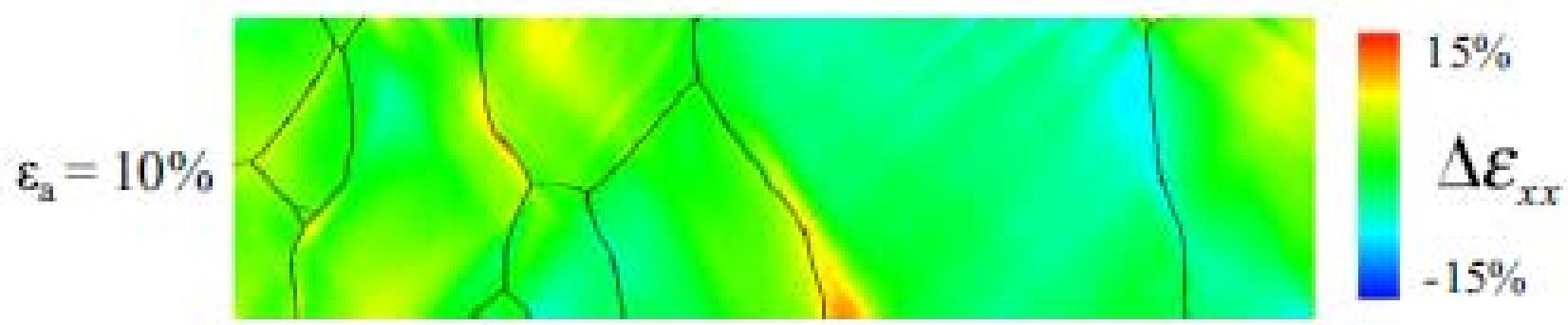


## The advantage of quantitative difference mapping:

$$\Delta\epsilon^{\text{avg}} = \sqrt{\frac{1}{N} \sum_{i=1}^N (\epsilon_i^{\text{DIC}} - \epsilon_i^{\text{sim}})^2}.$$

- A rational RMS goodness-of-fit metric to compare and discriminate effectiveness and locate deficiencies.

Deviation	Applied strain ( $\epsilon_a$ )				
	2%	4%	6%	8%	10%
$\Delta\epsilon_{xx}^{\text{avg}}$	0.0073	0.0102	0.0143	0.0215	0.0344
$\Delta\epsilon_{yy}^{\text{avg}}$	0.0059	0.0097	0.0116	0.0142	0.0180
$\Delta\epsilon_{xy}^{\text{avg}}$	0.0031	0.0071	0.0104	0.0136	0.0159



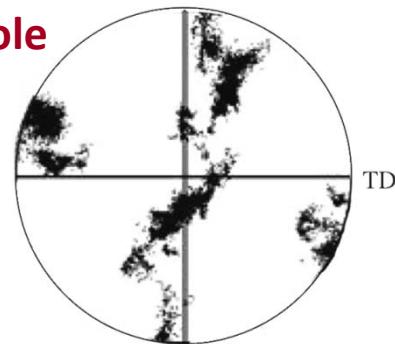
# Quantifying Rotation Change



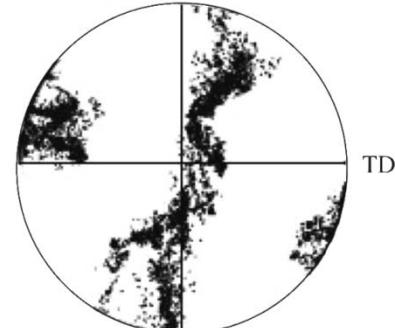
# Global vs Local Rotation Measurements

Global  
Texture  
Evolution

(100) X-ray Pole  
Figures



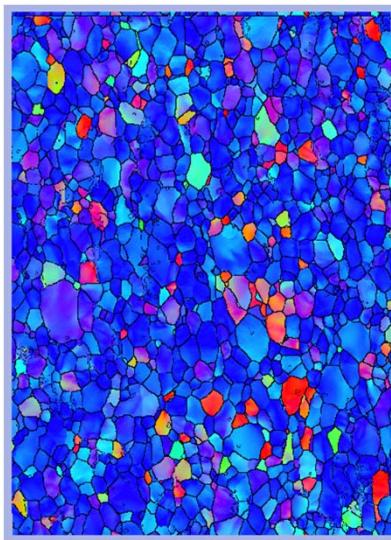
Experiment



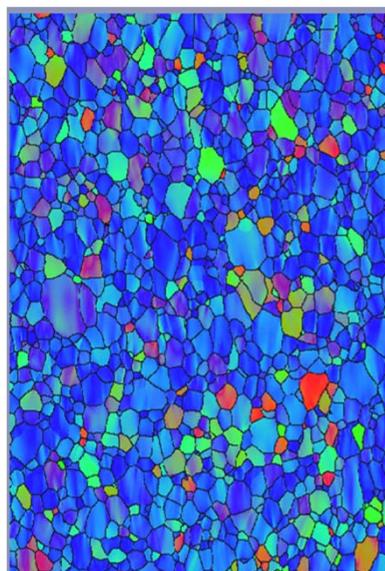
Prediction

S.R. Kalidindi, A. Bhattacharyya, and R.D. Doherty, *Proc. Roy. Soc. Lond. A* **460** (2004) 1-22.

Local Crystal  
Orientation

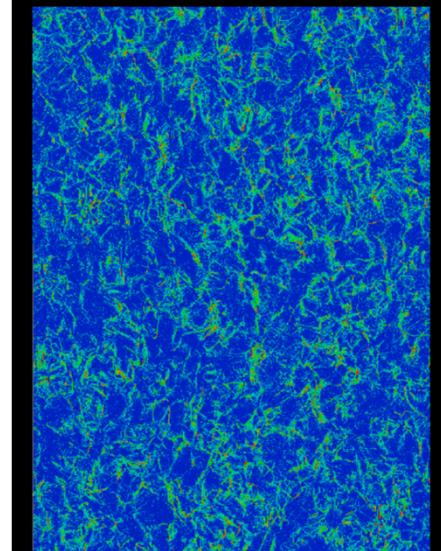


Experiment

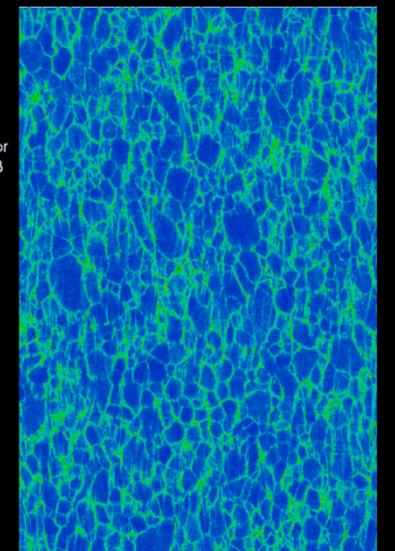


Simulation

Misorientation



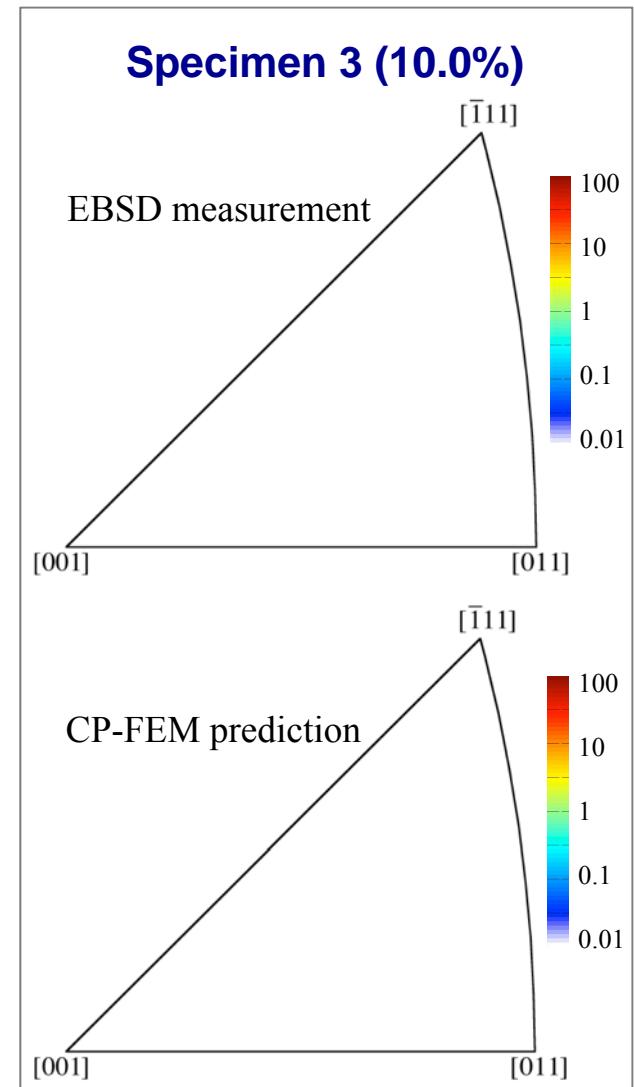
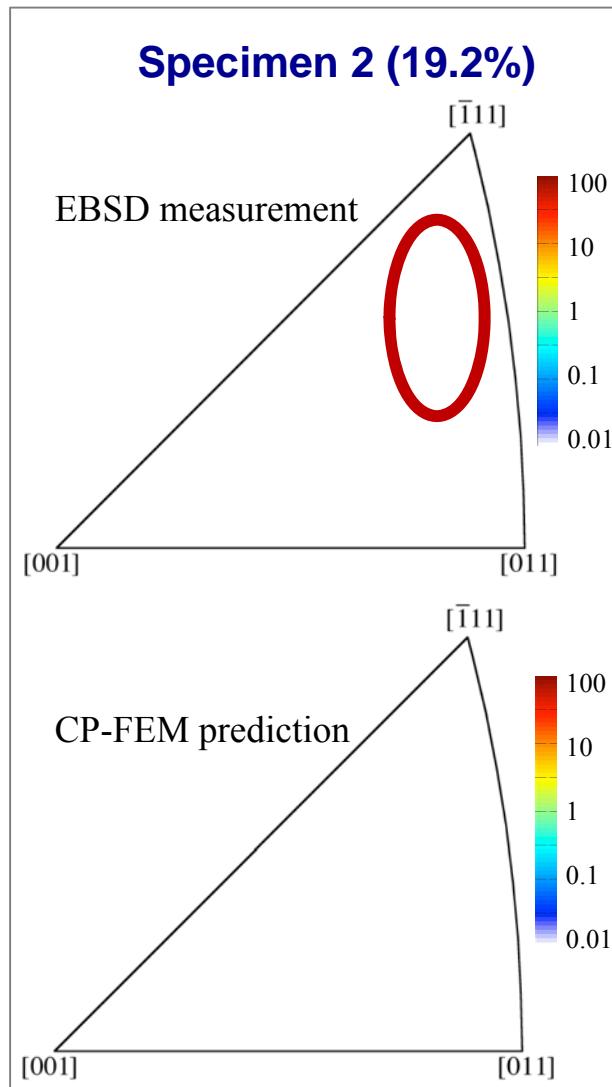
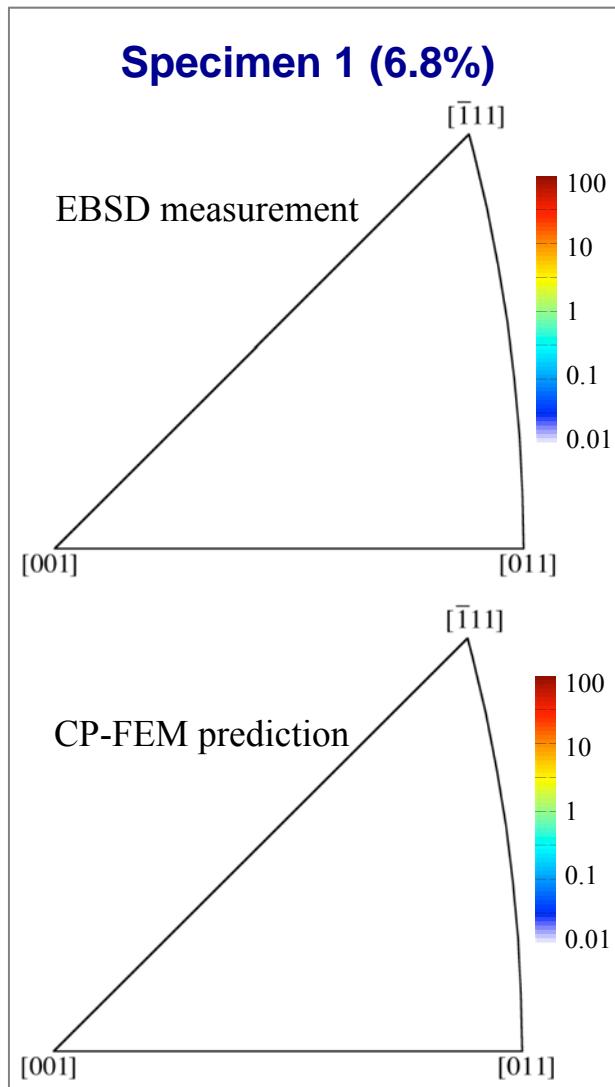
Experiment



Simulation

Courtesy of A.D. Rollett

# Texture Predictions



IPF contour plots indicate very good agreement between model and experiment.

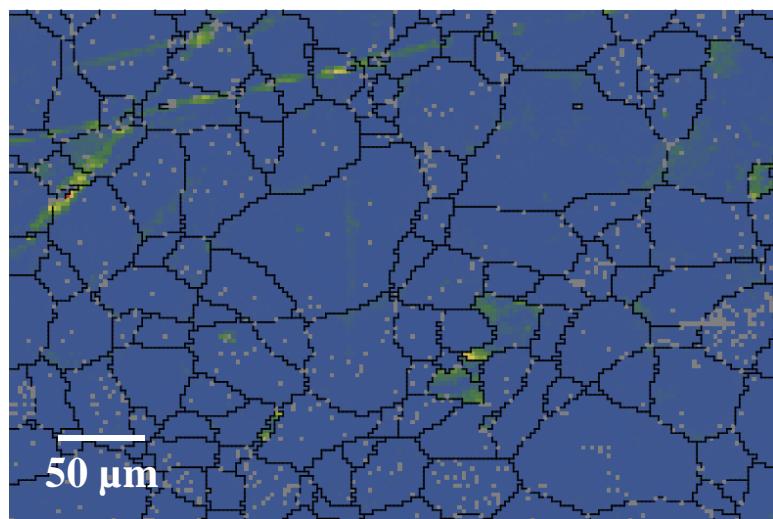
# Reference Orientation Deviation Map (ROD)



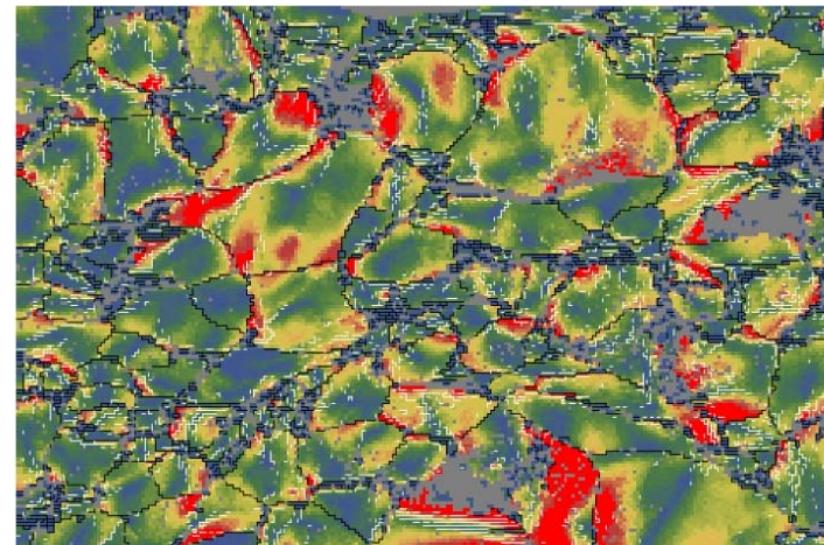
reference pixels to a specific orientation in a grain

Misorientation between all pixels in a grain and the grain's current average orientation

*Original Configuration*



*Deformed Configuration*  
~22% Strain (4<sup>th</sup> strain step)



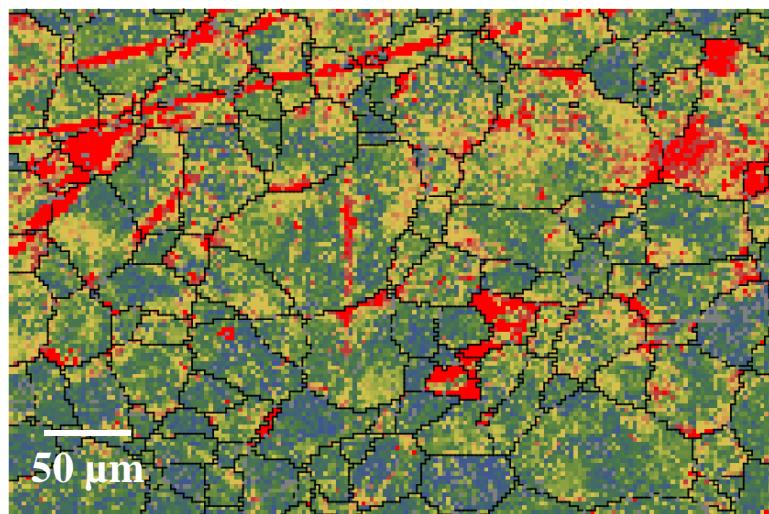
- Conventional approach –does not require a correlation between maps
- deformation history not captured



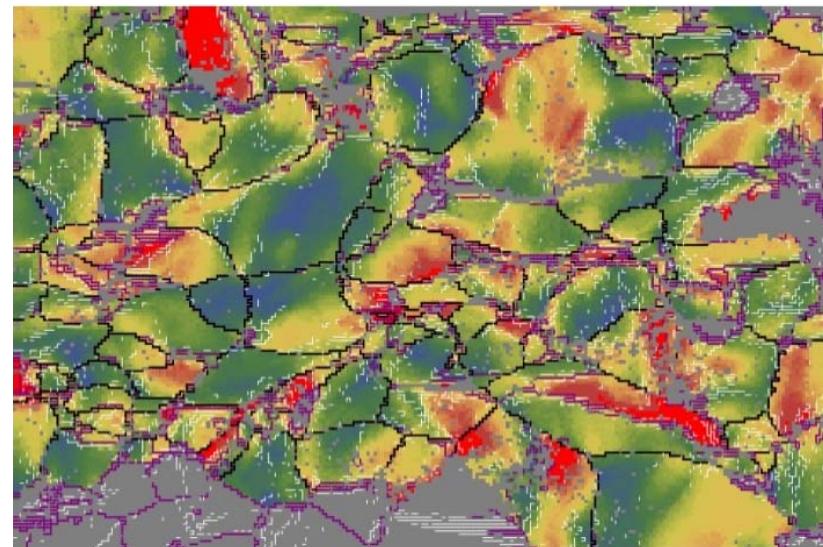
- Grain boundaries
- 2.5° threshold exceeded between adjacent pixels
- Pixels not indexed

# A new type of ROD map, referencing to the average orientation of *originally defined grains*

*Original Configuration*



*Deformed Configuration*  
~22% Strain (4<sup>th</sup> strain step)



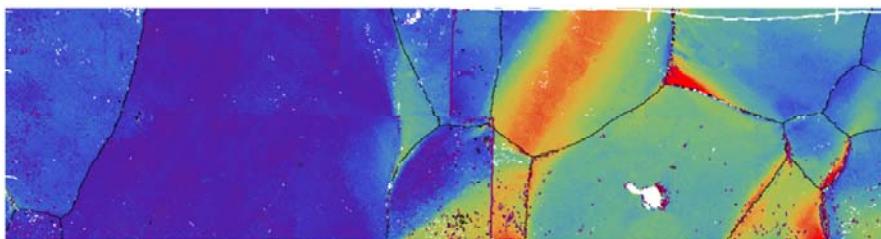
- Must track grain ID during deformation to allow orientation relative to original
- Requires ability to perform in-situ EBSD measurements during deformation
- Easily compared to a CPFEM model

- Boundaries of originally defined grains
- Boundaries of new grains
- 2.5° threshold exceeded between adjacent pixels
- Pixels not correlated or indexed

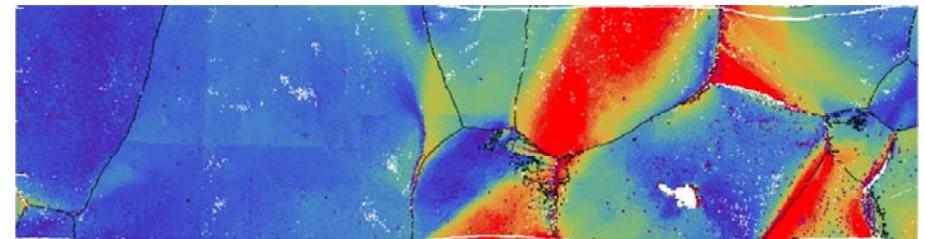
# Comparison of pixel misorientation *relative to original average grain orientation*

4.2% Strain

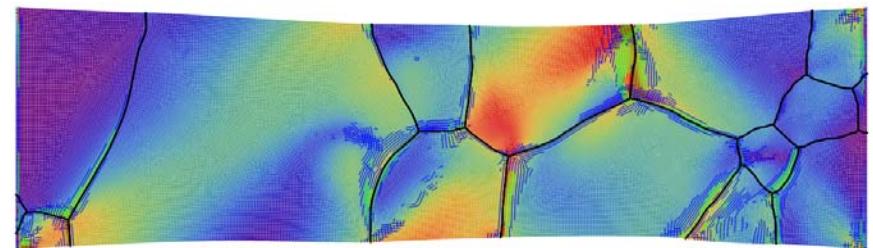
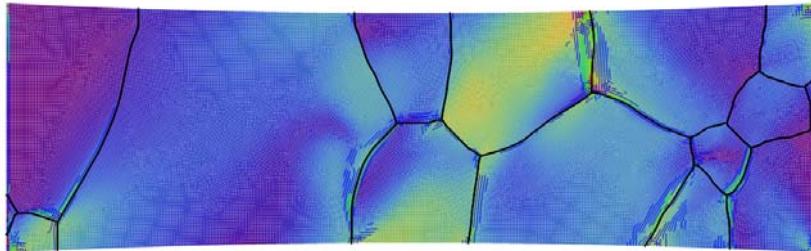
Experiments (EBSD Maps)



6.8% Strain



CPFEM Simulations



0°

10°

Minimum misorientation angle  
relative to the undeformed grain orientation

- 2.5°
- 1.0°
- 0.5°

# Grain boundary transmissivity

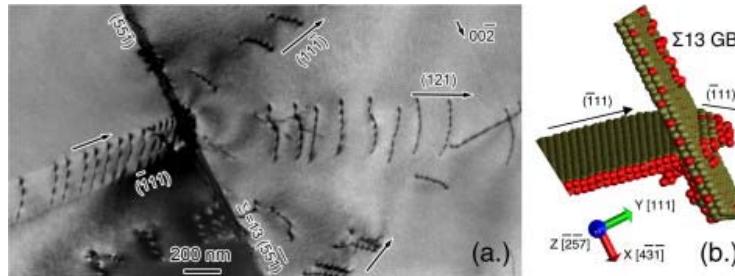
# There are many models for grain boundary slip transmissibility

## How does slip transfer across GBs? Dependence on GB type?

- Explicit MD examination

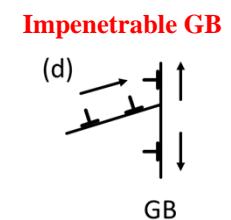
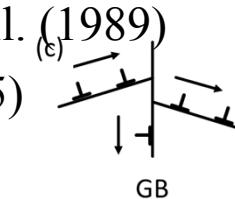
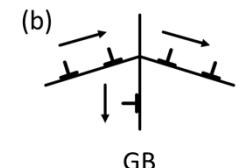
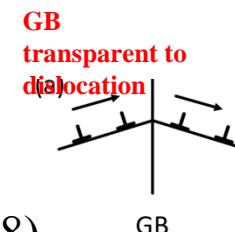
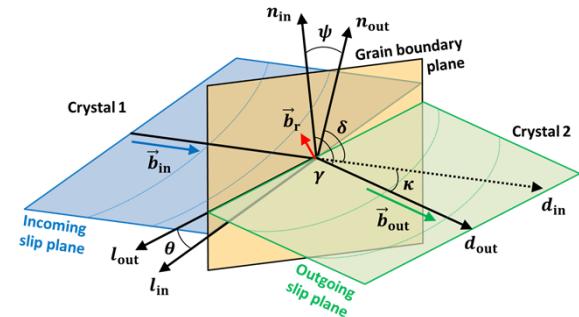
- Sangid-Ezaz-Sehitoglu-Robertson, Acta Mater. 2011

(3 boundaries)



- Geometrical criteria:

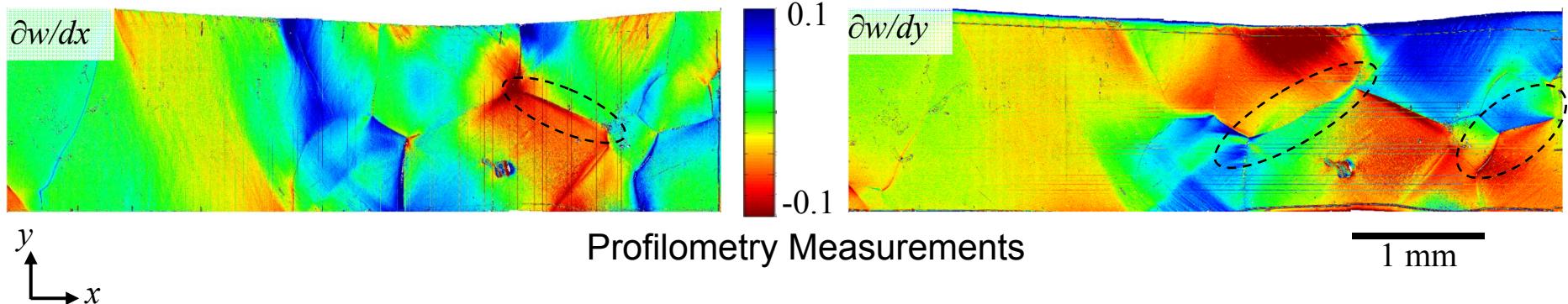
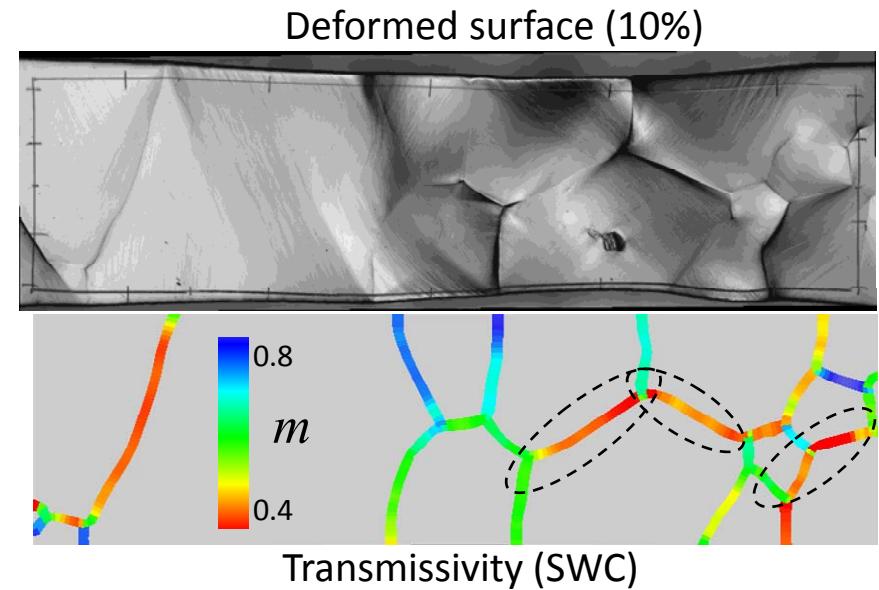
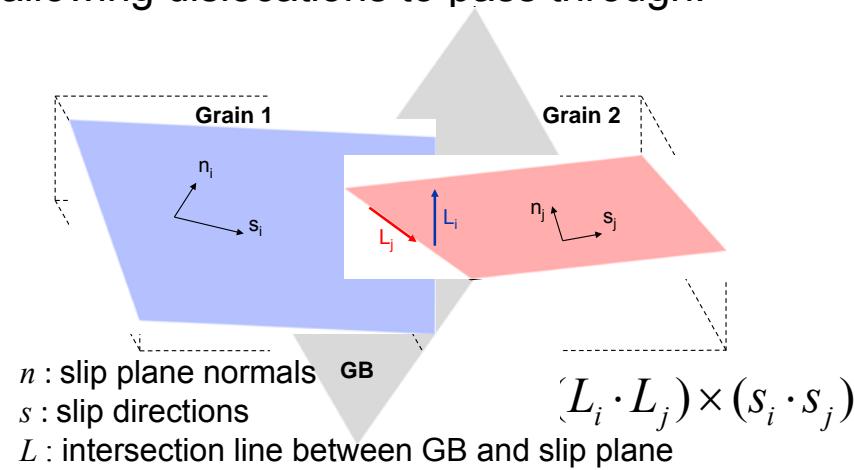
- ***N factor*** from Livingston-Chalmers, Acta Metall. (1957)
  - ***SWC factor*** from Shen-Wagoner-Clark, Acta Metall. (1988)
  - ***LRB factor*** from Lee-Robertson-Birnbaum, Scripta Metall. (1989)
  - ***m' factor*** from Luster -Morris, Metal. Mat. Trans. A (1995)
  - ***The residual Burgers vector***, Metal. Trans. (1970)
  - ***The  $\lambda$  function*** from Werner and Prantl, Acta Metall. (1990)



# Surface profile for interpreting grain boundary transmissivity



Grain boundary slip transmissivity provides an estimate for how resistant a grain boundary is to allowing dislocations to pass through.

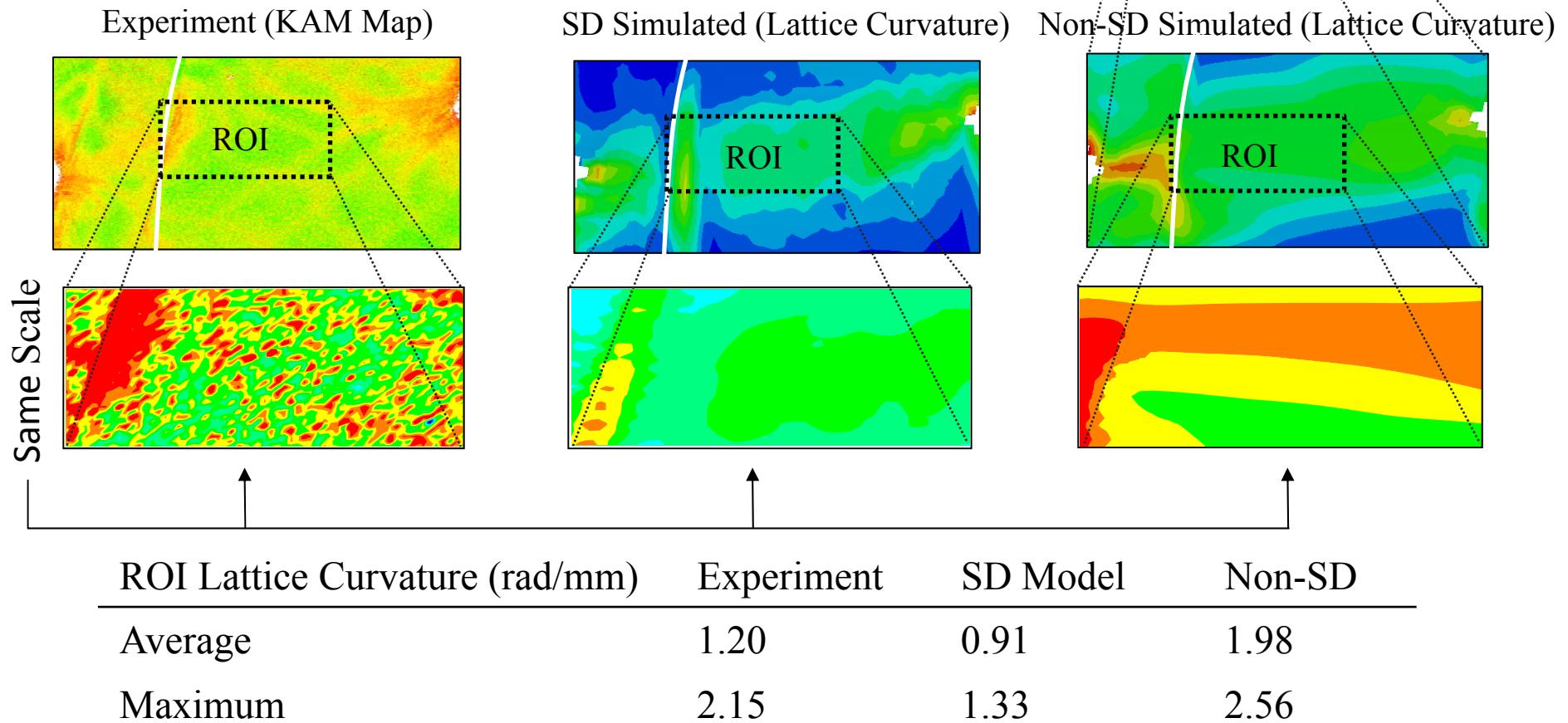


Our transmissivity-based model for boundary – dislocation interactions provides qualitative agreement with measurements of slip band formation and surface profilometry.

**Fullwood/Wagoner/Homer Collaboration:  
Quantitatively validate transmissibility laws at  
individual boundaries**

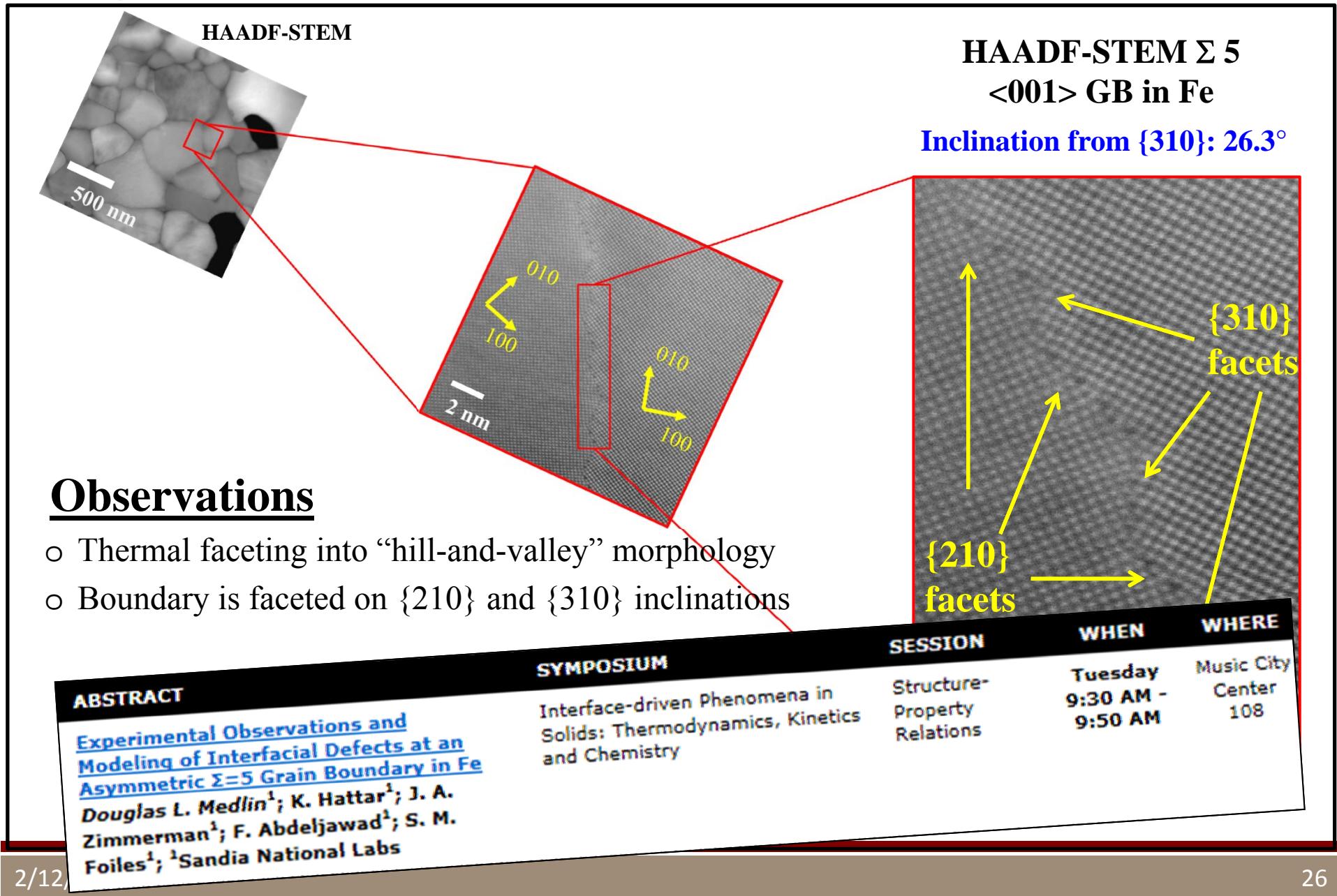
## Ta Bicrystal – Lattice Curvature

\* 0.1 mm Plastic Extension in Mini Instron



# Grain boundaries are not always as simple as 'just' 5 degrees of freedom!!!





The diagram illustrates a complex grain boundary in a polycrystalline material. On the left, a HAADF-STEM image shows a grain boundary with a 500 nm scale bar. A red box highlights a specific region, which is magnified on the right. The magnified view shows a stepped, faceted surface. Red lines indicate the facets, and yellow arrows labeled  $\{010\}$  and  $\{100\}$  indicate the crystallographic orientations of the facets. A 2 nm scale bar is also present. The text "HAADF-STEM  $\Sigma 5$  <001> GB in Fe" and "Inclination from  $\{310\}$ : 26.3°" is displayed above the magnified image.

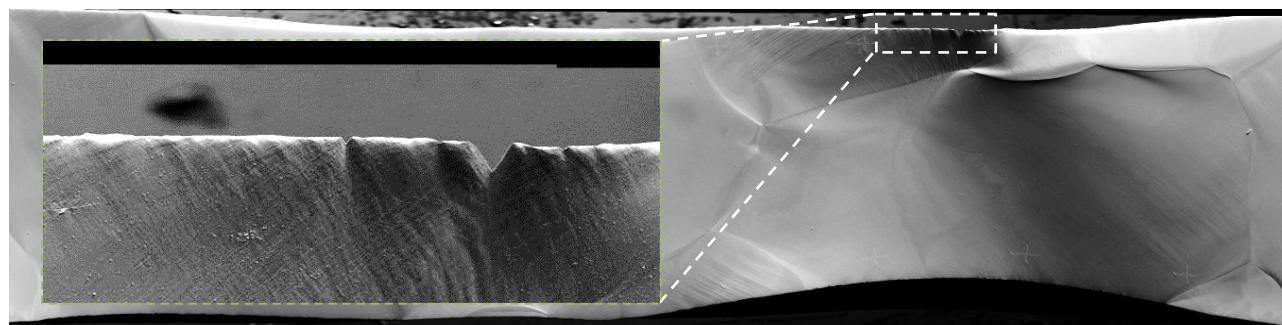
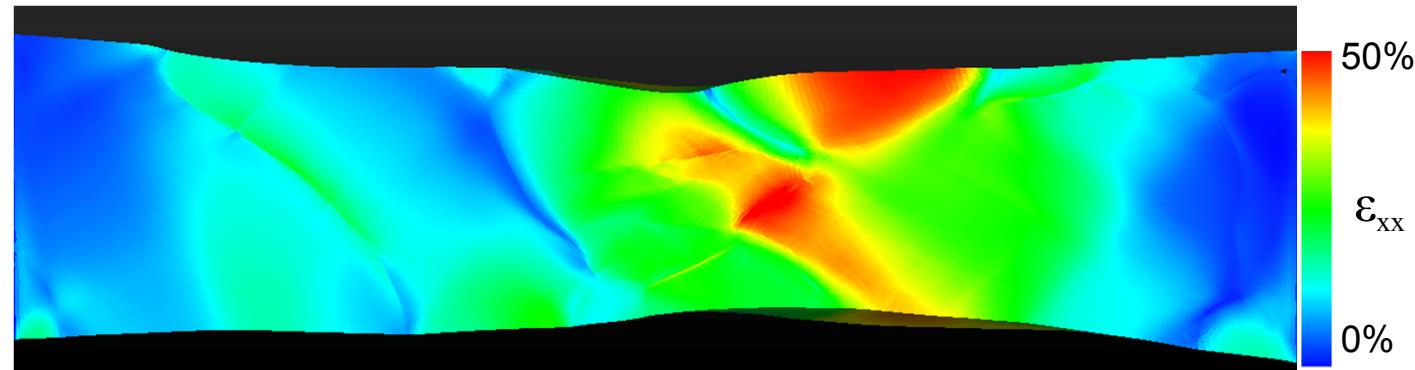
## Observations

- Thermal faceting into “hill-and-valley” morphology
- Boundary is faceted on  $\{210\}$  and  $\{310\}$  inclinations

ABSTRACT	SYMPOSIUM	SESSION	WHEN	WHERE
<u>Experimental Observations and Modeling of Interfacial Defects at an Asymmetric <math>\Sigma=5</math> Grain Boundary in Fe</u> Douglas L. Medlin <sup>1</sup> ; K. Hattar <sup>1</sup> ; J. A. Zimmerman <sup>1</sup> ; F. Abdeljawad <sup>1</sup> ; S. M. Foiles <sup>1</sup> ; <sup>1</sup> Sandia National Labs	Interface-driven Phenomena in Solids: Thermodynamics, Kinetics and Chemistry	Structure-Property Relations	Tuesday 9:30 AM - 9:50 AM	Music City Center 108

# Void Behavior and Damage

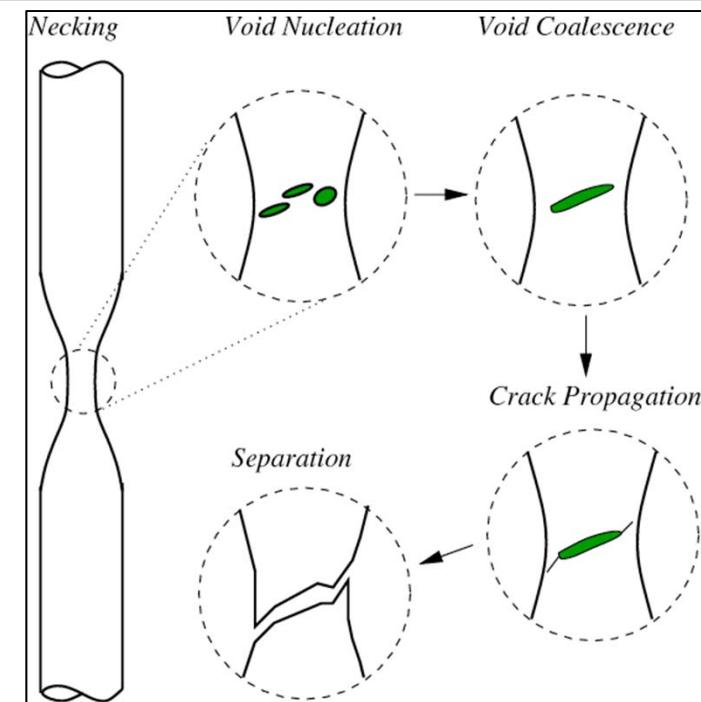
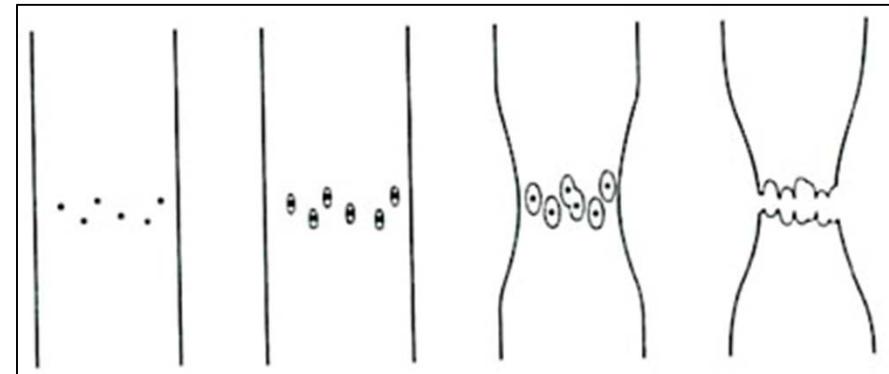
The crystal plasticity model predicts localized hot spots in strain at the same location where cracking is observed...



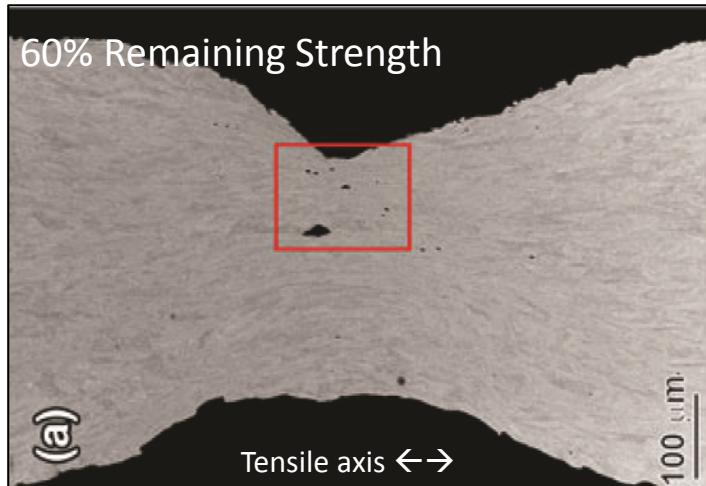
# Background: Ductile Fracture

- Initiation of voids through decohesion at second-phase particles or inclusions
- Voids continue to grow in response to high stresses
- Eventual coalescence of voids, leading to failure

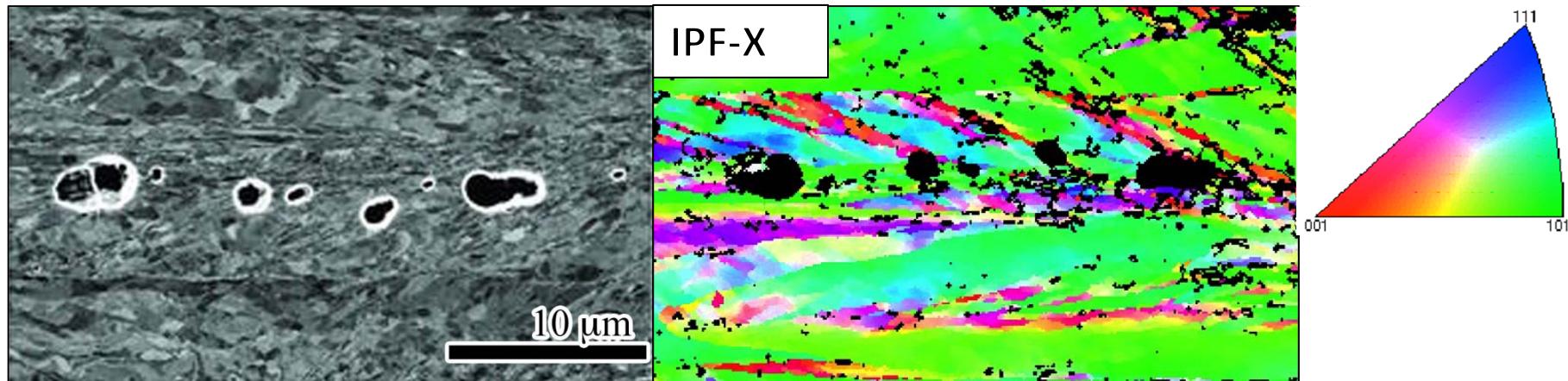
How do voids initiate in pure metals?



# Void Formation in 99.9%Ta

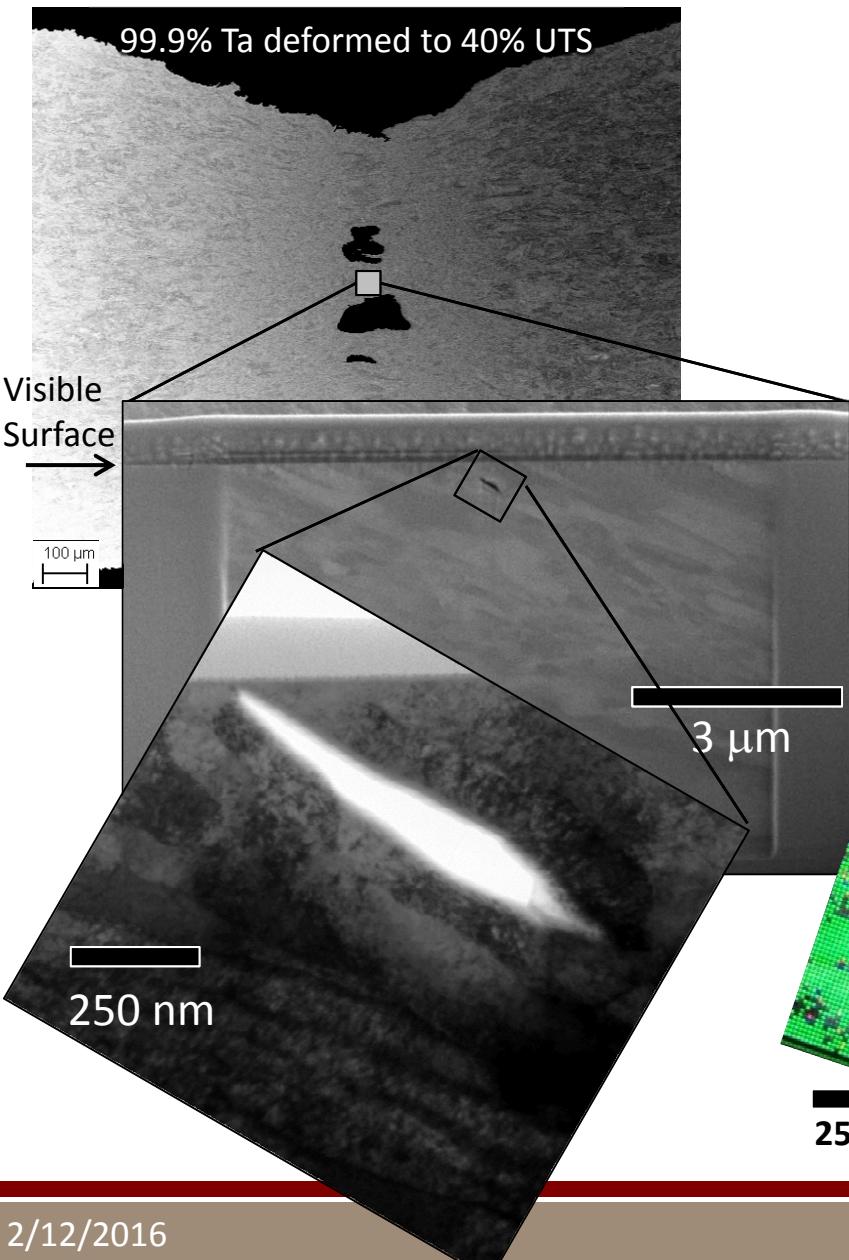


- Arrays of voids aligned along tensile axis
- EBSD shows elongated, inclined [001] subgrains associated with each void
- Alternating regions of [122] indicates high angle GBs

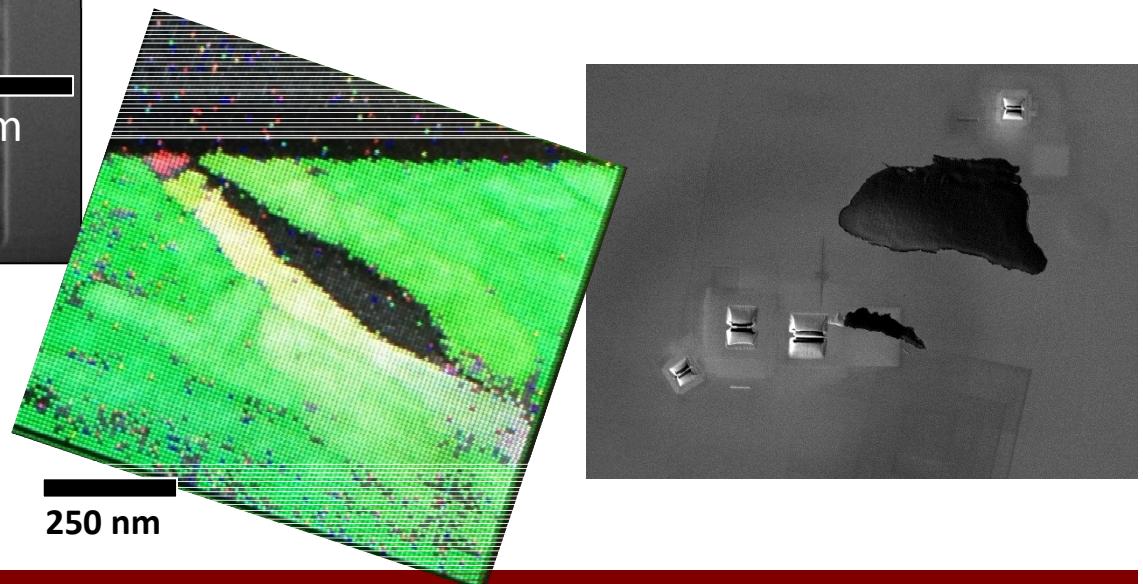


Ta failure is void-driven, with deformation-induced microstructural changes and stress state controlling the initiation/growth of voids

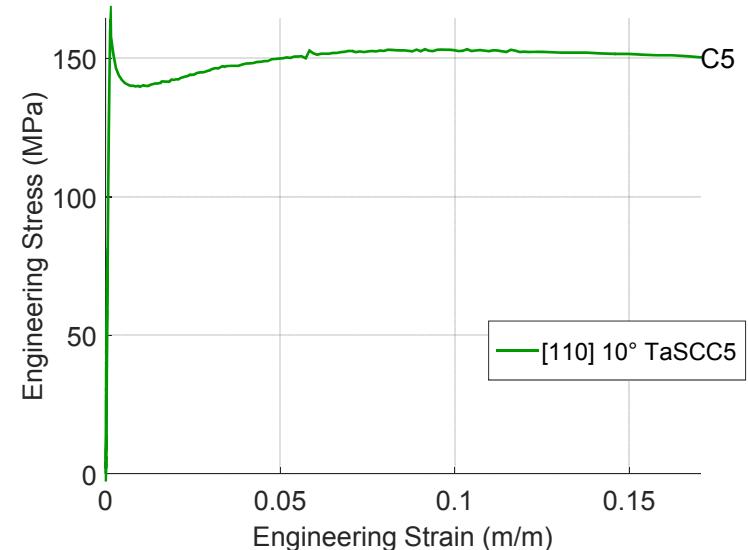
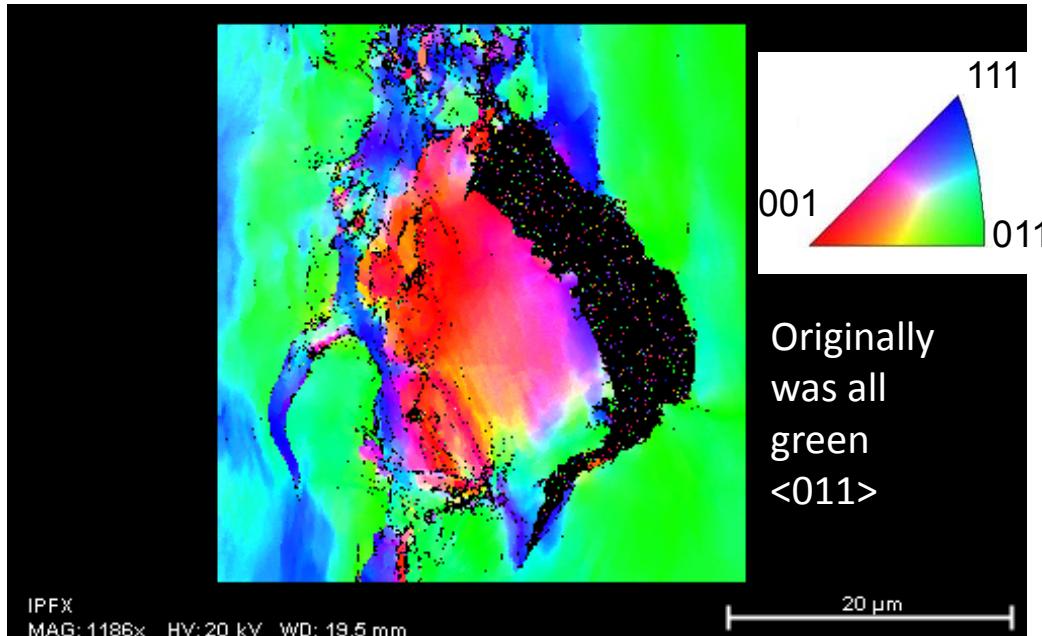
# Nanoscale Analysis of Void Initiation



- Focused Ion Beam (FIB) used to locate subsurface, deformation-induced voids in interrupted tensile bar.
- Preliminary TEM shows void shape aligned with angle of sub-boundaries
- Transmission Kikuchi Diffraction (TKD) to determine crystallographic orientation near void.
- Orientations are consistent with EBSD analysis showing void nucleation along high angle misorientation boundaries



# Probing relationships between void formation and crystallographic orientation



- Investigated a void formed during tensile testing of a Ta single crystal  $<011>$ . Imaging at the specimen midplane.
- Crystallographic rotations near a void in single crystal specimens improve our understanding of void formation in polycrystals.
- Void formation is associated with developing  $<001>$  and  $<111>$  crystallographic orientations.
- We are investigating whether substructure leads to these crystallographic rotations which leads to voids or whether the formation of voids causes the crystallographic rotations.

# Summary



- **Grain-scale validation of crystal-plasticity models is still largely qualitative**
- **Both distortion and rotation can be mapped relative to the original undeformed configuration**
- **With an ability to map back to the original undeformed configuration, it is possible to begin to assess quantitative difference metrics.**
- **These new statistical metrics may help identify and address gaps in CP-FEM theory:**
  - **Grain boundary slip transmissibility**
  - **Void nucleation and growth**