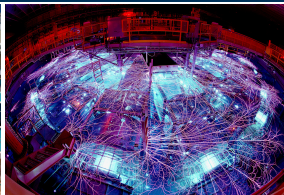


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Neighbor Discovery for Algebraic Multigrid and Matrix Migration

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6/22/16

Outline

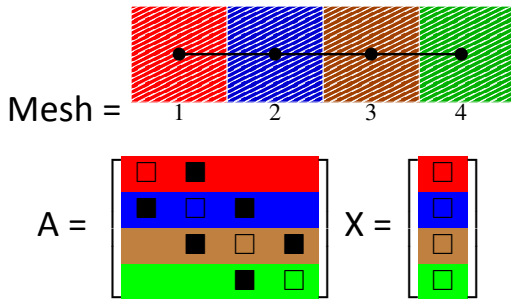
- What is neighbor discovery?
- Efficient neighbor discovery for matrix migration
- Conclusions

Parallel Sparse Matrices

- Congratulations! You can store a parallel sparse matrix w/ MPI!
What's next?
- You probably want to be able to *multiply* this matrix by a vector.
- What sort of communication structures do we need (presuming row-wise storage)?
 - The *domain* distribution of the vector.
 - The *column* distribution of the matrix.
 - The list of (data,destination) pairs each rank *sends*.
 - The list of (data,source) pairs each rank *receives*.

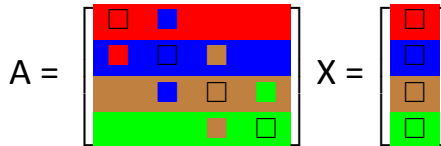
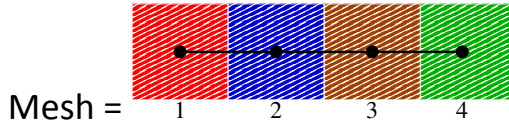
Finding Neighbors in General

- So, supposing we had this:



- How do we fill out our send and receive lists?

Data Distribution #1



Rank	Sends	Receives
Red	(1, Blue)	(2, Blue)
Blue	(2, Red) (2, Brown)	(1, Red) (3, Brown)
Brown	(3, Blue) (3, Green)	(2, Blue) (4, Green)
Green	(4, Brown)	(3, Brown)

- Idea: Use assumed partition [1] or rendezvous scheme.
 - Create assumed partition w/ easy to calculate range.
 - Each owning proc talks to assumed owner.
 - Each proc asks assumed owner who owns needed unknowns.
 - Requires $O(\log(p))$ distributed termination detection [2].
- Message: You need to exploit structure (of some kind) to get $O(1)$ storage and communication.
- BUT, once you have a hammer, everything looks like a nail.

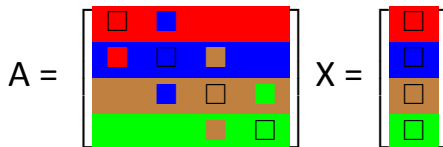
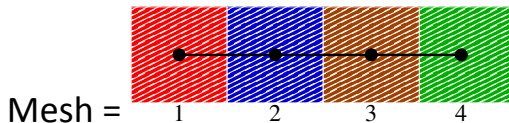
[1] Barker, Falgout and Yang, 2006.

[2] Pinar and Hendrickson, 2001.

Outline

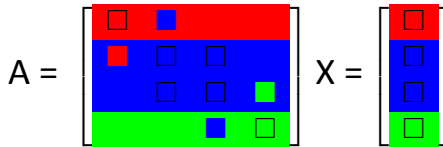
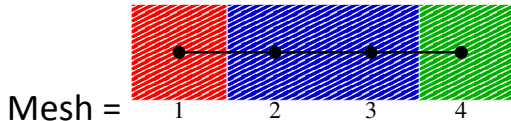
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Data Distribution #1



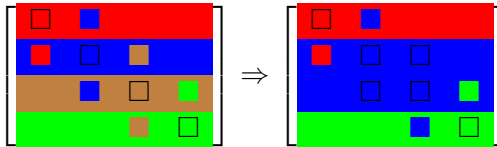
Rank	Sends	Receives
Red	(1, Blue)	(2, Blue)
Blue	(2, Red) (2, Brown)	(1, Red) (3, Brown)
Brown	(3, Blue) (3, Green)	(2, Blue) (4, Green)
Green	(4, Brown)	(3, Brown)

Data Distribution #2



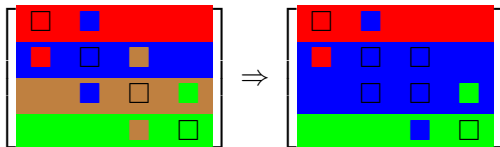
Rank	Sends	Receives
Red	(1, Blue)	(2, Blue)
Blue	(2, Red) (3, Green)	(1, Red) (4, Green)
Green	(4, Blue)	(3, Blue)

So what do we do?



- What happens?
 - Rank ■ gets row 3 from Rank ■.
 - Rank ■ now has a new neighbor, Rank ■ (and the reverse).
- How do we solve this? Try Rank ■'s perspective.
 - Rank ■ passes row 3 to Rank ■.
 - Rank ■ already knows that Rank ■ is a neighbor.
 - Basic Idea: What if Rank ■ tells ■ that?

Algorithm (■ edition)



- Forward round: If I pass a row to ■, I tell ■ who that row's neighbors are (e.g. ■).
- Reverse round: If I passed a row to ■ telling him that ■ is now his neighbor, I must tell ■ that ■ is now her neighbor.
- Idea: Use the send/rcv structure in *both* directions.

Algorithm (in more detail)

■ Forward round

- \forall send row id i , \forall nonzeros in row i , pass a (value, global column id, **owning rank**) triplet.
- Combine recv'd global column ids with existing global column ids to generate a column distribution map.

■ Reverse round

- \forall recv'd row id i , pass a list of ranks to whom an entry in global column i was sent during the forward round.

■ Send/rcv list generation

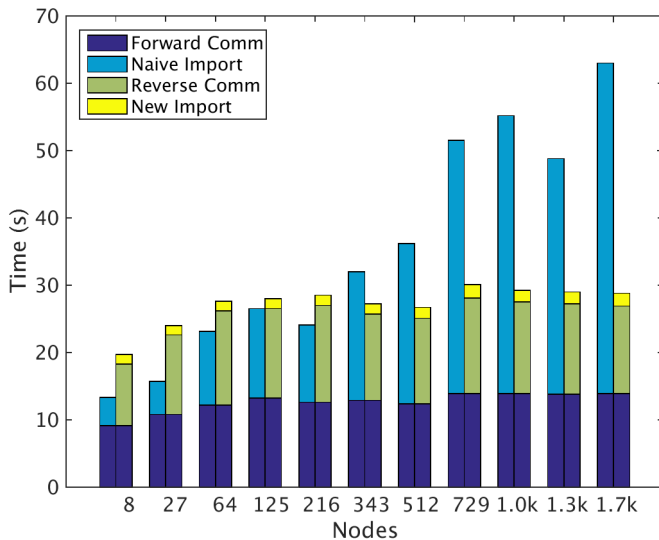
- Combine forward round “owning ranks” with other existing recvs to get recv list.
- Combine reverse round “communicated ranks” with other existing sends to get send list.

- Note: “New” stuff is in **blue**.

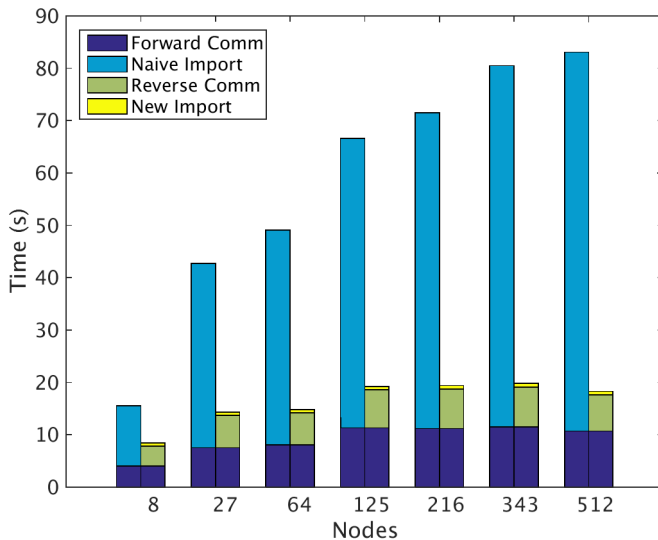
Computational Example

- Example: 3D Laplacian (A) and prolongator (P) from Trilinos/MueLu.
- Matrix migration: Off-processor portions of P needed to compute $C = A P$.
- Compare: Communication costs
 - Building communication structures *ex nihilo*.
 - Building them via the aforementioned algorithm.
 - Trilinos/Epetra code used in both cases.
- Two machines
 - SNL's Redsky.
 - NERSC's Edison.
- Note: Pack/unpack costs will be neglected to focus on comm.

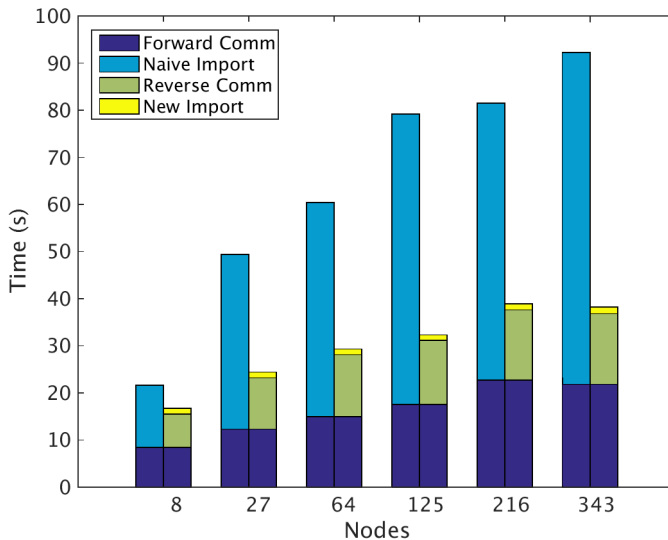
Edison: 15k Unknowns / Core



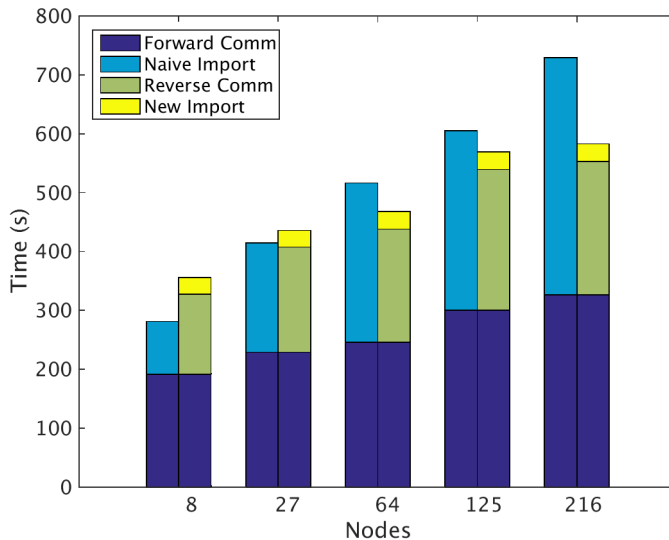
Redsky: 5k Unknowns / Core



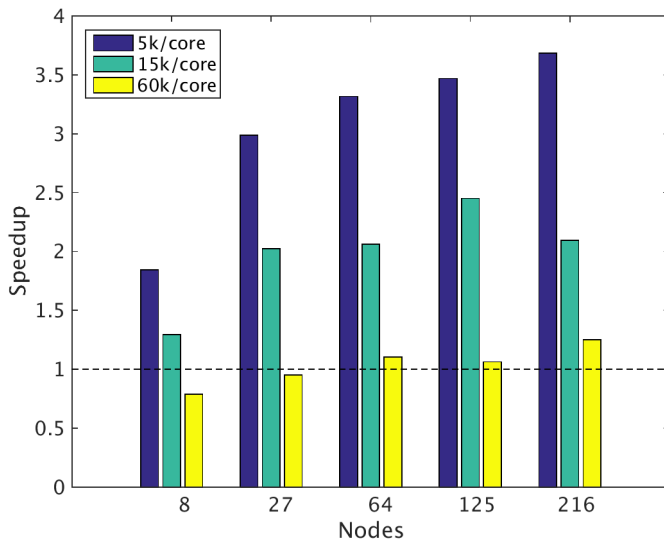
Redsky: 15k Unknowns / Core



Redsky: 60k Unknowns / Core



Redsky: Speedup



Outline

- What is neighbor discovery?
- Efficient neighbor discovery for matrix migration
- **Conclusions**

- There is enough structure in matrix migration to get $O(1)$ cost neighbor discovery.
 - This kernel is especially useful in AMG's triple product.
 - A screwdriver usually does a better job than a hammer...
 - But with the right machine and enough data per core, maybe a hammer is good enough.
- Future directions
 - Other applications: Repartitioning, off-processor FEM assembly.
 - Complete deployment in Trilinos/Tpetra utility routines.
 - Further optimization of communication.